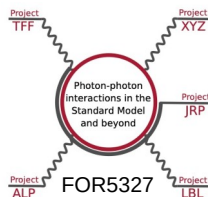


Experimental input from **BESIII** for the HLbL contribution

8th Plenary Workshop of the Muon $g-2$ Theory Initiative

2025-09-11 | Christoph Florian Redmer



DFG Deutsche
Forschungsgemeinschaft

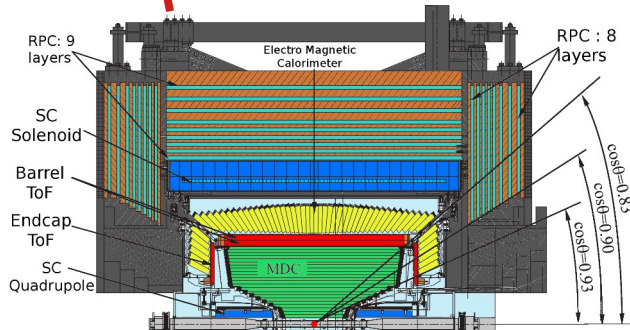
JOHANNES GUTENBERG
UNIVERSITÄT MAINZ



BESIII at BEPCII



- Center-of-mass energies from 2 – 5 GeV
- Design luminosity exceeded: $1.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ at 3.77 GeV



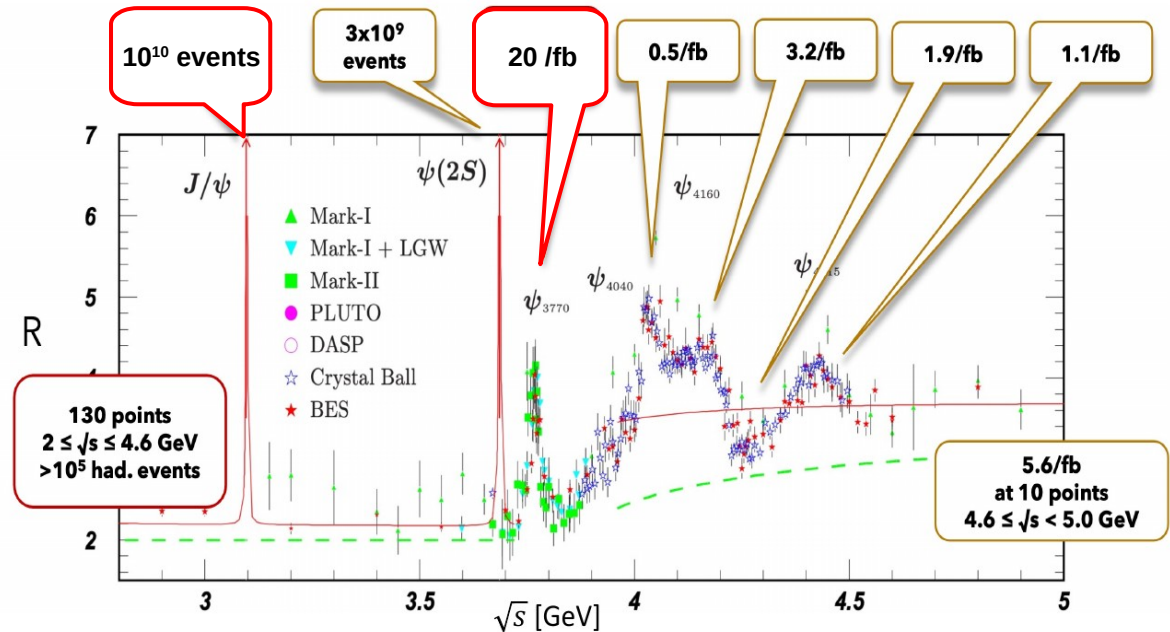
Time of Flight

EM Calorimeter

Muon Counter

Drift Chamber

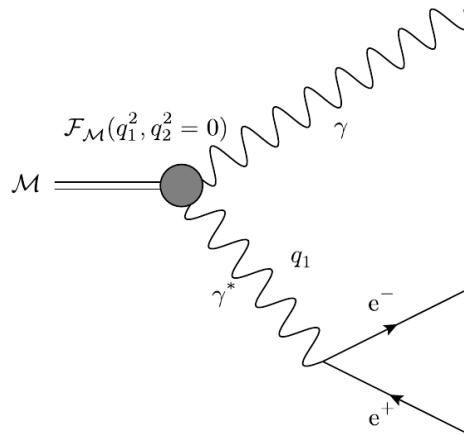
Solenoid



Worlds largest τ -charm data sets in e^+e^- collisions

Experimental Access to TFFs

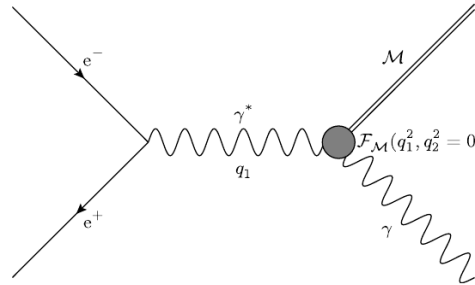
Meson Dalitz Decays



$$m_{ll}^2 < q^2 < m_P^2$$

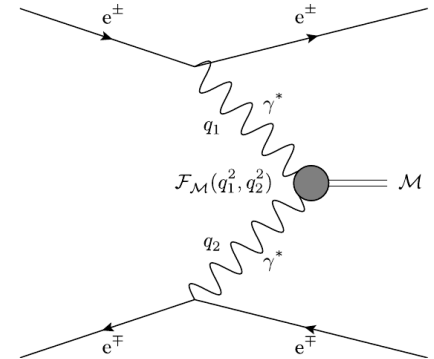
time-like

Radiative Meson Production



$$q^2 = s; \quad q^2 > m_P^2$$

Two-photon collisions



$$q_1^2 = -Q_1^2; \quad q_2^2 = -Q_2^2$$

space-like

“Wish Lists” from WPs 20 & 25

Table 14

Priorities for new experimental input and cross-checks.

issue	experimental input [I] or cross-checks [C]
axials, tensors, higher pseudoscalars missing states	$\gamma^{(*)}\gamma^* \rightarrow 3\pi, 4\pi, K\bar{K}\pi, \eta\pi\pi, \eta'\pi\pi$ [I] inclusive $\gamma^{(*)}\gamma^* \rightarrow$ hadrons at 1–3 GeV [I]
dispersive analysis of $\eta^{(\prime)}$ TFFs	$e^+e^- \rightarrow \eta\pi^+\pi^-$ [I] $\eta' \rightarrow \pi^+\pi^-\pi^+\pi^-$ [I] $\eta' \rightarrow \pi^+\pi^-e^+e^-$ [I] $\gamma\pi^- \rightarrow \pi^-\eta$ [C]
dispersive analysis of π^0 TFF	$\gamma\pi \rightarrow \pi\pi$ [I] high accuracy Dalitz plot $\omega \rightarrow \pi^+\pi^-\pi^0$ [C] $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ [C] $\omega, \phi \rightarrow \pi^0 l^+ l^-$ [C]
pseudoscalar TFF pion, kaon, $\pi\eta$ loops (including scalars and tensors)	$\gamma^{(*)}\gamma^* \rightarrow \pi^0, \eta, \eta'$ at arbitrary virtualities [I,C] $\gamma^{(*)}\gamma^* \rightarrow \pi\pi, K\bar{K}, \pi\eta$ at arbitrary virtualities, partial waves [I,C]

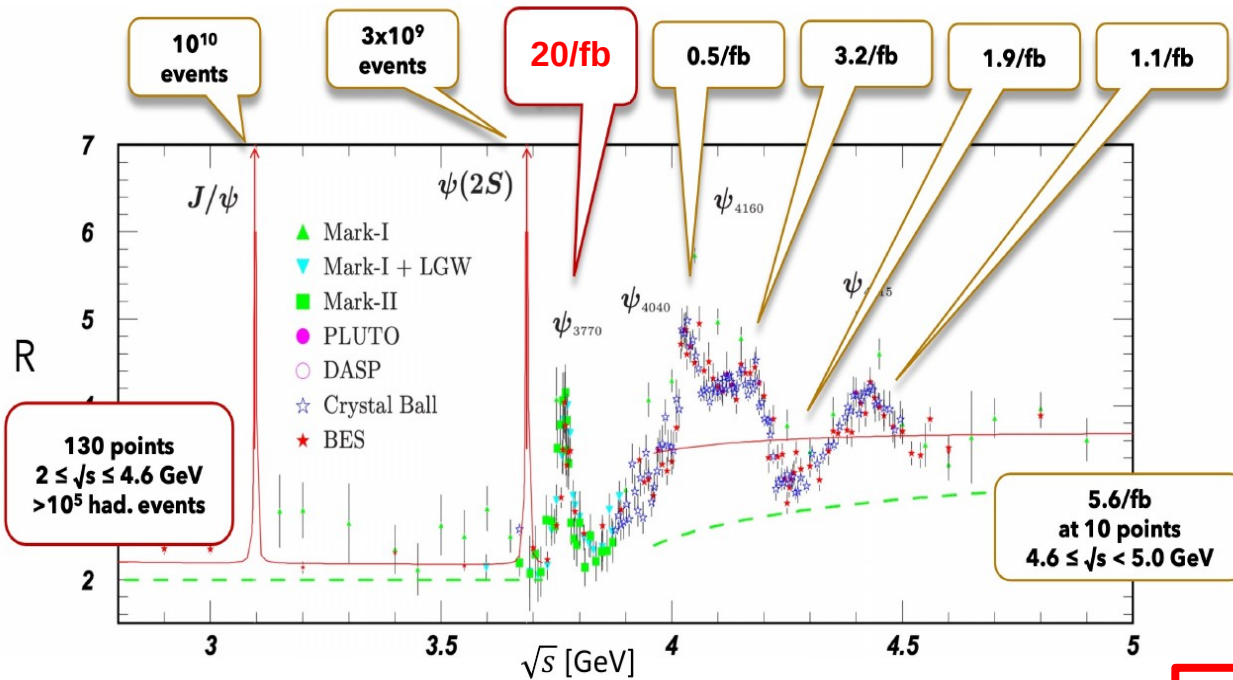
	Experimental input
	$e^+e^- \rightarrow e^+e^-A, A = f_1, f_1', a_1$
Axial-vector TFFs	Radiative decays $A \rightarrow V\gamma, V = \rho, \omega, \phi$ Dilepton decays $A \rightarrow e^+e^-$
Scalar and tensor TFFs	$\gamma^*\gamma^{(*)} \rightarrow \pi\pi, \pi\eta, \bar{K}K, \pi\pi\pi$
Pseudoscalar TFFs	$\gamma\gamma \rightarrow \eta, \eta'$ $e^+e^- \rightarrow e^+e^-(\gamma^*\gamma^{(*)} \rightarrow \pi^0, \eta, \eta')$ $e^+e^- \rightarrow e^+e^-(\gamma\gamma \rightarrow P), P = \pi(1300), \eta(1295), \eta(1405)$

Table 30: Examples of useful experimental inputs related to the exclusive hadronic channels.

Phys.Rept. 887 (2020) 1 – 166

arXiv:2505.21476

$\gamma^{(*)}\gamma^*$ results to be expected from BESIII



Worlds largest τ -charm data sets in e^+e^- collisions

- Richest data above open charm threshold
- Access to
 - Hadronic masses up to 2 GeV
 - $0.2 \leq Q^2 [\text{GeV}^2] \leq 3$
- Access to smaller Q^2 values at $\sqrt{s} \approx 2 \text{ GeV}$ (limited statistics)

New data at 3.77 GeV most relevant!

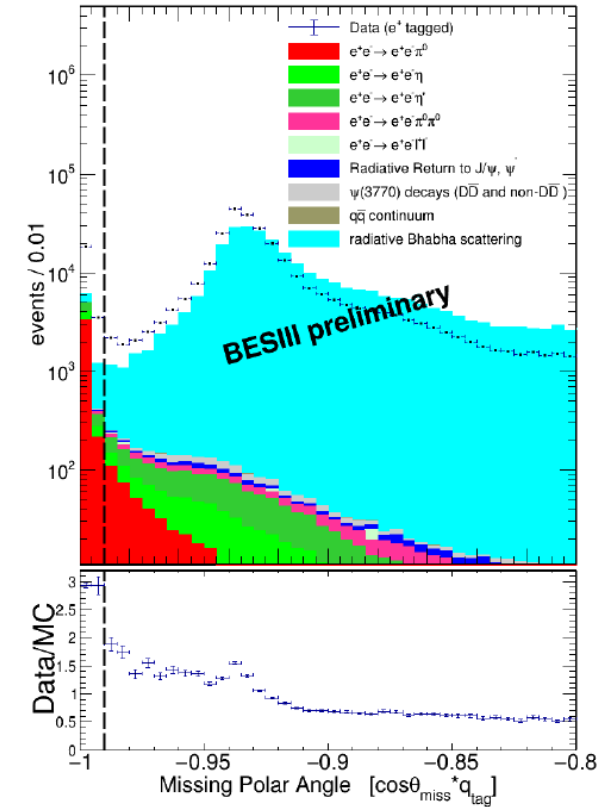
Data taking finished June 2024

$$\gamma^{(*)}\gamma^* \rightarrow \pi^0, \eta, \eta'$$

2.9 fb⁻¹, 3.773 GeV

Two-photon collision events:

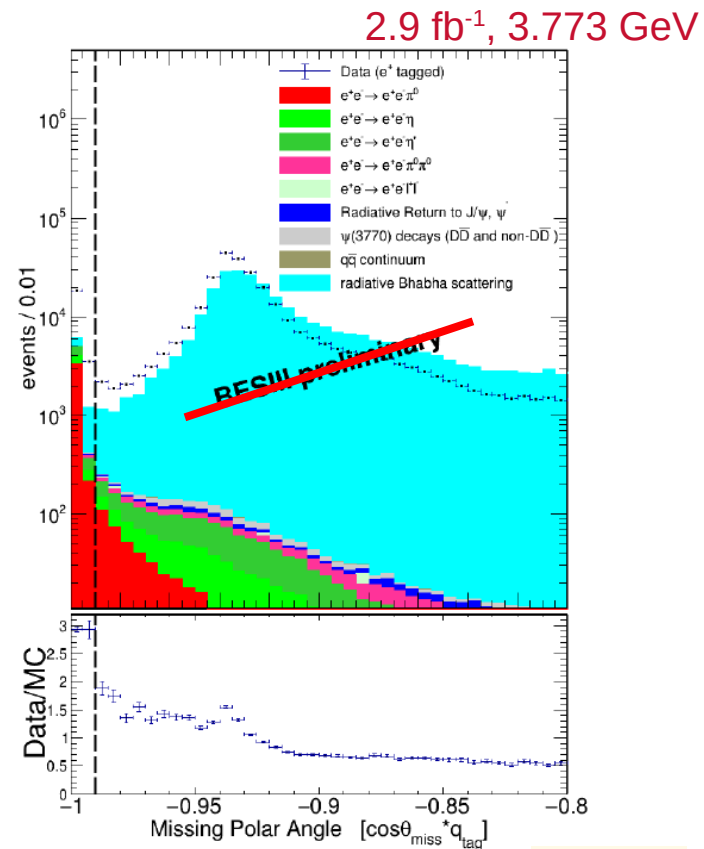
- Single-tag measurements
 - Require one quasi-real photon
- Select
 - One scattered lepton & meson decay products
 - Require small scattering angle of missing momentum



$$\gamma\gamma^* \rightarrow \pi^0$$

Two-photon collision events:

- Single-tag measurements
 - Require one quasi-real photon
- Select
 - One scattered lepton & meson decay products
 - Require small scattering angle of missing momentum



arXiv:2509.07685

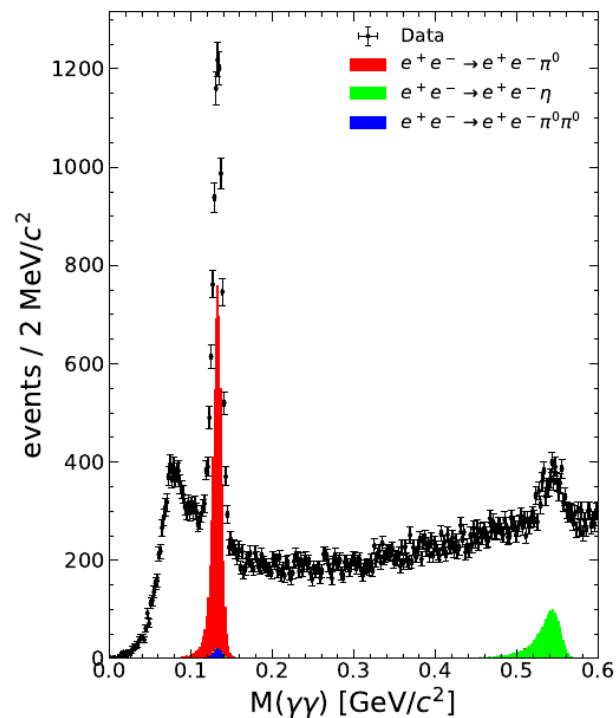
BESIII

$$\gamma\gamma^* \rightarrow \pi^0$$

Two-photon collision events:

- Single-tag measurements
 - Require one quasi-real photon
- Select
 - One scattered lepton & meson decay products
 - Require small scattering angle of missing momentum
- Reduce background by adequate conditions

2.9 fb⁻¹, 3.773 GeV



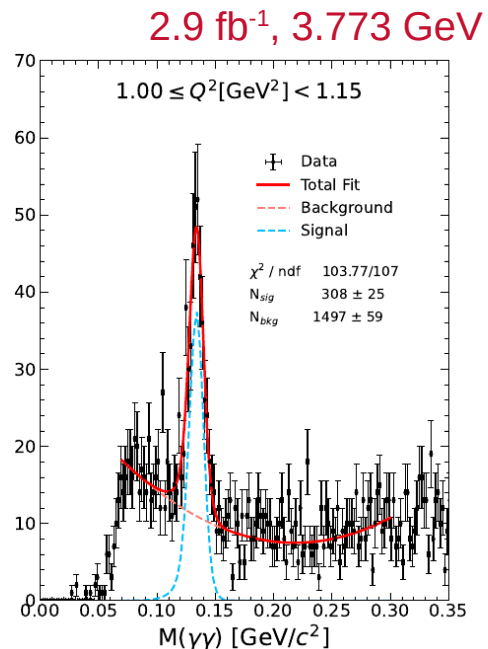
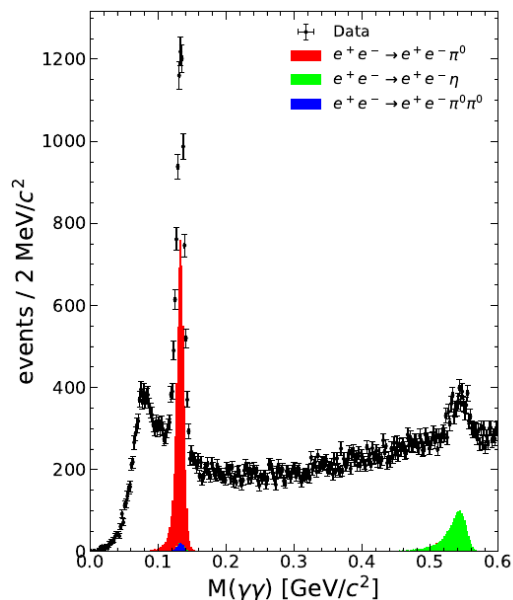
arXiv:2509.07685

BESIII

$$\gamma\gamma^* \rightarrow \pi^0$$

Two-photon collision events:

- Single-tag measurements
 - Require one quasi-real photon
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- Reduce background by adequate conditions
- Subtract background in bins of Q^2



arXiv:2509.07685

BESIII

$$\gamma\gamma^* \rightarrow \pi^0$$

Two-photon collision events:

- Single-tag measurements
 - Require one quasi-real photon
- Select
 - One scattered lepton & meson decay products
 - Require small scattering angle of missing momentum
- Reduce background by adequate conditions
- Subtract background in bins of Q^2

$$|\mathcal{F}(Q^2)|^2 = \frac{N_{\text{sig}}}{\Delta Q^2 \mathcal{L} \varepsilon (1 + \delta) \mathcal{B}_{\gamma\gamma}} \left(\frac{d\sigma_{WZW}}{dQ^2} \right)^{-1}$$

- Divide by point-like cross section
- Correct for radiative effects
- Correct for impact of finite 2nd virtuality

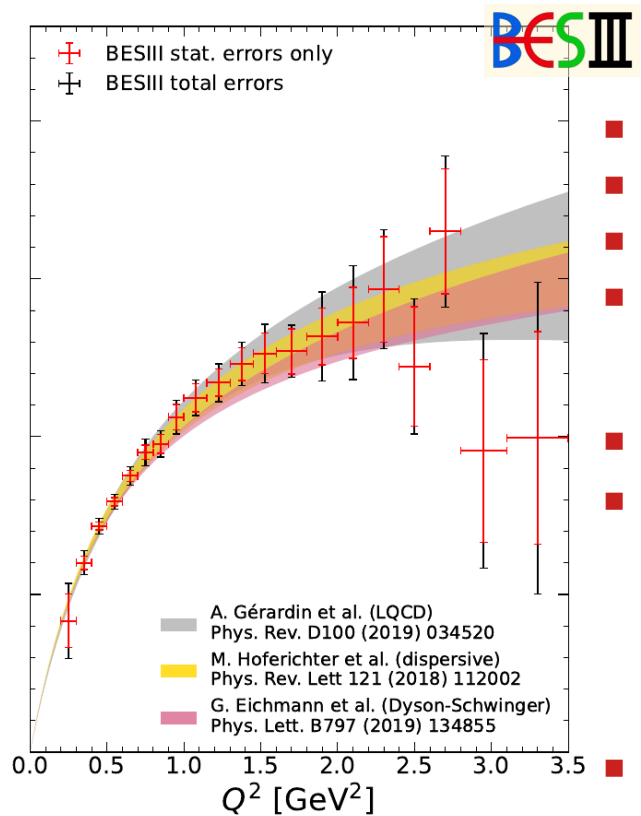
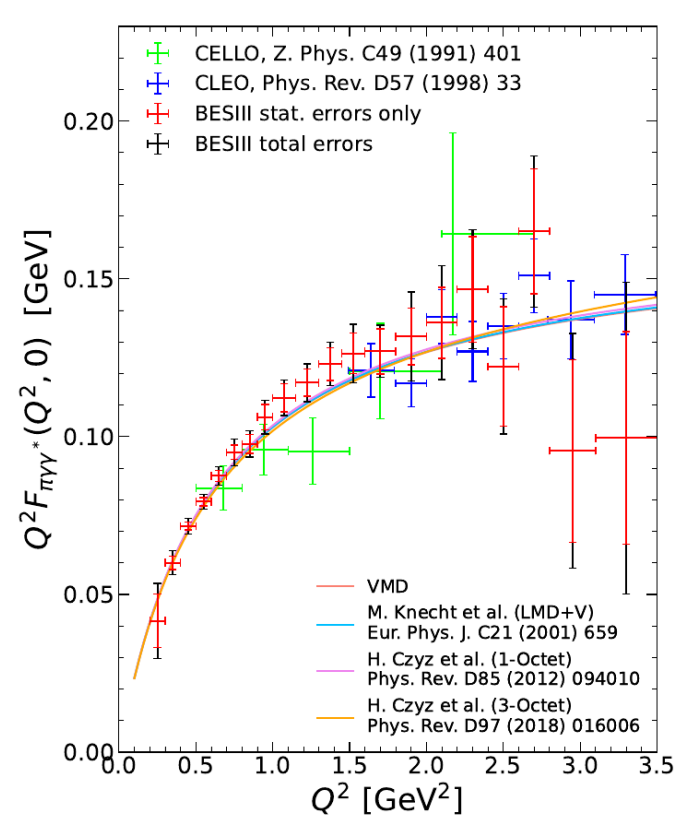
- Radiative effects at full NLO in Ekhar3.0
- NNLO calculations missing!
- Rule of thumb estimate suggested by Henryk:
 - 10% of reconstructed LO-NLO difference
- 1% uncertainty

- Comparison with TFF models for $|\mathcal{F}(Q^2, 0)|$
- Consistent deviation of 2% found

arXiv:2509.07685

BESIII

$$\gamma\gamma^* \rightarrow \pi^0$$



BESIII

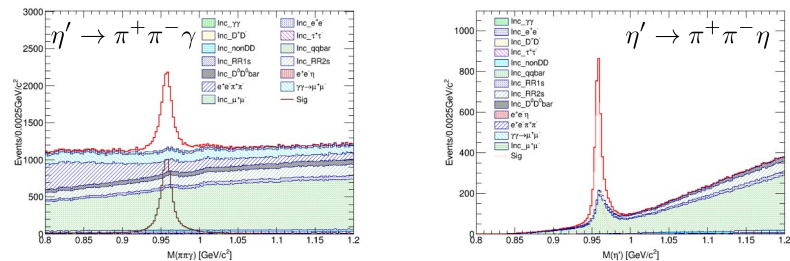
2.9 fb⁻¹, 3.773 GeV

- Largest systematics at $Q^2 < 0.3; > 2.7 \text{ GeV}^2$
- Statistically limited
- Agreement with previous measurements
- Significant improvement below 1.5 GeV²
- models deviate around 1.2 GeV² by 1σ
- Good agreement with
 - Lattice QCD
 - Dispersive construction
 - Dyson-Schwinger
- To be repeated on full 20 fb⁻¹ data set

arXiv:2509.07685

$$\gamma\gamma^* \rightarrow \eta, \eta'$$

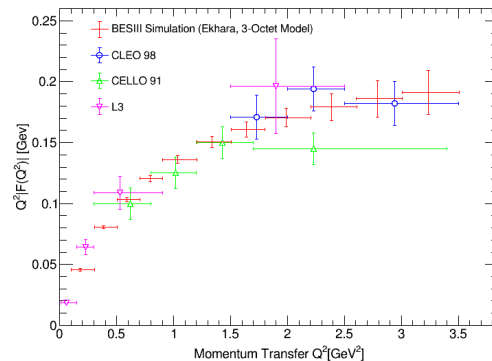
- Full 20 fb⁻¹ data
- Single-tag analysis using kinematic fit
- Using two decay modes



- Radiative corrections with Ekhara3.0
 - Rule-of-thumb estimate does not seem to work!
 - NNLO corrections needed!

Simulations using full 20 fb⁻¹

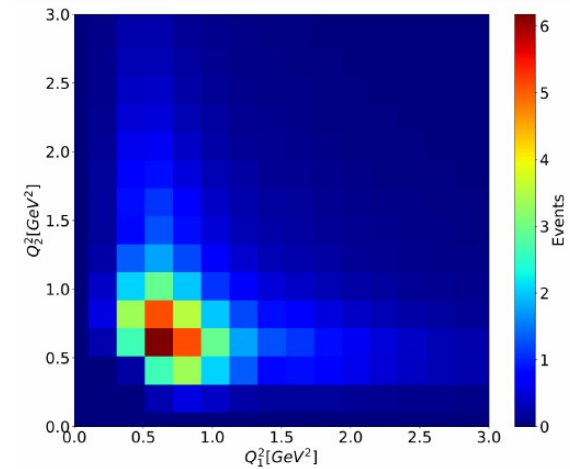
- First direct measurement at Q² < 0.3 GeV²
- Significant improvement compared to existing data expected



$$\gamma^* \gamma^* \rightarrow \pi^0, \eta, \eta'$$

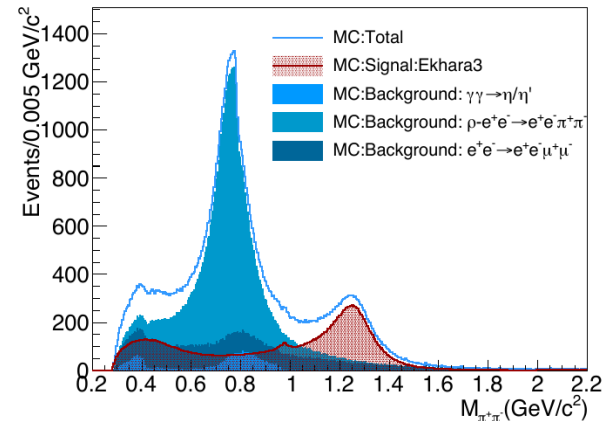
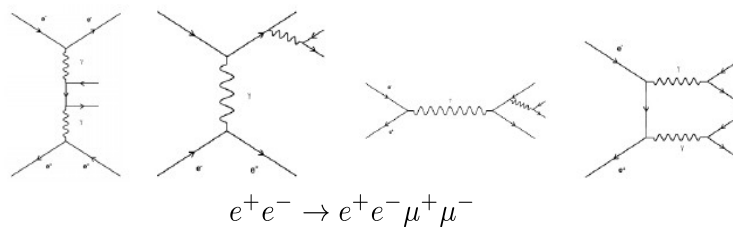
- Full 20 fb⁻¹ data
- Begin with $\gamma^* \gamma^* \rightarrow \eta, \eta'$
 - Favorable background situation
- Feasibility studies performed
- Results at $Q_1^2 \approx Q_2^2 \approx 1 \text{ GeV}^2$ expected
- s-channel process needs to be understood
- Data analysis ongoing for $\gamma^* \gamma^* \rightarrow \eta, \eta'$
- Follow-up: $\gamma^* \gamma^* \rightarrow \pi^0$

Simulation of expected yields
for 13 fb⁻¹ of data at $\sqrt{s} \geq 3.773 \text{ GeV}$

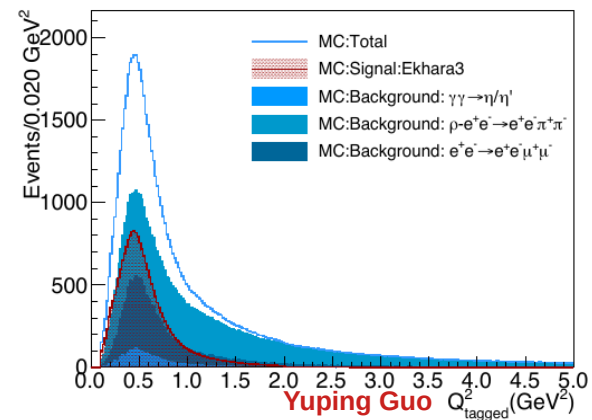
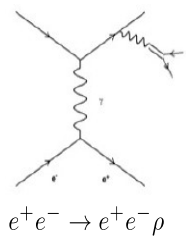


$$\gamma\gamma^* \rightarrow \pi^+\pi^-$$

- Classic single-tag event selection
- Background
 - Muon production



- Time-like pion production

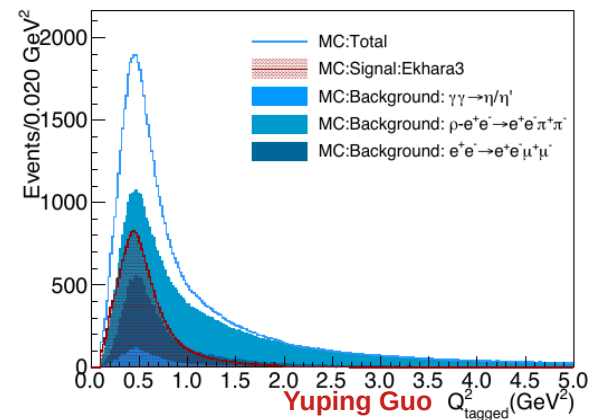
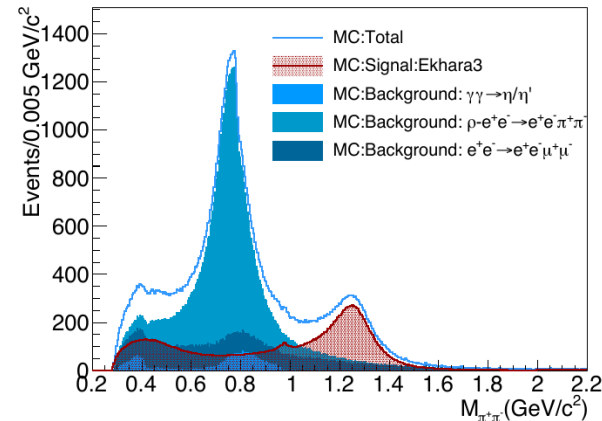


$$\gamma\gamma^* \rightarrow \pi^+\pi^-$$

- Classic single-tag event selection
- Background
 - Muon production \rightarrow machine learning for separation
 - Time-like pion production \rightarrow precise/tuned event generators to subtract distributions

- Invariant masses from threshold to 2 GeV
- $0.2 \leq Q^2 [\text{GeV}^2] \leq 3$
- Full coverage of helicity angle

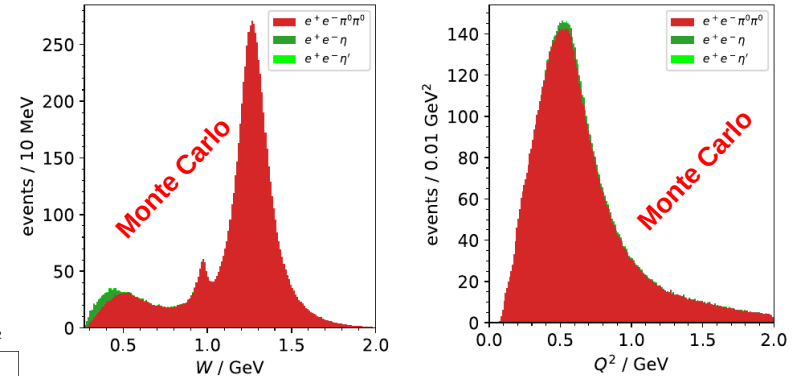
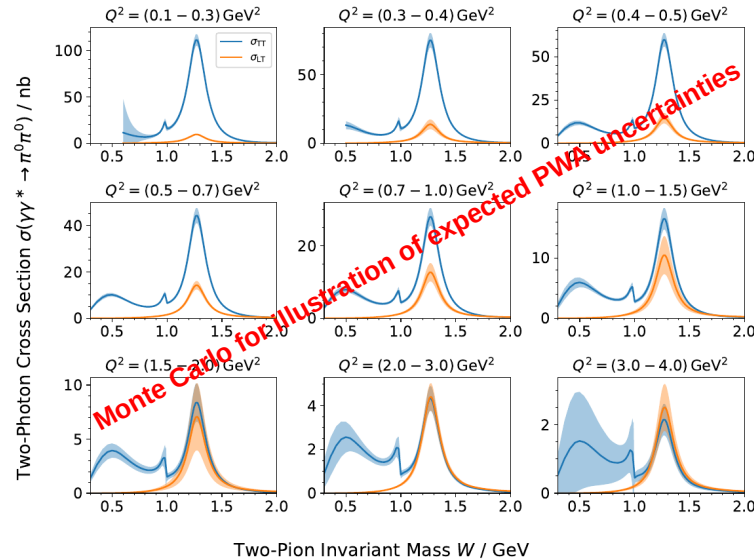
- Analysis transferred to new 20fb^{-1} data set
 - Reduced systematic effects
 - New training of PID time consuming



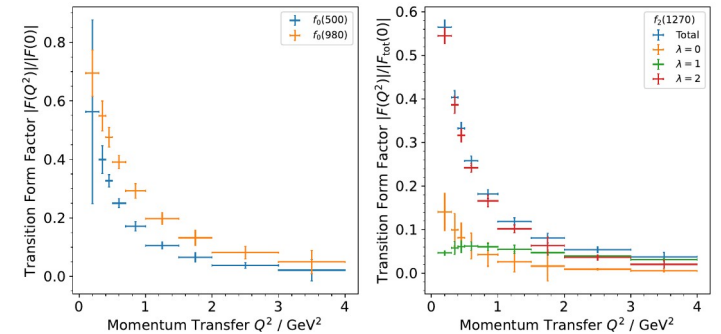
Yuping Guo

$$\gamma\gamma^* \rightarrow \pi^0 \pi^0$$

- Full new 20 fb⁻¹ data
- New strategy: Kinematic fit with missing track
 - improved resolution of 2nd virtuality
- Similar parameter ranges as for $\gamma\gamma^* \rightarrow \pi^+ \pi^-$
 - $0.3 \leq W[\text{GeV}] \leq 2$
 - $0.1 \leq Q^2[\text{GeV}^2] \leq 4$
 - $|\cos \theta^*| \leq 1$



p-pole TFF model for illustration of expected uncertainties



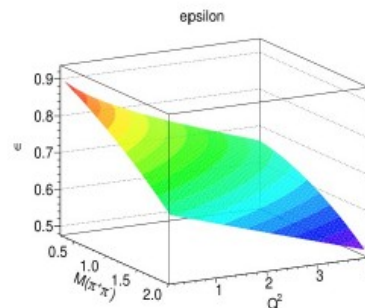
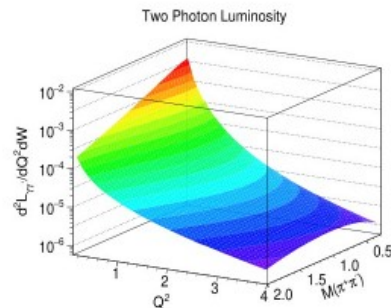
Two-photon cross section

Luminosity function needed to determine relevant cross sections

$$d\sigma_{ee} = \frac{\alpha^2}{16\pi^4 q_1^2 q_2^2} \sqrt{\frac{(q_1 \cdot q_2)^2 - q_1^2 q_2^2}{(p_1 \cdot p_2)^2 - m_e^4}} [4\rho_1^{++}\rho_2^{++}\sigma_{TT} + 2\rho_1^{++}\rho_2^{00}\sigma_{TL} + 2\rho_1^{00}\rho_2^{++}\sigma_{LT}] \frac{d^3p'_1 d^3p'_2}{E'_1 E'_2}$$

$$\frac{d^2\sigma_{ee}}{dQ^2 dW} = \frac{d\mathcal{L}_{\gamma\gamma}}{dQ^2 dW} (\sigma_{TT}(Q^2, 0, W) + \varepsilon\sigma_{TL}(Q^2, 0, W))$$

Analytic evaluation:



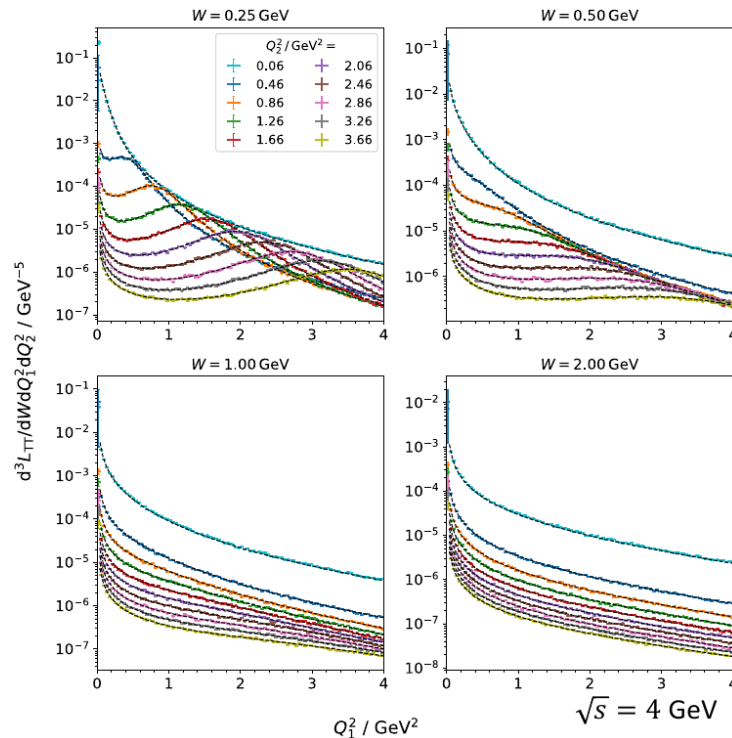
Using:
Phys. Rept. 15 (1975) 181
Nucl.Phys. B54 (1973) 573

Model dependent assumptions for finite 2nd virtuality necessary

Two-photon cross section

Numerical approach:

- Combine cross section equation with phase space generation algorithm by Schuler *et al.*



Agreement with analytic determination for all

- Energies
- Ranges of Q^2
- Hadronic masses

Two-photon cross section

Extend it to be an event generator for **Hadron** production in **Two-Photon Scattering**

- Allow for any number of particles
- Assume flat phase space distribution
- Need input for two-photon cross sections

Two-photon cross section

Extend it to be an event generator for Hadron production in Two-Photon Scattering

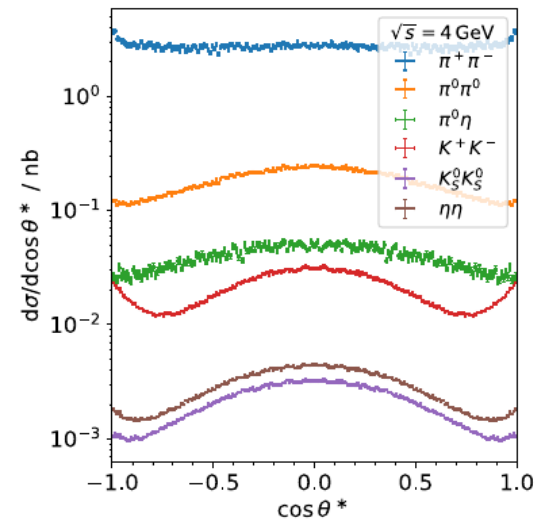
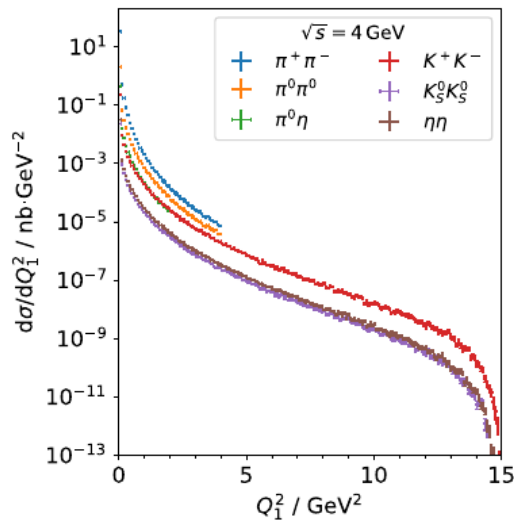
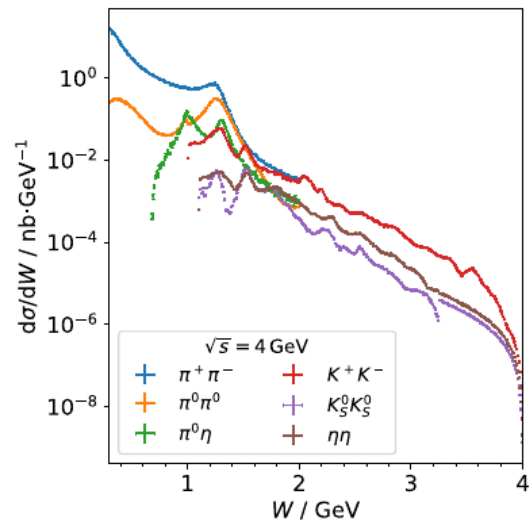
- Allow for any number of particles
- Assume flat phase space distribution
- Need input for two-photon cross sections
 - $\gamma\gamma \rightarrow \pi^+\pi^-/\pi^0\pi^0$ from dispersive analysis (Danilkin *et al.*, Phys.Rev.D 101 (2020) 054008)
 - $\gamma\gamma \rightarrow \pi^0\eta$ from dispersive analysis (Deneika *et al.*, Phys.Rev.D 111 (2025) 034009)
 - $\gamma\gamma \rightarrow \pi^+\pi^-\eta$ from phenomenology (Ren *et al.*, Phys. Rev. D 110 (2024) 094043)
 - Experimental results from Belle and BESIII on $K\bar{K}, \eta\eta$

Additional degree of freedom for two-body final states

- Formalism previously established for $e^+e^- \rightarrow e^+e^- X$
- Extended in collaboration with Marc Vanderhaeghen

Two-photon cross section

New event generator: **HadroTOPS**

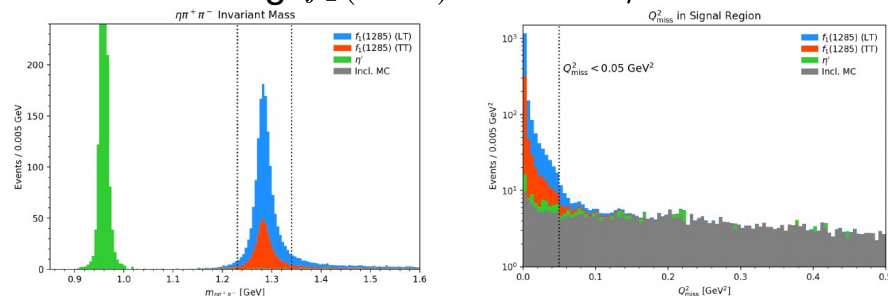


$\sqrt{s} = 4$ GeV

- Essential, since development of established generator (Ekhara) came to an end
- Publication in preparation

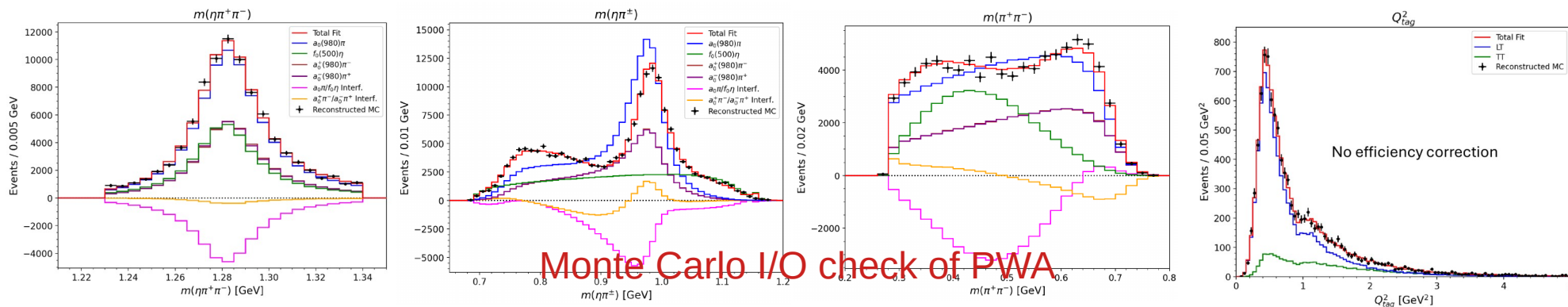
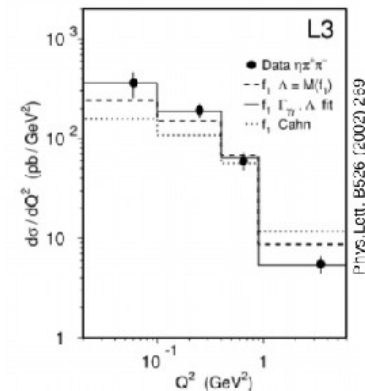
$$\gamma\gamma^* \rightarrow f_1(1285)$$

■ Reconstructing $f_1(1285) \rightarrow \pi^+\pi^-\eta$



- Possibility to separate helicity states from fit to angular distributions
- PWA required due to inseparable intermediate states $a_0^\pm(980)\pi^\mp \longleftrightarrow f_0(500)\eta$
- Amplitude based on Phys. Rev. D 110 (2024) 094043

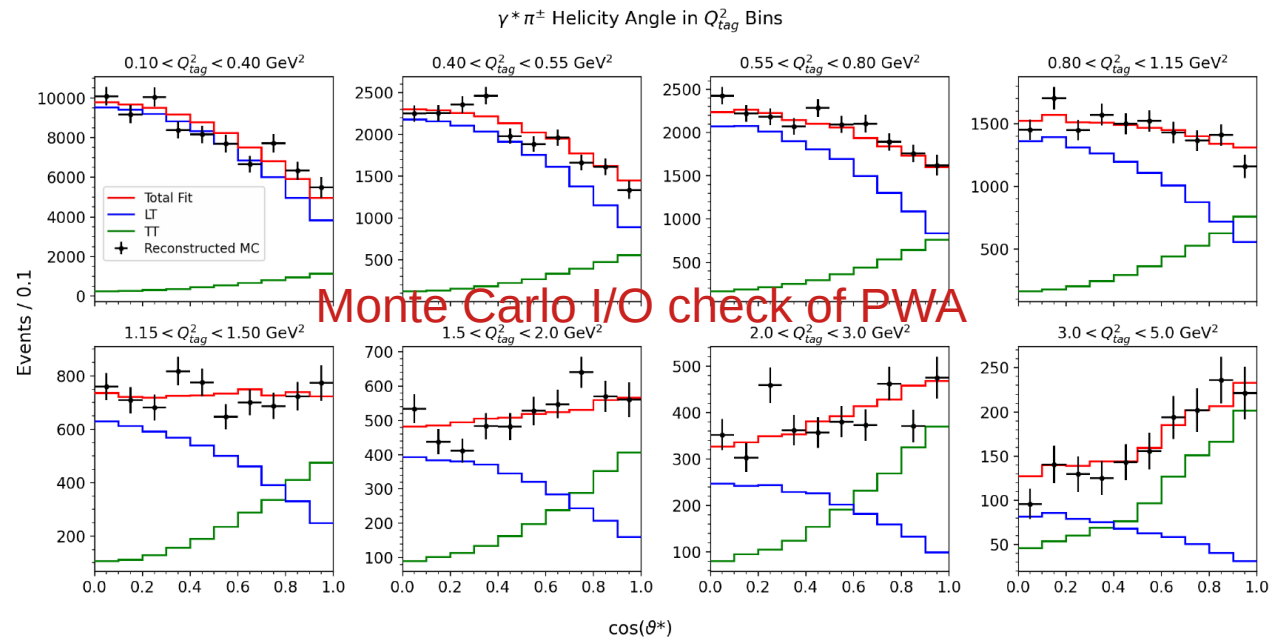
Only available data:



Monte Carlo I/O check of PWA

$$\gamma\gamma^* \rightarrow f_1(1285)$$

- Possibility to separate helicity states from fit to angular distributions



- Applied on full 20 fb⁻¹ data
- Systematic uncertainties under evaluation

See Poster of
Jan Muskalla

Summary

BESIII is an ideal laboratory to study two-photon reactions at $Q^2 \approx 1 \text{ GeV}^2$

- Single pseudoscalar meson TFFs
 - Single-tag measurements
 - $0.1 \leq Q^2 [\text{GeV}^2] \leq 5.0$
 - First TFF measurement released
 - High statistics results on π^0, η, η' in preparation
 - Double-tag measurements of π^0, η, η' in preparation
- Multi meson systems
 - Single-tag measurements
 - $\pi^0 \pi^0 / \pi^+ \pi^-$
 - masses from threshold to 2 GeV
 - virtualities from 0.2 to 2 GeV^2
 - full helicity angle coverage
 - $f_1(1285) \rightarrow \pi^+ \pi^- \eta$ with PWA to separate helicity amplitudes of TFF

arXiv:2509.07685

Development of new MC Generator facilitates studies of further multi meson systems

Summary

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arXiv:2509.07685

Preliminary results
by the end of this year!

Development of new MC Generator facilitates studies of further multi meson systems