

Current bistability in insulators with large localization lengths

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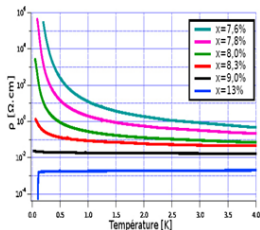
Outline

- Superconductor to insulator transitions
- Biestability in the insulating side
- Experimental results on $\text{Y}_x\text{Si}_{1-x}$ thin films
- Hot-electron model
- Extended hot-electron model
- Experimental results on InSb thin films
- Conclusions

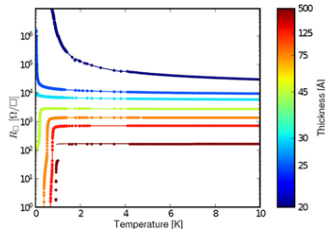
Superconductor to insulator transition

- Collaboration with experimental group of Claire Marrache-Kikuchi
- They can induce the transition by three different mechanisms

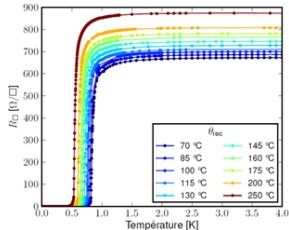
Composition



Thickness



Heat treatment

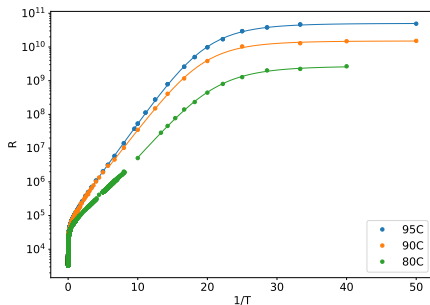


$\text{Y}_x\text{Si}_{1-x}$ thin films

Heat treatment

We consider insulating samples, close to the SIT

Effect of annealing



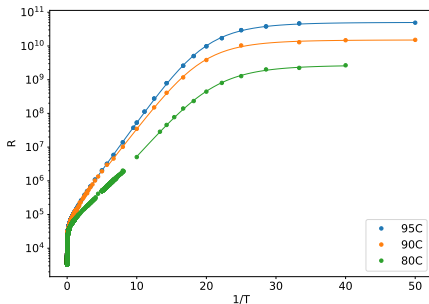
- Annealing increases disorder

$\text{Y}_x\text{Si}_{1-x}$ thin films

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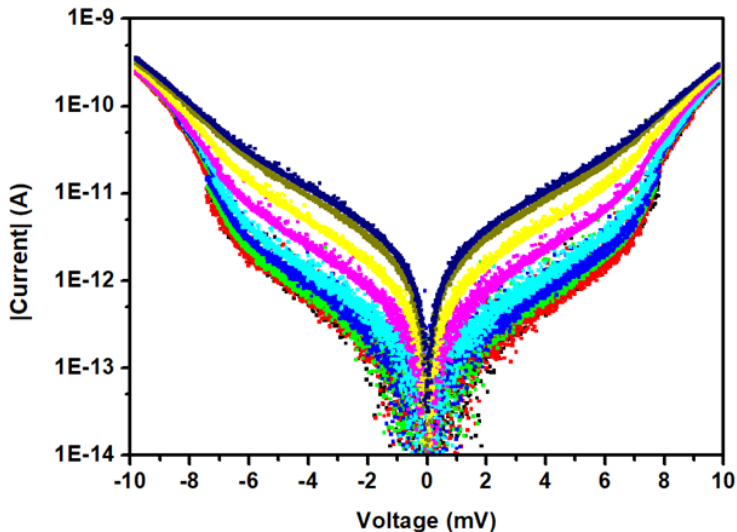


- Annealing increases disorder
- At low T , activated behavior
 - Mobility edge
 - Charging energy
 - Superconducting gap
 - Logarithmic interaction
 - Nearest neighbors

$\text{Y}_x\text{Si}_{1-x}$ thin films

$I - V$ curves

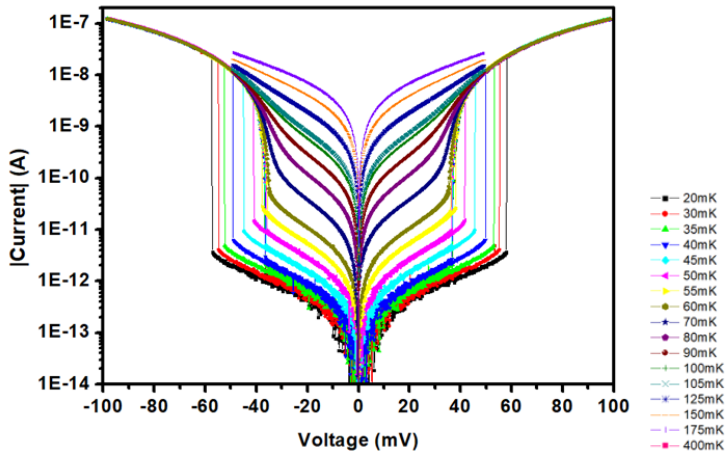
Annealing at 80°



$\text{Y}_x\text{Si}_{1-x}$ thin films

$I - V$ curves

Annealing at 95°



- Jumps in I by four orders of magnitude
- Strong hysteresis

Hot electron model

Similar results by Ovadia et al. (2009) and Ladieu et al. (2000)

They were explained by Altshuler et al. (2009) in terms of the hot-electron model (Wang, PRB, 1990)

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Effective temperature for electrons determines completely the resistance of the system $R(T, V) = R(T_{\text{eff}}, 0)$:

$$\frac{V}{I} = R_0 \exp \left(\frac{T_0}{T_{\text{eff}}} \right),$$

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$$\frac{V}{I} = R_0 \exp\left(\frac{T_0}{T_{\text{eff}}}\right),$$

The effective temperature relaxes to the phonon temperature T by phonon emission. The dissipated power is equal to

$$P = \alpha(T_{\text{eff}}^{\beta} - T_{\text{ph}}^{\beta})$$

α related to the electron-phonon coupling.

Self-consistent equation for the effective temperature

$$\frac{V^2}{R_0} \exp\left(-\frac{T_0}{T_{\text{eff}}}\right) = \alpha(T_{\text{eff}}^{\beta} - T_{\text{ph}}^{\beta})$$

Critical behavior

Critical point at

$$T_c = (\beta + 1)^{-\frac{\beta+1}{\beta}} T_0.$$

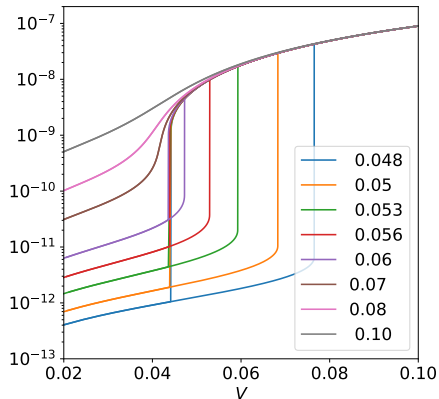
(parameter independent)

The critical voltage is

$$V_c = \sqrt{\frac{\alpha R_0 \beta T_0^\beta e^{\beta+1}}{(\beta + 1)^{\beta+1}}}$$

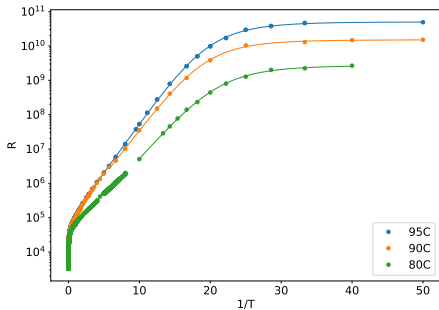
A similar transition should always occur for all insulating systems
(maybe unobservable)

Hot-electron model



Linear regime

Saturation



- Saturation can be explained with the hot-electron model

$$P_{\text{ext}} = \alpha(T_e^\beta - T_{\text{ph}}^\beta)$$

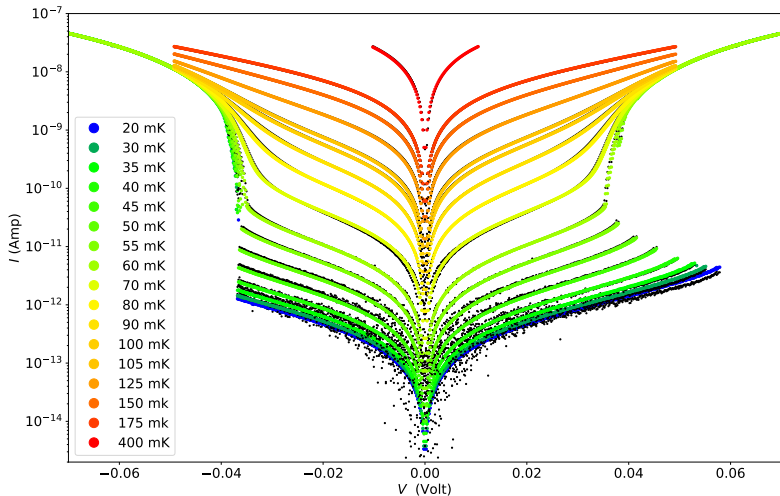
$$T_{\text{min}} = \frac{P_{\text{ext}}^{1/\beta}}{\alpha}$$

$$T_{\text{ap}}^\beta = T_{\text{ph}}^\beta + T_{\text{min}}^\beta$$

Fitting of experimental results

$I - V$ curves

Sample annealed at 95°

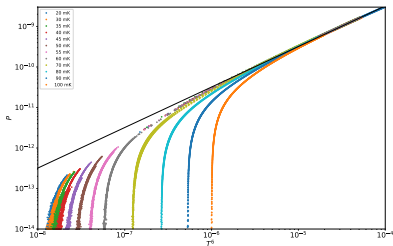


Free parameters: R_0 , T_0 , α (electron-phonon coupling), and P_{ext} ($\beta = 6$ fix)

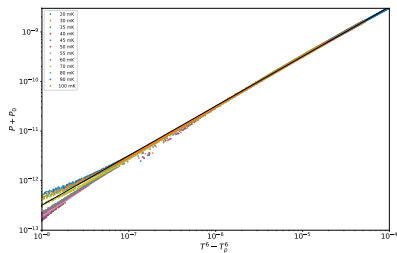
Dissipated power

$$P + P_{\text{ext}} = \alpha(T_{\text{eff}}^{\beta} - T_{\text{ph}}^{\beta}) \quad \beta = 6$$

Power vs T_{eff}



Renormalized power

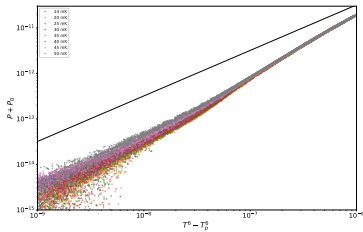


Sample annealed at 95°

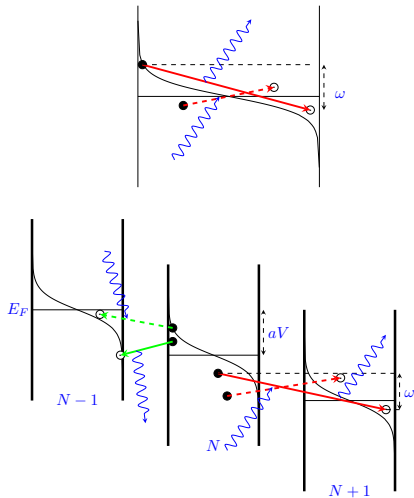
Dissipated power

Sample annealed at 80°

$$\beta = 6$$



- A second dissipation mechanism

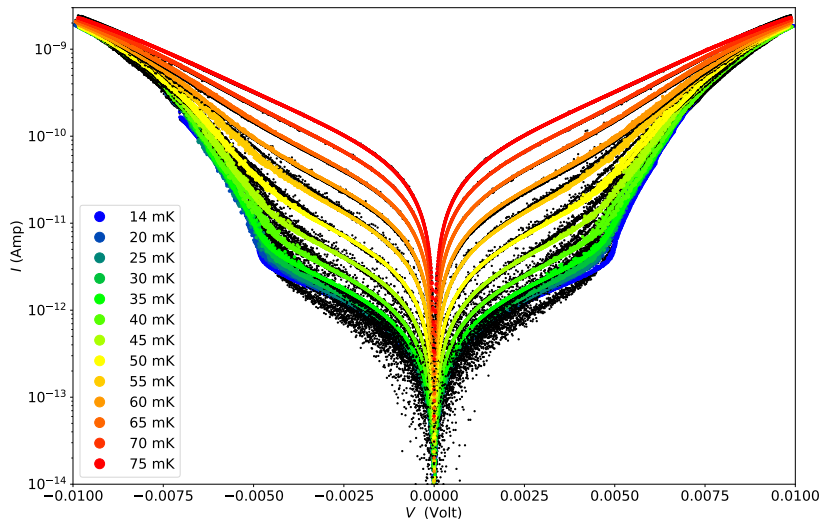


$$P_2 = \alpha_2((T_{\text{eff}} + aV)^\beta - T_{\text{ph}}^\beta)e^{-\frac{T_0 - aV}{T_{\text{eff}}}}$$

Fitting of experimental results

$I - V$ curves

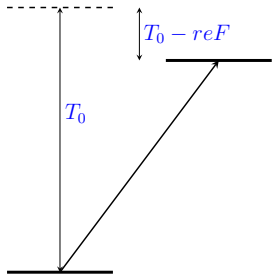
Sample annealed at 80°



Non-linear effects

We include the standard exponential field-effect in hopping conduction

$$R = R_0 \exp\left(\frac{T_0 - aV}{T_{\text{eff}}}\right)$$

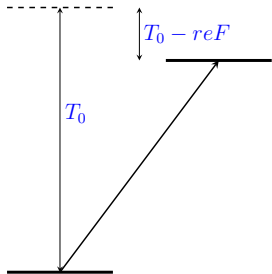


$$a = \frac{er}{2L} \quad r \approx \xi$$

Non-linear effects

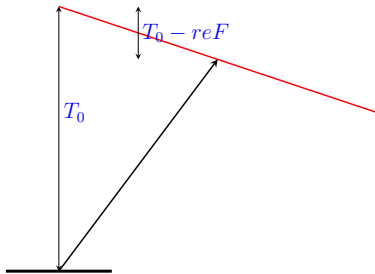
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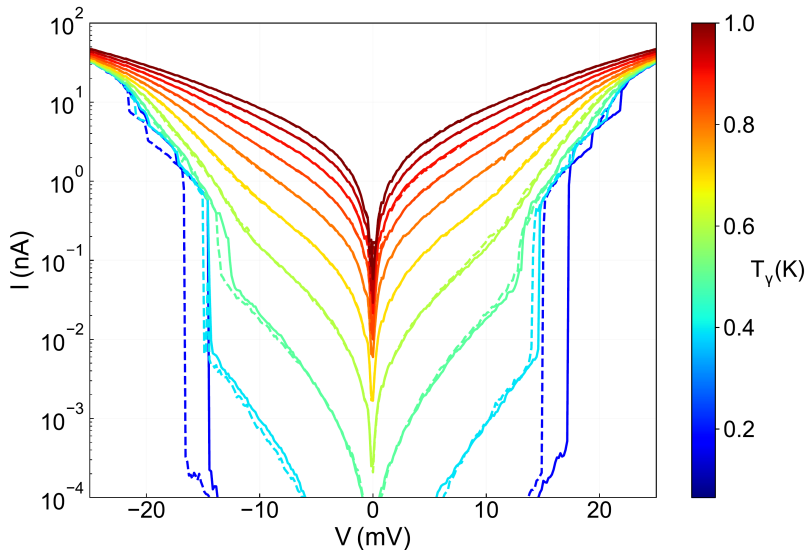
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The same effect should appear in an upper Hubbard band



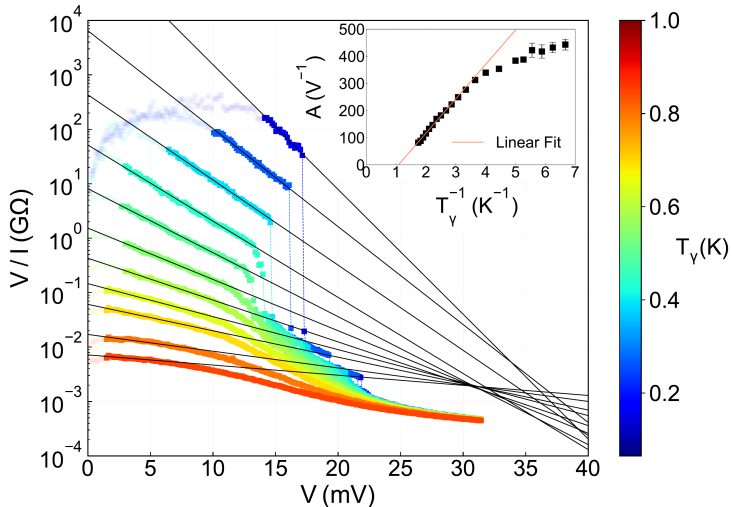
Experiments on InSb thin films

- J. Gough and M. Pepper, UCL



Experiments on InSb thin films

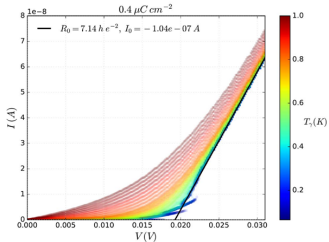
- Exponential field-effect



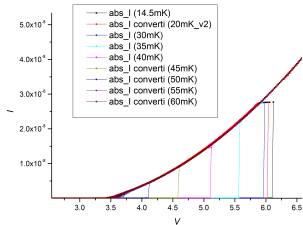
- No hot-electron effects

$I - V$ curves

InSb thin films

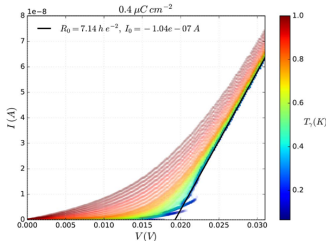


Y_xSi_{1-x} thin films

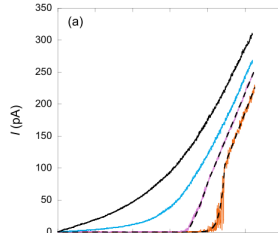


$I - V$ curves

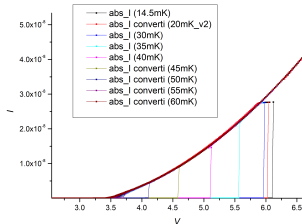
InSb thin films



MOSFETs



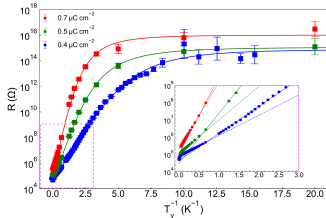
$\text{Y}_x\text{Si}_{1-x}$ thin films



- Claimed (by Munyan, Stemmer) to be a Wigner physics effect
- Transition from solid (glass) to fluid
- Avalanches

Overactivation

InSb thin films



- In disordered InSb with a large localization length, overactivation is observed
- In $\text{Y}_x\text{Si}_{1-x}$ thin films the overactivation was ascribed to the superconducting gap
- Saturation is also relevant in InSb, but probably with a different origin than in $\text{Y}_x\text{Si}_{1-x}$

Conclusions

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- Excellent procedure to determine the localization length ξ
- Understanding of nonlinear effects in hopping
- There are at least two types of bistabilities

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Open questions

- Nature of the activation energy
- Role of superconductivity