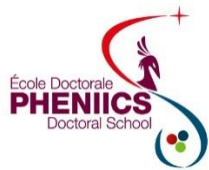


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Superconductivity and Cryogenics for Particle Accelerators

Akira Miyazaki

Laboratoire de Physique des 2 infinis Irène Joliot-Curie

Pôle Physique des Accélérateurs

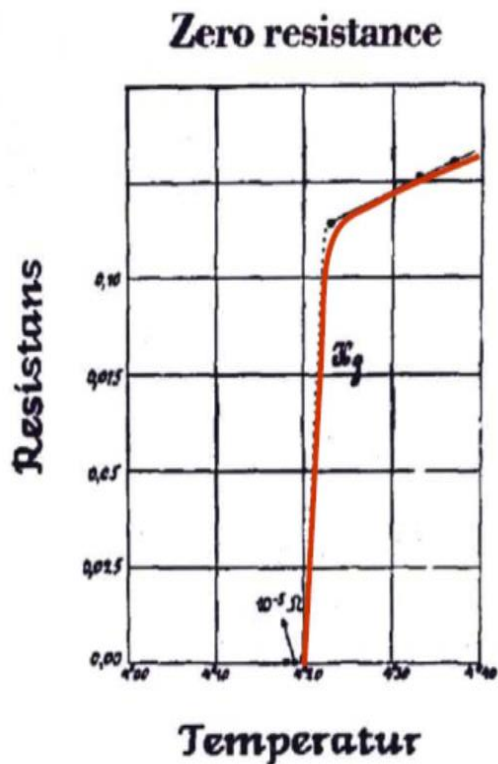
akira.miyazaki@ijclab.in2p3.fr

- Introduction: thermodynamics and benefit of cooling (10 min)
- Basics of cryogenics (15 min)
- BCS superconductivity (15 min)
- Non-BCS superconductivity (5 min)
- Break (10 min)
- Superconducting magnet (10 min)
- Superconducting RF cavities (20 min)
- Conclusion

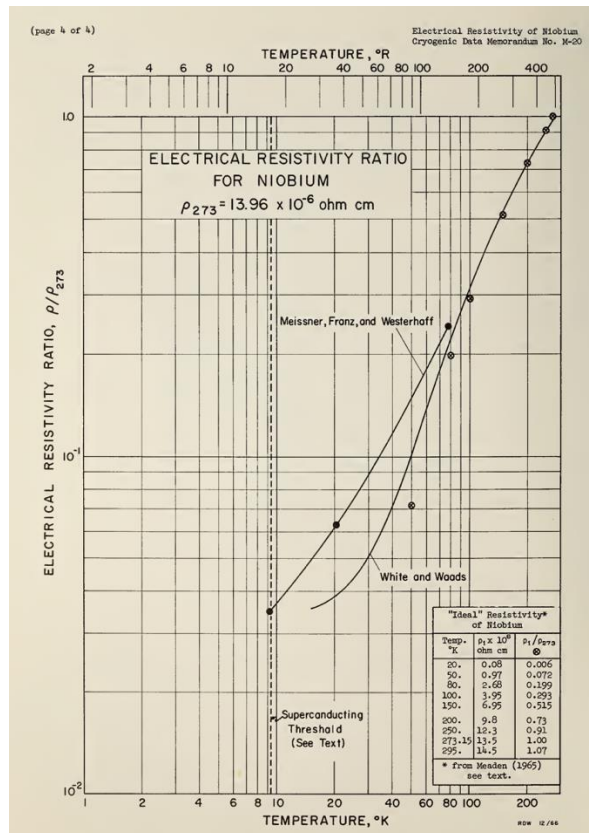
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Cooling down to reduce electric loss

Superconducting (Hg)

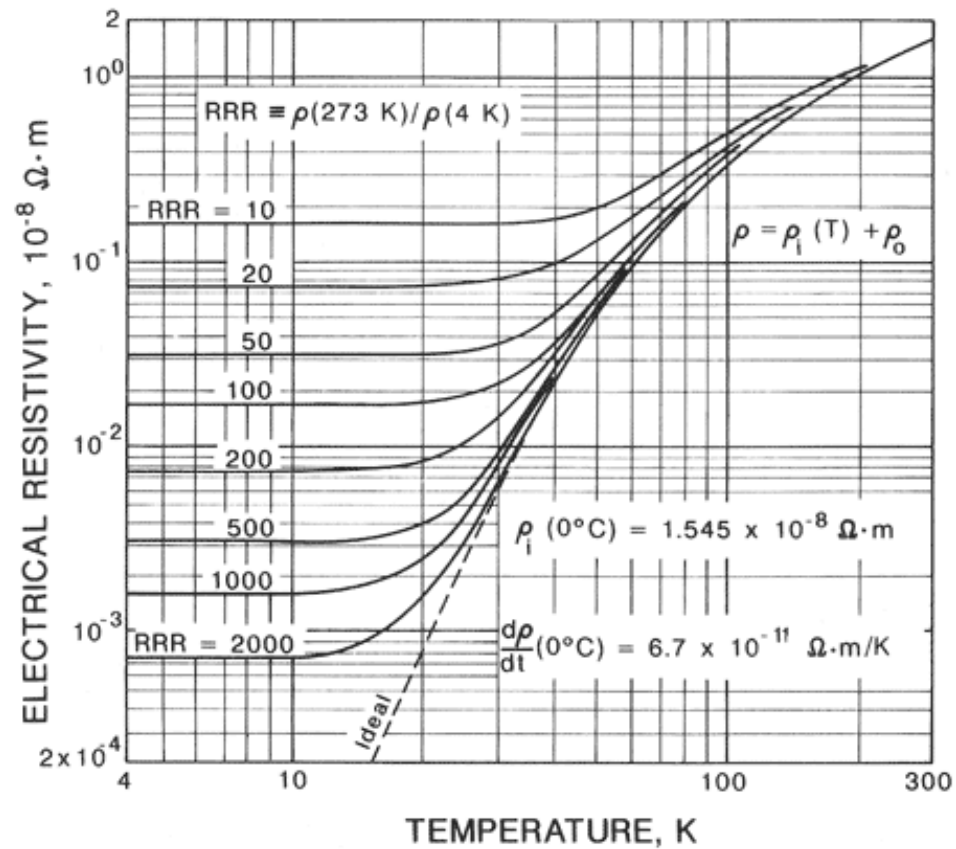


Niobium



<https://nvlpubs.nist.gov/nistpubs/Legacy/TN/nbstechnicalnote365.pdf>

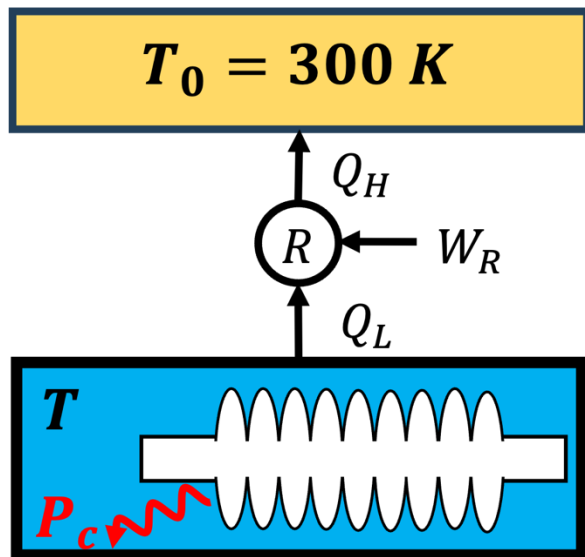
Copper



<https://www.copper.org/resources/properties/cryogenic/>

Cost of ideal cryogenics

Cooling power 1 W depends on temperature



Carnot's theorem

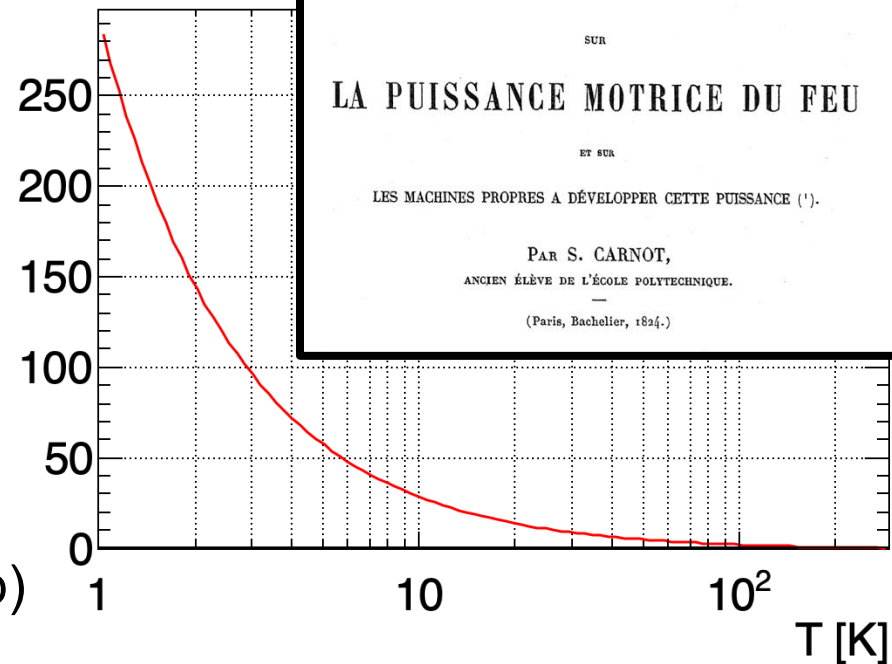
$$\beta = \frac{Q_L}{W_R} = \frac{Q_L}{Q_H - Q_L} = \frac{T}{T_0 - T}$$

Required power

$$P_{cryo} > \frac{P_c}{\beta}$$

(be careful about logical jump)

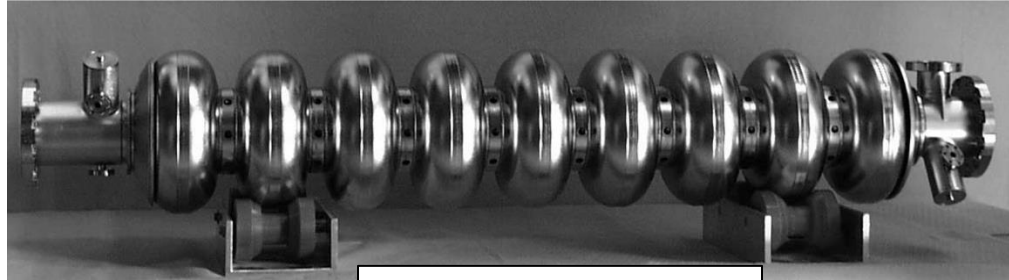
$1/\beta$



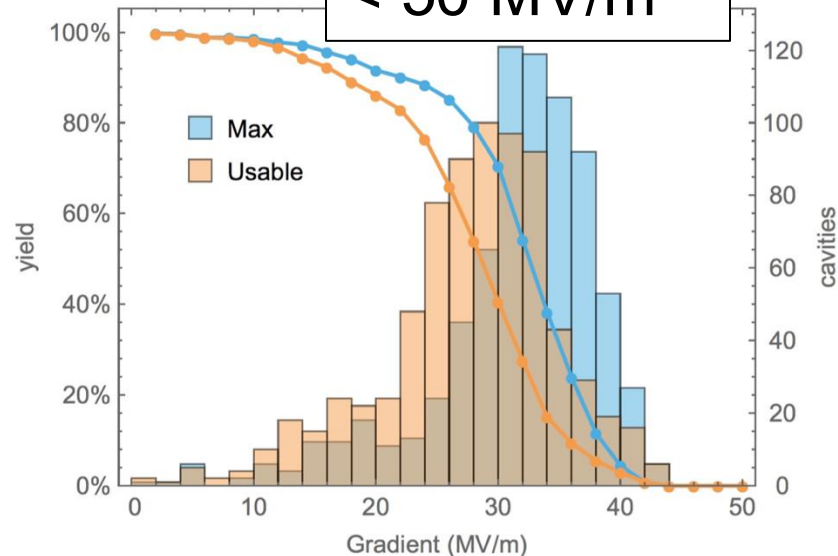
- We may need >150 W to evacuate 1 W from 2 K
- Cryogenics is an option if the resistance is improved better than this factor
 - Or some applications (eg superconductors) are not feasible at warm

Case study: superconducting vs normal conducting cavities

Superconducting niobium cavities (TESLA)

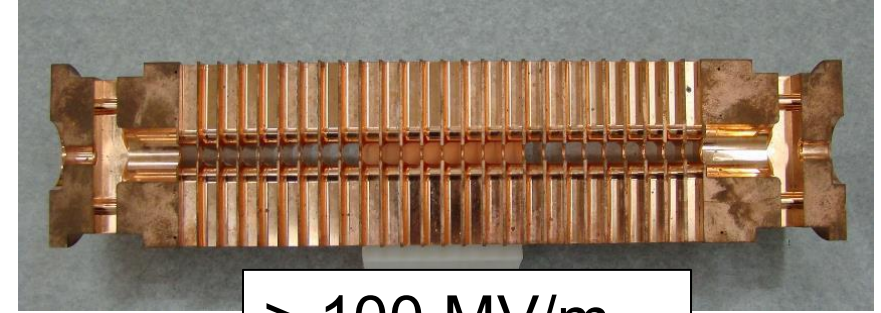


$< 50 \text{ MV/m}$

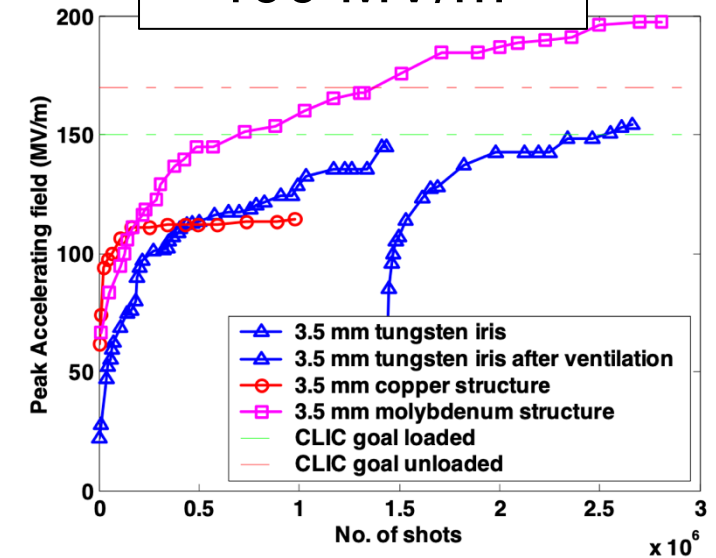


PHY REV ST - ACCEL BEAMS, **3**, 092001 (2000)
PHY REV ACCEL BEAMS **20**, 042004 (2017)

Normal conducting copper cavities



$> 100 \text{ MV/m}$



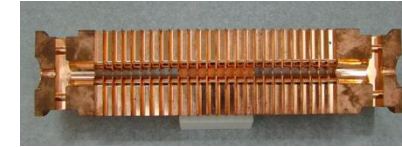
Courtesy: Walter Wuensch

$> \times 2$

Aperture

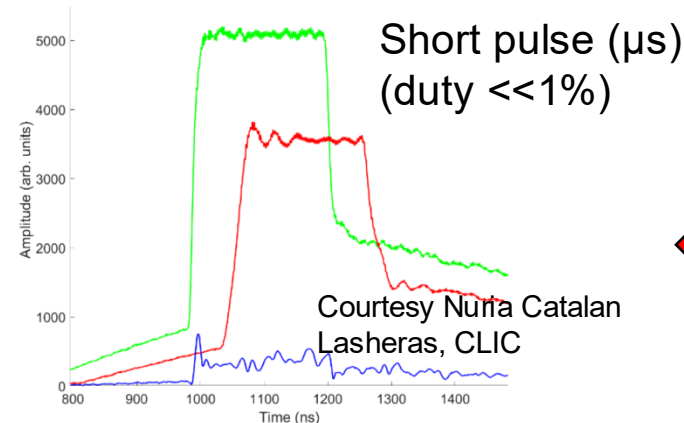
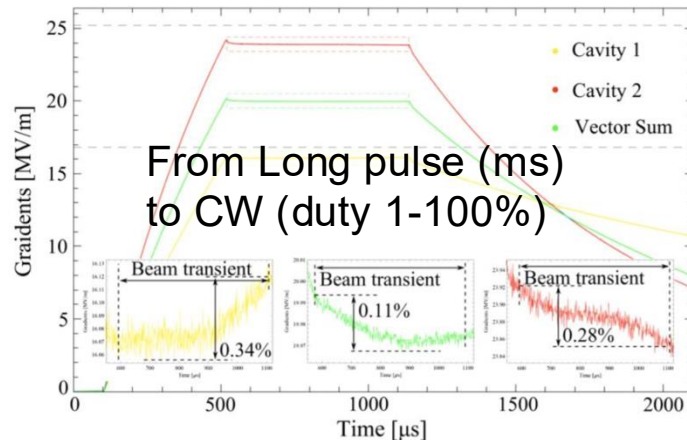


Superconducting cavities have high gradient at low frequency
→ large aperture (ILC: $\phi 70$ mm)



Normal conducting cavities are efficient at high frequency
→ small aperture (CLIC X-band: around $\phi 3$ mm)

Pulse length and duty cycle



SC cavities' quality factor

$\times 10^6$

than copper cavities
→ power dissipation

$\times 10^{-6}$

but in **cryogenics!**

SC vs NC cavities and cooling

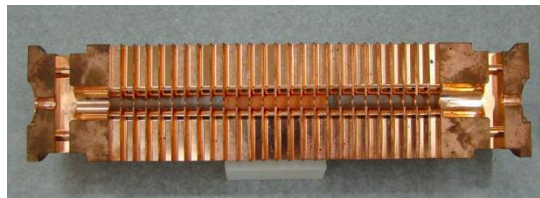


SC cavities

$P_c = 100 \text{ W (CW)}$

Duty cycle 10^{-2}

$T = 2 \text{ K}$

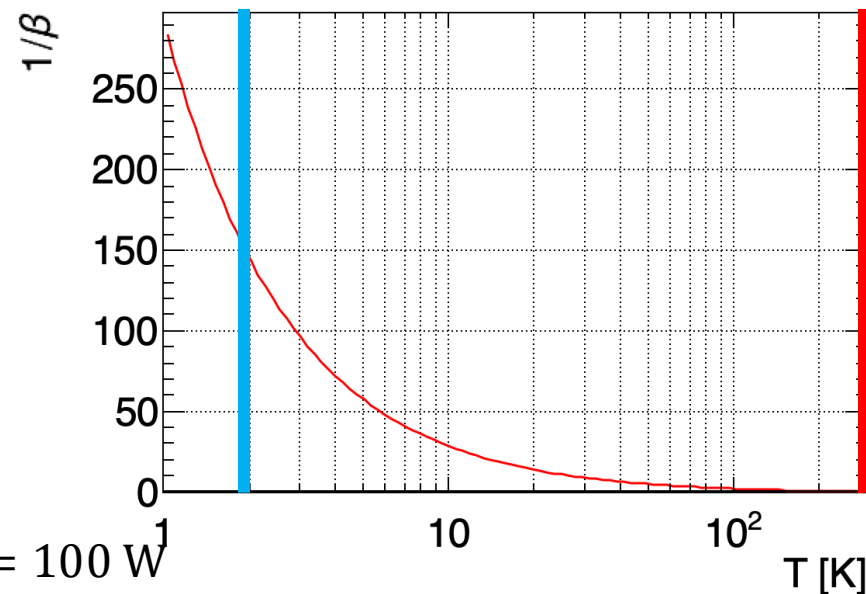


NC cavities

$P_c = 10 \text{ MW (CW)}$

Duty cycle 10^{-5}

Water cooling



$$P_{NET} \sim 100 \text{ W} \times 1\% \times 150 = 150 \text{ W} \quad P_{NET} \sim 10 \text{ MW} \times 10^{-5} \times 1 = 100 \text{ W}$$

- Short pulsed NC cavities and long pulsed SC cavities are similar in power consumption
 - If we need very long pulse or CW beam (LEP, FCCee, LCLSII) → SC cavities
 - If we need very short pulse beam (LCLS) → NC cavities
 - If we need CW but with low energy (may storage rings) → NC cavities
- Linear colliders are on the boarder: both SC (ILC) and NC (CLIC) may be OK

Carnot cycle is unrealistic at all

Thermodynamics does not include characteristic time constant

→ Carnot cycle gives maximum efficiency in quasi-static process ($\Delta t \rightarrow \infty$)

→ Power (work per time) is in trade off with the efficiency

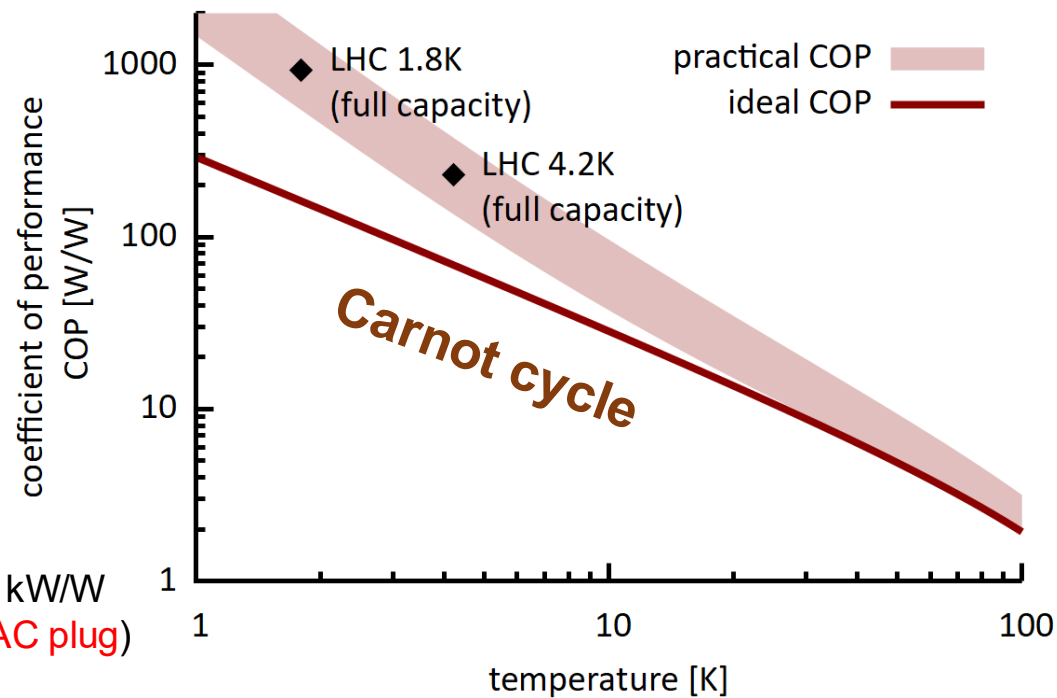
PRL117 190601 (2016)

$$P_c \leq \bar{\Theta} \beta_L \eta (\eta_c - \eta)$$

We lose useful power if efficiency η is too good approaching to Carnot η_c

In addition, more practical limitations further degrade the efficiency

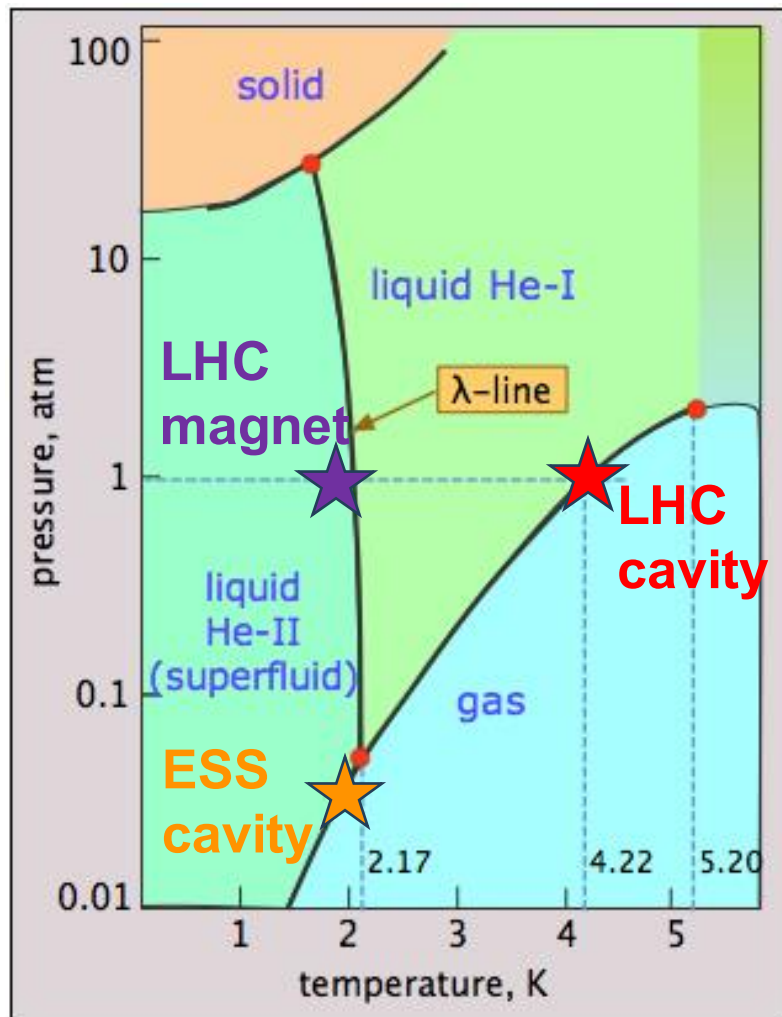
→ Around 1 kW is necessary to evacuate 1 W from 2 K (typically 5 kW/W @ 2 K for AC plug)



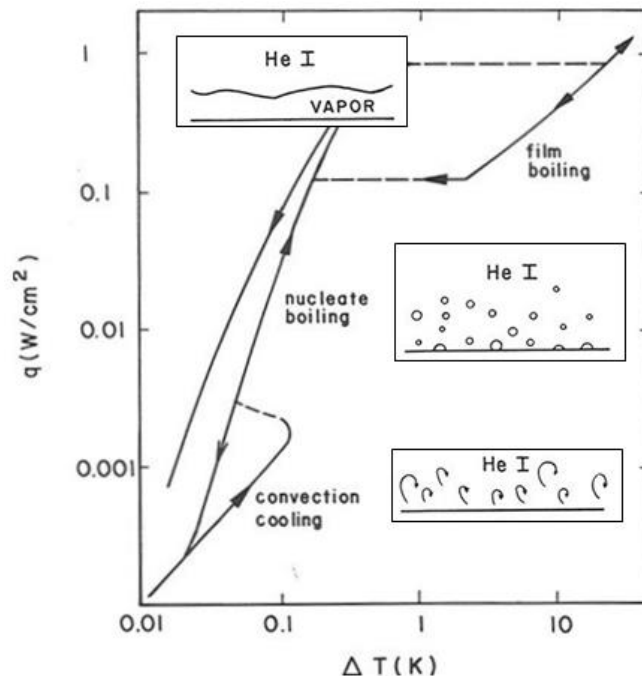
→ If the power loss of the device improves by $>10^3$ by cooling, 2 K operation is beneficial

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Cavities and magnets are in liquid helium

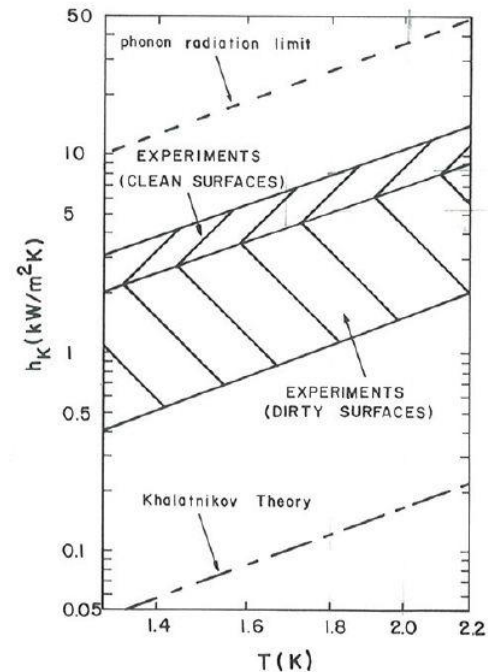


Normal helium (He-I)



$\sim 100 \text{ W}/\text{m}^2/\text{K}$

Superfluid helium (He-II)



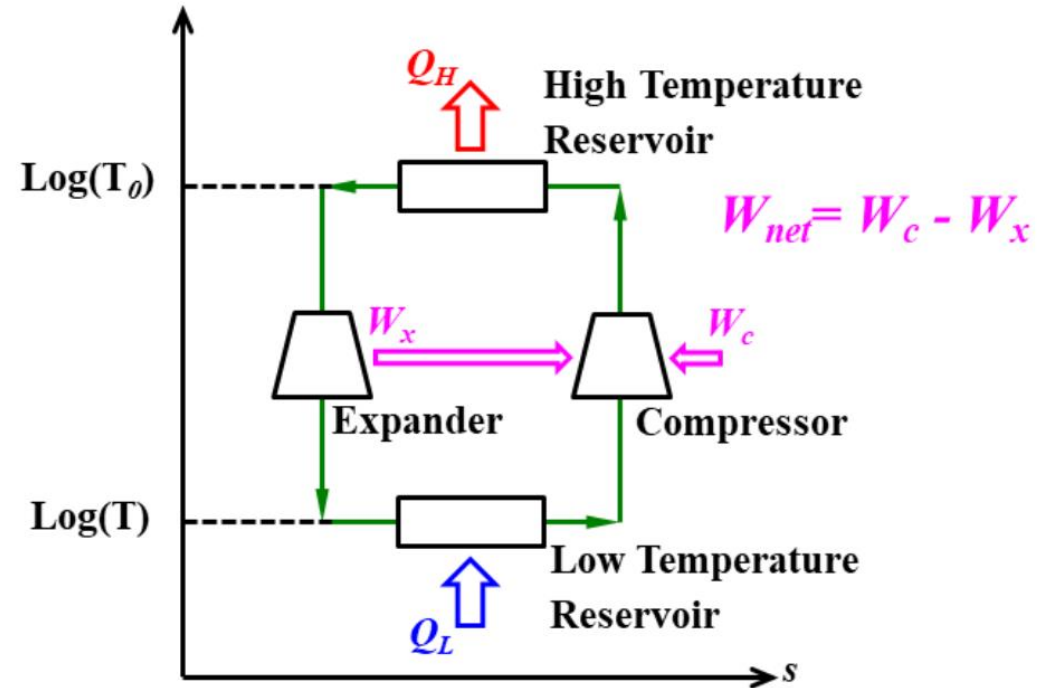
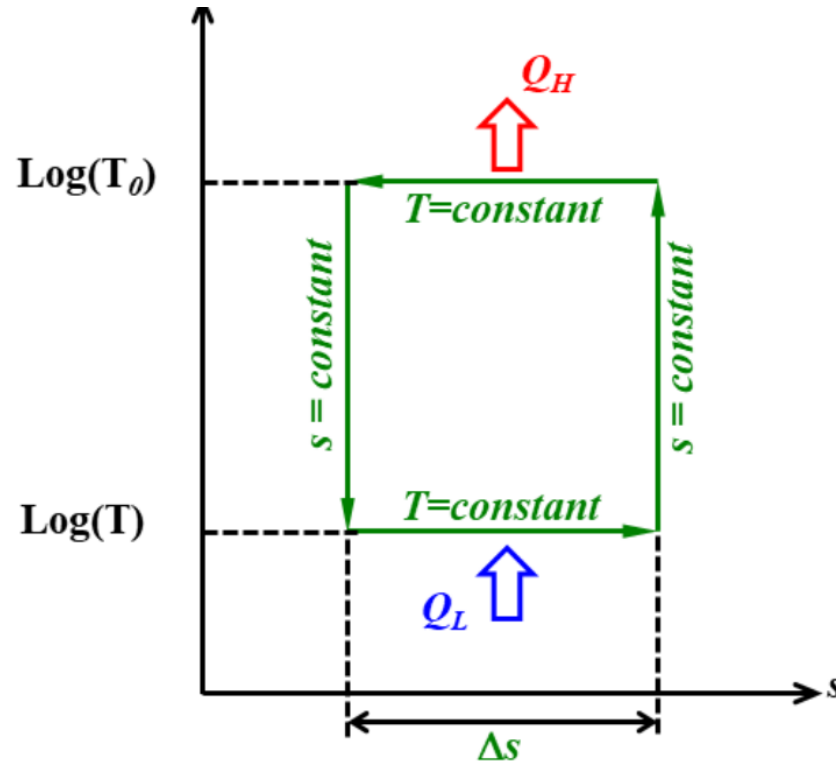
$\sim 5000 \text{ W}/\text{m}^2/\text{K}$

We need to liquify gas helium!

S. W. Van Sciver, "Helium cryogenics", Plenum press, 1986

Ideal cooling cycle: Carnot cycle

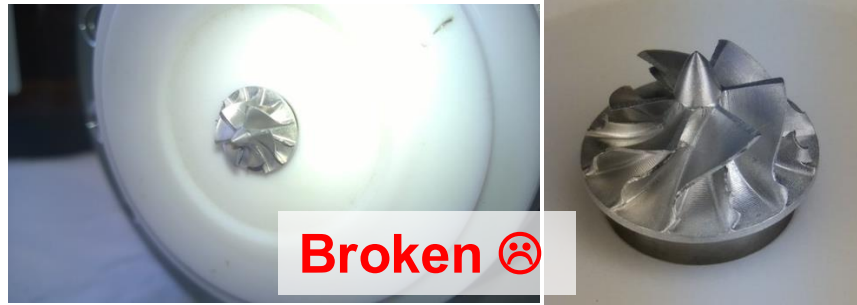
Courtesy: Nusair M. Hasan



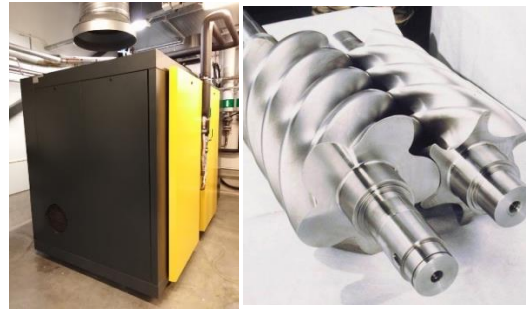
- Combination of adiabatic and isothermal processes
- Expander & compressor are the key components
- A Carnot cycle could theoretically generate LHe but requires unrealistically high pressure

Turboexpander (expansion turbine)

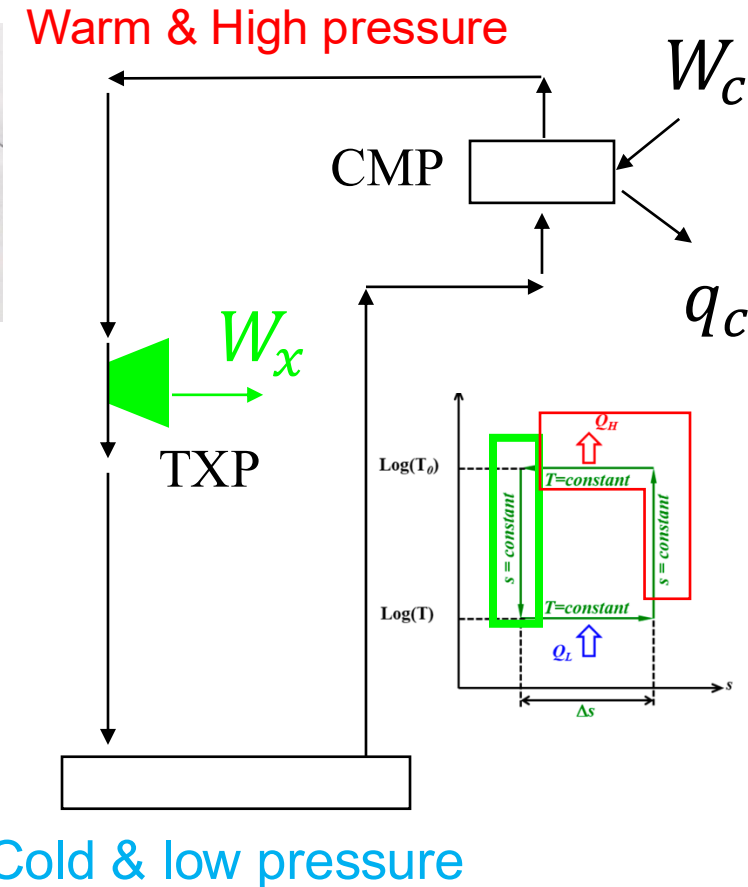
Courtesy: M. Pierens



Compressor



Reversed-modified Joule (Brayton) cycle



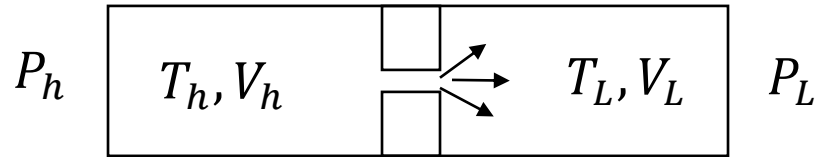
isentropic (=reversible adiabatic) expansion

Remarks

- Isobar process \rightarrow Joule cycle \neq Carnot cycle
 - Weak points (and expensive!) of a cryogenic facility
 - If your accelerator is down, maybe one of them are out of order
 - Not used for liquefaction of helium alone practically
 - Turbine does not like LHe
- \rightarrow Another process needs to be combined

Adiabatic expansion and Joule Thomson effect

Joule-Thomson (JT) process is isenthalpic (irreversible adiabatic)



$$H = U_h + P_h V_h = U_L + P_L V_L$$

JT coefficient

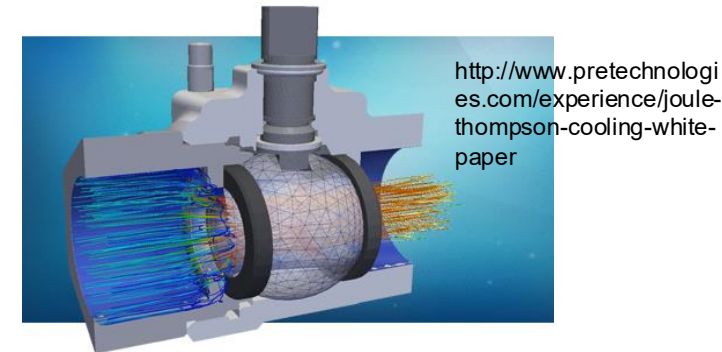
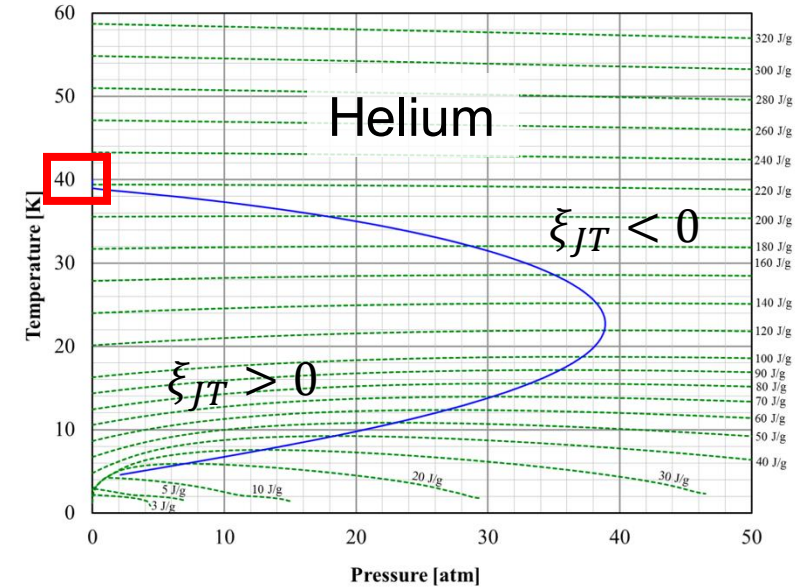
$$\xi_{JT} = \left(\frac{\partial T}{\partial P} \right)_H$$

$\xi_{JT} < 0 (\rightarrow T_h < T_L)$: heating
 $\xi_{JT} > 0 (\rightarrow T_h > T_L)$: cooling

$\xi_{JT} = 0$ at reverse temperature

He Liquefier is made of i) compressor ii) turbine iii) JT valve

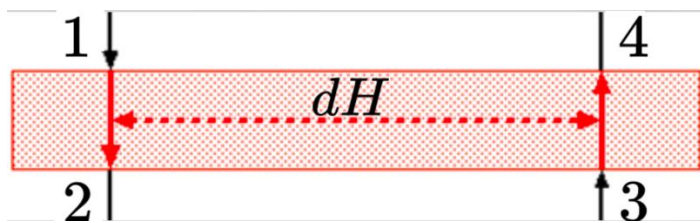
Adiabatic \neq isentropy ($ds \geq d'Q/T$)



Heat exchanger for pre-cooling

Heat exchanger profits from cold return gas to enhance the liquefaction yield

$$H_4 = H_3 + dH$$



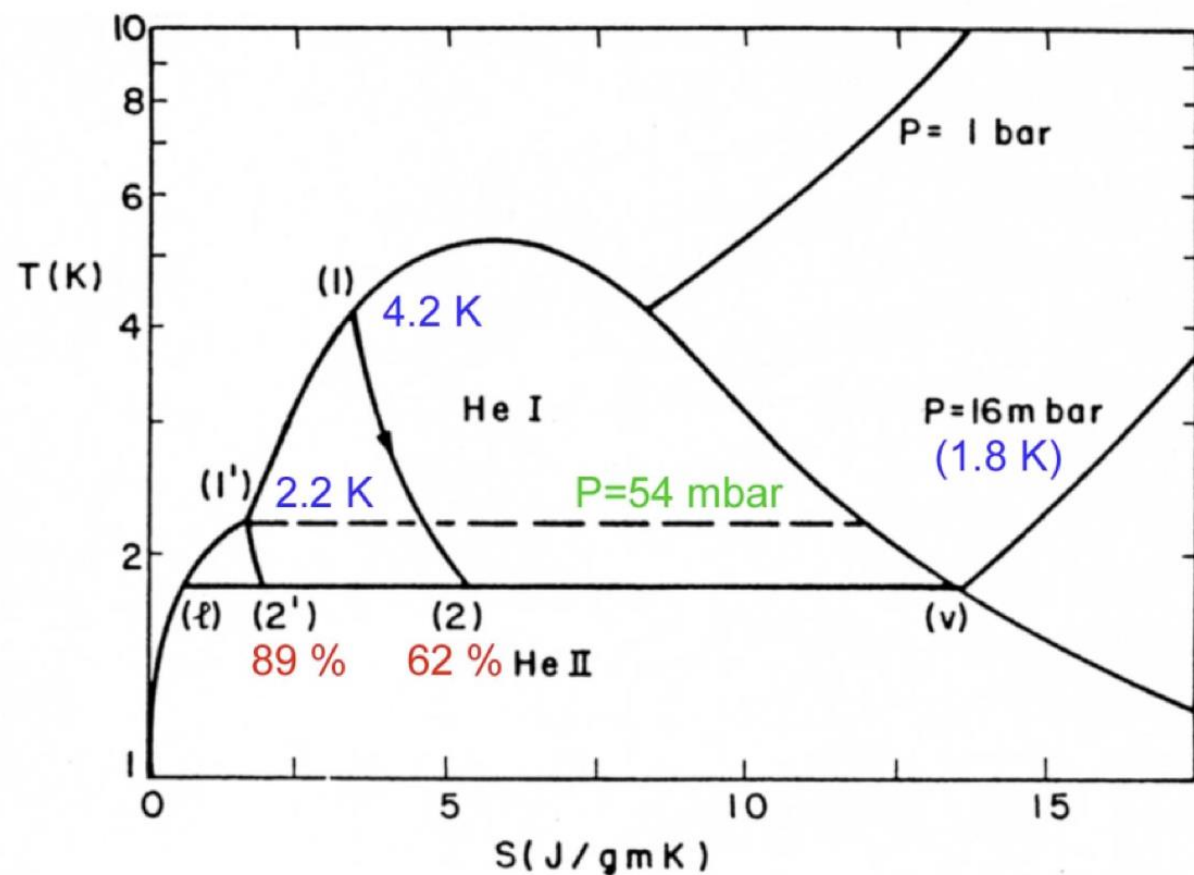
$$H_2 = H_1 - dH$$

If temperature before the JT valves is

- 4.2K \rightarrow 62%
- 2.2K \rightarrow 89%

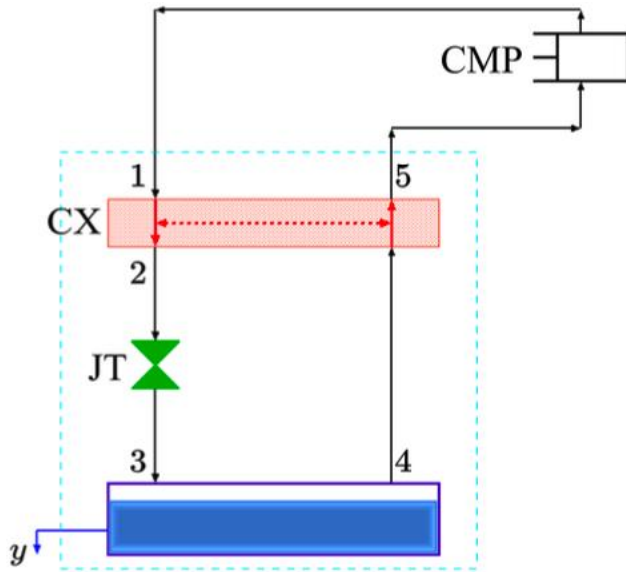
Superfluid is generated by pumping down to 30 mbar

Courtesy: Elias Waagaard

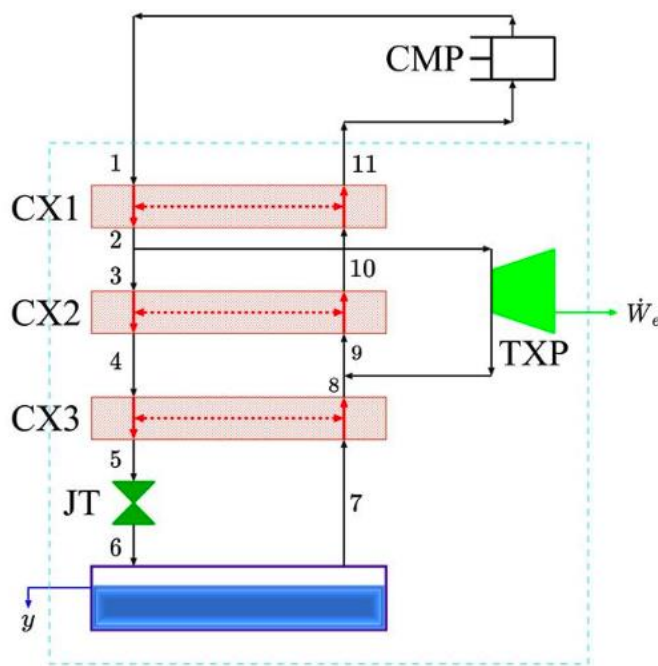


Van Sciver S. W. "Helium Cryogenics", Plenum Press (1986)

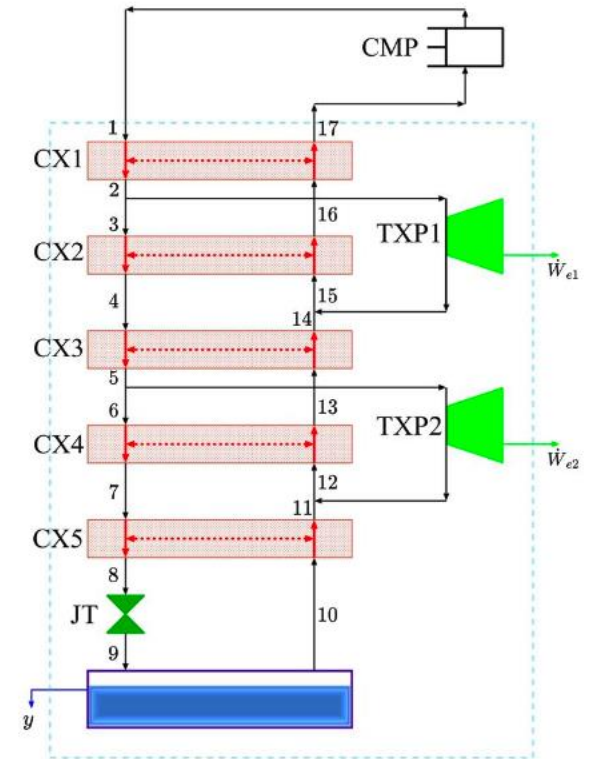
Linde cycle



Claude cycle



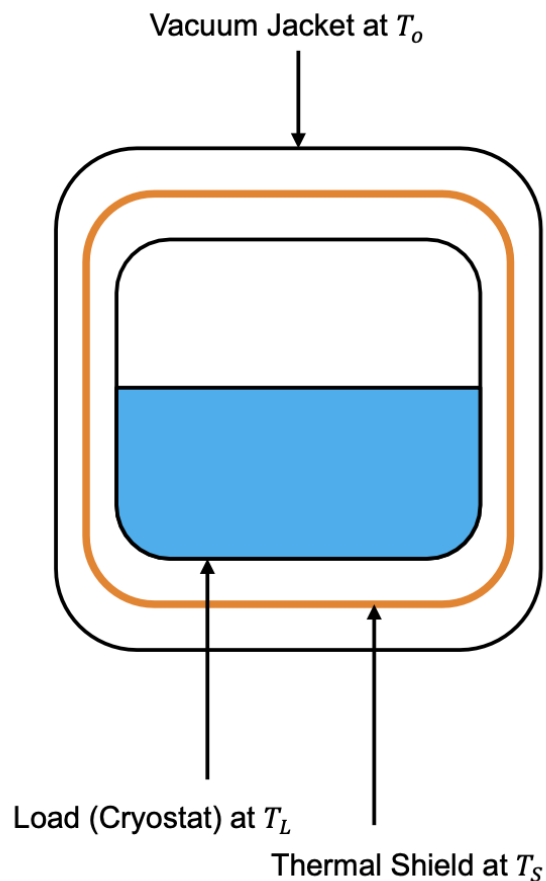
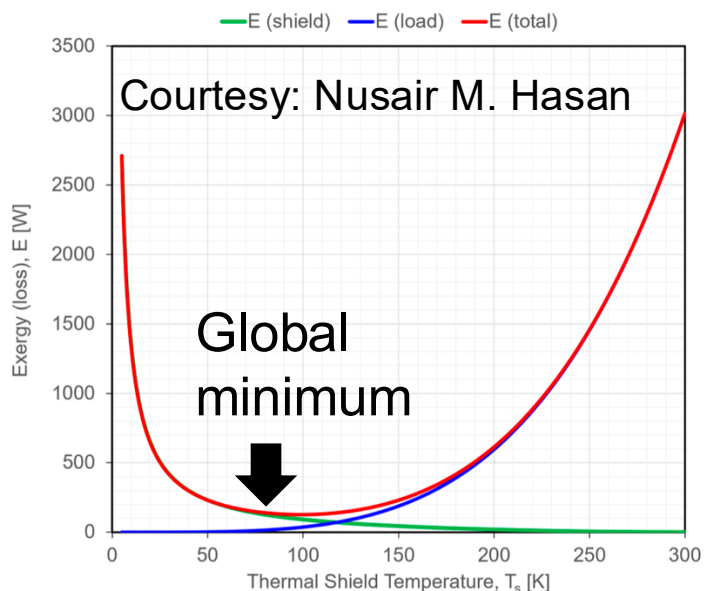
Collins cycle



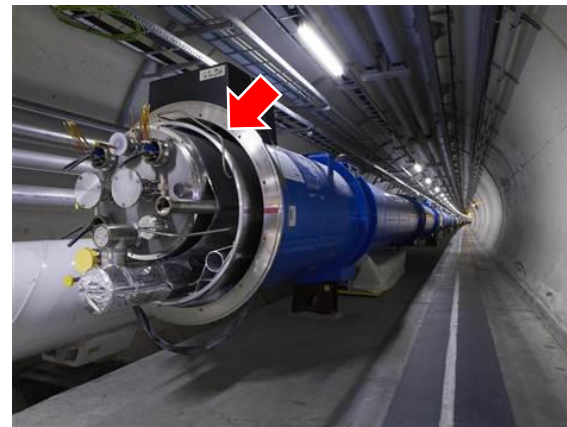
Courtesy: Elias Waagaard

Stephan Boltzmann: $q = \epsilon A \sigma T^4$

- Intercept the thermal radiation by intermediate temperature
- Easier to evacuate heat at higher temperature



Multilayer Insulation (MLI)



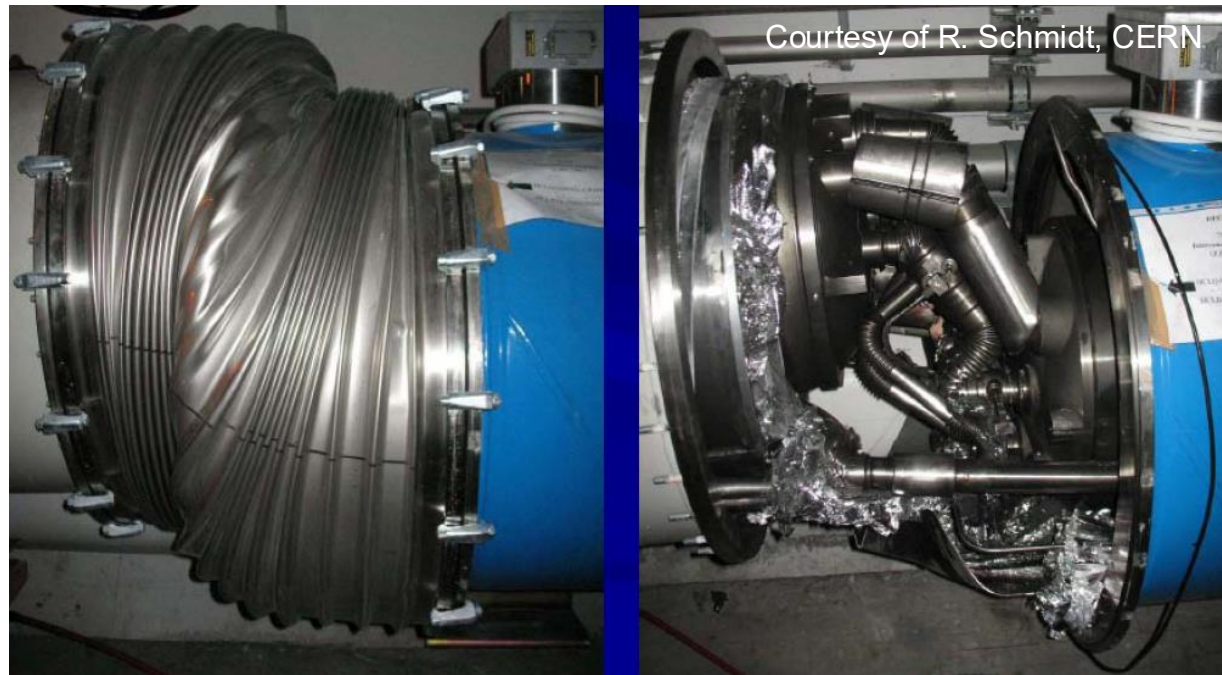
LHC dipole

3 months after I got a staff position



High power RF → SC cavity quenched by multipacting → wrong interlock setup → Overpressure in LHe → Rupture disk burst → no mechanical damage

3 months after I started PhD in particle physics



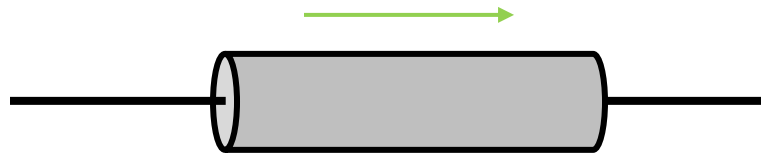
Courtesy of R. Schmidt, CERN

Defect in soldering joint → resistive (magnet quench itself was NOT the trigger) → Electrical arc → He goes into isolation vacuum → helium boiled off → mechanical damage

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Ohm's law

Applied DC electric field E



DC Current J

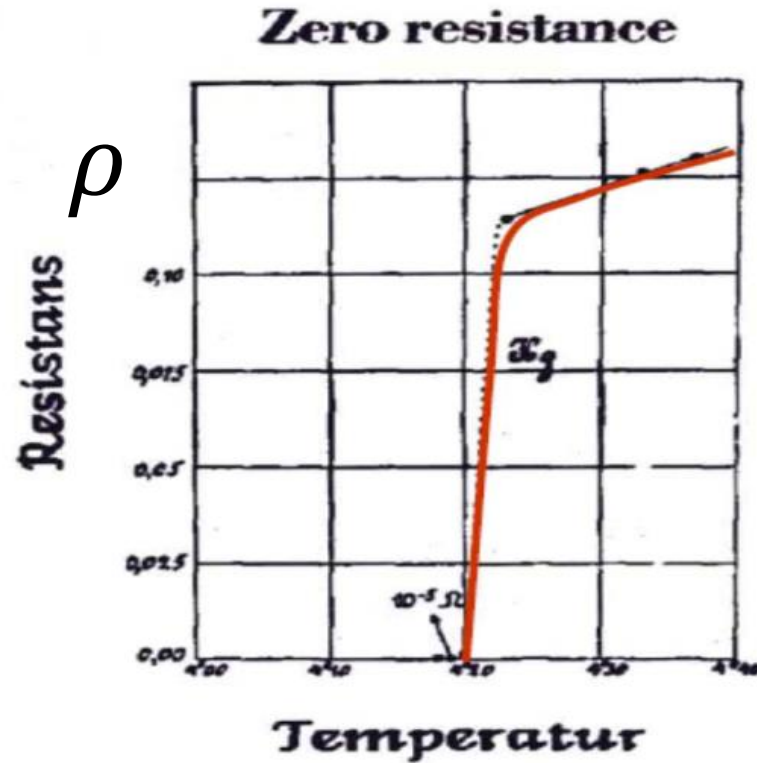
DC resistivity ρ

$$\rho \equiv \frac{E}{J}$$

DC conductivity σ

$$\sigma = \frac{1}{\rho} \equiv \frac{J}{E}$$

Cool down the resistor...



Heike Kamerlingh Onnes

Nobel prize in 1913

$\rho = 0$ below transition temperature T_c

Challengers for microscopic theory of superconductors

J. Schmalian, arxiv:1008.0447



Albert Einstein
(1879-1955)



Niels Bohr
(1885-1962)



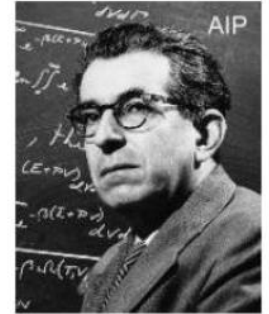
Ralph Kronig
(1905-1995)



John Bardeen
(1908-1991)



Werner Heisenberg
(1901-1976)



Fritz London
(1900-1954)



Lev D. Landau
(1908-1968)



Felix Bloch
(1905-1983)



Léon Brillouin
(1889 -1969)



Max Born
(1882-1970)



Herbert Fröhlich
(1905-1991)

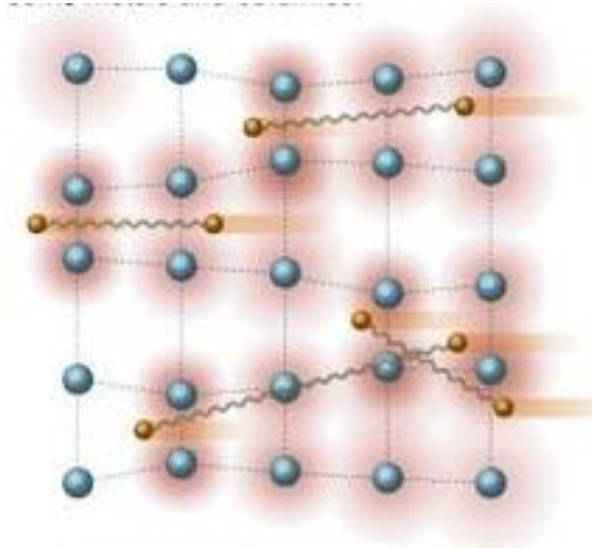
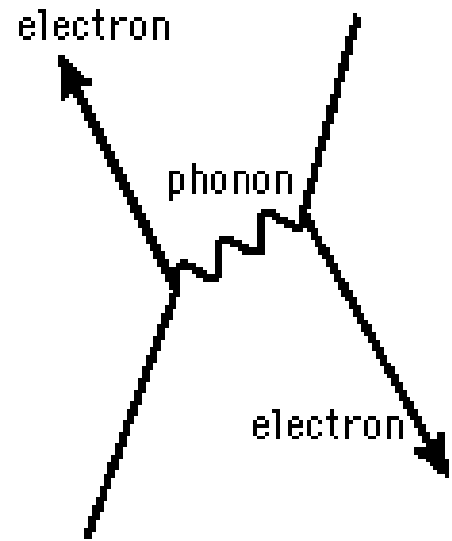


Richard Feynman
(1918-1988)

A lot of models...all failed ☹️

Development of quantum field theory in many body problems was necessary...

Theory of superconductor in equilibrium



John Bardeen



Leon Cooper



John Robert
Schrieffer

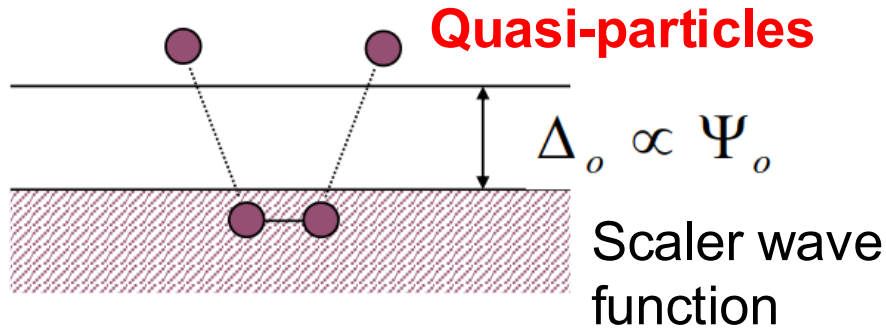
Cooper pair: Composite boson

Two electrons are bounded by something (phonon) \rightarrow effective Hamiltonian \mathcal{H}_{BCS}

Mean field approximation + Variational method (+other approximations...)

$$\mathcal{H}_{BCS}|\Phi_0\rangle = E|\Phi_0\rangle$$

Solution: superconducting gap



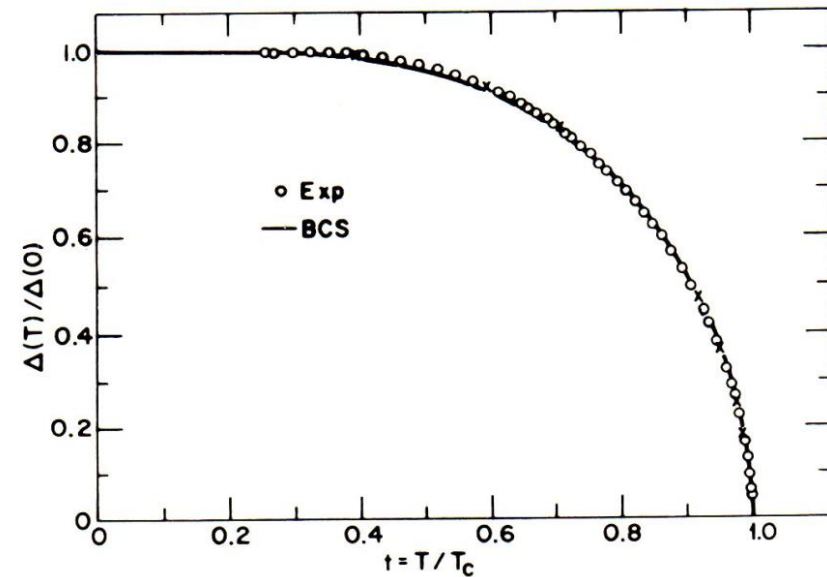
- The Cooper pair needs certain amount of energy to be broken
- The cause of Ohmic loss, stochastic scattering of one single electron by phonon or impurity **cannot break the pair**
→ No DC loss

The Equilibrium state of conventional superconductor was understood !

→ In this lecture, we try to obtain qualitative insight of the phenomenon

Self-consistent gap equation

$$\Delta = N(E_F)V \int_{\Delta}^{\hbar\omega_D} \frac{\Delta}{\sqrt{\xi^2 + \Delta^2}} \tanh\left(\frac{1}{2} \frac{\sqrt{\xi^2 + \Delta^2}}{k_B T}\right) d\xi$$





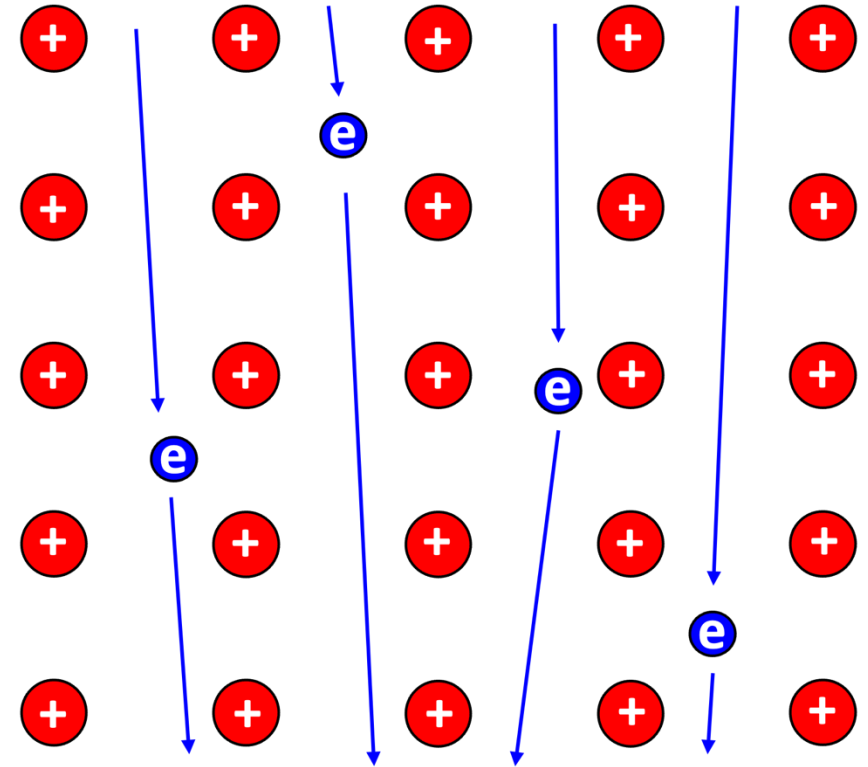
Electrons in a perfect metal are free (independent)

Perfectly periodic potential by ions does **NOT** scatter electrons (Bloch's theorem)

These electrons are **NOT** our favorite elementary particle of

$$m = 511 \text{ keV}$$

These electrons are **dressed** by complicated electromagnetic property of metals to have an effective mass m^* given by a band structure
→ **Quasi-particles**



In reality, imperfection causes quasi-particle scattering

Electrons in a real metals show Ohmic loss

Imperfections causes **local** scattering

1. Impurity, defects (scattering time τ_{def})
2. Lattice vibration, phonon (τ_{ph})

Total scattering time

$$\frac{1}{\tau} = \frac{1}{\tau_{def}} + \frac{1}{\tau_{ph}}$$

Macroscopic phenomenology (Drude model)

An electron accelerated by an electric field

$$m^* \frac{dv}{dt} = -eE$$

is scattered by imperfections per τ , and its velocity relaxes to a mean velocity

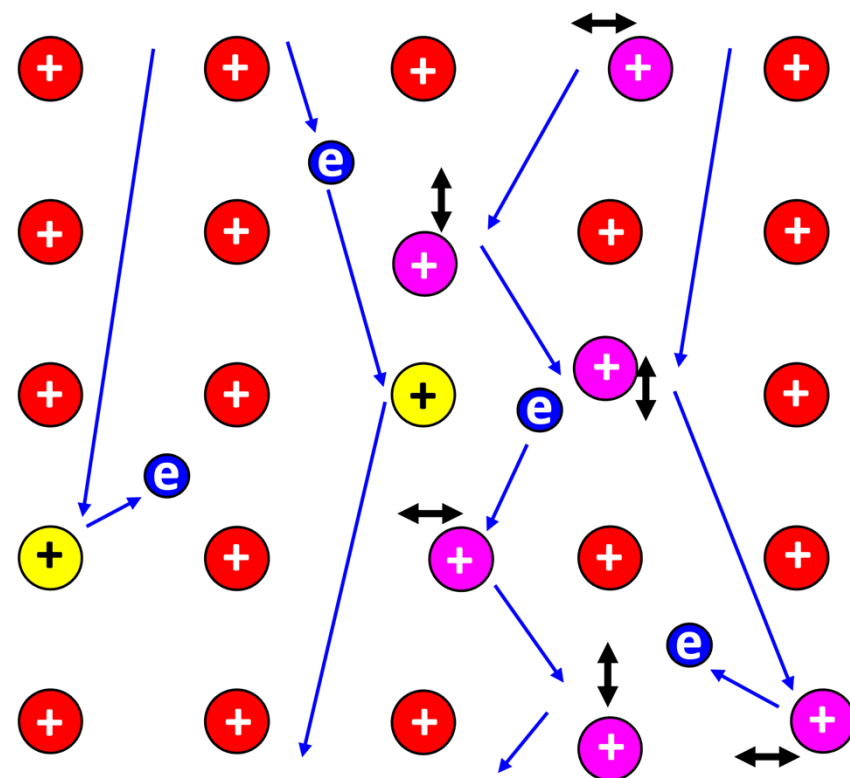
$$\langle v \rangle = -\frac{e}{m^*} E \tau$$

Electric current is a collective flow of n electrons

$$j = -en\langle v \rangle = \frac{e^2 n \tau}{m^*} E \quad \text{Ohm's law}$$

Electrical conductivity σ

$$j = \sigma E$$



Paired electrons can avoid Ohmic loss

If electrons *in a distance* (>39 nm) are bounded, *local* (< 0.5 nm) scattering can be avoided

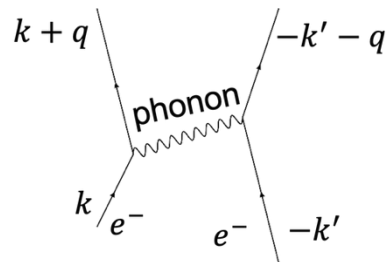
Any small attractive interaction V between electrons can lead to a **Cooper pair** coupled with an energy 2Δ , below critical temperature T_c

BCS gap equation (1957)

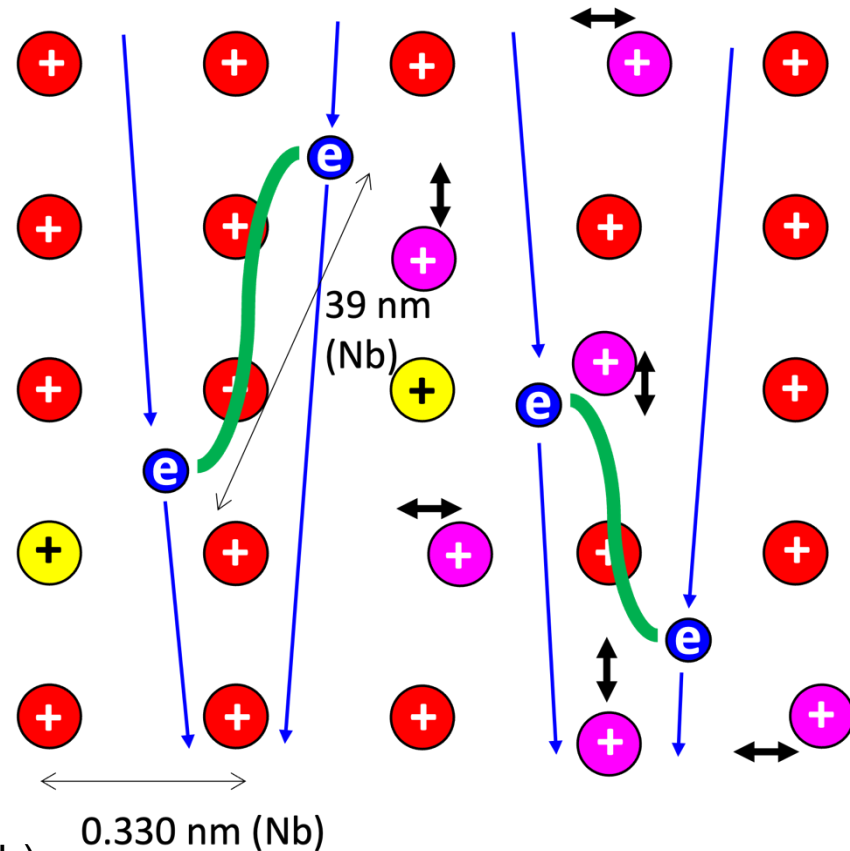
Non-perturbative!

$$\Delta = n(E_F)V \int_{\Delta}^{\hbar\omega_D} \frac{\Delta}{\sqrt{\xi^2 + \Delta^2}} \tanh\left(\frac{1}{2} \frac{\sqrt{\xi^2 + \Delta^2}}{k_B T}\right) d\xi$$

Classical superconductors' attractive potential is from **longitudinal mode of lattice vibration**



If energy transfer $|\epsilon_{k+q} - \epsilon_k|$ is smaller than phonon energy the interaction is attractive (Flöhlich)
 \rightarrow Eliashberg's strong coupling superconductor (1960)



Implication of no scattering?

No scattering

$$m^* \frac{\partial \langle v \rangle}{\partial t} = -eE$$

generates super-current

$$j_s = -en_s \langle v \rangle$$

$$\rightarrow \frac{\partial j_s}{\partial t} - \frac{n_s e^2}{m^*} E = 0$$

Apply $\nabla \times$ from the left

$$\frac{\partial}{\partial t} (\nabla \times j_s) - \frac{n_s e^2}{m^*} \nabla \times E = 0$$

$\sim \nabla \times \mathbf{B} / \mu_0$

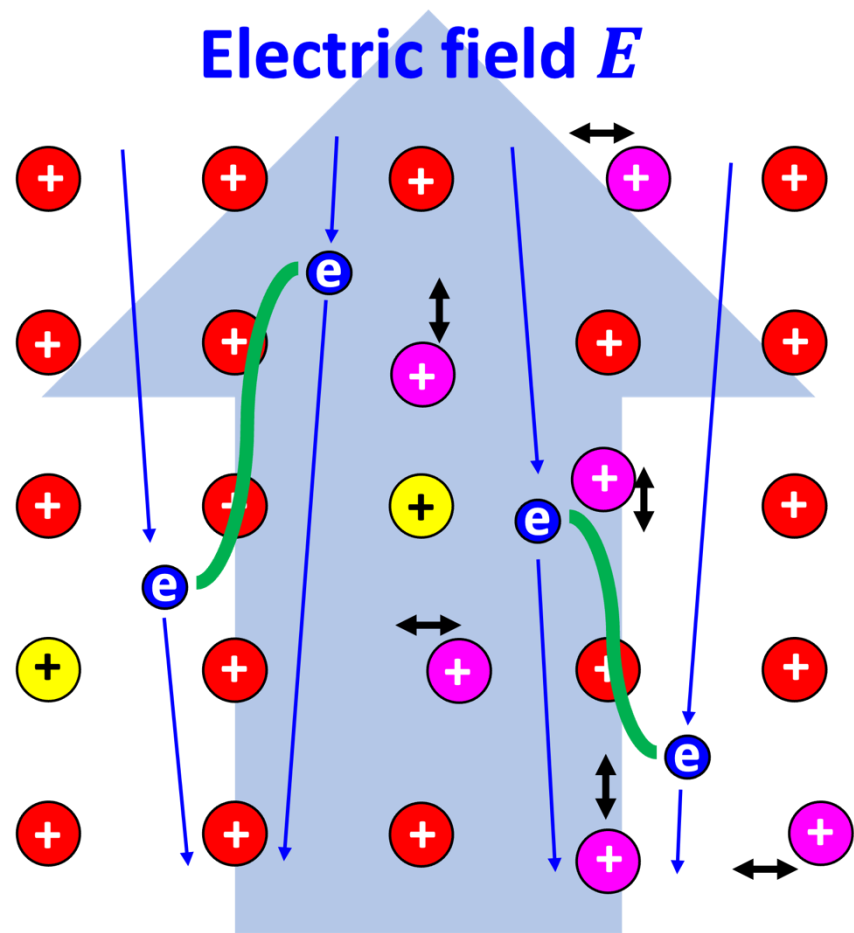
leads to

$$\frac{\partial}{\partial t} \left[\nabla^2 \mathbf{B} - \frac{1}{\lambda_L^2} \mathbf{B} \right] = 0$$

$$\lambda_L^2 \equiv \frac{m^*}{n_s e^2 \mu_0}$$

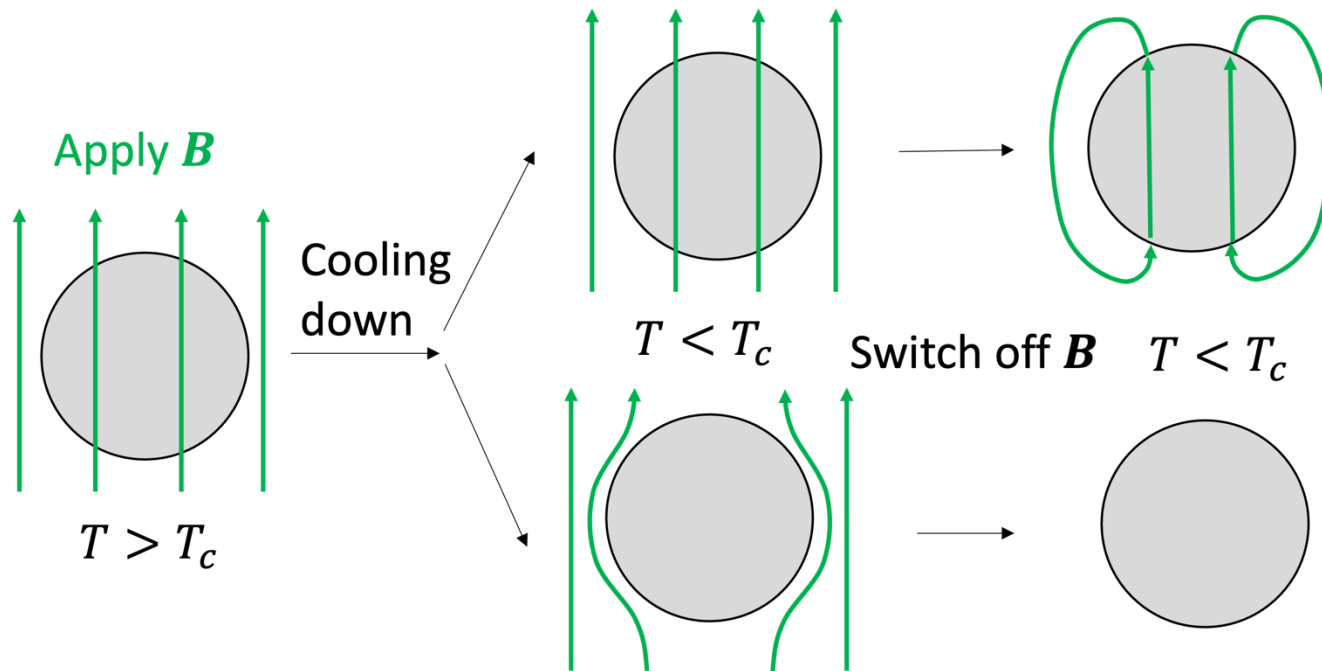
Constant of time

→ Initial condition before phase transition $T > T_c$ must be preserved



Superconductor \neq Perfect electric conductor

Meissner effect differentiates them



Perfect Electric Conductor

$$\nabla^2 \left(\frac{\partial \mathbf{B}}{\partial t} \right) - \frac{1}{\lambda_L^2} \left(\frac{\partial \mathbf{B}}{\partial t} \right) = 0$$

Preserve initial condition!

Superconductor

Zero field!

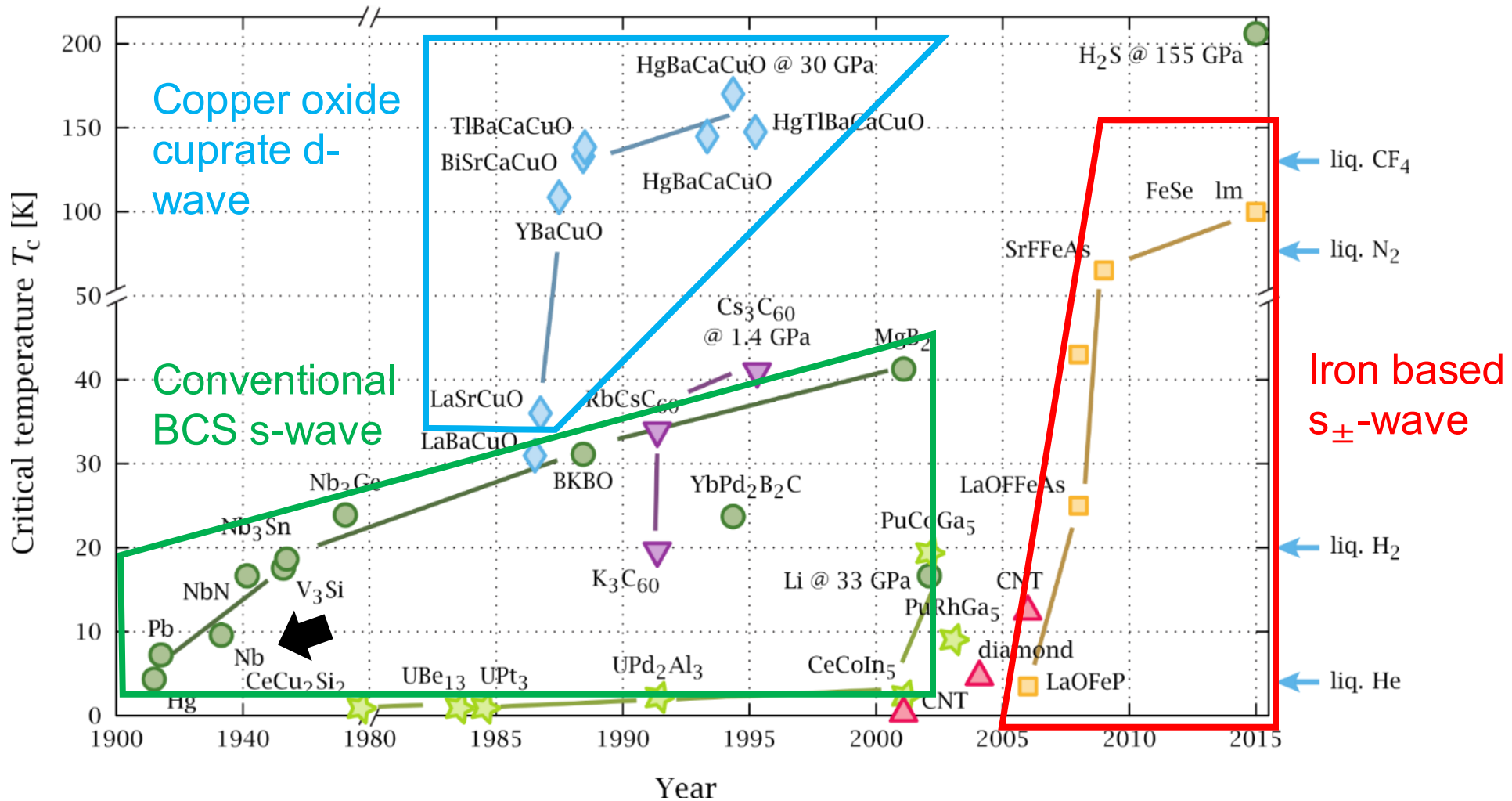
$$\nabla^2 \mathbf{B} - \frac{1}{\lambda_L^2} \mathbf{B} = 0$$

London equation (Additional constraint (broken Gauge symmetry))

Superconductivity is a thermodynamical state which expels magnetic fields and cannot be explained by classical electrodynamics \rightarrow beyond the scope of this lecture ☹

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BCS and non BCS superconductors



- **BCS superconductors (1911)**
 - Example: Hg, Al, Sn, Pb, Nb, NbN, NbTi, Nb₃Sn, ..., MgB₂ (?)
 - Phonon mediated Cooper pairs
 - Application: superconducting magnet, cavities, detectors, qubit
- **Cooper oxide superconductors (discovered in 1986)**
 - Example: YBCO, ...
 - Fundamental theory unknown (Coulomb repulsive force generates correlation ?)
 - Application: magnet, current lead, beam screen, dark matter detector, etc
- **Iron based superconductors (discovered in 2008)**
 - Example: Ba-122, FeSeTe, ...
 - Fundamental theory unknown (Spin interaction generates correlation ?)
 - Application: magnet, current lead, dark matter detector, cavities (?), etc
- **More fancy superconductors...**

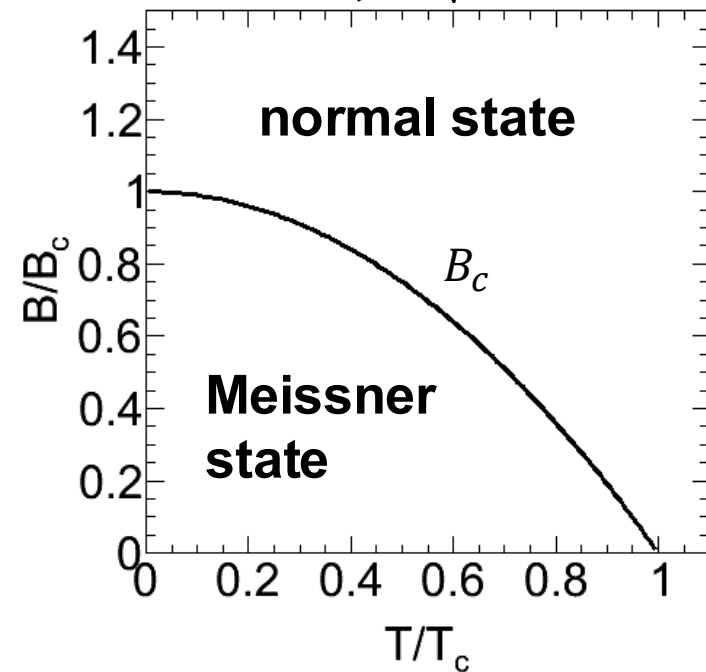
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Strong but *static* magnetic field: Type-I vs Type-II

Type-I

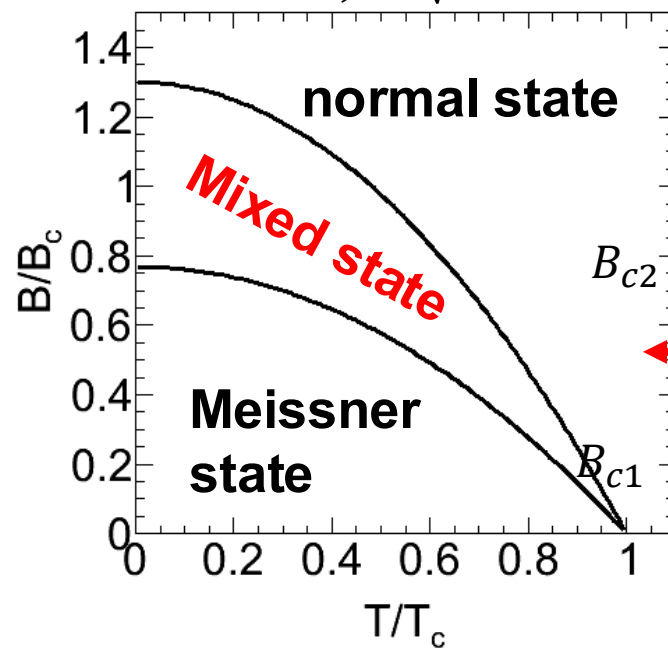
$$\kappa = \frac{\lambda}{\xi} < \frac{1}{\sqrt{2}} = 0.71$$



$$\kappa_{Pb} \sim \frac{28 \text{ nm}}{71 \text{ nm}} \sim 0.40$$

Type-2

$$\kappa = \frac{\lambda}{\xi} > \frac{1}{\sqrt{2}} = 0.71$$

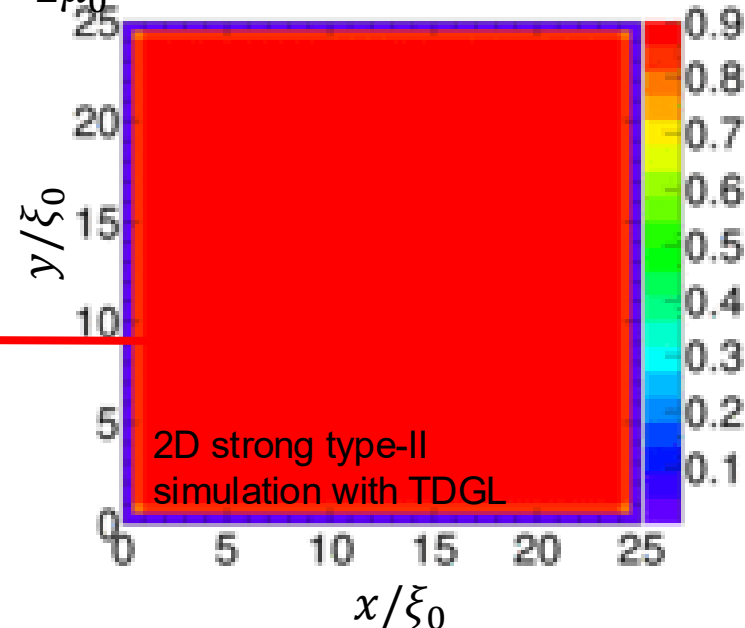


$$\kappa_{Nb} \sim \frac{36 \text{ nm}}{39 \text{ nm}} \sim 0.92$$

Quantized flux $\Phi_0 = \frac{h}{2e} = 2.07 \times 10^{-15} \text{ Wb}$

Stabilized by NC/SC boundary energy

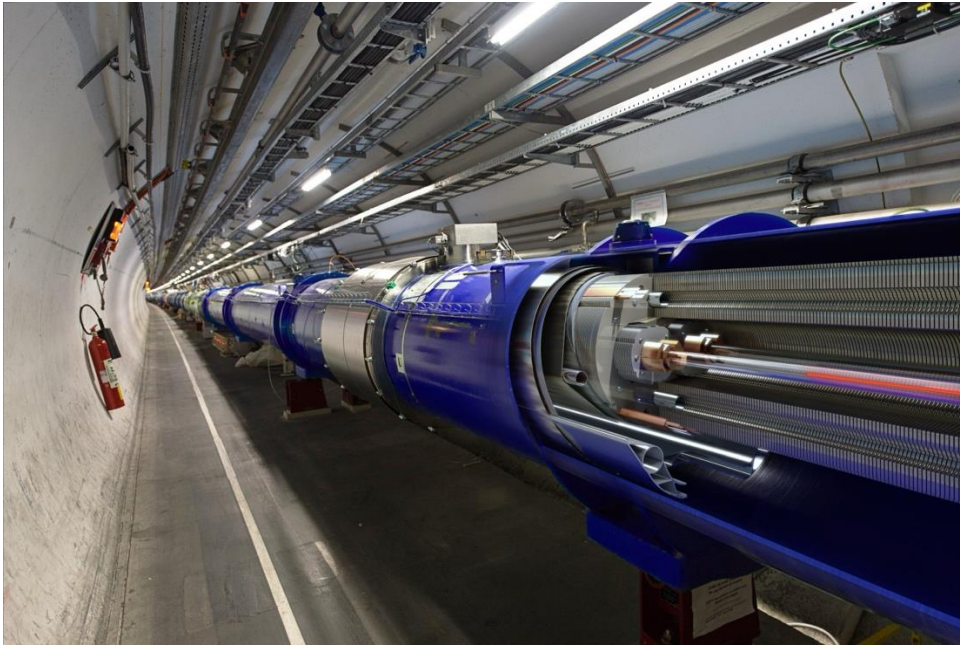
$$\frac{1}{2\mu_0} (\xi_0 B_c^2 - \lambda_L B^2) < 0 \text{ for } B > B_{c1}$$



Without pinning centers, type-II **traps** magnetic flux if $B > B_{c1}$

SC magnet and cavities in different states

DC Magnetic fields in magnets to bend the trajectory (**Mixed state**)



RF Electric fields in cavities to accelerate the beam (**Meissner state**)

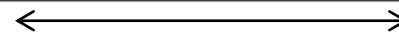
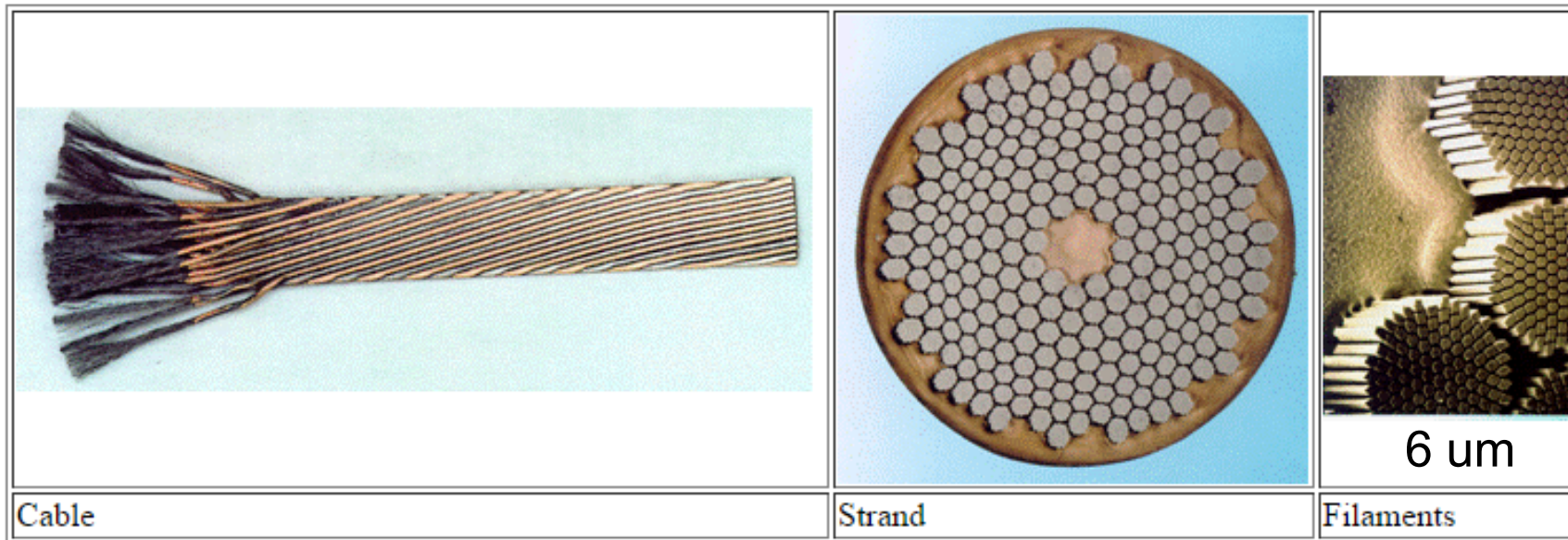


DC vs RF is qualitatively different in superconducting devices

SC magnet cables: made of filaments

Rutherford cable

NbTi filaments embedded in copper matrix for heat and current → LHC magnets



0.825 mm

6 μ m

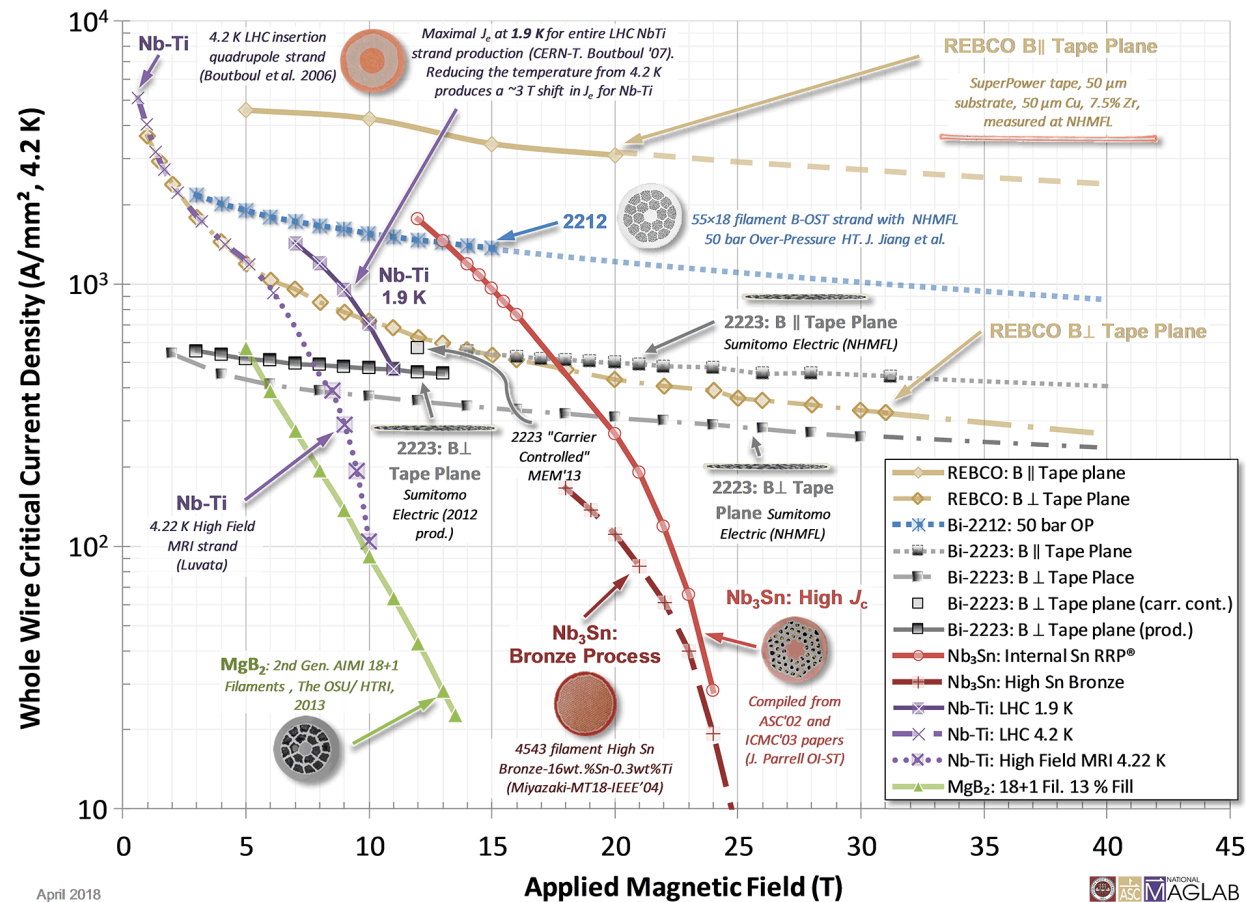
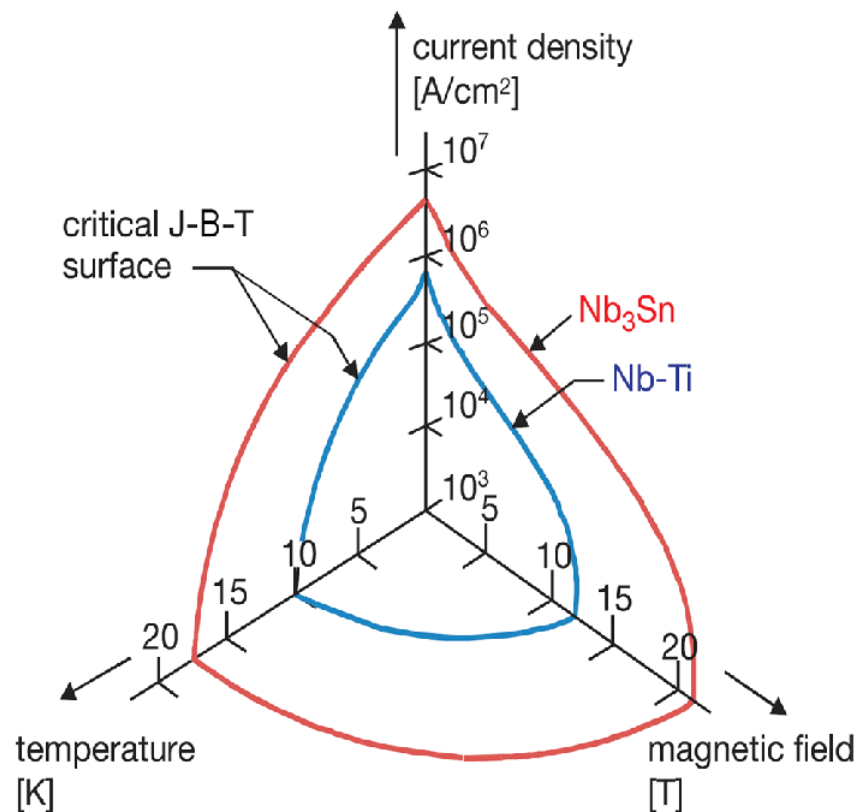
In LHC :

1200 magnets
 7600 km of cable
 36 strands per cable
 6400 filaments per strands

→ Total length of filaments
 10 times the distance
 between earth and sun !!!

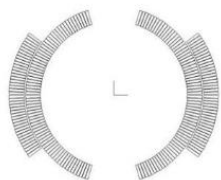
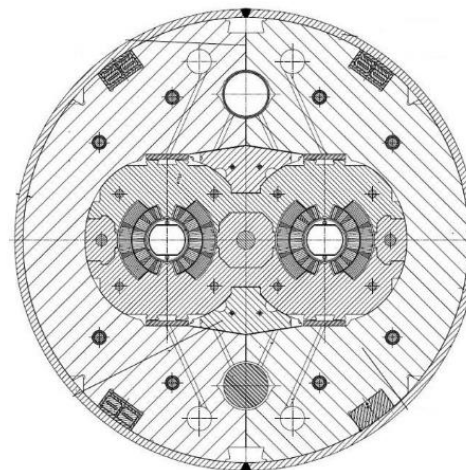
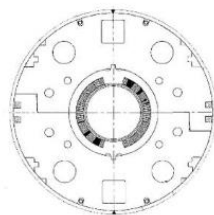
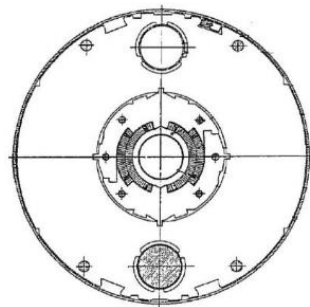
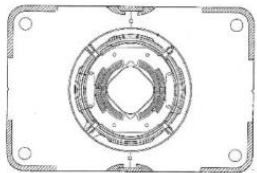
The NbTi materials is exposed to 8.3 T \gg H_{c1} at 1.9 K → Mixed state

Critical current density



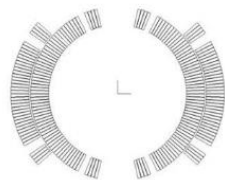
April 2018

SC dipole: history of NbTi



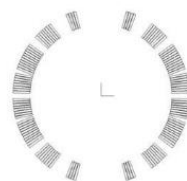
Tevatron

76 mm bore
B = 4.4 T
T = 4.2 K
first beam 1983



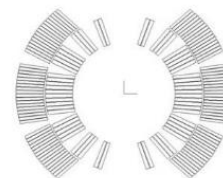
HERA

75 mm bore
B = 5.0 T
T = 4.5 K
first beam 1991



RHIC

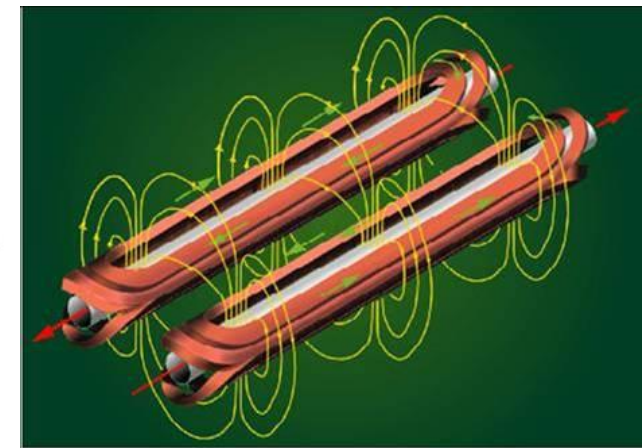
80 mm bore
B = 3.5 T
T = 4.3-4.6 K
first beam 2000



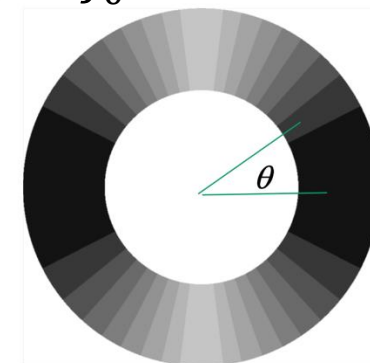
LHC

56 mm bore
B = 8.34 T
T = 1.9 K
first beam 2008

Courtesy G. d. Rijk and P. Ferracin, CERN



$$J = J_0 \cos \theta$$

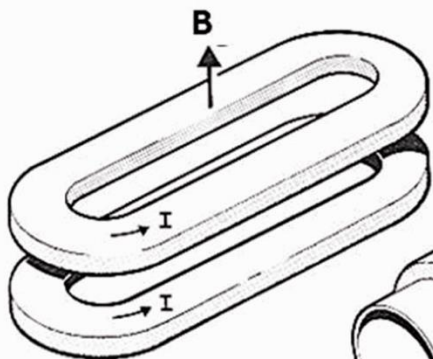


$\cos \theta$ current distribution
gives pure dipole field

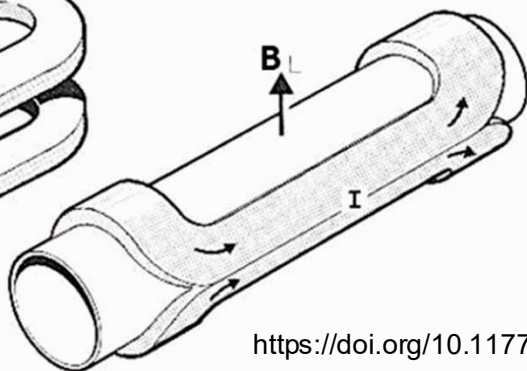
Different dipoles

Baseline: $\cos \theta$ (racetrack or saddle)

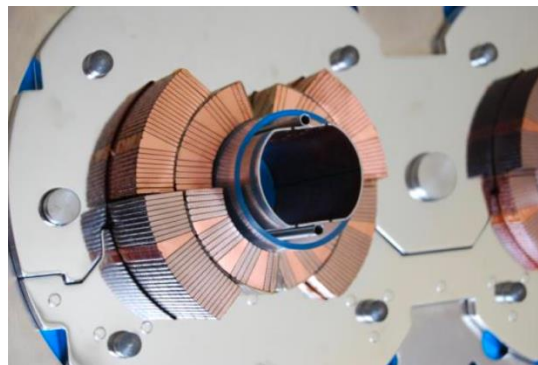
(b)



(c)



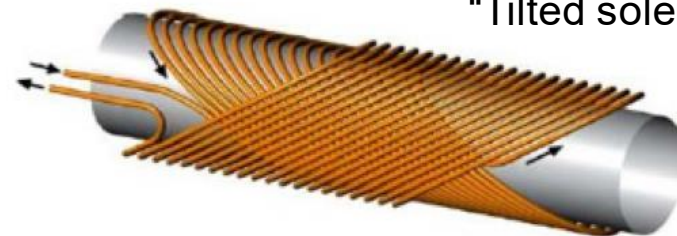
<https://doi.org/10.1177/15280837166612>



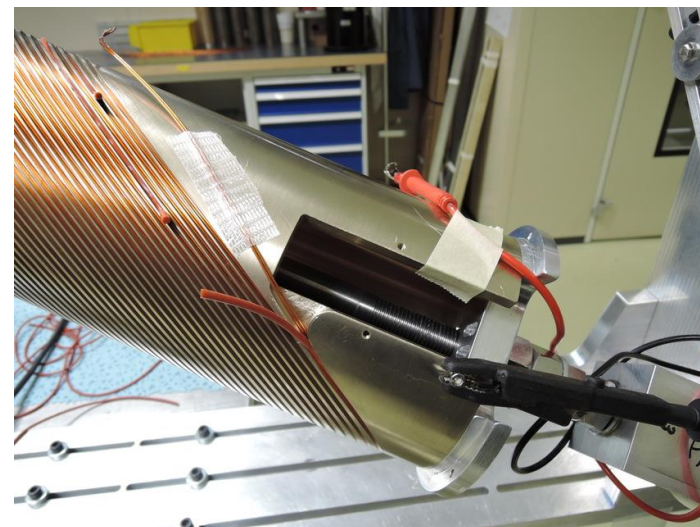
Courtesy G. d. Rij, M. Wilson,

Canted $\cos \theta$ (CCT)

“Tilted solenoid”



Proposed in 1960s realized recently

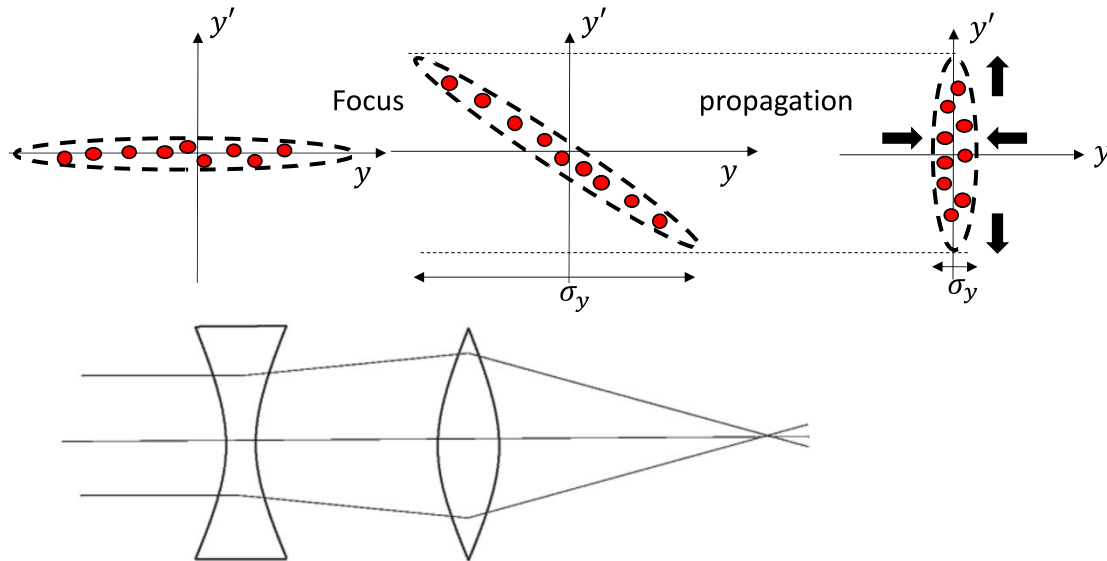


<https://home.cern/news/news/engineering/new-life-old-technology-canted-cosine-theta-magnets>

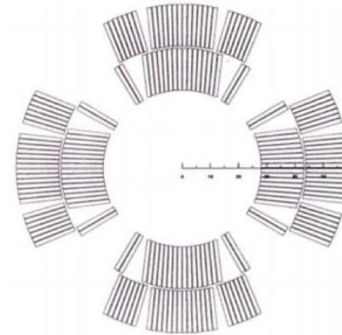
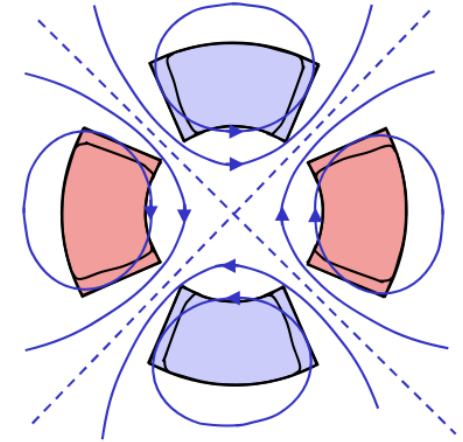
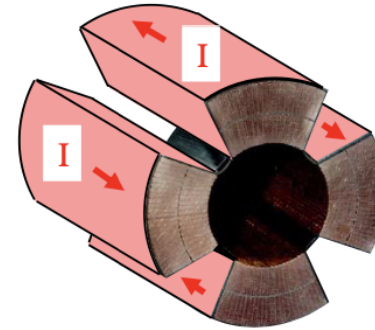
Lorentz force is not only for bending trajectory

$$\frac{d(mv_\theta)}{dt} \cdot \vec{u}_\theta - m \frac{v_\theta^2}{\rho} \cdot \vec{u}_r = eE_\theta \cdot \vec{u}_\theta + ev_\theta B_z \cdot \vec{u}_r$$

Focusing and defocusing of a group of charged particles (bunch) are crucial for beam transport and luminosity at collision



Implemented by quadrupole magnets



Courtesy G. d. Rij

SC vs NC magnets: typical and exception

$$p[\text{GeV}/c] = 0.3 \times \rho[\text{m}] \times B[\text{T}]$$

SC magnet

- Strong field (>0.2 T) **steady state**
- Typically proton circular machine
- Ex) 7 TeV & 8.3 T at LHC

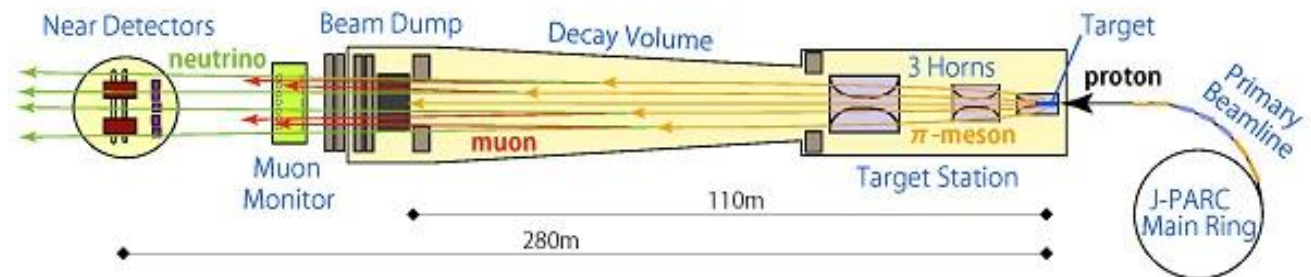
NC magnet

- Weak field (<0.2 T) **steady state**
- Typically electron circular machine
- Ex) 90 GeV & 0.13 T at LEP

Short pulsed NC magnet



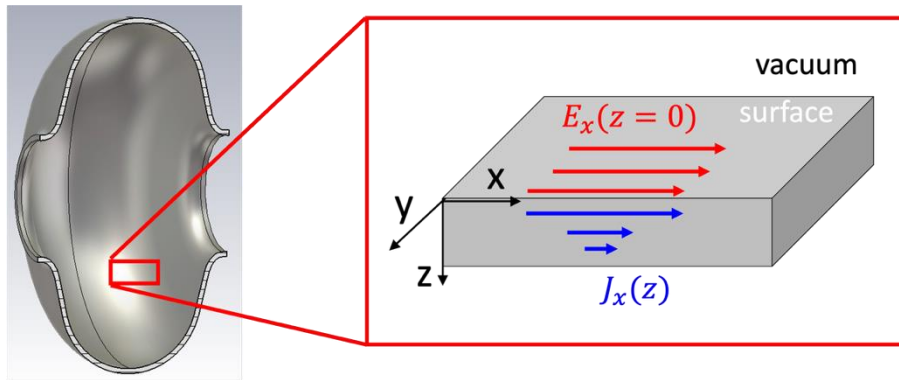
<https://j-parc.jp/Neutrino/en/nu-facility.html>



- Separate π^+ and π^- for neutrino and anti-neutrino
 - Too high radiation \rightarrow SC magnet may not survive
 - Coincidence time window with neutrino detector
- Strong field (2 T) for **short pulse** 5 μs (every 2-3 seconds)

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RF resistance R_s is non zero



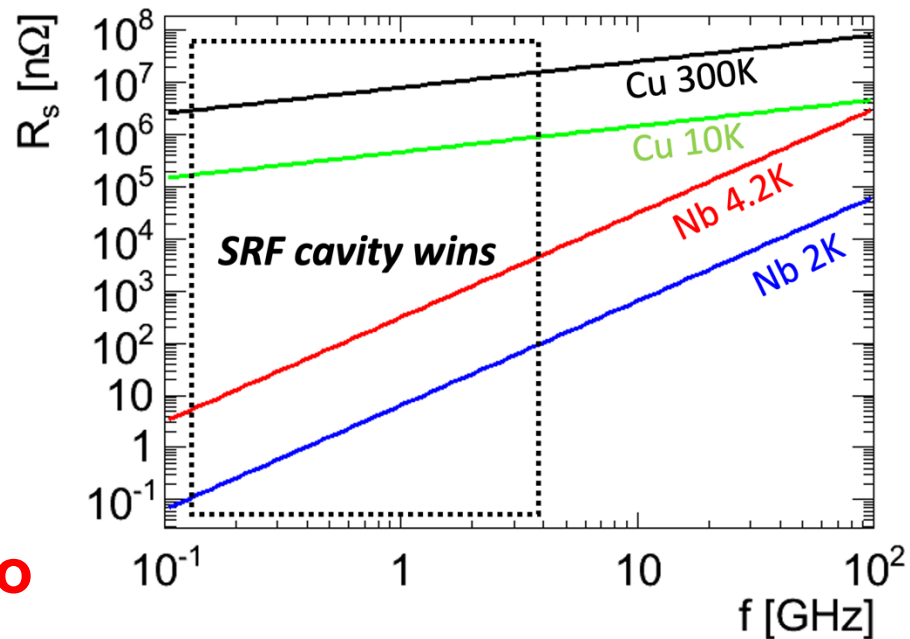
Local surface resistance

$$R_s \equiv \text{Re} \left(\frac{E_x(z=0)}{\int_0^\infty J_x(z) dz} \right)$$

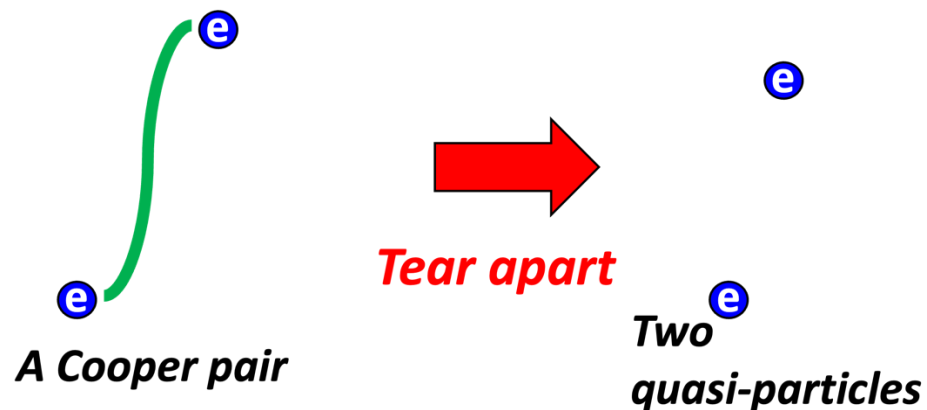
Normal conducting (Cu) $R_s = \sqrt{\frac{\pi f \mu_0}{\sigma}} \propto f^{1/2}$

Super- conducting (Nb) $R_s = \frac{A f^2}{T} \exp \left(-\frac{\Delta}{k_B T} \right) \propto f^2$

Superconducting R_s is small but non zero



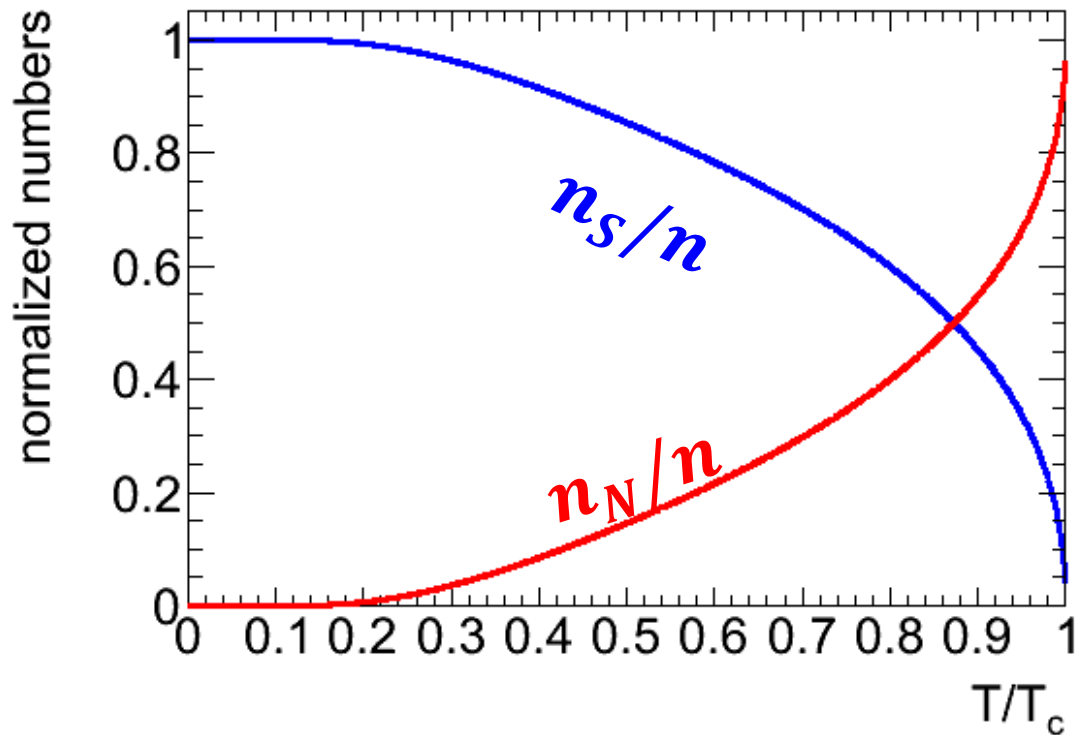
Thermal excitation of quasi-particles



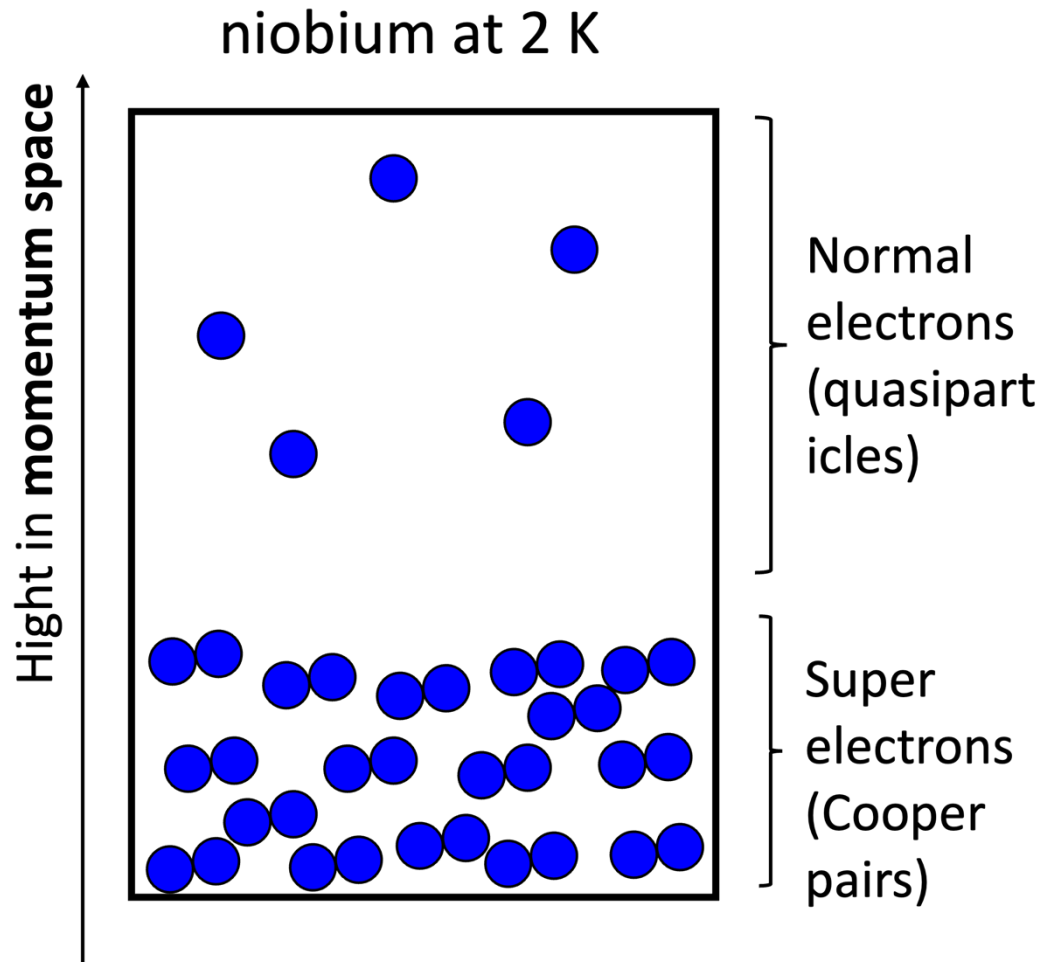
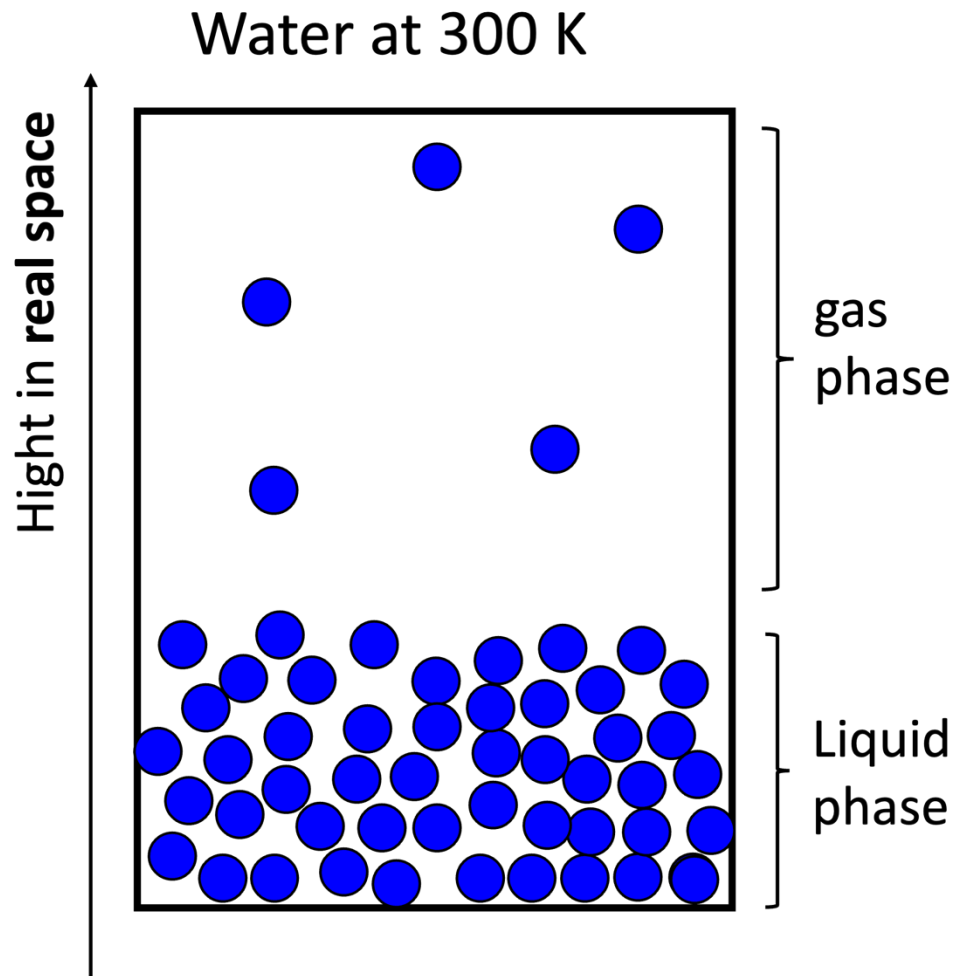
At finite temperature $0 < T < T_c$, these two states are **in thermal equilibrium**

of quasiparticles: $n_N \sim \exp\left(-\frac{\Delta}{k_B T}\right)$

of electrons in Cooper pairs: $n_S \sim n - n_N$



Quasi-particles (\sim normal conducting electrons) still exist if $T > 0$



Supercurrent

$$\frac{\partial j_s}{\partial t} - \frac{n_s e^2}{m^*} E = 0$$

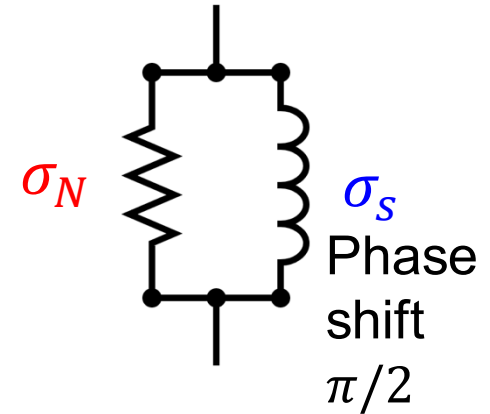
$$j_s = j_0 \exp(i\omega t)$$

$$j_s = -i \frac{n_s e^2}{m^* \omega} E \equiv \sigma_s$$

Normal current

Ohm's law \rightarrow

$$j_N = \frac{n_N e^2 \tau}{m^*} E \equiv \sigma_N$$



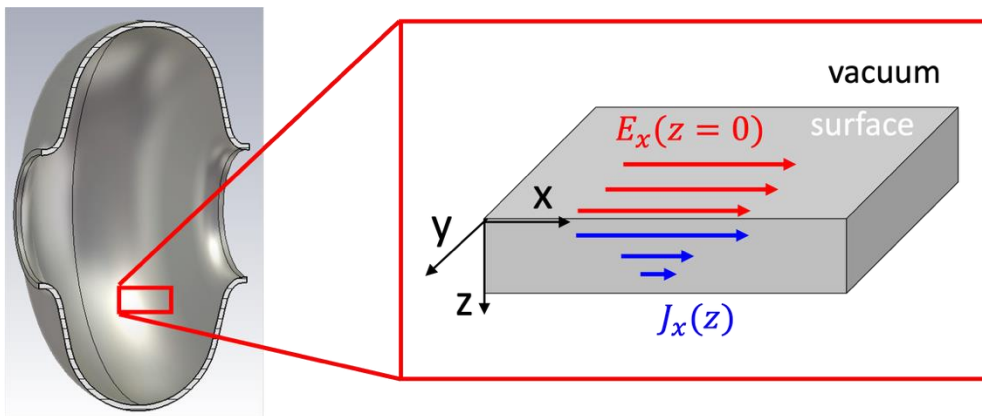
Total current induced by RF

$$j = j_s + j_N \rightarrow j = (\sigma_N - i\sigma_s)E$$

Dissipation by quasi-particles \rightarrow resistive

Inertia of Cooper pairs \rightarrow inductive

Surface resistance of superconductor



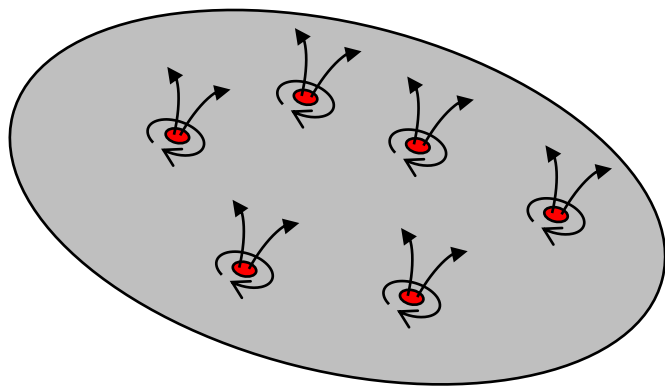
$$\sigma_N = \frac{e^2 n_N \tau}{m^*} \propto n_N \propto \exp\left(-\frac{\Delta}{k_B T}\right)$$

$$\begin{cases} j_x = (\sigma_N - i\sigma_S)E_x \\ E_x(z) = E_0 \exp(-z/\lambda_L) \end{cases} \rightarrow R_s \equiv \text{Re} \left(\frac{E_x(z=0)}{\int_0^\infty J_x(z) dz} \right) \sim \frac{1}{2} \frac{\sigma_N}{\sigma_S} \sqrt{\frac{\omega \mu_0}{\sigma_S}} = \frac{\mu_0^2}{2} \lambda_L^3 \sigma_N \omega^2 > 0$$

Lessons

- One origin of the finite R_s of superconductors is quasi-particles
- Quasi-particles are thermally activated from Cooper pairs at $0 < T < T_c$
- R_s exponentially decreases by lower T because quasi-particles are frozen out
- Higher RF frequency increases $R_s \sim \omega^2$
- Order of magnitude is 10 nΩ

Static trapped magnetic field in SC cavities



Normal
conducting
area

$$R_{\text{mag}} \sim N \times \pi \xi_0^2 \times R_n \sim \frac{B_{\text{ext}}}{2B_{c2}} R_n$$

Flux
number
density

Normal
conducting

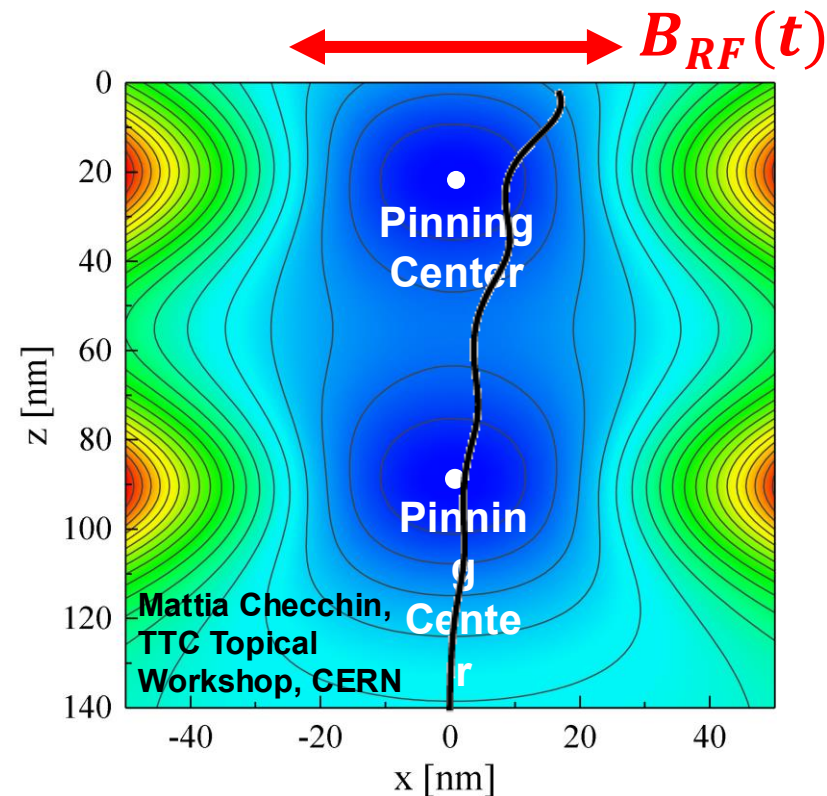
Earth field $B_{\text{ext}} = 50 \mu\text{T}$

$B_{c2} \sim 400 \text{ mT (Nb)}$

$R_n \sim 1.3 \text{ m}\Omega \text{ at } 1.3 \text{ GHz (Nb)}$

$$R_{\text{mag}} \sim 80 \text{ n}\Omega > R_{\text{BCS}}(2\text{K}) \sim 10 \text{ n}\Omega$$

An excellent magnetic shield is mandatory for SC cavities

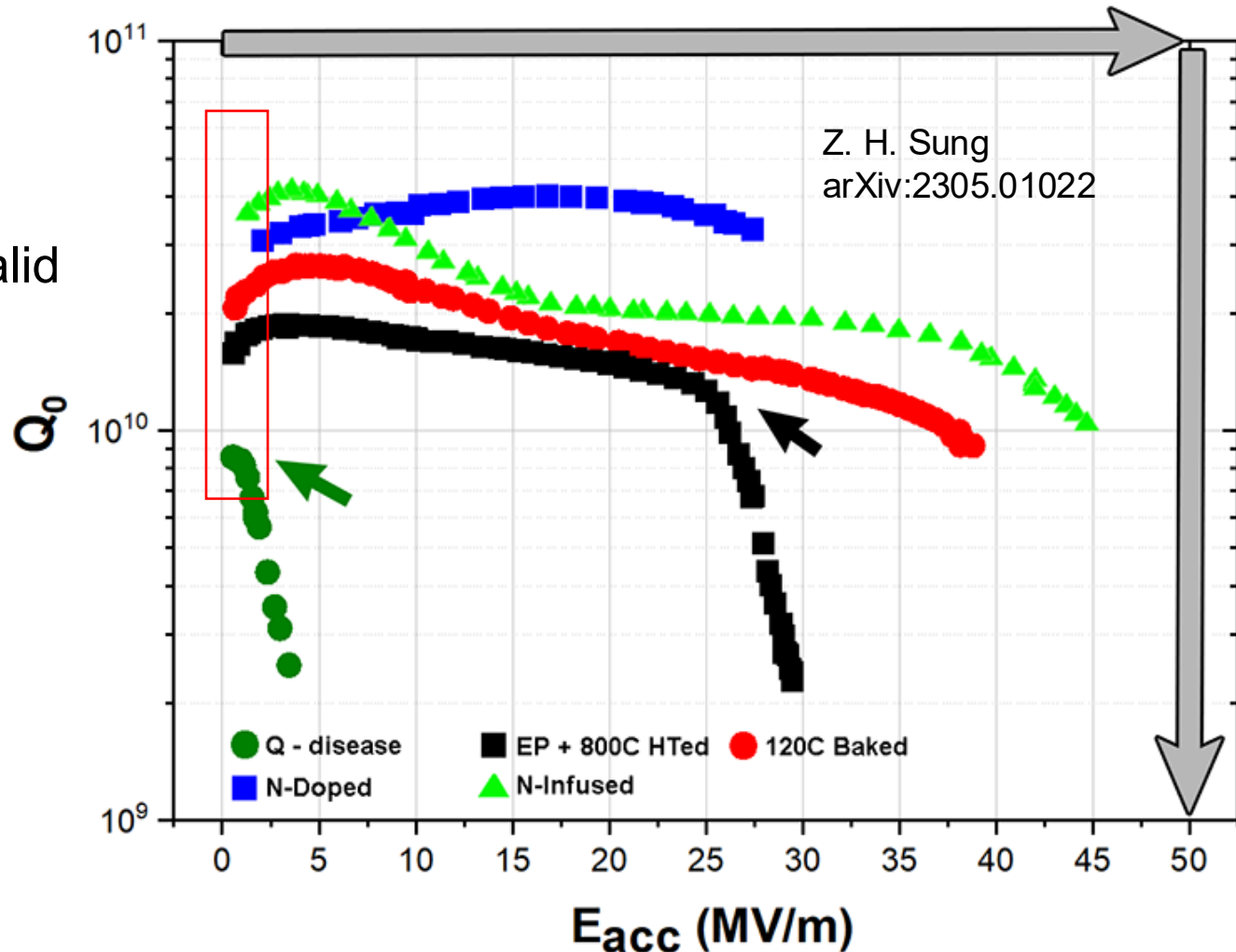


Quality factor vs accelerating gradient

$$Q_0 \equiv \frac{\omega U}{P_c} = \frac{1}{R_s} \omega \mu \frac{\int_V H^2 dV}{\int H^2 dS}$$

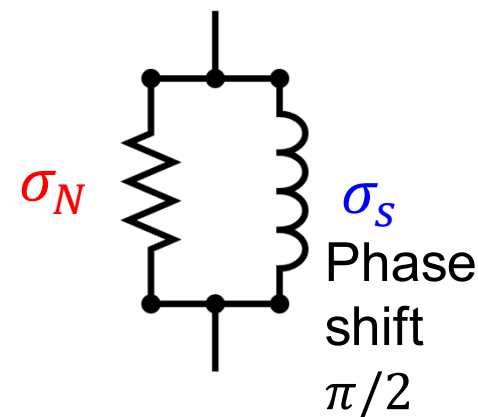
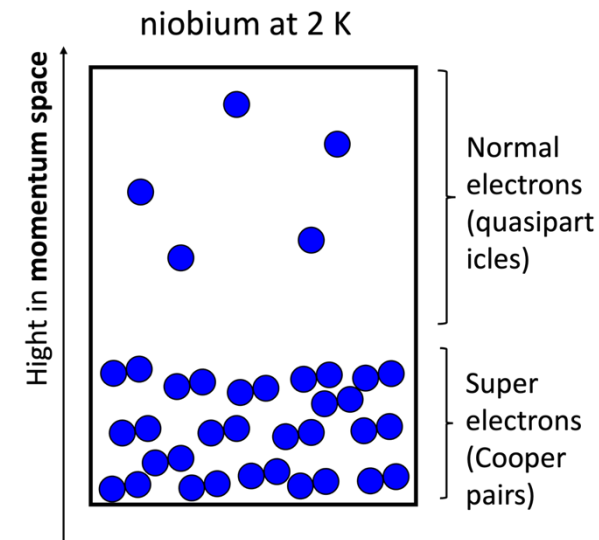
geometrical

- The established theory is only valid for low external RF field
- The simplest nonequilibrium problem is solved in the linear response theory
- Very tiny difference in surface impacts the results (<10 nΩ physics!)
- We do not have complete theory that explains the nonlinear phenomena in Q vs E
→ Open research field!



Z. H. Sung
arXiv:2305.01022

- Magnets are operated in strong DC fields
 - The two-fluid circuit is short \rightarrow no loss
 - Finite loss during ramping up and down the field
 - Magnetic fields are trapped in Mixed state
 - Strong pinning force is manipulated to avoid flux flow (otherwise, loss)
- Cavities are operated in RF fields
 - The phase shift due to Cooper pairs' inertia causes finite loss in quasiparticles
 - Oscillating trapped flux kills the cavity performance
 - Operation in as clean as the Meissner state
 - RF field itself does not penetrate due to superheating effect and surface barrier

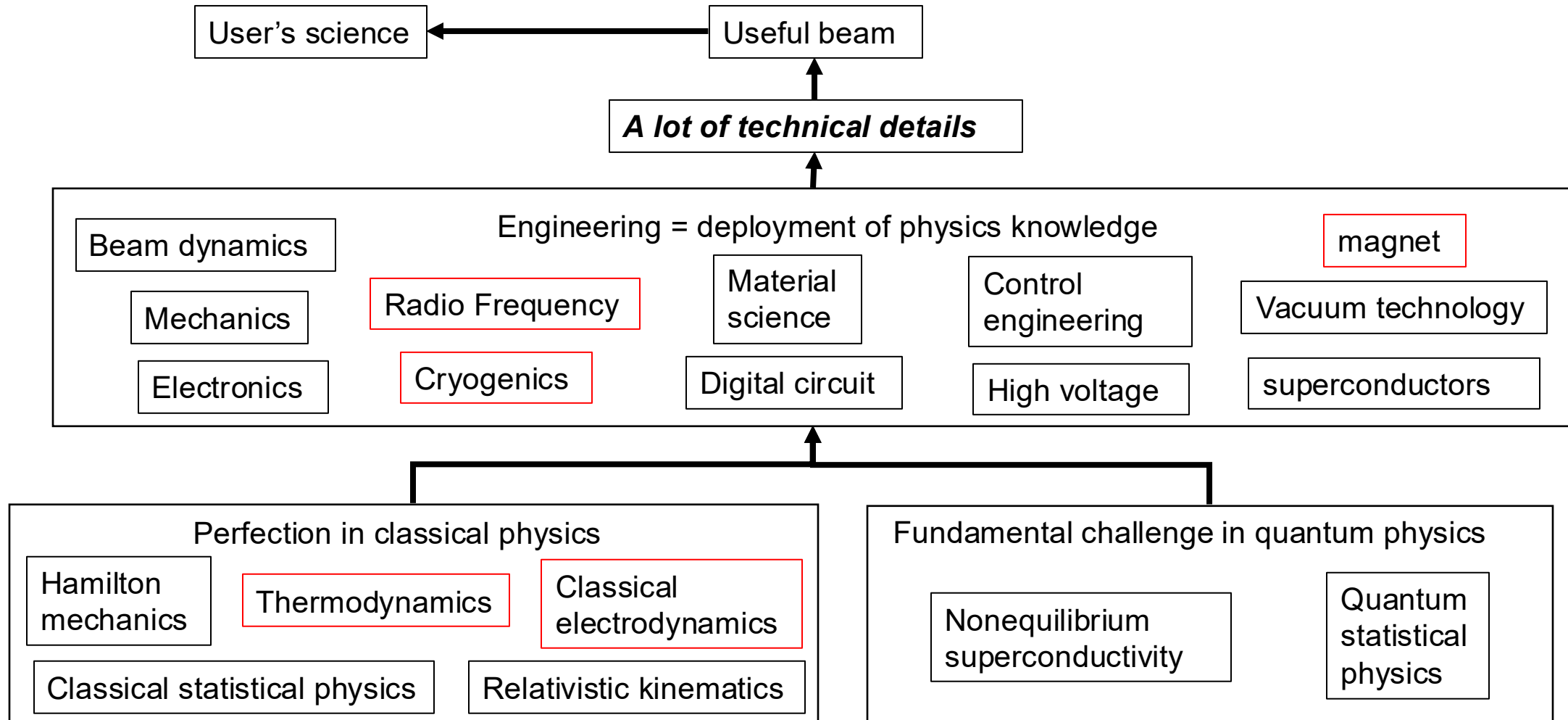


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- **Conclusion**

- **Cooling down improves loss but becomes less efficient**
 - Superconducting vs normal conducting under the ideal Carnot cycle
 - Carnot cycle is NOT realistic at all: trade off in efficiency and power evacuation
- **Superconducting devices are typically operated inside liquid helium**
 - Cryogenics is enabled by physics and engineering of thermodynamics
- **Superconductivity is macroscopic quantum phenomenon**
 - Meissner effect is the most characteristic phenomenon (spontaneously broken Gauge symmetry in the ground stage)
 - Zero DC loss is caused by Cooper pairs
 - Classical electrodynamics can give us some insight with limitation
- **Several different superconducting mechanisms are known**
 - Only BCS-type SCs are well understood (phonon-mediated correlation) and Copper oxide & iron-based SC are still under debate
- **SC magnet are operated in the Mixed state of type-II superconductors**
- **SC cavities are operated in the Meissner state of type-II superconductors**
 - Non-equilibrium phenomenon is the remaining challenge of BCS-type SCs
 - Two-fluid model gives us some insight with limitations



Conclusion: *rich physics in the research field of accelerators*



Summer Student Lecture Programme 2025

1 Jul 2025, 08:00 → 1 Aug 2025, 13:00 Europe/Zurich

500/1-001 - Main Auditorium (CERN)

Webcast

There is a live webcast for this event

[Watch](#)

MONDAY 21 JULY

09:15 → 10:10

RF Superconductivity

Speaker: Akira Miyazaki (Université Paris-Saclay (FR))

55m

10:25 → 11:20

Making Predictions at Hadron Colliders

Speaker: Alexander Yohei Huss (CERN)

55m

11:35 → 12:30

Nuclear Physics at CERN

Speaker: Magdalena Kowalska (CERN)

55m

TUESDAY 22 JULY

09:15 → 10:10

Nuclear Physics at CERN

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55m

10:25 → 11:20

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55m

11:35 → 12:30

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Speaker: Alexander Yohei Huss (CERN)

55m

<https://indico.cern.ch/event/1508891/timetable/>

More dedicated to students learning particle physics and engineering aspects of particle physics