

La taille des noyaux lourds sous la loupe de la spectroscopie laser

Benjamin Bally

Journée P2I - Orsay - 27/11/2024



Article

Smooth trends in fermium charge radii and the impact of shell effects

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The quantum-mechanical nuclear-shell structure determines the stability and limits of the existence of the heaviest nuclides with large proton numbers $Z \geq 300$ (refs. 1–3). Shell effects also affect the sizes and shapes of atomic nuclei, as shown by laser spectroscopy studies in lighter nuclides⁴. However, experimental information on the

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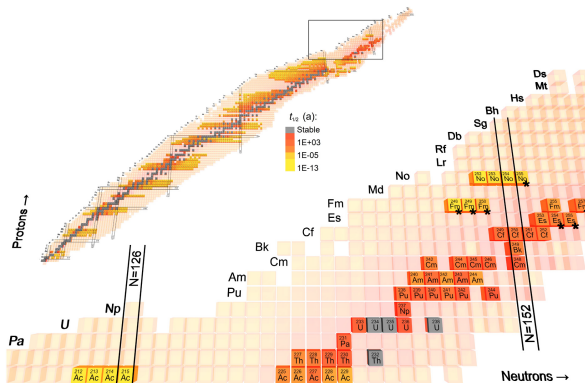
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- Article recently published: Warbinek *et al.*, *Nature* 634, 1075 (2024)
- Contribution from CEA (DRF and DAM)
 - ◇ **Experimental:** M. Vandebruslé, E. Rey-Herme, H. Savajols, N. Lecaene
 - ◇ **Theoretical:** B. Bally, S. Hilaire, S. Péru

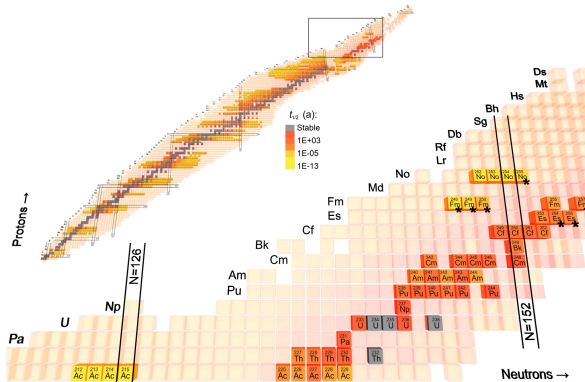
- Major line of research in modern nuclear physics
 - ◊ Rich variety of emergent phenomena (deformation, isomerism, fission, etc.)
 - ◊ What is the heaviest element in the periodic table?



Block, Prog. Part. Nucl. Phys. 116 (2021)

Context: study of heavy and superheavy atomic nuclei

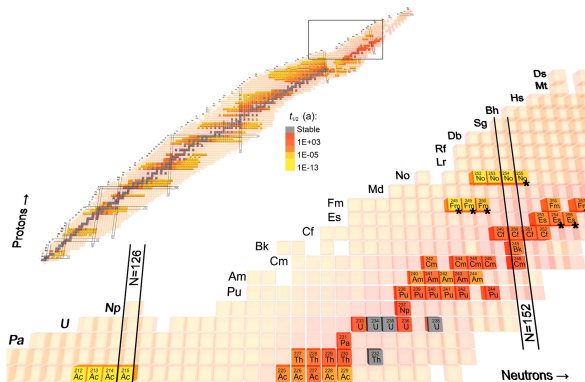
- Major line of research in modern nuclear physics
 - ◊ Rich variety of emergent phenomena (deformation, isomerism, fission, etc.)
 - ◊ What is the heaviest element in the periodic table?
- Difficulty: production cross sections are small



Block, Prog. Part. Nucl. Phys. 116 (2021)

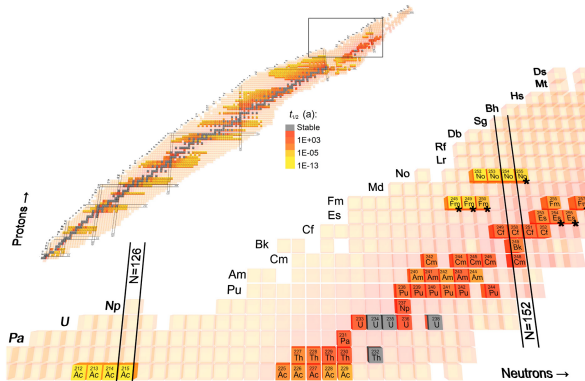
- Experimental techniques:

- ◇ Decay spectroscopy
- ◇ Laser spectroscopy
- ◇ ...



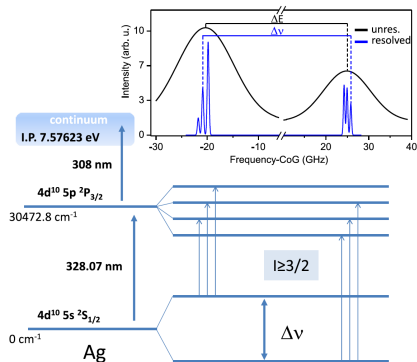
Block, Prog. Part. Nucl. Phys. 116 (2021)

- Experimental techniques:
 - ◊ Decay spectroscopy
 - ◊ Laser spectroscopy
 - ◊ ...
- Laser spectroscopy: expertise of the RADRIS collaboration at GSI



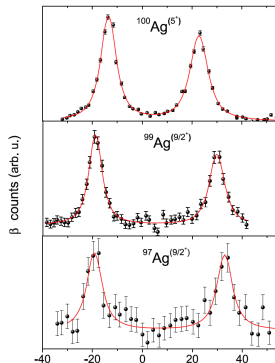
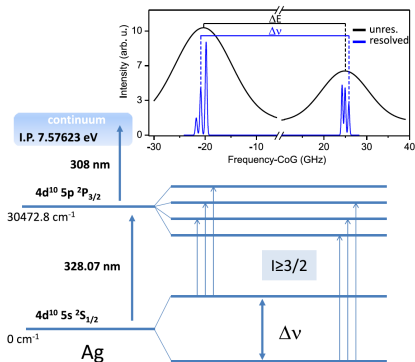
Block, Prog. Part. Nucl. Phys. 116 (2021)

- Example of Ag isotopes
 - ◊ Two-steps ionization scheme
 - ◊ Scan of transition λ_1
 - ◊ Count the number of ions as a function of the frequency λ_1

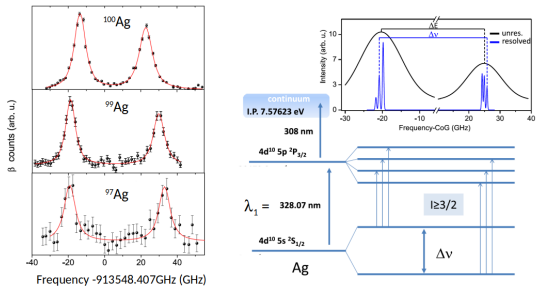


Ferrer, PLB 728, 191 (2014)

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Ferrer, PLB 728, 191 (2014)



Que mesure-t-on ?

Décalage isotopique/isomérique

Structure hyperfine

Que déduit-on ?

(indépendamment des modèles nucléaires)

Rayon de charge

Moment E quadrupolaire

Moment M dipolaire

Spins

Que déduit-on ?

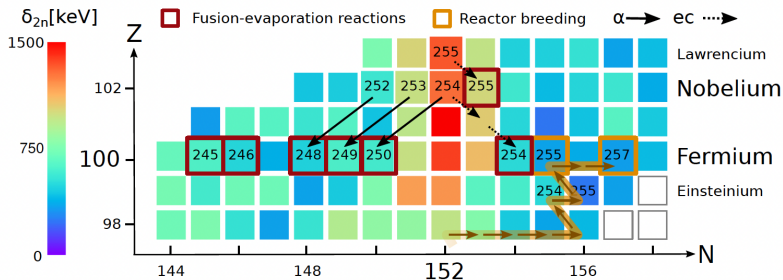
(dépendant des modèles nucléaires)

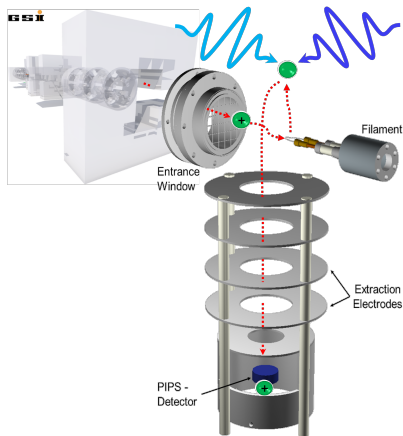
Forme/Paramètre de déformation

Configuration orbitales particules individuelles

- Combination of several production methods:

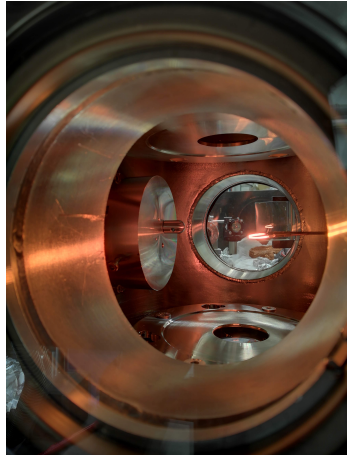
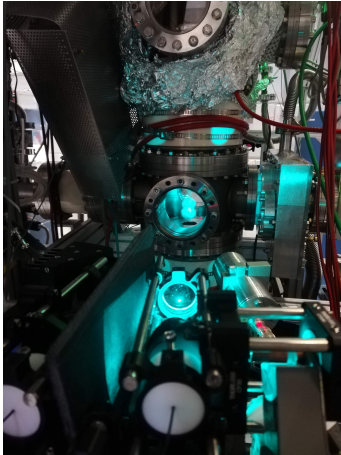
- Direct fusion-evaporation: $^{208}\text{Pb}(^{40}\text{Ar}, 2-3n)^{245,246}\text{Fm}$
- Indirect fusion-evaporation: $^{206,207,208}\text{Pb}(^{48}\text{Ca}, 2n)^{252,253,254}\text{No}$
- Re-irradiation of samples collected in nuclear reactor: $^{255,257}\text{Fm}$





Courtesy of S. Raeder

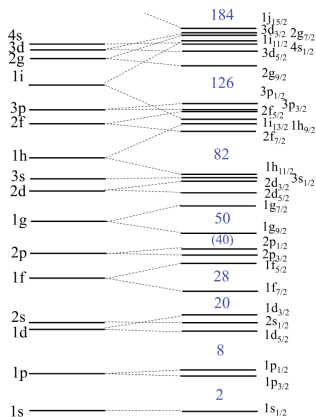
- Laser spectroscopy of 8 isotopes thanks to the RADRIS technique



Courtesy of A. Raggio and J. Warbinek

- Nucleon magic numbers: 2, 8, 20, 28, 50, 82, ...

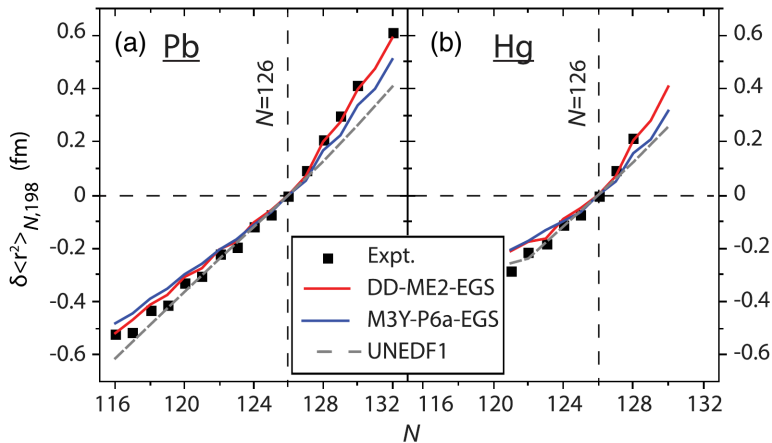
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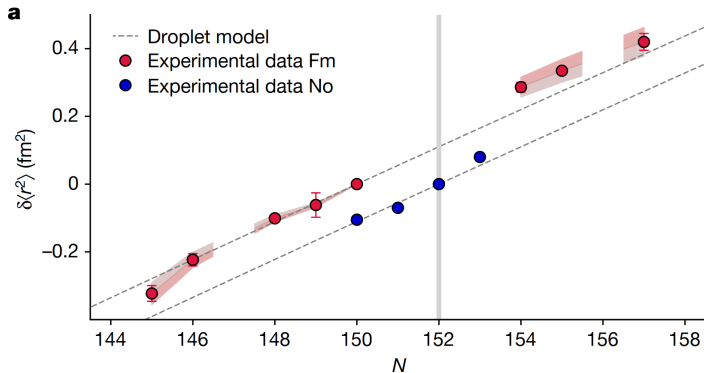
Hagino, Found. Chem. 22, 267 (2020)

-
- Energy level diagram for the hydrogen atom showing the correspondence between principal quantum number n and the number of states. The diagram shows levels for $n=1$ to $n=4$, with each level splitting into l and m sub-levels. The total number of states for each n is given in blue: 2 for $n=1$, 8 for $n=2$, 18 for $n=3$, and 32 for $n=4$. The levels are labeled with quantum numbers on the left and right, with dashed lines connecting them.
- | Principal Quantum Number (n) | Sub-levels (l, m) | Total Number of States |
|----------------------------------|-----------------------|------------------------|
| 4 | 4s, 3d, 2g, 1i | 32 |
| 3 | 3p, 2f, 1h | 18 |
| 2 | 2s, 1d | 8 |
| 1 | 1s | 2 |

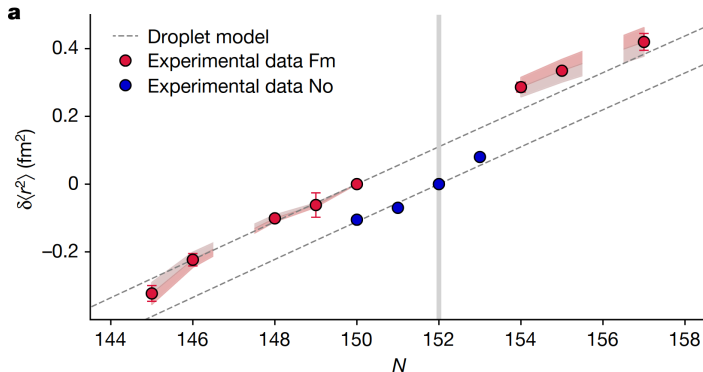
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Day Goodacre, PRL 126, 032502 (2021)



- Slight increase but no clear “kink” contrary to lighter nuclei
- Good agreement with simple liquid drop model: $r \propto A^{1/3}$



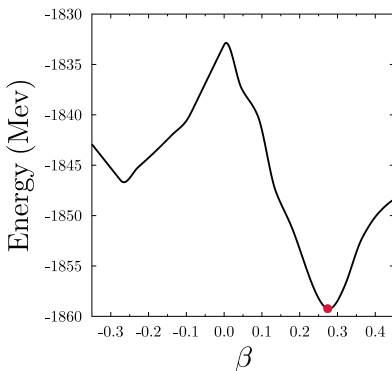
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→ Towards a more **macroscopic** behavior of nuclear matter?

- Phenomenological interactions (Skyrme, Gogny, Fayans)

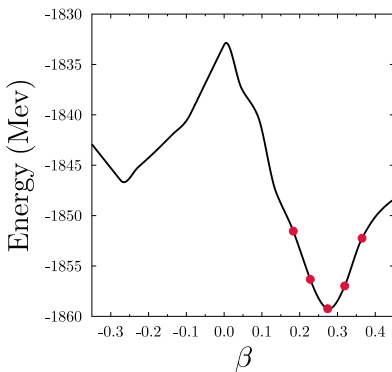
- Phenomenological interactions (Skyrme, Gogny, Fayans)
- Single-Reference Energy Density Functional (SR-EDF)
≡ “Mean field”, “Hartree-Fock-Bogoliubov”

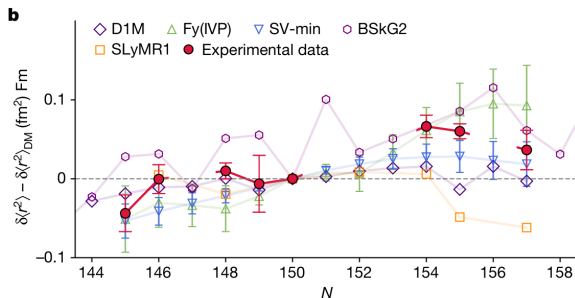
$$\delta\langle\Phi|H_{\text{eff}}|\Phi\rangle = 0$$



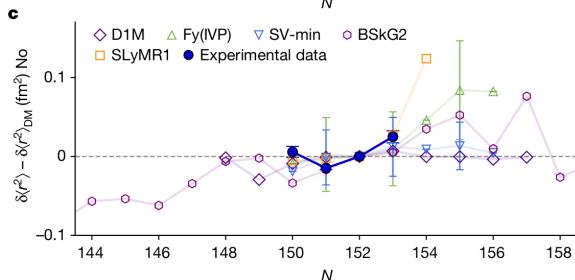
- Phenomenological interactions (Skyrme)
- **Multi-Reference** Energy Density Functional (MR-EDF)
≡ “Beyond the mean field”, “Generator Coordinate Method”

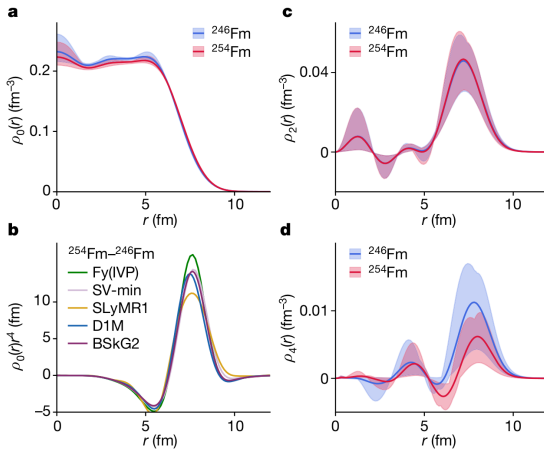
$$|\Psi^\Lambda\rangle = \sum_k f_k P^\Lambda |\Phi_k\rangle$$
$$\delta \langle \Psi^\Lambda | H_{\text{eff}} | \Psi^\Lambda \rangle = 0$$

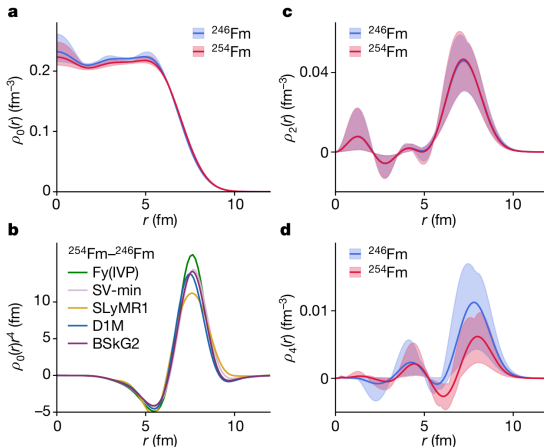




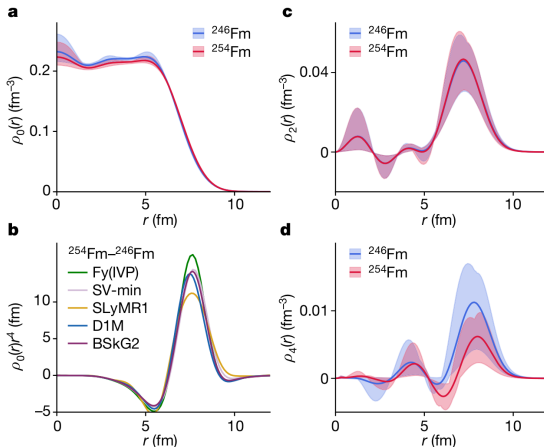
$$\frac{\Delta r^2 = 0.1}{r^2 = 36} \approx 0.3\%$$



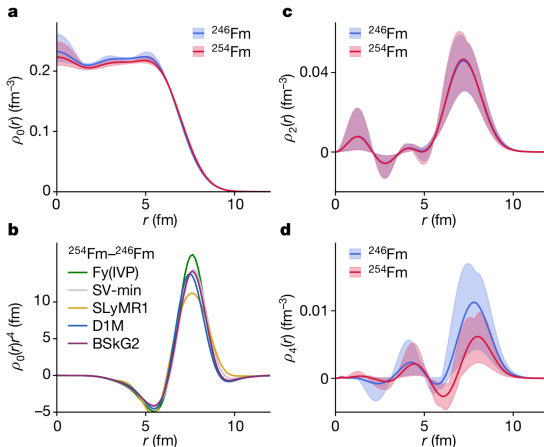




- Proton density of ^{246}Fm et ^{254}Fm very similar $[\rho_0(r) = \int \rho_p(\mathbf{r}) Y_{00}(\Omega) d\Omega]$



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- Same quadrupole deformations $[\rho_2(r) = \int \rho_p(\mathbf{r}) Y_{20}(\Omega) d\Omega]$
- Different hexadecapolar deformations $[\rho_4(r) = \int \rho_p(\mathbf{r}) Y_{40}(\Omega) d\Omega]$

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 - ◊ Moments: dipole magnetic (μ) and quadrupole electric (Q_5) of odd-mass nuclei
 - ◊ Physics case of S^3 at GANIL (Caen)



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 - ◇ Physics case of S^3 at GANIL (Caen)
 - ◇ Unique possibilities of MR-EDF calculations

