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HIDDe   
Hunting Invisibles: Dark sectors, Dark matter and Neutrinos



**ijc** Lab  
Irène Joliot-Curie  
Laboratoire de Physique  
des 2 Infinis

# Looking for new physics through the exclusive $b \rightarrow s\nu\nu$ modes

HEP Seminar @ IJCLab

Salvador Rosauero-Alcaraz, 19/03/2024

# Outline

- **Introduction**
- **$B \rightarrow K^{(*)}\nu\nu$  in the Standard Model**
  - Effective theory description
  - Sources of uncertainty
- **Belle-II results**
- **Implications for BSM physics**
  - LEFT
  - SMEFT
  - Light new physics
- **Summary and outlook**

# Introduction

## Flavor Physics

$$\mathcal{L}_{\text{Yukawa}} = -\bar{Q}Y_d H d_R - \bar{Q}Y_u \tilde{H} u_R - \bar{L}Y_\ell H e_R + \text{[redacted]} + h.c.$$

Most of the free parameters of the SM arise from  $\mathcal{L}_{\text{Yukawa}}$  and need to be extracted from experiment

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## Flavor Physics

Origin of neutrino masses?

$$\mathcal{L}_{\text{Yukawa}} = -\bar{Q}Y_d H d_R - \bar{Q}Y_u \tilde{H} u_R - \bar{L}Y_\ell H e_R + \bar{L}Y_\nu \tilde{H} N_R + \frac{1}{2}\bar{N}_R^c M N_R + h.c.$$

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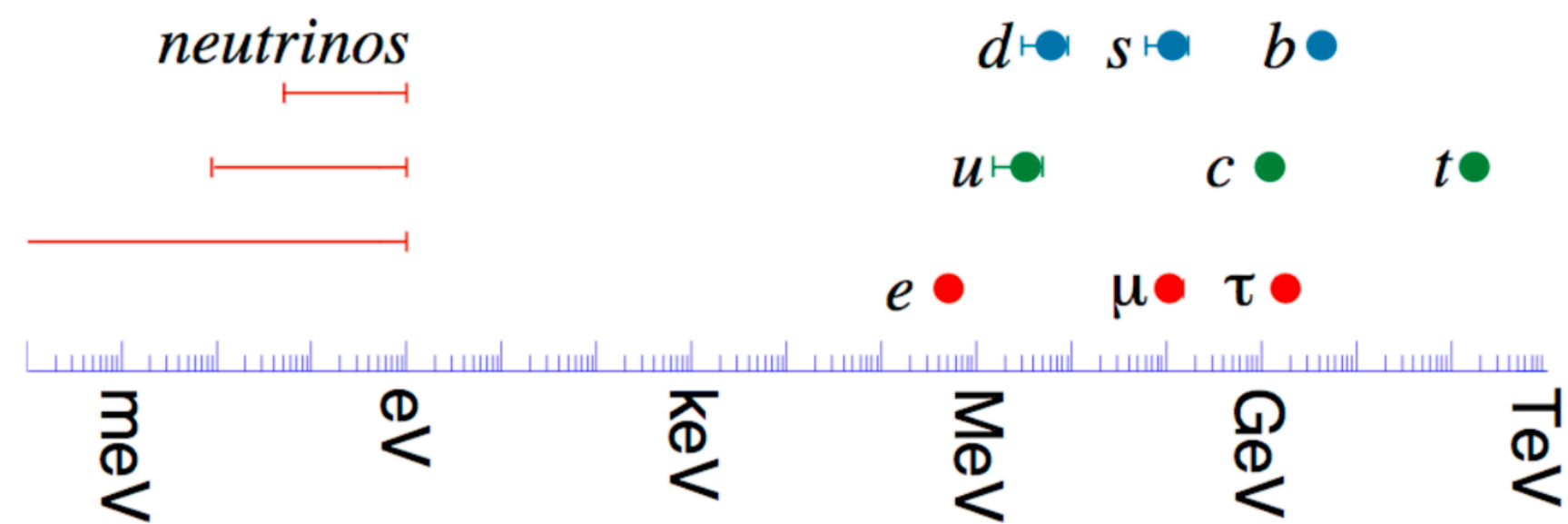
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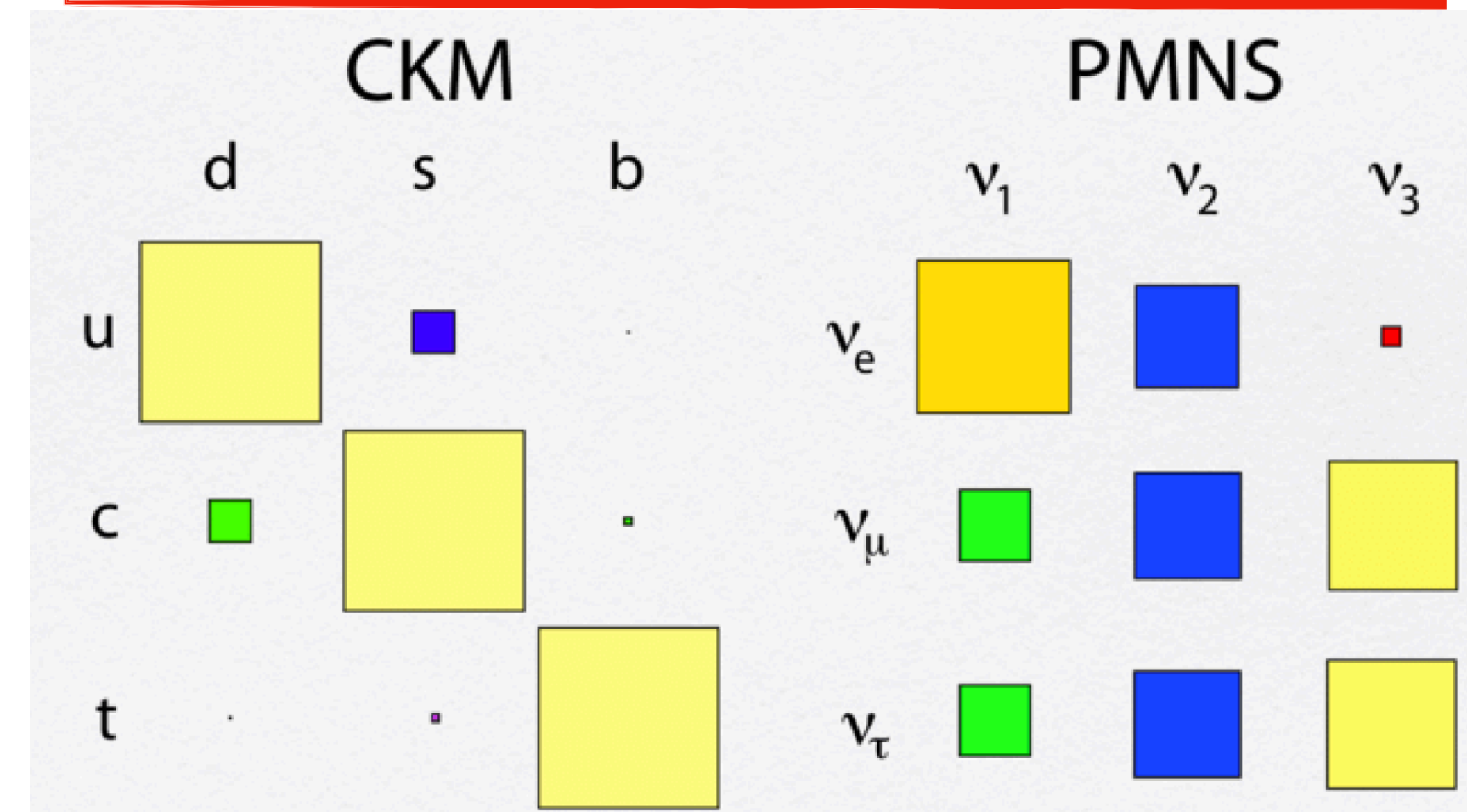
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Fermion masses span  $\sim 5$  orders of magnitude (not including  $m_\nu$ )



Why is the quark mixing so different from the leptonic one?



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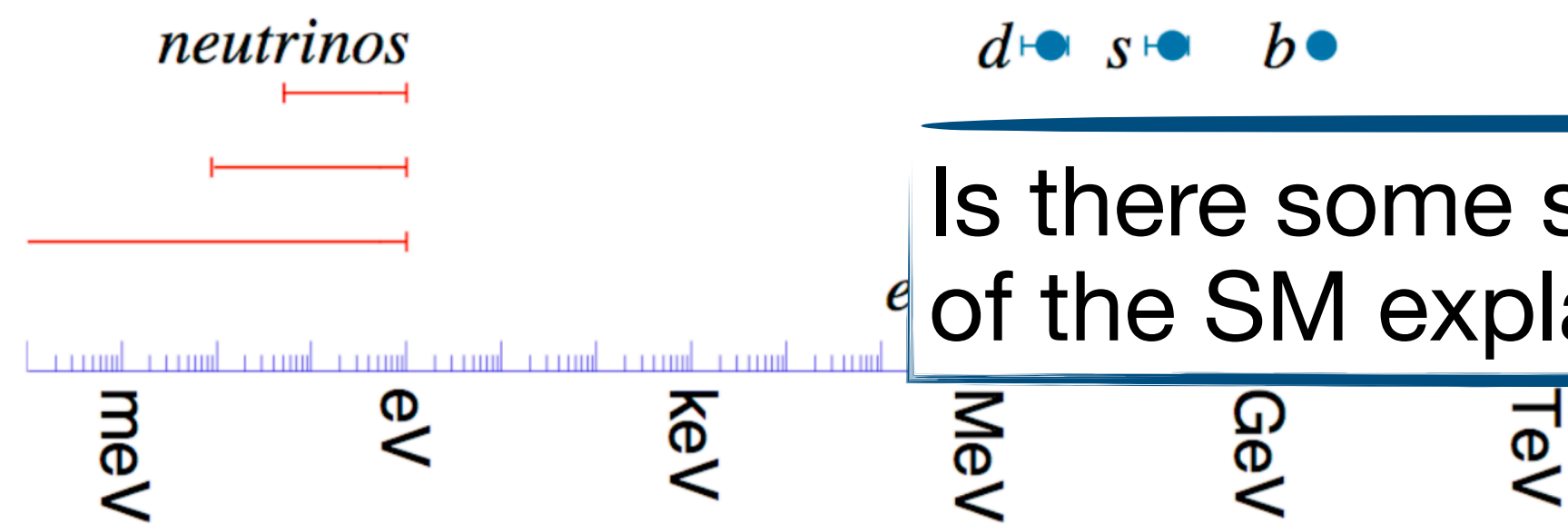
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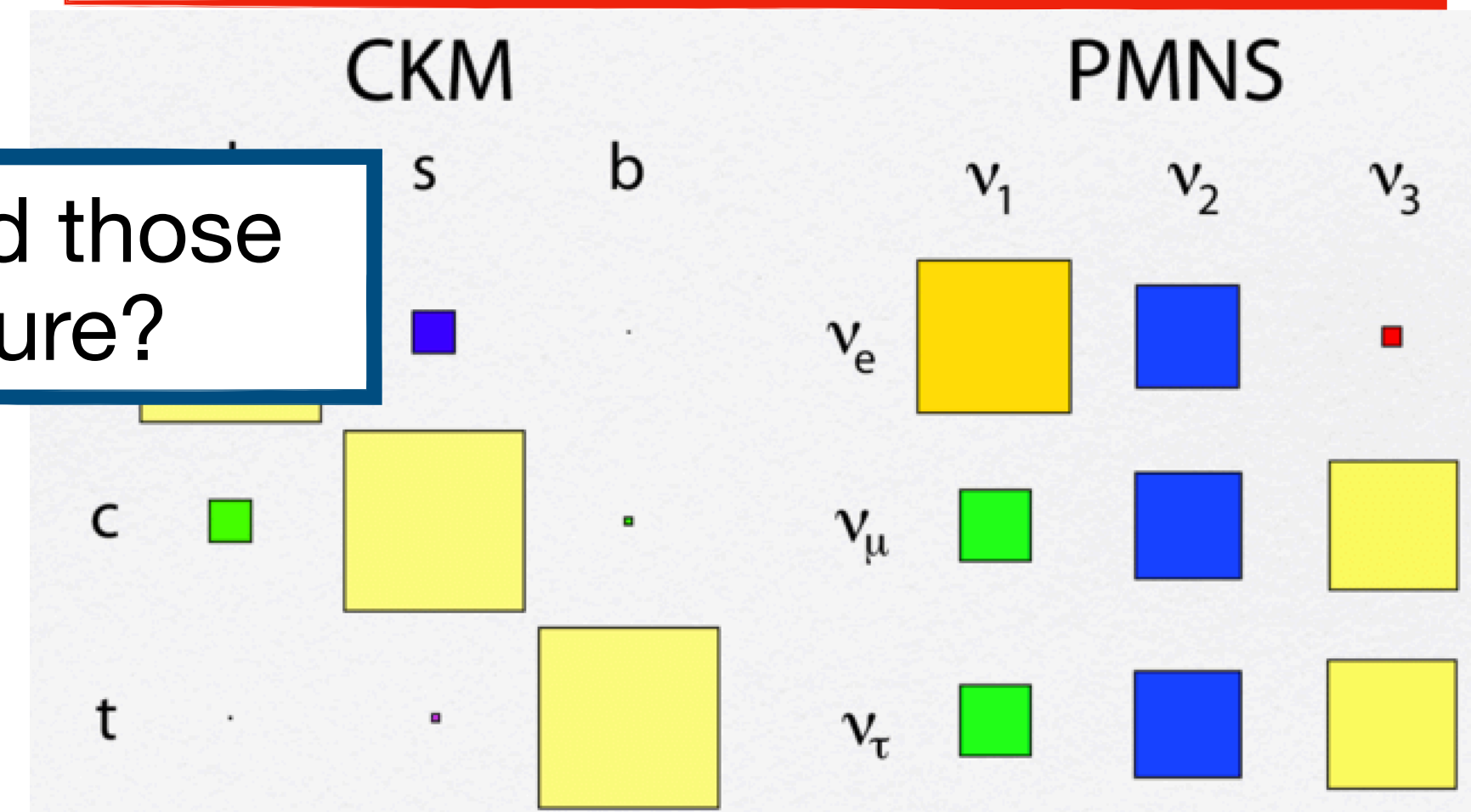
Most of the free parameters of the SM arise from  $\mathcal{L}_{\text{Yukawa}}$  and need to be extracted from experiment

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Is there some symmetry beyond those of the SM explaining this structure?

Why is the quark mixing so different from the leptonic one?



# Introduction

## Indirect searches for New Physics

We can look for rare/forbidden processes in the SM which would be sensitive to BSM physics effects

$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}} (1 + \delta_{\text{NP}})$$

Need to be very precise!

Deviation with respect to the SM prediction

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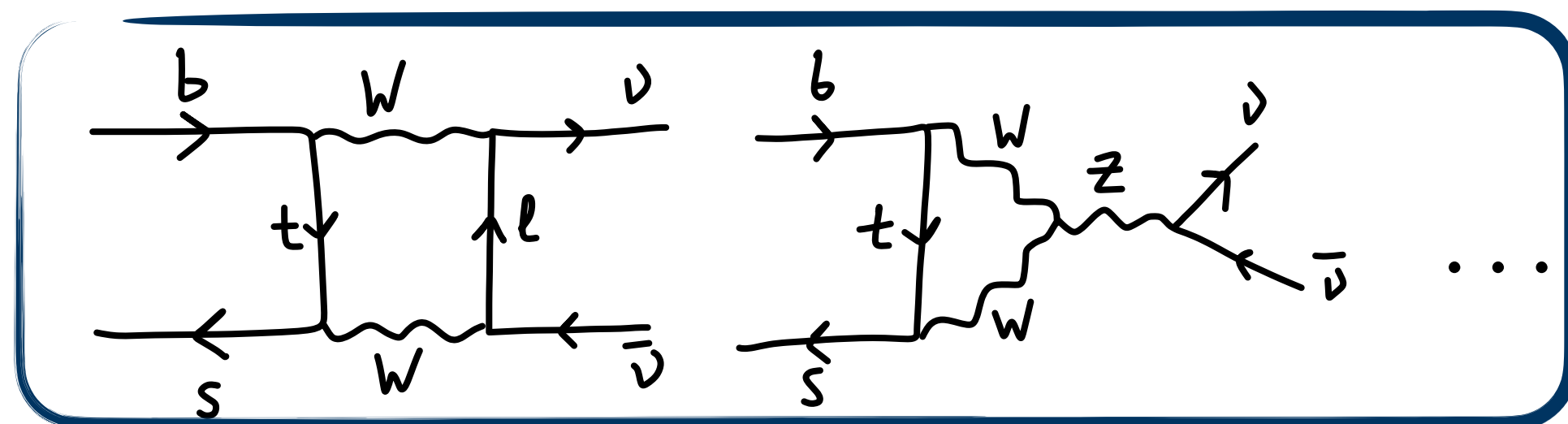
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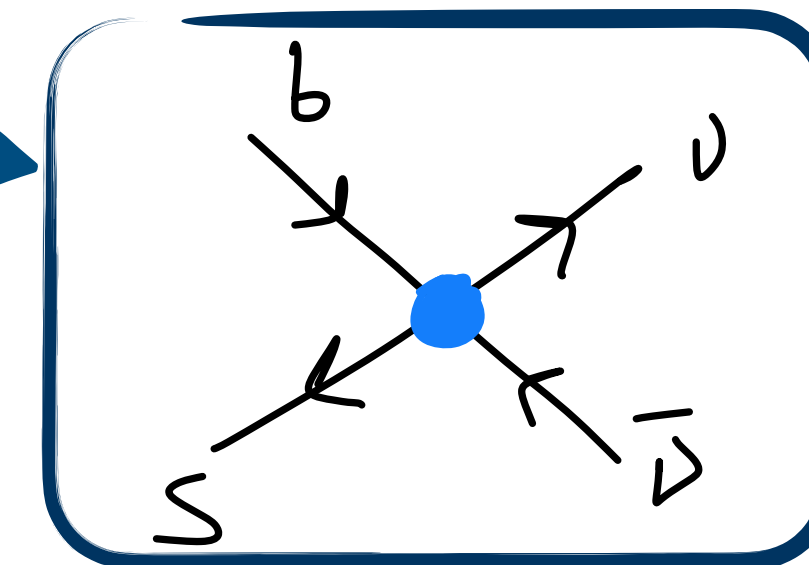
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Rare  $B$ -meson decays



$$E \ll M_{W,Z}$$

At low energies we use an EFT



$$B \rightarrow K^{(*)} \nu \nu$$
$$B \rightarrow K^{(*)} \ell \ell$$

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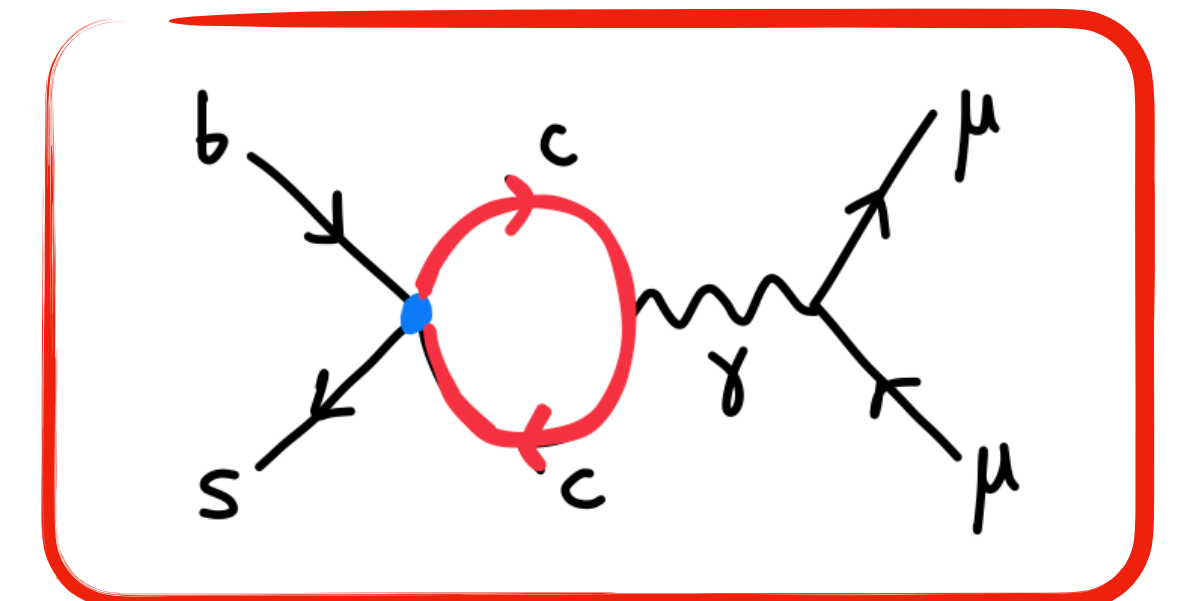
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Rare  $B$ -meson decays

Advantage of  $B \rightarrow K^{(*)} \nu \nu$  over the channel with charged leptons

Hadronic uncertainties might hinder their precise determination:

$b \rightarrow s \nu \nu$  is theoretically cleaner than  $b \rightarrow s \mu \mu$ , not affected by  $c\bar{c}$ -loops



$B \rightarrow K^{(*)} \nu \nu$  in the Standard Model

$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}} (1 + \delta_{\text{NP}})$$

# Effective lagrangian

$$b \rightarrow s\nu\nu$$

## Effective description in the SM

See e.g. A. Buras et al., 1409.4557

$$\mathcal{L}^{b \rightarrow s\nu\nu} = \frac{4G_F}{\sqrt{2}} \lambda_t \sum_a C_a \mathcal{O}_a + h.c.$$


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$$C_L^{\text{SM}} = -6.32(7)$$

Flavor diagonal  
and universal

NLO QCD & 2-loop  
EW corrections

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$$C_R^{\text{SM}} = 0$$



# Sources of uncertainty

## CKM matrix element determination

$$\mathcal{L}^{b \rightarrow s\nu\nu} = \frac{4G_F}{\sqrt{2}} \lambda_t \sum_a C_a \mathcal{O}_a + h.c.$$

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Inclusive vs exclusive

$$|\lambda_t| \times 10^3 = \begin{cases} 41.4 \pm 0.8, & B \rightarrow X_c \ell \bar{\nu} & \text{HFLAV, arXiv:2206.07501} \\ 39.3 \pm 1.0, & B \rightarrow D \ell \bar{\nu} & \text{FLAG, arXiv:2111.09849} \\ 37.8 \pm 0.7, & B \rightarrow D^{(*)} \ell \bar{\nu} & \text{HFLAV, arXiv:2206.07501} \end{cases}$$

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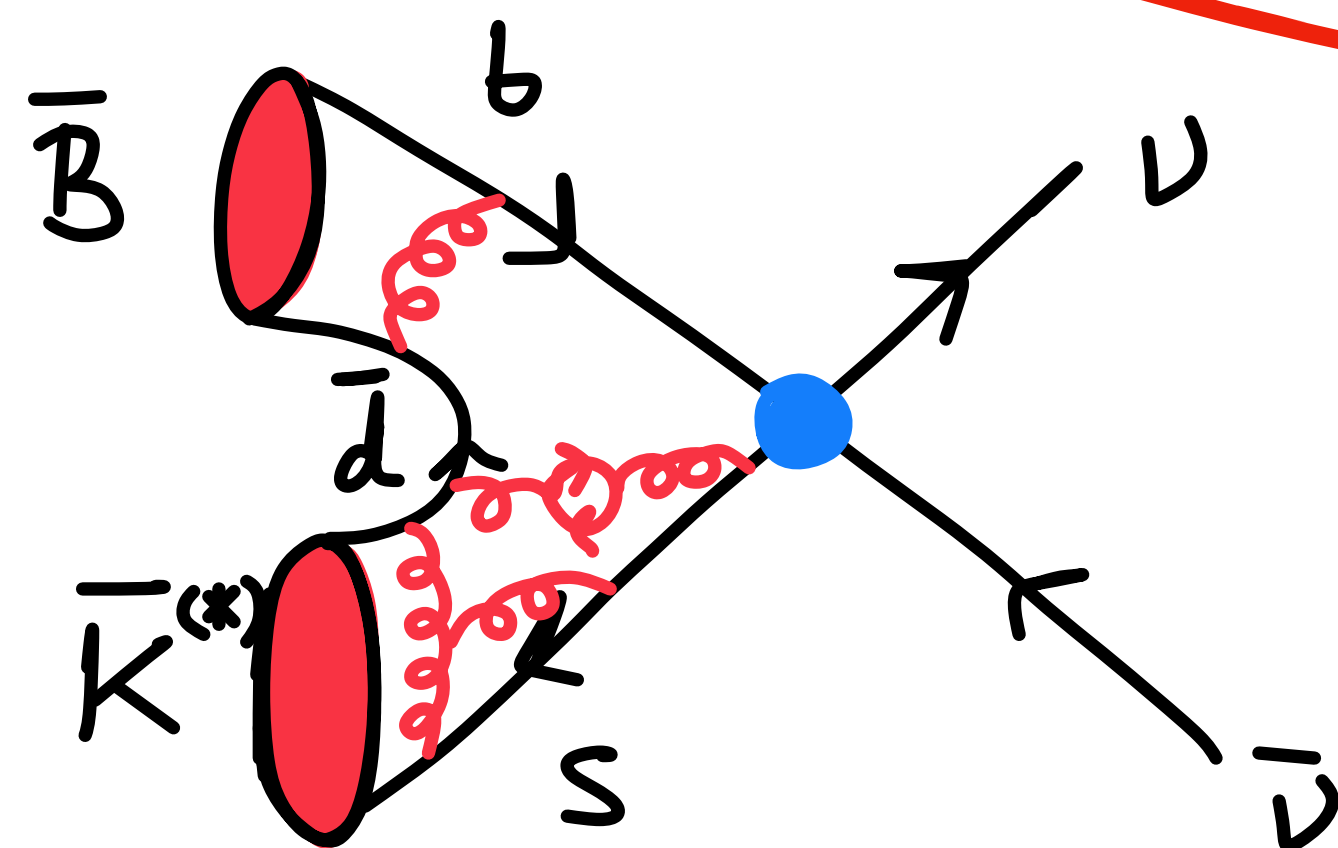
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Hadronic matrix element

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Lorentz structure

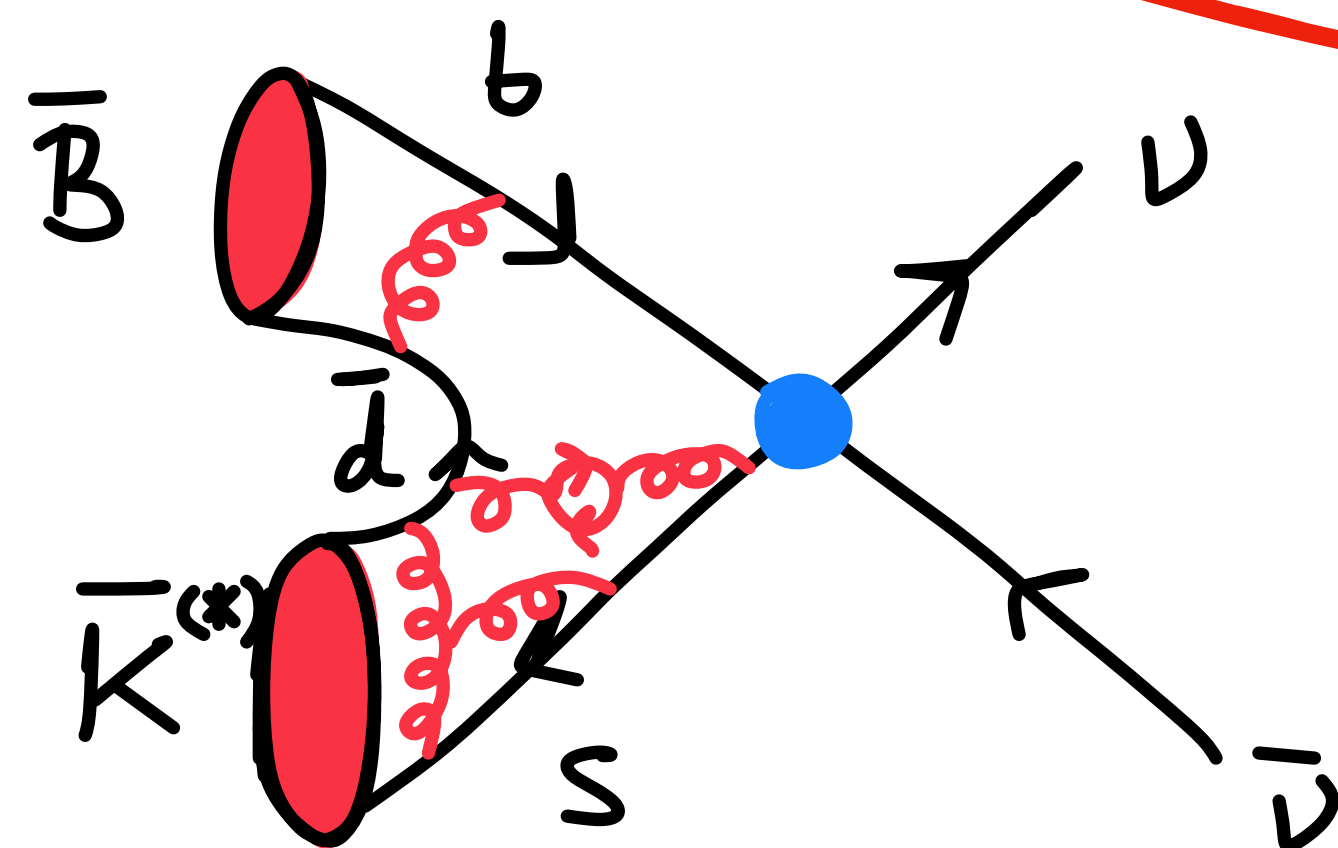
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Form factors (Lattice QCD, LCSR...)

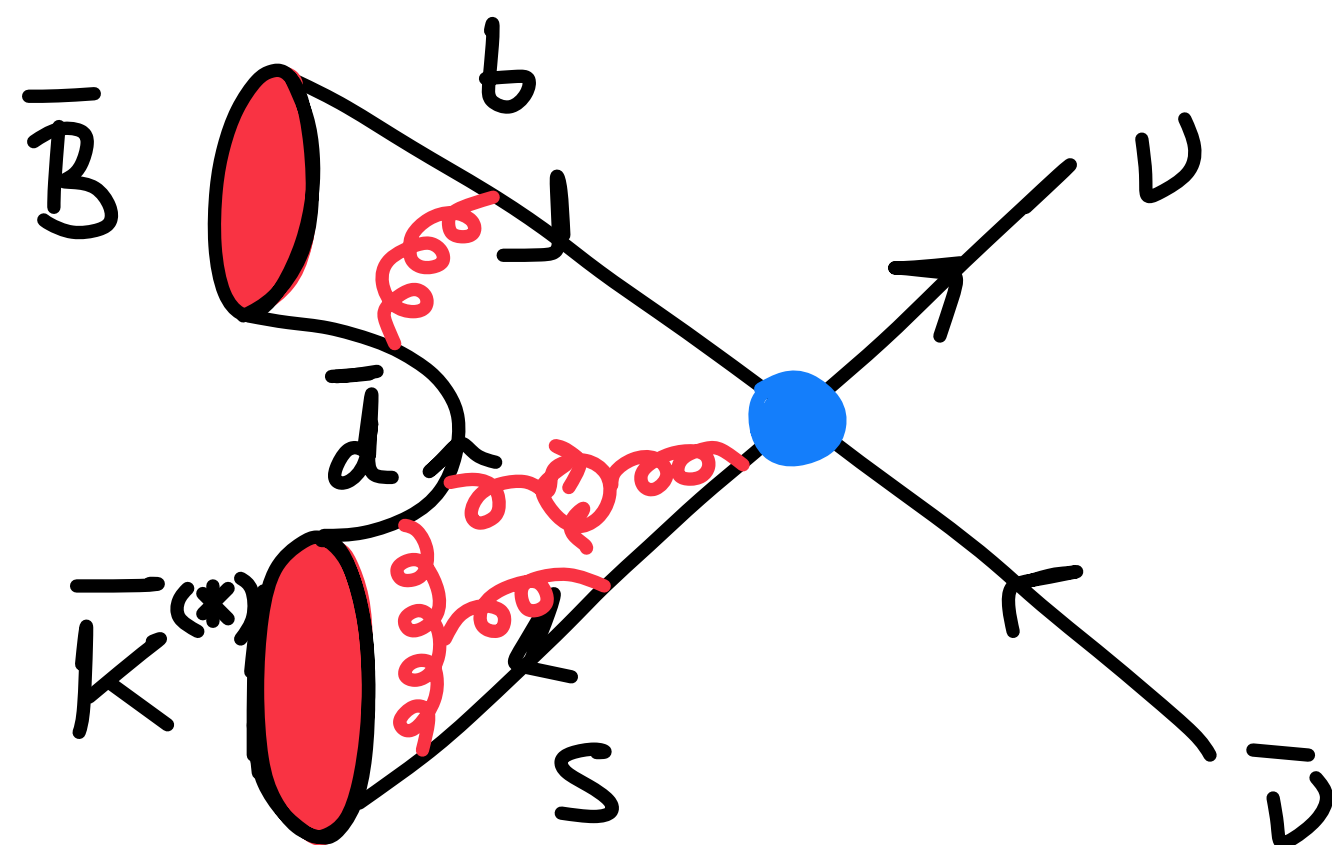


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# Form factors

$$B \rightarrow K \nu \bar{\nu}$$

HPQCD, arXiv:2207.12468  
FNAL/MILC, arXiv:1509.06235

Lattice determinations of the form factors (FF)

$$\langle \bar{K}(k) | \bar{s} \gamma^\mu b | \bar{B}(p) \rangle = \left[ (p + k)^\mu - \frac{m_B^2 - m_K^2}{q^2} q^\mu \right] f_+(q^2) + q^\mu \frac{m_B^2 - m_K^2}{q^2} f_0(q^2)$$

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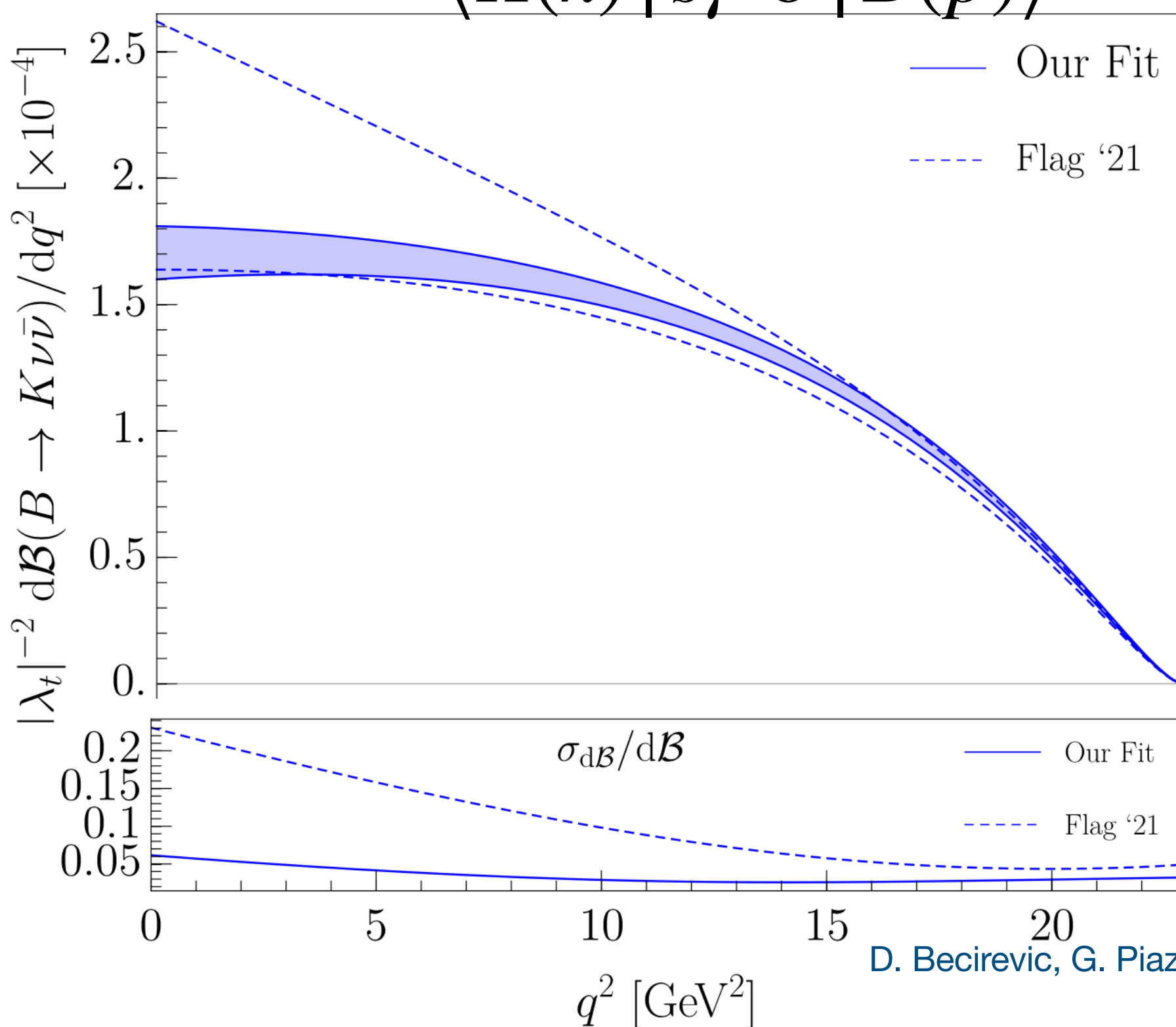
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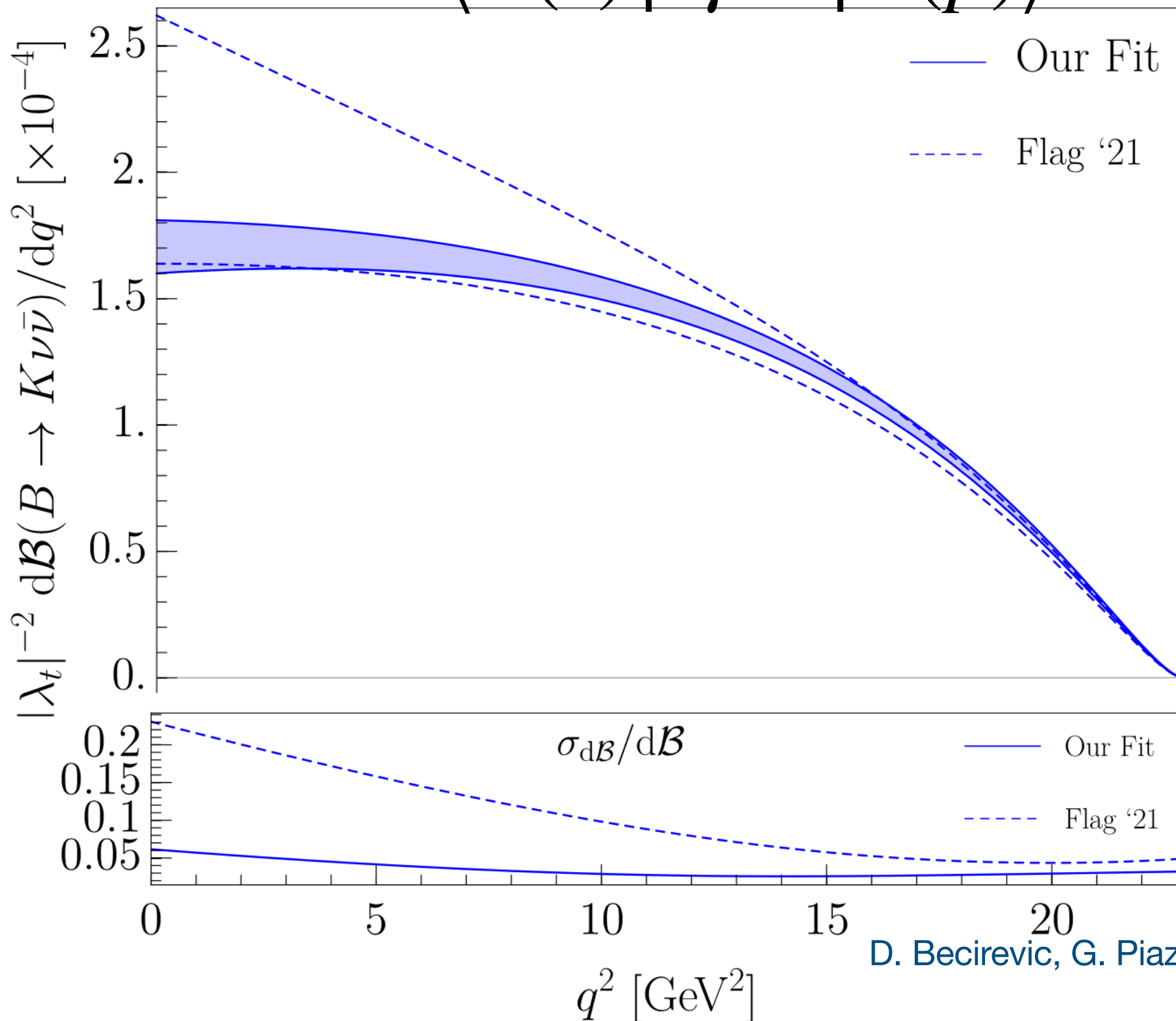
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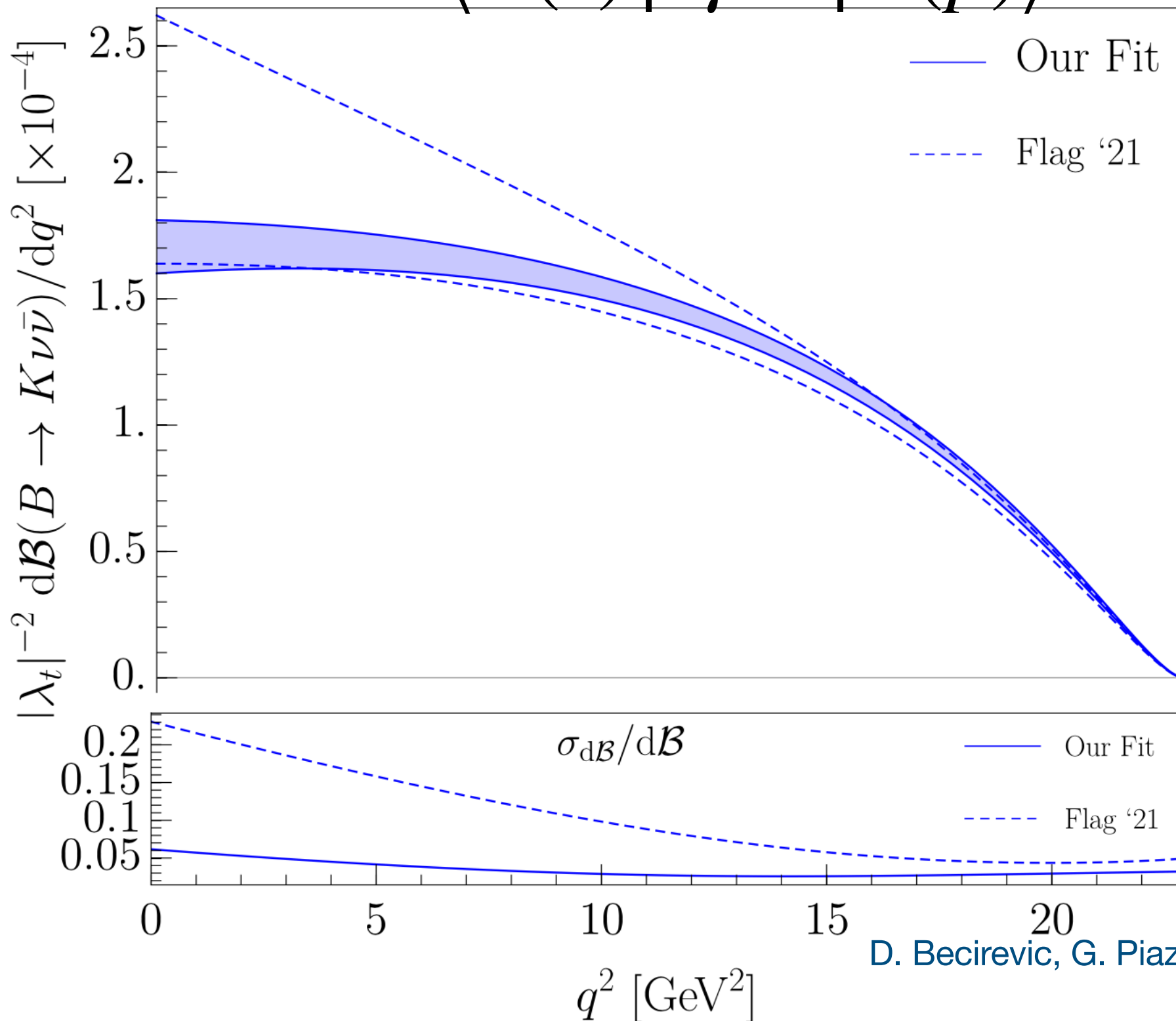
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Relative error related to FF determination  $\lesssim \mathcal{O}(5\%)$

Final prediction

$$\mathcal{B}(B^\pm \rightarrow K^\pm \nu \bar{\nu}) = (4.44 \pm 0.30) \times 10^{-6}$$

$\mathcal{O}(7\%)$  error

\*Only loop contribution

# Form factors

$$B \rightarrow K^* \nu \bar{\nu}$$

Several FF enter into the decay rate, determined through the combination of one LQCD result & LCSR

$$\begin{aligned} \langle \bar{K}^*(k) | \bar{s}_L \gamma^\mu b_L | \bar{B}(p) \rangle = & \epsilon_{\mu\nu\rho\sigma} \varepsilon^{*\nu} p^\rho k^\sigma \frac{2V(q^2)}{m_B + m_{K^*}} - i\varepsilon_\mu^* (m_B + m_{K^*}) A_1(q^2) \\ & + i(p+k)_\mu (\varepsilon^* \cdot q) \frac{A_2(q^2)}{m_B + m_{K^*}} + iq_\mu (\varepsilon^* \cdot q) \frac{2m_{K^*}}{q^2} [A_3(q^2) - A_0(q^2)] \end{aligned}$$

R. R. Horgan *et al.*, arXiv:1310.3722  
A. Bharucha, D. M. Straub & R. Zwicky, arXiv:1503.05534

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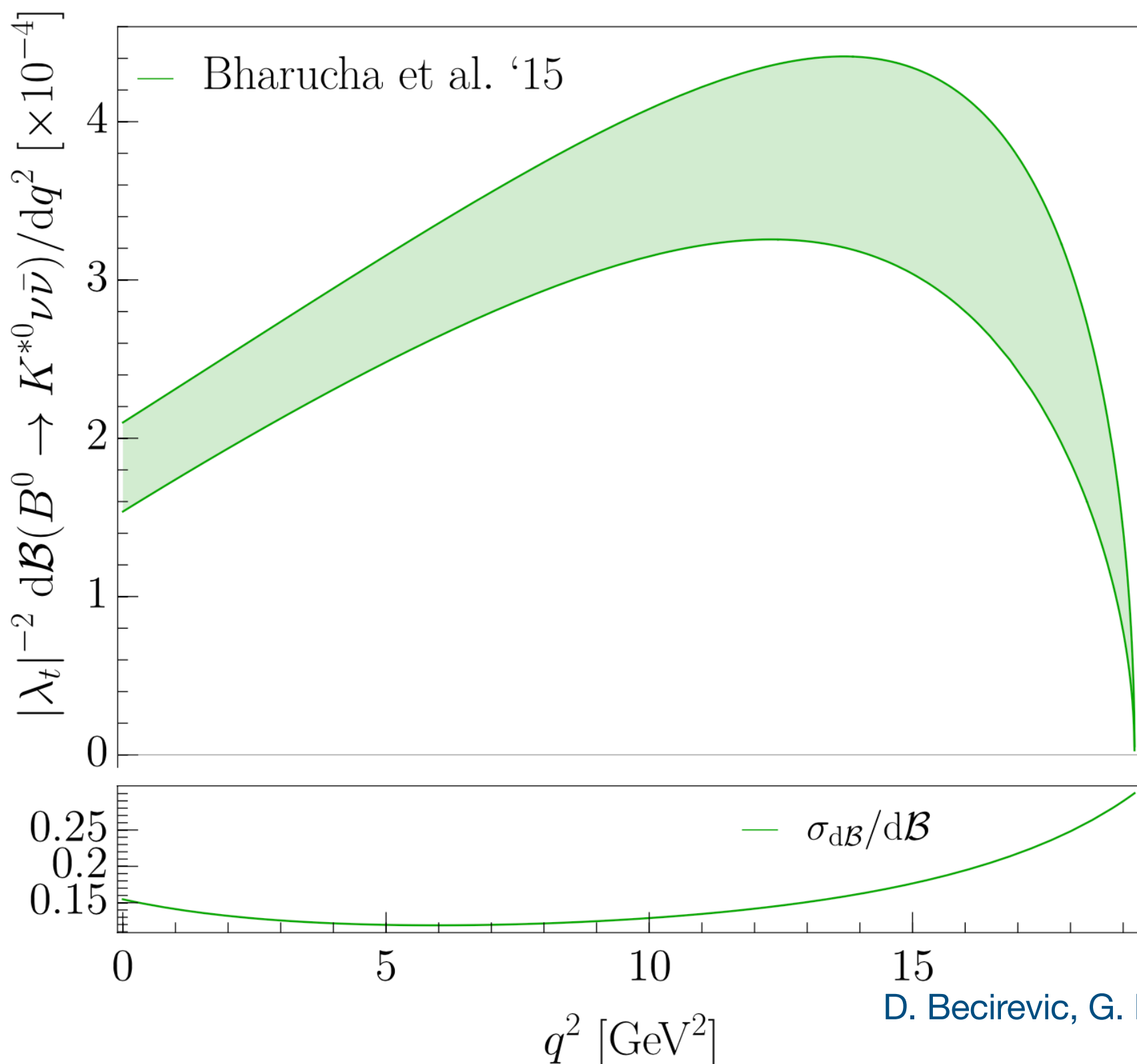
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Relative error related to FF determination  $\sim \mathcal{O}(15\%)$



D. Becirevic, G. Piazza & O. Sumensari, arXiv:2301.06990

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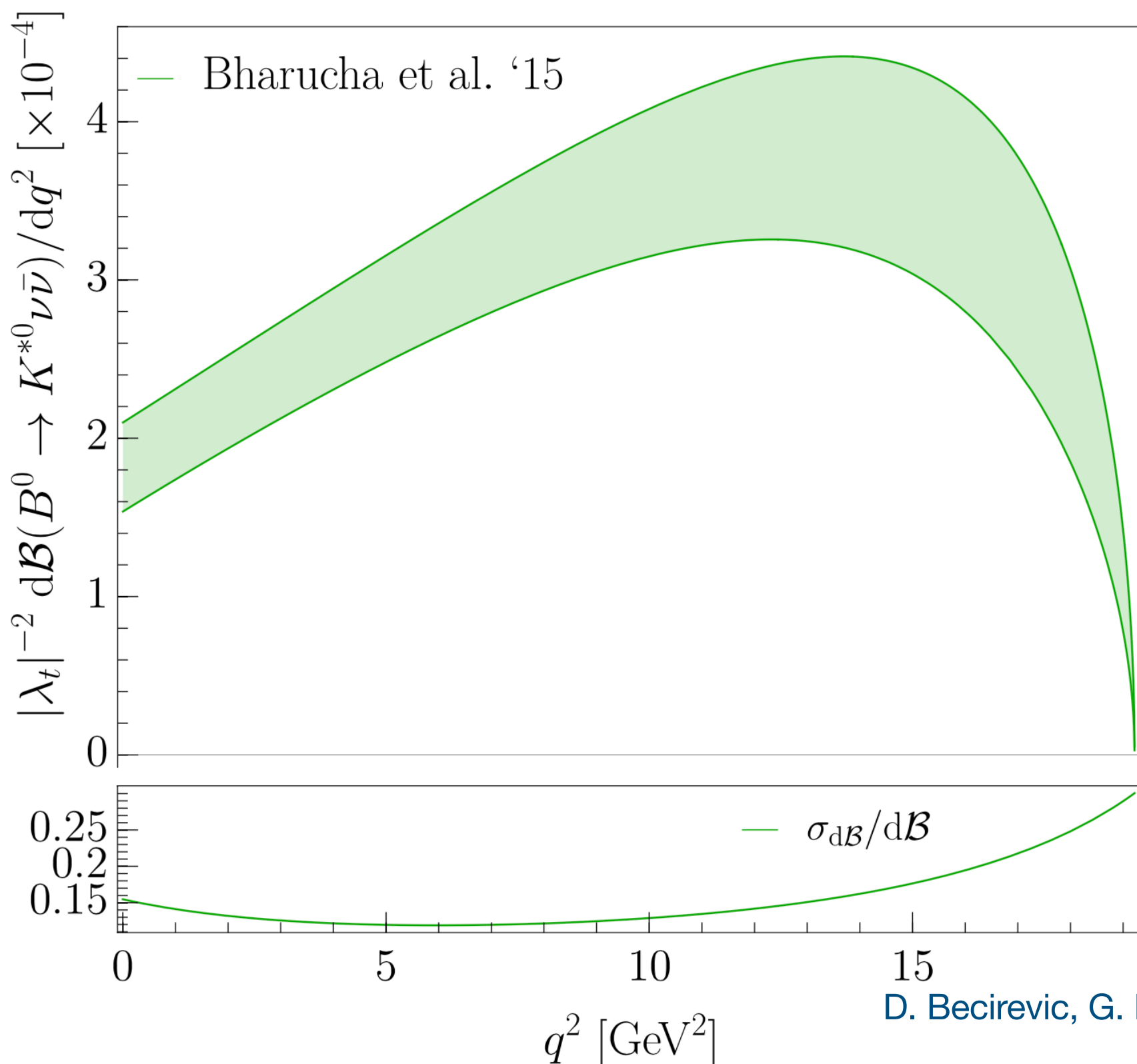
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**Final prediction**

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$\mathcal{O}(15\%)$  error

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# Summary

$B \rightarrow K^{(*)} \nu \bar{\nu}$  in the SM

Two main sources of uncertainty

Form factor determination

$$\langle K^{(*)} | \bar{s}_L \gamma^\mu b_L | B \rangle = \sum_i K_i^\mu \mathcal{F}_i(q^2)$$

Form factors (Lattice QCD, LCSR...)

CKM determination

$$\text{CKM unitarity} \quad |\lambda_t| \sim |V_{cb}| (1 + \mathcal{O}(\lambda^2))$$

Inclusive vs exclusive?

Expected BR in the SM using exclusive  $B \rightarrow D \ell \nu$  decays and available FF determinations as inputs

$$\mathcal{B} (B^\pm \rightarrow K^\pm \nu \bar{\nu}) \Big|_{\text{SM}} = (4.44 \pm 0.30) \times 10^{-6}$$

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# Belle-II results

$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}}(1 + \delta_{\text{NP}})$$

# Belle-II experiment

Belle-II (SuperKEKB) is an  $e^+e^-$  collider operating at  $\sqrt{s} \simeq m_{\Upsilon(4S)}$

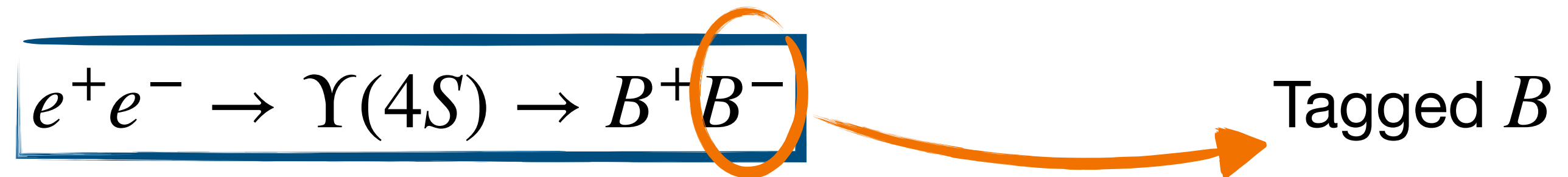
BELLE-II Collaboration, arXiv:2311.14647

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^+B^-$$

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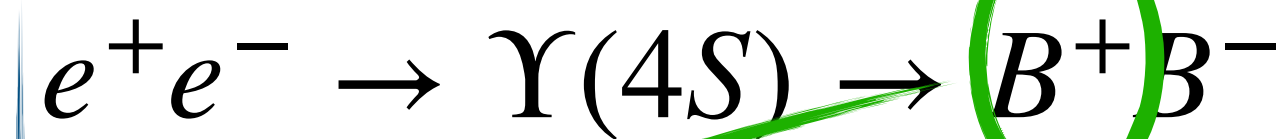


Tagging methods	Hadronic	Inclusive
Efficiency	0.5%	8 %
Backgrounds	Small	Large

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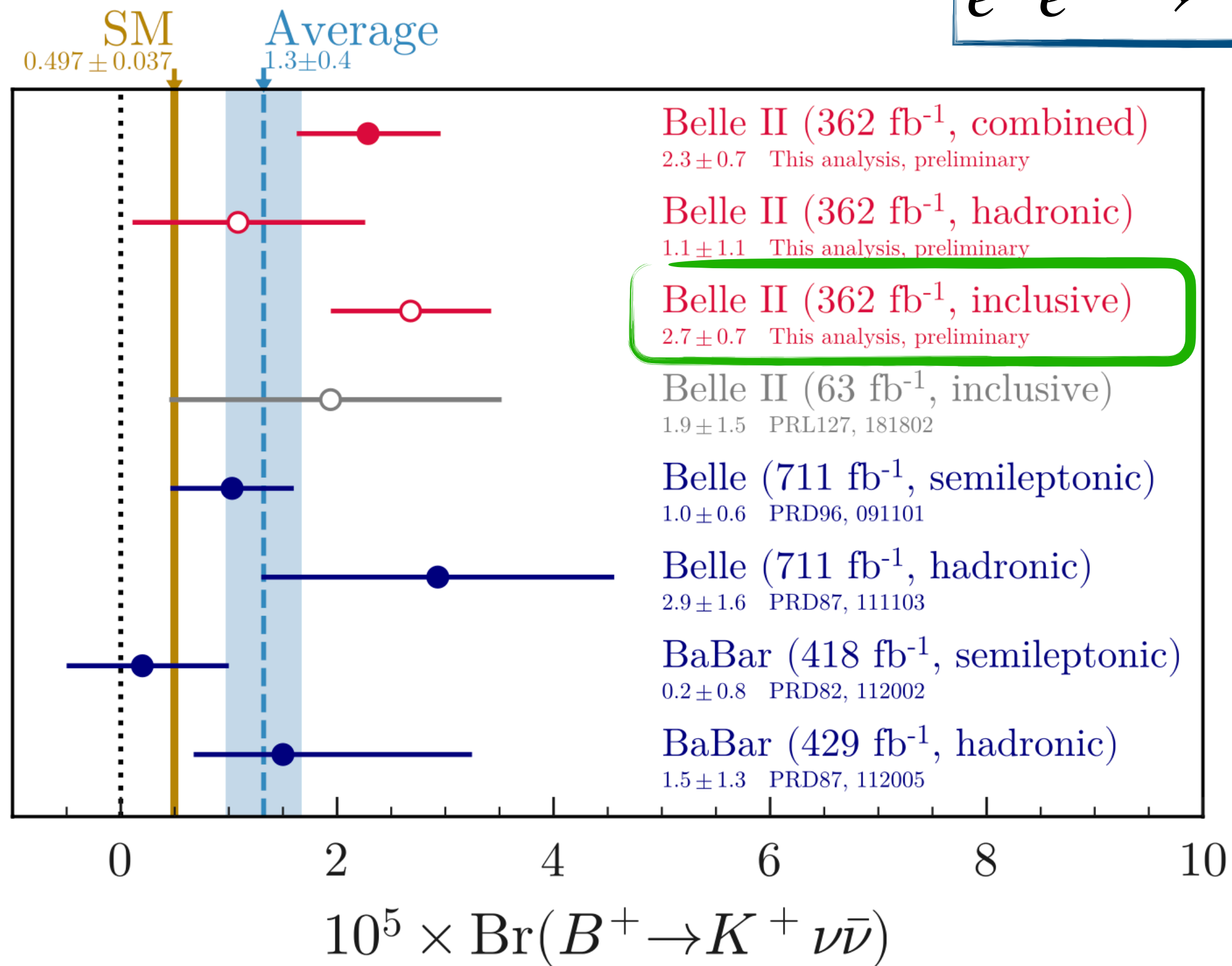
Signal:  $B^+ \rightarrow K^+\nu\nu$

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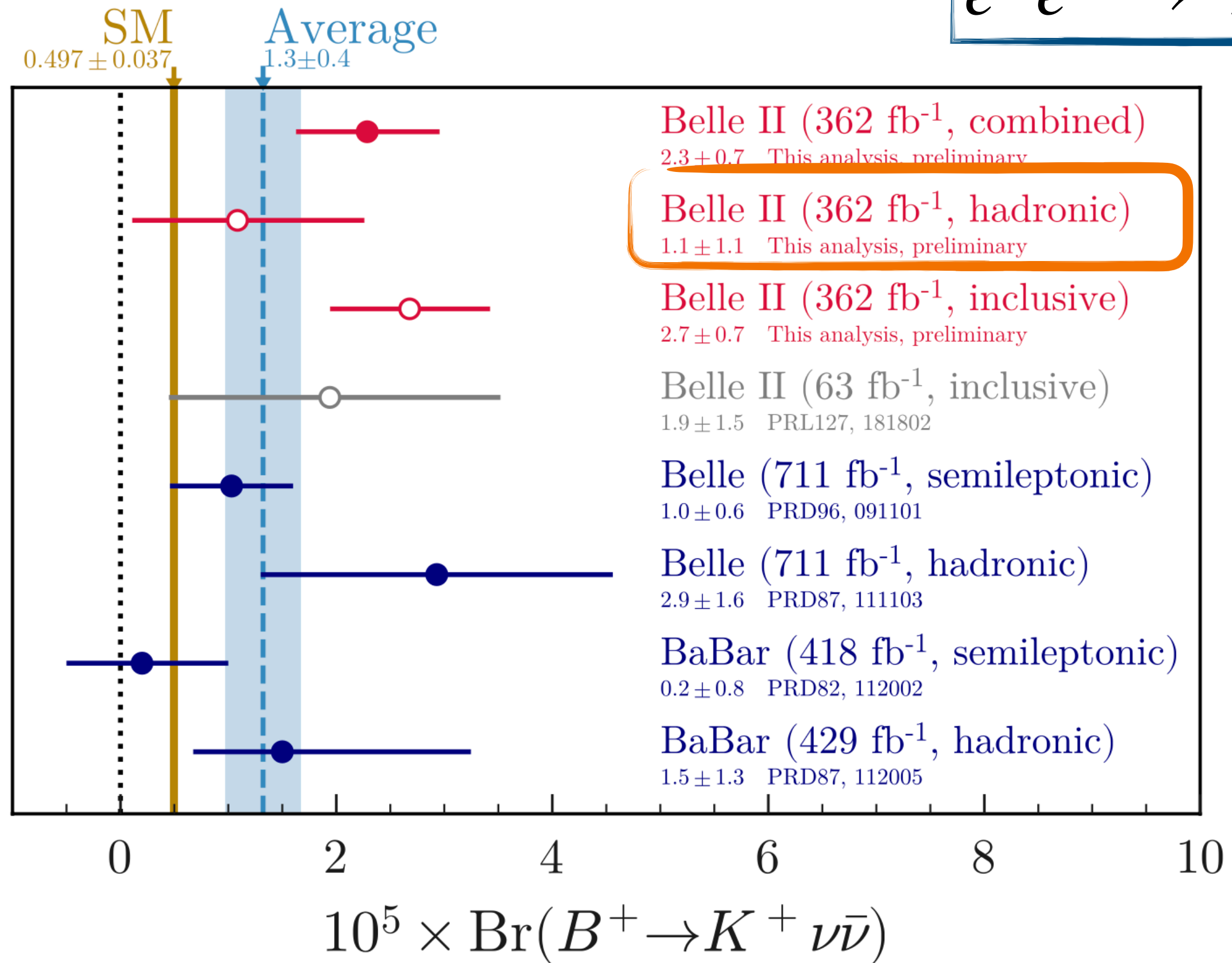


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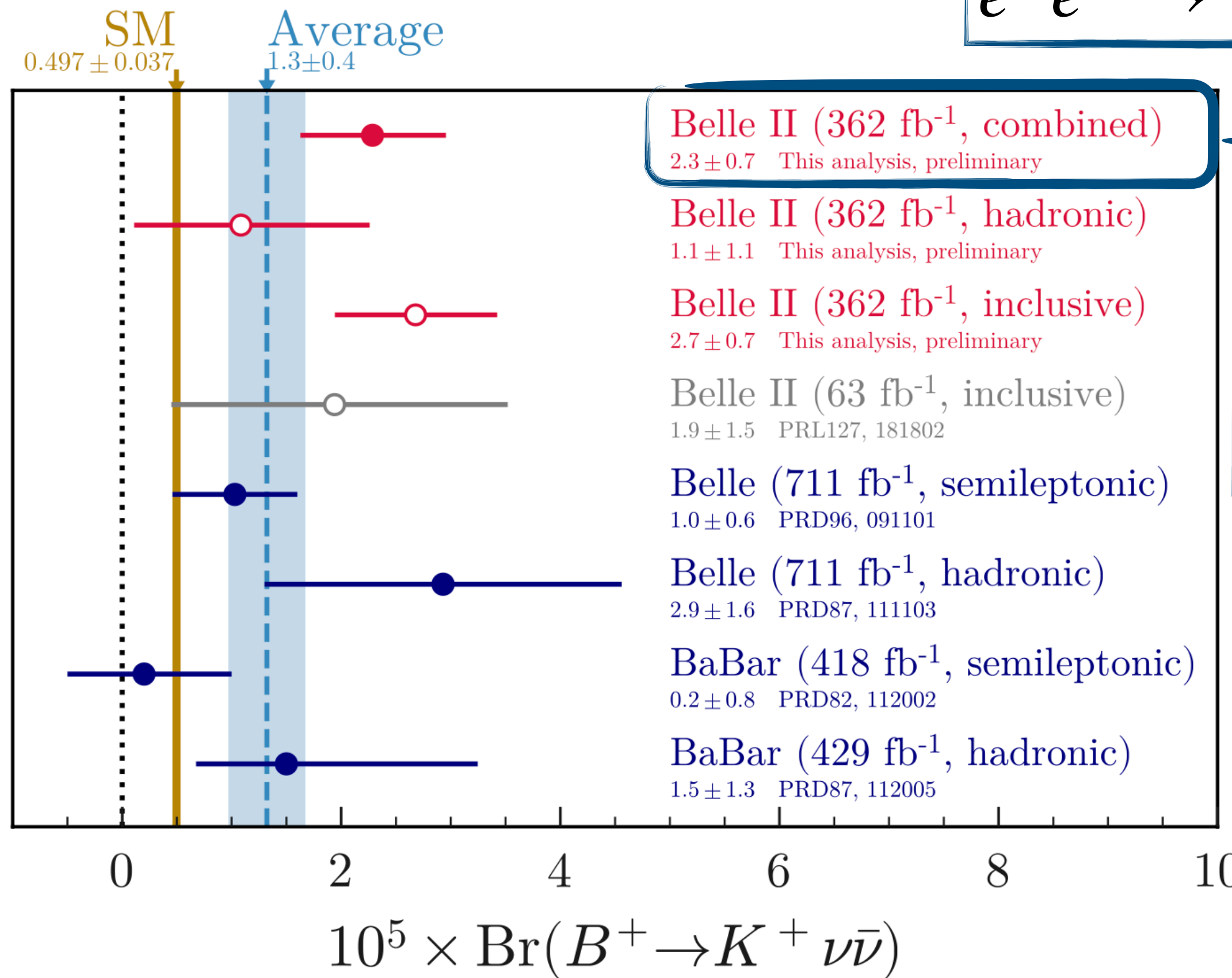
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BELLE-II Collaboration, arXiv:2311.14647

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^+B^-$$



$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (2.3 \pm 0.7) \times 10^{-5}$$

About  $3\sigma$  above the SM expectation

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) \Big|_{\text{SM}} = (4.44 \pm 0.30) \times 10^{-6}$$



# Implications of $B \rightarrow K\nu\bar{\nu}$ for BSM

- LEFT
- SMEFT
- Light new physics

$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}}(1 + \delta_{\text{NP}})$$

# BSM contributions

## Low-energy EFT with SM neutrinos

Including **BSM** contributions we can write (w/o  $N_R$ )

$$\mathcal{L}^{b \rightarrow s \nu \nu} = \frac{4G_F}{\sqrt{2}} \lambda_t \sum_{i,j} \left( C_L^{\nu_i \nu_j} \mathcal{O}_L^{\nu_i \nu_j} + C_R^{\nu_i \nu_j} \mathcal{O}_R^{\nu_i \nu_j} \right) + h.c.$$

$$C_L^{\nu_i \nu_j} = C_L^{\text{SM}} \delta_{ij} + \delta C_L^{\nu_i \nu_j} \quad C_R^{\nu_i \nu_j} = \delta C_R^{\nu_i \nu_j}$$

R. Bause, G. Hisbert & G. Hiller,  
arXiv:2309.00075  
P. Athron, R. Martinez & C. Sierra,  
arXiv:2308.13426  
L. Allwicher, D. Becirevic, G. Piazza,  
SRA & O. Sumensari, arXiv:2309.02246

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$$\mathcal{B} (B \rightarrow K^{(*)} \nu \bar{\nu}) = \mathcal{B} (B \rightarrow K^{(*)} \nu \bar{\nu}) \Big|_{\text{SM}} \left( 1 + \delta \mathcal{B}_{K^{(*)}} \right)$$

All **BSM** contributions are contained here

# BSM contributions

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Including **BSM** contributions we can write (w/o  $N_R$ )

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All **BSM** contributions are contained here

$$\delta \mathcal{B}_{K^{(*)}} = \sum_i \frac{2 \text{Re}[C_L^{\text{SM}} (\delta C_L^{\nu_i \nu_i} + \delta C_R^{\nu_i \nu_i})]}{3 |C_L^{\text{SM}}|^2}$$

$$+ \sum_{i,j} \frac{|\delta C_L^{\nu_i \nu_j} + \delta C_R^{\nu_i \nu_j}|^2}{3 |C_L^{\text{SM}}|^2} - \eta_V^{K^{(*)}} \sum_{i,j} \frac{\text{Re}[\delta C_R^{\nu_i \nu_j} (C_L^{\text{SM}} \delta_{ij} + \delta C_L^{\nu_i \nu_j})]}{3 |C_L^{\text{SM}}|^2}$$

$$\eta_V^K = 0$$

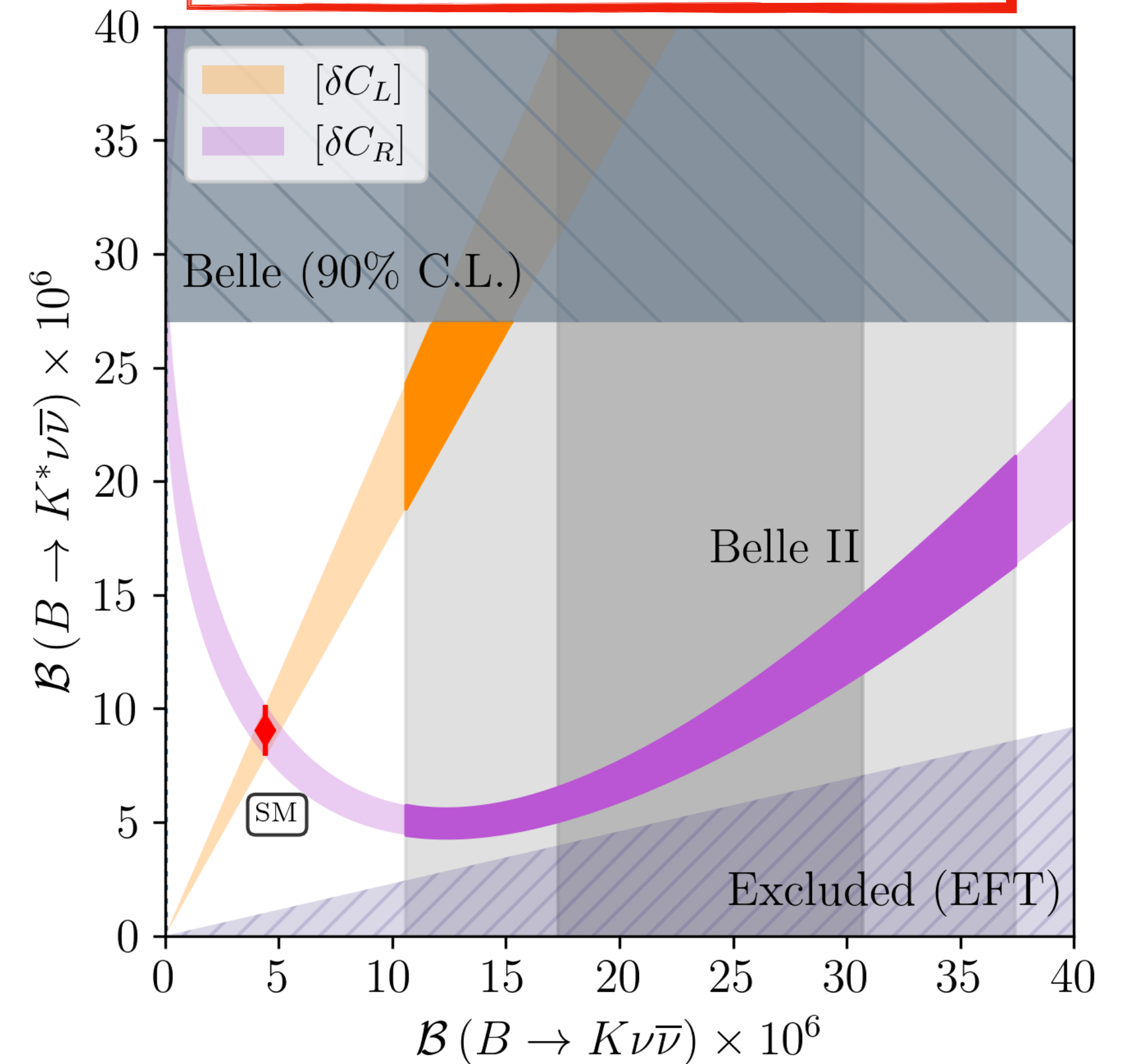
$$\eta_V^{K^*} = 3.33 \pm 0.07$$

D. Becirevic, G. Piazza & O. Sumensari, arXiv:2301.06990  
 L. Allwicher, D. Becirevic, G. Piazza, SRA & O. Sumensari, arXiv:2309.02246

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ with heavy NP

Correlations between  $B \rightarrow K \nu \bar{\nu}$  and  $B \rightarrow K^* \nu \bar{\nu}$

Assuming  $\delta C_{L(R)}^{\nu_i \nu_j} = \delta C_{L(R)} \delta_{ij}$



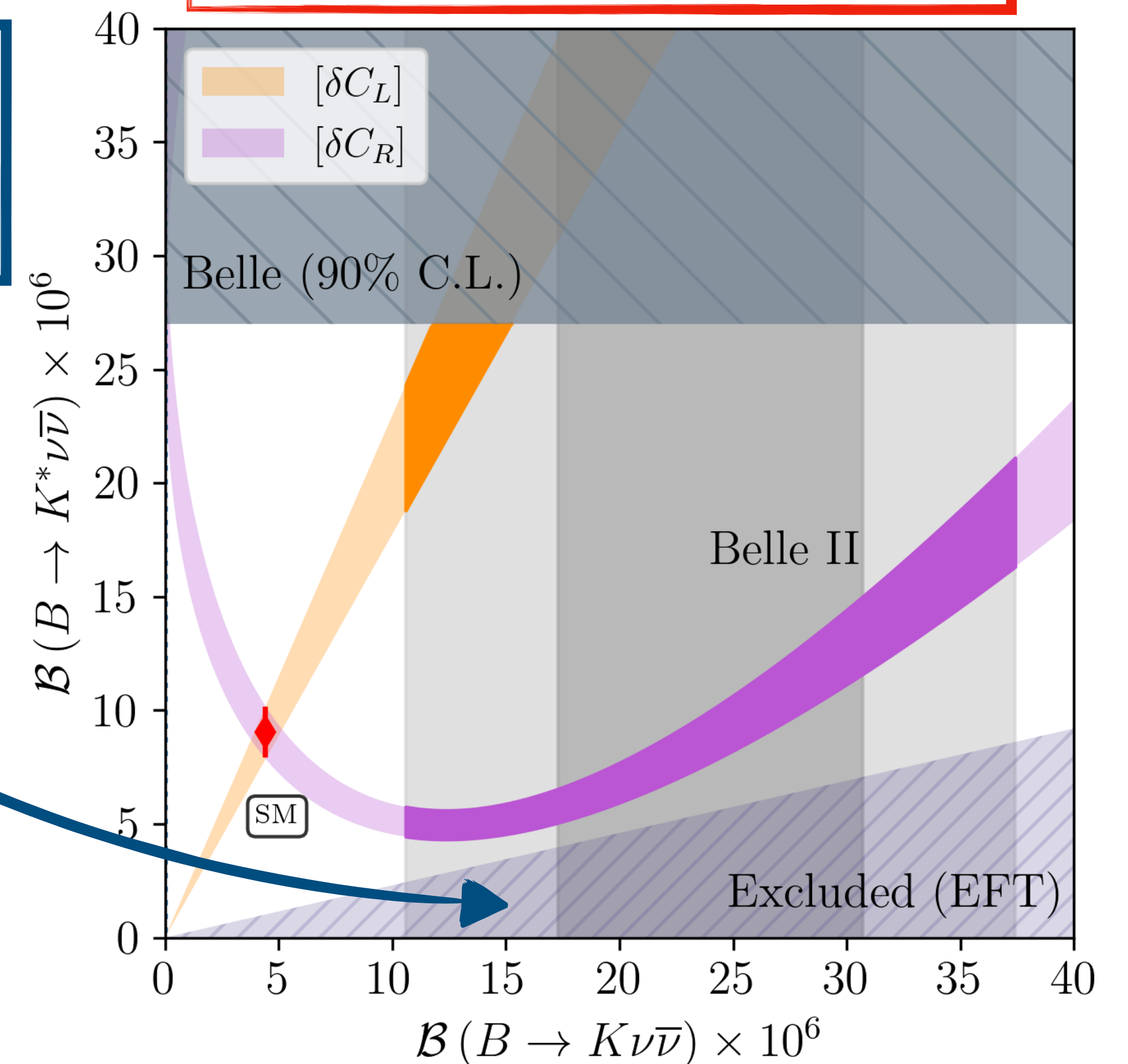
# $B \rightarrow K^{(*)} \nu \bar{\nu}$ with heavy NP

## Correlations between $B \rightarrow K \nu \bar{\nu}$ and $B \rightarrow K^* \nu \bar{\nu}$

One can find a lower bound for the validity of the EFT

$$\frac{\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})_{\text{SM}}} \geq \frac{\mathcal{B}(B \rightarrow K \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K \nu \bar{\nu})_{\text{SM}}} \left( 1 - \frac{\eta_V^{K^*}}{4} \right)$$

Assuming  $\delta C_{L(R)}^{\nu_i \nu_j} = \delta C_{L(R)} \delta_{ij}$



# $B \rightarrow K^{(*)} \nu \bar{\nu}$ with heavy NP

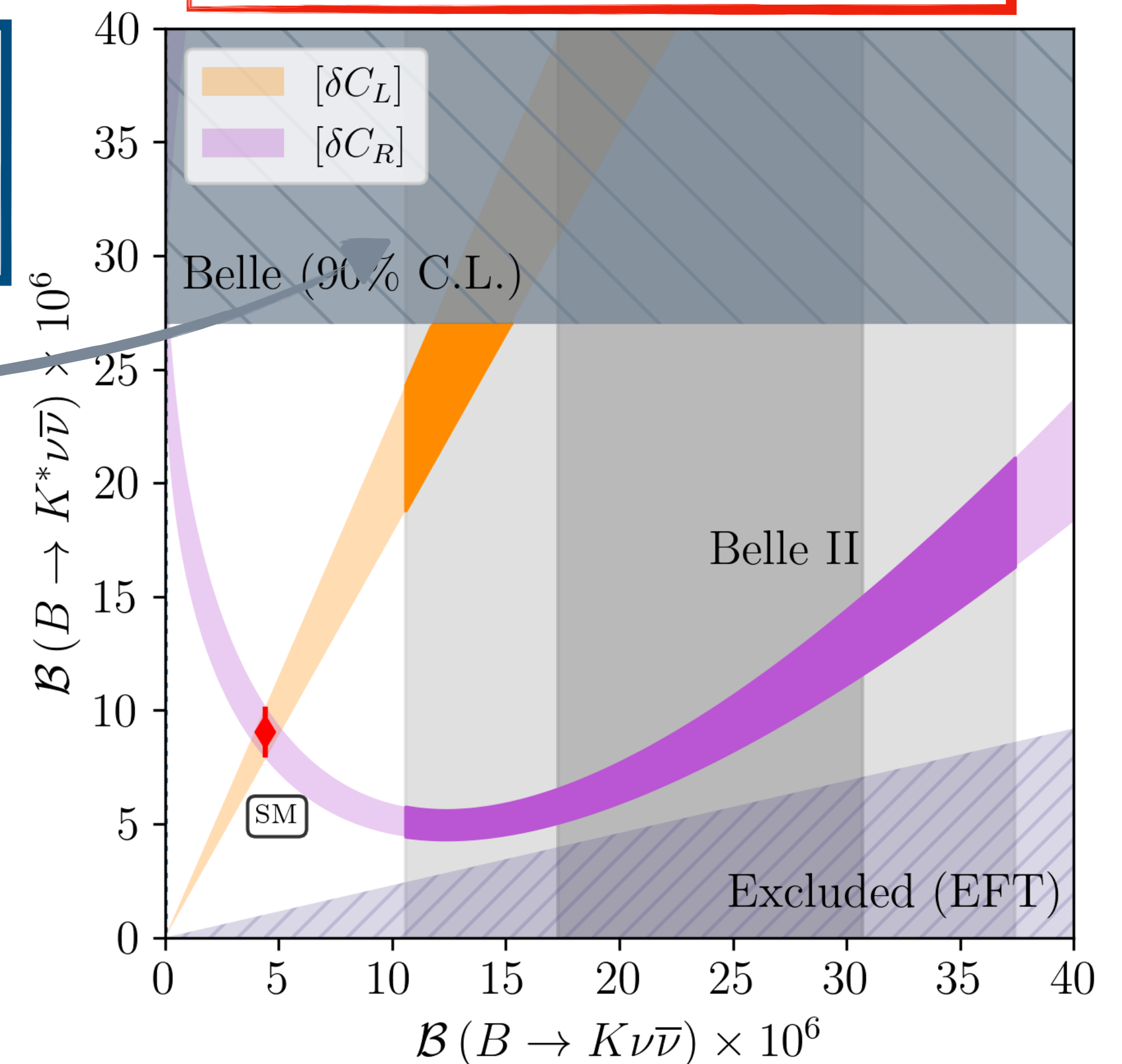
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Belle bounds  $\mathcal{B}(B \rightarrow K^* \nu \bar{\nu}) < 2.7 \times 10^{-5}$ ,  
constraining a solution **only** in terms of  $\delta C_L$

Assuming  $\delta C_{L(R)}^{\nu_i \nu_j} = \delta C_{L(R)} \delta_{ij}$



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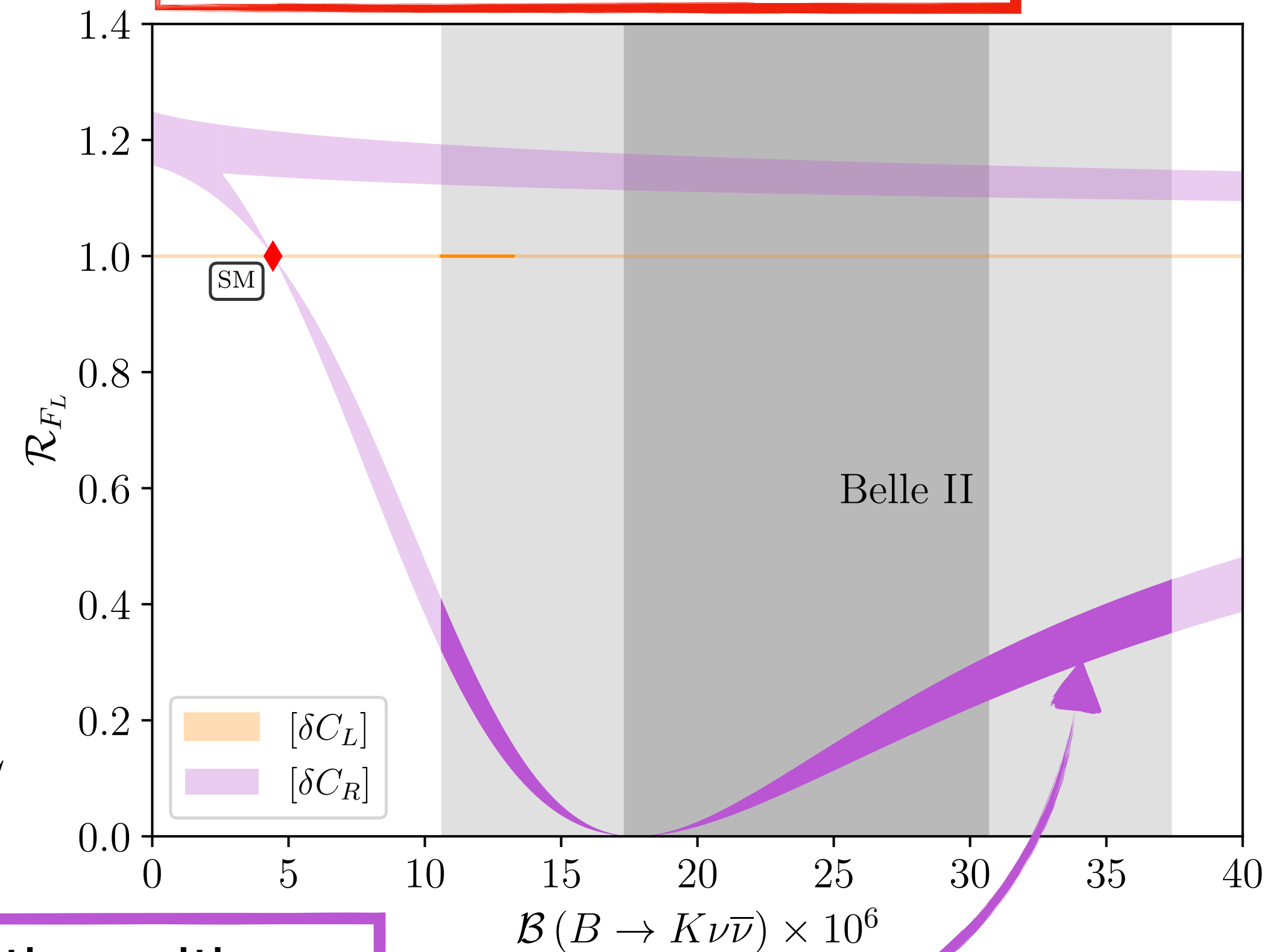
$$\frac{\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})_{\text{SM}}} \geq \frac{\mathcal{B}(B \rightarrow K \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K \nu \bar{\nu})_{\text{SM}}} \left( 1 - \frac{\eta_V^{K^*}}{4} \right)$$

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constraining a solution **only** in terms of  $\delta C_L$

Look for the fraction of longitudinally polarized  $K^*$ ,  $F_L$

$$\mathcal{R}_{F_L} = \frac{F_L}{F_L^{\text{SM}}}$$

Assuming  $\delta C_{L(R)}^{\nu_i \nu_j} = \delta C_{L(R)} \delta_{ij}$



Depletion with respect to the SM expectation



# Implications of $B \rightarrow K\nu\bar{\nu}$ for BSM

- LEFT
- SMEFT
- Light new physics

$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}}(1 + \delta_{\text{NP}})$$

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the SMEFT

## Four fermion operators\*

If the NP contribution is heavy enough,  $\Lambda > \nu$ , we can work in the SMEFT

$$\mathcal{L}_{\text{SMEFT}}^{(6)} \supset \frac{1}{\Lambda^2} \left\{ \left( \mathcal{C}_{lq}^{(1)} + \mathcal{C}_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu e_{Lj}) + \left( \mathcal{C}_{lq}^{(1)} - \mathcal{C}_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) \right. \\ \left. + 2 V_{cs} \left[ \mathcal{C}_{lq}^{(3)} \right]_{ij} (\bar{c}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu \nu_{Lj}) + [\mathcal{C}_{ld}]_{ij} (\bar{s}_R \gamma^\mu b_R) [(\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) + (\bar{e}_{Li} \gamma_\mu e_{Lj})] + \text{h.c.} \right\}$$

$$\left[ \mathcal{O}_{LQ}^{(1)} \right]_{ijkl} = (\bar{L}_i \gamma^\mu L_j) (\bar{Q}_k \gamma_\mu Q_l)$$

$$\left[ \mathcal{O}_{LQ}^{(3)} \right]_{ijkl} = (\bar{L}_i \gamma^\mu \tau^I L_j) (\bar{Q}_k \gamma_\mu \tau^I Q_l)$$

$$\left[ \mathcal{O}_{Ld} \right]_{ijkl} = (\bar{L}_i \gamma^\mu L_j) (\bar{d}_k \gamma_\mu d_l)$$

\* Operators with Higgs severely constrained!

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the SMEFT

## Four fermion operators

If the NP contribution is heavy enough,  $\Lambda > \nu$ , we can work in the SMEFT

$$\mathcal{L}_{\text{SMEFT}}^{(6)} \supset \frac{1}{\Lambda^2} \left\{ \left( c_{lq}^{(1)} + c_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu e_{Lj}) + \left( c_{lq}^{(1)} - c_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) \right. \\ \left. + 2 V_{cs} \left[ c_{lq}^{(3)} \right]_{ij} (\bar{c}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu \nu_{Lj}) + [c_{ld}]_{ij} (\bar{s}_R \gamma^\mu b_R) [(\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) + (\bar{e}_{Li} \gamma_\mu e_{Lj})] + \text{h.c.} \right\}$$

Correlations between  $b \rightarrow s \nu \nu$ ,  $b \rightarrow s \ell_\alpha^- \ell_\beta^+$  and  $b \rightarrow c \ell_\alpha \nu$

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the SMEFT

## Four fermion operators

If the NP contribution is heavy enough,  $\Lambda > v$ , we can work in the SMEFT

$$\mathcal{L}_{\text{SMEFT}}^{(6)} \supset \frac{1}{\Lambda^2} \left\{ \left( c_{lq}^{(1)} + c_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu e_{Lj}) + \left( c_{lq}^{(1)} - c_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) \right. \\ \left. + 2 V_{cs} \left[ c_{lq}^{(3)} \right]_{ij} (\bar{c}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu \nu_{Lj}) + [C_{ld}]_{ij} (\bar{s}_R \gamma^\mu b_R) [(\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) + (\bar{e}_{Li} \gamma_\mu e_{Lj})] + \text{h.c.} \right\}$$

Correlations between  $b \rightarrow s \nu \nu$ ,  $b \rightarrow s \ell_\alpha^- \ell_\beta^+$  and  $b \rightarrow c \ell_\alpha \nu$

Matching to the low-energy NP couplings

$$\delta C_L^{\nu_i \nu_j} = \frac{\pi}{\alpha_{\text{em}} \lambda_t} \frac{v^2}{\Lambda^2} \left\{ [c_{lq}^{(1)}]_{ij} - [c_{lq}^{(3)}]_{ij} \right\}$$



$$\delta C_R^{\nu_i \nu_j} = \frac{\pi}{\alpha_{\text{em}} \lambda_t} \frac{v^2}{\Lambda^2} [C_{ld}]_{ij}$$

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the SMEFT

## Correlations between observables

If the NP contribution is heavy enough,  $\Lambda > \nu$ , we can work in the SMEFT

$$\mathcal{L}_{\text{SMEFT}}^{(6)} \supset \frac{1}{\Lambda^2} \left\{ \left( C_{lq}^{(1)} + C_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu e_{Lj}) + \left( C_{lq}^{(1)} - C_{lq}^{(3)} \right)_{ij} (\bar{s}_L \gamma^\mu b_L) (\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) \right. \\ \left. + 2 V_{cs} \left[ C_{lq}^{(3)} \right]_{ij} (\bar{c}_L \gamma^\mu b_L) (\bar{e}_{Li} \gamma_\mu \nu_{Lj}) + [C_{ld}]_{ij} (\bar{s}_R \gamma^\mu b_R) [(\bar{\nu}_{Li} \gamma_\mu \nu_{Lj}) + (\bar{e}_{Li} \gamma_\mu e_{Lj})] + \text{h.c.} \right\}$$

- Coupling to muons are tightly constrained by  $\mathcal{B} (B_s \rightarrow \mu\mu)$  and  $R_{K^{(*)}}$  
- Coupling to taus allowed, predicting 

$$\frac{\mathcal{B} (B_s \rightarrow \tau\tau)}{\mathcal{B} (B_s \rightarrow \tau\tau)_{\text{SM}}} \simeq \frac{\mathcal{B} (B \rightarrow K^{(*)} \tau\tau)}{\mathcal{B} (B \rightarrow K^{(*)} \tau\tau)_{\text{SM}}} \simeq 10$$

# Examples for concrete models

- $Z'$  coupled to RH quarks

$$\mathcal{L}_{Z'} \supset g_{bs} (\bar{s}_R \gamma^\mu b_R) Z'_\mu + g_{\tau\tau} (\bar{L}_3 \gamma^\mu L_3) Z'_\mu$$

$B^0 - \bar{B}^0$  mixing constrain  $|g_{sb}|/m_{Z'} \lesssim 2 \times 10^{-3} \text{ TeV}^{-1}$

Cannot fit data with perturbative  $g_{\tau\tau}$

- $\tilde{R}_2$  leptoquark

$$\mathcal{L}_{\tilde{R}_2} \supset y_{ij}^R (\bar{d}_{Ri} \tilde{R}_2 i \tau_2 L_j) + h.c.$$

Upper bound  $m_{LQ} \lesssim 3 \text{ TeV}$

Difficult to accommodate such a large excess, but possible

# Implications of $B \rightarrow K\nu\bar{\nu}$ for BSM

- LEFT
- SMEFT
- Light new physics

$$\mathcal{O}_{\text{exp}} = \mathcal{O}_{\text{SM}}(1 + \delta_{\text{NP}})$$

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the $\nu$ SMEFT

Include a light RH neutrino field

$$\mathcal{L}_{\text{Yukawa}} = -\bar{Q}Y_d H d_R - \bar{Q}Y_u \tilde{H} u_R - \bar{L}Y_\ell H e_R + \bar{L}Y_\nu \tilde{H} N_R + \frac{1}{2} \bar{N}_R^c M N_R + h.c.$$

Only mass scale not set by the Higgs mechanism

Relation between flavor and mass eigenstates

$$\nu_{L\alpha} = \sum_{i=1}^4 U_{\alpha i} P_L n_i$$

$$N_R = \sum_{i=1}^4 U_{si}^* P_R n_i$$



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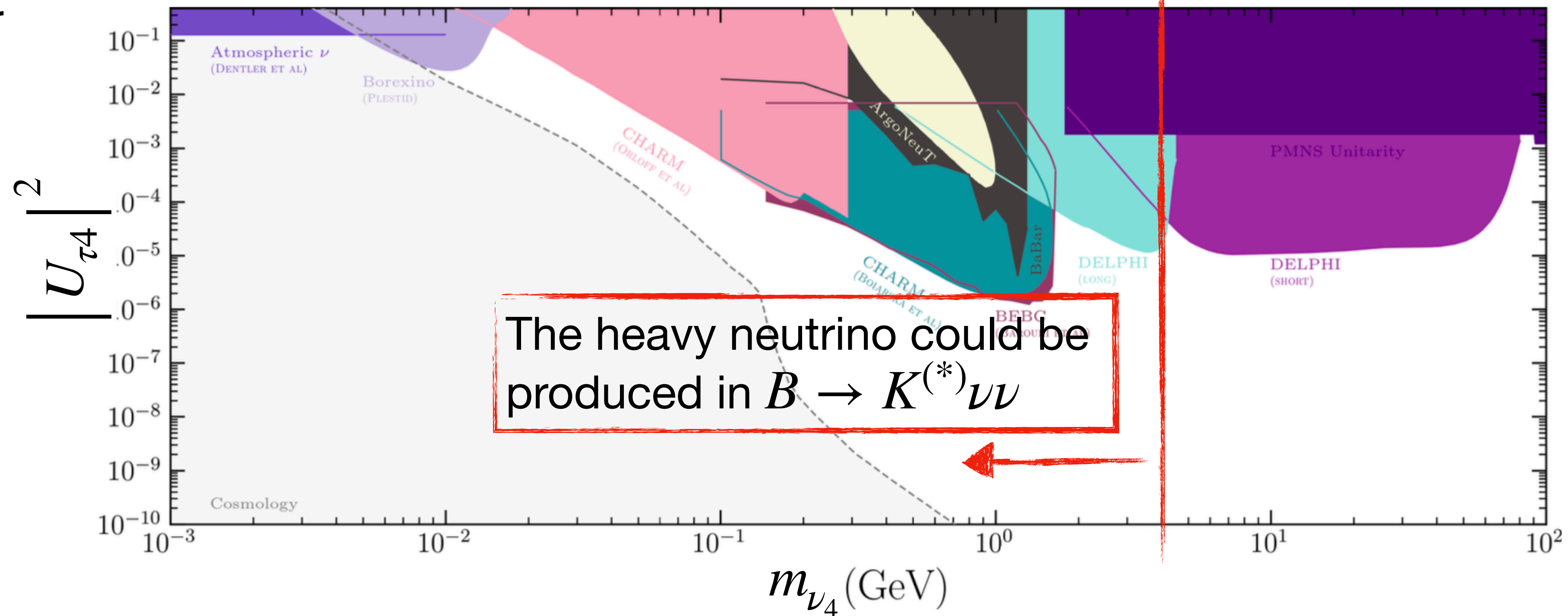
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E. Fernández-Martínez et al., arXiv:2304.06772

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$$N_R = \sum_{i=1}^4 U_{si}^* P_R n_i$$



**Need to include  $N_R$  in the EFT description!**

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the $\nu$ SMEFT

## Include a light RH neutrino field

Many more contributions when having a light RH neutrino

See T. Felkl *et al.*, arXiv:2111.04327  
& arXiv:2309.02940

L. Leal & SRA, work in progress

$$\mathcal{L}_{\nu\text{SMEFT}}^{(6)} \supset \frac{1}{\Lambda^2} \left\{ \begin{aligned} & \mathcal{C}_{Nd} (\bar{s}_R \gamma_\mu b_R) (\bar{N}_R \gamma^\mu N_R) + \mathcal{C}_{NQ} (\bar{s}_L \gamma_\mu b_L) (\bar{N}_R \gamma^\mu N_R) \\ & + [\mathcal{C}_{LNQd}]_i (\bar{s}_L b_R) (\bar{\nu}_{Li} N_R) - V_{cs} [\mathcal{C}_{LNQd}]_i (\bar{c}_L b_R) (\bar{\ell}_{Li} N_R) \\ & + [\mathcal{C}_{LNQdT}]_i (\bar{s}_L \sigma^{\mu\nu} b_R) (\bar{\nu}_{Li} \sigma_{\mu\nu} N_R) - V_{cs} [\mathcal{C}_{LNQdT}]_i (\bar{c}_L \sigma^{\mu\nu} b_R) (\bar{\ell}_{Li} \sigma_{\mu\nu} N_R) + h.c \end{aligned} \right\}$$

Correlation between  $b \rightarrow s\nu\nu$  and  $b \rightarrow c\tau\nu$

In the LEFT we find additional operators

$$\mathcal{L}^{b \rightarrow s\nu\nu} = \frac{4G_F}{\sqrt{2}} \lambda_t \sum_a C_a \mathcal{O}_a + h.c. \quad \begin{aligned} \mathcal{O}_{V_{R(L)}} &= (\bar{s}_L \gamma_\mu b_L) (n_i \gamma^\mu (1 \pm \gamma_5) n_j) \\ \mathcal{O}_{S_{R(L)}} &= (\bar{s}_L b_R) (n_i (1 \pm \gamma_5) n_j) \\ \mathcal{O}_T &= (\bar{s}_L \sigma_{\mu\nu} b_R) (n_i \sigma^{\mu\nu} n_j) \end{aligned}$$

Also different kinematics when final state neutrino is massive  $\rightarrow m_{\nu_4} \neq 0$

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the $\nu$ SMEFT

## Include a light RH neutrino field

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See T. Felkl *et al.*, arXiv:2111.04327  
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Correlation between  $b \rightarrow s \nu \nu$  and  $b \rightarrow c \tau \nu$

Going from the  $\nu$ SMEFT to the LEFT with massive neutrinos

$$\nu_{L\alpha} = \sum_{i=1}^4 U_{\alpha i} P_L n_i$$

$$N_R = \sum_{i=1}^4 U_{si}^* P_R n_i$$

$$\mathcal{L}_{\nu\text{SMEFT}}^{(6)} \sim \frac{1}{\Lambda^2} C_{Nd} (\bar{s}_L \gamma_\mu b_L) (\bar{N}_R \gamma^\mu (1 + \gamma_5) N_R)$$

$$\mathcal{L}_{\text{LEFT}}^{(6)} \sim \frac{1}{\Lambda^2} \sum_{i,j} U_{si} C_{Nd} U_{sj}^* (\bar{s}_L \gamma_\mu b_L) (\bar{n}_i \gamma^\mu (1 + \gamma_5) n_j)$$

# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the $\nu$ SMEFT

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Correlation between  $b \rightarrow s \nu \nu$  and  $b \rightarrow c \tau \nu$

Going from the  $\nu$ SMEFT

**Neglect active-heavy mixing!**

$$\nu_{L\alpha} \simeq \sum_{i=1}^3 U_{\alpha i} P_L n_i$$

$$N_R \simeq P_R n_4$$

$$\mathcal{L}_{\nu\text{SMEFT}}^{(6)} \sim \frac{1}{\Lambda^2} C_{Nd} (\bar{s}_L \gamma_\mu b_L) (\bar{N}_R \gamma^\mu (1 + \gamma_5) N_R)$$

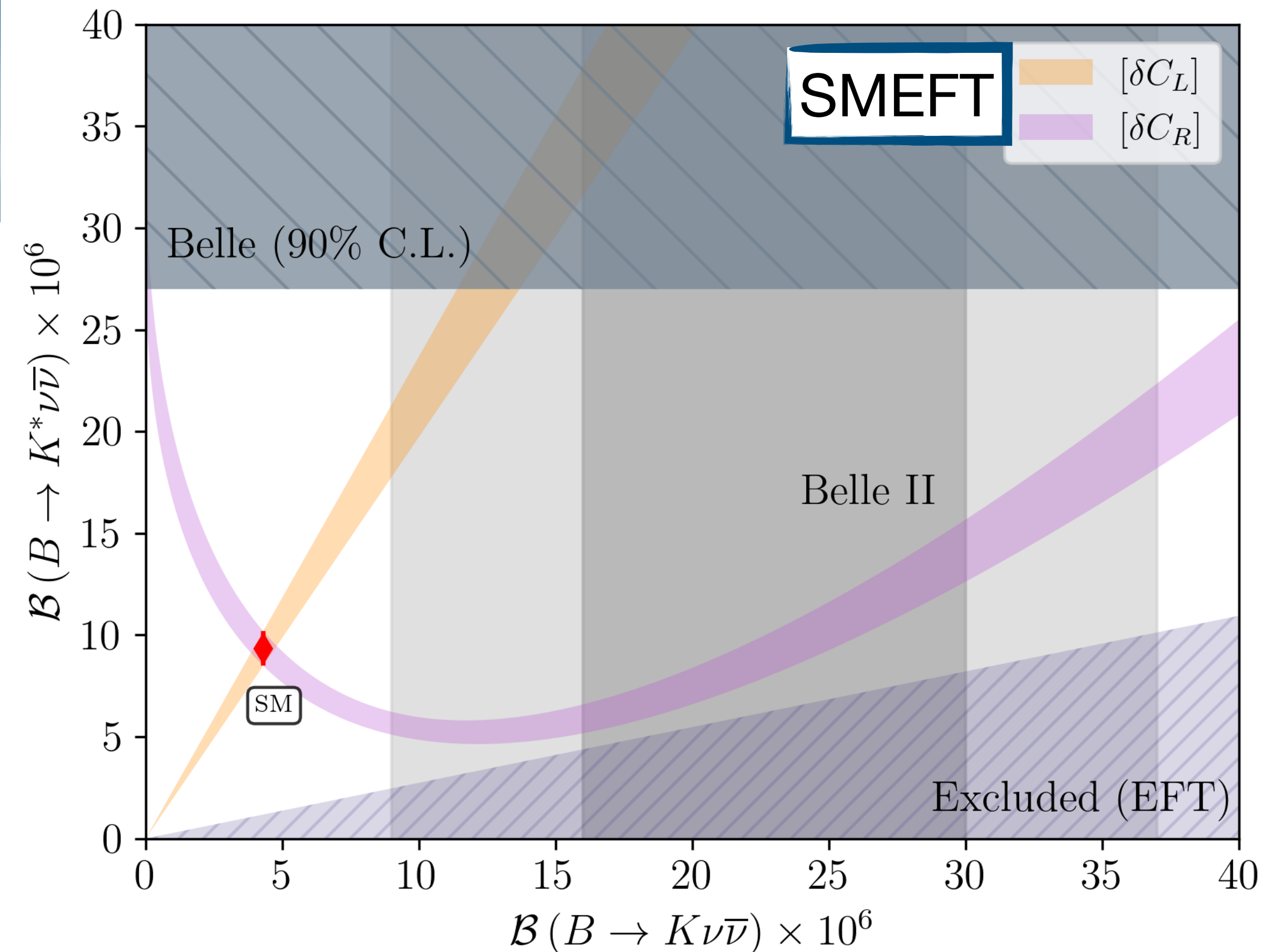
$$\mathcal{L}_{\text{LEFT}}^{(6)} \sim \frac{1}{\Lambda^2} C_{Nd} (\bar{s}_L \gamma_\mu b_L) (\bar{n}_4 \gamma^\mu (1 + \gamma_5) n_4)$$

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## Can we tell apart between SMEFT and $\nu$ SMEFT?

For vector and tensor operators with (**massless**)  
RH neutrinos the EFT bound still applies

$$\frac{\mathcal{B}(B \rightarrow K^{*} \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K^{*} \nu \bar{\nu})_{\text{SM}}} \geq \frac{\mathcal{B}(B \rightarrow K \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K \nu \bar{\nu})_{\text{SM}}} \left( 1 - \frac{\eta_V^{K^{*}}}{4} \right)$$

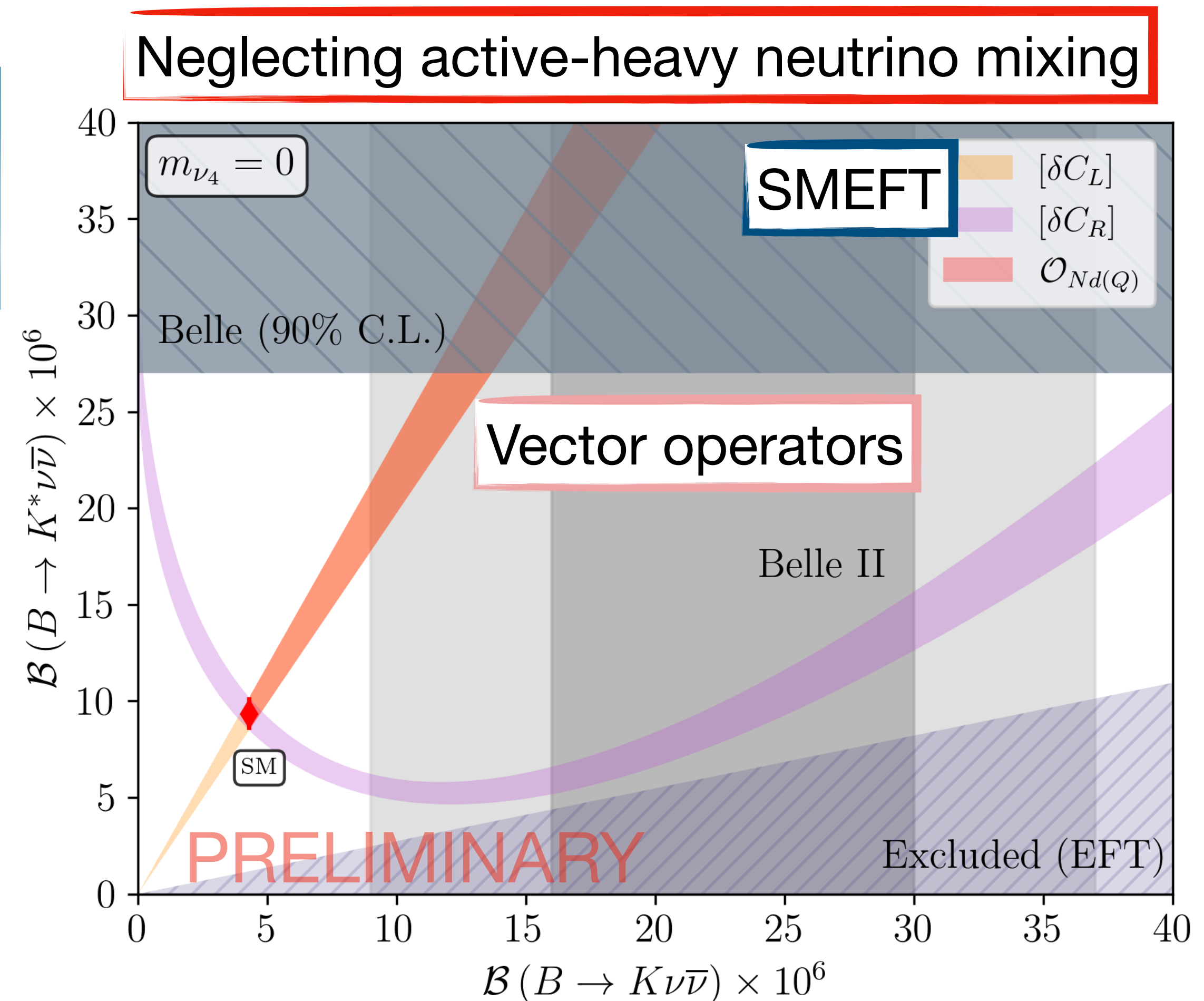


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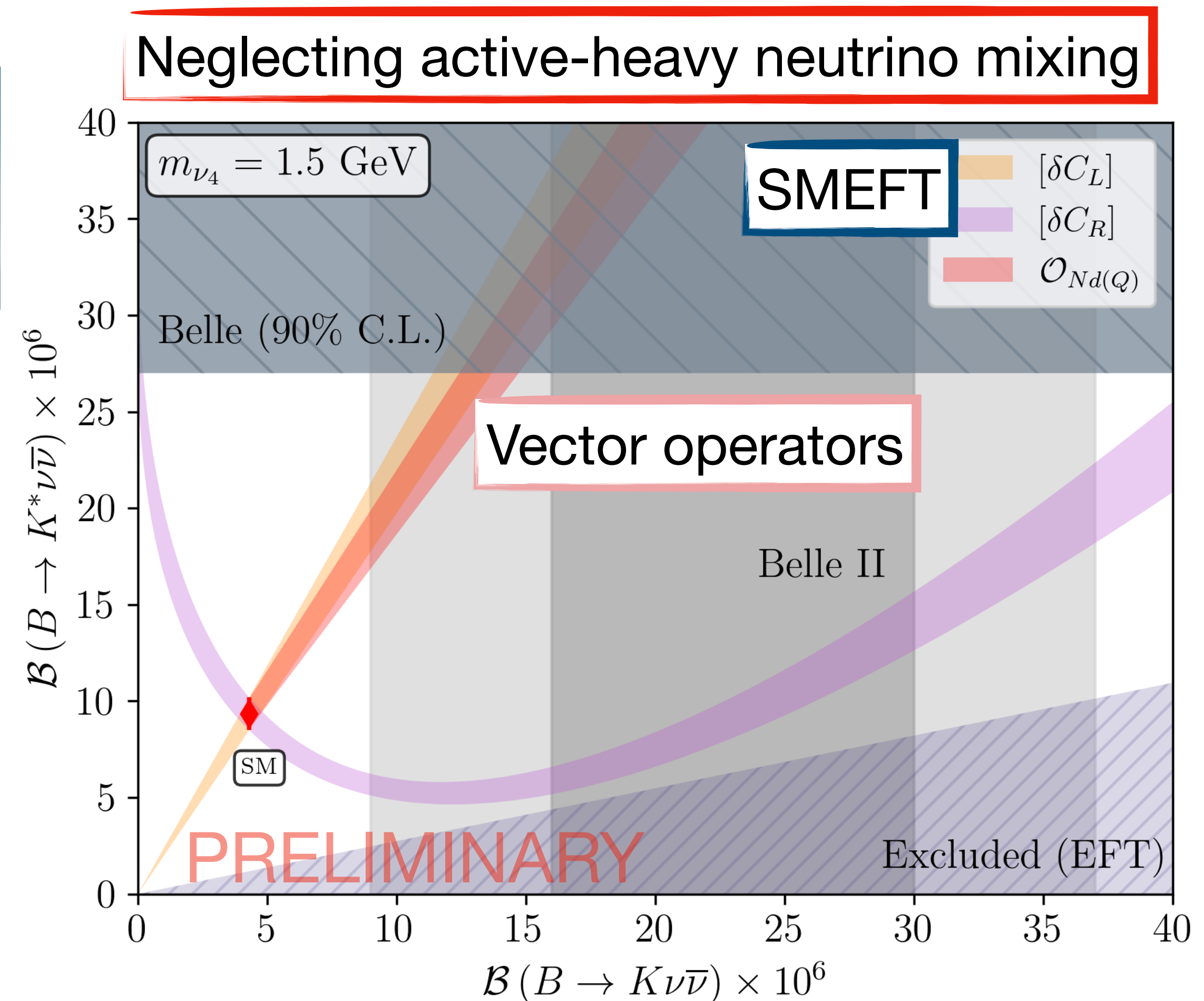
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Having  $m_{\nu_4} \neq 0$  suppresses  $\mathcal{B}(B \rightarrow K^* \nu \bar{\nu})$



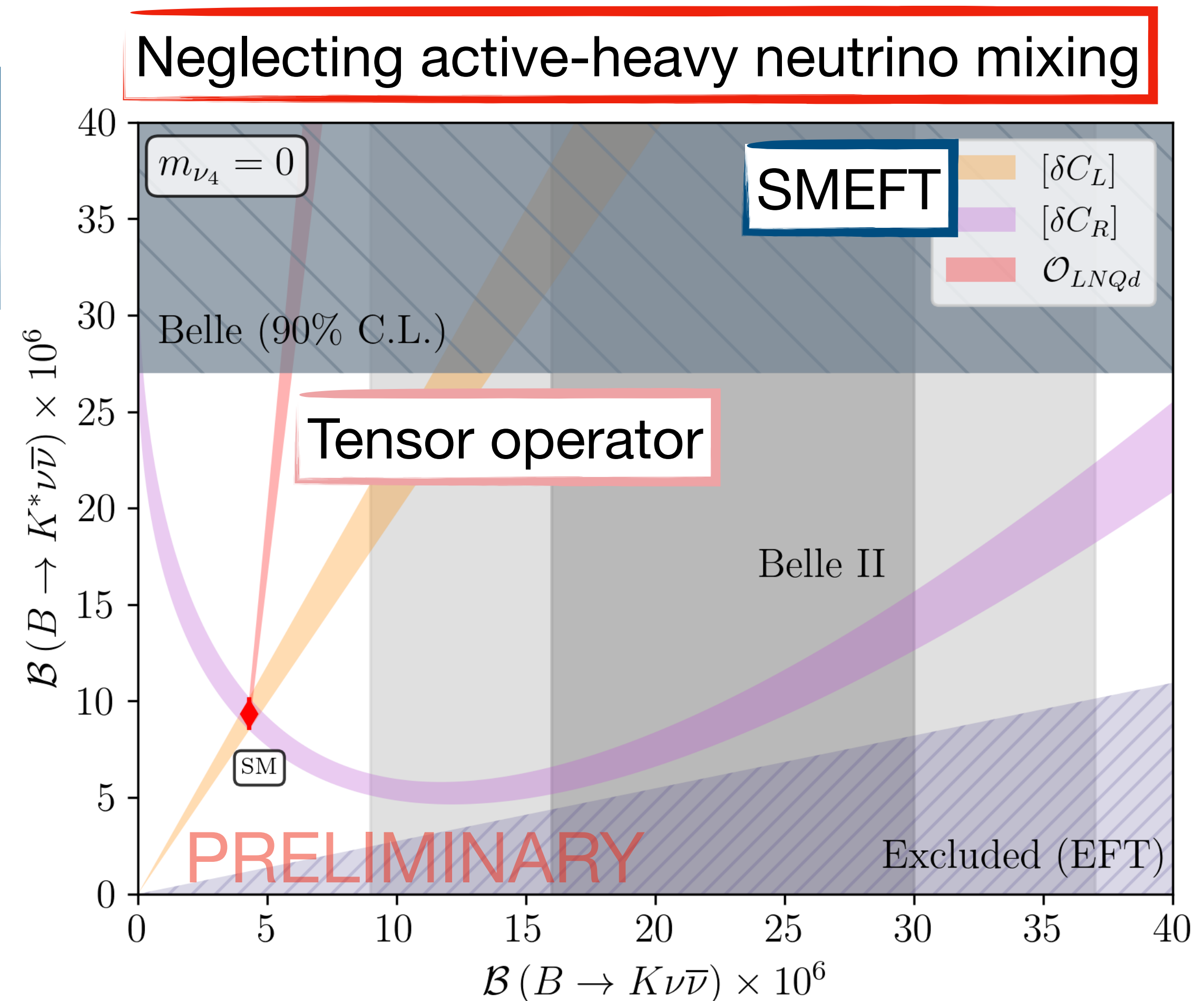
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Only for  $m_{\nu_4} \simeq (m_B - m_{K^{*}})$  the  
tensor operator is not ruled out





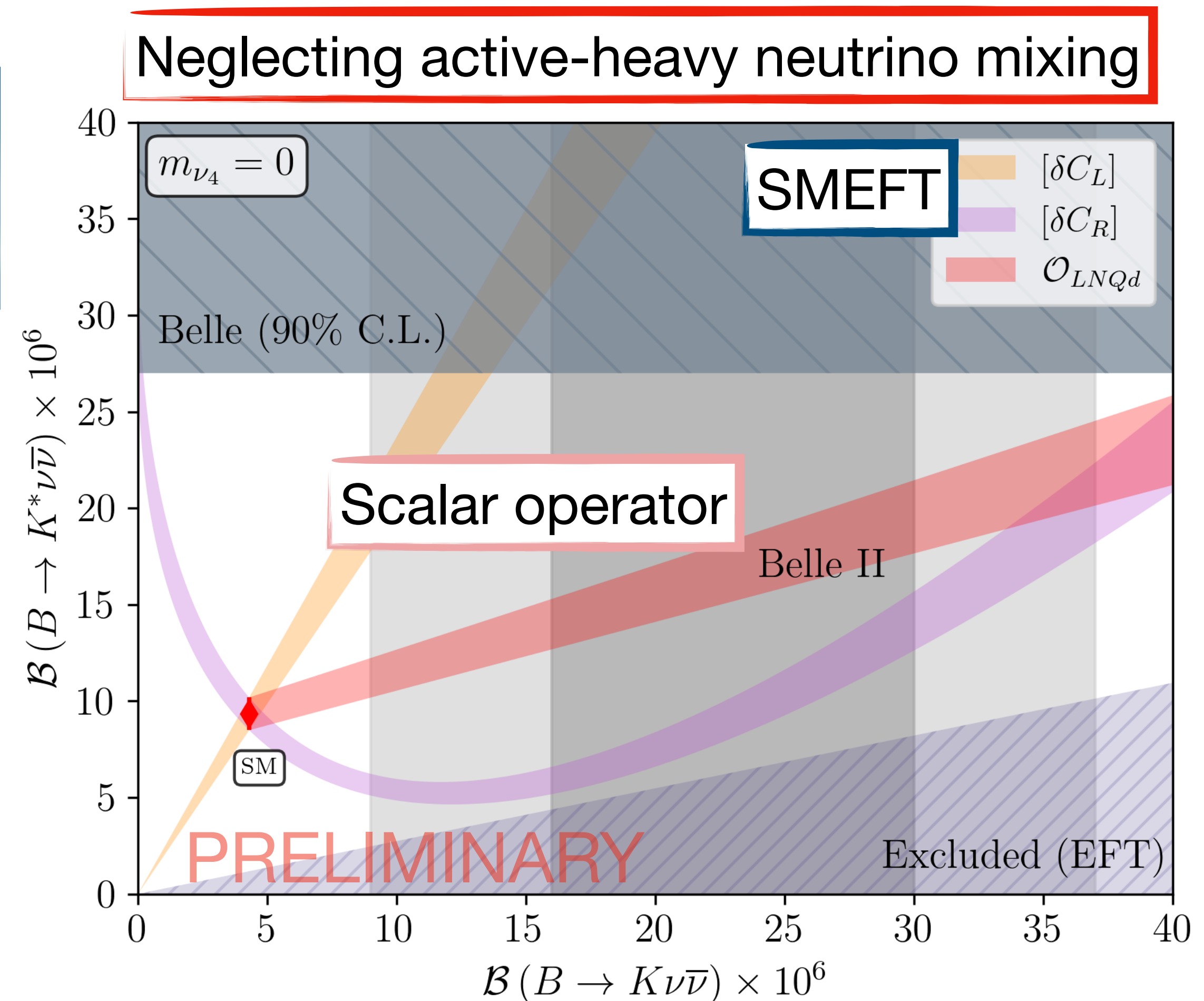
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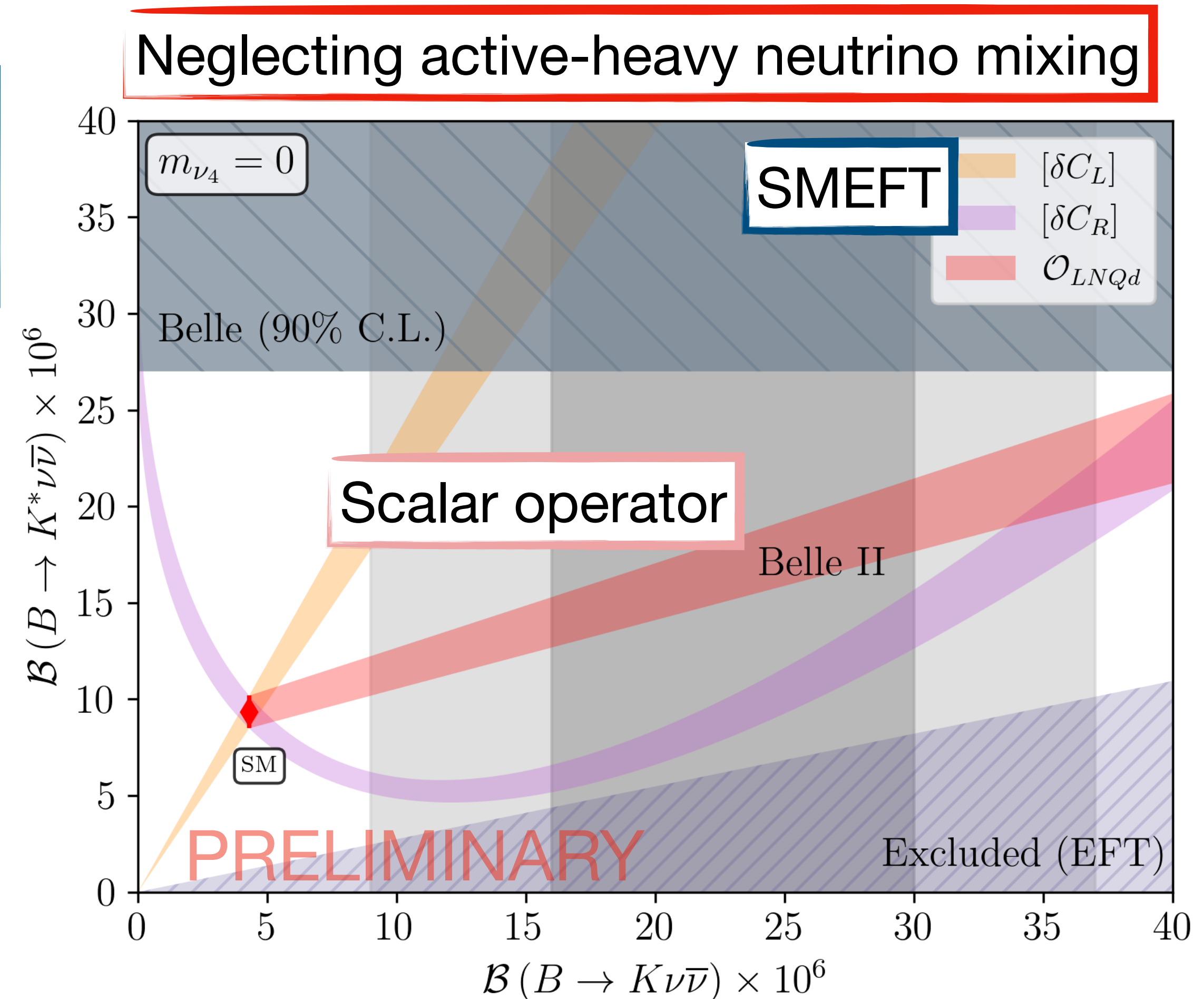
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Only realized when

$$\frac{\mathcal{B}(B \rightarrow K \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K \nu \bar{\nu})_{\text{SM}}} \geq 11.4(5)$$

**Experimentally excluded**



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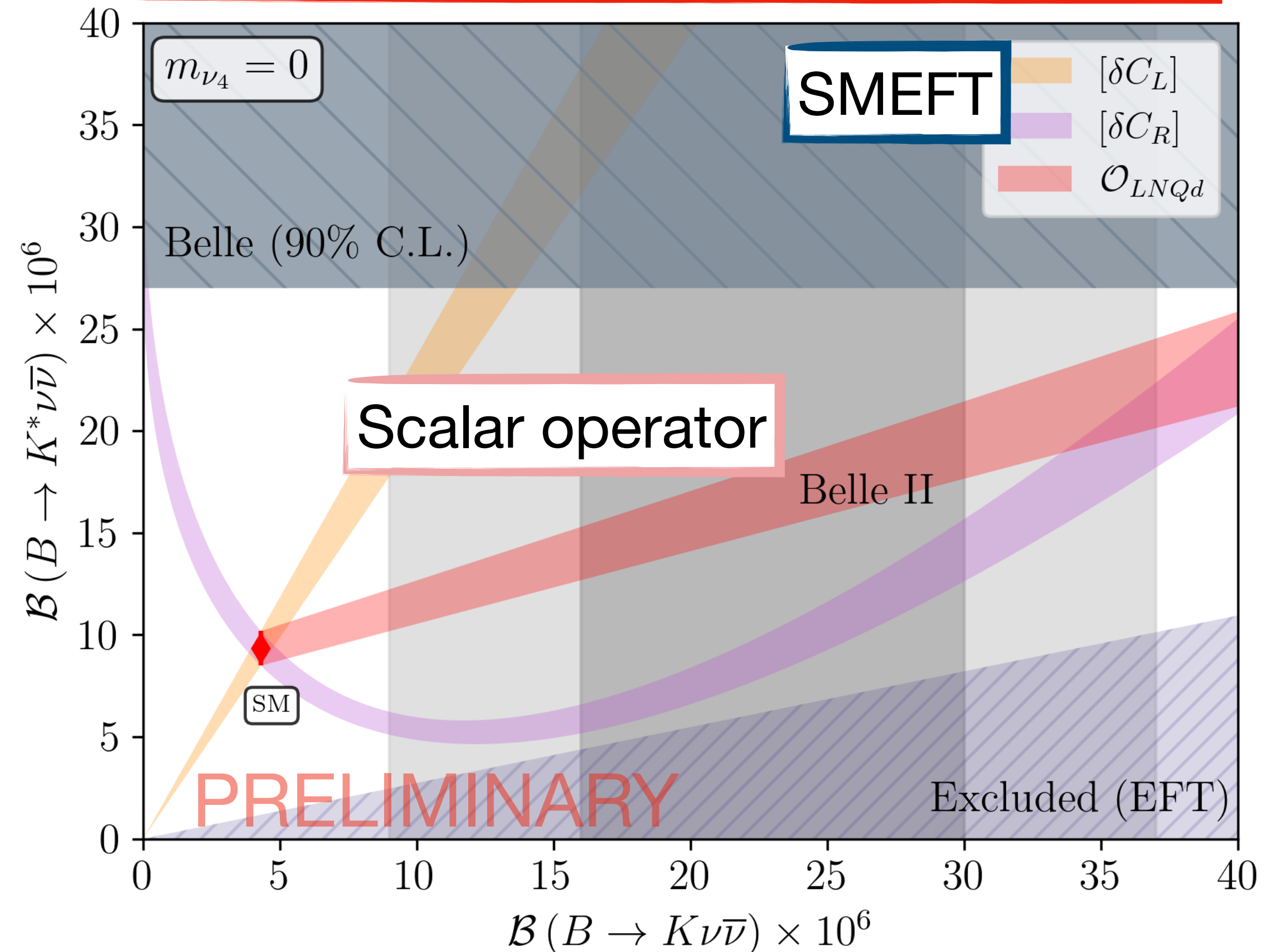
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$$[\mathcal{C}_{LNQd}]_i (\bar{s}_L b_R) (\bar{\nu}_{Li} N_R) - V_{cs} [\mathcal{C}_{LNQd}]_i (\bar{c}_L b_R) (\bar{\ell}_{Li} N_R)$$

Effect of non-zero  $U_{\alpha 4}$ ?

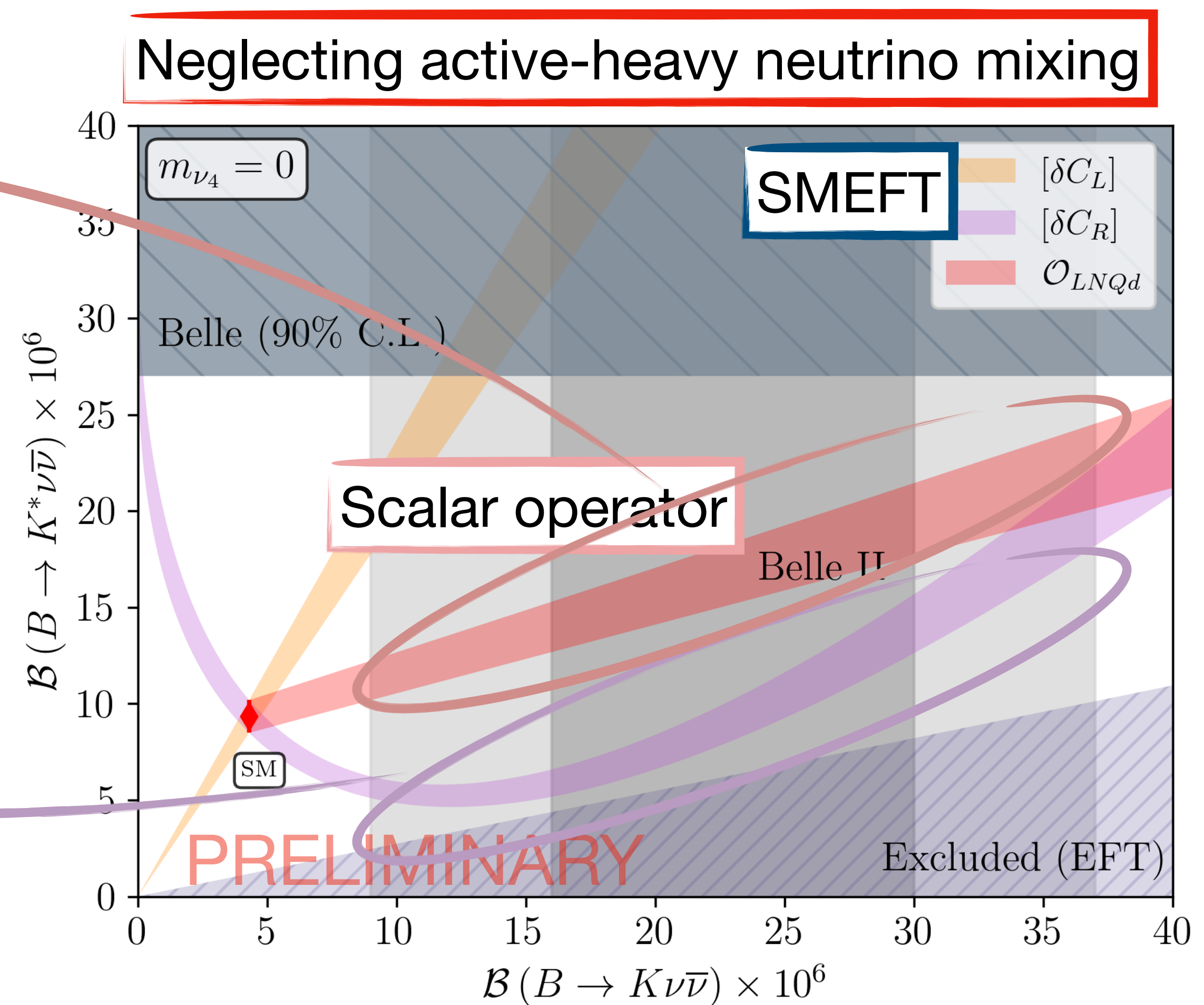
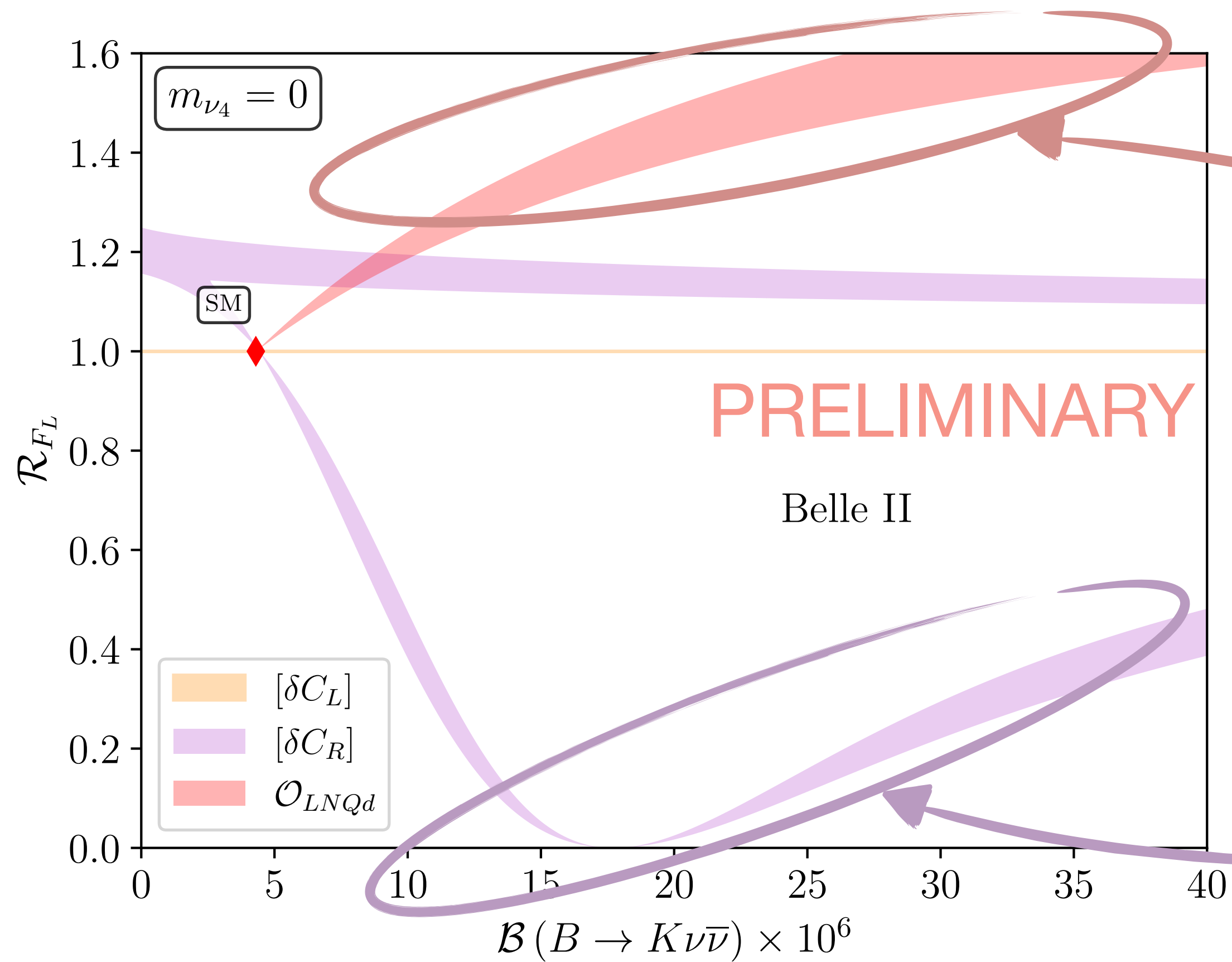
Impact on  $R_D^{(*)}$

Neglecting active-heavy neutrino mixing



# $B \rightarrow K^{(*)} \nu \bar{\nu}$ in the $\nu$ SMEFT

Can we tell apart between SMEFT and  $\nu$ SMEFT?



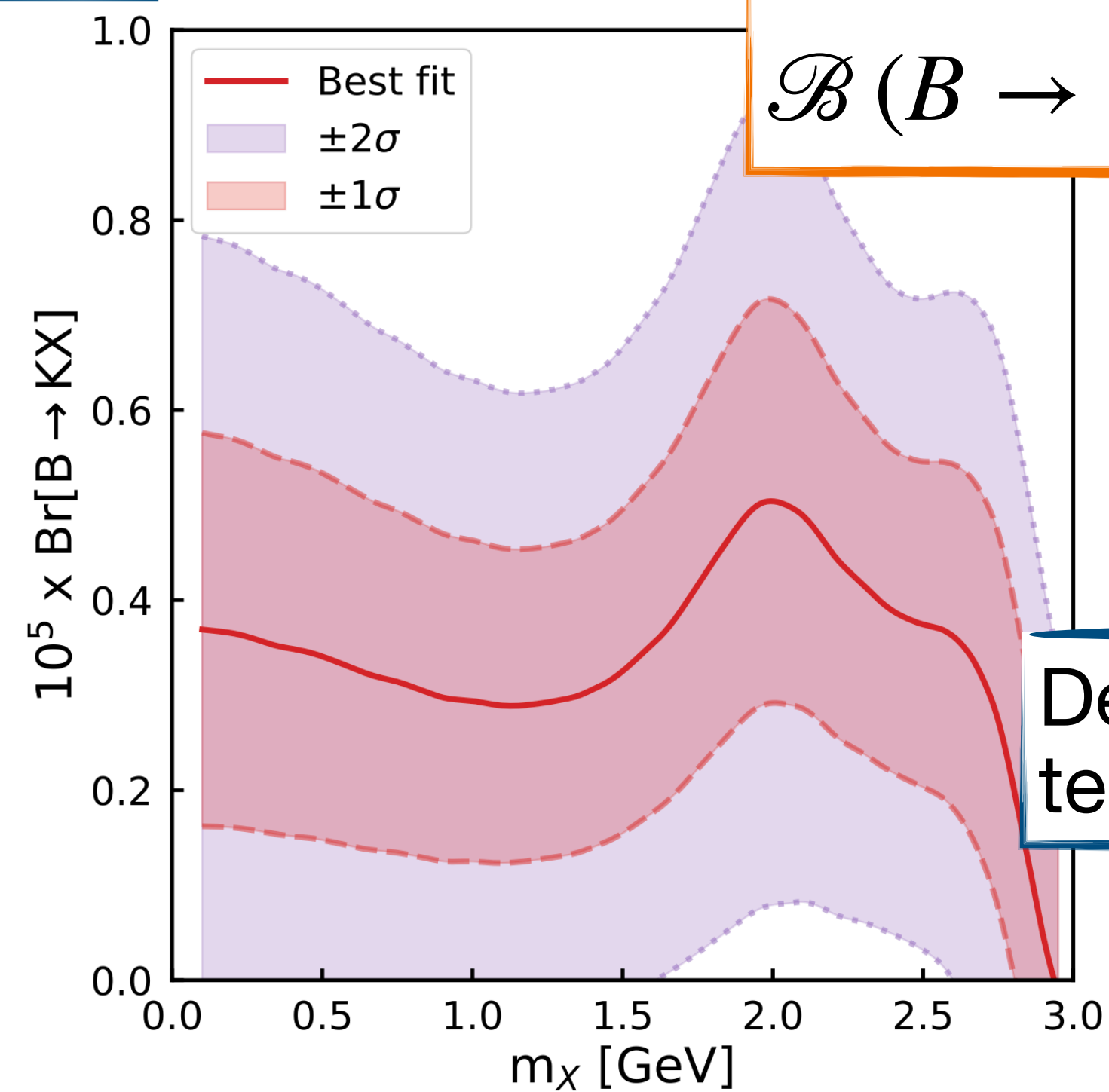
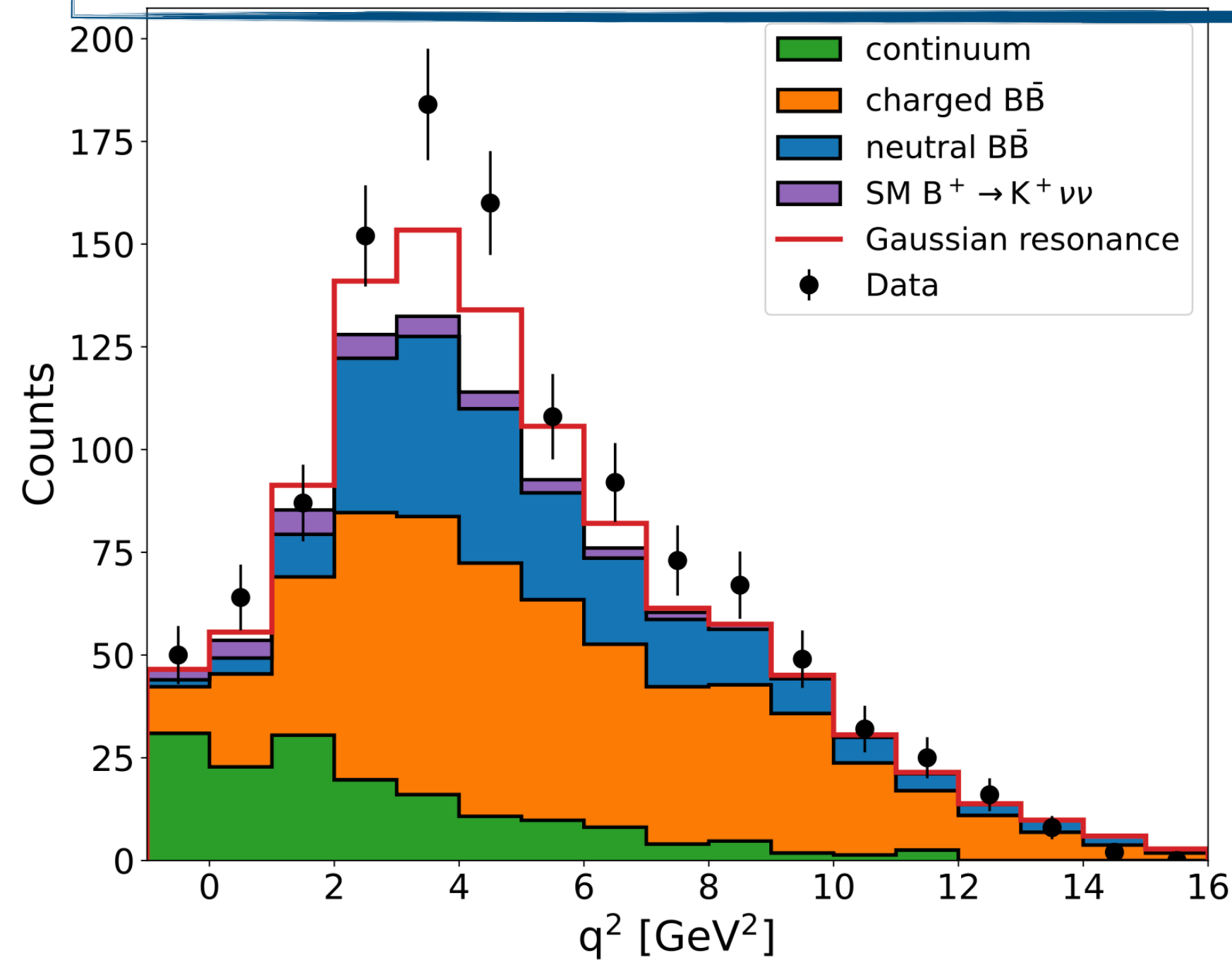
# Light mediators?

## Effect of a light vector mediator

W. Altmannshofer *et al.*, arXiv:2311.14629

The excess is compatible with  $B \rightarrow KX(\rightarrow \nu\nu)$  with  $X$  produced on-shell

Resonance in the  $q^2$ -distribution at  $q^2 \simeq m_X^2$



Best fit:  $m_X \simeq 2$  GeV

$$\mathcal{B}(B \rightarrow KX) = (5.1 \pm 2.1) \times 10^{-6}$$

Significance of  $2.4\sigma$

Dedicated searches could test this hypothesis!

# Summary and outlook

# Conclusions

$$\mathcal{B} (B^\pm \rightarrow K^\pm \nu \bar{\nu}) \Big|_{\text{SM}} = (4.44 \pm 0.30) \times 10^{-6}$$

Theoretically cleaner than  $B \rightarrow K^{(*)} \mu \mu$

Two main uncertainties from the theory side:

- CKM matrix element determination: **Inclusive vs exclusive**  $V_{cb}$  Can change prediction by  $\mathcal{O}(10\%)$

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Eventually need to match the expected sensitivity by Belle-II

$$\mathcal{B} (B^+ \rightarrow K^+ \nu \bar{\nu}) \Big|_{\text{Belle-II}} = (2.3 \pm 0.7) \times 10^{-5}$$

$$\mathcal{L}^{b \rightarrow s \nu \nu} = \frac{4G_F}{\sqrt{2}} \lambda_t \sum_{i,j} (C_L^{\nu_i \nu_j} \mathcal{O}_L^{\nu_i \nu_j} + C_R^{\nu_i \nu_j} \mathcal{O}_R^{\nu_i \nu_j}) + h.c.$$

Contributions from **only**  $C_L^{\nu_i \nu_j}$  are tightly **constrained by Belle**

Contributions from **only**  $C_R^{\nu_i \nu_j}$  can explain  $B \rightarrow K \nu \bar{\nu}$ , correlated with  $\mathcal{B} (B \rightarrow K^* \nu \bar{\nu})$  and  $F_L$

# Conclusions

## SMEFT

- Couplings to  $\mu$  constrained by  $B_s \rightarrow \mu\mu$
- NP couplings allowed in  $\tau$  leptons:

$$\frac{\mathcal{B}(B_s \rightarrow \tau\tau)_{\text{BSM}}}{\mathcal{B}(B_s \rightarrow \tau\tau)_{\text{SM}}} \sim 10$$

## $\nu$ SMEFT

- Scalar and tensor operators also contribute
- One can always suppress the NP effect on  $B \rightarrow K^* \nu\nu$  with  $m_{\nu_4} \sim (m_B - m_{K^*})$

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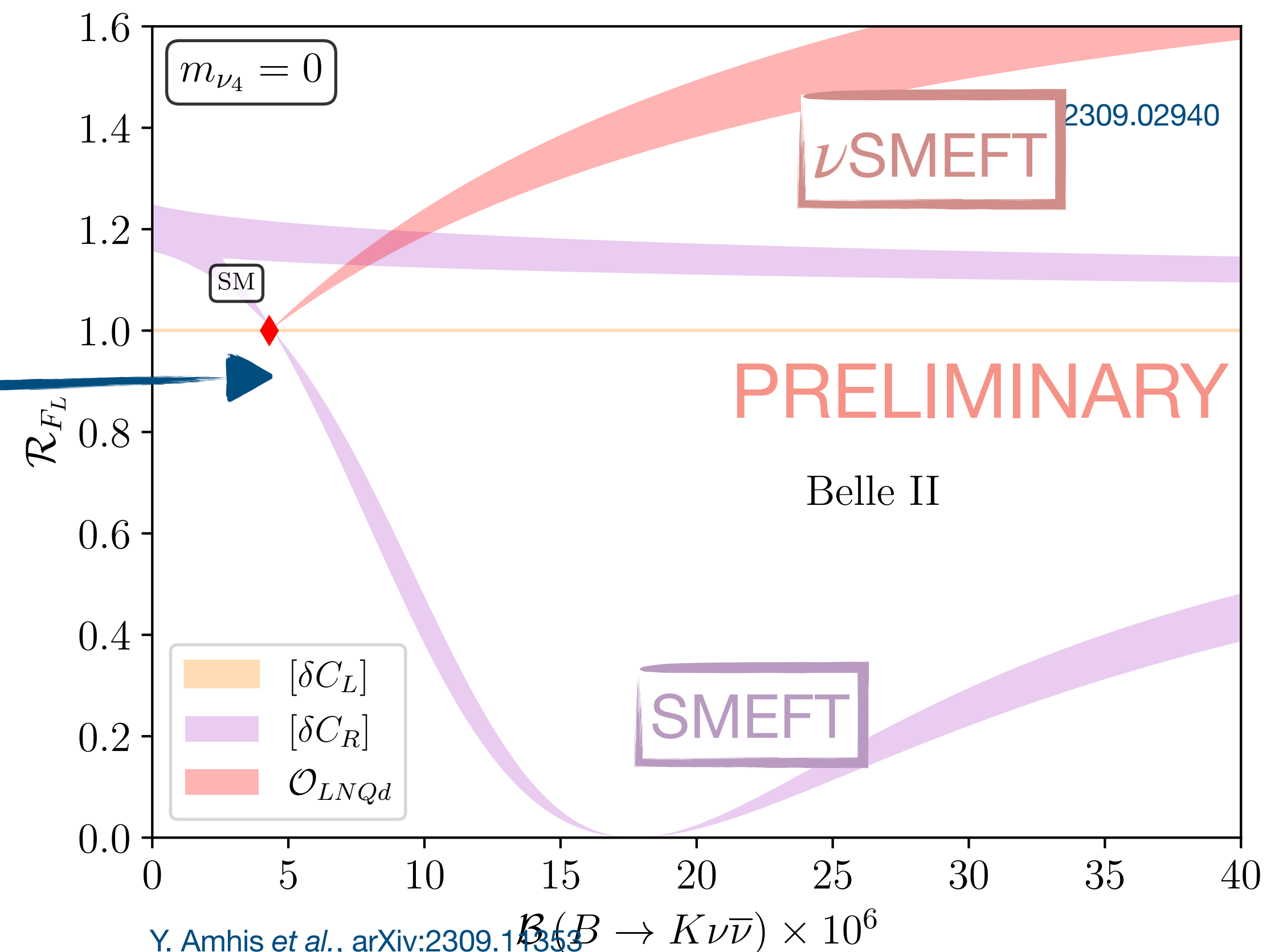
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- Measurement of  $F_L$
- $B_s \rightarrow \nu\nu$
- $q^2$ -distribution of events
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- Complementary processes:  $B^0 -$

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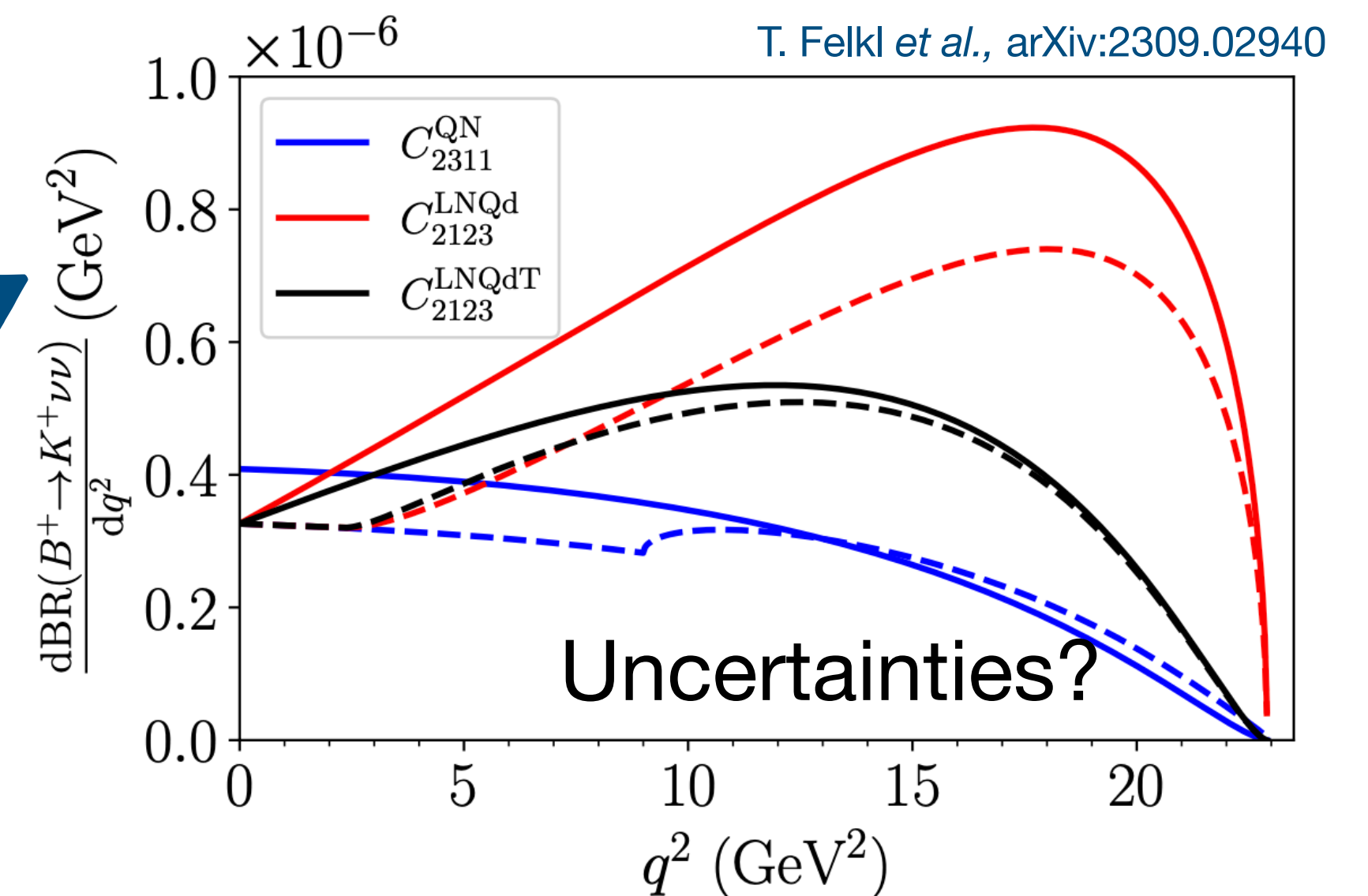
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T. Felkl et al., arXiv:2309.02940

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Thank you!

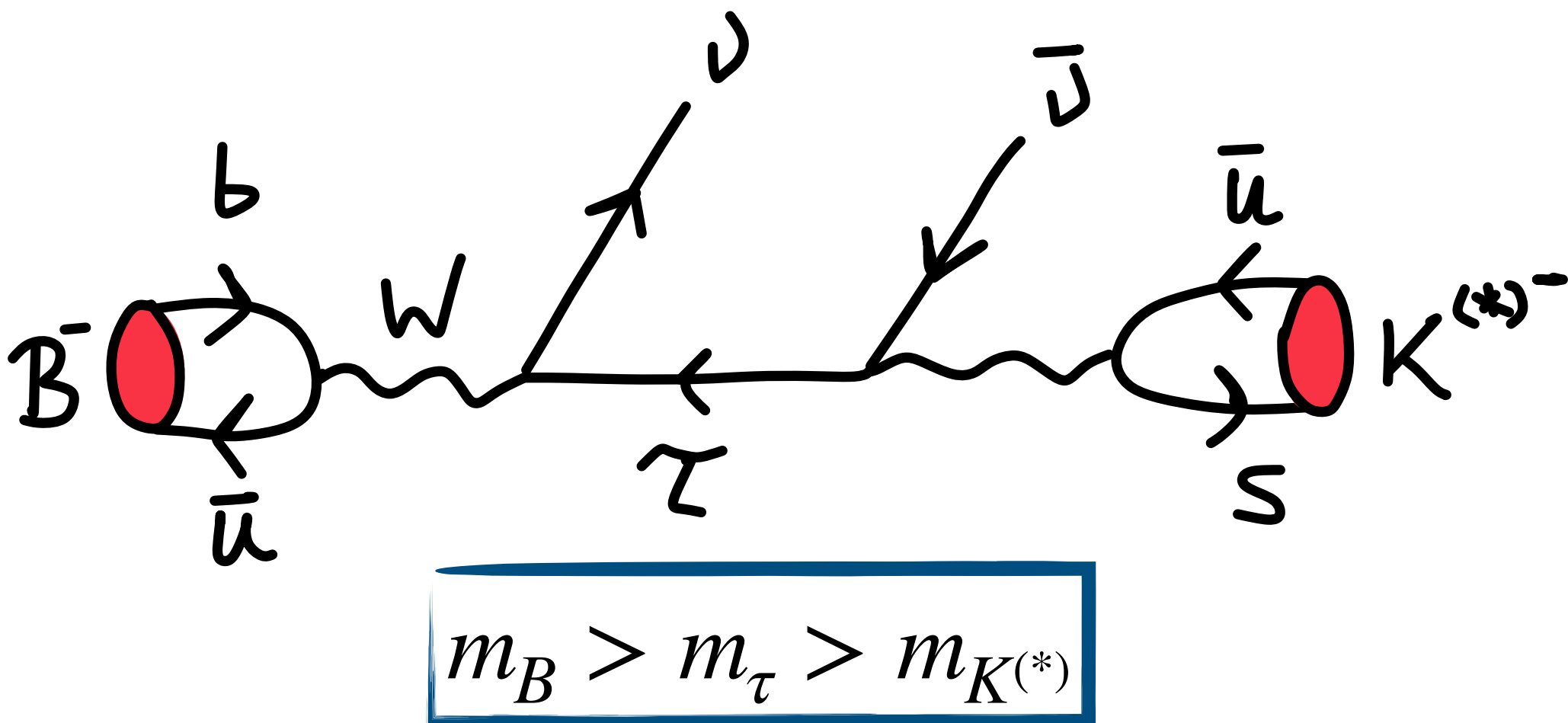
**Back-up slides**

# Tree-level contribution

$$B^{\pm} \rightarrow K^{\pm(*)} \nu \bar{\nu}$$

J. F. Kamenik & C. Smith, arXiv:0908.1174

Charged meson decay modes have a **tree-level** contribution from the **annihilation to an intermediate  $\tau$**



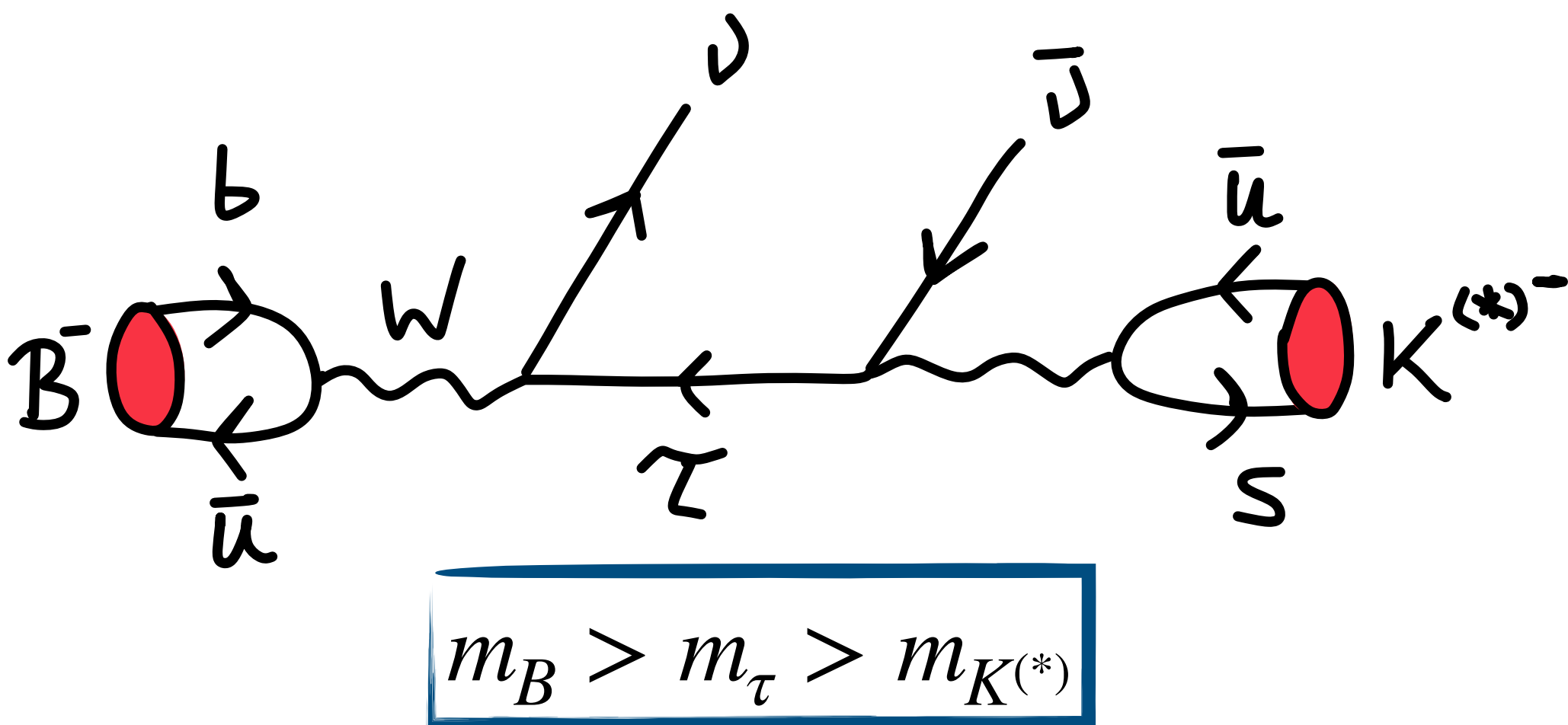


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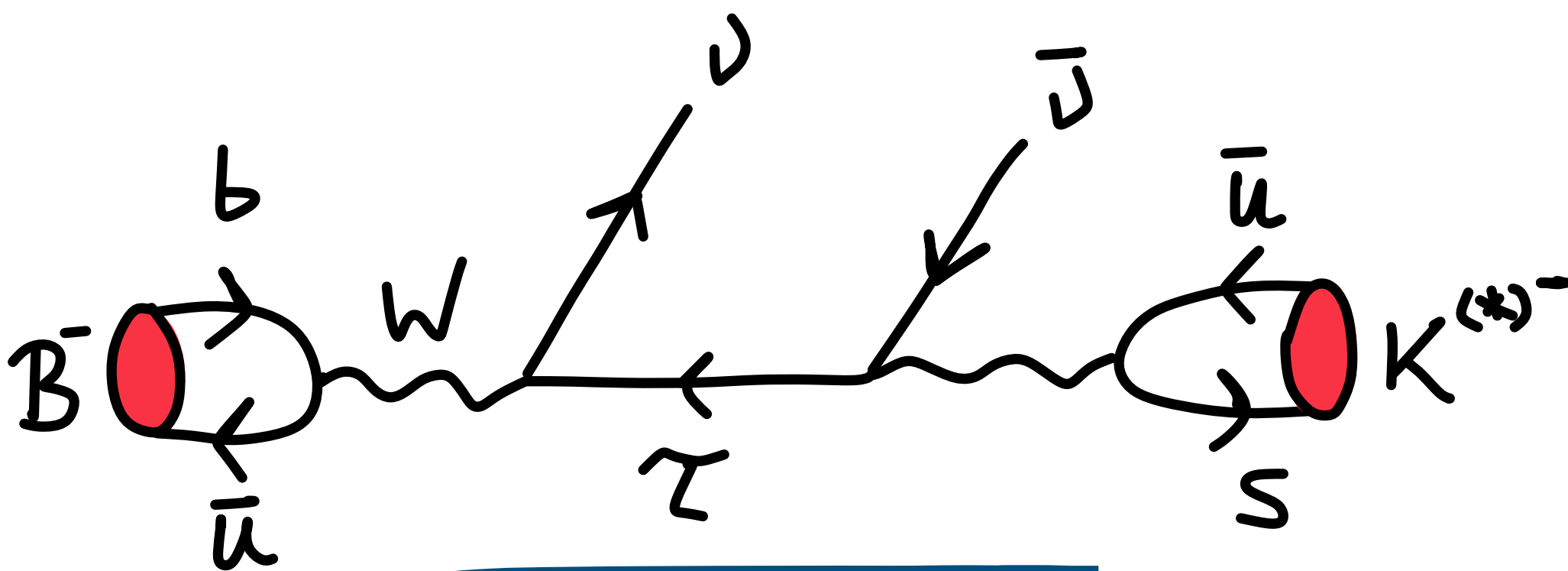
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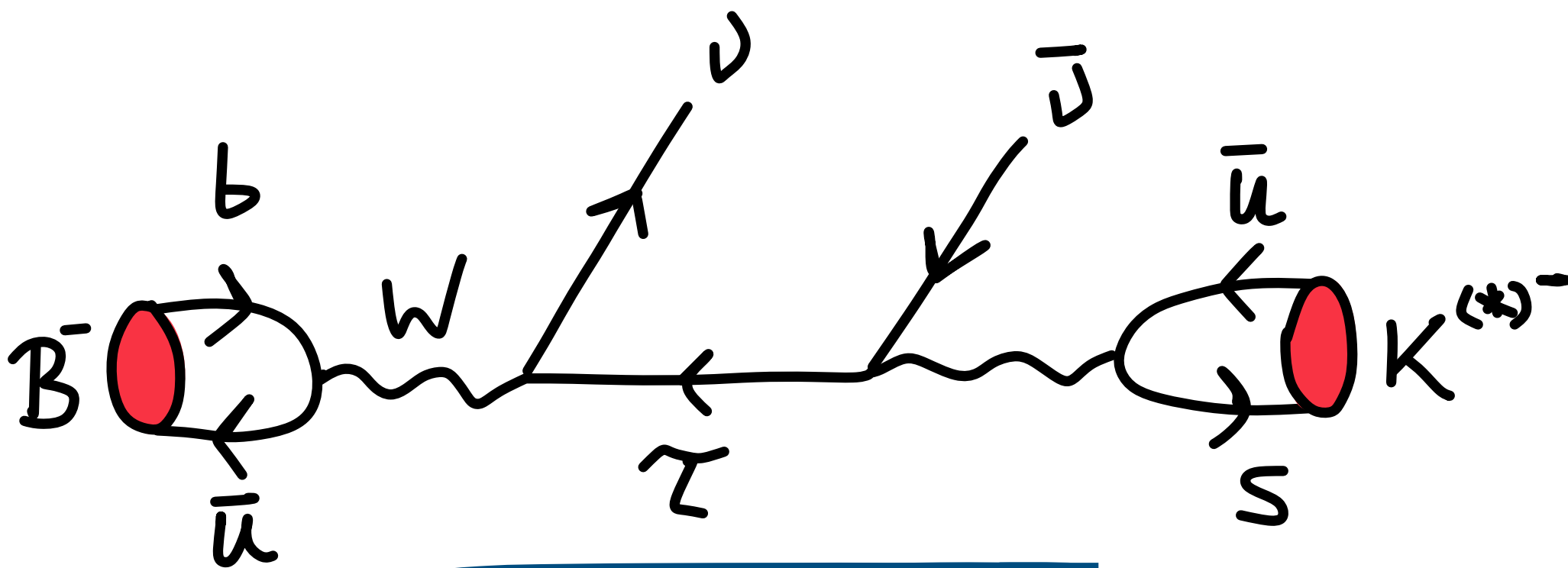
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Belle-II can in principle disentangle these two contributions

# Reduction of uncertainties

## Ratio between low and high- $q^2$ regions

D. Becirevic, G. Piazza & O. Sumensari, arXiv:2301.06990

Binned information would allow one to study the following CKM-free ratio

$$r_{\text{low/high}} \equiv \frac{\mathcal{B} (B \rightarrow K^{(*)} \nu \bar{\nu})_{\text{low-}q^2}}{\mathcal{B} (B \rightarrow K^{(*)} \ell \ell)_{\text{high-}q^2}}$$

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Take bins  $(0, q_{\text{max}}^2/2)$  and  $(q_{\text{max}}^2/2, q_{\text{max}}^2)$ :

$$r_{\text{low/high}} = 1.91 \pm 0.06$$

Using previous FLAG average

$$r_{\text{low/high}} = 2.15 \pm 0.26$$

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Partial branching fractions integrated in the same  $q^2$  range

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Using perturbative calculations for the  $c\bar{c}$ -loops one finds

$$\mathcal{R}_K^{(\nu/\mu)}[1.1, 6] = 7.58 \pm 0.04$$

$\lesssim \mathcal{O}(1\%)$  uncertainty

$$\mathcal{R}_{K^*}^{(\nu/\mu)}[1.1, 6] = 8.6 \pm 0.3$$

$\lesssim \mathcal{O}(5\%)$  uncertainty

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But we can use this ratio to extract  $C_9$ !

$$\frac{1}{\mathcal{R}_K^{\nu/\mu}[1.1, 6]} \Big|_{\text{SM}} \simeq \left[ 7.5 - 0.45 C_9^{\text{eff}} + 0.42 \cdot (C_9^{\text{eff}})^2 \right]$$

# Correlations between observables

## Coupling to muons only

One can relate  $B \rightarrow K\nu\bar{\nu}$  with  $B_s \rightarrow \mu\mu$

$$\mathcal{B}(B_s \rightarrow \mu\mu) = (3.35 \pm 0.27) \times 10^{-9}$$

ATLAS, arXiv:1812.03017  
LHCb, arXiv:2108.09283  
CMS, arXiv:2212.10311

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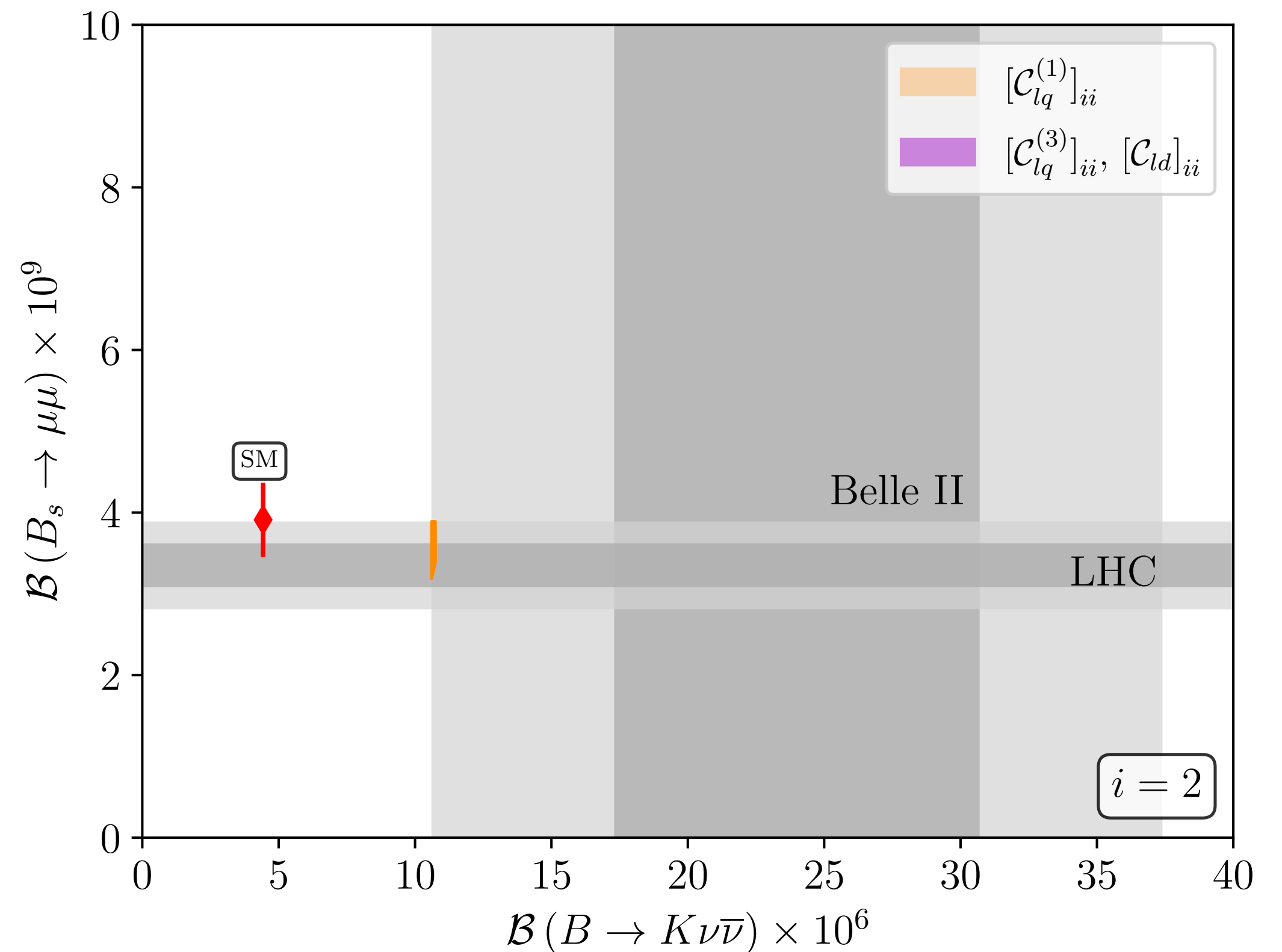
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$$\mathcal{O}_{10} = \frac{e^2}{(4\pi)^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

ATLAS, arXiv:1812.03017  
LHCb, arXiv:2108.09283  
CMS, arXiv:2212.10311

$$\delta C_{10}^{l_i l_i} = \frac{\pi}{\alpha_{\text{em}} \lambda_t} \frac{v^2}{\Lambda^2} \left\{ [C_{ld}]_{ii} - [C_{lq}^{(1)}]_{ii} - [C_{lq}^{(3)}]_{ii} \right\}$$



# Correlations between observables

## Coupling to muons only

One can relate  $B \rightarrow K\nu\bar{\nu}$  with  $B_s \rightarrow \mu\mu$

$$\mathcal{B}(B_s \rightarrow \mu\mu) = (3.35 \pm 0.27) \times 10^{-9}$$

$$\mathcal{O}_{10} = \frac{e^2}{(4\pi)^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

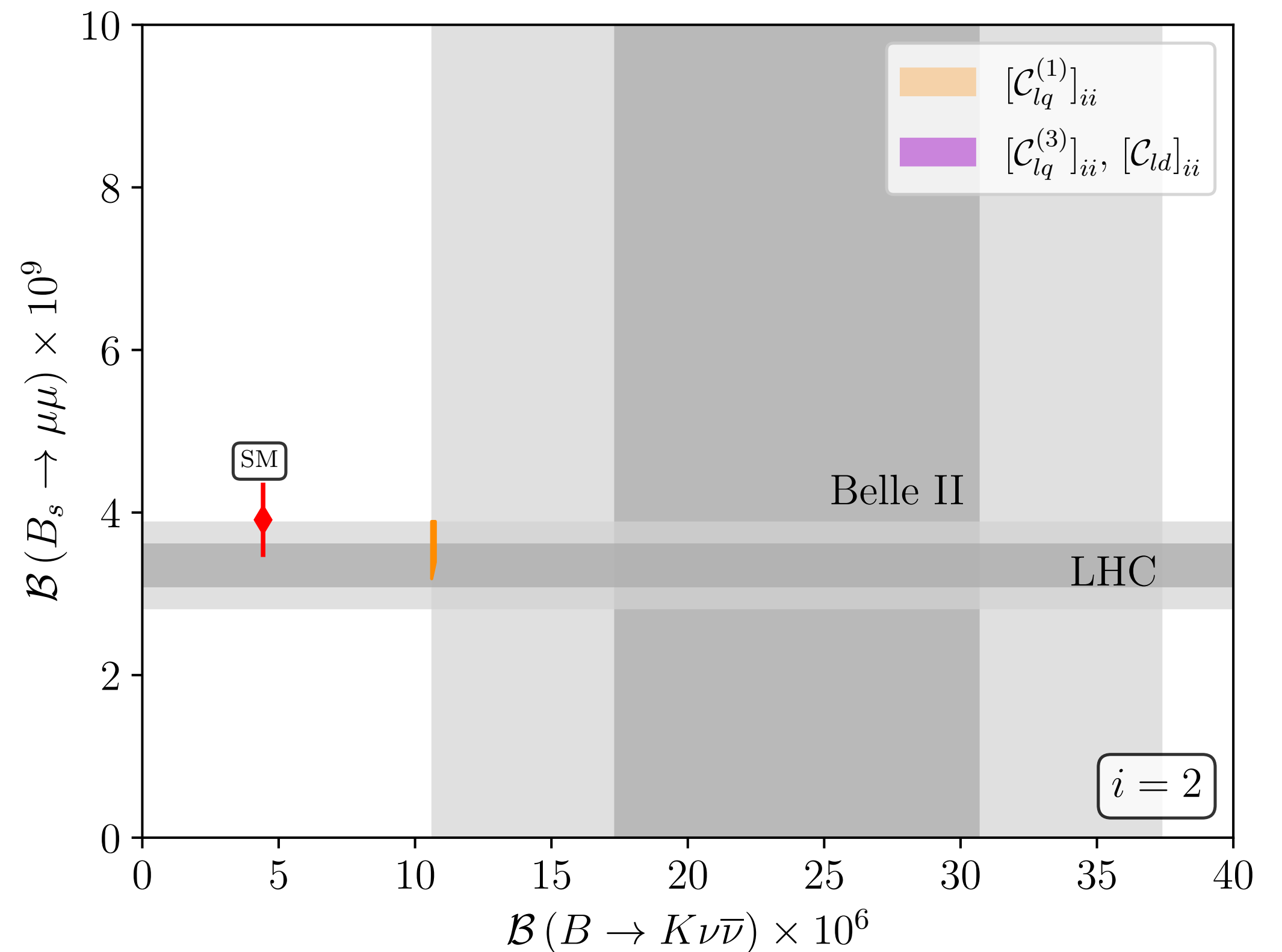
ATLAS, arXiv:1812.03017  
LHCb, arXiv:2108.09283  
CMS, arXiv:2212.10311

$$\delta C_{10}^{l_i l_i} = \frac{\pi}{\alpha_{\text{em}} \lambda_t} \frac{v^2}{\Lambda^2} \left\{ [C_{ld}]_{ii} - [C_{lq}^{(1)}]_{ii} - [C_{lq}^{(3)}]_{ii} \right\}$$

Note that one could also use  $R_{K^{(*)}}$  now as well as a constrain

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu\mu)}{\mathcal{B}(B \rightarrow K^{(*)} ee)}$$

**NP coupled to muons cannot explain Belle-II**



# Correlations between observables

## Coupling to tau leptons

Can we introduce NP to simultaneously explain the Belle-II result and  $R_D^{(*)}$ ?

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)}\ell\bar{\nu})}, \text{ with } \ell = e, \mu$$

HFLAV, arXiv:2206.07501

$$R_{D^{(*)}}^{\text{exp}}/R_{D^{(*)}}^{\text{SM}} = 1.16 \pm 0.05$$

# Correlations between observables

## Coupling to tau leptons

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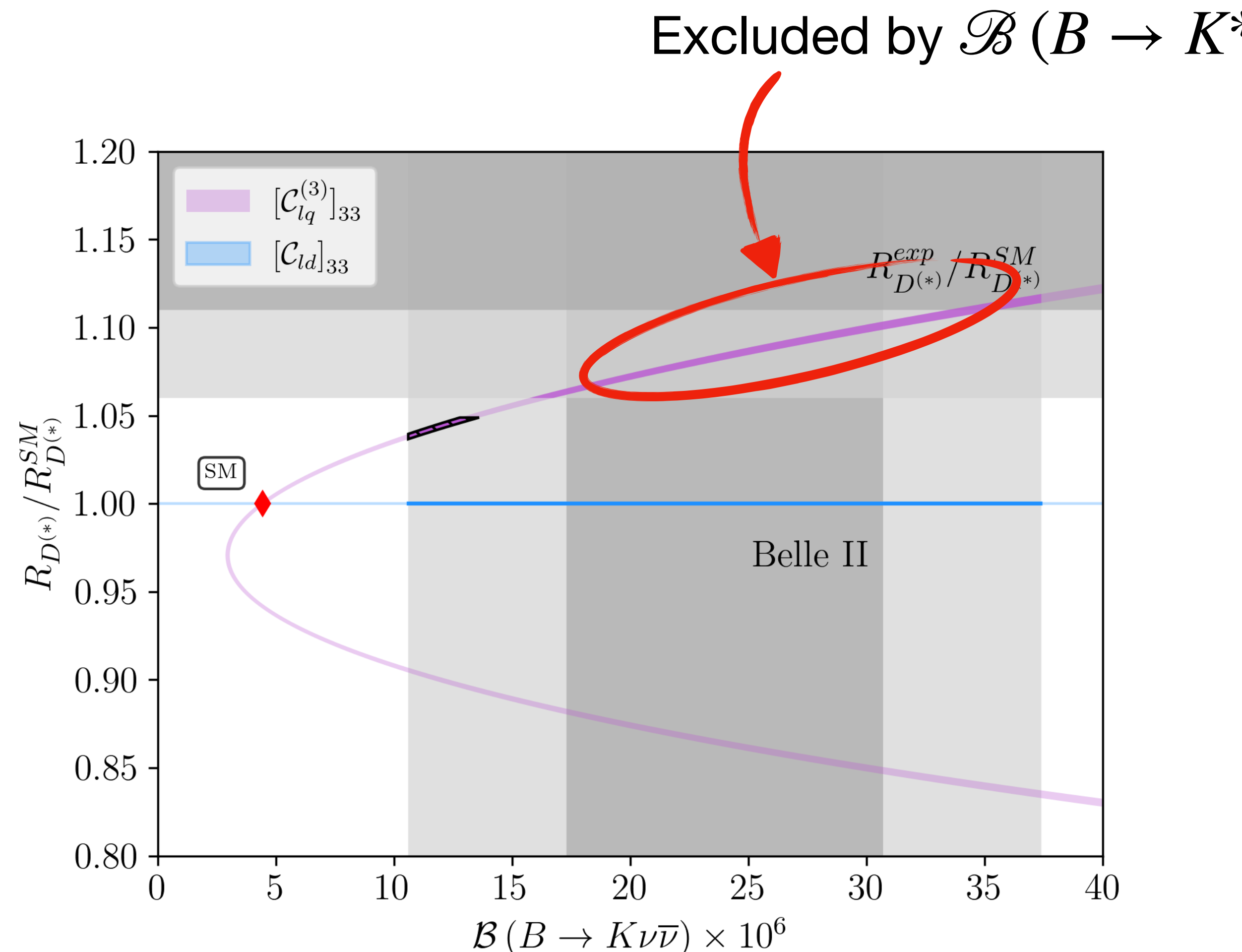
$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)}\ell\bar{\nu})}, \text{ with } \ell = e, \mu$$

HFLAV, arXiv:2206.07501

$$R_{D^{(*)}}^{\text{exp}}/R_{D^{(*)}}^{\text{SM}} = 1.16 \pm 0.05$$

BSM contributions to this process given by

$$\frac{R_{D^{(*)}}}{R_{D^{(*)}}^{\text{SM}}} = \left(1 - \frac{v^2}{\Lambda^2} \frac{V_{cs}}{V_{cb}} \mathcal{C}_{lq}^{(3)}\right)^2$$



# Correlations between observables

## Coupling to tau leptons

Can we introduce NP to simultaneously explain the Belle-II result and  $R_{D^{(*)}}^{(*)}$ ?

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)}\ell\bar{\nu})}, \text{ with } \ell = e, \mu$$

HFLAV, arXiv:2206.07501

$$R_{D^{(*)}}^{\text{exp}}/R_{D^{(*)}}^{\text{SM}} = 1.16 \pm 0.05$$

In this region  $\mathcal{B}(B \rightarrow K^*\nu\bar{\nu})$  is ok and we expect for example

$$\frac{\mathcal{B}(B_s \rightarrow \tau\tau)_{\text{BSM}}}{\mathcal{B}(B_s \rightarrow \tau\tau)_{\text{SM}}} \simeq 10$$

