

Mapping the one-loop structure of the linear SM extensions

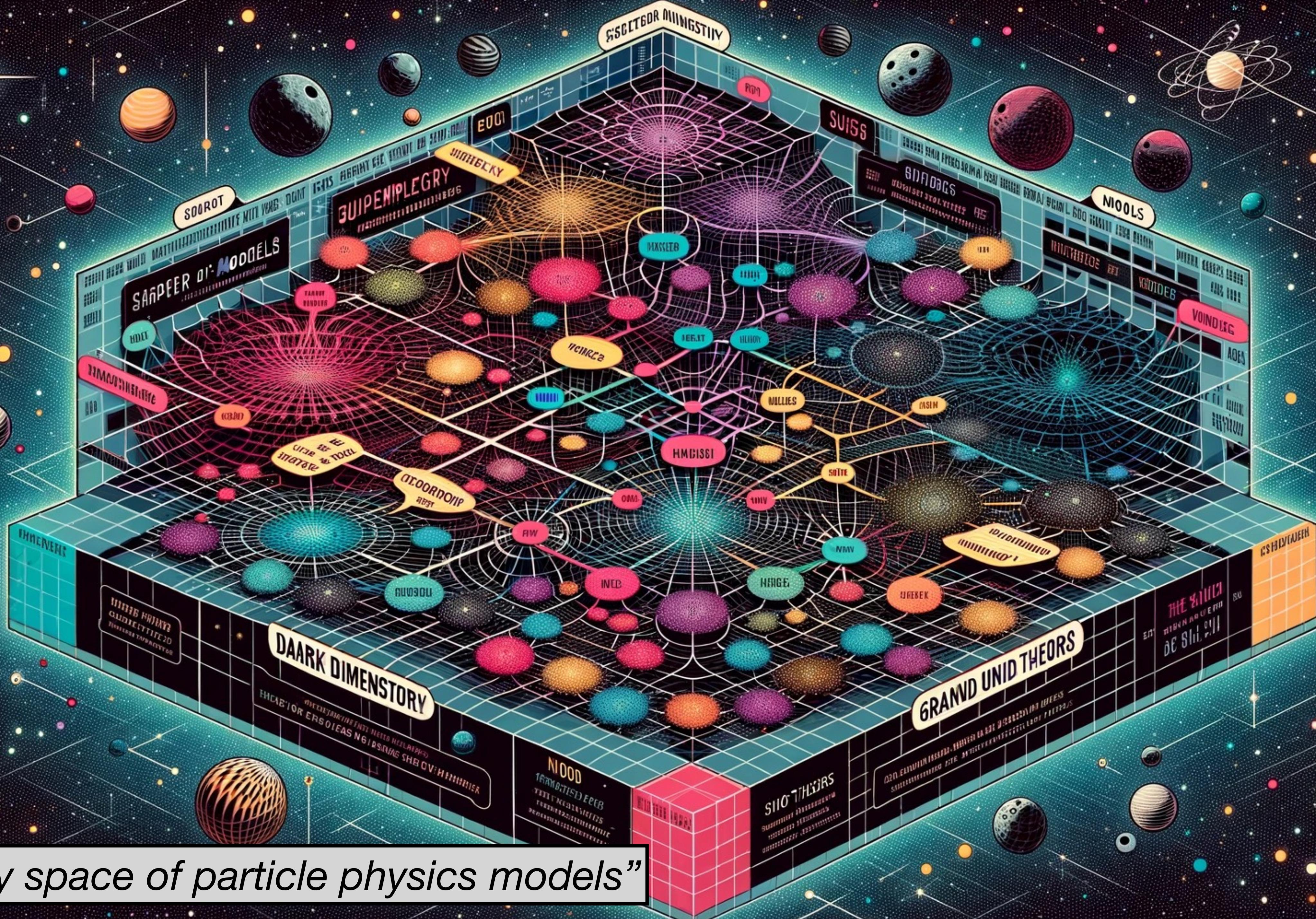
John Gargalionis, Jérémie Quevillon, Pham Ngoc Hoa Vuong, Tevong You
[arXiv: 24XX.XXXX]

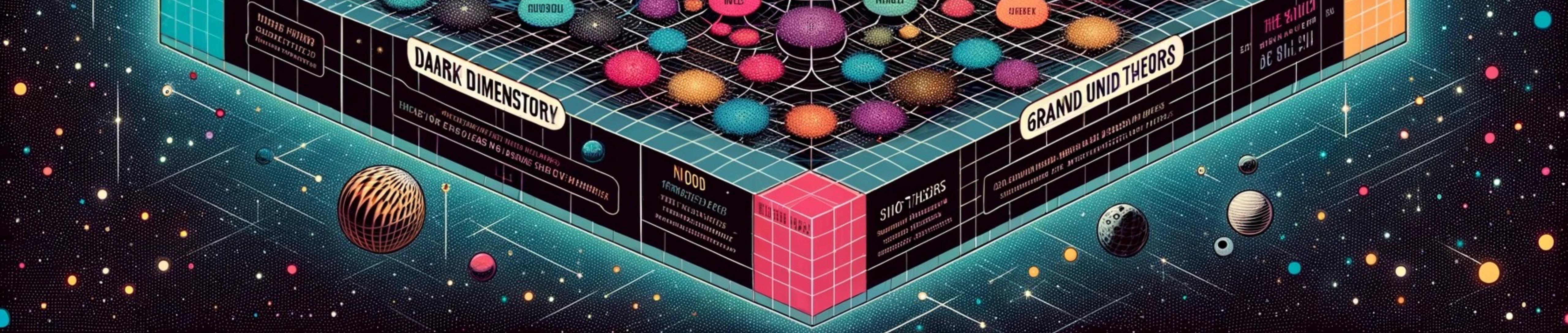


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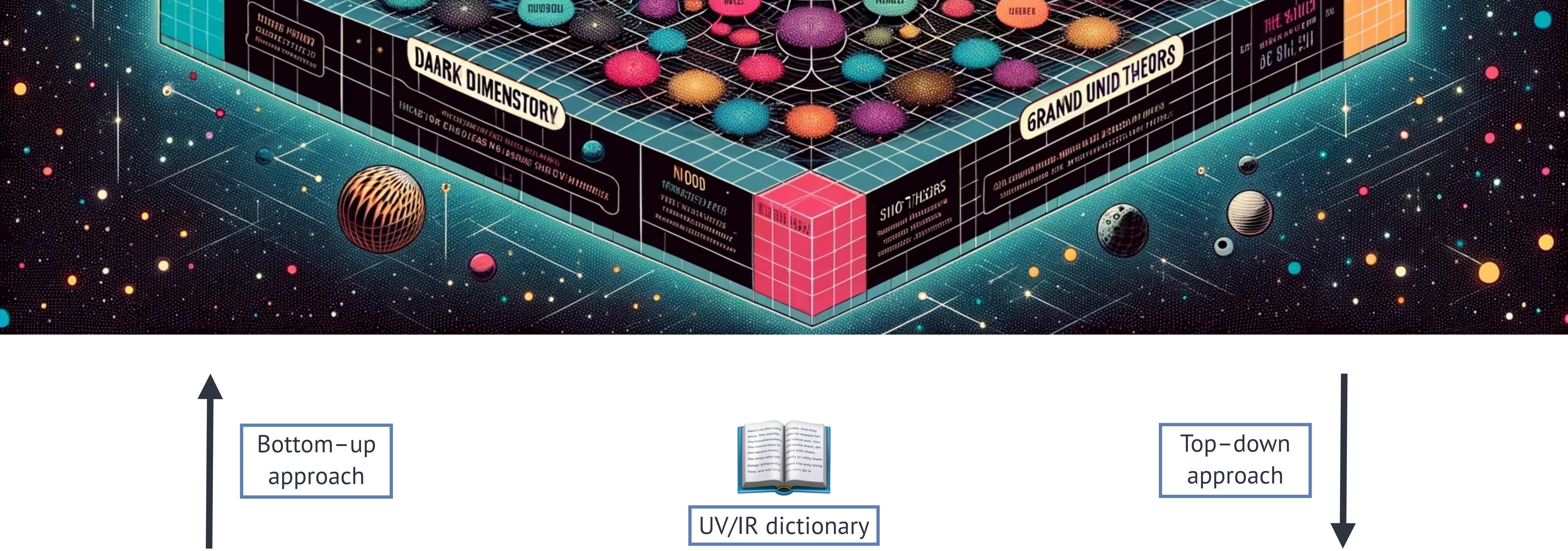
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$$H \sim (1, 2, \frac{1}{2}), \quad Q \sim (3, 2, \frac{1}{6}), \quad \bar{u} \sim (\bar{3}, 1, -\frac{2}{3}), \quad \bar{d} \sim (\bar{3}, 1, \frac{1}{3}), \quad L \sim (1, 2, -\frac{1}{2}), \quad \bar{e} \sim (1, 1, 1)$$

$$\mathcal{L}_{\text{SM}} = \mathcal{L}_{d \leq 4} + \sum_{p,q} \frac{c_{pq}^{(5)}}{\Lambda} (L_p L_q) H H + \sum_{i=1}^{2499} \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{d=6} + \dots$$



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$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{p,q} c_{pq}^{(5)} (L_p L_q) H H + \sum_{i=1}^{2499} \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{d=6} + \dots$$

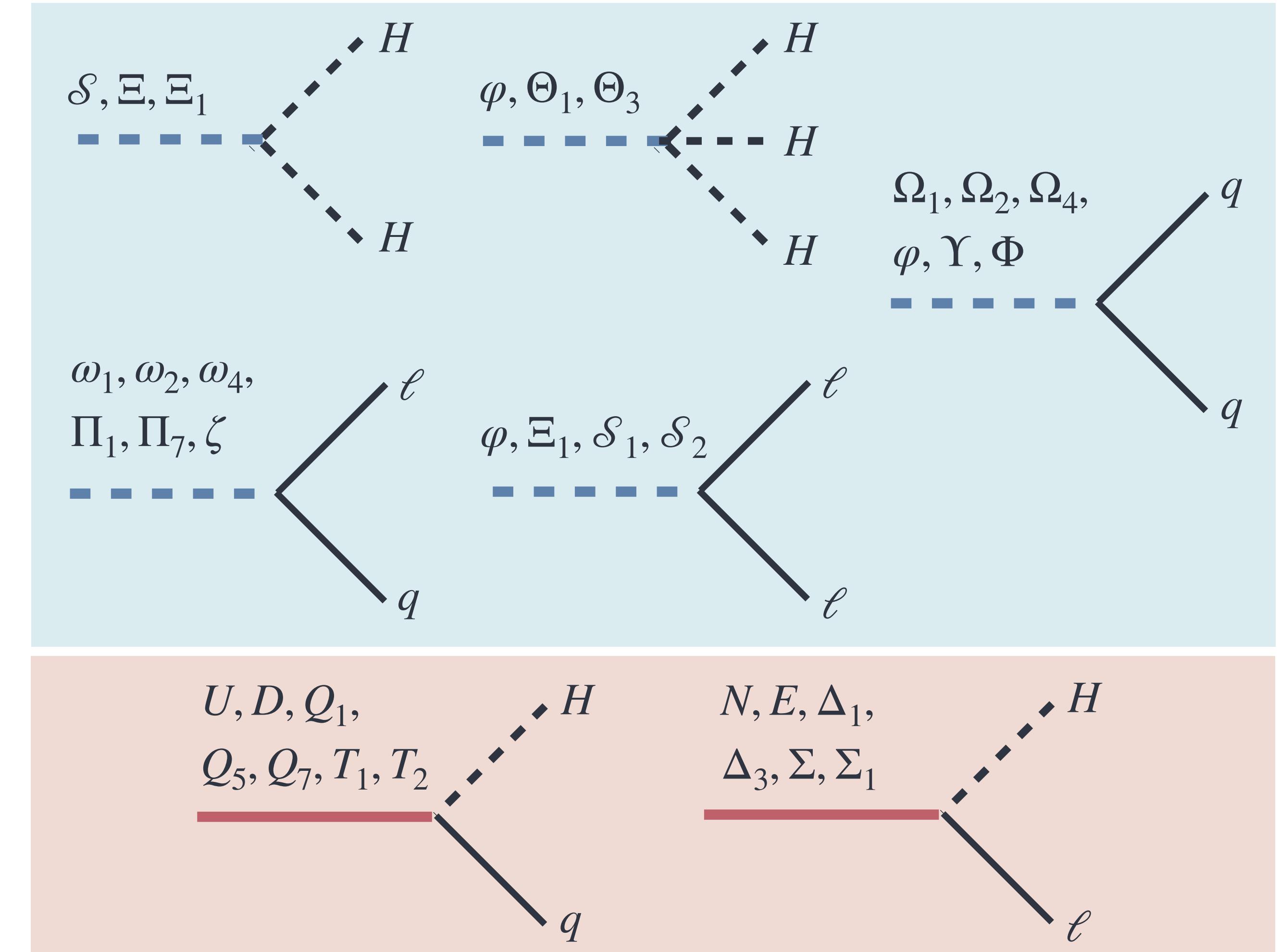
Linear SM extensions

Granada dictionary: de Blas, Criado, Pérez-Victoria, Santiago arXiv:1711.10391
MatchingTools: Criado arXiv:1710.06445

- Patterns of **minimal tree-level deviation** from the SM can be understood in terms of **linear SM extensions**

$$\mathcal{L}_{\text{int}} \sim \text{SM} \cdot \text{SM} \cdot X + \text{SM} \cdot \text{SM} \cdot \text{SM} \cdot X + \dots$$

- 48 exotic multiplets** generating $d = 6$ operators at tree level, we leave out vector bosons
- Fermions enter as vector-like or Majorana
- Represent a **non-trivial cross section** of exotics search programme at the LHC



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Name	\mathcal{S}	\mathcal{S}_1	\mathcal{S}_2	φ	Ξ	Ξ_1	Θ_1	Θ_3
Irrep	$(1, 1)_0$	$(1, 1)_1$	$(1, 1)_2$	$(1, 2)_{\frac{1}{2}}$	$(1, 3)_0$	$(1, 3)_1$	$(1, 4)_{\frac{1}{2}}$	$(1, 4)_{\frac{3}{2}}$
Name	ω_1	ω_2	ω_4	Π_1	Π_7	ζ		
Irrep	$(3, 1)_{-\frac{1}{3}}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{4}{3}}$	$(3, 2)_{\frac{1}{6}}$	$(3, 2)_{\frac{7}{6}}$	$(3, 3)_{-\frac{1}{3}}$		
Name	Ω_1	Ω_2	Ω_4	Υ	Φ			
Irrep	$(6, 1)_{\frac{1}{3}}$	$(6, 1)_{-\frac{2}{3}}$	$(6, 1)_{\frac{4}{3}}$	$(6, 3)_{\frac{1}{3}}$	$(8, 2)_{\frac{1}{2}}$			

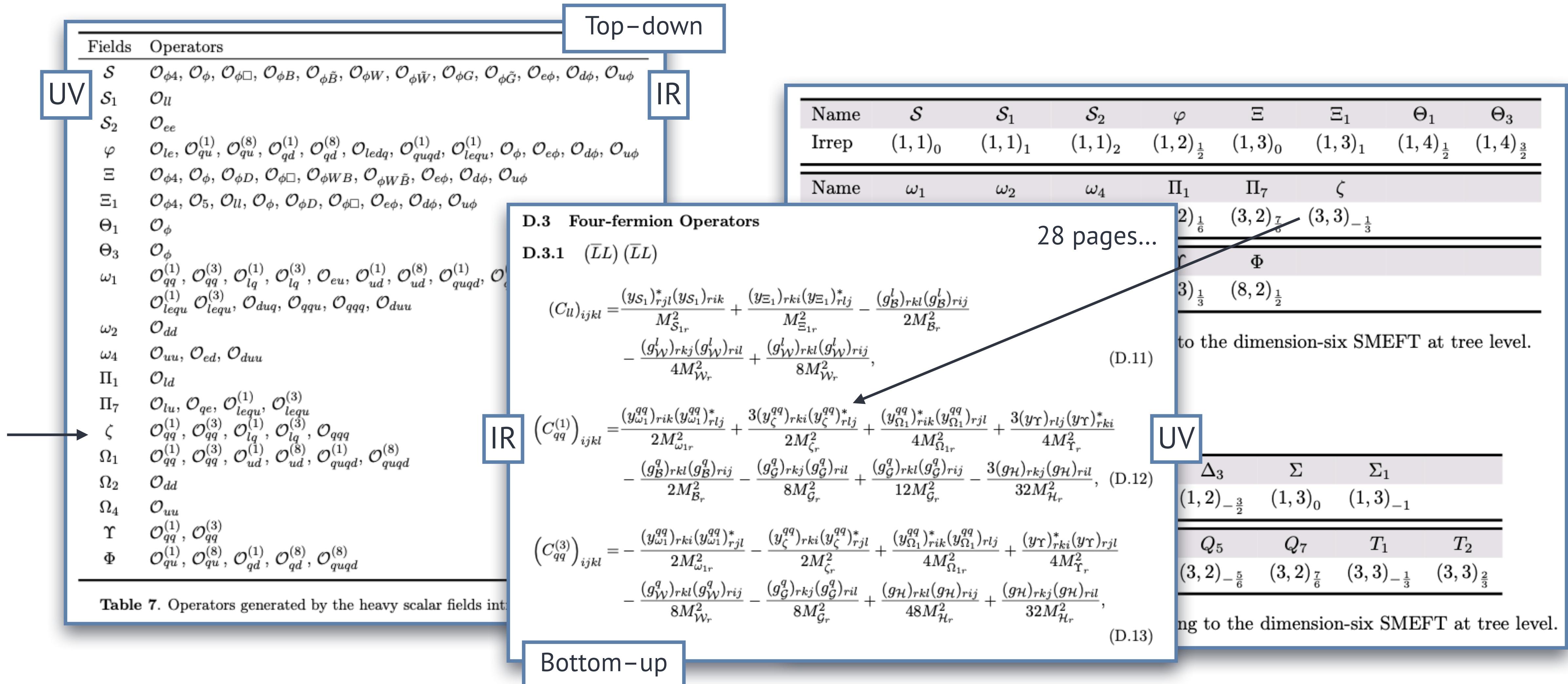
Table 1. New scalar bosons contributing to the dimension-six SMEFT at tree level.

Name	N	E	Δ_1	Δ_3	Σ	Σ_1	
Irrep	$(1, 1)_0$	$(1, 1)_{-1}$	$(1, 2)_{-\frac{1}{2}}$	$(1, 2)_{-\frac{3}{2}}$	$(1, 3)_0$	$(1, 3)_{-1}$	
Name	U	D	Q_1	Q_5	Q_7	T_1	T_2
Irrep	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$	$(3, 2)_{\frac{1}{6}}$	$(3, 2)_{-\frac{5}{6}}$	$(3, 2)_{\frac{7}{6}}$	$(3, 3)_{-\frac{1}{3}}$	$(3, 3)_{\frac{2}{3}}$

Table 2. New vector-like fermions contributing to the dimension-six SMEFT at tree level.

Tree-level UV/IR dictionary

Granada dictionary: de Blas, Criado, Pérez-Victoria, Santiago arXiv:1711.10391
 MatchingTools: Criado arXiv:1710.06445



One-loop tools

Impressive recent progress in automating one-loop matching:

- CoDeX implements UOLEA results
- MatchMakerEFT implements diagrammatic matching
- Matchete uses functional techniques (built upon SuperTracer)

CoDeX:

UOLEA results:

Bakshi Chakrabortty, Patra arXiv:1808.04403

Drozd, Ellis, Quevillon, You arXiv:1512.03003

Ellis, Quevillon, You, Zhang arXiv:1604.02445

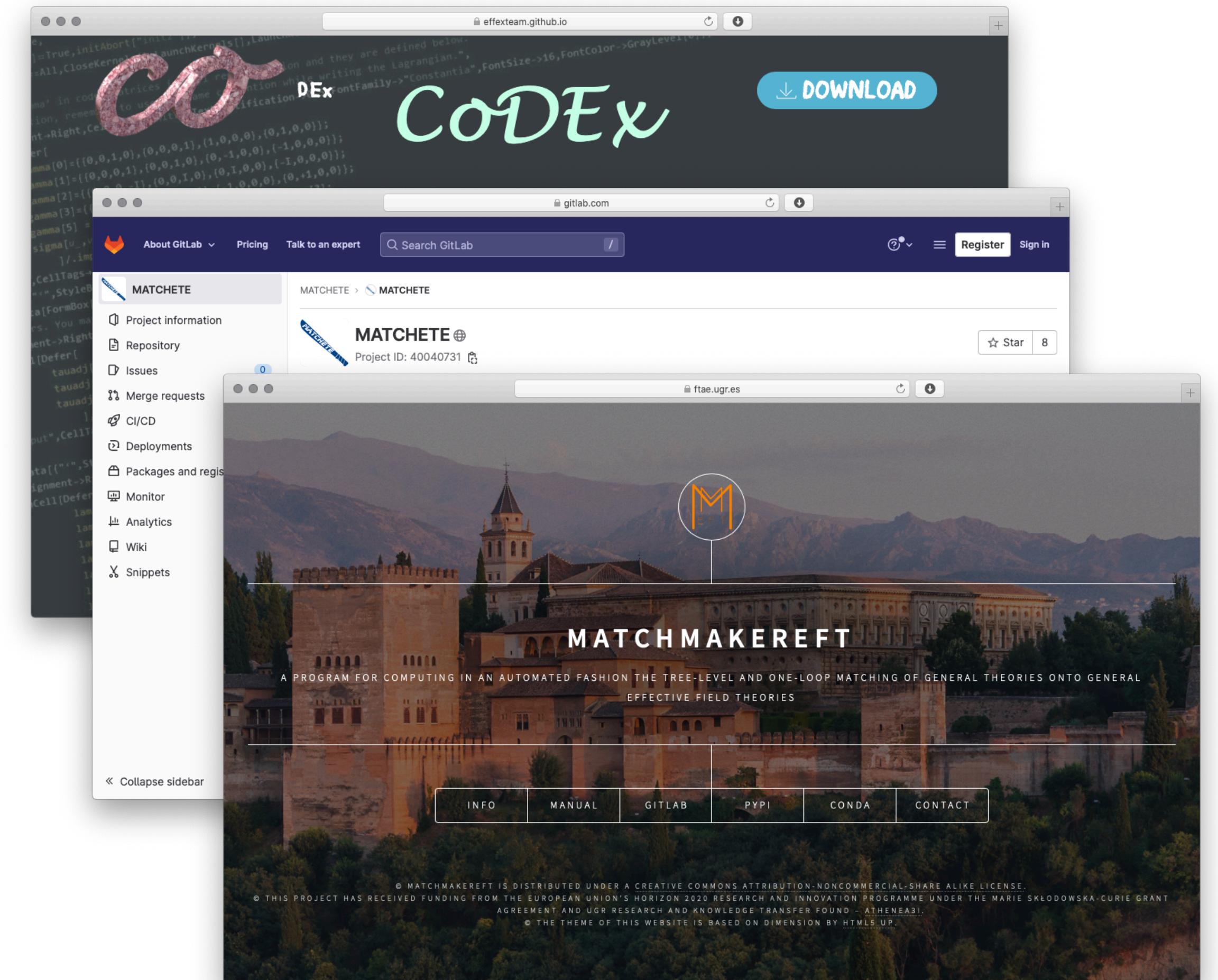
Ellis, Quevillon, Vuong, You, Zhang arXiv:2006.16260

Larue, Quevillon arXiv:2303.10203

MatchMakerEFT:

SOLD:

Matchete & SuperTracer: Fuentes-Martín, Koenig, Pagès, Thomsen, Wilsch arXiv:2212.04510, arXiv:2012.08506

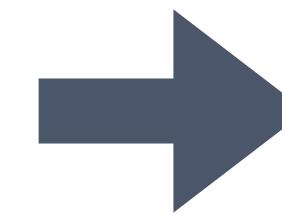
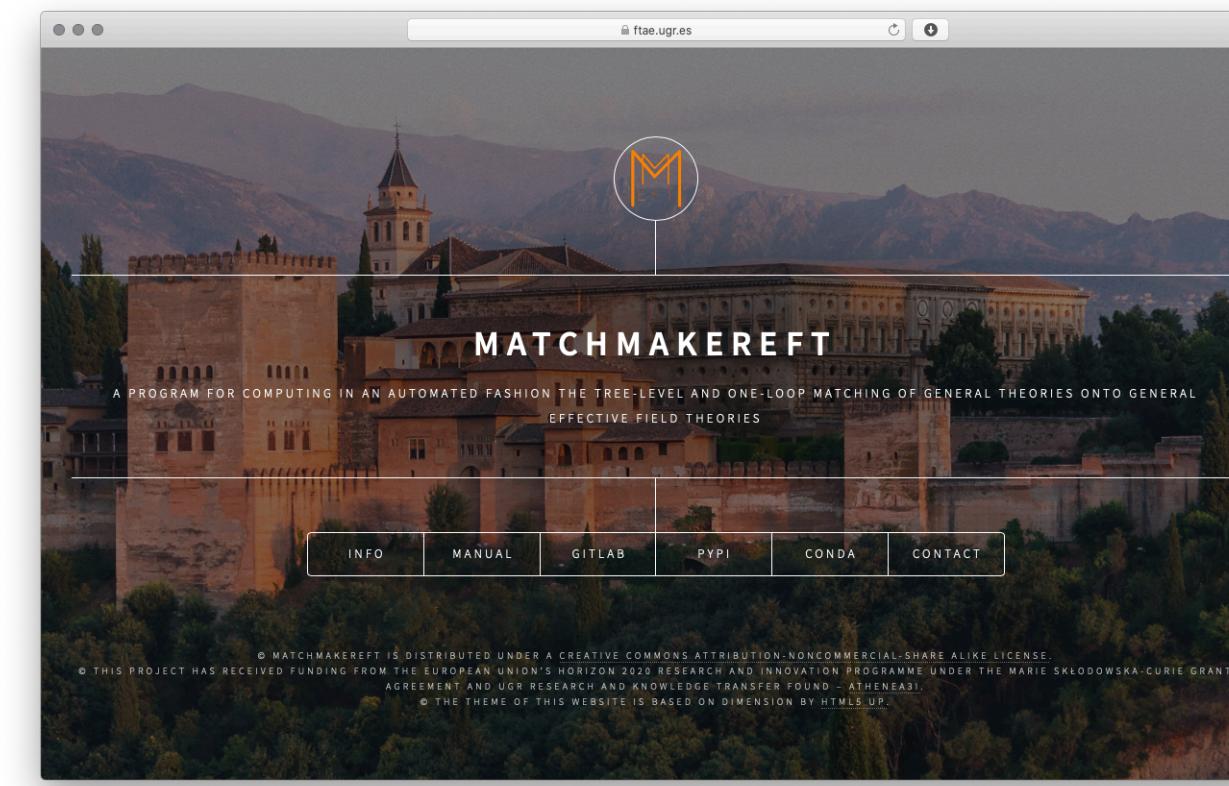
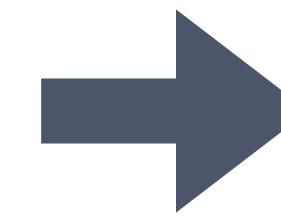


A one-loop dictionary for the linear SM extensions

Main aim:

Use these tools to extend results for the **linear SM extensions** to the **one-loop level**

Extend Lagrangian sufficient to generate dimension-6 operators at one loop



MatchMakerParser:
Parses Mathematica to Python, writes classes for each multiplet

TLR

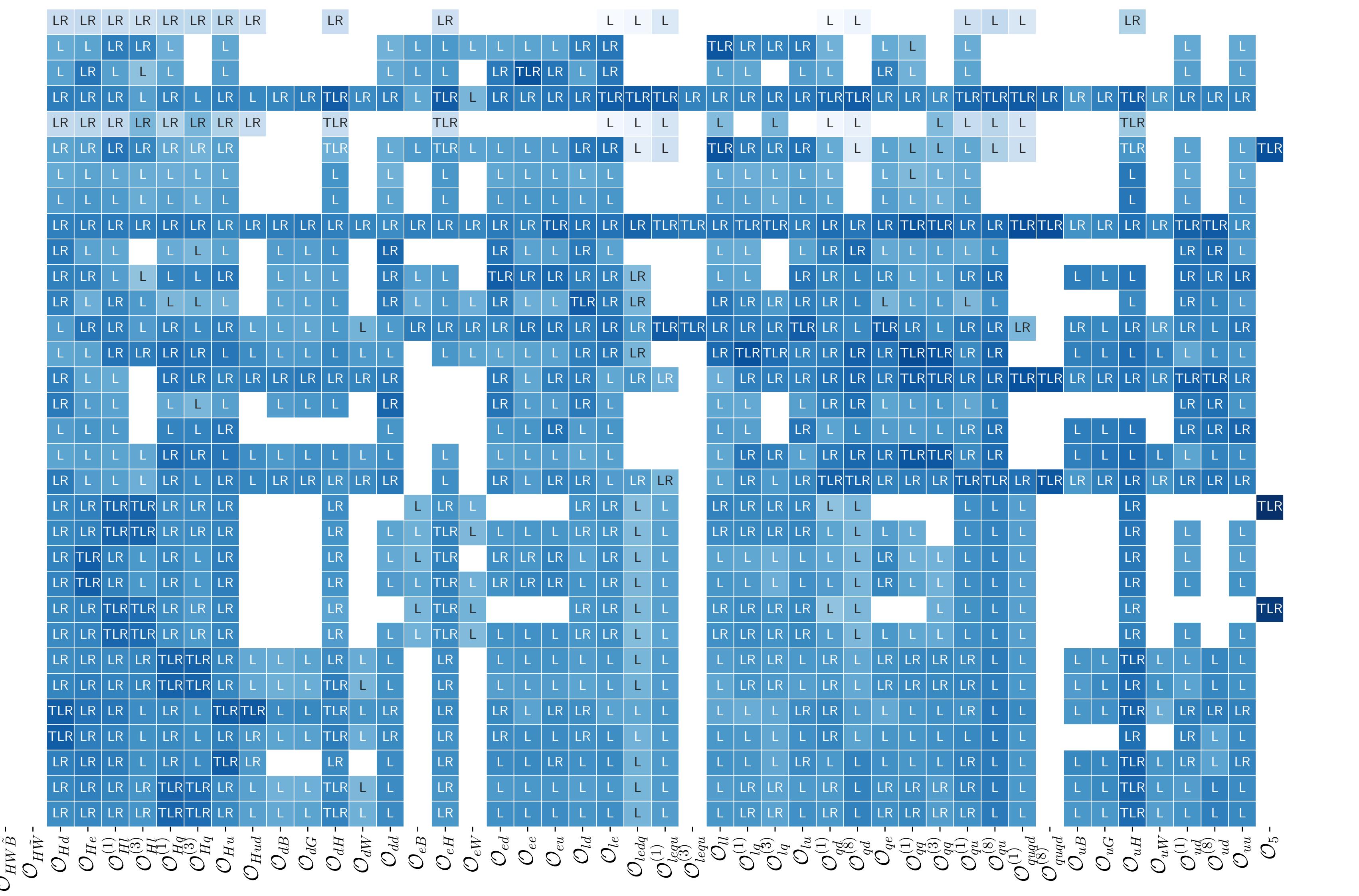
Tree generated
Loop generated
GE induced

Scalars

	T_2	T_1	Q_7	Q_1	D	$U\Sigma_1$	$\Sigma\Delta_3\Delta_1$	E	N	Φ	Υ	Ω_4	Ω_2	Ω_1	$\zeta\Pi_7\Pi_1$	ω_4	ω_2	ω_1	Θ_3	Θ_1	Ξ_1	φ	S_2	S_1	S
\mathcal{O}_G	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{\tilde{G}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
\mathcal{O}_W	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{\tilde{W}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
\mathcal{O}_H	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H\tilde{B}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H D}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H G}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H W}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H \tilde{B}^*}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H D^2}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H \tilde{G}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H W B^-}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H \tilde{W}^-}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L

Fermions

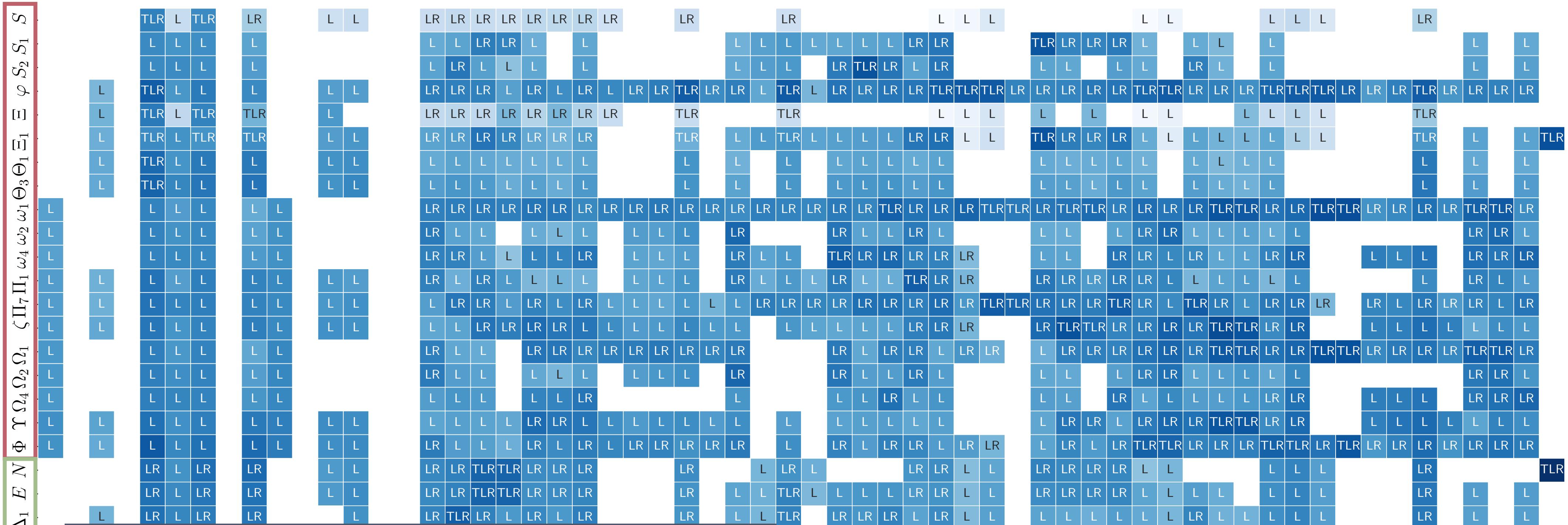
	T_2	T_1	Q_7	Q_1	D	$U\Sigma_1$	$\Sigma\Delta_3\Delta_1$	E	N	Φ	Υ	Ω_4	Ω_2	Ω_1	$\zeta\Pi_7\Pi_1$	ω_4	ω_2	ω_1	Θ_3	Θ_1	Ξ_1	φ	S_2	S_1	S
\mathcal{O}_G	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{\tilde{G}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
\mathcal{O}_W	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{\tilde{W}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
\mathcal{O}_H	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H\tilde{B}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H D}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H G}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H W}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H \tilde{B}^*}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H D^2}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H \tilde{G}}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H W B^-}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L
$\mathcal{O}_{H \tilde{W}^-}$	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L	L



TLR

Tree generated
Loop generated
GE induced

Scalars

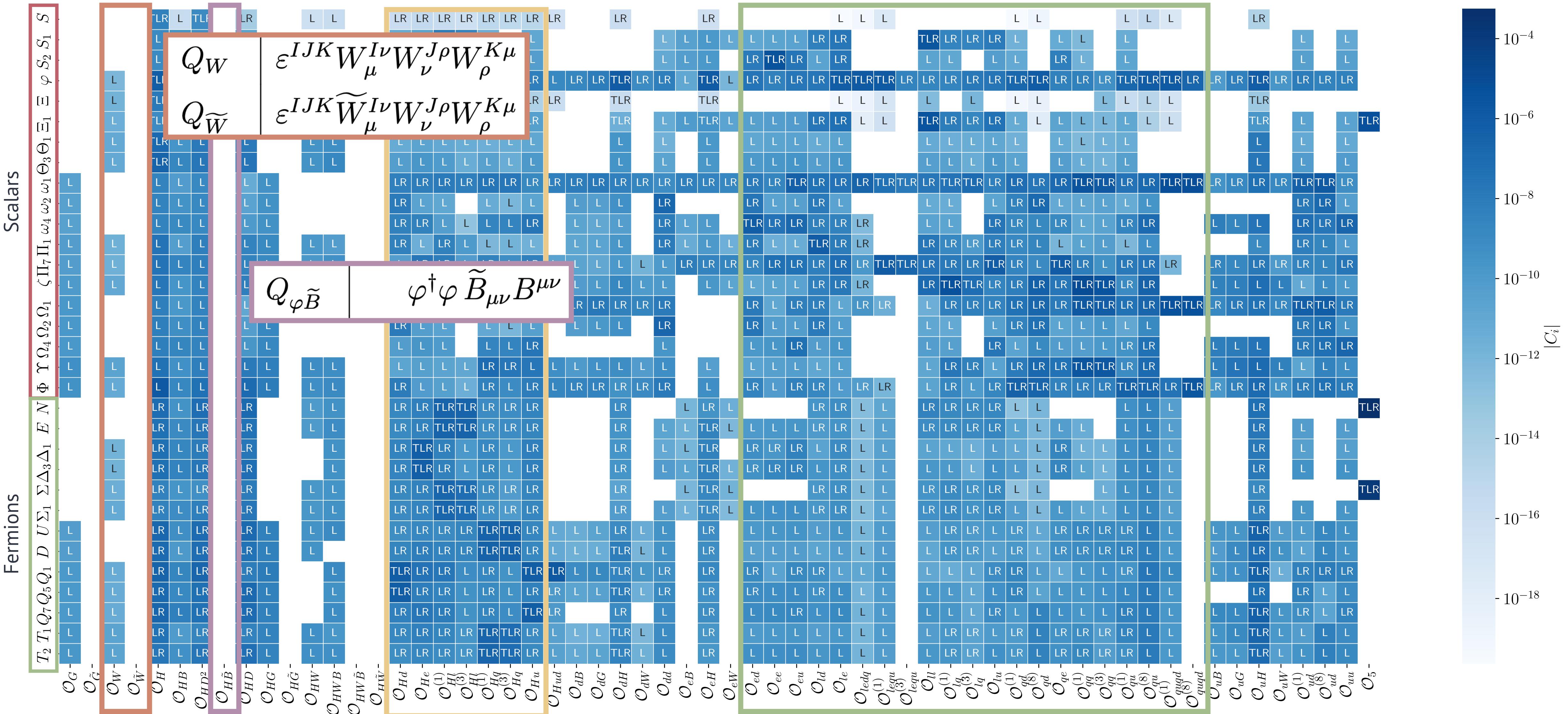


Assumptions:

- Only one multiplet at a time
- All NP couplings set to 1
- All dimensionful UV parameters set to 1 TeV

TLR

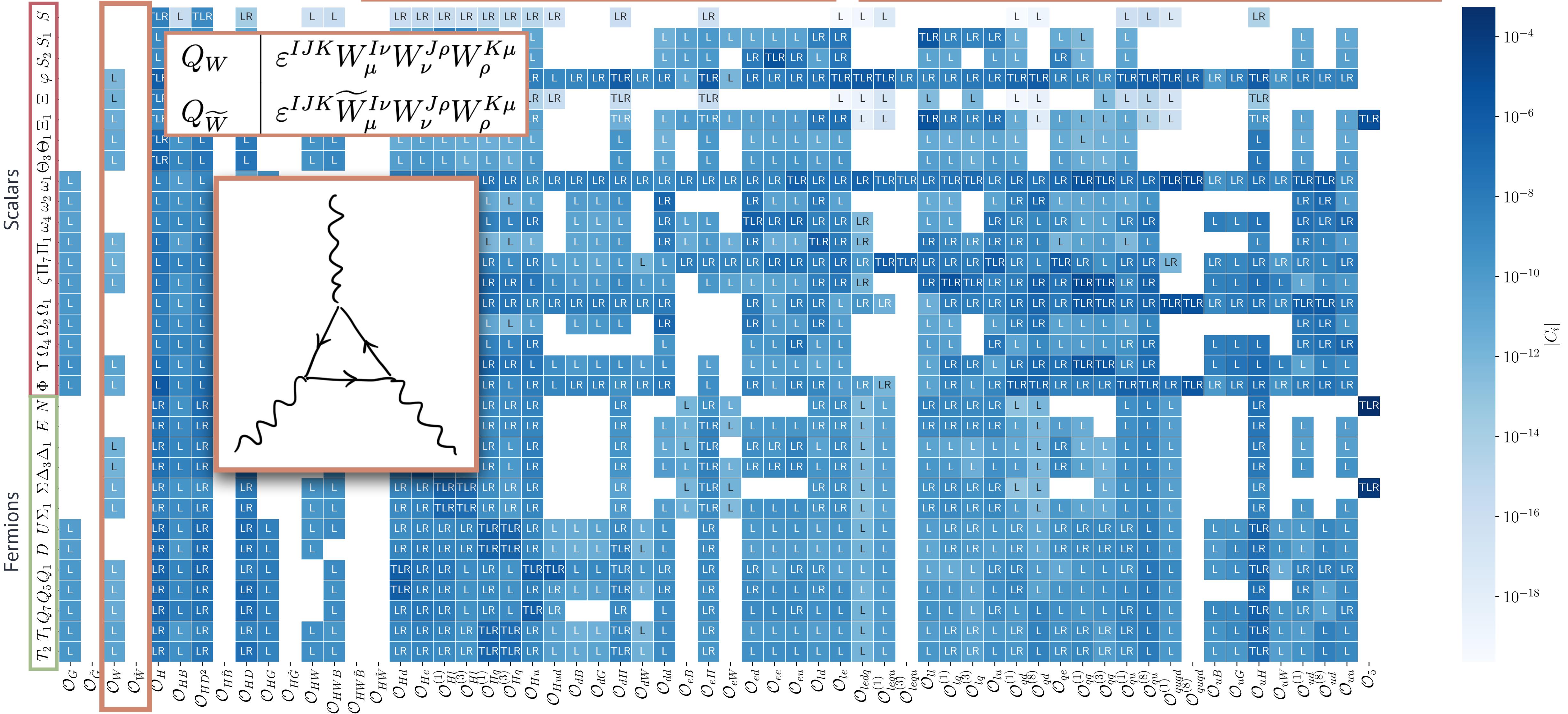
Tree generated
Loop generated
GE induced



TLR
Loop generated
RGE induced

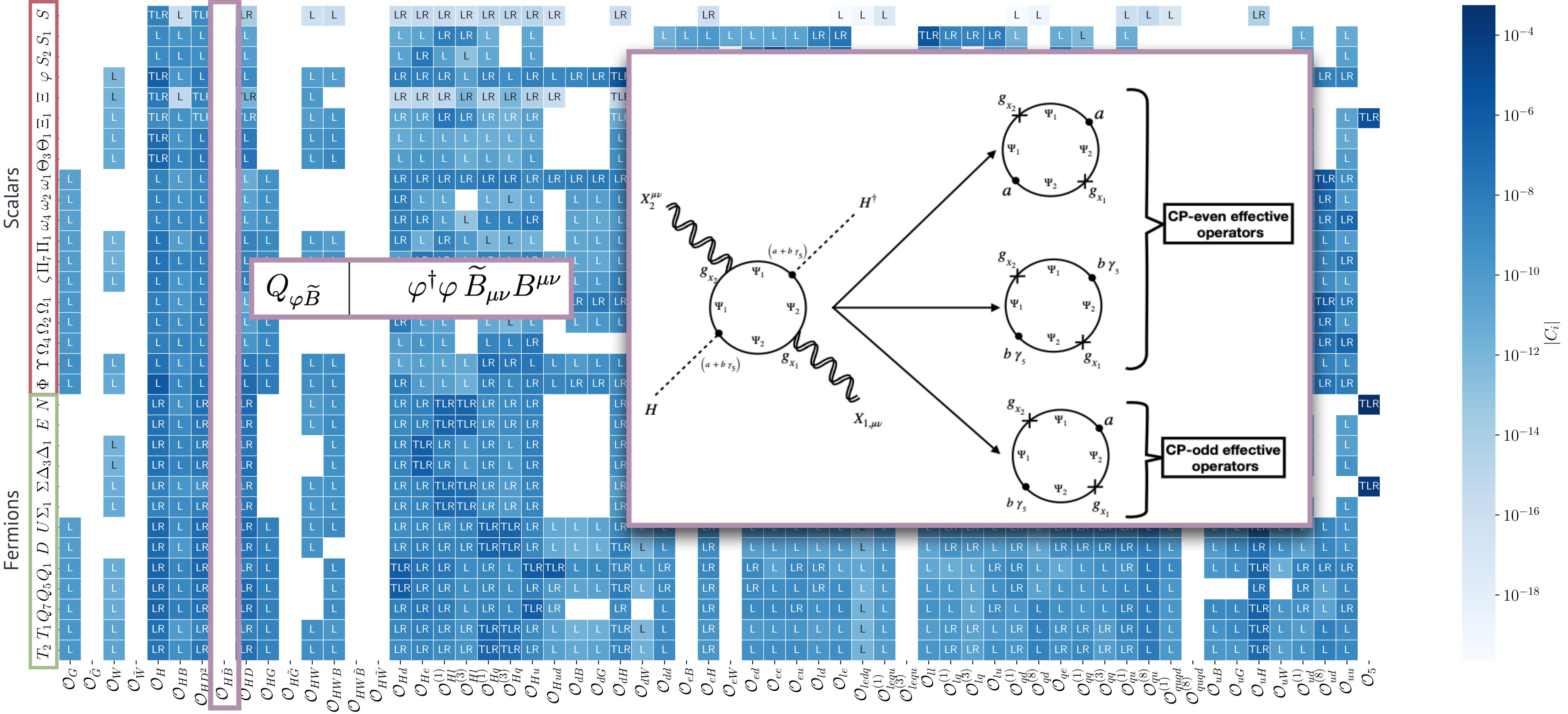
CP-even triple-gauge operators not generated at tree-level

CP-odd triple-gauge operators not generated at one loop:
Clear already from UOLEA



Tree generated
Loop generated
R GE induced

Other CP-odd bosonic operators can be generated at one loop,
require **two** exotic multiplets



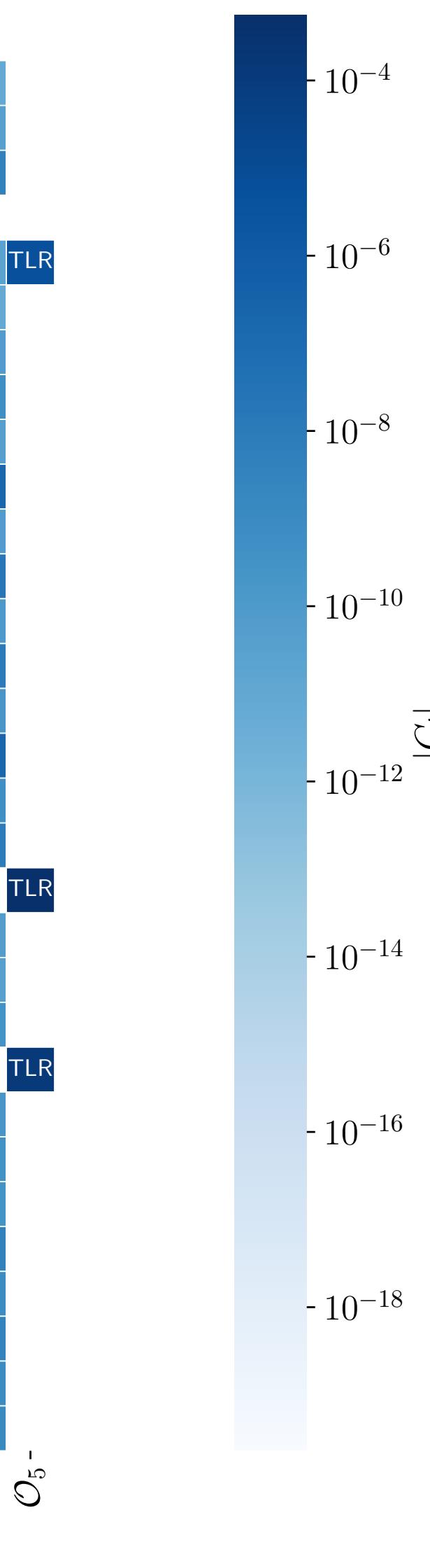
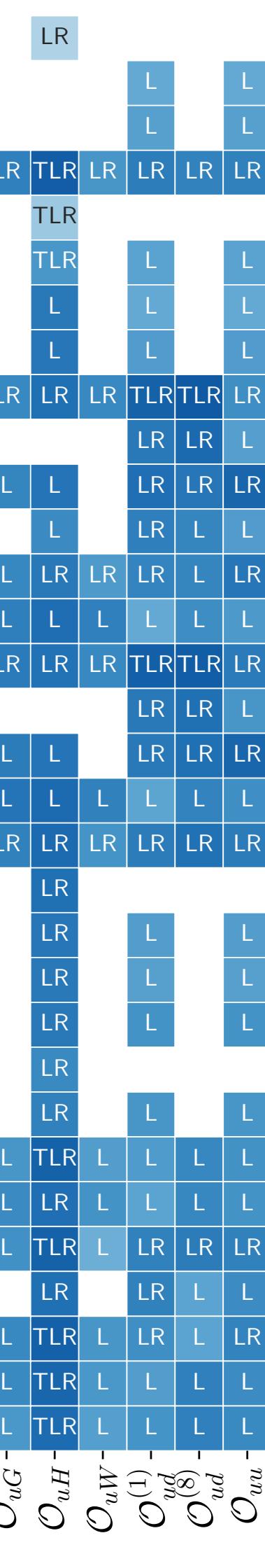
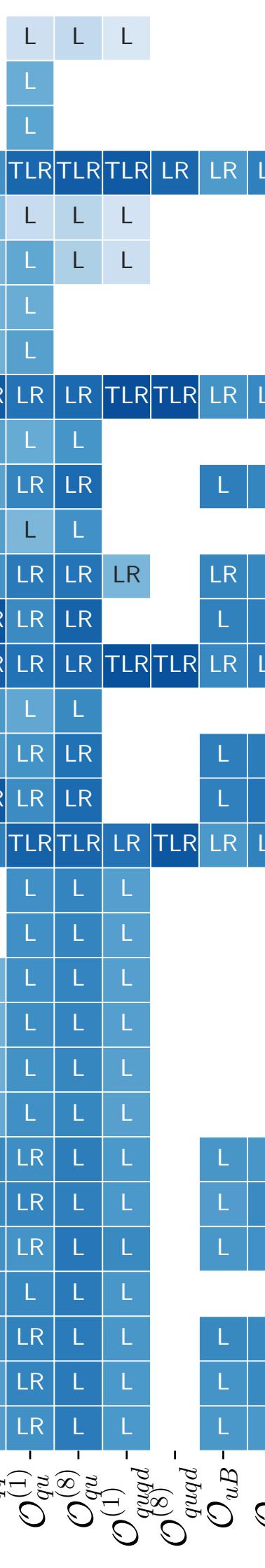
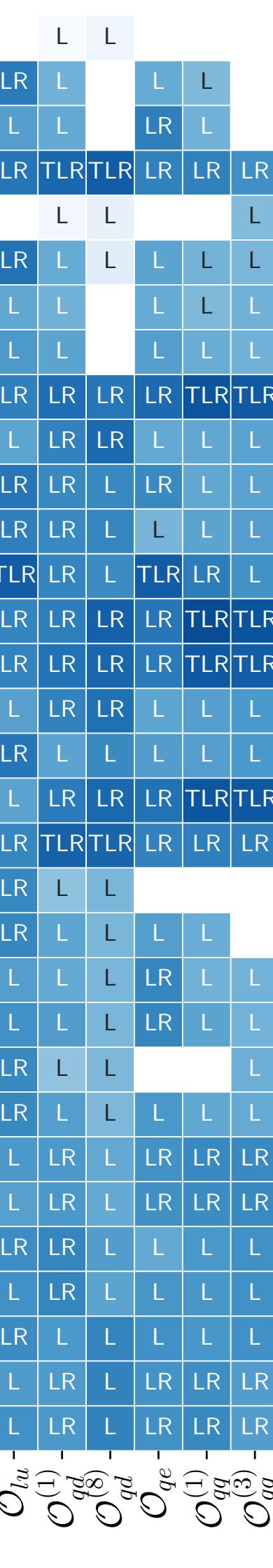
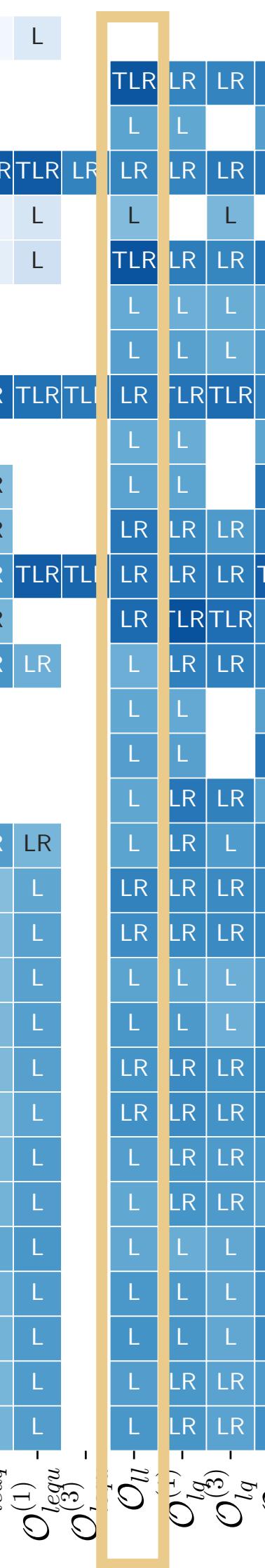
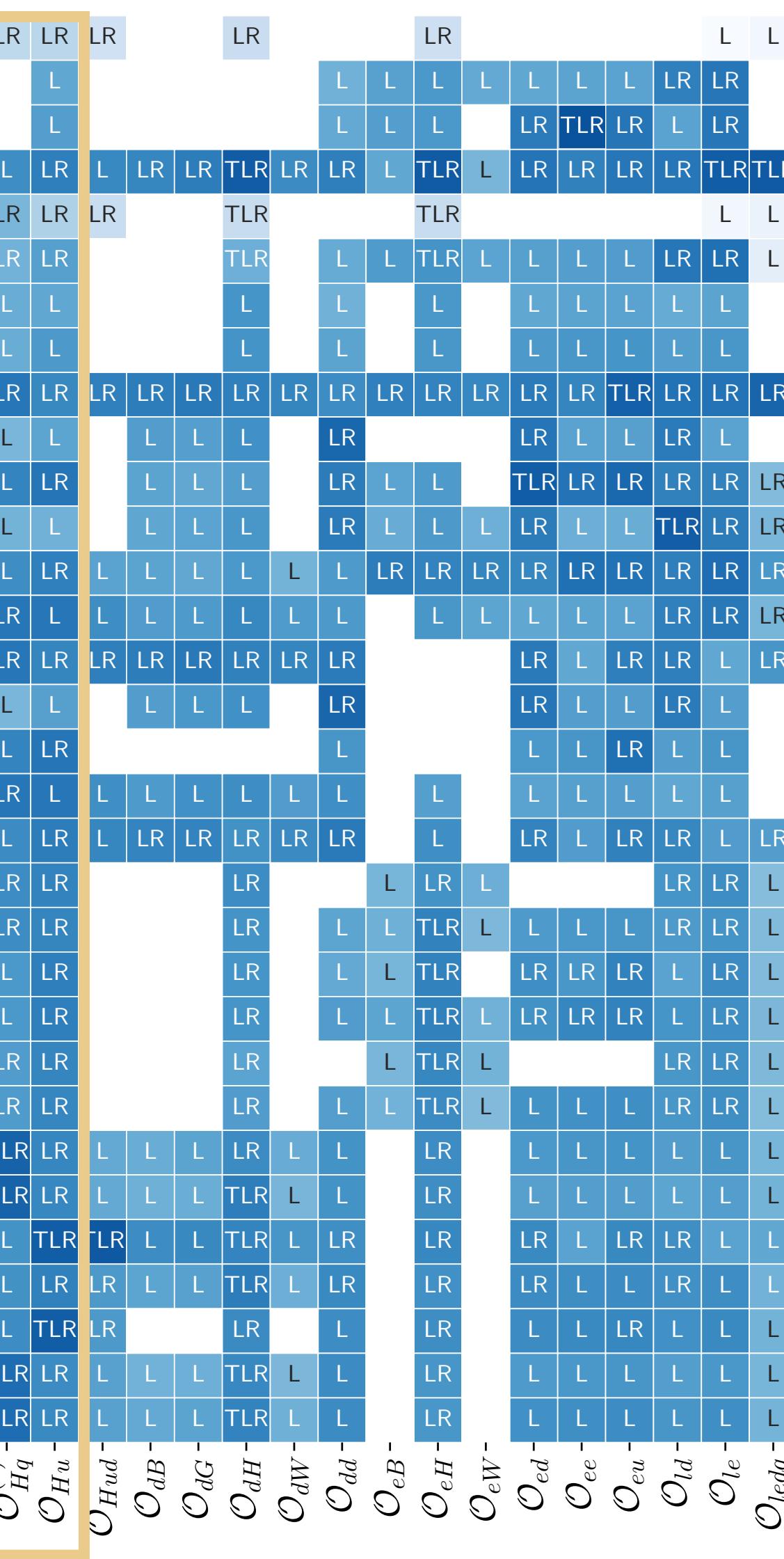
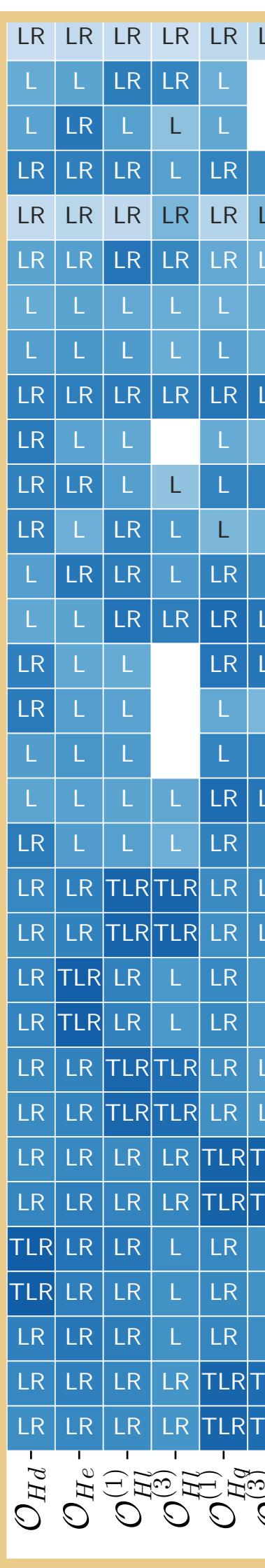
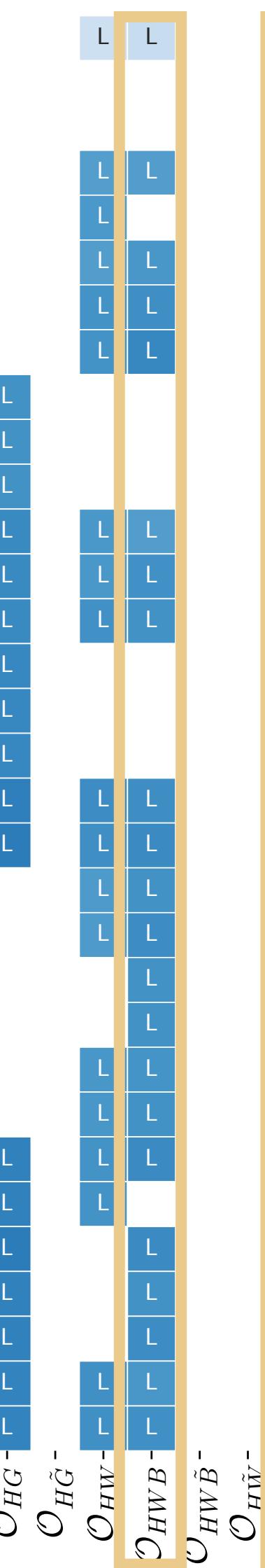
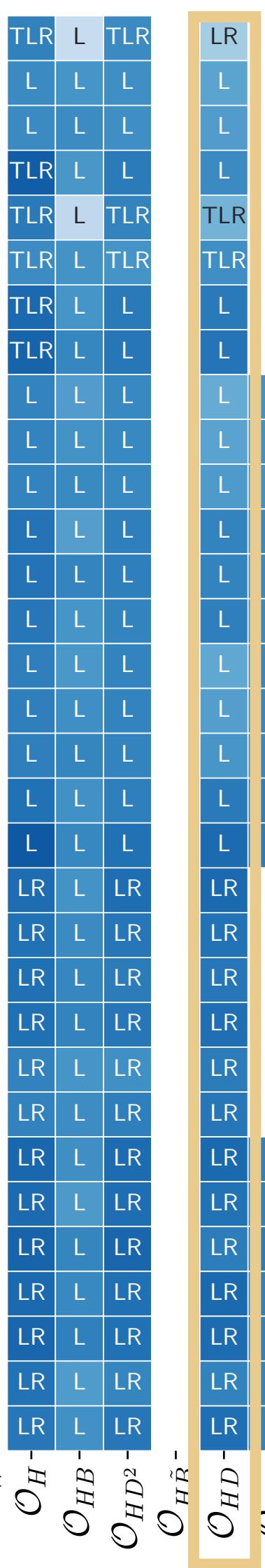
TLR

Tree generated
Loop generated
R GE induced

 $\sim T$ and S parameters

Scalars

	T_2	T_1	$Q_7 Q_1 D$	$U \Sigma_1 \Sigma \Delta_3 \Delta_1 E N$	$\Phi \Upsilon \Omega_4 \Omega_2 \Omega_1 \zeta \Pi_7 \Pi_1 \omega_1 \Theta_3 \Theta_1 \Xi_1 \varphi S_2 S_1 S$
\mathcal{O}_G -	L	L	L	L	L
$\mathcal{O}_{\tilde{G}}$ -	L	L	L	L	L
\mathcal{O}_W -	L	L	L	L	L
$\mathcal{O}_{\tilde{W}}$ -	L	L	L	L	L
\mathcal{O}_H -	L	L	L	L	L
$\mathcal{O}_{H\tilde{B}}$ -	L	L	L	L	L
\mathcal{O}_{HD^2} -	L	L	L	L	L
$\mathcal{O}_{H\tilde{D}^2}$ -	L	L	L	L	L
$\mathcal{O}_{H\tilde{H}}$ -	L	L	L	L	L
$\mathcal{O}_{H\tilde{G}}$ -	L	L	L	L	L
$\mathcal{O}_{HW\tilde{B}}$ -	L	L	L	L	L
$\mathcal{O}_{HW\tilde{H}}$ -	L	L	L	L	L



Operators contributing to EWPO

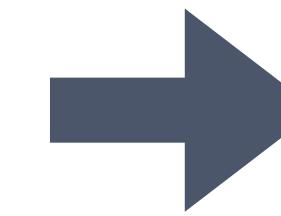
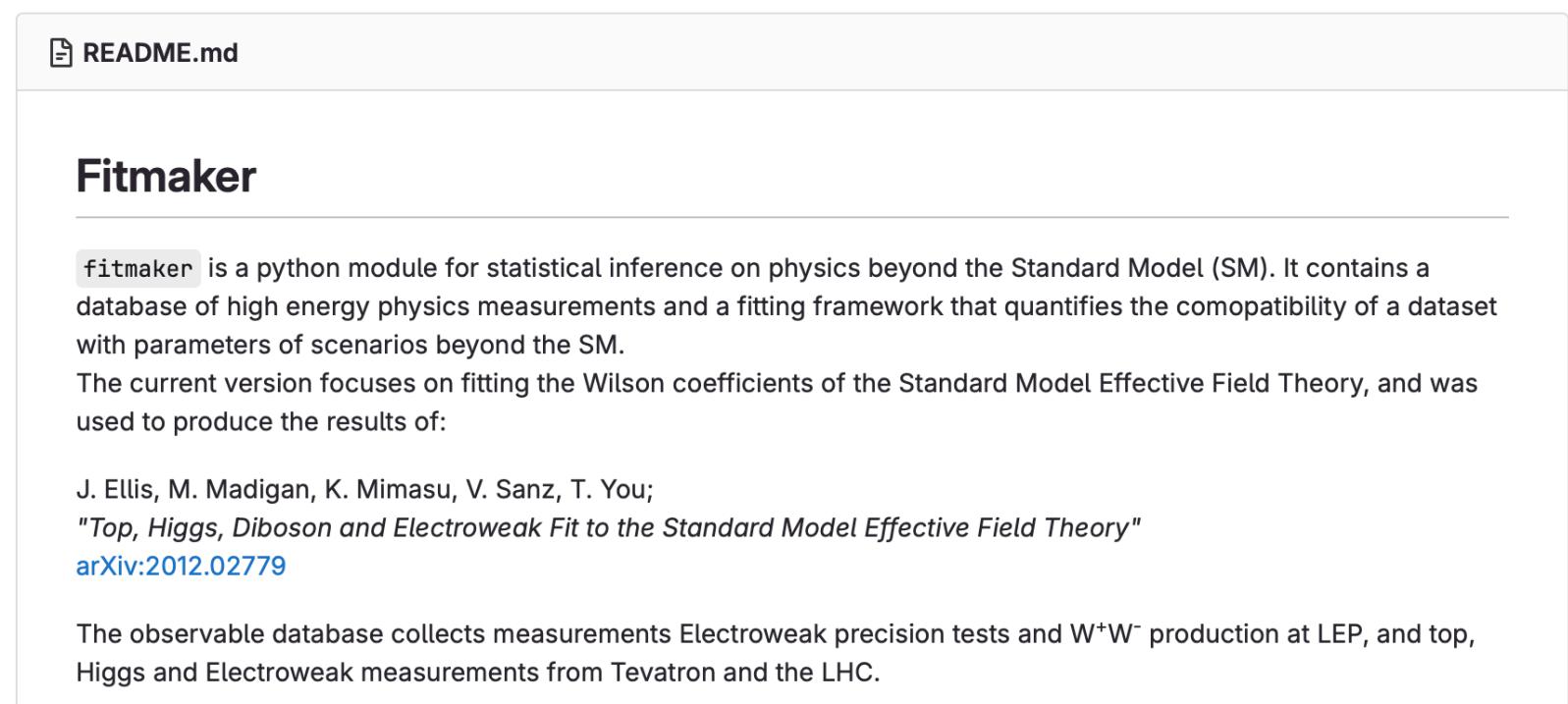
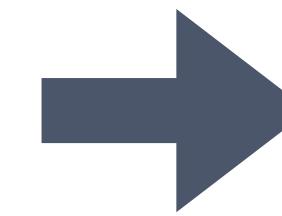
Allwicher, McCullough, Renner arXiv:2408.03992

Tera-Z sensitivity to linear SM extensions

Allwicher, McCullough, Renner arXiv:2408.03992

All of the linear SM extensions contribute at loop level to EWPO and can be probed at a Tera-Z run

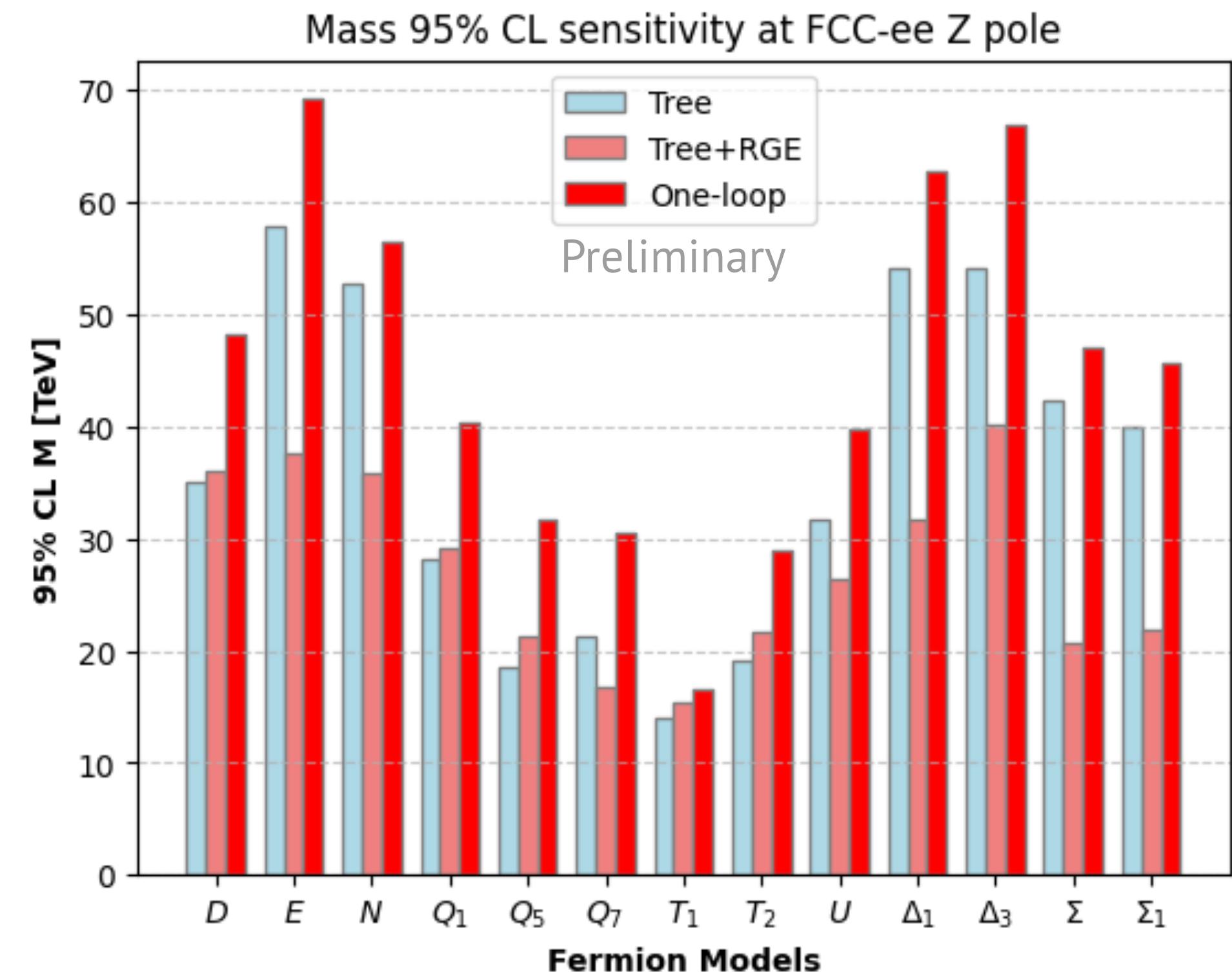
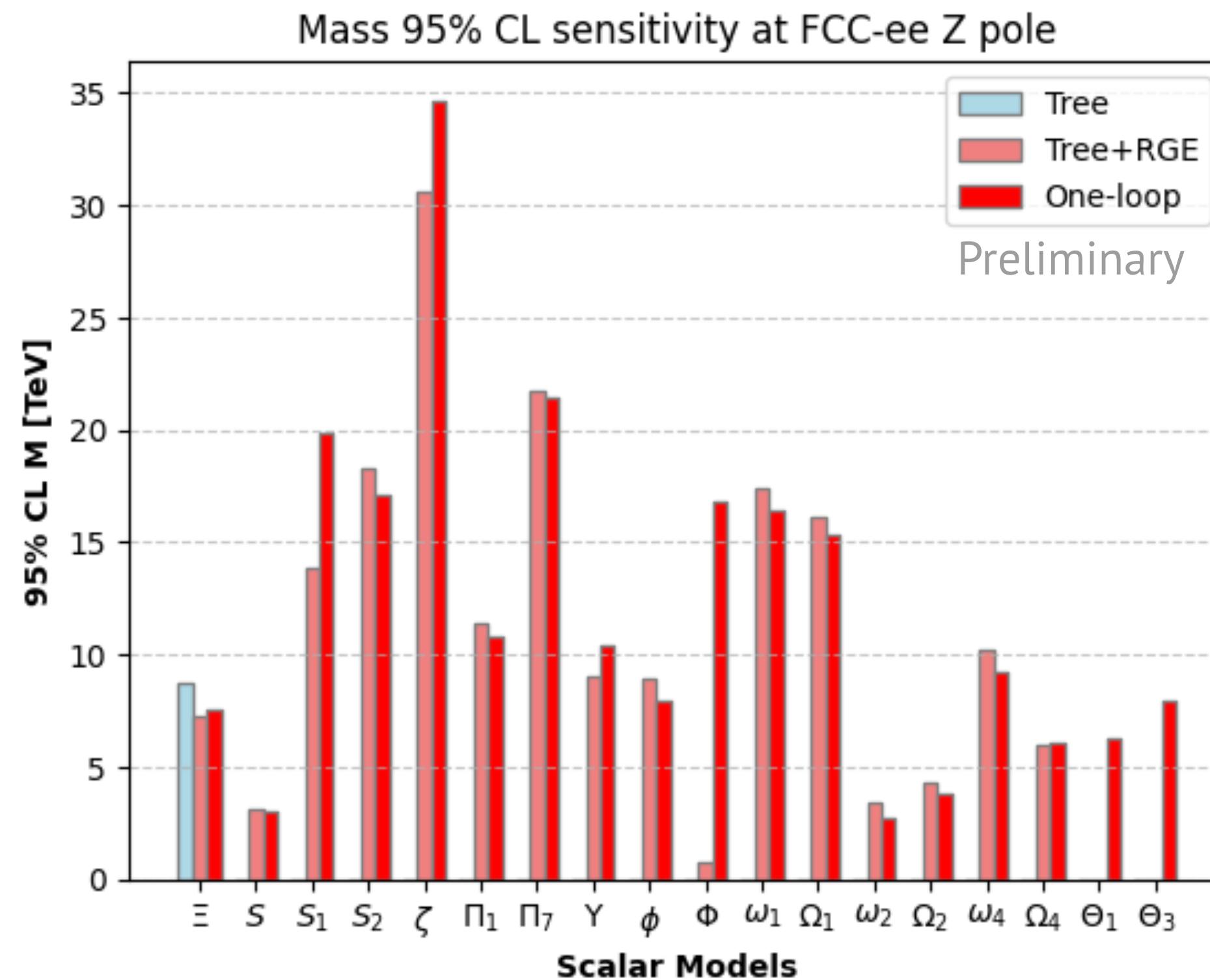
UV models and matching data from MME and MatchMakerParser



Projected bounds on linear SM extensions at one loop

Tera-Z sensitivity to linear SM extensions

FCC-ee sensitivities:
arXiv:2203.06520 (Snowmass 2021)



Conclusions and outlook

- The linear SM extensions are a useful framework for thinking about UV physics
- Computational tools are essential for the publishing and querying of UV/IR dictionaries going forward
- We use MatchMakerEFT and our MatchMakerParser to present our UV/IR dictionary for the linear SM extensions at one loop
- Our results strengthen the case for the potential of a Tera-Z run to constrain a wide range of new-physics models

$$\mathcal{O}_{HG} = H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{HB} = H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D^\mu D_\mu)$$

Merci beaucoup!

$$\mathcal{O}_{ll} = (\bar{l}_p \gamma_\mu l_q)$$

$$\mathcal{O}_{lq}^{(1)} =$$

$$\mathcal{O}_{lq}^{(3)} =$$

$$\mathcal{O}_{HG} = H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{HB} = H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D^\mu D_\mu)$$

Backup

$$\mathcal{O}_{ll} = (\bar{l}_p \gamma_\mu l_q)$$

$$\mathcal{O}_{lq}^{(1)} =$$

$$\mathcal{O}_{lq}^{(3)}$$

Linear SM extensions are complicated

de Blas, Criado, Pérez-Victoria, Santiago arXiv:1711.10391
 MatchingTools: Criado arXiv:1710.06445

$$\begin{aligned} -\mathcal{L}_{\text{leptons}}^{(4)} = & (\lambda_N)_{ri} \bar{N}_{Rr} \tilde{\phi}^\dagger l_{Li} + (\lambda_E)_{ri} \bar{E}_{Rr} \phi^\dagger l_{Li} \\ & + (\lambda_{\Delta_1})_{ri} \bar{\Delta}_{1Lr} \phi e_{Ri} + (\lambda_{\Delta_3})_{ri} \bar{\Delta}_{3Lr} \tilde{\phi} e_{Ri} \\ & + \frac{1}{2} (\lambda_\Sigma)_{ri} \bar{\Sigma}_{Rr}^a \tilde{\phi}^\dagger \sigma^a l_{Li} + \frac{1}{2} (\lambda_{\Sigma_1})_{ri} \bar{\Sigma}_{1Rr}^a \phi^\dagger \sigma^a l_{Li} \\ & + (\lambda_{N\Delta_1})_{rs} \bar{N}_{Rr}^c \phi^\dagger \Delta_{1Rs} + (\lambda_{E\Delta_1})_{rs} \bar{E}_{Lr} \phi^\dagger \Delta_{1Rs} \\ & + (\lambda_{E\Delta_3})_{rs} \bar{E}_{Lr} \tilde{\phi}^\dagger \Delta_{3Rs} + \frac{1}{2} (\lambda_{\Sigma\Delta_1})_{rs} \bar{\Sigma}_{Rr}^{ca} \tilde{\phi}^\dagger \sigma^a \Delta_{1Rs} \end{aligned}$$

Exotic fermion interactions

$$-\mathcal{L}_S^{(5)} = \frac{1}{f} \left[(\tilde{k}_S^\phi)_r \mathcal{S}_r D_\mu \phi^\dagger D^\mu \phi + (\tilde{\lambda}_S)_r \mathcal{S}_r |\phi|^4 \right]$$

Dimension-5 scalar interactions

$$\begin{aligned} -\mathcal{L}_q^{(5)} = & (\tilde{k}_S^B)_r \mathcal{S}_r B_{\mu\nu} B^{\mu\nu} + (\tilde{k}_S^W)_r \mathcal{S}_r W_{\mu\nu}^a W^{a\mu\nu} + (\tilde{k}_S^G)_r \mathcal{S}_r G_{\mu\nu}^A G^{A\mu\nu} \\ & + (\tilde{k}_S^{\tilde{B}})_r \mathcal{S}_r B_{\mu\nu} \tilde{B}^{\mu\nu} + (\tilde{k}_S^{\tilde{W}})_r \mathcal{S}_r W_{\mu\nu}^a \tilde{W}^{a\mu\nu} + (\tilde{k}_S^{\tilde{G}})_r \mathcal{S}_r G_{\mu\nu}^A \tilde{G}^{A\mu\nu} \\ & + \{ (\tilde{y}_S^e)_{rij} \mathcal{S}_r \bar{e}_{Ri} \phi^\dagger l_{Lj} + (\tilde{y}_S^d)_{rij} \mathcal{S}_r \bar{d}_{Ri} \phi^\dagger q_{Lj} + (\tilde{y}_S^u)_{rij} \mathcal{S}_r \bar{u}_{Ri} \} \\ & + (\tilde{k}_\Xi^{\phi})_r \Xi_r^a D_\mu \phi^\dagger \sigma^a D^\mu \phi + (\tilde{\lambda}_\Xi)_r \Xi_r^a |\phi|^2 \phi^\dagger \sigma^a \phi \\ & + (\tilde{k}_\Xi^{WB})_r \Xi_r^a W_{\mu\nu}^a B^{\mu\nu} + (\tilde{k}_\Xi^{W\tilde{B}})_r \Xi_r^a W_{\mu\nu}^a \tilde{B}^{\mu\nu} \\ & + \{ (\tilde{y}_\Xi^e)_{rij} \Xi_r^a \bar{e}_{Ri} \phi^\dagger \sigma^a l_{Lj} + (\tilde{y}_\Xi^d)_{rij} \Xi_r^a \bar{d}_{Ri} \phi^\dagger \sigma^a q_{Lj} + (\tilde{y}_\Xi^u)_{rij} \Xi_r^a \bar{u}_{Ri} \} \\ & + \{ (\tilde{k}_{\Xi_1})_r \Xi_{1r}^{a\dagger} D_\mu \tilde{\phi}^\dagger \sigma^a D^\mu \phi + (\tilde{\lambda}_{\Xi_1})_r \Xi_{1r}^{a\dagger} |\phi|^2 \tilde{\phi}^\dagger \sigma^a \phi + (\tilde{y}_{\Xi_1}^e)_r \} \\ & + (\tilde{y}_{\Xi_1}^d)_{rij} \Xi_{1r}^{a\dagger} \bar{d}_{Ri} \tilde{\phi}^\dagger \sigma^a q_{Lj} + (\tilde{y}_{\Xi_1}^u)_{rij} \Xi_{1r}^{a\dagger} \bar{q}_{Li} \sigma^a \phi u_{Rj} + \text{h.c.} \end{aligned}$$

- Lagrangian contains terms up to dimension 5 **sufficient to generate dimension-6 operators at tree level**
- Also includes “mixed” terms with multiple exotic multiplets

$$\begin{aligned} -\mathcal{L}_{SV} = & (\delta_{BS})_{rs} \mathcal{B}_{r\mu} D^\mu \mathcal{S}_s + (\delta_{W\Xi})_{rs} \mathcal{W}_{r,\mu} D^\mu \Xi_s \\ & + \{ (\delta_{\mathcal{L}^1\varphi})_{rs} \mathcal{L}_{1r\mu}^{1\dagger} D^\mu \varphi_s + (\delta_{\mathcal{W}^1\Xi_1})_{rs} \mathcal{W}_{1r\mu}^{1\dagger} D^\mu \Xi_{1s} + \text{h.c.} \} \\ & + (\varepsilon_{S\mathcal{L}_1})_{rst} \mathcal{S}_r \mathcal{L}_{1s\mu}^\dagger \mathcal{L}_{1t}^\mu + (\varepsilon_{\Xi\mathcal{L}_1})_{rst} \Xi_r^a \mathcal{L}_{1s\mu}^\dagger \sigma^a \mathcal{L}_{1t}^\mu \\ & + \{ (\varepsilon_{\Xi_1\mathcal{L}_1})_{rst} \Xi_{1i}^a \mathcal{L}_{1s\mu}^\dagger \sigma^a \tilde{\mathcal{L}}_{1t}^\mu + \text{h.c.} \} \\ & + \{ (g_{S\mathcal{L}_1})_{rs} \phi^\dagger (D_\mu \mathcal{S}_r) \mathcal{L}_{1s}^\mu + (g'_{S\mathcal{L}_1})_{rs} (D_\mu \phi)^\dagger \mathcal{S}_r \mathcal{L}_{1s}^\mu \} \\ & + (g_{\Xi\mathcal{L}_1})_{rs} \phi^\dagger \sigma^a (D_\mu \Xi_r^a) \mathcal{L}_{1s}^\mu + (g'_{\Xi\mathcal{L}_1})_{rs} (D_\mu \phi)^\dagger \sigma^a \Xi_r^a \mathcal{L}_{1s}^\mu \\ & + (g_{\Xi_1\mathcal{L}_1})_{rs} \tilde{\phi}^\dagger \sigma^a (D_\mu \Xi_{1r}^a)^\dagger \mathcal{L}_{1s}^\mu + (g'_{\Xi_1\mathcal{L}_1})_{rs} (D_\mu \tilde{\phi})^\dagger \sigma^a \Xi_{1r}^{a\dagger} \mathcal{L}_{1s}^\mu + \text{h.c.} \} , \end{aligned}$$

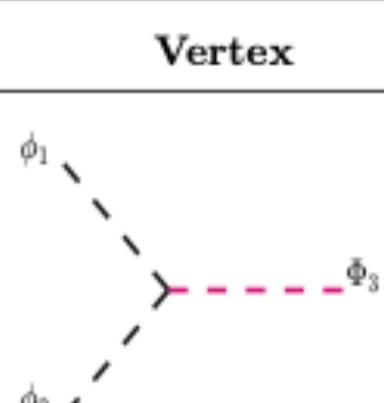
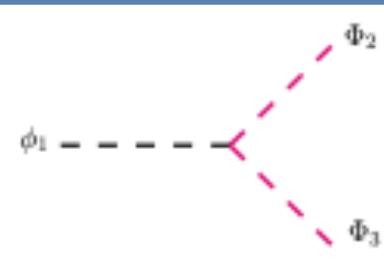
7 pages...

Lagrangian

- Similar assumptions to tree-level dictionary: limit ourselves to scalars and vector-like and Majorana fermions.
- Our Lagrangian matches the conventions of the tree-level dictionary**
- We don't consider mixed terms
 - For one-loop matching, only need to alter scalar interactions

$$\begin{aligned} \Delta\mathcal{L} = & \sum_S \hat{\lambda}_S (H^\dagger H)(S^\dagger S) + \hat{\lambda}'_\varphi (H^\dagger \varphi)(\varphi^\dagger H) + \sum_{i \in \{1, 3\}} \hat{\lambda}'_{\Theta_i} (\Theta_i^\dagger T_4^a \Theta_i)(H^\dagger \sigma^a H) \\ & + \sum_{i \in \{1, 7\}} \hat{\lambda}'_{\Pi_i} (\Pi_i^\dagger H)(H^\dagger \Pi_i) + \hat{\lambda}'_\Phi \text{Tr}[(\Phi^\dagger \cdot \lambda H)(H^\dagger \Phi \cdot \lambda)] \\ & + \sum_{S \in \{\zeta, Y\}} \hat{\lambda}' f_{abc} (S^{a\dagger} S^b)(H^\dagger \sigma^c H) \\ & + \left\{ \hat{\lambda}''_{\Theta_1} \frac{8}{3\sqrt{5}} (\Theta_1^I \epsilon_{IJ} [T_4^a]_K^K \Theta_1^K)(H^\dagger \sigma^a \tilde{H}) + \hat{\lambda}''_\Phi \text{Tr}[(H^\dagger \Phi \cdot \lambda)(H^\dagger \Phi \cdot \lambda)] + \text{h.c.} \right\} \end{aligned}$$

Bakshi, Chakrabortty, Prakash, Rahaman, Spannowsky
arXiv:2103.11593

Vertex	S. No.	Light fields	Heavy field(s)
	V1-(i)	$\phi_1 = \phi_2 = H_{(1,2,\frac{1}{2})} \text{ or } H_{(1,2,-\frac{1}{2})}^\dagger$	$\Phi_3 \in \{(1,3,\pm 1), (1,1,\pm 1)\}$
	V1-(ii)	$\phi_1 = H, \phi_2 = H^\dagger$	$\Phi_3 \in \{(1,3,0), (1,1,0)\}$
	V2	$\phi_1 = H \text{ or } H^\dagger$	$\Phi_2 \in (R_{C_2}, R_{L_2}, Y_2), \Phi_3 \in (R_{C_3}, R_{L_3}, Y_3)$ with $R_{C_2} \otimes R_{C_3} \equiv 1, R_{L_2} \otimes R_{L_3} \equiv 2$ and $Y_2 + Y_3 = \pm \frac{1}{2}$.
	V3-(i)	$\phi_1 = \phi_2 = \phi_3 = H \text{ or } H^\dagger$	$\Phi_4 \in \{(1,4,\pm \frac{3}{2}), (1,2,\pm \frac{3}{2})\}$
	V3-(ii)	$\phi_1 = \phi_2 = H, \phi_3 = H^\dagger$	$\Phi_4 \in \{(1,4,\pm \frac{1}{2}), (1,2,\pm \frac{1}{2})\}$
	V4-(i)	$\phi_1 = H, \phi_2 = H^\dagger$	$\Phi_3 \in (\{1, R_C\}, \{1, R_L\}, \{0, Y\}), \Phi_4 = \Phi_3^\dagger$ $\Phi_3 \in (R_{C_3}, R_{L_3}, Y_3), \Phi_4 \in (R_{C_4}, R_{L_4}, Y_4)$
	V4-(ii)	$\phi_1 = \phi_2 = H \text{ or } H^\dagger$	with $R_{C_3} \otimes R_{C_4} \equiv 1, R_{L_3} \otimes R_{L_4} \equiv 1 \text{ or } 3$ and $Y_3 + Y_4 = \pm 1$.

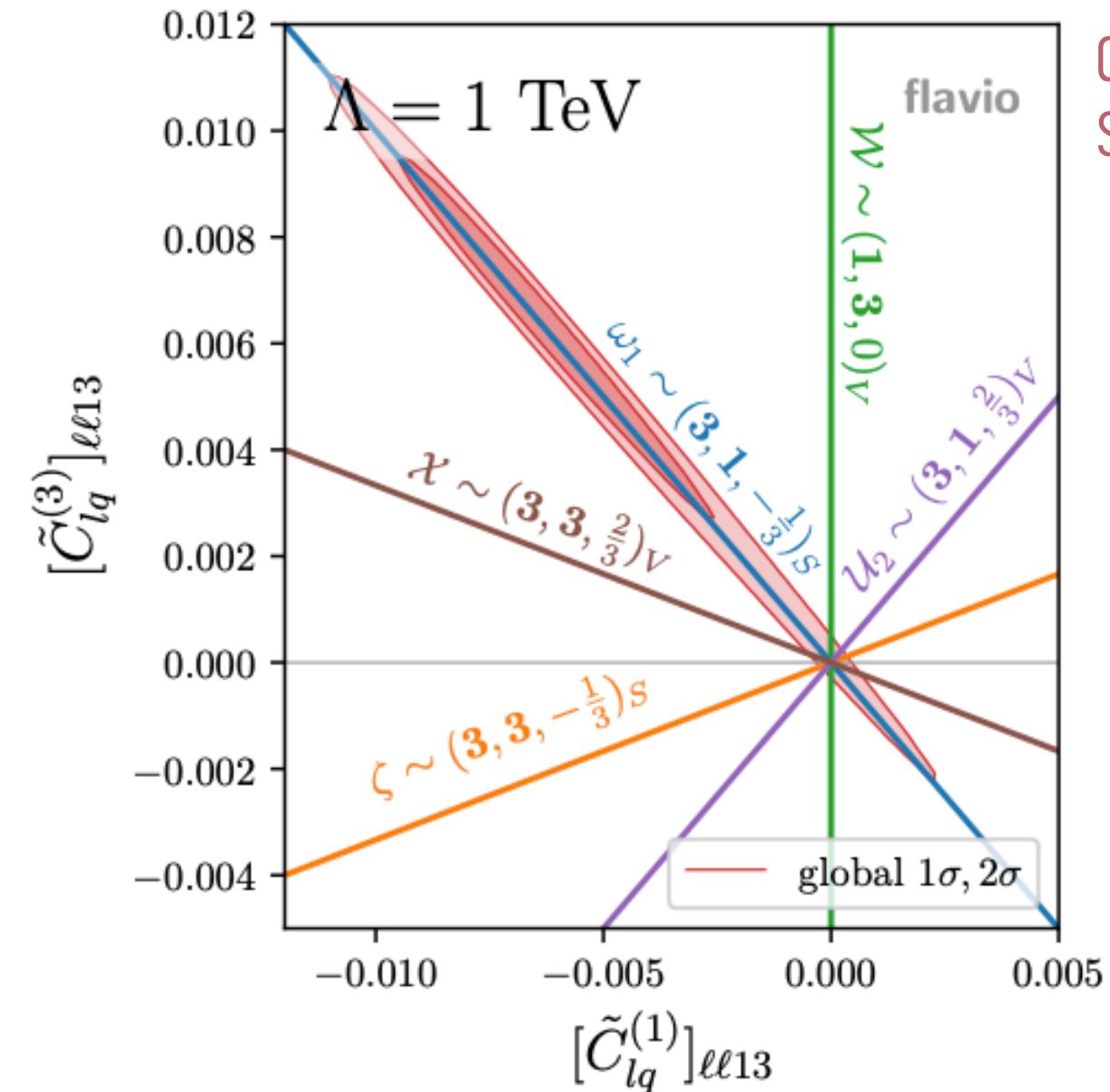
Linear SM extensions are useful

- Linear SM extensions are a physically motivated subset of toy models

Herrero-Garcia, Schmidt arXiv:1903.10552

- Can be used to organise complex UV models

- Can motivate directions in the space of WCs



Greljo, Salko, Smolkovic,
Stangl arXiv:2306.09401

Study of tension in
exclusive V_{ub}
extraction

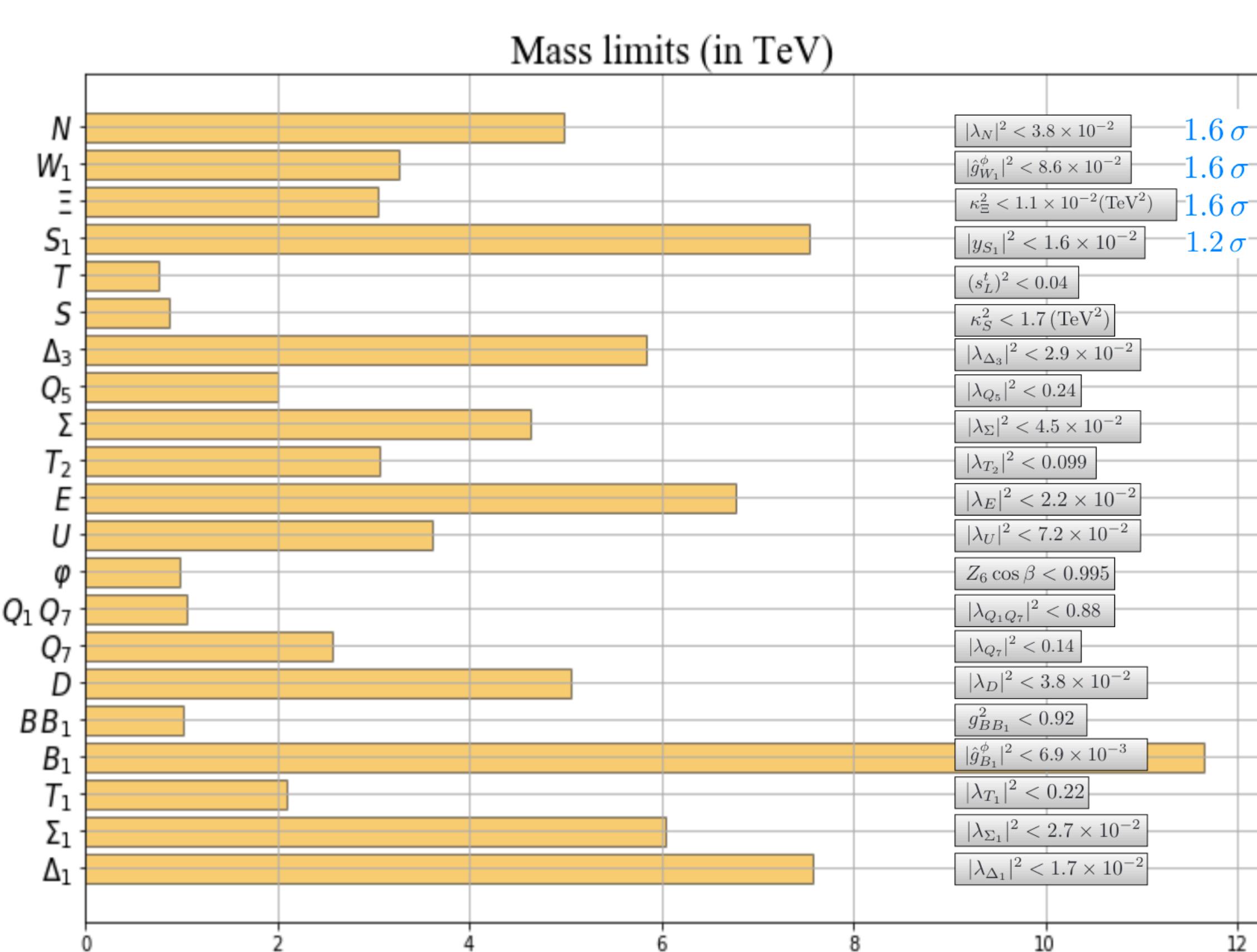
Model	C_{HD}	C_{ll}	C_{Hl}^3	C_{Hl}^1	C_{He}	$C_{H\square}$	$C_{\tau H}$	C_{tH}	C_{bH}
S							$-\frac{1}{2}$		
S_1		1							
Σ			$\frac{1}{16}$	$\frac{3}{16}$			$\frac{y_\tau}{4}$		
Σ_1			$-\frac{1}{16}$	$-\frac{3}{16}$			$\frac{y_\tau}{8}$		
N			$-\frac{1}{4}$	$\frac{1}{4}$					
E			$-\frac{1}{4}$	$-\frac{1}{4}$			$\frac{y_\tau}{2}$		
Δ_1						$\frac{1}{2}$	$\frac{y_\tau}{2}$		
Δ_3						$-\frac{1}{2}$	$\frac{y_\tau}{2}$		
B_1	1						$-\frac{1}{2}$	$-\frac{y_\tau}{2}$	$-\frac{y_t}{2}$
Ξ	-2						$\frac{1}{2}$	y_τ	y_t
W_1	$-\frac{1}{4}$						$-\frac{1}{8}$	$-\frac{y_\tau}{8}$	$-\frac{y_t}{8}$
φ							$-y_\tau$	$-y_t$	$-y_b$
$\{B, B_1\}$							$-\frac{3}{2}$	$-y_\tau$	$-y_t$
$\{Q_1, Q_7\}$									y_t

Model	C_{Hq}^3	C_{Hq}^1	$(C_{Hq}^3)_{33}$	$(C_{Hq}^1)_{33}$	C_{Hu}	C_{Hd}	C_{tH}	C_{bH}
U	$-\frac{1}{4}$	$\frac{1}{4}$	$-\frac{1}{4}$	$\frac{1}{4}$			$\frac{y_t}{2}$	
D	$-\frac{1}{4}$	$-\frac{1}{4}$	$-\frac{1}{4}$	$-\frac{1}{4}$				$\frac{y_b}{2}$
Q_5						$-\frac{1}{2}$		$\frac{y_b}{2}$
Q_7						$\frac{1}{2}$		$\frac{y_t}{2}$
T_1	$-\frac{1}{16}$	$-\frac{3}{16}$	$-\frac{1}{16}$	$-\frac{3}{16}$			$\frac{y_t}{4}$	$\frac{y_b}{8}$
T_2	$-\frac{1}{16}$	$\frac{3}{16}$	$-\frac{1}{16}$	$\frac{3}{16}$			$\frac{y_t}{8}$	$\frac{y_b}{4}$
T			$-\frac{1}{2} \frac{M_T^2}{v^2}$	$\frac{1}{2} \frac{M_T^2}{v^2}$			$y_t \frac{M_T^2}{v^2}$	

Ellis, Madigan, Mimasu, Sanz, You arXiv:2012.02779

FitMaker group: Fit to top, Higgs, diboson and EW data

Linear SM extensions are useful



Model	C_{HD}	C_{ll}	C_{Hl}^3	C_{Hl}^1	C_{He}	$C_{H\square}$	$C_{\tau H}$	C_{tH}	C_{bH}
S							$-\frac{1}{2}$		
S_1		1							
Σ			$\frac{1}{16}$	$\frac{3}{16}$			y_τ		
Σ_1			$-\frac{1}{16}$	$-\frac{3}{16}$			y_τ		
N			$-\frac{1}{4}$	$\frac{1}{4}$					
E			$-\frac{1}{4}$	$-\frac{1}{4}$			y_τ		
Δ_1						$\frac{1}{2}$	y_τ		
Δ_3						$-\frac{1}{2}$	y_τ		
B_1	1						$-\frac{1}{2}$	$-\frac{y_\tau}{2}$	$-\frac{y_t}{2}$
Ξ	-2						$\frac{1}{2}$	y_τ	y_t
W_1	$-\frac{1}{4}$						$-\frac{1}{8}$	$-\frac{y_\tau}{8}$	$-\frac{y_t}{8}$
φ							$-y_\tau$	$-y_t$	$-y_b$
$\{B, B_1\}$							$-\frac{3}{2}$	$-y_\tau$	$-y_t$
$\{Q_1, Q_7\}$									y_t

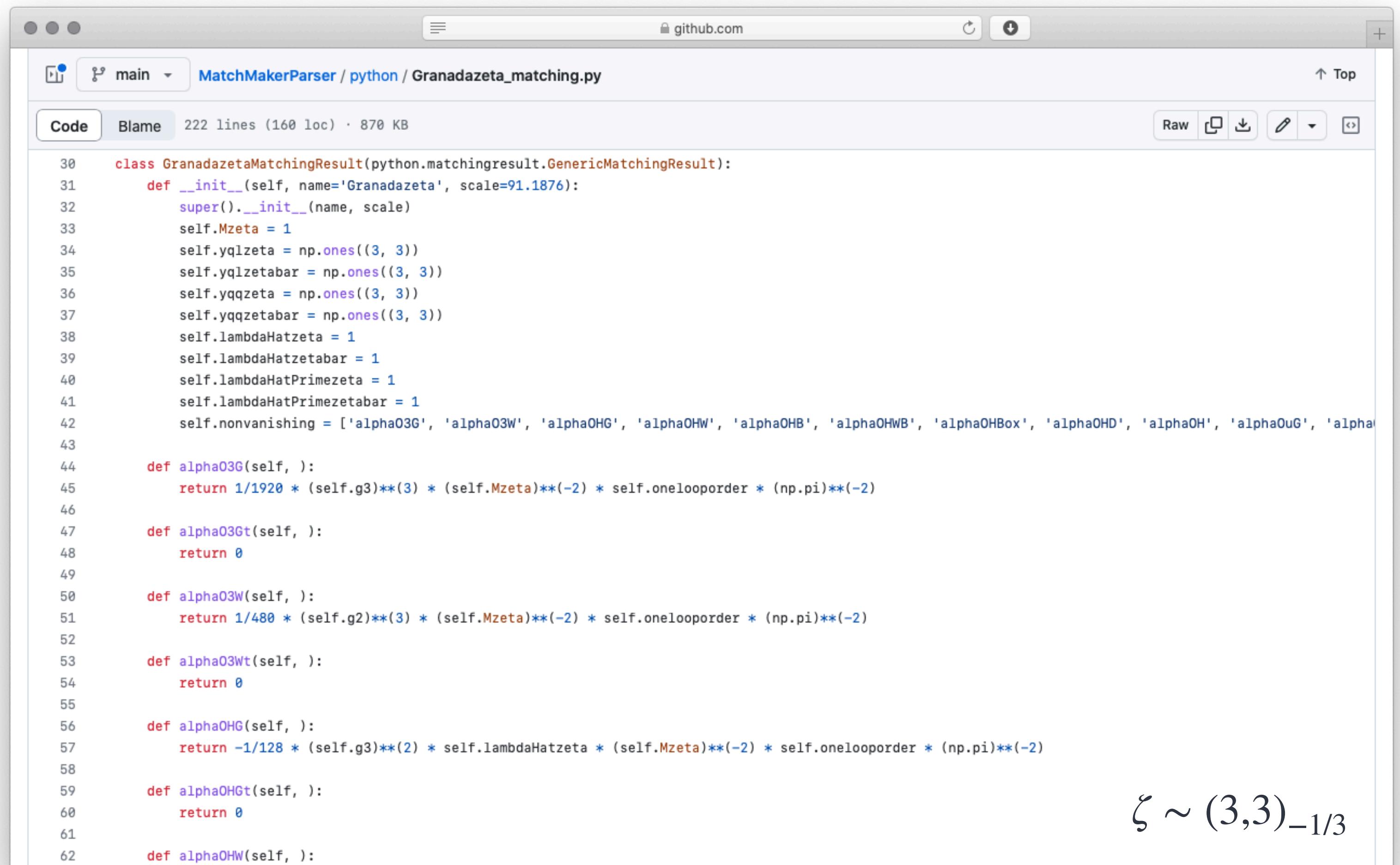
Model	C_{Hq}^3	C_{Hq}^1	$(C_{Hq}^3)_{33}$	$(C_{Hq}^1)_{33}$	C_{Hu}	C_{Hd}	C_{tH}	C_{bH}
U	$-\frac{1}{4}$	$\frac{1}{4}$	$-\frac{1}{4}$	$\frac{1}{4}$			$\frac{y_t}{2}$	
D	$-\frac{1}{4}$	$-\frac{1}{4}$	$-\frac{1}{4}$	$-\frac{1}{4}$				$\frac{y_b}{2}$
Q_5							$-\frac{1}{2}$	$\frac{y_b}{2}$
Q_7						$\frac{1}{2}$		$\frac{y_t}{2}$
T_1	$-\frac{1}{16}$	$-\frac{3}{16}$	$-\frac{1}{16}$	$-\frac{3}{16}$			$\frac{y_t}{4}$	$\frac{y_b}{8}$
T_2	$-\frac{1}{16}$	$\frac{3}{16}$	$-\frac{1}{16}$	$\frac{3}{16}$			$\frac{y_t}{8}$	$\frac{y_b}{4}$
T			$-\frac{1}{2} \frac{M_T^2}{v^2}$	$\frac{1}{2} \frac{M_T^2}{v^2}$			$y_t \frac{M_T^2}{v^2}$	

Ellis, Madigan, Mimasu, Sanz, You arXiv:2012.02779

FitMaker group: Fit to top, Higgs, diboson and EW data

Reading the Lagrangian and parsing the output: MatchMakerParser

- Written a lightweight wrapper around FeynRules to encode Lagrangians with less boilerplate code and more consistency checks
- A simple implementation of missing PythonForm to parse results from MatchMaker
- Outputs are Python classes with coefficients as methods.



```
30     class GranadazetaMatchingResult(python.matchingresult.GenericMatchingResult):
31         def __init__(self, name='Granadazeta', scale=91.1876):
32             super().__init__(name, scale)
33             self.Mzeta = 1
34             self.yqlzeta = np.ones((3, 3))
35             self.yqlzetabar = np.ones((3, 3))
36             self.yqqzeta = np.ones((3, 3))
37             self.yqqzetabar = np.ones((3, 3))
38             self.lambdahatzeta = 1
39             self.lambdahatzetabar = 1
40             self.lambdahatprimezeta = 1
41             self.lambdahatprimezetabar = 1
42             self.nonvanishing = ['alpha03G', 'alpha03W', 'alphaOHG', 'alphaOHW', 'alphaOHB', 'alphaOHWB', 'alphaOHBox', 'alphaOHD', 'alphaOH', 'alphaOuG', 'alphaOuH']
43
44         def alpha03G(self, ):
45             return 1/1920 * (self.g3)**(3) * (self.Mzeta)**(-2) * self.onelooporder * (np.pi)**(-2)
46
47         def alpha03Gt(self, ):
48             return 0
49
50         def alpha03W(self, ):
51             return 1/480 * (self.g2)**(3) * (self.Mzeta)**(-2) * self.onelooporder * (np.pi)**(-2)
52
53         def alpha03Wt(self, ):
54             return 0
55
56         def alphaOHG(self, ):
57             return -1/128 * (self.g3)**(2) * self.lambdahatzeta * (self.Mzeta)**(-2) * self.onelooporder * (np.pi)**(-2)
58
59         def alphaOHT(self, ):
60             return 0
61
62         def alphaOHW(self, ):  
 $\zeta \sim (3,3)_{-1/3}$ 
```

Reading the Lagrangian and parsing the

- Written a lightweight wrapper around FeynRules to encode Lagrangians with less boilerplate code and more consistency checks
- A simple implementation of missing PythonForm to parse results from MatchMaker
- Outputs are Python classes with coefficients as methods.

The screenshot shows a Jupyter Notebook cell with the following content:

```
In [10]: from python.Granadazeta_matching import GranadazetaMatchingResult
In [11]: zeta_matching = GranadazetaMatchingResult(scale=1e3)
In [12]: zeta_matching.alpha0HD()
Out[12]: -0.0063515302515737395
In [13]: 
```

Below the cell, a code editor window displays the `GranadazetaMatchingResult` class definition:

```
30  class GranadazetaMatchingResult:
31      def __init__(self, name='GranadaZeta'):
32          super().__init__(name, scale)
33          self.Mzeta = 1
34          self.yqlzeta = np.ones((3, 3))
35          self.yqlzetabar = np.ones((3, 3))
36          self.yqqzeta = np.ones((3, 3))
37          self.yqqzetabar = np.ones((3, 3))
38          self.lambdaHatzeta = 1
39          self.lambdaHatzetabar = 1
40          self.lambdaHatPrimezeta = 1
41          self.lambdaHatPrimezetabar = 1
42          self.nonvanishing = ['alpha03G', 'alpha03W', 'alpha0HG', 'alpha0HW', 'alpha0HB', 'alphaOHWB', 'alphaOHBox', 'alphaOHD', 'alphaOH', 'alphaOuG', 'alphaOHBoxBar']
43
44      def alpha03G(self, ):
45          return 1/1920 * (self.g3)**(3) * (self.Mzeta)**(-2) * self.onelooporder * (np.pi)**(-2)
46
47      def alpha03Gt(self, ):
48          return 0
49
50      def alpha03W(self, ):
51          return 1/480 * (self.g2)**(3) * (self.Mzeta)**(-2) * self.onelooporder * (np.pi)**(-2)
52
53      def alpha03Wt(self, ):
54          return 0
55
56      def alpha0HG(self, ):
57          return -1/128 * (self.g3)**(2) * self.lambdaHatzeta * (self.Mzeta)**(-2) * self.onelooporder * (np.pi)**(-2)
58
59      def alpha0Hgt(self, ):
60          return 0
61
62      def alpha0HW(self, ):
```

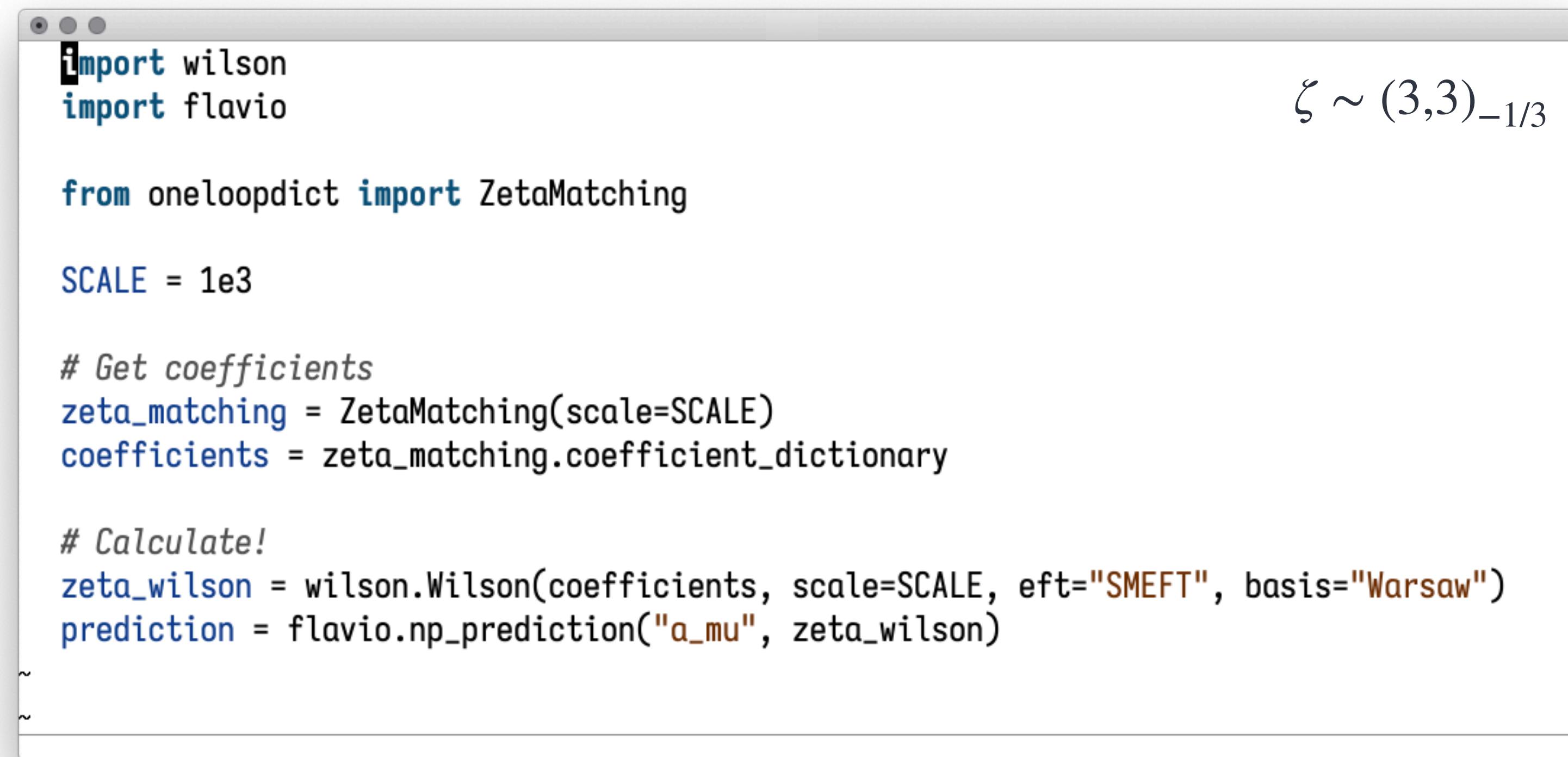
On the right side of the slide, there is a mathematical expression: $\zeta \sim (3,3)_{-1/3}$.

Connection to Python ecosystem

Wilson: Aebischer, Kumar, Straub arXiv:1804.05033
flavio: Straub arXiv:1810.08132

MatchingDB: Criado gitlab.com/jccriado/matchingdb

- Plans to put one-loop dictionary on PyPI for easy use with other tools
- Limited searching and querying ability, looking into other export options



The image shows a screenshot of a Jupyter Notebook cell. The code imports `wilson` and `flavio`, then uses `oneloopdict` to import `ZetaMatching`. It defines a scale of `1e3` and gets coefficients using `ZetaMatching`. It then calculates Wilson coefficients using `wilson.Wilson` and performs a prediction using `flavio.np_prediction` for the `"a_mu"` observable. To the right of the code, there is a mathematical expression: $\zeta \sim (3,3)_{-1/3}$.

```
import wilson
import flavio

from oneloopdict import ZetaMatching

SCALE = 1e3

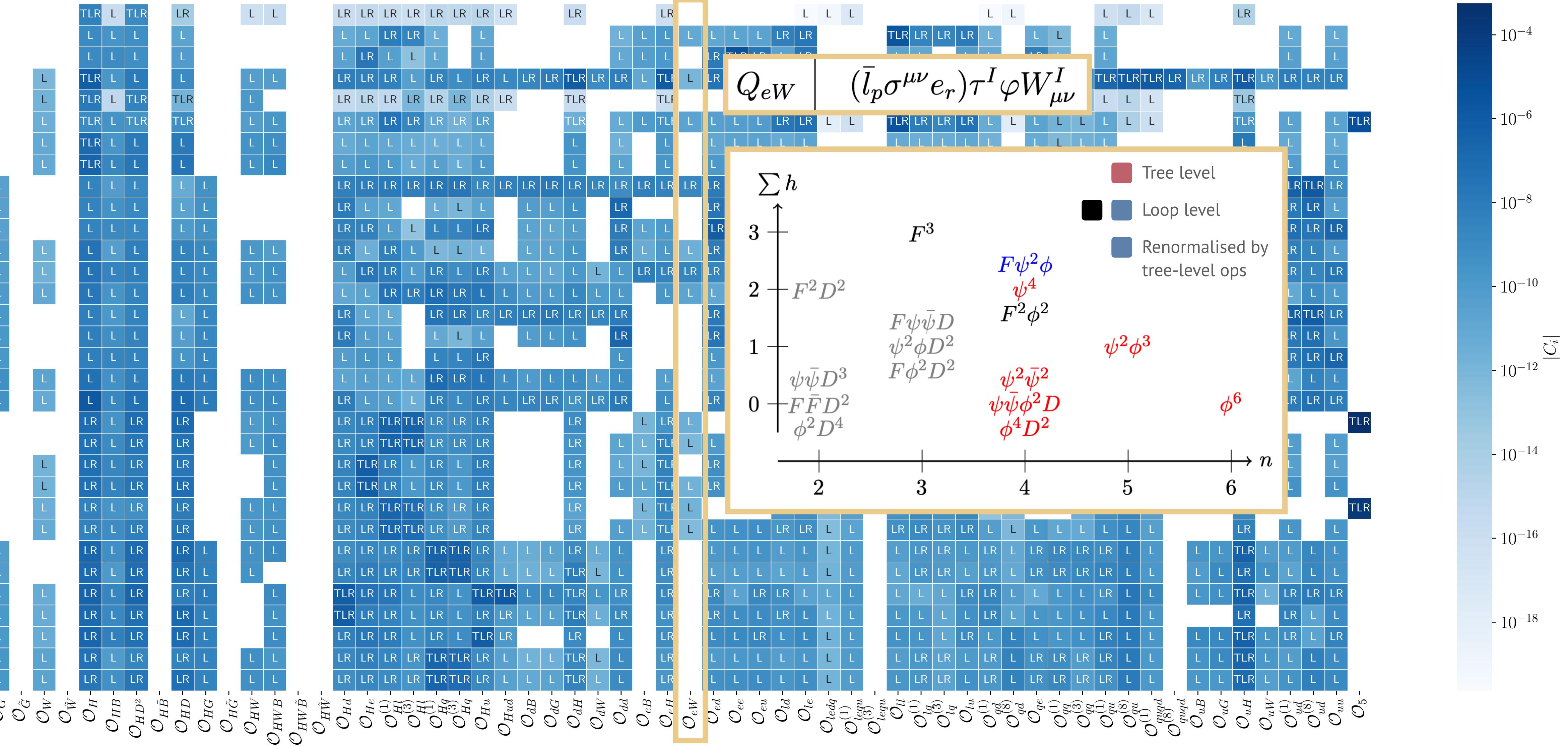
# Get coefficients
zeta_matching = ZetaMatching(scale=SCALE)
coefficients = zeta_matching.coefficient_dictionary

# Calculate!
zeta_wilson = wilson.Wilson(coefficients, scale=SCALE, eft="SMEFT", basis="Warsaw")
prediction = flavio.np_prediction("a_mu", zeta_wilson)

~
```

$$\zeta \sim (3,3)_{-1/3}$$

Operators of the form $F\psi^2\phi^2$ are renormalised by four-fermion operators



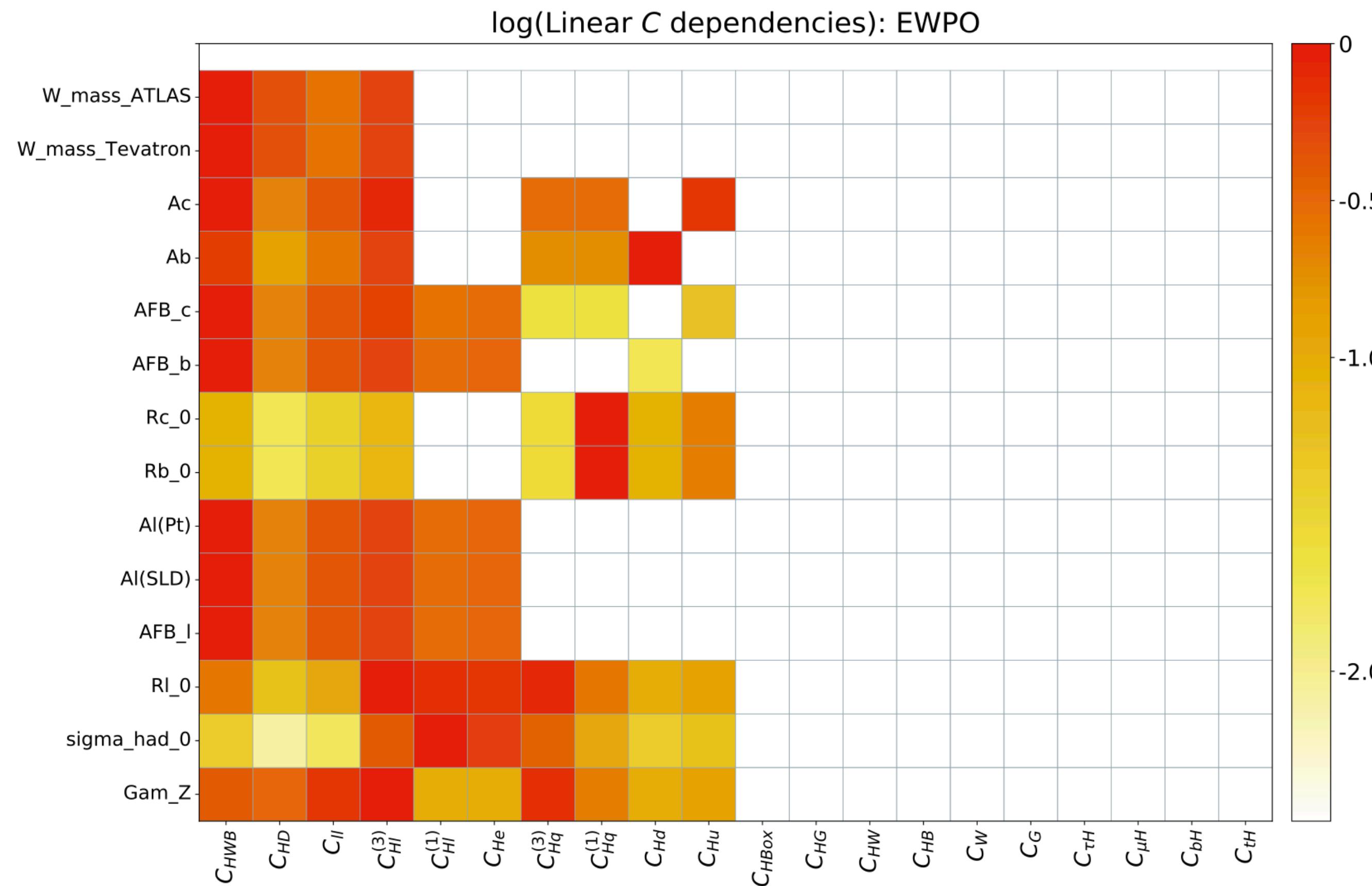
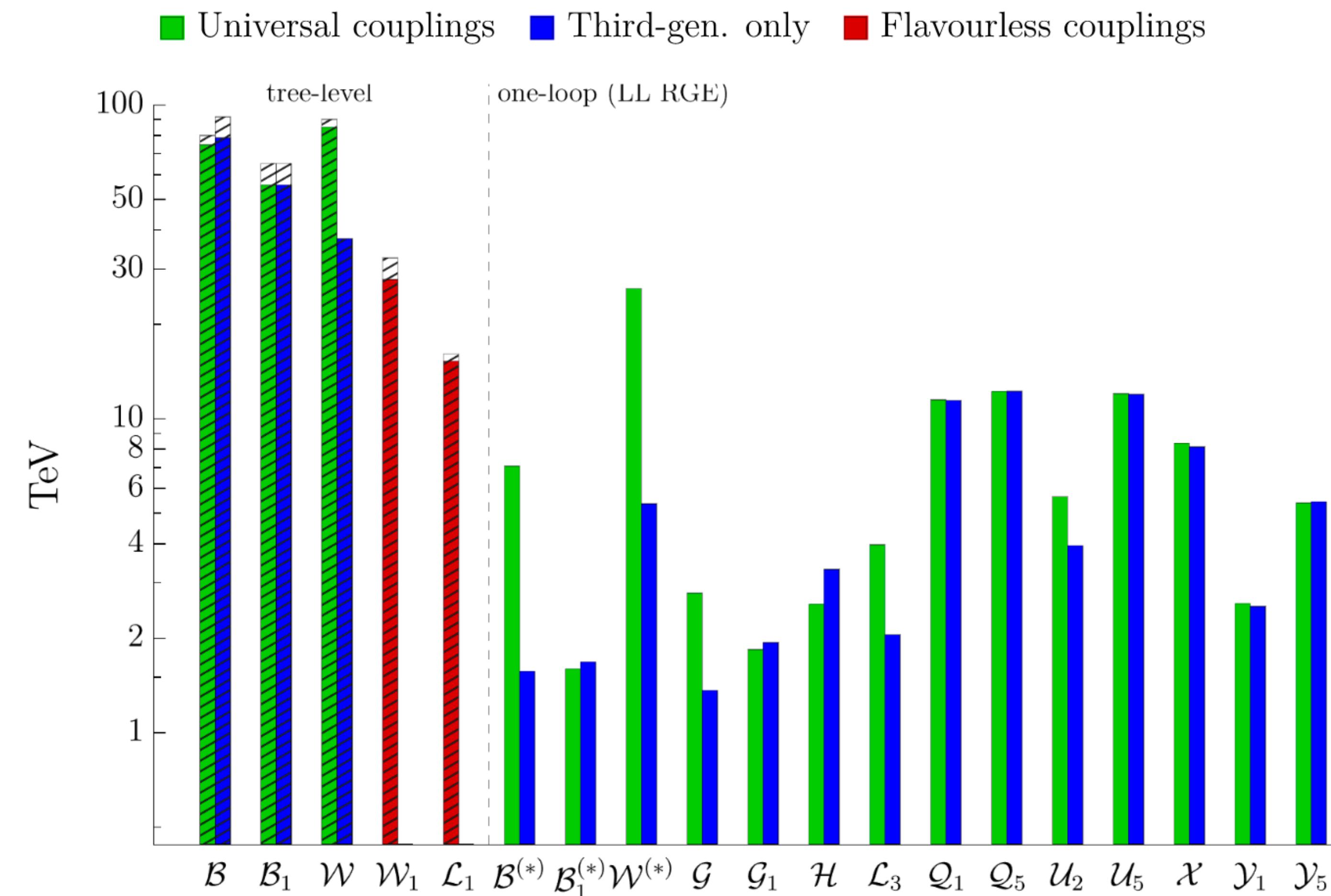


Fig. 7: Logarithm of normalised linear dependences for electroweak measurements. The entries are normalised by dividing each one by the largest operator dependence of a given measurement, a_i^X , such that the colour map depicts $\log(a_i^X / a_{max}^X)$.

Limits on vectors

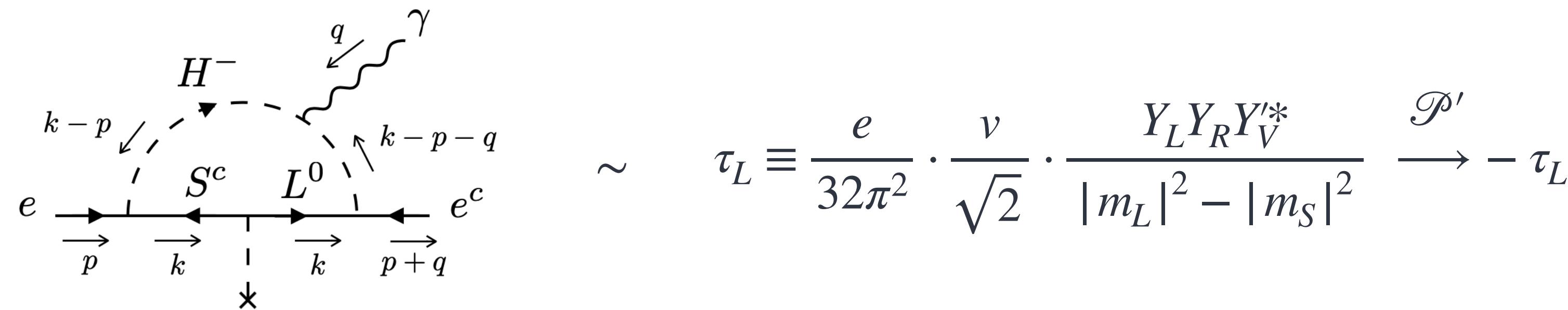


Investigation of *magic* zeros

Arkani-Hamed, Harigaya arXiv:2106.01373
 Craig, Garcia Garcia, Vainshtein, Zhang arXiv:2112.05770

- Magic zero: a quantity suppressed without an *apparent* symmetry explanation
- E.g. Vanishing dipole coefficient $H^\dagger \ell \sigma^{\mu\nu} e^c F_{\mu\nu}$ in model with two vector-like Dirac fermions: $S \sim (1,1)_0$ and $L \sim (1,2)_{1/2}$

$$\mathcal{L} \supset -m_L L^0 L^{c0} - m_S S S^c - \boxed{Y'_V H^0 L^0 S^c} + Y_L H^+ e S^c - Y_R H^- L^0 e^c + \text{h.c.}$$



- Generalised parity symmetry \mathcal{P}' : $L^0 \leftrightarrow S^{c\dagger}$, $L^{c0} \leftrightarrow S^\dagger$, $m_L \leftrightarrow m_S^*$, $Y'_V \leftrightarrow Y_V'^*$, $Y_L \leftrightarrow Y_R^*$
- But dipole operator even under parity!

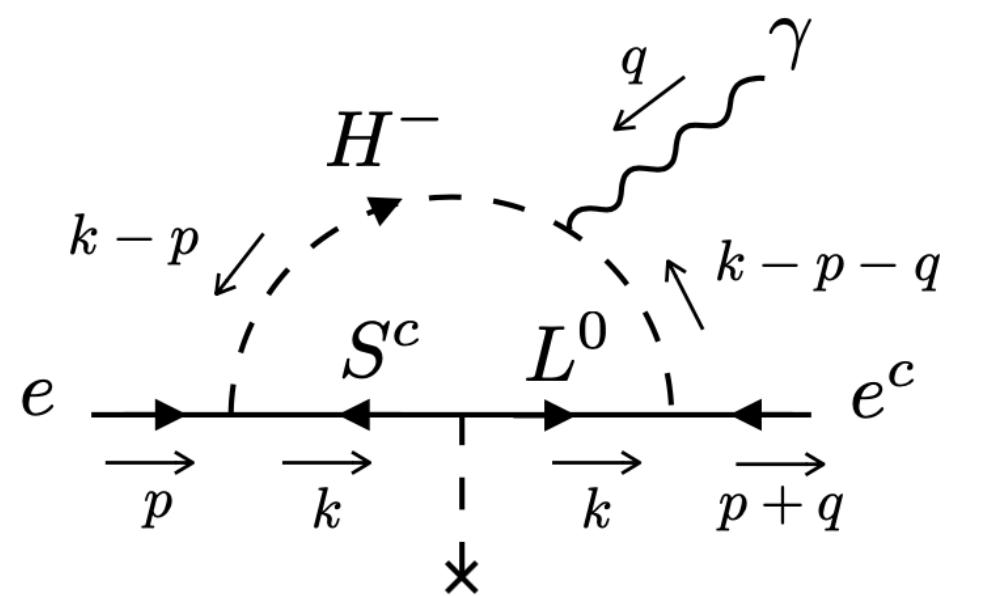
Investigation of *magic zeros*

Arkani-Hamed, Harigaya arXiv:2106.01373

Craig, Garcia Garcia, Vainshtein, Zhang arXiv:2112.05770

- Magic zero: a quantum number
- E.g. Vanishing dipole moment
 $L \sim (1,2)_{1/2}$

```
In[3]:= alpha0eB[1, 1] /. MatchingResult
Out[3]=  $\frac{1}{384 M\Delta_1^2 M N^2 \pi^2}$ 
g1 onelooporder (4 M N^2 lambdaDelta1[1]  $\times$  lambdaDelta1bar[mif3]  $\times$  yl[1, mif3] -
3 iCPV^2 M N^2 lambdaDelta1[1]  $\times$  lambdaDelta1bar[mif3]  $\times$  yl[1, mif3] +
M\Delta_1^2 lambdaN[mif3]  $\times$  lambdaNbar[1]  $\times$  yl[mif3, 1])
In[4]:= alpha0eB[1, 1] /. MatchingResult /. yl[x_, y_] :> 0
Out[4]= 0
```



$$\sim \tau_L \equiv \frac{e}{32\pi^2} \cdot \frac{v}{\sqrt{2}} \cdot \frac{Y_L Y_R Y_V^*}{|m_L|^2 - |m_S|^2} \xrightarrow{\mathcal{P}'} -\tau_L$$

- Generalised parity symmetry \mathcal{P}' : $L^0 \leftrightarrow S^{c\dagger}$, $L^{c0} \leftrightarrow S^\dagger$, $m_L \leftrightarrow m_S^*$, $Y'_V \leftrightarrow Y_V^*$, $Y_L \leftrightarrow Y_R^*$
- But dipole operator even under parity!