

Cérémonie du prix Joliot-Curie 2022

modeling finite nuclei and dense matter in neutron stars

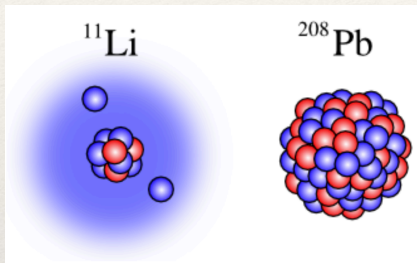
Jérôme Margueron

IP2I Lyon, France

*IRL Nuclear Physics and Nuclear Astrophysics
(NPA), East Lansing, USA*

halo nuclei

1 or 2 weakly bound nucleons change the size of the nucleus tremendously!

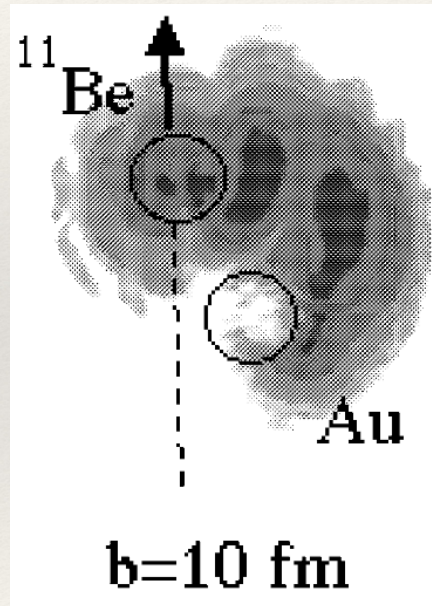


Also called Borromean nuclei (in reference to the flag of the Italian House of Borromeo).



Break-up mechanism: simple expressions for the break-up of halo nuclei including non-perturbative Coulomb-nuclear interference effects.

Towing mode:



$$i\hbar \frac{\partial \phi(\mathbf{r}, \mathbf{d}, t)}{\partial t} = (H_r + V_{nt}(\mathbf{r} + \mathbf{R}(t)) + V_{\text{eff}}(\mathbf{r}, \mathbf{R}(t)))\phi(\mathbf{r}, \mathbf{d}, t)$$

$$g_{\text{CN}}^{\text{BBM1}} \approx g_{\text{C}}^{\text{pert1}} + g_{\text{N}}^{\text{pert1}} + (g_{\text{CN}}^{\text{sudd}} - g_{\text{C}}^{\text{sudd1}} - g_{\text{N}}^{\text{sudd1}})$$

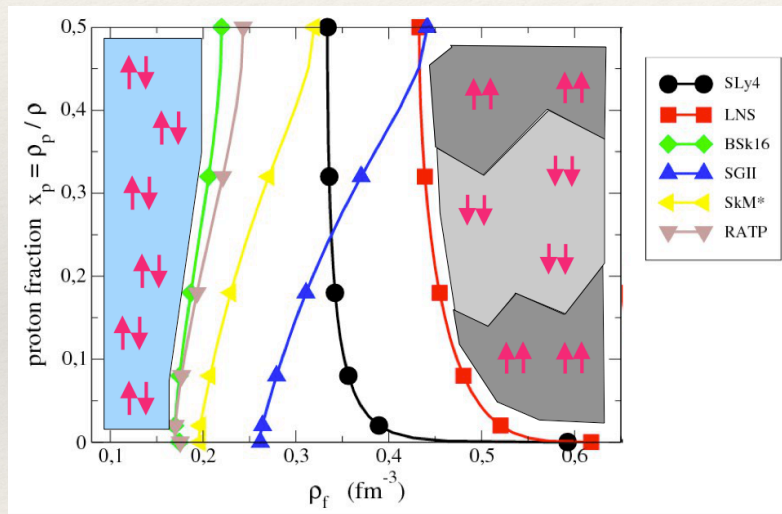
$$\equiv g_{\text{C}}^{\text{pert1}} + (g_{\text{CN}}^{\text{sudd}} - g_{\text{C}}^{\text{sudd1}}).$$

Quantum SuSy transformations for state removal and phase equivalent potentials:

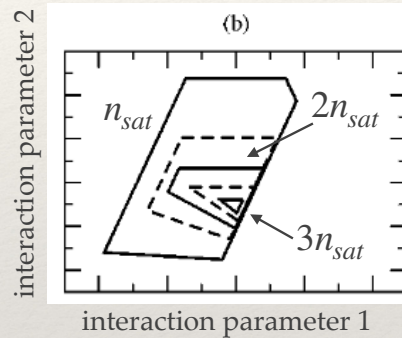
instabilities in the mean field

Many predictions in finite nuclei and in dense matter are based on Skyrme-type interactions. These functionals however predict some instabilities of the ground-state.

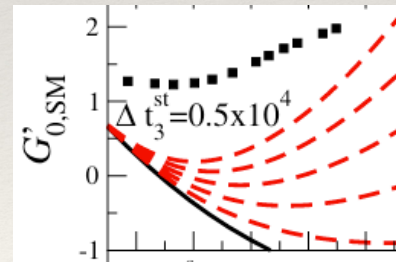
Spin instability



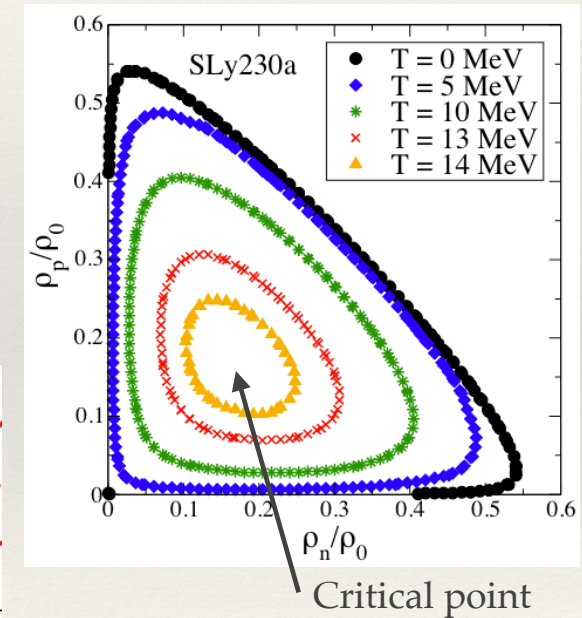
Skyrme interactions instabilities



Extended Skyrme interactions with no spin long-range instability

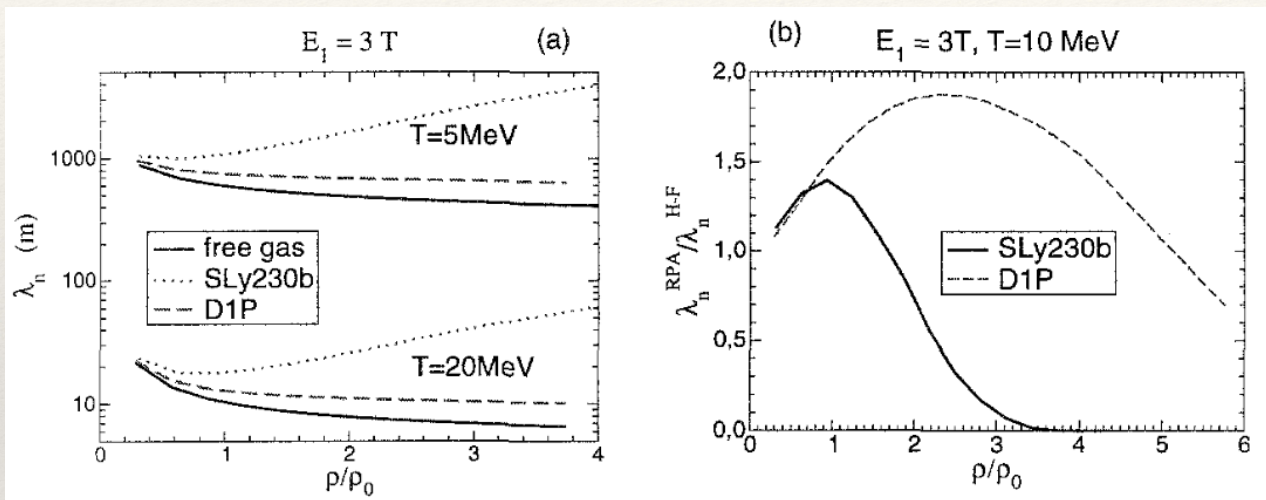


liquid-gas phase transition: Spinodal zone is an exemple of expected instability

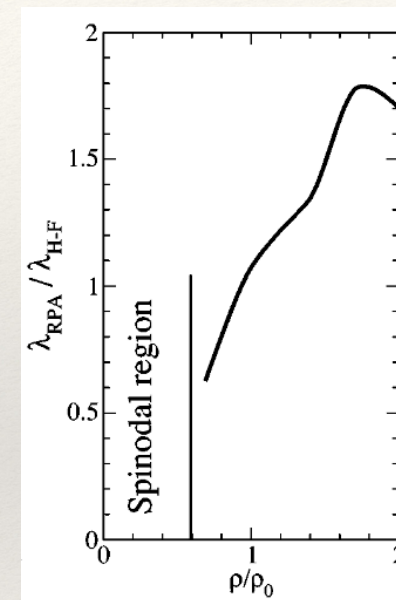


core-collapse supernovae: neutrino propagation

neutrino mean free path in dense matter



neutrino trapping near the liquid-gas phase transition



critical opalescence



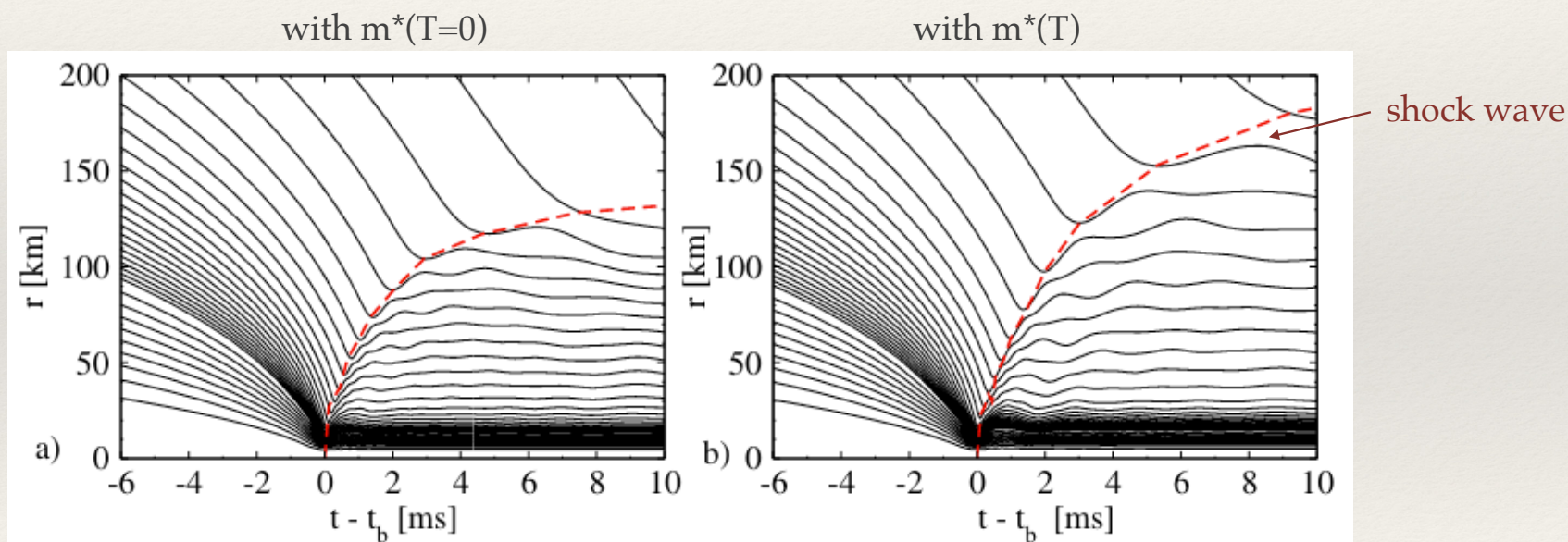
A new scenario where neutrino are delayed further more before they escape the central object. They also shift the beta equilibrium and increase the pressure in the crust
 → second shock
 (efficient transfer of energy to matter).

core-collapse supernovae: effect of nuclear correlations

Effect of $m^*(T)$ on the symmetry energy

The symmetry energy is the cost in energy to convert symmetric matter into neutron rich matter (Neutron Stars). Except at sat, it is poorly known and can be modified by nuclear dynamical correlations, i.e., $m^*(T)$.

1D core-collapse
supernova
simulation:



superfluidity in neutron stars

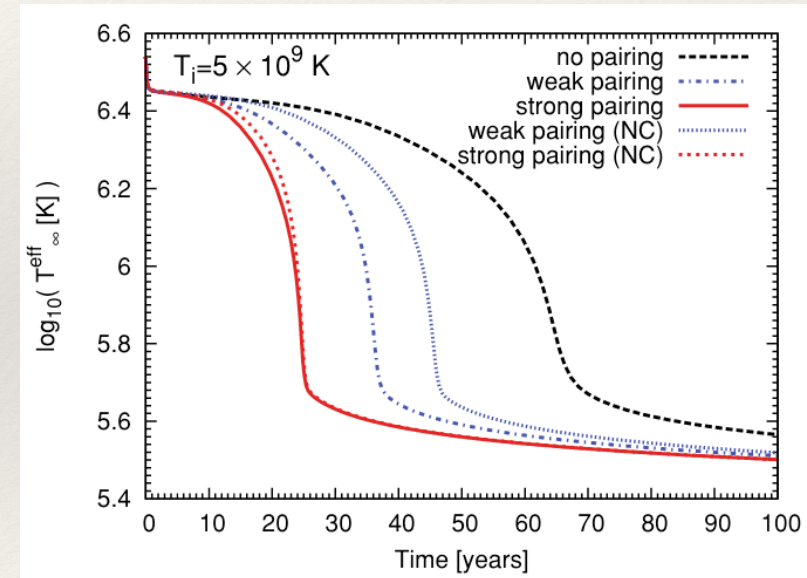
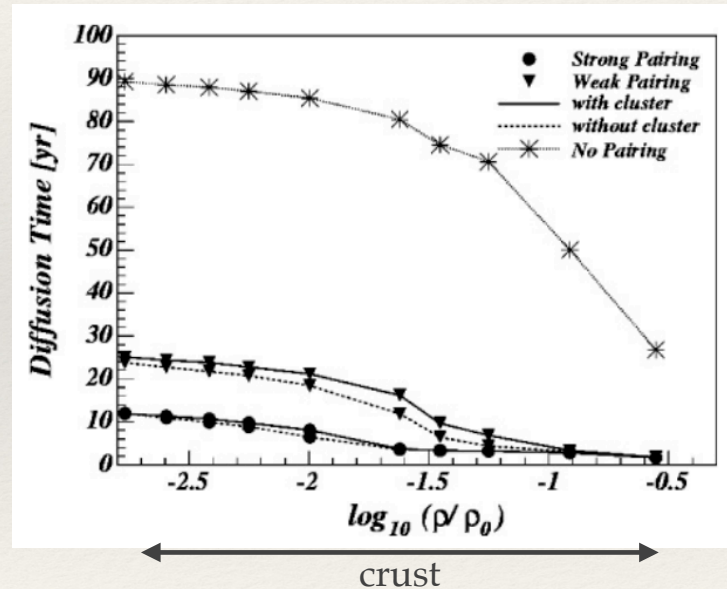
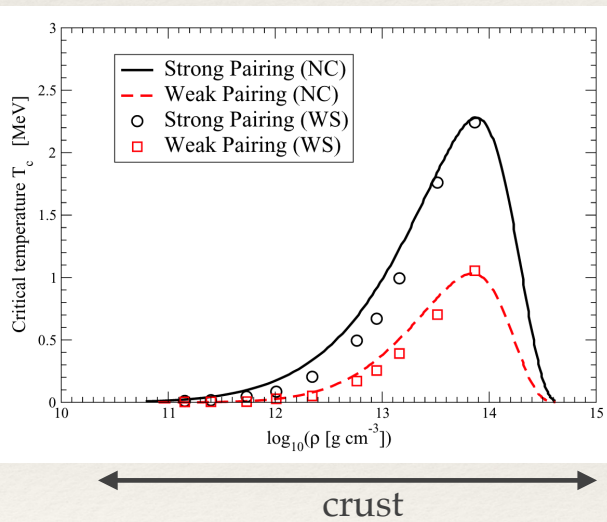
thermal relaxation in neutron stars

Relativistic heat equation:

$$\frac{\partial}{\partial r} \left[\frac{Kr^2}{\Gamma(r)} e^\phi \frac{\partial}{\partial r} (e^\phi T) \right] = r^2 \Gamma(r) e^\phi \left(C_V \frac{\partial T}{\partial t} + e^\phi Q_\nu \right)$$

specific heat
neutrino emission rate

The pairing gap in the crust of neutron stars is poorly known.



Nicolae Sandulescu, NIPNE Bucharest
Nguyen Van Giai, IPN Orsay

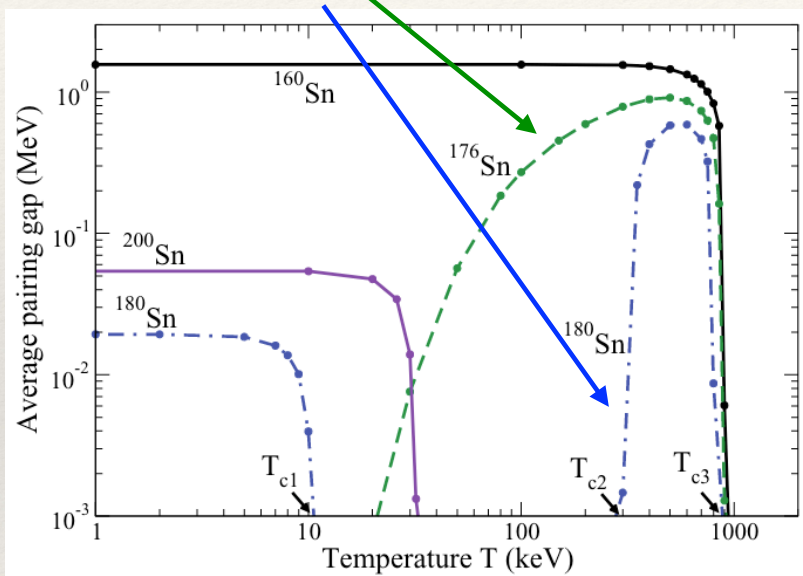
Elias Khan, IPN Orsay
Marcella Grasso, IPN Orsay

Nicolas Chamel, ULB Bruxelles
Charlotte Monrozeau, IPN Orsay

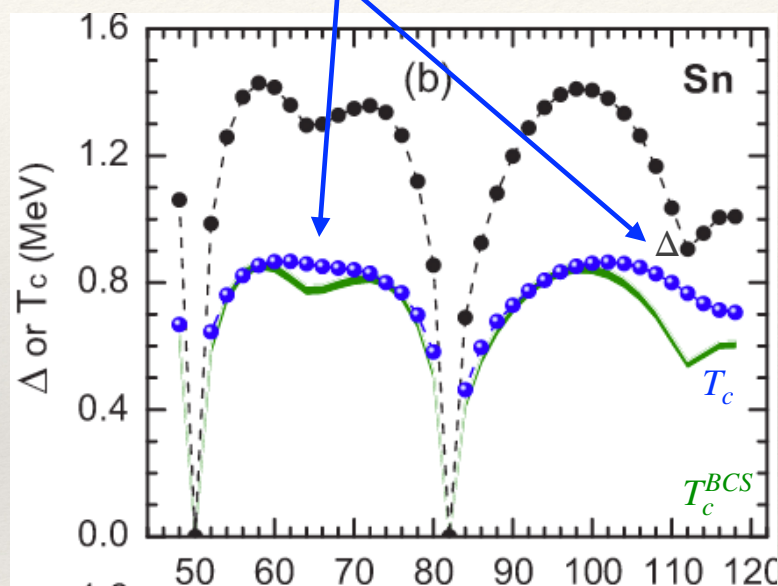
Morgane Fortin, ENS Paris
Dany Page, UNAM Mexico

nuclear pairing

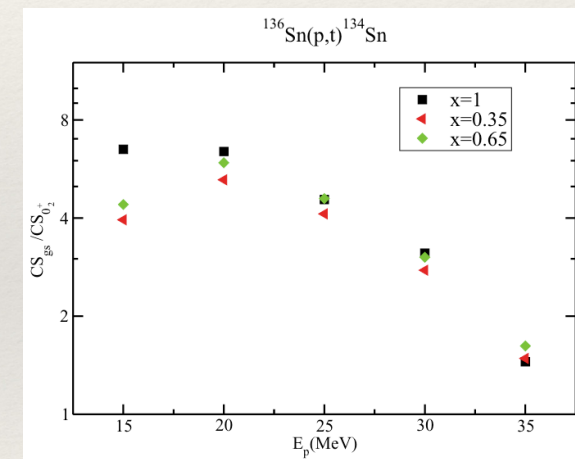
pairing re-entrance



pairing persistence



Experimental test of the impact of different pairing force on 2-neutron transfer reactions at various incident energies:

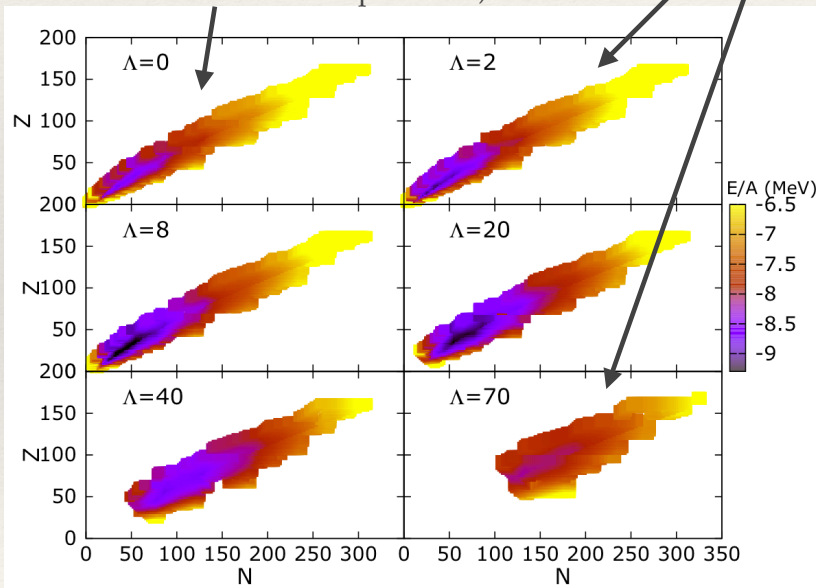


hypernuclei

=nuclei with hyperons (Λ , Ξ , or Σ)

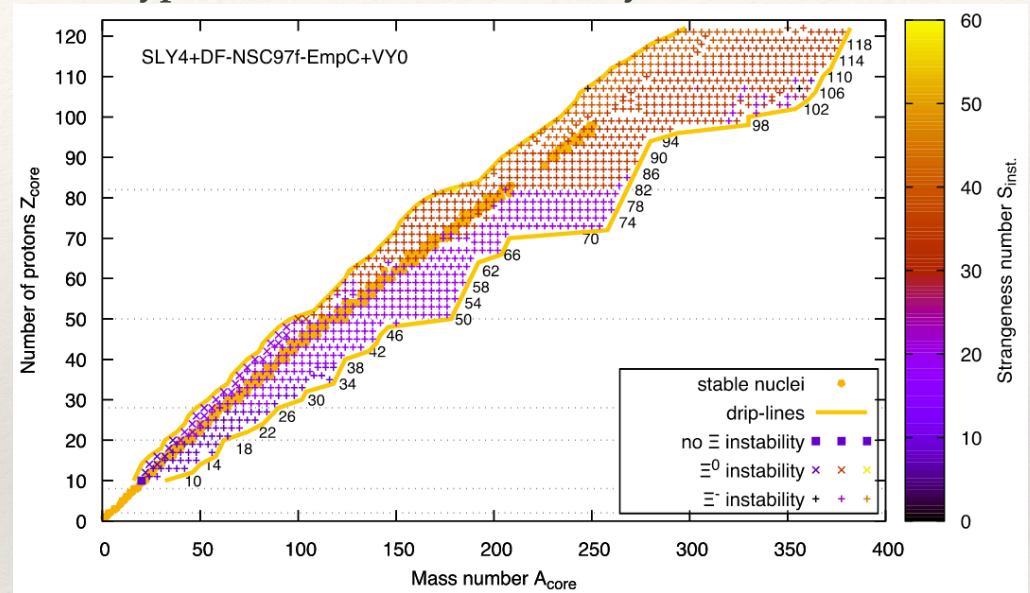
The hyper-Nuclear chart (with only Λ)

Normal nuclear chart (less than 1/2 of the total number of nuclei have been produced)



hyper-nuclear chart with various number of Λ .

The hyper-Nuclear chart (with only Λ and Ξ)



Ordinary nuclei: about 8,000 (total), about 3,300 have been produced.
hypernuclei: about 600,000 (total), about 20 have been produced.

meta-modeling of extreme matter EoS

Energy in asymmetric matter: $e(n, \delta) \approx e_{sat}(n) + e_{sym,2}(n)\delta^2 + e_{sym,4}(n)\delta^4 + \dots$ with $\delta = (n_n - n_p)/(n_n + n_p)$

where the isoscalar and isovector terms are expressed as a Taylor expansion in x :

$$e_{sat}(n) = E_{sat} + \frac{1}{2}K_{sat}x^2 + \frac{1}{6}Q_{sat}x^3 + \frac{1}{24}Z_{sat}x^4 + \dots \quad e_{sym}(n) = E_{sym} + L_{sym}x + \frac{1}{2}K_{sym}x^2 + \frac{1}{6}Q_{sym}x^3 + \frac{1}{24}Z_{sym}x^4 + \dots$$

with $x = (n - n_{sat})/(3n_{sat})$

The **nuclear empirical parameters** (NEP) capture the (topological) properties of the EoS around n_{sat} .

Small uncertainties

Large uncertainties

Some uncertainties

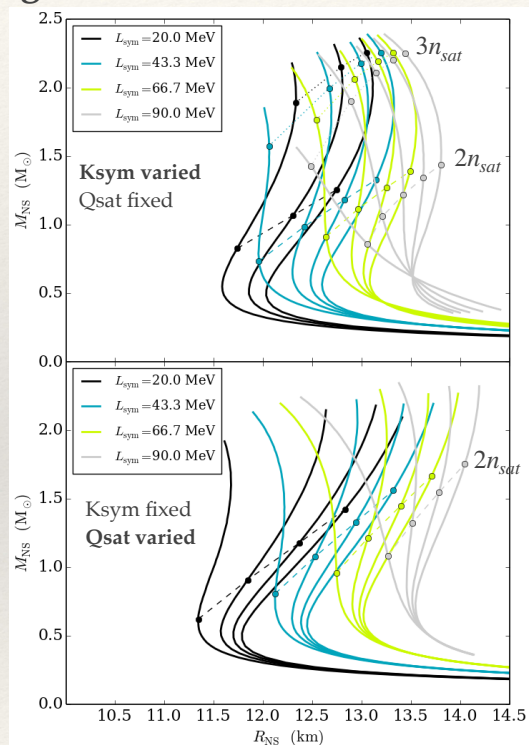
P_α	E_{sat} MeV	E_{sym} MeV	n_{sat} fm^{-3}	L_{sym} MeV	K_{sat} MeV	K_{sym} MeV	Q_{sat} MeV	Q_{sym} MeV	Z_{sat} MeV	Z_{sym} MeV	m_{sat}^*/m	$\Delta m_{sat}^*/m$
$\langle P_\alpha \rangle$	-15.8	32	0.155	60	230	-100	300	0	-500	-500	0.75	0.1
σ_{P_α}	± 0.3	± 2	± 0.005	± 15	± 20	± 100	± 400	± 400	± 1000	± 1000	± 0.1	± 0.1

Small impact at T=0

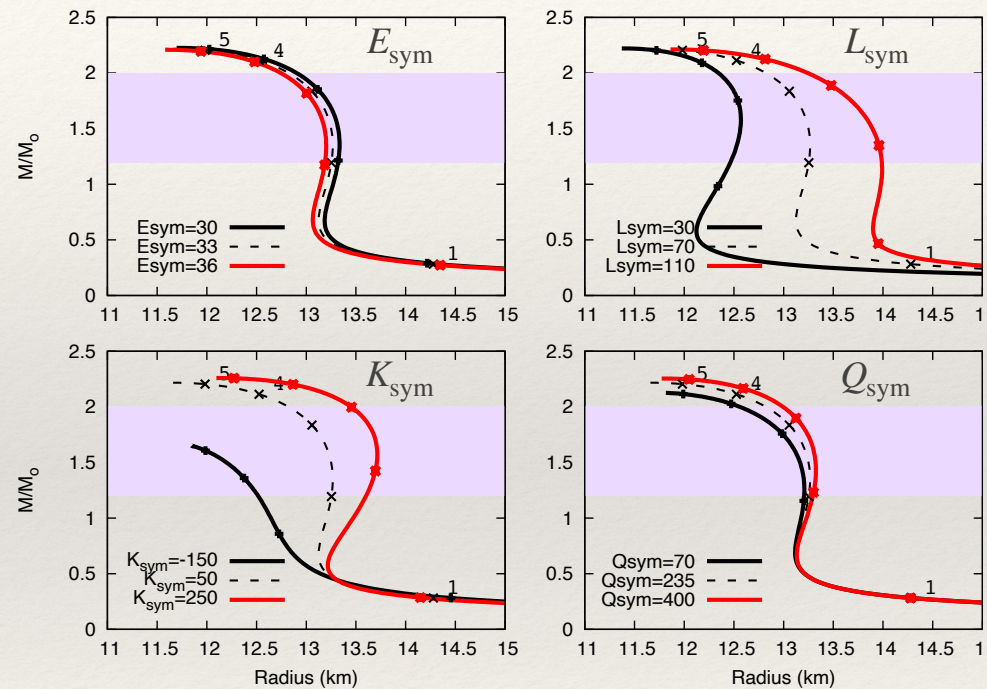
⚠ These parameters are correlated among each other.

meta-modeling of extreme matter EoS

Impact of changing the NEP on the MR relation of neutron stars:



Isovector channel



Rudiney Hofman Casali, IPN Lyon
Francesca Gulminelli, LPC Caen

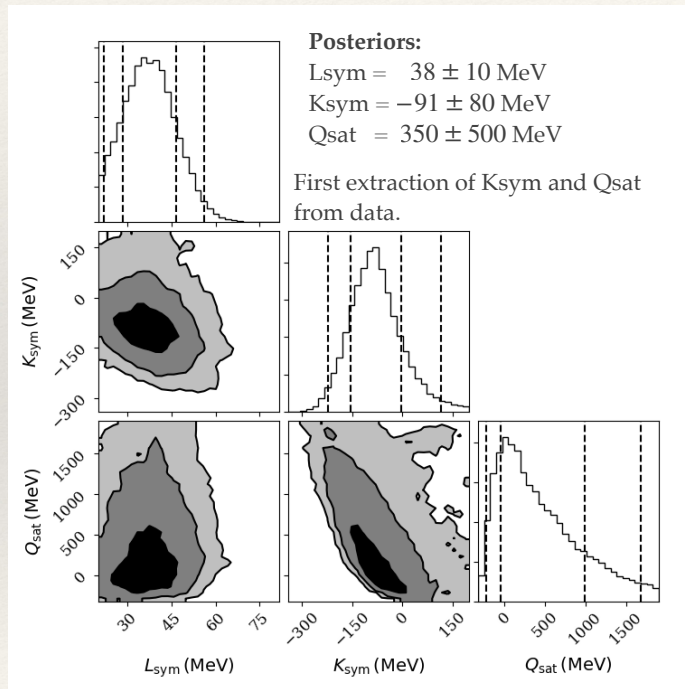
Camille Ducoin, University of Coimbra
Elias Khan, IPN Orsay

Nicolas Baillet d'Etivaux, IPN Lyon
Sébastien Guillot, IRAP Toulouse

Rahul Somasundaram, IP2I Lyon
Guilherme Grams, IP2I Lyon

confrontation to data with Bayesian statistics

Confronting qLMXB with nuclear EOS:



There are a lot of new data which brings information on dense matter properties.

Astro data:

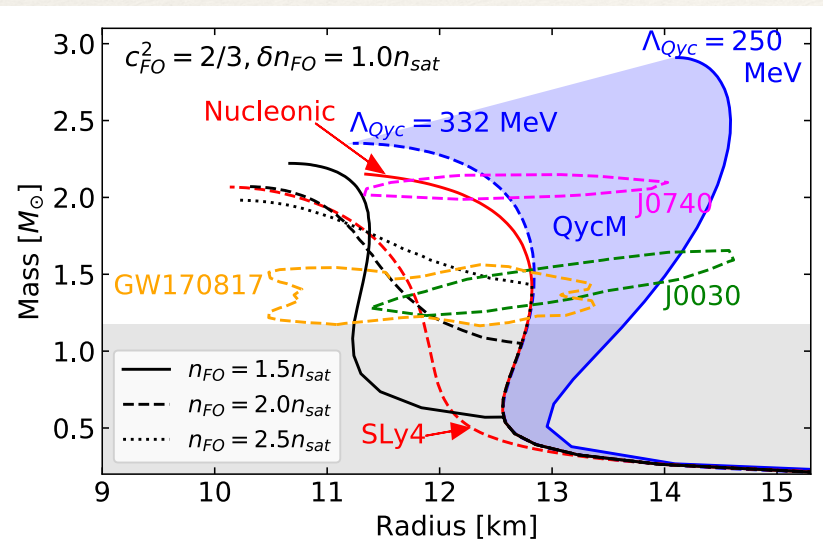
- radio-astronomy,
- x-ray thermal emission from qLMXB,
- gravitational waves from binary neutron stars (LVK),
- non-thermal x-ray emission (NICER).

Theory:

- causality and stability of dense matter,
- chiral effective field theory,
- perturbative QCD,
- phase transitions

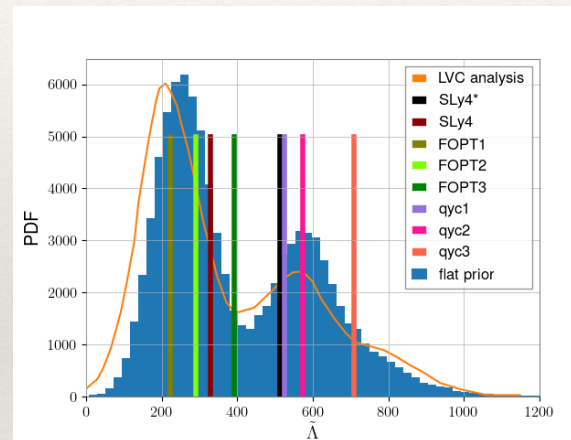
confrontation to data with Bayesian statistics

Impact of phase transitions in the core of neutron stars

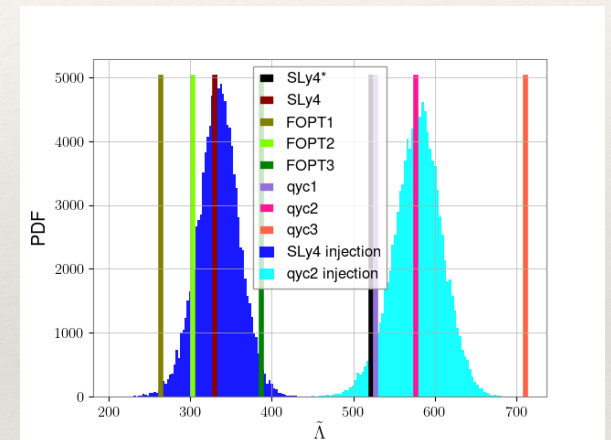


Expectations from GW analysis:

Observation in 2017:



As it would be seen if detected in 2024:



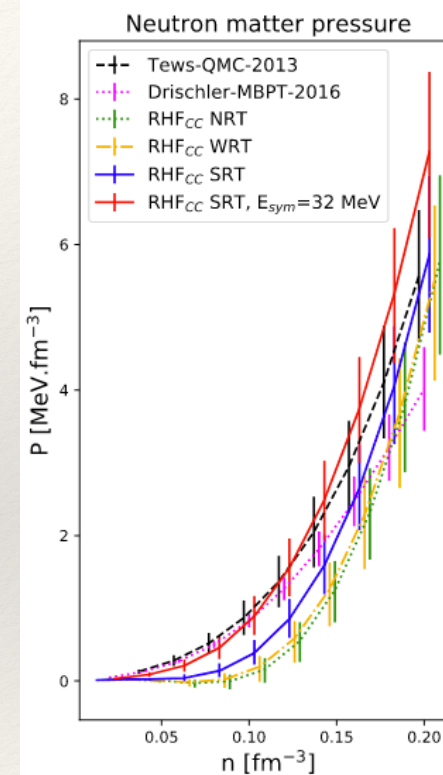
covariant approaches for dense matter

Above n_{sat} the sound speed in dense matter overcomes 10% of the light speed \rightarrow covariant approaches are necessary.

A modern covariant model (by Guy Chanfray) includes chiral symmetry breaking, quark confinement, nucleon form factor and short-range correlations + constraints from NJL quark model and Lattice QCD calculations.

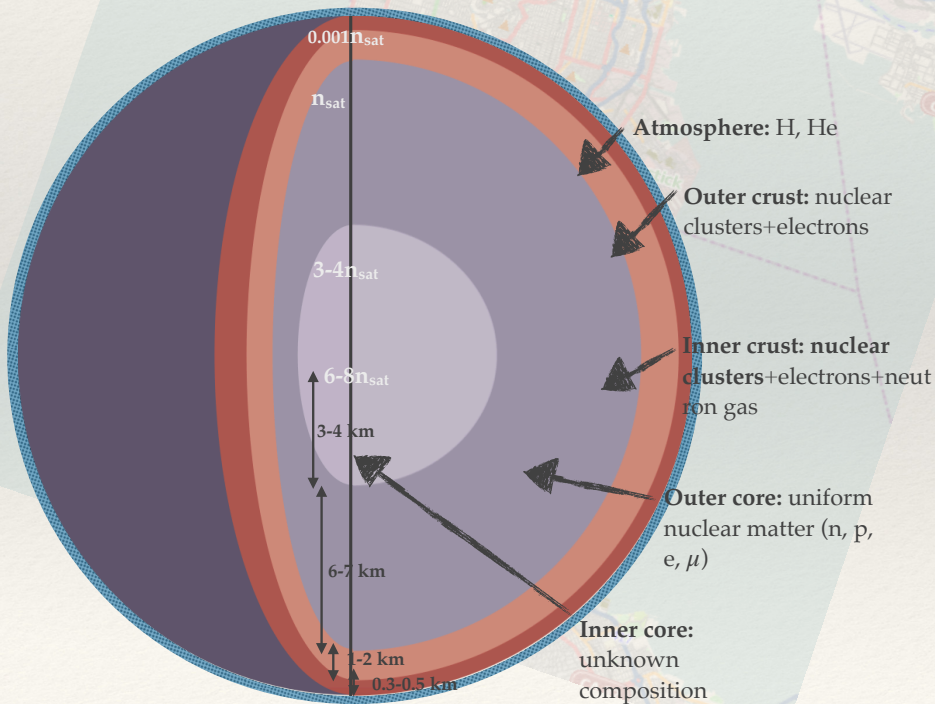
$$\begin{aligned}
 \mathcal{L}_s &= (M_N - M_N(s)) \bar{\psi} \psi - v(s) + \frac{1}{2} \partial^\mu s \partial_\mu s, \\
 \mathcal{L}_\omega &= -g_\omega \omega_\mu \bar{\psi} \gamma^\mu \psi + \frac{1}{2} m_\omega^2 \omega^\mu \omega_\mu - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}, \\
 \mathcal{L}_\rho &= -g_\rho \rho_{a\mu} \bar{\psi} \gamma^\mu \tau_a \psi + g_\rho \frac{\kappa_\rho}{2M_N} \partial_\nu \rho_{a\mu} \bar{\psi} \sigma^{\mu\nu} \tau_a \psi \\
 &\quad + \frac{1}{2} m_\rho^2 \rho_{a\mu} \rho_a^\mu - \frac{1}{4} G_a^{\mu\nu} G_{a\mu\nu}, \\
 \mathcal{L}_\delta &= -g_\delta \delta_a \bar{\psi} \tau_a \psi - \frac{1}{2} m_\delta \delta_a \delta_a + \frac{1}{2} \partial^\mu \delta_a \partial_\mu \delta_a, \\
 \mathcal{L}_\pi &= \frac{g_A}{2f_\pi} \partial_\mu \varphi_{\pi a} \bar{\psi} \gamma^\mu \gamma^5 \tau_a \psi - \frac{1}{2} m_\pi^2 \varphi_{\pi a} \varphi_{\pi a} \\
 &\quad + \frac{1}{2} \partial^\mu \varphi_{\pi a} \partial_\mu \varphi_{\pi a},
 \end{aligned}$$

\longrightarrow RHF-CC \longrightarrow



tentative conclusions

The near future will see an accumulation of more and more data containing dense matter properties. It is very possible that the question of the existence of phase transition(s) in the core of neutron stars will get an answer in the next 10 years.



But, it will not necessarily be easy since:

- The properties of neutron star core at the densities above n_{sat} are yet impossible to determine from first principle.
- Data alone may not be accurate enough (despite tremendous progress in nuclear experiments and astrophysical observations).

Future discoveries require :

- reliable model(s) for dense matter,
- new data with improved accuracy,
- and an efficient way to combine data and model together.