

$$E = mc^2$$

Beyond the Higgs

LAL, February 8, 2010

$$E = \hbar\nu$$

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi G T_{\mu\nu}$$



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Why do we need to go beyond the SM Higgs?

1 unsuccessful searches for a Higgs boson

2 EW precision data:

- consistency with a light Higgs
- strong constraints on anything else

'legacy of last 20 years of expts.'



we have to live with either
fine-tuning in parameter space
or
larger theory space



The source of the Goldstone's

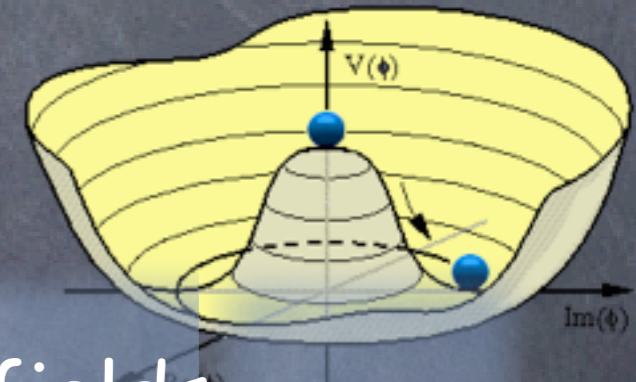
symmetry breaking: new phase with more degrees of freedom

massive W^\pm, Z : 3 physical polarizations=eaten Goldstone bosons $\frac{SU(2)_L \times SU(2)_R}{SU(2)_V}$

\Rightarrow Where are these Goldstone's coming from? \Leftarrow

what is the sector responsible for the breaking $SU(2)_L \times SU(2)_R$ to $SU(2)_V$?
with which dynamics? with which interactions to the SM particles?

common lore: from a scalar Higgs doublet



$$H = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix}$$

Higgs doublet = 4 real scalar fields

3 eaten \leftarrow One physical degree of freedom
Goldstone bosons \rightarrow the Higgs boson

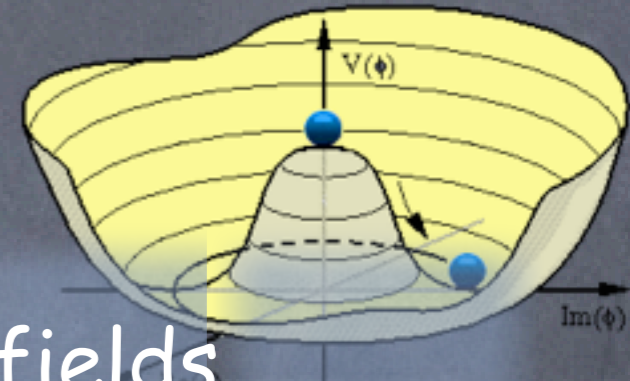
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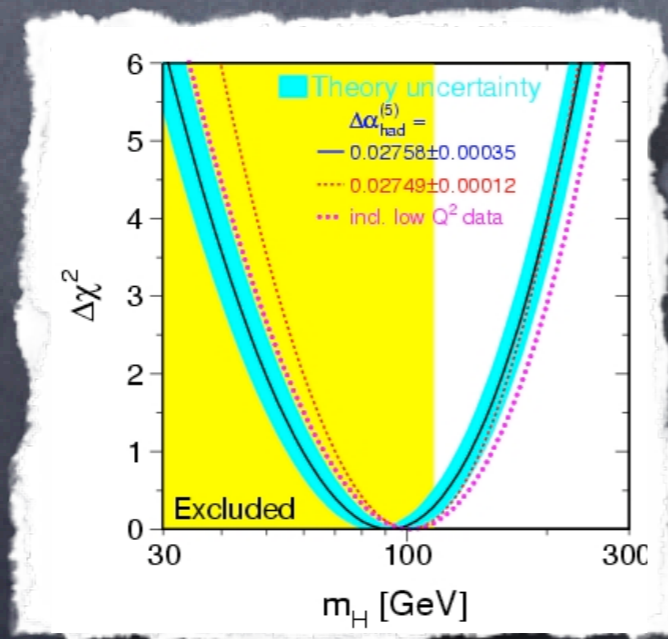
$$H = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix}$$

Higgs doublet = 4 real scalar fields

3 eaten
Goldstone bosons

One physical degree of freedom
the Higgs boson

Good agreement with EW data (doublet $\Leftrightarrow \rho=1$)



	Measurement	Fit	$ \sigma_{meas} - \sigma_{fit} / \sigma_{meas}$
$\Delta\alpha_{had}^{(5)}$	0.02758 ± 0.00035	0.02767	0.0003
m_Z [GeV]	91.1875 ± 0.0021	91.1874	0.0001
Γ_Z [GeV]	2.4952 ± 0.0023	2.4959	0.0003
σ_{had}^0 [nb]	41.540 ± 0.037	41.478	0.0015
R_f	20.767 ± 0.025	20.743	0.0012
$A_{fb}^{0,l}$	0.01714 ± 0.00095	0.01642	0.0042
$A_f(P_f)$	0.1465 ± 0.0032	0.1480	0.0089
R_b	0.21629 ± 0.00066	0.21579	0.0007
R_c	0.1721 ± 0.0030	0.1723	0.0001
$A_{fb}^{0,b}$	0.0992 ± 0.0016	0.1037	0.0045
$A_{fb}^{0,c}$	0.0707 ± 0.0035	0.0742	0.0050
A_b	0.923 ± 0.020	0.935	0.0130
A_c	0.670 ± 0.027	0.668	0.0030
$A_f(SLD)$	0.1513 ± 0.0021	0.1480	0.0021
$\sin^2\theta_{eff}^{lept}(Q_{fb})$	0.2324 ± 0.0012	0.2314	0.0043
m_W [GeV]	80.404 ± 0.030	80.377	0.0034
Γ_W [GeV]	2.115 ± 0.058	2.092	0.0110
m_t [GeV]	172.7 ± 2.9	173.3	0.0035

But the Higgs hasn't been seen yet...

other origins of the Goldstone's: condensate of techniquarks, A_5 ...

Which Higgs?

UnHiggs?

Private Higgs?

Guralnik's Higgs?

Gaugephobic Higgs?

Kibble's Higgs?

Little Higgs?

Buried Higgs?

Intermediate Higgs?

Littlest Higgs?

Composite Higgs?

Fat Higgs?

Slim Higgs?

Portal Higgs?

Peter's Higgs?

Higgsless?

Gauge-Higgs?

Brout-Englert's Higgs?

Lone Higgs?

Simplest Higgs?

Twin Higgs?

Phantom Higgs?



$$H = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix}$$

Higgs doublet = 4 real scalar fields

3 eaten
Goldstone bosons

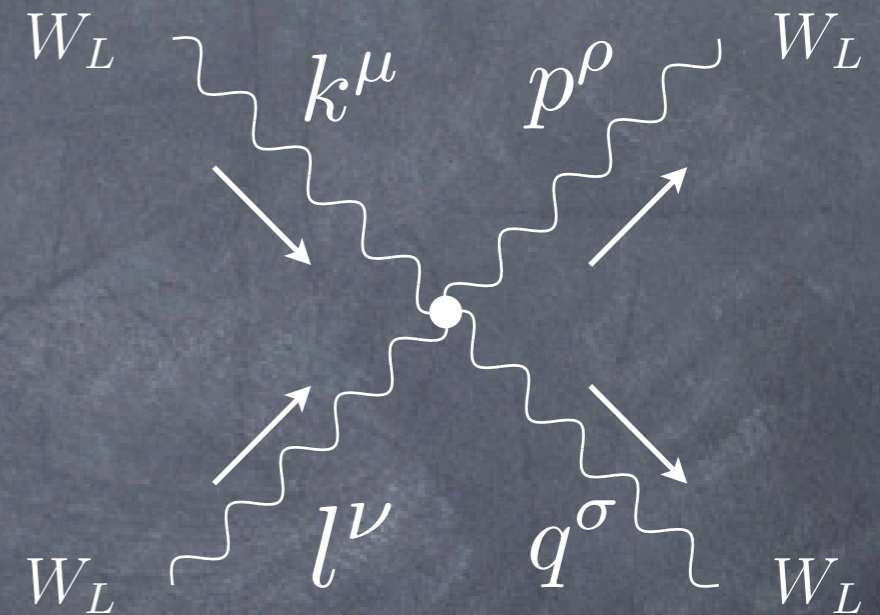
One physical degree of freedom
the Higgs boson

Higgs as a UV moderator

Why do we need a Higgs ?

The W and Z masses are inconsistent with the known particle content! Need more particles to soften the UV behavior of massive gauge bosons.

Bad UV behavior for the scattering of the longitudinal polarizations



$$A \propto g^2 \frac{E^4}{M^4}$$

violations of perturbative unitarity around $E \sim M$

A QCD antecedent

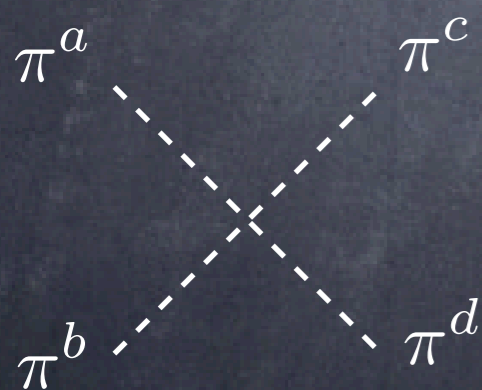
QCD pions are Goldstone bosons associated to $SU(2)_L \times SU(2)_R / SU(2)_V$

$$U = e^{i\pi^a \sigma^a / f_\pi} \begin{pmatrix} 0 \\ \frac{f_\pi}{\sqrt{2}} \end{pmatrix}$$

kinetic terms for $U \Leftrightarrow$ interaction terms for π^a

$$\mathcal{L} = |\partial_\mu U|^2 = \frac{1}{2} (\partial_\mu \pi^a)^2 - \frac{1}{6f_\pi^2} \left((\pi^a \partial_\mu \pi^a)^2 - (\pi^a)^2 (\partial_\mu \pi^a)^2 \right) + \dots$$

contact interaction growing with energy



$$\mathcal{A}(\pi^a \pi^b \rightarrow \pi^c \pi^d) = \mathcal{A}(s, t, u) \delta^{ab} \delta^{cd} + \mathcal{A}(t, s, u) \delta^{ac} \delta^{bd} + \mathcal{A}(u, t, s) \delta^{ad} \delta^{bc}$$

$$\mathcal{A}(s, t, u) = \frac{s}{f_\pi^2}$$

$$f_\pi = 93 \text{ MeV}$$

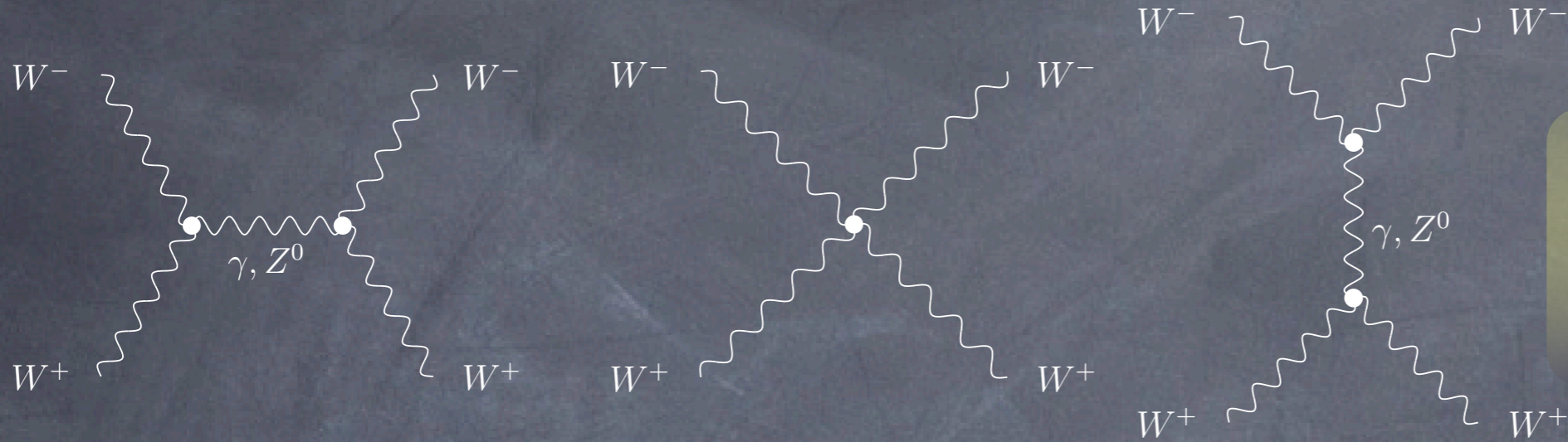


unitarity bound

$$\sqrt{s} \sim 4\sqrt{\pi} f_\pi = 660 \text{ MeV}$$

rho meson ($m=770 \text{ MeV}$) is restoring unitarity

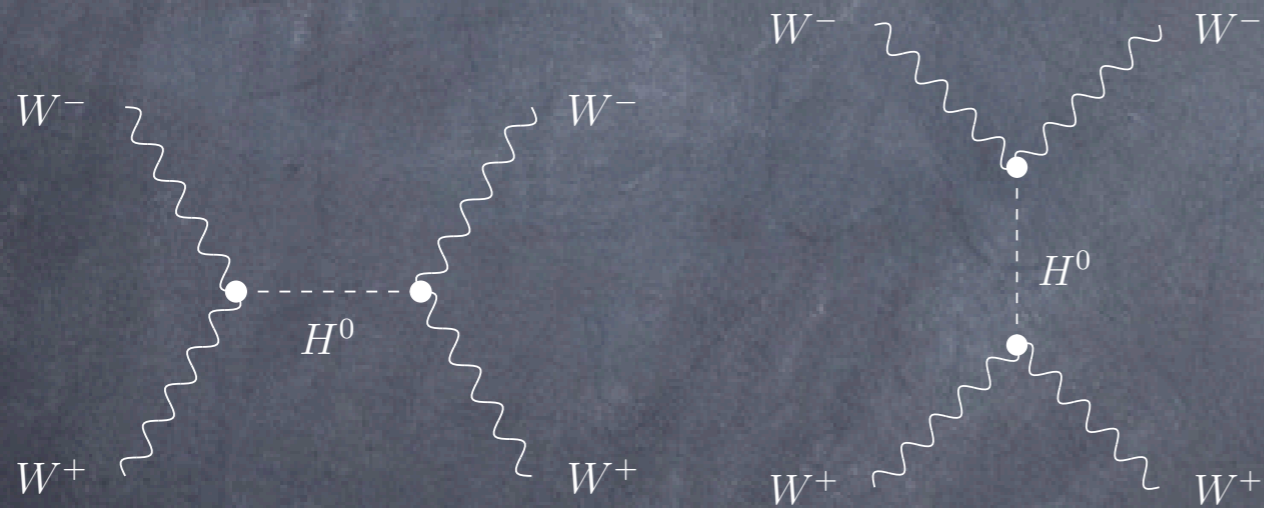
Why do we need a Higgs ?



$$\mathcal{A} = g^2 \left(\frac{E}{M_W} \right)^2$$

+

+



$$\mathcal{A} = -g^2 \left(\frac{E}{M_W} \right)^2$$

The Higgs boson unitarize the W scattering
(if its mass is below ~ 700 GeV)



$$\mathcal{A} = g^2 \left(\frac{M_H}{2M_W} \right)^2$$

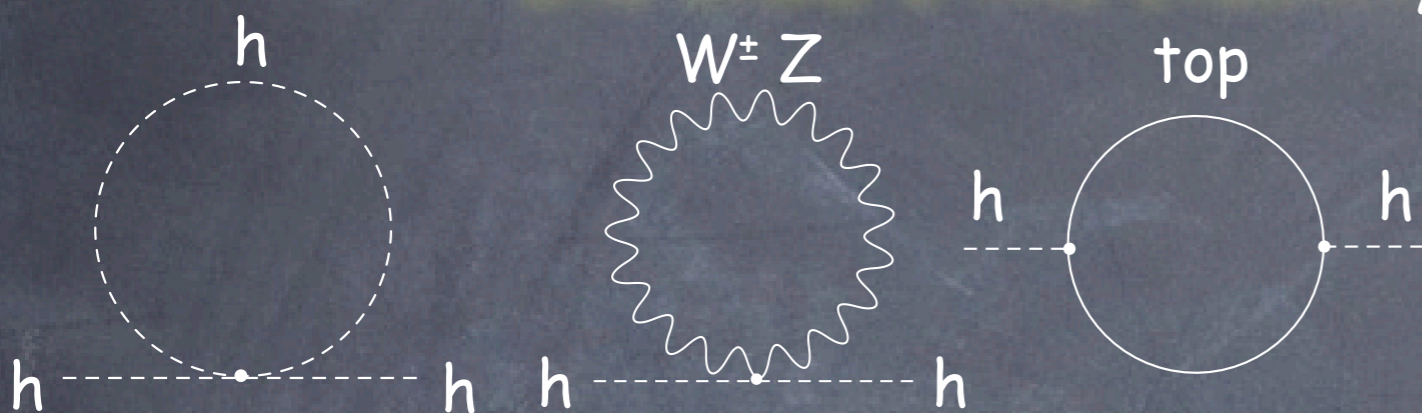
W_L scattering = pion scattering
Goldstone equivalence theorem

Lewellyn Smith '73
Dicus, Mathur '73
Cornwall, Levin, Tiktopoulos '73

New physics: hierarchy pb @ flavor

The hierarchy problem

need new degrees of freedom to cancel Λ^2 divergences
and ensure the stability of the weak scale



$$m_H^2 \sim m_0^2 - (115 \text{ GeV})^2 \left(\frac{\Lambda}{400 \text{ GeV}} \right)^2$$

- 1 add a sym. such that a Higgs mass is forbidden until this sym. is broken
 - supersymmetry [Witten, '81]
 - gauge-Higgs unification [Manton, '79, Hosotani '83]
 - Higgs as a pseudo Nambu-Goldstone boson [Georgi-Kaplan, '84]
- 2 lower the UV scale
 - large extra-dimension [Arkani-Hamed-Dimopoulos-Dvali, '98]
 - 10^{32} species [Dvali '07]
- 3 remove the Higgs
 - technicolor [Weinberg '79, Susskind '79]

Hierarchy problem vs flavor: tension

Clash of Scales

Higgs sector

$$\Lambda < 3\text{-}4 \text{ TeV}$$

Flavor

$$\Lambda > 10^{4\div 5} \text{ TeV}$$

the higher the scale of new physics, the more fine-tuned the Higgs, the less likely a discovery at LHC

Weak

Strong

SM & al.

$H = \text{elem. scalar: dim}=1$

$$\Lambda^2 |H|^2$$

sick when $\Lambda \rightarrow \infty$

$$y_{ij} H q_i \bar{q}_j \quad \& \quad \frac{1}{\Lambda^2} (q_i \bar{q}_j q_k \bar{q}_l)$$

fine when $\Lambda \rightarrow \infty$

Technicolor

$H = \langle q\bar{q} \rangle: \text{dim}=3$

$$\frac{1}{\Lambda^2} |H|^2$$

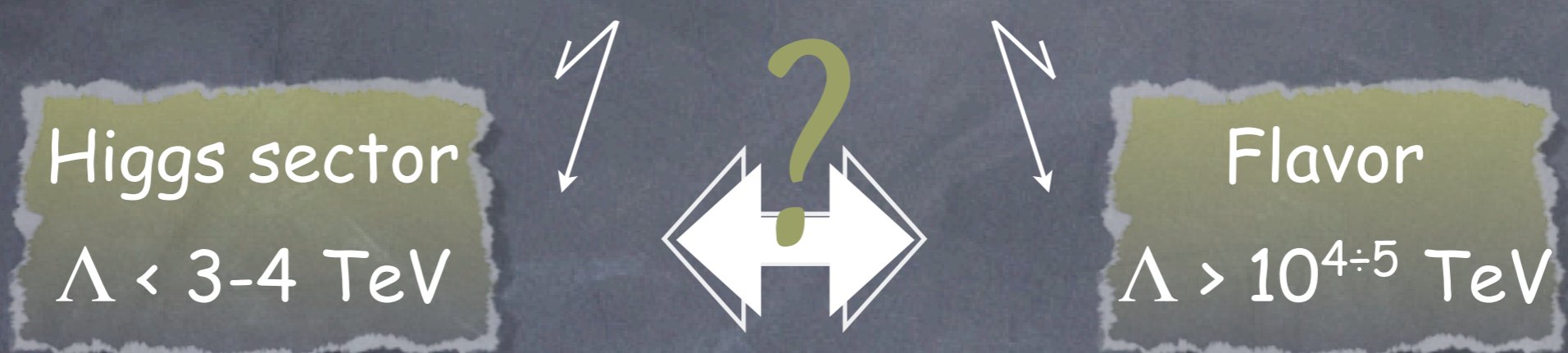
fine when $\Lambda \rightarrow \infty$

$$\frac{1}{\Lambda^2} H q_i \bar{q}_j \quad \& \quad \frac{1}{\Lambda^2} (q_i \bar{q}_j q_k \bar{q}_l)$$

sick when $\Lambda \rightarrow \infty$

Hierarchy problem vs flavor: lesson?

Clash of Scales



Is flavor telling us anything about the solution to the hierarchy problem?

1

conformal TC
 $\dim_H = 1$ but $\dim_{|H|^2} = 4$
 would solve both pbs
 but it seems impossible to realize

[Luty-Okui '04, Rattazzi et al '08]

Weak

SM & al.

$H = \text{elem. scalar: dim}=1$
 $\Lambda^2 |H|^2$
 sick when $\Lambda \rightarrow \infty$

$y_{ij} H q_i \bar{q}_j$ & $\frac{1}{\Lambda^2} (q_i \bar{q}_j q_k \bar{q}_l)$
 fine when $\Lambda \rightarrow \infty$

Strong

Technicolor

$H = \langle q\bar{q} \rangle: \text{dim}=3$
 $\frac{1}{\Lambda^2} |H|^2$
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Hierarchy problem vs flavor: lesson?

Clash of Scales



Is flavor telling us anything about the solution to the hierarchy problem?

1

conformal TC

2

[Kaplan '91]

partial compositeness
 mixing elem. and composite fermions
 $\dim q_{R,L} = 3/2, \dim \mathcal{O}_{R,L} = d_{R,L}$

$$\frac{q_L \mathcal{O}_R}{\Lambda_R^{d_R - 5/2}} + \frac{q_R \mathcal{O}_L}{\Lambda_L^{d_R - 5/2}} + \frac{\mathcal{O}_L \mathcal{O}_R}{\Lambda^{d_L + d_R - 4}}$$

$d_{R,L} \approx 5/2$ solves the flavor pb

Weak

SM & al.

$H = \text{elem. scalar: dim}=1$
 $\Lambda^2 |H|^2$
 sick when $\Lambda \rightarrow \infty$

$y_{ij} H q_i \bar{q}_j$ & $\frac{1}{\Lambda^2} (q_i \bar{q}_j q_k \bar{q}_l)$
 fine when $\Lambda \rightarrow \infty$

Strong

Technicolor

$H = \langle q \bar{q} \rangle: \text{dim}=3$
 $\frac{1}{\Lambda^2} |H|^2$
 fine when $\Lambda \rightarrow \infty$

$\frac{1}{\Lambda^2} H q_i \bar{q}_j$ & $\frac{1}{\Lambda^2} (q_i \bar{q}_j q_k \bar{q}_l)$
 sick when $\Lambda \rightarrow \infty$

Partial compositeness: fermion masses

partial compositeness
 mixing elem. and composite fermions
 $\dim q_{R,L}=3/2, \dim \mathcal{O}_{R,L}=d_{R,L}$

$$\frac{q_L \mathcal{O}_R}{\Lambda_R^{d_R-5/2}} + \frac{q_R \mathcal{O}_L}{\Lambda_L^{d_R-5/2}} + \frac{\mathcal{O}_L \mathcal{O}_R}{\Lambda^{d_L+d_R-4}}$$

integrating out heavy fields

amount of
 compositeness
 $f_{q_{L,R}}$

$$\frac{\Lambda_R \Lambda_L}{\Lambda} \left(\frac{\Lambda}{\Lambda_R} \right)^{d_R} \left(\frac{\Lambda}{\Lambda_L} \right)^{d_L} q_L q_R$$

1 fermion mass hierarchy easily generated by small diff. in anomalous dims

2 alignment mixing angles/masses is also explained

$$V_{CKM} \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

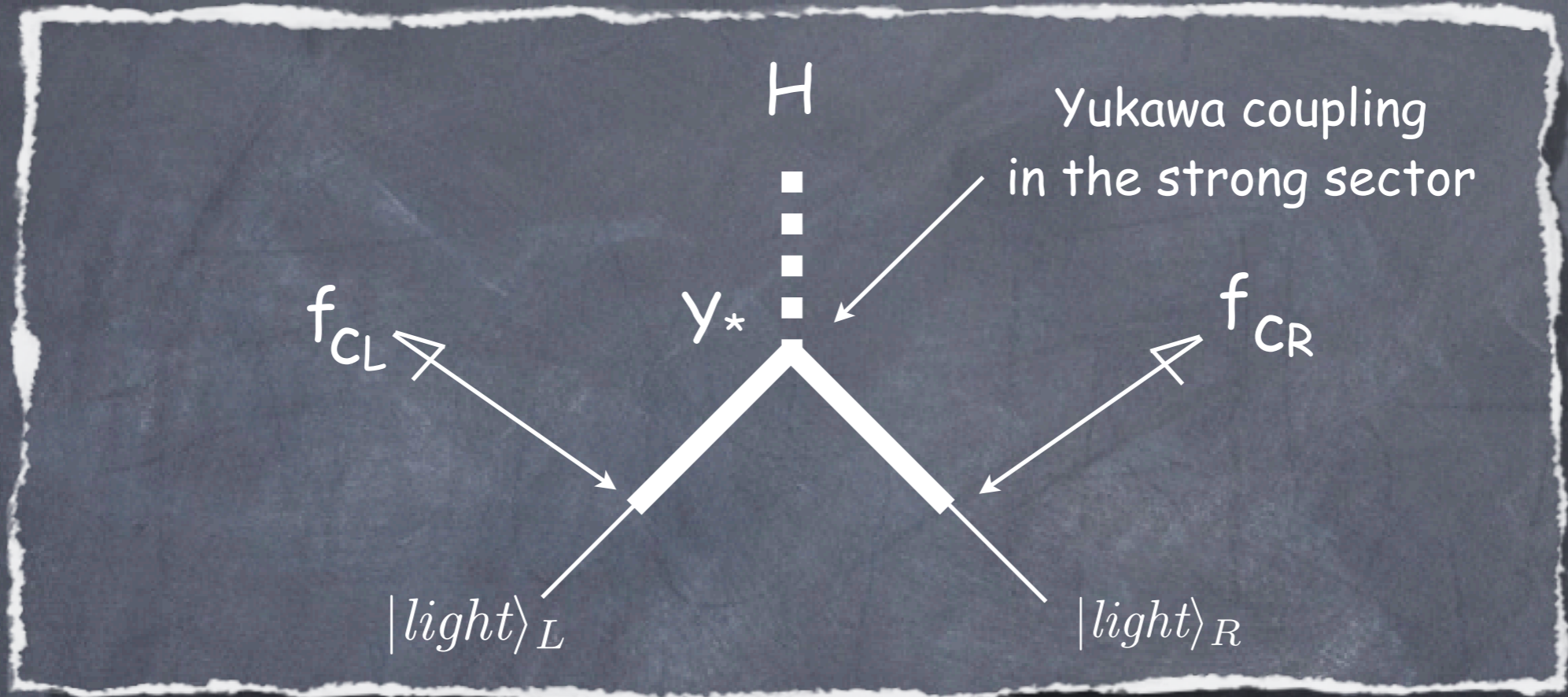
$$m_{u_i} \propto f_{q_i} f_{u_i}$$

$$m_{d_i} \propto f_{q_i} f_{d_i}$$

$$V_{CKM}^{ij} \sim f_{q_i} / f_{q_j}$$

Partial Compositeness: fermion masses

Higgs part of the strong sector: it couples only to composite fermions



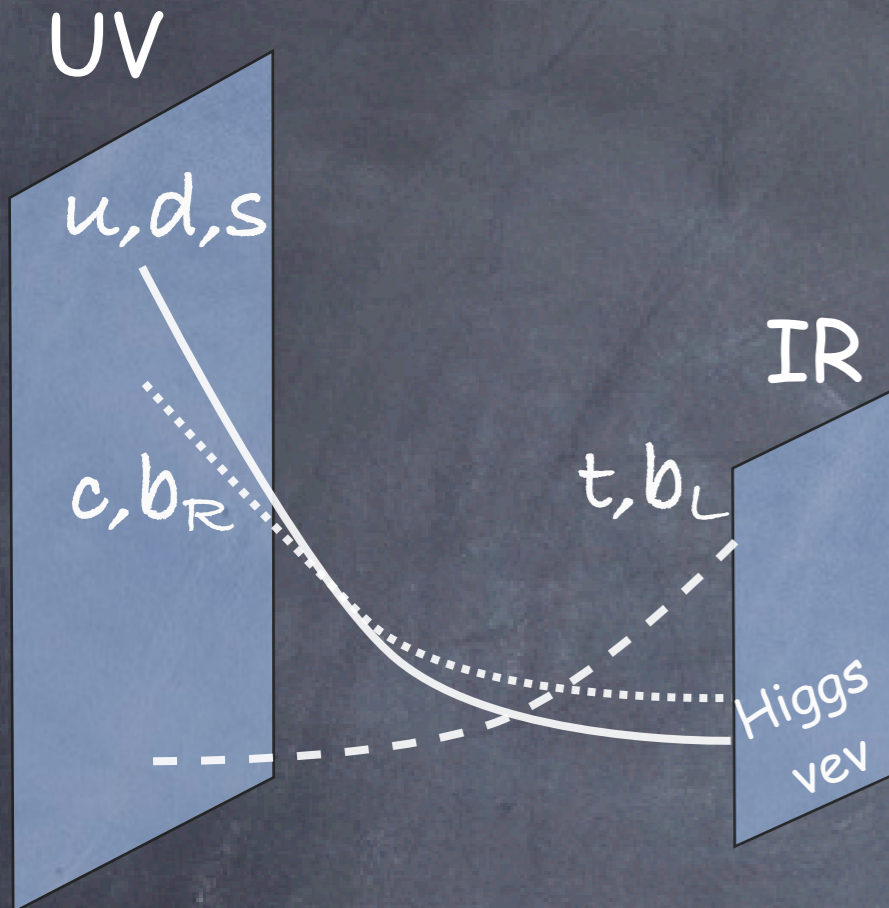
when the Higgs gets a vev, the light dof will acquire a mass prop. to

$$Y^{eff} = Y_{\star} f_{CL} f_{CR}$$

Yukawa hierarchy comes from the hierarchy of compositeness
the lighter the fermion, the less coupled to the strong sector

Partial compositeness: xdim realization

[Grossman and Neubert, '00]
 [Gherghetta and Pomarol, '00]
 [Huber, '03]



fermion zero-mode has
 an exponential profile
 in the bulk

$$\chi(z) = \frac{f_c}{\sqrt{R'}} \left(\frac{z}{R}\right)^2 \left(\frac{z}{R'}\right)^{-c}$$

f_c is the "value" of wavefct. on the IR:

$$f_c = \sqrt{\frac{1-2c}{1-(R/R')^{1-2c}}}$$

$c < 1/2$: heavy fermion
 $f_c \sim \mathcal{O}(1)$

$c > 1/2$: light fermion
 $f_c \sim (R/R')^{c-1/2} \ll 1$

light fermion exponentially localized on the UV brane

⇒ overlap with Higgs vev on the IR tiny

⇒ exponentially small 4D mass

UV localized fermion=elementary

IR localized fermion=composite

5D models=weakly coupled dual of 4D strongly models

Holographic Models of EWSB

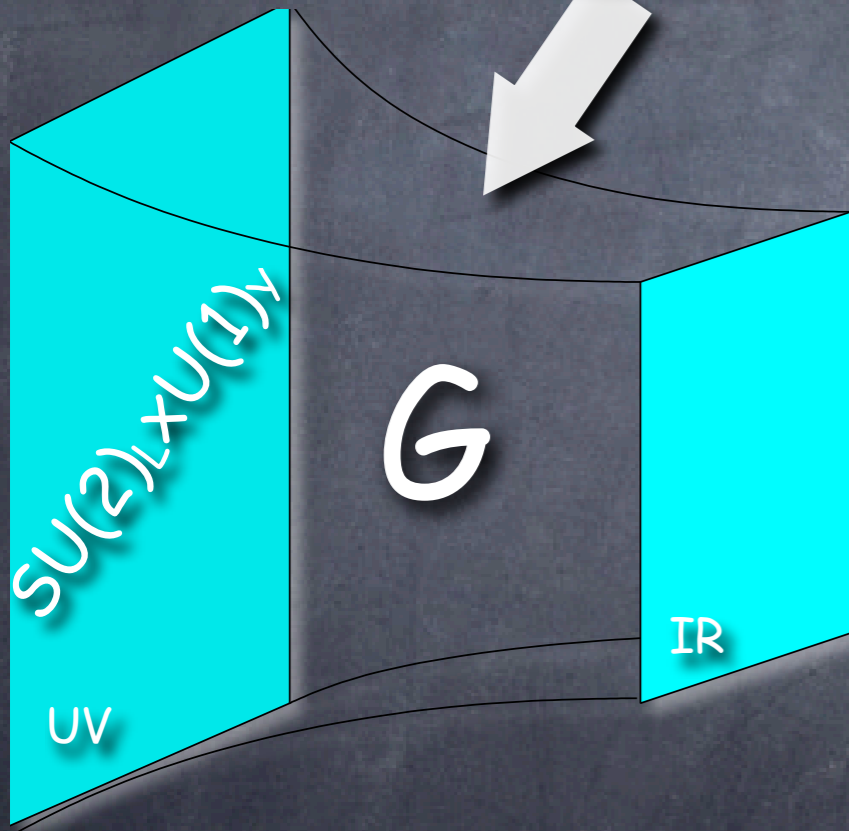
Bulk gauge fields: [Pomarol, '00]

Holographic technicolor=Higgsless: [Csaki et al., '03]

Holographic composite Higgs: [Agashe et al., '04]

Gauge fields + fermions
in the bulk

Higgs on the IR brane
or
Gauge breaking by
boundary conditions



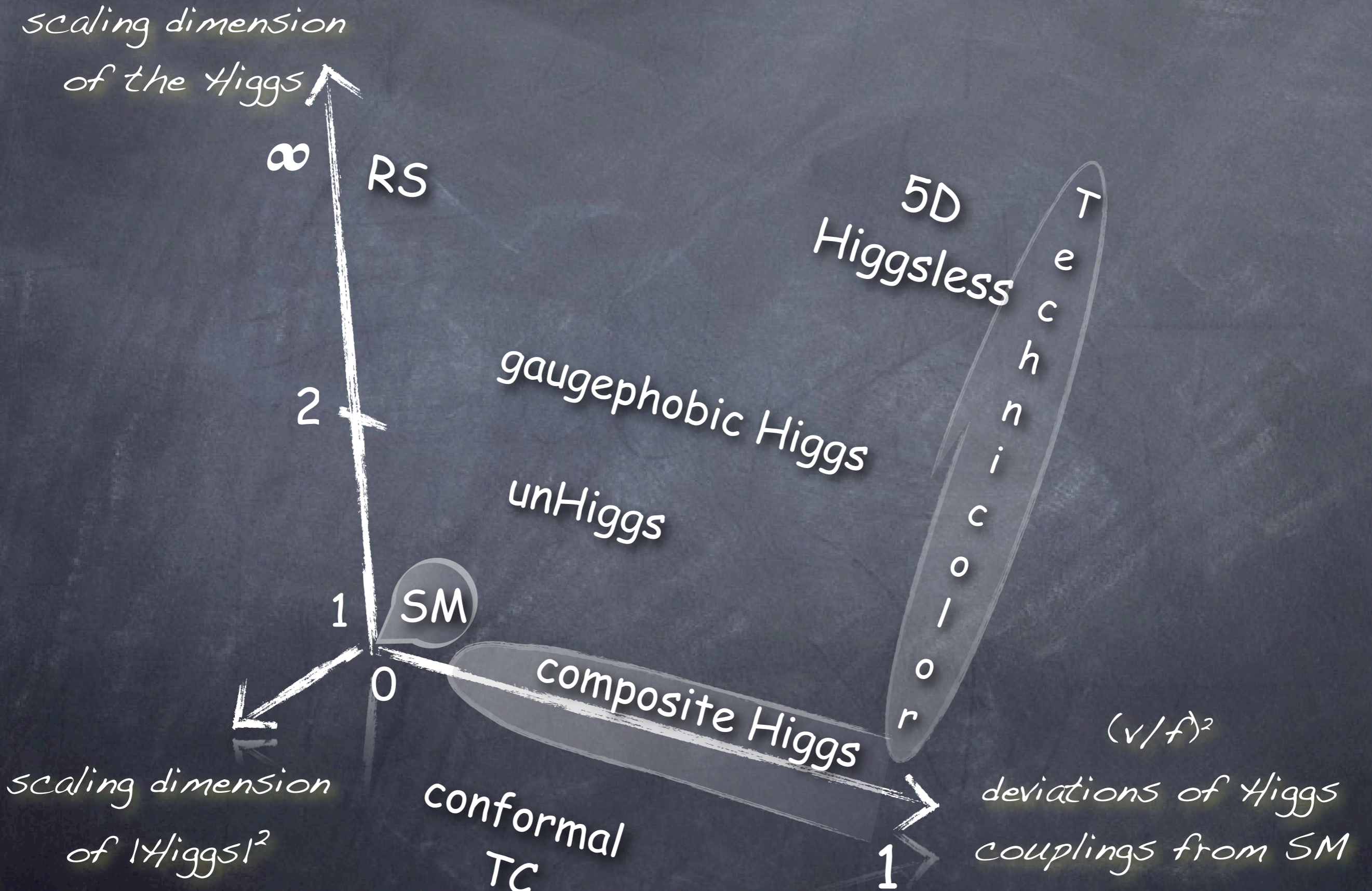
$$G = SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

$$G = SO(5) \times U(1)_X$$

$$G = SO(6) \times U(1)_X$$

- UV completion: log running of gauge couplings
- Custodial symmetry from bulk $SU(2)_R$

A multi-dimensional deformation of the SM

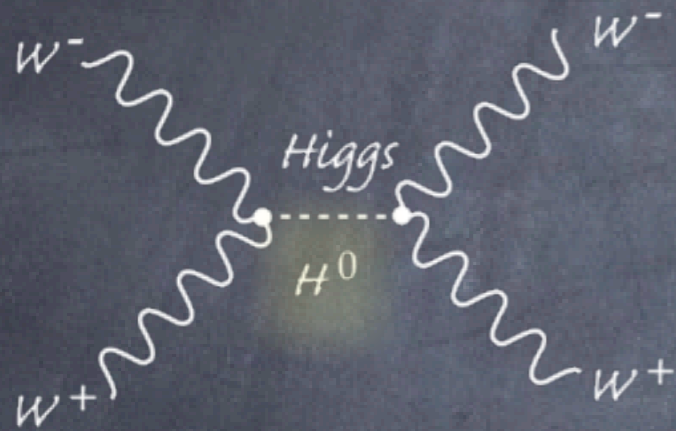


SM Higgs as a peculiar scalar resonance

A single scalar degree of freedom with no charge under $SU(2)_L \times U(1)_Y$

$$\mathcal{L}_{\text{EWSB}} = a \frac{v}{2} h \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) + b \frac{1}{4} h^2 \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma)$$

'a' and 'b' are arbitrary free couplings



$$\mathcal{A} = \frac{1}{v^2} \left(s - \frac{a^2 s^2}{s - m_h^2} \right)$$

growth cancelled for
 $a = 1$
restoration of
perturbative unitarity

For $b = a^2$: perturbative unitarity also maintained in inelastic channels

'a=1' & 'b=1' define the SM Higgs

$\mathcal{L}_{\text{mass}} + \mathcal{L}_{\text{EWSB}}$ can be rewritten as $D_\mu H^\dagger D_\mu H$

$$H = \frac{1}{\sqrt{2}} e^{i\sigma^a \pi^a / v} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

h and π^a (ie W_L and Z_L) combine to form a linear representation of $SU(2)_L \times U(1)_Y$

Higgs properties depend on a single unknown parameter (m_H)

Continuous interpolation between SM and TC

$$\xi = \frac{v^2}{f^2} = \frac{(\text{weak scale})^2}{(\text{strong coupling scale})^2}$$

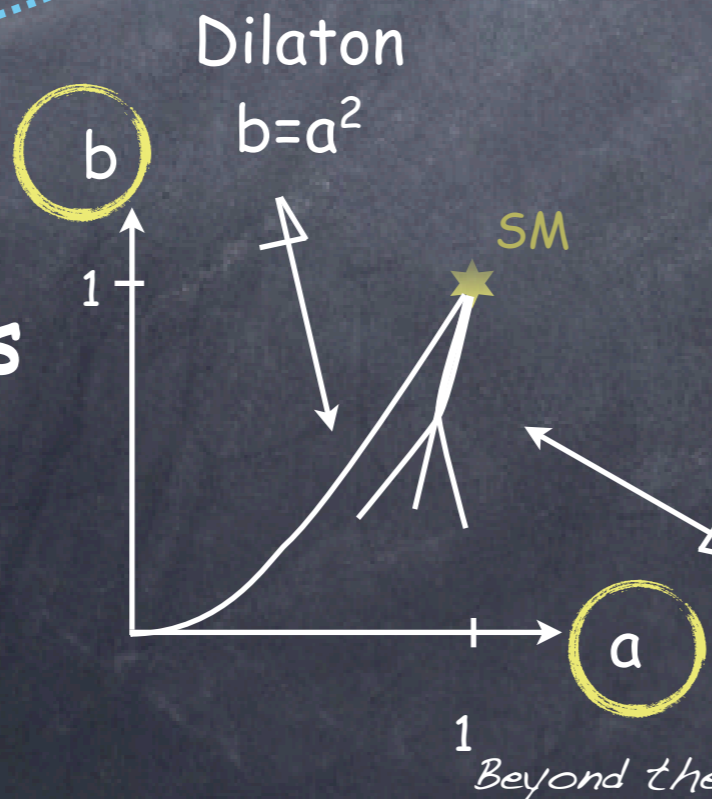
$\xi = 0$
SM limit

all resonances of strong sector, except the Higgs, decouple

$\xi = 1$
Technicolor limit

Higgs decouple from SM; vector resonances like in TC

Composite Higgs vs. SM Higgs

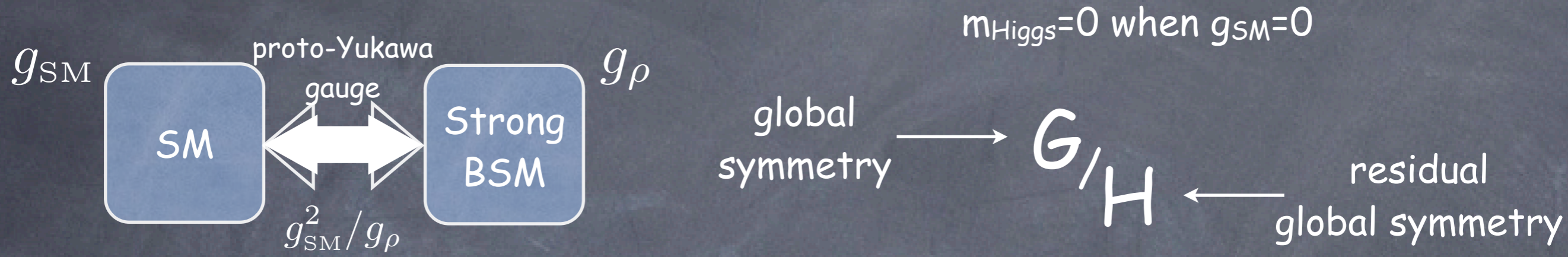


$$\mathcal{L}_{\text{EWSB}} = \left(a \frac{v}{2} h + b \frac{1}{4} h^2 \right) \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma)$$

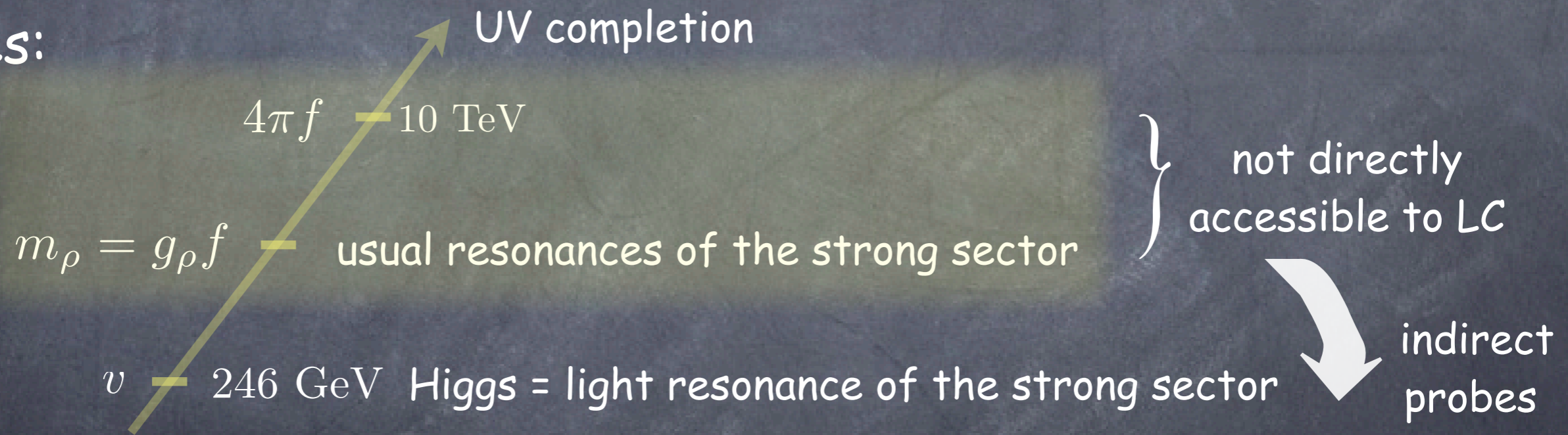
Composite Higgs universal behavior for large f
 $a=1-v/2f$ $b=1-2v/f$

How to obtain a light composite Higgs?

Higgs=Pseudo-Goldstone boson of the strong sector



3 scales:



strong sector broadly characterized by 2 parameters

m_{ρ} = mass of the resonances

g_{ρ} = coupling of the strong sector or decay cst of strong sector $f = \frac{m_{\rho}}{g_{\rho}}$

Testing the composite nature of the Higgs?

if LHC sees a Higgs and nothing else*:
is it elementary or composite?

??? evidence for fine-tuning & string landscape ???

??? Higgs forces have a secret hidden gauge origin ???

- **Model-dependent:** production of resonances at m_ρ
- **Model-independent:** study of Higgs properties & W scattering
 - strong WW scattering
 - strong HH production
 - Higgs anomalous coupling
 - anomalous gauge bosons self-couplings

* a likely possibility that precision data seems to point to,
at least in strongly coupled models

What distinguishes a composite Higgs?

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

$$U = e^{i \begin{pmatrix} & H/f \\ H^\dagger/f & \end{pmatrix}} U_0$$

$$f^2 \text{tr} (\partial_\mu U^\dagger \partial^\mu U) = |\partial_\mu H|^2 + \frac{\#}{f^2} (\partial |H|^2)^2 + \frac{\#}{f^2} |H|^2 |\partial H|^2 + \frac{\#}{f^2} |H^\dagger \partial H|^2$$

Anomalous Higgs Couplings

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

$$H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \Rightarrow \mathcal{L} = \frac{1}{2} \left(1 + c_H \frac{v^2}{f^2} \right) (\partial^\mu h)^2 + \dots$$

Modified
Higgs propagator

\sim

Higgs couplings
rescaled by

$$\frac{1}{\sqrt{1 + c_H \frac{v^2}{f^2}}} \sim 1 - c_H \frac{v^2}{2f^2} \equiv 1 - \xi/2$$

SILH Effective Lagrangian

(strongly-interacting light Higgs)

Giudice, Grojean, Pomarol, Rattazzi '07

extra Higgs leg: H/f

extra derivative: ∂/m_ρ

Genuine strong operators (sensitive to the scale f)

$$\frac{c_H}{2f^2} (\partial_\mu (|H|^2))^2$$

$$\frac{c_T}{2f^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right)^2$$

custodial breaking

$$\frac{c_y y_f}{f^2} |H|^2 \bar{f}_L H f_R + \text{h.c.}$$

$$\frac{c_6 \lambda}{f^2} |H|^6$$

Form factor operators (sensitive to the scale m_ρ)

$$\frac{i c_W}{2m_\rho^2} \left(H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i$$

$$\frac{i c_B}{2m_\rho^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu})$$

$$\frac{i c_{HW}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i$$

$$\frac{i c_{HB}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

minimal coupling: $h \rightarrow \gamma Z$

loop-suppressed strong dynamics

$$\frac{c_\gamma}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\frac{c_g}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$$

Goldstone sym.

EWPT constraints

$$\hat{T} = c_T \frac{v^2}{f^2} \implies |c_T \frac{v^2}{f^2}| < 2 \times 10^{-3} \quad \text{removed by custodial symmetry}$$

$$\hat{S} = (c_W + c_B) \frac{m_W^2}{m_\rho^2} \implies m_\rho \geq (c_W + c_B)^{1/2} 2.5 \text{ TeV}$$

There are also some 1-loop IR effects

Barbieri, Bellazzini, Rychkov, Varagnolo '07

$$\hat{S}, \hat{T} = a \log m_h + b$$

modified Higgs couplings to matter

$$\hat{S}, \hat{T} = a \left((1 - c_H \xi) \log m_h + c_H \xi \log \Lambda \right) + b$$

effective Higgs mass

$$m_h^{eff} = m_h \left(\frac{\Lambda}{m_h} \right)^{c_H v^2 / f^2} > m_h$$

LEP II, for $m_h \sim 115 \text{ GeV}$: $c_H v^2 / f^2 < 1/3 \sim 1/2$

IR effects can be cancelled by heavy fermions (model dependent)

Flavor Constraints

$$\left(1 + \frac{c_{ij}|H|^2}{f^2}\right) y_{ij} \bar{f}_{Li} H f_{Rj} = \left(1 + \frac{c_{ij}v^2}{2f^2}\right) \frac{y_{ij}v}{\sqrt{2}} \bar{f}_{Li} f_{Rj} + \left(1 + \frac{3c_{ij}v^2}{2f^2}\right) \frac{y_{ij}}{\sqrt{2}} h \bar{f}_{Li} f_{Rj}$$

mass terms \nearrow

Higgs fermion interactions \nearrow

mass and interaction matrices are not diagonalizable simultaneously
if c_{ij} are arbitrary

\Rightarrow FCNC

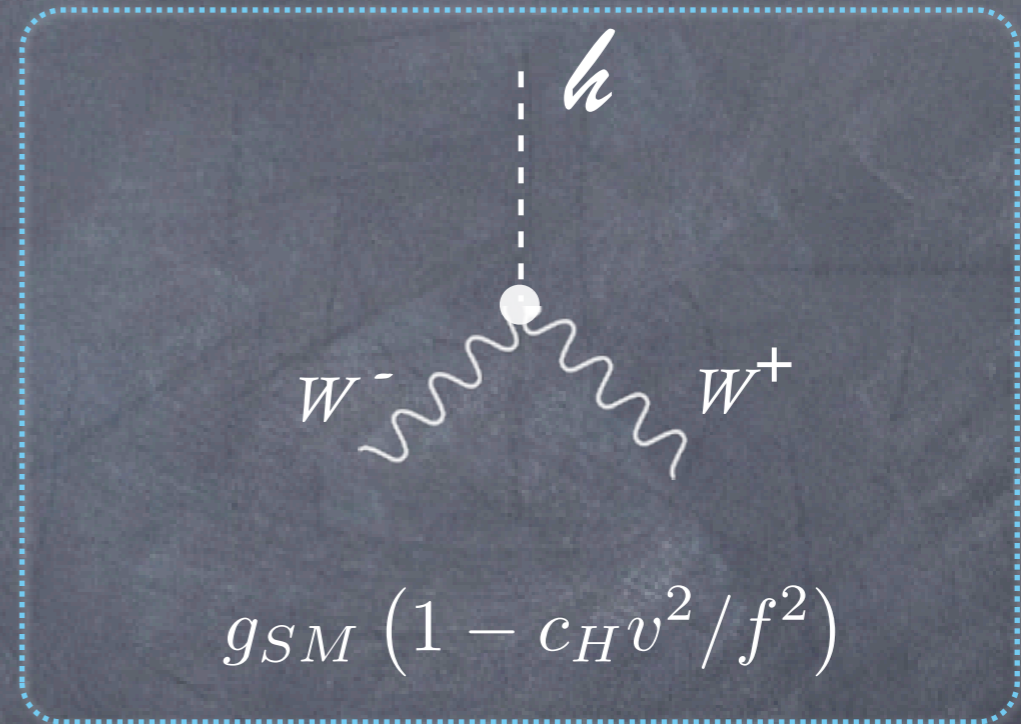
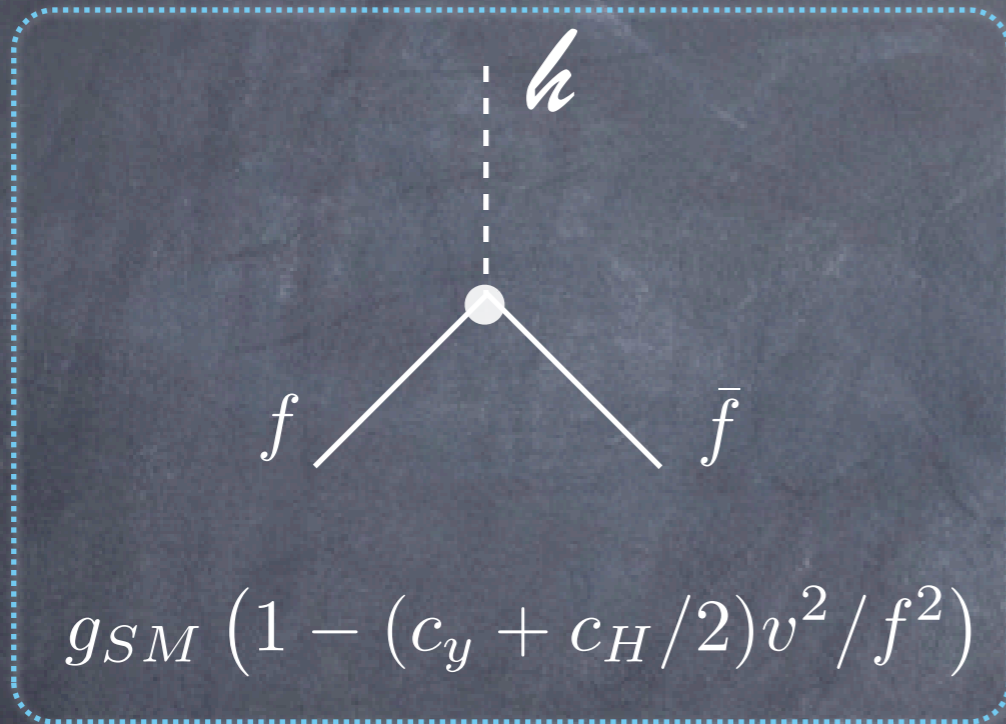
SILH: c_y is flavor universal

\Rightarrow Minimal flavor violation built in

Higgs anomalous couplings

Lagrangian in unitary gauge

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \left(-\frac{m_H^2}{2v} (c_6 - 3c_H/2) h^3 + \frac{m_f}{v} \bar{f} f (c_y + c_H/2) h - c_H \frac{m_W^2}{v} h W_\mu^+ W^{-\mu} - c_H \frac{m_Z^2}{v} h Z_\mu Z^\mu \right) \frac{v^2}{f^2} + \dots$$



$$\Gamma(h \rightarrow f\bar{f})_{\text{SILH}} = \Gamma(h \rightarrow f\bar{f})_{\text{SM}} \left[1 - (2c_y + c_H) v^2 / f^2 \right]$$

$$\Gamma(h \rightarrow gg)_{\text{SILH}} = \Gamma(h \rightarrow gg)_{\text{SM}} \left[1 - (2c_y + c_H) v^2 / f^2 \right]$$

Note: same Lorentz structure as in SM. Not true anymore if form factor ops. are included

Higgs anomalous couplings for large v/f

The SILH Lagrangian is an expansion for small v/f

The 5D MCHM gives a completion for large v/f

$$m_W^2 = \frac{1}{4} g^2 f^2 \sin^2 v/f \quad \Rightarrow \quad g_{hWW} = \sqrt{1 - \xi} g_{hWW}^{\text{SM}}$$

Fermions embedded in spinorial of $SO(5)$

$$m_f = M \sin v/f$$



$$g_{hff} = \sqrt{1 - \xi} g_{hff}^{\text{SM}}$$

universal shift of the couplings
no modifications of BRs

$$\left(\xi = v^2/f^2 \right)$$

Fermions embedded in 5+10 of $SO(5)$

$$m_f = M \sin 2v/f$$



$$g_{hff} = \frac{1 - 2\xi}{\sqrt{1 - \xi}} g_{hff}^{\text{SM}}$$

BRs now depends on v/f

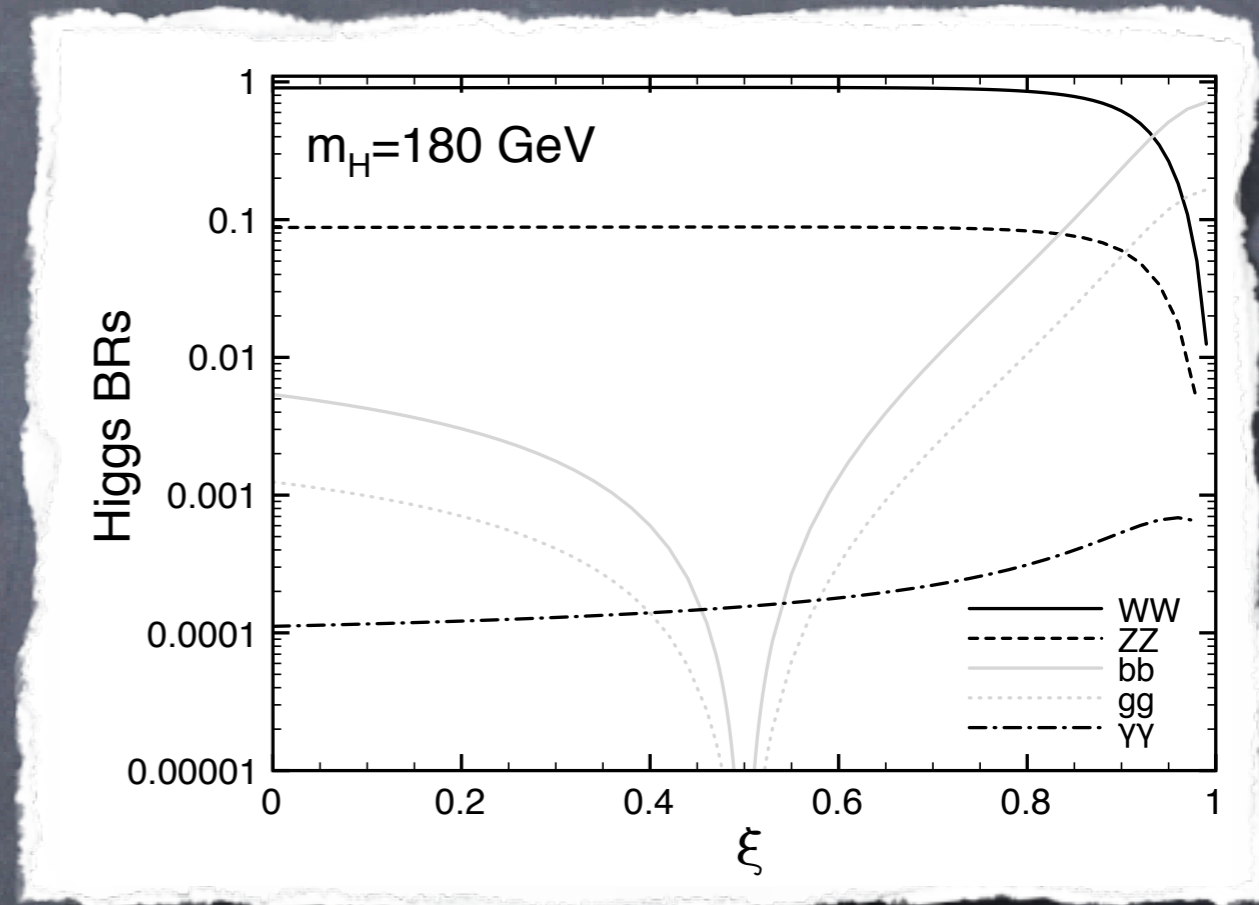
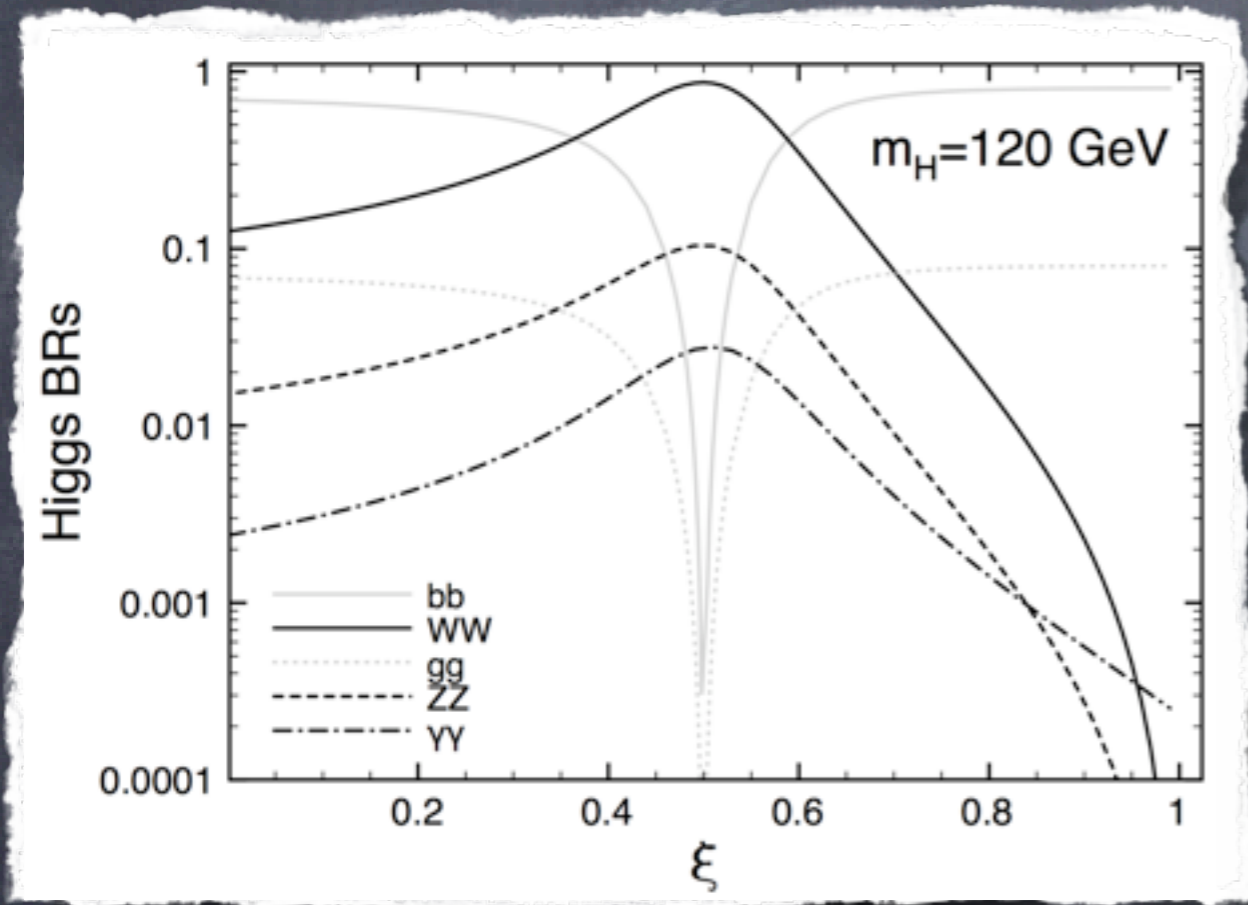
MCHM4

MCHM5

Higgs BRs

Fermions embedded in 5+10 of $SO(5)$

MC4/M5



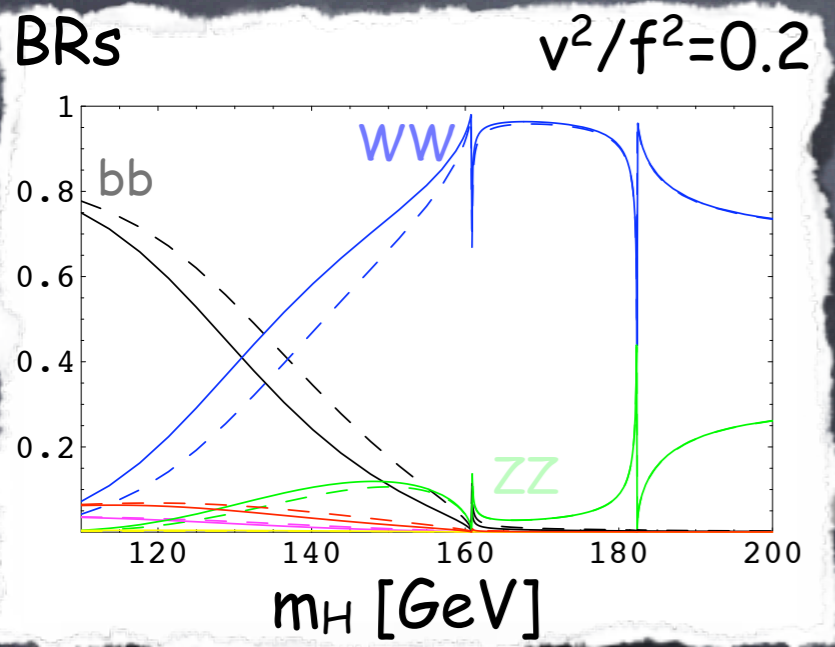
$h \rightarrow WW$ can dominate even for low Higgs mass

BRs remain SM like except for very large values of v/f

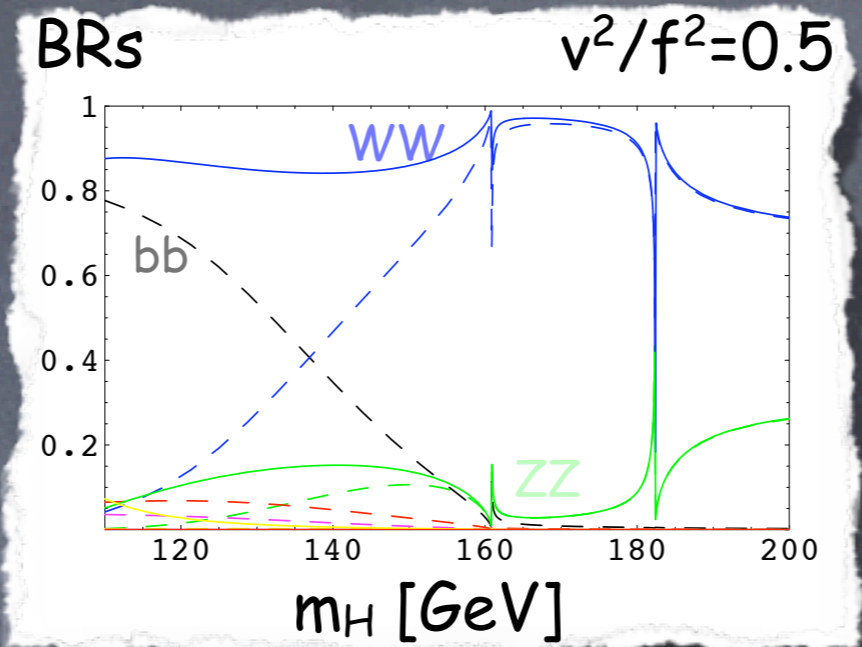
Higgs BRs and total width

Fermions embedded in 5+10 of $SO(5)$

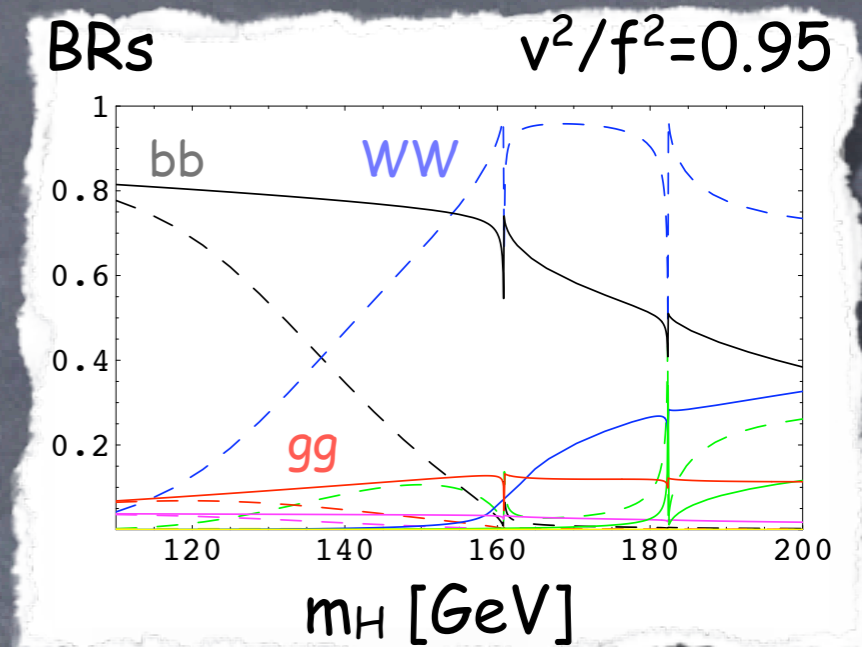
MCHM5



slight modifications

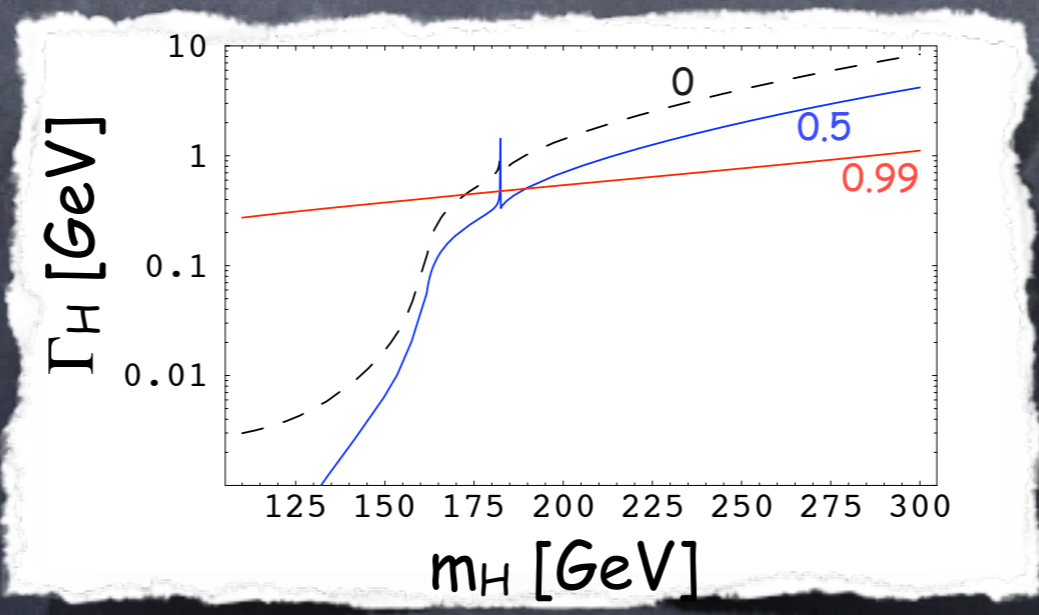


suppress bb



suppress WW

Higgs total width



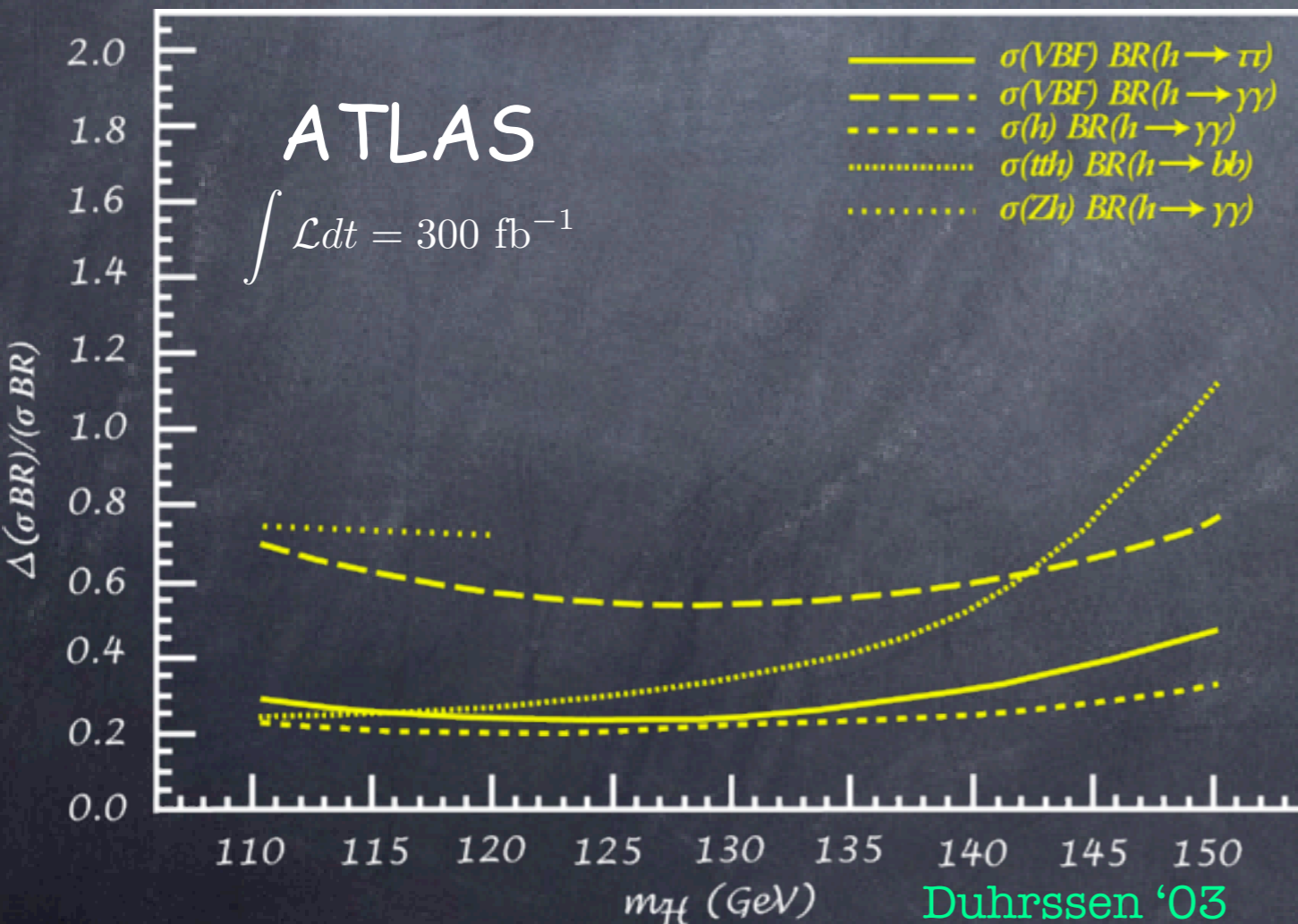
Beyond the Higgs

Higgs anomalous couplings @ LHC

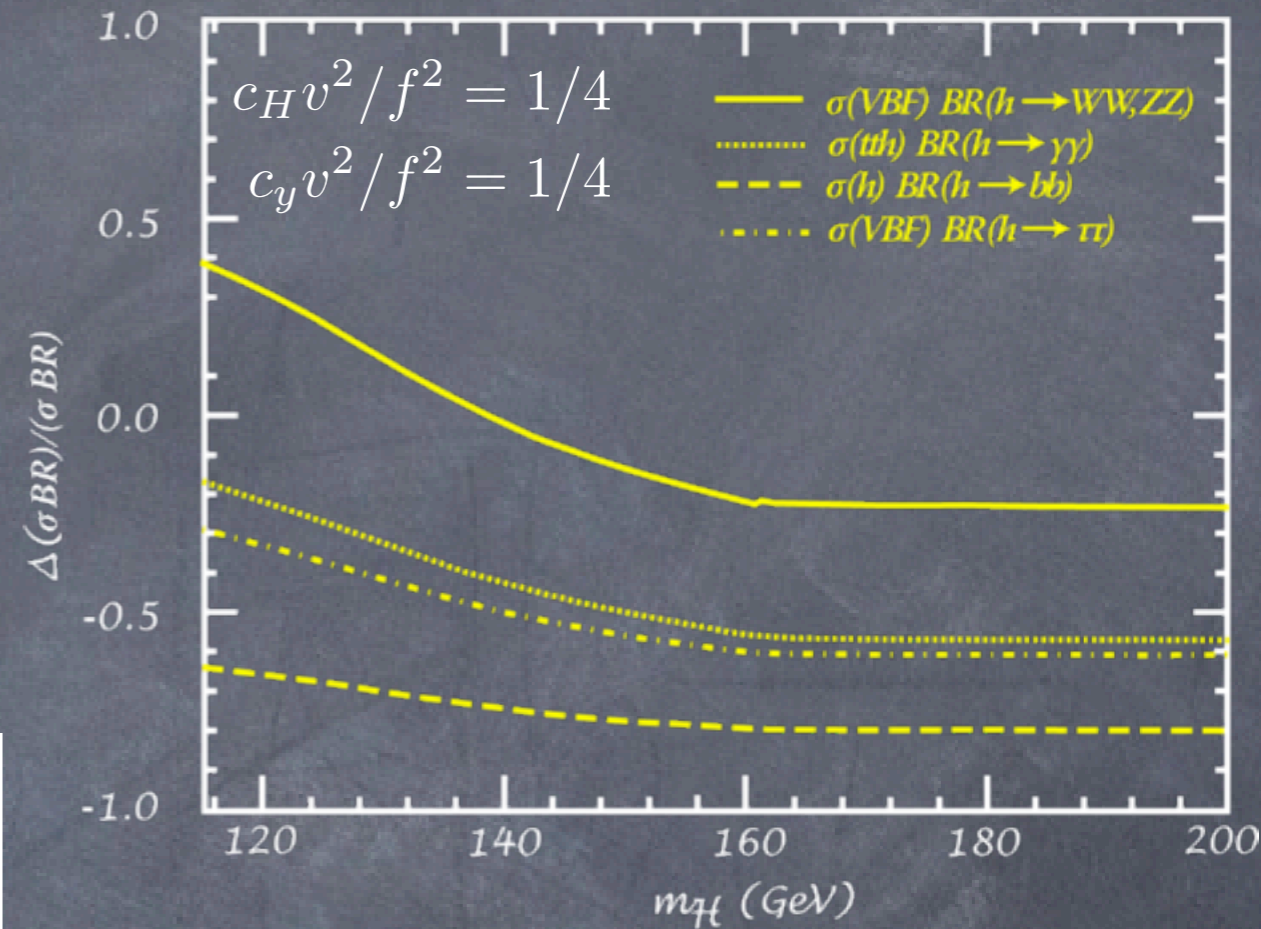
$$\Gamma(h \rightarrow f\bar{f})_{\text{SILH}} = \Gamma(h \rightarrow f\bar{f})_{\text{SM}} \left[1 - (2c_y + c_H) v^2 / f^2 \right]$$

$$\Gamma(h \rightarrow gg)_{\text{SILH}} = \Gamma(h \rightarrow gg)_{\text{SM}} \left[1 - (2c_y + c_H) v^2 / f^2 \right]$$

observable @ LHC?



Duhrssen '03



LHC can measure

$$c_H \frac{v^2}{f^2}, \quad c_y \frac{v^2}{f^2}$$

up to 0.2-0.4

i.e. $4\pi f \sim 5 - 7 \text{ TeV}$

(ILC could go to few % ie
 test composite Higgs up to $4\pi f \sim 30 \text{ TeV}$)

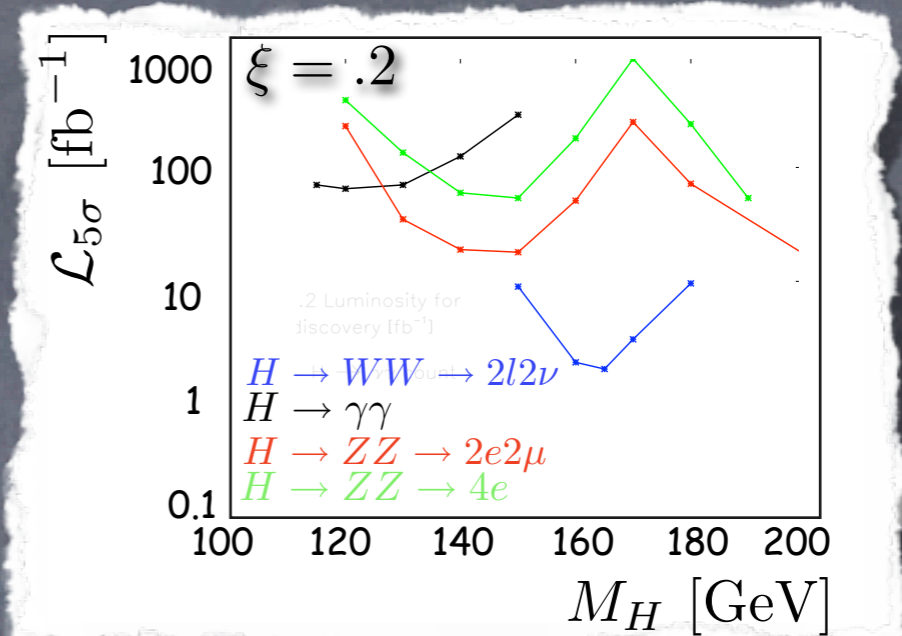
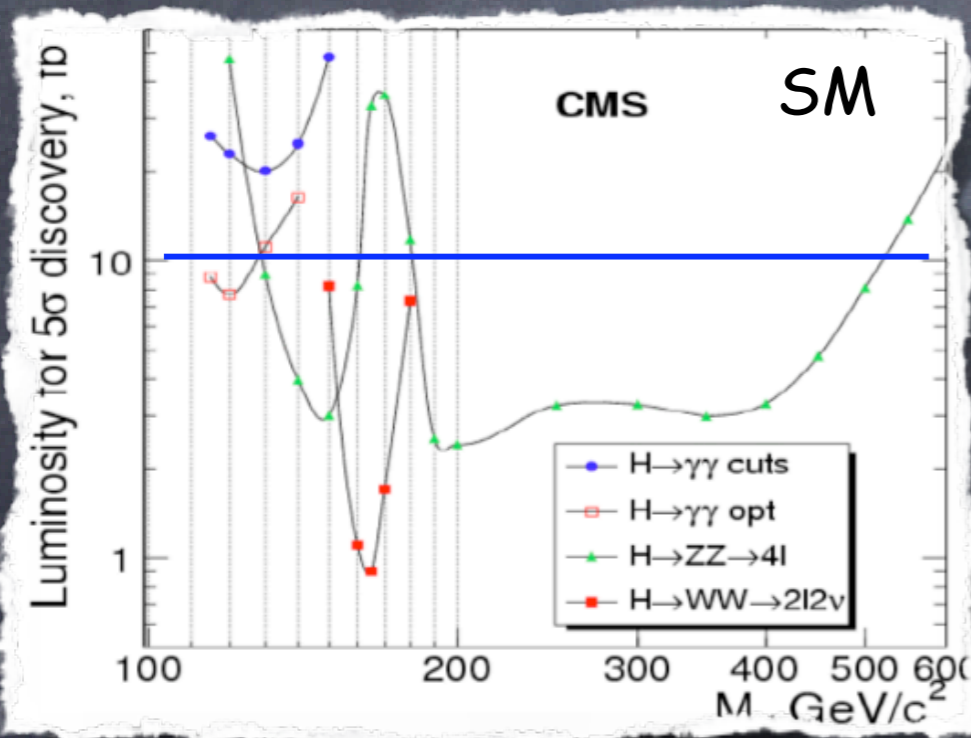
Composite Higgs search @ LHC

[Espinosa, Grojean, Muehlleitner 'to appear']

the modification of Higgs couplings and BRs affects the Higgs search

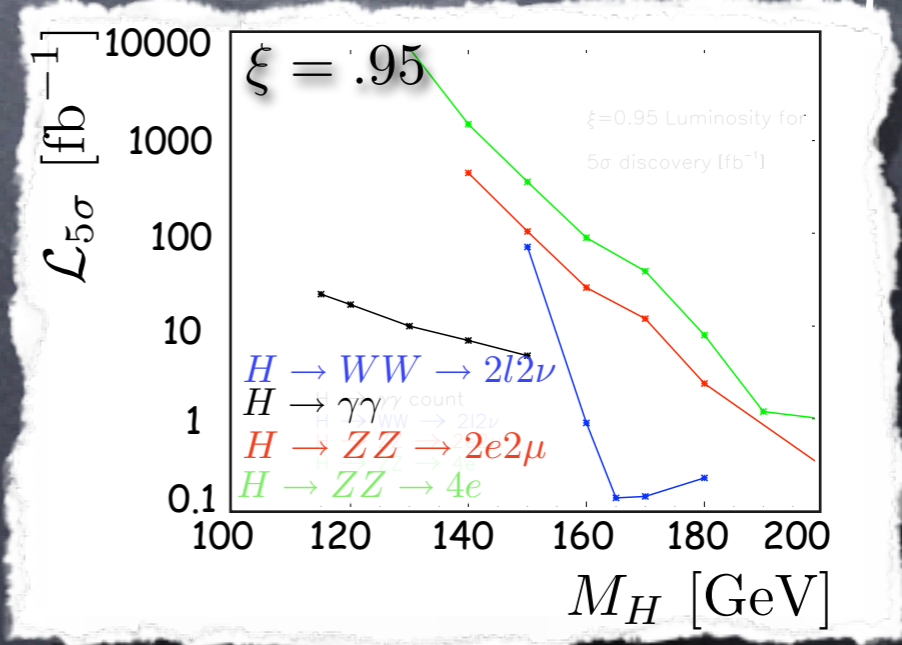
MCHMs

large compositeness scale



more luminosity required
less luminosity required

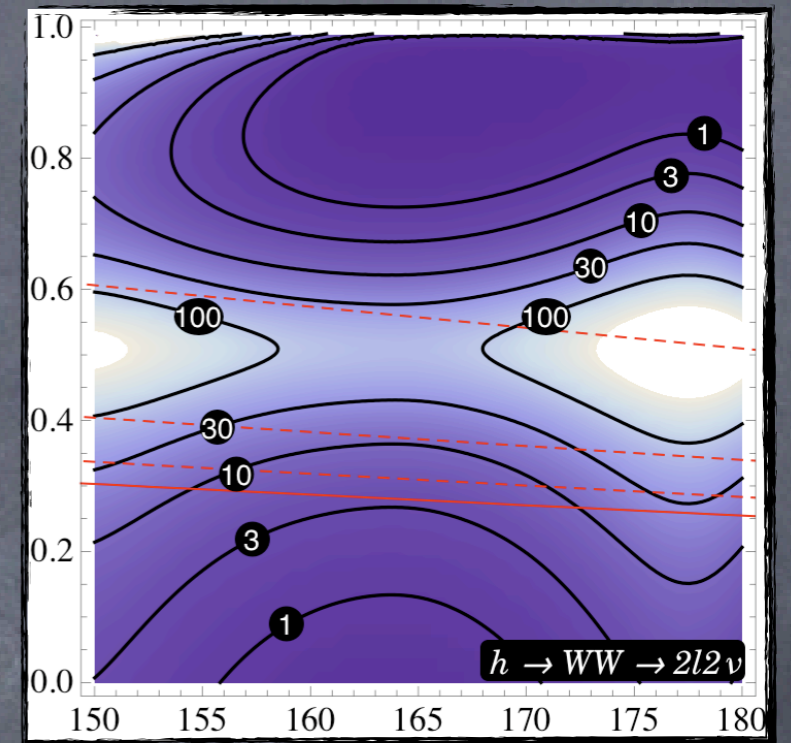
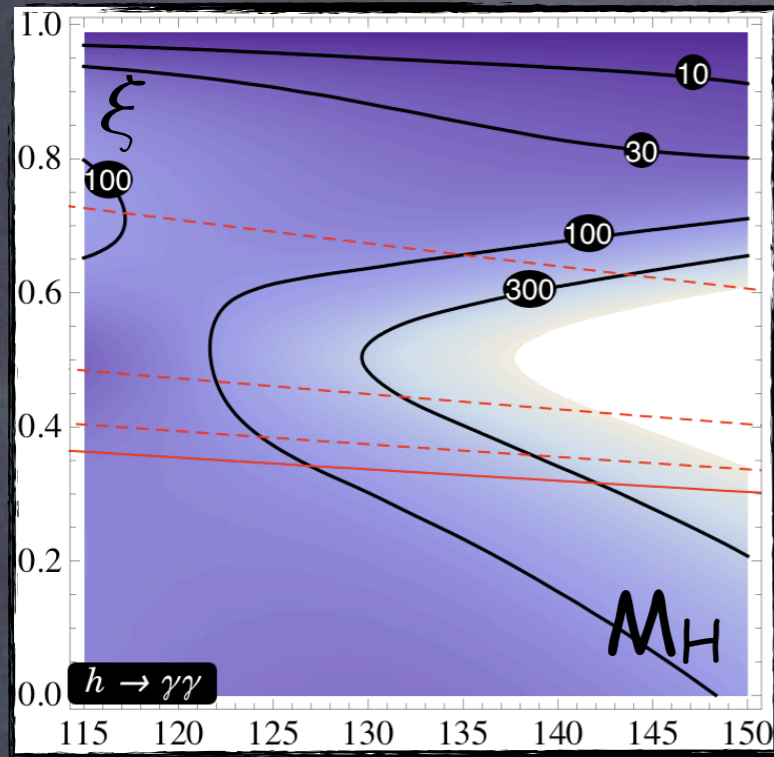
small compositeness scale



Composite Higgs search @ LHC

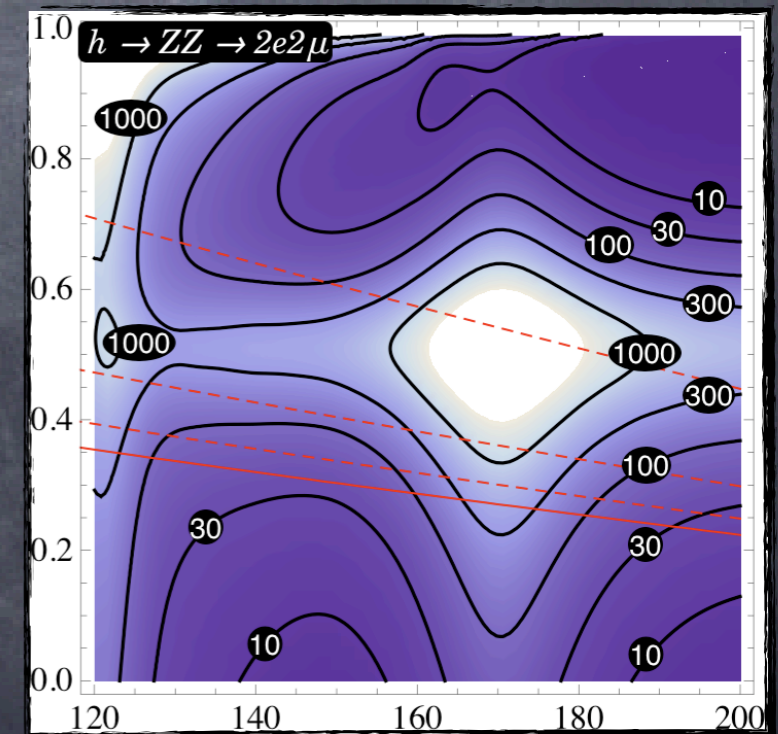
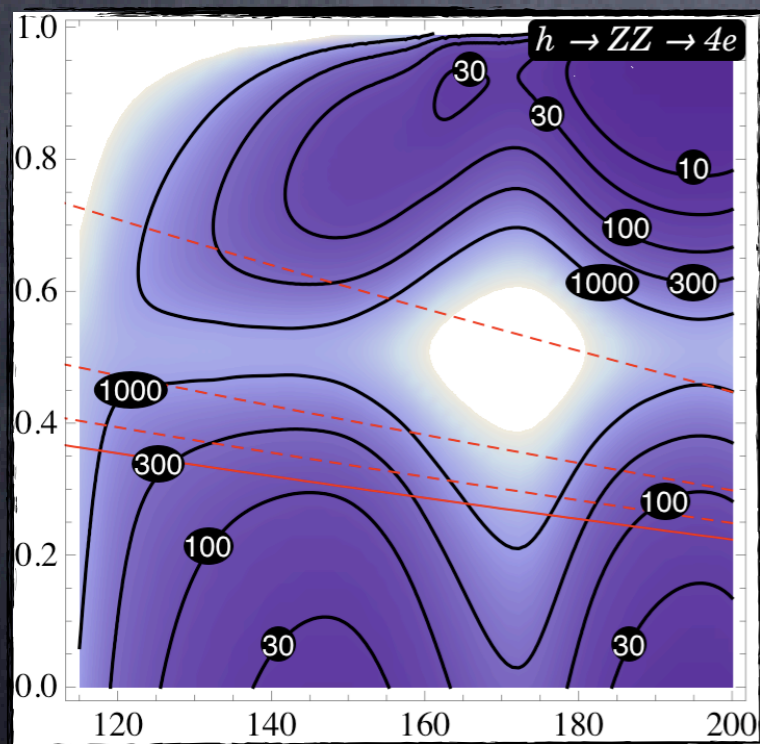
[Espinosa, Grojean, Muehlleitner 'to appear']

the modification of Higgs couplings and BRs affects the Higgs search



MCHM5

contour lines of
luminosity needed
for 5σ discovery
in the (ξ, M_H) plane



(neglect effects from heavy resonances)

Triple gauge boson couplings (TGC) @ LC

$$\mathcal{L}_V = -ig \cos \theta_W g_1^Z Z^\mu (W^{+\nu} W_{\mu\nu}^- - W^{-\nu} W_{\mu\nu}^+) - ig (\cos \theta_W \kappa_Z Z^{\mu\nu} + \sin \theta_W \kappa_\gamma A^{\mu\nu}) W_\mu^+ W_\nu^-$$

TGC are generated by heavy resonances

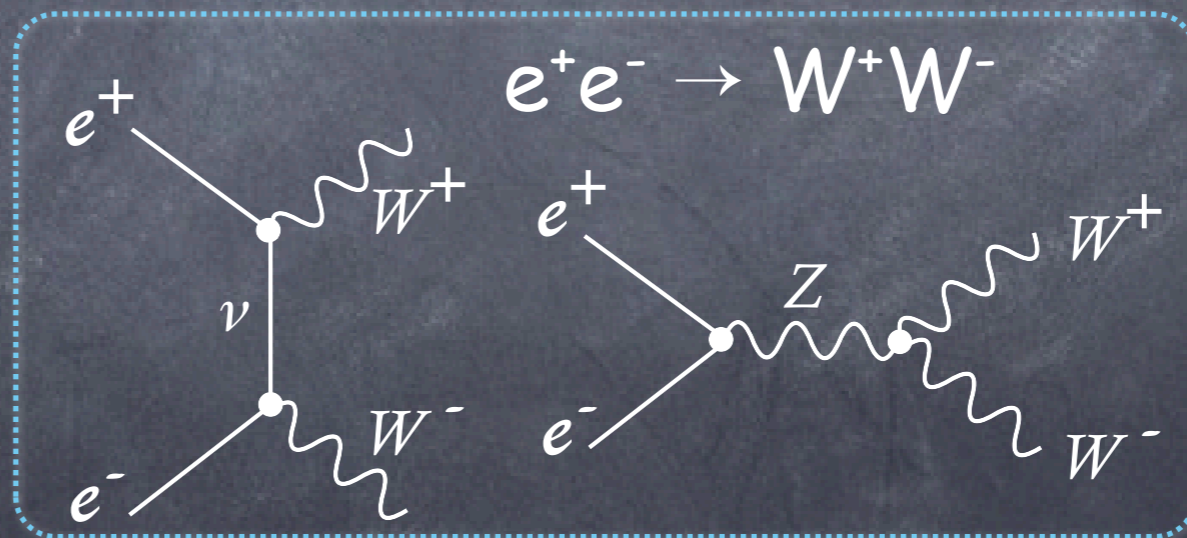
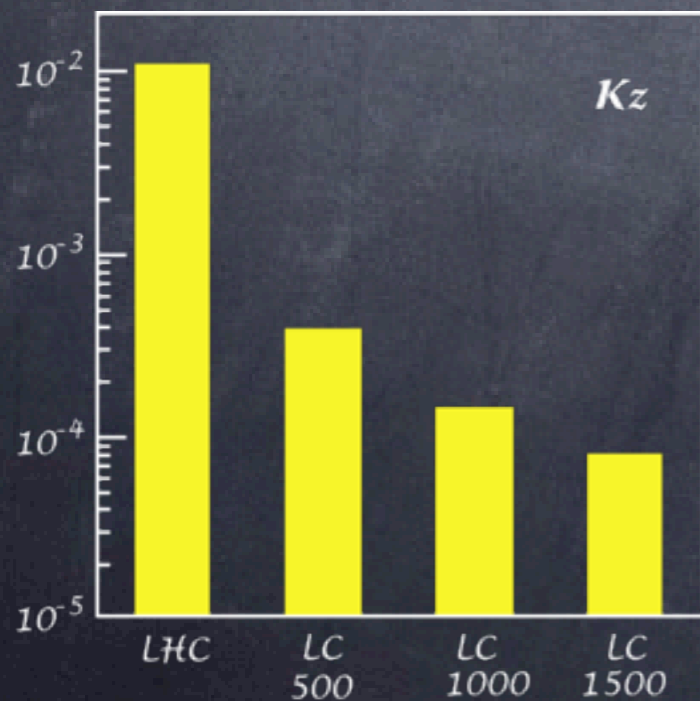
$$g_1^Z = \frac{m_Z^2}{m_\rho^2} c_W \quad \kappa_\gamma = \frac{m_W^2}{m_\rho^2} \left(\frac{g_\rho}{4\pi} \right)^2 (c_{HW} + c_{HB}) \quad \kappa_Z = g_1^Z - \tan^2 \theta_W \kappa_\gamma$$

@ LHC 100fb^{-1} $g_1^Z \sim 1\%$ $\kappa_\gamma \sim \kappa_Z \sim 5\%$

sensitive to resonance
up to $m_\rho \sim 800 \text{ GeV}$

not competitive with the measure of S at LEP II

@ ILC



0.1% accuracy \Rightarrow

sensitive to resonance
up to $m_\rho \sim 8 \text{ TeV}$

T. Abe et al, Snowmass '01

Beyond the Higgs

Strong WW scattering

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

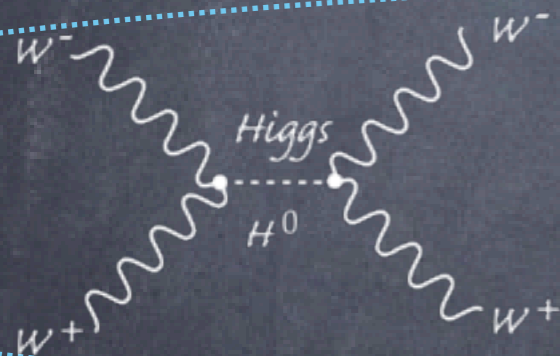
$$H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \longrightarrow \mathcal{L} = \frac{1}{2} \left(1 + c_H \frac{v^2}{f^2} \right) (\partial^\mu h)^2 + \dots$$

Modified
Higgs propagator

\sim

Higgs couplings
rescaled by

$$\frac{1}{\sqrt{1 + c_H \frac{v^2}{f^2}}} \sim 1 - c_H \frac{v^2}{2f^2} \equiv 1 - \xi/2$$



$$= -(1 - \xi) g^2 \frac{E^2}{M_W^2}$$

no exact cancellation
of the growing amplitudes

Even with a light Higgs, growing amplitudes (at least up to m_ρ)

$$\mathcal{A}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \mathcal{A}(s, t, u) \delta^{ab} \delta^{cd} + \mathcal{A}(t, s, u) \delta^{ac} \delta^{bd} + \mathcal{A}(u, t, s) \delta^{ad} \delta^{bc}$$

$$\mathcal{A}_{\text{LET}}(s, t, u) = \frac{s}{v^2}$$

LET=SM-Higgs



$$\mathcal{A}_\xi = \xi \mathcal{A}_{\text{LET}}$$

Beyond the Higgs

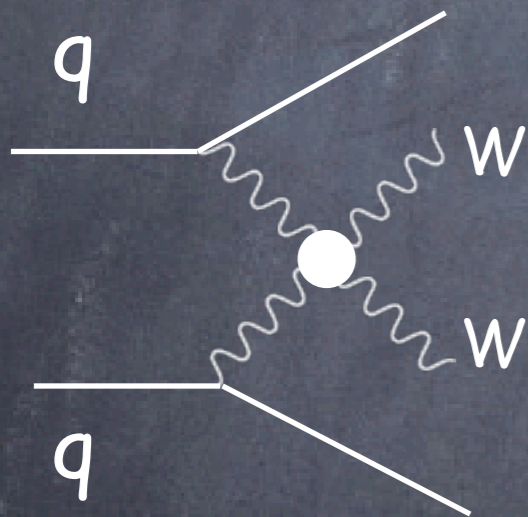
Strong WW scattering @ LHC

Even with a light Higgs, growing amplitudes (at least up to m_ρ)

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow W_L^+ W_L^-) = \mathcal{A}(W_L^+ W_L^- \rightarrow Z_L^0 Z_L^0) = -\mathcal{A}(W_L^\pm W_L^\pm \rightarrow W_L^\pm W_L^\pm) = \frac{c_H s}{f^2}$$

$$\mathcal{A}(W^\pm Z_L^0 \rightarrow W^\pm Z_L^0) = \frac{c_H t}{f^2}, \quad \mathcal{A}(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = \frac{c_H (s+t)}{f^2}$$

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow Z_L^0 Z_L^0) = 0$$



$$\sigma(pp \rightarrow V_L V_L X)_\xi = \xi^2 \sigma(pp \rightarrow V_L V_L X)_{\text{LET}}$$

leptonic vector decay channels

forward jet-tag, back-to-back lepton, central jet-veto



	LET($\xi = 1$)	SM bckg
ZZ	4.5	2.1
W^+W^-	15.0	36
$W^\pm Z$	9.6	14.7
$W^\pm W^\pm$	39	11.1

Bagger et al '95
Butterworth et al. '02

$$\mathcal{L} = 300 \text{ fb}^{-1}$$

Scale of Strong WW scattering?

$$A_{TT \rightarrow TT} \sim g^2 f(t/s)$$

f is a rational fct
expected O(1) for $t \sim -s/2$

$$A_{LL \rightarrow LL} \sim \frac{s}{v^2}$$

onset of strong scattering at the weak scale

hard cross-section

$$\frac{d\sigma_{LL \rightarrow LL}/dt}{d\sigma_{TT \rightarrow TT}/dt} \Big|_{t \sim -s/2} = N_h \frac{s^2}{M_W^4}$$

'inclusive' cross-section

$$(-s + Q_{\min}^2 < t < -Q_{\min}^2)$$

$$\frac{\sigma_{LL \rightarrow LL}(Q_{\min})}{\sigma_{TT \rightarrow TT}(Q_{\min})} = N_s \frac{s Q_{\min}^2}{M_W^4}$$

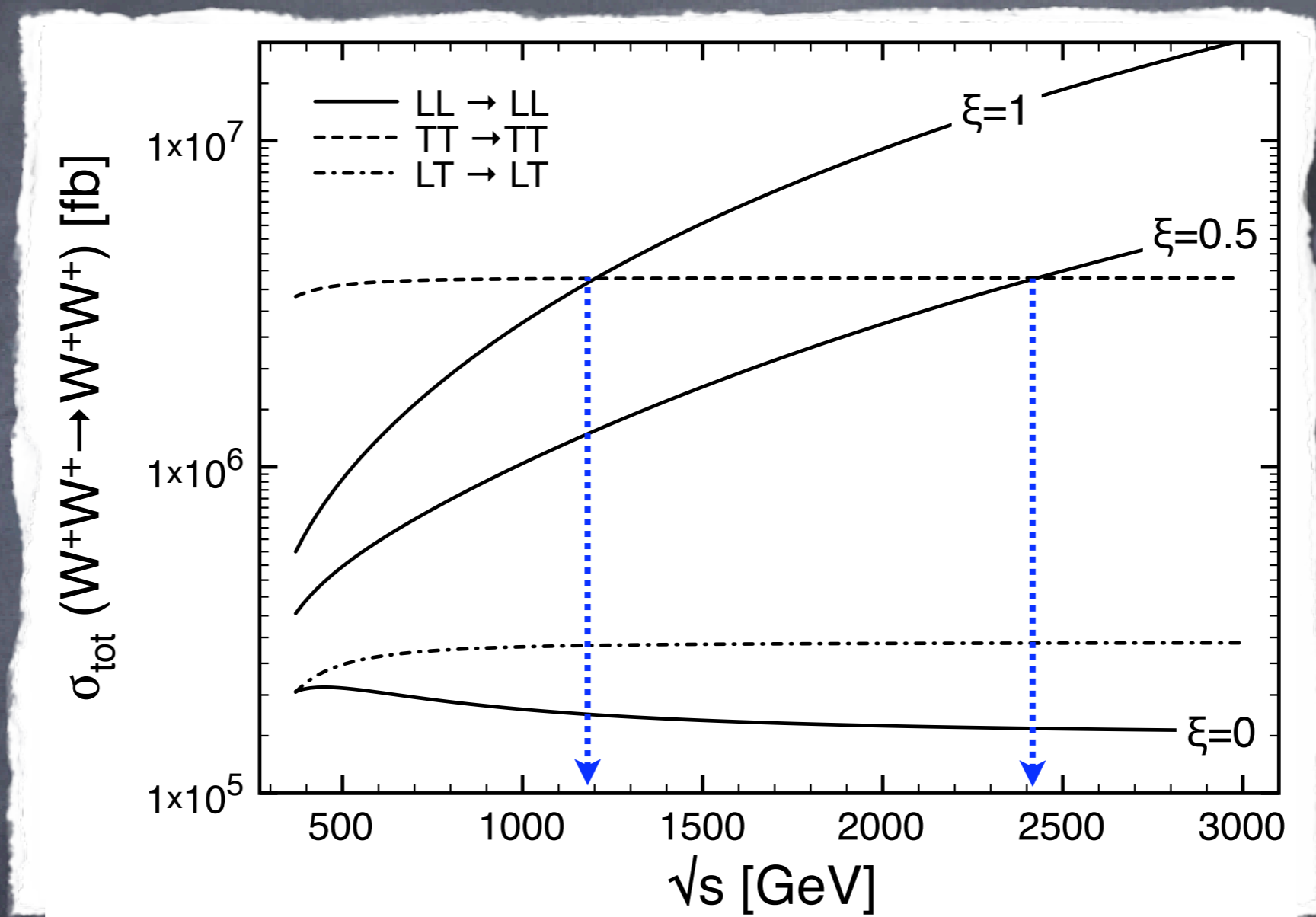
NDA estimates

$$N_h \sim 1$$

$$N_s \sim 1$$

Total cross sections

disentangling L from T polarization is hard



The onset of strong scattering is delayed to larger energies due to the dominance of $TT \rightarrow TT$ background

The dominance of T background will be further enhanced by the pdfs since the luminosity of W_T inside the proton is $\log(E/M_W)$ enhanced

Coulomb enhancement (SM)

the total cross section is dominated by the poles in the exchange of γ and Z in the t- and u-channels

$W^+W^+ \rightarrow W^+W^+$

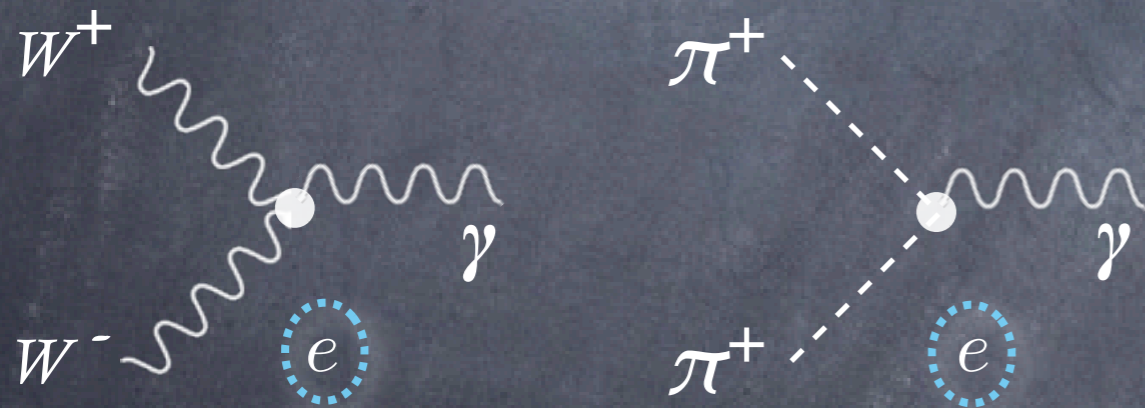
$$A = \frac{a_\gamma^t s}{t} + \frac{a_Z^t s}{t - M_Z^2} + \frac{a_\gamma^u s}{u} + \frac{a_Z^u s}{u - M_Z^2} + \dots \Rightarrow \sigma \sim \frac{1}{16\pi} \left(\frac{a_\gamma^t{}^2 + a_\gamma^u{}^2}{M_\gamma^2} + \frac{a_Z^t{}^2 + a_Z^u{}^2}{M_\gamma^2 + M_Z^2} \right)$$

$M_\gamma = \text{regulateur of Coulomb singularity} = \text{off-shellness of } W \sim M_W$

eikonal limit

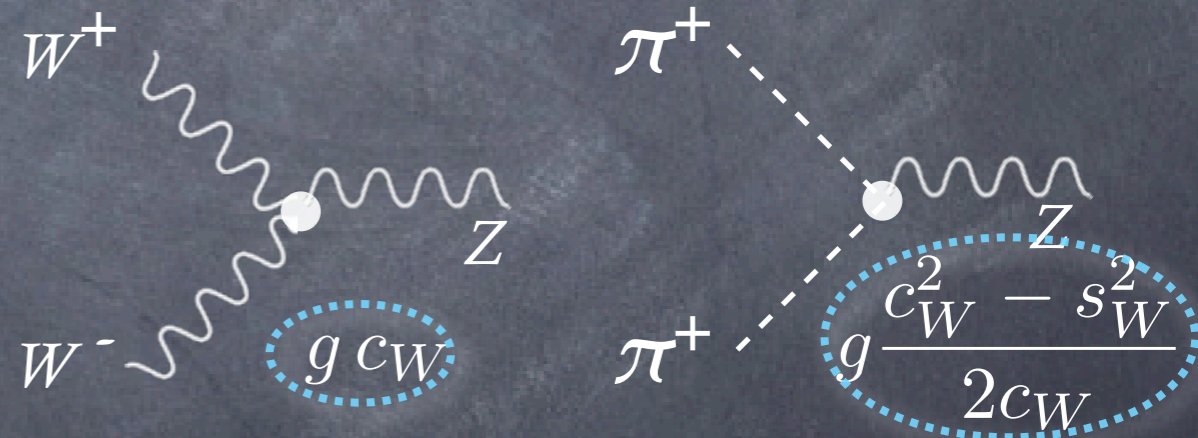
$$a_\gamma = 2 \cdot (\text{electric charge of } W^+)^2$$

universal for T and L



$$a_Z = 2 \cdot (\text{"SU(2) charge" of } W^+)^2$$

different for T and L



SM

$$\frac{\sigma_{TT \rightarrow TT}}{\sigma_{LL \rightarrow LL}} \sim 20$$

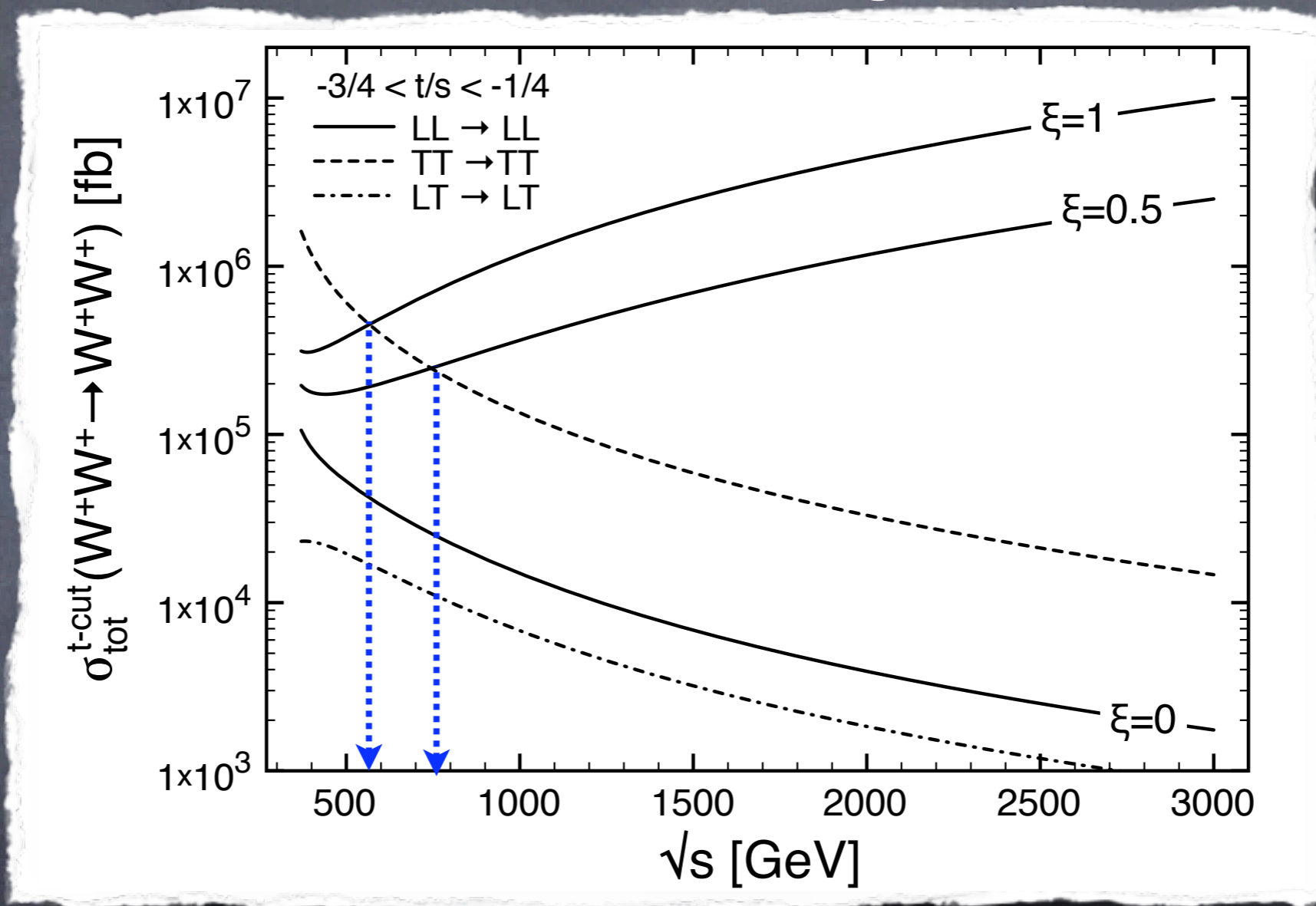
(for $M_\gamma \sim M_Z$)

$$N_s \sim 1/500$$

\Rightarrow T-dominance is the result of multiplicity and larger SU(2) charges \Leftarrow

Hard scattering (central region)

we need to look at the central region, i.e. large scattering angle, to be sensitive to strong EWSB

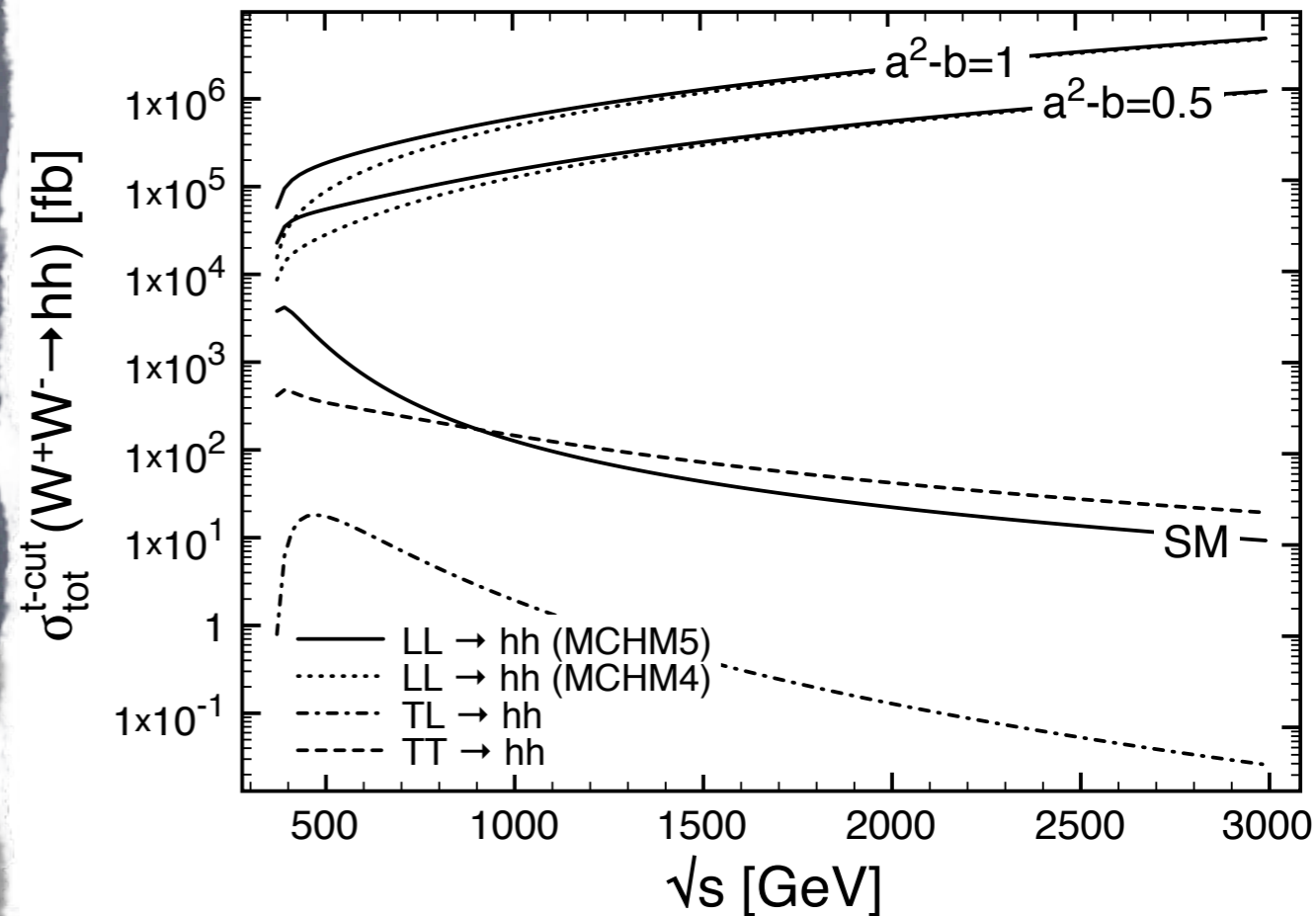
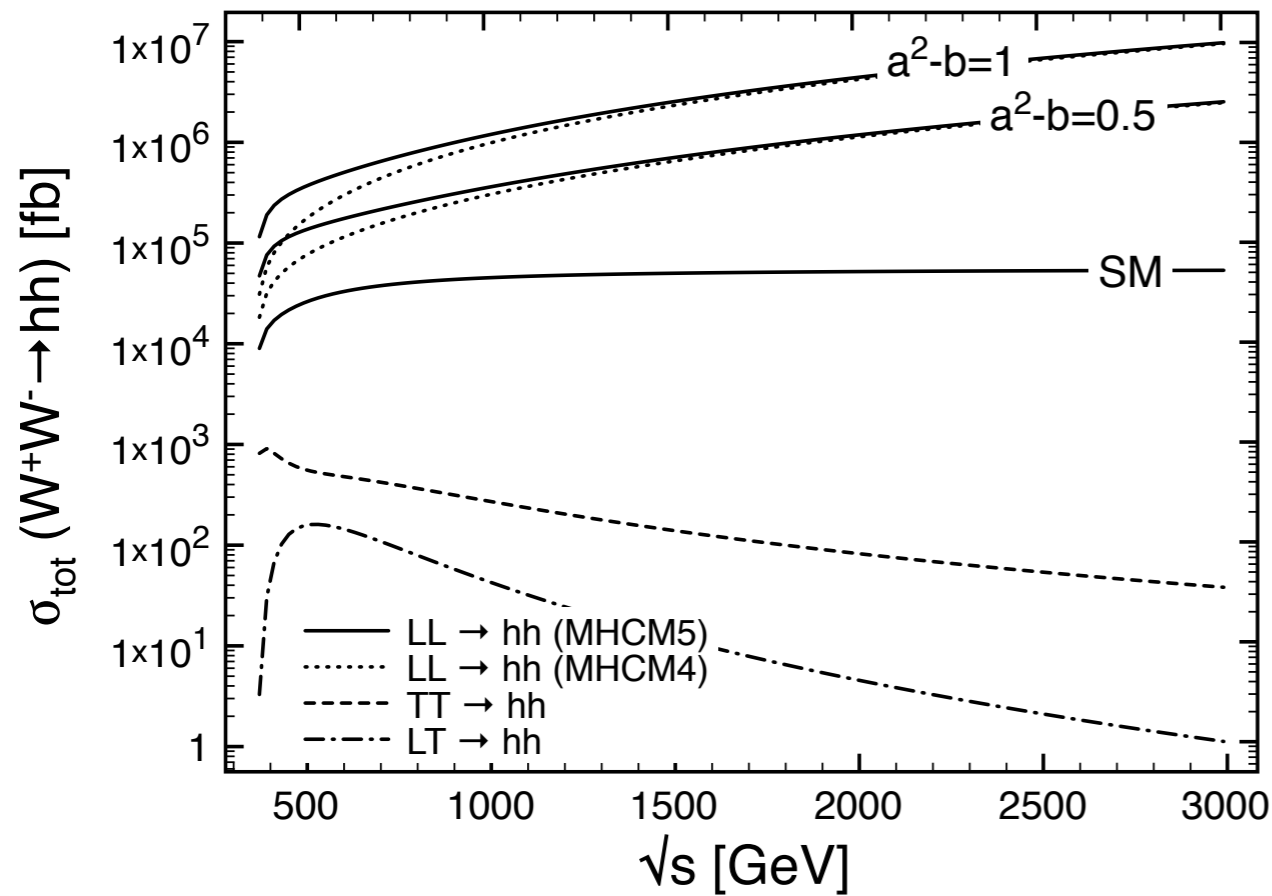


$$\frac{\sigma_{LL \rightarrow LL}^{\text{hard}}}{\sigma_{TT \rightarrow TT}^{\text{hard}}} \simeq \left(\frac{\sqrt{s}}{7.4 M_W} \right)^4 \xi^2$$

$$N_h = 1/2304$$

- hard cross-section = faster growth with energy
- onset of strong scattering still at high scale

EW bckg for $WW \rightarrow hh$



$$\frac{d\sigma^{LL \rightarrow hh} / dt}{d\sigma^{TT \rightarrow hh} / dt} = \frac{1}{8} \frac{\xi^2}{\xi^2 + (1 - \xi)^2} \left(\frac{\sqrt{s}}{M_W} \right)^4$$

no T polarization pollution,
neither in the total cross section,
nor in the central region

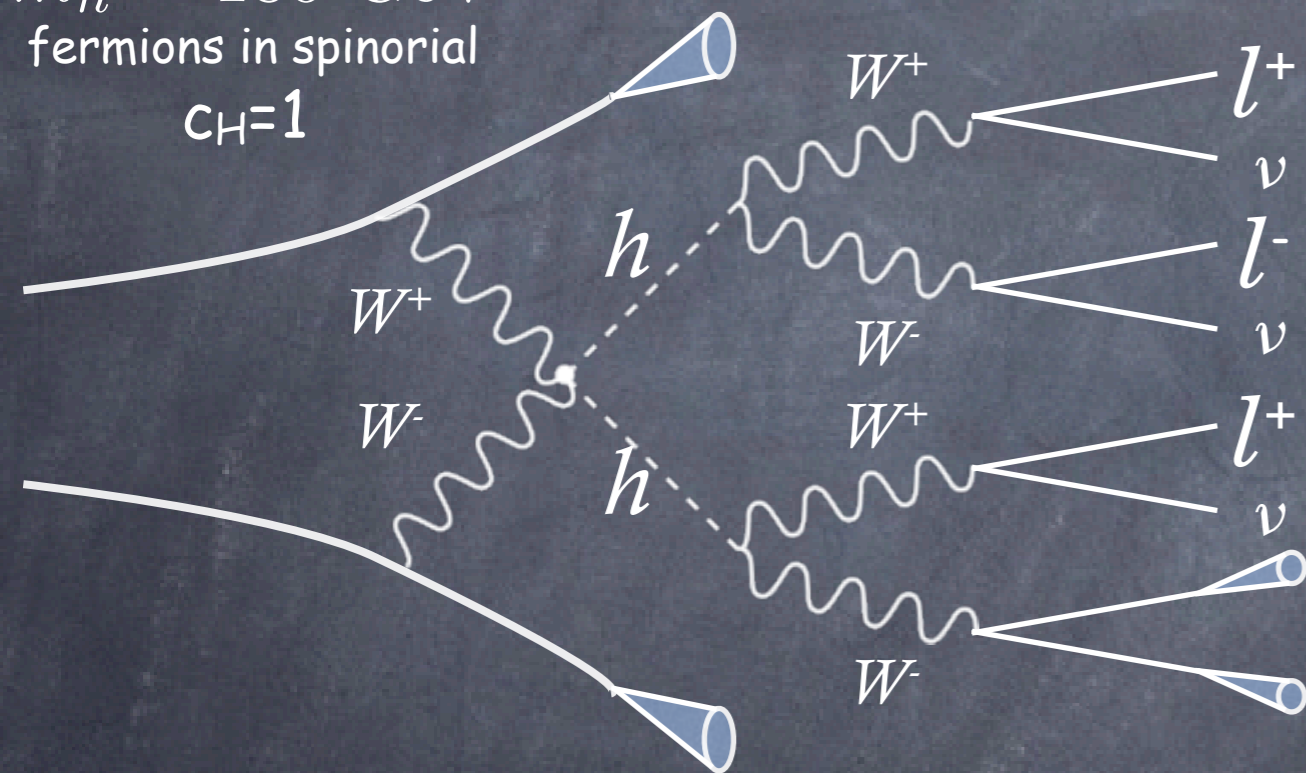
Strong Higgs production: (3L+jets) analysis

Contino, Grojean, Moretti, Piccinini, Rattazzi '10

strong boson scattering \Leftrightarrow strong Higgs production

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow hh) = \mathcal{A}(W_L^+ W_L^- \rightarrow hh) = \frac{c_H s}{f^2}$$

$m_h = 180$ GeV
fermions in spinorial
 $c_H = 1$



jets	leptons
$p_T \geq 30$ GeV	$p_T \geq 20$ GeV
$\delta R_{jj} > 0.7$	$\delta R_{lj(ll)} > 0.4(0.2)$
$ \eta_j \leq 5$	$ \eta_j \leq 2.4$

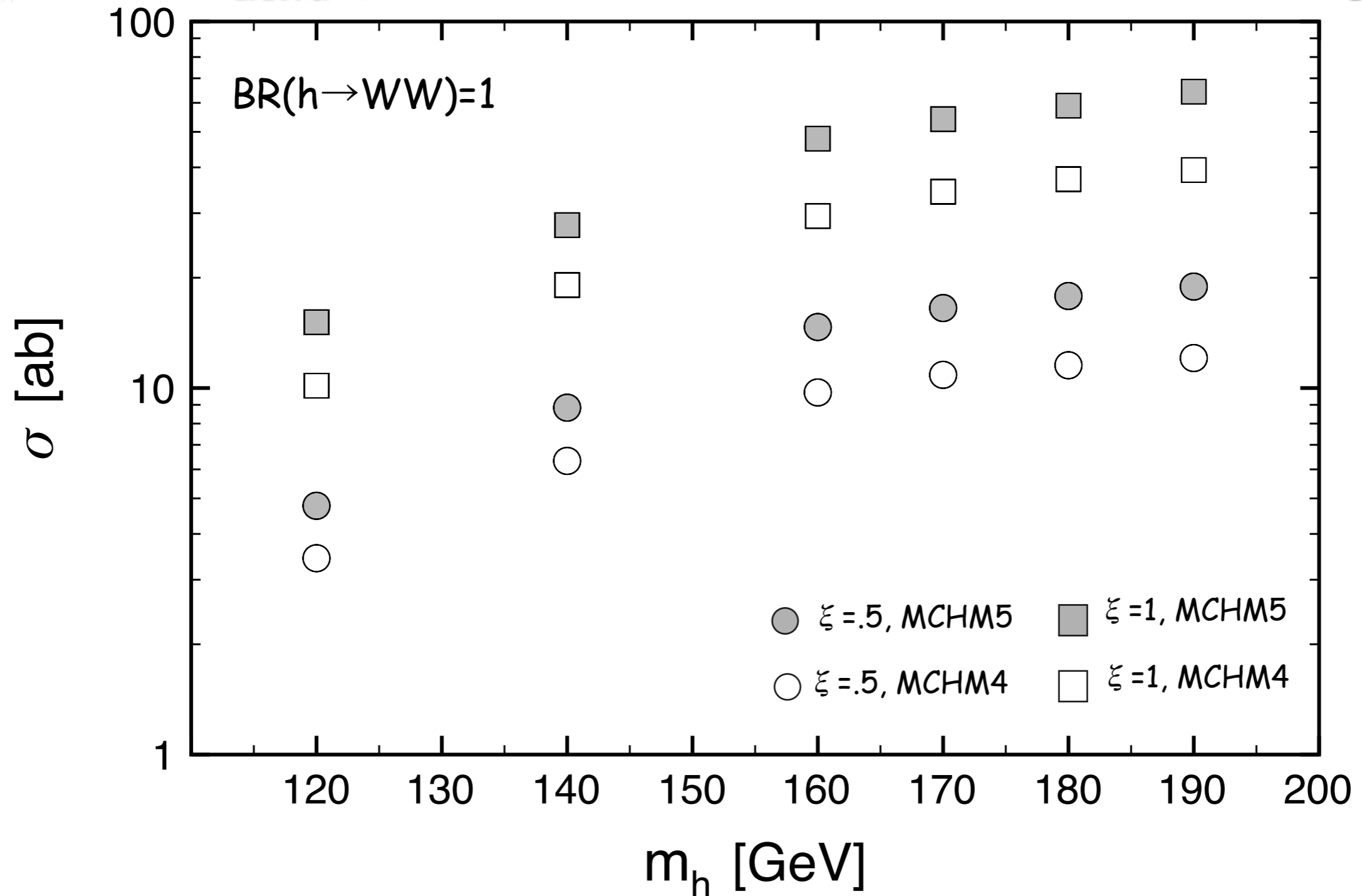
Dominant backgrounds: $Wll4j$, $t\bar{t}W2j$, $t\bar{t}2W(j)$, $3W4j$...

forward jet-tag, back-to-back lepton, central jet-veto

v/f	1	$\sqrt{.8}$	$\sqrt{.5}$
significance (300 fb^{-1})	4.0	2.9	1.3
luminosity for 5σ	450	850	3500

\Leftarrow good motivation to SLHC

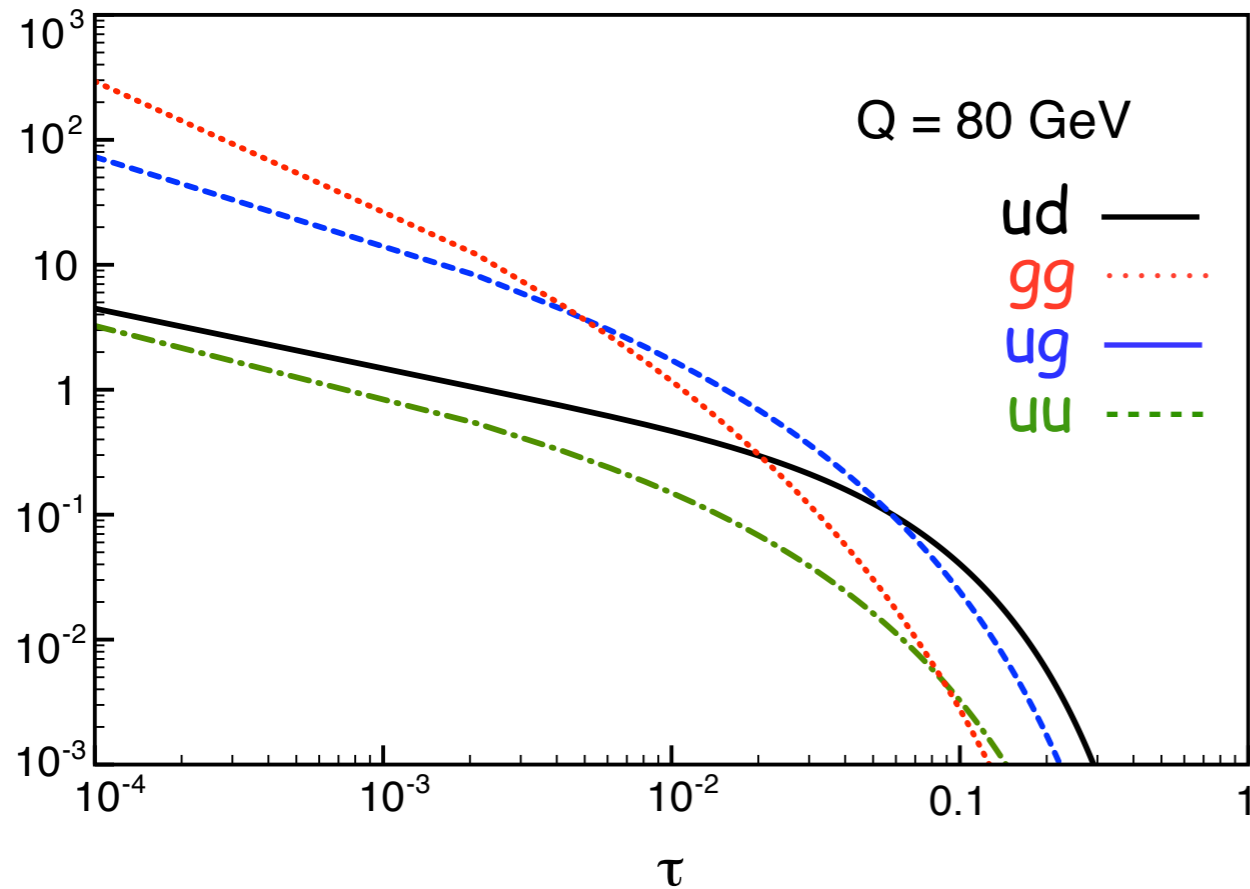
Higgs mass dependence



- production at threshold: $x_1 x_2 \sim 4m_h^2/s$ $\sigma \searrow$ w/. m_h
- lighter Higgs, softer decay products, less effective cuts $\sigma \nearrow$ w/. m_h

Threshold production

$$\frac{d\sigma}{d\hat{s}} = \frac{1}{\hat{s}} \hat{\sigma}(q_A q_B \rightarrow hh) \rho_{AB}(\hat{s}/s, Q^2)$$



$$\sigma = \hat{\sigma}(s_0) \times \int_{s_0} \frac{d\hat{s}}{\hat{s}} \frac{\hat{\sigma}(\hat{s})}{\hat{\sigma}(s_0)} \rho(\hat{s}/s)$$

integral is saturated at threshold



inclusive cross-section is not probing the asymptotic regime of hard scattering

sensitivity on Higgs self-coupling and not only on strong scattering ($b-a^2$)

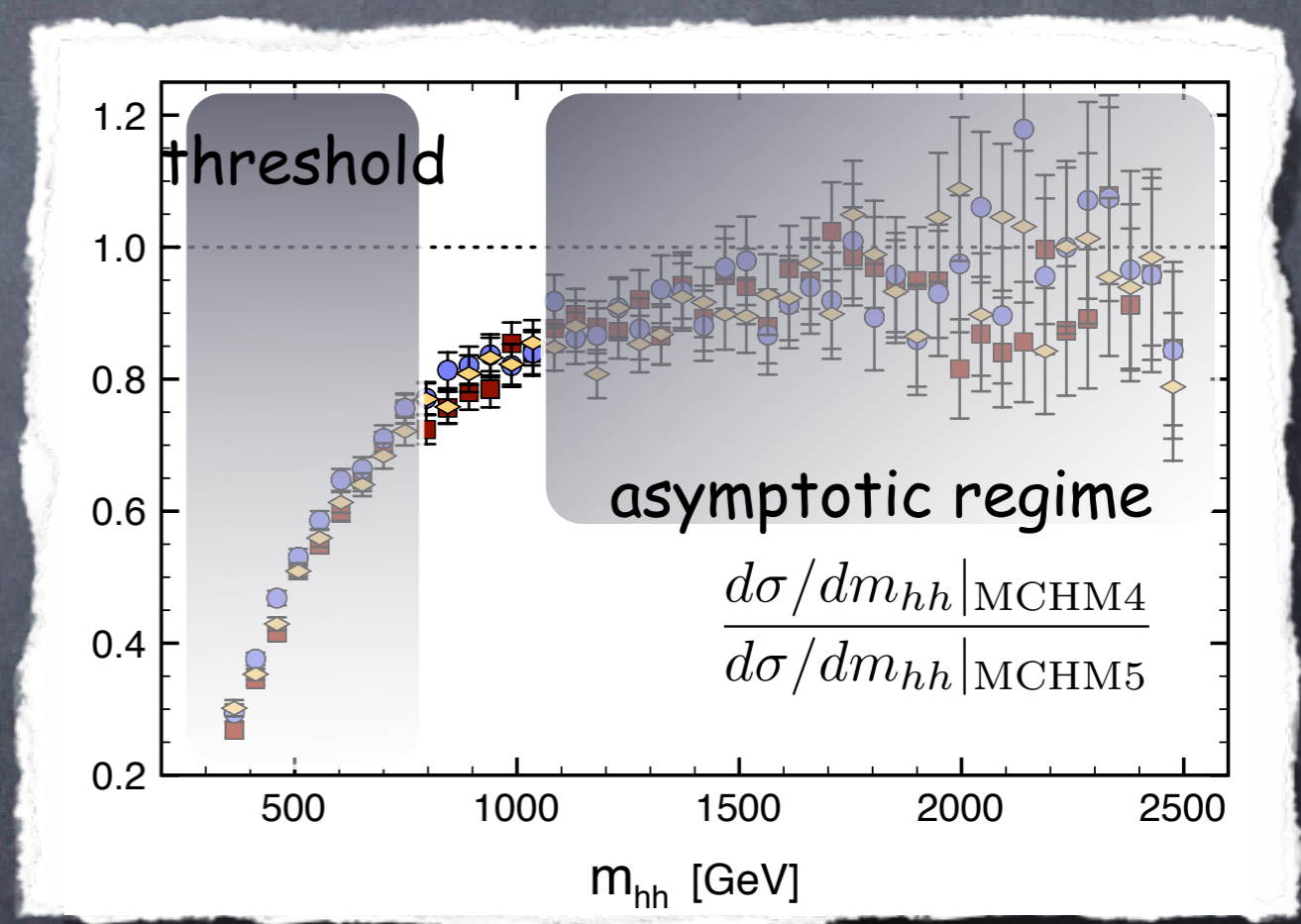
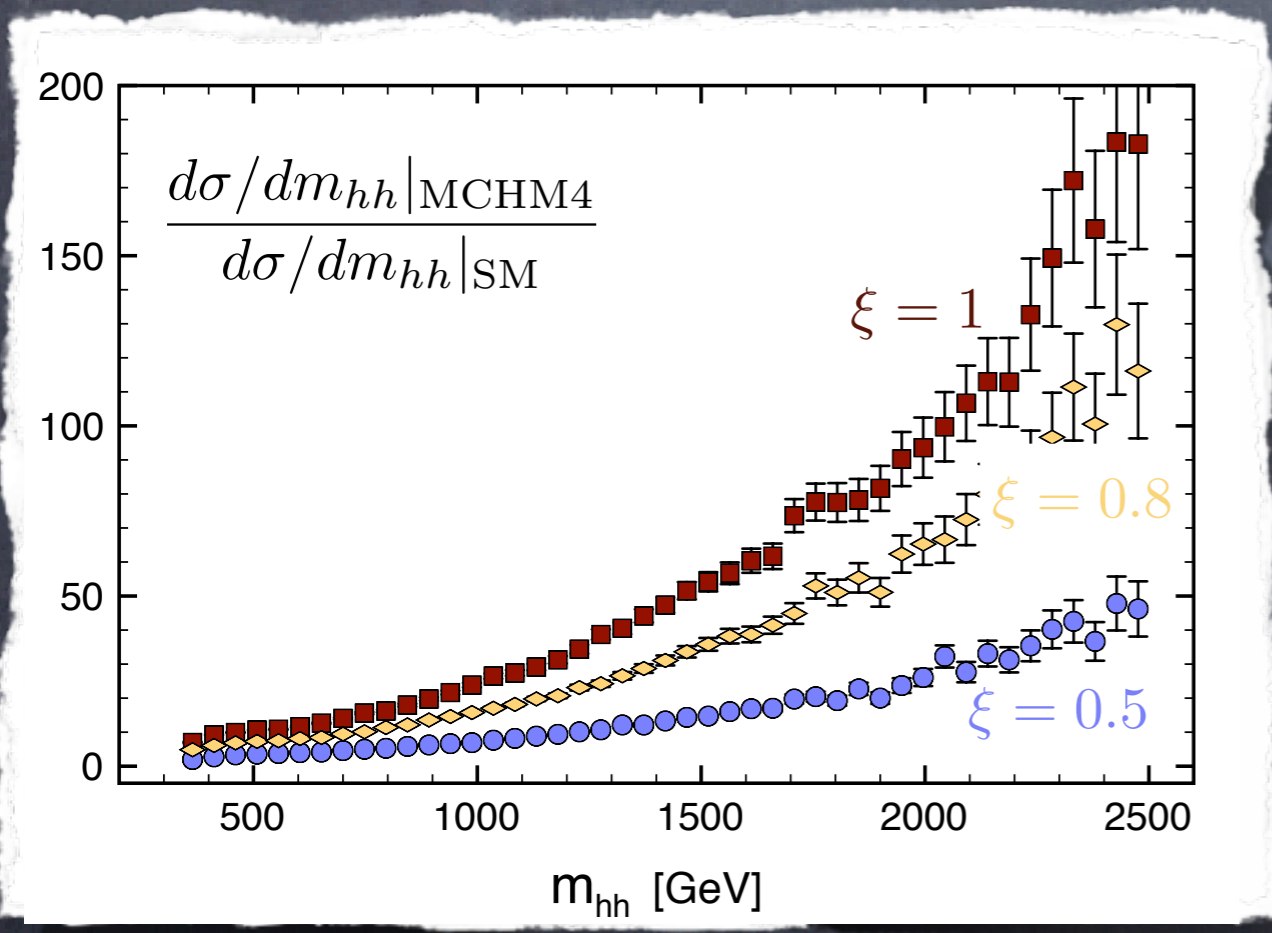
Isolating Hard Scattering

isolate events with large m_{hh}

luminosity factor drops out in ratios: extract the growth with m_{hh}

measure
 H^3

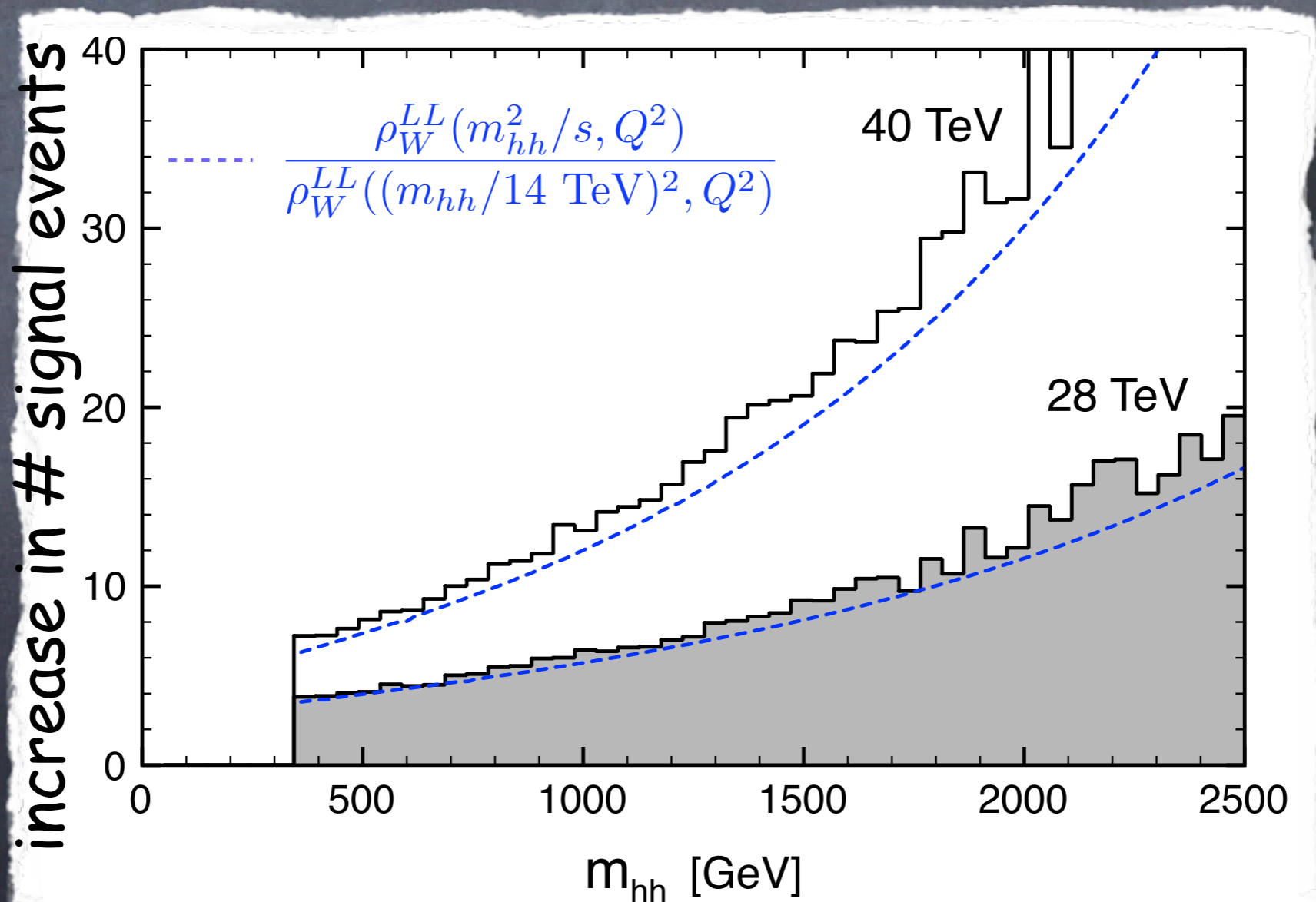
measure
 $b-a^2$



Dependence on Collider Energy

$$\sigma = \hat{\sigma}(s_0) \times \int_{s_0} \frac{d\hat{s}}{\hat{s}} \frac{\hat{\sigma}(\hat{s})}{\hat{\sigma}(s_0)} \rho(\hat{s}/s)$$

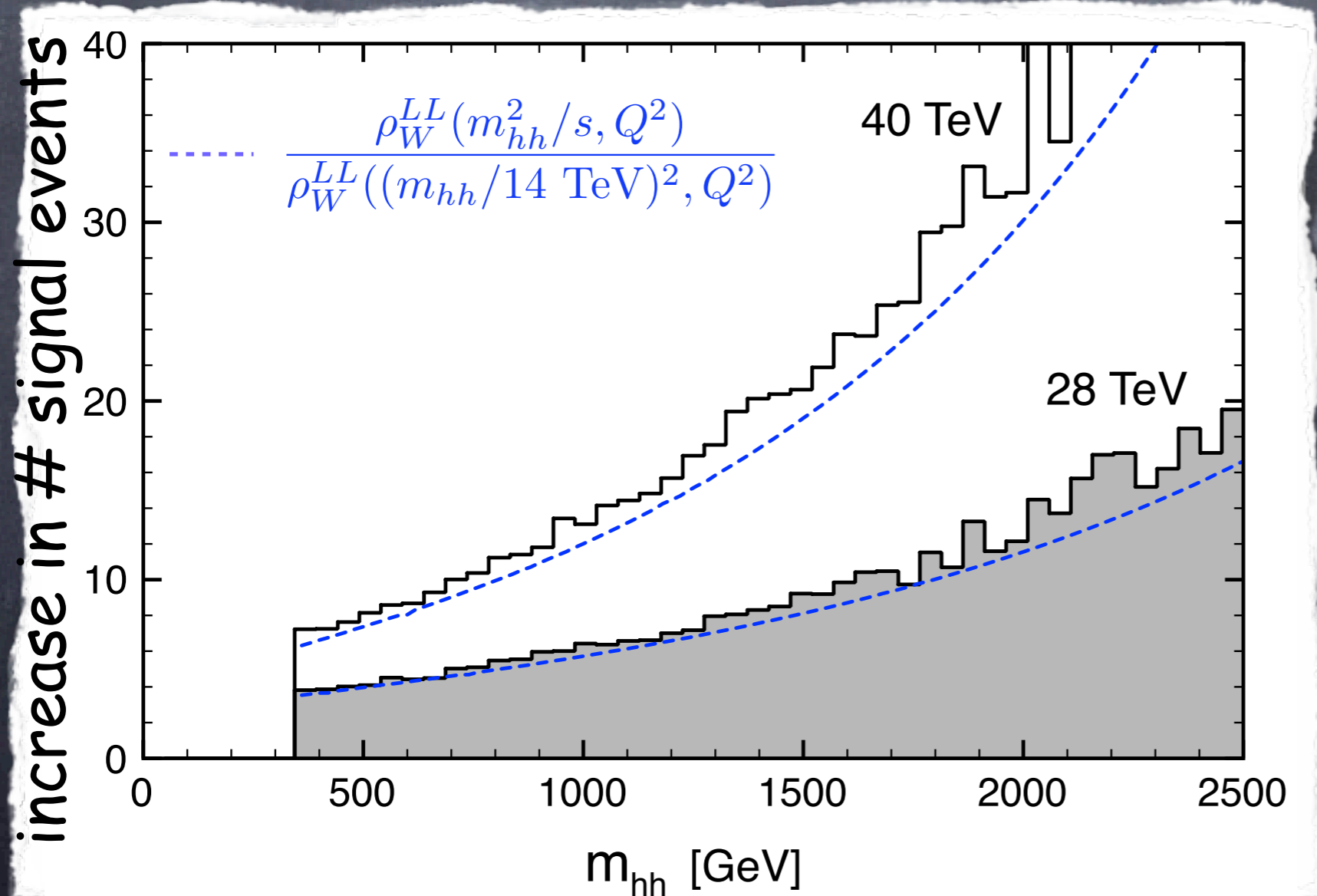
increase collider energy s = sensitive to PDFs at smaller x
bigger cross-sections



Dependence on Collider Energy

$$\sigma = \hat{\sigma}(s_0) \times \int_{s_0} \frac{d\hat{s}}{\hat{s}} \frac{\hat{\sigma}(\hat{s})}{\hat{\sigma}(s_0)} \rho(\hat{s}/s)$$

increase collider energy s = sensitive to PDFs at smaller x
 bigger cross-sections

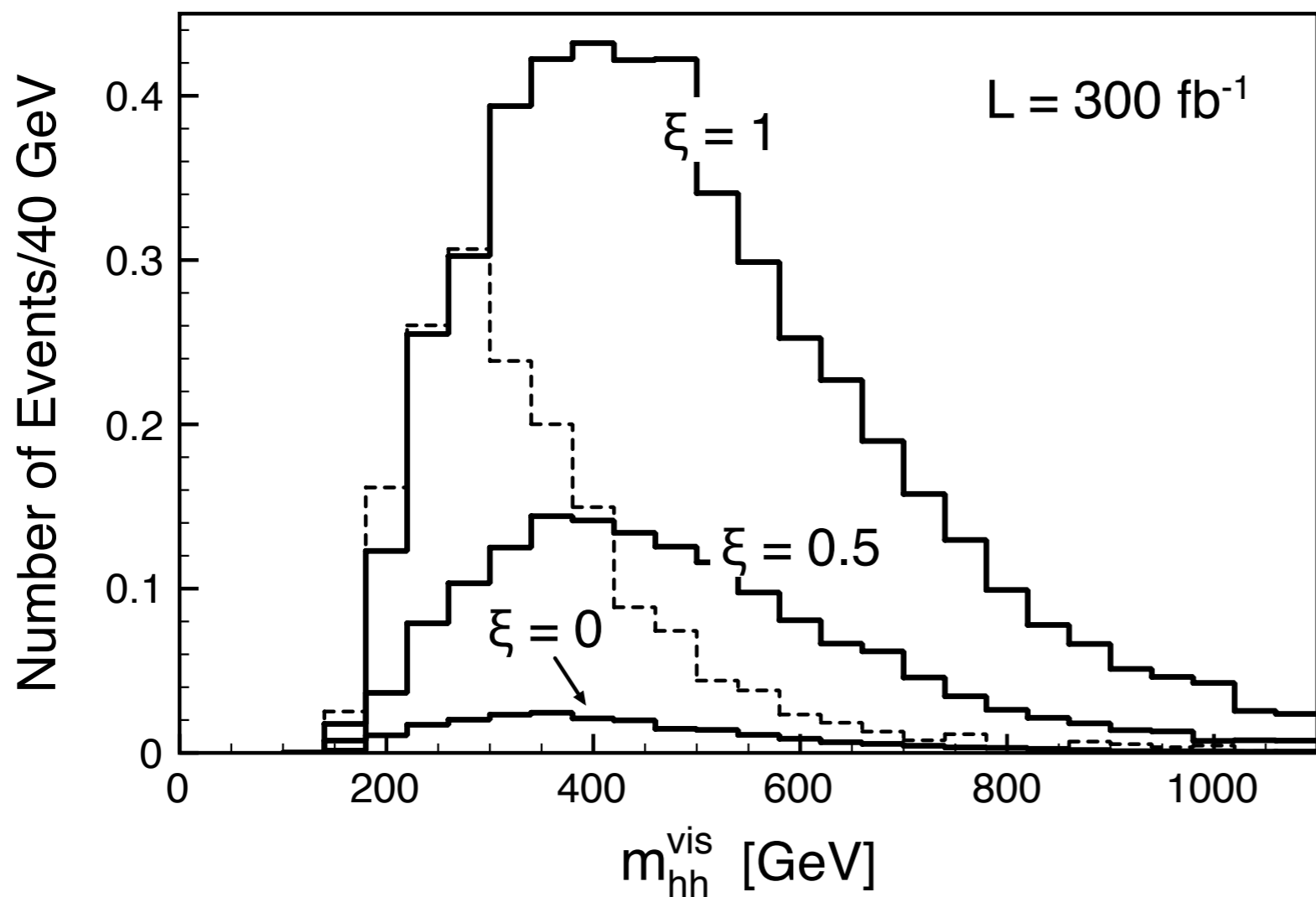


SLHC vs. VLHC

Dependence on Collider Energy

$$\sigma = \hat{\sigma}(s_0) \times \int_{s_0} \frac{d\hat{s}}{\hat{s}} \frac{\hat{\sigma}(\hat{s})}{\hat{\sigma}(s_0)} \rho(\hat{s}/s)$$

increase collider energy s = sensitive to PDFs at smaller x
bigger cross-sections



sLHC vs. VLHC

10 x lum = 10 x events

2 x \sqrt{s} = 10 x events
iif $m_{hh} > 1.6 \text{ TeV}$

sLHC might be better

Conclusions

EW interactions need Goldstone bosons to provide mass to W, Z



EW interactions also need a UV moderator/new physics
to unitarize WW scattering amplitude

We'll need another Gargamelle experiment
to discover the still missing neutral current of the SM: the Higgs
weak NC \Leftrightarrow gauge principle
Higgs NC \Leftrightarrow ?

LHC is prepared to discover the "Higgs"

collaboration EXP-TH is important to make sure

e.g. that no unexpected physics (unparticle, hidden valleys) is missed (triggers, cuts...)

Should not forget that the LHC will be a (quark) top machine

and there are many reasons to believe that the top is an important agent of the Fermi scale