Super-radiance during reheating

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[credit: RIIS at Okayama U.]

Outline



Introduction

- Dicke super-radiance
- Beyond Dicke

Macro-coherence during reheating

- Preheating in Schrödinger picture
- Parametrically amplified macro-coherence

Abrupt end of reheating

- Dicke model during reheating
- Super-radiant burst

Introduction

Dicke's work on super-radiance

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Coherence in Spontaneous Radiation Processes

R. H. DICKE Palmer Physical Laboratory, Princeton University, Princeton, New Jersey (Received August 25, 1953)



[Princeton U.]

Consider a totally excited two-level atomic system:

Spontaneous emission happens when

- atoms are well-separated and random
- separation between atoms \gg photon wave length
- ⇒ exponential decay
- Super-radiant emission happens when
 - atoms are close and phase-aligned
 - separation between atoms \ll photon wave length
 - \Rightarrow pulse-like burst

Coherence of radiated photon is a key for super-radiance

Super-radiance in laboratories

MIT group observed super-radiance for the first time [Skribanowitz et al, '73]



- Irradiated atoms by laser emit puls-like radiation
 - Radiated light is highly directional (phase-aligned)

Beyond Dicke super-radiance

Super-radiant region for single photon emission is limited to the laser direction
dipole transition:

$$|\psi\rangle = c_e |e\rangle + c_g |g\rangle, \qquad \qquad H = \begin{pmatrix} \hbar \omega_0/2 & d_{eg} \\ d_{ge} & -\hbar \omega_0/2 \end{pmatrix}$$

• single photon emission (wavelength $\lambda \sim 1/k$):

$$\begin{split} d_{ge} \quad &\text{from} \quad \langle g | H_{\rm NR} | e \rangle \sim \sum_{a=1}^{N} \vec{d} \cdot \vec{A}(\vec{r}_{a}) \sim \sum_{a=1}^{N} \vec{d} \cdot \vec{\epsilon}_{\lambda} e^{i \vec{k} \cdot \vec{r}_{a}} \\ N \gg 1 \quad \Rightarrow \quad &\text{(transition amp.)} \propto \int d^{3} r e^{i \vec{k} \cdot \vec{r}} \sim \begin{cases} \text{vol.} \times (kR)^{-2} & (R \gg 1/k) \\ \text{vol.} & (R \ll 1/k) \end{cases} \end{split}$$

super-radiant emission only when (target length) « (photon wavelength)
Macro-coherence to extend the super-radiant region [Yoshimura et al, '08]

- photon pair emission: $|e\rangle \rightarrow |g\rangle + \gamma(k_1) + \gamma(k_2)$
- kinematically $ec{k}=ec{k}_1+ec{k}_2 \ \Rightarrow \$ easily k o 0 for the collimated photons
- macroscopic coherence (phase alignment) may be realized

Macro-coherence during reheating

Preheating after the end of inflation



Focus on the reheating stage

Harmonic oscillator approximation:

$$V(\phi) \simeq \frac{1}{2} m_{\phi}^2 \phi^2$$

Particle creation

- Suppose ϕ decays into a pair of photons $\phi(\vec{k}=0) \rightarrow \gamma(\vec{k}_1)\gamma(\vec{k}_2)$, then $\vec{k}_2 = -\vec{k}_1$
- Phase of the decay products is aligned
- Macro-coherence may naturally be realized during preheating

Parametric resonance during preheating

Consider the $\{\phi, \gamma\}$ -system, and neglect expansion of the Universe (for simplicity)

E.g. ϕ - γ - γ coupling: $\mathcal{L}_{int} = -\frac{1}{4}K\phi(F_{\mu\nu})^2$ ($K \sim b\alpha/4M_P$ for conformal anomaly)



• EoM:
$$\ddot{\vec{A}}_k + k^2 \vec{A}_k + \frac{K\phi}{1+K\phi} \dot{\vec{A}}_k = 0$$

 After field redefinition and some approximation, each polarization satisfies

$$A_k'' + (a - 2q\cos 2\tau)A_k = 0$$

(\tau = m_\phi(t + \tau)/2, a = (2k/m_\phi)^2, q = K\phi_e)

• $q \ll 1$ (narrow resonance)

- ▶ perturbative production around $a = n^2$ $(n = 1, 2, 3, \cdots)$
- \blacktriangleright corresponds to $n\times\phi\to\gamma\gamma$
- $q \gg 1$ (broad resonance)
 - non-perturbative production for $a \leq 2q$
 - occupation number grows exponentially

Parametrically amplified macro-coherent state

Consider parametric resonance in Schrödinger picture [Yoshimura '95]

Hamiltonian of a bosonic field b may be given by

$$H = \int d^3x \frac{1}{2} \left[\pi_b^2 + (\vec{\nabla}b)^2 + m_b^2(t)b^2 \right], \qquad m_b^2(t) \sim m_0^2 + f(\phi(t))$$

• For each Fourier mode b_k , the wave functional ψ satisfies the Schrödinger eq.:

$$i\frac{\partial\psi}{\partial t} = -\frac{1}{2}\frac{\partial^2\psi}{\partial b_k^2} + \frac{1}{2}\omega_k^2(t)b_k^2\psi \quad \Rightarrow \quad \psi(b_k,t) = \left(\frac{\mathrm{Re}D}{\pi}\right)^{1/4}e^{-(D/2)b_k^2}$$

• $D = \pi/|u|^2 - (i/2)\frac{d}{dt}\ln|u|^2$ with $\ddot{u} + \omega_k^2(t)u = 0 \quad \Leftrightarrow \quad \text{Mathieu equation}$



Im D ~ d/dt ln |u|² ~ const. (related to the Floquet exponent)
Phase in \u03c6 aligns after a number of oscillations
Macro-coherent state is achieved, leading to super-radiant decay of inflaton

Abrupt end of reheating

Dicke model during reheating

- Super-radiance becomes possible when $ImD \rightarrow const.$ (phase aligned)
 - Analogy: atoms \leftrightarrow harmonic oscillators of inflaton
 - Number of oscillator per Hubble volume: $N_\phi \sim n_\phi/H^3 \sim \rho_\phi/m_\phi H^3 \sim 10^{12}$
- Excitation and de-excitation of the oscillators may be described by the algebra of the total angular momentum [Dicke '53]
 - $\bullet~$ For the $a{\rm th}$ oscillator, $[R^{(a)}_i,R^{(a)}_j]=i\epsilon_{ijk}R^{(a)}_k$
 - Raising/lowering ops. $R_{\pm}^{(a)}=R_1^{(a)}\pm iR_2^{(a)}$ to describe excitation and de-excitation
 - For the entire system, $R_i = \sum_{a=1}^{\mathcal{N}_{\phi}} R_i^{(a)}$, satisfying $[R_i, R_j] = i\epsilon_{ijk}R_k$



[Gross, Haroche '82]

• System expressed as the eigenstate of R^2 and R_3 :

$$\begin{split} R^2|J,M\rangle &= J(J+1)|J,M\rangle,\\ R_3|J,M\rangle &= M|J,M\rangle \end{split}$$

• $J \sim \mathcal{N}$ (number of excited states):

 $\mathcal{N} \sim \mathcal{N}_{\phi} \times \mathcal{M}_P/m_{\phi} \sim 10^{15}$

number of oscillators

number of levels

Evolution of population probability

The probability $P_M(t)$ of finding the system at $|J, M\rangle$:

$$\frac{dP_M}{dt} = \gamma \left(\underbrace{|\langle J, M+1|R^+|J, M\rangle|^2 P_{M+1}}_{\text{populate } M \text{ state by annihilating } M+1 \text{ state}} - \underbrace{|\langle J, M-1|R^-|J, M\rangle|^2 P_M}_{\text{annihilate } M \text{ state}} \right)$$



- γ : the decay rate of a single inflaton oscillator
- $R^{\pm} \equiv R_1 \pm i R_2$: excitation and de-excitation operators
- $\bullet \hspace{0.1 in} |\langle J,M\pm 1|R^{\pm}|J,M\rangle|^2 = (J\mp M)(J\pm M+1)$

• Initial condition:
$$P_M(t=0) = \delta_{J,M}$$

Stays $M \sim J$ until $J\gamma t \sim 6$, then quickly decays to reach the grand state

Delay time and the end of reheating

- **D**uration to deplete all excited states (delay time t_D)
 - 2n = J M photons are emitted
 - Decay rate of $M \to M 1$: $\Gamma_{M \to M 1} = \gamma (J + M)(J M + 1) \sim \gamma Jn \sim \gamma \mathcal{N}n$
 - $t_1 = (\gamma \mathcal{N})^{-1}, t_2 = (2\gamma \mathcal{N})^{-1}, t_3 = (3\gamma \mathcal{N})^{-1}, \dots$

$$t_D \sim t_1 + t_2 + t_3 + \dots + t_N \sim \frac{\ln \mathcal{N}}{\mathcal{N}} \times \frac{1}{\gamma} \ll \frac{1}{\gamma}$$



 Intensity (number of photons emitted per unit time)

$$I(t) = -\frac{d}{dt} \langle M \rangle = -\frac{d}{dt} \sum_{M=-J}^{J} M P_M(t)$$

• Peak at $t \sim t_D$

- $\gamma_{\rm eff} \sim \gamma \times \mathcal{N} / \ln \mathcal{N}$
- Crudely, $T_{\rm RH} \sim \sqrt{\gamma M_P} \times (\mathcal{N}/\ln \mathcal{N})^{1/2}$

Summary



Summary

- Reheating by super-radiance is proposed
- The phase of decay products is aligned during preheating, leading to the super-radiance
- Super-radiant decay of inflaton is faster by a factor of $\ln \mathcal{N}/\mathcal{N}$ than the spontaneous decay
- Outlook
 - More precise study is needed (e.g. expansion rate, backreaction, etc)
 - De-phasing effects should be incorporated (e.g. interactions among decay products)
 - Implications (e.g. DM, BAU, etc)