



# Magnetic studies of a new insertion device: Bi-periodic undulator

**PHENIICS FEST 2024**  
**May 16-17**

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**PhD: 2<sup>nd</sup> year**  
**Synchrotron SOLEIL, France**



# Outline

*1/ Scientific context*

*2/ Bi-periodic undulator concept*

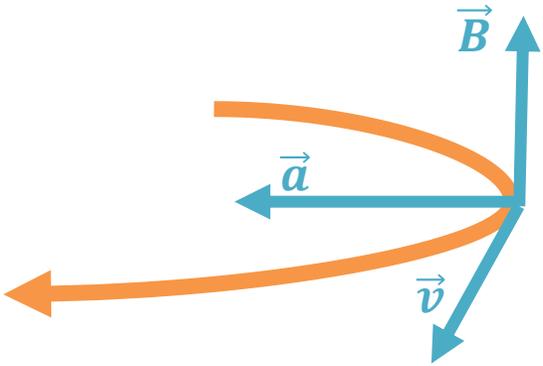
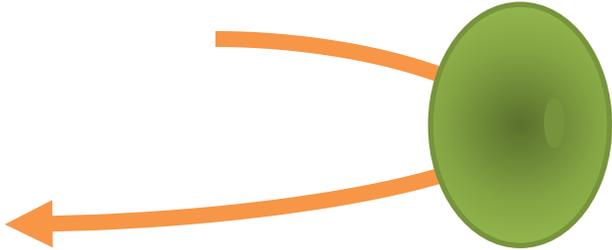
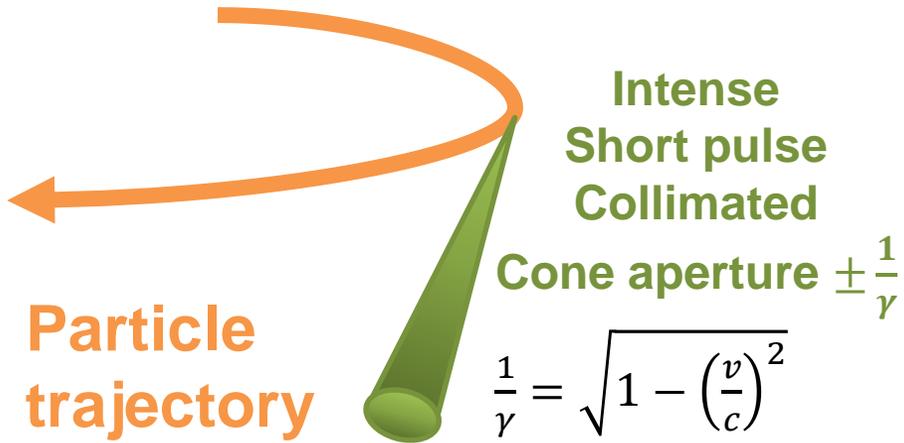
*3/ Magnetic studies of a prototype*

*4/ Conclusion and outlook*



## 1/ Scientific context

- Synchrotron: Particle accelerator designed to accelerate charged particles to obtain a beam of ultra-relativistic charged particles **to produce light**.

 <p><math>\vec{F} = q \vec{v} \times \vec{B}</math></p>	 <p><b>Particle trajectory</b> All directions <math>\pm \frac{\pi}{2}</math></p>	 <p><b>Particle trajectory</b> Intense Short pulse Collimated Cone aperture <math>\pm \frac{1}{\gamma}</math></p> <p><math>\frac{1}{\gamma} = \sqrt{1 - \left(\frac{v}{c}\right)^2}</math></p>
<p>Magnetic field: trajectory deviation + synchrotron radiation</p>	<p>Particles with a speed much lower than speed of light</p>	<p>Particles with a speed close to speed of light (ultra-relativistic)</p>

## Synchrotron SOLEIL

Since 2006  
Beam of electrons

Linac: first acceleration, 27 m

Booster: Brings electrons energy to 2.75 GeV

### Storage ring:

Circumference 354 m

Small bunches, total stored current 500mA

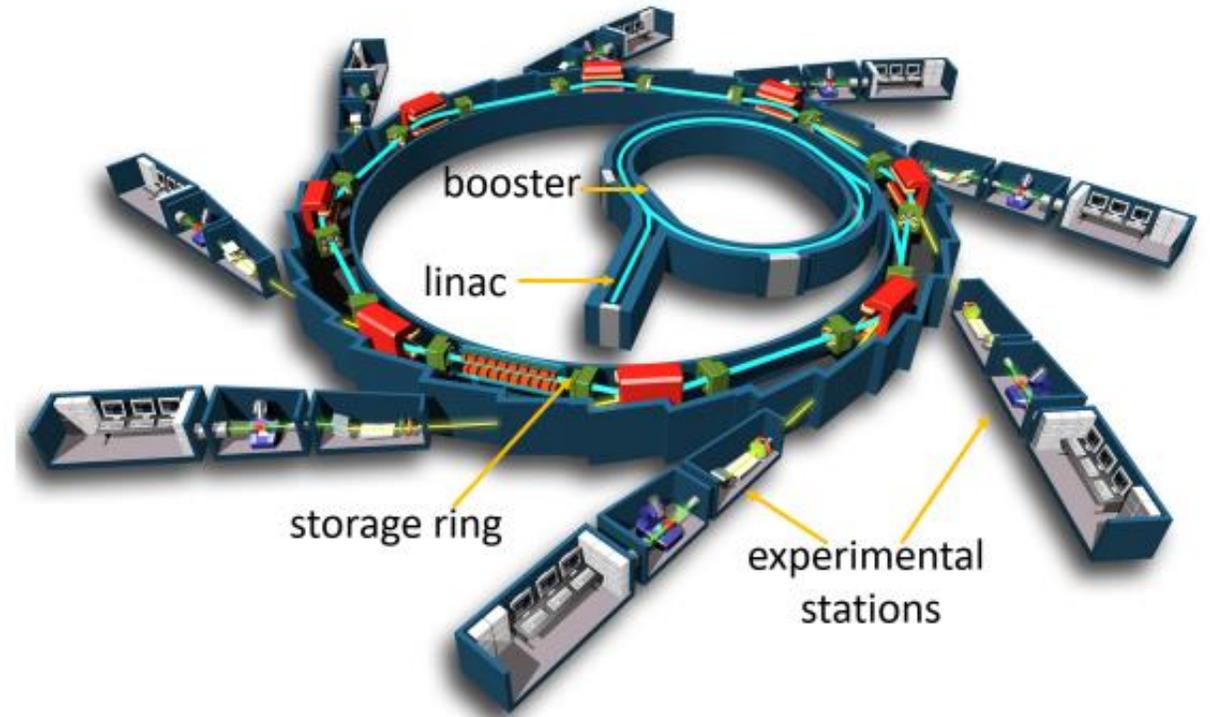
Horizontal emittance 3.9 nm.rad

Photon sources like bending magnets,  
wigglers, **undulators**

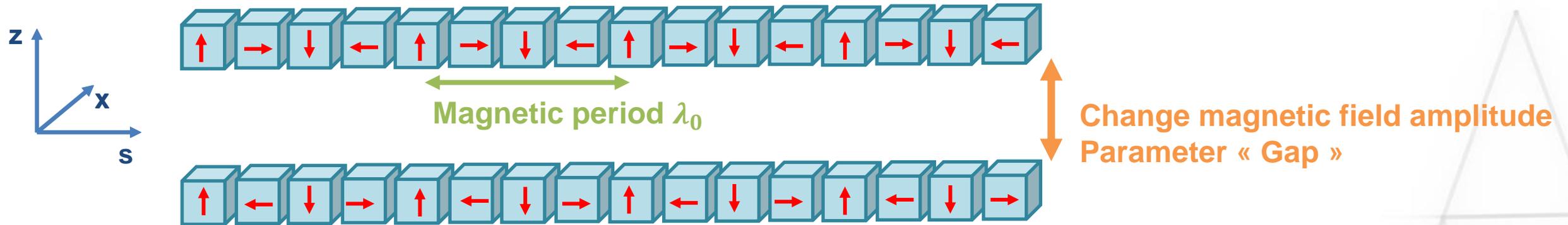
### Experimental stations:

29 beamlines

Laboratory, cover all field of science

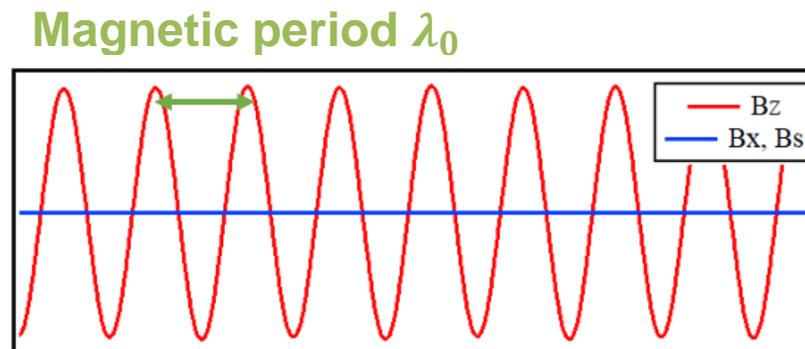


- Strong periodic magnetic field uniformly over a large distance
- Permanent magnets or electromagnets
- Example: Planar undulators

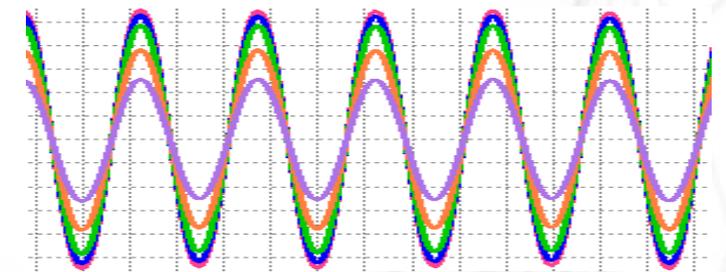


**Magnets**

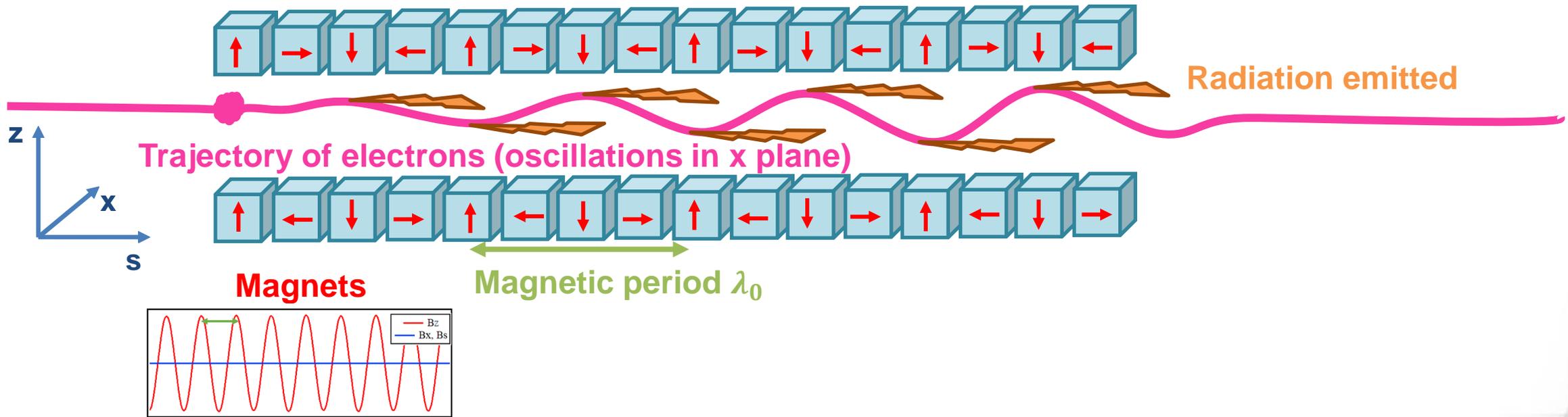
**Periodic vertical magnetic fields**



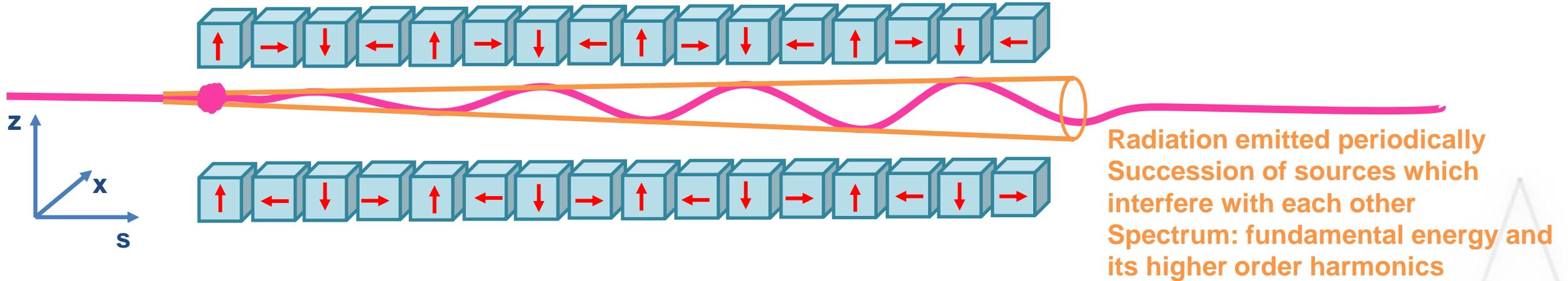
Gap: 15.5 mm 16 mm 17 mm 20 mm 25 mm



# Synchrotron radiation with planar undulators

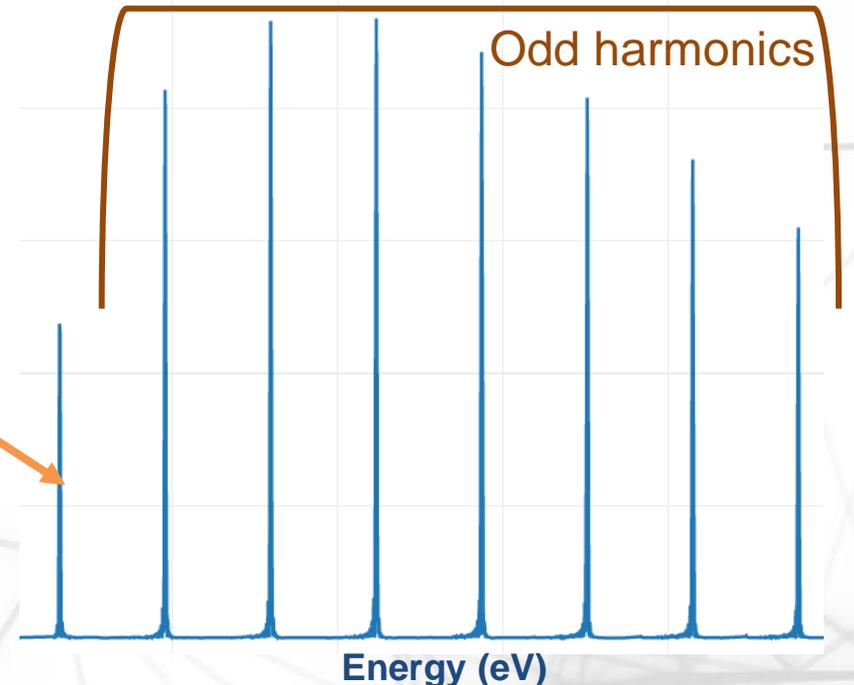


# Synchrotron radiation with planar undulators

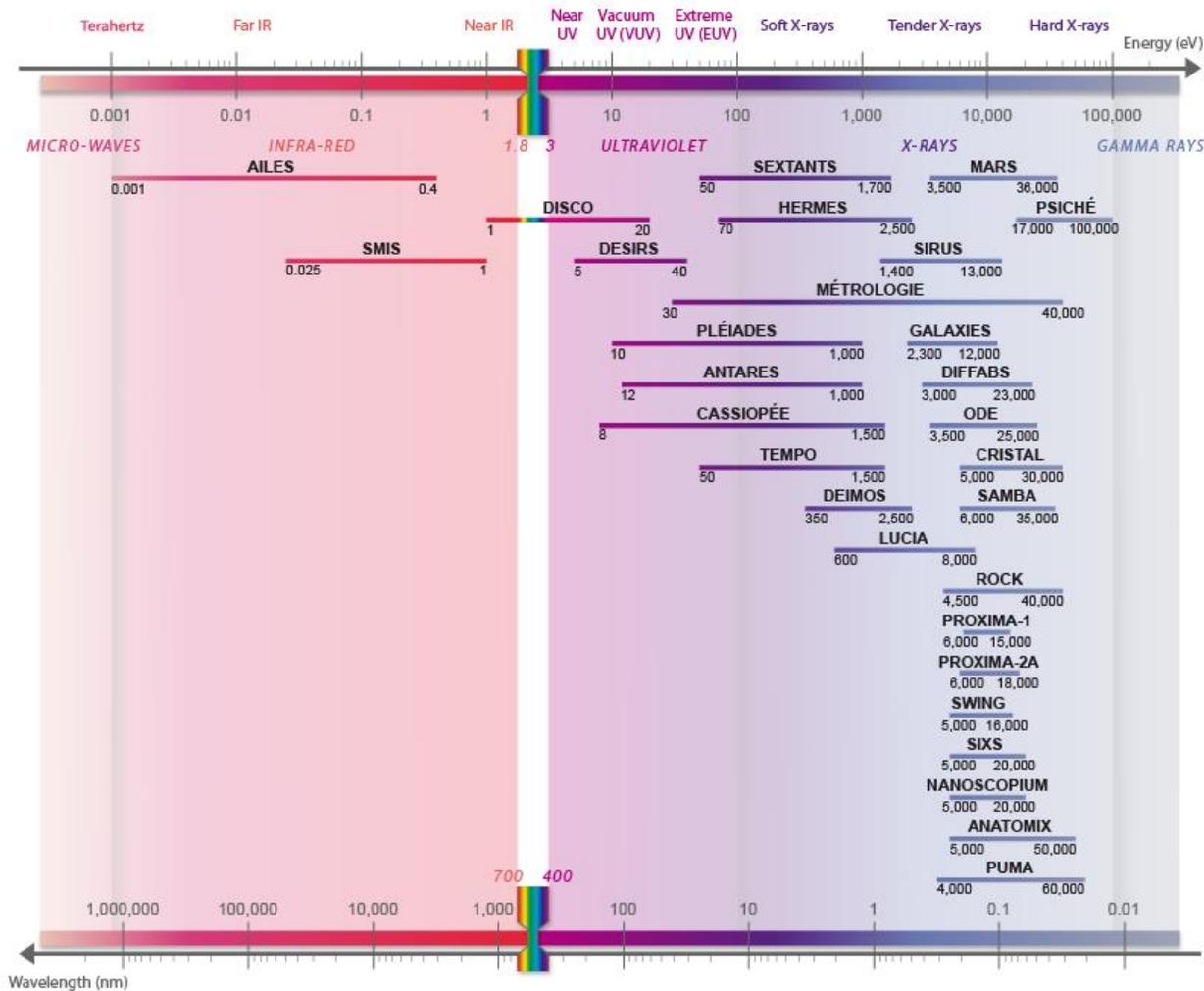


Fundamental energy

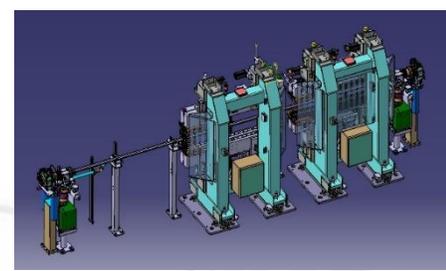
$$E_{photons}[keV] = 0.950 \times \frac{E^2[GeV]}{\lambda_0[cm] \times \left\{ 1 + \frac{1}{2} \left( \sum_i 0.934 \times B_i[T] \times \frac{\lambda_0[cm]}{i} \right)^2 \right\}}$$



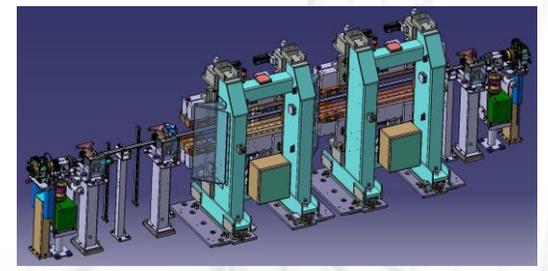
**Wide range of energy thanks to the complementarity and diversity of light sources**



**from infrared to hard x-rays**



**HERMES Beamline**



**TEMPO Beamline**

## Objective: Increase photon beam flux density and brightness

Reduce electron beam emittance from 3.9 nm.rad to **<100 pm.rad** to obtain smaller and less divergence source

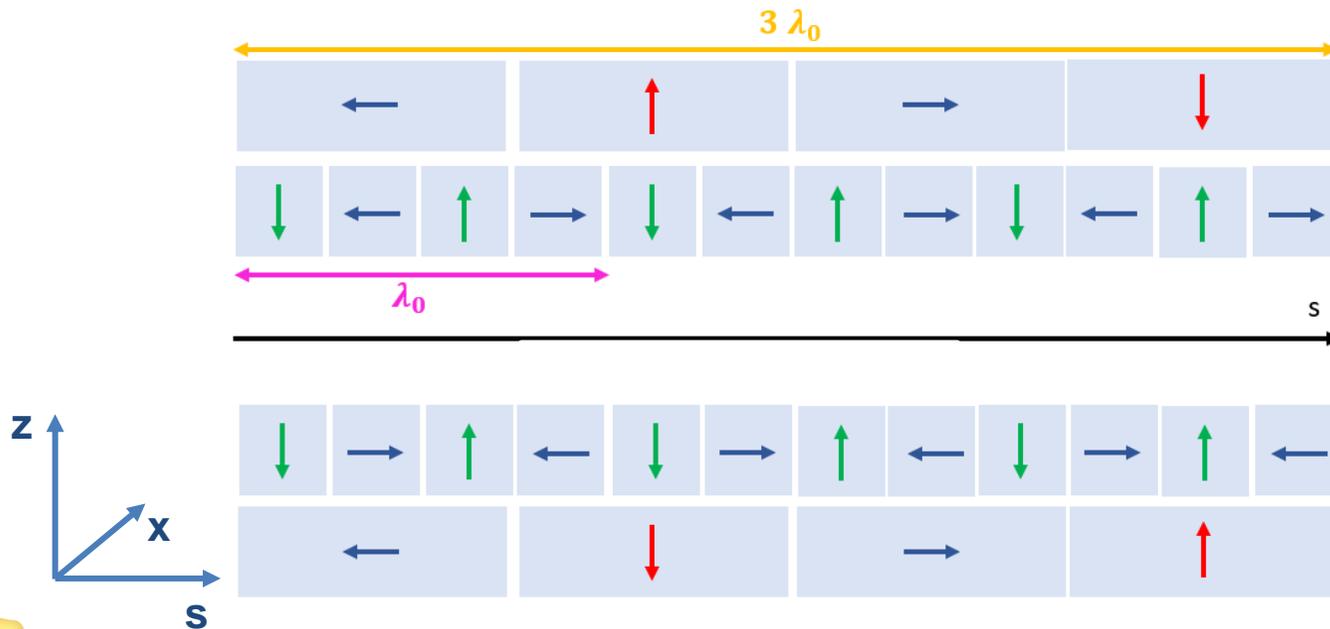
Increase number of magnetic elements for focusing and guiding beam.

**Reduce space reserved for insertion devices (30%).**

No space to juxtapose two undulators to maintain present spectral range for users

***Find technical solutions to the problem of limited space and search for compact radiation sources to maintain present spectral range for beamlines***

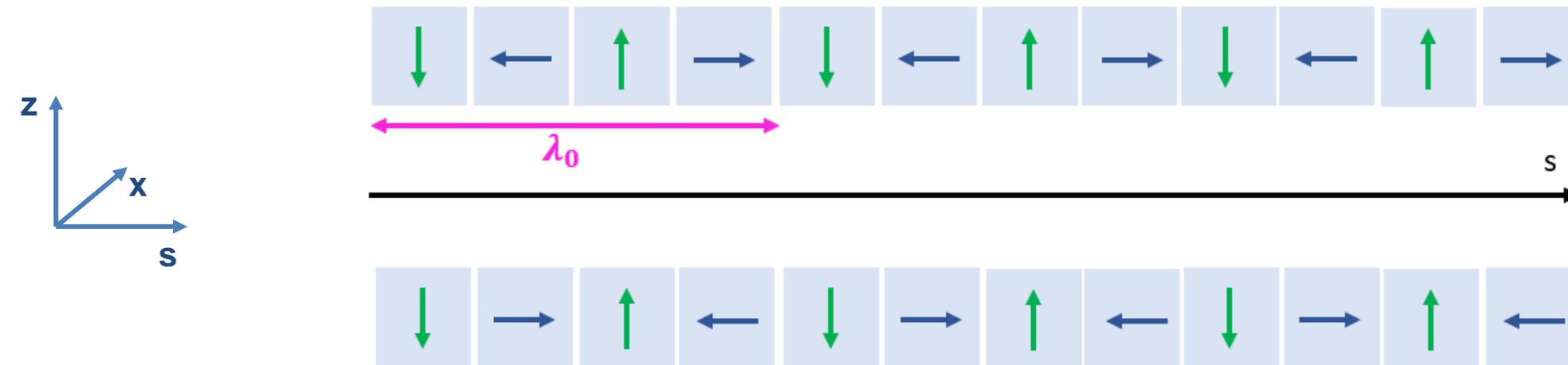
## Bi-Periodic undulator (Concept patented\*):



Innovative and compact device  
**Two selectable magnetic periodicities**  
 by superimposition of magnets  
**Select a magnetic period or its triple**  
**value** by longitudinal mechanical shift of  
 magnetic arrays

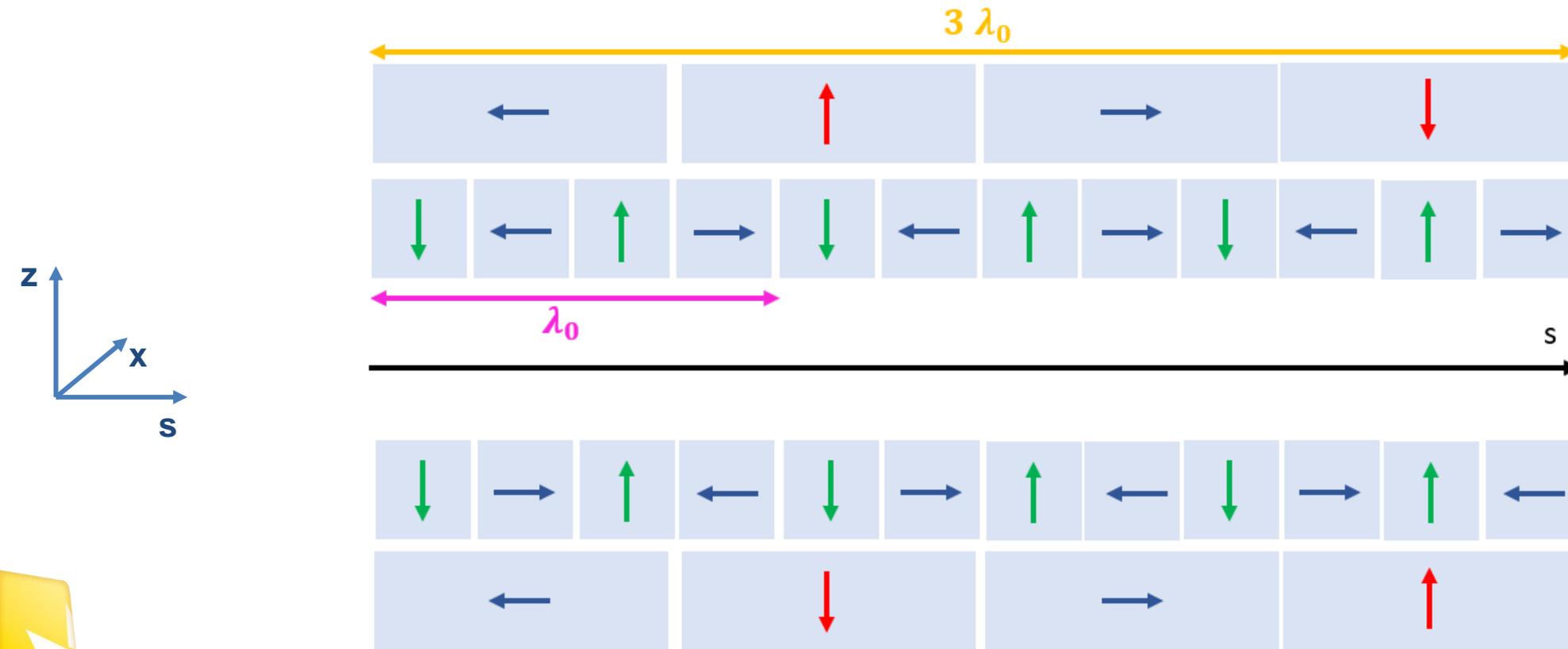
## 2/ Bi-periodic undulator concept

- System of magnets in Halbach\* configuration with one periodicity

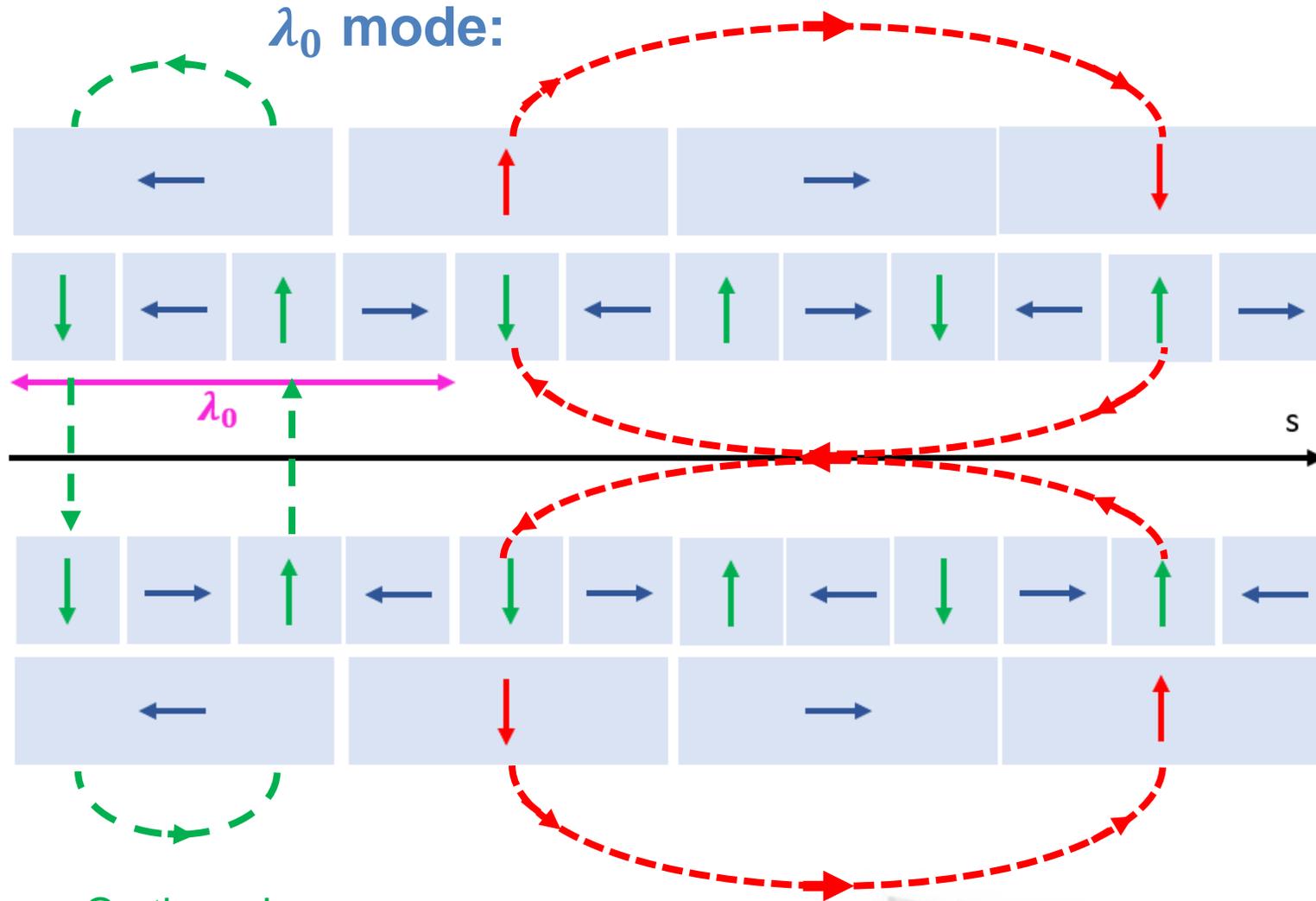


\* Halbach Configuration : K.Halbach, Nucl. Instrum. Methods, 169 (1980) 1–10

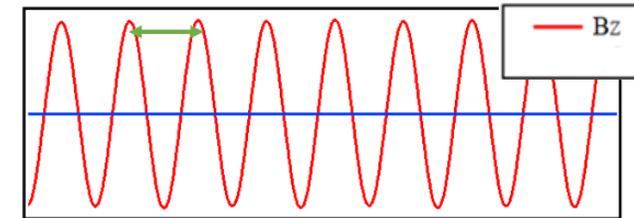
- Another array of magnets with triple periodicity



→ *Special arrangement of magnets enables two operating modes*

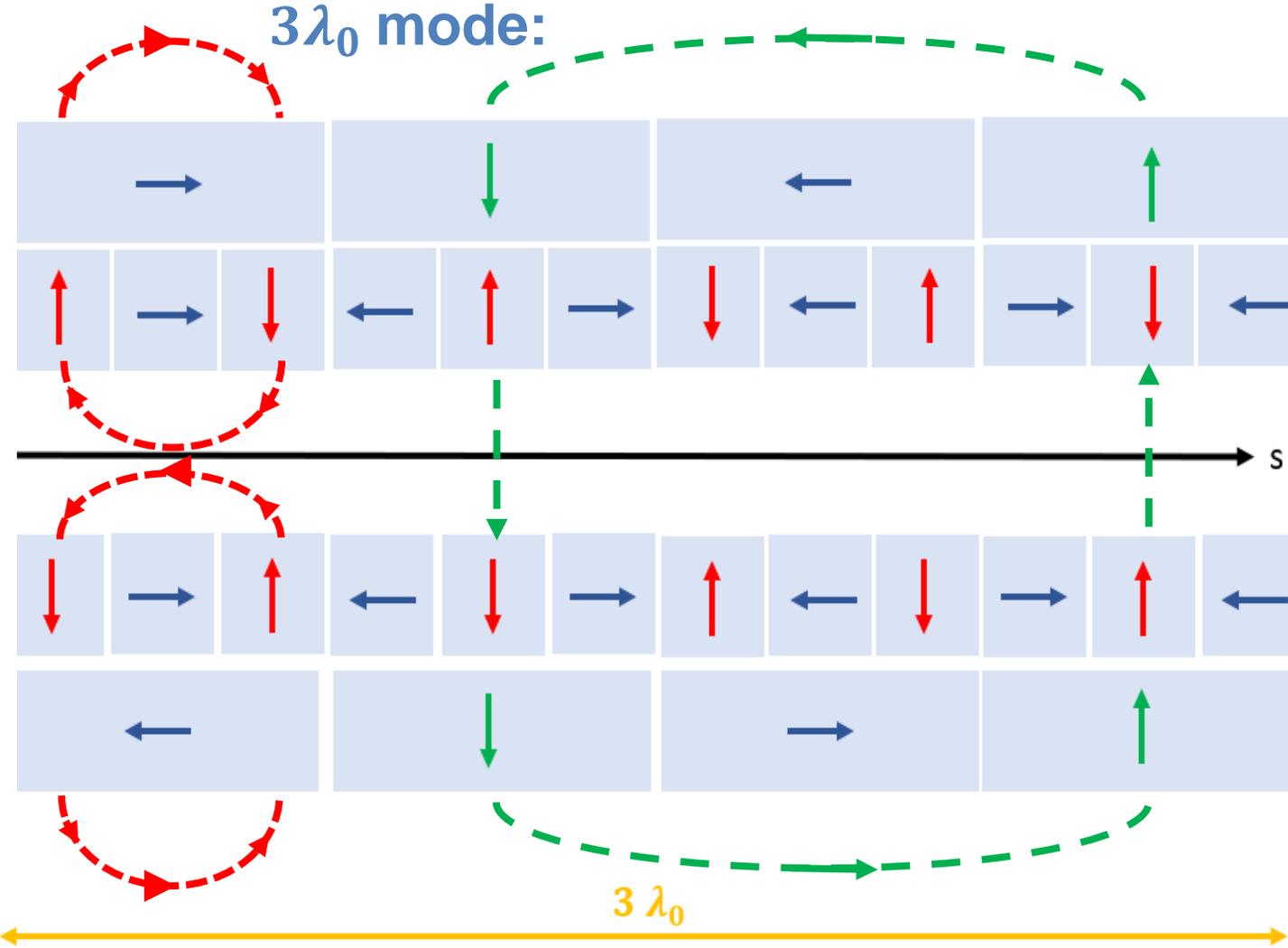


Magnetic field with a period  $\lambda_0$



On the axis:  
Vertical magnetic field contribution with a periodicity of  $\lambda_0$

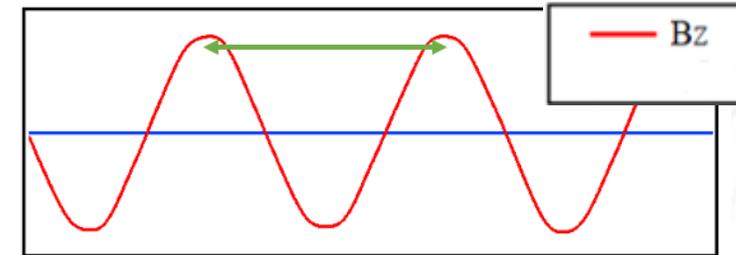
On the axis:  
Cancellation of vertical magnetic field contribution with a periodicity  $3\lambda_0$



Moving longitudinally the magnetic arrays

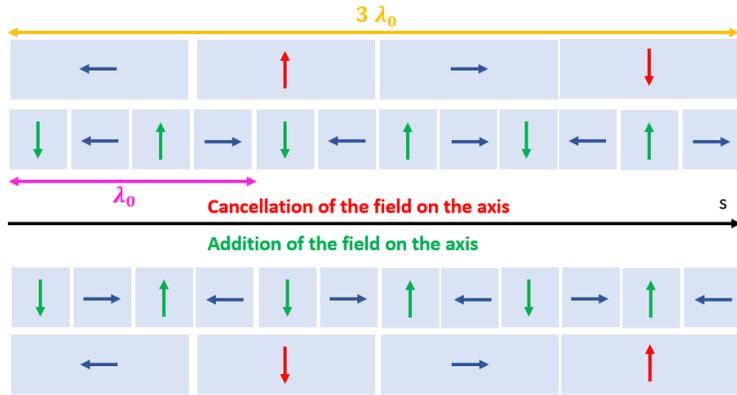
$$\Delta = \frac{3\lambda_0}{2}$$

Magnetic field with a period  $3\lambda_0$

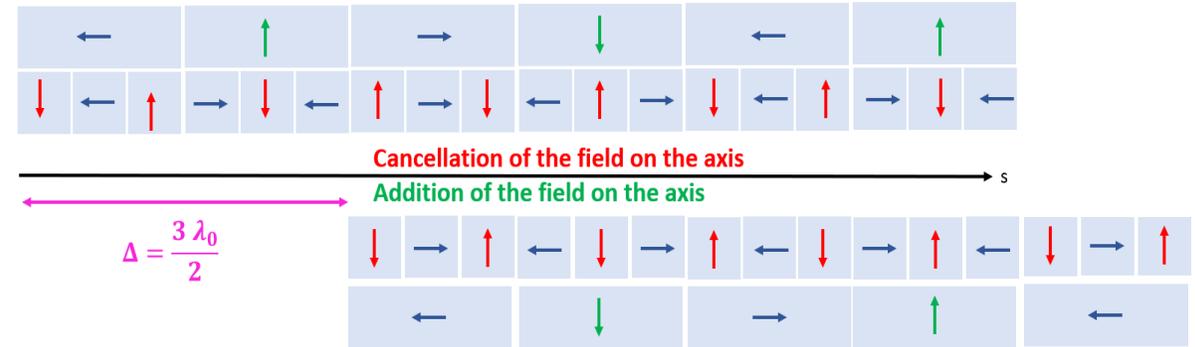


On the axis:  
Cancellation of vertical magnetic field contribution with a periodicity of  $\lambda_0$

On the axis:  
Vertical magnetic field contribution with a periodicity  $3\lambda_0$

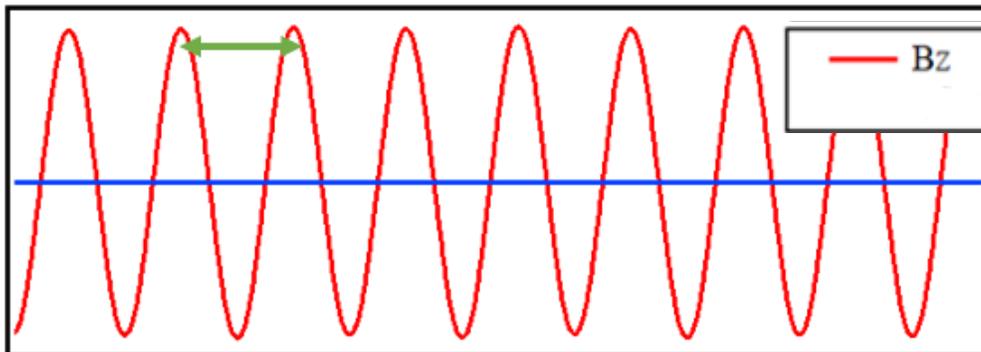


$\lambda_0$  mode:

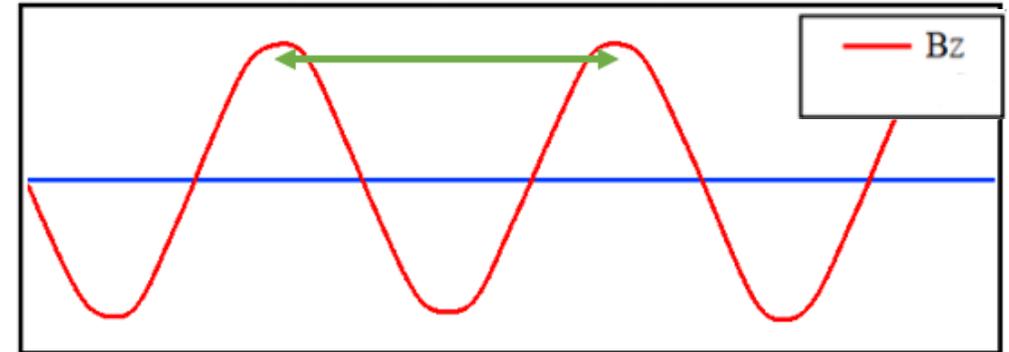


$3\lambda_0$  mode:

Magnetic period  $\lambda_0$



Magnetic period  $3\lambda_0$



- On axis: can select one or the other period only by changing operating mode
- Change magnetic period and energy range
- Performances of two undulators for one insertion device

## 3/ Magnetic studies of a prototype

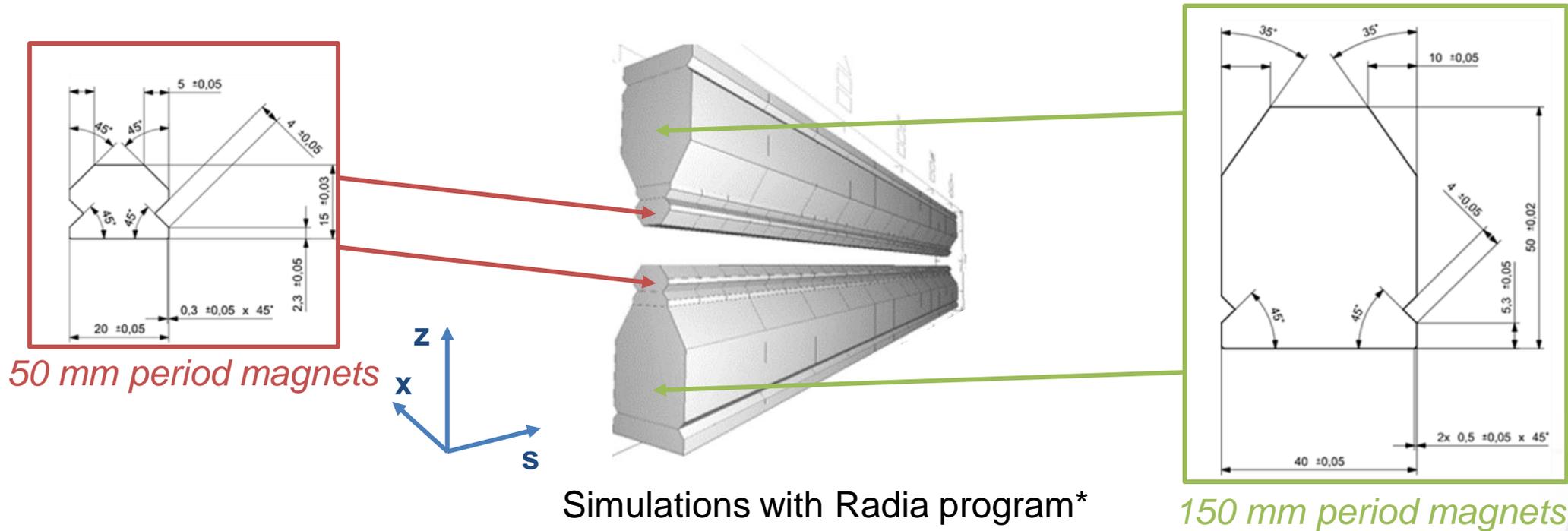
- Design for SOLEIL II + Construction of prototype

In this presentation

- Verify possibility to select only one period
- Verify magnetic performance
- Validate mechanical design

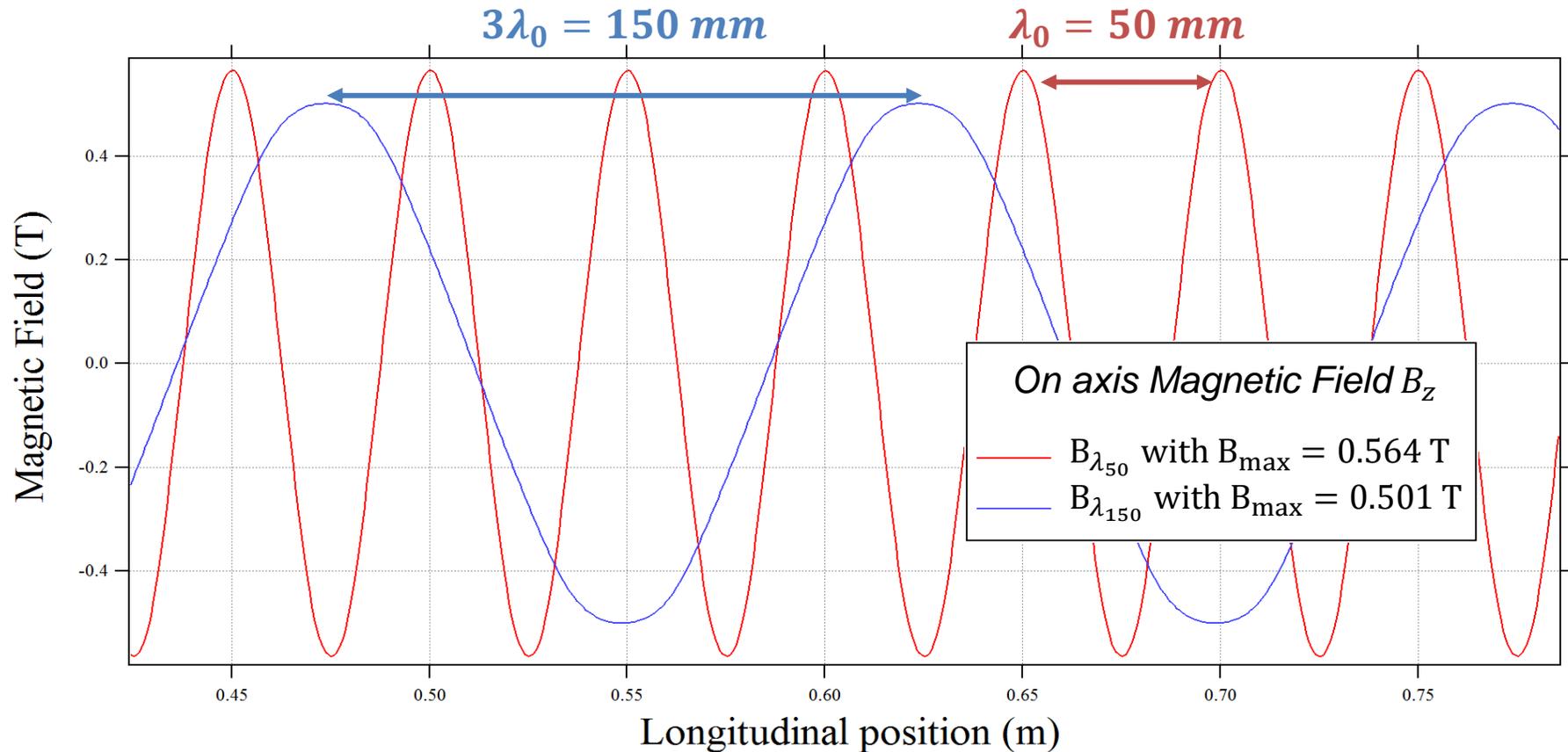
- Test on SOLEIL I

- Characterize beam dynamics
- Validate spectral performance

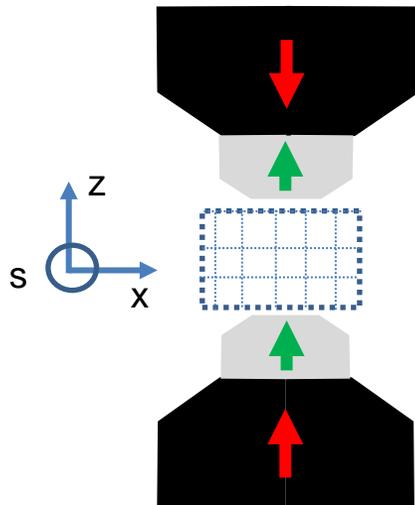
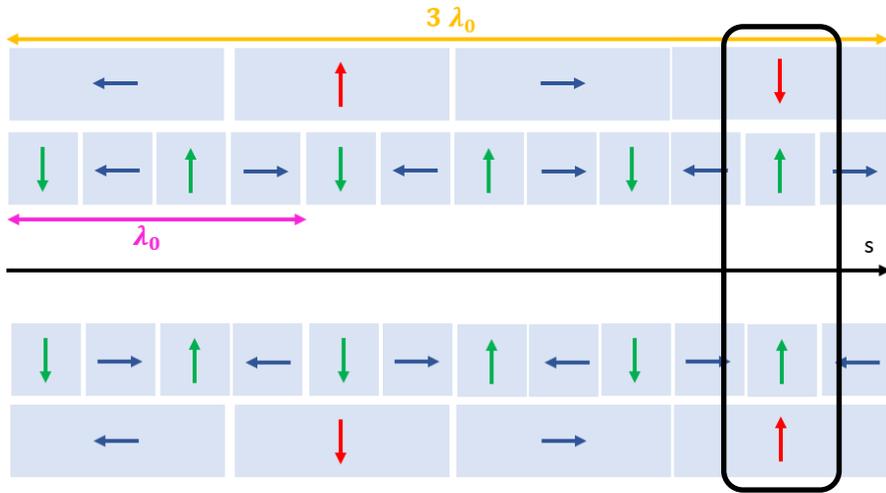


Periodicity	$\lambda_0 = 50 \text{ mm}$ and $3 \lambda_0 = 150 \text{ mm}$
Magnets	Permanent magnets NdFeB: Trapezoidal geometry
Magnetization	$\lambda_0 = 50 \text{ mm} \rightarrow M_{\text{avg}} = 1.38 \text{ T}$ $3 \lambda_0 = 150 \text{ mm} \rightarrow M_{\text{avg}} = 1.42 \text{ T}$

Vertical magnetic field on axis for two operating modes at gap 15.5 mm (minimal gap)



→ *On axis: can select one or the other period only*



Consider the system as two independent planar undulators operating at  $\lambda_0 = 50$  mm and  $3\lambda_0 = 150$  mm

Express magnetic field as a periodic signal defined by a sum of Fourier coefficients:

$$A1_{x,z,s}(x, z) = \frac{2}{L_u} \int_{-L_u/2}^{+L_u/2} B_{x,z,s}(s) \sin\left(\frac{k_0}{3}s\right) ds$$

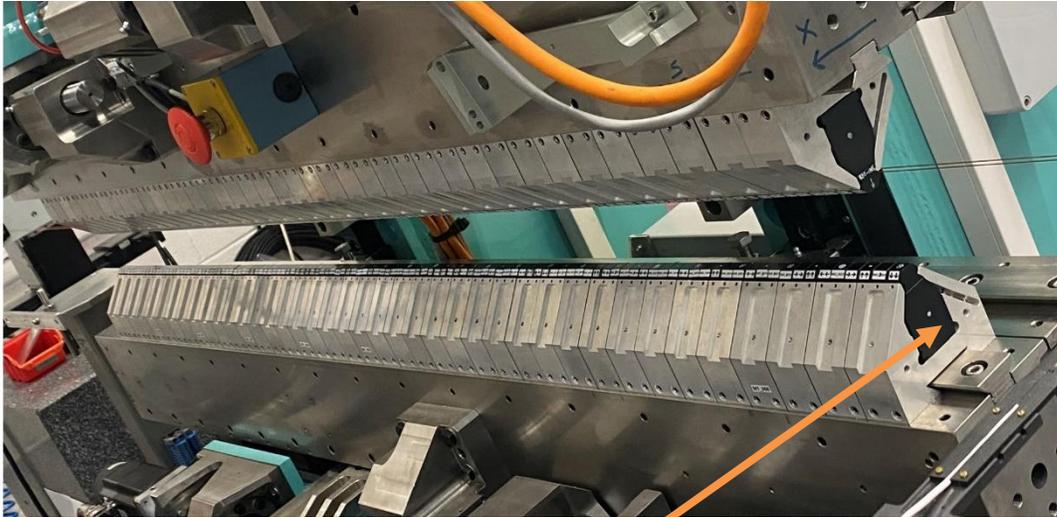
$$A3_{x,z,s}(x, z) = \frac{2}{L_u} \int_{-L_u/2}^{+L_u/2} B_{x,z,s}(s) \sin(k_0 s) ds$$

$$B1_{x,z,s}(x, z) = \frac{2}{L_u} \int_{-L_u/2}^{+L_u/2} B_{x,z,s}(s) \cos\left(\frac{k_0}{3}s\right) ds$$

$$B3_{x,z,s}(x, z) = \frac{2}{L_u} \int_{-L_u/2}^{+L_u/2} B_{x,z,s}(s) \cos(k_0 s) ds$$

**Magnetic axis:**

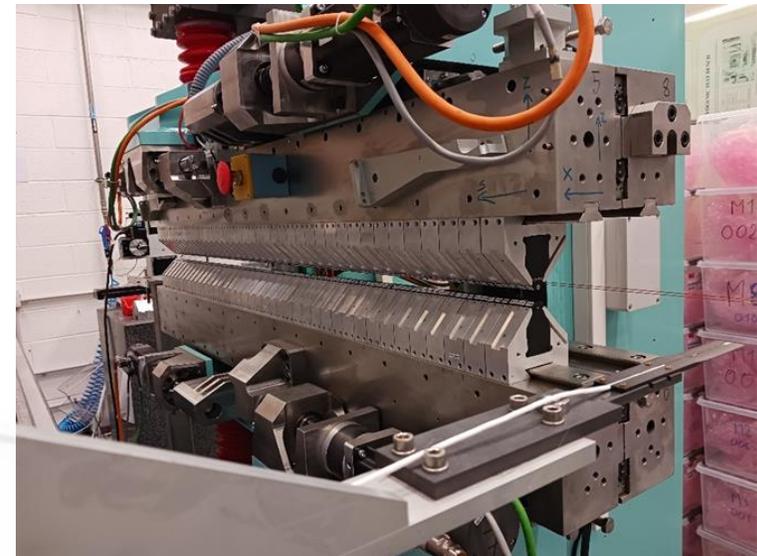
50 mm mode: Coefficient  $A1_z$  is canceled  
 150 mm mode: Coefficient  $A3_z$  is canceled



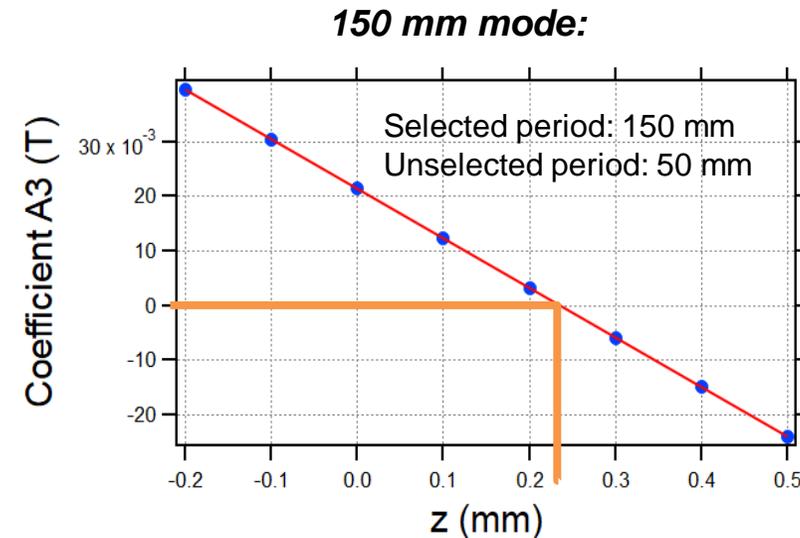
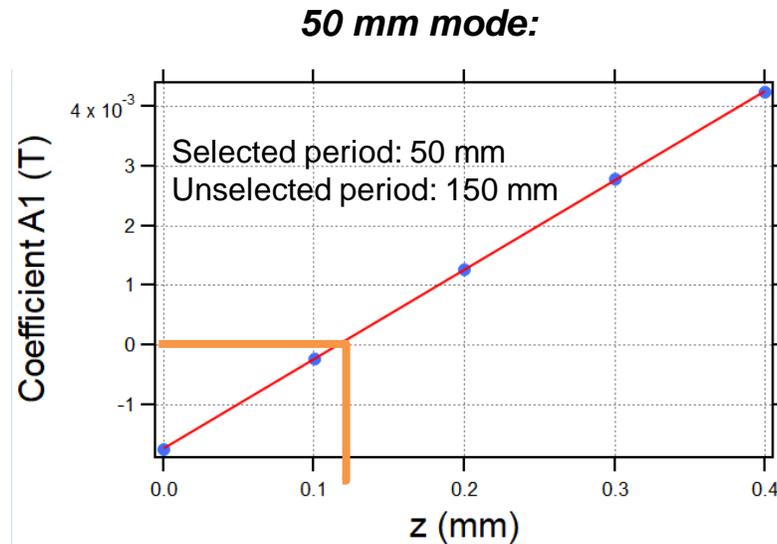
3 magnets  
(50 mm period)

1 magnet  
(150 mm period)

Periodicity	$\lambda_0 = 50 \text{ mm}$ and $3 \lambda_0 = 150 \text{ mm}$
Magnets	Permanent magnets NdFeB Trapezoidal geometry
Magnetization	$\lambda_0 = 50 \text{ mm} \rightarrow M_{\text{avg}} = 1.38 \text{ T}$ $3 \lambda_0 = 150 \text{ mm} \rightarrow M_{\text{avg}} = 1.42 \text{ T}$
Length	$l = 1.5 \text{ m}$
Instrumentation of measuring bench	Hall probe and Flipping coils



- Hall probe alignment on magnetic axis: study of Fourier coefficients



Each mode had its own magnetic axis because of magnetic and mechanical defects (the two are separated by less than 100  $\mu\text{m}$ )  
 → Determine average axis

Gap 15,5 mm	50 mm mode	150 mm mode
% unselected period	<b>0,25 %</b>	<b>1,6 %</b>

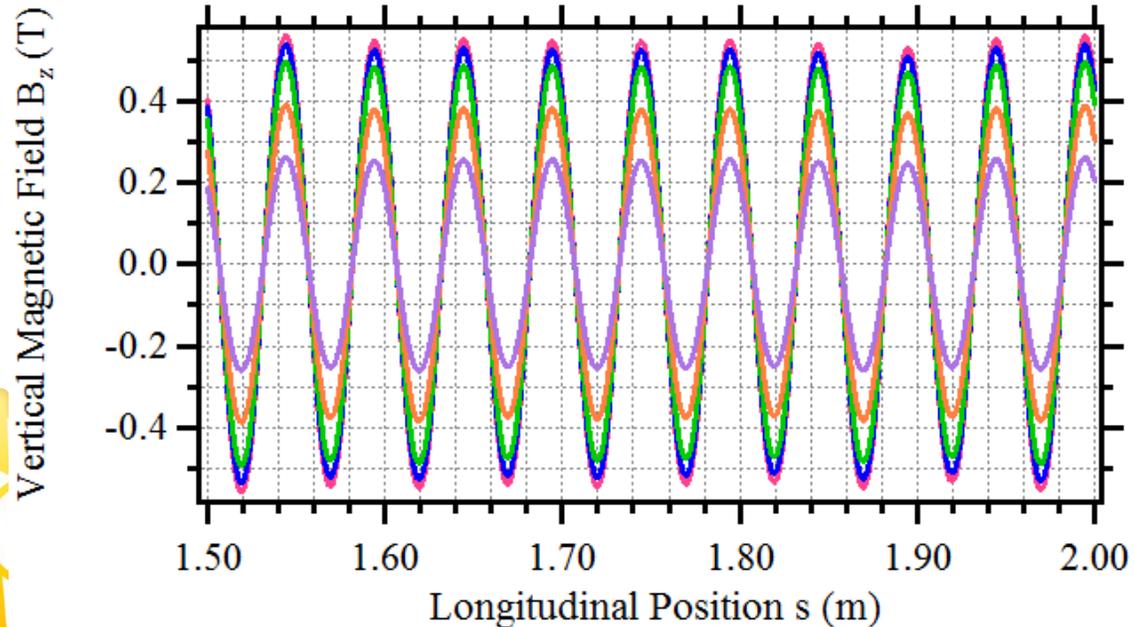
- Prototype: Be able to cancel almost the unselect period on the axis for the two operating modes

- Measurements for different gaps:

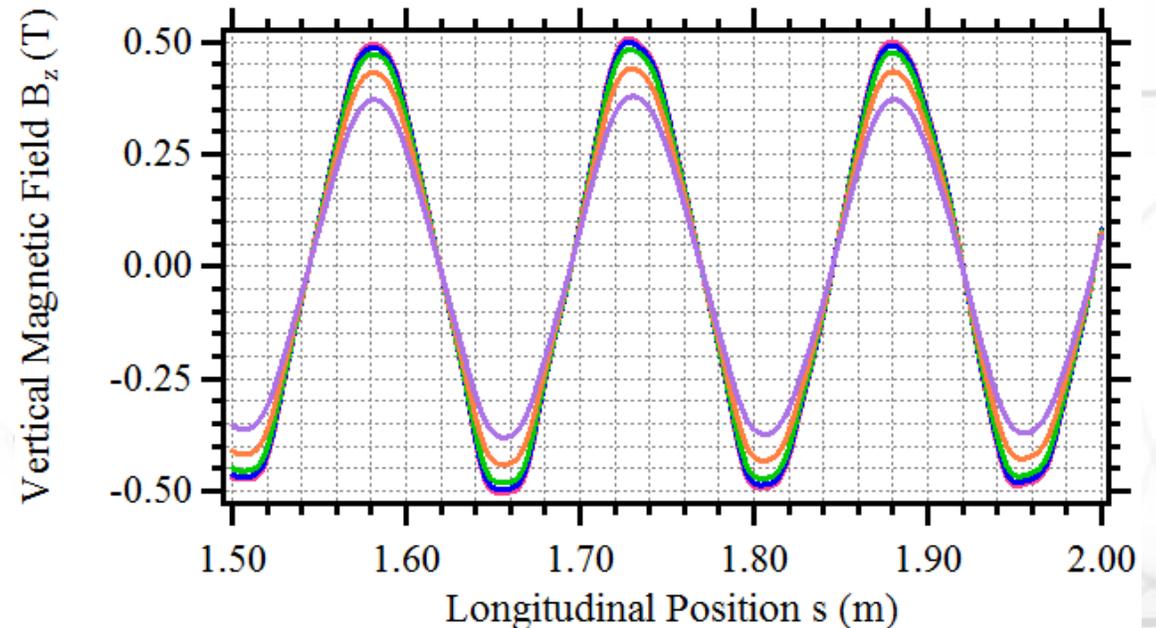
Gap: — 15.5 mm — 16 mm — 17 mm — 20 mm — 25 mm

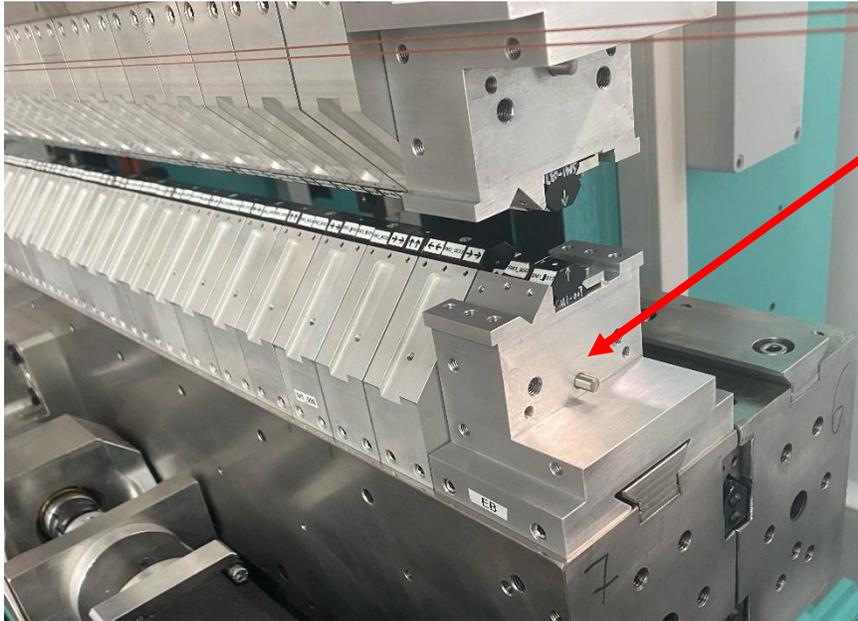
Gap	Period: 50 mm		Period: 150 mm	
15.5 mm	0.55 T	330 eV	0.50 T	19 eV
16 mm	0.52 T	350 eV	0.49 T	19.5 eV
17 mm	0.48 T	395 eV	0.47 T	20.6 eV
20 mm	0.38 T	546 eV	0.43 T	24.6 eV
25 mm	0.25 T	823 eV	0.37 T	32.5 eV

**50 mm of period**

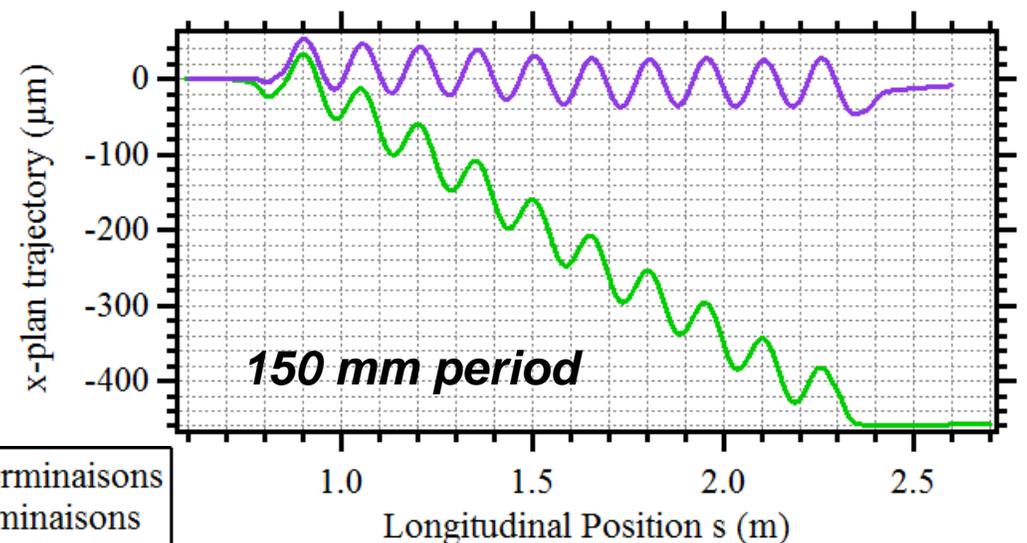
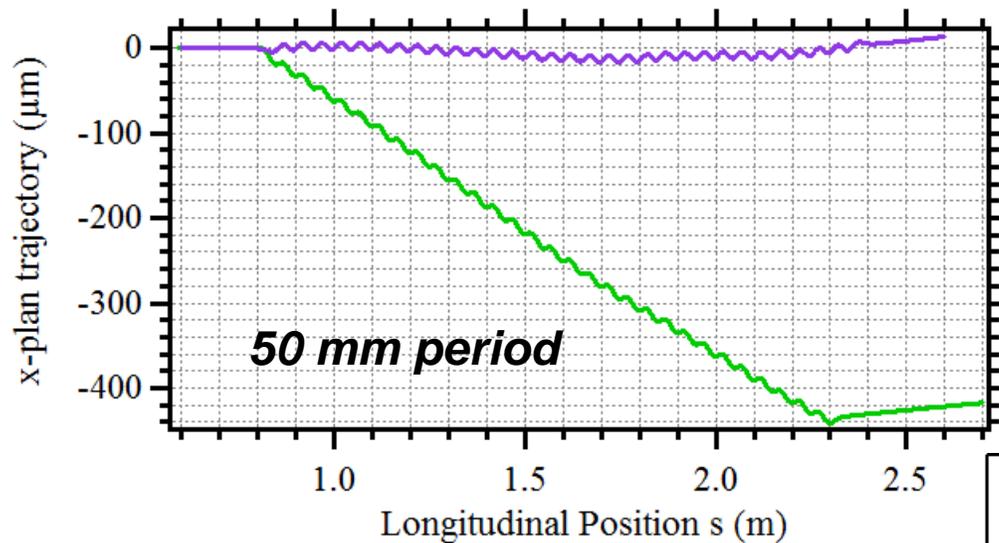
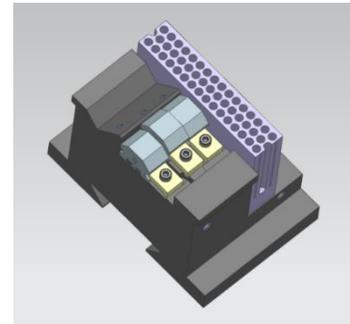


**150 mm of period**

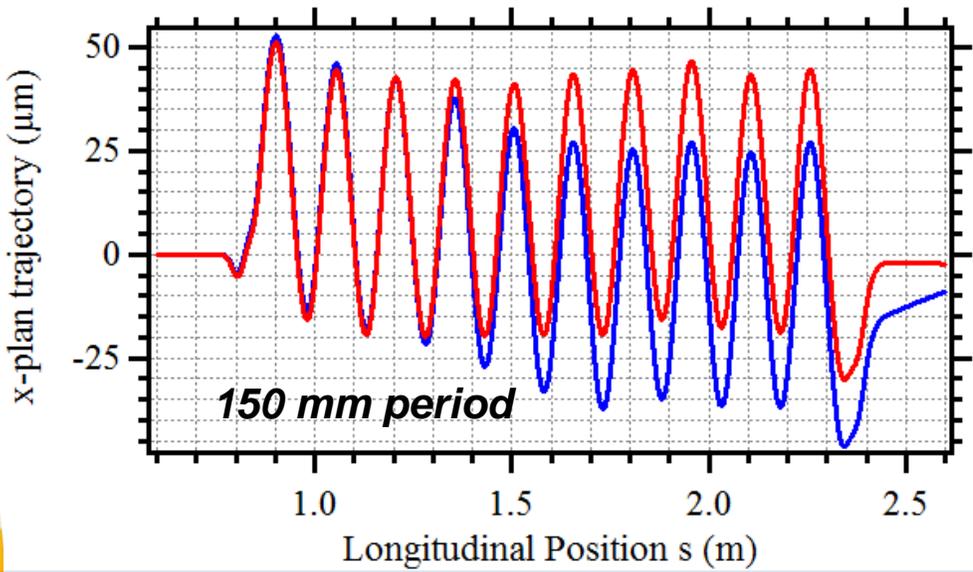
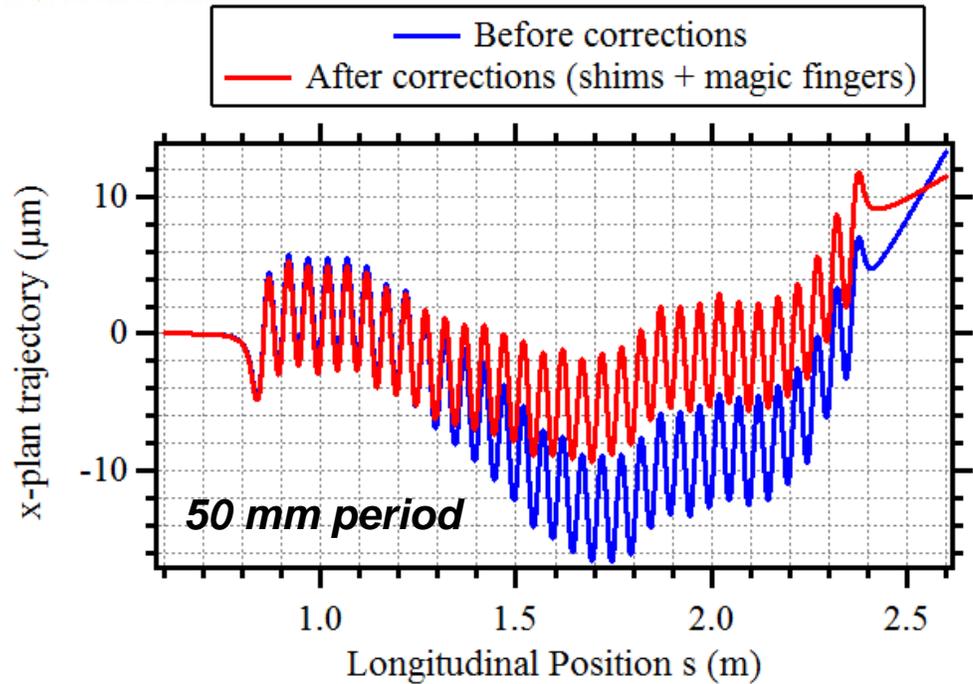




**End terminaisons:**  
 At the ends of the undulator (at the input and output) magnetic environment disrupts electron trajectory and generates angular deviations. Impacts on the electron trajectory and on emission axis of the radiation.



# Magnetic corrections



## Shims:

250  $\mu\text{m}$  thick iron shims.  
Installed on magnets at precise positions along the prototype to reduce the field locally where there is an excess of magnetic field.

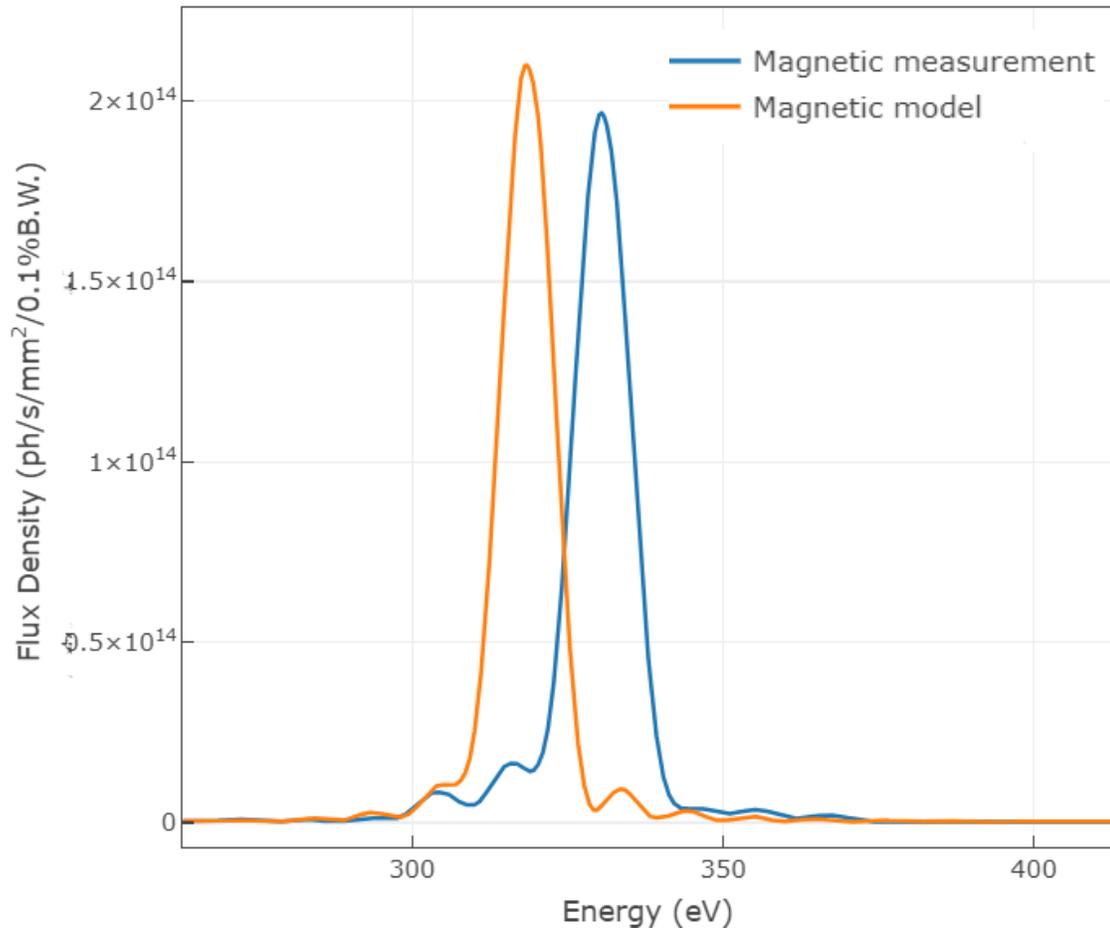
## Magic Fingers:

Small cylindrical magnets in small boxes  
Installed at the ends of the undulator to locally correct off-axis impacts and trajectory at the ends by imposing new transverse distribution of the field

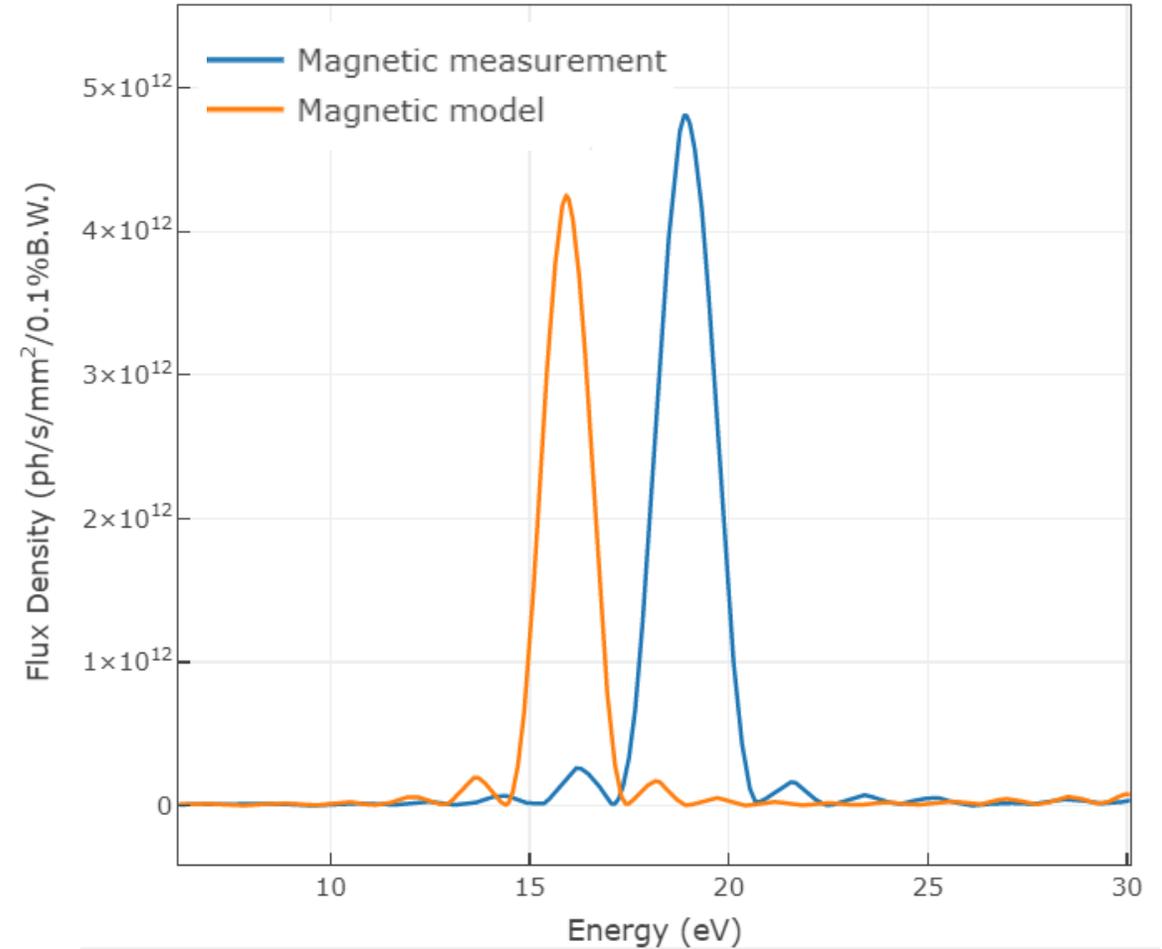


## 15,5 mm gap

### 50 mm period



### 150 mm period

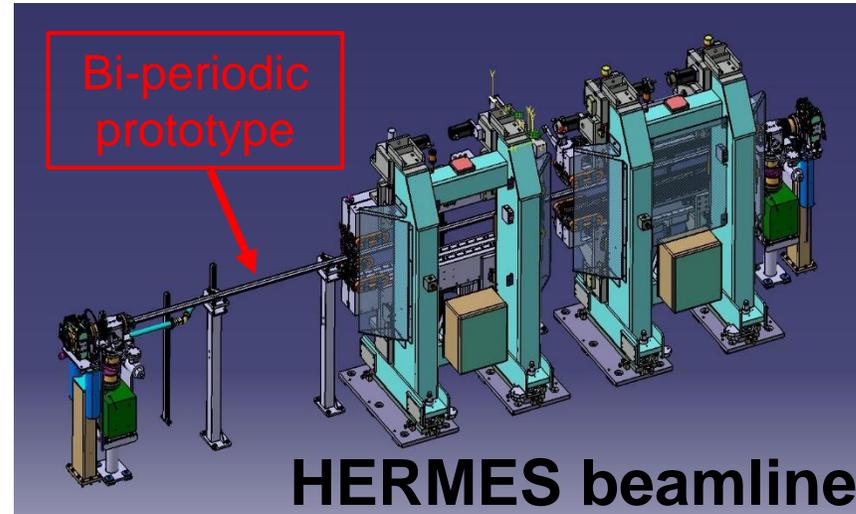


\* SPECTRA - a synchrotron radiation calculation code, T. Tanaka and H. Kitamura, J. Synchrotron Radiation 8, 1221 (2001)

## 4/ Conclusion and outlook

- Replace two undulators by one which have the same spectral domain
- Prototype: to validate the concept of the bi-periodic undulator and to identify the potential constraints
- Encouraging results: possibility to select one of the two periods only

# Outlook: Experimental study on storage ring



*(DENNETIERE David, BELKHOU Rachid, optic group)*

**January 2024**

Prototype installation on present storage ring

**March 2024**

We began the study of the radiation obtained on the beamline

**February 2024**

We began the study of the impact on the beam dynamics

An aerial photograph of the SOLEIL synchrotron facility, showing a large circular building with a grid-like roof structure, surrounded by other buildings and greenery. The image is faded and serves as a background for the text.

***Thank you  
for your attention!***