

Simulation Based Inference for X-ray astrophysics

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Lumières Workshop (2026)



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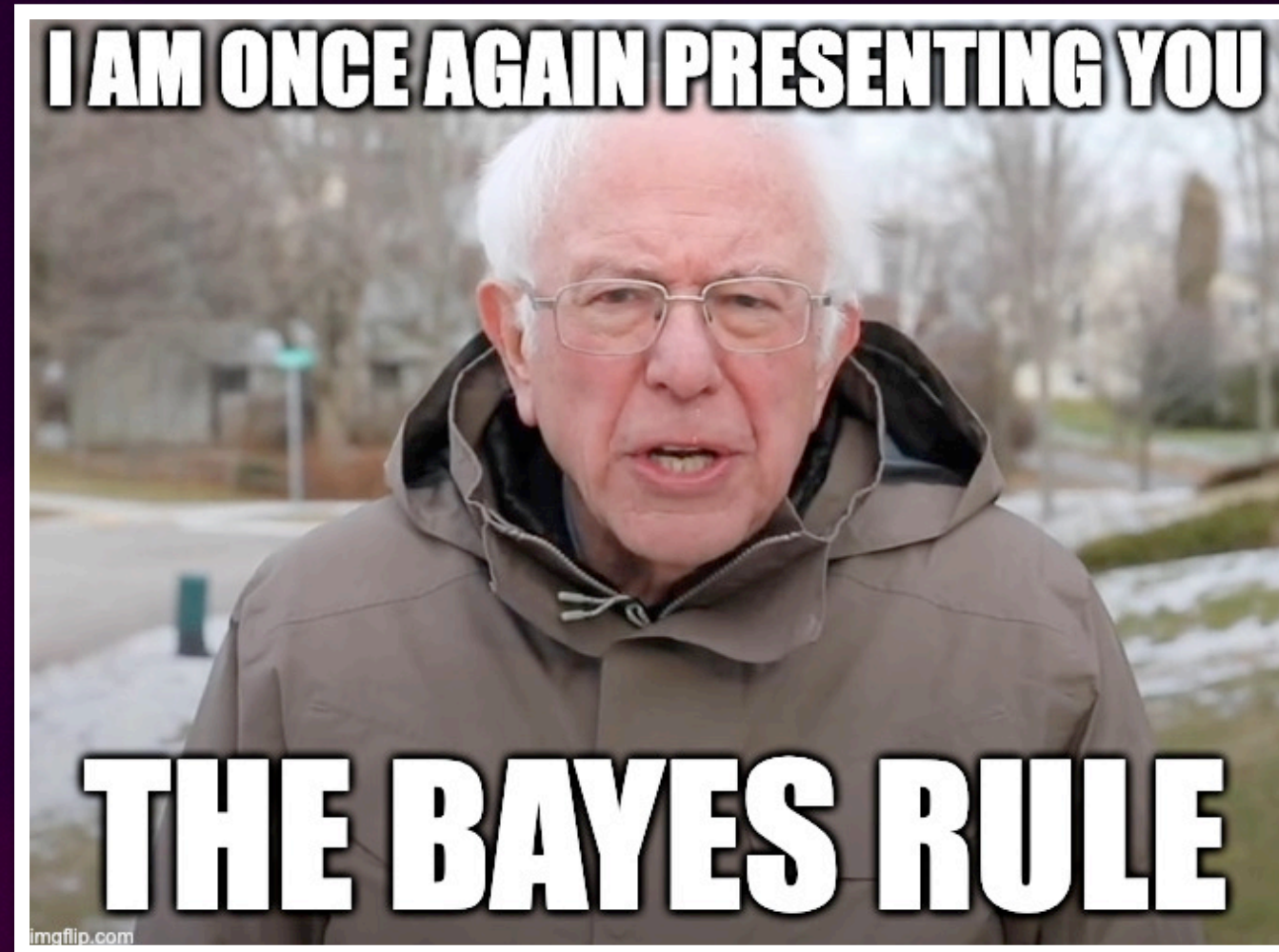
1. A short recap on Bayesian inference
 2. Introduction to Simulation-Based Inference (SBI) and its building blocks
- } X-ray spectroscopy
as an example
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3. Turbulence and surface brightness fluctuations in galaxy clusters
- } Application to X-COP
and CHEXMATE
cluster samples

Bayesian inference

θ : parameters

X : observation(s)

Bayesian inference

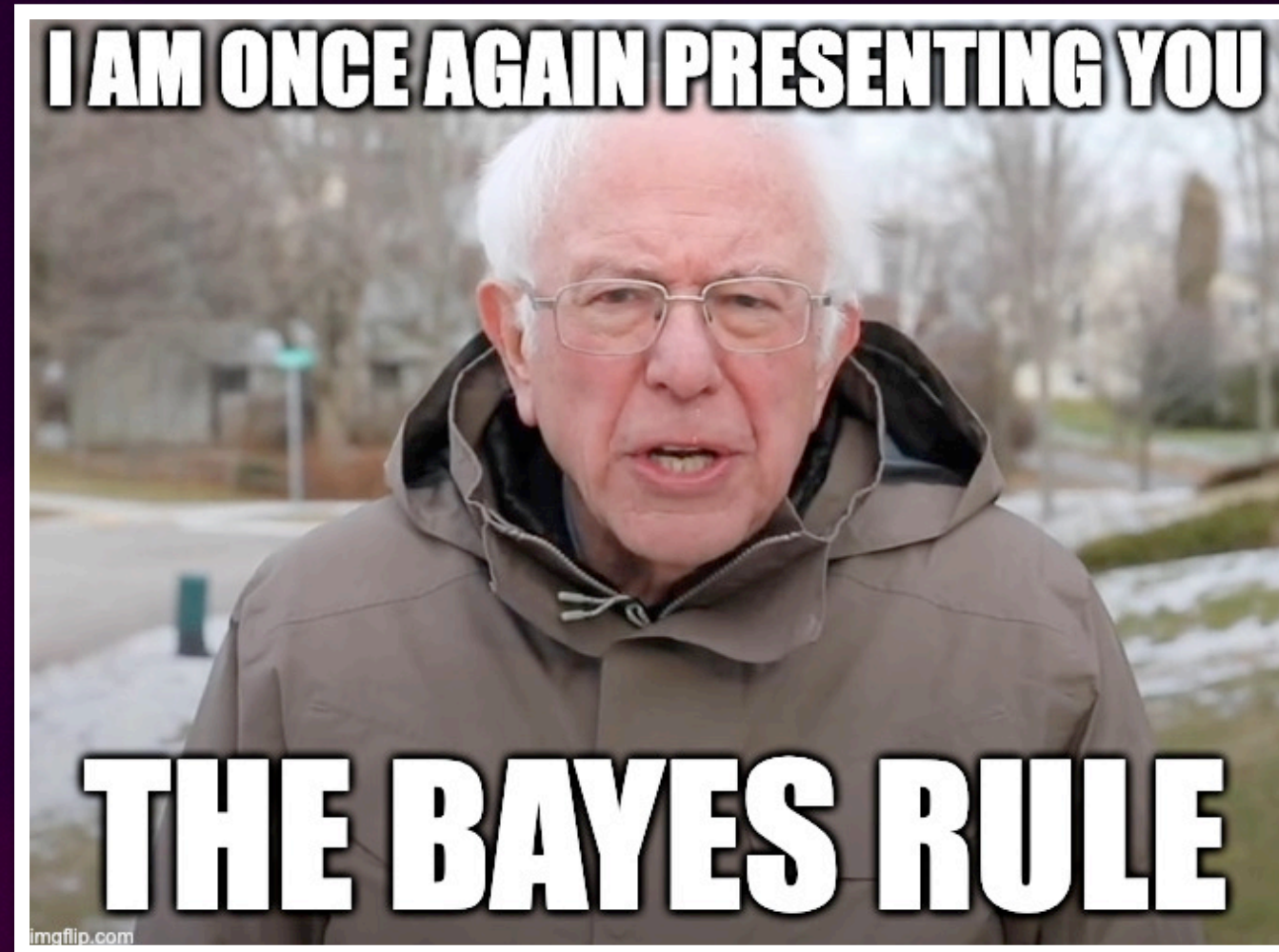


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$$P(\theta | X) = \frac{P(X | \theta)}{P(X)} P(\theta)$$

Bayesian inference



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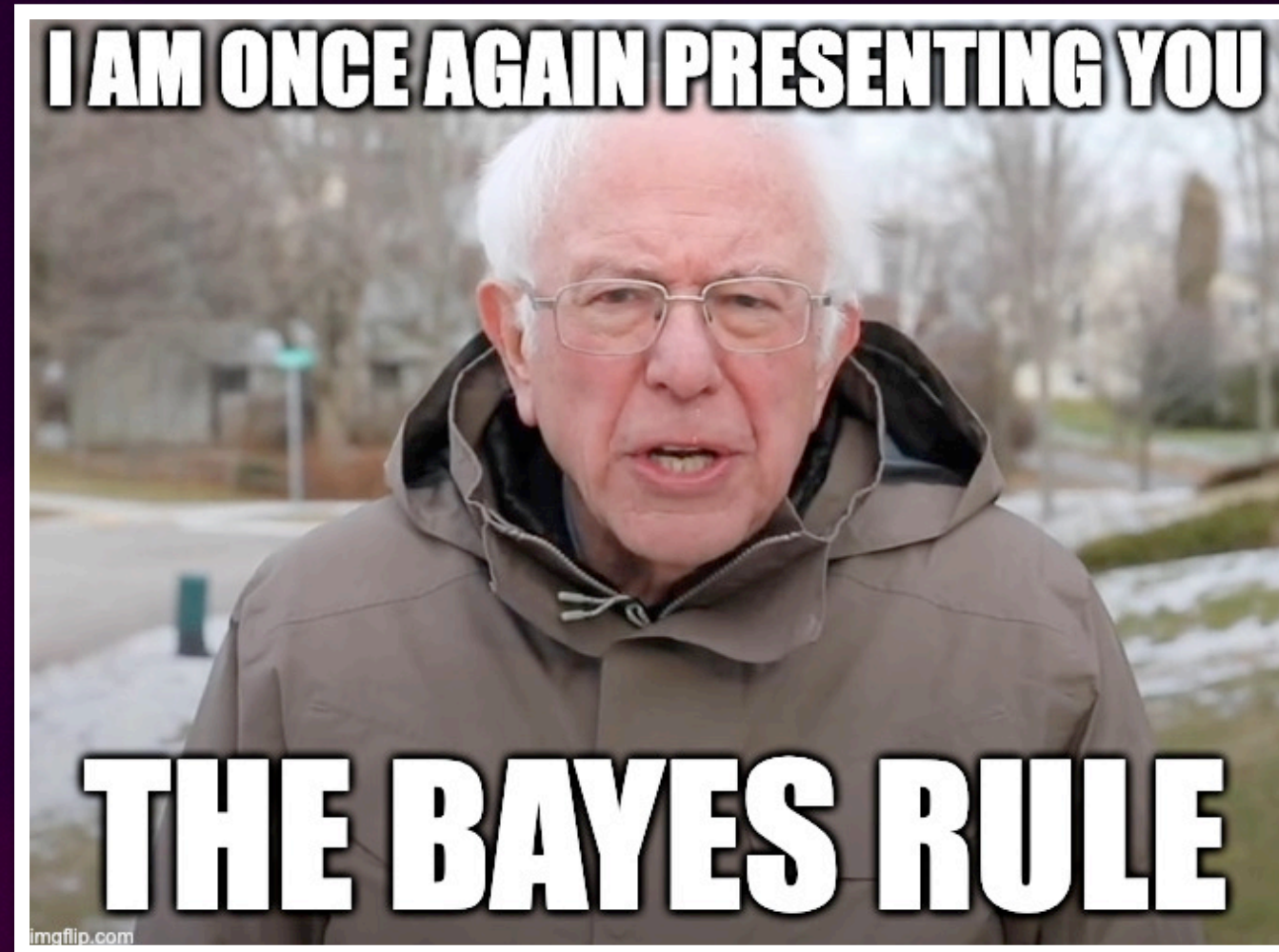
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Prior

A priori probability
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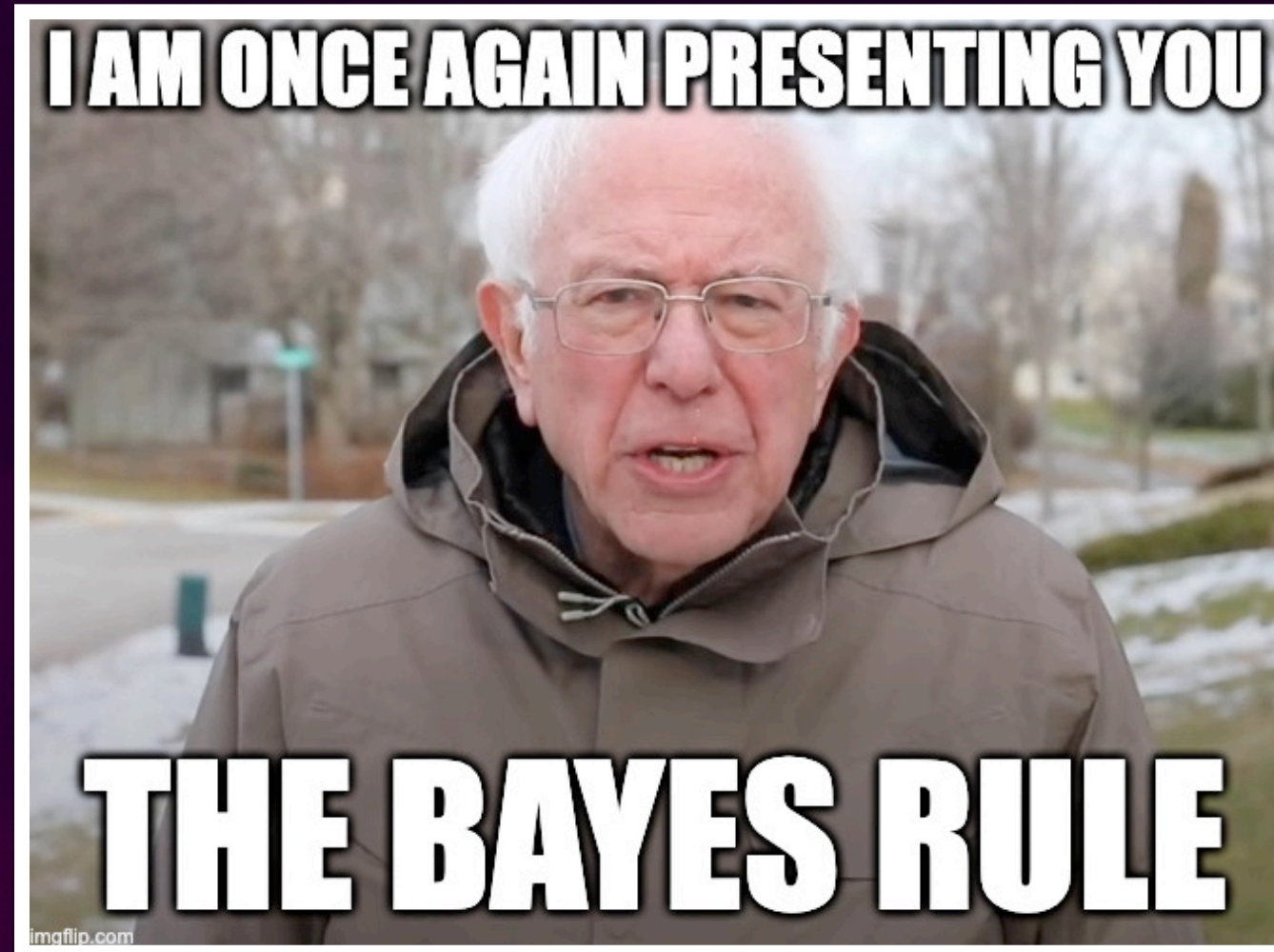
Likelihood

Probability of the observation(s) given the parameters

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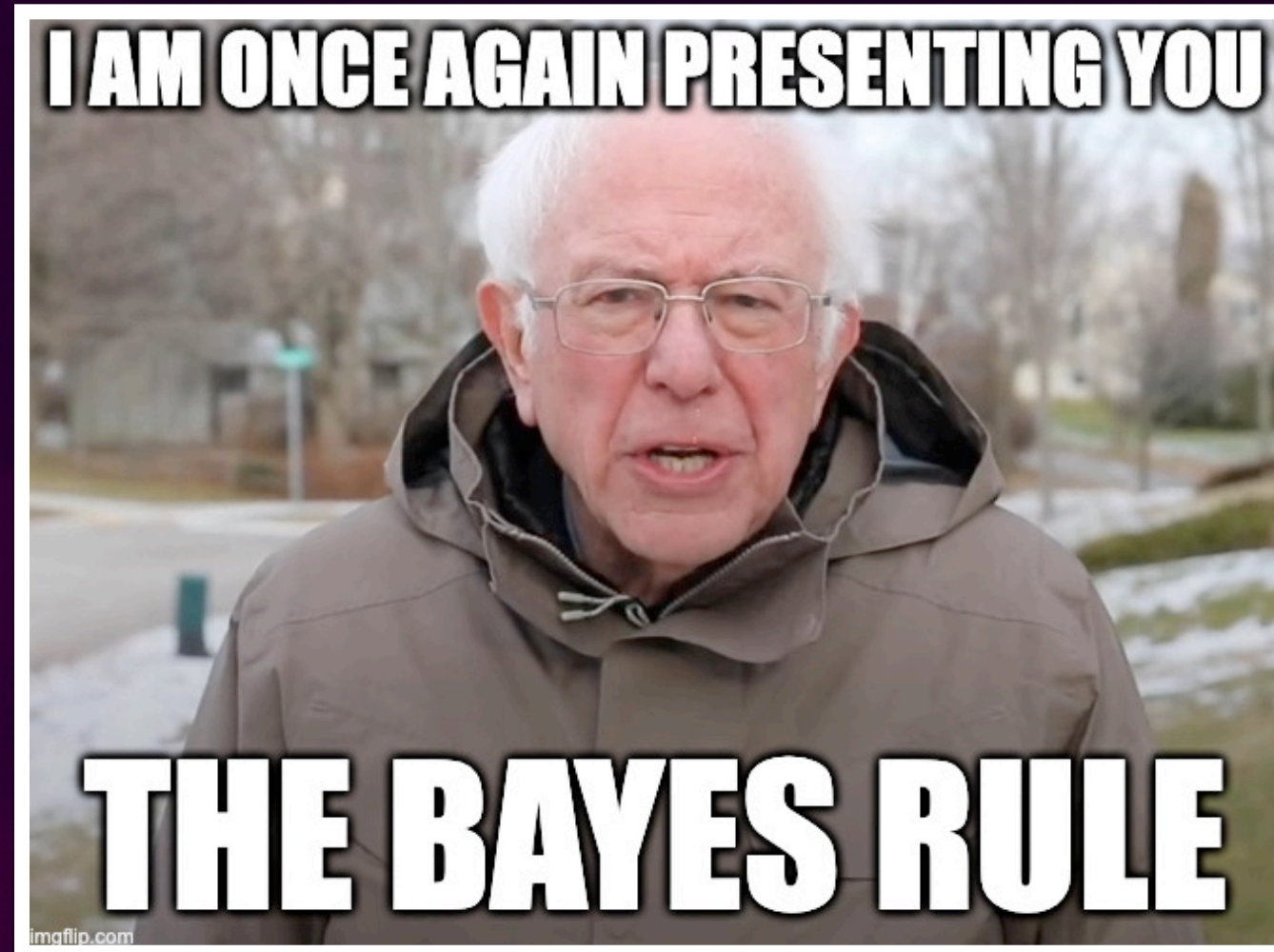
Posterior

A posteriori of the parameters given the observation(s)

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A *posteriori* of the parameters given the observation(s)

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Reason why Bayesian inference is hard to perform

Illustration with X-ray spectroscopy

$$\mathcal{S}(E, \theta) = \mathcal{R} * \mathcal{M}(E, \theta)$$

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Observed data

Spectra measured by the instrument

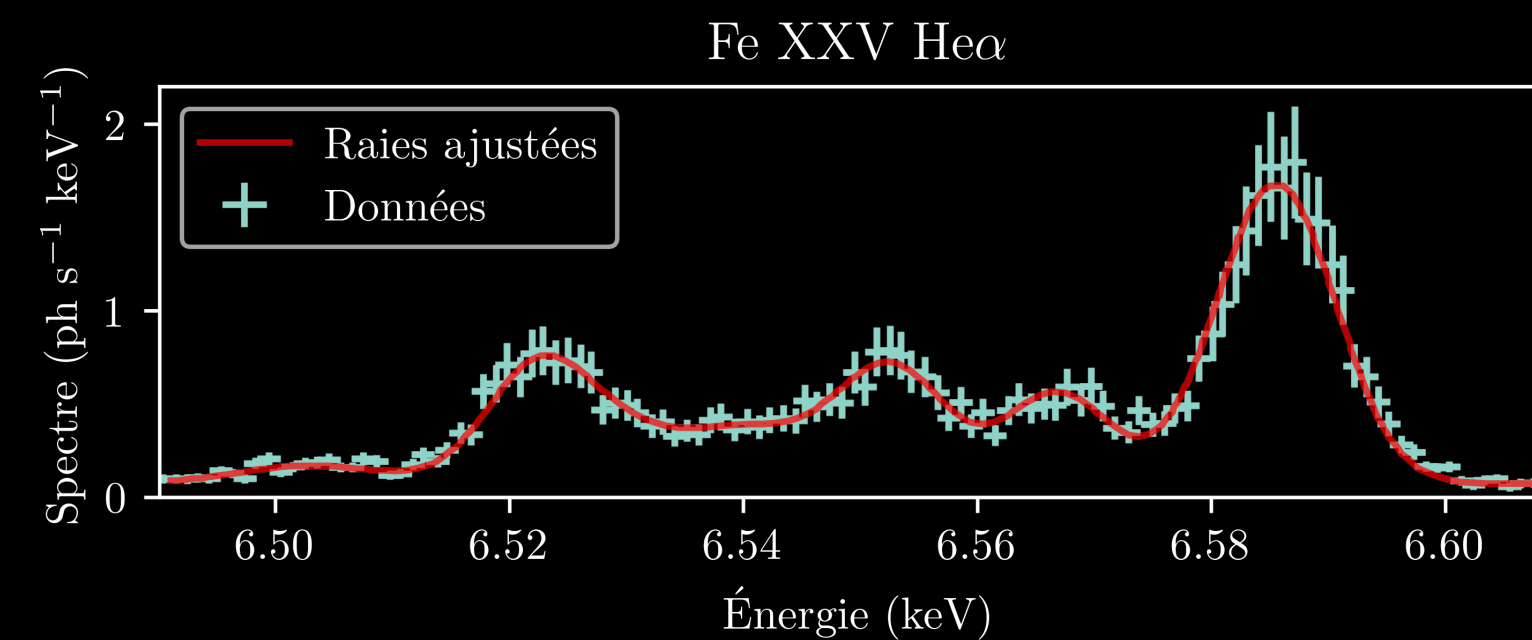
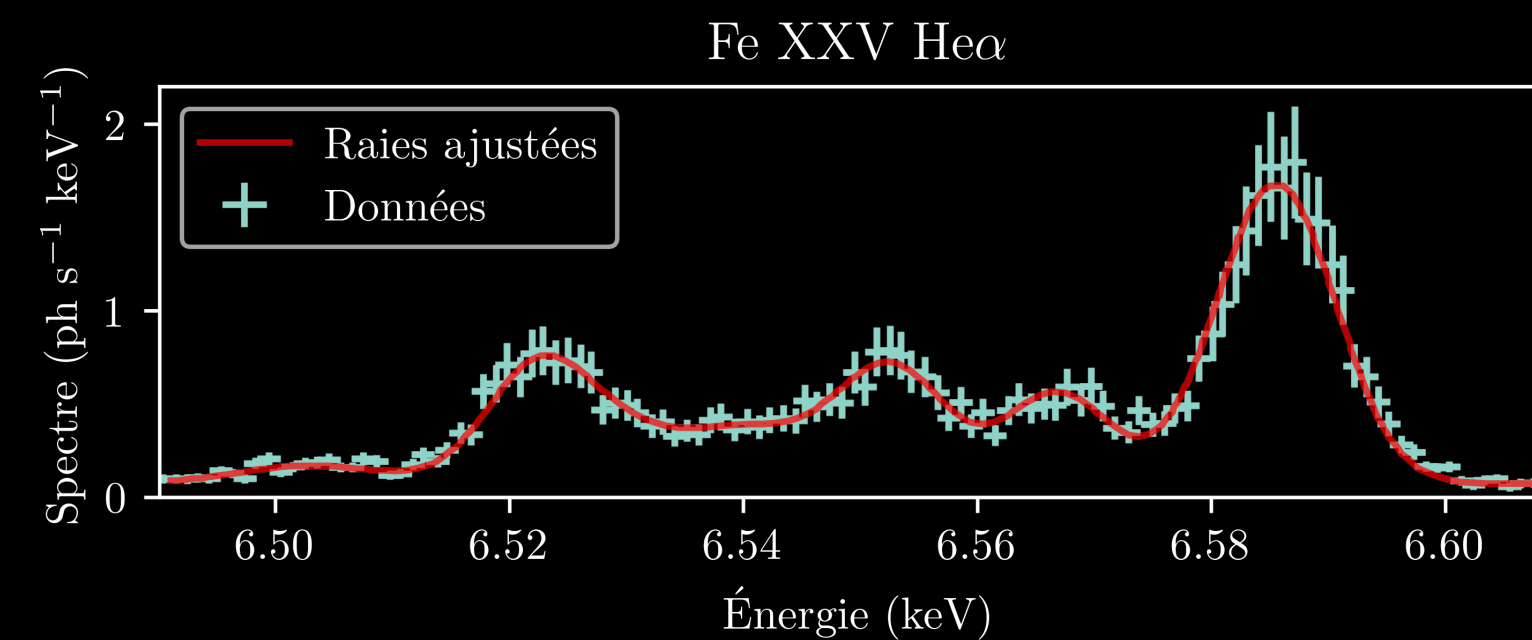


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Model

Spectral model and instrumental convolution

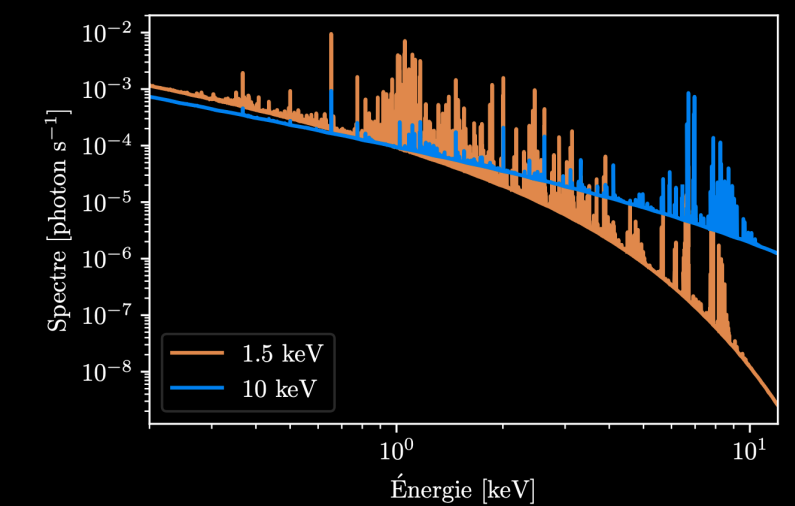


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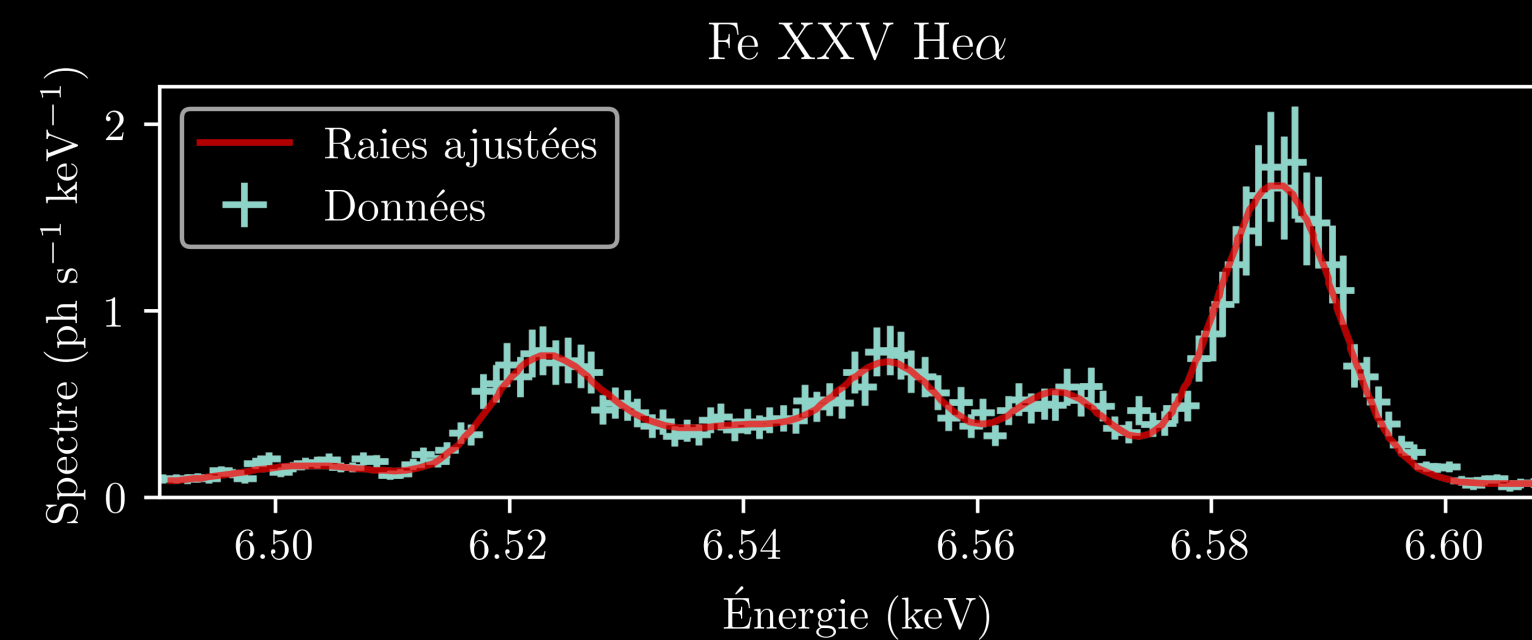
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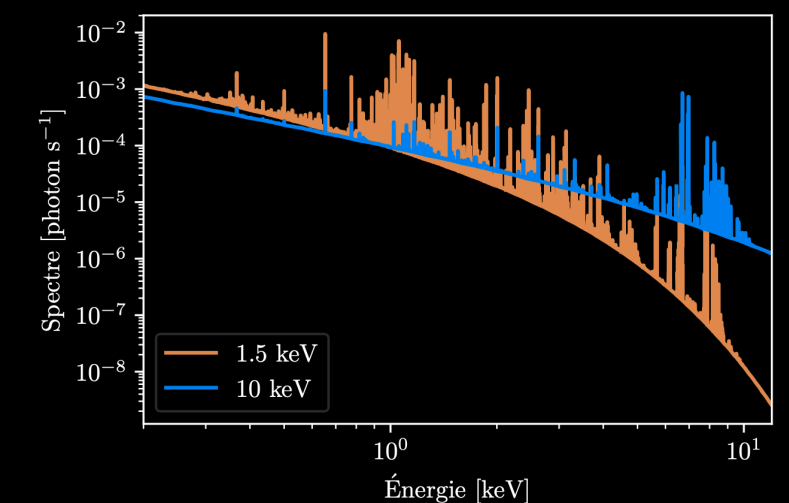
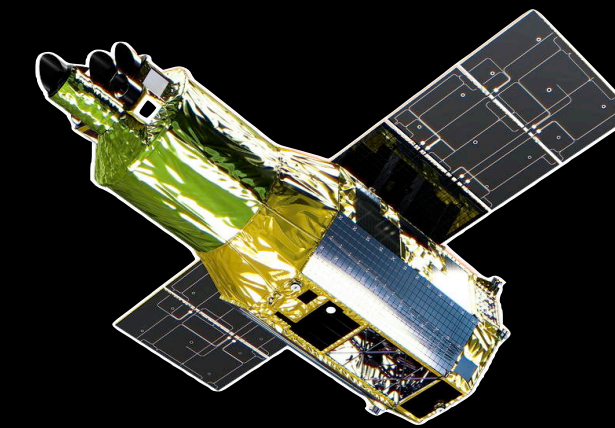


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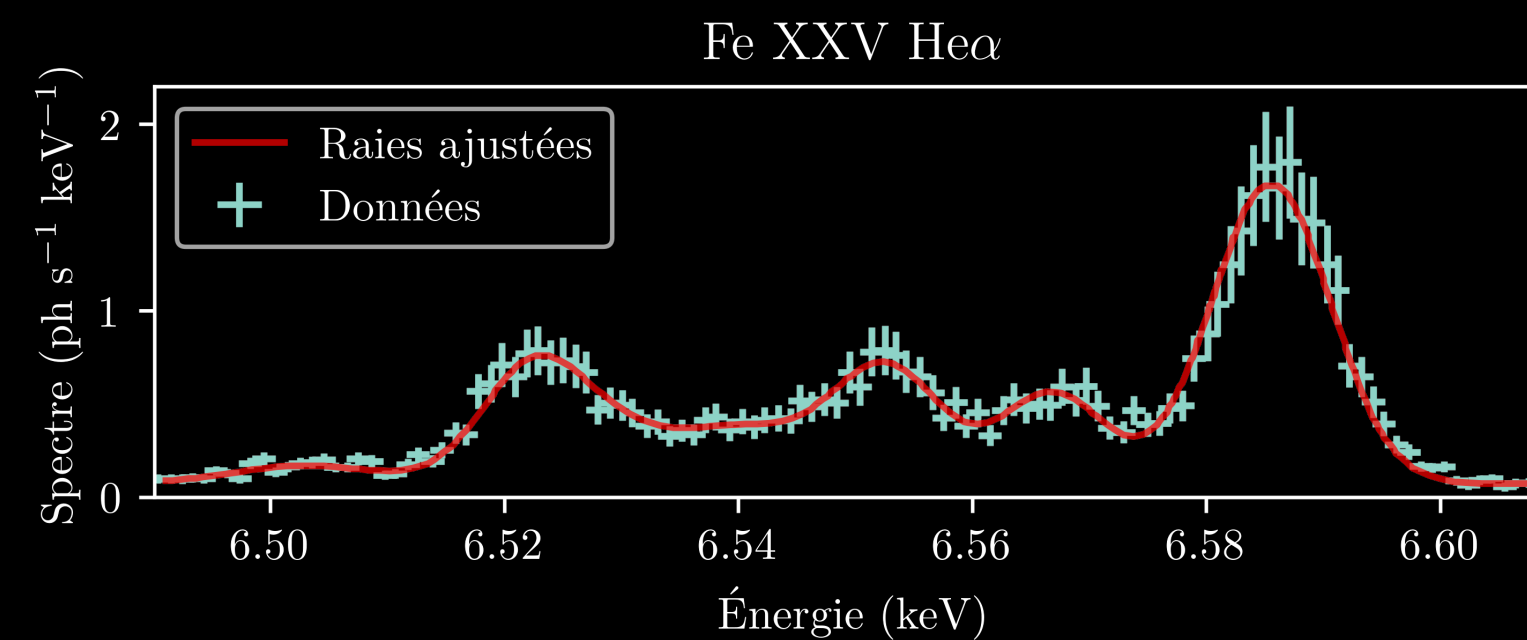
Parameters

Temperature,
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Expected photons
in each channel
 $\lambda \equiv S(E, \theta)$

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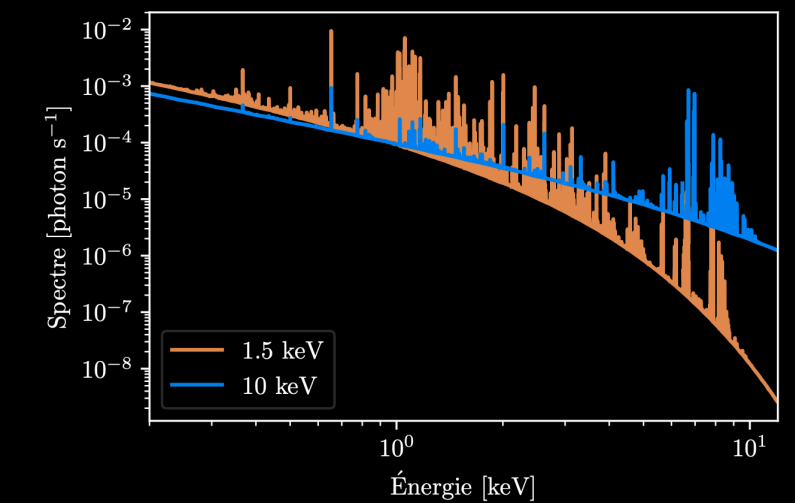
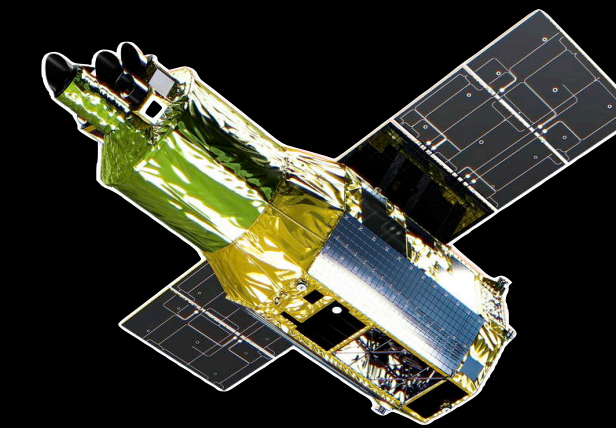


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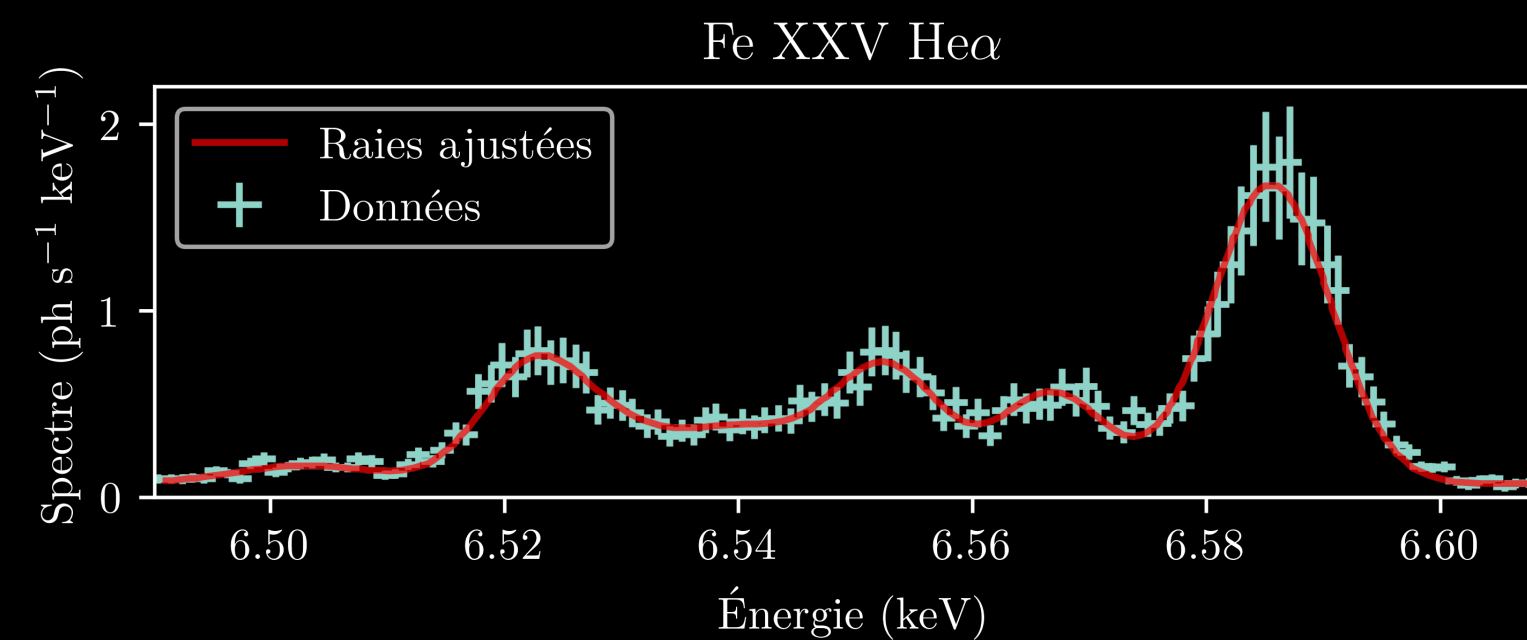
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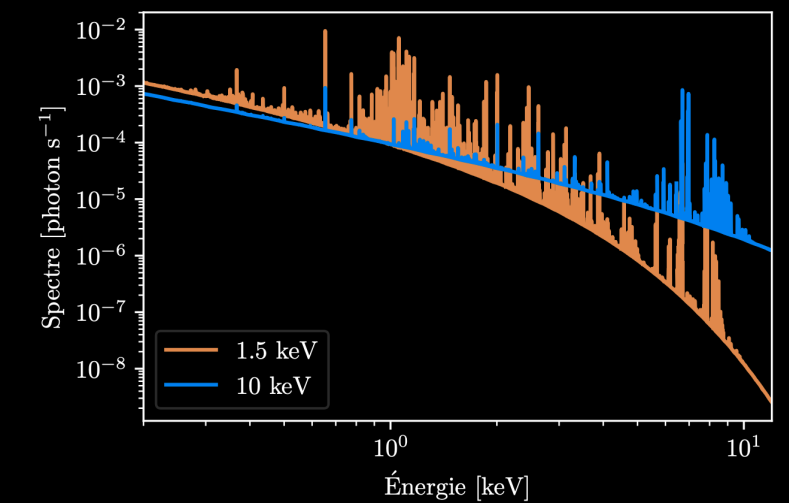
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Counting process : Poisson likelihood

$$P(X = k | \theta) = \frac{\lambda^k e^{-\lambda}}{k!}$$

Turn the likelihood into
a posterior distribution

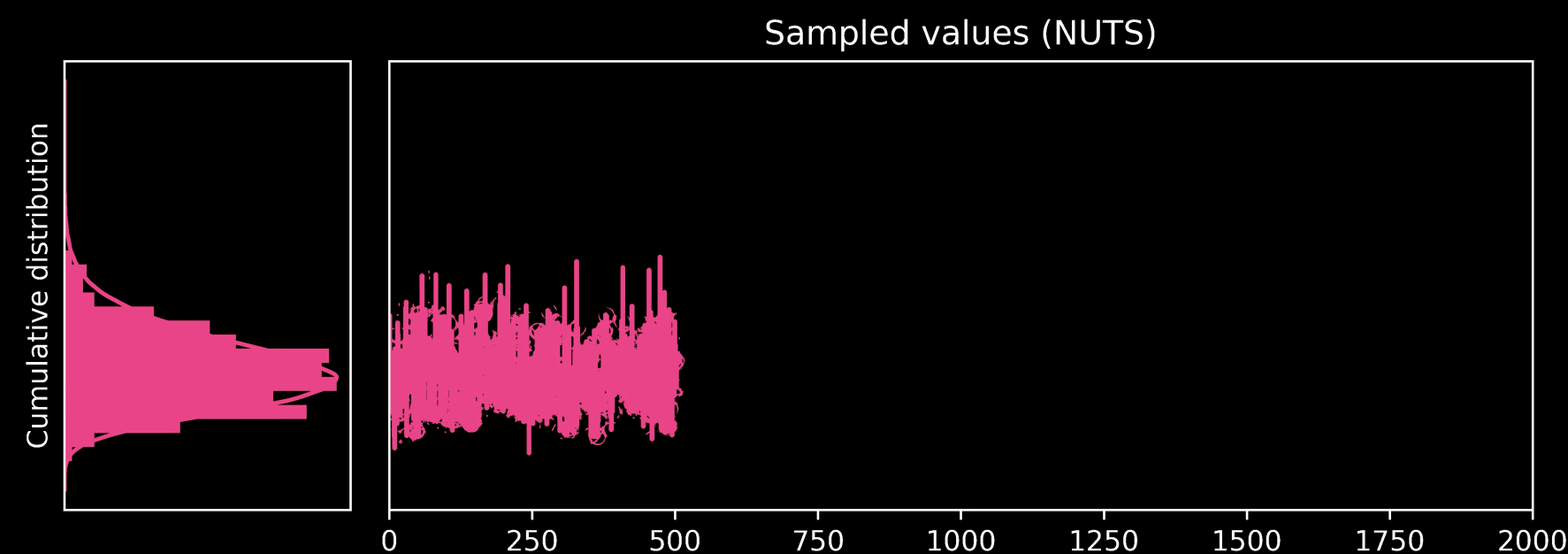
Traditional Bayesian inference

Evaluate
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Traditional Bayesian inference

Sampling $\{\theta\}_i \sim P(\theta|X)$

Monte Carlo Markov Chain (HMC,
NUTS, AIES), Nested Sampling



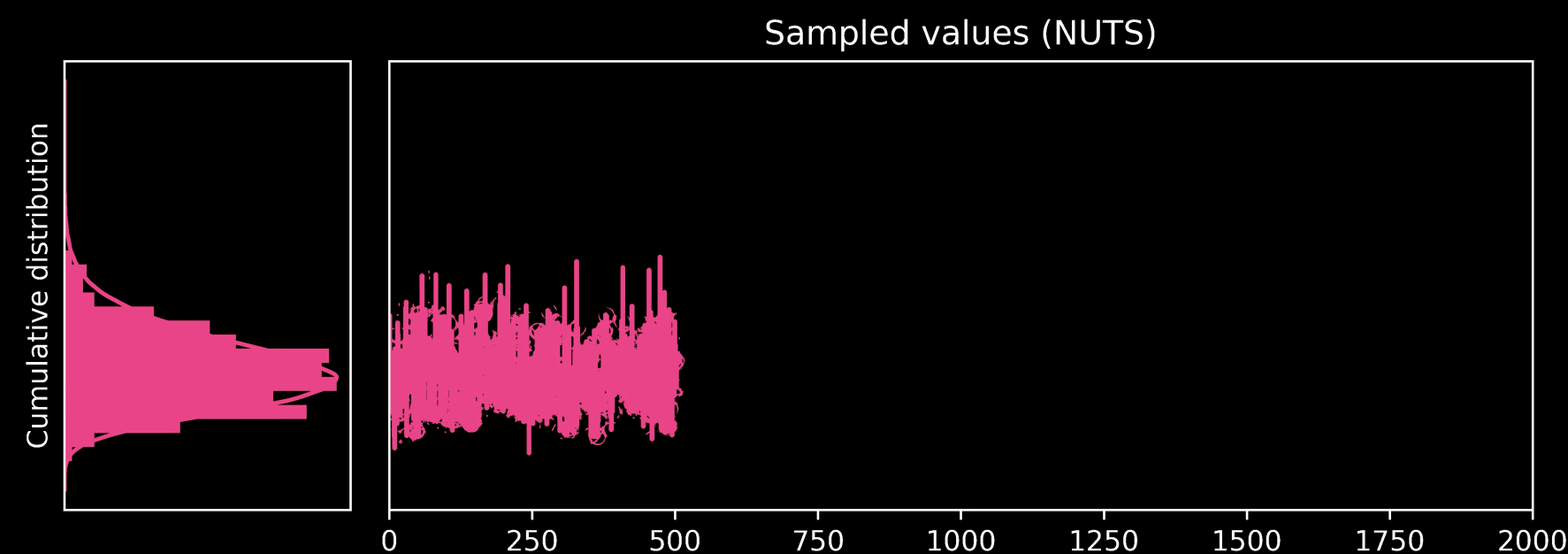
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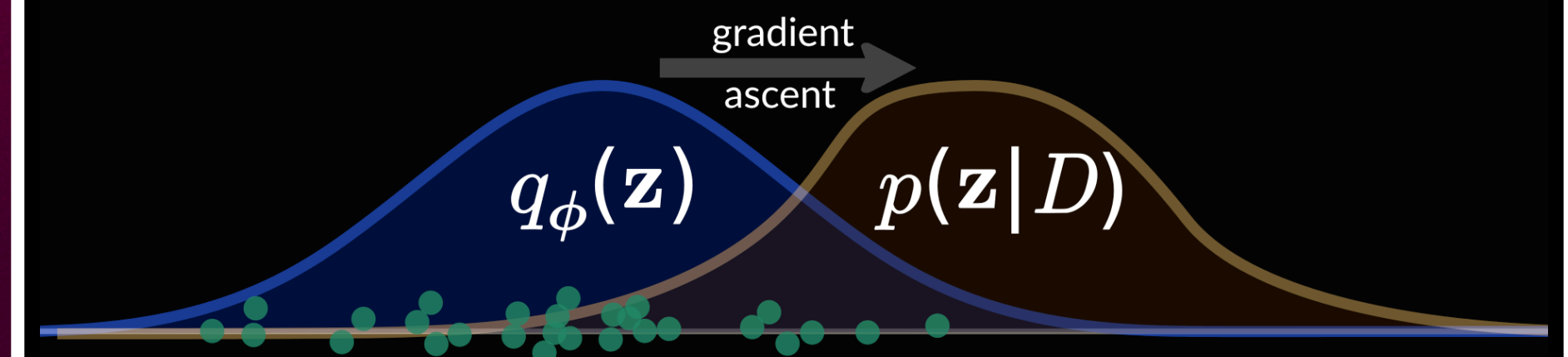
Monte Carlo Markov Chain (HMC, NUTS, AIES), Nested Sampling



Evaluate
 $P(X|\theta)$

Variational $q(\theta) \simeq P(\theta|X)$

Minimize Evidence Lower Bound for a parametric and analytical approximation of the posterior distribution



Simulation-based inference (SBI)

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- Use simulations of the observable to train a neural density estimator to either learn the posterior distribution $P(\theta | X)$, the likelihood $P(X | \theta)$ or Bayes ratios.

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- Works with intractable likelihood functions and transformed representations of the observable

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- Train a neural network to learn the distribution of parameters and observables

Normalizing flows

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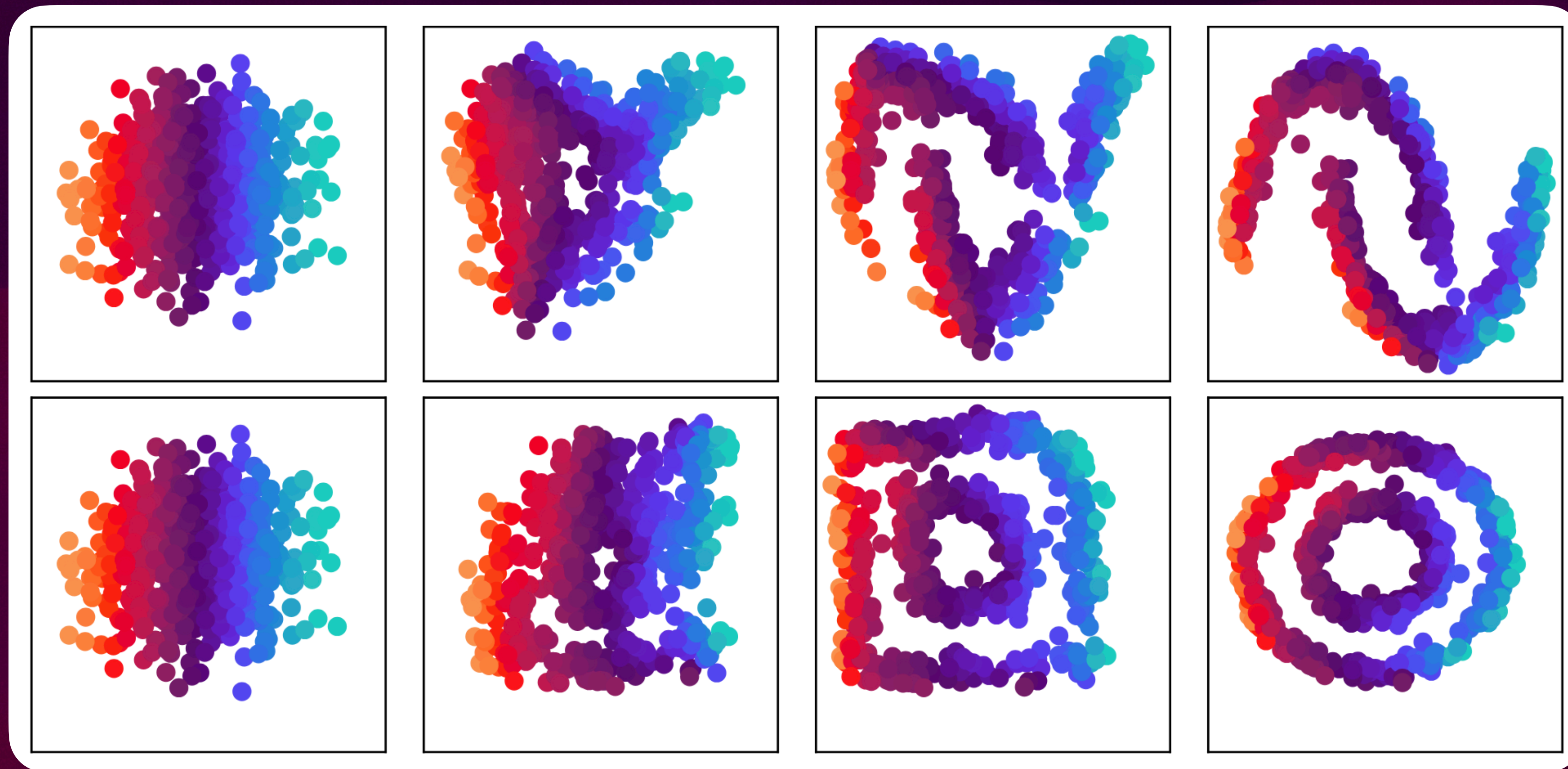
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- Learn any distribution as the **transformation** of a **Gaussian** latent variable
- Works by stacking reversible blocks of e.g. **Masked Auto-Encoders**

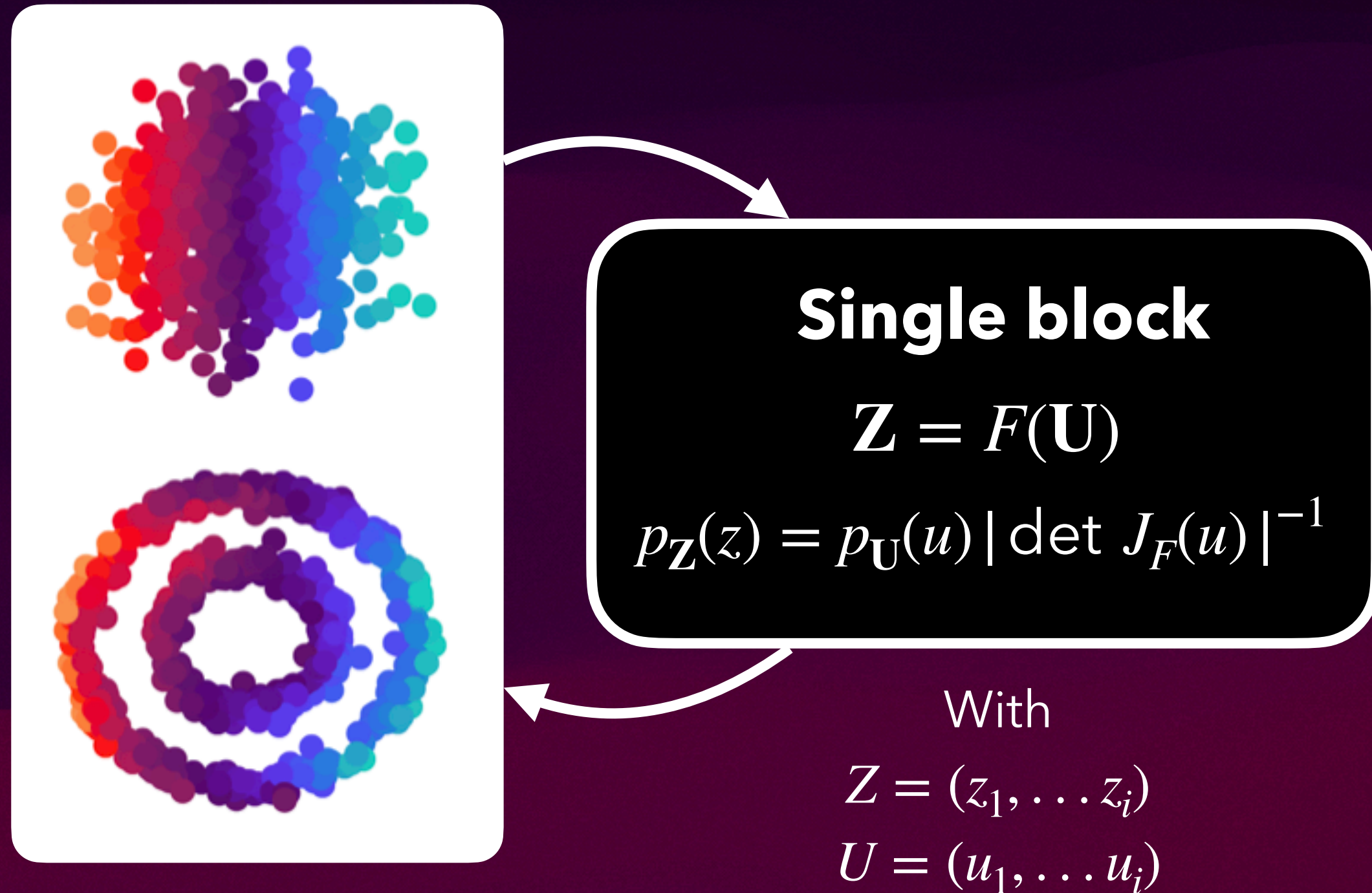
Latent
distribution



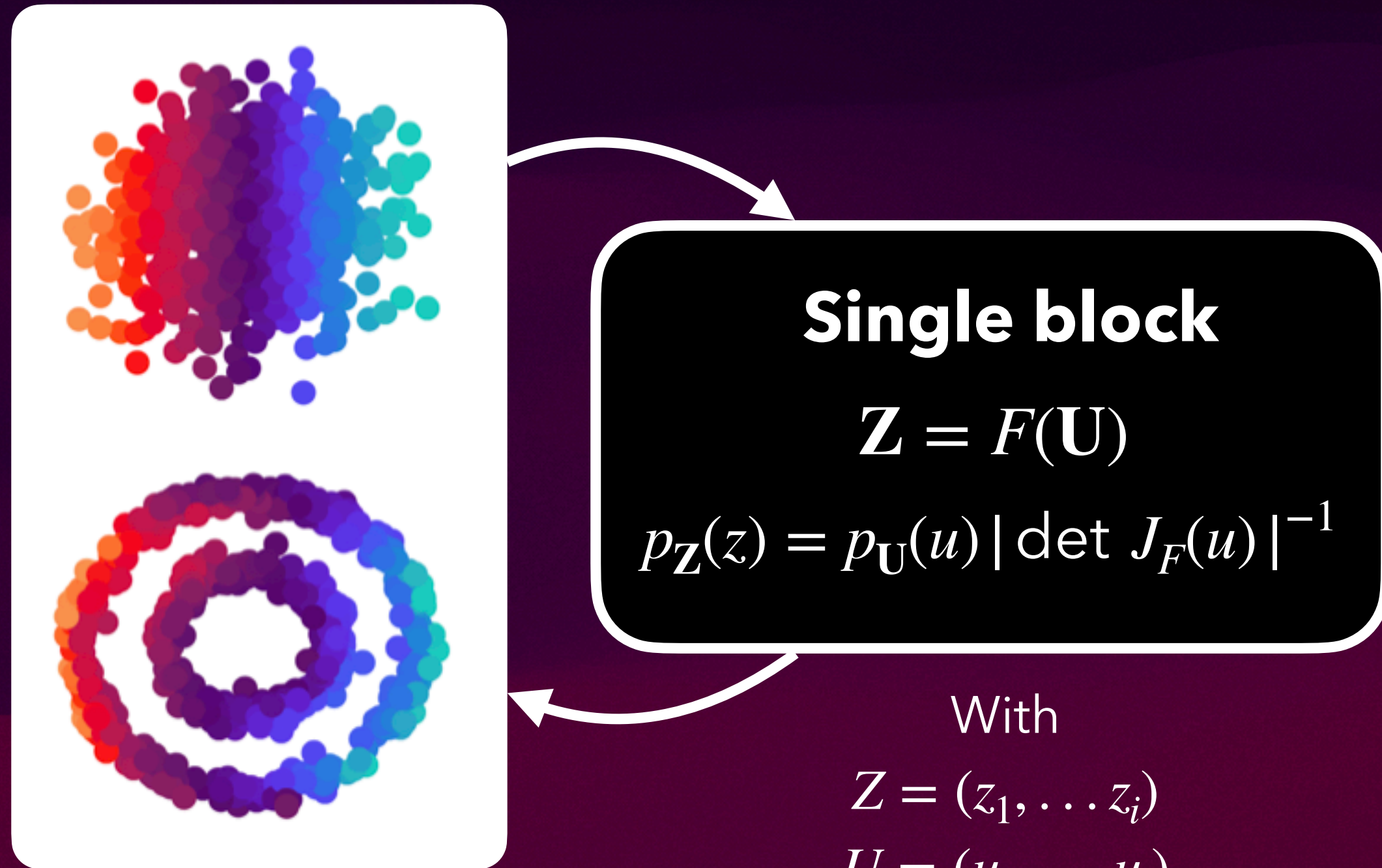
Learned
distribution

$$Z_1 \xrightarrow{F_1(Z)} Z_2 \xrightarrow{F_2(Z)} Z_3 \xrightarrow{F_3(Z)} Z_4$$

Building the transform blocks

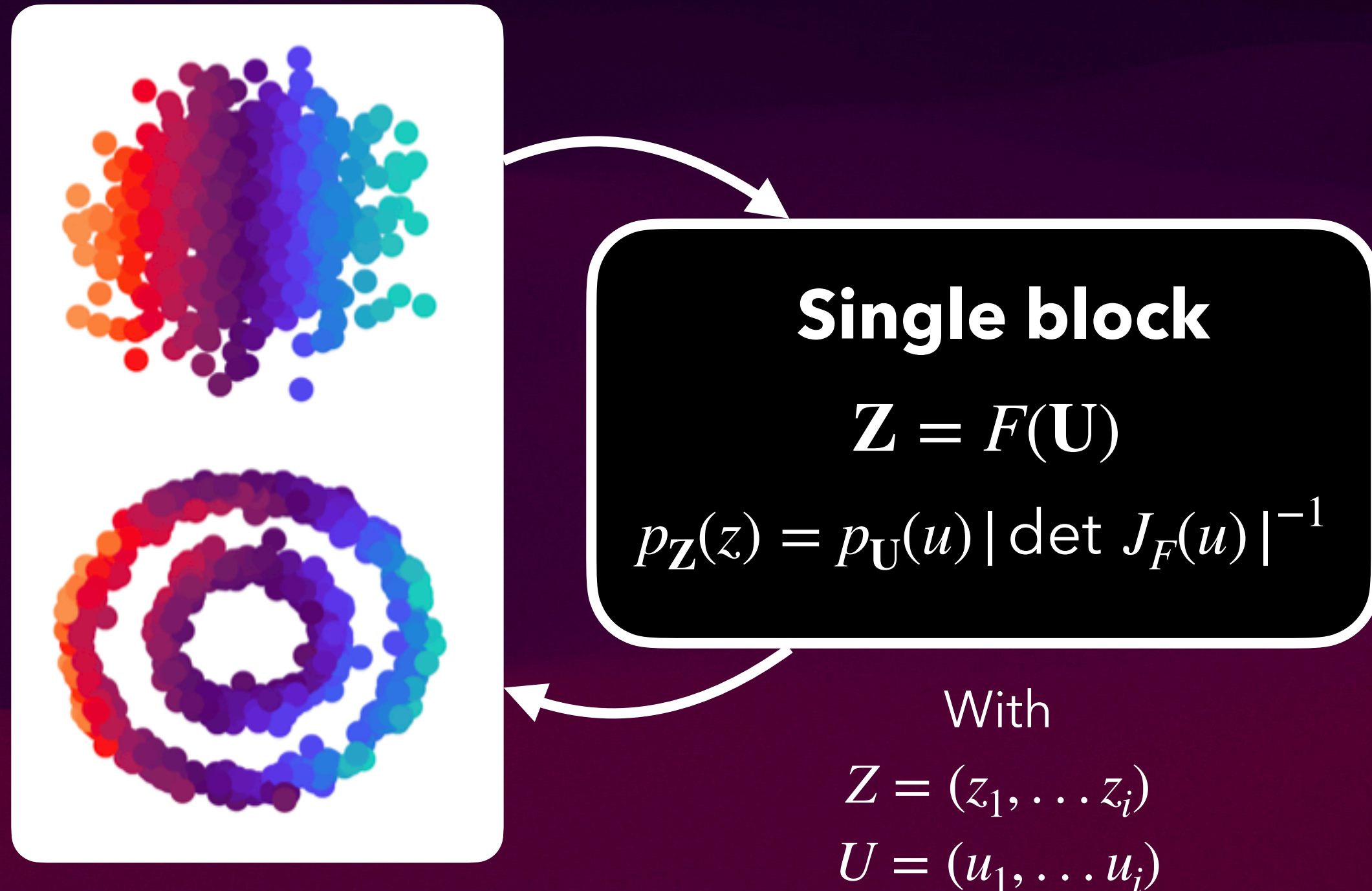


Building the transform blocks



The determinant of the
Jacobian is the bottleneck
→ Make it **triangular**

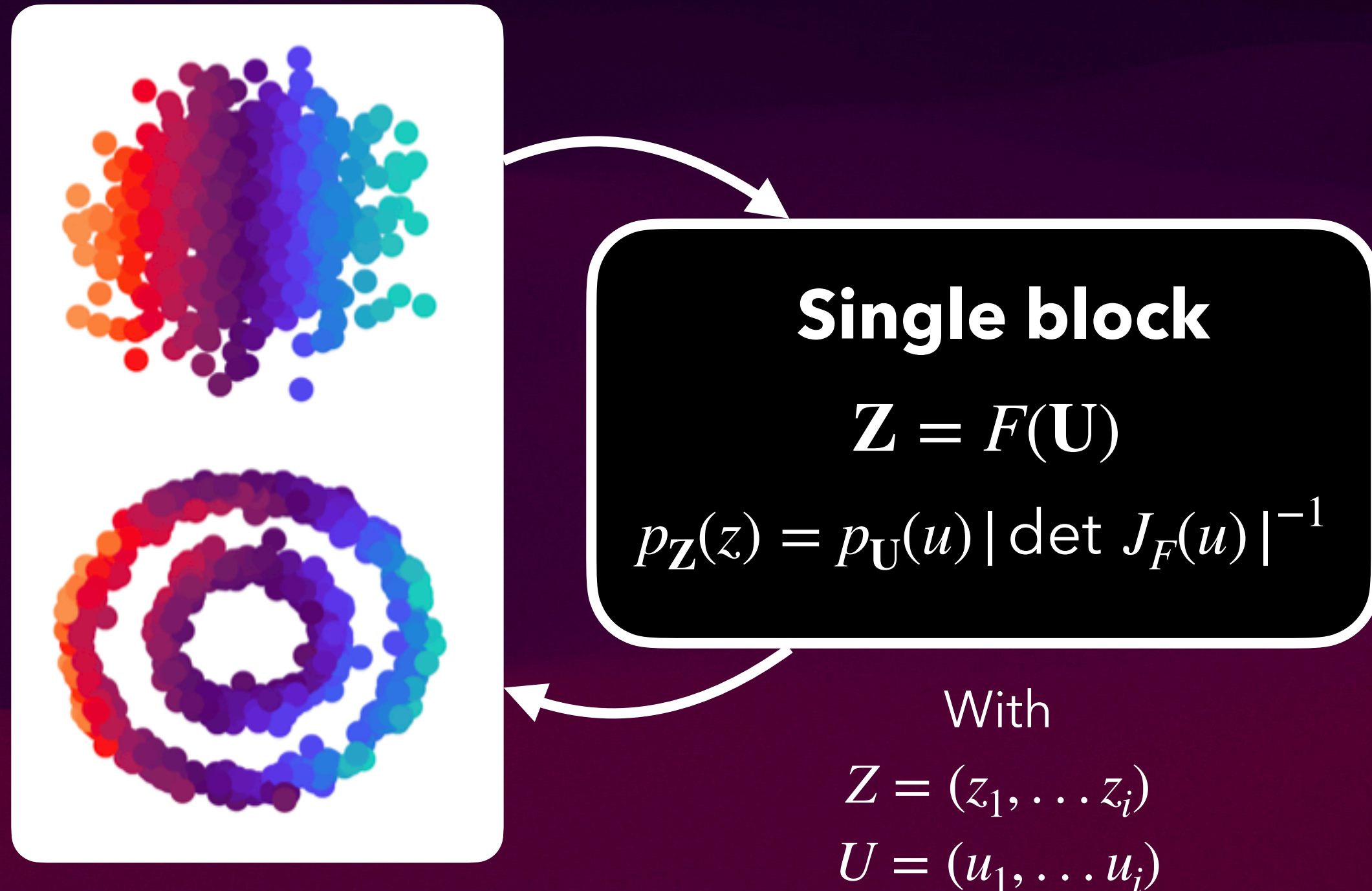
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 $z_i = f(u_i, u_{i-1}, \dots, u_0)$

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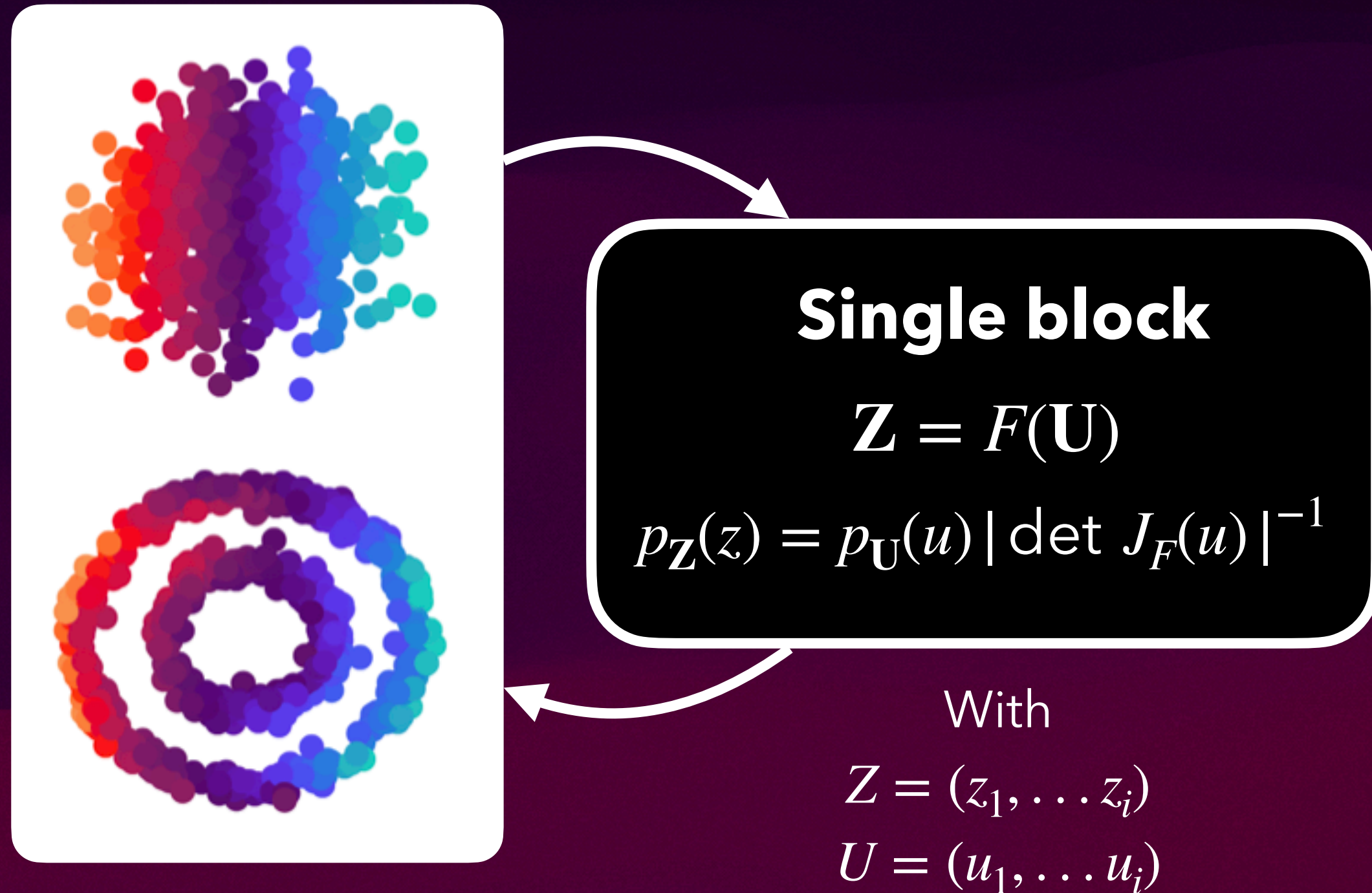


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In general : $z_i = \theta_1 \times u_i + \theta_2$
where
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Building the transform blocks



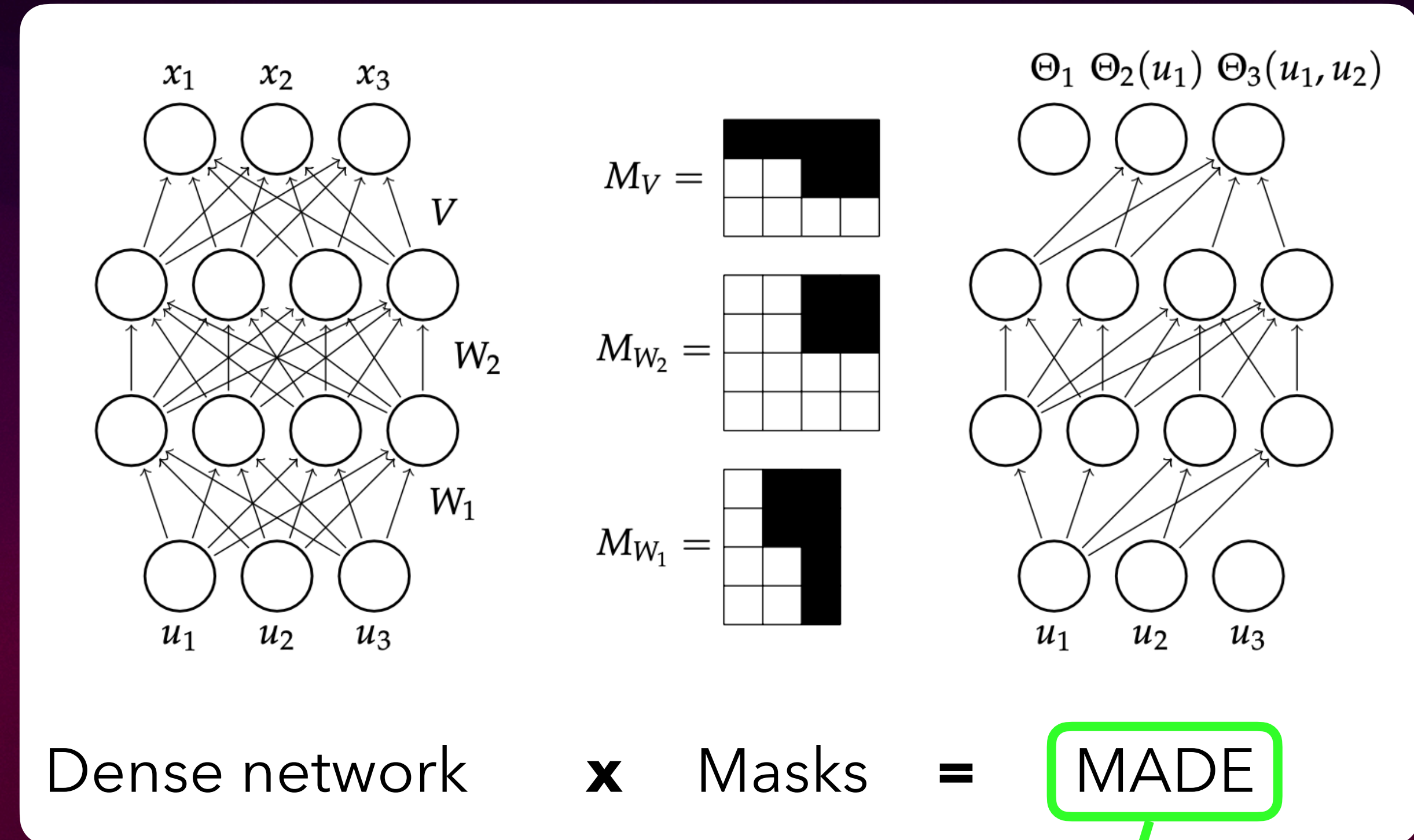
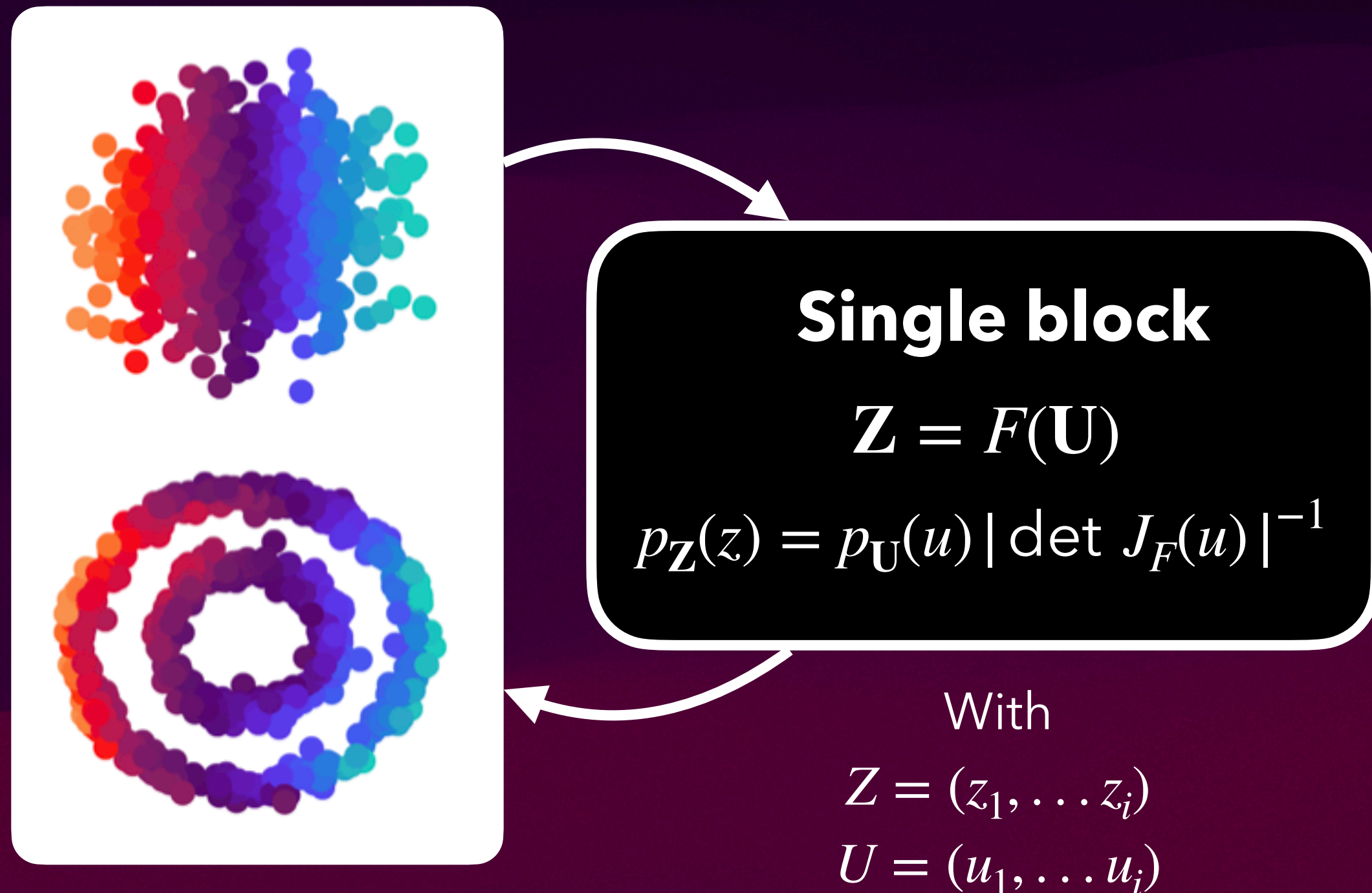
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Masked Autoencoder
for Density Estimation

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Two flavors of SBI

**Single round for
amortized inference**

**Multiple round for
fast convergence**

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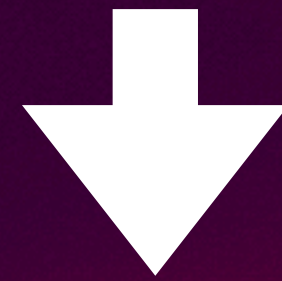
Many simulations for the training set ($\sim 100k$)

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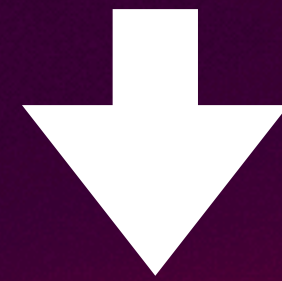
Training of the normalizing flow

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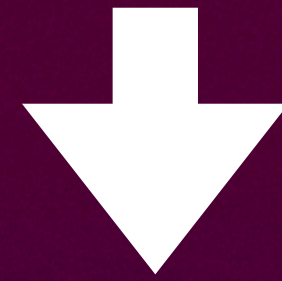
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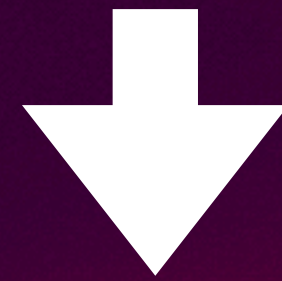
Posterior parameters for multiple
observations using the same network

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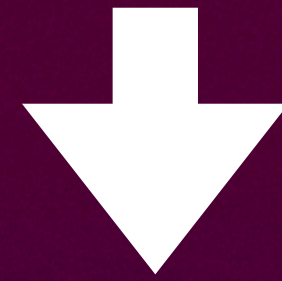
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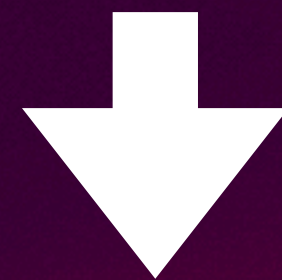
**Fast inference for
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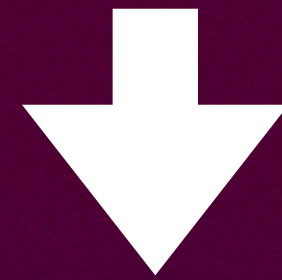
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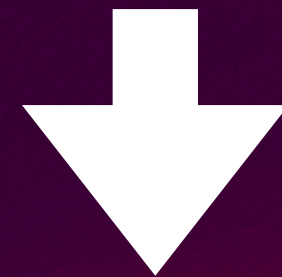
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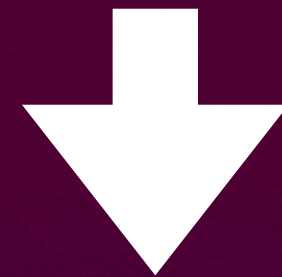
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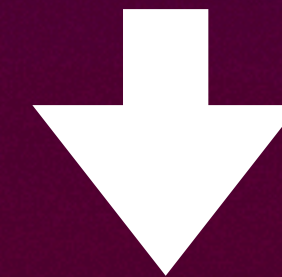


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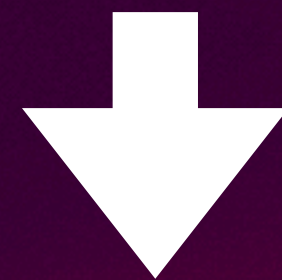


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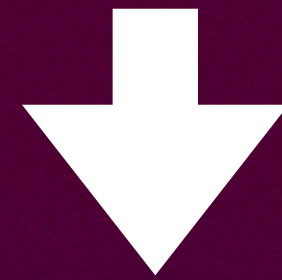
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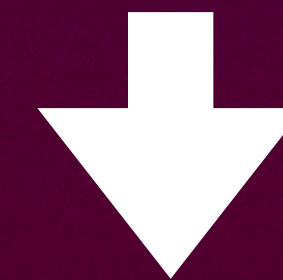


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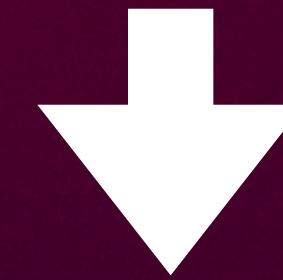
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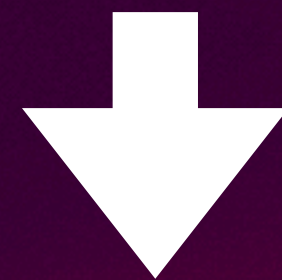


Posterior parameters for a
single fine-tuned observation

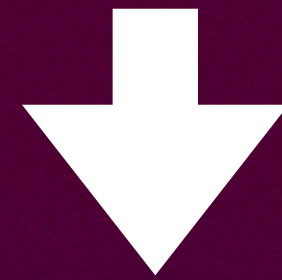
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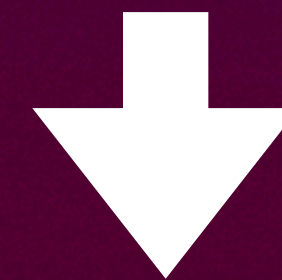


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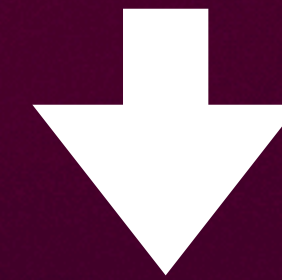
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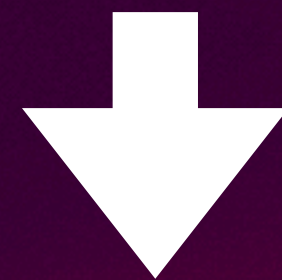
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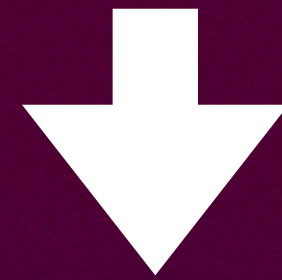
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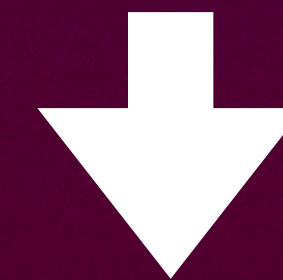


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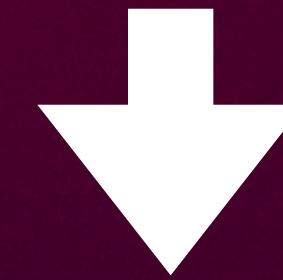
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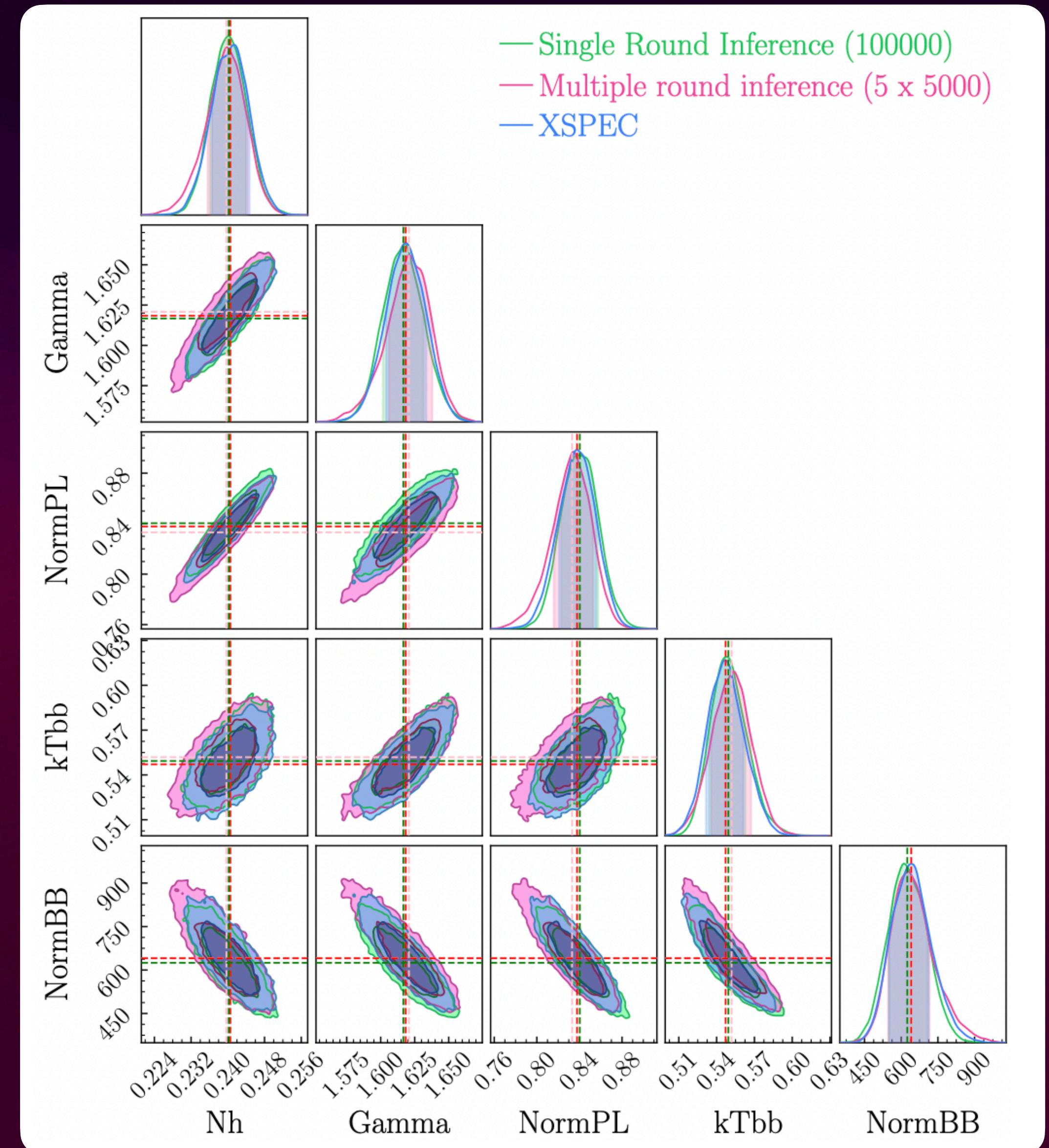


Comparison with Bayesian Inference

Direct comparison between SBI and traditional Bayesian Inference for a XMM-Newton source

Green and **Red** : two flavors of SBI
Blue : reference (MCMC)

SBI performs **similarly** as **MCMC** in X-ray spectroscopy while being much faster



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- **Automatic marginalization** : You have nuisance parameters or extra noise but analytical marginalization is unfeasible. Example : **calibration uncertainties**

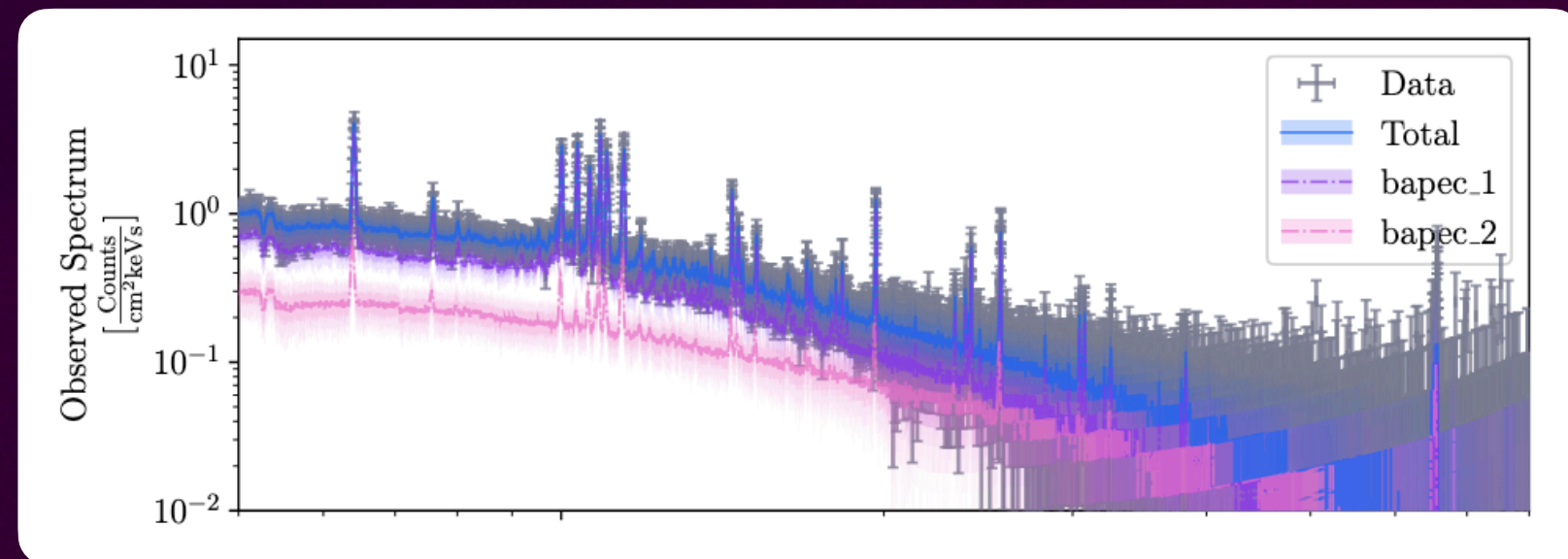
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- **Bulk inference** : You have numerous similar observables that you would want to fit at once. Example : **time-resolved spectroscopy**
- **Automatic marginalization** : You have nuisance parameters or extra noise but analytical marginalization is unfeasible. Example : **calibration uncertainties**
- **Likelihood free inference**: The maths are too hard and you can't derive a satisfactory likelihood for your observable Example : **compressed representation**

Most important thing for SBI users

Look for meaningful representation of your observables (Feature Engineering)

X-IFU ~ 24k dimensions mapping a 10 parameter space

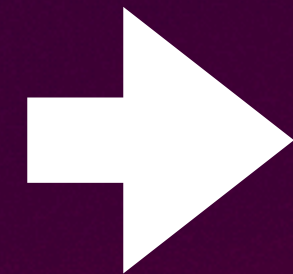
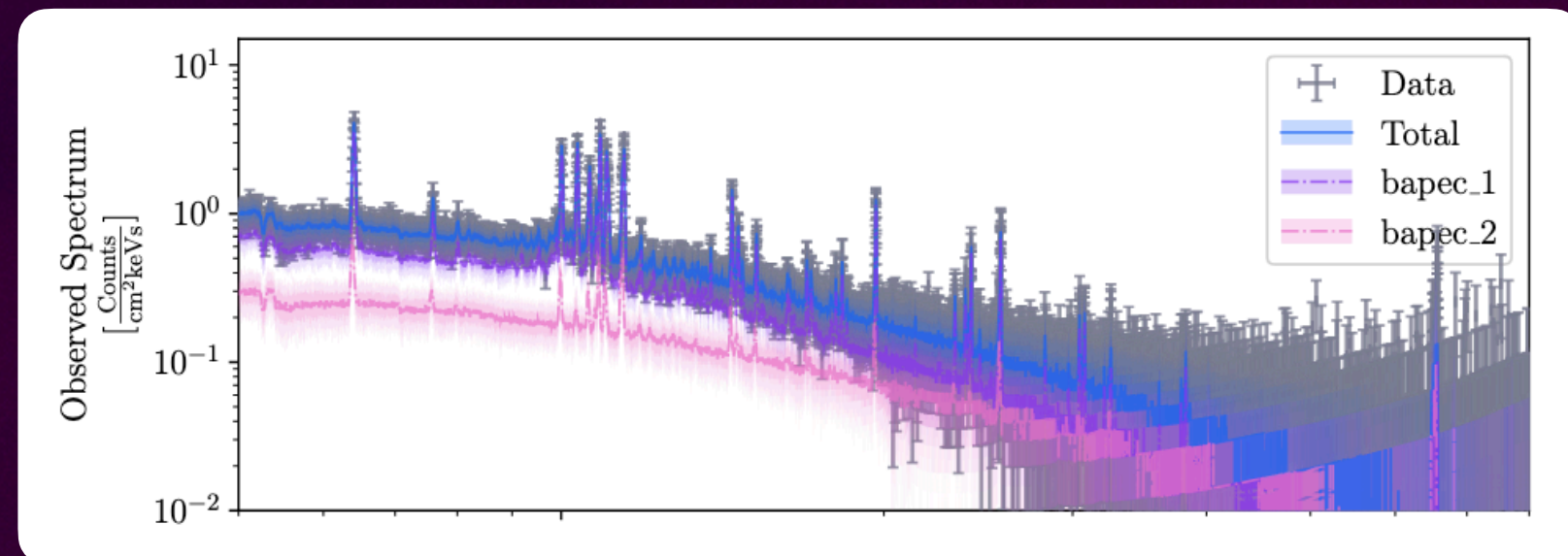


Reduce high dimension
observables to small and
weakly covariant statistics

Most important thing for SBI users

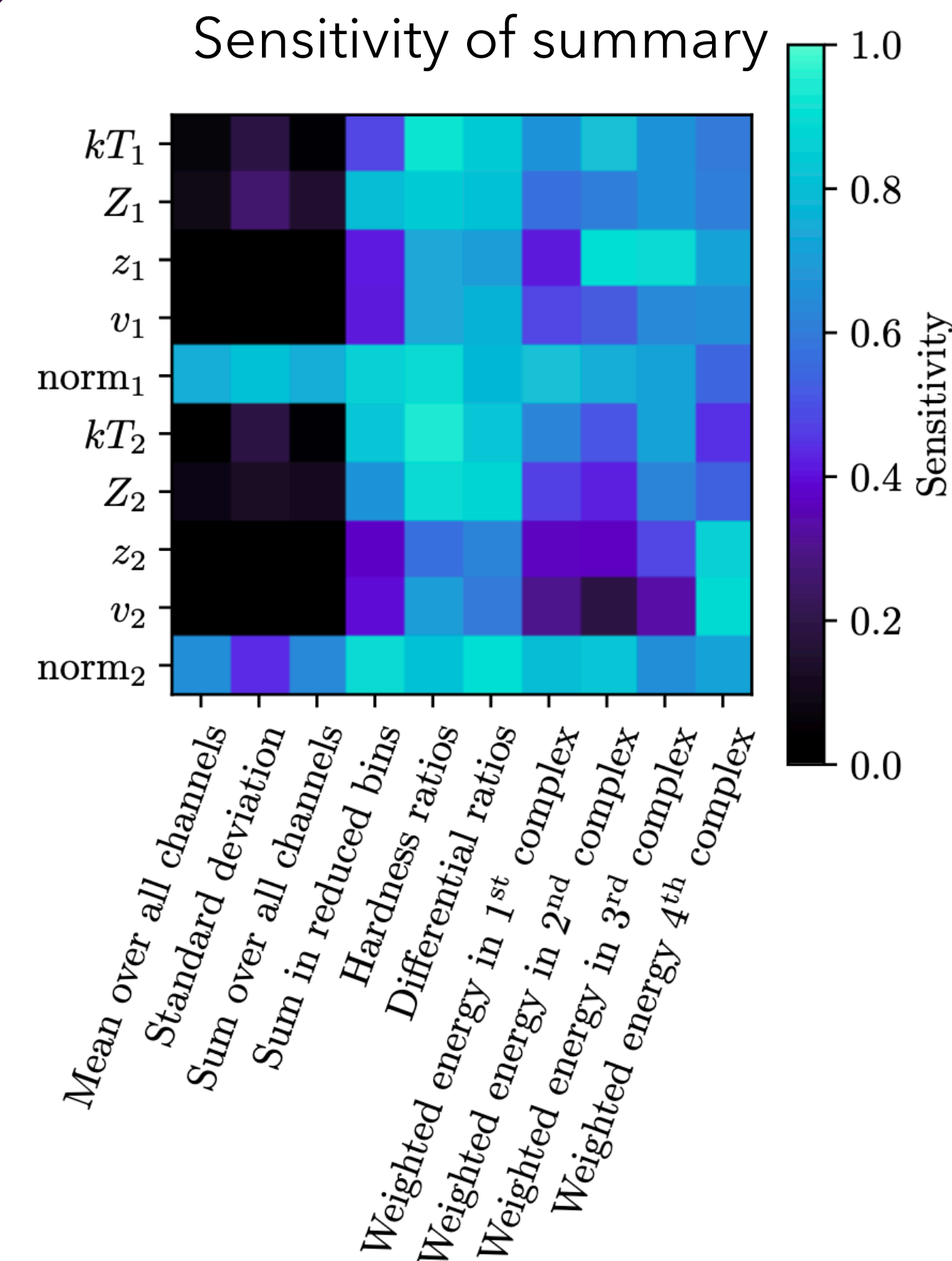
Look for meaningful representation of your observables (Feature Engineering)

X-IFU ~ 24k dimensions mapping a 10 parameter space



Physically motivated & handcrafted statistics

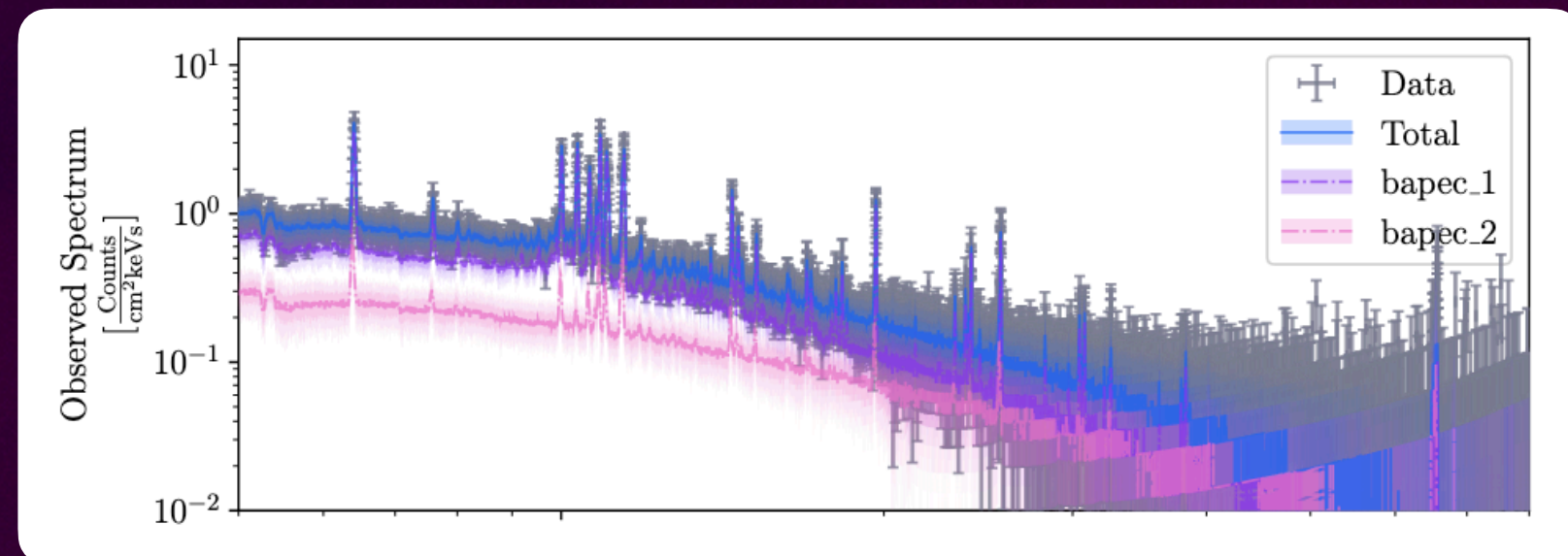
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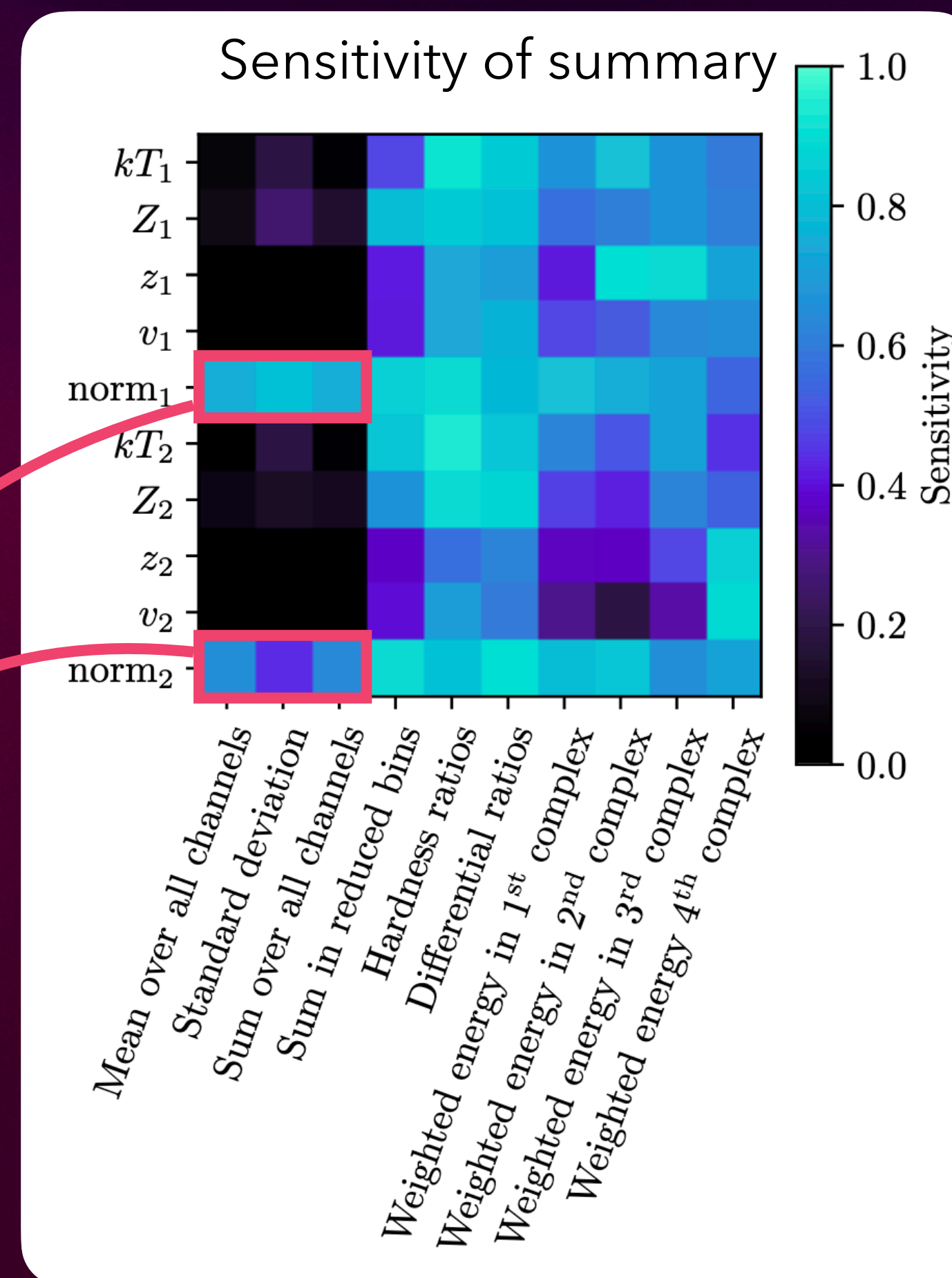
X-IFU ~ 24k dimensions mapping a 10 parameter space



Physically motivated &
handcrafted statistics

Reduce high dimension
observables to small and
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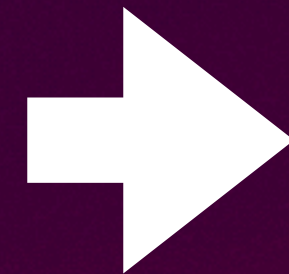
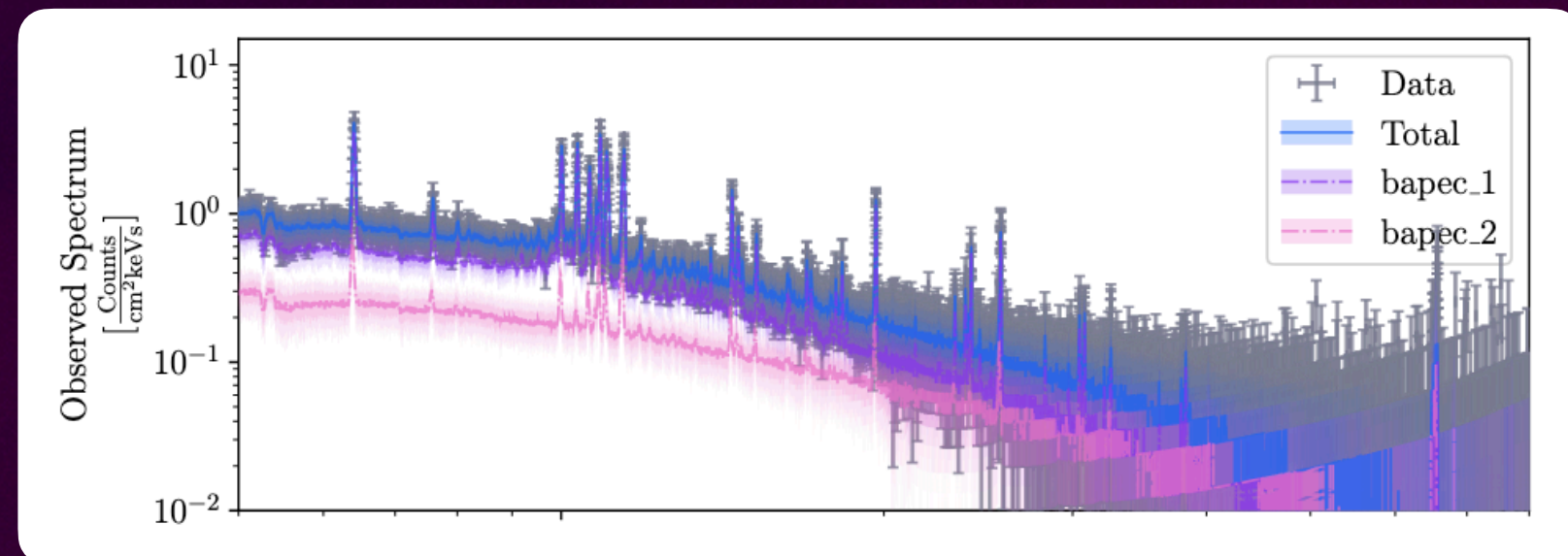
Global summaries
correlate with the
total photon
information



Most important thing for SBI users

Look for meaningful representation of your observables (Feature Engineering)

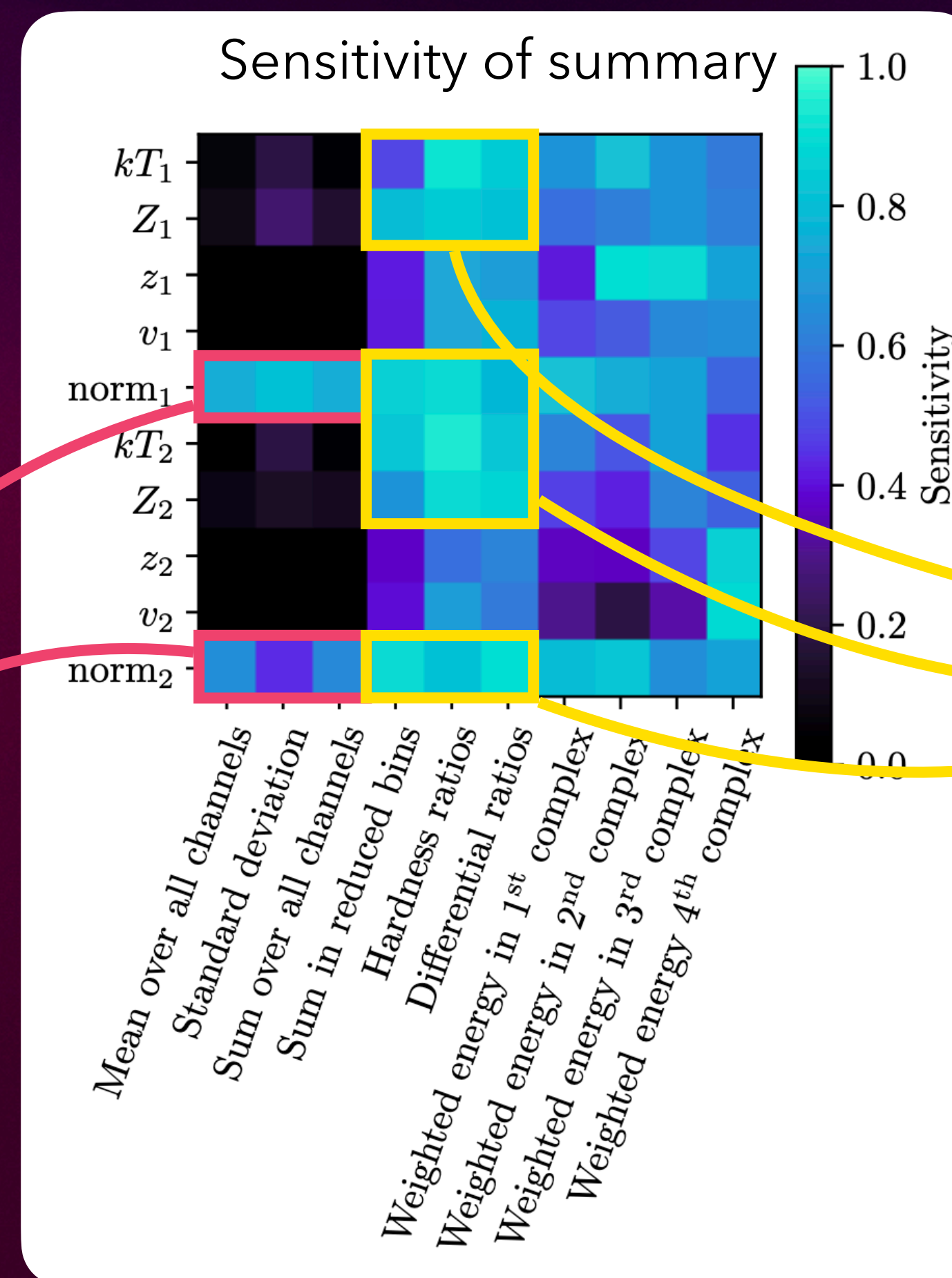
X-IFU ~ 24k dimensions mapping a 10 parameter space



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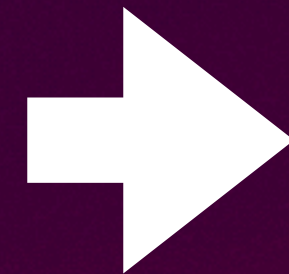
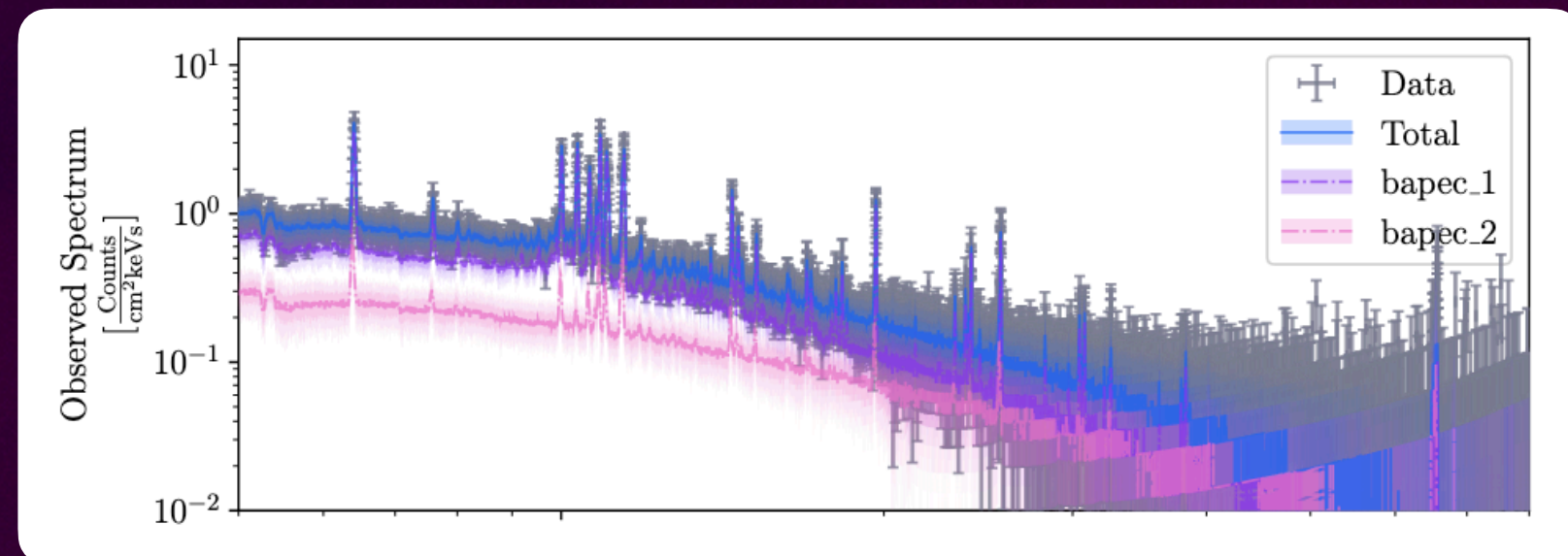


Shape summaries
correlate *mostly*
with global shape
parameters

Most important thing for SBI users

Look for meaningful representation of your observables (Feature Engineering)

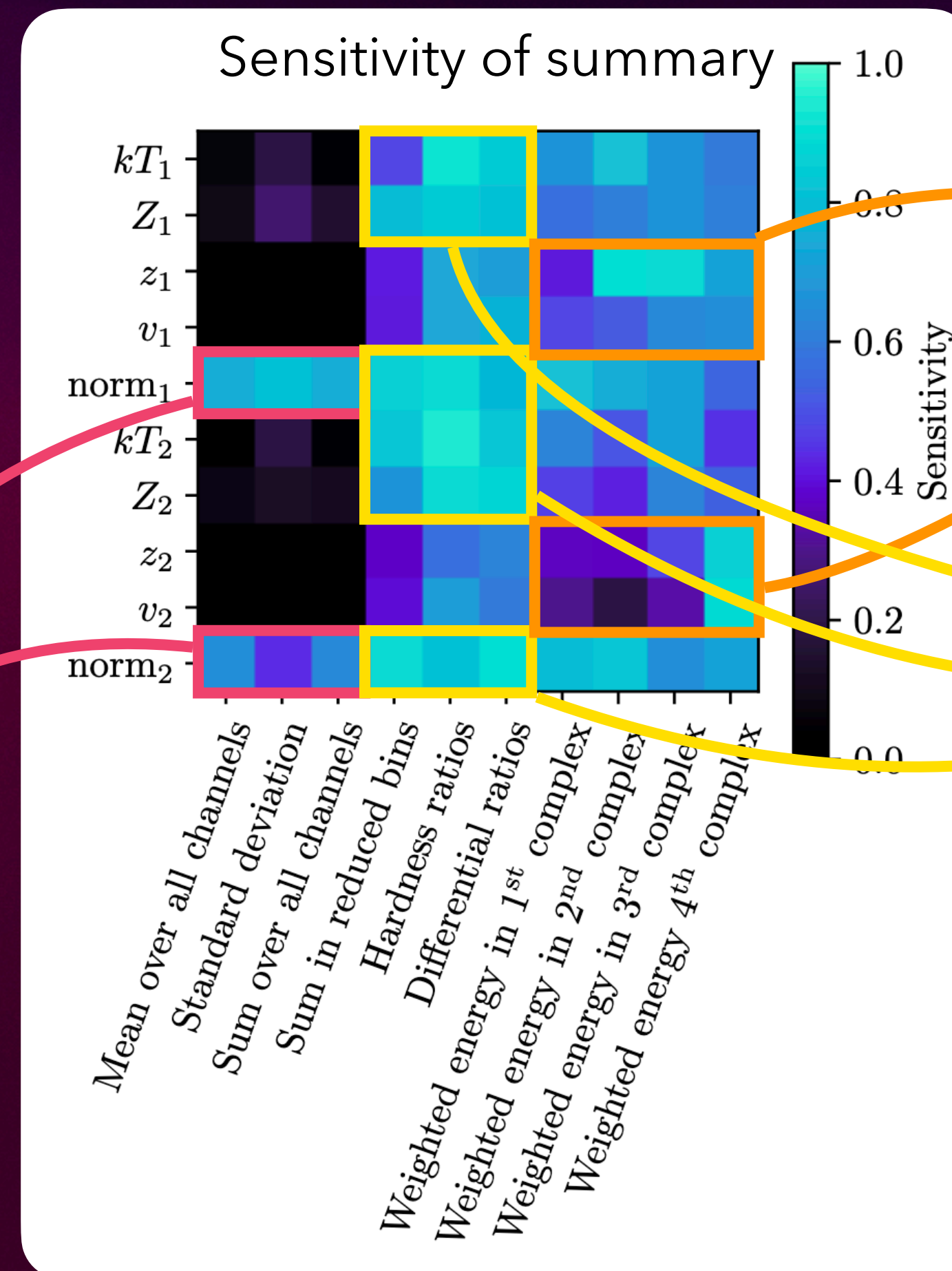
X-IFU ~ 24k dimensions mapping a 10 parameter space



Physically motivated &
handcrafted statistics

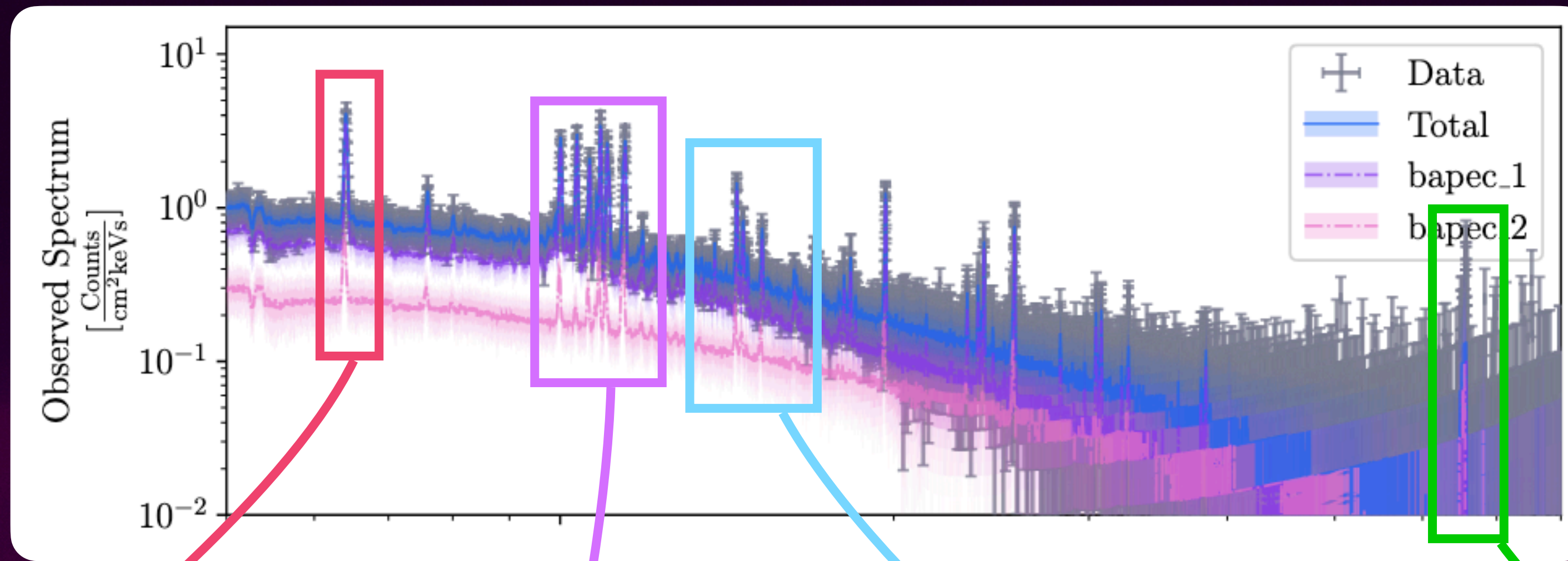
Reduce high dimension
observables to small and
weakly covariant statistics

Global summaries
correlate with the
total photon
information

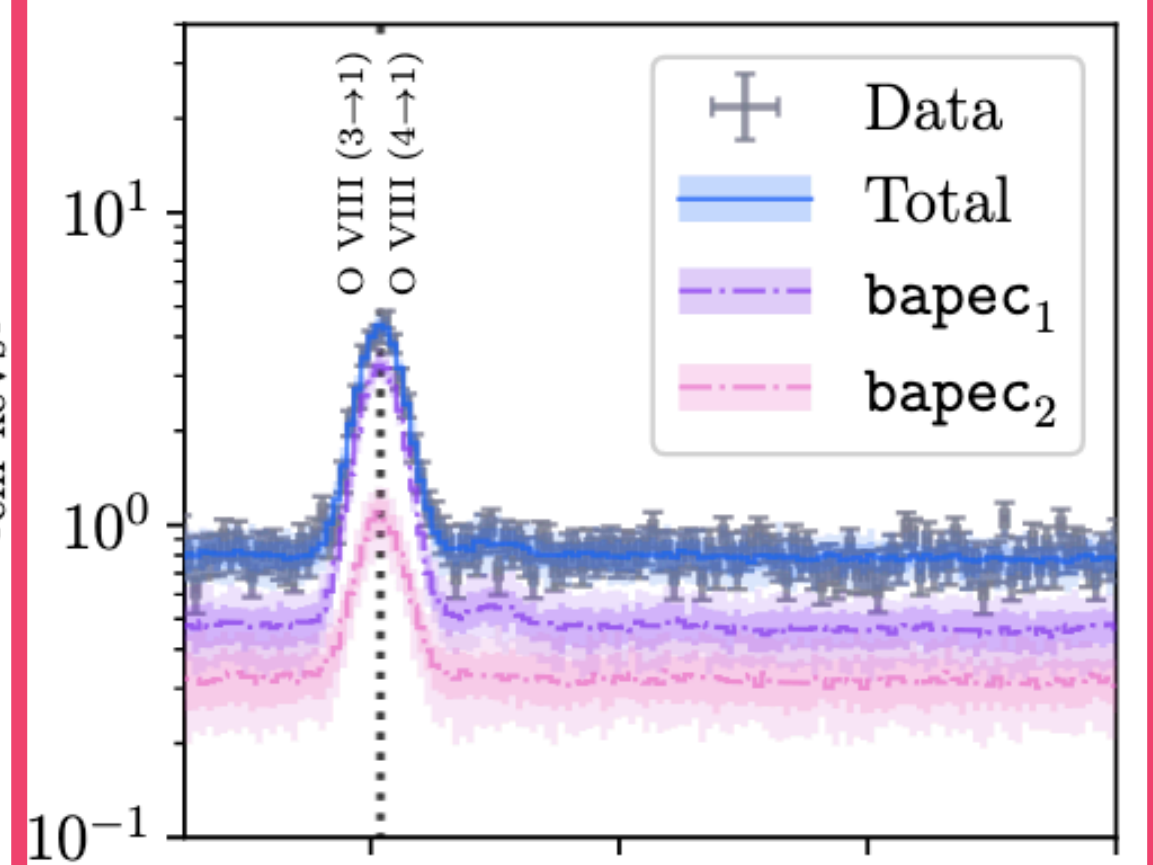


Line parameters
correlate with the
motion and
composition of the
plasma

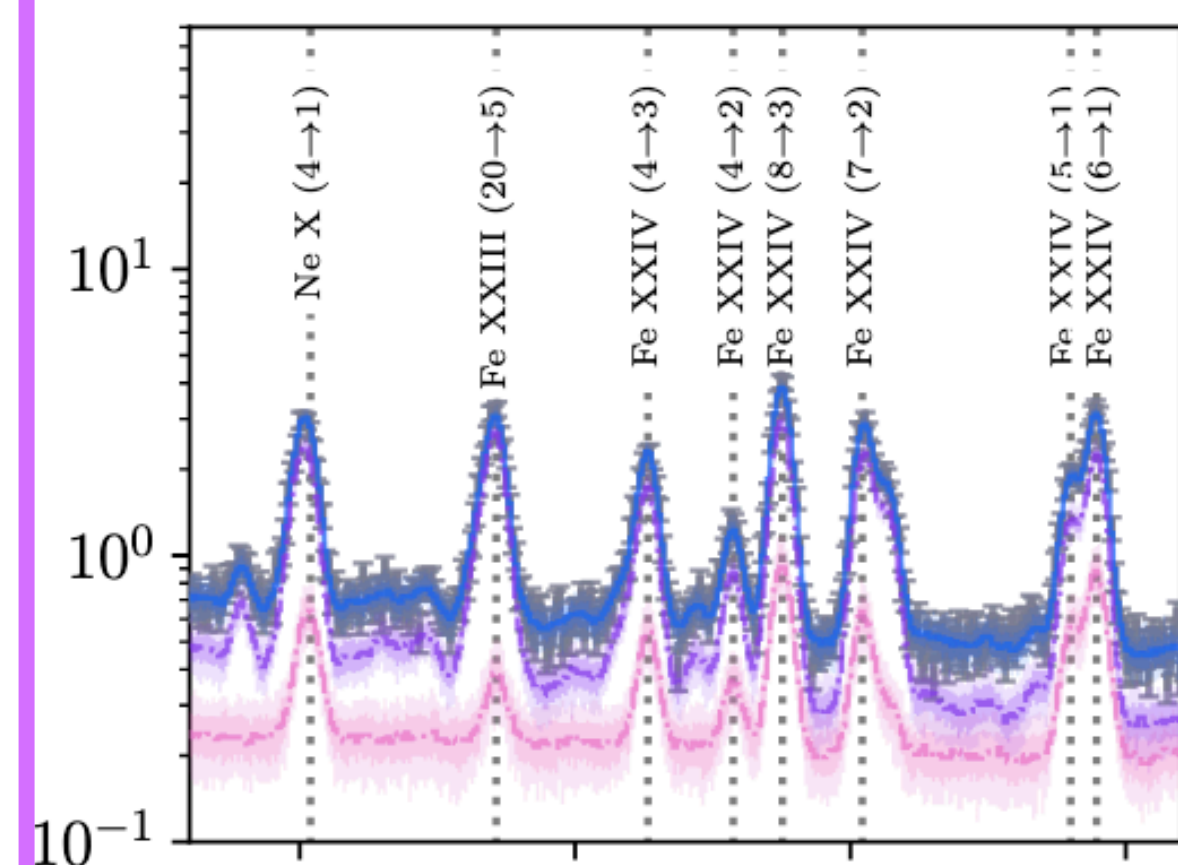
Shape summaries
correlate *mostly*
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parameters



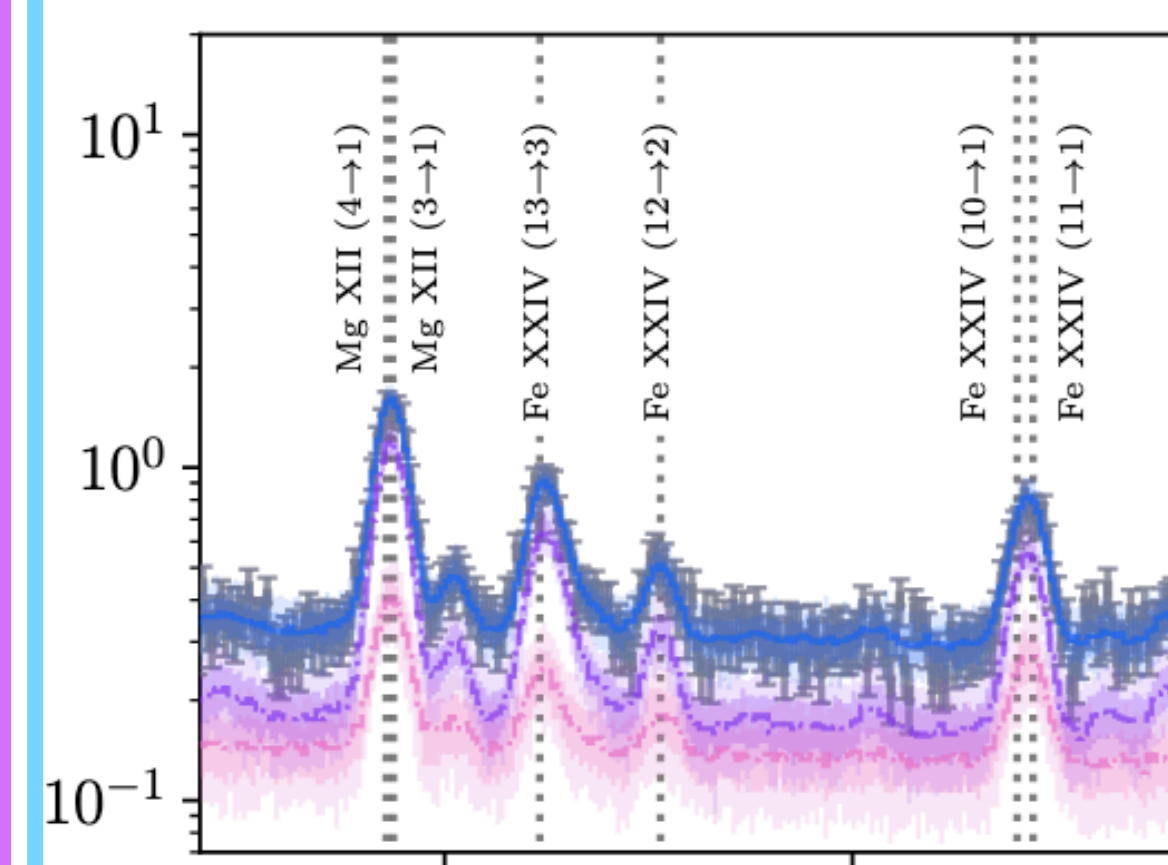
Observed Spectrum $\left[\frac{\text{Counts}}{\text{cm}^2 \text{keV s}} \right]$



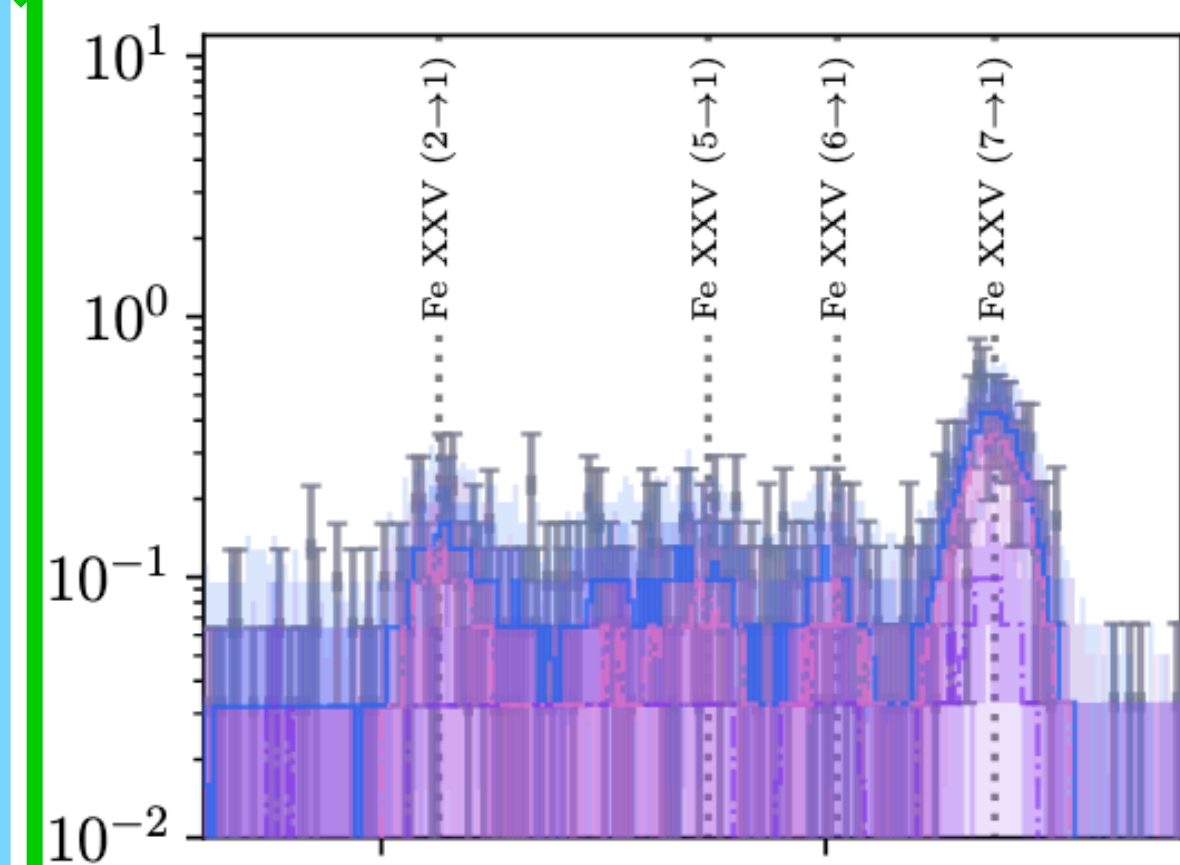
(a) O VIII



(b) Fe XXIV + Ne X

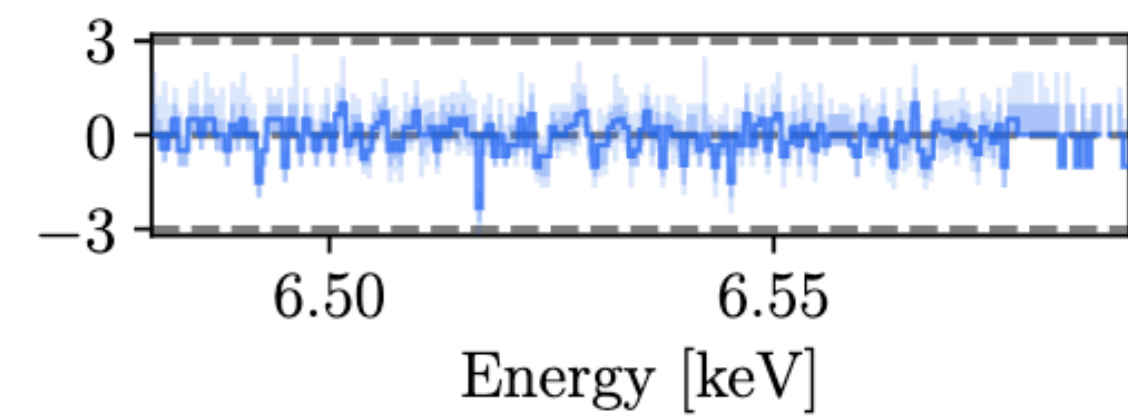
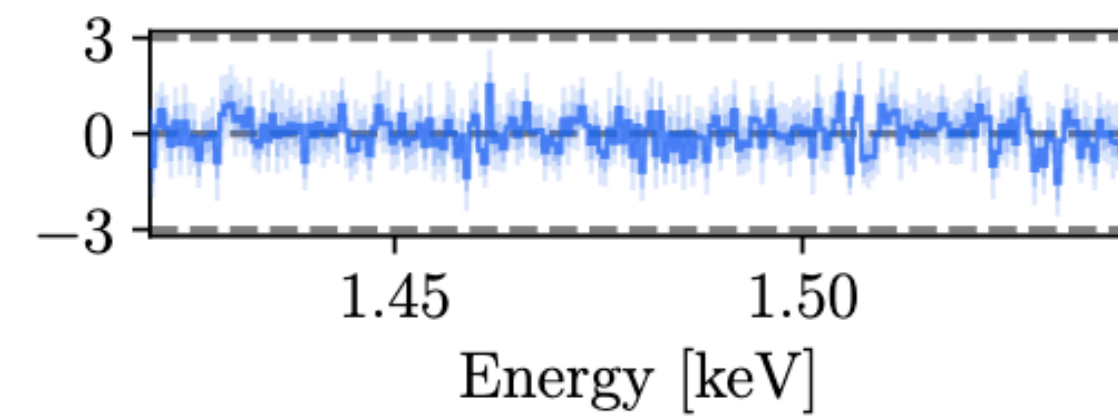
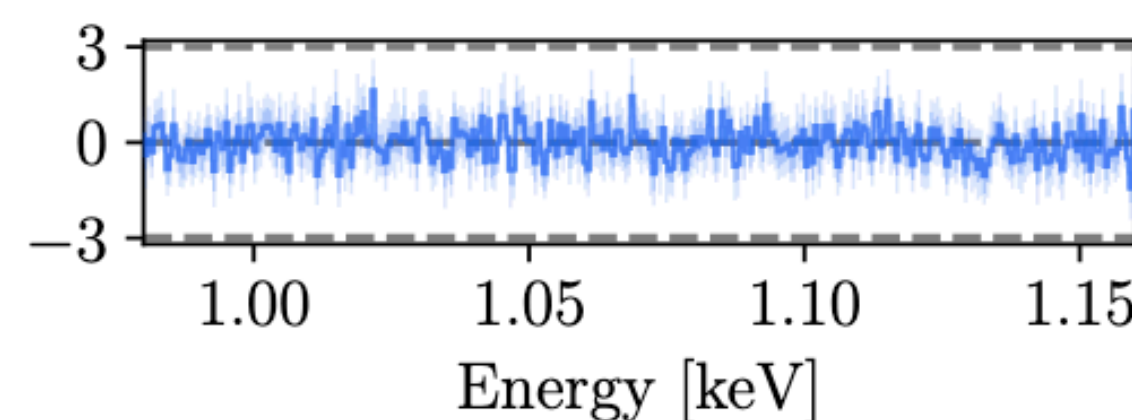
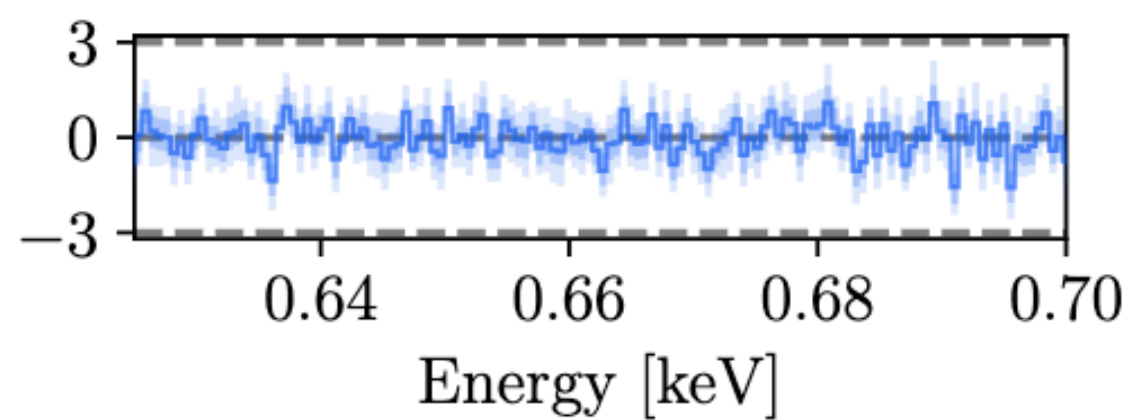


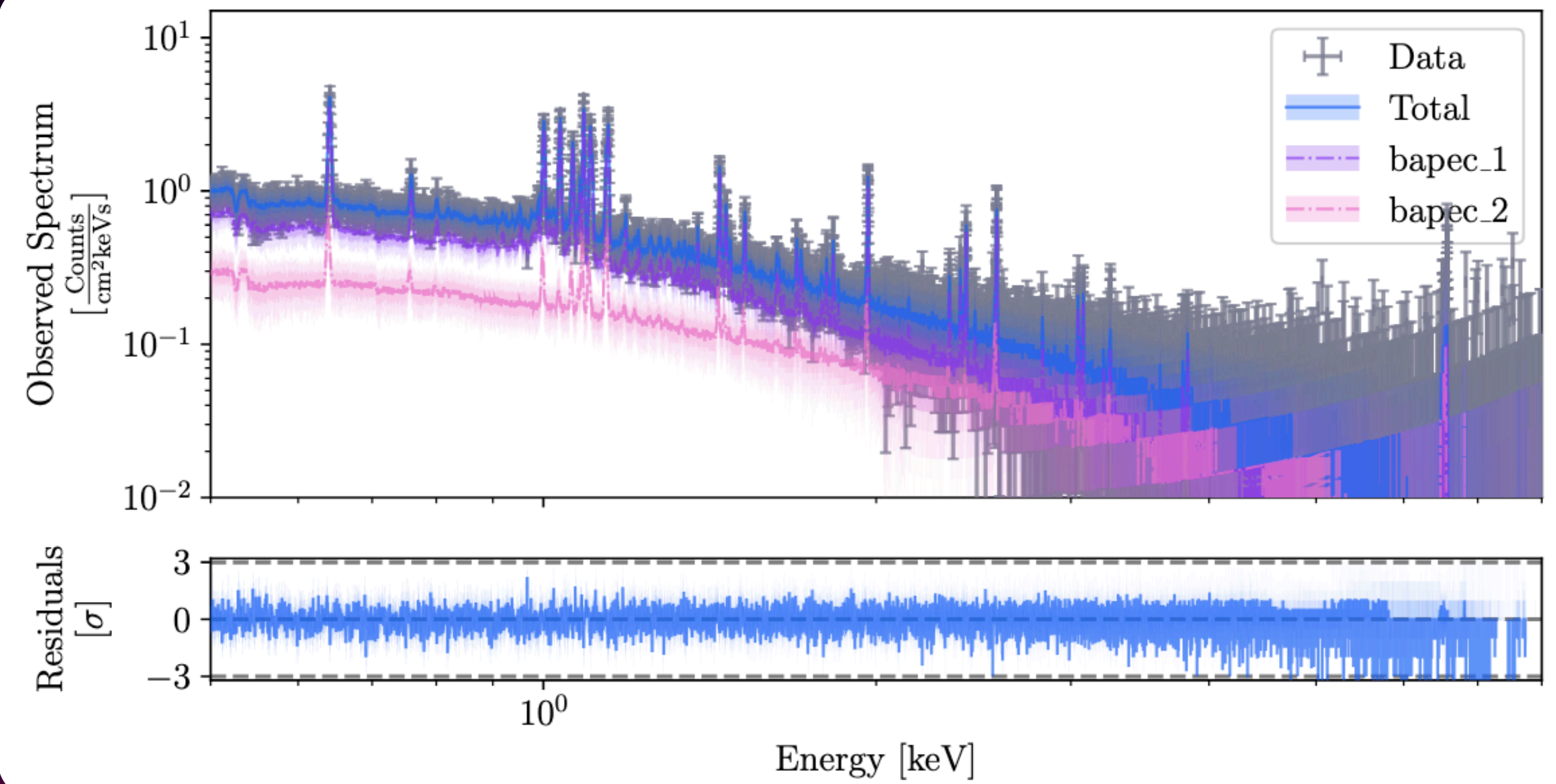
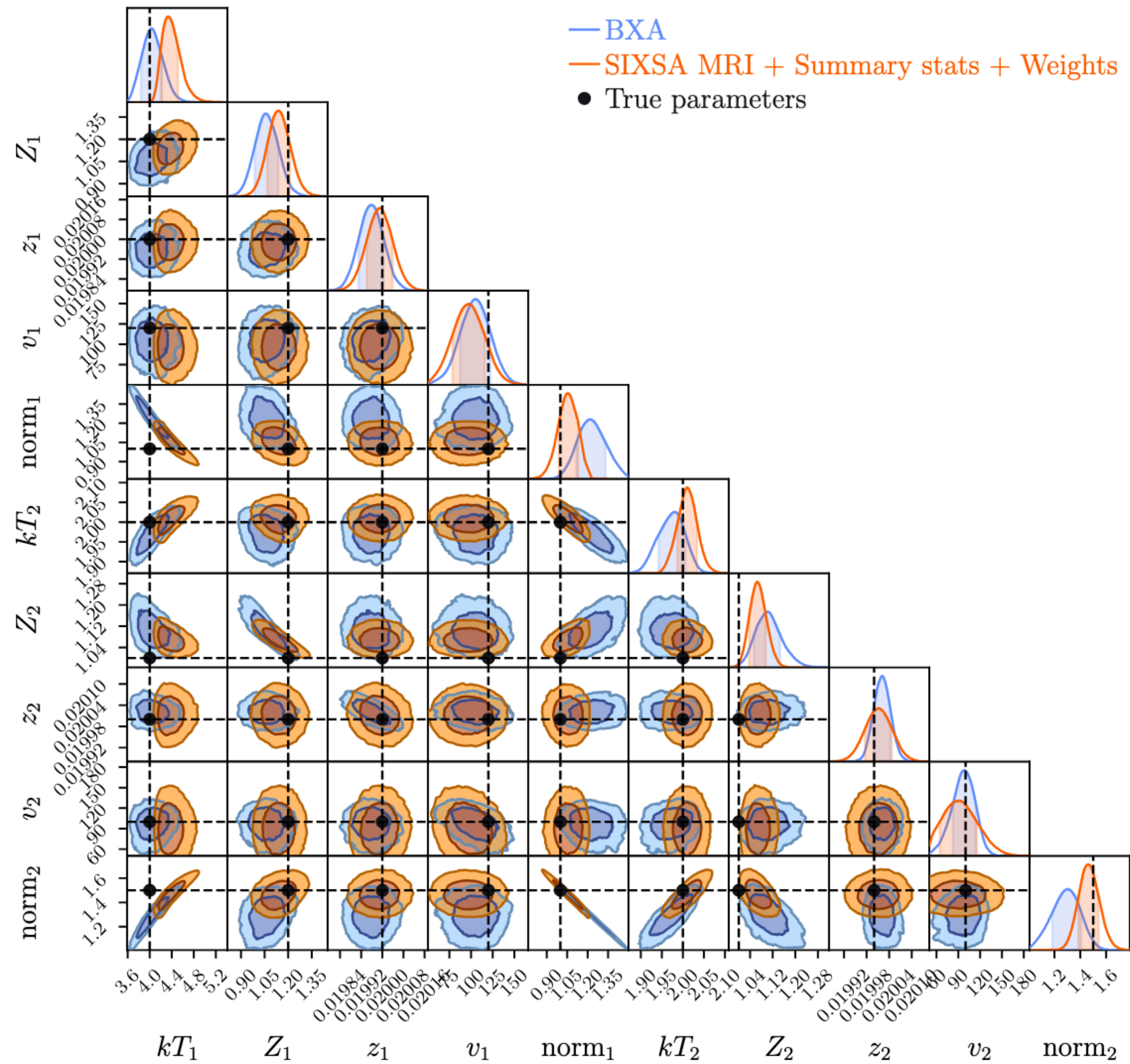
(c) Fe XXIV + Mg XII



(d) Fe XXV

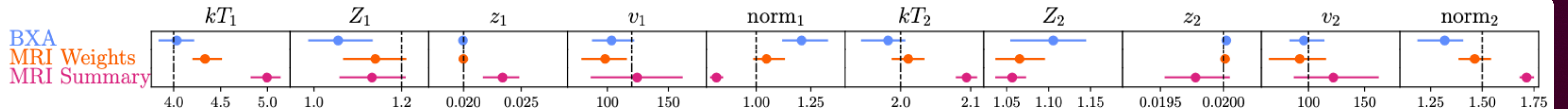
Residuals $[\sigma]$



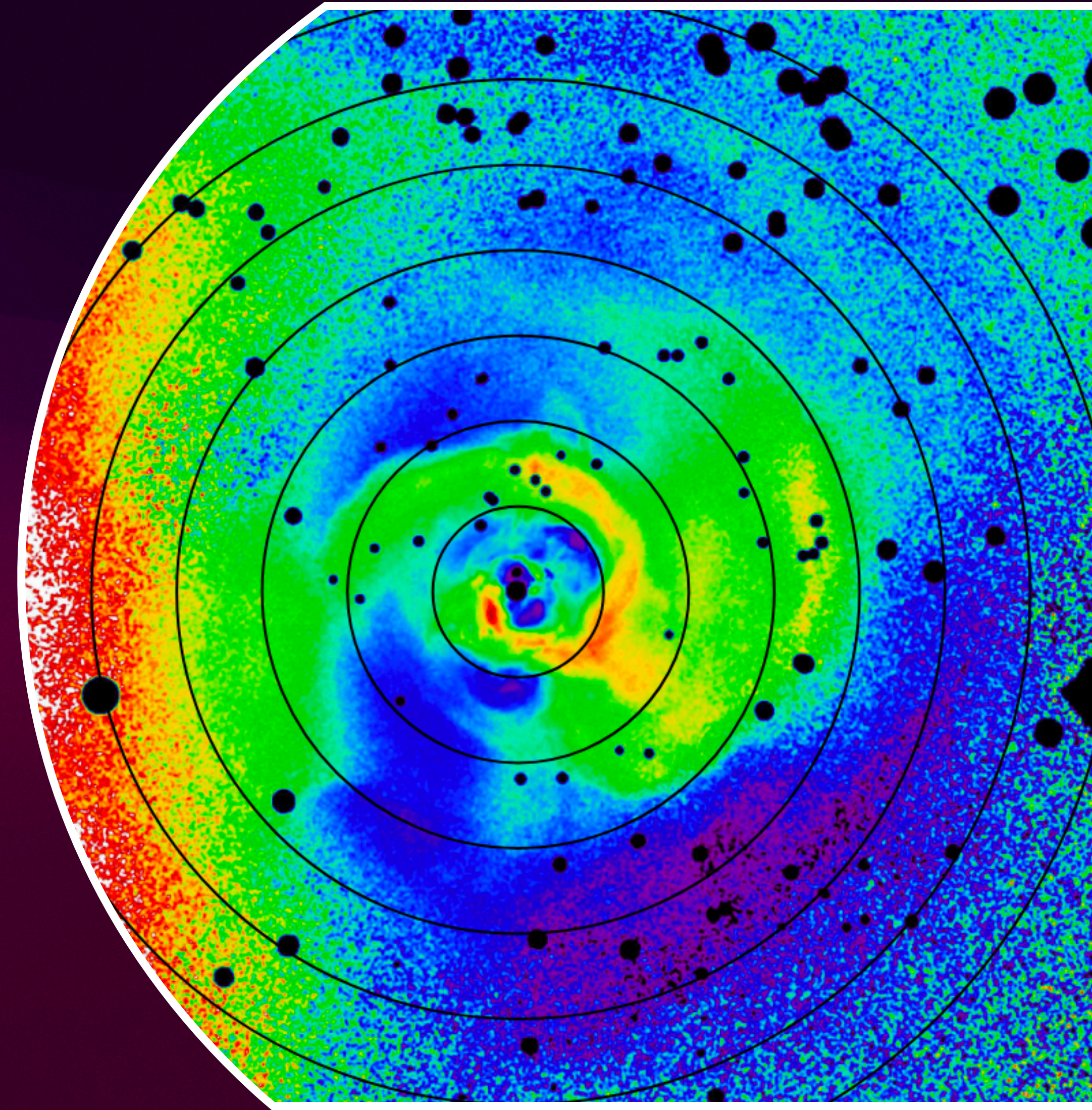


There is room for improvement

- Improve the compression
 - Use the likelihood information
- Check Didier's talk!



SBI and the dynamic assembly of galaxy clusters



Adapted from Zhuravleva & al. 2015

Galaxy clusters in a nutshell

Galaxy clusters in a nutshell

- **Largest gravitationally bound structures** in the Universe 📈



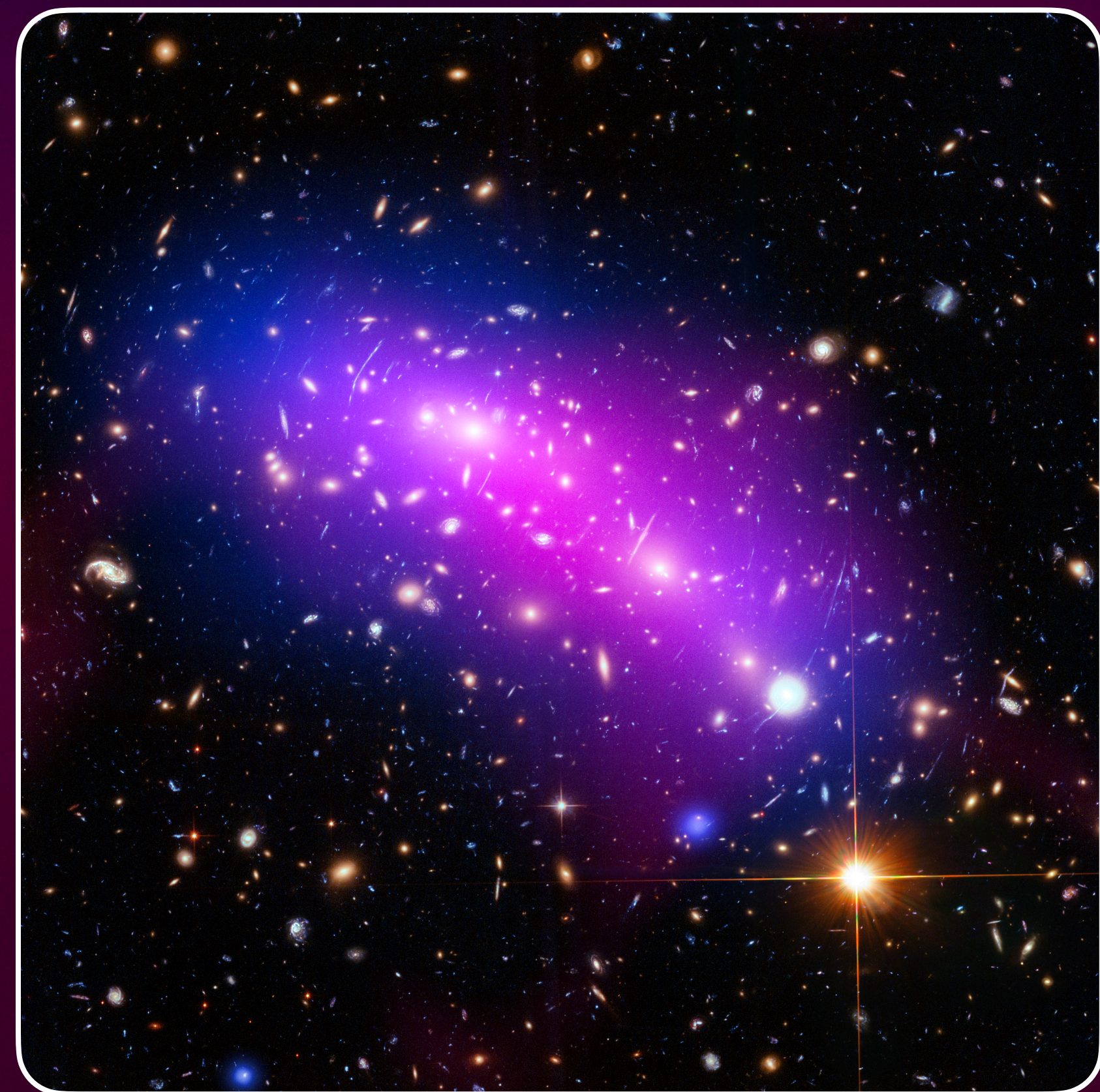
Galaxies only

Galaxy clusters in a nutshell

- **Largest gravitationally bound structures** in the Universe 📈
- **Galaxies** (1%), significant amount of **baryonic gas** (10%) and mostly **dark matter** (89%)



Galaxies only



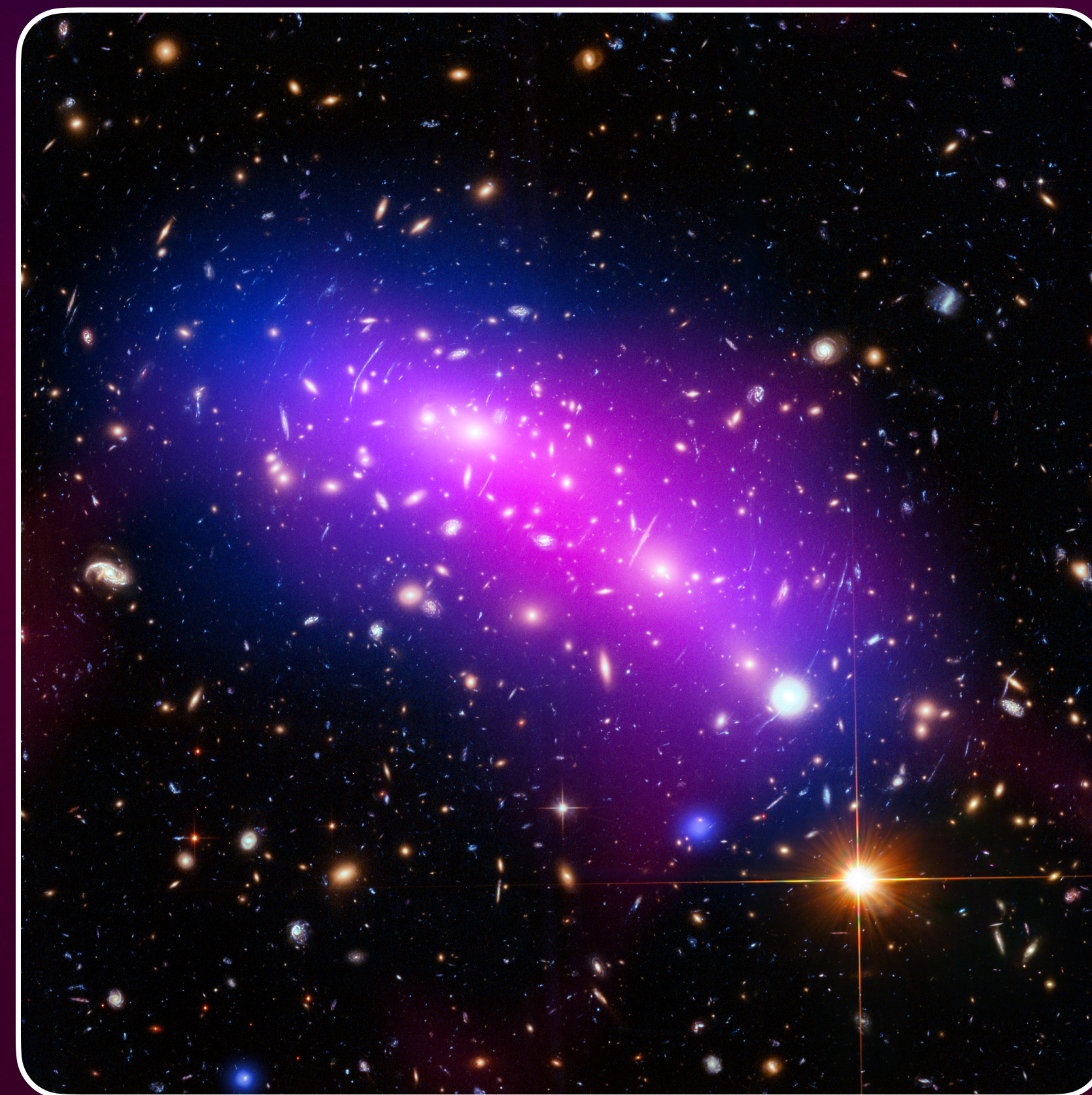
Galaxies + gas + dark matter

Galaxy clusters in a nutshell

- **Largest gravitationally bound structures** in the Universe 📈
- **Galaxies** (1%), significant amount of **baryonic gas** (10%) and mostly **dark matter** (89%)
- The **baryonic gas** deviates from hydrostatic equilibrium, probably due to **turbulent motion**
- Better understanding this motion is key to use galaxy clusters as **cosmological probes**



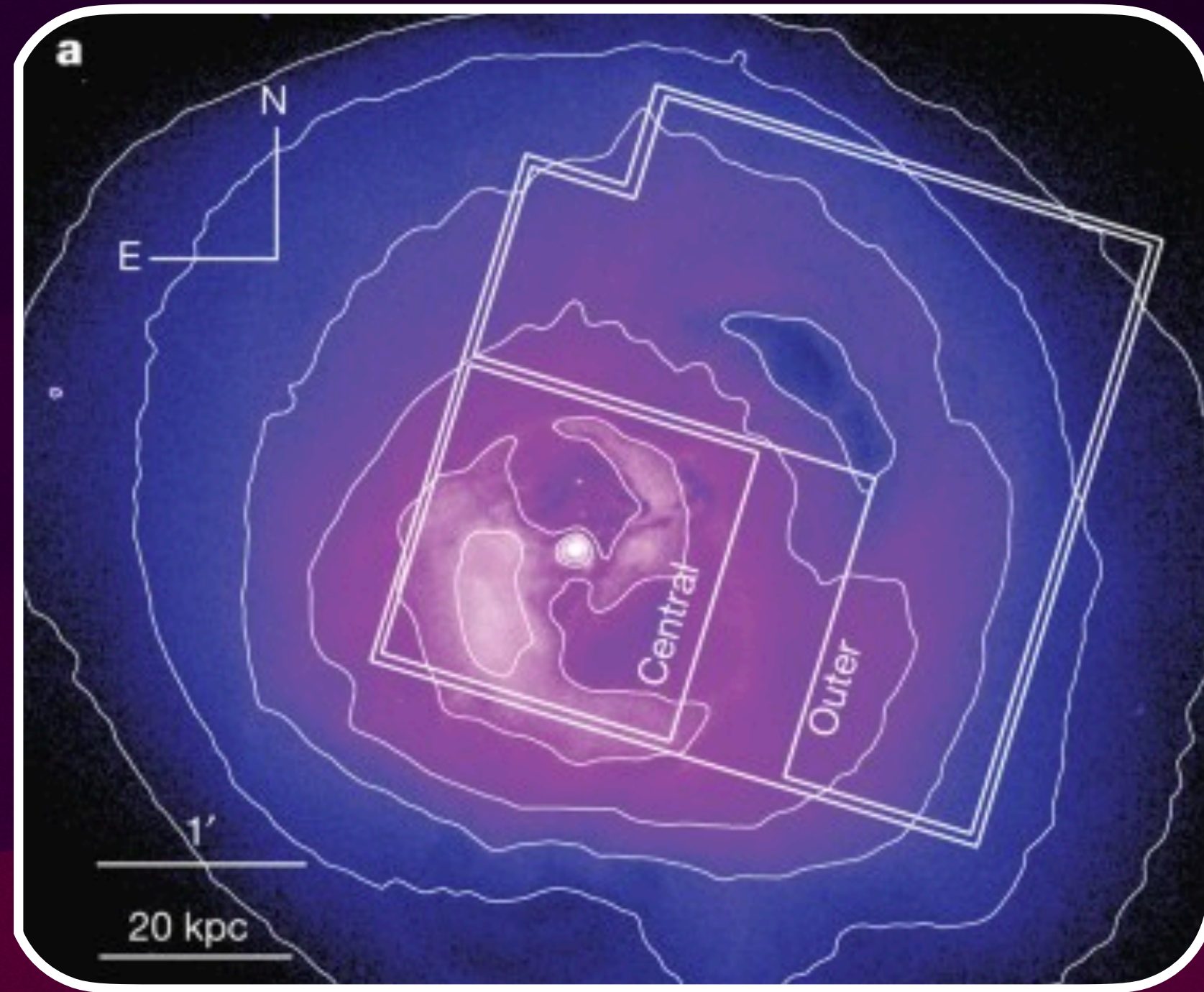
Galaxies only



Galaxies + gas + dark matter

Direct view

Adapted from Hitomi Collaboration (2016)

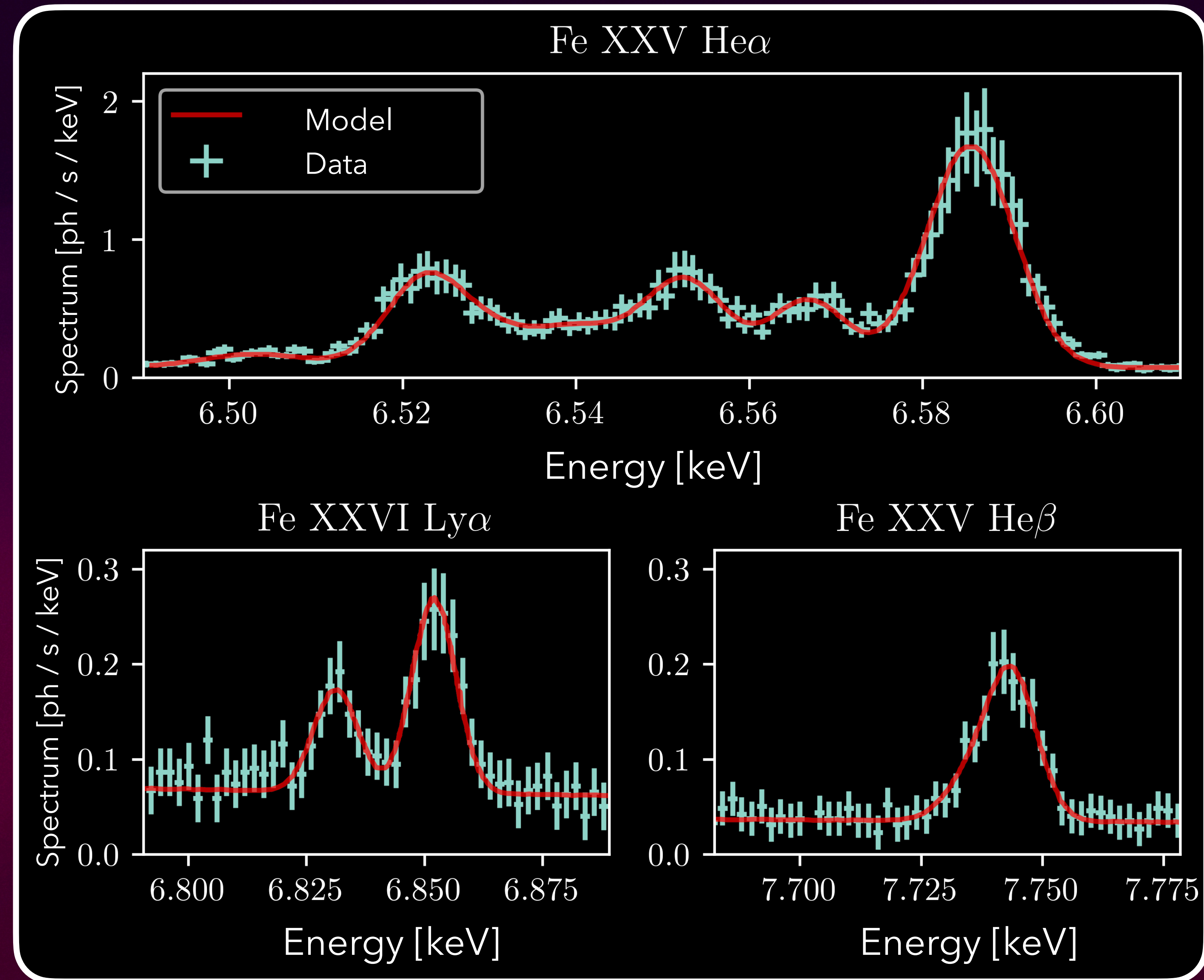


Gas motion has a direct effect on emission lines

Centroid shift \Leftrightarrow Bulk motion

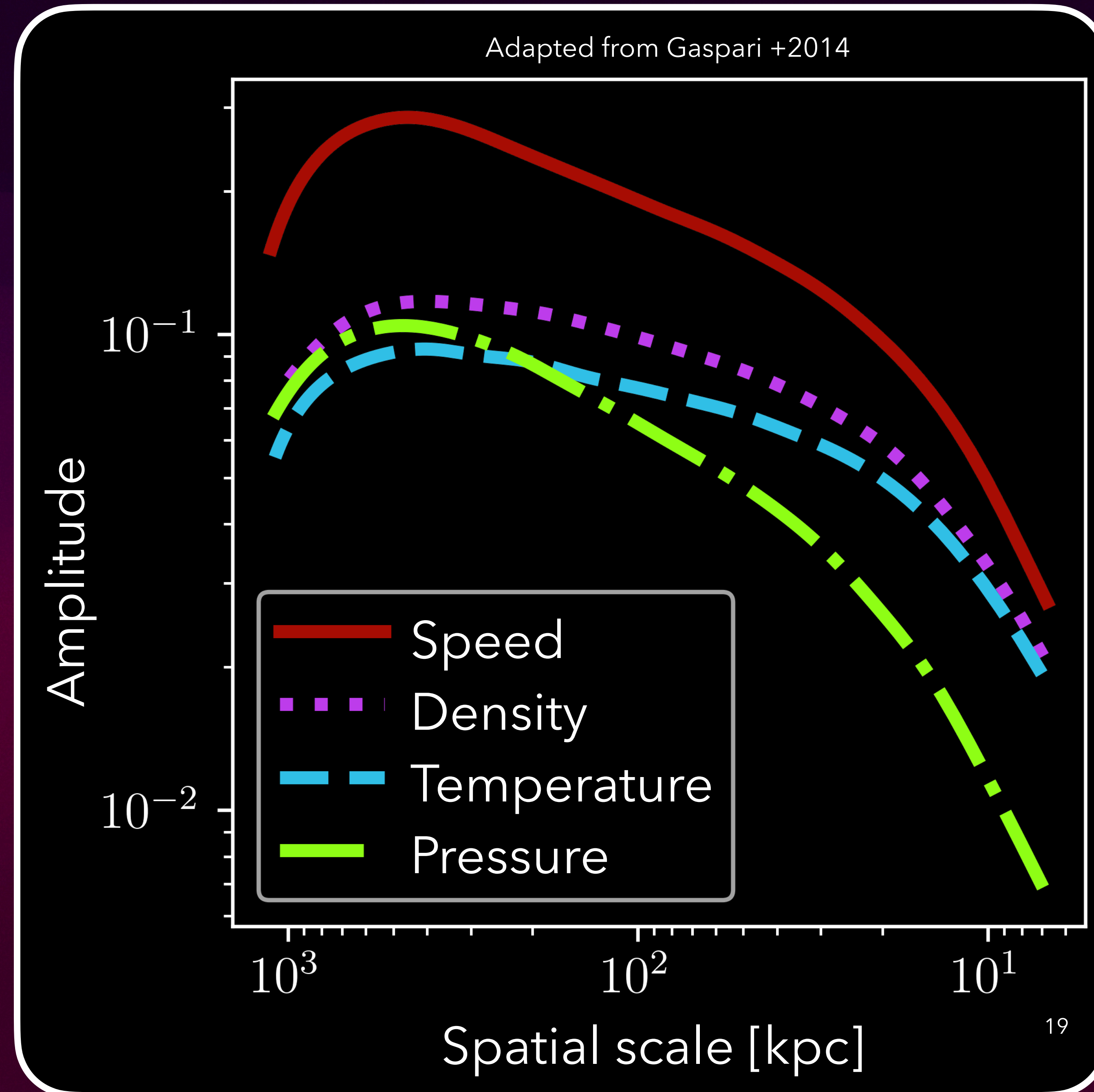
Broadening \Leftrightarrow Integrated motion

XRISM results in Dominique's talk

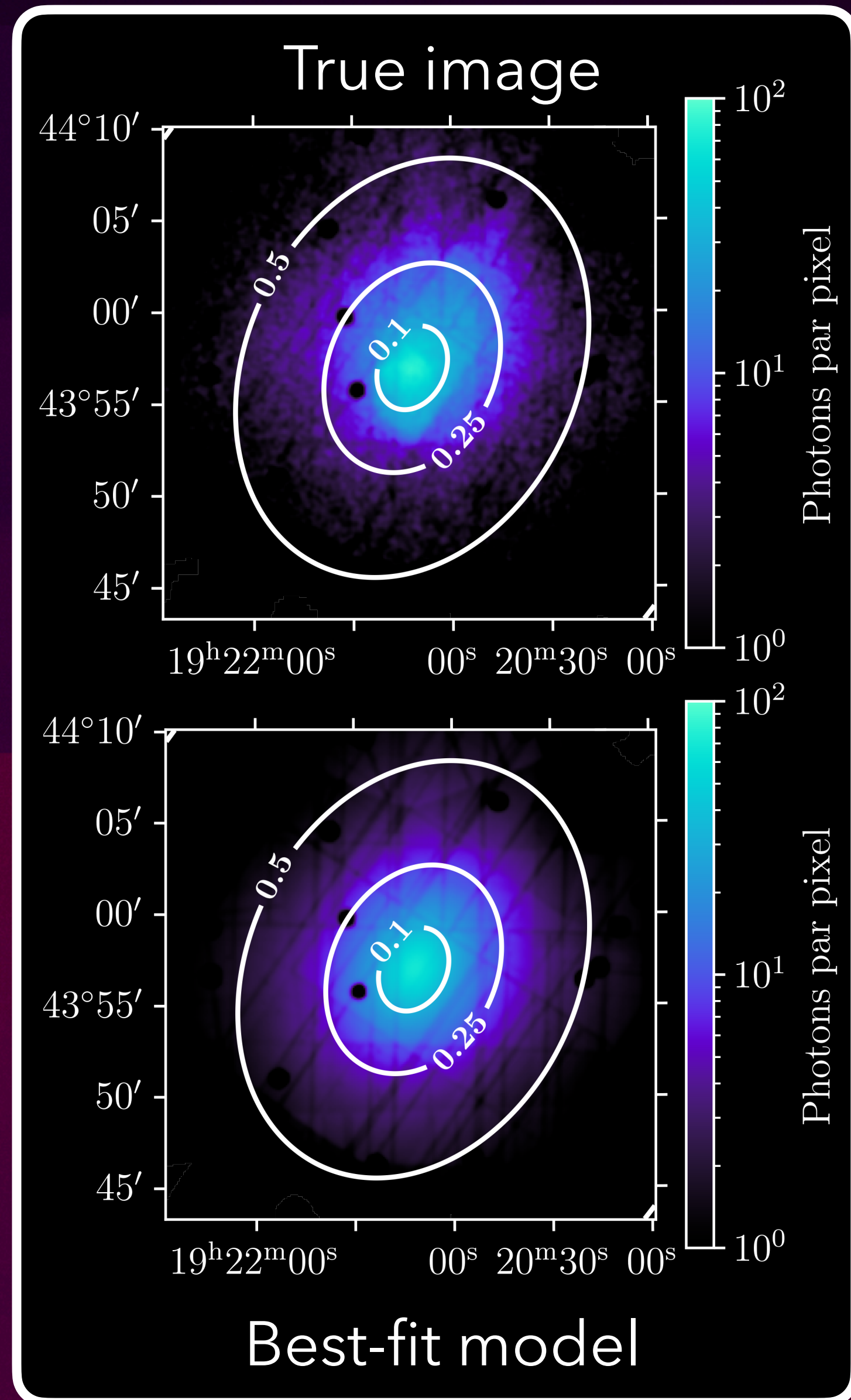


Indirect view

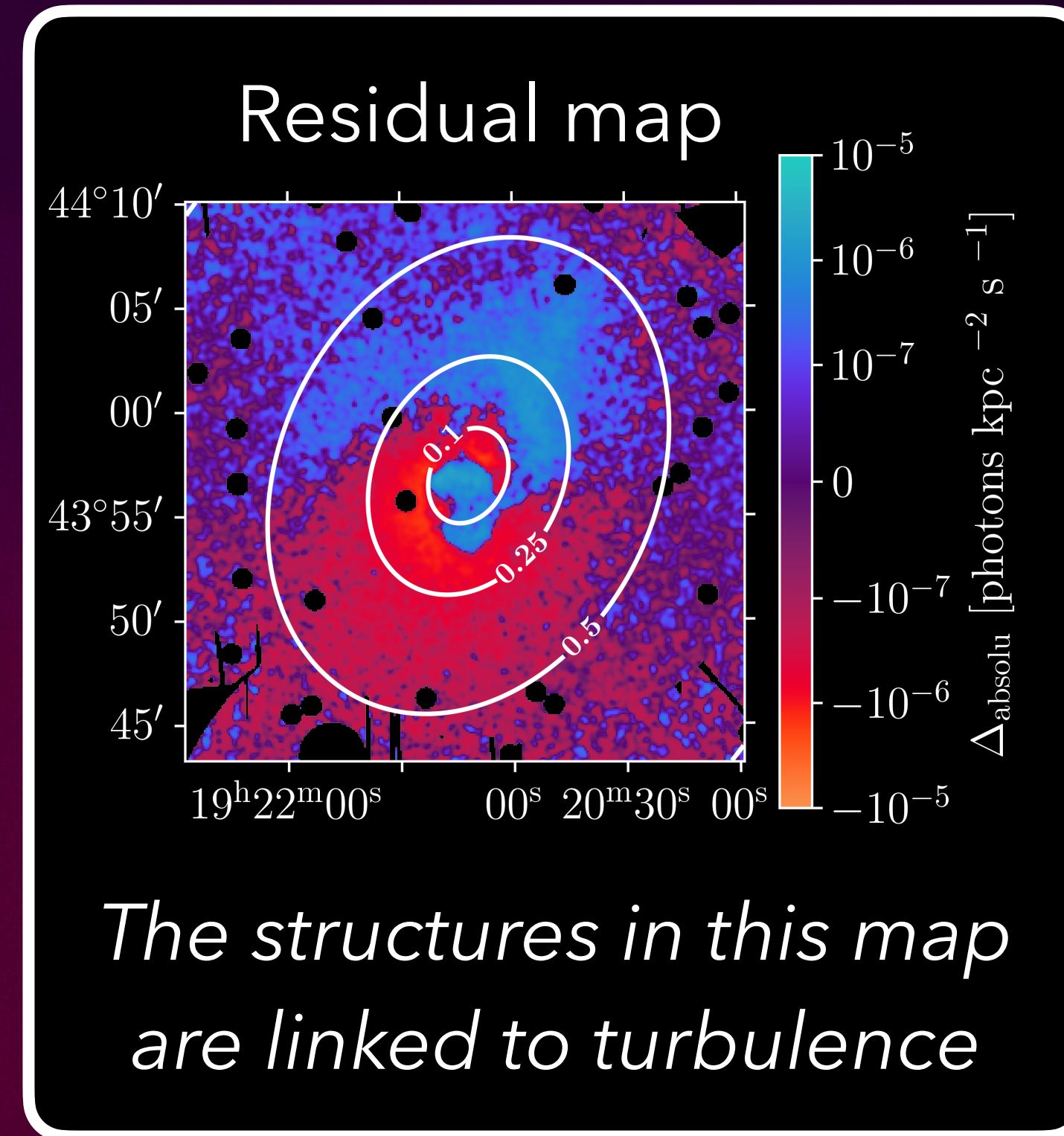
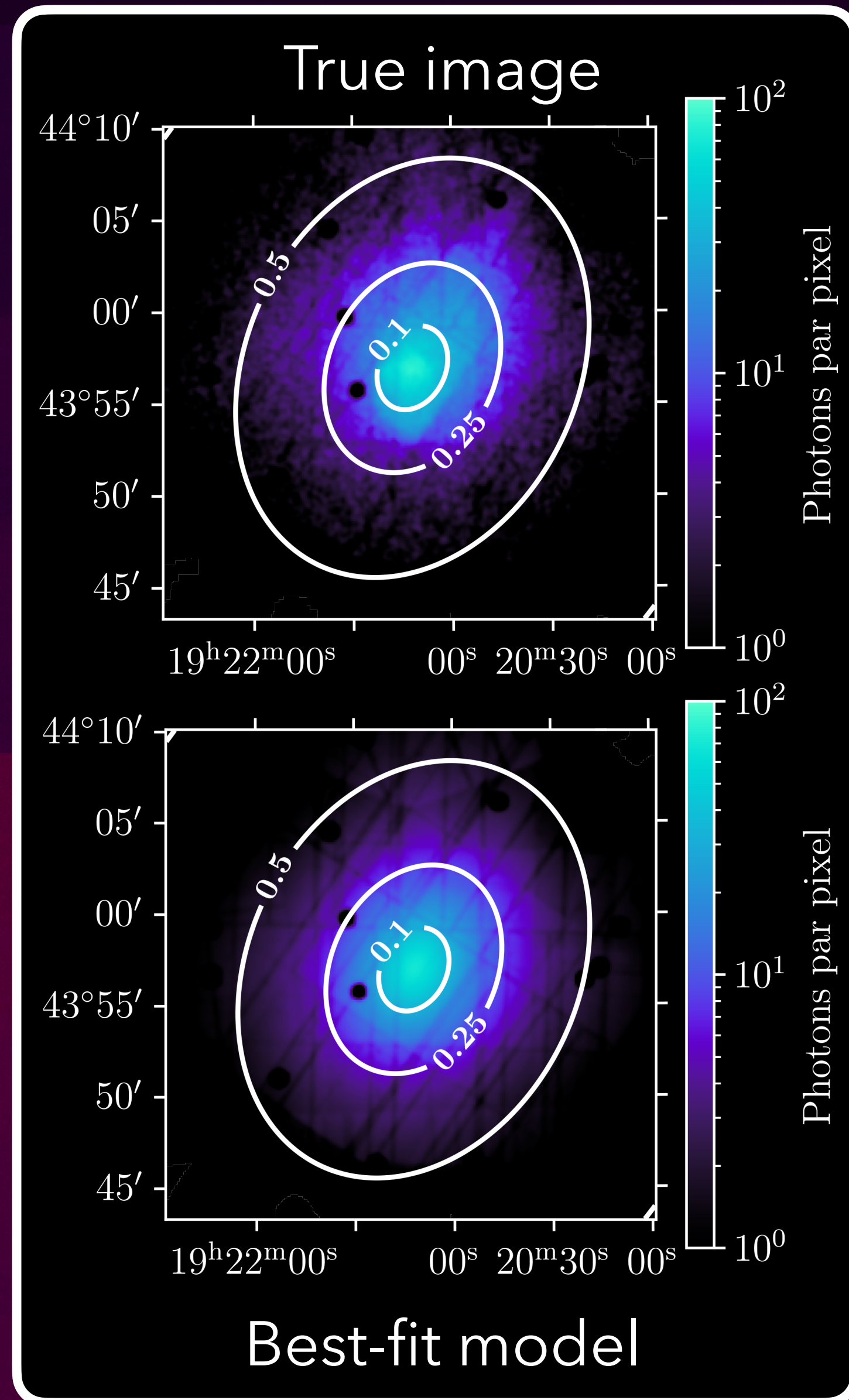
1. Gas motions induce thermodynamical fluctuations
2. Thermodynamical fluctuations translate in observable fluctuations (i.e. X-ray or SZ)
3. Correlations between the fluctuations and the gas motions are quantified with numerical simulations



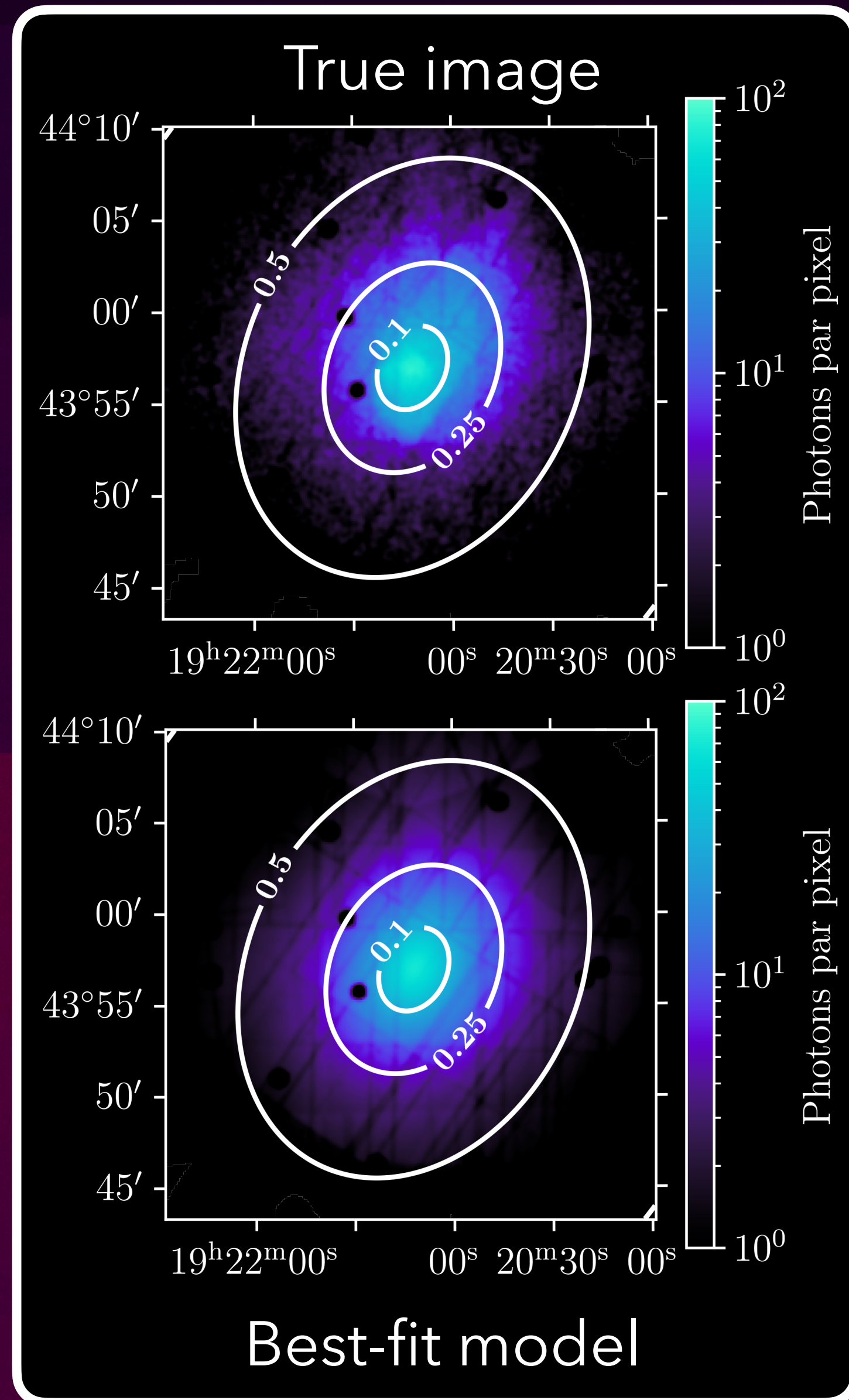
Probing the turbulent motion with fluctuations



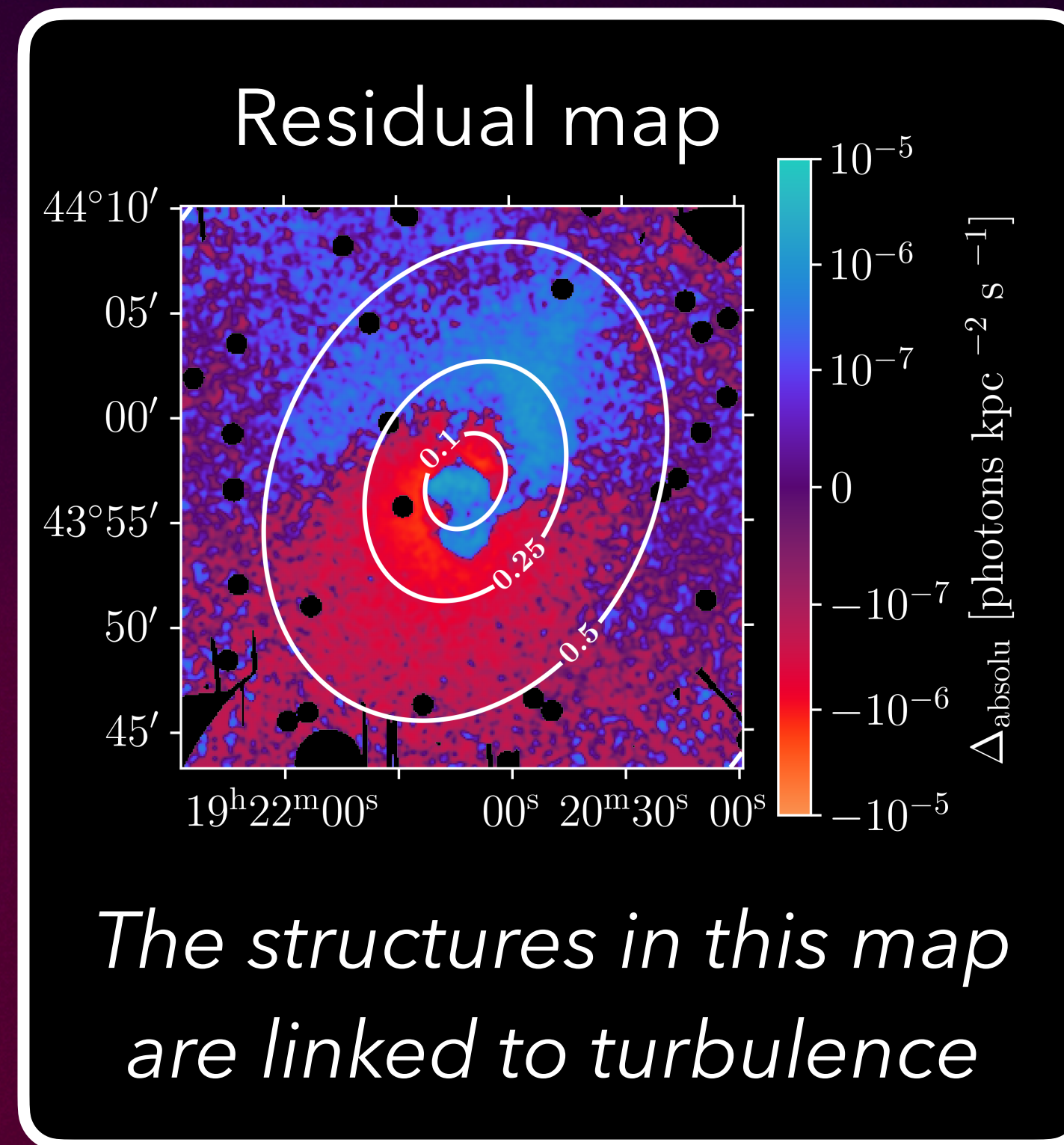
Probing the turbulent motion with fluctuations



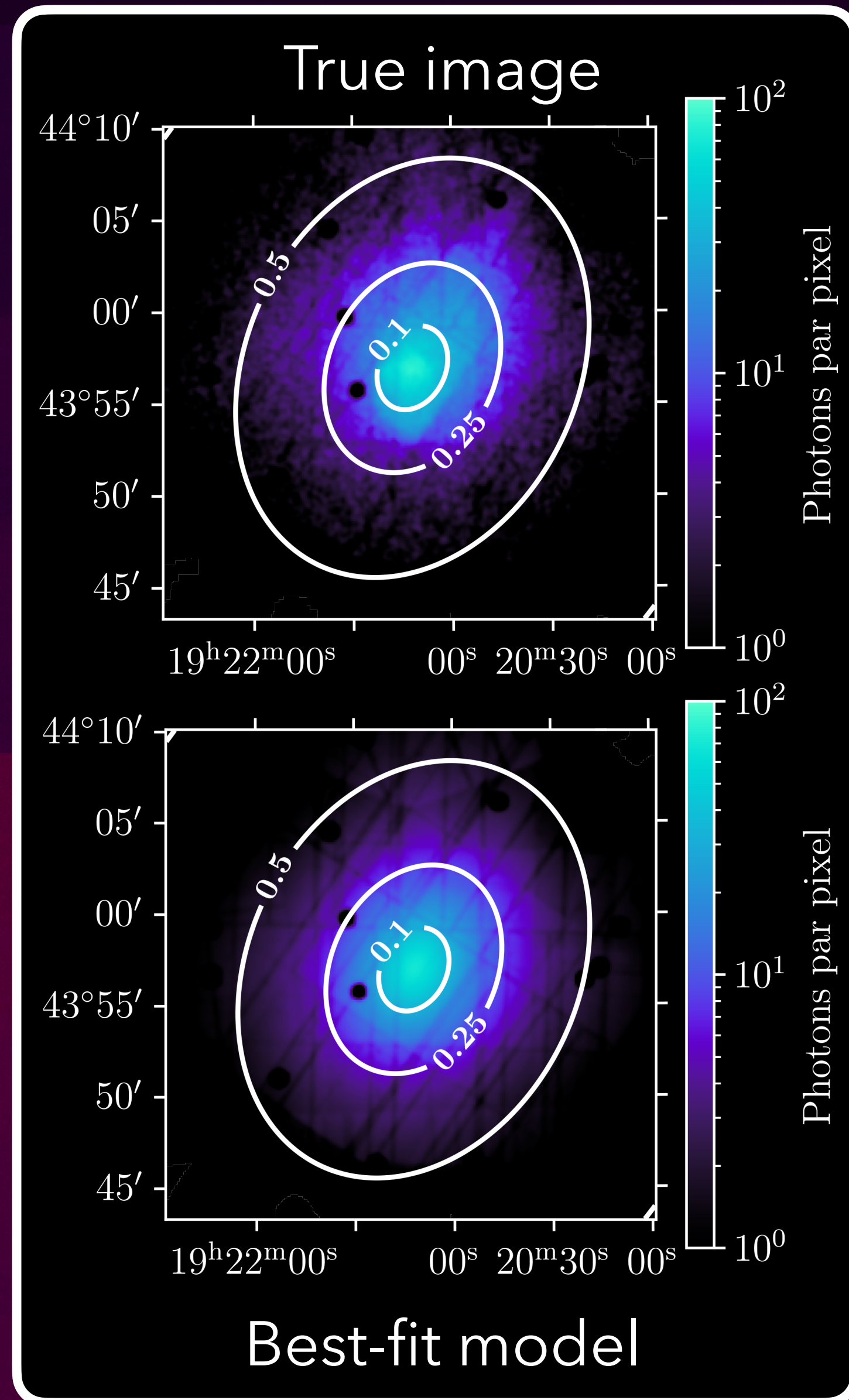
Probing the turbulent motion with fluctuations



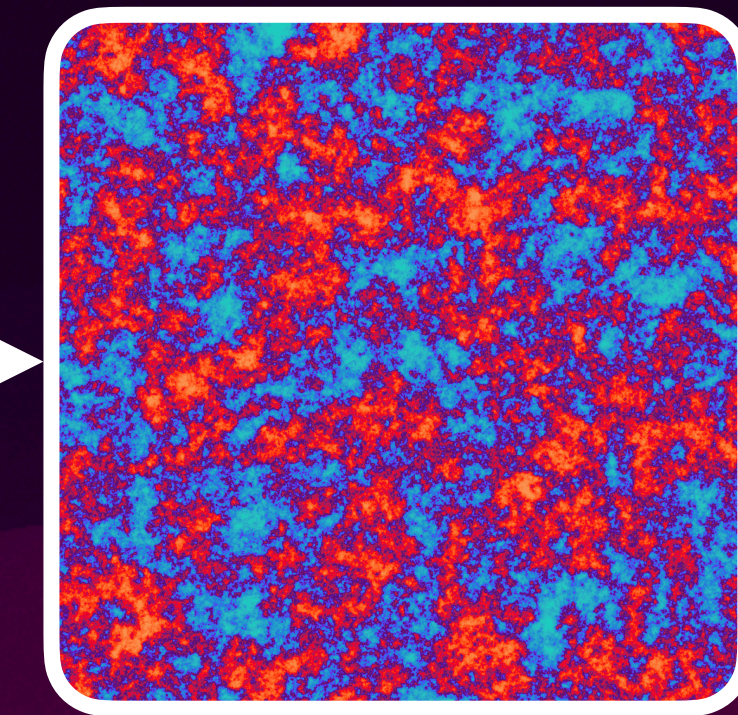
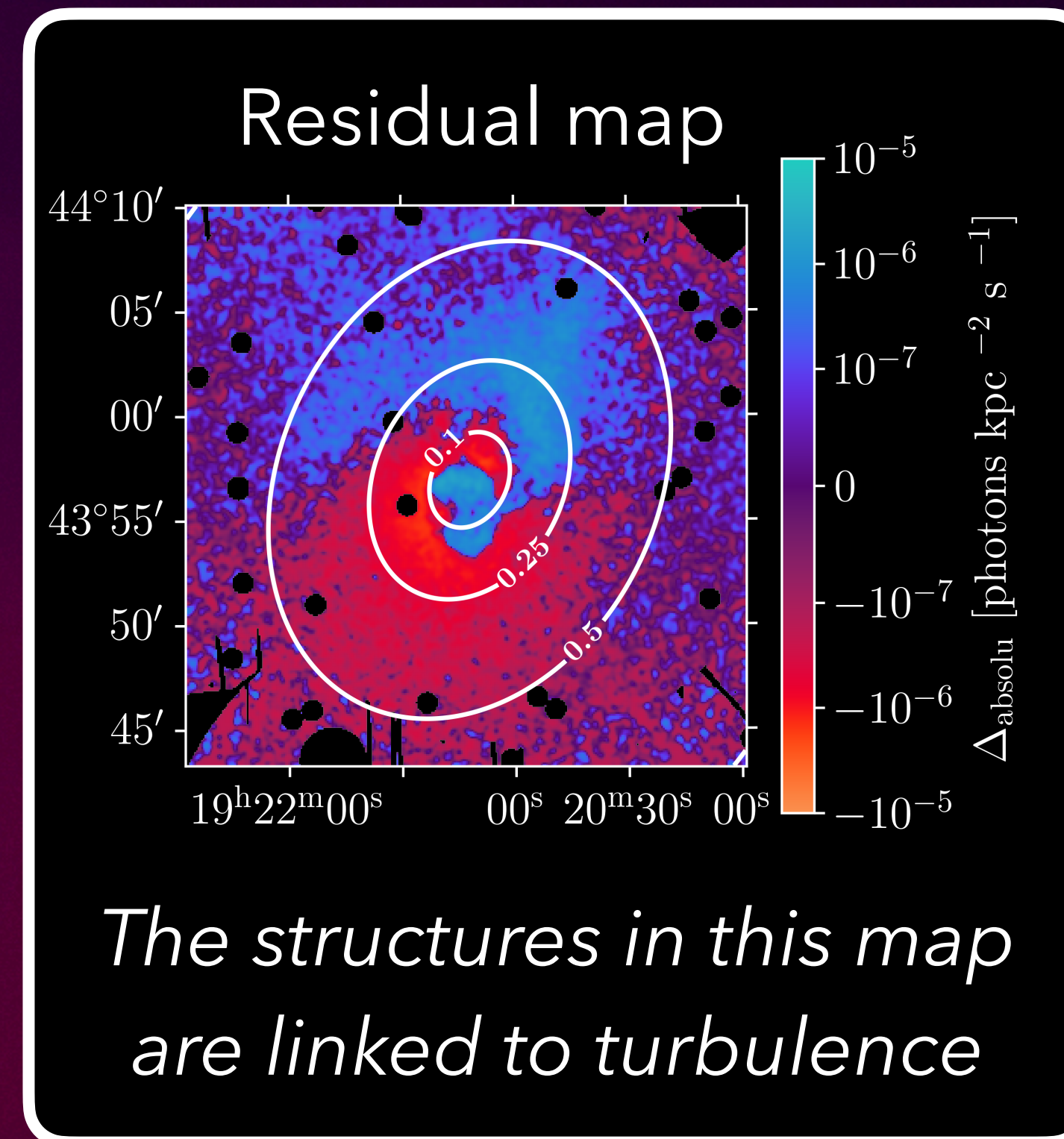
**Assume that fluctuations are a GRF
with Kolmogorov-like spectrum**



Probing the turbulent motion with fluctuations

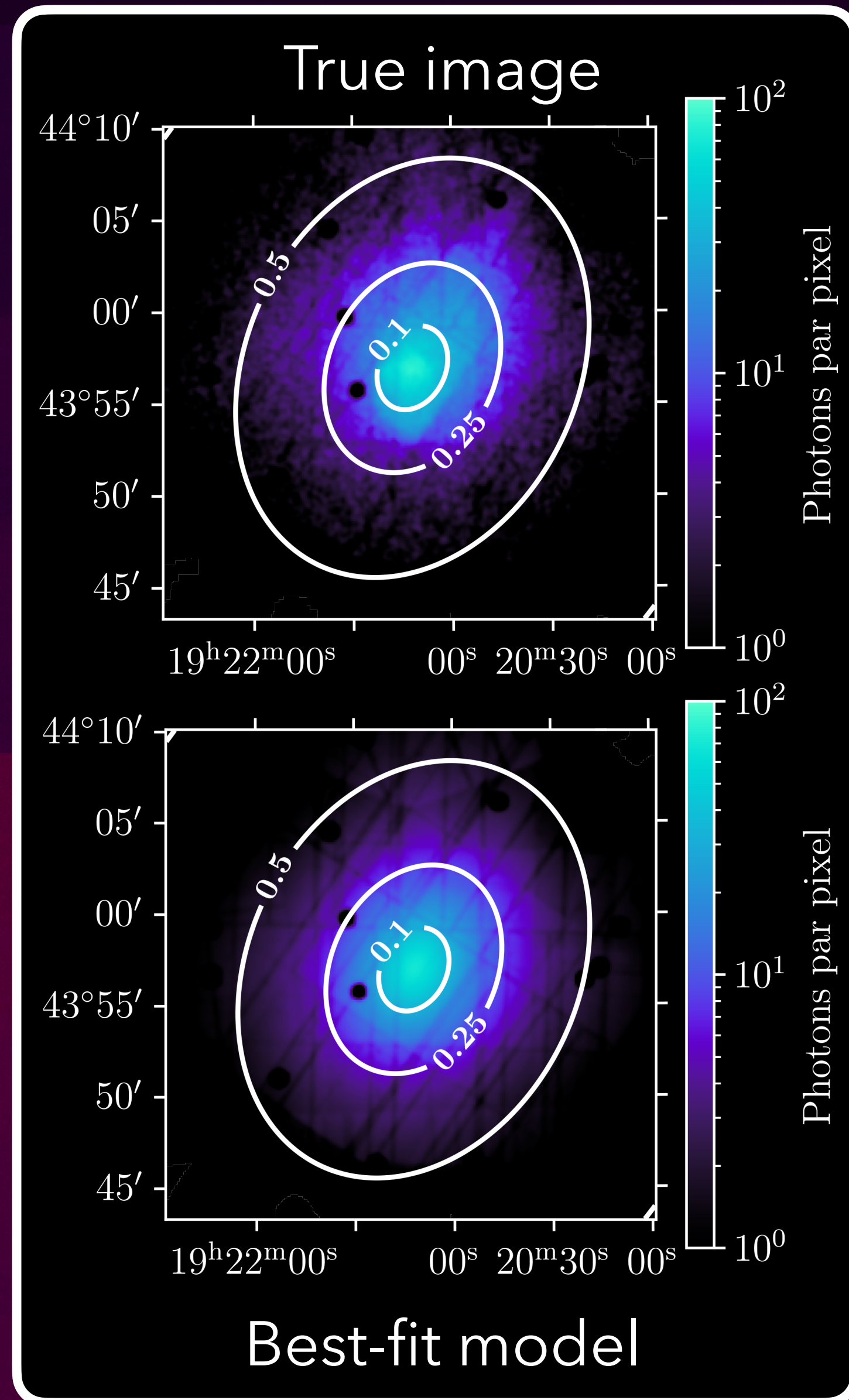


**Assume that fluctuations are a GRF
with Kolmogorov-like spectrum**

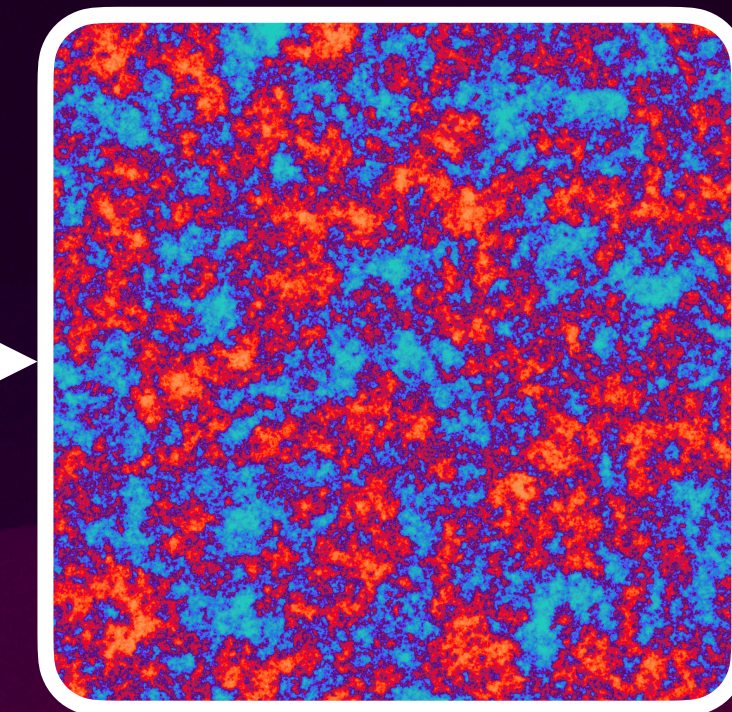
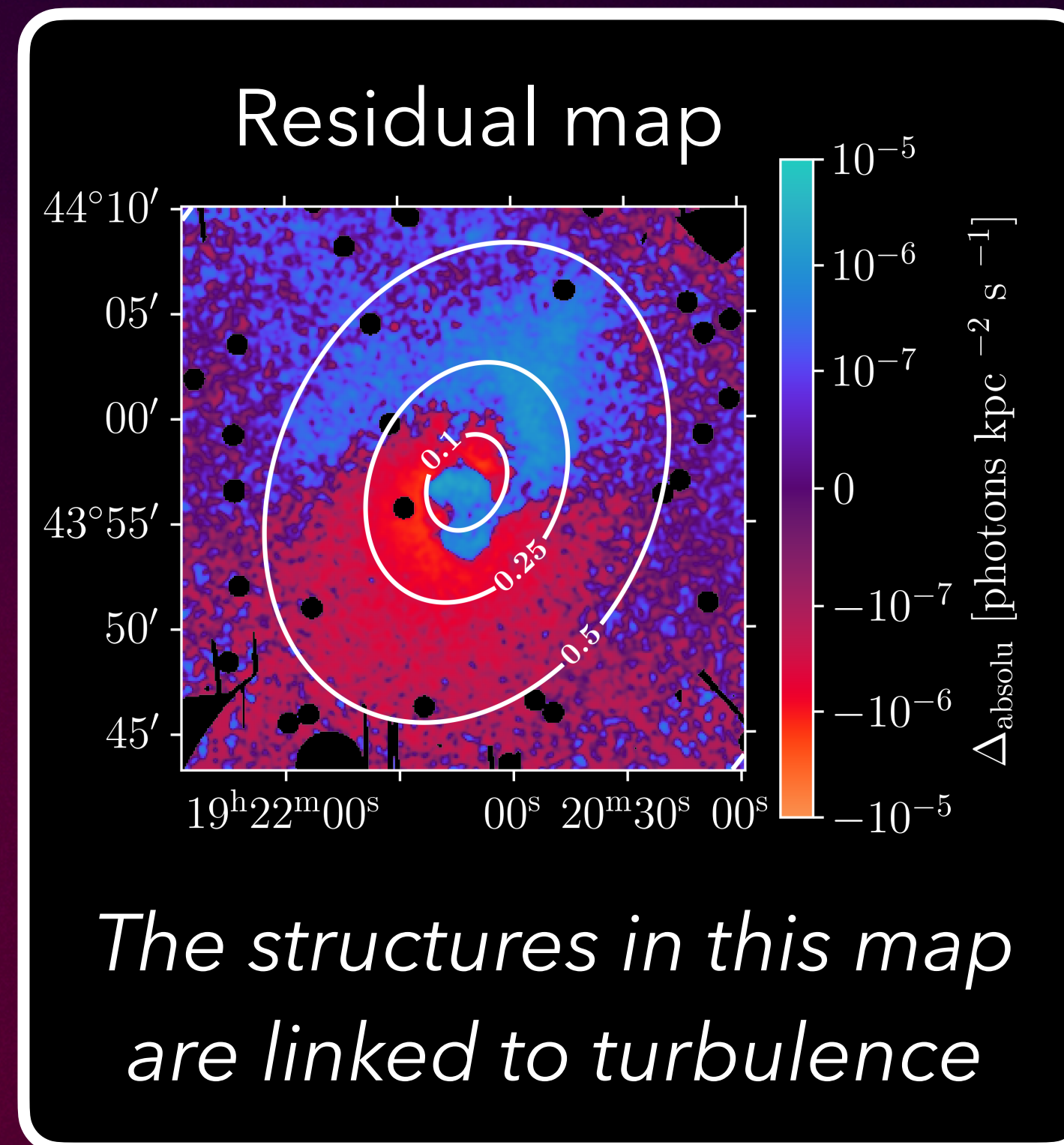


Mach number
→ hydrostatic
bias

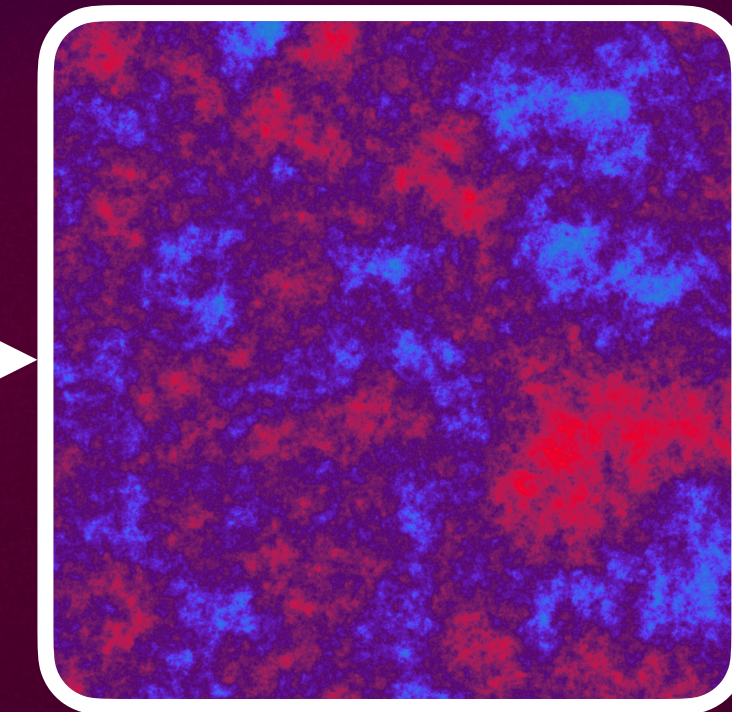
Probing the turbulent motion with fluctuations



**Assume that fluctuations are a GRF
with Kolmogorov-like spectrum**

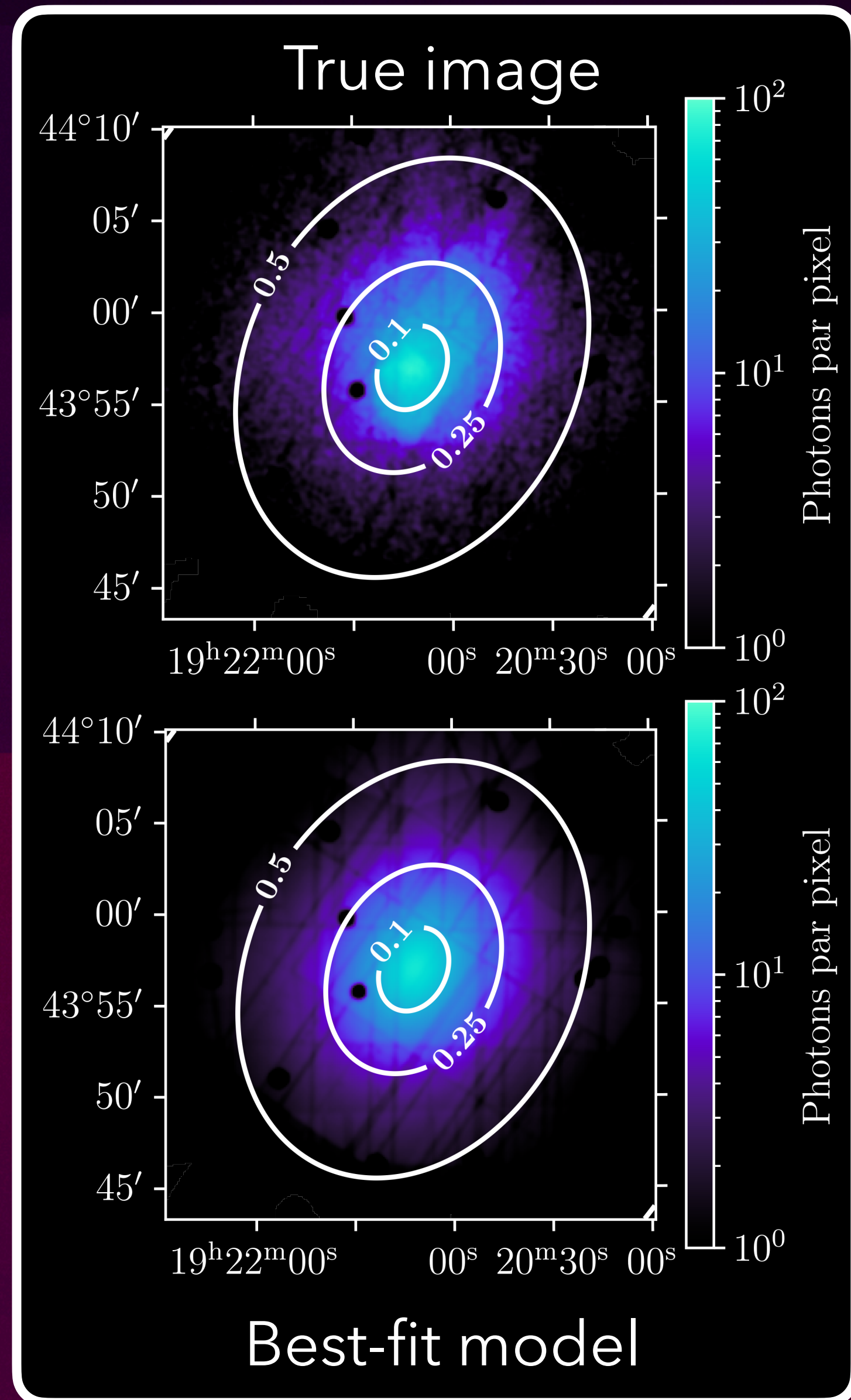


Mach number
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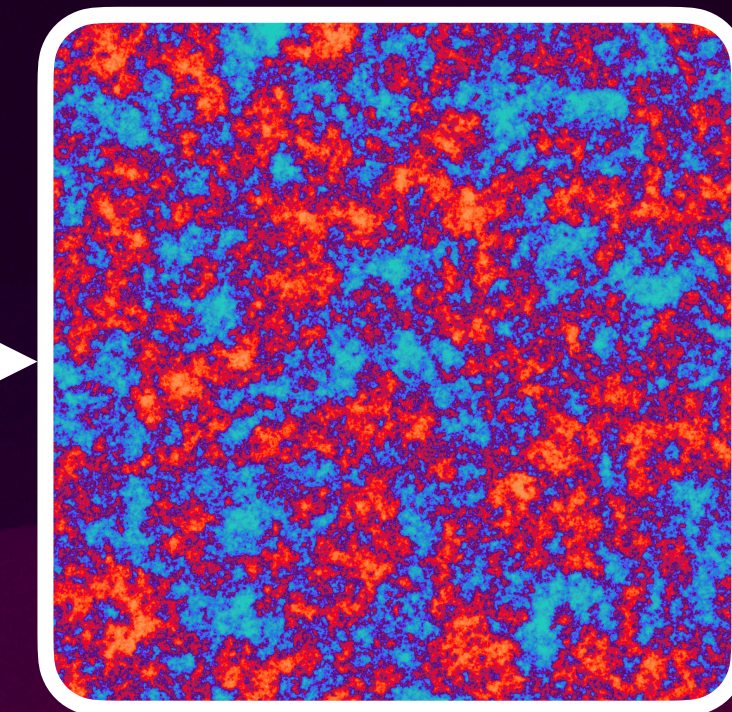
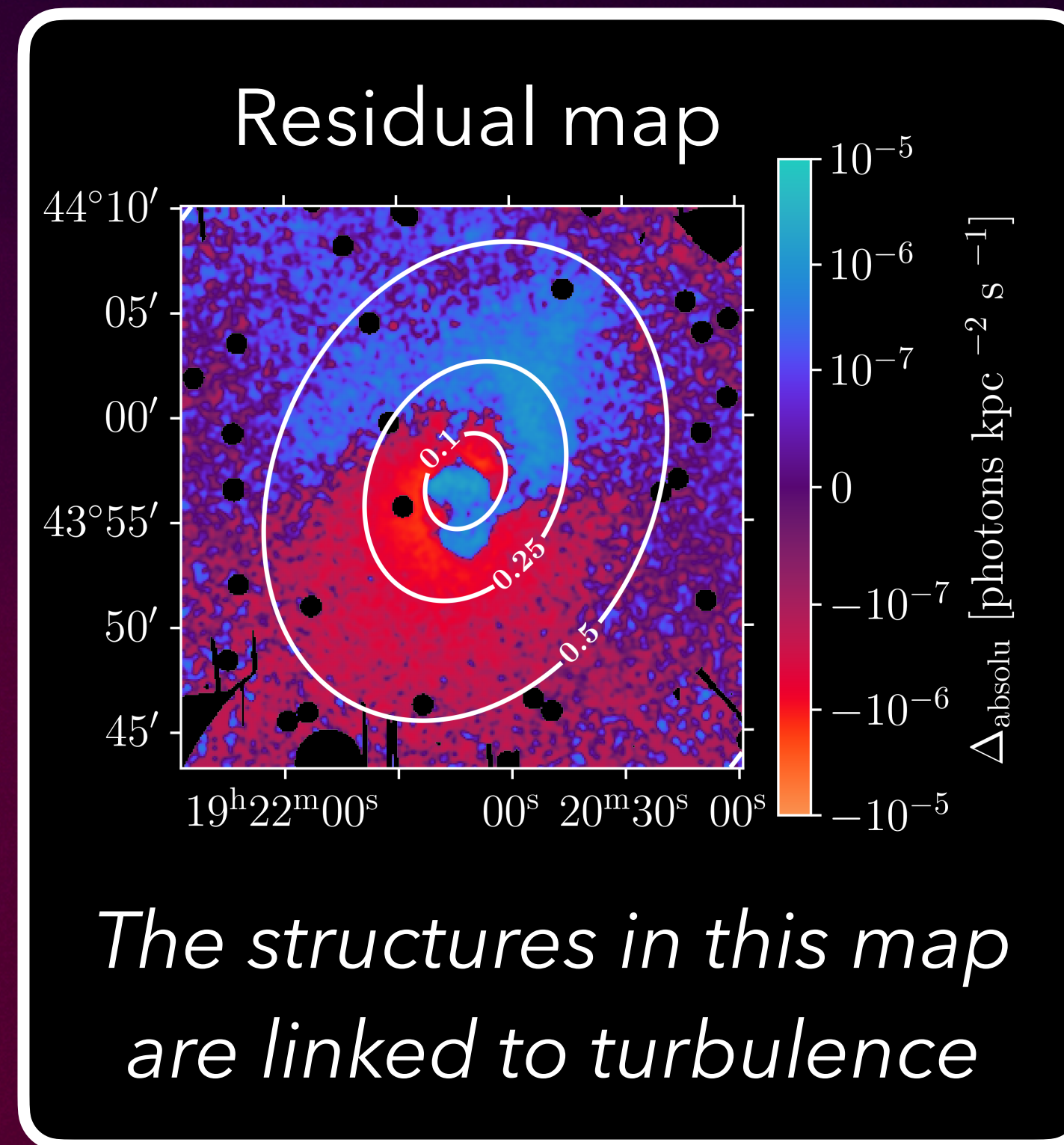


Injection scale
→ turbulence
driver

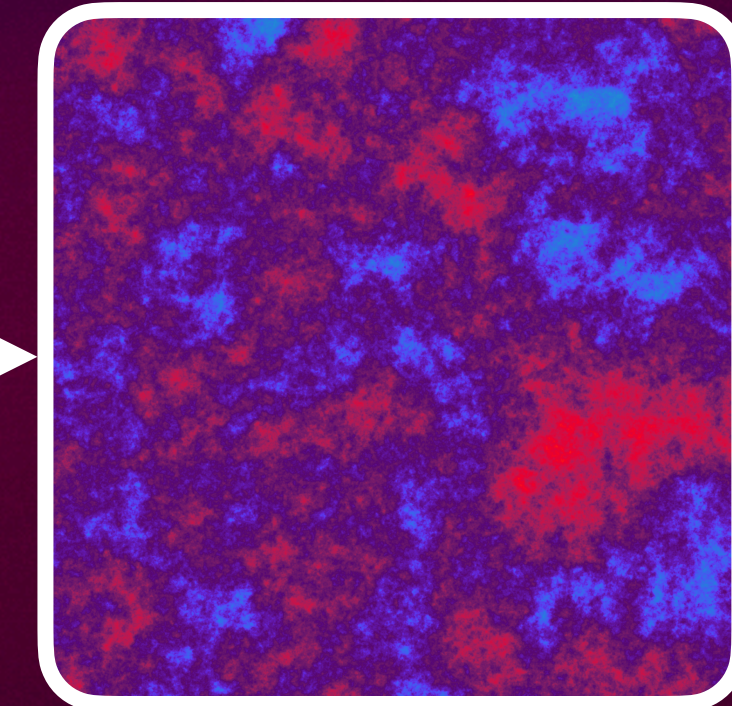
Probing the turbulent motion with fluctuations



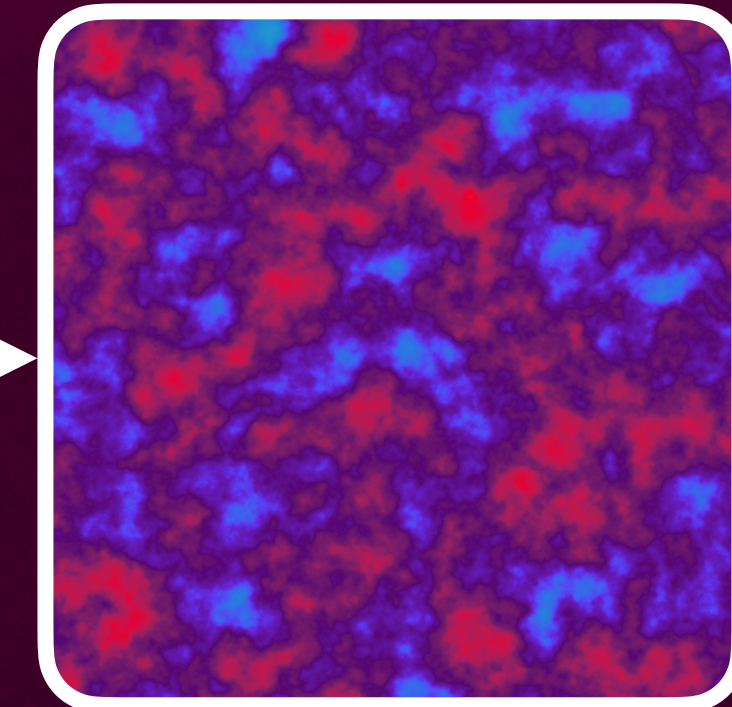
**Assume that fluctuations are a GRF
with Kolmogorov-like spectrum**



Mach number
→ hydrostatic
bias

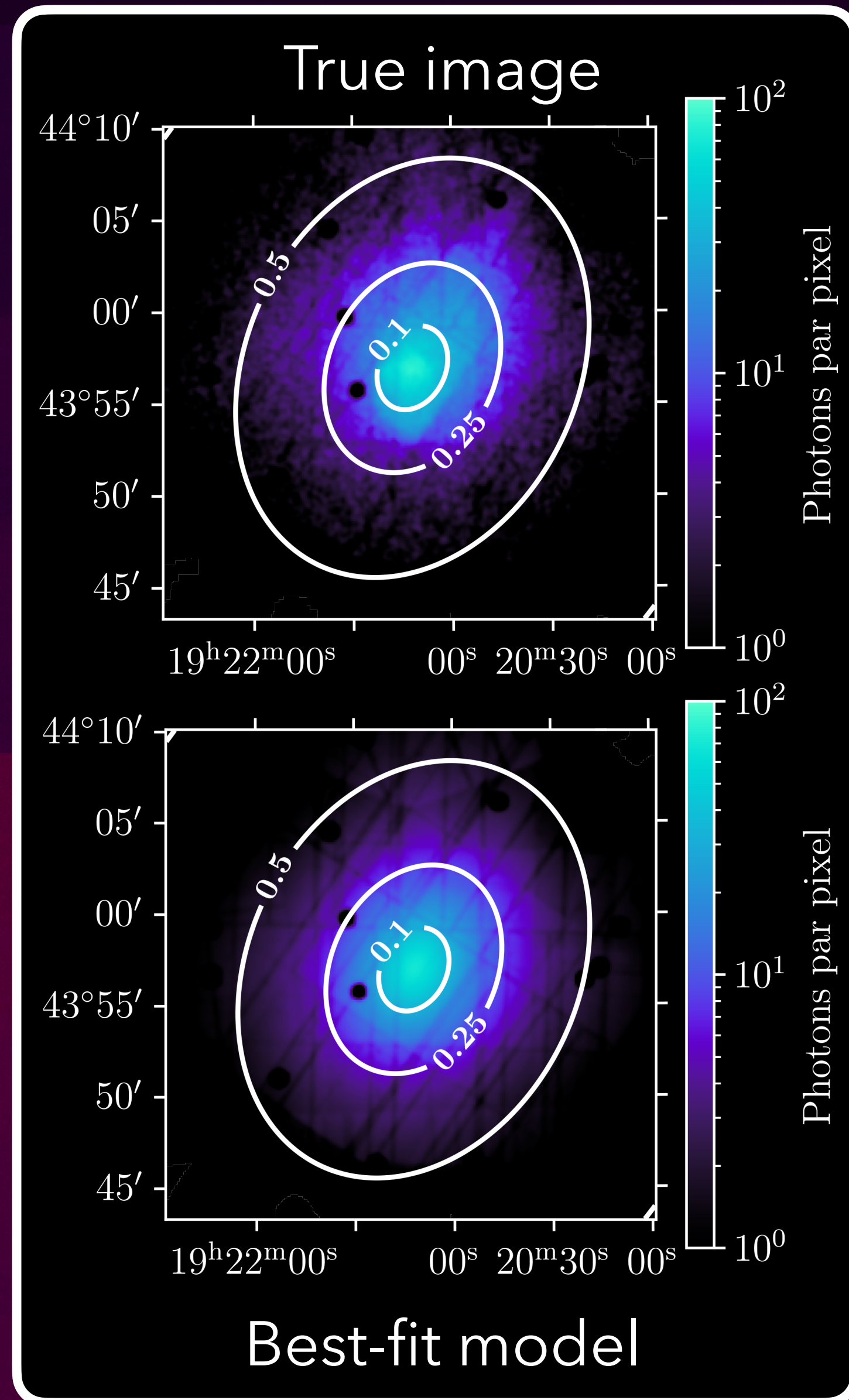


Injection scale
→ turbulence
driver

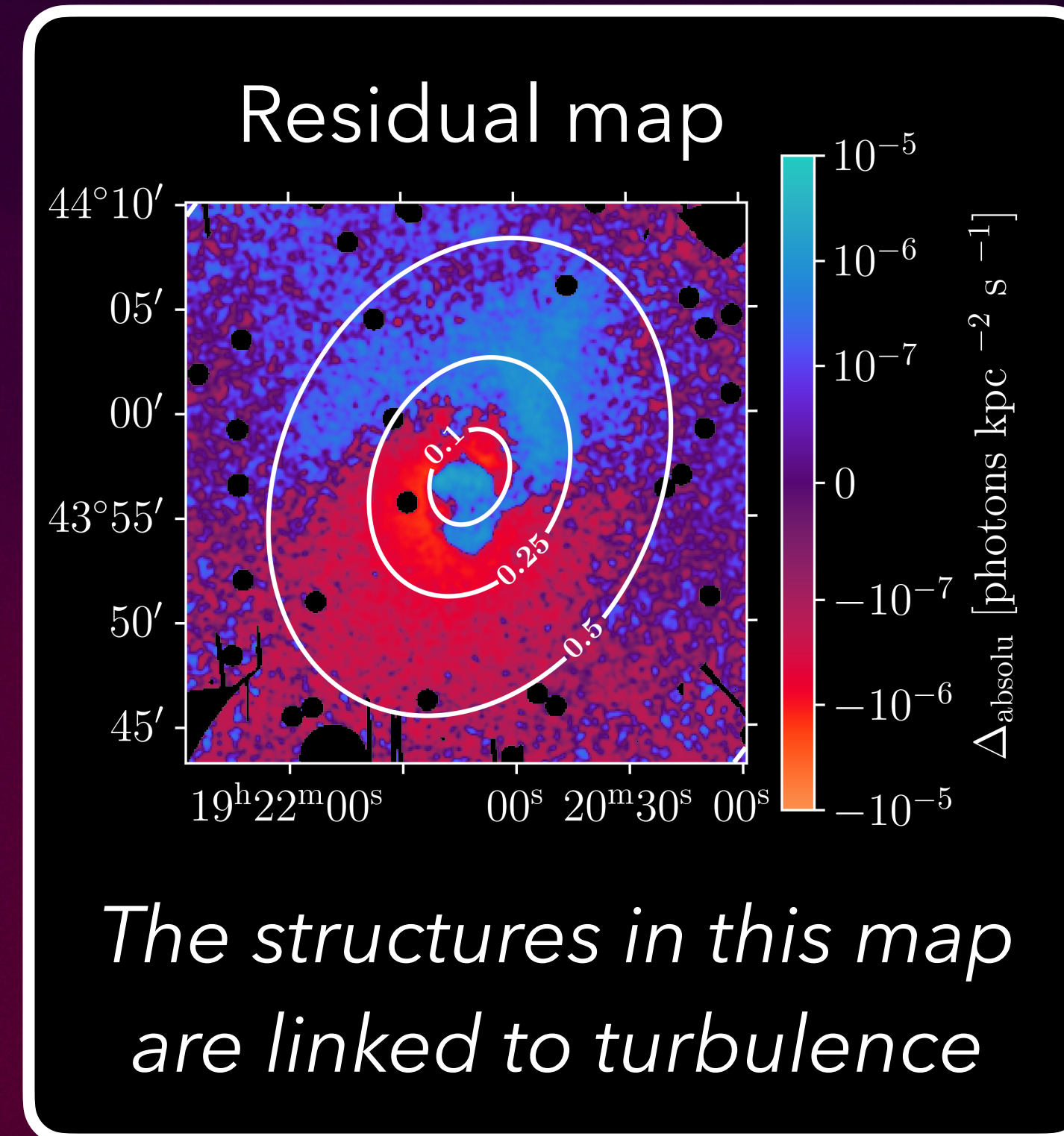


Cascading rate
→ gas physics

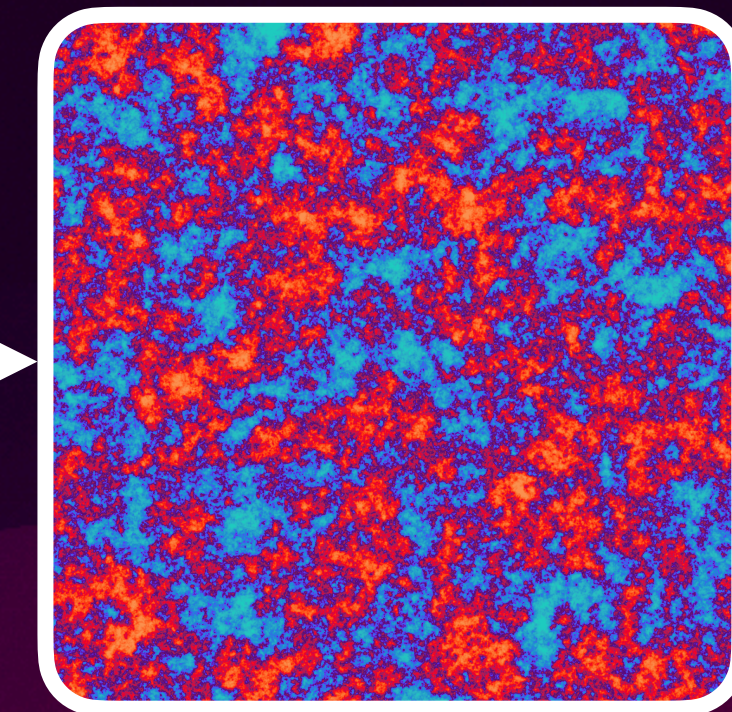
Probing the turbulent motion with fluctuations



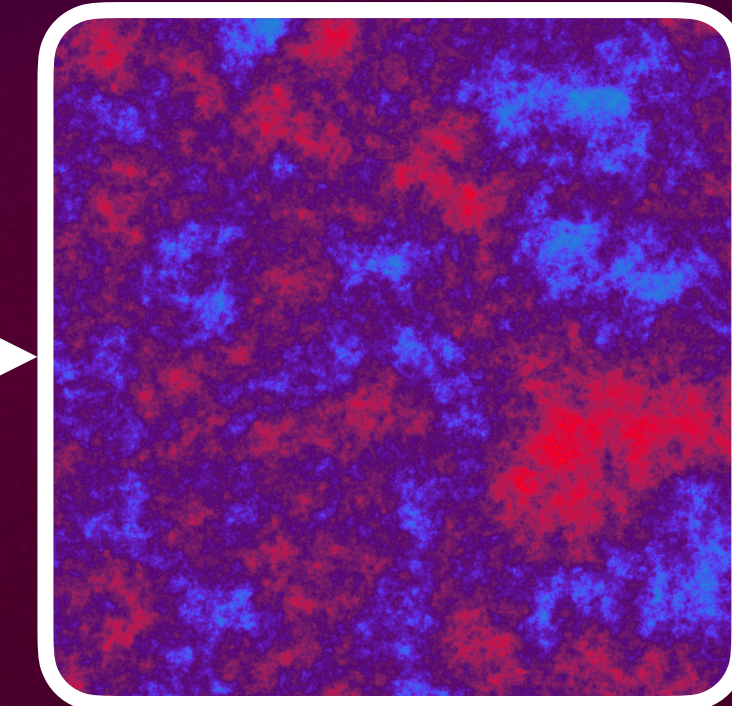
**Assume that fluctuations are a GRF
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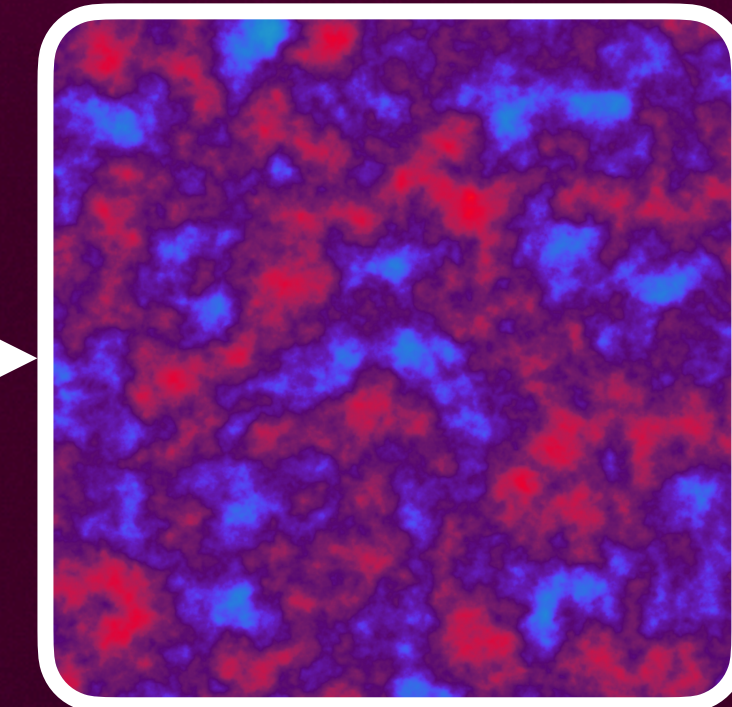
**No likelihood because of
sample variance (and masking)**



Mach number
→ hydrostatic
bias



Injection scale
→ turbulence
driver

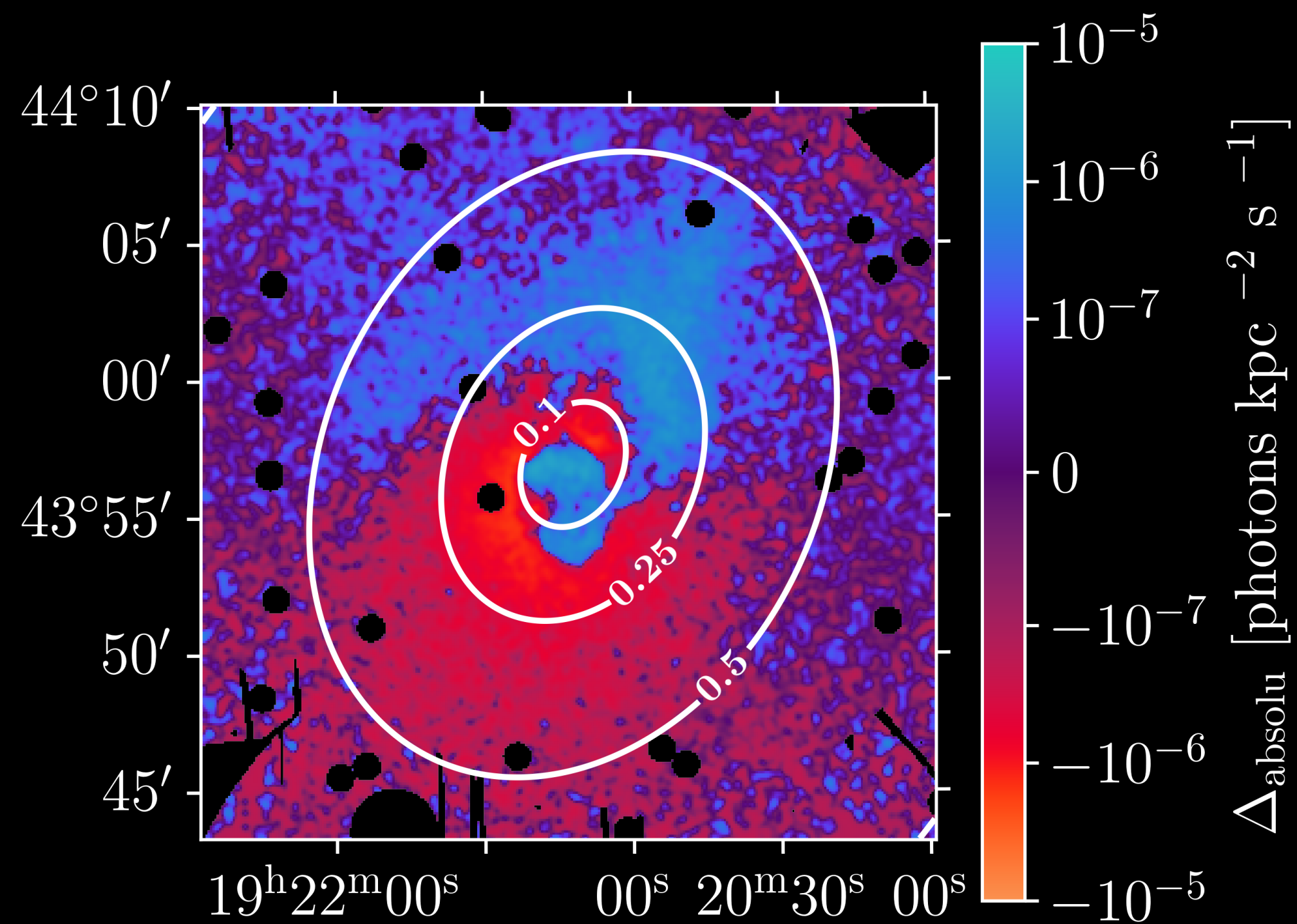


Cascading rate
→ gas physics

Crafting an observable for the fluctuation map

Crafting an observable for the fluctuation map

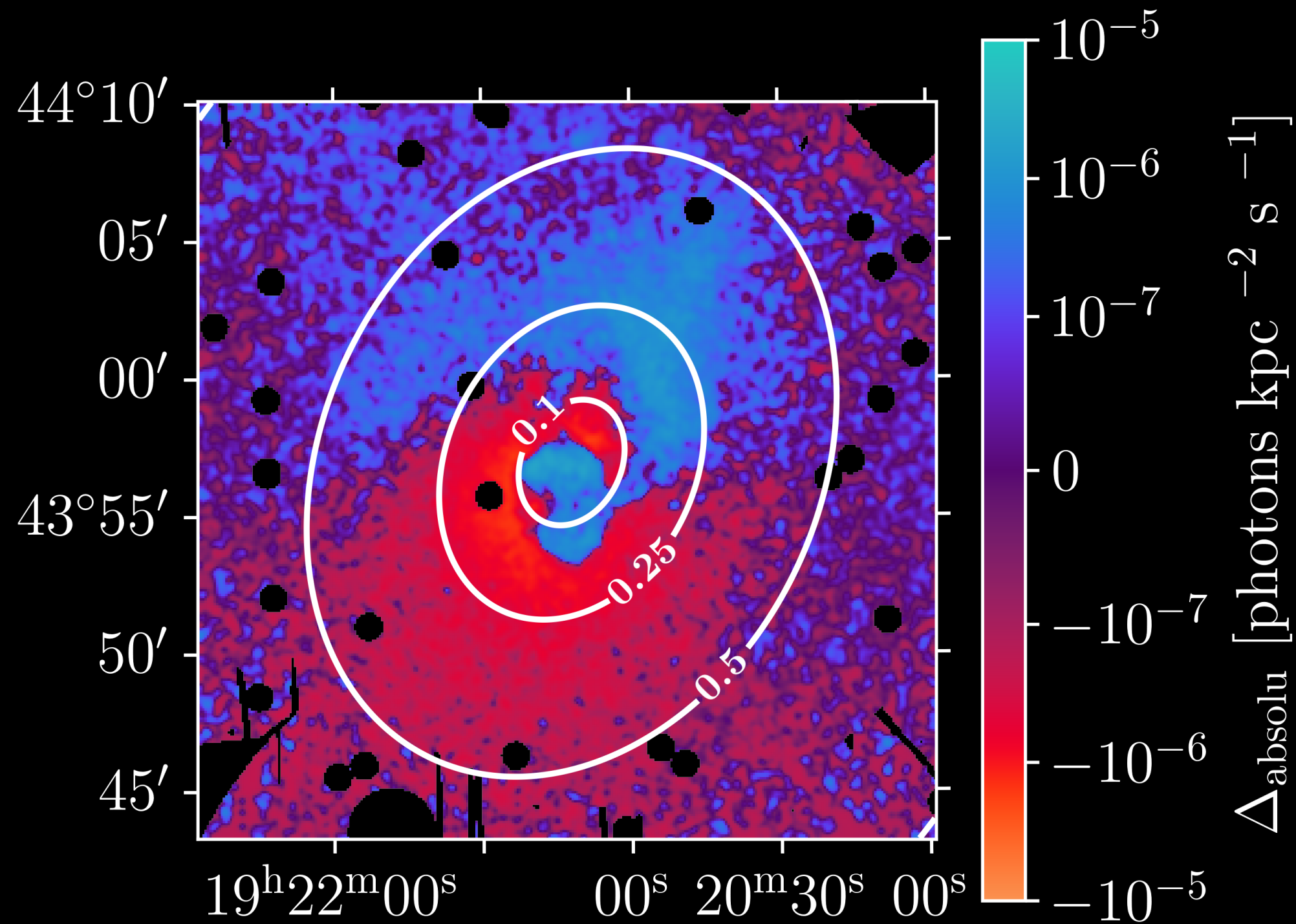
Residual map



- Low interpretability
- High-dimension

Crafting an observable for the fluctuation map

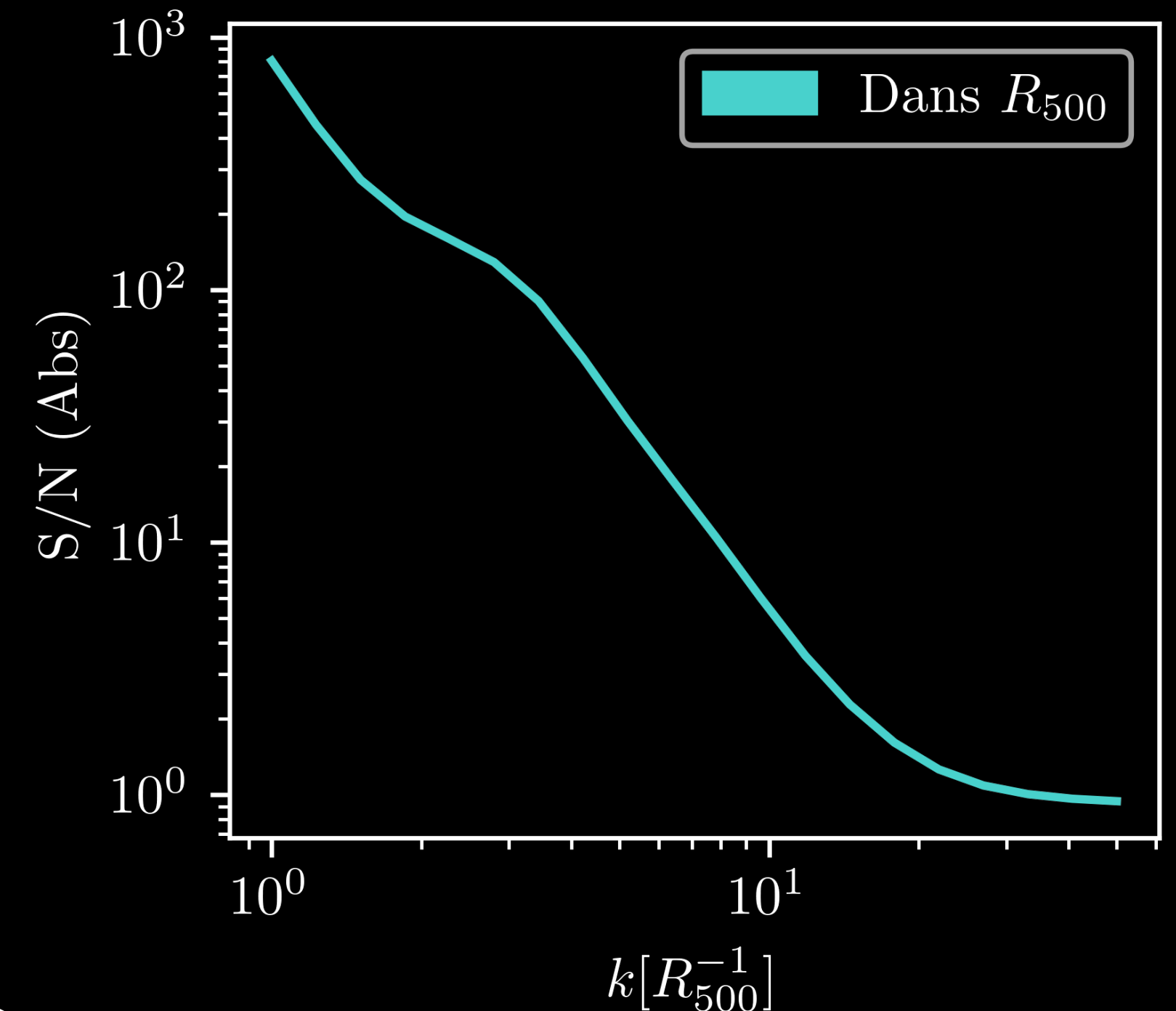
Residual map



Fourier transform
with Mexican Hats
(Arévalo + 2012)



Power spectrum (-ish)



- Low interpretability
- High-dimension

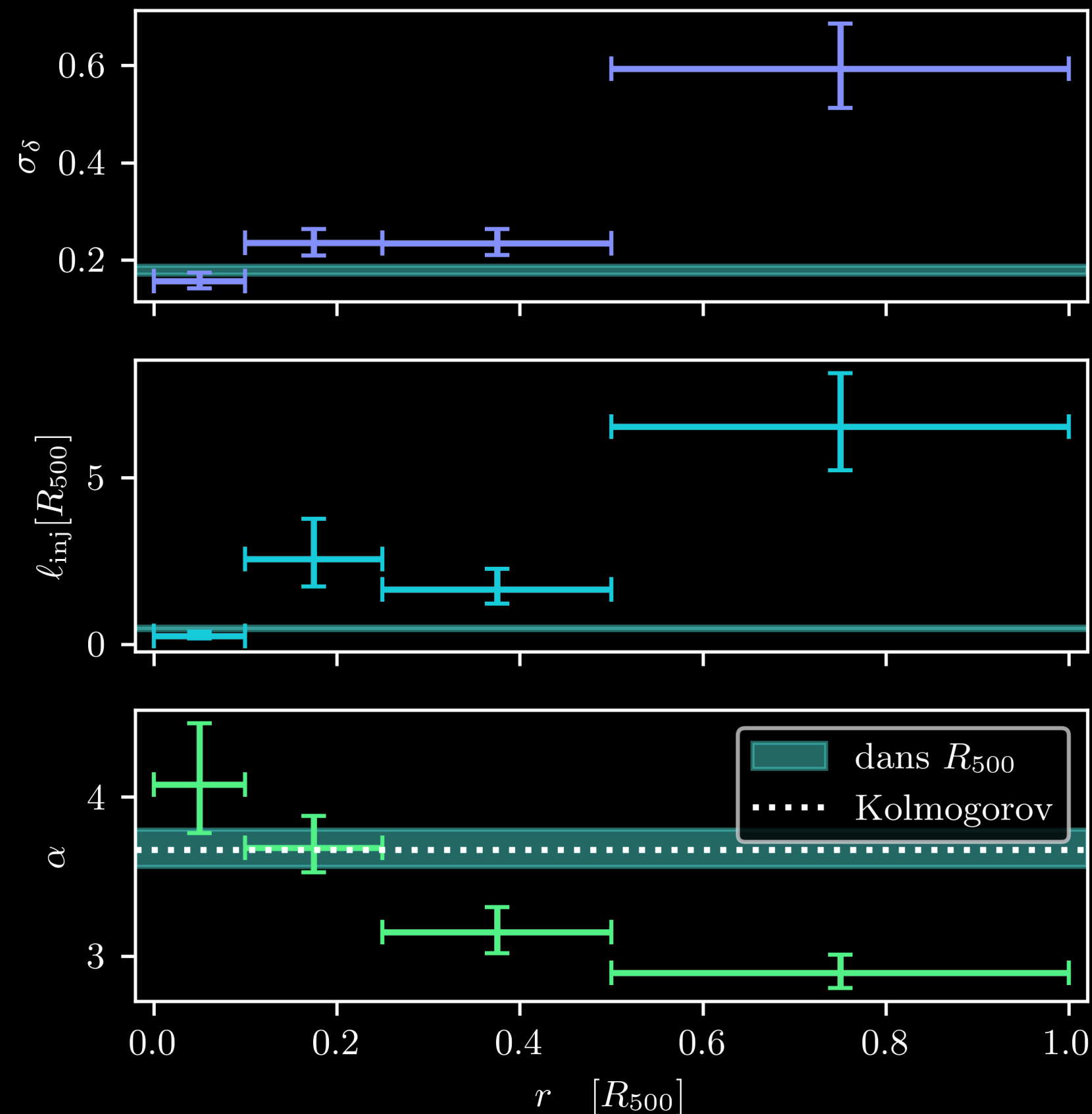
- High interpretability
- Low-dimension

- SBI can learn a likelihood function for many clusters using simulated fluctuation spectra
- Doing so, it automatically **marginalize** over the fluctuation variance
- These likelihoods can be combined to perform **survey over cluster samples**

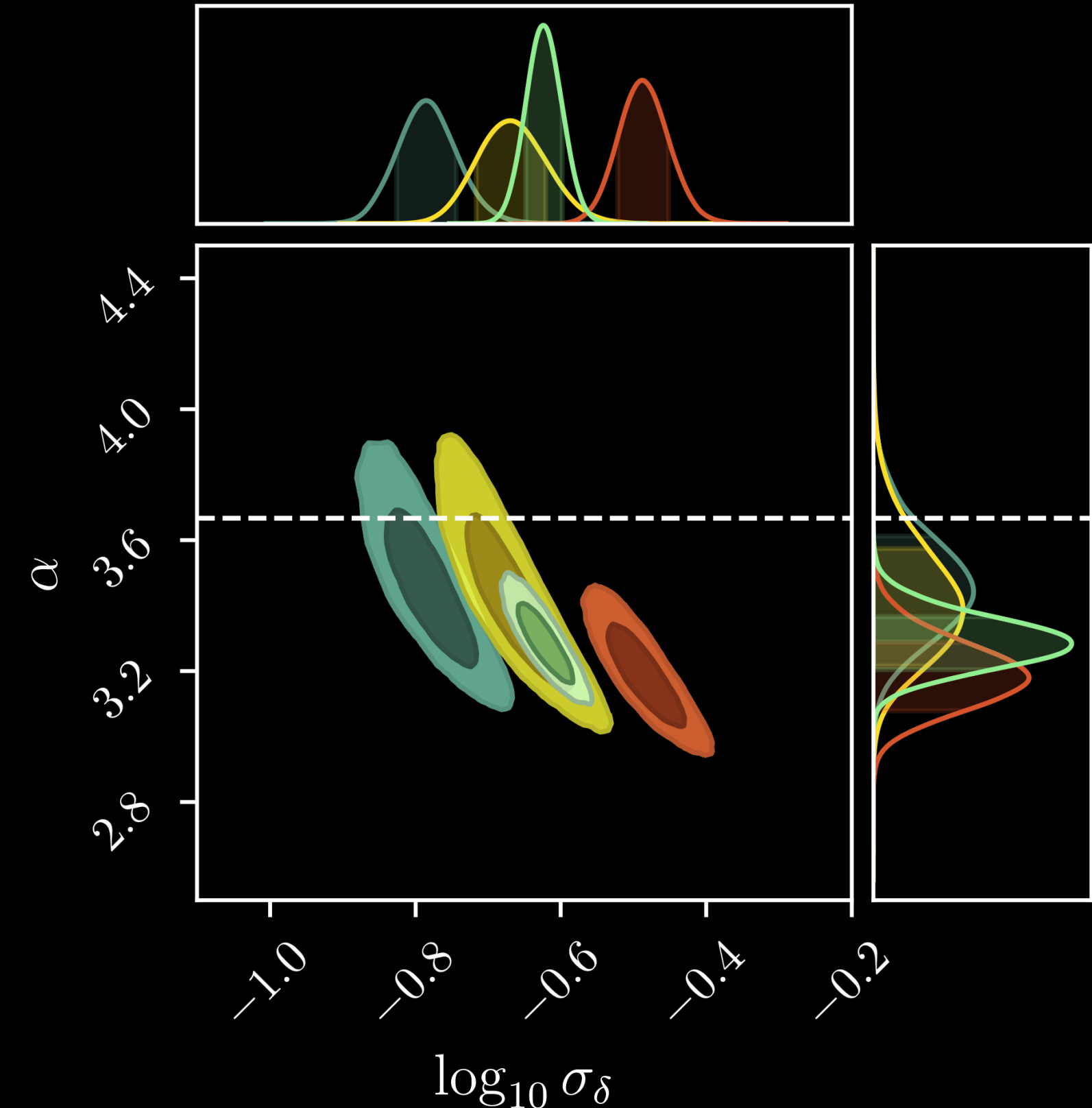
- SBI can learn a likelihood function for many clusters using simulated fluctuation spectra
- Doing so, it automatically **marginalize** over the fluctuation variance
- These likelihoods can be combined to perform **survey over cluster samples**

Apply it to two cluster samples

X-COP sample (N=12)



CHEX-MATE sample (N=118)



Openings on SBI & Clusters

- **Direct Observations**

- SBI has been successfully applied on true XRISM data in the Coma Cluster (Eckert & al 2025)
- X-IFU prospective analyses (see Alexei's talk!)

- **SZ Fluctuations**

- Work leaded by R. Adam on NIKA2 clusters (check PITSZI)
- Coma fluctuations with Planck revisited (B. Sigal)

Conclusions

SBI can solve inference problems where the likelihood is **intractable** while being **much faster** than regular inference. It turns inference problems in feature engineering problems.

Relevant use cases

- We achieved high-resolution spectroscopy with SBI using physically motivated summary statistics for the **X-ray spectra from XRISM/Resolve and new Athena/X-IFU**.
- We successfully used SBI to probe **turbulence in the ICM**. It enabled large scale study of the X-ray fluctuations in both the X-COP and CHEX-MATE cluster samples.

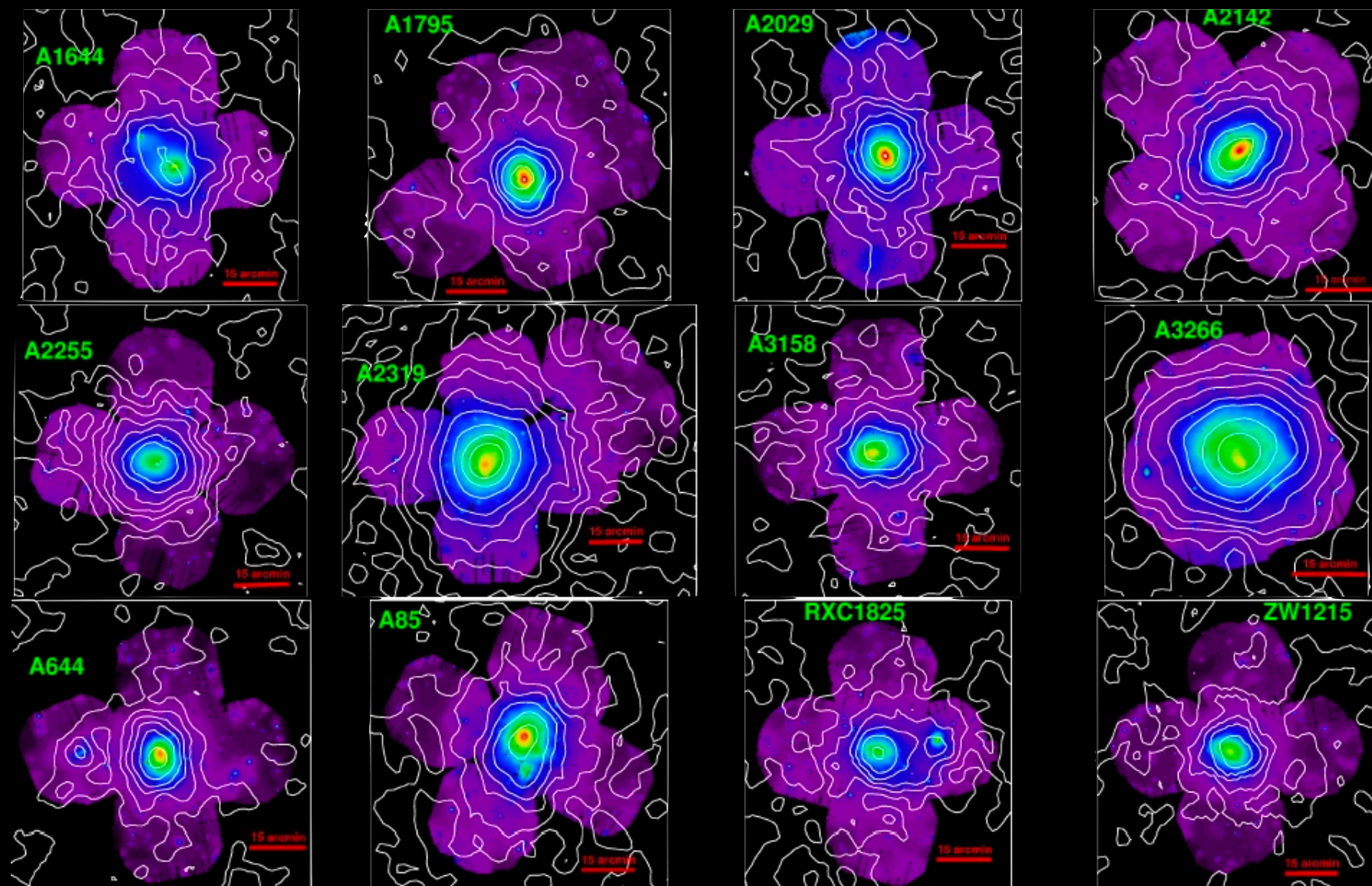
Backup

- SBI can learn a likelihood function using simulated fluctuation images
- Doing so, it automatically **marginalize** over the fluctuation variance
- These likelihoods can be combined to perform **survey over cluster samples**

- SBI can learn a likelihood function using simulated fluctuation images
- Doing so, it automatically **marginalize** over the fluctuation variance
- These likelihoods can be combined to perform **survey over cluster samples**

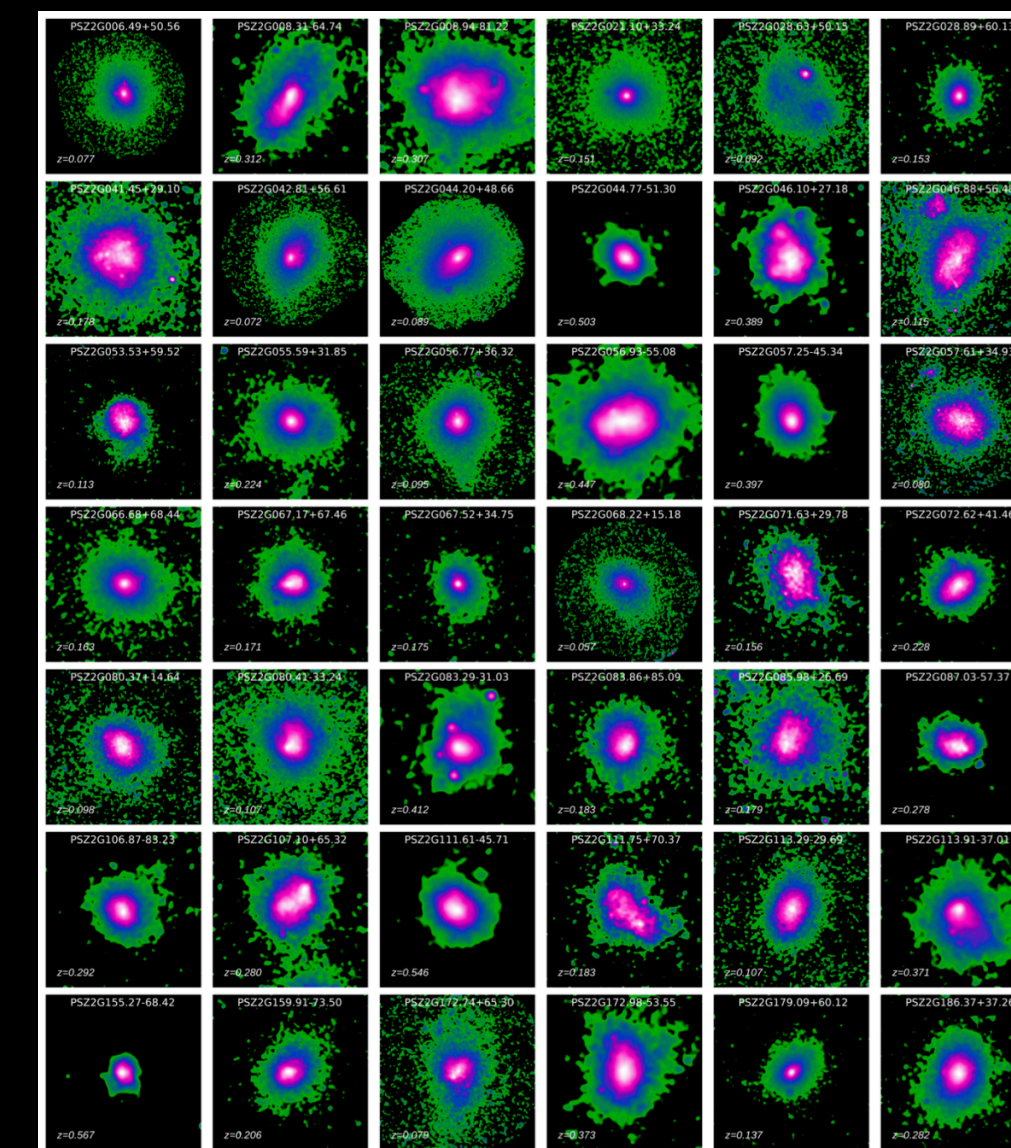
Apply it to two cluster samples

X-COP (Eckert & al. 2017)

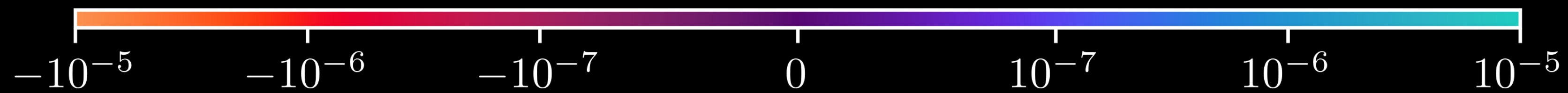
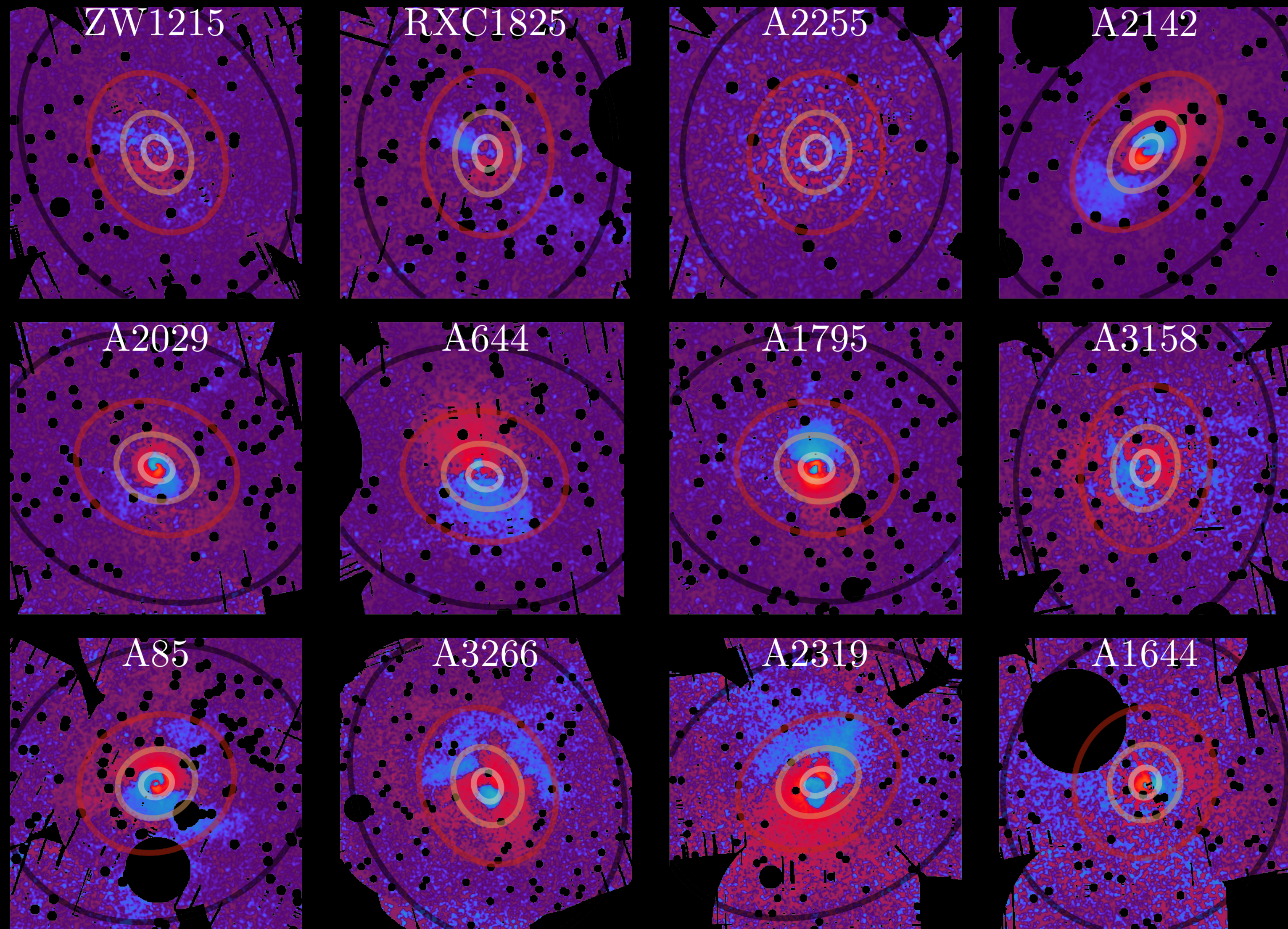


12 massive, nearby clusters observed
up to R_{200} ($z < 0.07$, $M \sim 10^{15} M_{\odot}$)

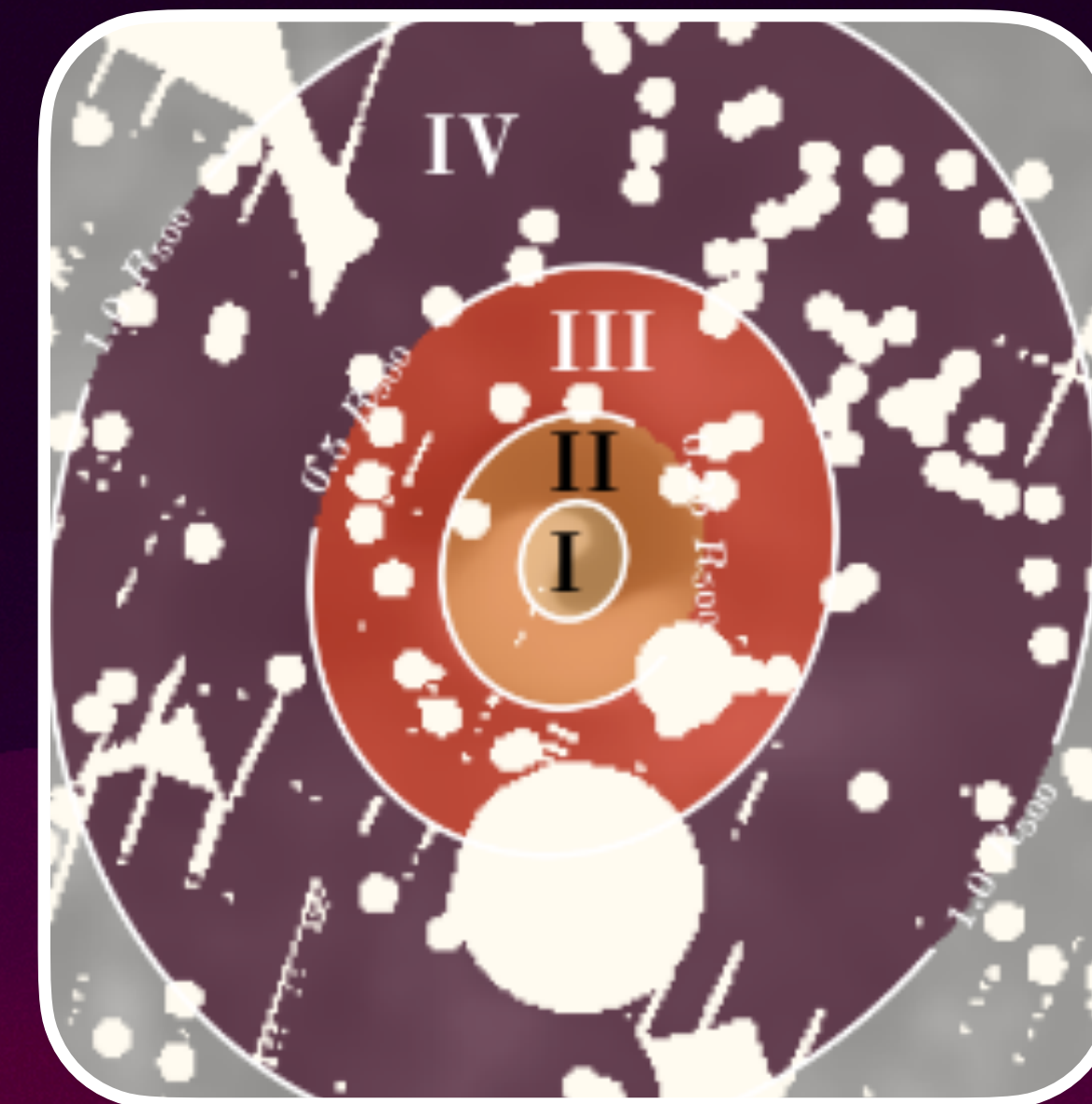
CHEX-MATE (CHEX-MATE Collaboration, 2021)



- 118 clusters in the local Universe
- Homogeneous measurements up to R_{500}
 $z < 0.6$,
 $[2 \sim 20] 10^{14} M_{\odot}$



Surface brightness fluctuations Δ [photons $\text{kpc}^{-2} \text{s}^{-1}$]

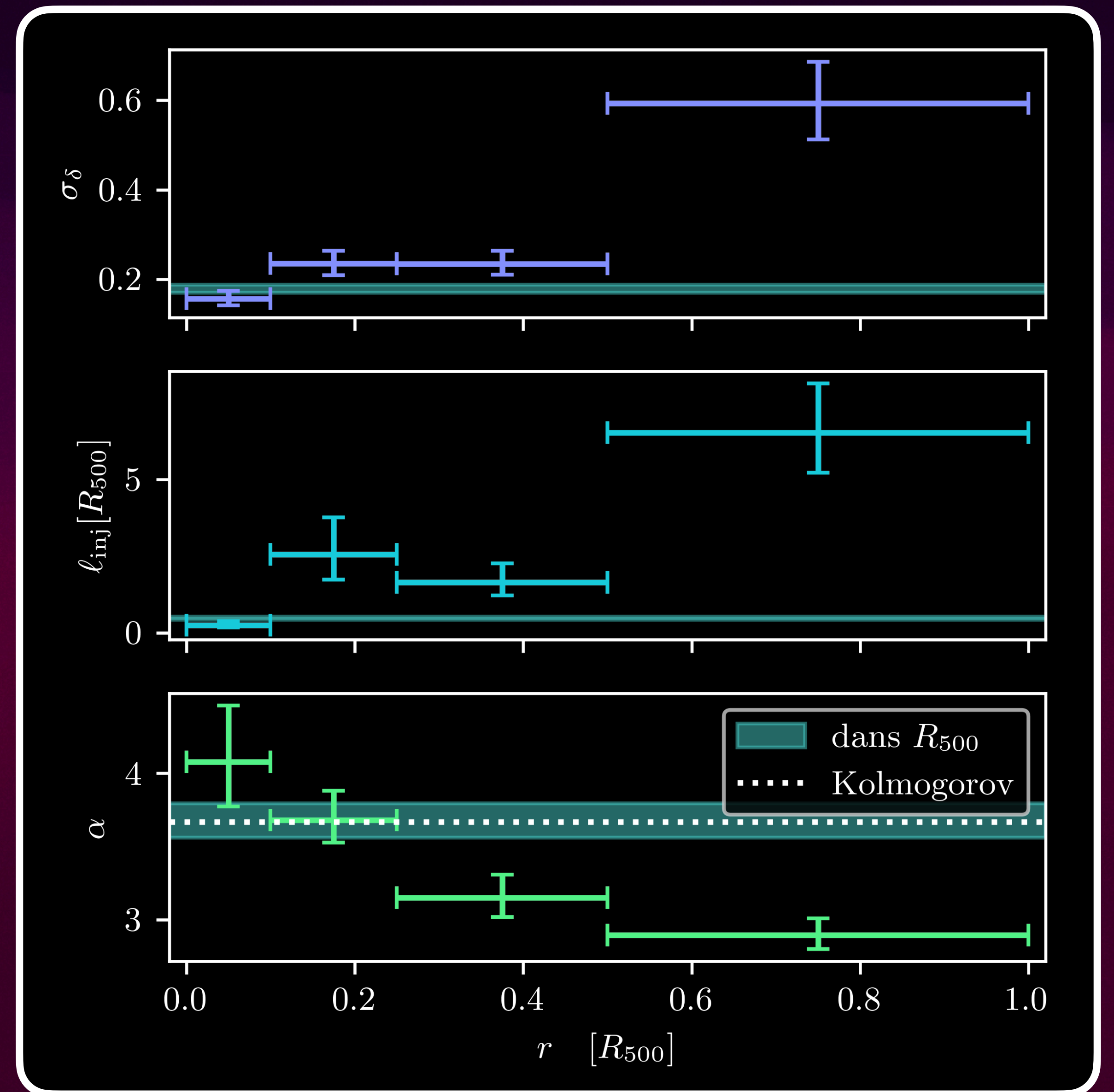


Region	Radius
(I)	$0 < r < R_{500}/10$
(II)	$R_{500}/10 < r < R_{500}/4$
(III)	$R_{500}/4 < r < R_{500}/2$
(IV)	$R_{500}/2 < r < R_{500}$

Split the analysis in 4 regions

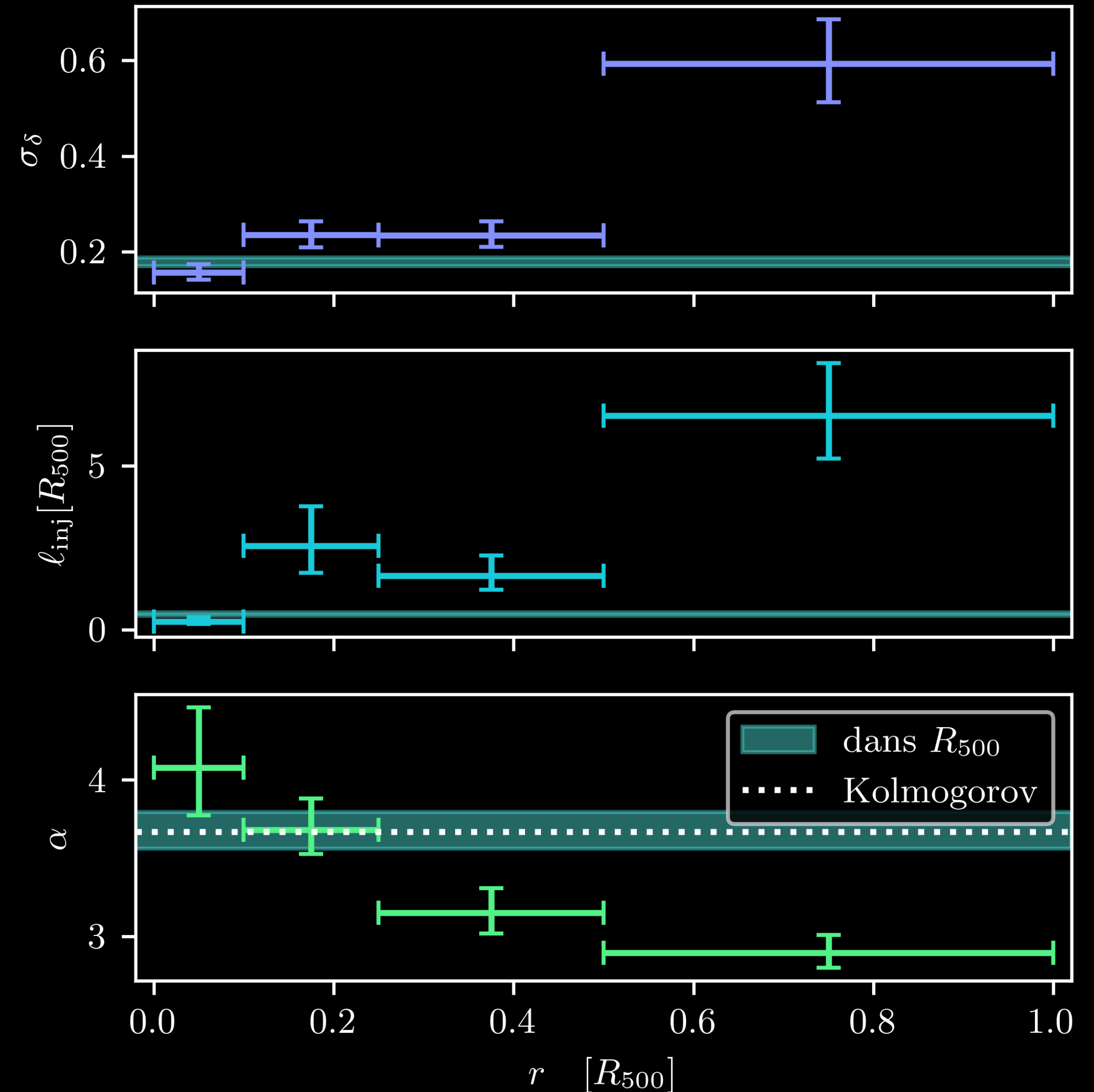
Radial evolution in X-COP

Radial evolution in X-COP



Radial evolution in X-COP

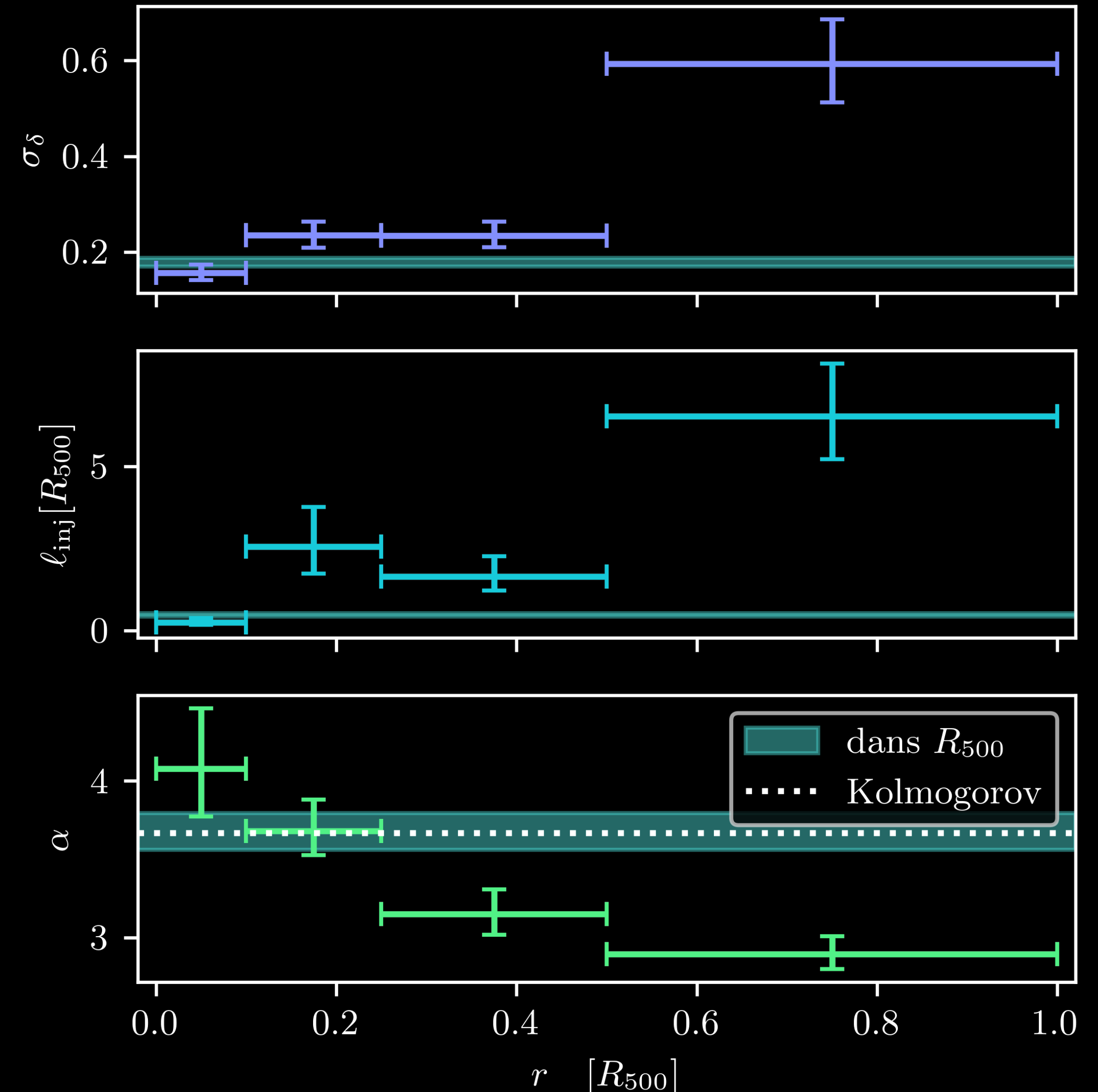
- **Profile** : the normalisation increases with radius \rightarrow the overall disturbance increases in external regions
- **Global** : $\mathcal{M} \sim 0.1$, subsonic



Radial evolution in X-COP

- **Profile** : the normalisation increases with radius \rightarrow the overall disturbance increases in external regions
- **Global** : $\mathcal{M} \sim 0.1$, subsonic

- **Profile** : the injection scale increases with radius \rightarrow transition between feedback, sloshing and merging
- **Global** : dominated by central region



Radial evolution in X-COP

- **Profile** : the normalisation increases with radius \rightarrow the overall disturbance increases in external regions

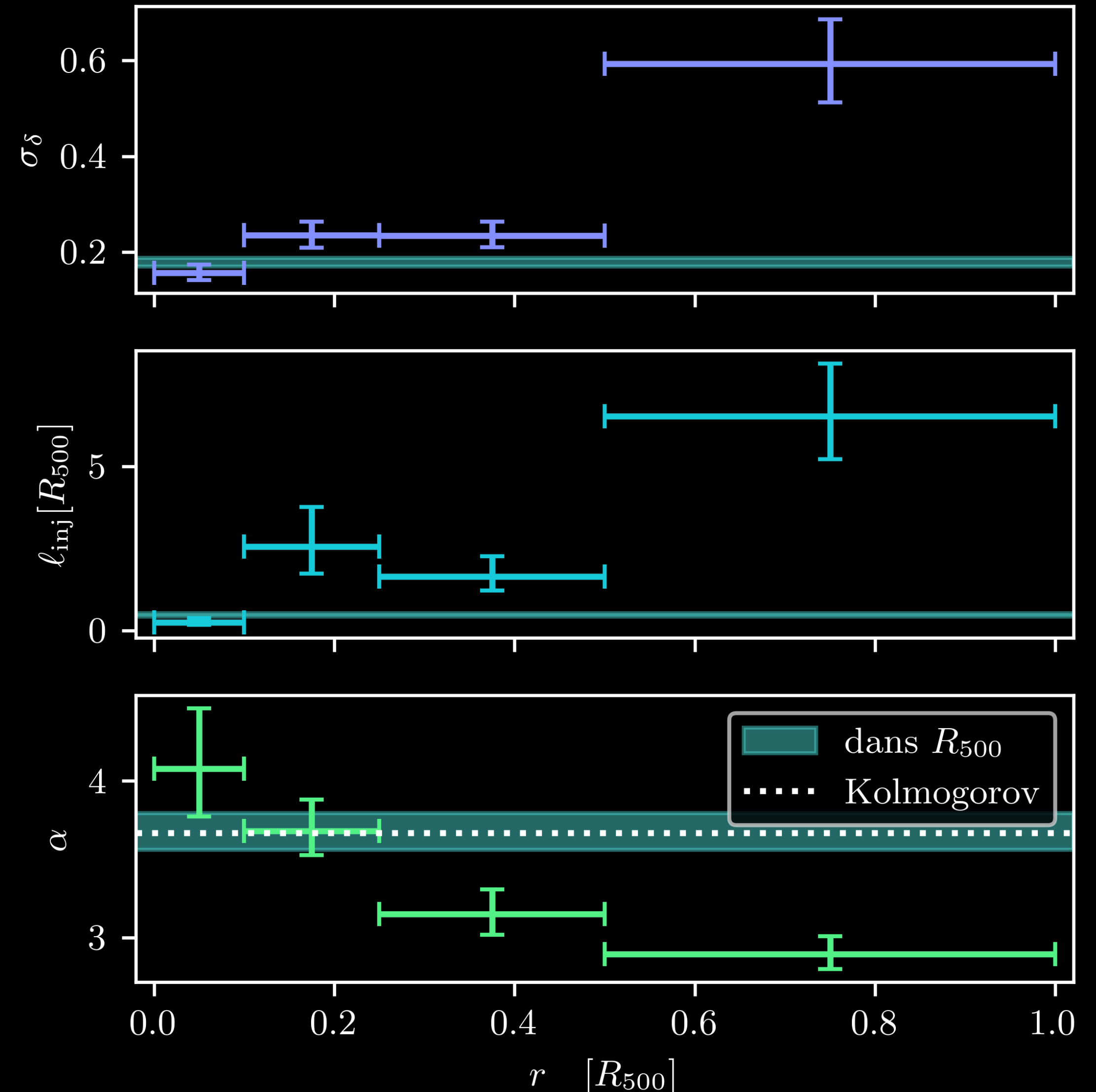
- **Global** : $\mathcal{M} \sim 0.1$, subsonic

- **Profile** : the injection scale increases with radius \rightarrow transition between feedback, sloshing and merging

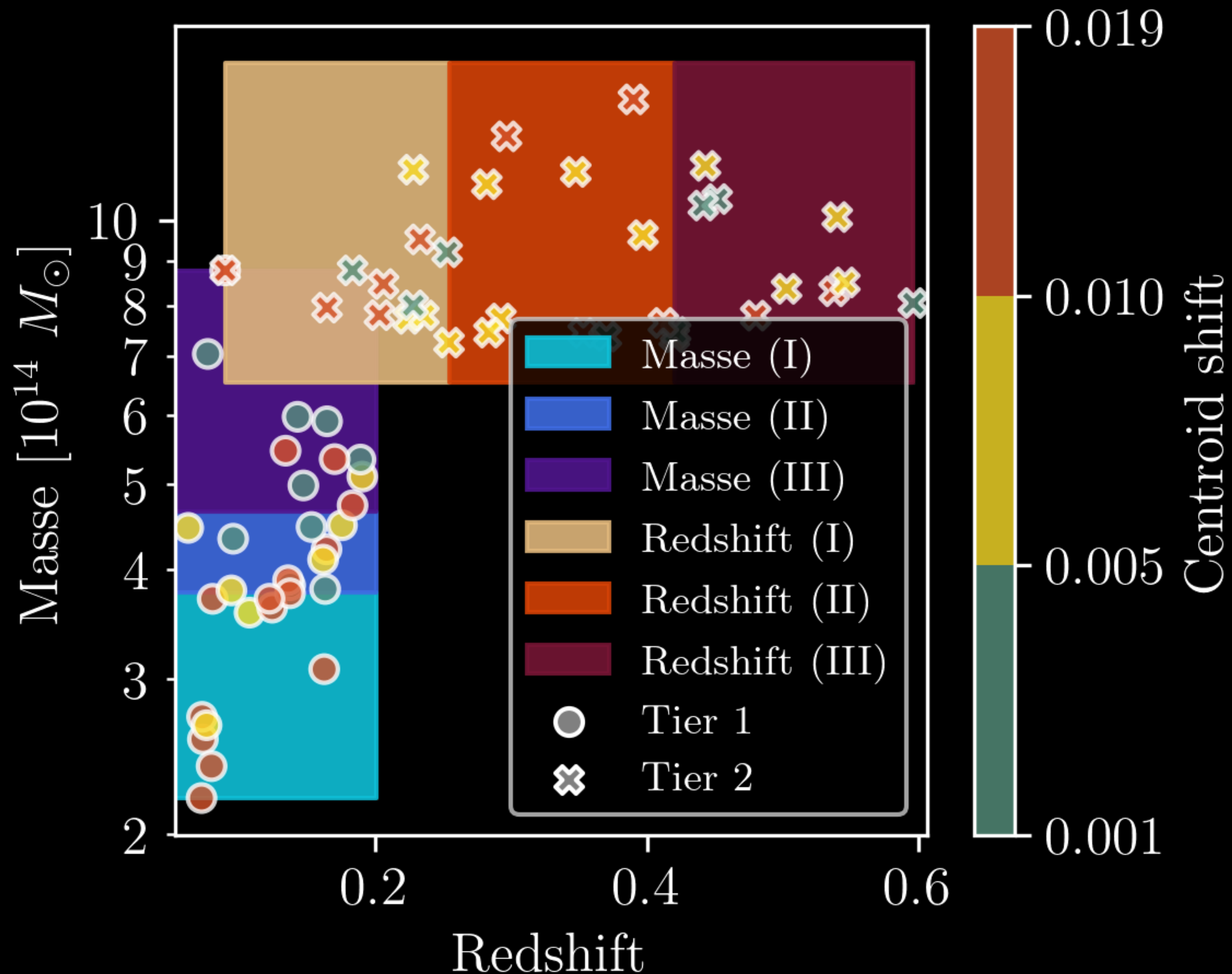
- **Global** : dominated by central region

- **Profile** : the spectral slope decreases with radius \rightarrow transition between structured and noisy fluctuations

- **Global** : Kolmogorov-like!

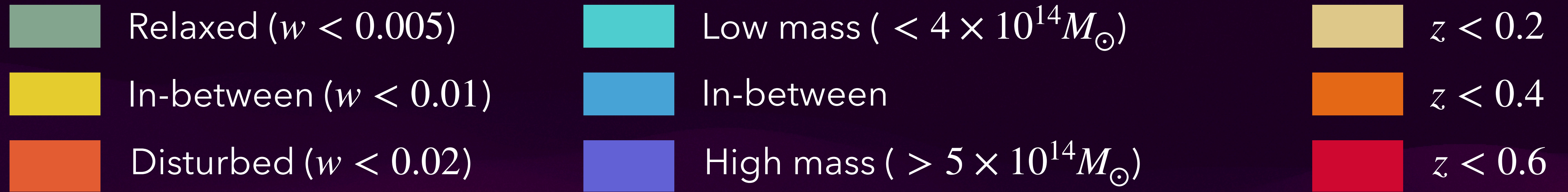


Sample study with CHEX-MATE

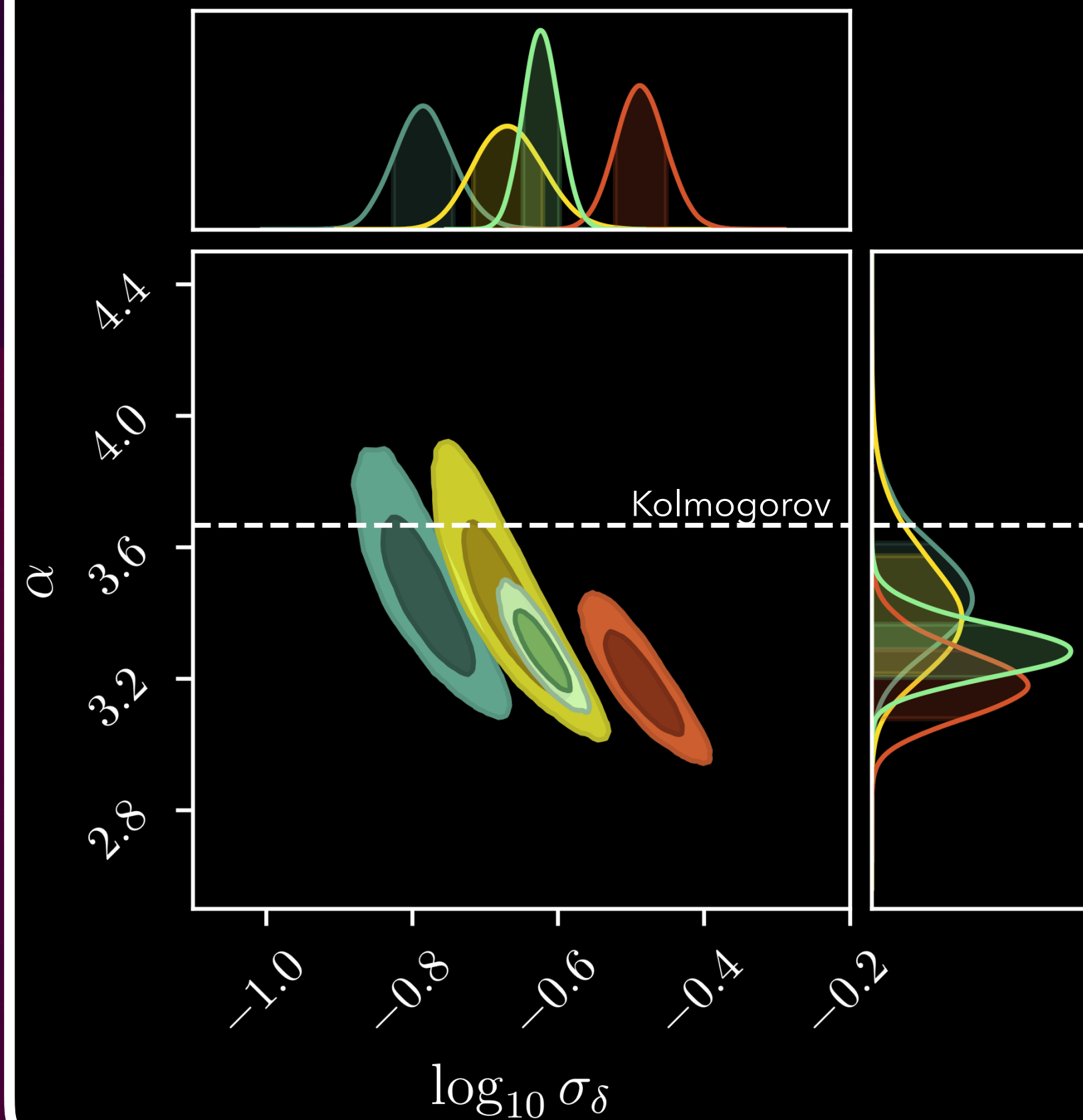


Investigate the link between cluster properties and turbulence

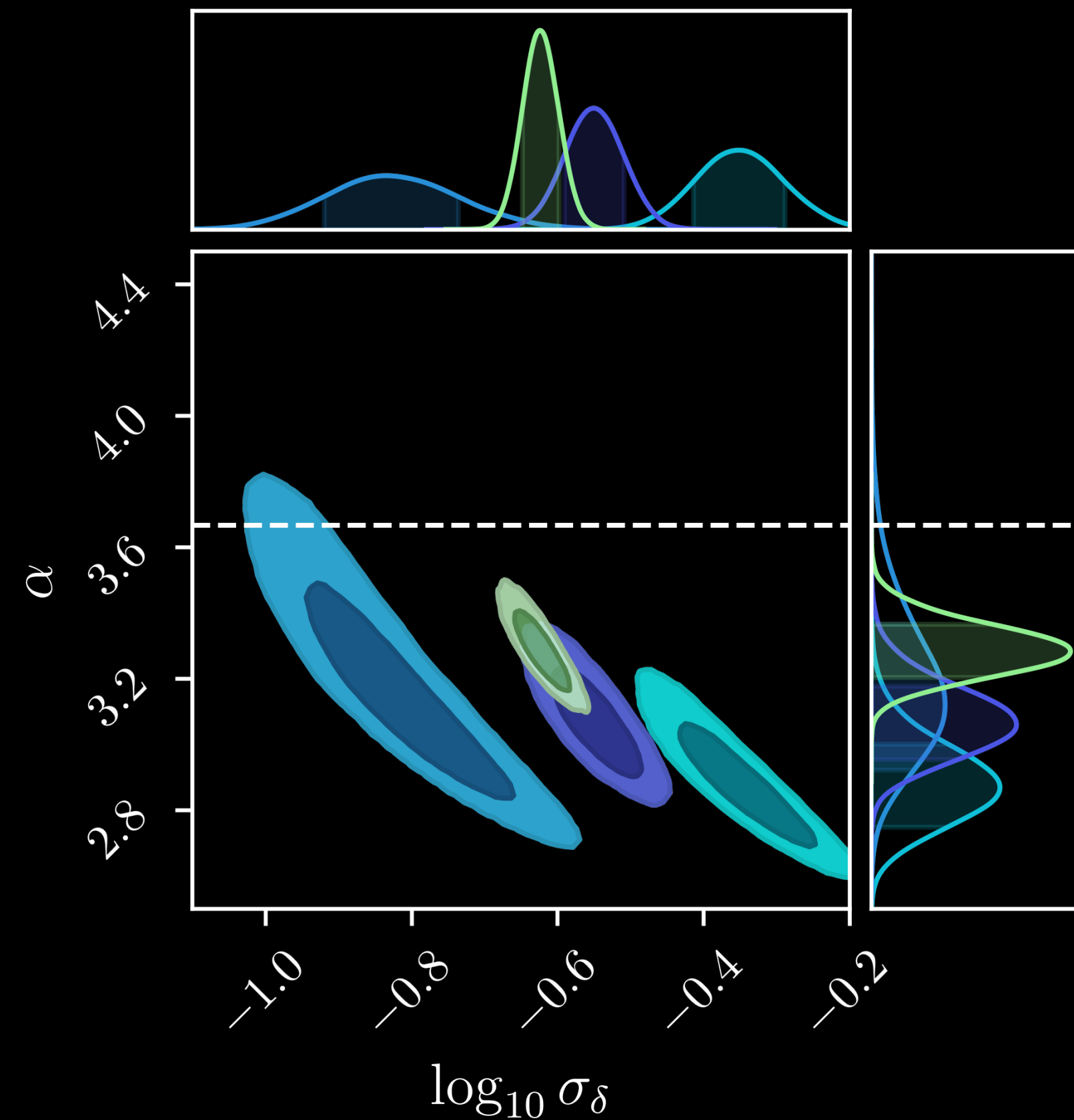
- Study on 64 cluster, after cleaning the sample from the most irregular ones
- Subdivide in three sub-samples in mass, redshift and dynamic state



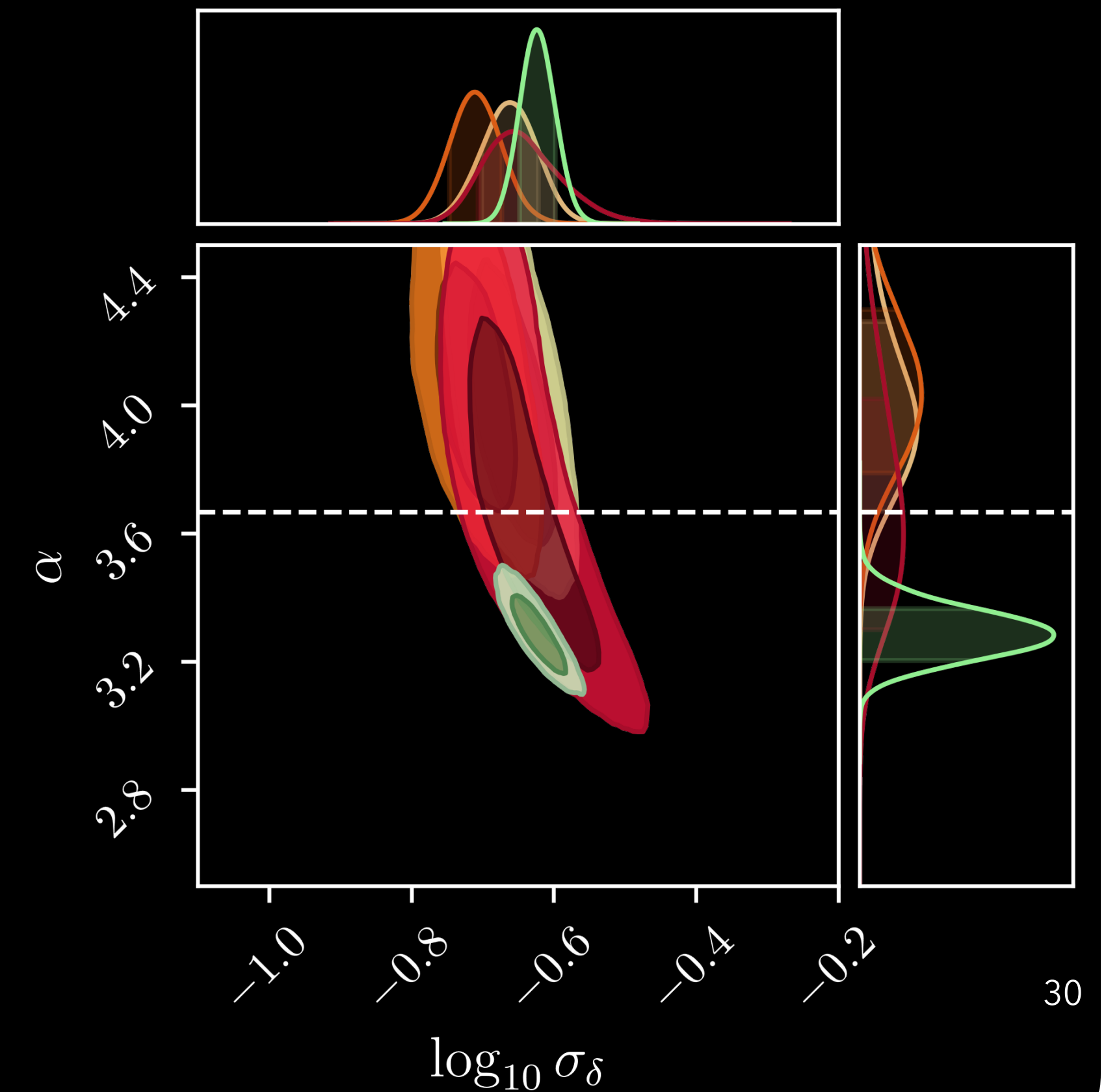
Splitting on dynamical state



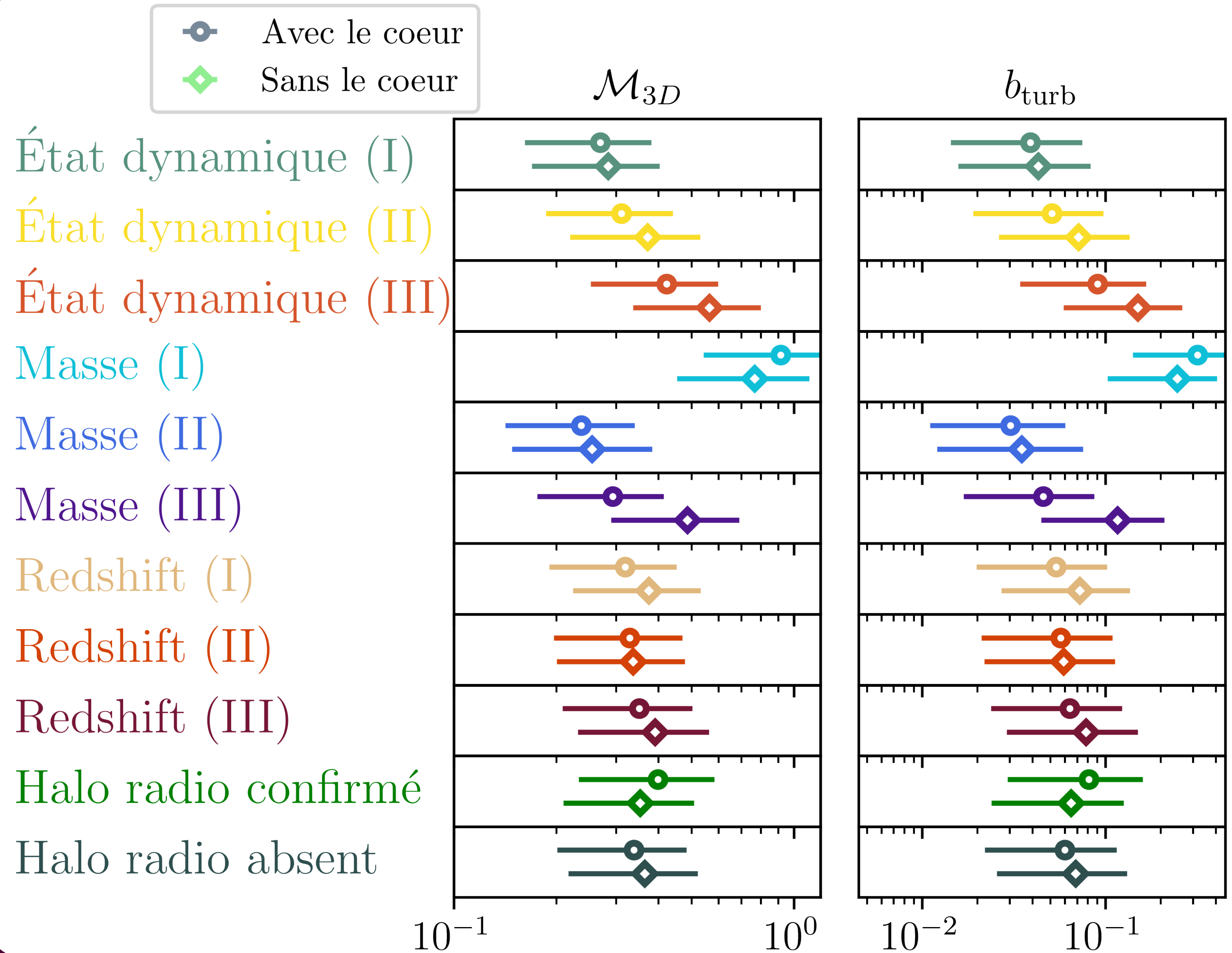
Splitting on mass



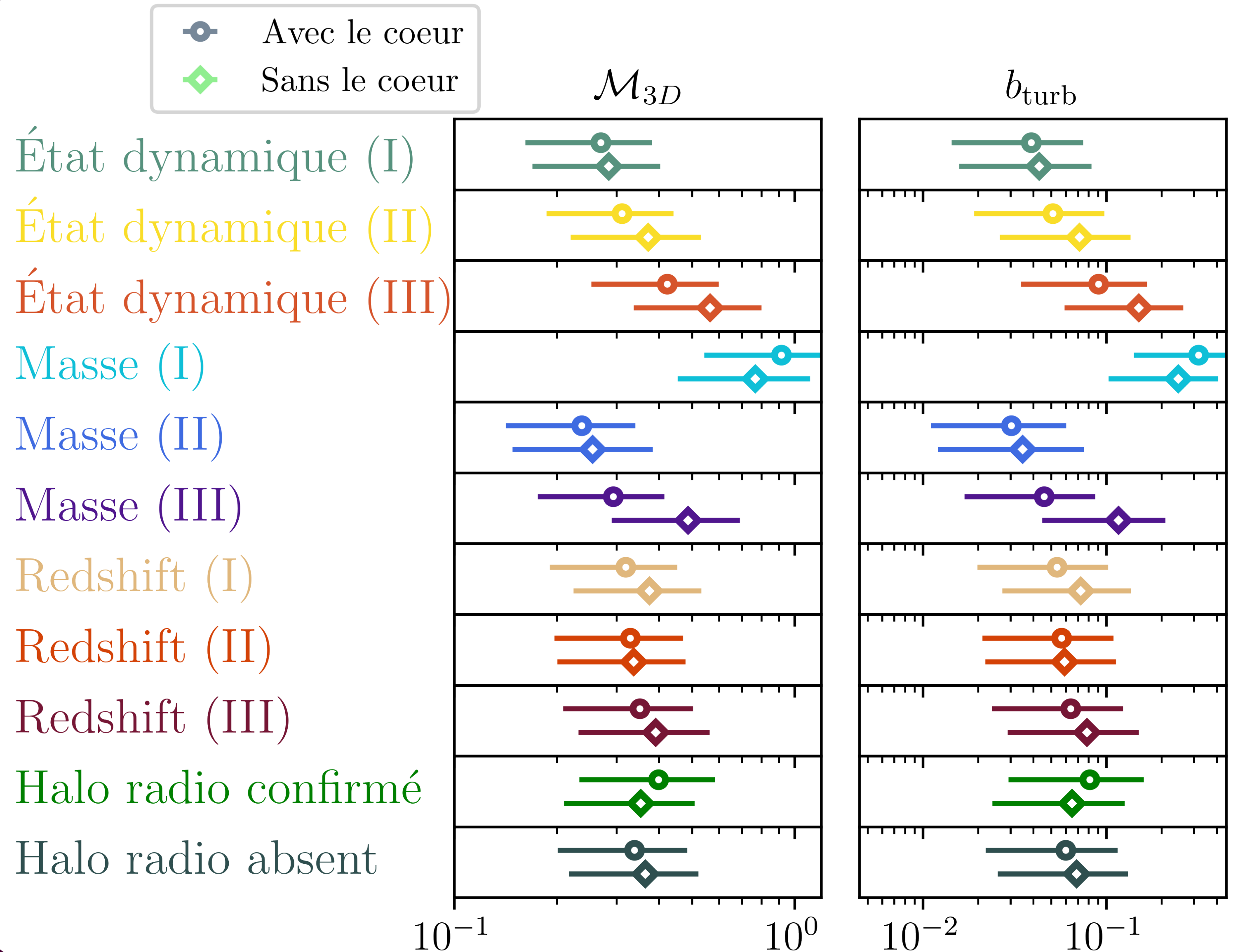
Splitting on redshift



Turbulence & hydrostatic mass bias



Turbulence & hydrostatic mass bias



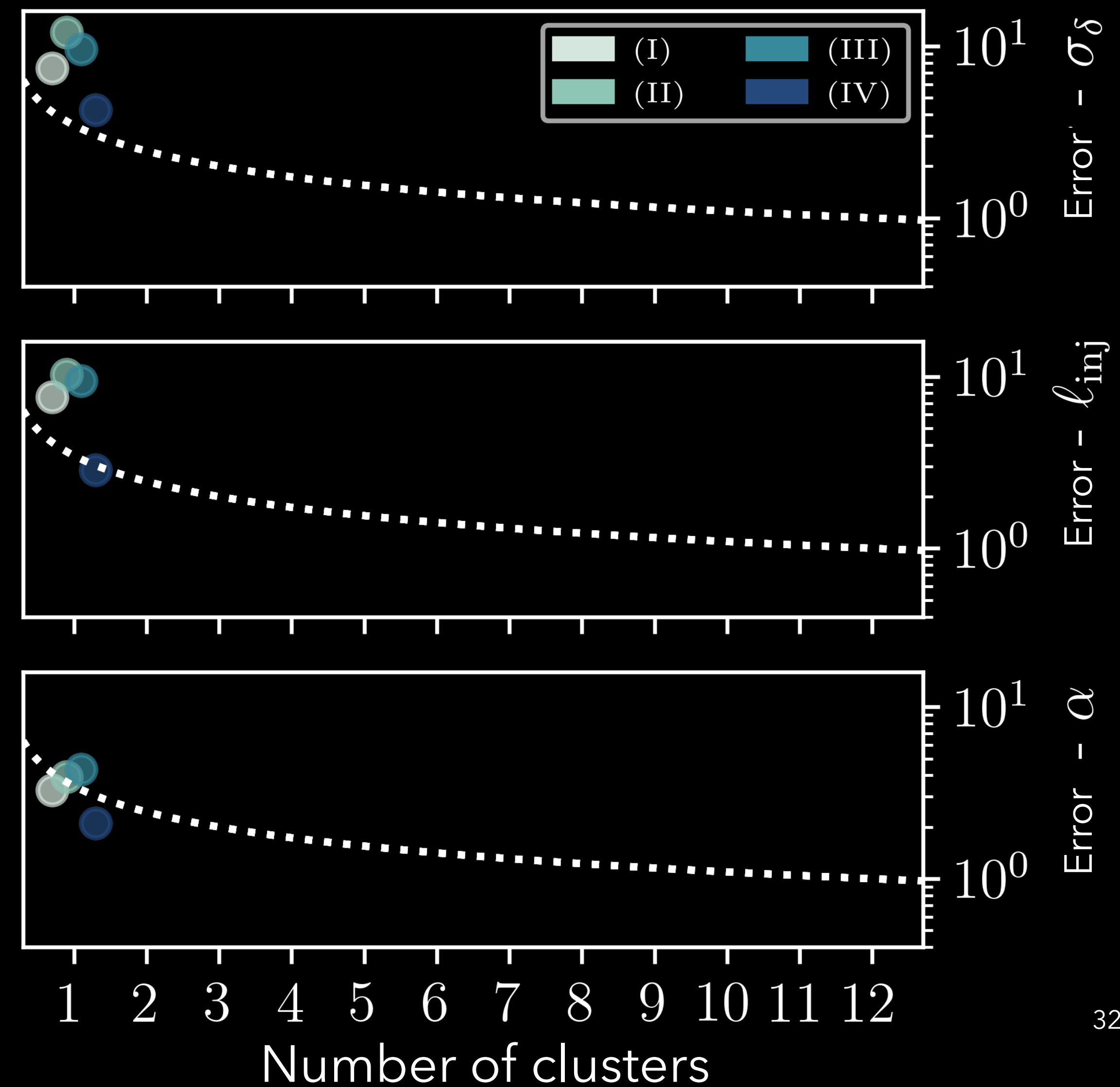
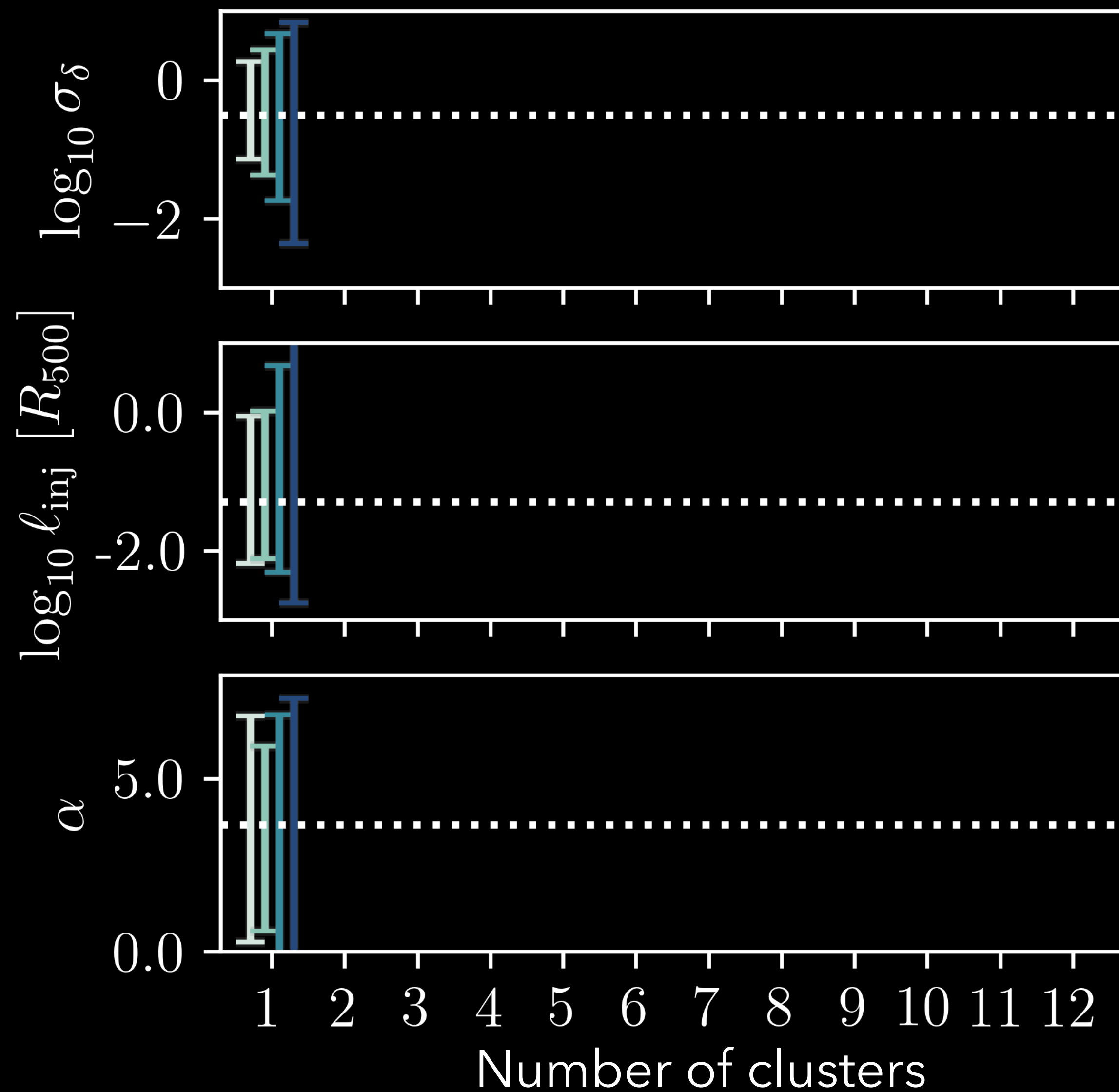
$$\mathcal{M}_{3D} \sim 0.3 - 0.5$$

$$b_{\text{turb}} \sim (9 \pm 6) \%$$

Coherent with direct
and indirect
observations, and
numerical simulations

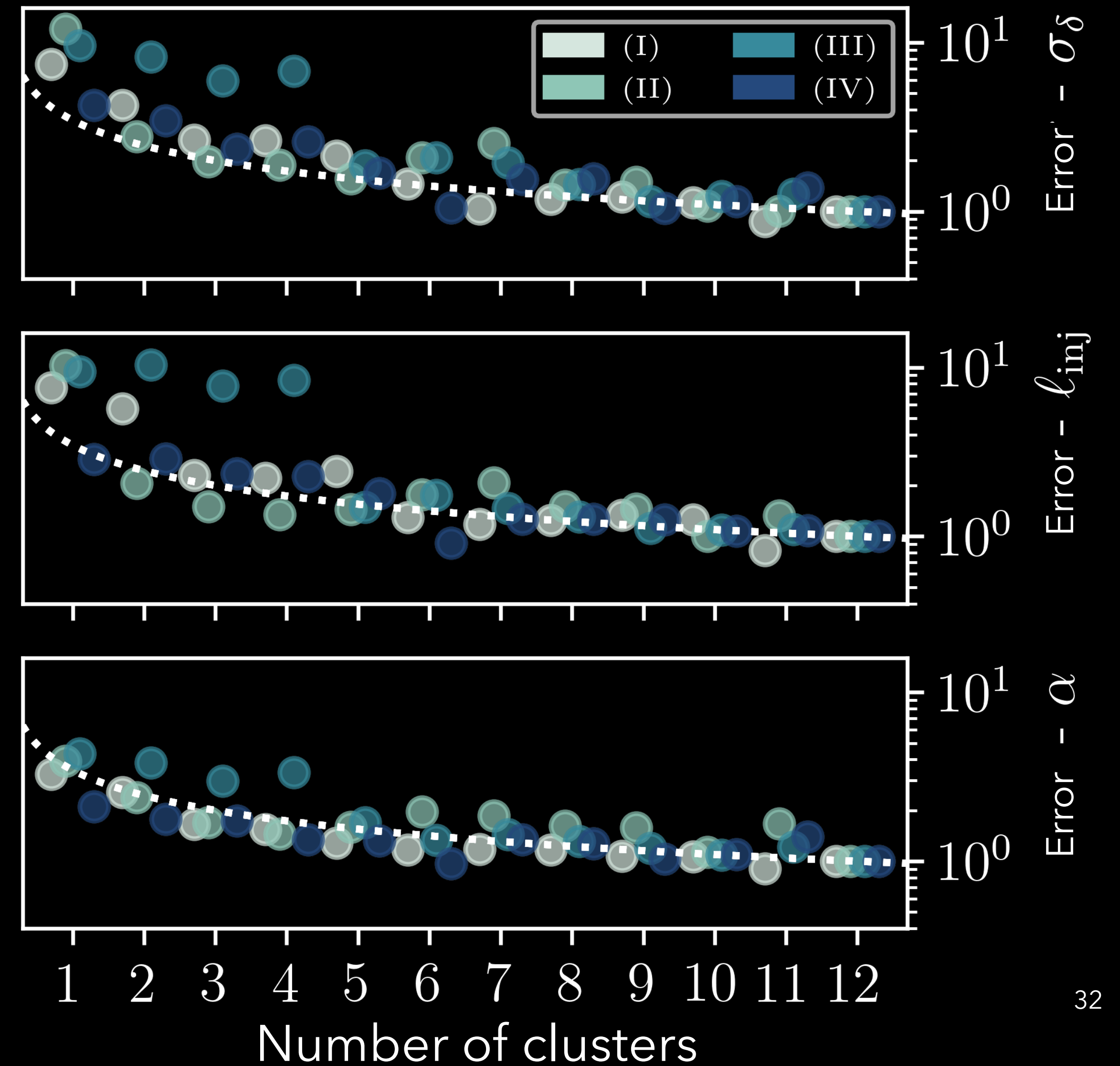
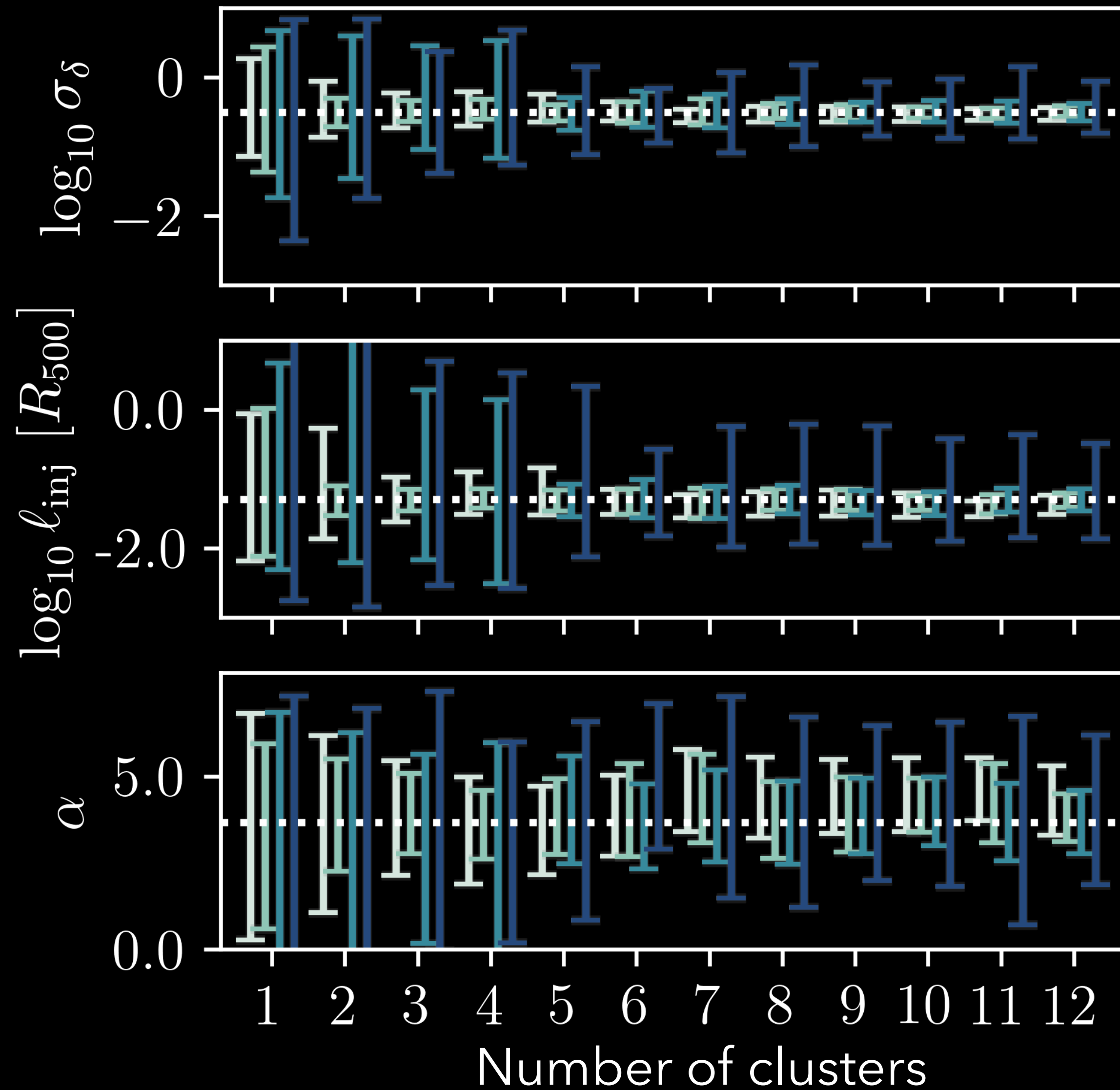
Validating SBI for galaxy clusters

(I)	$0 < r < R_{500}/10$
(II)	$R_{500}/10 < r < R_{500}/4$
(III)	$R_{500}/4 < r < R_{500}/2$
(IV)	$R_{500}/2 < r < R_{500}$



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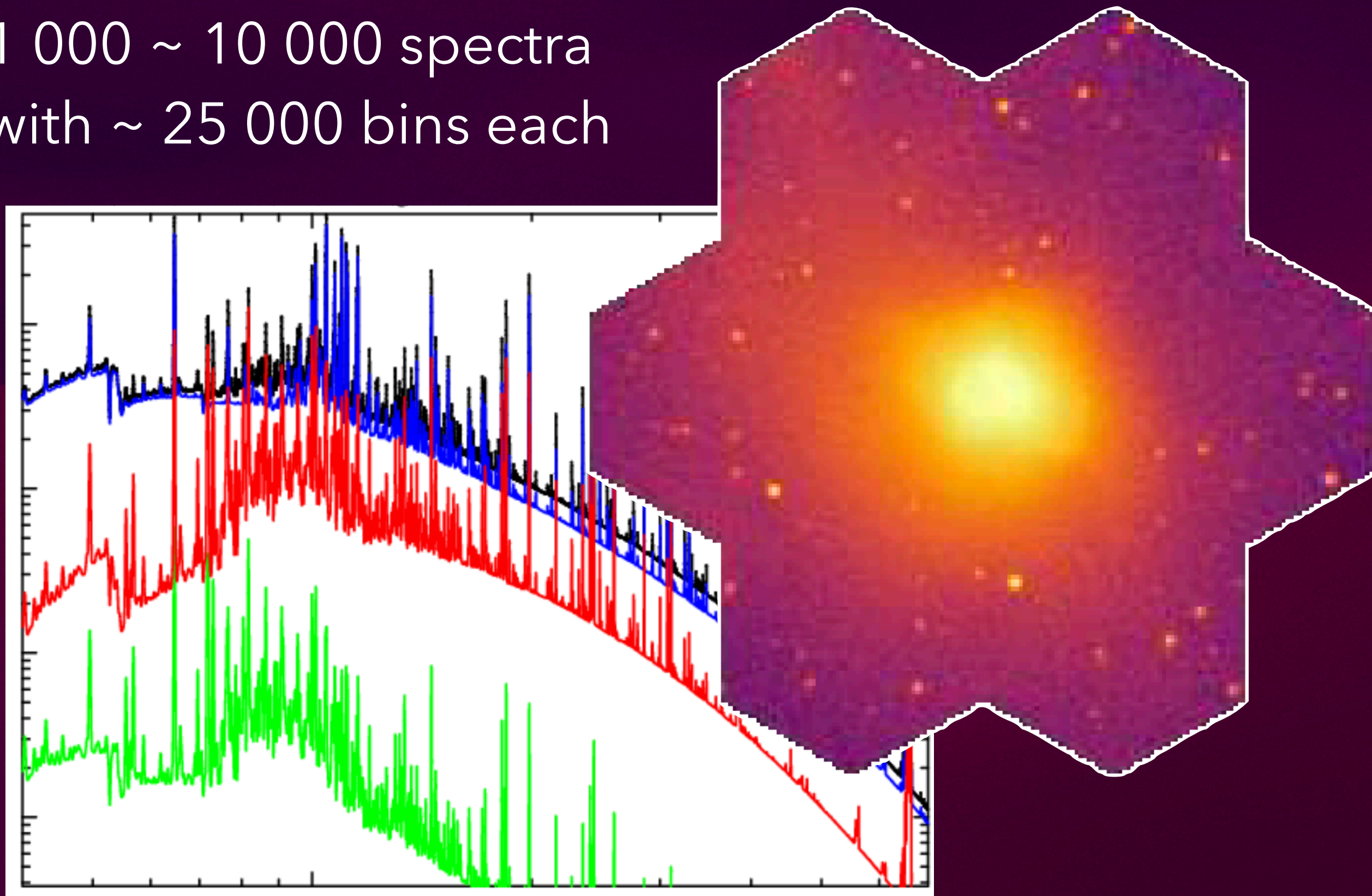


What is it to fit an X-IFU cube?

X-IFU : high resolution spectrometer in X-ray (~ 2038)

Mock X-IFU mosaic of a close cluster ($z < 0.1$)

1 000 ~ 10 000 spectra
with $\sim 25\,000$ bins each

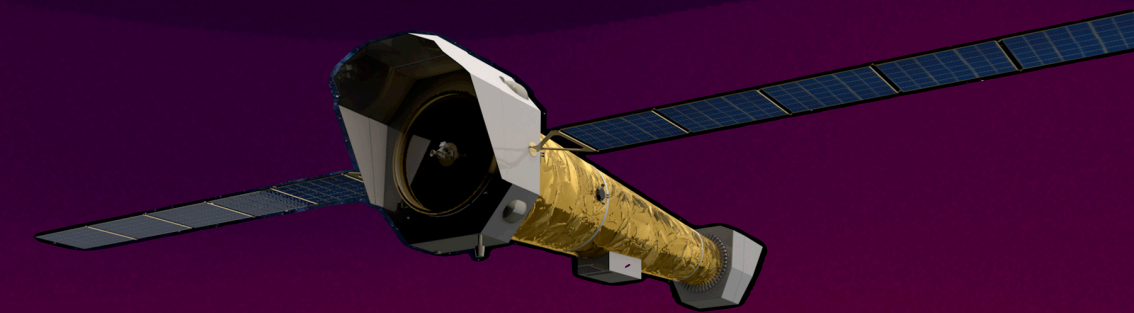
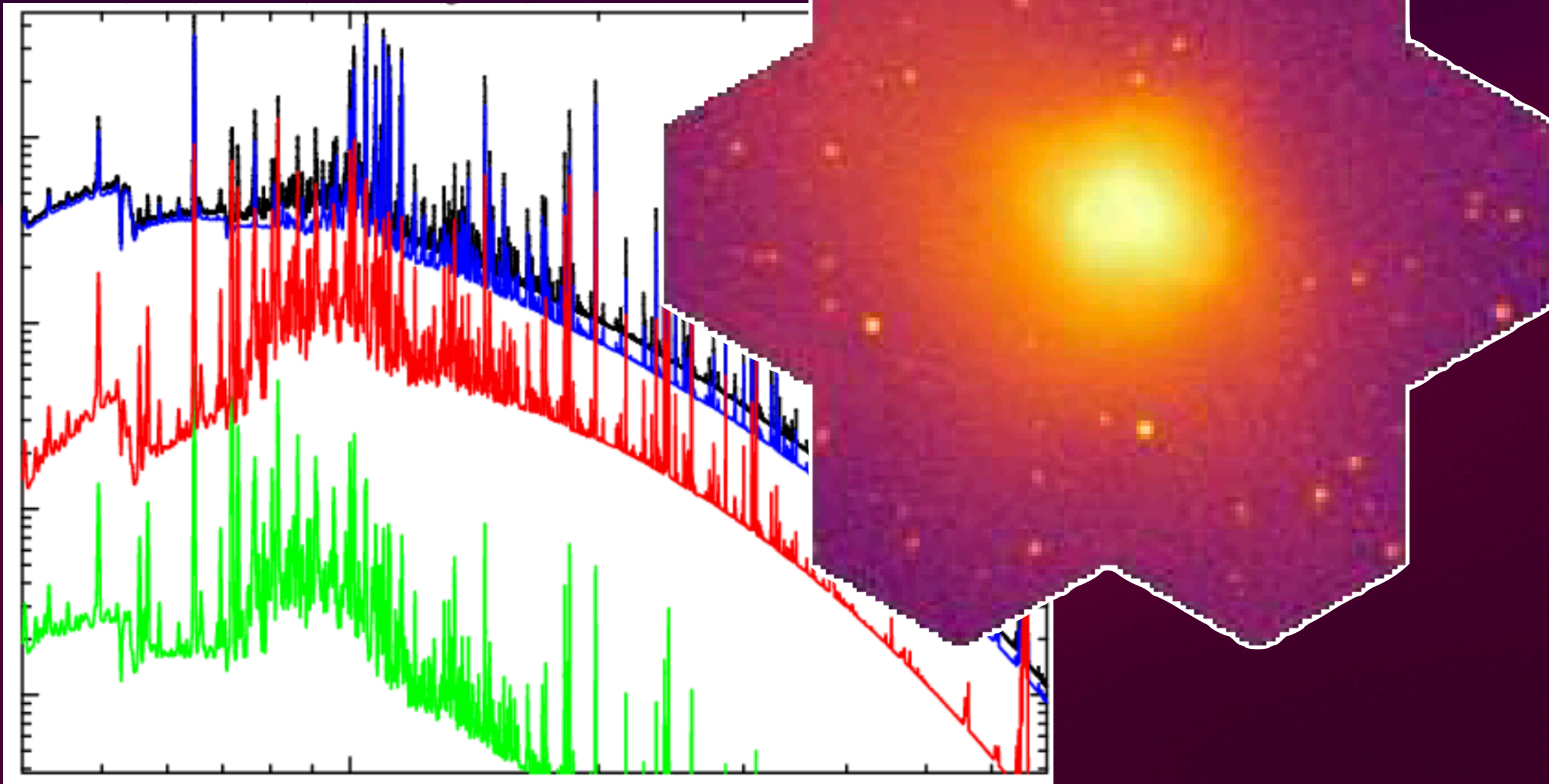


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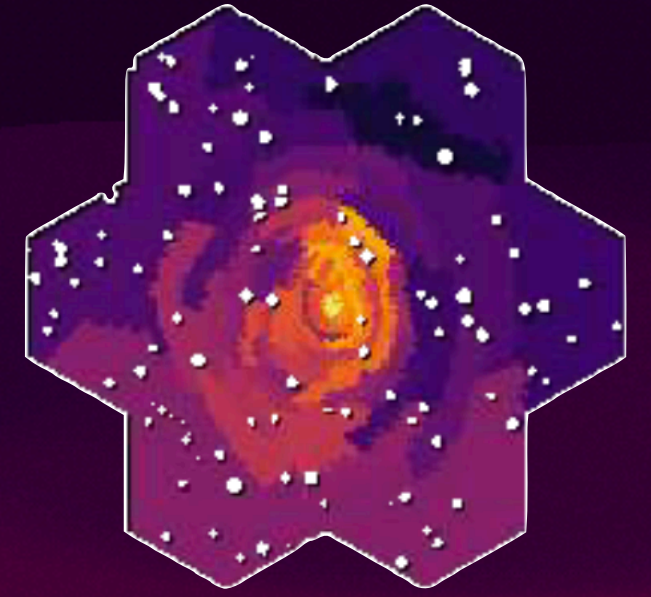
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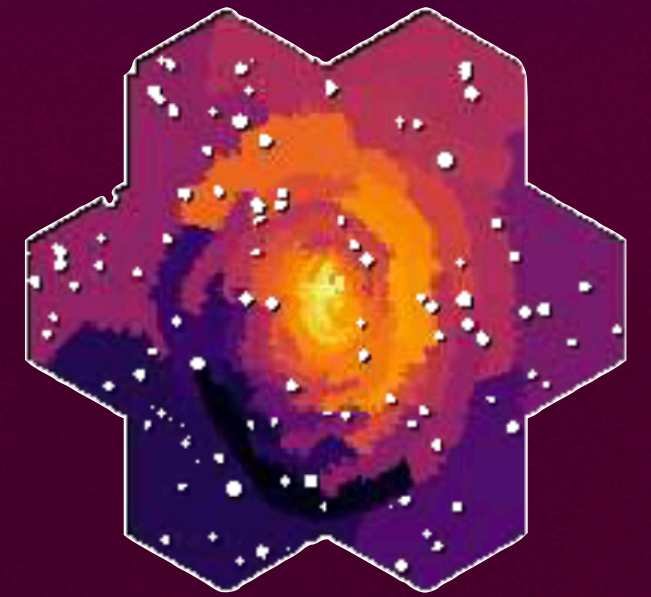
Spatial binning
Model fitting

$\sim 100\text{k CPU Hours}$

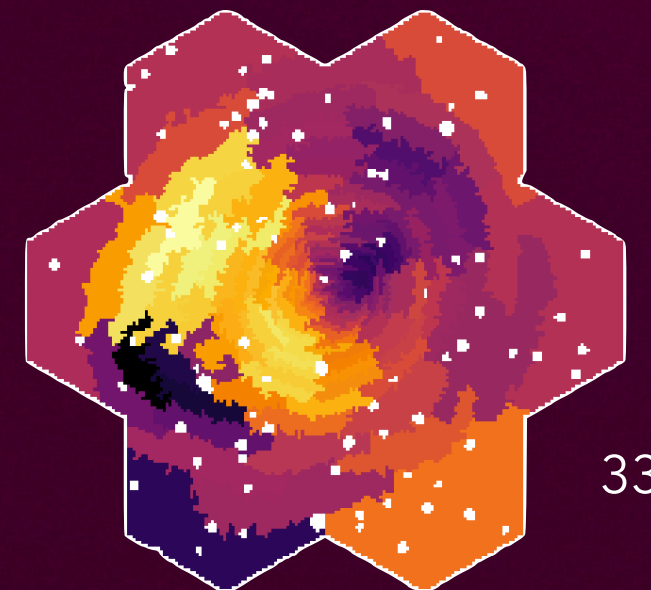
Oxygen



Temperature



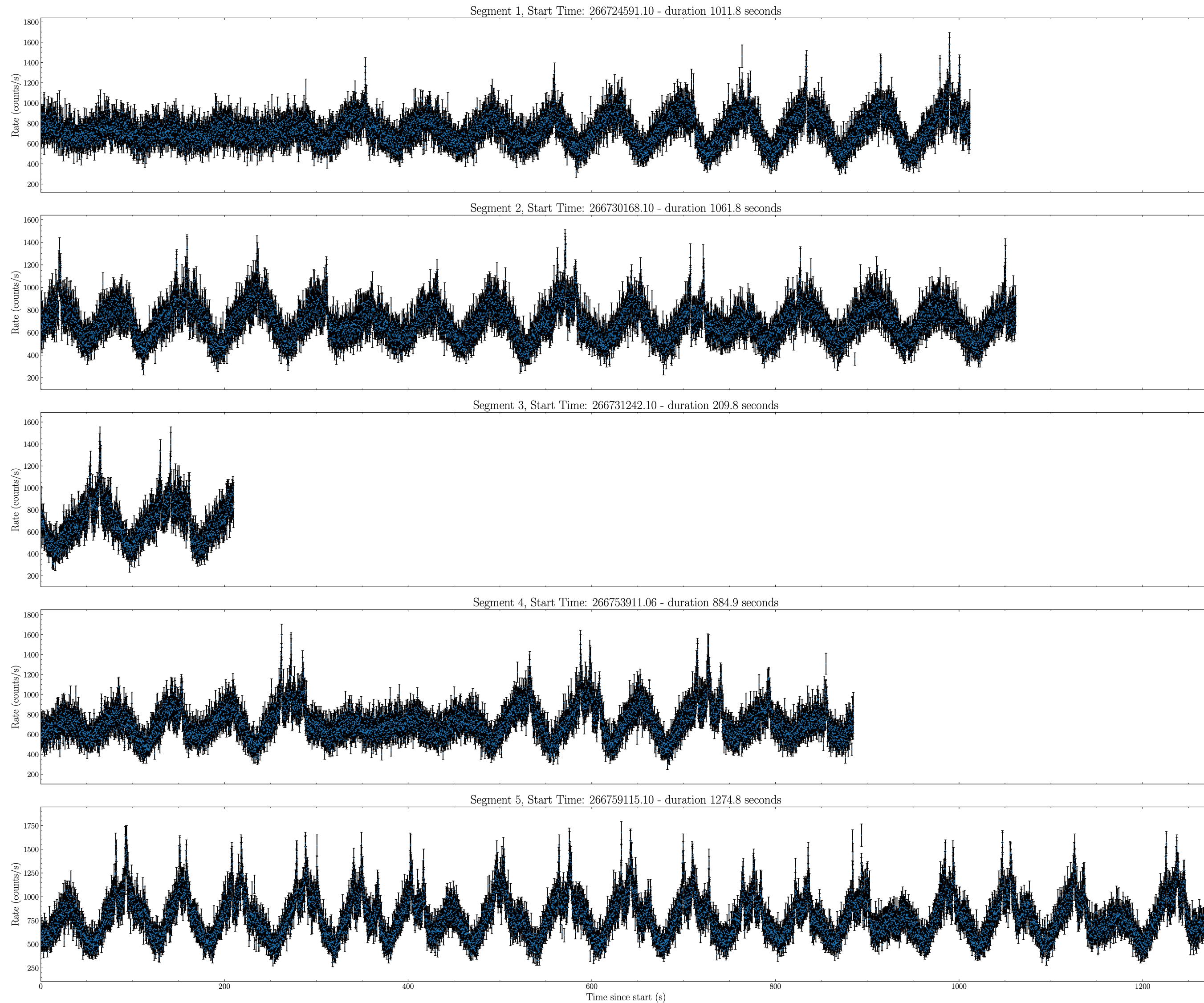
Bulk motion



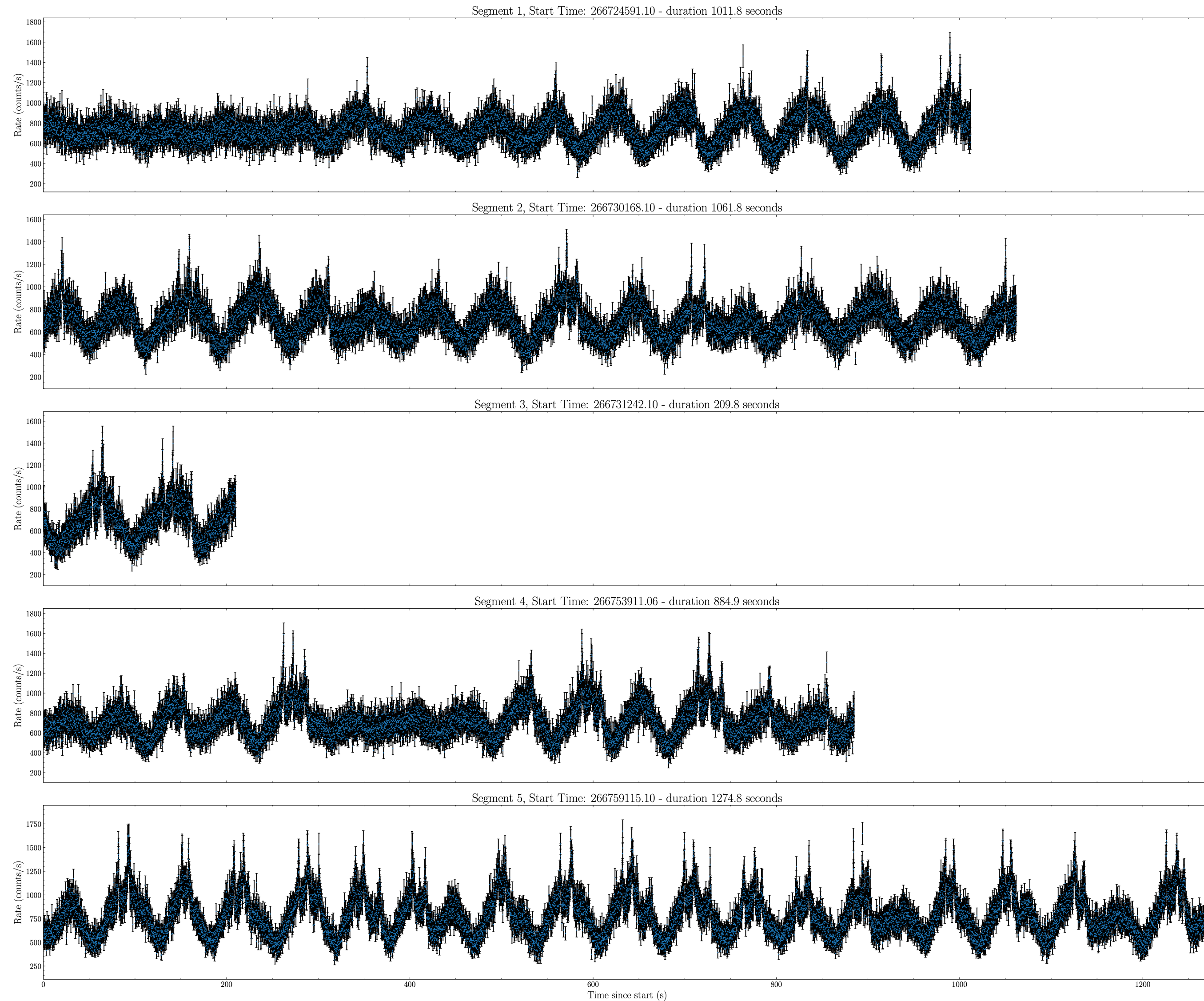
Single round inference with true data

Single round inference with true data

Example : time-resolved spectroscopy



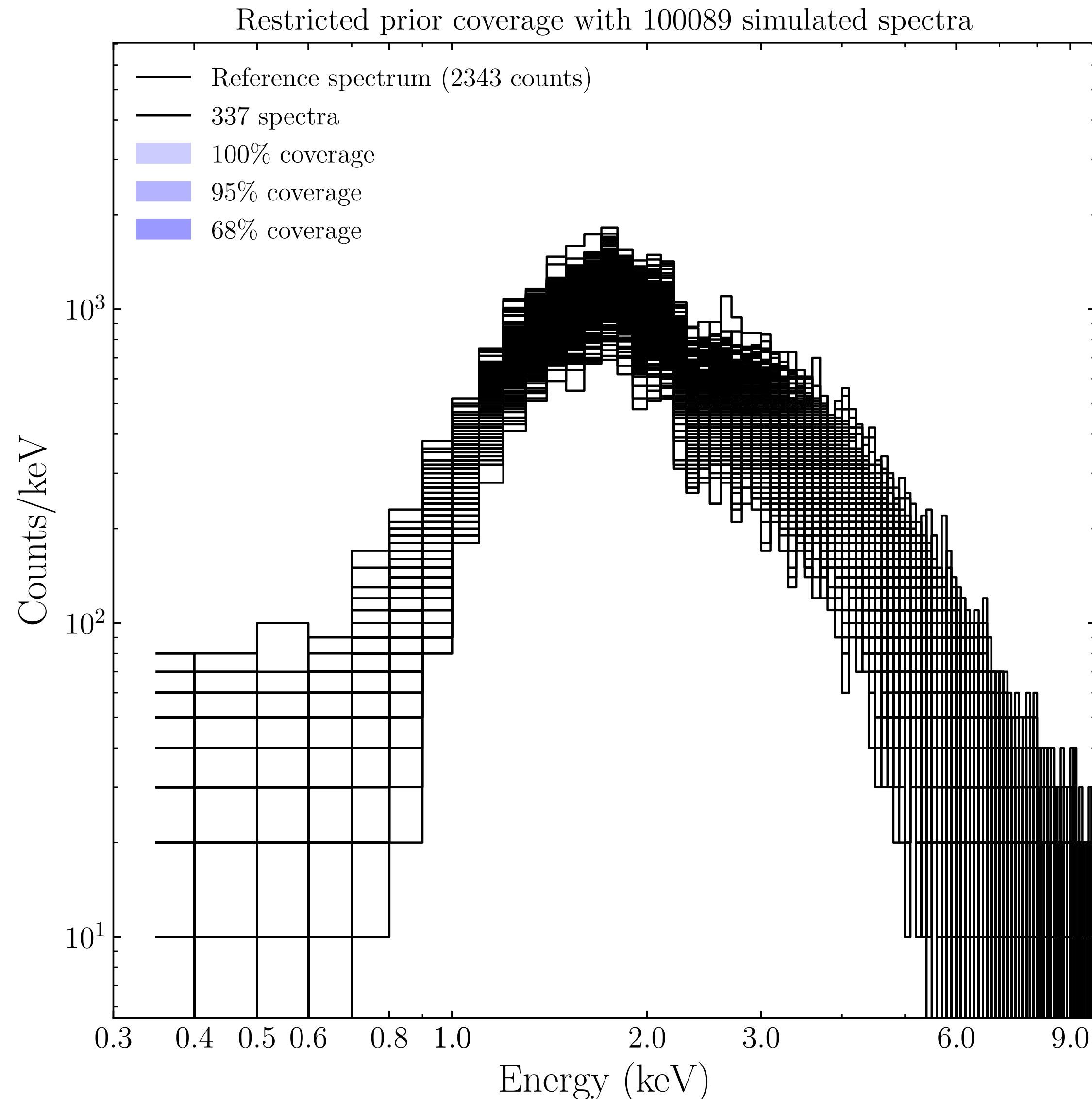
Single round inference with true data



Example : time-resolved spectroscopy

- Split observation of bright sources in hundreds/thousands of smaller observations and study the variability

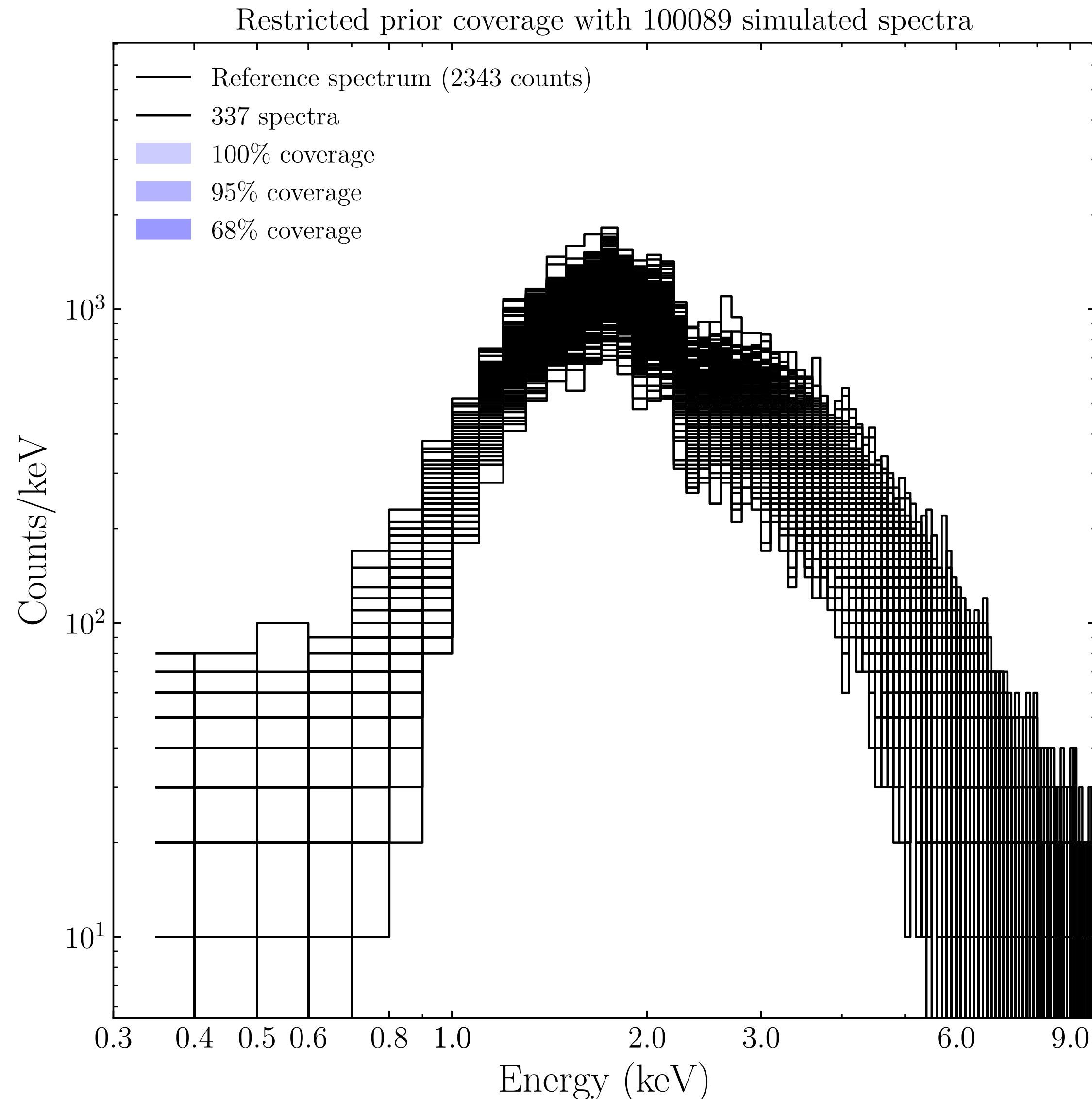
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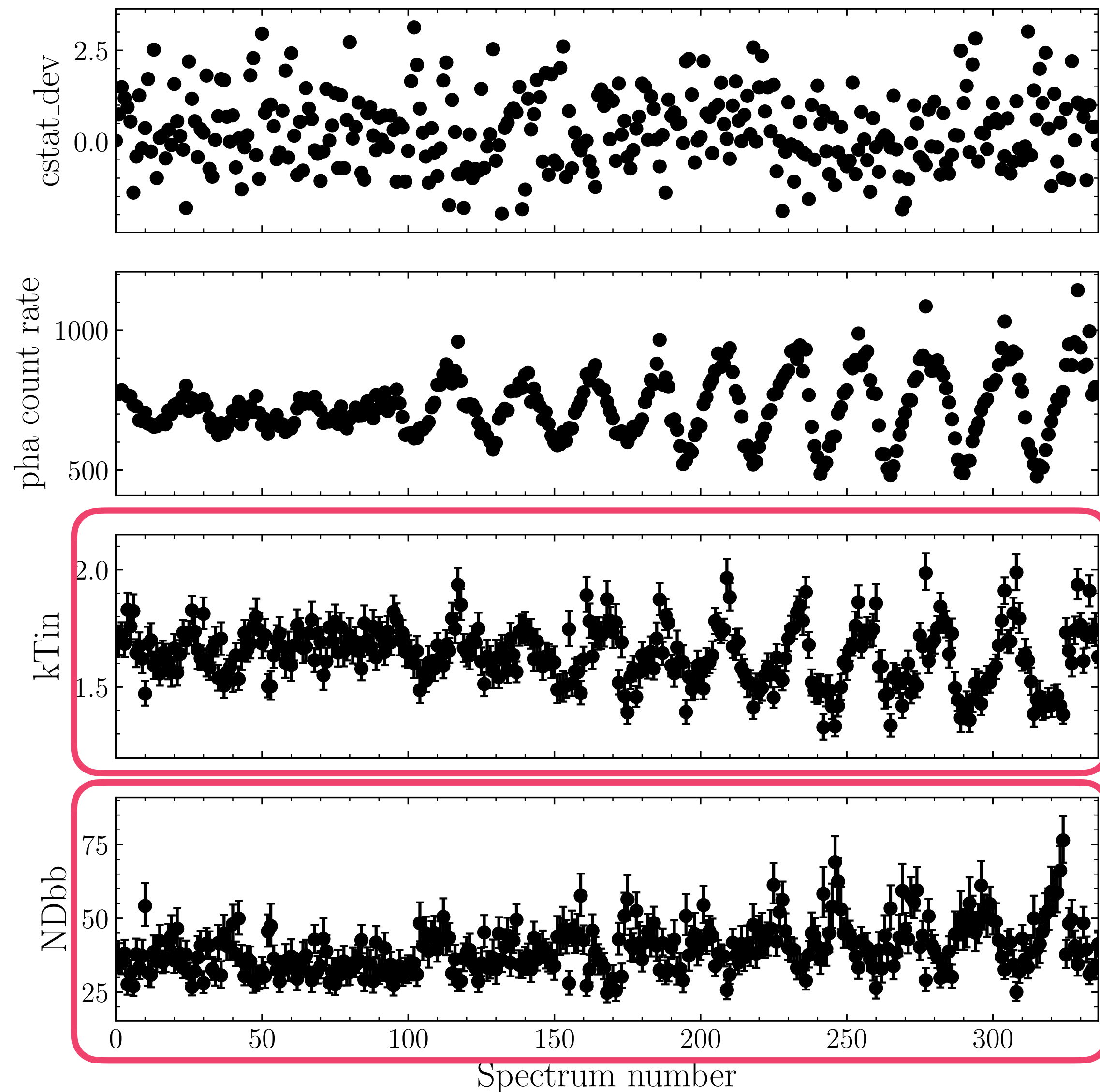
Single round inference with true data



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- Training a 3 parameter model using 10^5 simulations (absorbed thermal emission from an accretion disk)

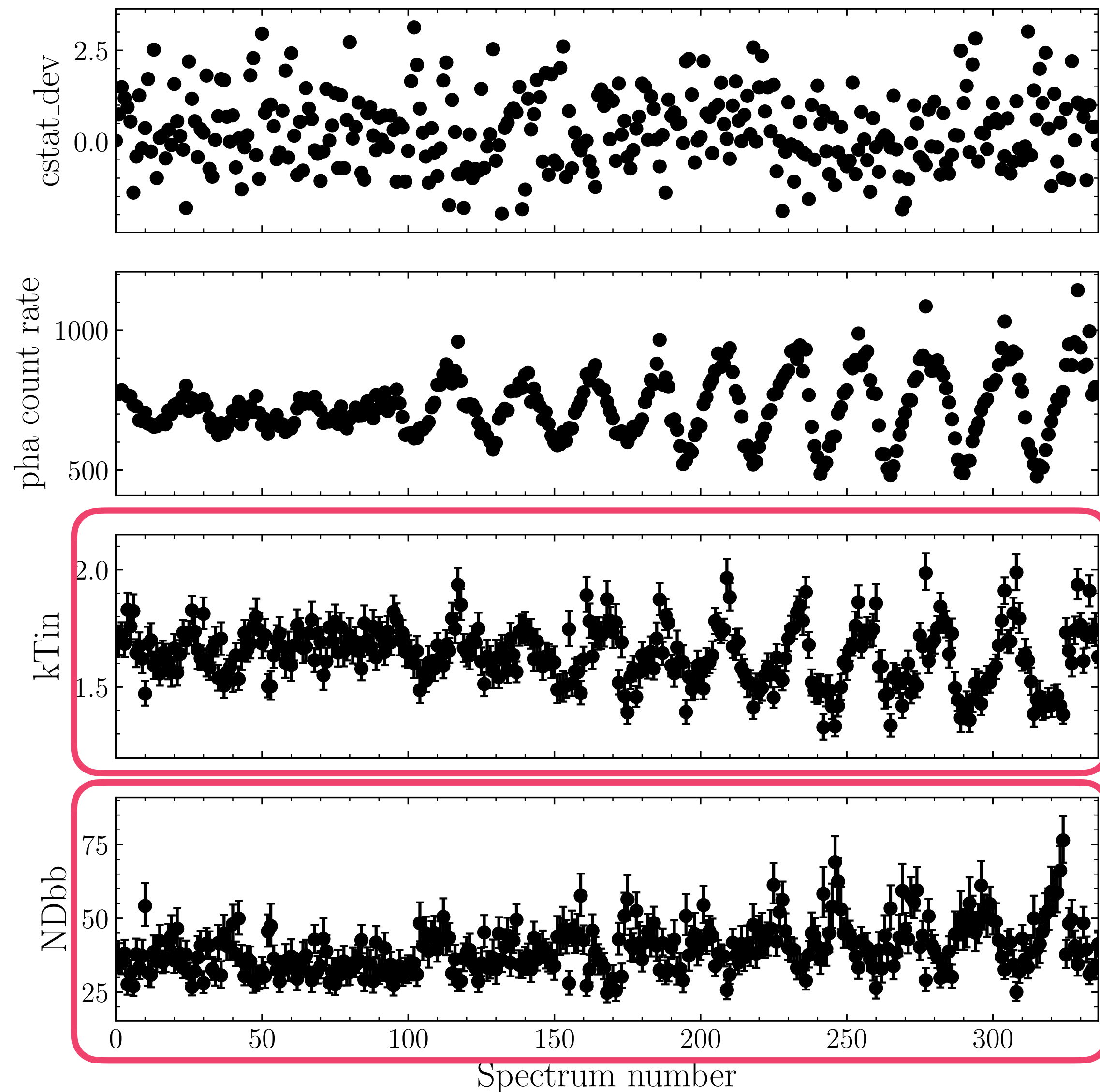
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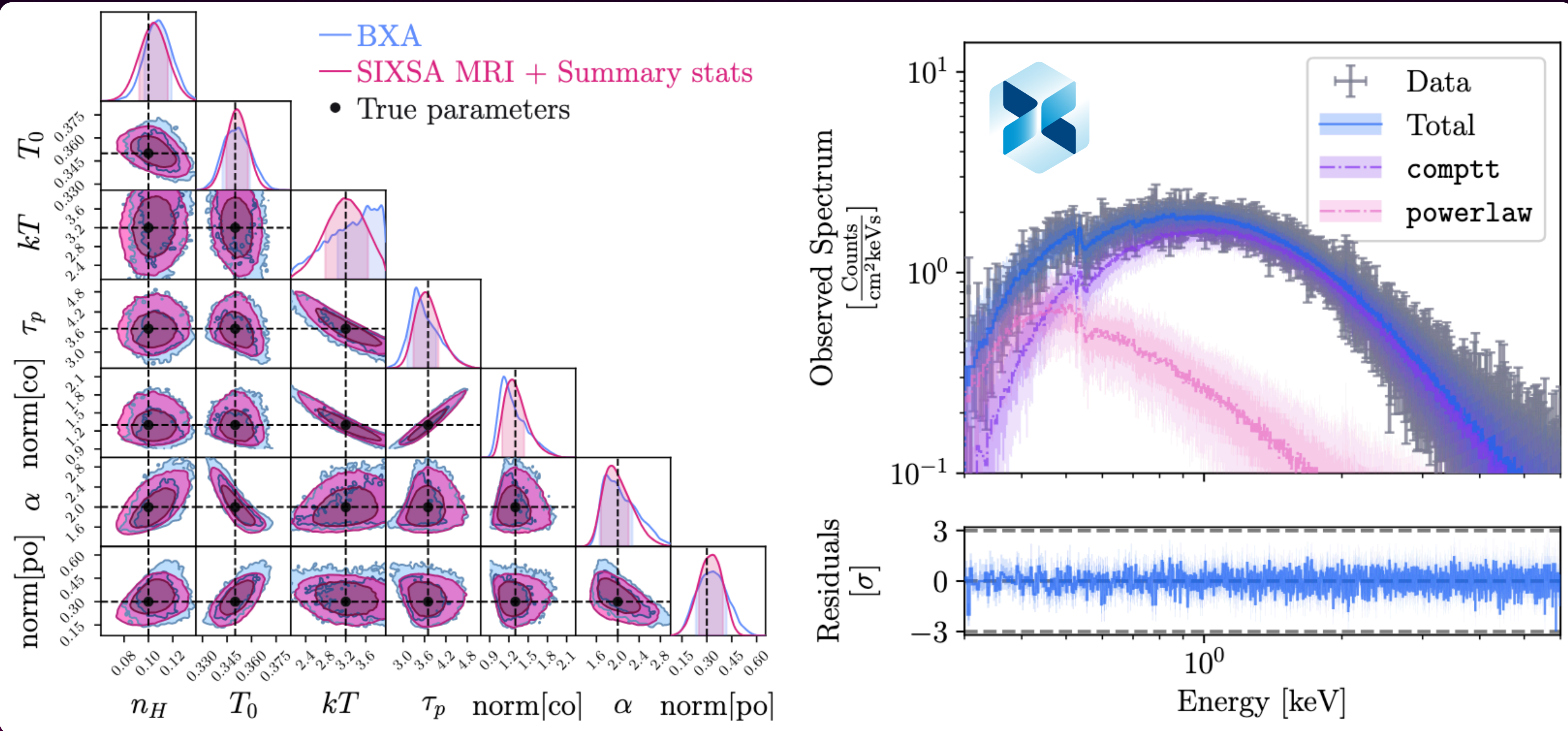


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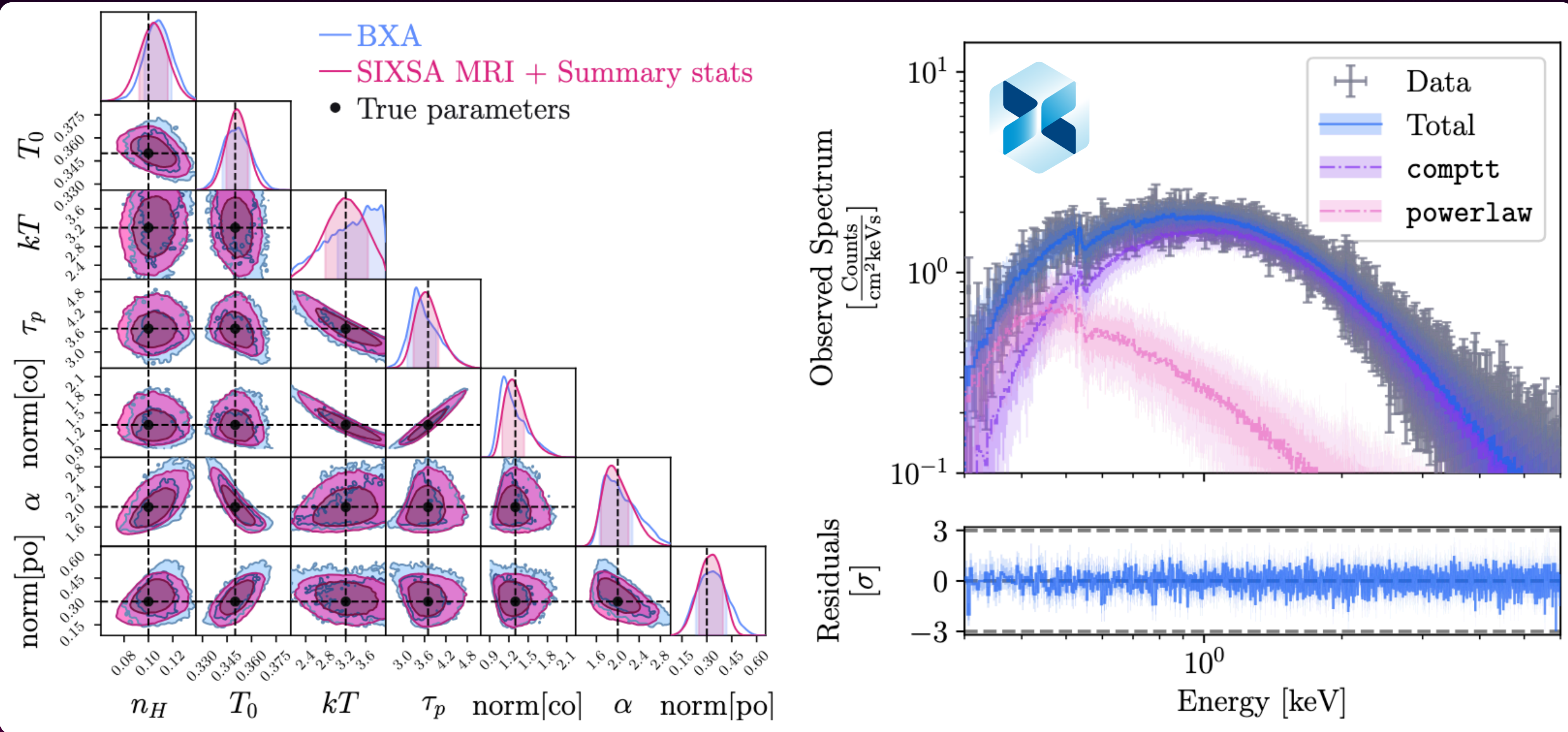
Up to 3 orders of magnitude faster than comparable methods if applied on a full X-IFU FOV

Multiple round inference with X-IFU



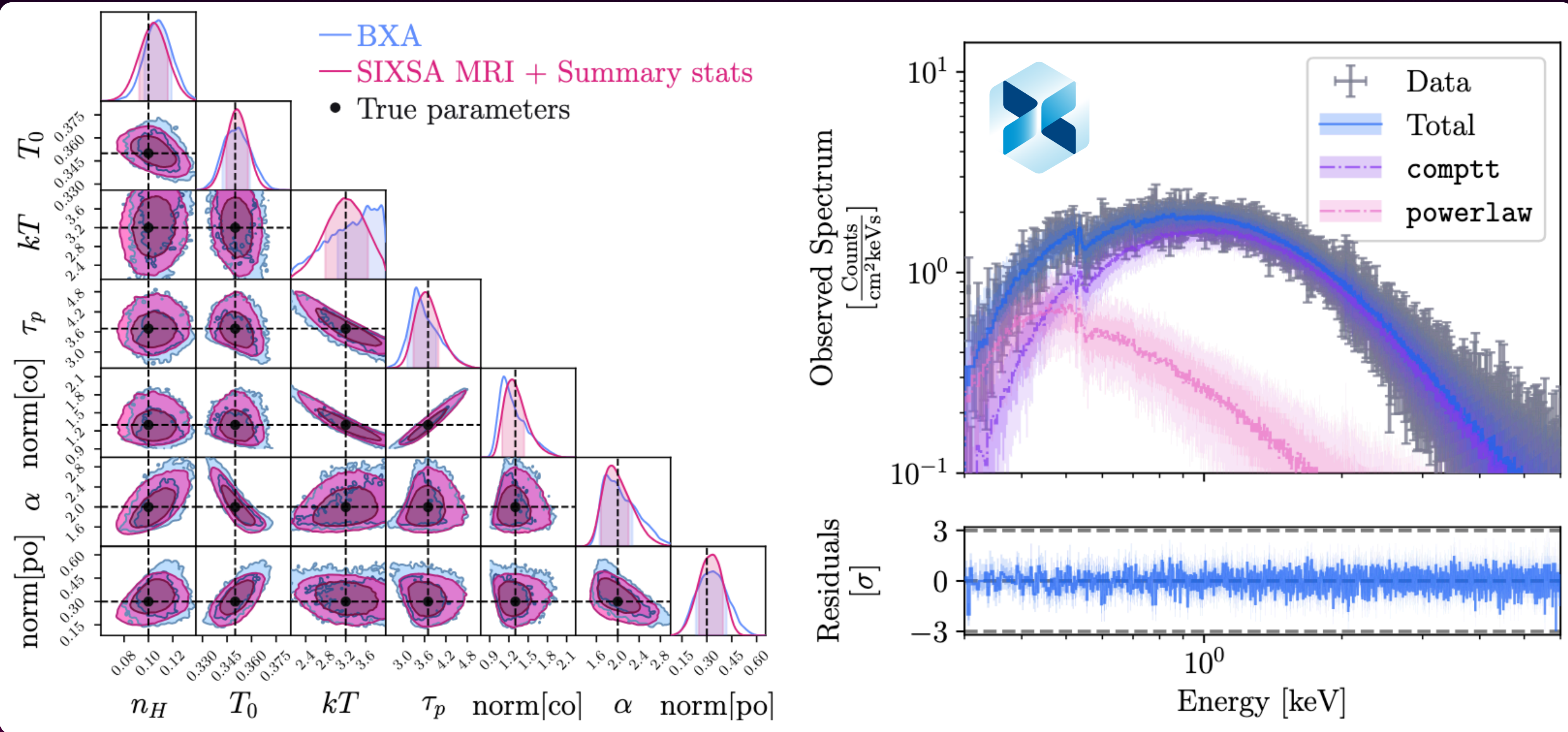
- Two components spectrum with X-IFU on a low-count regime (7 parameters)

Multiple round inference with X-IFU



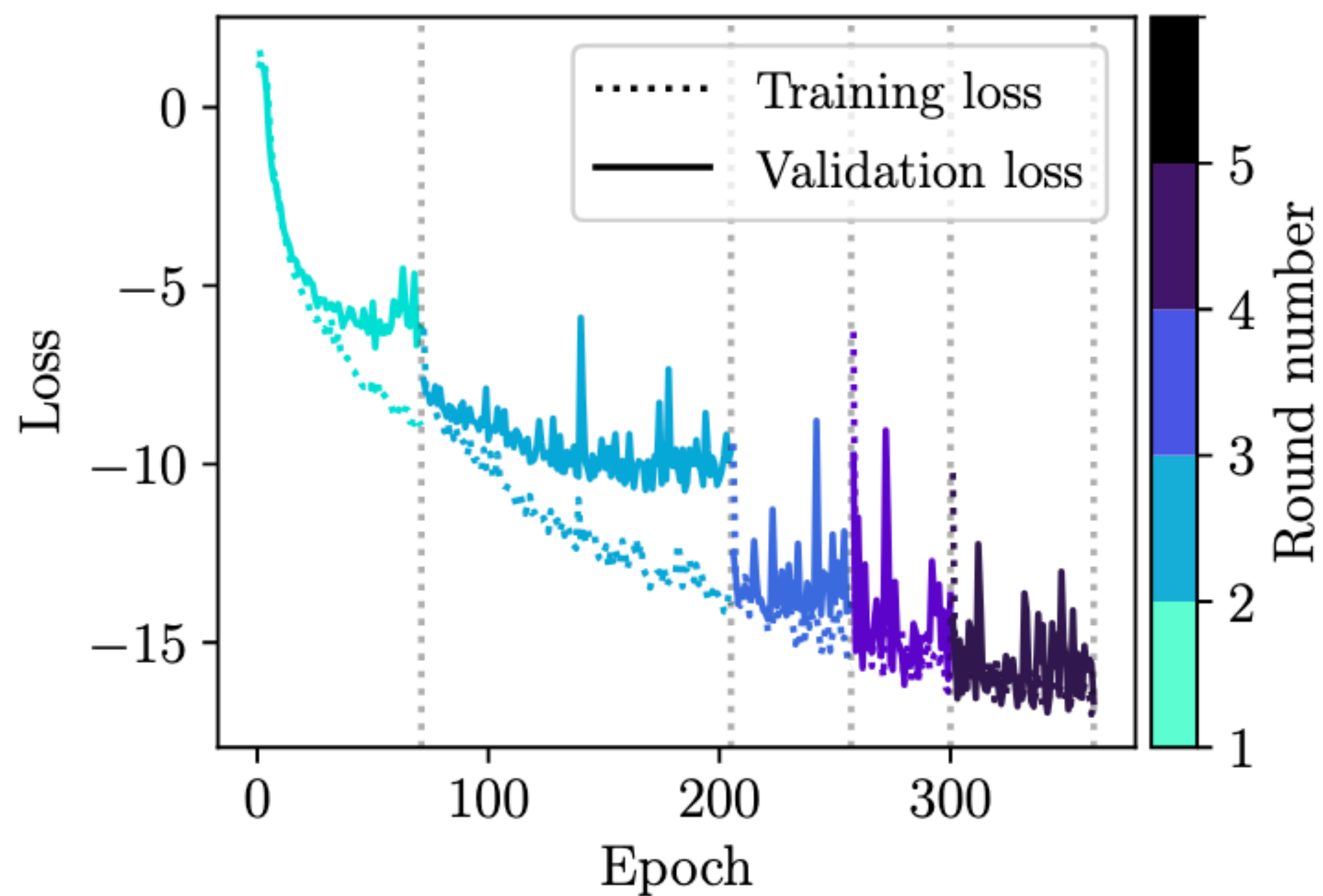
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Multiple round inference with X-IFU



- Two components spectrum with X-IFU on a low-count regime (7 parameters)
- MRI on high resolution data is equally performant as SOTA for Bayesian Inference
- It requires ~250 fewer simulations than SOTA and is ~2 order of magnitude faster

Training for $\text{tbabs}*(\text{comptt}+\text{powerlaw})$



Training for $\text{tbabs}*(\text{bapec}+\text{bapec})$

