

Sub-gap modes observed with Kinetic Inductance Detectors (KIDs): source of extra-dissipation in disordered thin superconductors ?



Florence Levy-Bertrand, Néel Institute, Grenoble (France)



Outline:

- Working principle of Kinetic Inductance Detector (KID)
- Sub-gap modes in amorphous indium oxide
- Sub-gap modes in granular aluminum
- Sub-gap modes: source of extra-dissipation ?

RELATED TO « ANOMALOUS METAL » ???

TEMPERATURE & ENERGY SCALE ?

RELATED TO STRANGE TLS AND SATURATION OF LIFE TIME ?

Sub-gap modes observed with Kinetic Inductance Detectors (KIDs): source of extra-dissipation in disordered thin superconductors ?



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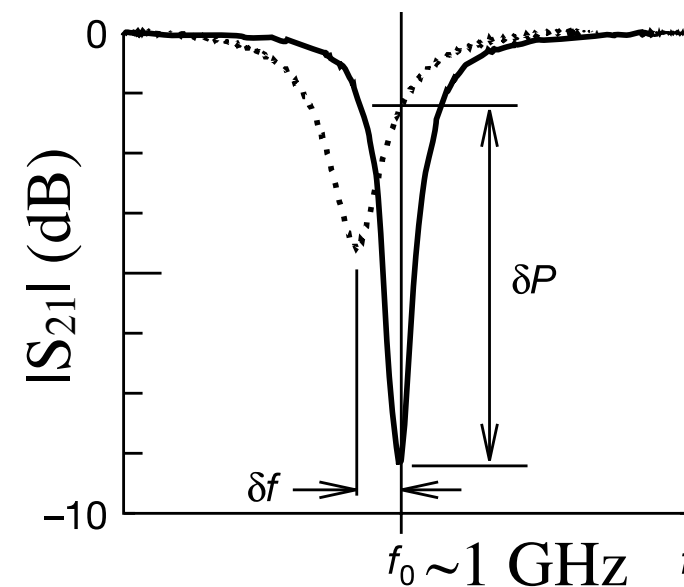
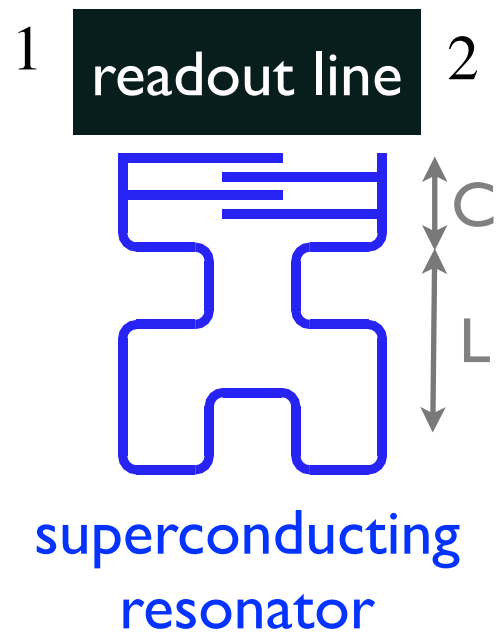
A. Gomez

Working principle of KID

Day et al, Nature 425, 817 (2003)

Superconducting LC resonator:
design and electrical measurement

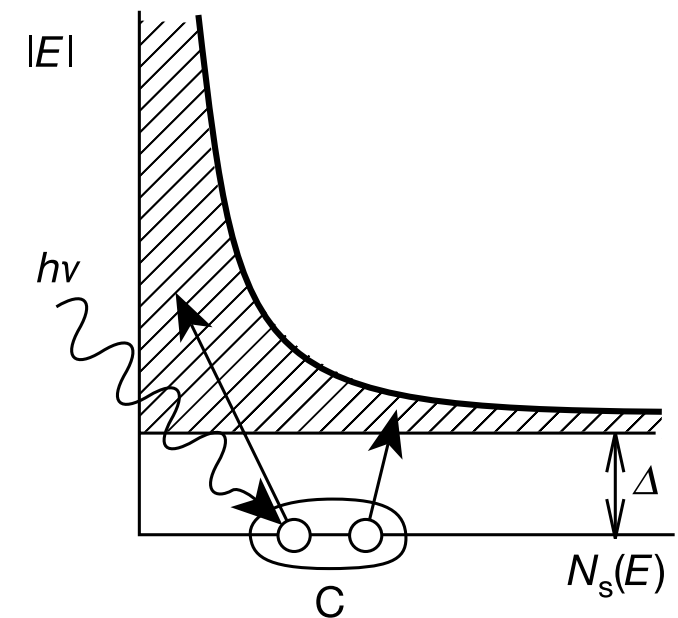
photon detection principle :
 $h\nu > 2\Delta$



$$f_0 \sim (LC)^{-1/2}$$

$L \sim$ kinetic inductance of the superfluid

$$L \sim 1/n_s$$

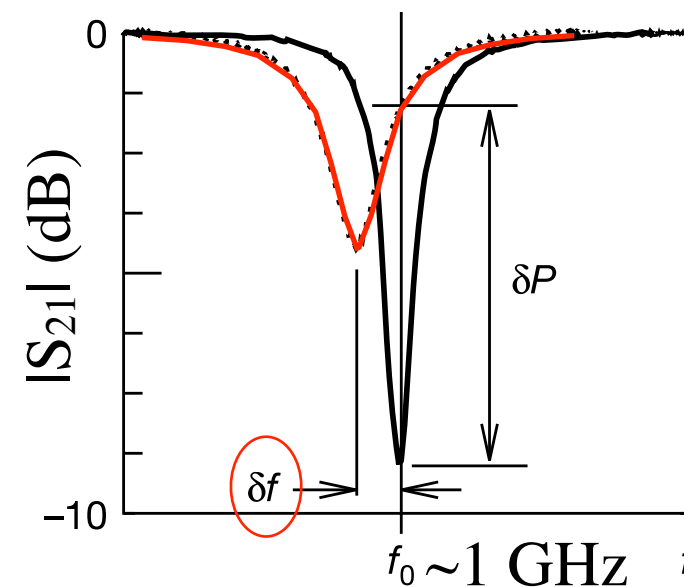
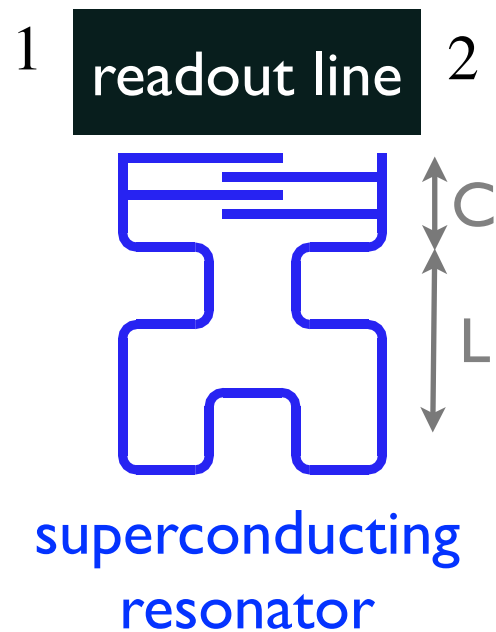


Working principle of KID

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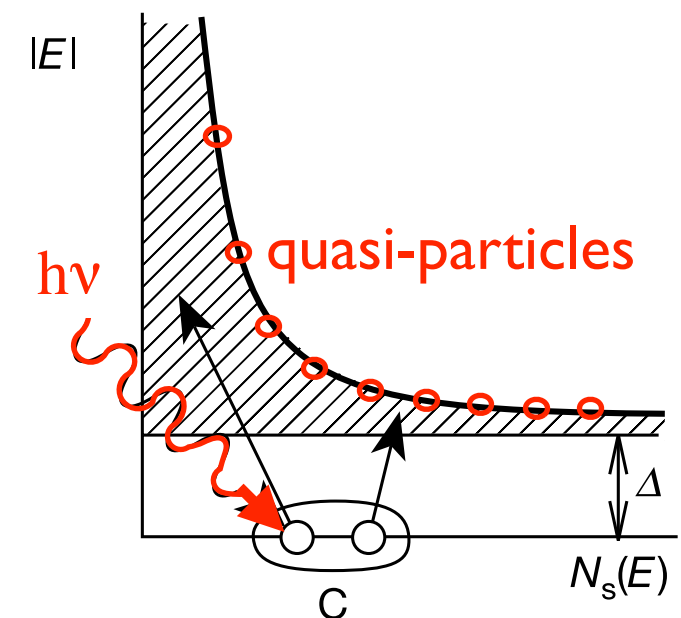
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frequency shift: δf due to $n_s \downarrow$

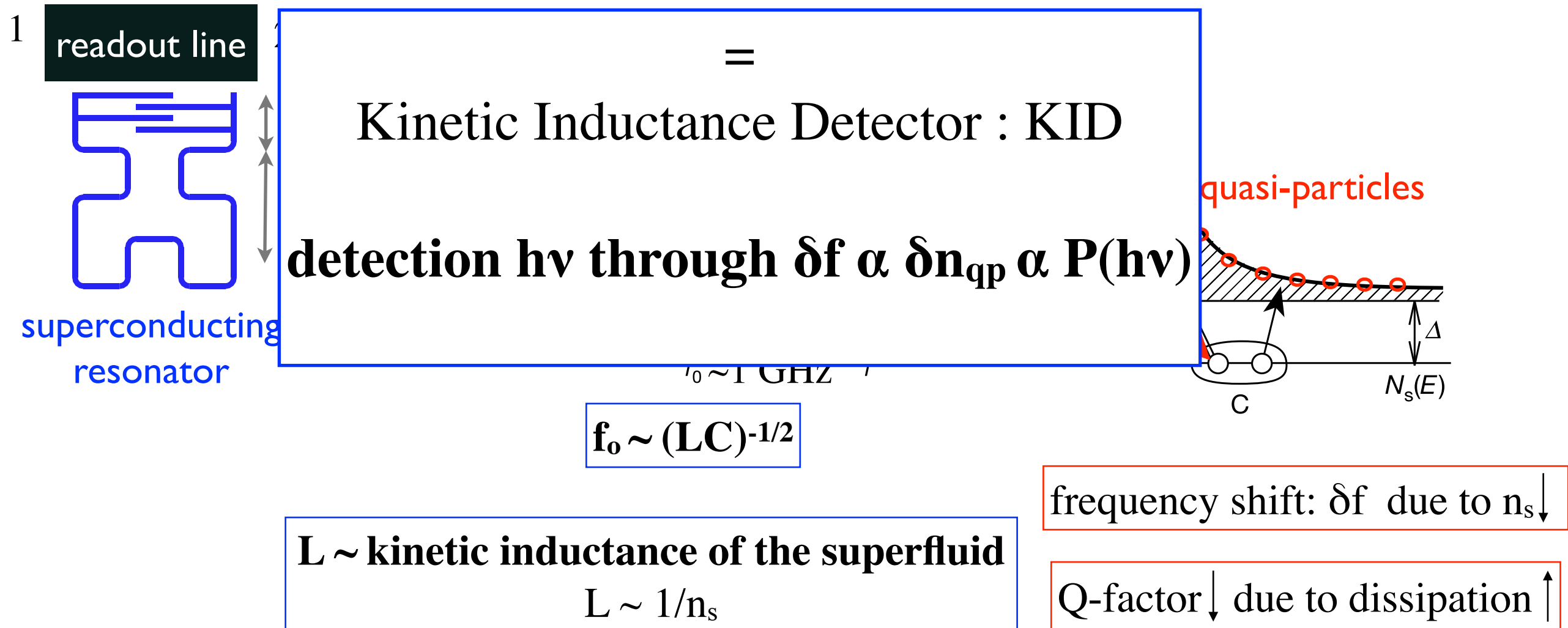
Q-factor $\downarrow$ due to dissipation $\uparrow$

Working principle of KID

Day et al, Nature 425, 817 (2003)

Superconducting LC resonator:
design and electrical measurement

photon detection principle :
 $h\nu > 2\Delta$

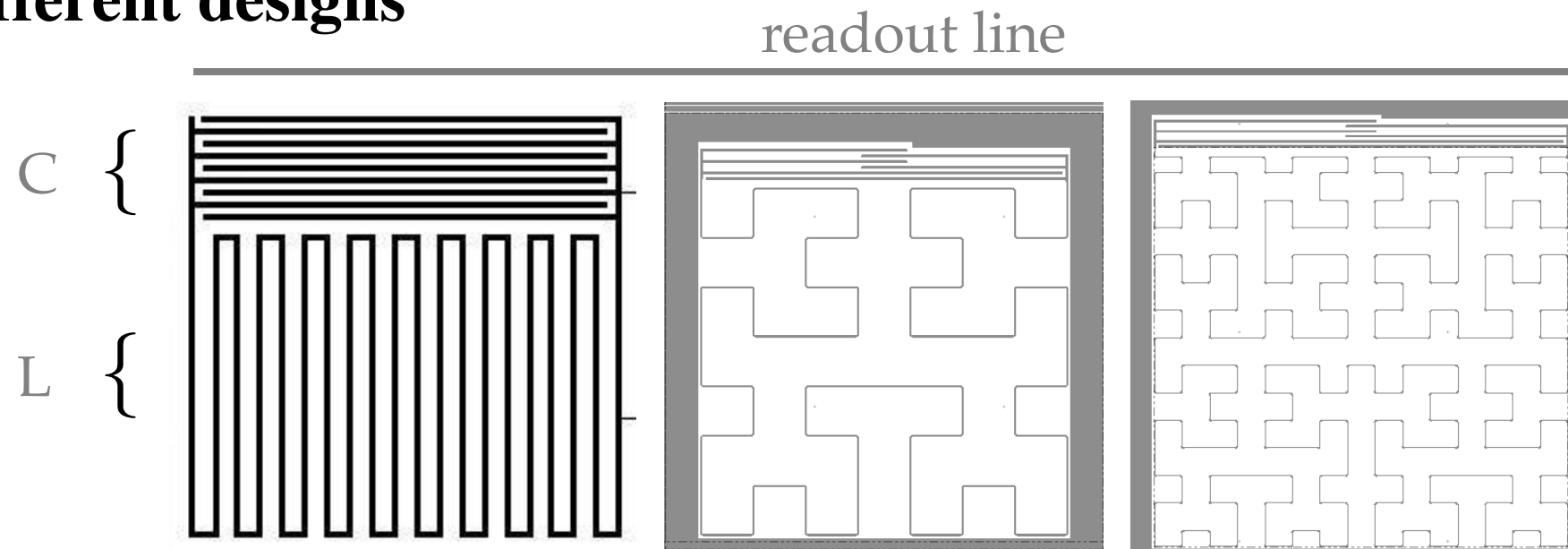


Working principle of KID

Superconducting LC resonator:

Superconducting thin film on insulating substrate (Si, MgO, Al₂O₃,...)

different designs

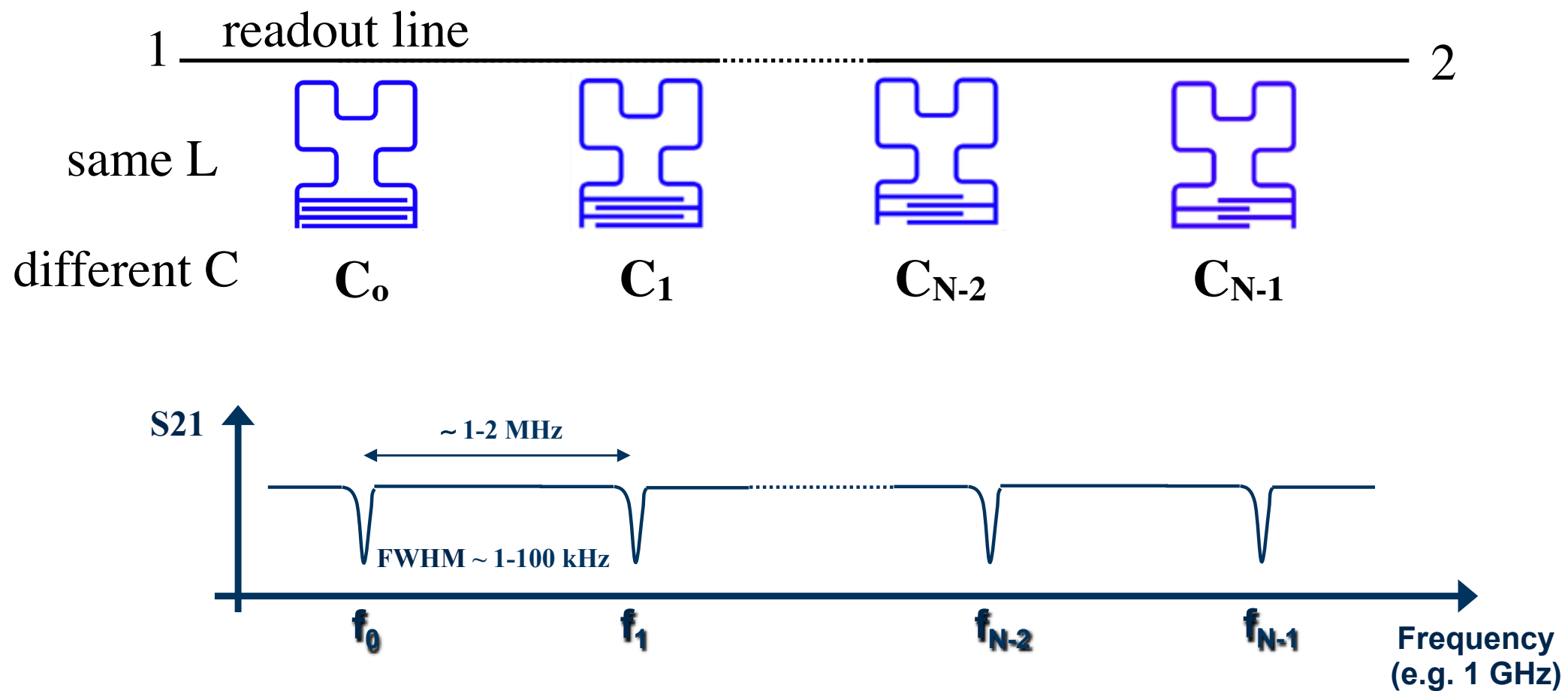


different superconducting materials: Al, Nb, NbN, ...

-> key point: planar lithography

Working principle of KID

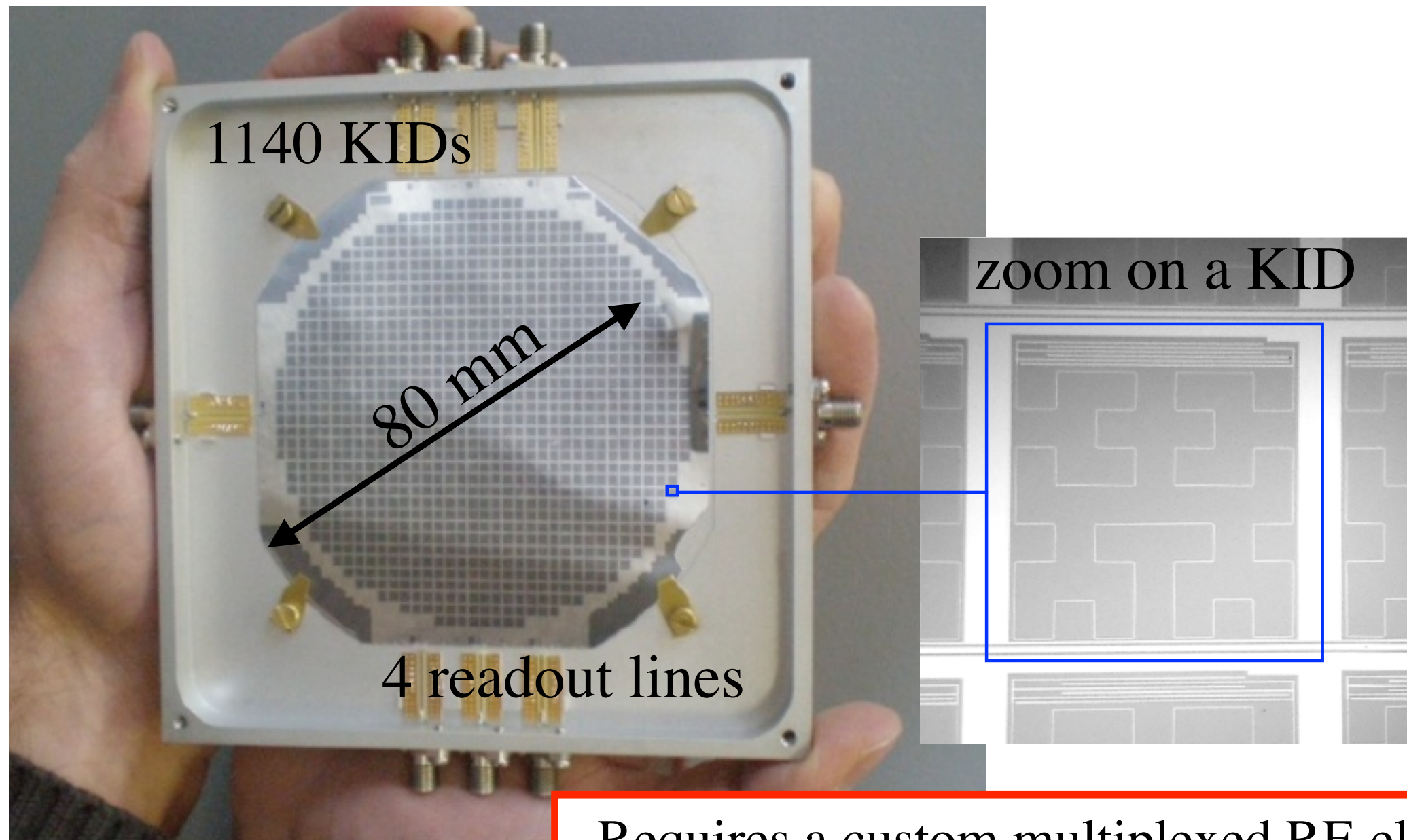
Frequency multiplexing: $f \sim (LC)^{-1/2}$



-> one line to address hundreds of detectors

Working principle of KID

Frequency multiplexing: $f \sim (LC)^{-1/2}$

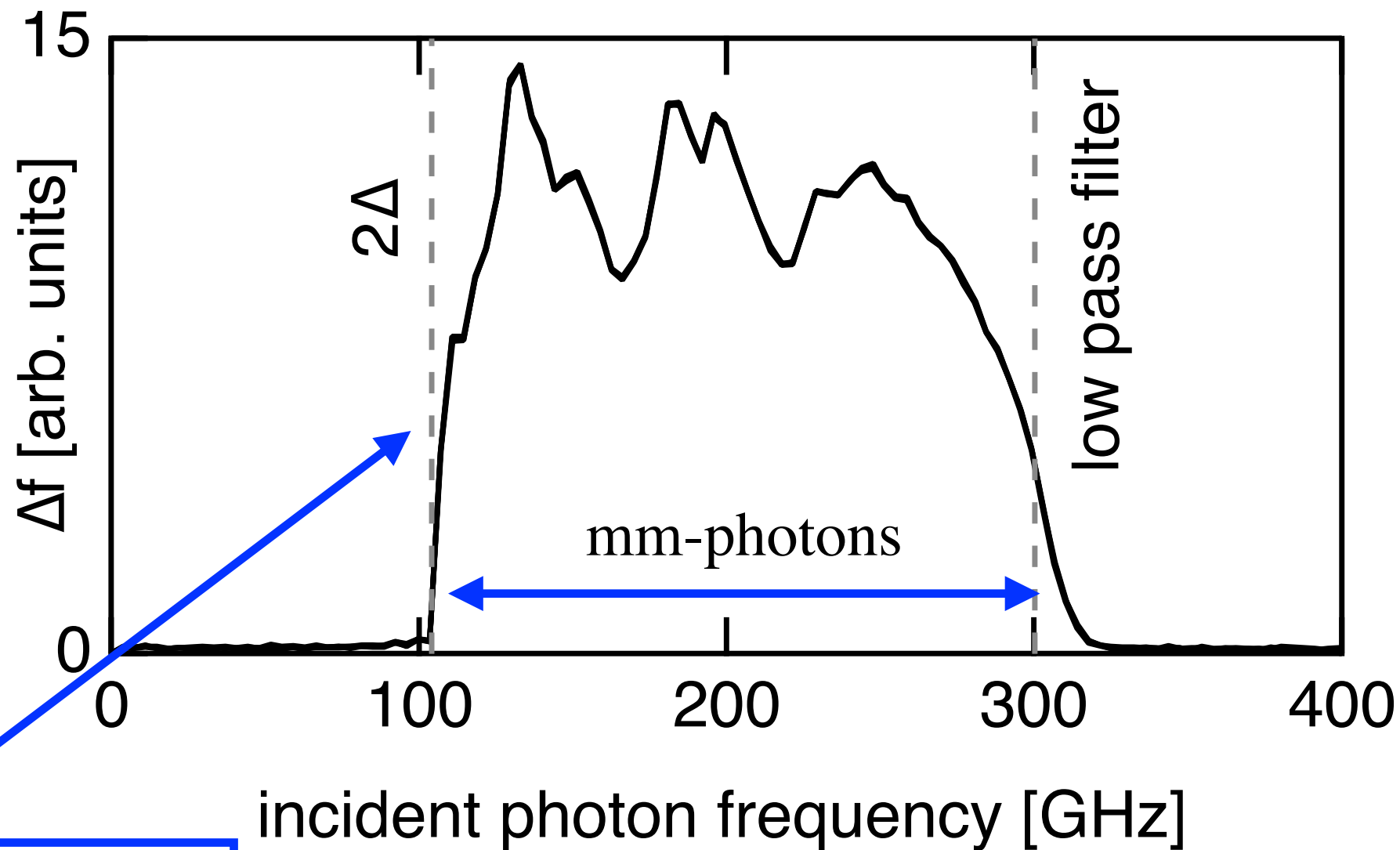


Requires a custom multiplexed RF-electronic

Working principle of KID

Optical response of KIDs made of 20nm-thick Al

@ $T \sim 100\text{mK}$, $T \ll T_c \sim 1.4\text{ K}$



cutoff detection
 $h\nu > 2\Delta = 3.52 k_B T_c$

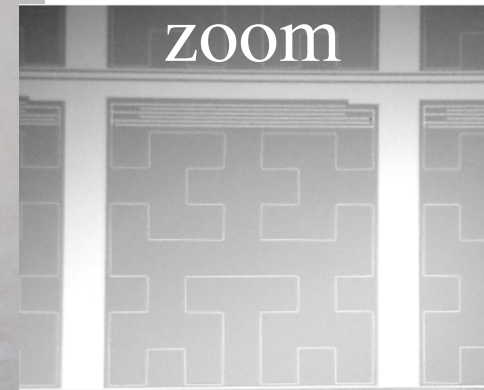
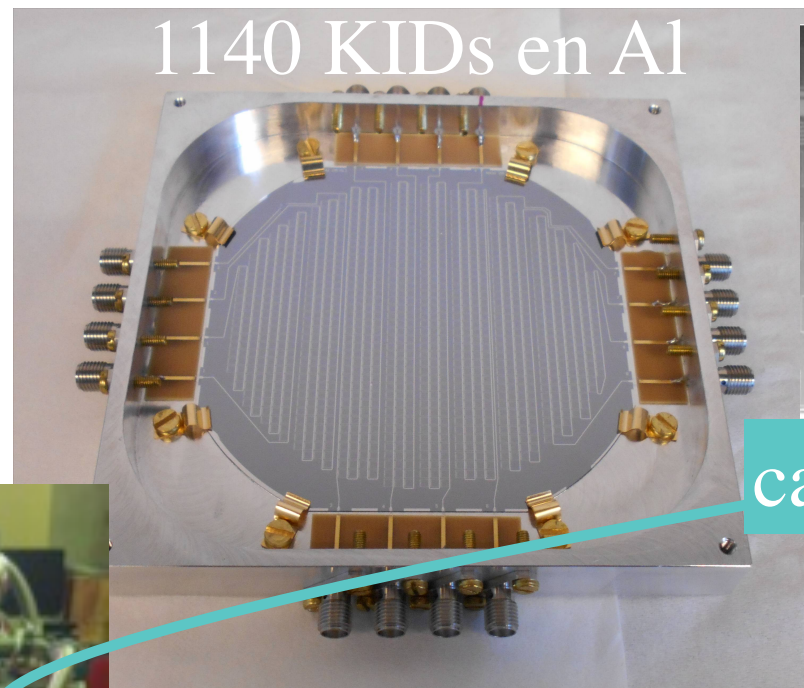
Requires a custom optical dilution refrigerator

KID for astrophysics observations

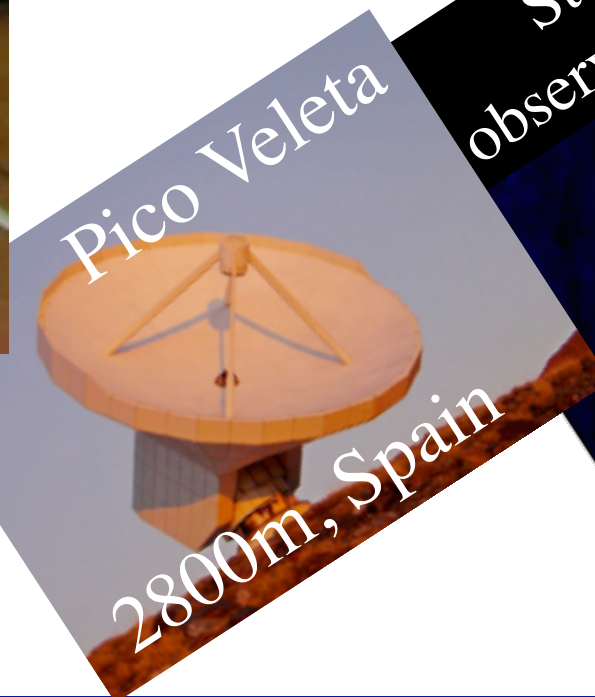
NIKA2 mm-camera (2800m, Spain)



Installation in 2015



calibrated KIDs

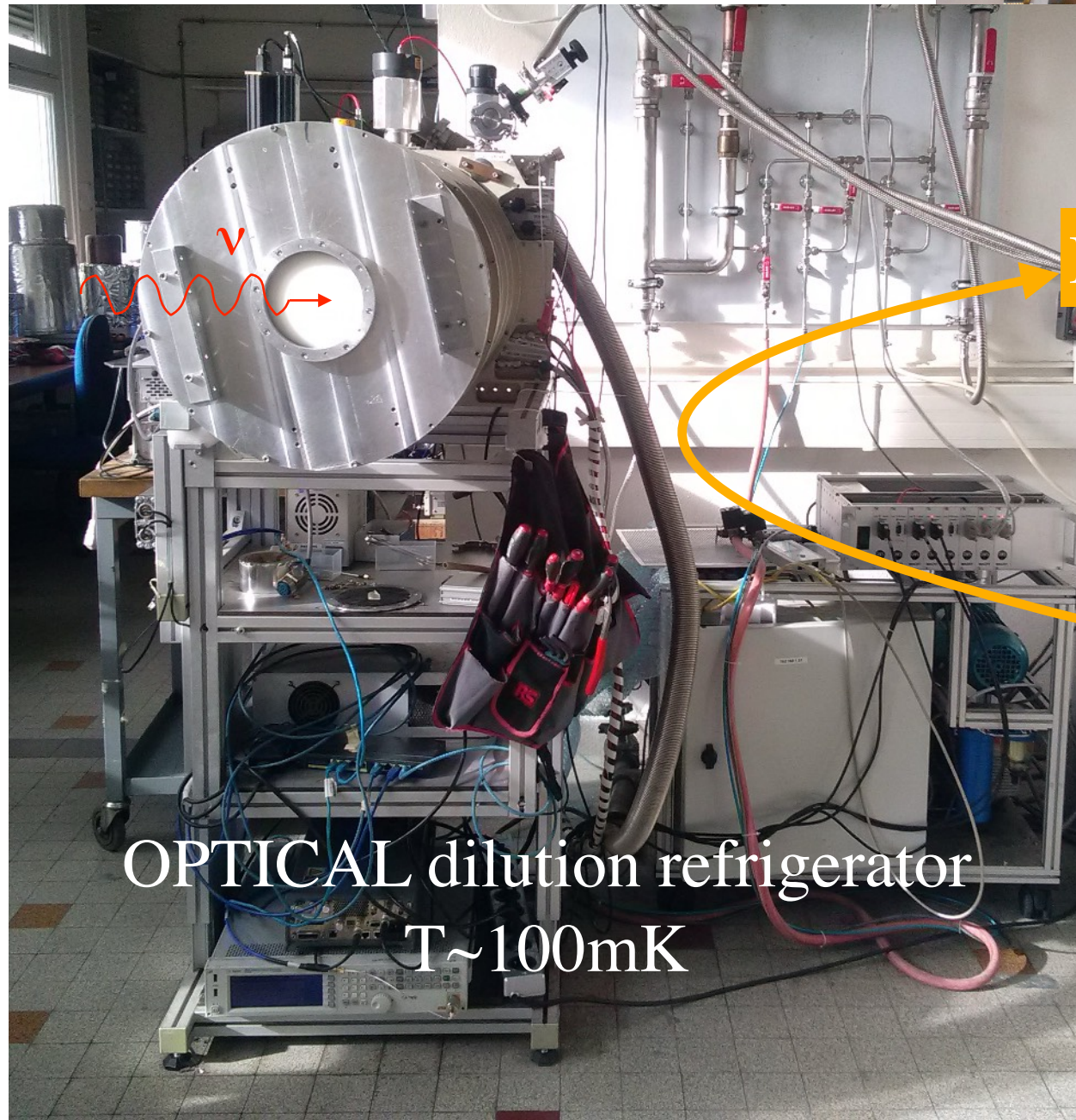


Star formation:
observation @150 GHz

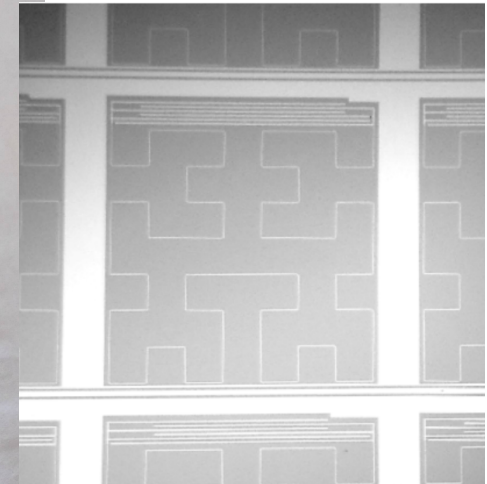
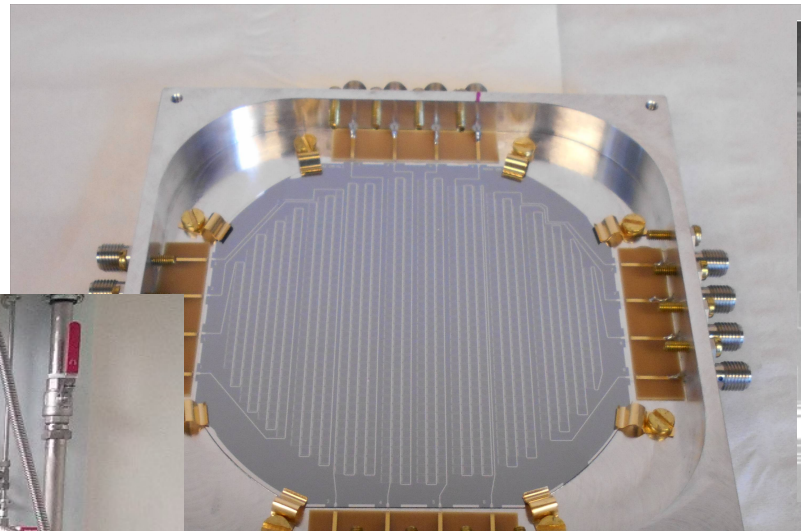
unknown sources

consortium NIKA2

KID to access the electrodynamics of superconductors



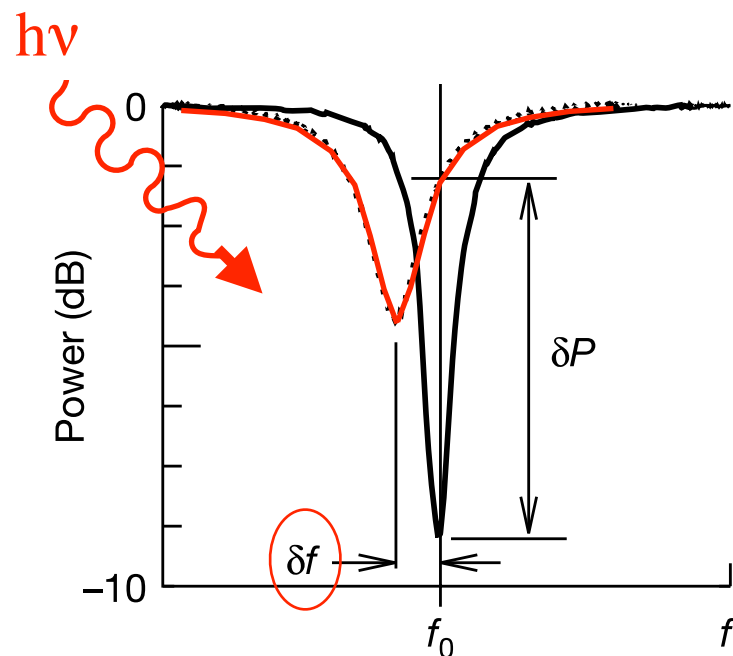
OPTICAL dilution refrigerator
 $T \sim 100\text{mK}$



KIDs made from various superconductors

known sources

KID to access the electrodynamics of superconductors



$$f_0 = 1/(2\pi\sqrt{LC})$$

$$Q = 1/R\sqrt{L/C}$$

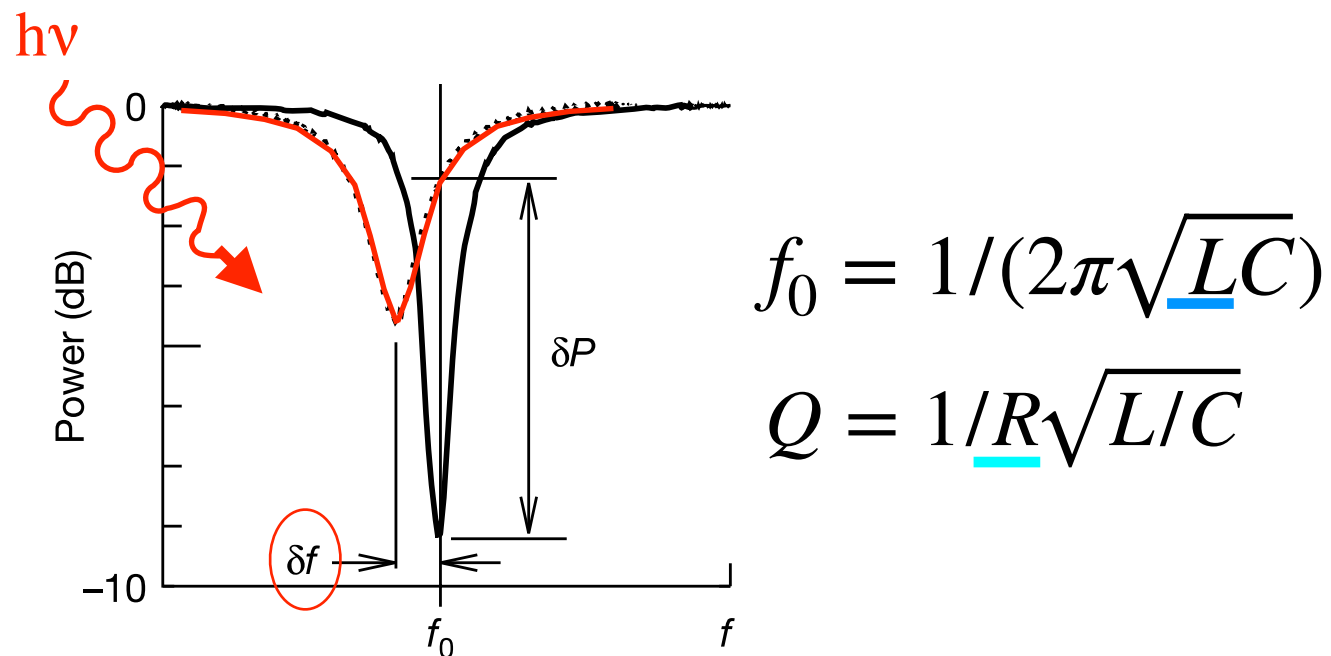
f_0 and Q are related to

- the optical complex conductivity $\sigma(\omega) = \sigma_1 - i\sigma_2$
 - the complex impedance $Z = R_{qp} + i\omega L_k$
- for $d \ll \lambda$
 $Z = 1/(\sigma d)$

quasi-particles
dissipative response

SC- condensate
inductive response

KID to access the electrodynamics of superconductors



$$\frac{\delta f_0}{f_0} \sim -\frac{\alpha}{2} \frac{\delta L_k}{L_k} \sim +\frac{\alpha}{2} \frac{\delta n_s}{n_s}$$

SC- condensate

with $\alpha = L_k/(L_k + L_g)$

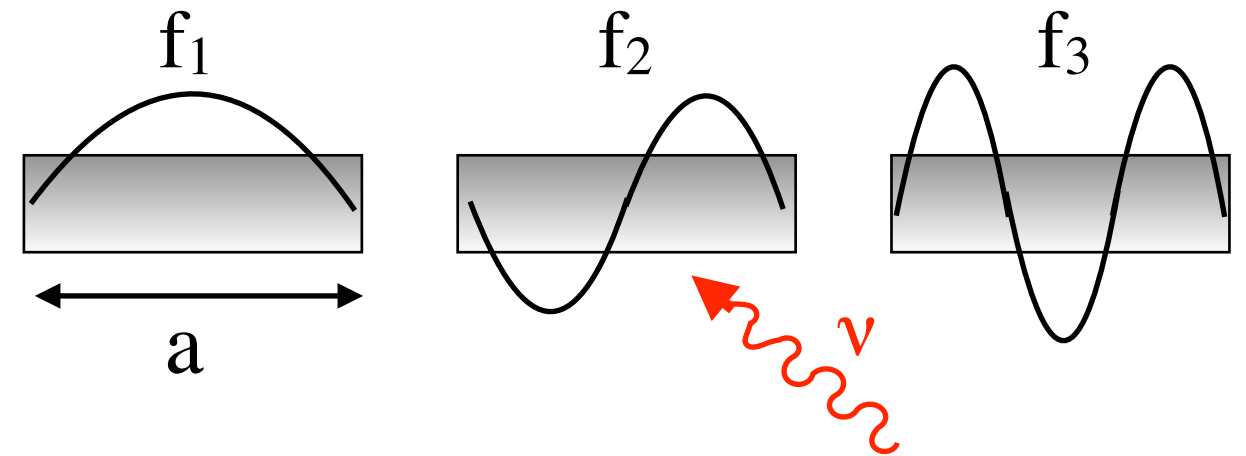
$$\frac{\delta Q}{Q} \sim -\frac{\delta R_{qp}}{R_{qp}} + \frac{\alpha}{2} \frac{\delta L_k}{L_k}$$

quasi-particles

Sub-gap modes in amorphous indium oxide

In superconducting resonator:

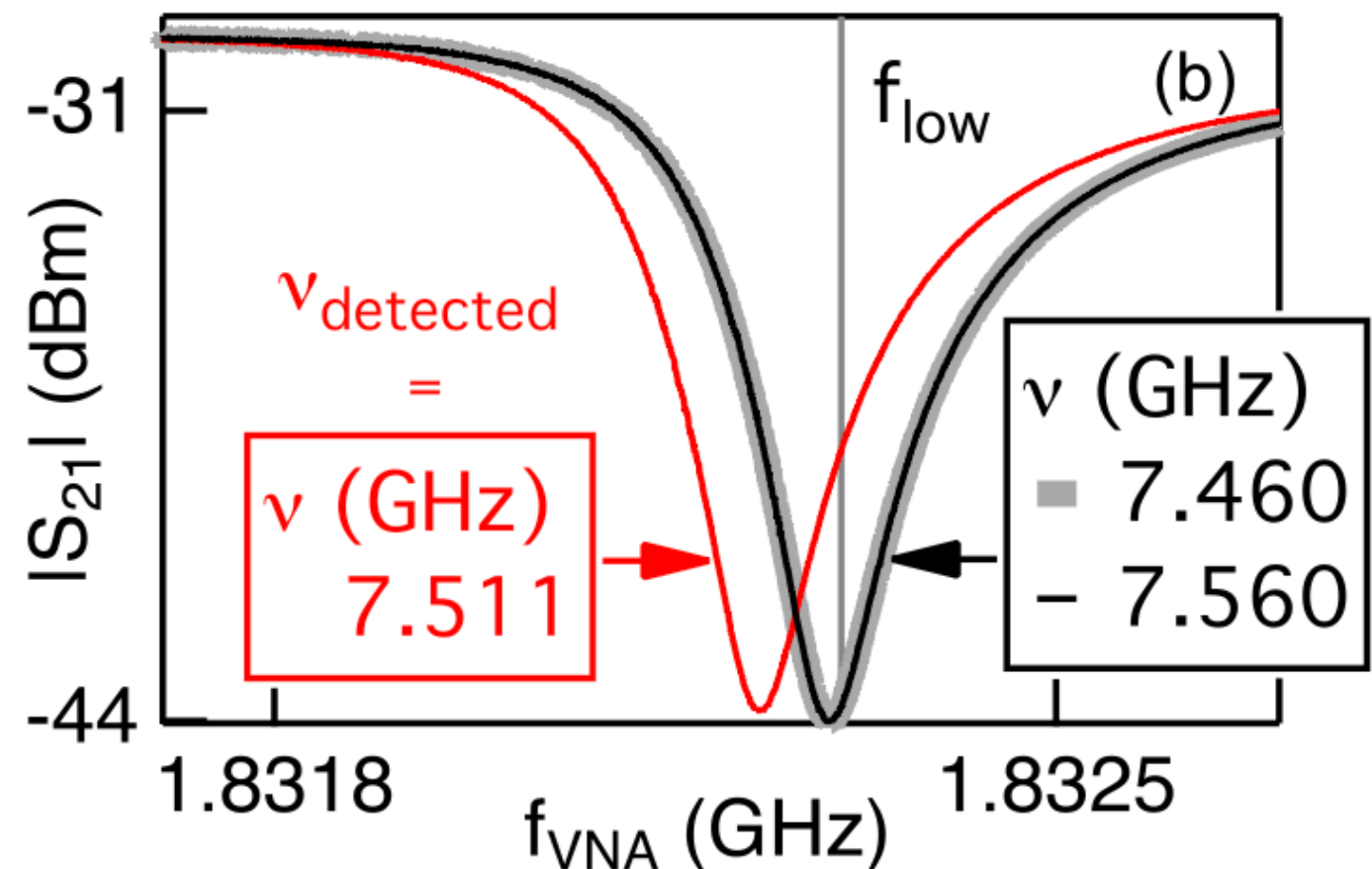
fundamental mode and harmonics f_n ,
current oscillations of n_s .



ν -detected = third harmonic

In amorphous InO, $2\Delta \sim 200$ GHz

- STM: fully gap
- Optics: sub-gap state(s)



O. Dupré et al, SuST 30, 045007 (2017).

Sub-gap modes in amorphous indium oxide

Strong sub-gap modes in a:InO

because of large non-linearity:

$$L_k(I) \sim L_k(0)[1 + I^2/I_*^2]$$

because of low $I_* \sim I_c$

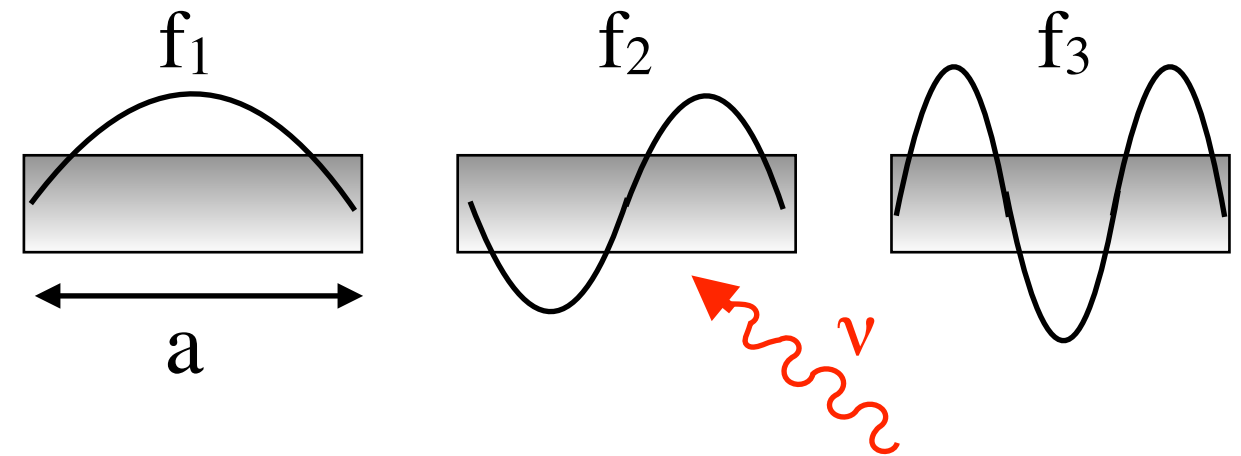
$$\frac{\delta f_0}{f_0} \sim -\frac{\alpha}{2} \frac{\delta L_k}{L_k}$$

$$\frac{\delta n_s}{n_s} \sim \frac{I^2}{I_*^2} \quad \text{incident power}$$

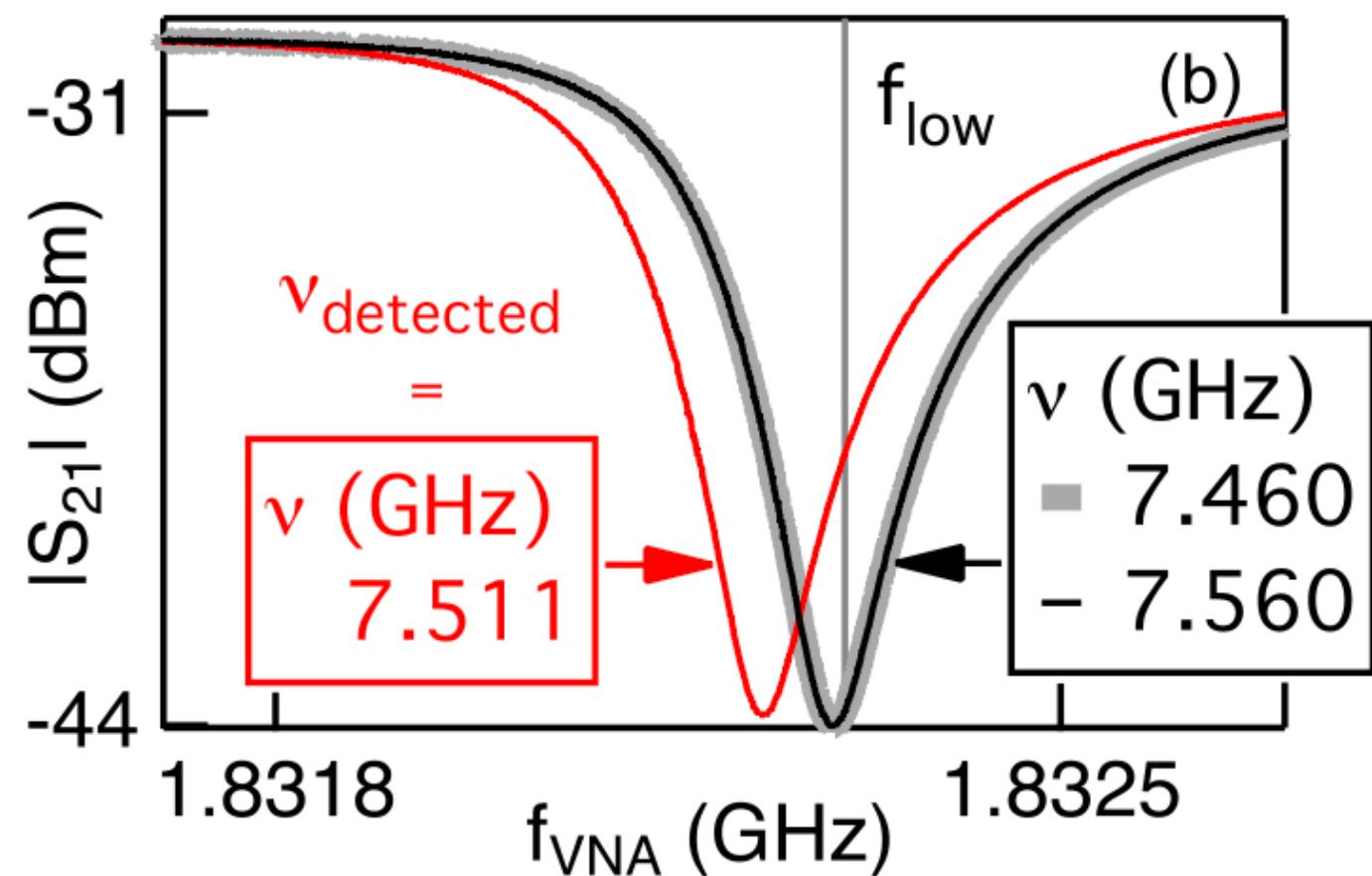
and $I_* \propto n_s$

$$\delta n_s \propto I^2/I_*$$

O. Dupré et al, SuST 30, 045007 (2017).



v -detected = third harmonic



Sub-gap modes in amorphous indium oxide

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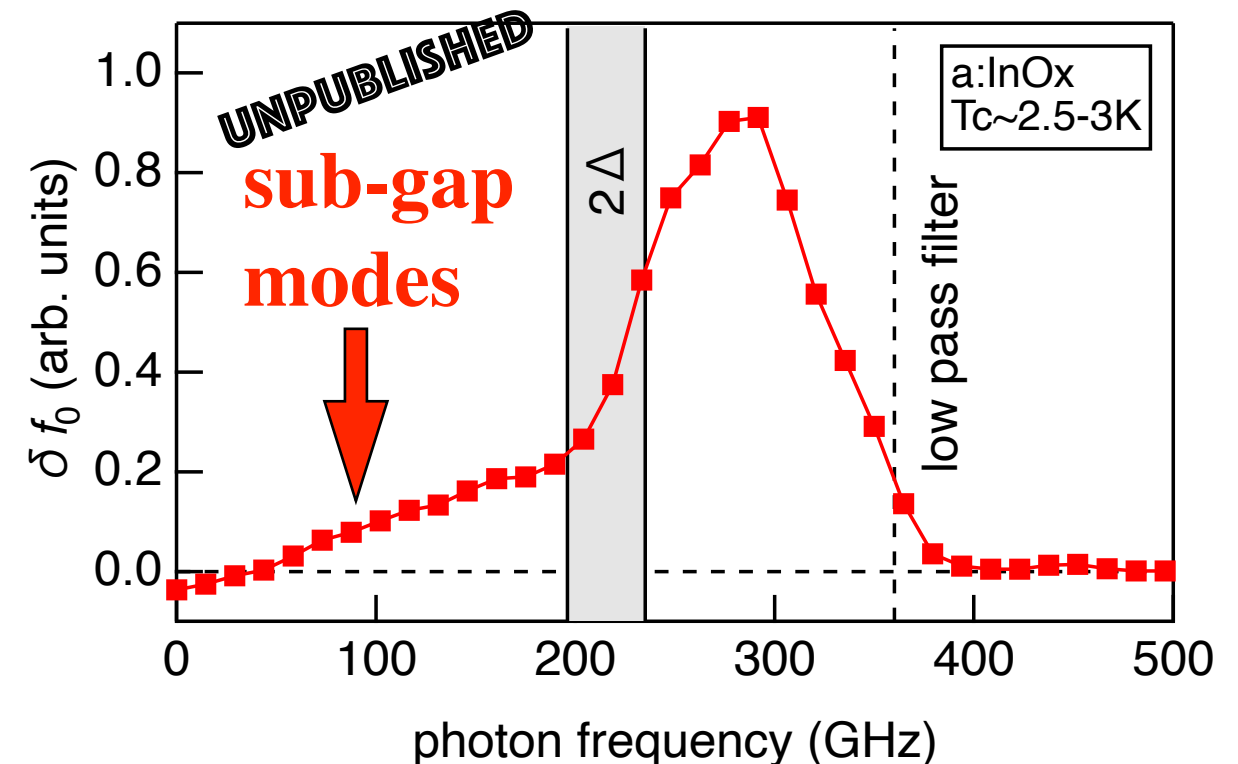
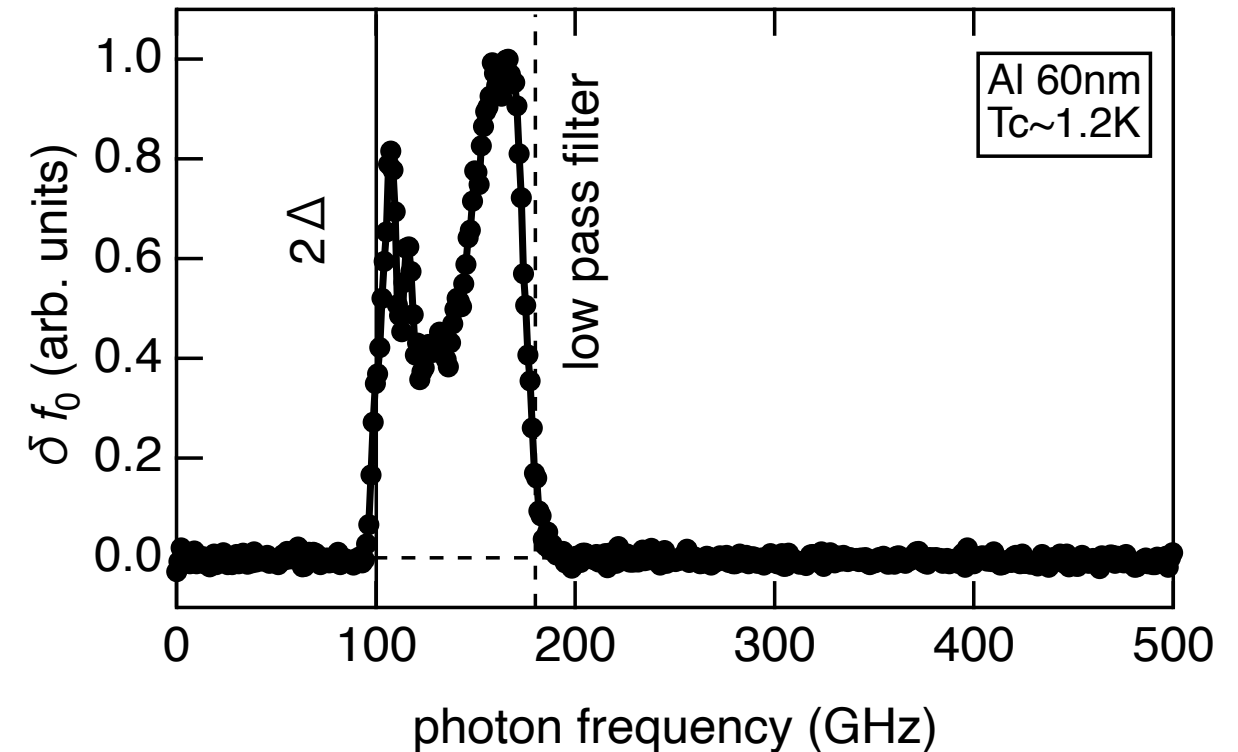
because of low $I_* \sim I_c$

$$J^*(Al) \sim 1.10^{12} A/m^2$$

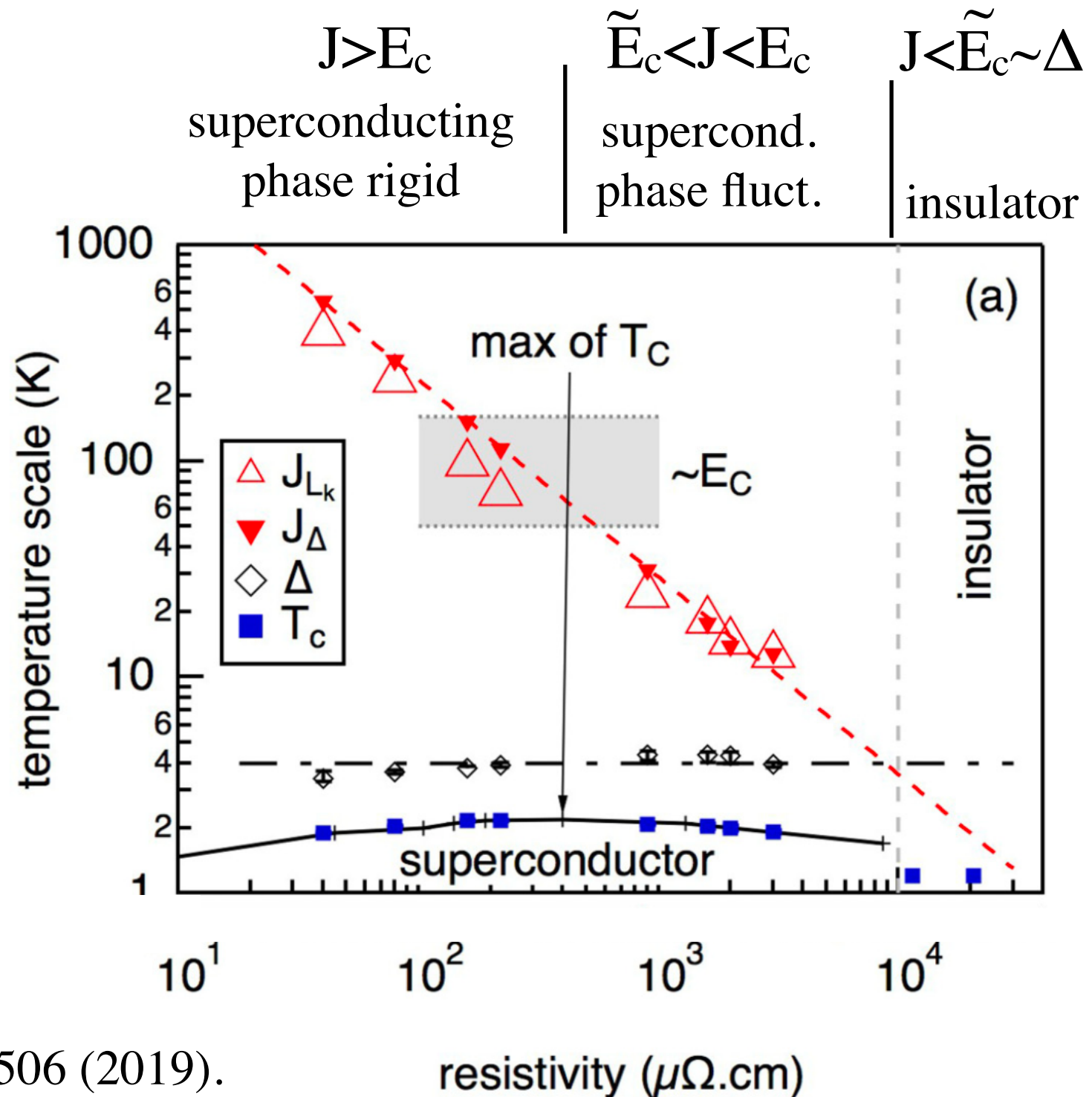
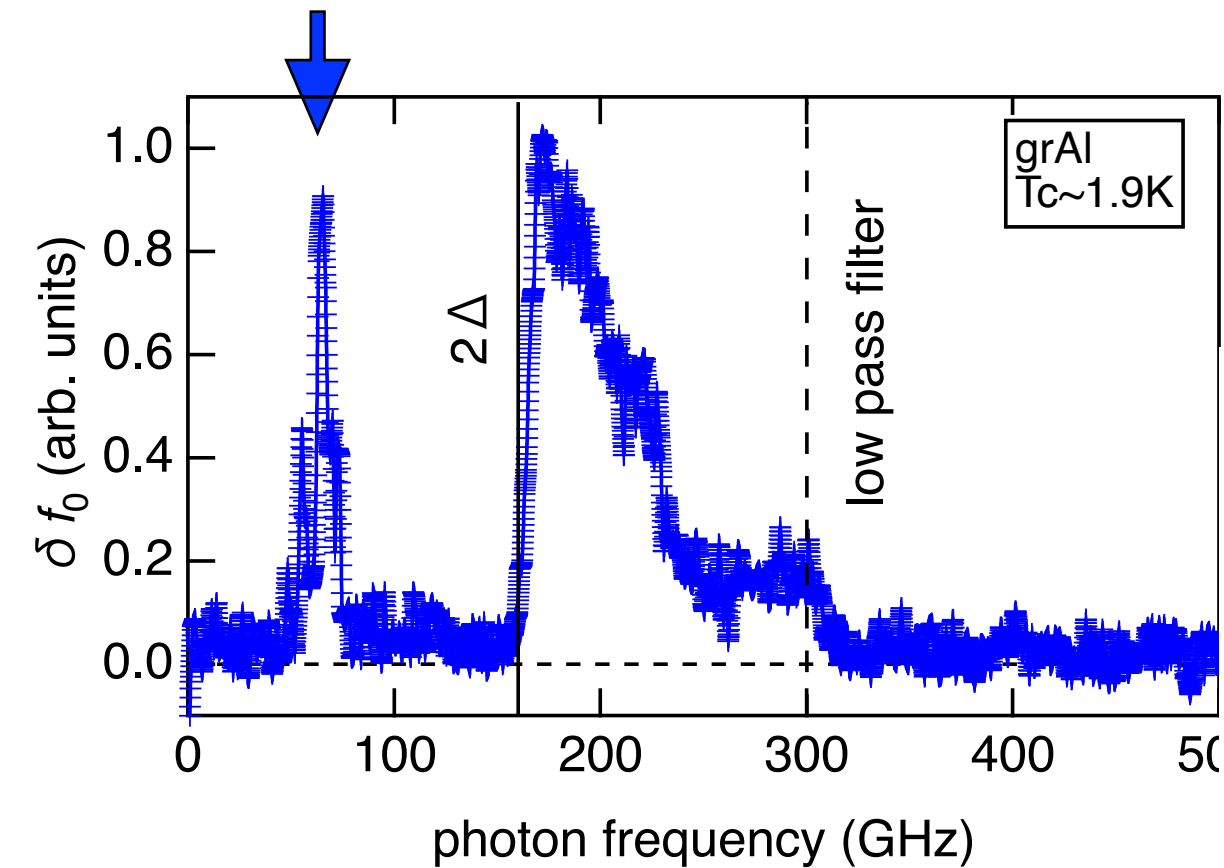
$$\delta n_s \propto I^2/I_*$$

$$10^3 \times n_{qp}$$

$$J^*(a : InO) \sim 4.10^9 A/m^2$$

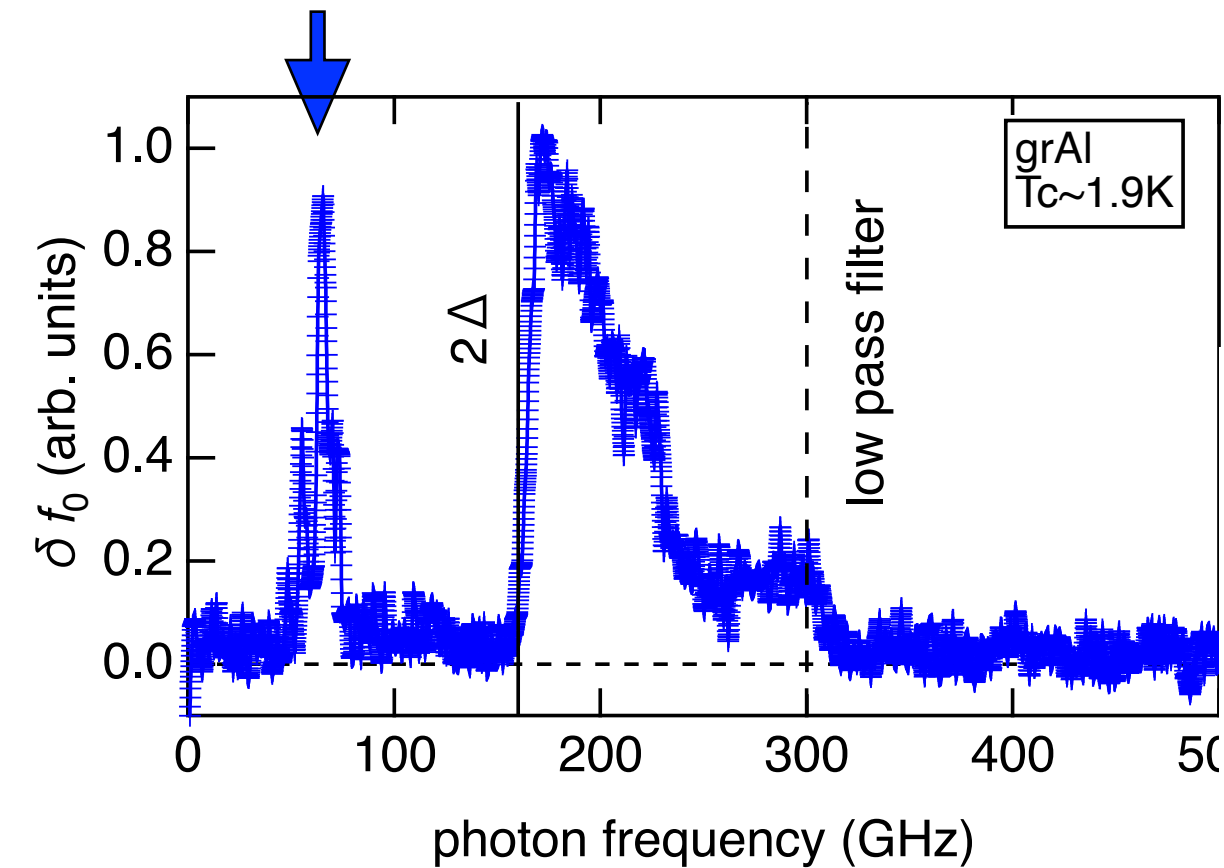


Sub-gap modes in granular aluminum

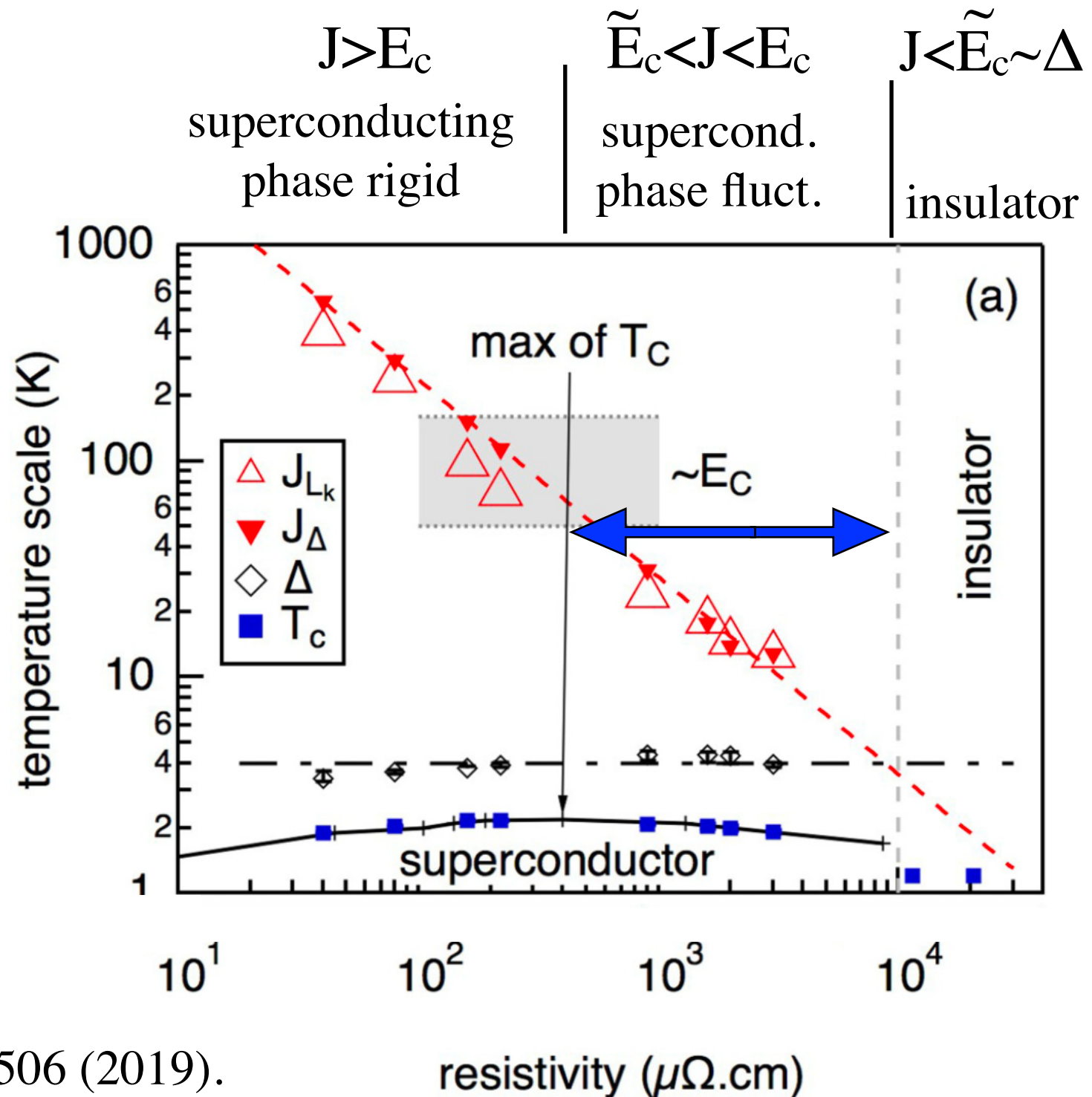


F. Levy-Bertrand et al, Phys. Rev. B 99, 094506 (2019).

Sub-gap modes in granular aluminum



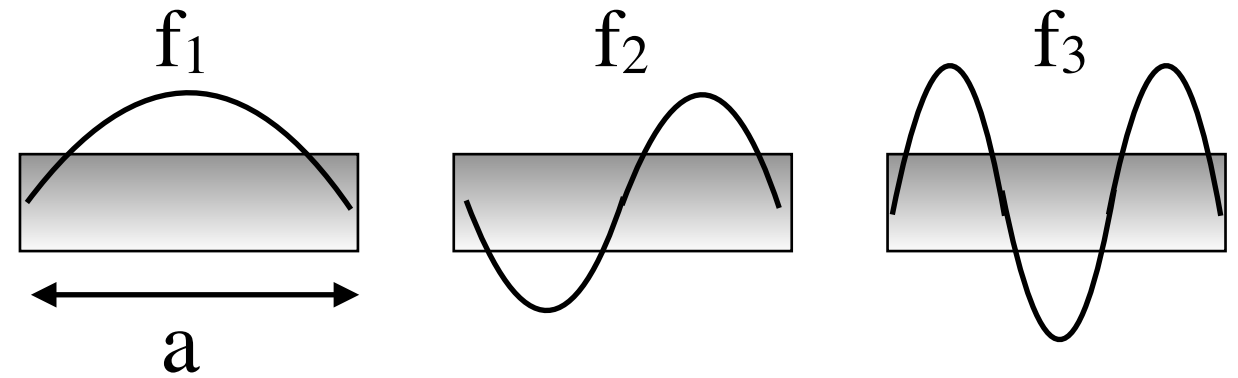
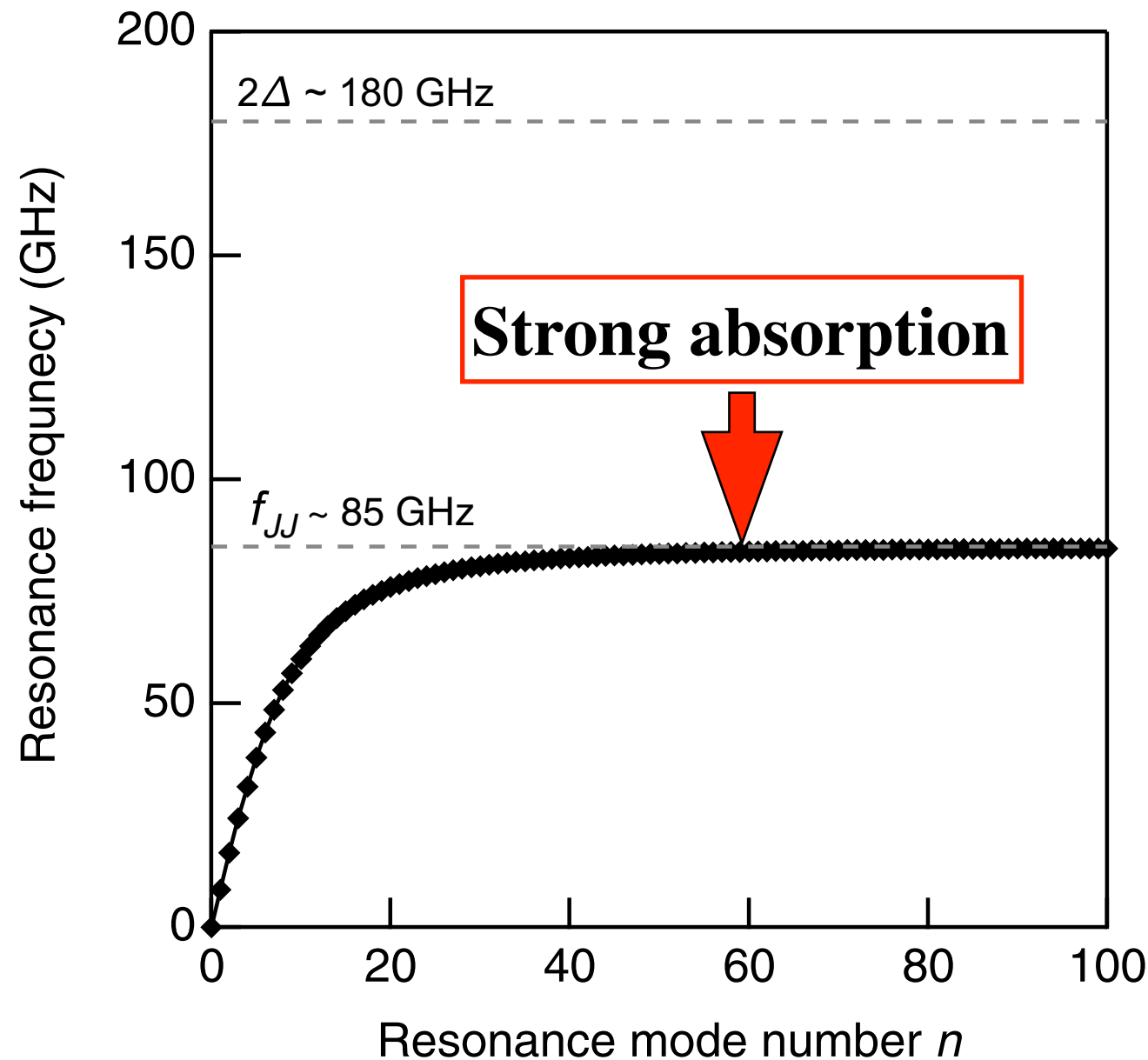
Sub-gap modes when $J < E_c$



F. Levy-Bertrand et al, Phys. Rev. B 99, 094506 (2019).

Sub-gap modes in granular aluminum

Dispersion of the resonances:



array of JJ (like in grAl), saturation at the **JJ plasma frequency**

$$f_{JJ} = \frac{1}{2\pi} \sqrt{\frac{2eI_c}{\hbar C_J}}$$

the density of sub-gap modes diverges, a **strong photon absorption** is expected.

N. Maleeva and al, Nature Communications 9, 3889 (2018).

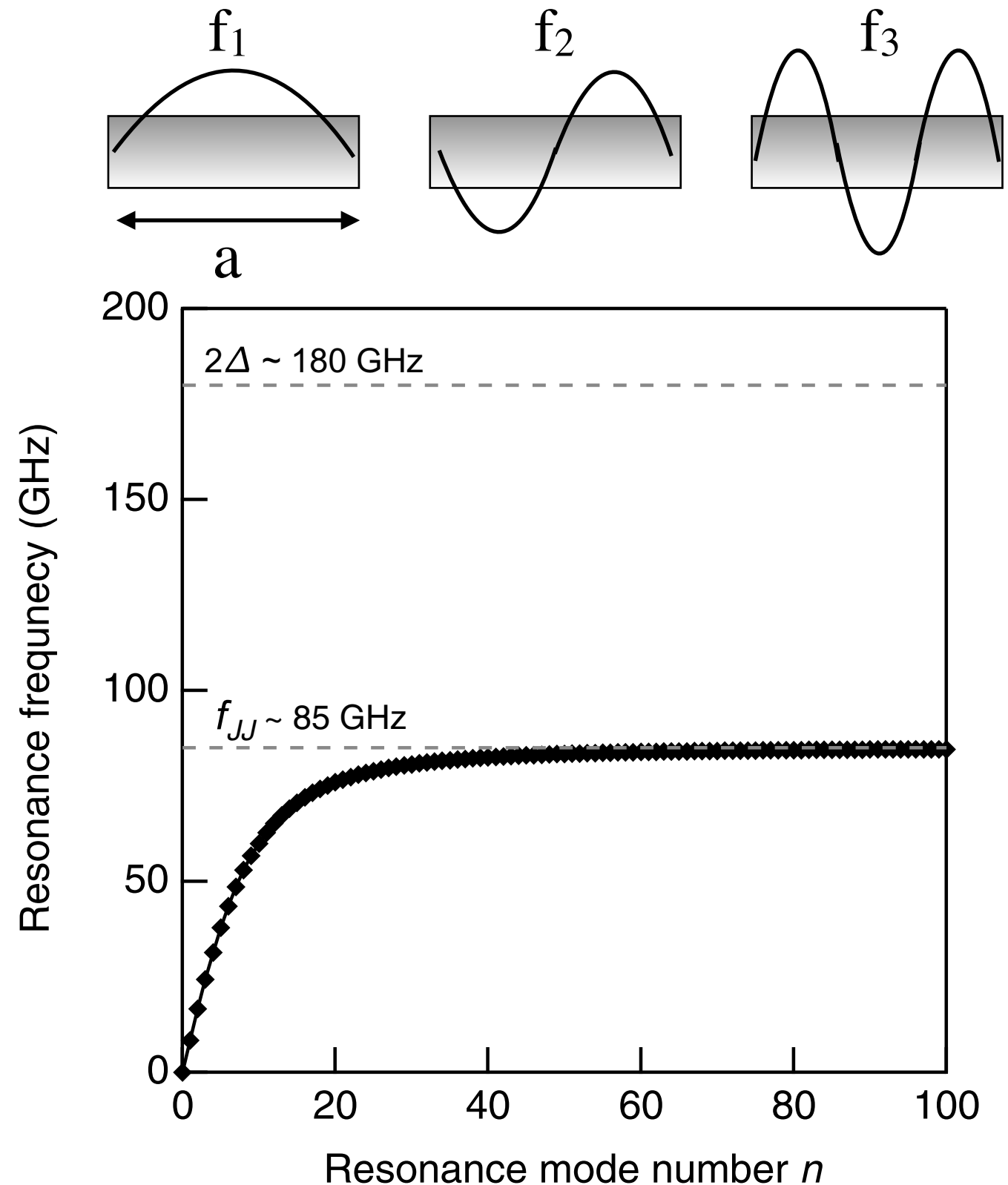
Sub-gap modes: source of extra-dissipation ?

Harmonic sub-gap states f_n
in any **thin superconductor**.

$$\text{And } \frac{\delta n_s}{n_s} \sim - \frac{I^2}{I_c^2}$$

Low critical current $I_c \propto n_s$
results in extra-dissipation
for identical incident power

$$\delta n_s \propto P_{\text{incident}}/I_c$$



Sub-gap modes: source of extra-dissipation ?

Harmonic sub-gap states in thin superconductor

- Sub-gap quasi-particles (with long relaxation time)
- Enhanced dissipation for low critical current (=large L_K)
- ➔ Probable source of extra-dissipation scaling with L_K

$$L_K = \frac{m}{n_s e^2 d} = \frac{\hbar R_{\square}}{\pi \Delta}$$

RELATED TO « ANOMALOUS METAL » ???

Sub-gap modes: source of extra-dissipation ?

Probable extra-dissipation scaling with L_K

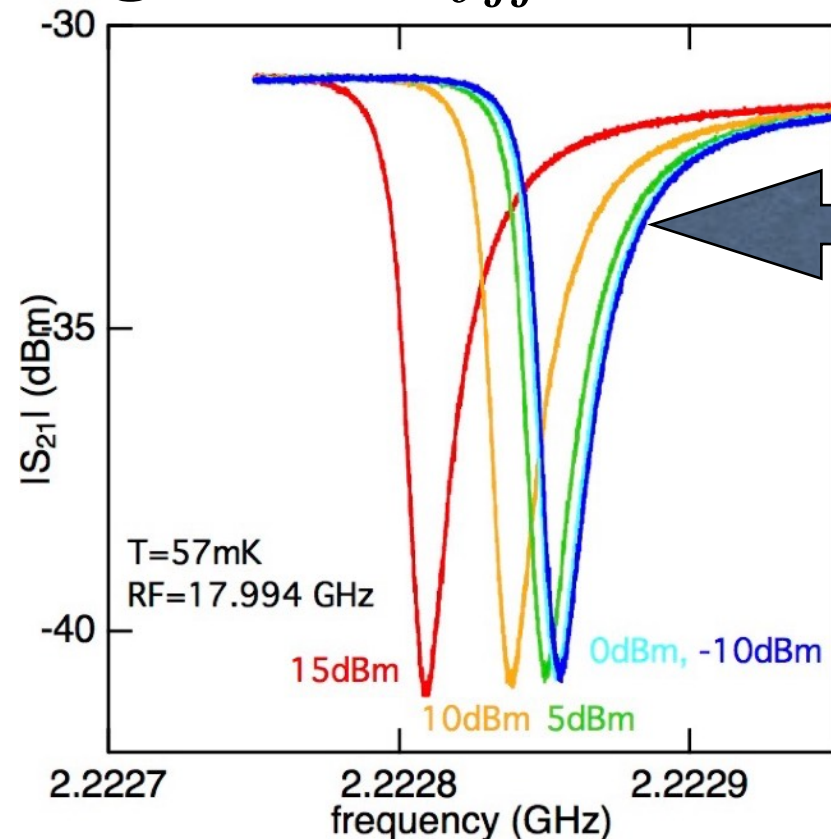
$$L_K = \frac{m}{n_s e^2 d} = \frac{\hbar R_{\square}}{\pi \Delta}$$

Relevant temperature and energy ?

Guess: two level systems (TLS) approach with population: $\exp(-\beta \Delta_{TLS})$

-> because of observation of (strange) TLS behavior ...

grAl: $\nu \ll f_{JJ}$ @ various P

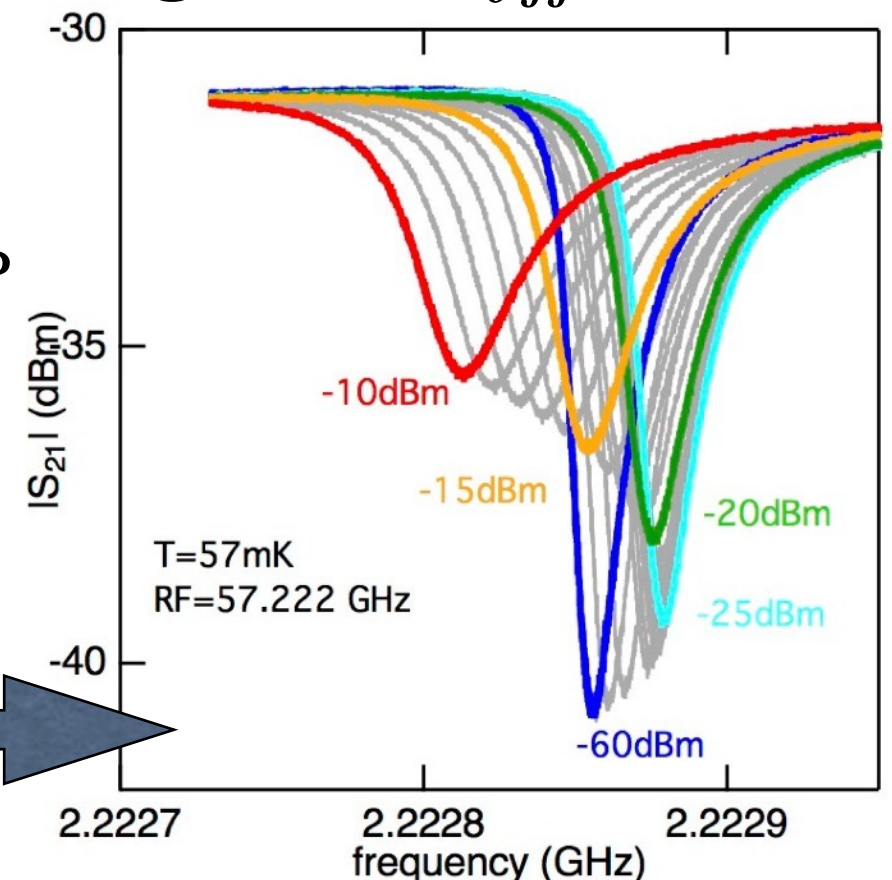


Normal behavior:
 f_{JJ} and Q decrease with P

UNPUBLISHED

« TLS » behavior

grAl: $\nu \sim f_{JJ}$ @ various P



Sub-gap modes: source of extra-dissipation ?

Probable extra-dissipation scaling with L_K

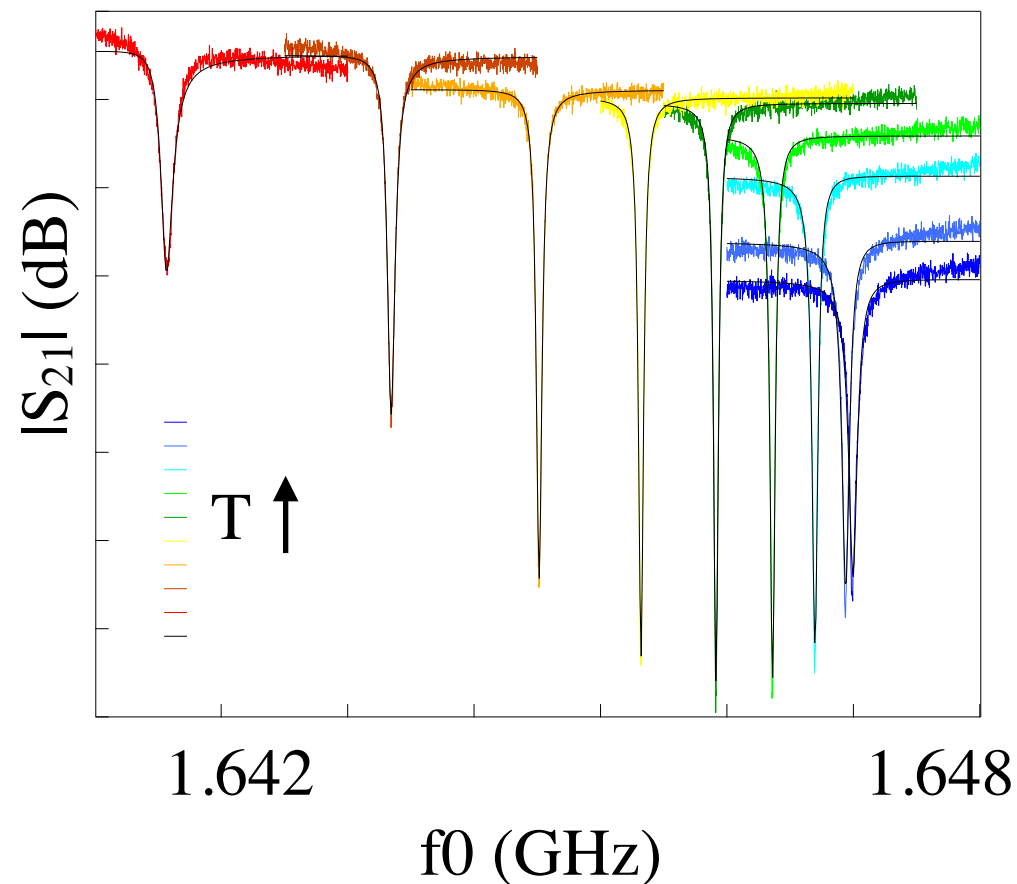
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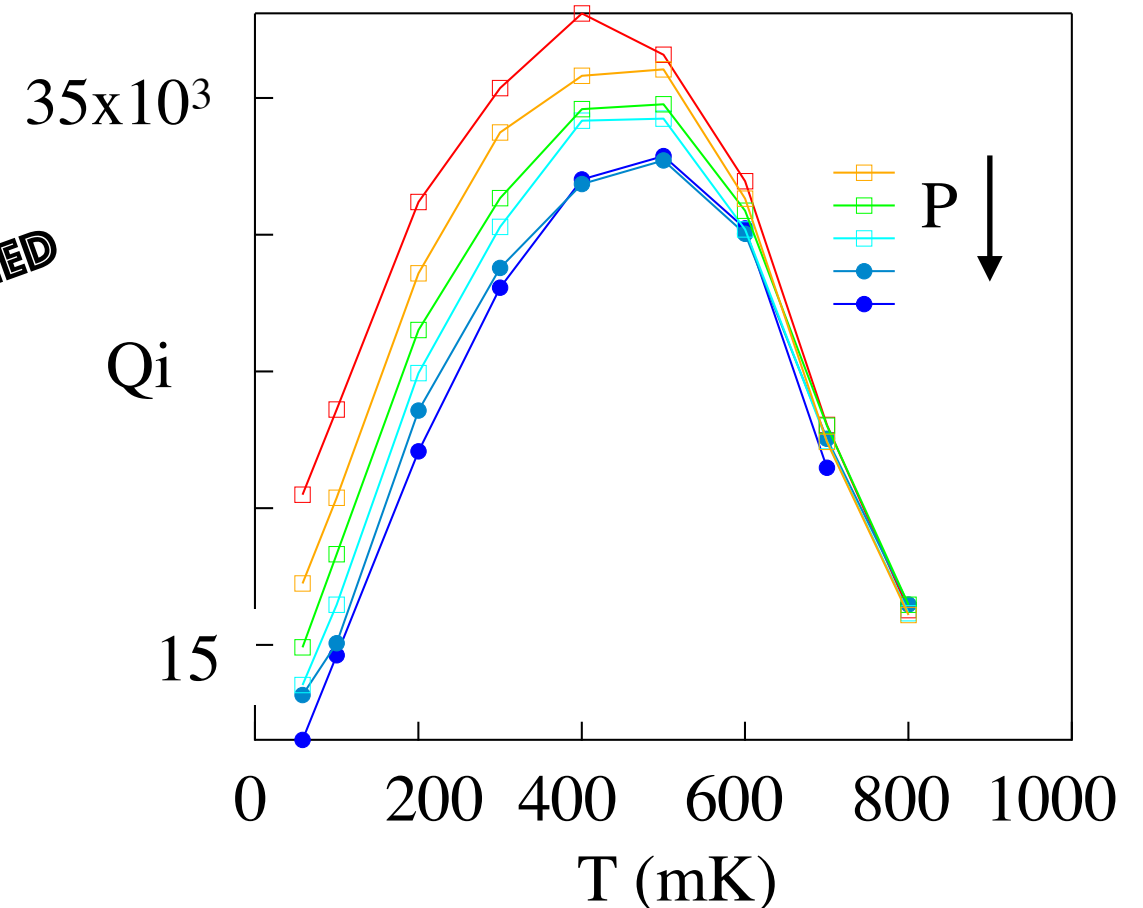
-> because of observation of (strange) TLS behavior ...

a:InO: VNA@various T



a:InO: « TLS » behavior of Q

UNPUBLISHED



Sub-gap modes: source of extra-dissipation ?

Probable extra-dissipation scaling with L_K

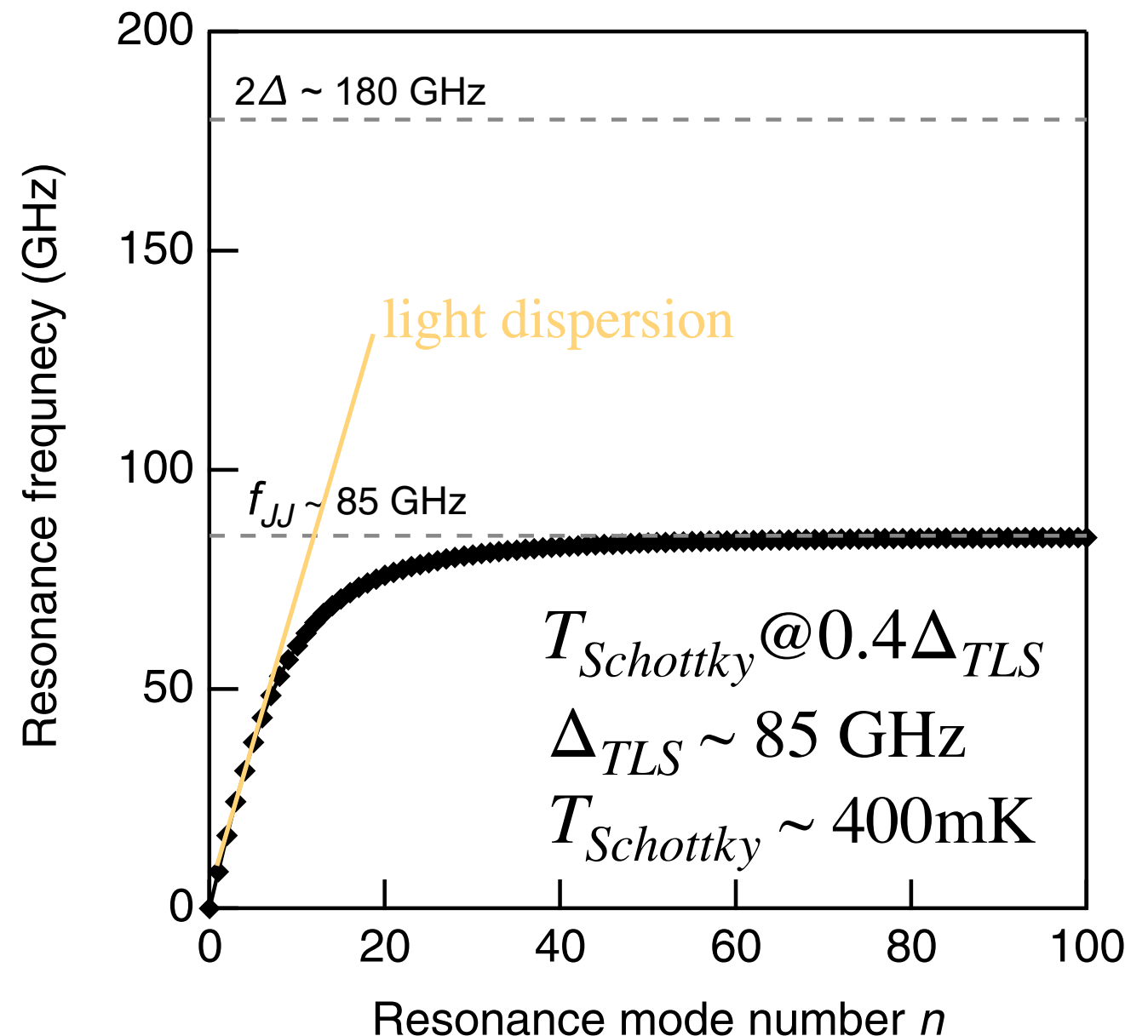
$$L_K = \frac{m}{n_s e^2 d} = \frac{\hbar R_{\square}}{\pi \Delta}$$

Relevant temperature and energy ?

Two level systems (TLS) approach with modes' dispersion ?

Does the deviation from light dispersion matter ?

- modes are more pack in energy
- extra-momenta needed



Sub-gap modes observed with Kinetic Inductance Detectors (KIDs): source of extra-dissipation in disordered thin superconductors ?

Strong sub-gap modes due to harmonic resonances observed in

- amorphous InO KIDs
- granular aluminum KIDs

Strong sub-gap modes due to harmonic resonances:

- Expected in any thin superconductor
- Originating out-of-equilibrium quasi-particles
- Enhanced for low I_c

➡ Probable source of extra-dissipation scaling with L_k

RELATED TO « ANOMALOUS METAL » ???

TEMPERATURE & ENERGY SCALE ?

RELATED TO STRANGE TLS AND SATURATION OF LIFE TIME ?