# Exciting THE (FRUSTRATING) SEARCH FOR STERILE NEUTRINOS

Jordy de Vries University of Amsterdam & Nikhef







#### Tiny masses

- In the original formulation of the Standard Model (Weinberg 1967) neutrinos were considered to be massless particles
- Not crazy: from beta decay experiments  $m_{\nu} \ll m_{e} \ll m_{p}$

Neutrinos, they are very small.
They have no charge and have no mass
And do not interact at all.
The earth is just a silly ball
To them, through which they simply pass.

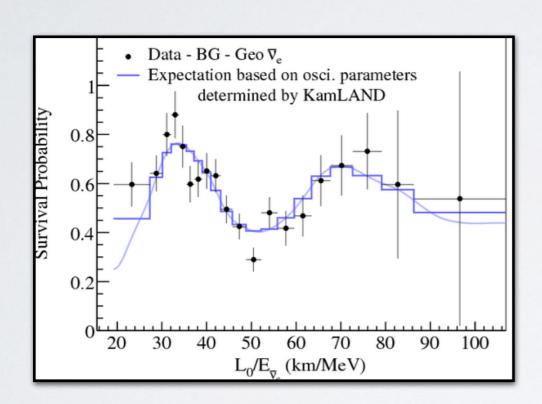
John updike's Cosmic Gall (1960)

#### Tiny masses

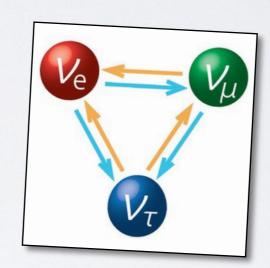
- In the original formulation of the Standard Model (Weinberg 1967) neutrinos were considered to be massless particles
- Not crazy: from beta decay experiments

$$m_{\nu} \ll m_{e} \ll m_{p}$$

#### But neutrinos do have mass!



$$P(\nu_{\mu} \to \nu_{e}) \sim \sin \frac{\Delta m^{2} L}{2E}$$



$$|\Delta m| \simeq 0.05 \, eV$$

Smallest:

$$|\delta m| \simeq 0.008 \, eV$$

Direct limits:

$$m_{\nu_e} \le 0.8 \, eV$$

 $m_{\nu_a} \le 0.8 \, eV$  • Cosmology (DESI 2024)

$$\sum m_{\nu_i} \le 0.15 \, eV(IH)$$

$$\sum m_{\nu_i} \le 0.11 \, eV(NH)$$

#### Tiny masses

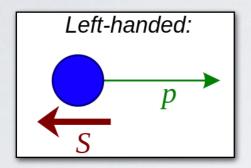
- In the original formulation of the Standard Model (Weinberg 1967) neutrinos were considered to be massless particles
- Not crazy: from beta decay experiments  $m_{\nu} \ll m_{e} \ll m_{p}$
- But neutrinos do have mass!

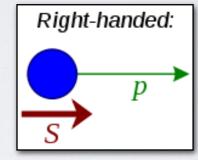


 The problem of neutrino masses points towards new fields/new scales/new symmetries

## Mass generation in the Standard Model

- How does the electron get a mass in the Standard Model?
- It's tricky: a mass term connects a left-handed to a right-handed field





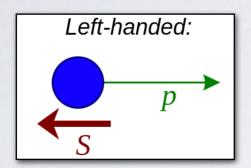
Left-handed fields have a 'weak' charge

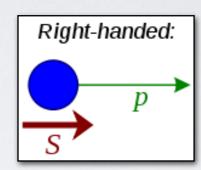
Right-handed fields have no 'weak' charge

- We cannot just write down a mass term:
- $\mathcal{L} = -m_e \bar{e}_L e_R$
- This would violate 'weak charge' conservation (or SU(2) gauge invariance)

## Mass generation in the Standard Model

- How does the electron get a mass in the Standard Model?
- It's tricky: a mass term connects a left-handed to a right-handed field





# Left-handed fields have a 'weak' charge

Right-handed fields have no 'weak' charge

• We cannot just write down a mass term:

$$\mathscr{L} = -m_e \, \bar{e}_L \, e_R$$

- This would violate 'weak charge' conservation (or SU(2) gauge invariance)
- The Standard Model overcomes this problem through the **Higgs** mechanism

$$\mathcal{L} = -y_e \bar{e}_L e_R \varphi \qquad \qquad \mathcal{L} = -y_e \bar{e}_L e_R \mathbf{v} \qquad \qquad m_e = y_e \mathbf{v}$$

 The scalar field has a weak charge and a nonzero value v in the vacuum (spontaneous symmetry breaking)

• Easy fix: Insert gauge-singlet right-handed neutrino  $v_{
m R}$ 

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi \qquad y_{\nu} \sim 10^{-12} \rightarrow m_{\nu} \sim 0.1 \text{ eV}$$

- Nothing really wrong with this....
- The v-nightmare scenario



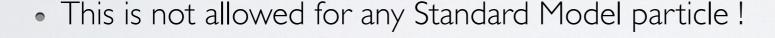
• Easy fix: Insert gauge-singlet right-handed neutrino  $v_{
m R}$ 

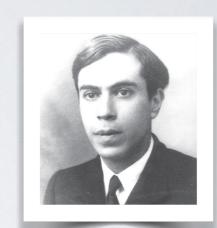
$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi \qquad y_{\nu} \sim 10^{-12} \rightarrow m_{\nu} \sim 0.1 \text{ eV}$$

Nothing really wrong with this.... But nothing forbids a Majorana Mass term

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi - M_{R} \nu_{R}^{T} C \nu_{R}$$

'Everything that is not forbidden is compulsary'





Ettore Majorana

M<sub>R</sub> not connected to electroweak scale: could be a completely new scale

 Footnote: by far not the only way to generate neutrino masses! Can be done without right-handed neutrino's (see e.g. type-II seesaw with a new triplet scalar field)

• Easy fix: Insert gauge-singlet right-handed neutrino  $v_{
m R}$ 

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi \qquad y_{\nu} \sim 10^{-12} \rightarrow m_{\nu} \sim 0.1 \text{ eV}$$

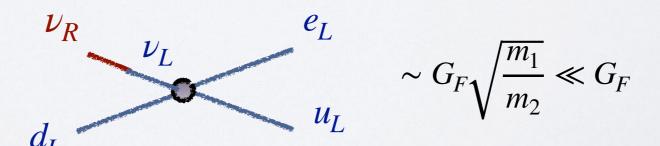
Nothing really wrong with this.... But nothing forbids a Majorana Mass term

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi - M_{R} \nu_{R}^{T} C \nu_{R}$$

- I+I case: diagonalization leads to **Majorana** mass eigenstates  $\nu_i^c = \nu_i$
- If M<sub>R</sub> is significantly larger than active neutrino masses: **see-saw mechanism**

$$m_1 \simeq \left| \frac{y_\nu^2 v^2}{M_R} \right| \ll m_2 \simeq M_R$$
 Active neutrino + heavier sibling (sterile neutrino)

Sterile neutrinos





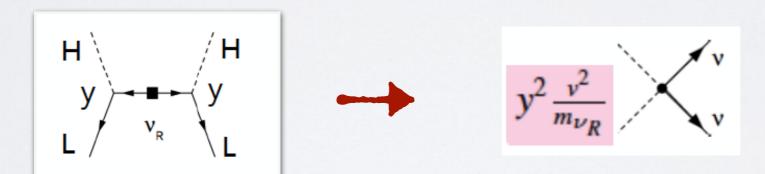
• Easy fix: Insert gauge-singlet right-handed neutrino  $v_R$ 

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi \qquad y_{\nu} \sim 10^{-12} \rightarrow m_{\nu} \sim 0.1 \text{ eV}$$

Nothing really wrong with this.... But nothing forbids a Majorana Mass term

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi - M_{R} \nu_{R}^{T} C \nu_{R}$$

• If M<sub>R</sub> is significantly larger than electroweak scale: integrate it out



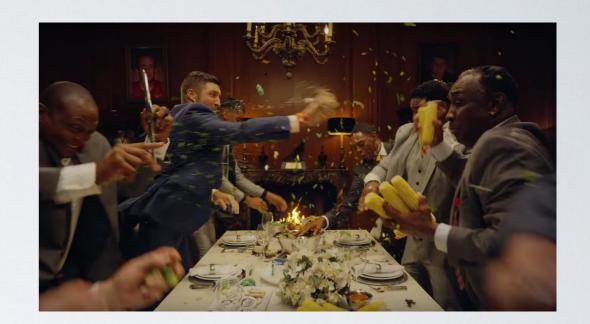
Obtain dimension-5 SMEFT operator that lead to active neutrino Majorana mass

$$\mathcal{L}_5 = C_5 (L^T C \tilde{H}) (\tilde{H}^T L)$$
 Weinberg '79

Weinberg operator describes many 'high-scale' mechanisms

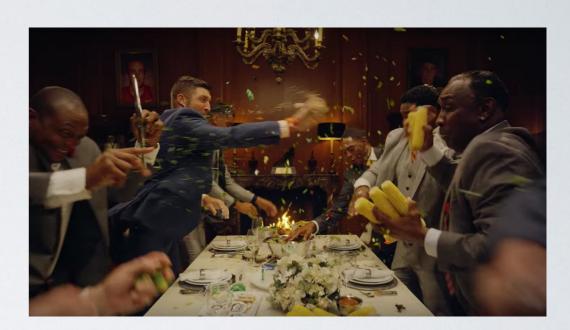
#### Are neutrino masses BSM?

- A question to fight about at lunch
- Not uncommon opinion: Standard Model can be redefined to include neutrino masses



#### Are neutrino masses BSM?

- A question to fight about at lunch
- Not uncommon opinion: Standard Model can be redefined to include neutrino masses



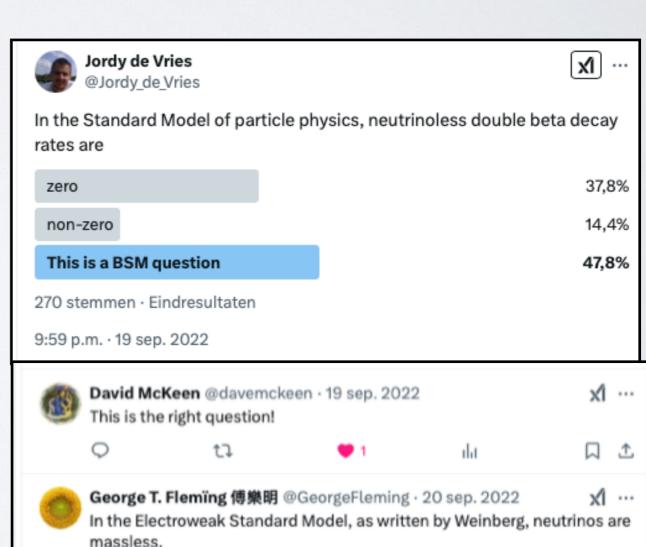
#### • But which mechanism?

**A)** 
$$\mathscr{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi$$

**B)** 
$$\mathscr{L} = C_5 \left( L^T C \tilde{H} \right) (\tilde{H}^T L)$$

$$\mathcal{L} = -y_{\nu} \bar{\nu}_{L} \nu_{R} \varphi - M_{R} \nu_{R}^{T} C \nu_{R}$$





#### The plan of attack

I. Motivation: the puzzle of neutrino masses

#### 2. Probing sterile neutrinos directly and indirectly

- Effective field theory for Ovbb
- 3. Connection to low-scale leptogenesis

# In this talk: minimal option C setup

See-saw (variants) can work for essentially any right-handed scale

eV keV MeV GeV TeV .....  $10^{15}\,\mathrm{GeV}$ • If Yukawa coupling order I then  $m_1\simeq\left|\frac{v^2}{M_R}\right| \to M_R\simeq 10^{15}\,\mathrm{GeV}$ 

# In this talk: minimal option C setup

See-saw (variants) can work for essentially any right-handed scale

MR? eV GeV keV MeV TeV 1015 GeV

• If Yukawa coupling order I then

$$m_1 \simeq \left| \frac{v^2}{M_R} \right| \rightarrow M_R \simeq 10^{15} \, \mathrm{GeV}$$
Fukugita, Yanagadi '86

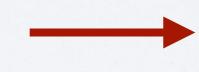
• Thermal leptogenesis possible  $M_R \ge 10^9 \, {\rm GeV}$ 

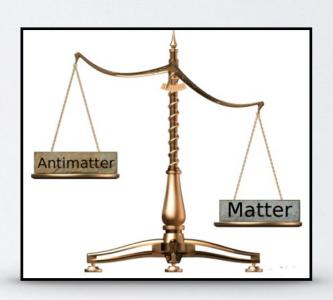
$$M_R \ge 10^9 \, \mathrm{GeV}$$

Davidson Ibarra '02



13.7 billion year





 Hard to test directly but smoking gun evidence: neutrinos are Majorana + CPV in neutrino sector

## Mass ranges

See-saw (variants) can work for essentially any right-handed scale

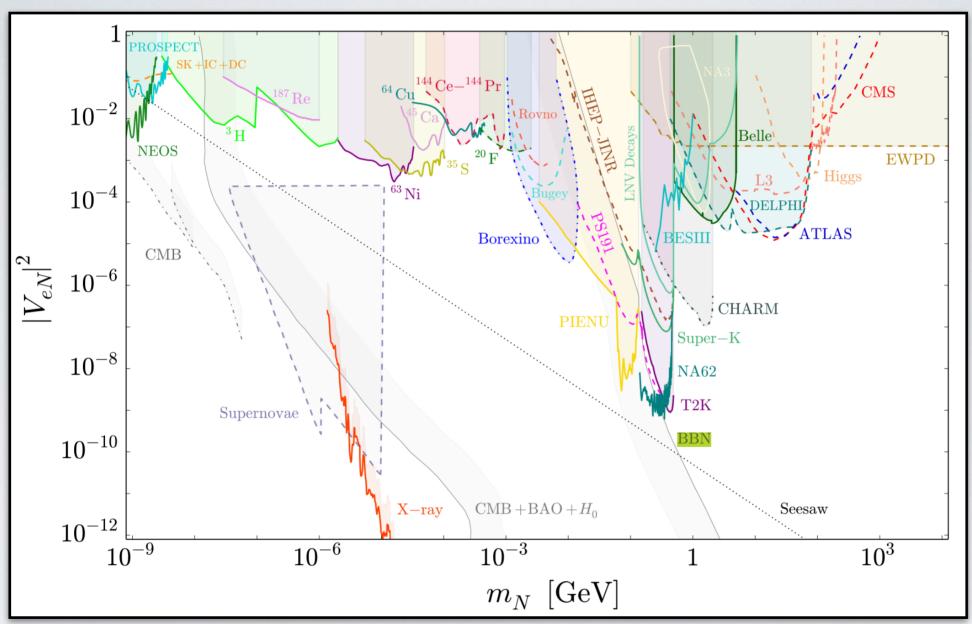
MR? 1015 GeV eV keV MeV GeV TeV  $m_1 \simeq \left| \frac{v^2}{M_R} \right| \rightarrow M_R \simeq 10^{15} \, \mathrm{GeV}$ Fukugita, Yanagadi '86 • If Yukawa coupling order I then  $M_R \ge 10^9 \, \text{GeV}$  Davidson Ibarra '02 Thermal leptogenesis possible

- But also leptogenesis possible with **TeV** sterile neutrinos!
- See e.g. Shaposhnikov et al (many works) And even in the MeV-GeV range Drewes et al '21
- KeV sterile neutrino could be Dark Matter (but getting more difficult) and essentially decoupled from neutrino mass generation

Dodelson. Widrow '97 Shaposhnikov et al '05

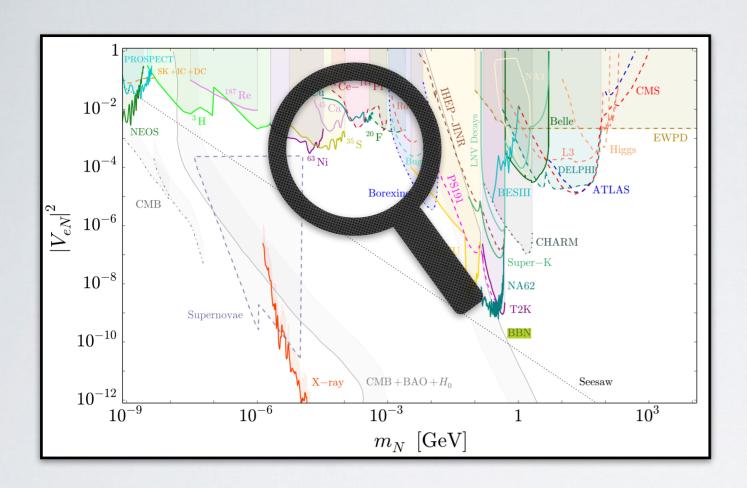
Pilaftsis '97, Akhmedov et al '98

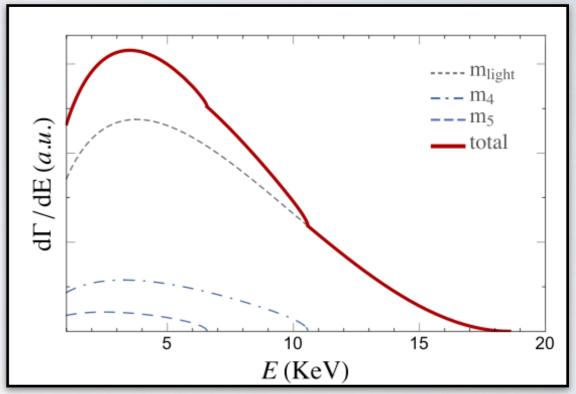
Motivation to look for a broad range of sterile neutrino masses



Bolton, Deppisch, Dev JHEP '20

- If they exist with masses below I TeV or so, we might find them directly!
- Very interesting experimental signatures depending on the mass range





$$m_4 = 8 \text{ keV}$$
,  $U_{e4} = 0.1$   $m_5 = 12 \text{ keV}$ ,  $U_{e5} = 0.1$ 

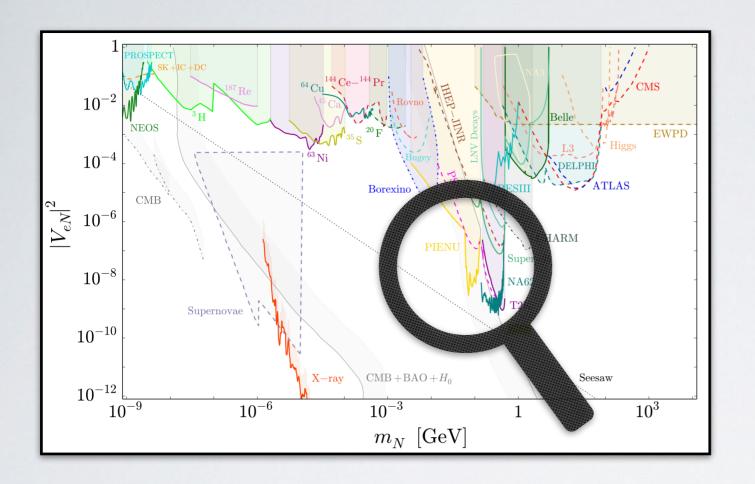
• Light sterile neutrinos can be produced in beta-decays  ${}^{A}_{Z}X \rightarrow {}^{A}_{Z+1}Y + e^{-} + \nu$ 

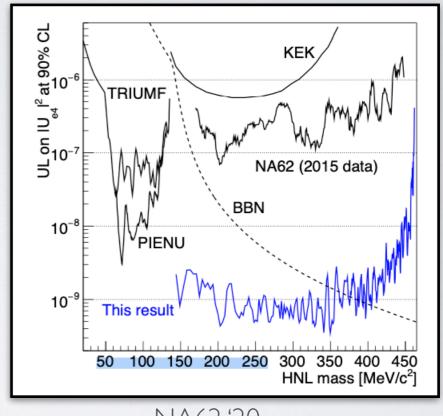
$${}_{Z}^{A}X \rightarrow {}_{Z+1}^{A}Y + e^{-} + \iota$$

Measure the sum of decay rates, for example:

$$\frac{d\Gamma}{dE_e} = \frac{d\Gamma_{\nu}}{dE_e} + U_{e4}^2 \frac{d\Gamma_4}{dE_e} + U_{e5}^2 \frac{d\Gamma_5}{dE_e}$$

• Sensitivity limited by experimental accuracy and theoretical control of spectral shape



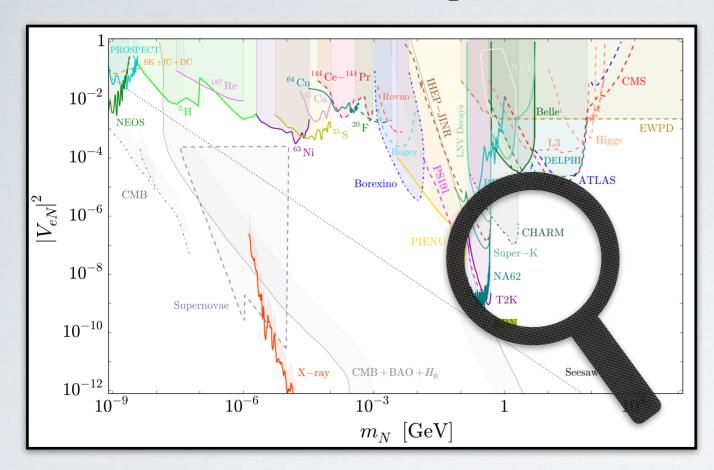


NA62 '20

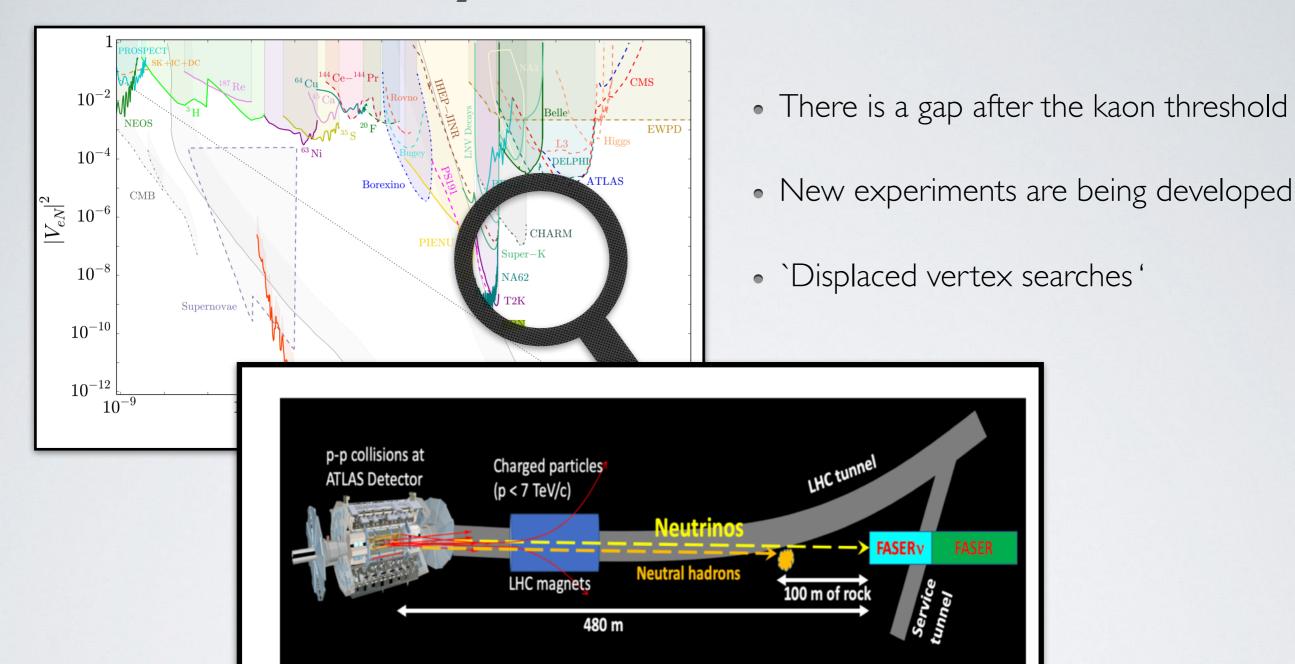
• Light sterile neutrinos can be produced in meson-decays  $K^{\pm}$ ,  $\pi^{\pm} \rightarrow e^{\pm} + N$ 

$$K^{\pm}, \pi^{\pm} \rightarrow e^{\pm} + N$$

- Much cleaner than beta-decay and much more phase space —> Stronger limits
- Works up to Kaon mass threshold ~ 450 MeV.
- Sensitivity limited by statistics (number of mesons)/background control



- There is a gap after the kaon threshold
- New experiments are being developed
- `Displaced vertex searches '



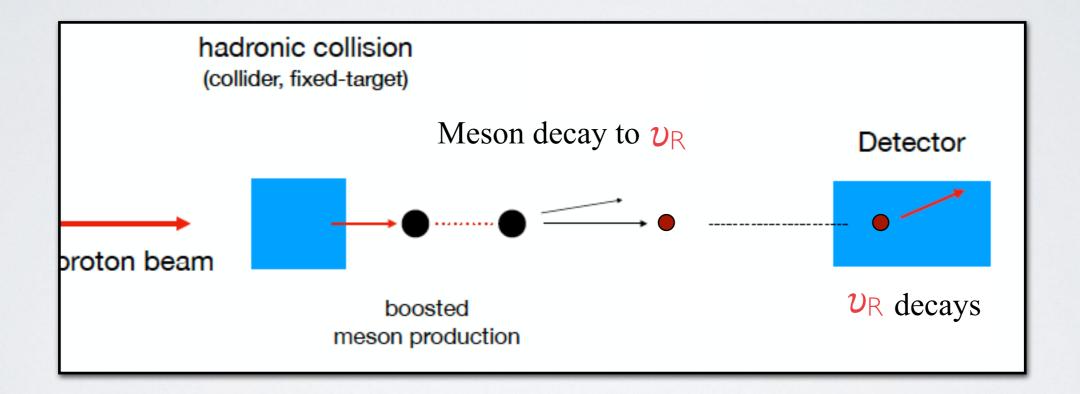
arXiv:2303.14185 (hep-ex)

[Submitted on 24 Mar 2023]

First Direct Observation of Collider Neutrinos with FASER at the LHC

#### Sterile neutrino from meson decay

- Idea: at colliders huge amount of mesons are produced (strong interaction)
- Some mesons decay through weak interaction -> better chance to produce  $v_R$
- Sterile neutrinos are relatively **long-lived**: escape conventional detectors

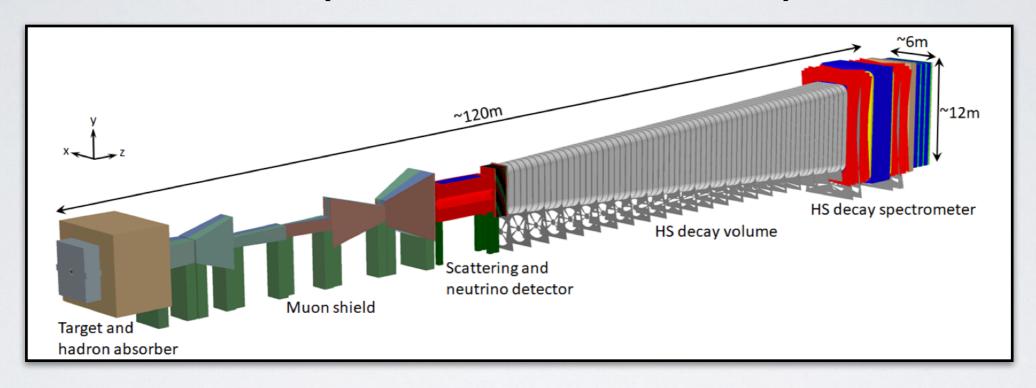


- Detector is placed far away from interaction point (tens to hundreds of meters)
- Space to install veto and shielding segments

#### **New experiments**

Many proposed experiments (MATHUSLA, CODEX-b, ANUBIS, MoEDAL)....

#### ShiP (Search for hidden Particles)

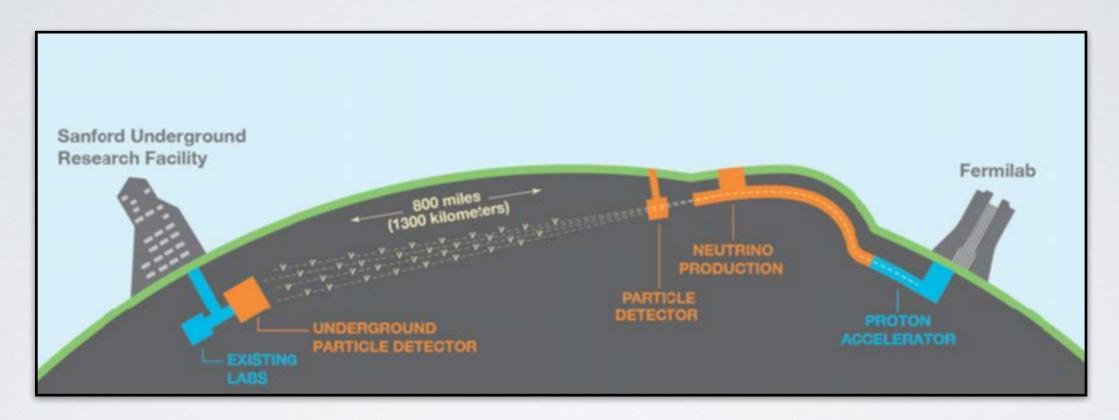


- Dump the SPS CERN beam (Super Proton Synchrotron) (400 GeV) on a dense target
- Huge amount of charm  $(10^{17})$  and beauty  $(10^{13})$  mesons produced in 4 year of running
- Data-taking to start in 2030.

#### New experiments

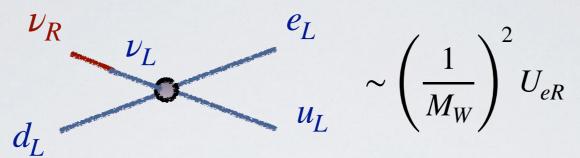
Many proposed experiments (MATHUSLA, CODEX-b, ANUBIS, MoEDAL)....

#### **DUNE (Deep Underground Neutrino Experiment)**

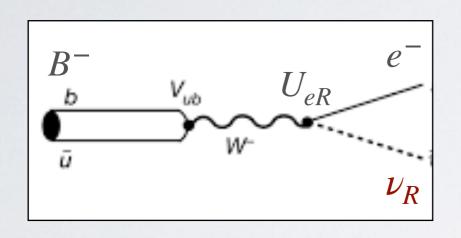


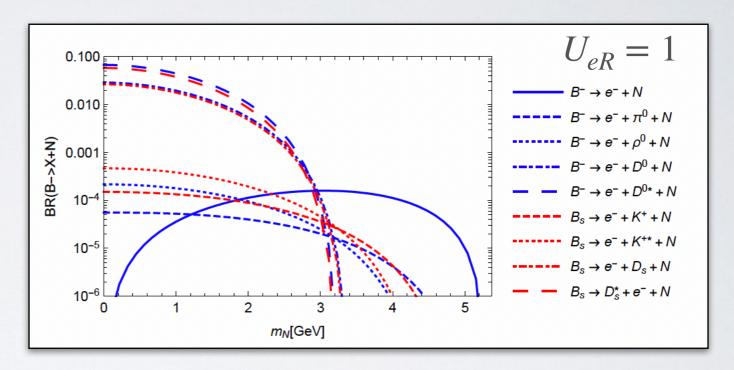
- 120 GeV proton beam on target to produce a neutrino beam
- 'Near'-detector roughly 574 m away
- Experiment operational end of this decade

#### Production and decay of sterile neutrinos



#### Example: Sterile neutrino production from beauty (B) meson decays





#### In turn sterile neutrino decays to visible or invisible final states

$$\nu_R \to e^- + \pi^+ \qquad \nu_R \to \nu_L + K^0$$

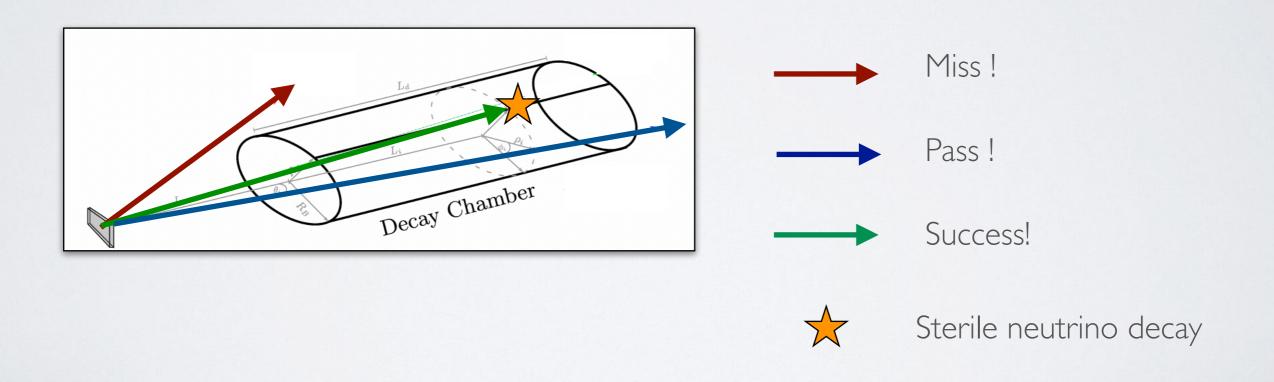
$$\nu_R \to e^- + e^+ + \nu_L \qquad \nu_R \to \nu_L + \bar{\nu}_L + \nu_L$$

#### **Simulations**

Compute meson production at experiments with Pythia simulations

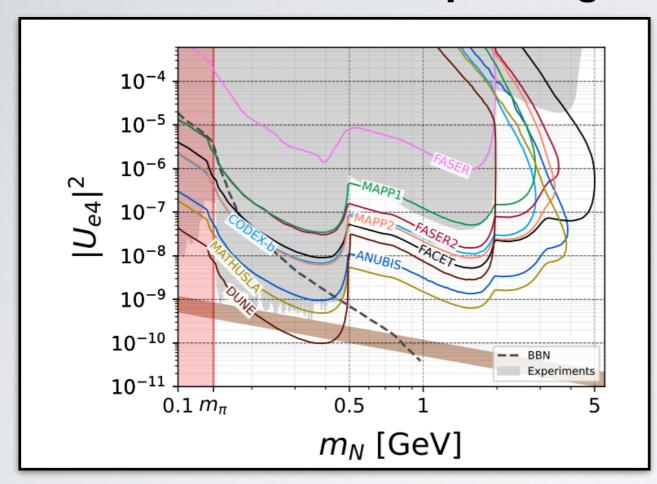
$$N_N^{\text{prod}} = \sum N_{M_i} \cdot \text{Br}(M_i \to N + X)$$

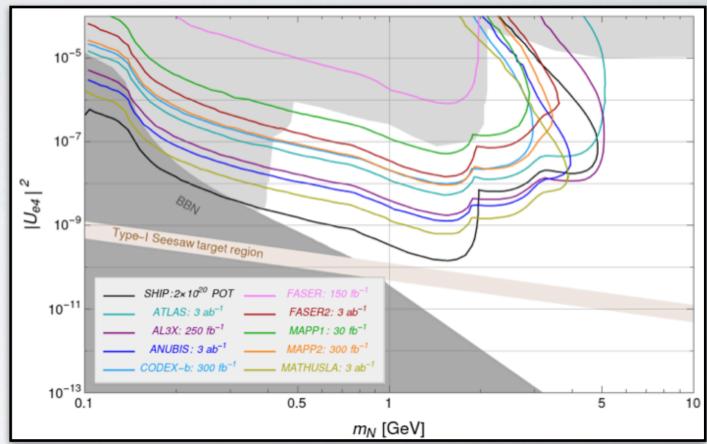
- Simulate around 106 events and rescale to total number of produced mesons in experiment
- For each proposed experiment then determine probability of decay in detector



#### **Minimal scenarios**

Current limits will improve significantly with new experiments



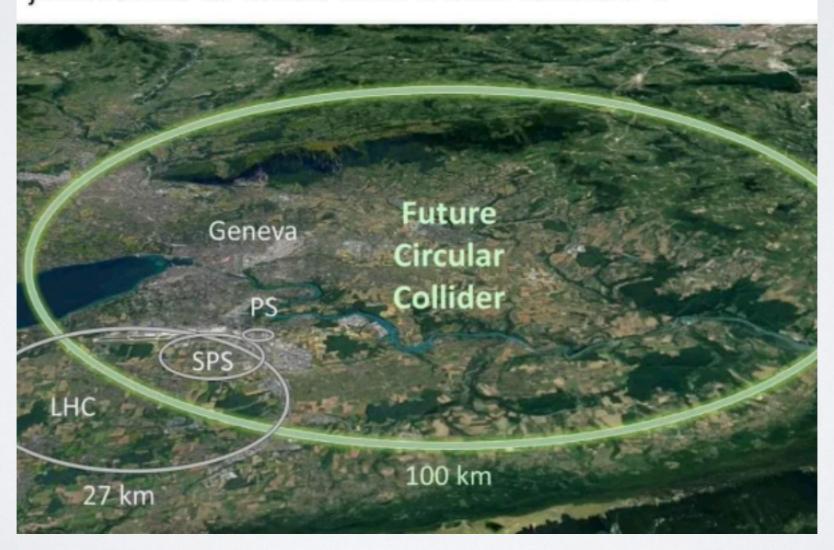


JdV et al JHEP '21 '23

See also many other works: Bondarenko et al, Shaposhnikov et al, Drewes et al, Pascoli et al

- Proposed experiments can come pretty close or even cover the seesaw band
- Unfortunately only works in mass range MeV-GeV.

just one more collider bro. i promise bro just one more collider and we'll find all the particles bro. it's just a bigger collider bro. please just one more. one more collider and we'll figure out dark matter bro. bro cmon just give me 22 billion dollars and we'll solve physics i promise bro. bro bro please we just need to build one more collider t

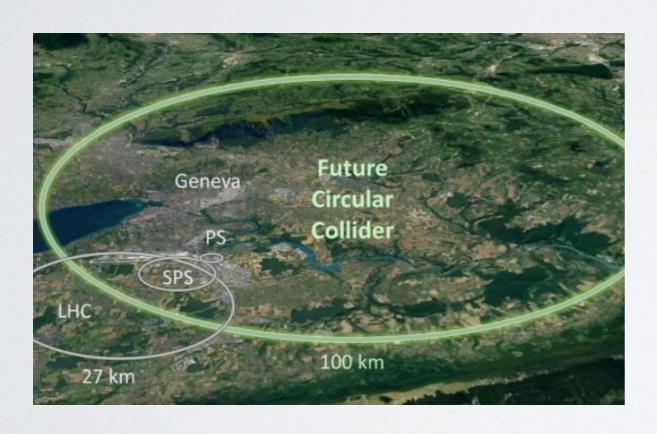


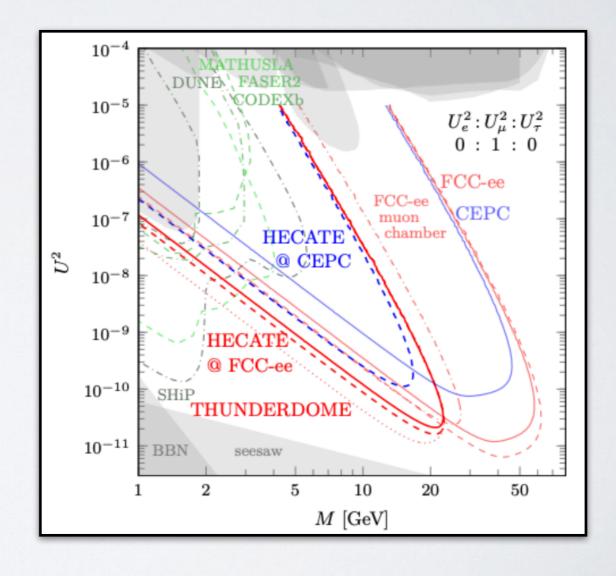
#### The future is now

• FCC-ee running at the Z-pole would produce huge amounts of on-shell Z bosons

$$e^- + e^+ \rightarrow Z \rightarrow \nu_L + \nu_R$$

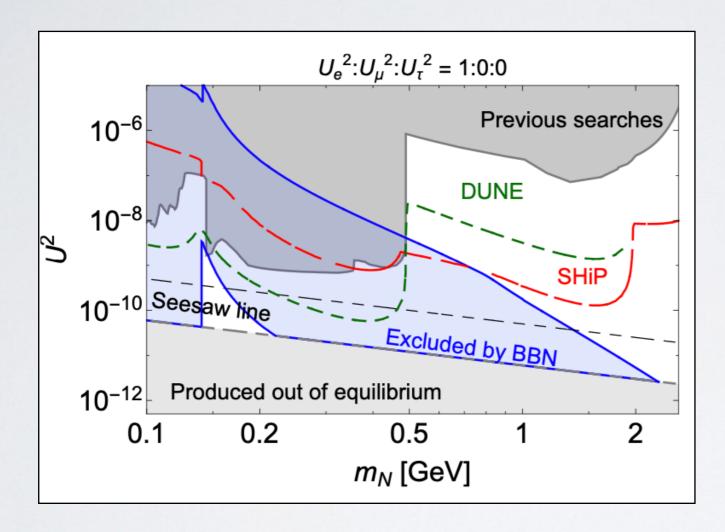
• Then perform a displaced vertex search of the sterile neutrino decay





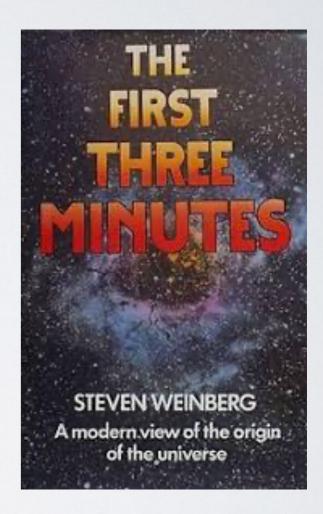
# Big Bang Nucleosynthesis

- Sterile neutrinos with can modify BBN
- Most couplings lead to thermal equilibrium in early universe —> relativistic freeze out
- Require that they decay before BBN times (~ I sec)



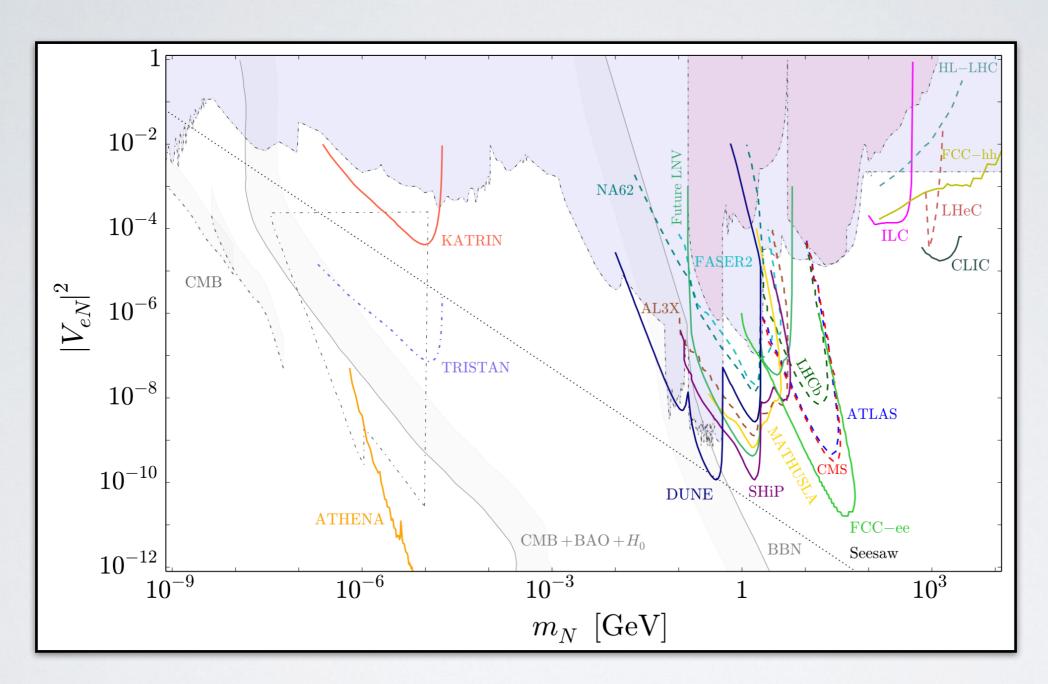
Boyarsky et al '20

- BBN bounds can be avoided in more complicated cosmological models
- Minimal models essentially require masses above MeV scale



Dolgov et al '00 Ruchayskiy et al '12 Pospelov/Pradler '10

#### Summary of future prospects

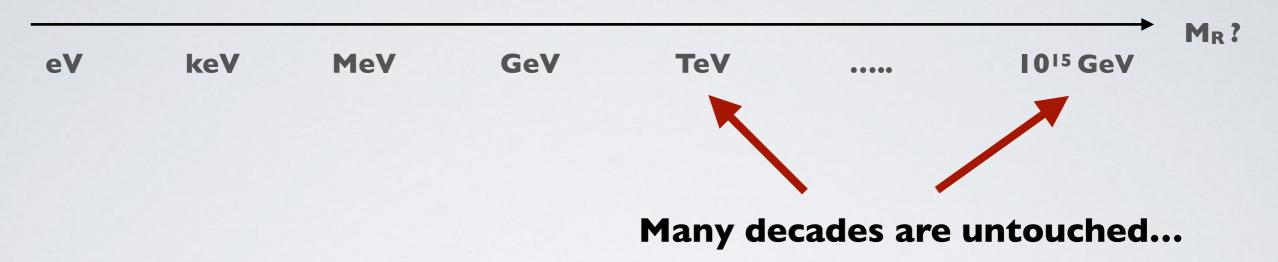


• Sterile neutrinos below I TeV: we can really discover them!

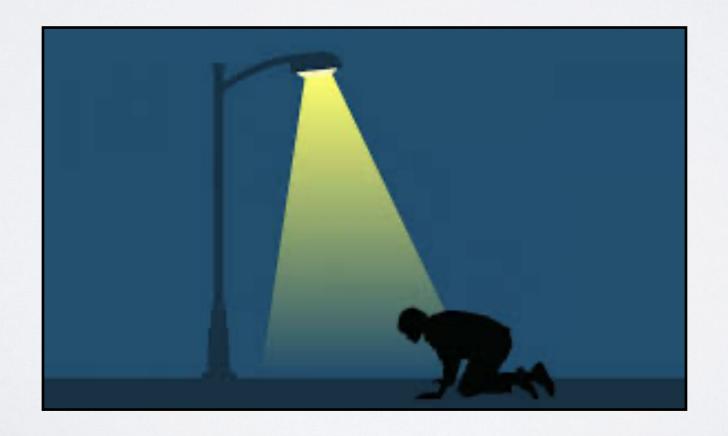


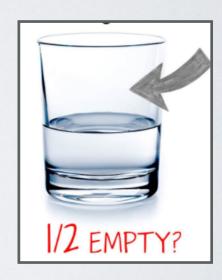
## Heavy-weight neutrinos

See-saw (variants) can work for essentially any right-handed scale ...



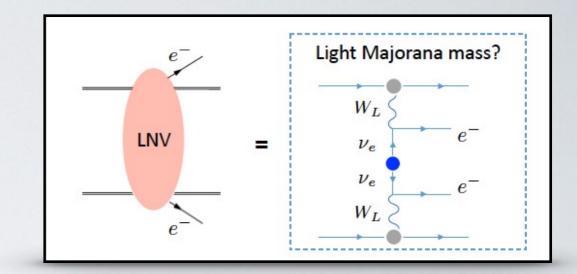
• For  $m_R \ge 10$  TeV or so, we'll probably not be able to produce them this century





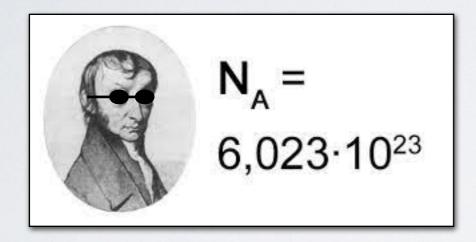
Most promising way: look at `neutrinoless' processes

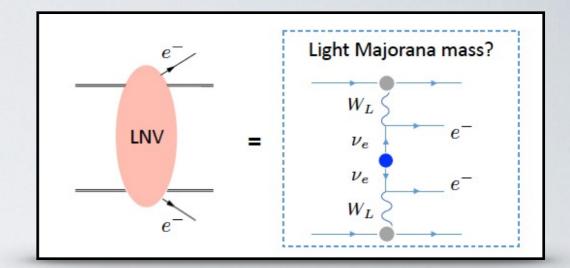
$$K^- \to \pi^+ + e^- + e^- \quad pp \to e^+ + e^+ + \text{jets}$$
  
 $X(Z, N) \to Y(Z + 2, N - 2) + e^- + e^-$ 



Most promising way: look at `neutrinoless' processes

$$K^{-} \to \pi^{+} + e^{-} + e^{-}$$
  $pp \to e^{+} + e^{+} + \text{jets}$   
 $X(Z, N) \to Y(Z + 2, N - 2) + e^{-} + e^{-}$ 





Most promising way: look at `neutrinoless' processes

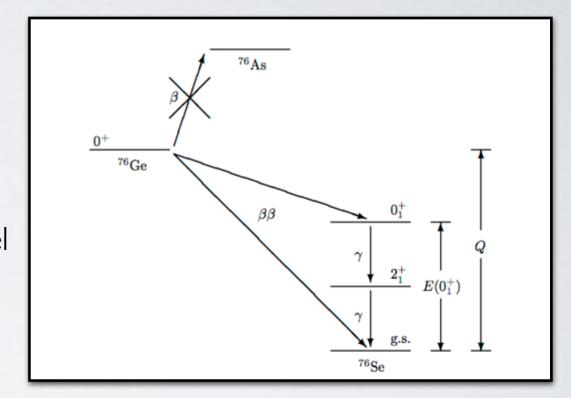
$$K^{-} \to \pi^{+} + e^{-} + e^{-}$$
  $pp \to e^{+} + e^{+} + \text{jets}$ 

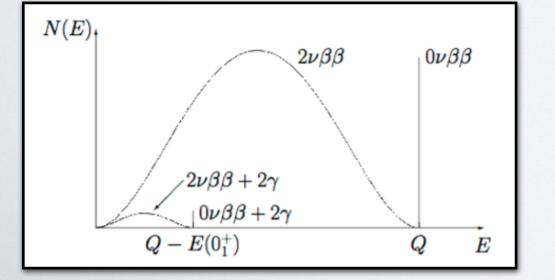
$$X(Z,N) \rightarrow Y(Z+2,N-2) + e^- + e^-$$

- Isotopes protected from single beta decay
- Neutrinofull double beta decay from Standard Model

$$X(Z,N) \rightarrow Y(Z+2,N-2) + 2e^{-} + 2\bar{\nu}_{e}$$

$$T_{1/2}^{2\nu} \left( {^{76}Ge} \rightarrow {^{76}Se} \right) = \left( 1.84_{-0.10}^{+0.14} \right) \times 10^{21} \ yr$$





	Lifetime	Experiment	Year
76Ge	$8.0 \cdot 10^{25}  y$	GERDA	2018
130Te	$3.2 \cdot 10^{25}  y$	CUORE	2019
136Xe	$3.8 \cdot 10^{26}  \mathrm{y}$	KamLAND-Zen	2024

Note: age of universe  $\sim 10^{10}$  year

Most promising way: look at `neutrinoless' processes

$$K^{-} \to \pi^{+} + e^{-} + e^{-} \quad pp \to e^{+} + e^{+}$$

$$X(Z,N) \to Y(Z+2,N-2) + e^{-} + e^{-}$$

- Isotopes protected from single beta decay
- Neutrinofull double beta decay from Standa

$$X(Z,N) \rightarrow Y(Z+2,N-2) + 2e^{-} + 2\bar{\nu}_{e}$$

$$T_{1/2}^{2\nu} \left( {^{76}Ge} \rightarrow {^{76}Se} \right) = \left( 1.84_{-0.10}^{+0.14} \right) \times 10^{21} \ yr$$

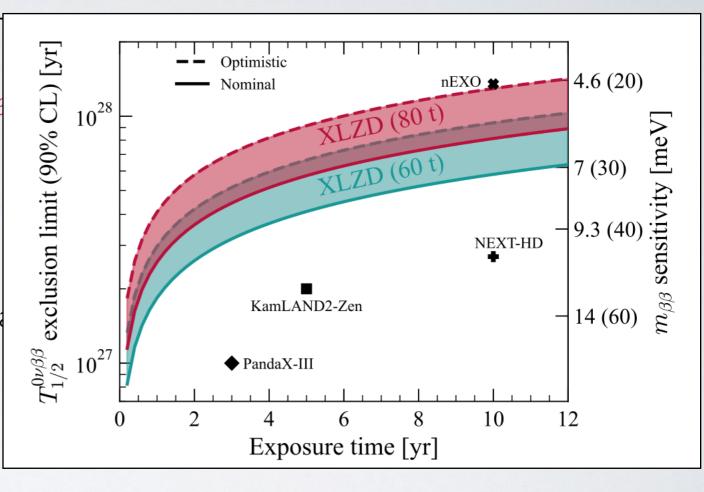


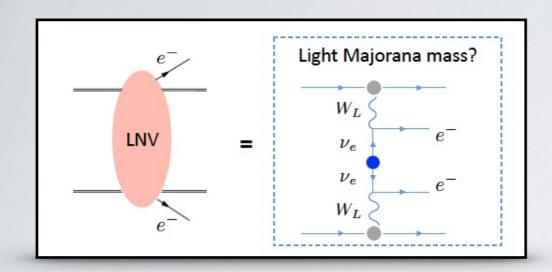
Figure from XLZD collaboration, 2410.19016

N(E)	2 uetaeta	0 uetaeta
	$2\nu\beta\beta+2\gamma$	
st.	$2\nu\beta\beta + 2\gamma$ $0\nu\beta\beta + 2\gamma$	
سنائد	$Q - E(0_1^+)$	Q   E

	Lifetime	Experiment	Year
76Ge	$8.0 \cdot 10^{25}  y$	GERDA	2018
130Te	$3.2 \cdot 10^{25}  y$	CUORE	2019
136Xe	$3.8 \cdot 10^{26} \mathrm{y}$	KamLAND-Zen	2024

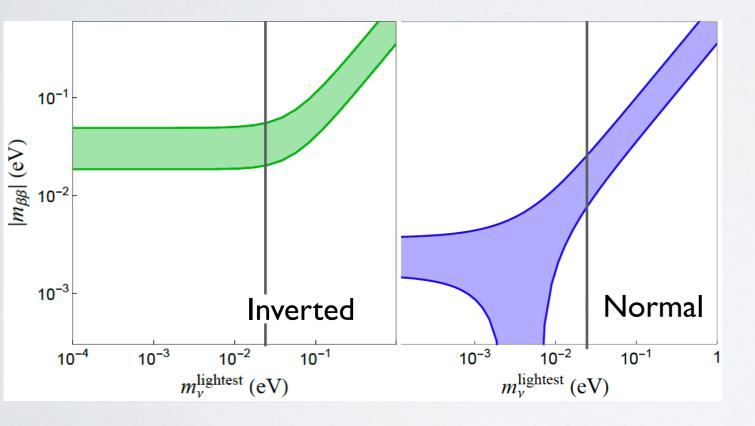
Note: age of universe ~ 10<sup>10</sup> year

# Interpreting 10<sup>26</sup> years....



$$1/\tau \sim |M_{0\nu}|^2 m_{\beta\beta}^2 \qquad m_{\beta\beta} = \sum_i U_{ei}^2 m_i$$

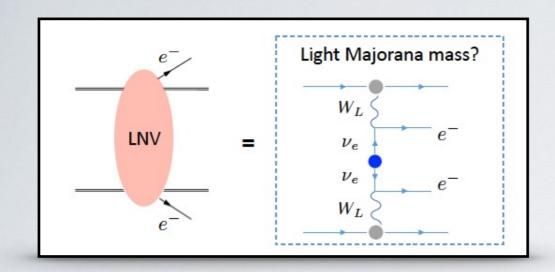
$$m_{\beta\beta} = m_1 c_{12}^2 c_{13}^2 + m_2 s_{12}^2 c_{13}^2 e^{2i\lambda_1} + m_3 s_{13}^2 e^{2i(\lambda_2 - \delta_{13})} = \text{Effective neutrino mass}$$



Vary the lightest mass and the ordering Band from varying unknown phases

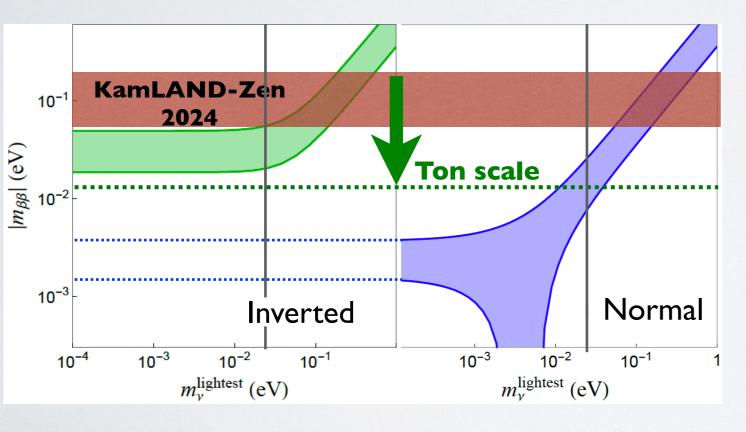
How close are experiments?

# Interpreting 10<sup>26</sup> years....



$$1/\tau \sim |M_{0\nu}|^2 m_{\beta\beta}^2 \qquad m_{\beta\beta} = \sum_i U_{ei}^2 m_i$$

$$m_{\beta\beta} = m_1 c_{12}^2 c_{13}^2 + m_2 s_{12}^2 c_{13}^2 e^{2i\lambda_1} + m_3 s_{13}^2 e^{2i(\lambda_2 - \delta_{13})} = \text{Effective neutrino mass}$$



#### Quite close !!

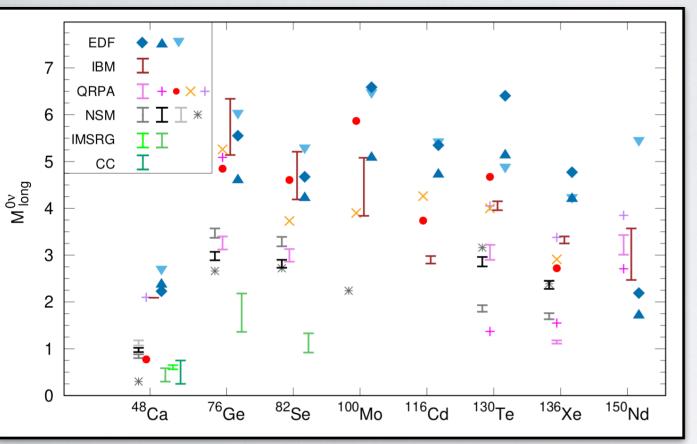
Next-generation discovery possible if inverted hierarchy or m<sub>lightest</sub> >0.01 eV

Note: FUNNEL OF DESPAIR and THE DEAD ZONE

See Denton & Gehrlein '23 for the likelihood that we live in the funnel

#### Predictions are hard, especially about the future nuclei

From: Menendez et al review '22



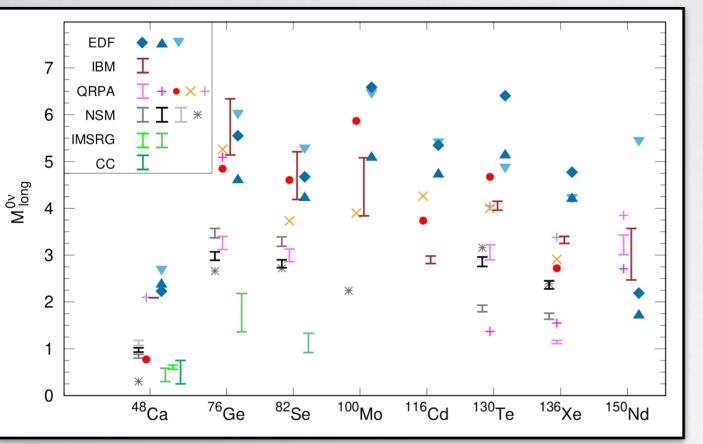
$$1/\tau \sim |M_{0\nu}|^2 m_{\beta\beta}^2$$

Uncertainties factor 5!
So factor 25 on the life time!

Where is this coming from?

#### Predictions are hard, especially about the future nuclei

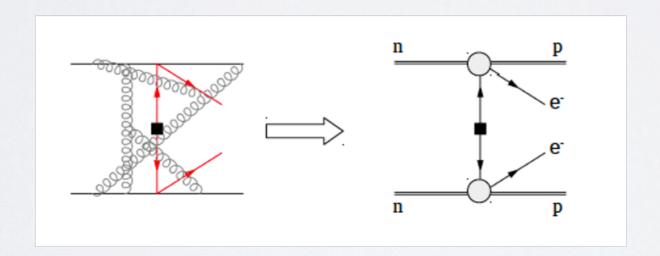
From: Menendez et al review '22



$$1/\tau \sim |M_{0\nu}|^2 m_{\beta\beta}^2$$

Uncertainties factor 5!
So factor 25 on the life time!

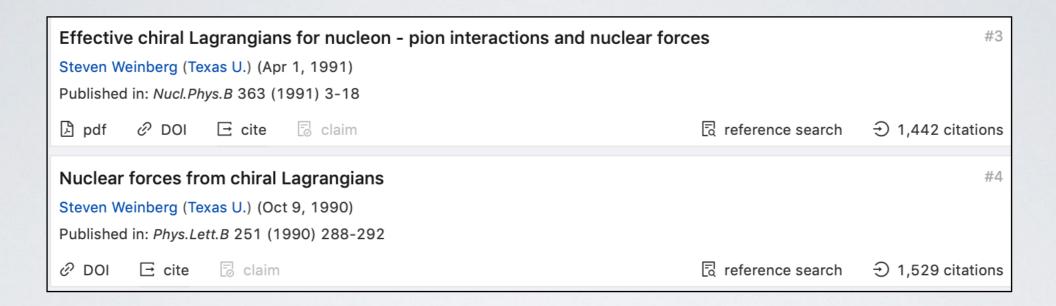
Where is this coming from?



- Large nuclei —> complicated many-body nuclear matrix elements
- Nuclear methods and codes are benchmarked on 'single-nucleon-currents' physics

#### **Nuclear physics from QCD**

• In the 90's Weinberg (who else) wrote 2 very nice papers



[Submitted on 16 Feb 2025]

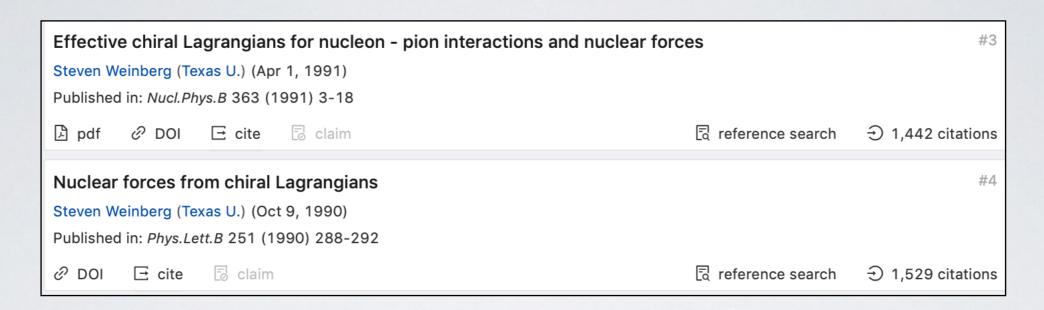
### Steven Weinberg: A Scientific Life

C.P. Burgess, F. Quevedo

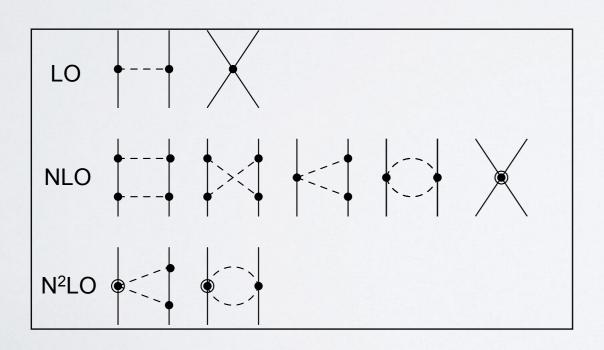
Weinberg used similar tools to compute the inter-nucleon forces implied at low energies by generalizing the effective theory governing low-energy pion interactions to include nonrelativistic nucleons [85–87] (see also [88]). By so doing he enabled the calculation of *ab initio* nuclear energy levels for the first time, at least for light nuclei involving comparatively few protons and neutrons. Nuclear physicists at the time were instead fitting data from nuclear measurements with models in which meson exchange between nucleons assumed phenomenological couplings.

### **Nuclear physics from QCD**

• In the 90's Weinberg (who else) wrote 2 very nice papers



Describe the nucleon-nucleon force from chiral perturbation theory



- Effective field theory description of nuclear forces and currents
- Systematic expansion
- Nuclei from solving Schrodingerlike equations
- Wilson coefficient (low-energy constants fitted to few-nucleon data) -> predict larger systems

Developed by van Kolck, Meißner, Epelbaum, Machleidt and many others ....

#### **Example at leading order**

$$V_{NN} = C_0 - \frac{g_A^2}{4f_\pi^2} \frac{m_\pi^2}{\mathbf{q}^2 + m_\pi^2}$$

$$= V_{NN} + V_{NN} V_{NN} + V_{NN} V_{NN} V_{NN} + \cdots$$

Loops appearing here typically diverge and one has to regulate (typically numerically)

$$V_{\rm NN} \rightarrow e^{-p^6/\Lambda^6} \times V_{\rm NN} \times e^{-p^{'6}/\Lambda^6}$$

• Fit counter term  $C_0$  to nucleon-nucleon scattering data for each  $\Lambda$ 

#### **Example at leading order**

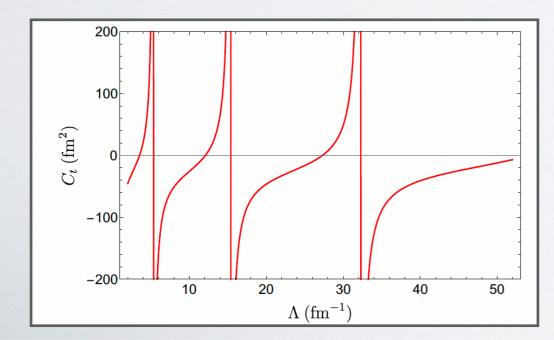
$$V_{NN} = C_0 - \frac{g_A^2}{4f_\pi^2} \frac{m_\pi^2}{\mathbf{q}^2 + m_\pi^2}$$

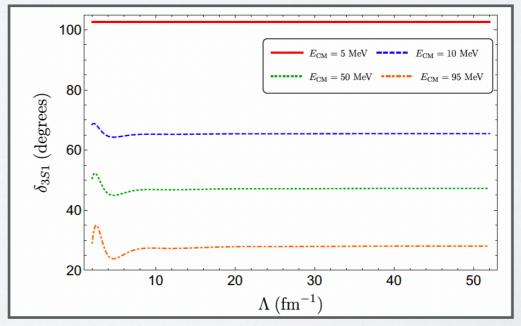
$$= V_{NN} + V_{NN} V_{NN} + V_{NN} V_{NN} V_{NN} + \cdots$$

Loops appearing here typically diverge and one has to regulate (typically numerically)

$$V_{\rm NN} \rightarrow e^{-p^6/\Lambda^6} \times V_{\rm NN} \times e^{-p^{'6}/\Lambda^6}$$

- Fit counter term  $C_0$  to nucleon-nucleon scattering data for each  $\Lambda$
- This is called 'non-perturbative renormalization'. This is now down at very high order.
- Use nucleon-nucleon + three-nucleon data to fit constants —> predict nuclear physics





Nogga, Timmermans, van Kolck '05

#### Some successes (not by me)

• Chiral EFT —> derive nuclear properties + reactions —> equation of state + neutron stars

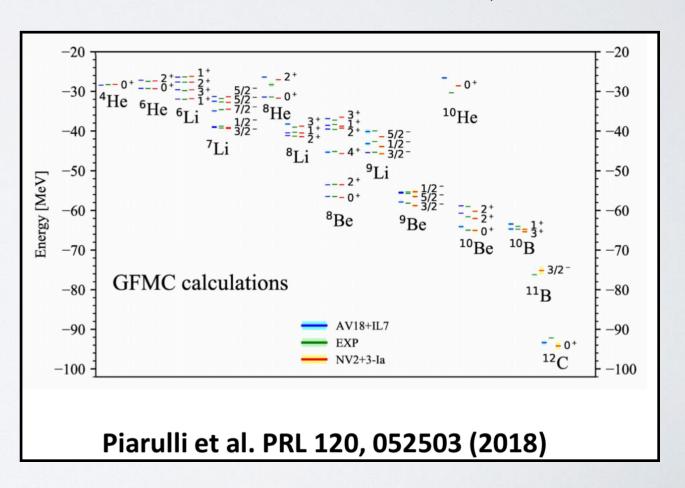


Hu et al '22





Gysbers et al '20

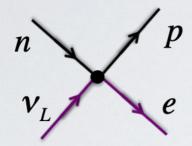


# Light Majorana neutrinos (standard mechanism)

Neutrinos are still degrees of freedom in low-energy chiral EFT



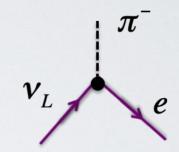
Basically just use low-energy chiral Lagrangian with weak interactions



$$P \qquad L_{\chi,Fermi} = G_F f_{\pi} \left( \partial_{\mu} \pi^{-} \overline{e}_{L} \gamma^{\mu} v_{L} \right)$$

$$e \qquad + G_F \overline{p} \left( \gamma^{\mu} - g_{A} \gamma^{\mu} \gamma^{5} \right) n \overline{e}_{L} \gamma^{\mu} v_{L} + \cdots$$

$$P \qquad V_{L} \qquad e$$



# Light Majorana neutrinos (standard mechanism)

Neutrinos are still degrees of freedom in low-energy chiral EFT

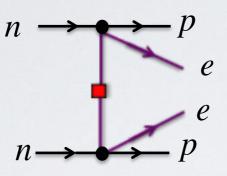


Basically just use low-energy chiral Lagrangian with weak interactions

- This is the leading-order 'neutrino potential'.
- Then insert this 'potential' between nuclear wave functions  $A_{\nu} = \langle \Psi_f | V_{\nu} | \Psi_i \rangle$
- Note: the nucleons appear in a bound state and q is a loop momentum

# Light Majorana neutrinos (standard mechanism)

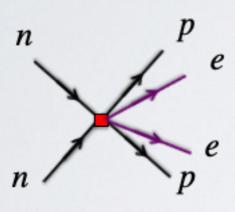
Leads to 'long-range' nn → pp + ee



$$V_{\nu} \sim \frac{m_{\beta\beta}}{\mathbf{q}^2}$$

$$\mathbf{q} \sim k_F \sim m_\pi$$

 $\mathbf{q} \sim \Lambda_{\gamma} \sim 1 \,\mathrm{GeV}$ 



- Contributions from virtual hard neutrinos
- Naive-dimensional analysis tells us this is NNLO

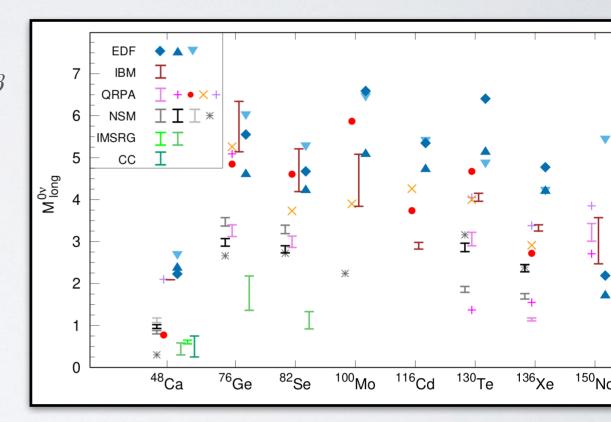
$$V_{\nu}^{short} \sim \frac{m_{\beta\beta}}{\Lambda_{\chi}^2}$$

Loops and other corrections at higher order in chiral EFT expansion

# Leading-order transition currents

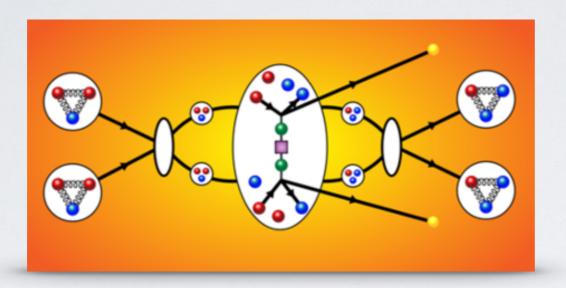
$$V_{\nu} = (2G_F^2 m_{\beta\beta}) \tau_1^+ \tau_2^+ \frac{1}{\mathbf{q}^2} \left[ (1 + 2g_A^2) + \frac{g_A^2 m_{\pi}^4}{(\mathbf{q}^2 + m_{\pi}^2)} \right] \otimes \bar{e}_L e_L^c$$

- Leading-order Ovbb current is very simple
- ullet No unknown hadronic input! Only unknown is  $m_{etaeta}$
- Many-body methods disagree significantly
- Original idea: study simpler nuclear systems
- Not relevant for experiments but as a theoretical laboratory



### **Neutron-Neutron** → **Proton-Proton**

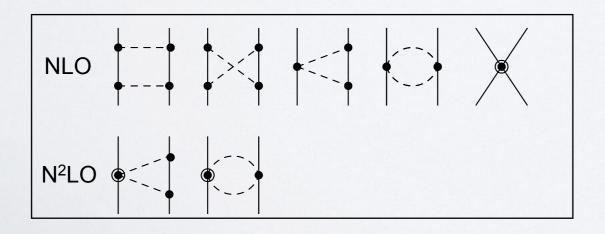
Study simplest nuclear process: nn → pp + ee



Derive wave functions from chiral effective field theory

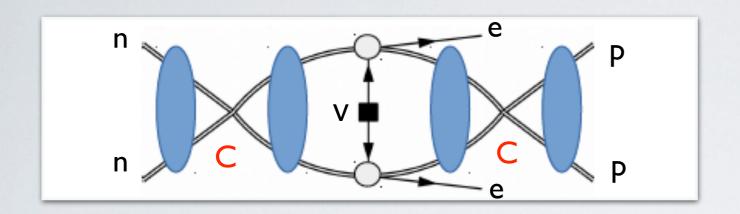


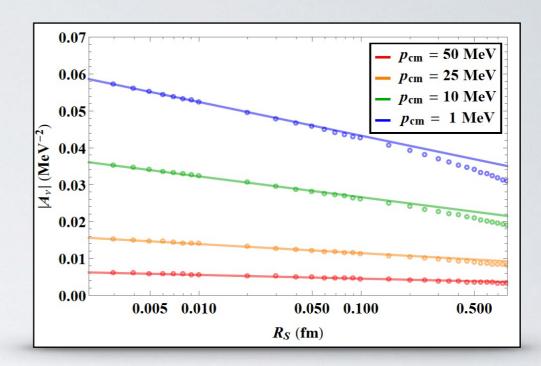
Weinberg 90'91'



Weinberg
Van Kolck et al,
Epelbaum et al,
Machleidt et al,
And many more...

#### It doesn't work





$$\sim (1 + 2g_A^2) \left(\frac{m_N C_0}{4\pi}\right)^2 \left(\frac{1}{\epsilon} + \log \frac{\mu^2}{p^2}\right)$$

#### **New divergences**

#### The leading order amplitude is not renormalized!

Featured in Physics

**Editors' Suggestion** 

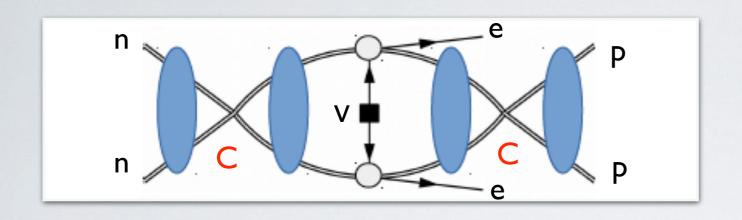
**Open Access** 

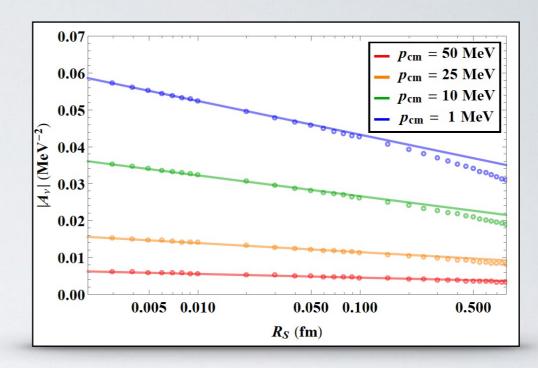
New Leading Contribution to Neutrinoless Double- $\beta$  Decay

Vincenzo Cirigliano, Wouter Dekens, Jordy de Vries, Michael L. Graesser, Emanuele Mereghetti, Saori Pastore, and Ubirajara van Kolck

Phys. Rev. Lett. 120, 202001 - Published 16 May 2018

#### It doesn't work

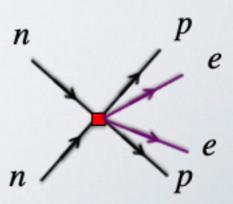




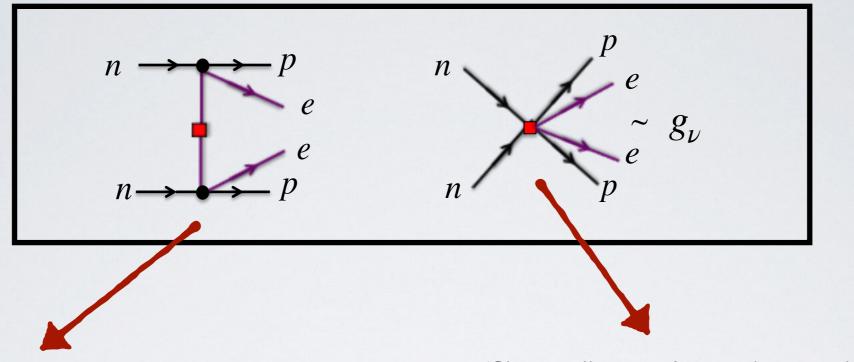
$$\sim (1 + 2g_A^2) \left(\frac{m_N C_0}{4\pi}\right)^2 \left(\frac{1}{\epsilon} + \log \frac{\mu^2}{p^2}\right)$$

#### **New divergences**

- Logarithmic regulator dependence
- Divergence indicates sensitivity to short-distance physics (hard-neutrino exchange)
- Suggest to add a counter term: a short-range nn → pp + ee operator
- Literature: 'breakdown of Weinberg power counting'



# A new leading-order contribution



'Long-range' neutrino-exchange

'Short-distance' neutrino exchange required by renormalization of amplitude

### ullet Short-distance piece depends on QCD matrix element $ullet g_{ u}$

This was initially unknown but has now been determined (long story for a technical talk)

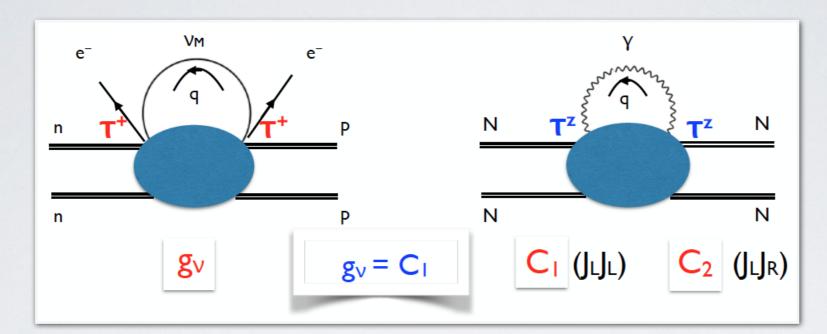
Cirigliano, Dekens, JdV, Hoferichter, Mereghetti PRC '19 PRL '21 JHEP '21 Davoudi, Kadam PRL '21 Briceno et al '19 '20 Van Groffier '24

Richardson, Schindler, Pastore, Springer '21 Tuo et al. '19; Detmold, Murphy '20 '22 Yang, Zhao '23 '24

• Ovbb calculations have to be redone —> This is now happening by many groups

# A connection to electromagnetism

A neutrino-exchange process looks like a photon-exchange process

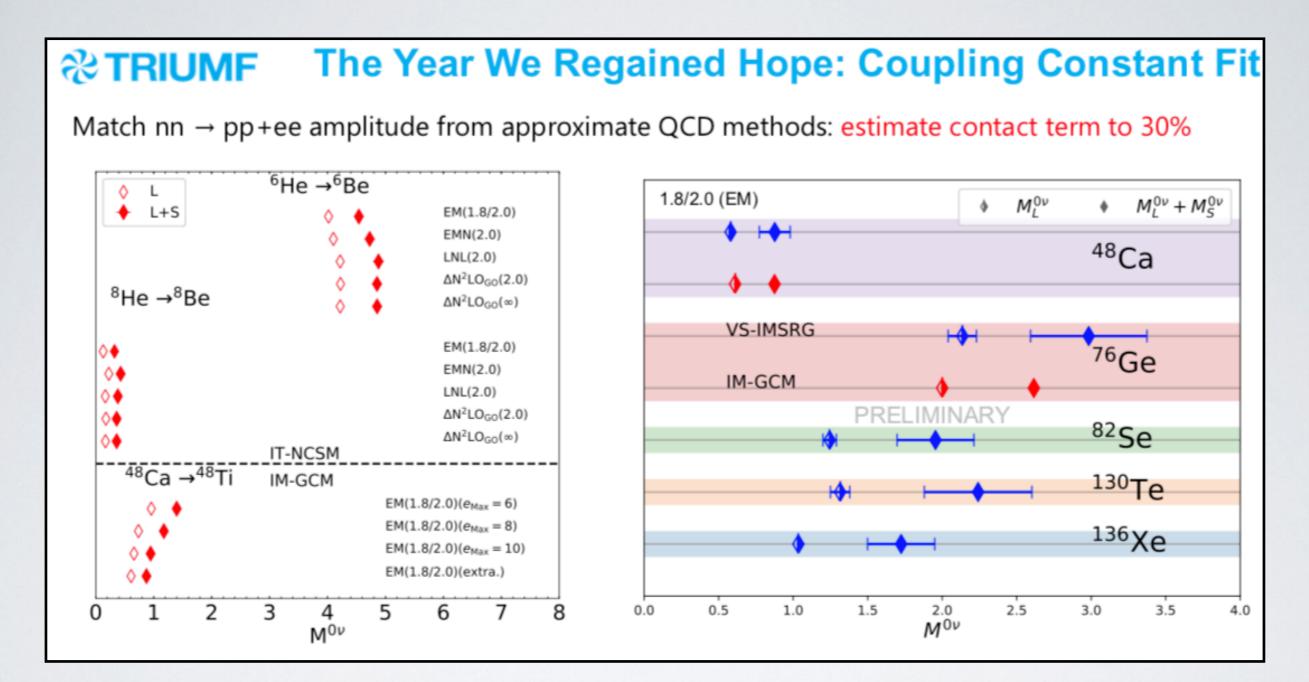


Cirigliano et al 19

Walzl, Meißner, Epelbaum '01

- Chiral connection between double-weak and double-EM NN interactions
- Isospin-breaking nucleon-nucleon scattering data determines C<sub>1</sub>+C<sub>2</sub>
- Electromagnetism conserves **parity** coupling and  $g_v \sim C_1$  only
- Large-Nc arguments indicates  $C_1 + C_2 \gg C_1 C_2$  Richardson, Schindler, Pastore, Springer PRC'21
- This seems to work surprisingly well
   Cirigliano, Dekens, JdV, Hoferichter, Mereghetti PRL '21
   Van Groffier '24
   Yang, Zhao PLB '23 '24

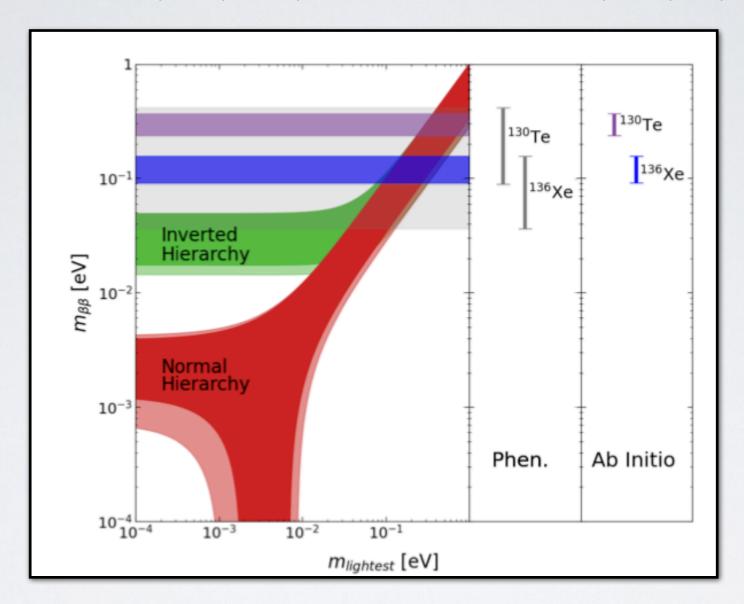
## Impact on realistic nuclei



- Slides from Jason Holt (TRIUMF) at Institute of Nuclear Physics Seattle (2024)
- The contact term enhances NMEs by 100% (Ca) to 70% (Xe) (factor 3-4 on the lifetime)

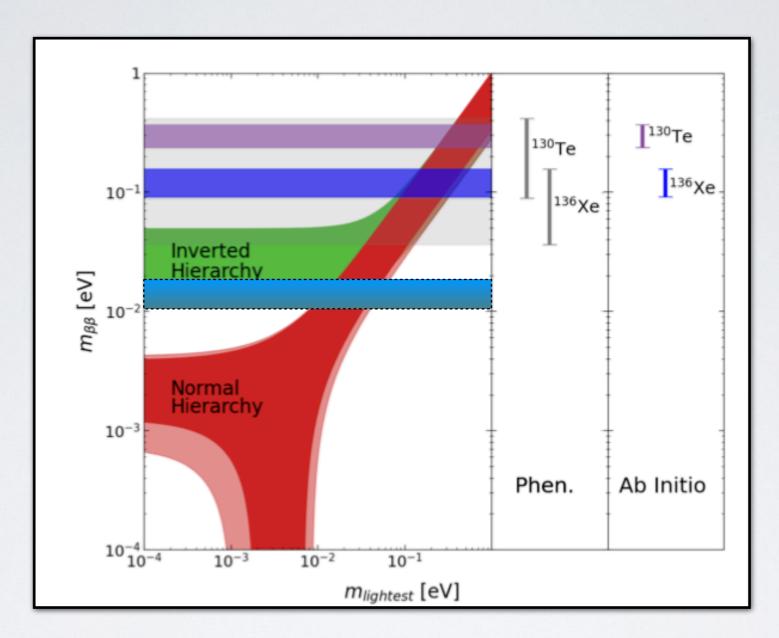
## Impact on realistic nuclei

Results from 2307.15156 (Belley et al) and PRL 132, 182502 (2024) + papers from '21 '22



- Ab initio calculations find rather small NME compensated by contact term
- Counter term leads to smaller model dependence: uncertainties at 30-40% level
- Not clear to me how to connect chiral EFT to phenomenological nuclear models

## Intermediate summary



- NMEs are still a big problem but there has been progress
- Next-gen experiments to reach inverted hierarchy but normal hierarchy remains difficult (unless  $m_1 \sim 0.01 \text{ eV}$ )

## The plan of attack

I. Motivation: the puzzle of neutrino masses

- 2. Probing sterile neutrinos directly and indirectly
  - Effective field theory for Ovbb

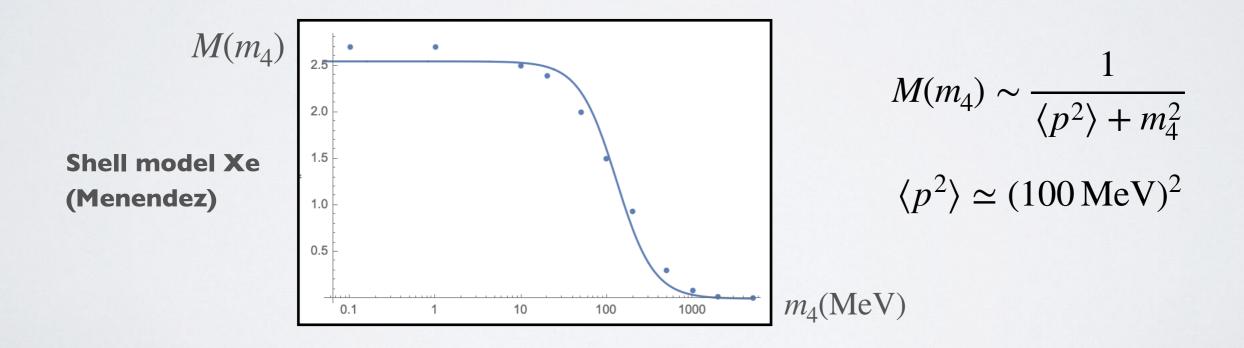
3. Connection to low-scale leptogenesis

# Impact of light sterile neutrinos?



• For masses below a GeV, the sterile neutrinos become explicit degrees of freedom

$$|M_{0\nu}(m_R)|^2 = |\langle 0^+ | V_{\nu}(m_R) | 0^+ \rangle|^2$$



# Revisit the light regime

$$A_{\nu} \sim \sum_{i=1}^{3} U_{ei}^{2} m_{i} \frac{1}{\langle p^{2} \rangle} + U_{e4}^{2} m_{4} \frac{1}{\langle p^{2} \rangle + m_{4}^{2}} \qquad \xrightarrow{m_{4} \ll 100 \,\text{MeV}} \qquad A_{\nu} \sim \sum_{i=1}^{4} U_{ei}^{2} m_{i} \frac{1}{\langle p^{2} \rangle} + \mathcal{O}\left(\frac{m_{i}^{3}}{\langle p^{2} \rangle^{2}}\right)$$

- The first term depends on  $\sum_{i=1}^4 U_{ei}^2 m_i = M_{ee} = 0 \qquad M = \begin{pmatrix} 0 & v y_\nu \\ v y_\nu & M_R \end{pmatrix}$

$$M = \begin{pmatrix} 0 & vy_{\nu} \\ vy_{\nu} & M_R \end{pmatrix}$$

- The 'GIM' mechanism for neutrinos! (only valid if all steriles are light)
- The amplitude is strongly suppressed  $A_{\nu} \sim \sum_{ei}^{4} U_{ei}^2 m_i^3$  Blennow et al '10 JHEP

$$A_{\nu} \sim \sum_{i=1}^{4} U_{ei}^2 m_i^3$$

# Revisit the light regime

$$A_{\nu} \sim \sum_{i=1}^{3} U_{ei}^{2} m_{i} \frac{1}{\langle p^{2} \rangle} + U_{e4}^{2} m_{4} \frac{1}{\langle p^{2} \rangle + m_{4}^{2}}$$

$$A_{\nu} \sim \sum_{i=1}^{3} U_{ei}^{2} m_{i} \frac{1}{\langle p^{2} \rangle} + U_{e4}^{2} m_{4} \frac{1}{\langle p^{2} \rangle + m_{4}^{2}} \qquad \xrightarrow{m_{4} \ll 100 \,\text{MeV}} \qquad A_{\nu} \sim \sum_{i=1}^{4} U_{ei}^{2} m_{i} \frac{1}{\langle p^{2} \rangle} + \mathcal{O}\left(\frac{m_{i}^{3}}{\langle p^{2} \rangle^{2}}\right)$$

• The first term depends on 
$$\sum_{i=1}^4 U_{ei}^2 m_i = M_{ee} \ = 0 \qquad \qquad M = \begin{pmatrix} 0 & v y_\nu \\ v y_\nu & M_R \end{pmatrix}$$

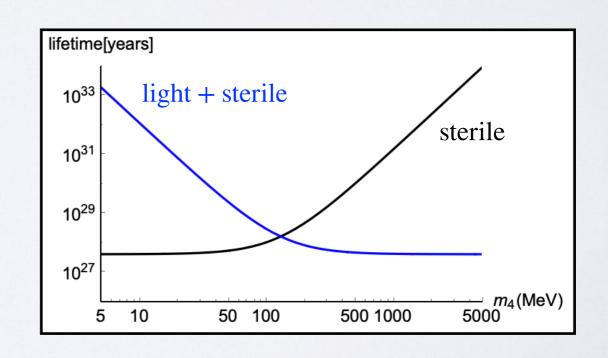
$$M = \begin{pmatrix} 0 & vy_{\nu} \\ vy_{\nu} & M_R \end{pmatrix}$$

- The 'GIM' mechanism for neutrinos! (only valid if all steriles are light)
- The amplitude is strongly suppressed

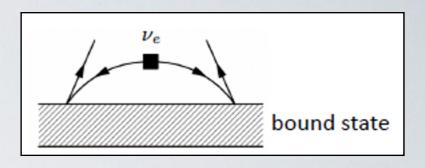
$$A_{\nu} \sim \sum_{i=1}^{4} U_{ei}^2 m_i^3$$
 Blennow et al '10 JHEP

- Example in 3+1 model
- Cancellation between light + sterile contributions leads to

$$\tau_{1/2} \sim m_4^4$$



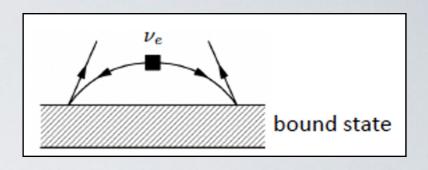
- Is there a way to avoid the GIM mechanism?
- There are additional contributions from 'ultra-soft' neutrinos



$$\sum_{n} \langle f | J_{\mu} | n \rangle \langle f | J^{\mu} | i \rangle \times \int \frac{d^{3}k}{(2\pi)^{3}} \frac{1}{E_{\nu}[E_{\nu} + (E_{n} - E_{0}) - i\epsilon]} \qquad E_{\nu} = \sqrt{k^{2} + m_{i}^{2}}$$

- The neutrinos see the nucleus as a whole and becomes sensitive to nuclear structure effects
- Depends on nuclear excited states. Normally these are tiny effects (5%)

- Is there a way to avoid the GIM mechanism?
- There are additional contributions from 'ultra-soft' neutrinos



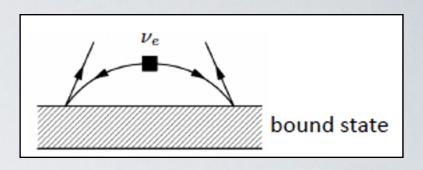
$$\sum_{n} \langle f | J_{\mu} | n \rangle \langle f | J^{\mu} | i \rangle \times \int \frac{d^{3}k}{(2\pi)^{3}} \frac{1}{E_{\nu}[E_{\nu} + (E_{n} - E_{0}) - i\epsilon]} \qquad E_{\nu} = \sqrt{k^{2} + m_{i}^{2}}$$

- The neutrinos see the nucleus as a whole and becomes sensitive to nuclear structure effects
- Depends on nuclear excited states. Normally these are tiny effects (5%)

$\frac{E_n - E_i}{\mathrm{MeV}}$	$\langle 1_n^+   \boldsymbol{\sigma} \tau^+   0_i^+ \rangle$	$\left \langle 0_f^+   \boldsymbol{\sigma} \tau^+   1_n^+ \rangle\right $	$\frac{E_n - E_i}{\text{MeV}}$	$\langle 1_n^+   \boldsymbol{\sigma} \tau^+   0_i^+ \rangle$	$\langle 0_f^+   \boldsymbol{\sigma} \tau^+   1_n^+ \rangle$	$\frac{E_n - E_i}{\mathrm{MeV}}$	$\langle 1_n^+   \boldsymbol{\sigma} \tau^+   0_i^+ \rangle$	$\langle 0_f^+   \boldsymbol{\sigma} \tau^+   1_n^+ \rangle$
0.17	1.	0.13	3.3	0.39	-0.0013	9.1	0.8	0.0038
0.63	-0.19	-0.0063	3.6	0.39	0.0021	9.4	0.59	0.0014
0.89	-0.25	-0.016	3.8	0.45	-0.013	9.8	-0.5	0.0027
1.02	0.3	0.036	4.0	-0.44	-0.0032	10.1	0.35	-0.0027
1.05	0.23	0.025	4.3	-0.35	-0.0038	10.5	0.26	-0.00053
1.1	-0.13	-0.00076	4.6	-0.36	-0.0067	10.9	-0.22	-0.00021
1.2	0.12	-0.0052	4.8	0.44	0.0083	11.3	0.17	-0.00037
1.3	0.16	-0.0028	5.1	0.44	0.0066	11.7	-0.16	-0.00054
1.4	-0.23	-0.0098	5.4	-0.55	-0.0093	12.0	-0.16	-0.001
1.5	0.2	-0.012	5.7	0.63	0.012	12.4	0.14	0.00092
1.6	-0.36	0.0084	6.1	0.85	0.013	12.8	0.12	-0.00014
1.7	-0.24	0.00058	6.3	-1.2	-0.016	13.1	0.092	-0.0004
1.9	0.22	0.011	6.7	-1.3	-0.014	13.5	-0.079	-0.00019
2.0	0.34	0.007	7.0	-1.9	-0.016	13.9	0.071	-0.00026
2.2	0.35	0.006	7.3	3.1	0.023	14.2	-0.07	0.000031
2.3	-0.49	-0.0086	7.5	-4.	-0.028	14.6	-0.035	0.00021
2.6	0.62	0.021	7.7	2.6	0.017	15.1	-0.051	-0.00015
2.7	-0.91	-0.024	8.1	1.4	0.0091	16.2	-0.039	0.00011
2.9	0.37	0.0064	8.4	-1.	-0.0057	17.3	-0.043	-0.000091
3.1	0.3	0.0013	8.8	-0.93	-0.0064	17.7	0.11	-0.000029

 Javier Menendez and his group computed the transition matrix elements for us

- Is there a way to avoid the GIM mechanism?
- There are additional contributions from 'ultra-soft' neutrinos



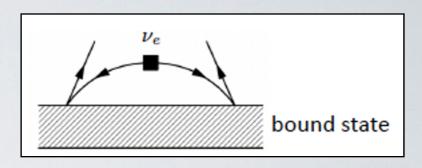
$$\sum_{n} \langle f | J_{\mu} | n \rangle \langle f | J^{\mu} | i \rangle \times \int \frac{d^{3}k}{(2\pi)^{3}} \frac{1}{E_{\nu}[E_{\nu} + (E_{n} - E_{0}) - i\epsilon]} \qquad E_{\nu} = \sqrt{k^{2} + m_{i}^{2}}$$

- The neutrinos see the nucleus as a whole and becomes sensitive to nuclear structure effects
- Depends on nuclear excited states. Normally these are tiny effects (5%)
- This becomes dominant in the GIM mechanism!  $\sim U_{ei}^2 m_i^3$
- For  $m_i \sim \text{MeV}$ : new contributions  $\sim U_{ei}^2 m_i^2$

Dekens, JdV et al '23 '24

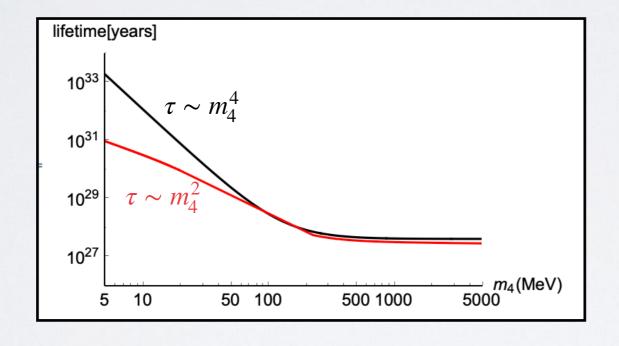
• For  $m_i << MeV$ : new contributions  $\sim U_{ei}^2 m_i^3 \log \frac{(E_n - E_0)^2}{m_i^2}$ 

- Is there a way to avoid the GIM mechanism?
- There are additional contributions from 'ultra-soft' neutrinos



$$\sum_{n} \langle f | J_{\mu} | n \rangle \langle f | J^{\mu} | i \rangle \times \int \frac{d^{3}k}{(2\pi)^{3}} \frac{1}{E_{\nu}[E_{\nu} + (E_{n} - E_{0}) - i\epsilon]} \qquad E_{\nu} = \sqrt{k^{2} + m_{i}^{2}}$$

$$E_{\nu} = \sqrt{k^2 + m_i^2}$$



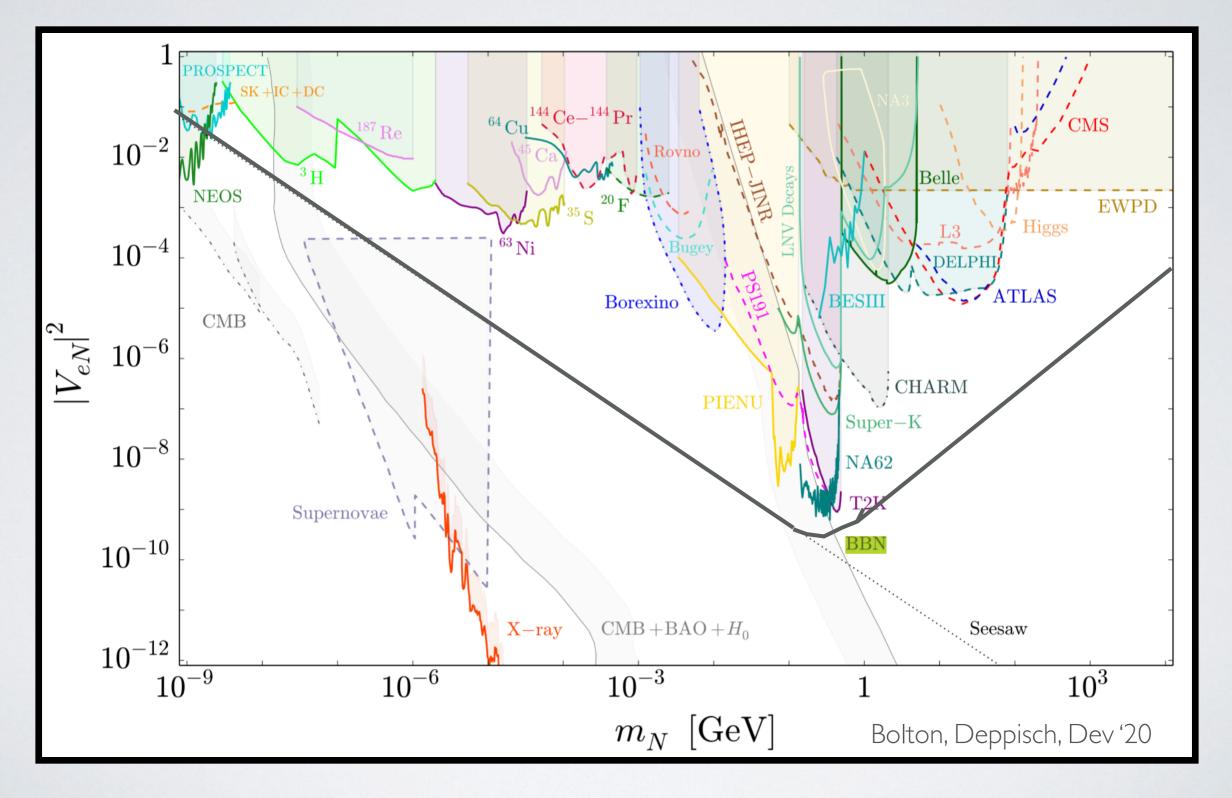
#### 100x larger decay rates

Dekens, JdV et al '23 '24

- Lifetimes are still suppressed for small sterile neutrino masses but not as much
- Not today: short-distance piece becomes mass dependent too  $\mathbf{g}_{\nu}^{\mathbf{NN}}(m_i)$

## Compared to 0vbb

• Naively saturate the Ovbb lifetime with just the m4 contribution



Bounds can be weakened by considering pseudo-Dirac sterile neutrino pairs

# This is perhaps not fair

Consider minimal 3+2 extension (lightest active neutrino is massless)

$$m_4 = \bar{M} - \Delta M/2 \,, \qquad m_5 = \bar{M} + \Delta M/2 \,, \qquad \mu = \frac{\Delta M}{\bar{M}}$$

- For small mass splittings, the heavy neutrino pair can form a pseudo-Dirac neutrino

• Ovbb amplitude proportional to 
$$\bar{m}_{\beta\beta} = m_{\beta\beta} \left[ 1 - \frac{M(\bar{M})}{M(0)} \right] + f(\bar{M}) \, \mu \, U_e^2 + \mathcal{O}(\mu^2)$$

## This is perhaps not fair

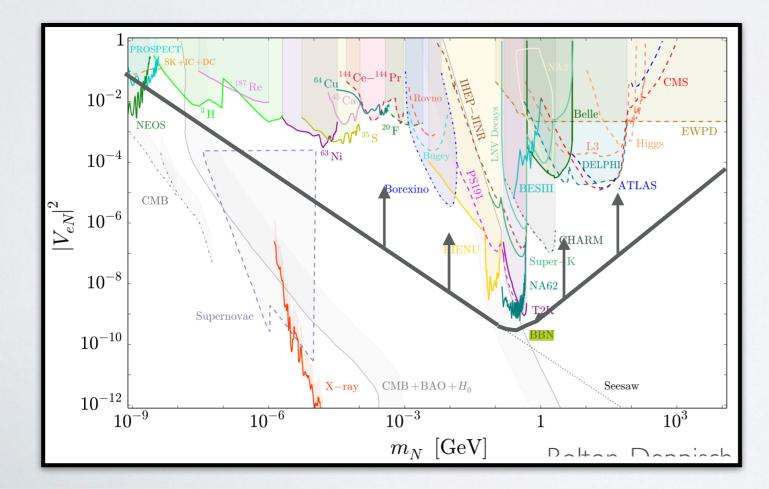
Consider minimal 3+2 extension (lightest active neutrino is massless)

$$m_4 = \bar{M} - \Delta M/2 \,, \qquad m_5 = \bar{M} + \Delta M/2 \,, \qquad \mu = \frac{\Delta M}{\bar{M}}$$

- For small mass splittings, the heavy neutrino pair can form a pseudo-Dirac neutrino

• Ovbb amplitude proportional to 
$$\bar{m}_{\beta\beta} = m_{\beta\beta} \left[ 1 - \frac{M(\bar{M})}{M(0)} \right] + f(\bar{M}) \mu U_e^2 + \mathcal{O}(\mu^2)$$

• Bounds can be moved up for small and/or degenerate masses.



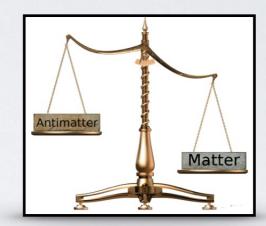
- **Ovbb becomes weak** for (pseudo-)Dirac sterile neutrinos
- **Need** an independent handle on the mass splitting

- Low-scale leptogenesis requires a small mass splitting as well!
- We can do leptogenesis at the same time in the minimal 3+2 extension



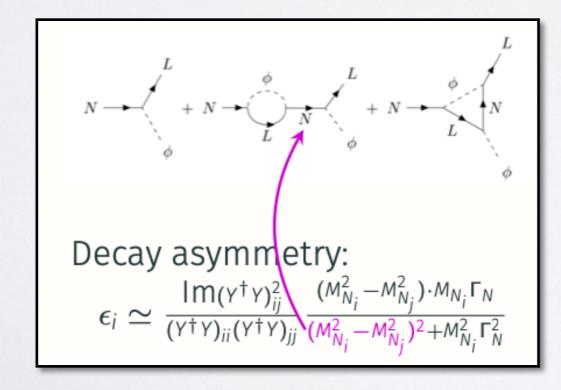
13.7 billion year







Production of asymmetries enhanced by small mass splittings



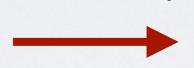
Akhmedov/Rubakov/Smirnov '98 Pilaftsis/Underwood '03 Asaka/Shaposhnikov '05

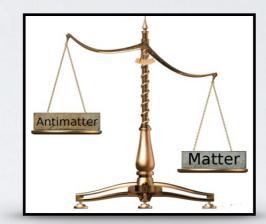


- Low-scale leptogenesis requires a small mass splitting as well!
- We can do leptogenesis at the same time in the minimal 3+2 extension



13.7 billion year





- Production of asymmetries enhanced by small mass splittings
- Scan over parameters in the 3+2 extension (masses, angles, phases  $\sim O(10)$ )



Neutrino masses



Matter/Antimatter asymmetry



Consistent with all current experiments



Sterile neutrino masses below 10 GeV

Arxiv:2407.10560







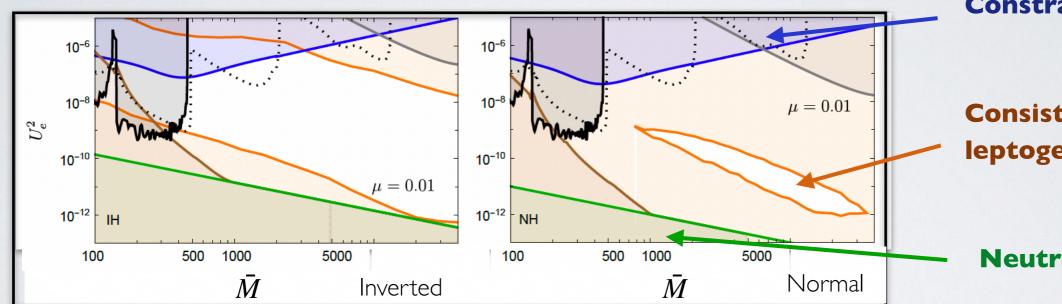
Juraj Klaric, Vaisakh Plakkot, Yannis Georis

Leptogenesis contours calculated by Drewes/Georis/Klaric

Simplest solution to neutrino masses + matter/antimatter asymmetry

Arxiv:2407.10560

Scans give contours like this (fixed mass splitting at 1%)



**Constraints from 0vbb** 

Consistent with leptogenesis

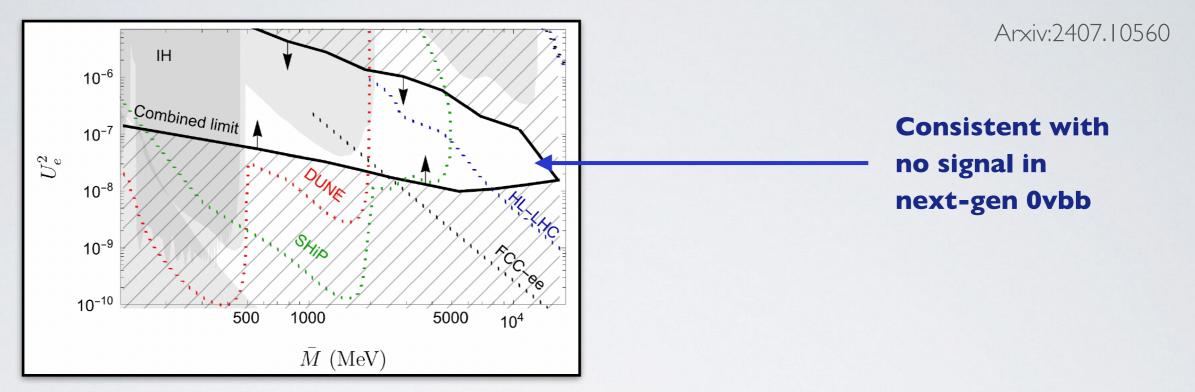
**Neutrino** masses

• For inverted hierarchy, 0vbb is ruling out part of the space

$$\bar{m}_{\beta\beta} = m_{\beta\beta} \left[ 1 - \frac{M(\bar{M})}{M(0)} \right] + f(\bar{M}) \mu U_e^2$$

In inverted hierarchy, next-gen should see something unless we have a cancellation!

• The IH scenario can be falsified if we don't see 0vbb in next-gen

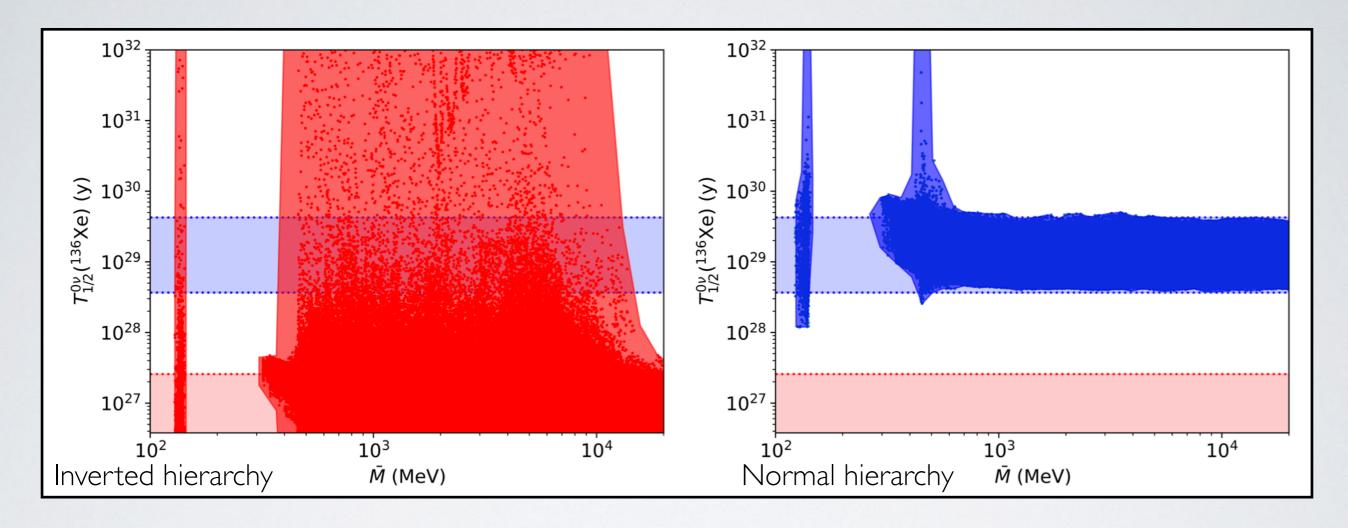


Inverted hierarchy

- If we do see a signal —> Nobel prize, neutrinos are Majorana, but.... not clear if light sterile neutrinos were involved. Need more tests
- Normal hierarchy: similar to IH but requires 10x better 0vbb experiments then IH.
- Analysis much harder for 3+3 (see e.g. Chrzaszcz, Weniger et al' 19) 18 parameters ....

## Is the signal 'outside' the band

• If we do see a 0vbb signal, Question: is it different from the 'standard mechanism'



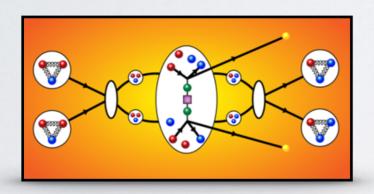
- Unfortunately: within 3+2 leptogenesis it is hard to enhance 0vbb rates in normal hierarchy
- Key lessons: we should all hope we live in the Inverted Hierarchy

## Summary and outlook

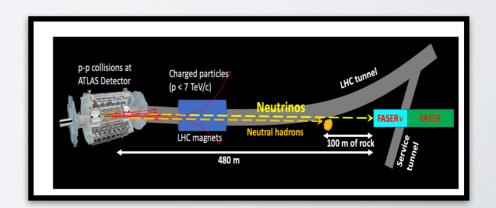
- Neutrino masses requires an explanation!!
- Good motivation for sterile neutrinos (also leptogenesis) but mass range unclear

eV keV MeV GeV TeV ..... 10<sup>15</sup> GeV

- Excellent experimental prospects for large chunk of mass range
- Neutrinoless double beta decay important for entire mass range



- Exciting experimental program
- Theory improvements needed but good progress last 5 years
- Crucial to test leptogenesis at all scales
- Great activity to find long-lived particles
- New experiments Ship/Dune/Faser very promising
- Low-scale leptogenesis can be tested by the combined experimental program!



# Backup