

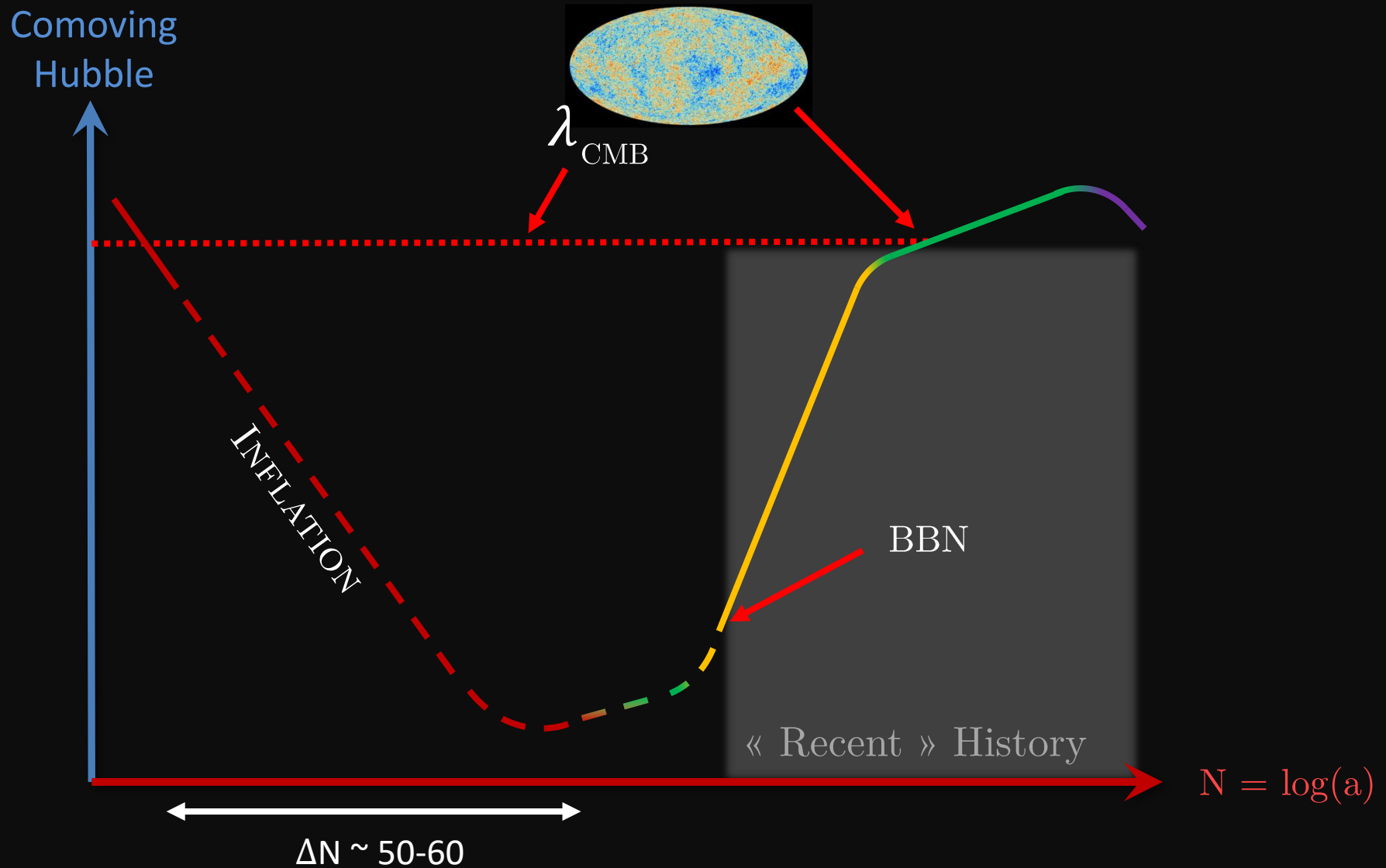
LUCIEN HEURTIER

IS INFLATION ON THE RUN?

ArXiv:[2511.01612](#) – M. Fairbairn, LH, M.O. Olea-Romacho

ArXiv:[2511.05296](#) – J. Alexandre, LH, S. Pla

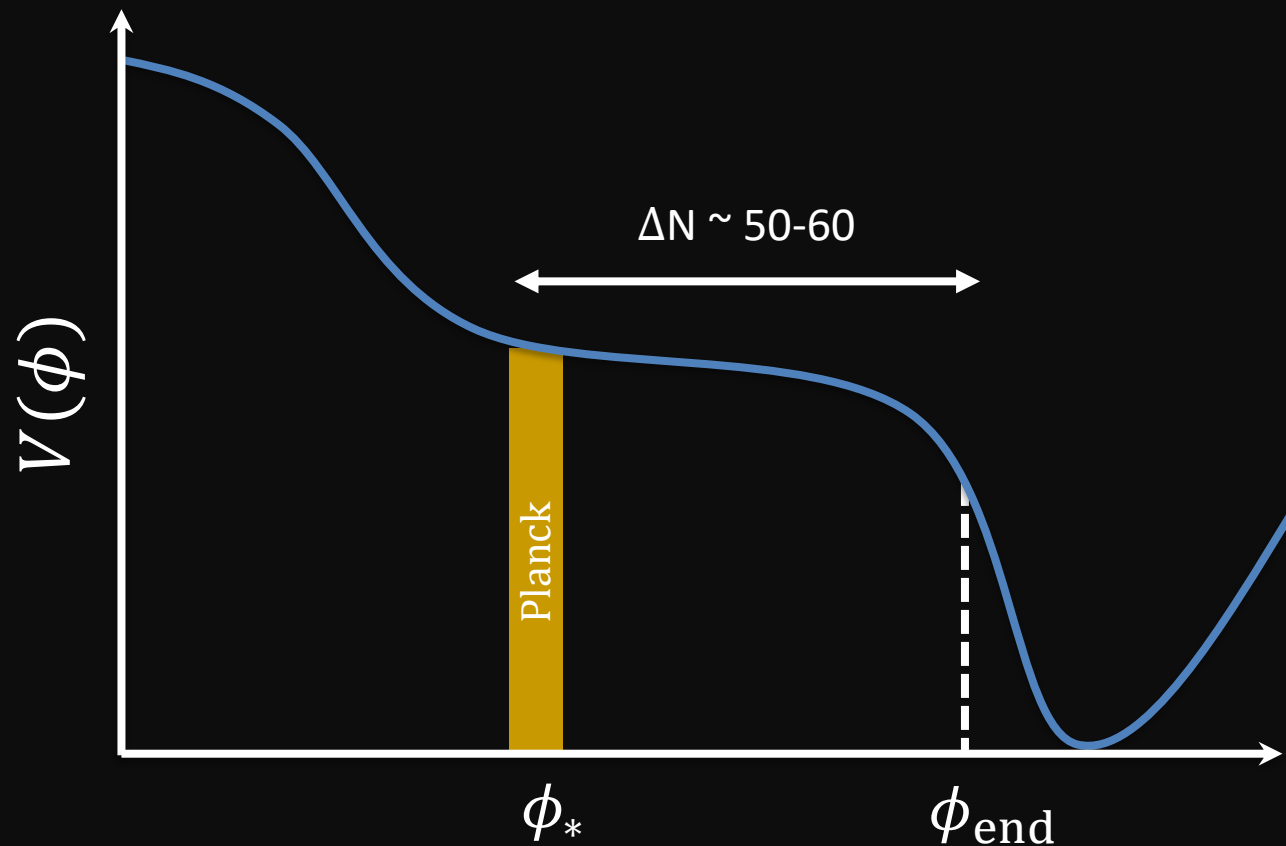
Inflation in a sketch



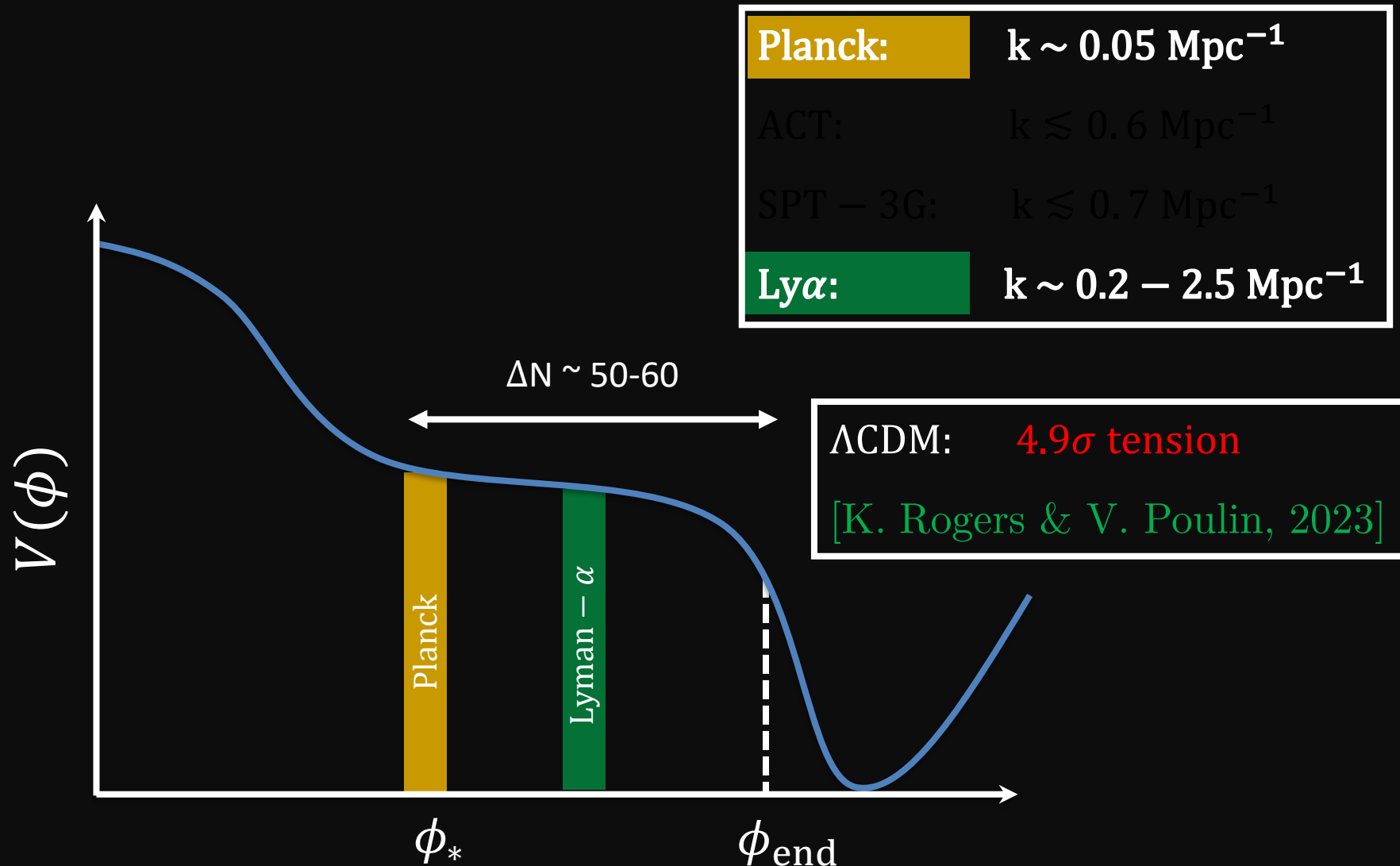
Inflation Model Building

Planck:

$k \sim 0.05 \text{ Mpc}^{-1}$



Constraints Across Scales



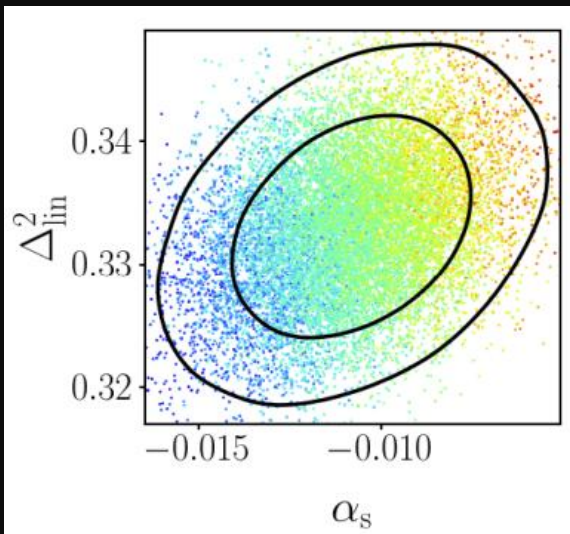
Λ CDM:

$$\ln \Delta_{\mathcal{R}}^2(k) \equiv \ln A_s + (n_s - 1) \ln \left(\frac{k}{k_\star} \right)$$



Λ CDM + α_s :

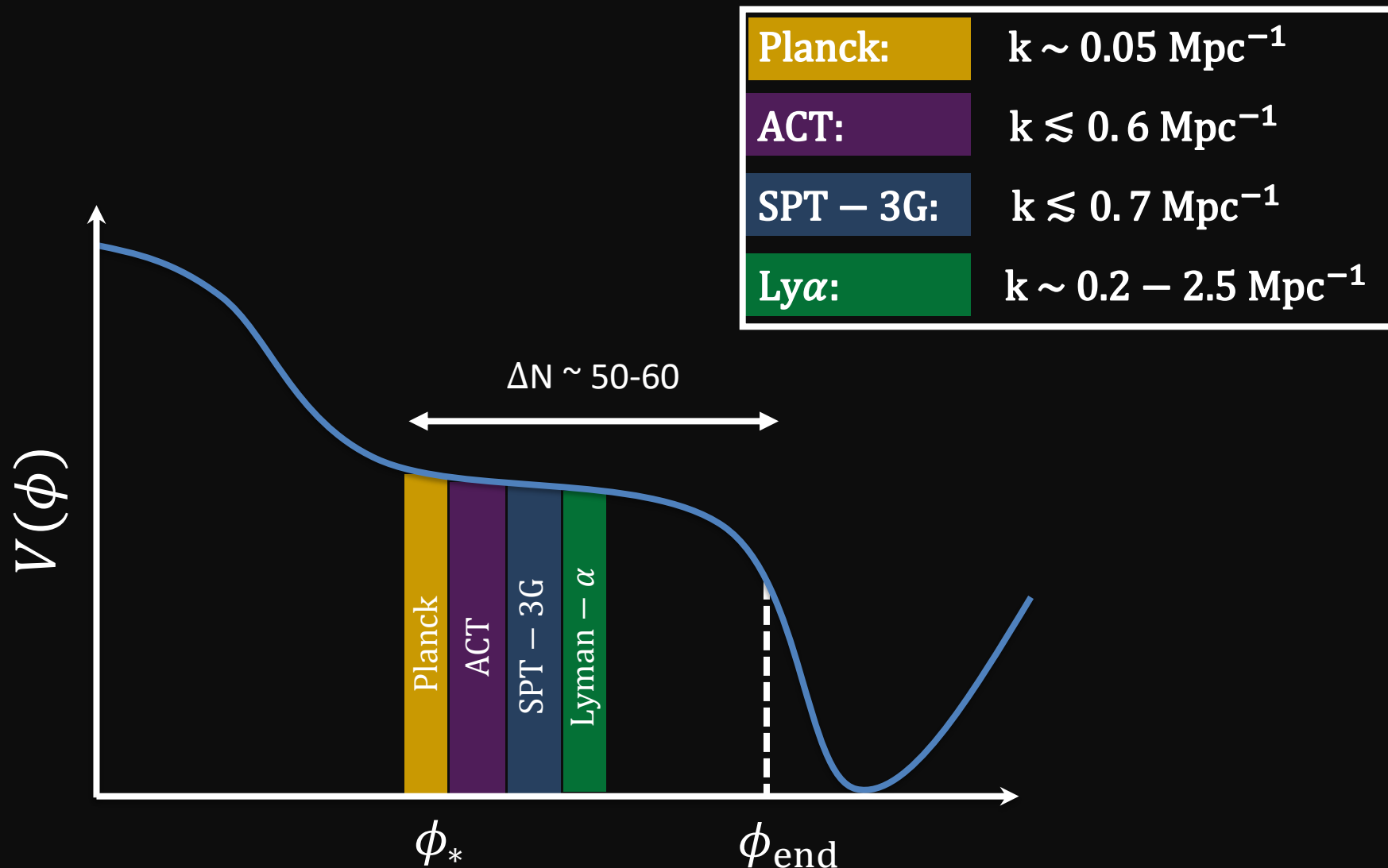
$$\ln \Delta_{\mathcal{R}}^2(k) \equiv \ln A_s + (n_s - 1) \ln \left(\frac{k}{k_\star} \right) + \frac{\alpha_s}{2} \ln \left(\frac{k}{k_\star} \right)^2 + \dots$$



tension $\sim 1\sigma$

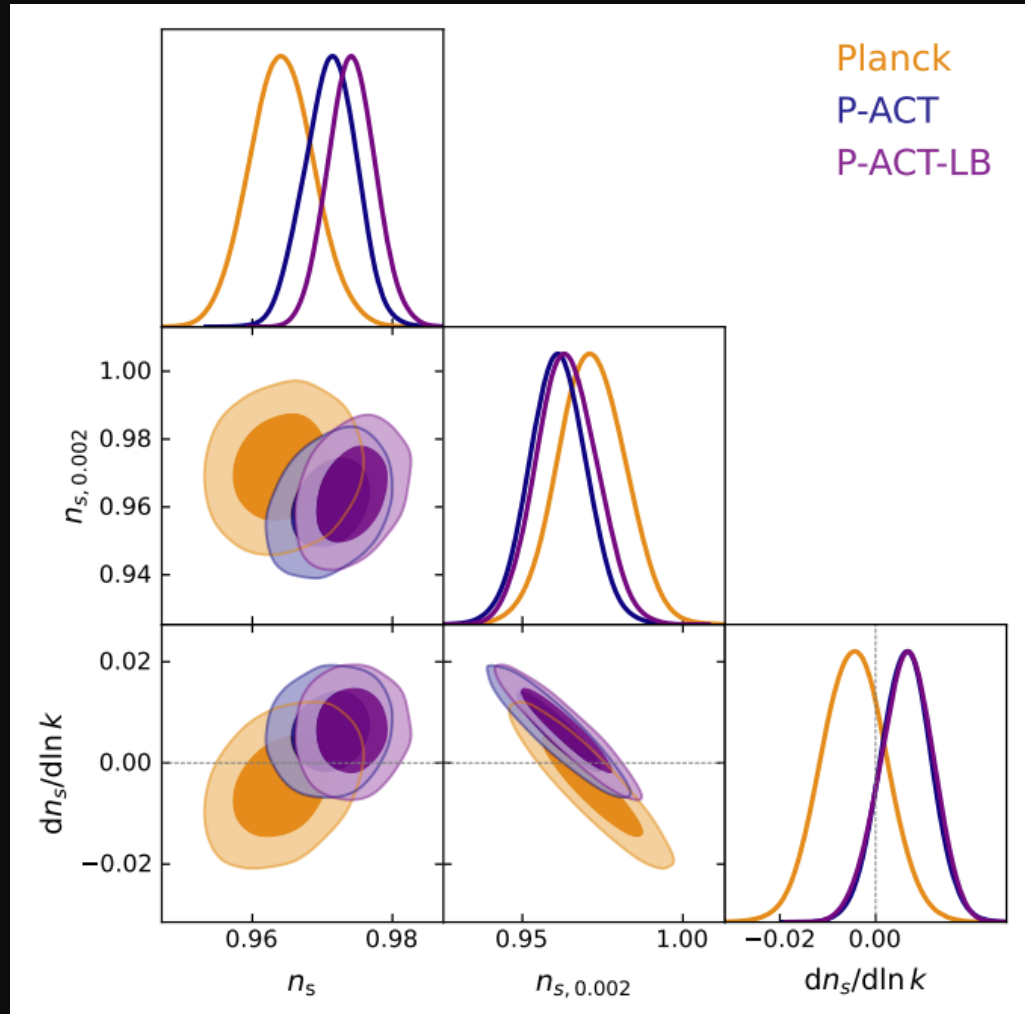
[K. Rogers & V. Poulin, 2023]

Constraints Across Scales



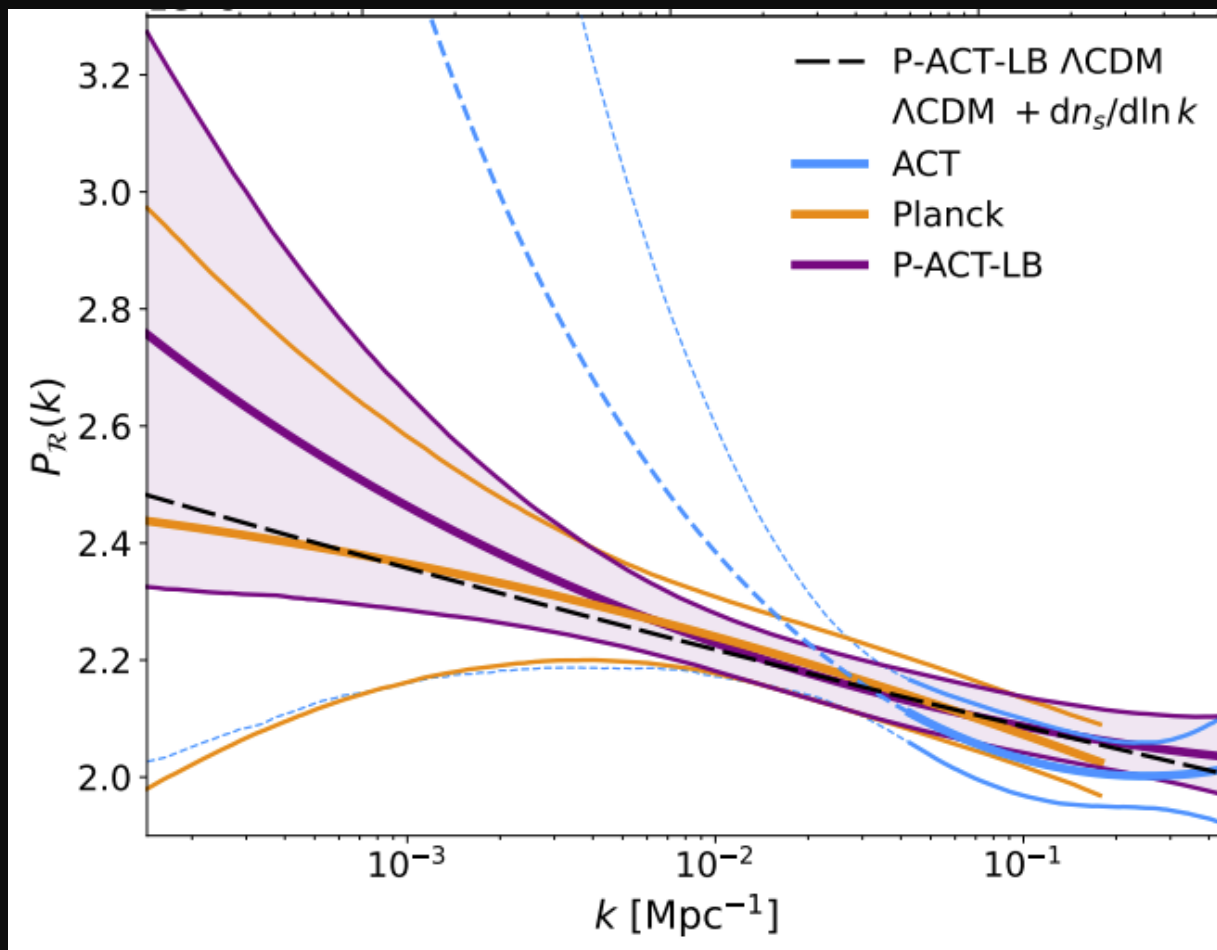
Spectral Index Running

ACT DR6, March 2025



Spectral Index Running

ACT DR6, March 2025



Λ CDM:

$$\ln \Delta_{\mathcal{R}}^2(k) \equiv \ln A_s + (n_s - 1) \ln \left(\frac{k}{k_\star} \right)$$


Λ CDM + α_s :

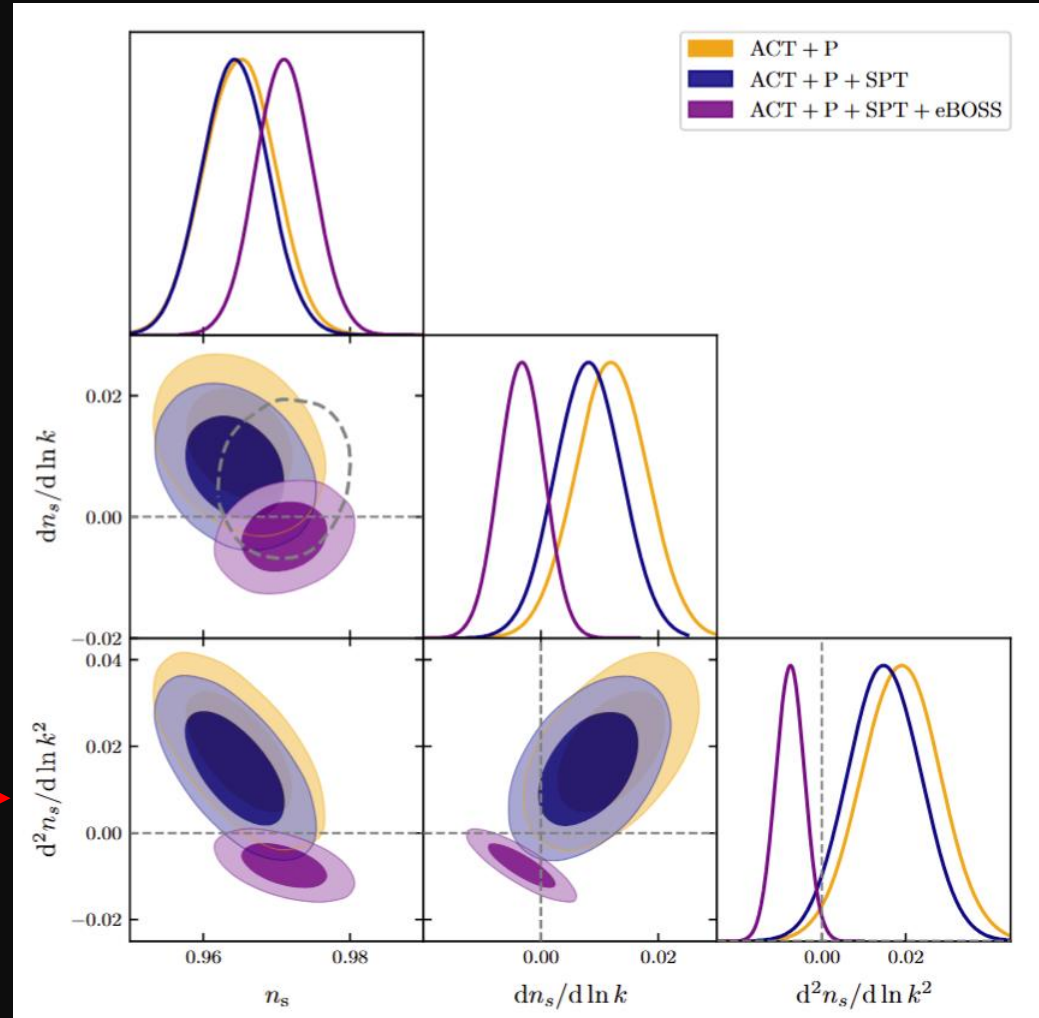
$$\ln \Delta_{\mathcal{R}}^2(k) \equiv \ln A_s + (n_s - 1) \ln \left(\frac{k}{k_\star} \right) + \frac{\alpha_s}{2} \ln \left(\frac{k}{k_\star} \right)^2 + \dots$$


Λ CDM
+ $\alpha_s + \beta_s$:

$$\ln \Delta_{\mathcal{R}}^2(k) \equiv \ln A_s + (n_s - 1) \ln \left(\frac{k}{k_\star} \right) + \frac{\alpha_s}{2} \ln \left(\frac{k}{k_\star} \right)^2 + \frac{\beta_s}{6} \ln \left(\frac{k}{k_\star} \right)^3 + \dots$$

ΛCDM
 $+\alpha_s + \beta_s$:

$\beta_s \rightarrow$



α_s



PIPE – Potential Inflation Posterior Emulator

gitlab.com/cosmoPipe/pipe-inflation

$$\log \mathcal{L}(A_s, n_s, \alpha_s, \beta_s) \longrightarrow \log \mathcal{L}(V_0, \dots)$$

Power-law +
Gaussian bump/dip

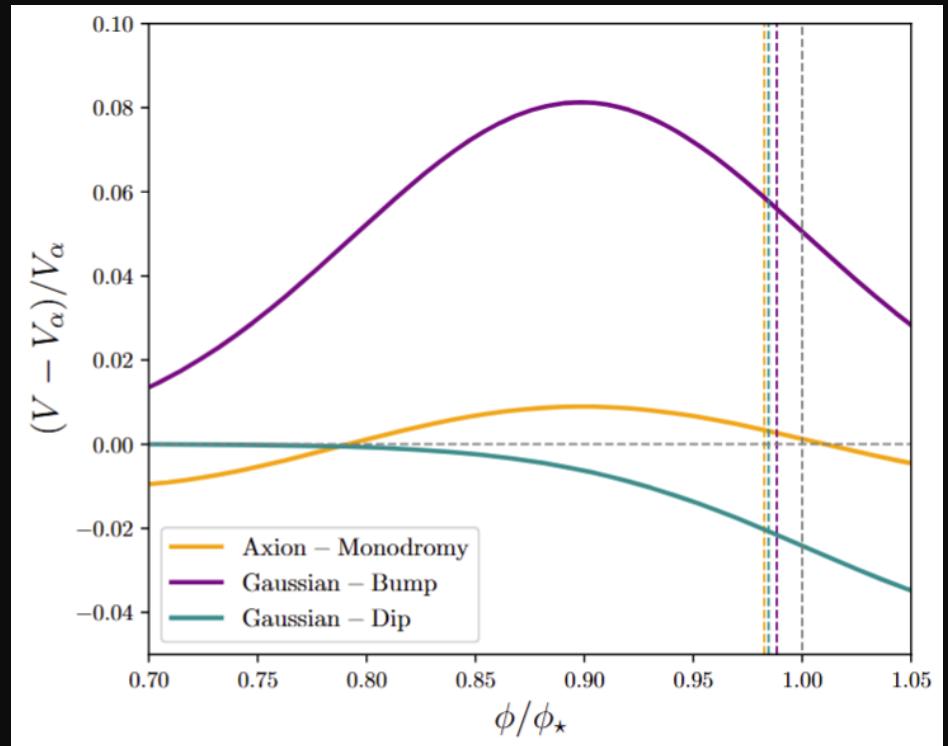
$$V = V_\alpha \left[1 \pm A \exp \left(-\frac{(\phi - \phi_0)^2}{2\sigma^2} \right) \right]$$

Axion Monodromy

$$V = V_0 \left[\left| \frac{\phi}{M_p} \right|^\alpha + A \cos \left(\gamma + \frac{M_p}{f} \left| \frac{\phi}{M_p} \right|^{1+p_f} \right) \right]$$

Dataset	Model	$\Delta\chi^2$	ΔAIC
ACT+P	Powerlaw+Bump	-7.27	-1.27
	Powerlaw+Dip	-7.27	-1.27
	Axion-Monodromy	-7.27	0.73
+SPT	Powerlaw+Bump	-5.52	0.48
	Powerlaw+Dip	-5.52	0.48
	Axion-Monodromy	-5.57	2.43
+eBOSS	Powerlaw+Bump	-107.09	-101.09
	Powerlaw+Dip	-107.09	-101.09
	Axion-Monodromy	-107.09	-99.09

Local feature
preferred by data at $> 10\sigma$



Power-law +
Gaussian bump/dip

$$V = V_\alpha \left[1 \pm A \exp \left(-\frac{(\phi - \phi_0)^2}{2\sigma^2} \right) \right]$$

Axion Monodromy

$$V = V_0 \left[\left| \frac{\phi}{M_p} \right|^\alpha + A \cos \left(\gamma + \frac{M_p}{f} \left| \frac{\phi}{M_p} \right|^{1+p_f} \right) \right]$$

INFLATION
EXACT RG-EVOLUTION

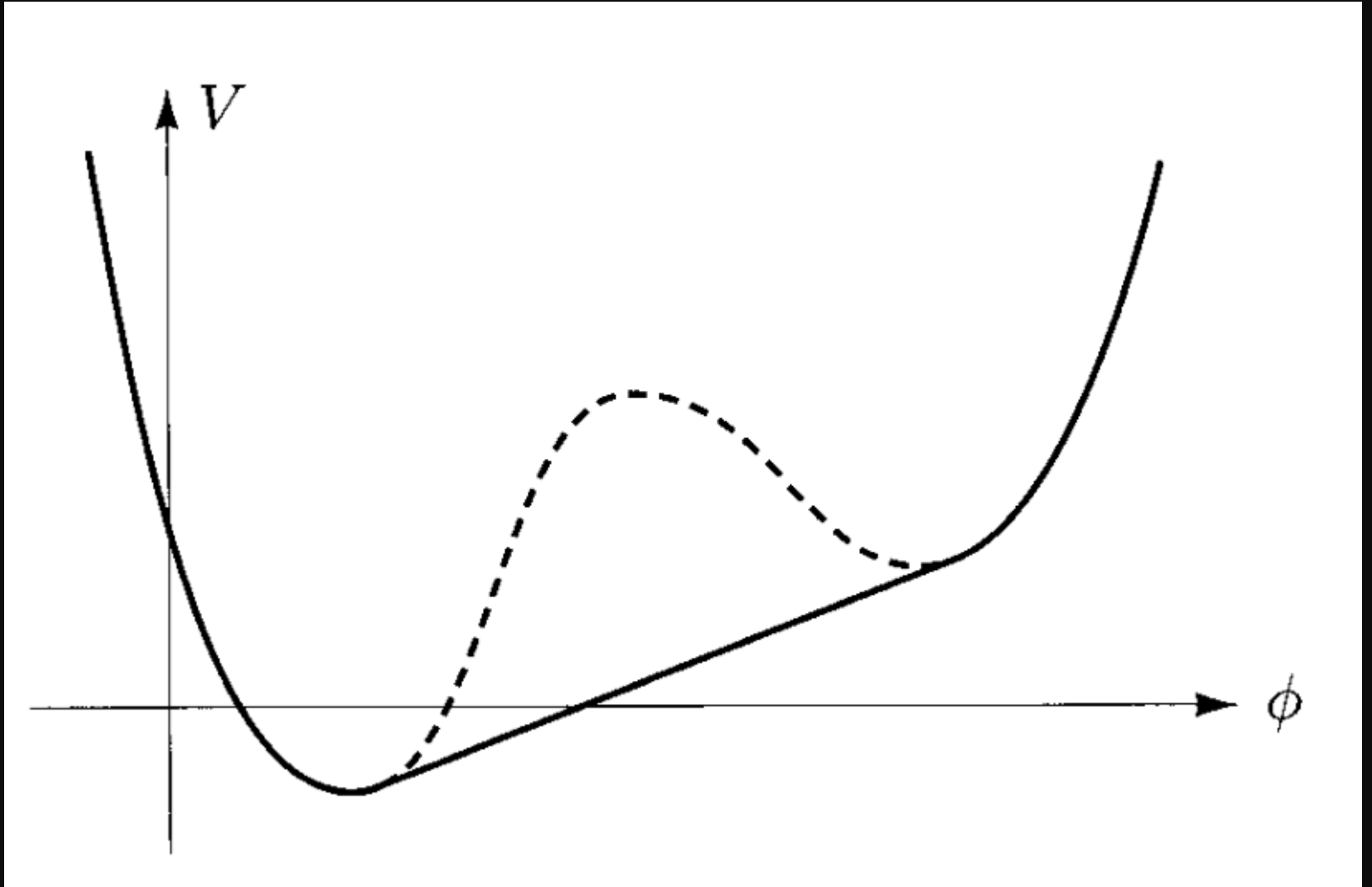
EFFECTIVE ACTION

$$Z[J] = e^{-iE[J]} = \int \mathcal{D}\phi \exp \left[i \int d^4x (\mathcal{L}[\phi] + J\phi) \right].$$

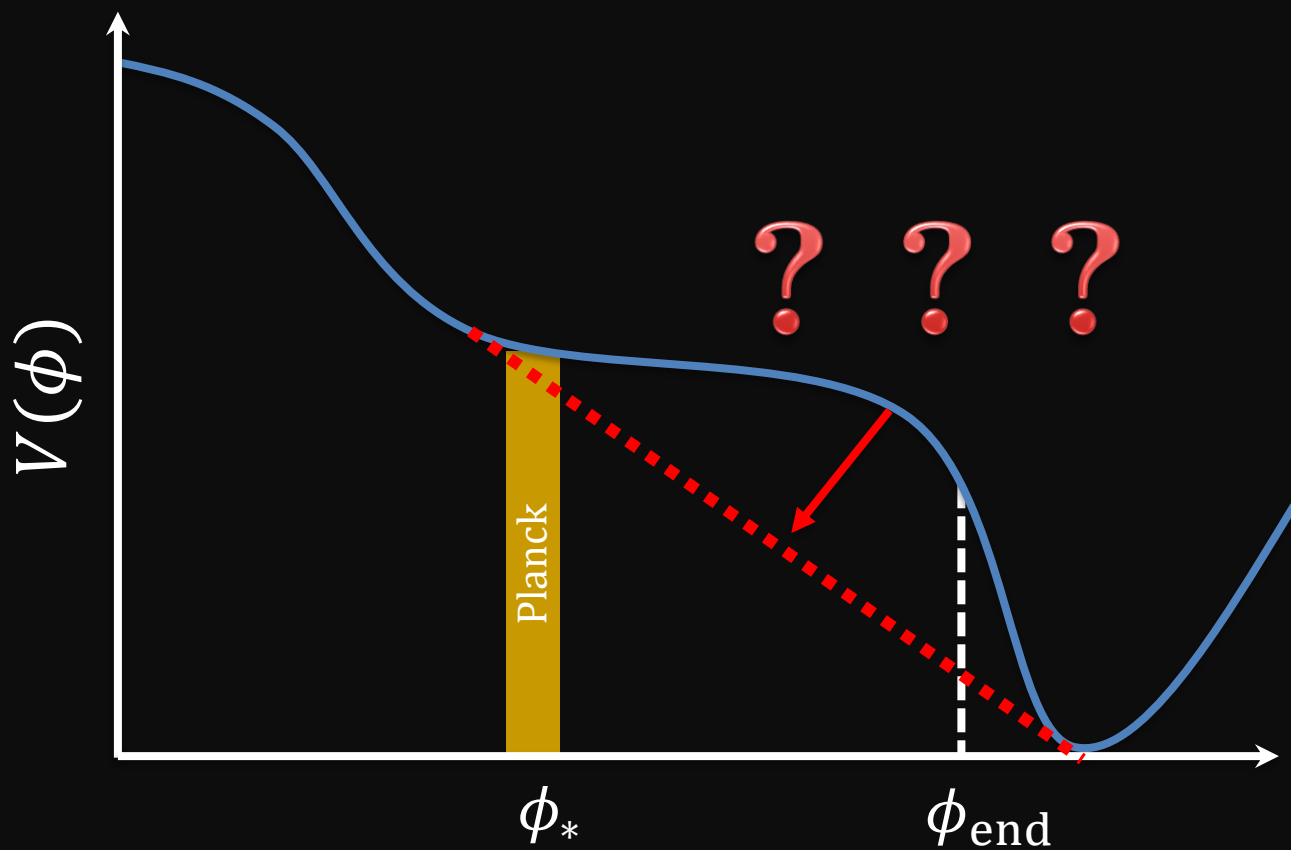
$$\Gamma[\phi_{\text{cl}}] \equiv -E[J] - \int d^4y J(y)\phi_{\text{cl}}(y).$$

$$\Gamma[\phi_{\text{cl}}] = -(VT) \cdot V_{\text{eff}}(\phi_{\text{cl}}).$$

EFFECTIVE ACTION

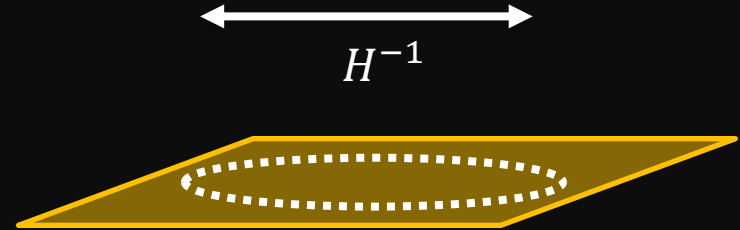


EFFECTIVE ACTION



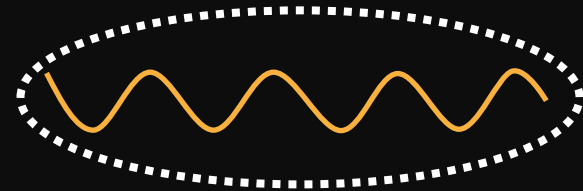
EFT of inflation

Homogeneous Background:



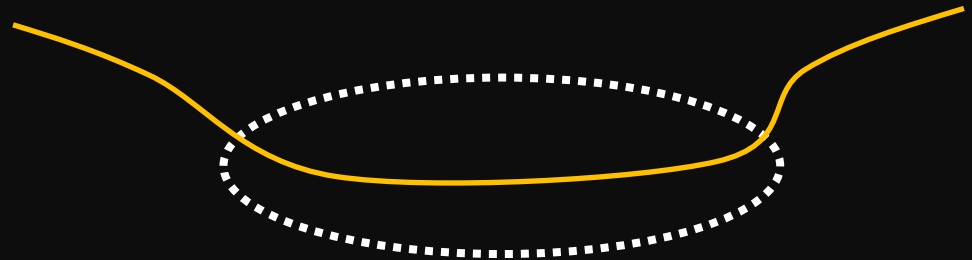
=

Quantum Perturbations
(integrated out)

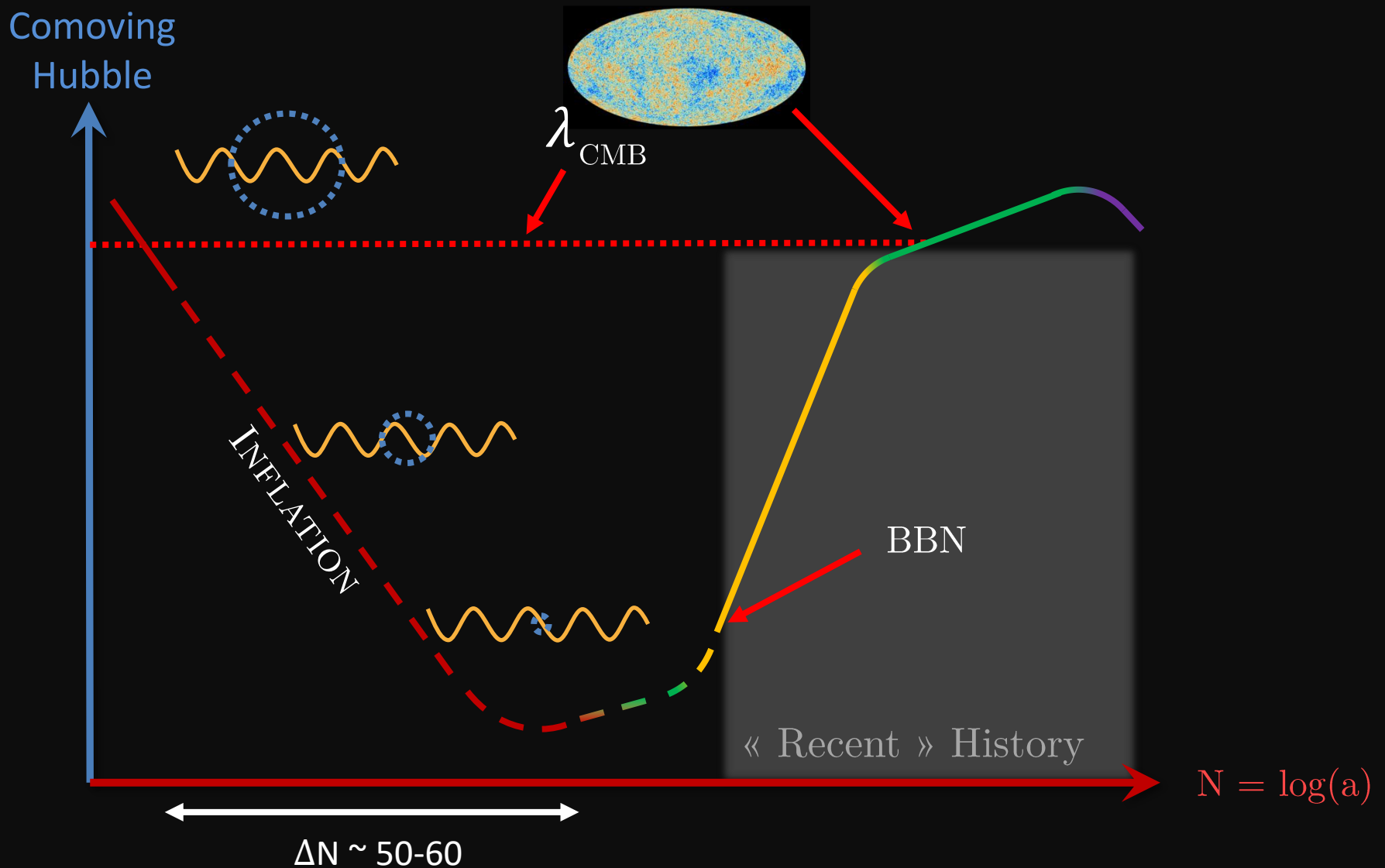


+

Classical Perturbations
(super-horizon)



EFT of inflation



RG running of inflation

Bare potential $V(\phi)$ $\longrightarrow$ RG-Improved potential $U(\phi)$

Static field: $\phi \sim \text{cst.}$ $\longrightarrow$ $H = H(\phi)$ $\longrightarrow$ $U = V_{RGI}(\phi)$

Valid in the deep slow-roll era: See Wenqi Ke's talk !

Rolling field: $\phi(t), \dot{\phi}(t)$ $\longrightarrow$ $\phi(t), H(t)$ $\longrightarrow$ $U = U(\phi, H)$



What about deviations from slow-roll ?

EXACT RENORMALISATION GROUP

At every scale: coarse grain the theory.

- Short wavelengths are integrated out.
- Large wavelengths live in the effective field theory.

Litim, Wetterich, and many

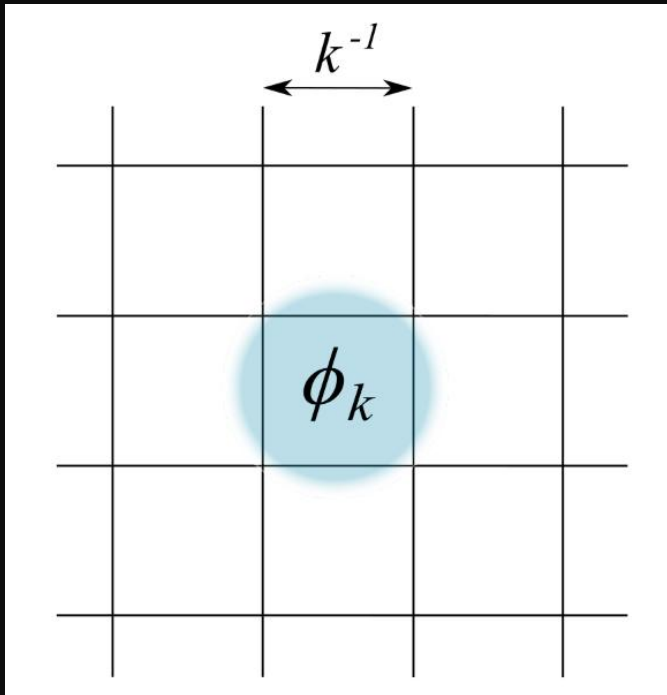
$$\Delta S = \frac{1}{2} \Omega \sum_q R_k(q) \chi_a^*(q) \chi^a(q),$$

$$S_k = S + \Delta S - \sum_q J_a^*(q) \chi^a(q).$$

$$W_k[J] = \ln Z_k[J] = \ln \int \mathcal{D}\chi \exp(-S_k[\chi, J]).$$

$$\tilde{\Gamma}_k[\varphi_k] + W_k[J] - \sum_q J_a^*(q) \varphi_k^a(q) = 0,$$

$$\Gamma_k = \tilde{\Gamma}_k - \Delta S = S.$$



EXACT RENORMALISATION GROUP

At every scale: coarse grain the theory.

- Short wavelengths are integrated out.
- Large wavelengths live in the effective field theory.

Litim, Wetterich, and many

$$\frac{\partial}{\partial t} \Gamma_k[\varphi] = \frac{1}{2} \text{Tr} \left[(\Gamma_k^{(2)}[\varphi] + R_k)^{-1} \partial_t R_k \right].$$

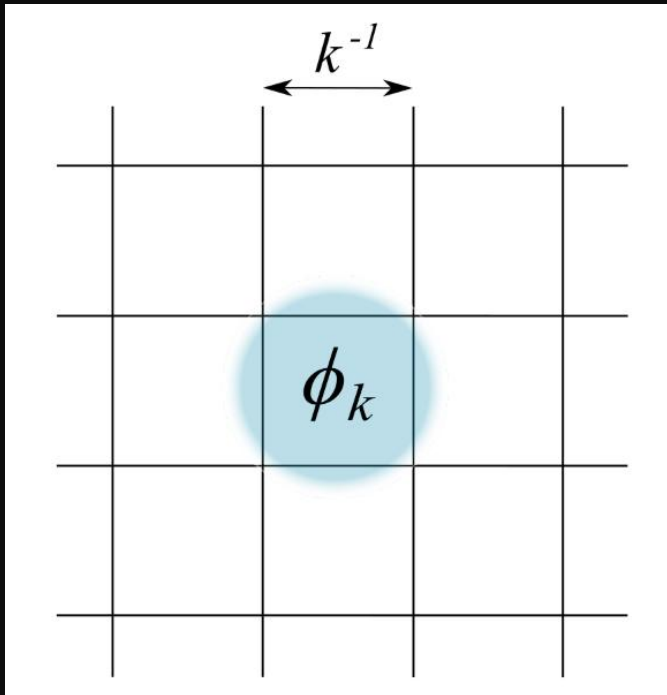
$$\lim_{k \rightarrow 0} R_k(q) = 0$$

$$\lim_{k \rightarrow 0} \Gamma_k[\varphi] = \Gamma[\varphi],$$

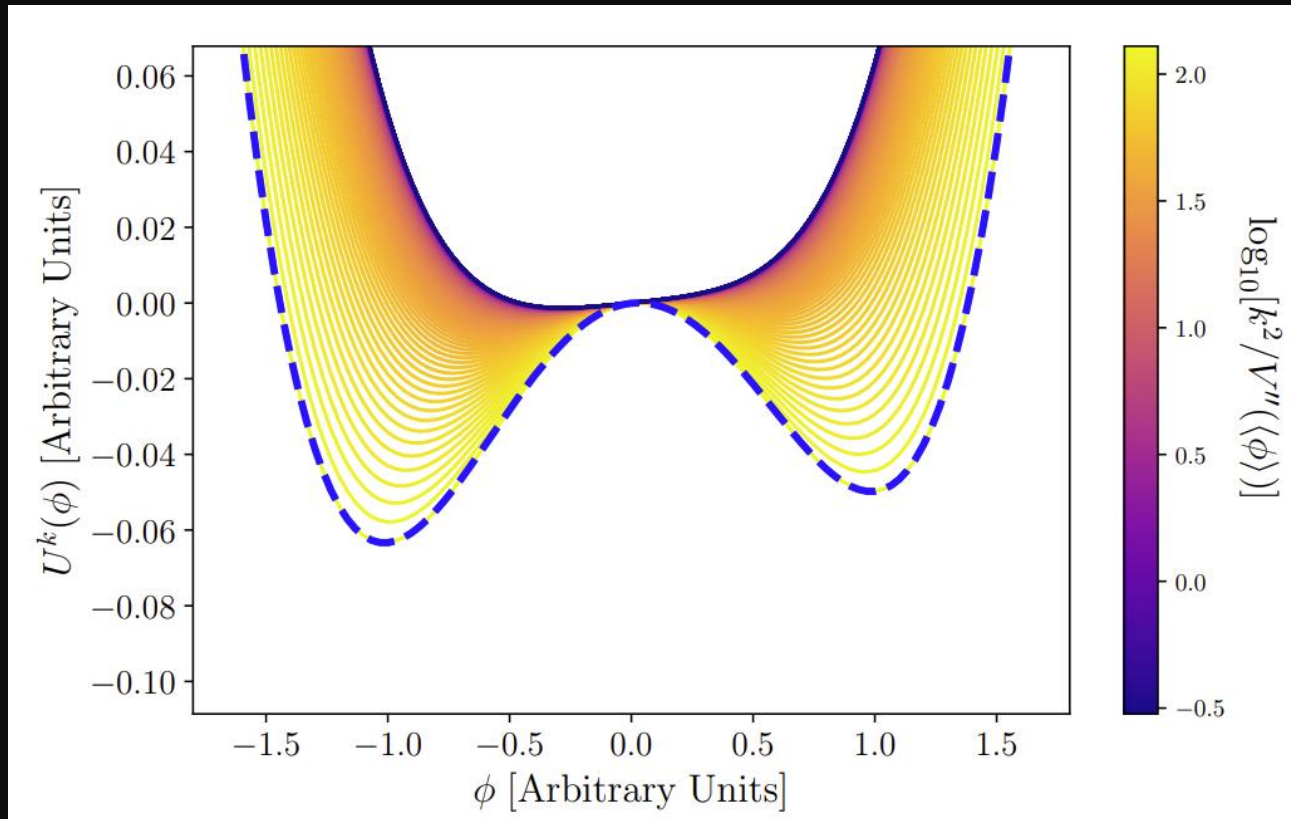
$$\frac{\partial}{\partial t} \Gamma_k = \frac{1}{2} \times \text{diagram}$$

$$\times = \frac{\partial}{\partial t} R_k$$

—●— = full k -dependent propagator



EXACT RENORMALISATION GROUP



S. Abel, LH, JHEP 08 (2025) 198

EXACT RENORMALISATION GROUP

4D-Euclidean space $\longrightarrow$ 3+1 FLRW problem

$$\frac{\delta\Gamma_k}{\delta k(t)} = \frac{\sqrt{-g(t)}}{2} \int \frac{d^3p}{(2\pi)^3} \int \frac{d^3q}{(2\pi)^3} \delta(\vec{p} + \vec{q}) \int dt' \delta(t - t') \mathcal{O}(t, t', \vec{p}, \vec{q}) \partial_k C_k(p) , \quad (5)$$

where

$$\mathcal{O}(t, t', \vec{p}, \vec{q}) = \left[\sqrt{|g|} (C_k(p) - i\varepsilon) \delta(\vec{p} + \vec{q}) \delta(t - t') - \frac{\delta^2 \Gamma_k}{\delta \varphi_b(t, \vec{p}) \delta \varphi_b(t', \vec{q})} \right]^{-1} , \quad (6)$$

EXACT RENORMALISATION GROUP

4D-Euclidean space $\longrightarrow$ 3+1 FLRW problem

+ Local Potential Approximation

$$\Gamma_k[\phi] = \int dt \sqrt{-g} \int d^3x \left(-\frac{g^{\mu\nu}}{2} \partial_\mu \phi \partial_\nu \phi - U_k(\phi) \right)$$

+ Top-Hat Regulator

$$\partial_\kappa U_\kappa(\phi) = \frac{aT^{-1}}{6\pi^2} \mathcal{D}_E^{-1} (a^{-1} \kappa^4) , \quad (9)$$

where

$$\mathcal{D}_E = -\frac{d^2}{dt^2} - 3H \frac{d}{dt} + \kappa^2 + \partial_\phi^2 U_\kappa(\phi) , \quad (10)$$

EXACT RENORMALISATION GROUP

4D-Euclidean space $\longrightarrow$ 3+1 FLRW problem

+ Local Potential Approximation

$$\Gamma_k[\phi] = \int dt \sqrt{-g} \int d^3x \left(-\frac{g^{\mu\nu}}{2} \partial_\mu \phi \partial_\nu \phi - U_k(\phi) \right)$$

+ Top-Hat Regulator

$$\ddot{F} + H\dot{F} + (\partial_\phi^2 U - H^2 - \dot{H})F = \frac{H_0 H^4}{6\pi^2} ,$$

where $F \equiv \partial_H U$

EXACT RENORMALISATION GROUP

4D-Euclidean space $\longrightarrow$ 3+1 FLRW problem

$U = U(\phi, H)$ $\longrightarrow$ Modified Friedmann Equations

$$\ddot{\phi} + 3H\dot{\phi} + \partial_{\phi}U = 0 , \quad (13)$$

$$3M_p^2 H^2 = \frac{1}{2}(\dot{\phi})^2 + U - HF , \quad (14)$$

$$M_p^2 \left(2\frac{\ddot{a}}{a} + H^2 \right) + \frac{1}{2}(\dot{\phi})^2 - U + HF + \frac{\dot{F}}{3} = 0 . \quad (15)$$

EXACT RENORMALISATION GROUP

4D-Euclidean space $\longrightarrow$ 3+1 FLRW problem

Set of Equations

$$\begin{aligned} F'' &= \frac{H_0 H^2}{6\pi^2} - \left(1 + \frac{H'}{H}\right) F' - \left(\frac{\partial_\phi^2 U}{H^2} - \frac{H'}{H} - 1\right) F, \\ \phi'' &= -\left(3 + \frac{H'}{H}\right) \phi' - \frac{\partial_\phi U}{H^2}, \\ H' &= -\frac{H}{2M_p^2} \left((\phi')^2 + \frac{F'}{3H}\right). \end{aligned} \tag{17}$$

EXACT RENORMALISATION GROUP

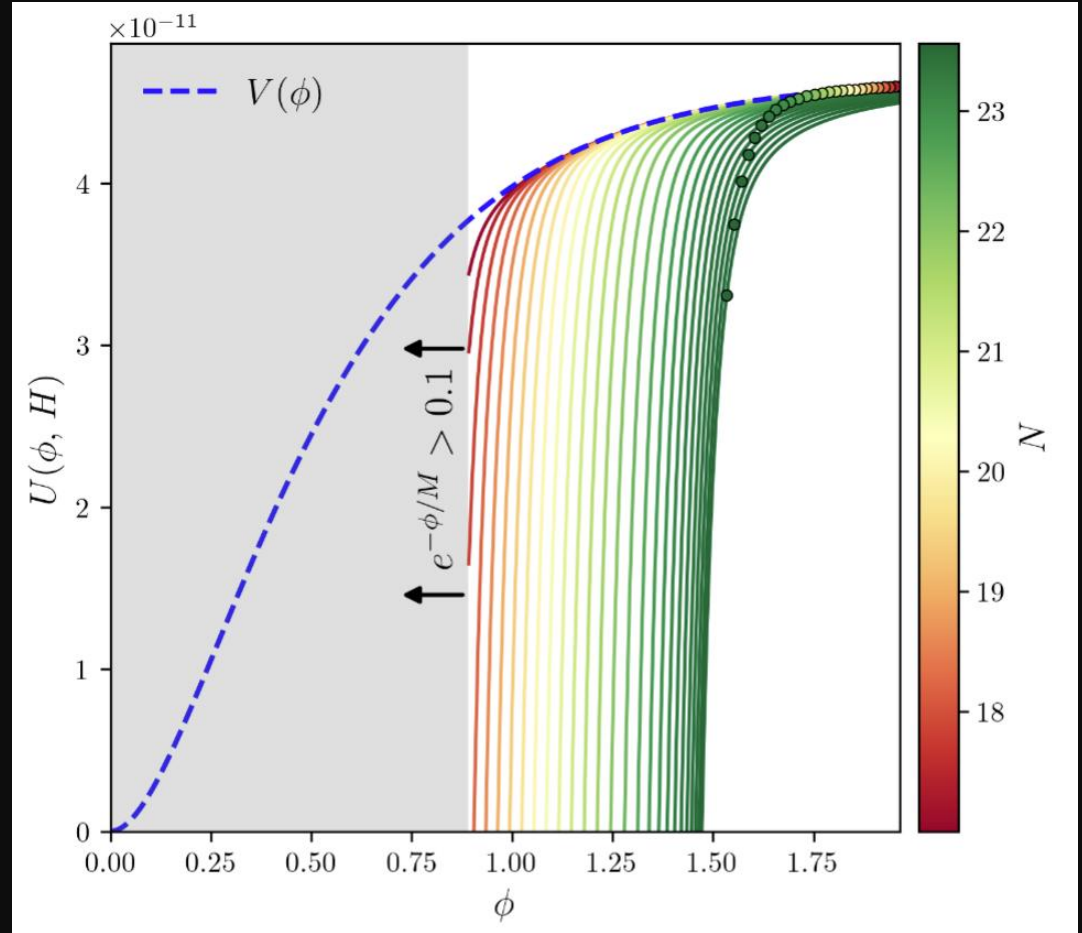
E-models

$$U(\phi, H_0) = V(\phi) = V_0 \left(1 - e^{\sqrt{\frac{2}{3\alpha}} \frac{\phi}{M_p}} \right)^2 .$$

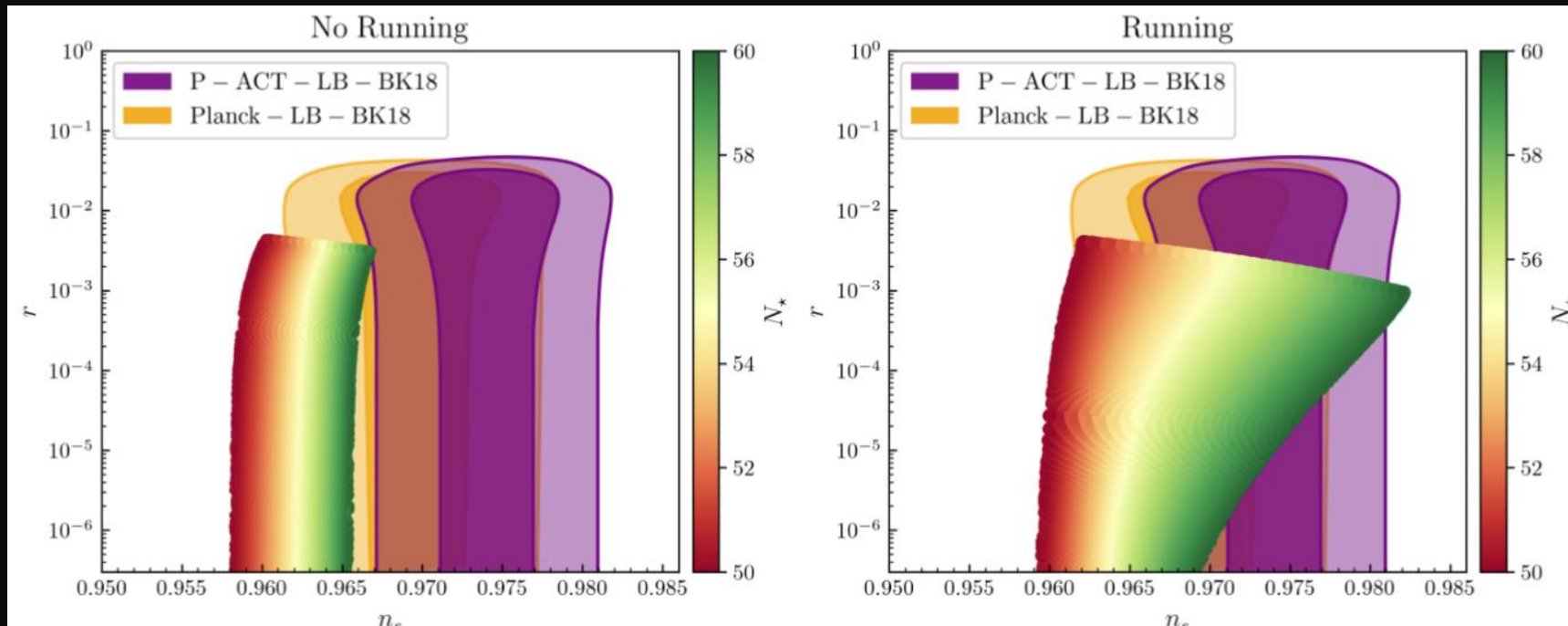
$$U_H(\phi) = \sum_{n=0}^{\infty} U_n(H) e^{-n\phi/M}$$

$$F = \sum_{n=0}^{\infty} F_n e^{-n\phi/M} , \text{ with } F_n = \frac{dU_n}{dH}$$

$$\begin{aligned} F_n'' = & \delta_{n,0} \frac{H_0 H^2}{6\pi^2} - F_n' \left[-2n \frac{\phi'}{M} + \left(1 + \frac{H'}{H} \right) \right] \\ & + F_n \left[n \frac{\phi''}{M} - \left(n \frac{\phi'}{M} \right)^2 + \left(1 + \frac{H'}{H} \right) \left(1 + n \frac{\phi'}{M} \right) \right] \\ & - \frac{1}{H^2 M^2} \left(\sum_{l=0}^n l^2 U_l F_{n-l} \right) , \quad n \geq 0. \end{aligned} \quad (26)$$



EXACT RENORMALISATION GROUP



Effect on Observables:

Reduced number of e-folds $\longrightarrow$ Shift to larger n_s

THANK YOU FOR YOUR ATTENTION!