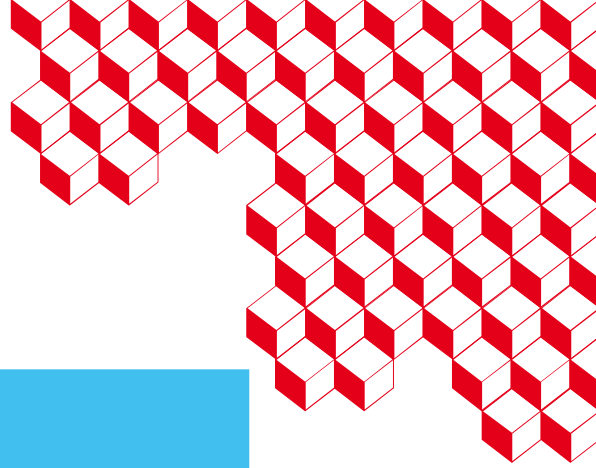




Pre-equilibrium Nuclear Reactions: Reaction Mechanisms and Impact on Observables

M. Dupuis, CEA, DAM, DIF

IJCLab, 5 Feb. 2026

Collaborators

Microscopic inelastic scattering modeling :

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Application to surrogate studies : B. Jurado et al. (LP2I Bordeaux)



Applications to nuclear data:

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Applications to nuclear structure studies :

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N. Pillet, N. Dubray, S. Péru, J.-P. Ebran (CEA, DAM, DIF)



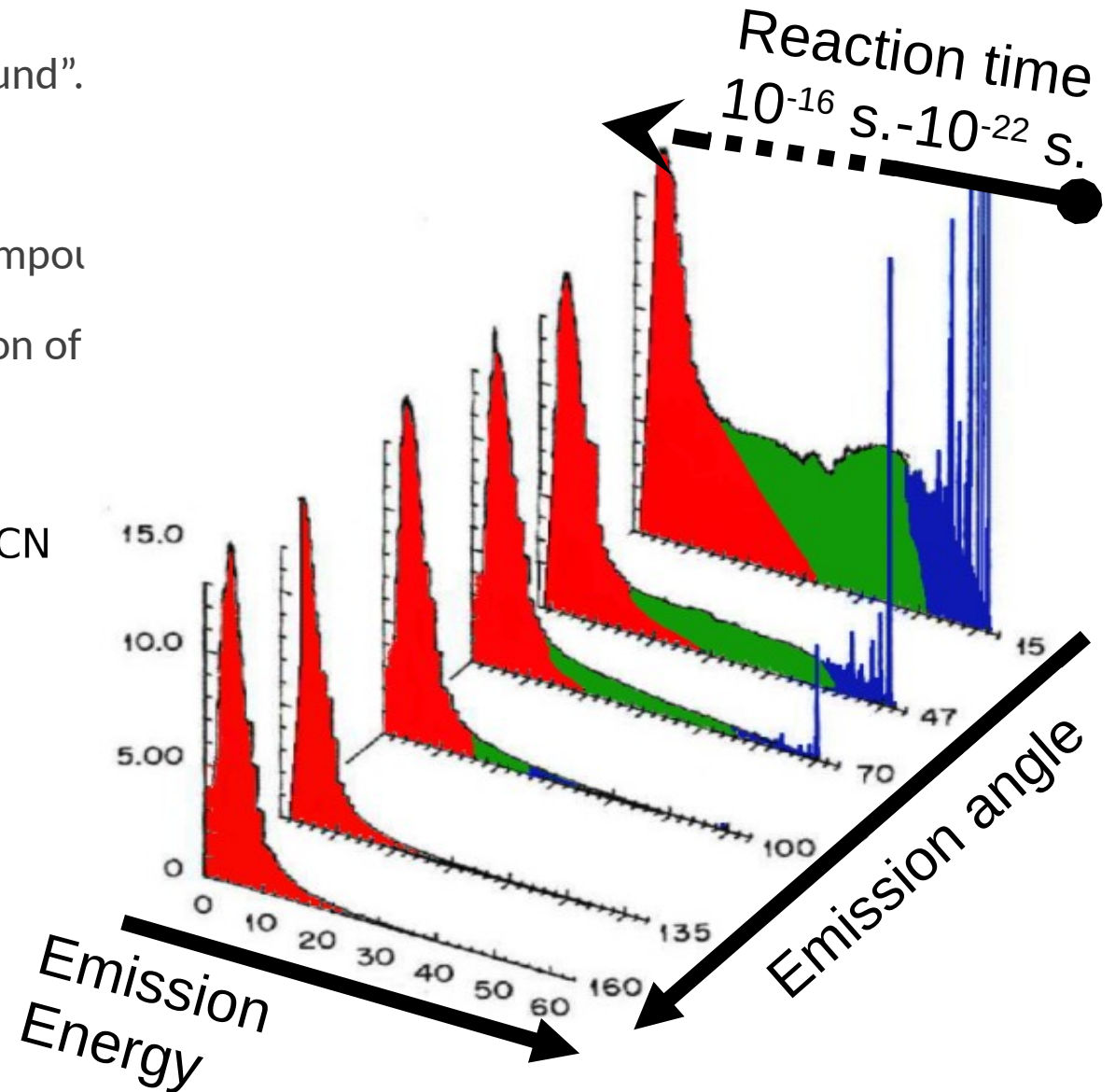
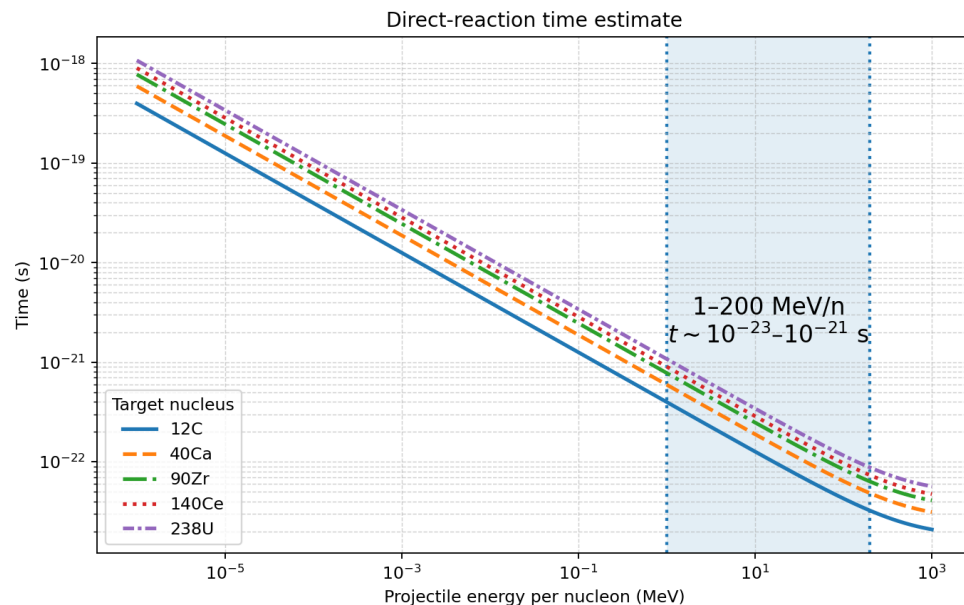
Outline

- Microscopic inelastic scattering modeling, to discrete levels and continuum, spherical/deformed targets : answer to applicative questions ?
 - Nuclear data production
 - Experimental set-up optimization
 - Experimental interpretation, especially for exotic nuclei.
- Applications for nuclear data : $(n,n'\gamma)$; (n,xn) ; fission ; isomer production ; (n,γ) .
- Nuclear reaction modeling input for surrogate reaction method.
- Applications for nuclear structure : new mean field input.
- Three main directions of improvements : NS input / reaction mechanisms / UQ and propagation.
- Conclusions and perspectives.

What pre-equilibrium means ?

- Inclusive spectra often require more than “direct + compound”.
- Process of thermalisation of the composite system
- Reaction time : longer than direct but much faster than compound
- Pre-equilibrium emission = emission before full equilibration of compound nucleus.

$$\frac{d^2\sigma}{dE d\Omega} \approx \left(\frac{d^2\sigma}{dE d\Omega}\right)_{\text{direct}} + \left(\frac{d^2\sigma}{dE d\Omega}\right)_{\text{preeq}} + \left(\frac{d^2\sigma}{dE d\Omega}\right)_{\text{CN}}$$

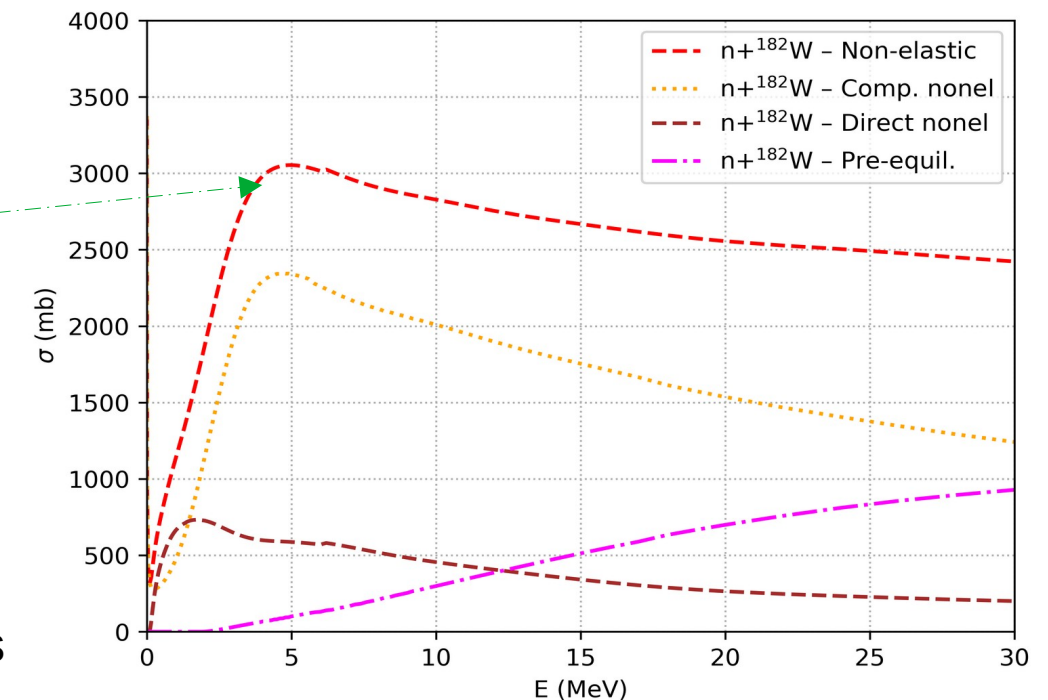
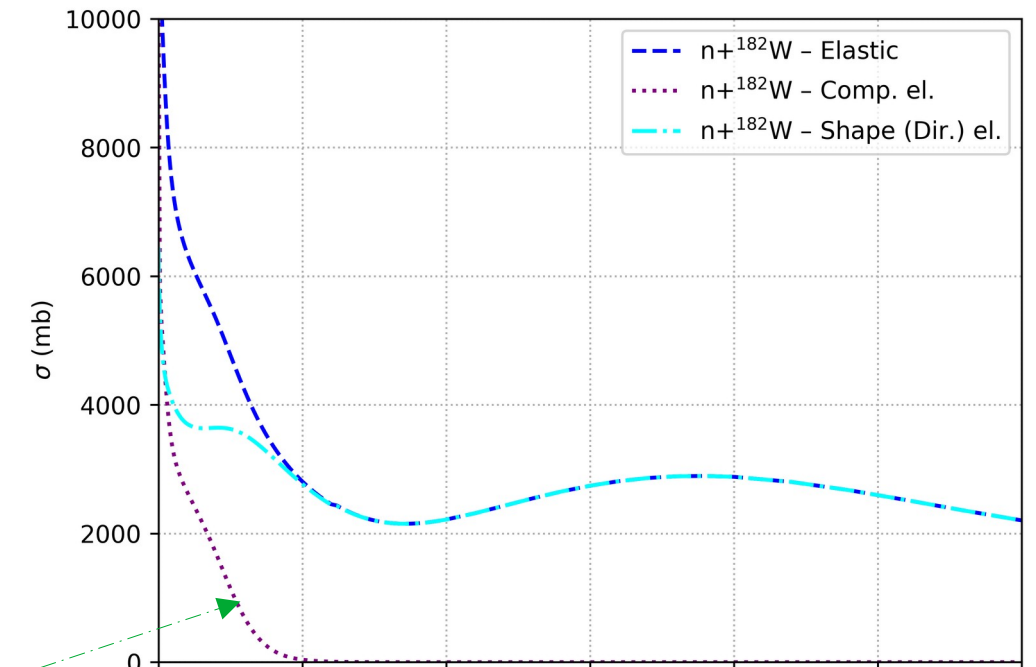
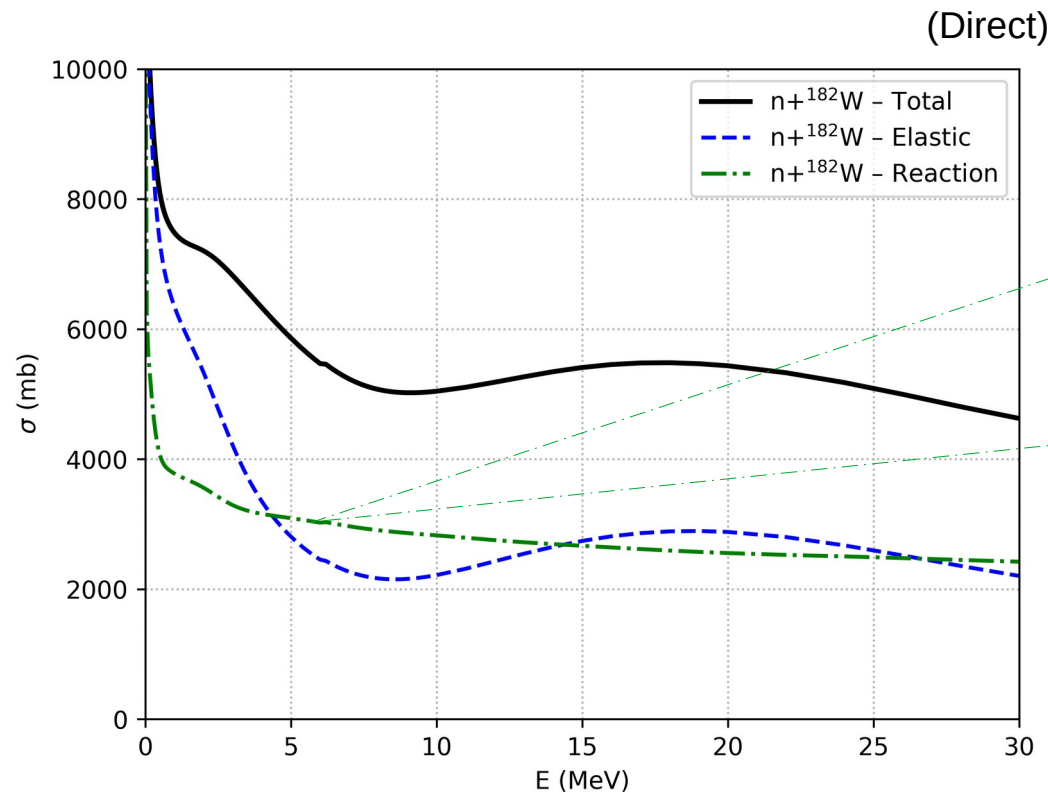


Pre-equilibrium Emission

Total = Dir. Elastic + Reaction

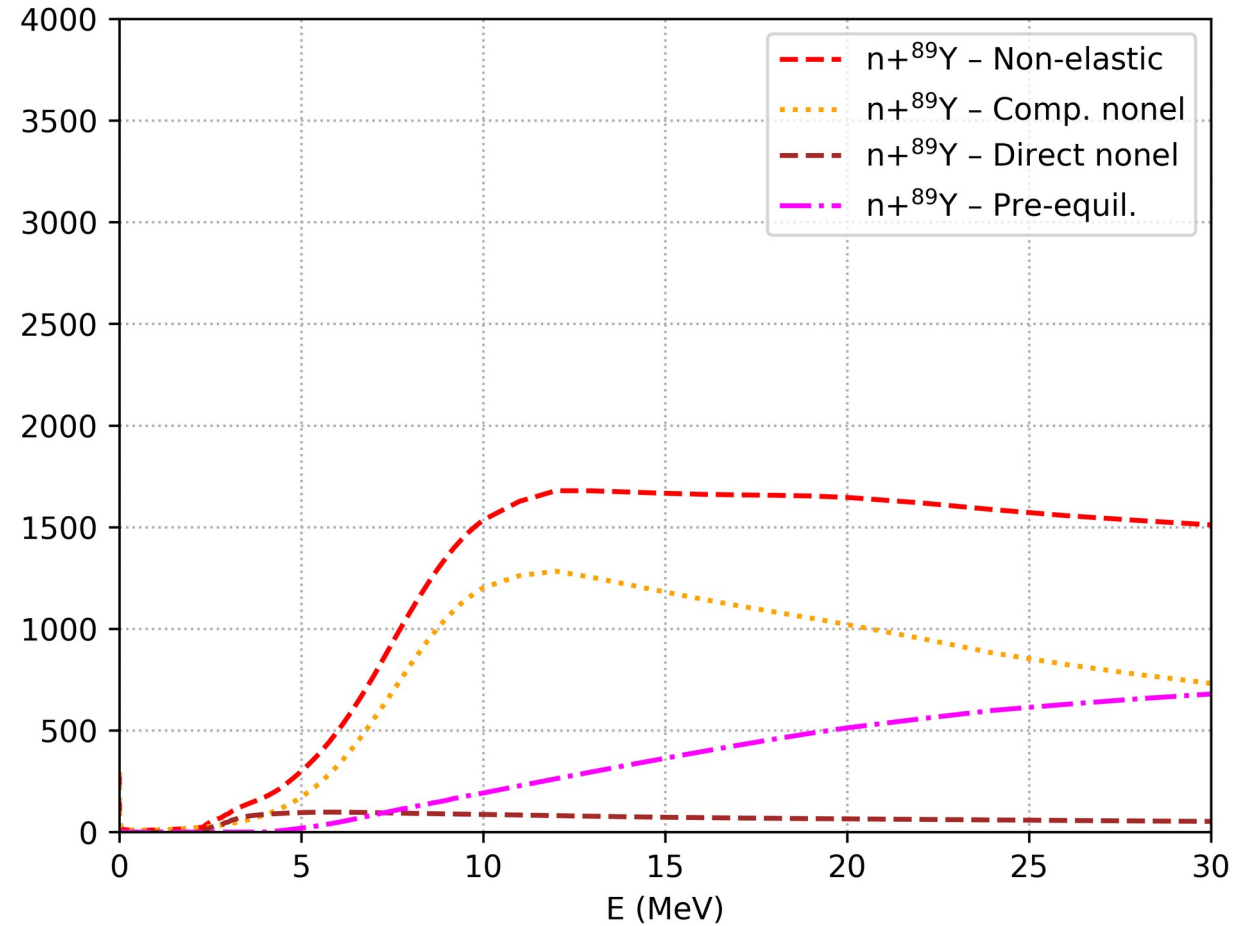
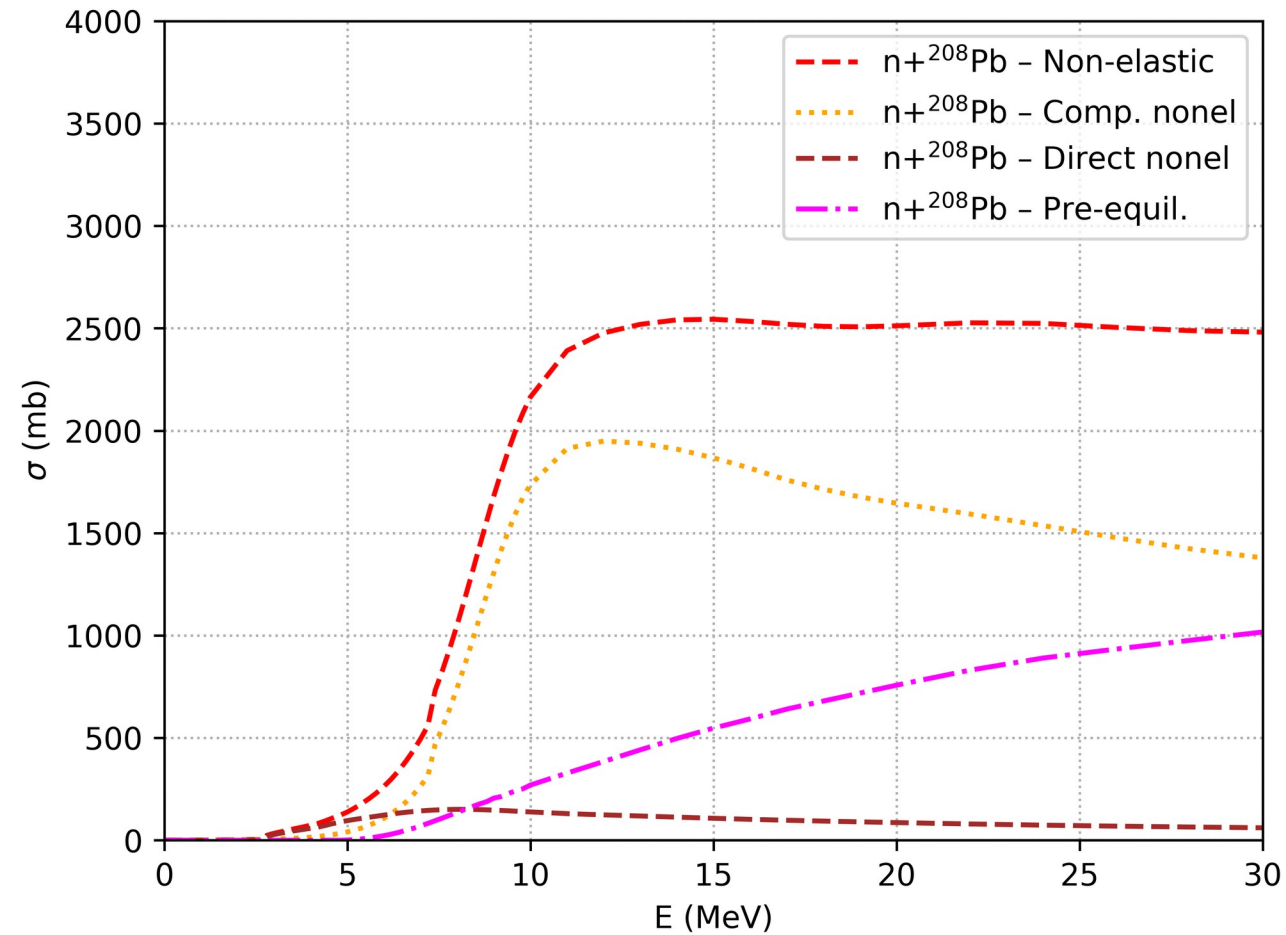
Reaction = Non Elastic + CN elastic

Non Elastic = Dir Non el. + Pre-eq + CN non-eq



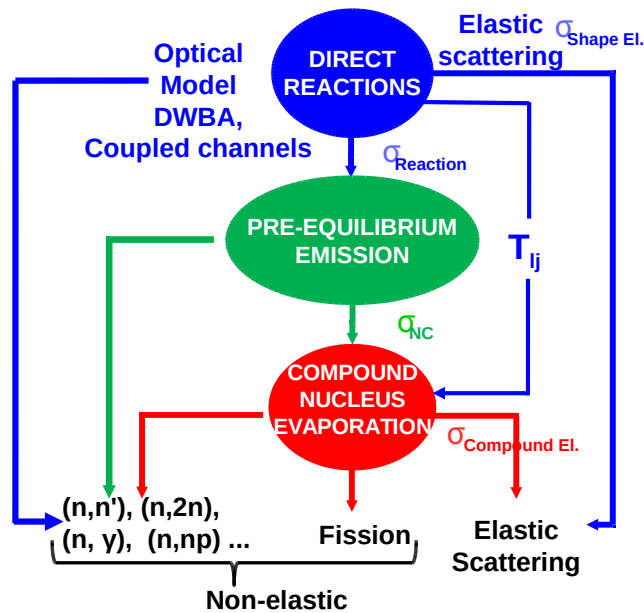
Calculated with code Talys

Pre-equilibrium Emission



Calculated with code Talys

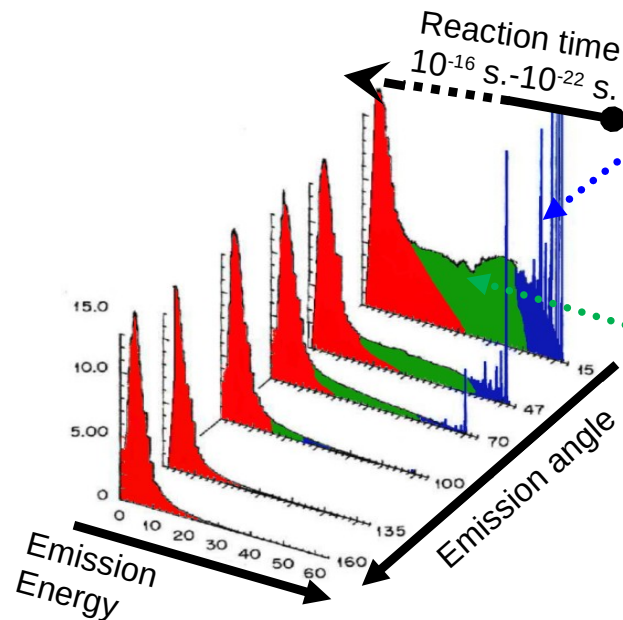
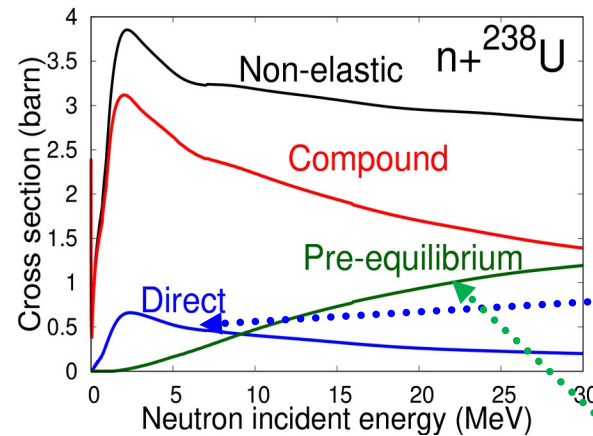
Reaction mechanisms



Compound elastic
Compound inelastic : optical potential, CC, LD
Gamma emission : GSF

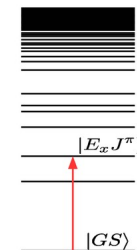
Compound Emission

Hauser-Feshbach
Width fluctuations
LD, GSF, OMP, NS



Direct reactions

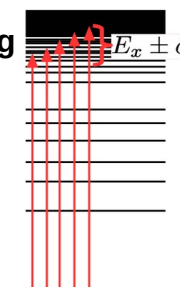
Shape elastic
Inelastic to discrete levels and GR
Transfer



Optical Potential
Coupled Channels, DWBA
Sensitivity to NS
Details (matter densities)

Pre-equilibrium

Inelastic scattering to continuum
Multiple emission



Phenomenological (exciton)
Hybrid, semi-classical (intranuclear cascade)
Quantum approaches (FKK, NWW, TUL)
Multistep process

Pre-equilibrium Models

- Exciton (statistical master equation) : $E = \text{few MeV} - 200 \text{ MeV}$
- Quantum multistep direct and compound (MSD vs MSC) : $E = \text{threshold} - 200 \text{ MeV}$, perturbative, statistical approximation (energy/ensemble averaging, sudden/adiabatic approximation ...)
- Hybrids (non-equilibrium nuclear dynamics, smooth connection to CN regime, excited configuration with time evolution) $\rightarrow$ solve effective transport equation in exciton space. $E = 20-200 \text{ MeV}$
- Intra-nuclear cascade (INC, classical trajectory, event by event dynamic, quantum correction) : $E > 100 \text{ MeV}$, but good results for $E > 14 \text{ MeV}$,
- Eikonal/Glauber : $E > 100 \text{ MeV}$

Exciton model for pre-equilibrium emission

- Time evolution of excitons number which characterise the system state
- Incident nucleon, n particle – n hole excitation : $N = 2n + 1$ excitons (projectile count as 1)
- $N=2n+1 \rightarrow p=n+1$;
- transition rate : $\lambda^{\pm}(n, E) \sim |M|^2 \omega^{\pm}(n, E)$

→ Master equation for occupation probability :

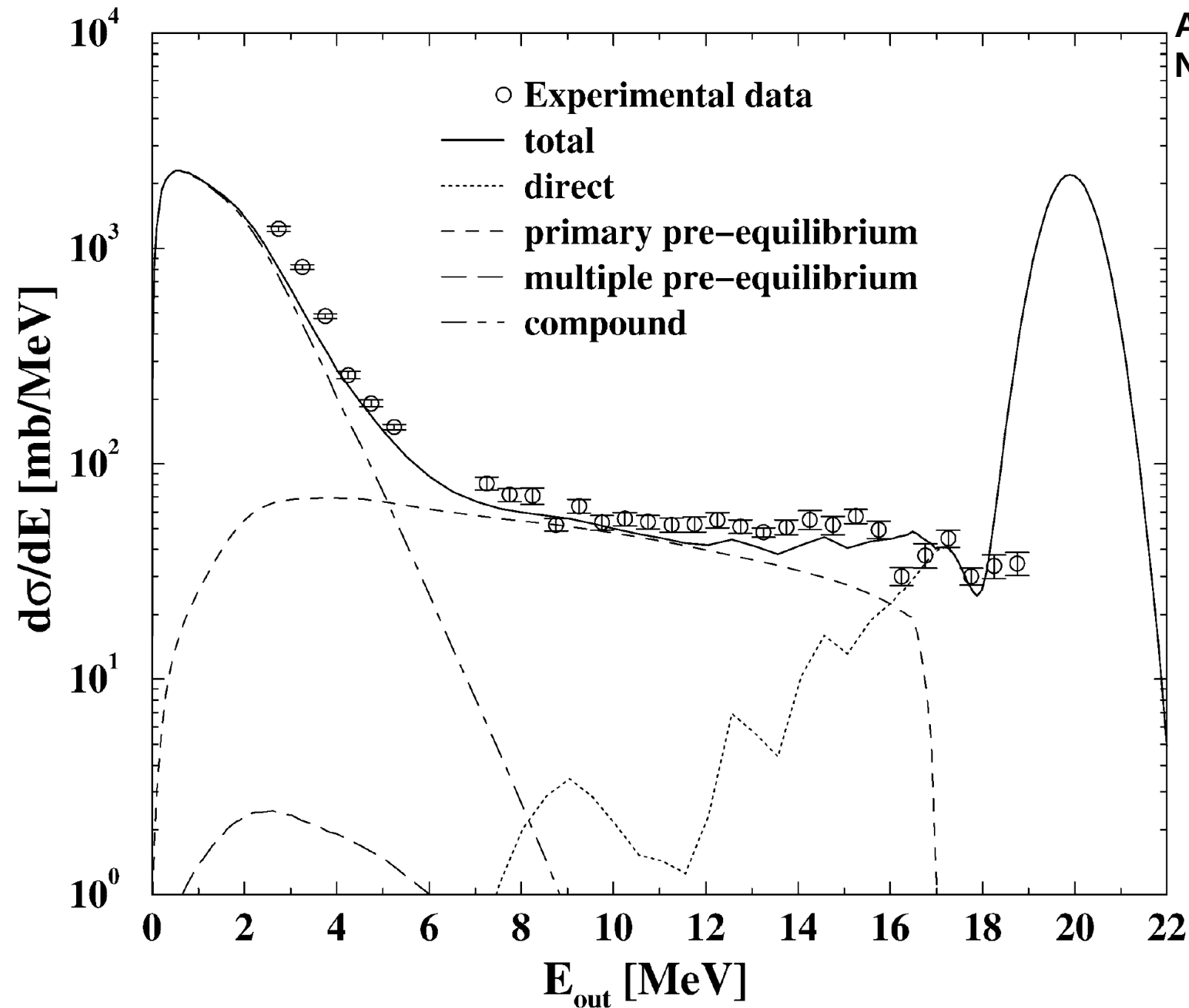
$$\frac{dP(n, t)}{dt} = P(n-2, t) \cdot \lambda^{+}(n-2, E) + P(n+2, t) \lambda^{-}(n+2, E) - P(n, t) [\lambda^{+}(n+2, E) + \lambda^{-}(n-2, E) + L(n, E)]$$

- Ingredients : **M** → matrix element is an adjustable parameter.

$\rho_{n'}$ → model level density for n' particle- n' hole.

- Angular distribution : not modeled, use Kalbach systematics (emperical shape).
- **Pros** : fast calculations – good fit of energy distribution of emitted particles

- **cons** : do not predict angular distribution nor spin transfer,
do not include collective effects – transition direct – pre-equilibrium



**$^{209}\text{Bi}(n, xn)$
spectrum
at 20 MeV.**

**Transition
Direct – Pre-
eq : ad-hoc →
subjective**

**Double-
counting**

Why quantum model ?

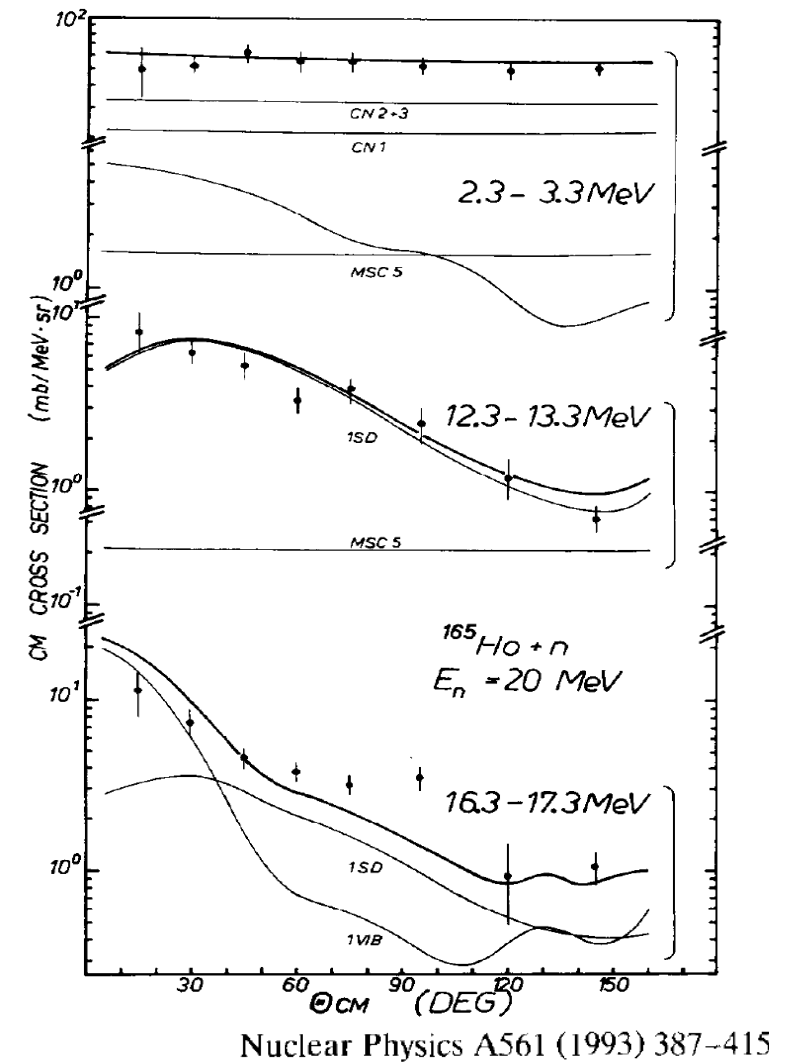
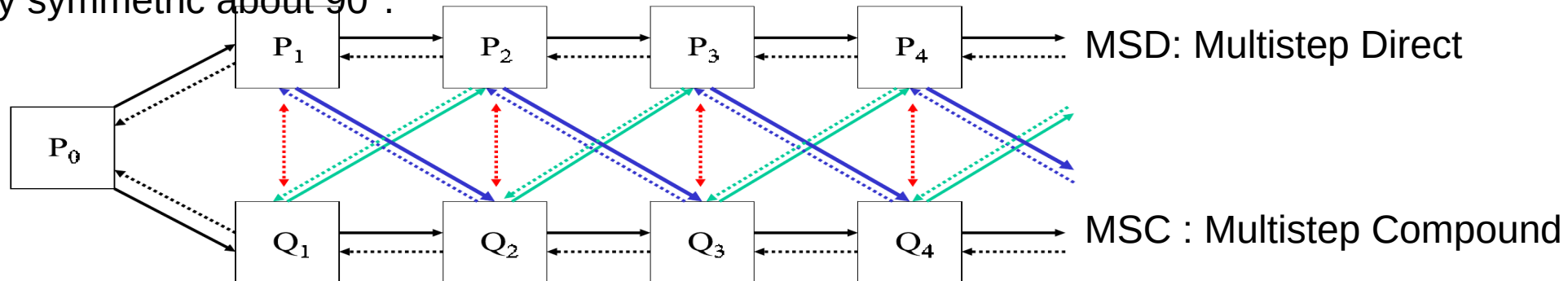
$$T_{f \leftarrow i} = \langle f | V \sum_{n=0}^{\infty} \left(\frac{1}{H - E + i\eta} V \right)^n | i \rangle$$

→ Semi-classical models (such as the exciton model) capture part of the reaction evolution but remain limited in their treatment of nuclear structure.

→ **Coherent effects (collectivity: vibrations/rotations, interference effects)** are intrinsically quantum-mechanical.

→ A quantum framework allows a unified treatment of both incoherent excitations (1p1h, 2p2h, ..) and collective modes.

→ Quantum models separate the spectrum into continuum (P) and bound-state (Q) components, which lead to very different angular distributions: the continuum may be forward-peaked, whereas the bound-state contribution is necessarily symmetric about 90°.



Multi-step Direct Theories

$$T_{f \leftarrow i} = \langle \chi^{(-)}(\mathbf{k}_f), F | V + V G^{(+)} V + V G^{(+)} V G^{(+)} V + \dots | \chi^{(+)}(\mathbf{k}_i), 0 \rangle$$

→ FKK: Feshbach, Kerman, Koonin (1980) On-Shell Approximation for Green's Function + Non-normal matrix elements.

→ TUL: Tamura, Udagawa, Lenske (1982) : Adiabatic Approximation for the Second Step

→ NWY: Nishioka, Weidenmüller, Yoshida (1988) : GOE for residual interaction, Sudden Approximation for the Second Step

H. Feshbach, A. Kerman, S. Koonin, Ann. Phys. (N.Y.) **125** (1980) 429.

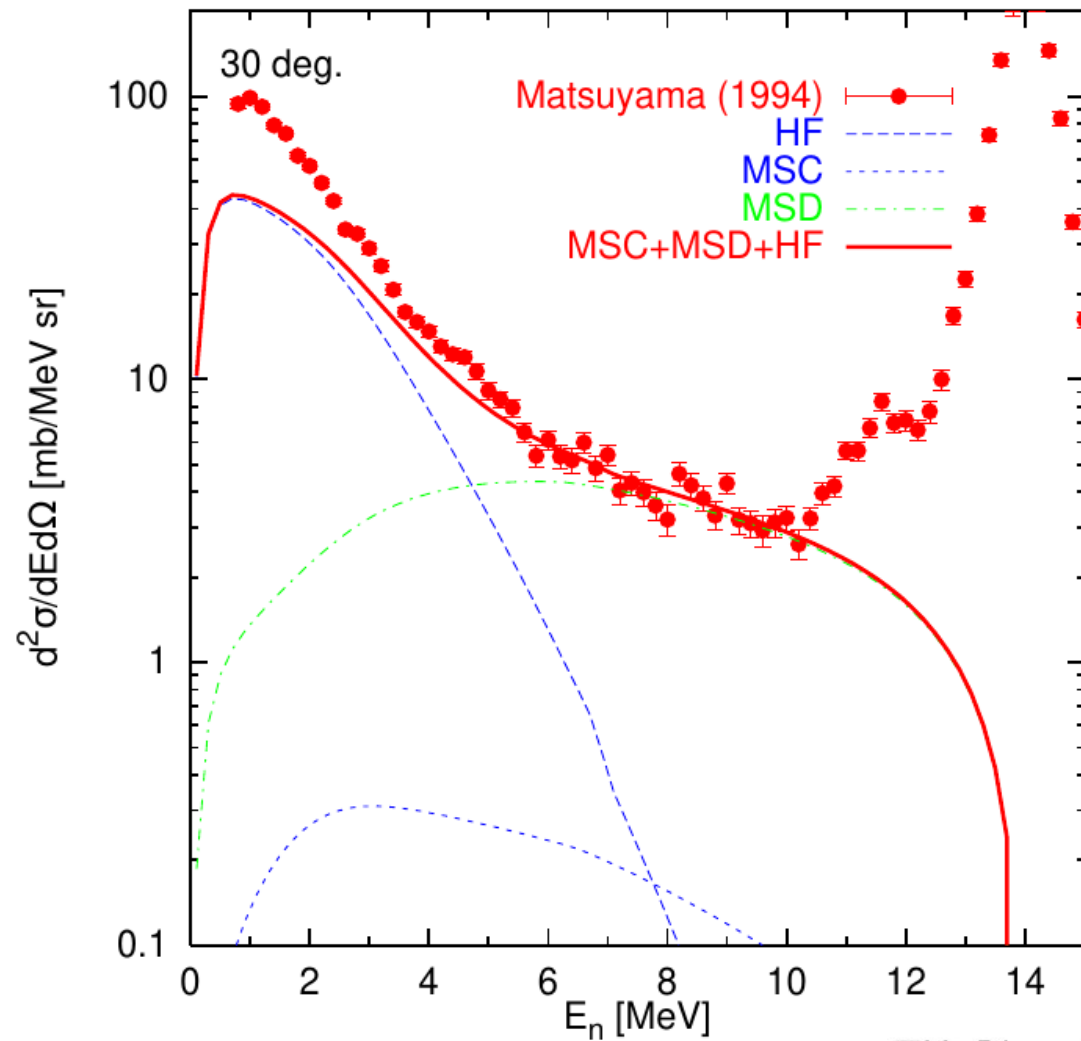
H. Nishioka, H.A. Weidenmüller, S. Yoshida, Ann. Phys. (N.Y.) **183** (1988) 166.

T. Tamura, T. Udagawa, H. Lenske, Phys. Rev. C **26** (1982) 379.

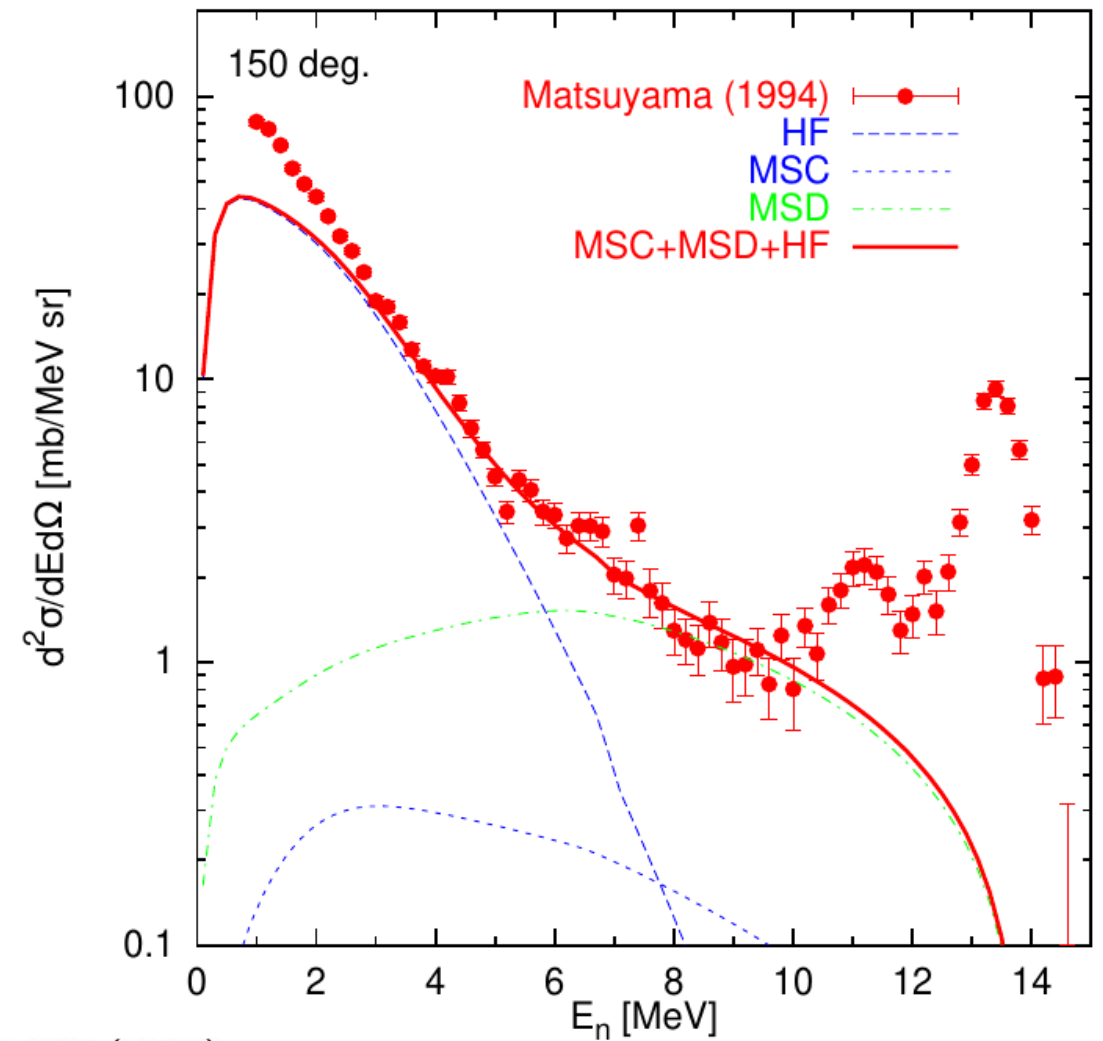
→ One-step process is believed to be dominant below 10-20 MeV

→ The First step expression of FKK, TUL, and NWY is the same ; various implementation : **choice of nuclear structure**

Multistep Direct and Multistep Compound Contribution



TK, Phys. Rev. C, **59**, 865 (1999).

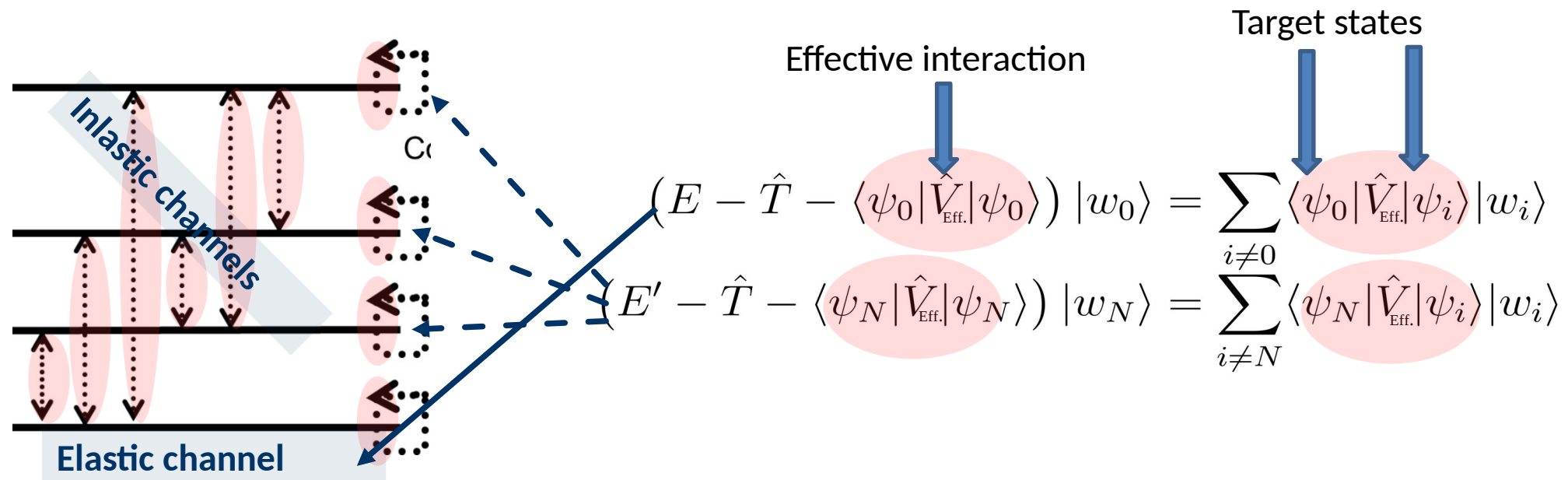


MSD : focus on first step

- Description of direct inelastic scattering and one-step process within the same formalism :
- Effective interaction for projectile – target interactions
- Accurate description of target excitations within a large range of excitation energy.
- Pros:
 - No ad-hoc transition direct – pre-eq, no double-counting
 - predicts angular distribution
 - predicts spin transfer,
 - includes collective effects

One microscopic approach to direct inelastic scattering

Folding potentials derived from nuclear-matter interaction : **very successful for medium mass to heavy nuclei, nucleon and ion scattering.**



Inelastic scattering to discrete levels

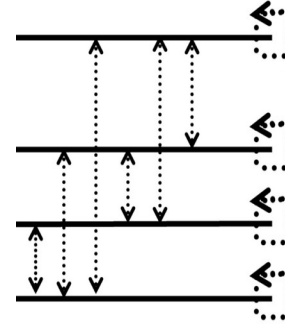
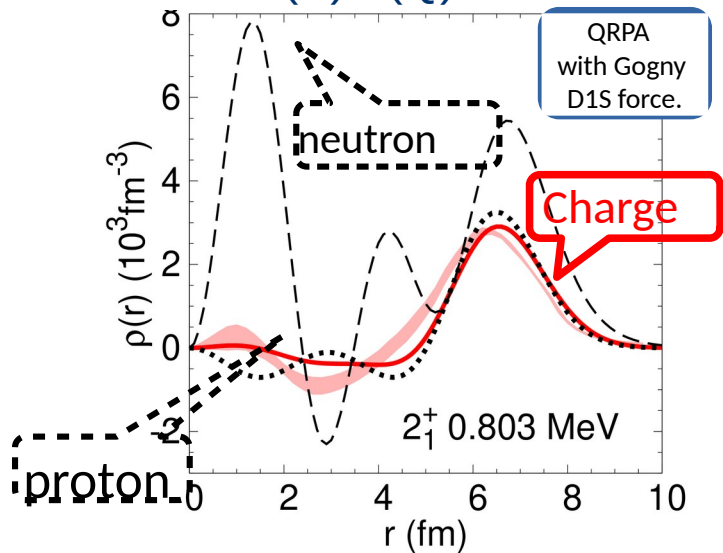
$$U_T(r, E, t_i, t_r) = (t \sqrt{\pi})^{-3} \int \left[\text{Re}[V_T(\rho_p(r_t), \rho_n(r_t), E, V_c(r_t))] e^{-|\vec{r}-\vec{r}_t|^2/t_r^2} + \text{Im}[V_T(\rho_p(r_t), \rho_n(r_t), E, V_c(r_t))] e^{-|\vec{r}-\vec{r}_t|^2/t_i^2} \right] \rho_T d^3 \vec{r}_t$$

Nuclear optical/transition potentials

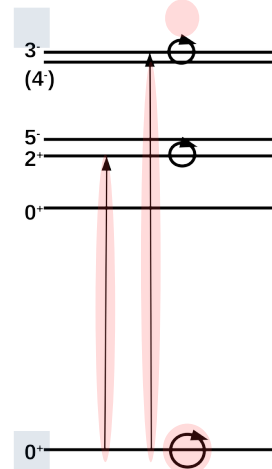
+ Rearrangement

$$\rho_{T=0/1} = \rho_n \pm \rho_p$$

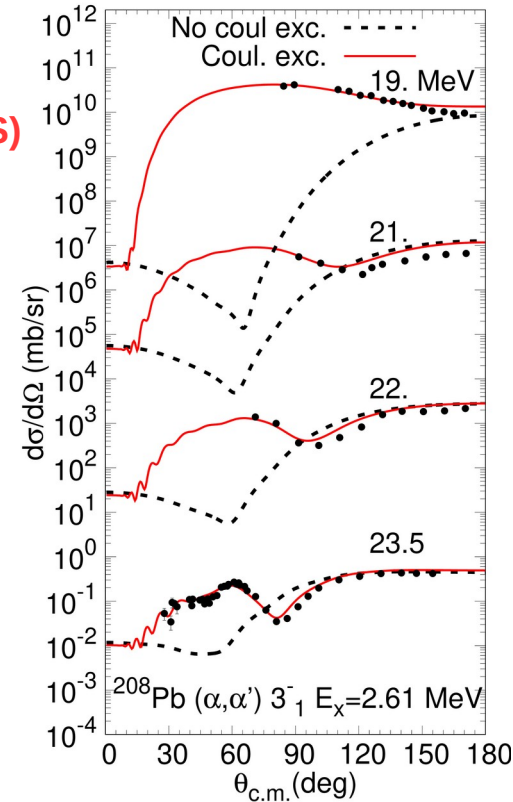
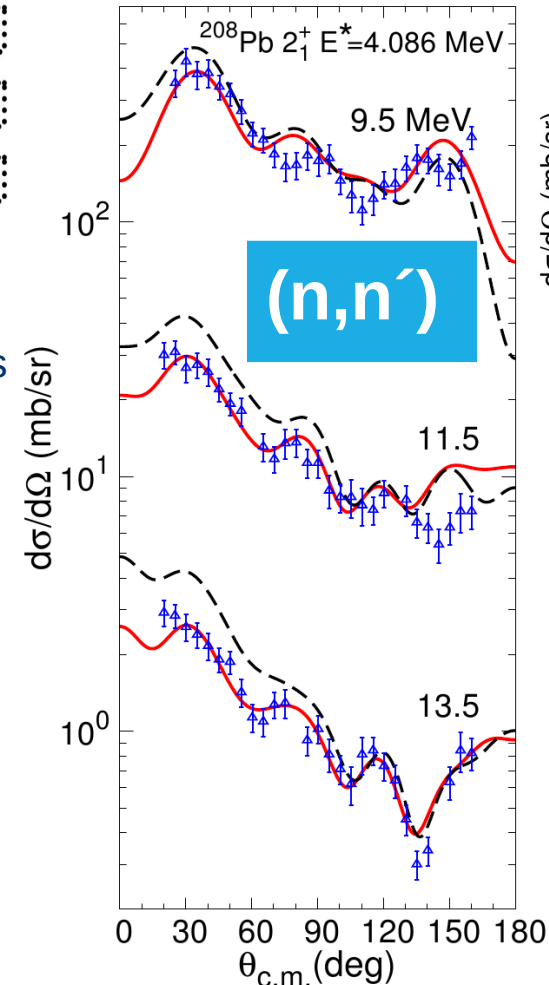
HF(B) / (Q)RPA densities



DWBA:
spherical,
vibrational nucleus



JLM + (Q)RPA-Gogny-D1S



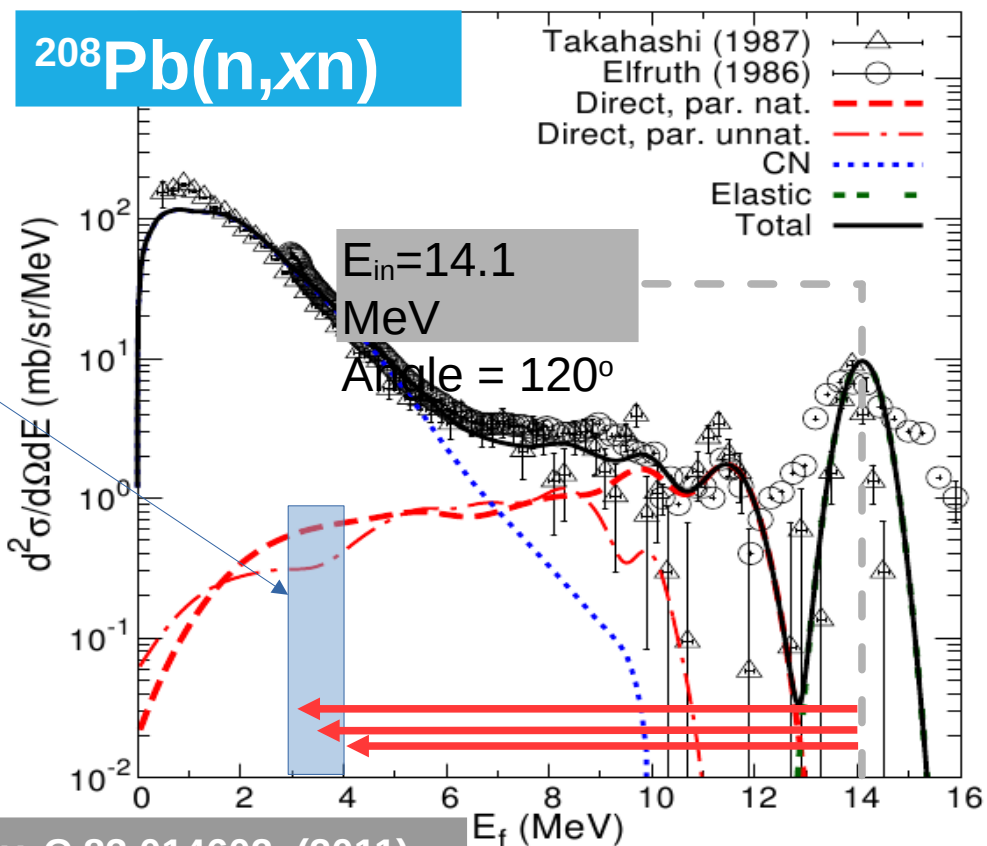
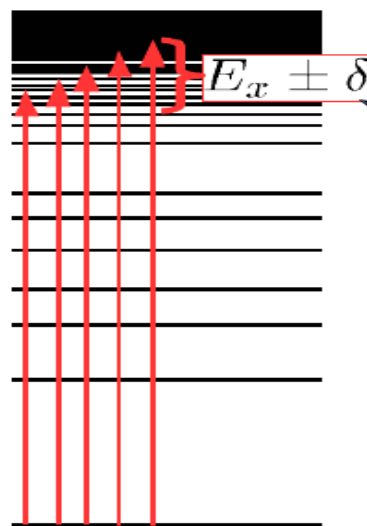
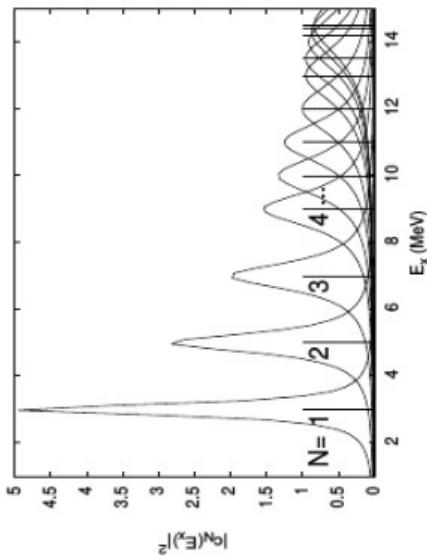
(α, α')
Double
folding

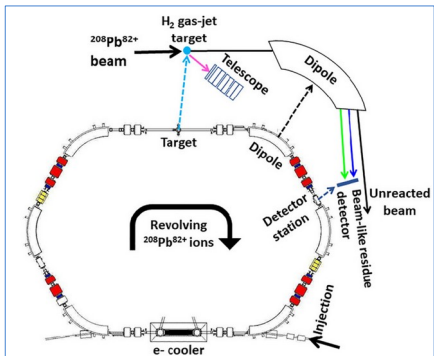
Inelastic to the continuum

Pre-equilibrium emission $E_{in} < 20$ MeV: one-step direct

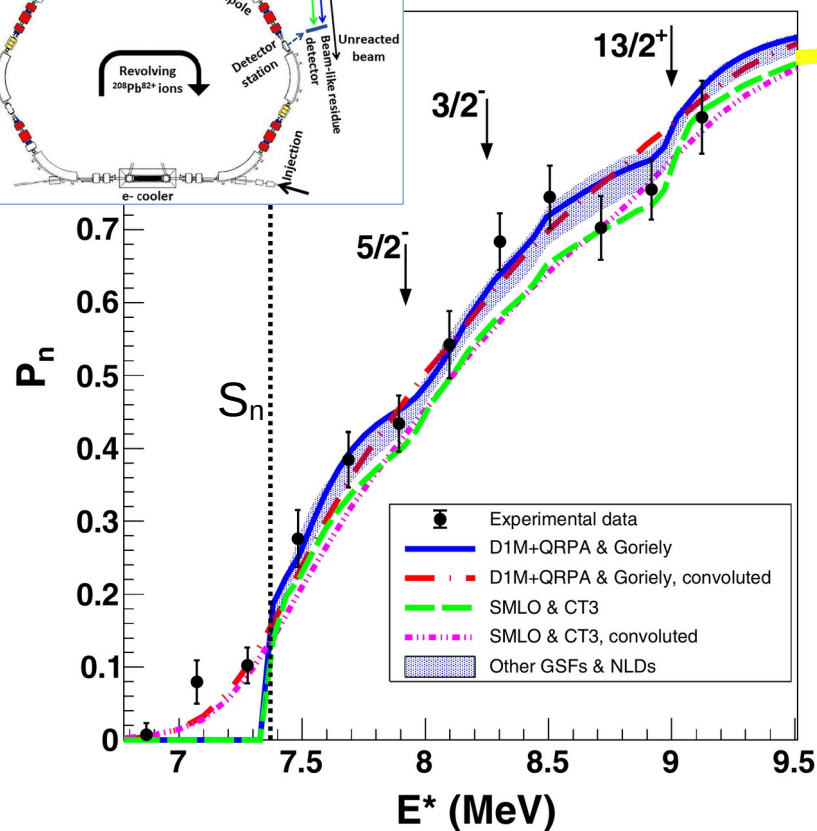
$$\frac{d\sigma(\mathbf{k}_i, \mathbf{k}_f)}{d\Omega dE_f} \sim \frac{1}{2\delta} \int_{E_f-\delta}^{E_f+\delta} dE \sum_N \frac{\Gamma_N}{2} \frac{1}{(E_i - E - E_N)^2 + \frac{\Gamma_N^2}{4}} \left| \langle \chi_{\mathbf{k}}^-, N^{RPA} | V | \chi_{\mathbf{k}_i}^+, \tilde{0} \rangle \right|^2$$

Target excited states : RPA one-phonon + damping widths

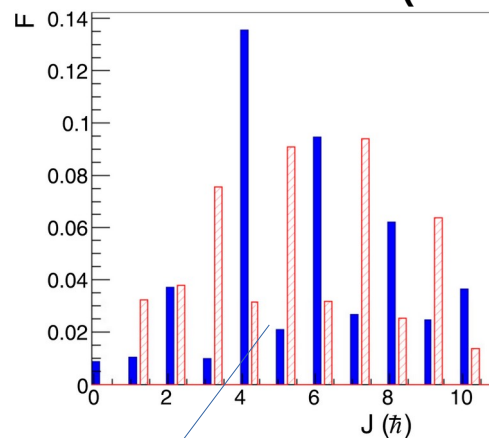




Surrogate studies: $^{208}\text{Pb}(p,p') \leftrightarrow ^{207}\text{Pb}(n,\gamma)$



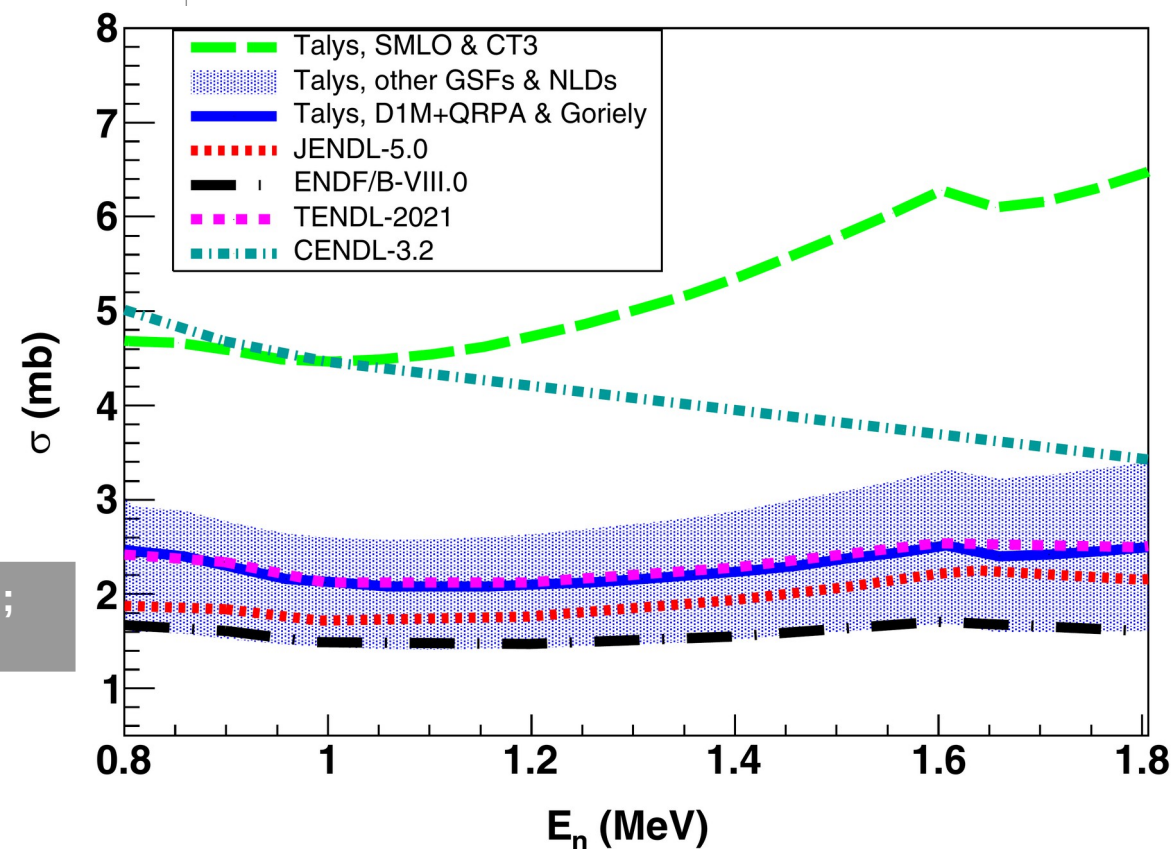
Spin distribution in $^{208}\text{Pb}^*$
 JLMB / RPA-D1S (Nat. Par.)
 Melbourne/KD (Unnat. Par.)



Details later on

$$P_{\chi}(E^*) = \sum_{J^{\pi}} F(E^*, J^{\pi}) \cdot G_{\chi}(E^*, J^{\pi}) \text{ TALYS}$$

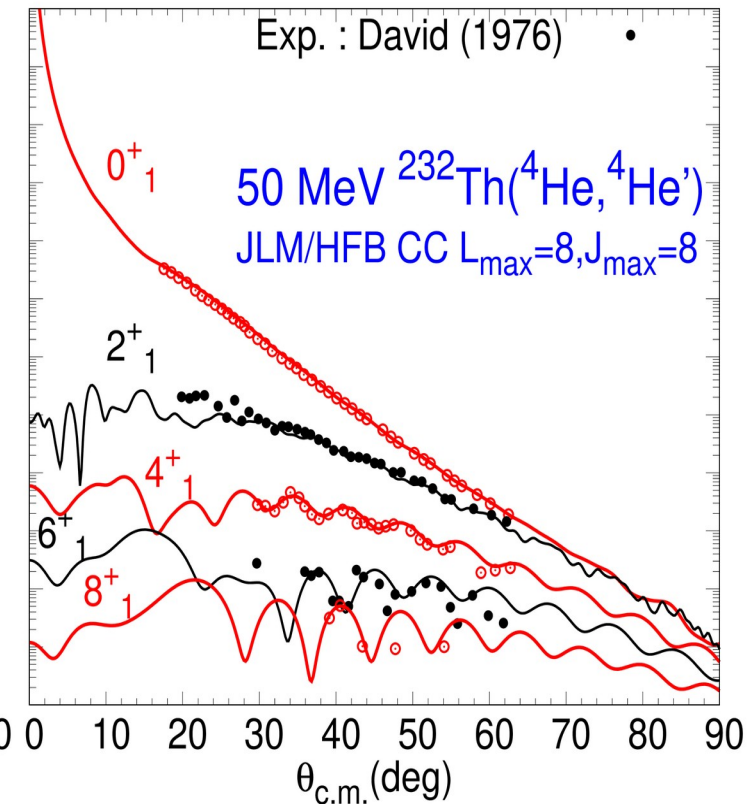
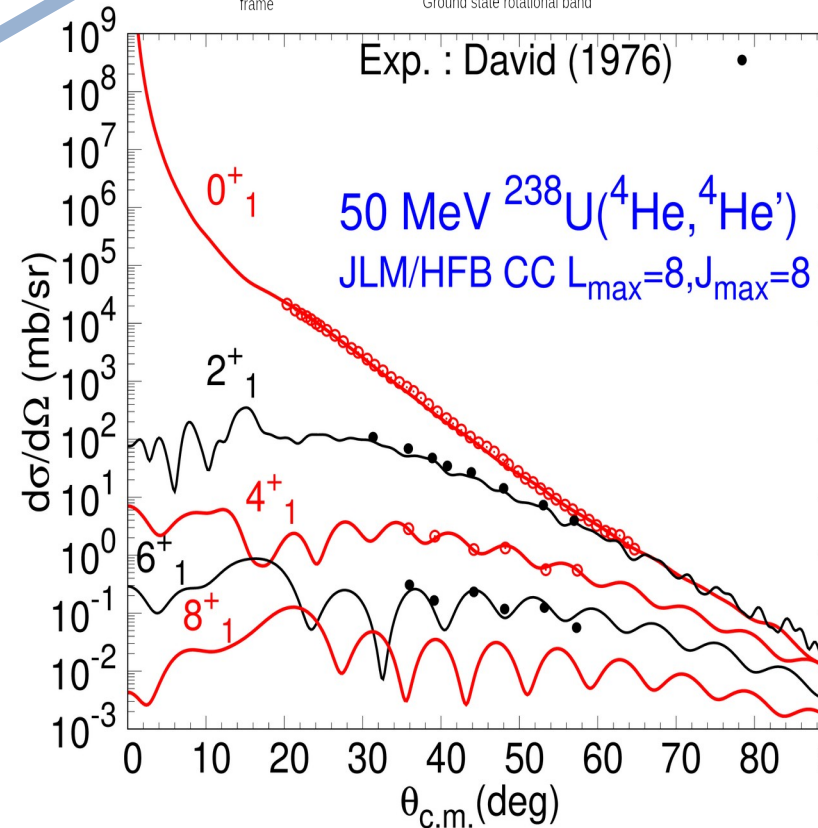
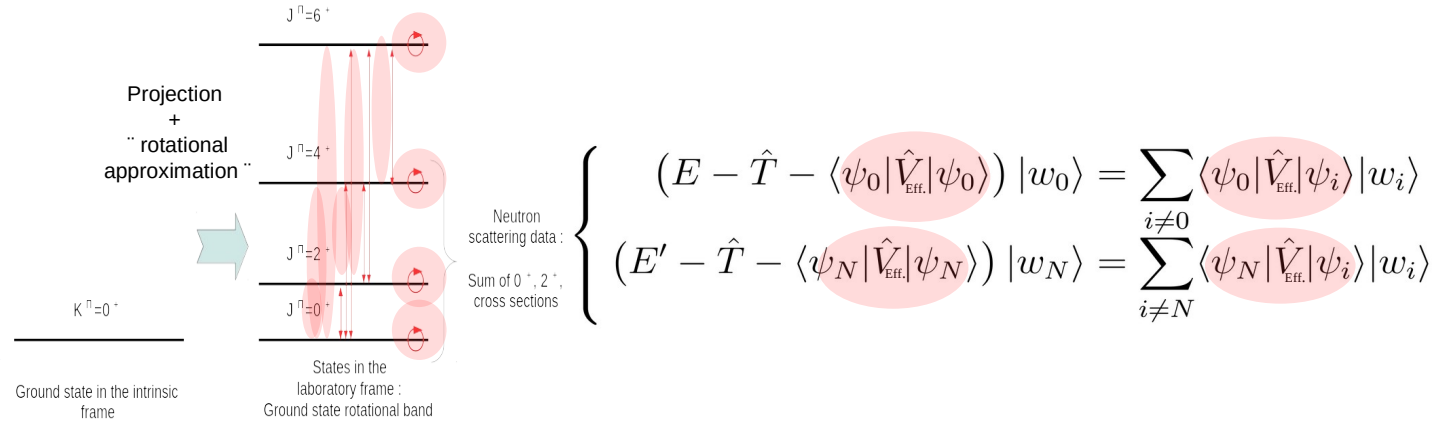
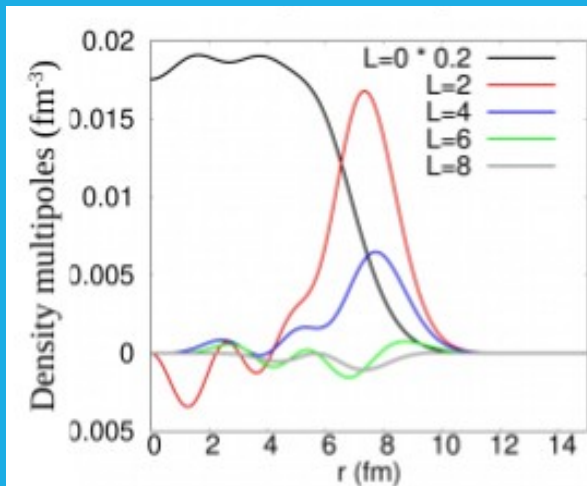
$$\sigma^A_{n,\chi}(E^*) = \sigma^{A+1}_{CN}(E^*) \sum_{J^{\pi}} S(E^*, J^{\pi}) \cdot G_{\chi}(E^*, J^{\pi})$$



S. Sguazzin, B. Jurado et al., Phys. Rev. Lett. 134, 072501 (2025) ;
 Phys. Rev. C 111 024614 (2025)

Deformed targets

Nuclear structure
input :HFB-Gogny D1S
deformed axial densities



JLM deformed with state of the art NR and NS codes

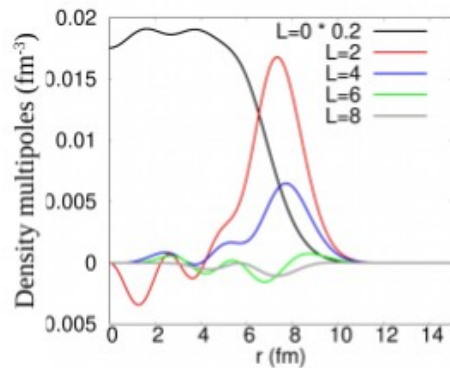
→ TALYS 1.97

→ HFB3 1.0



HFB solver, N. Dubray, et al.

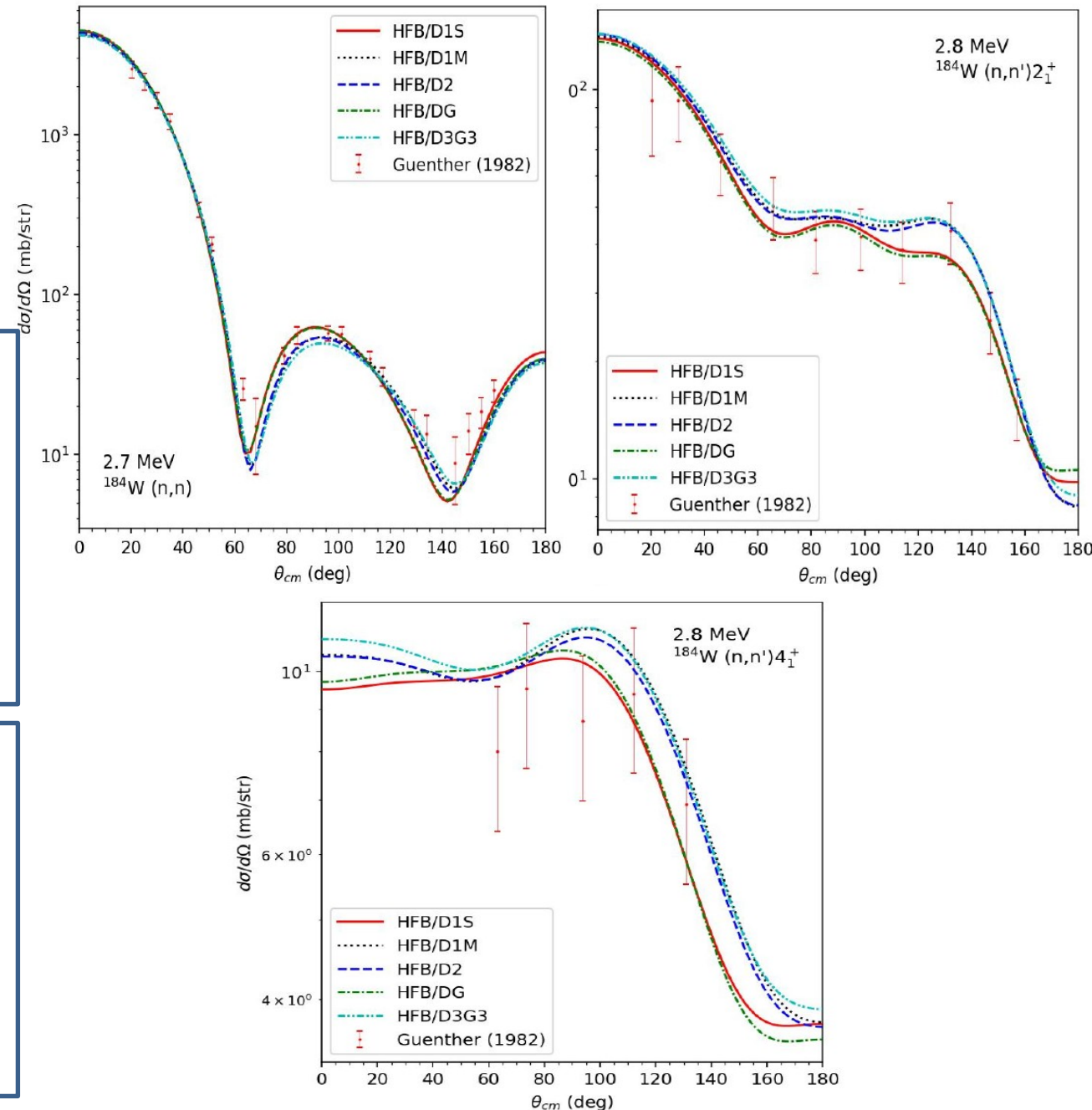
→ to built nuclear structure database for various Gogny forces : D1S, D1M, D2, DG ...



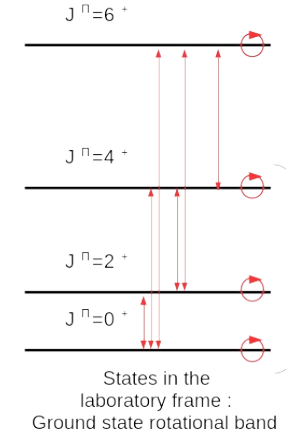
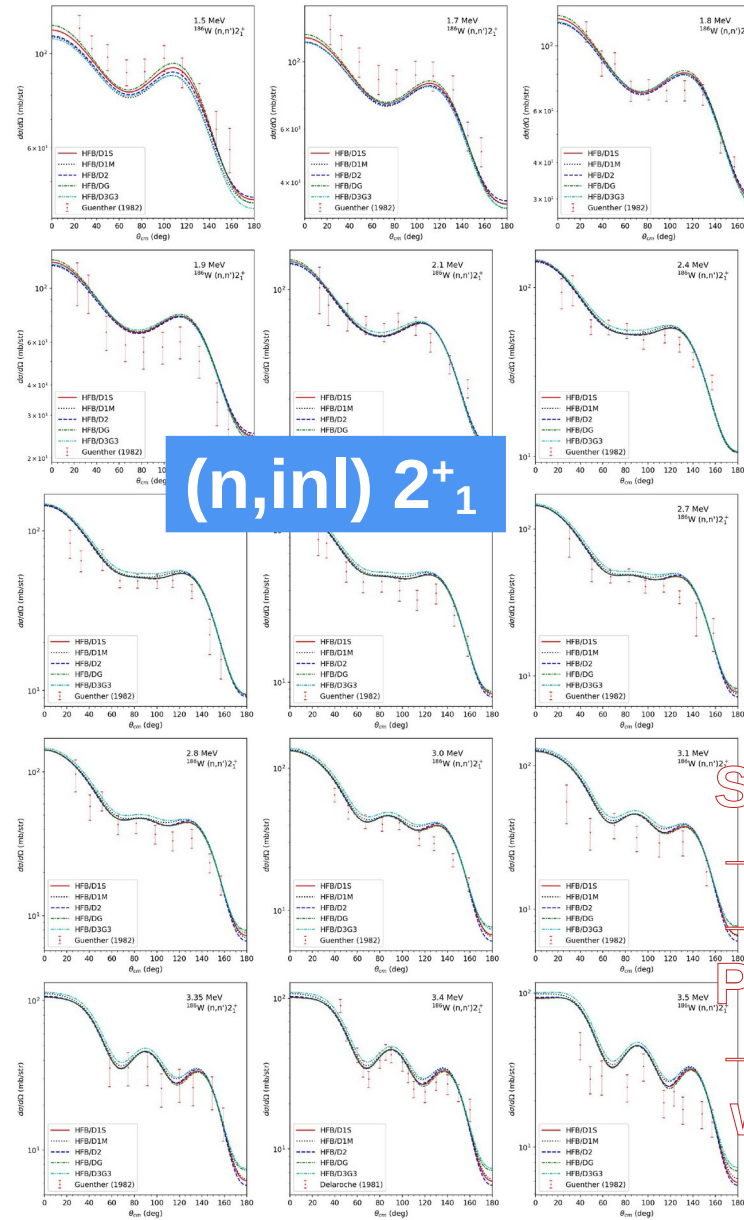
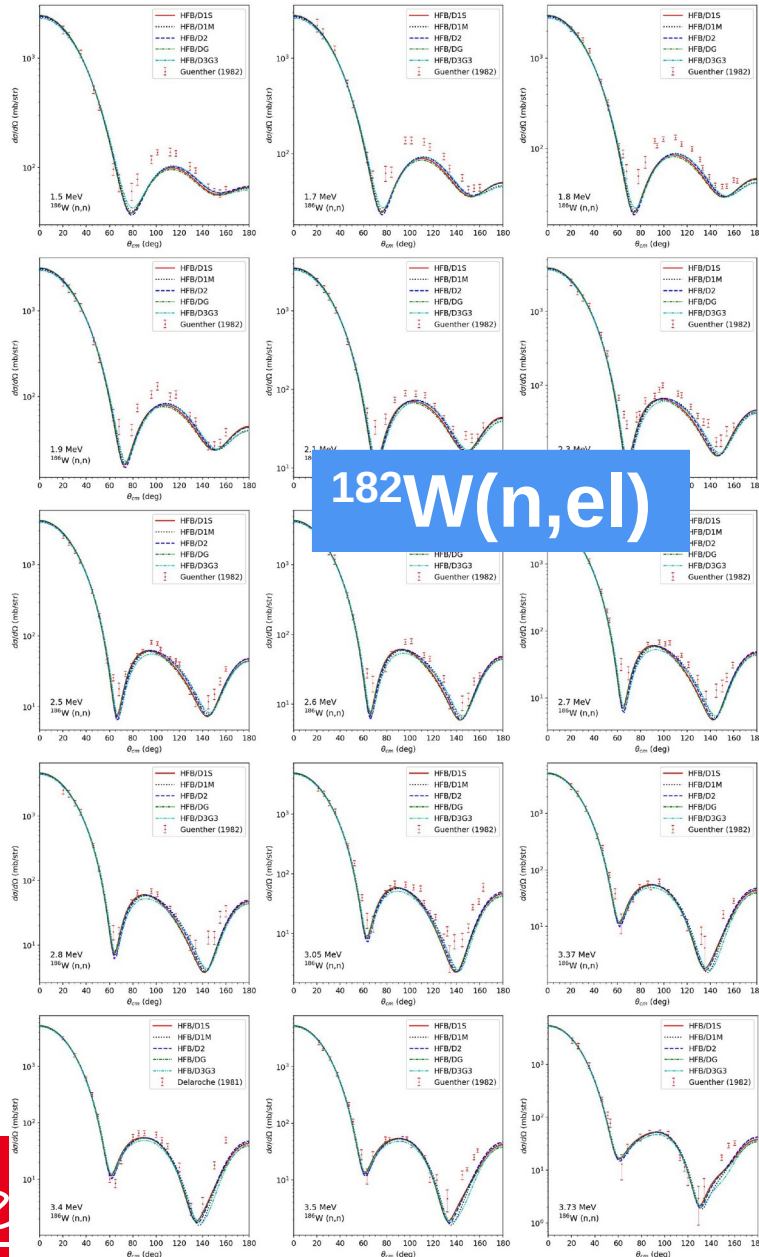
Local CEA Talys-1.97 :

→ include latest developpement (EWT, pre-eq micro ...)

→ Now microscopic deformed JLM model for incident channel and CN decay.



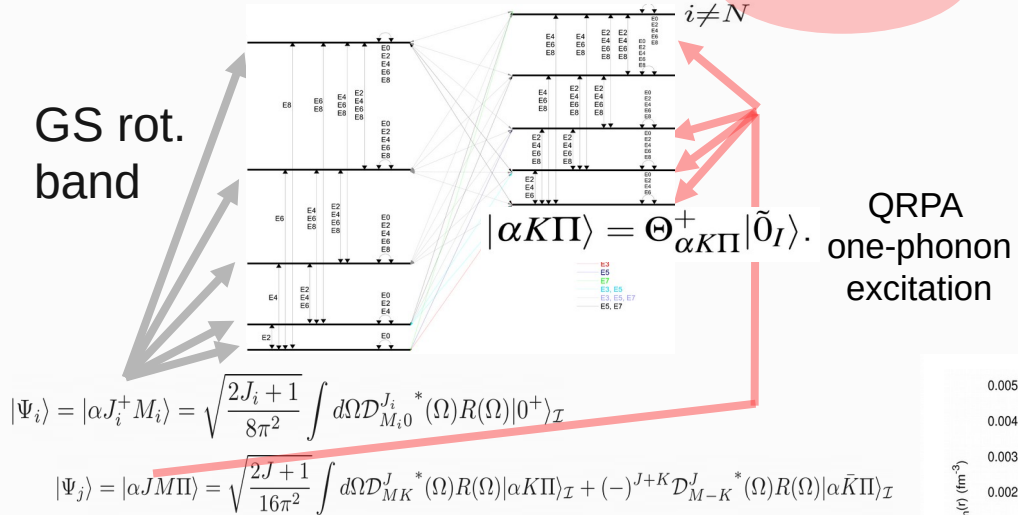
Systematic study of neutron cross sections for GS band levels for deformed nuclei In progress (actinides, rare earth ..) : ntot, excitation functions, differential cross sections



State of the Art NS Models :

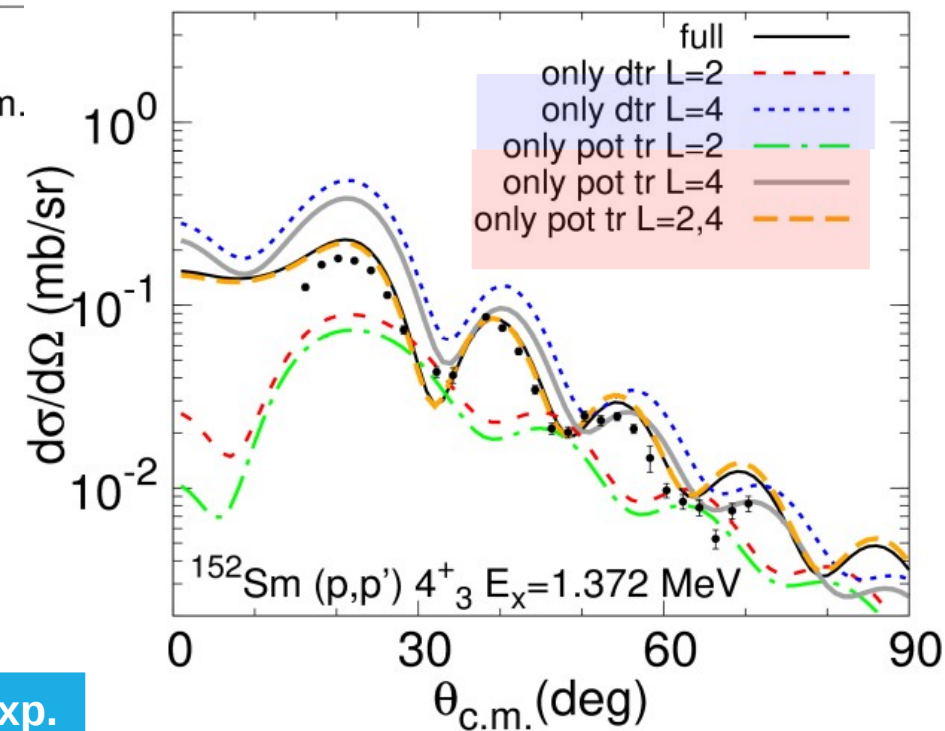
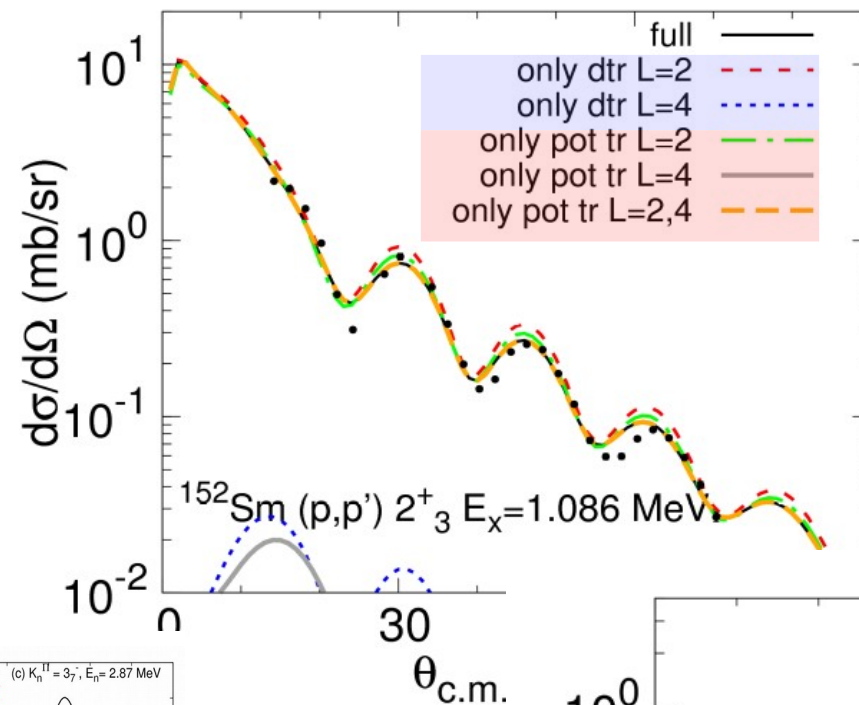
- HFB with new interactions
- Beyond HFB (QRPA, MPMH, PGCM/5DCH ...)
- Prediction for targets/energies with no data :
 - * fission fragments
 - * astrophysics

$$\begin{aligned} (E - \hat{T} - \langle \psi_0 | \hat{V}_{\text{eff.}} | \psi_0 \rangle) |w_0\rangle &= \sum_{i \neq 0} \langle \psi_0 | \hat{V}_{\text{eff.}} | \psi_i \rangle |w_i\rangle \\ (E' - \hat{T} - \langle \psi_N | \hat{V}_{\text{eff.}} | \psi_N \rangle) |w_N\rangle &= \sum_{i \neq N} \langle \psi_N | \hat{V}_{\text{eff.}} | \psi_i \rangle |w_i\rangle \end{aligned}$$

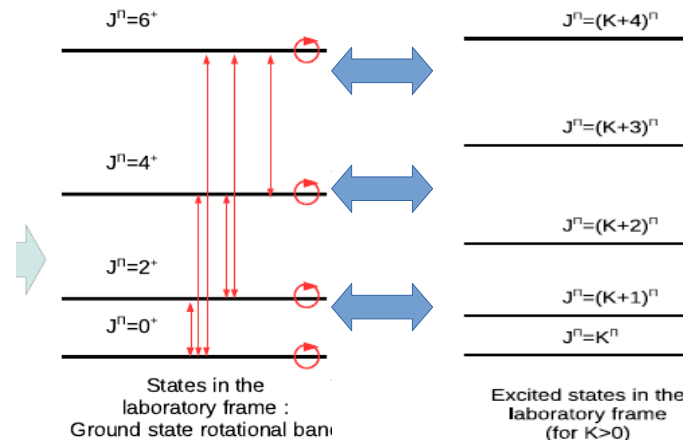


$$U_{L'}^{\tilde{0} \rightarrow K^\Pi}(r_1) = \int Y_K^{L'}(\Omega_1) \left(\int V(|\mathbf{r}_1 - \mathbf{r}_2|, \bar{\rho}) \sum_L \rho_L^{\tilde{0} \rightarrow K^\Pi}(r_2) Y_K^L(\Omega_2) d\mathbf{r}_2 \right) d\Omega_1$$

+ Rear.

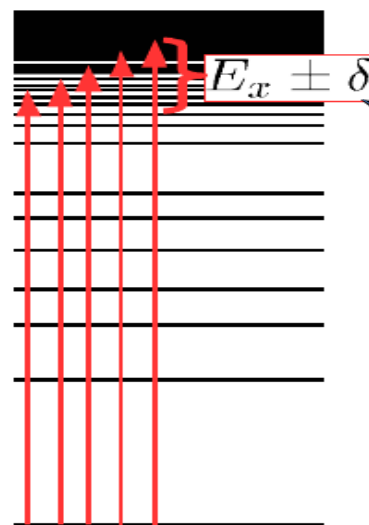
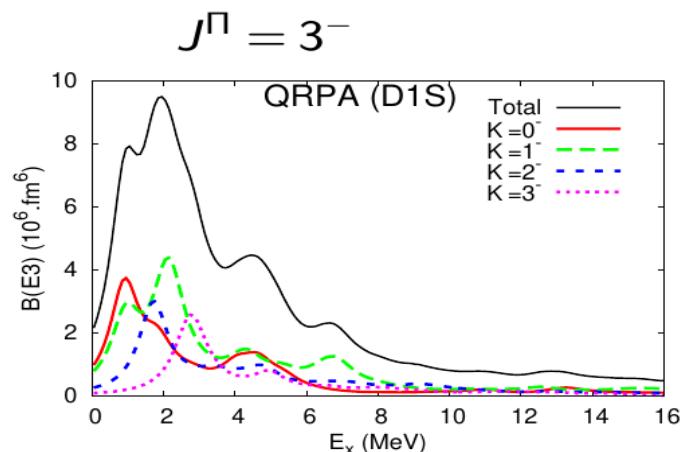


Inelastic to the continuum

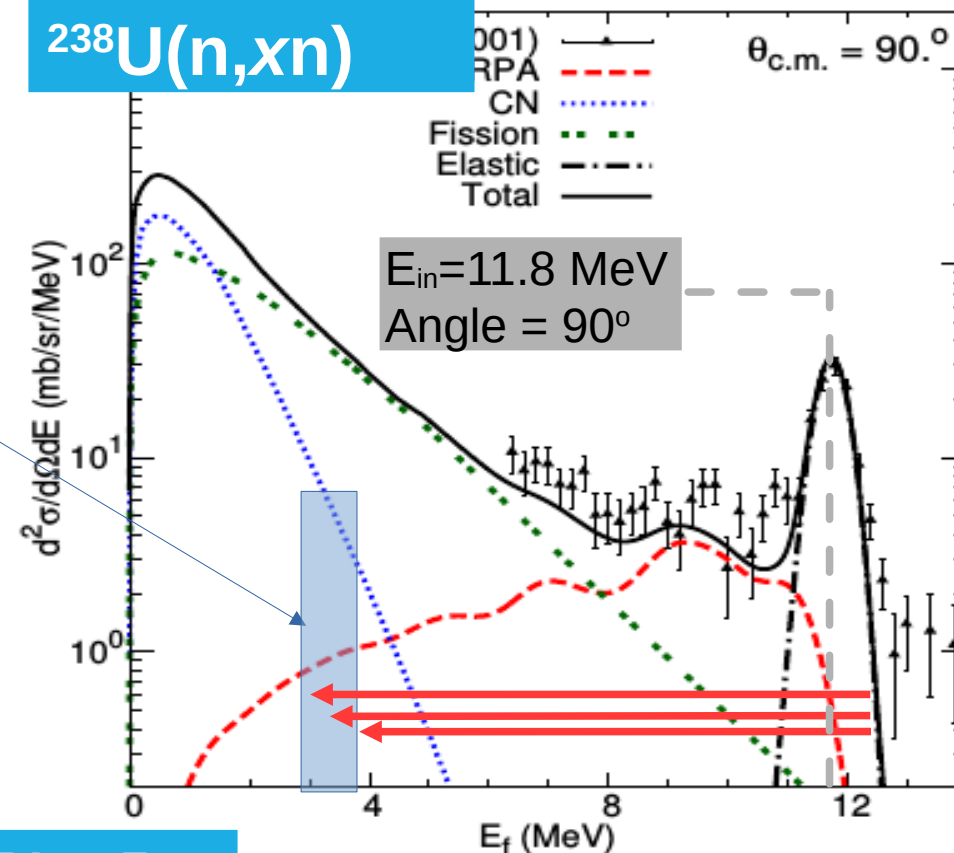


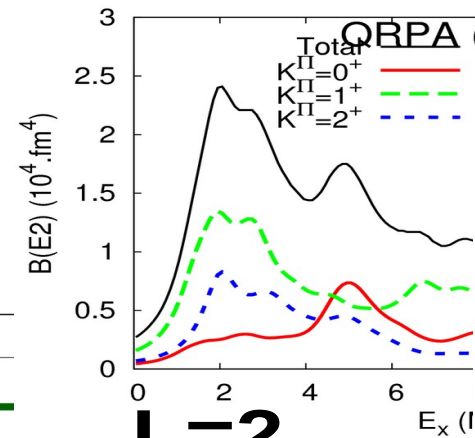
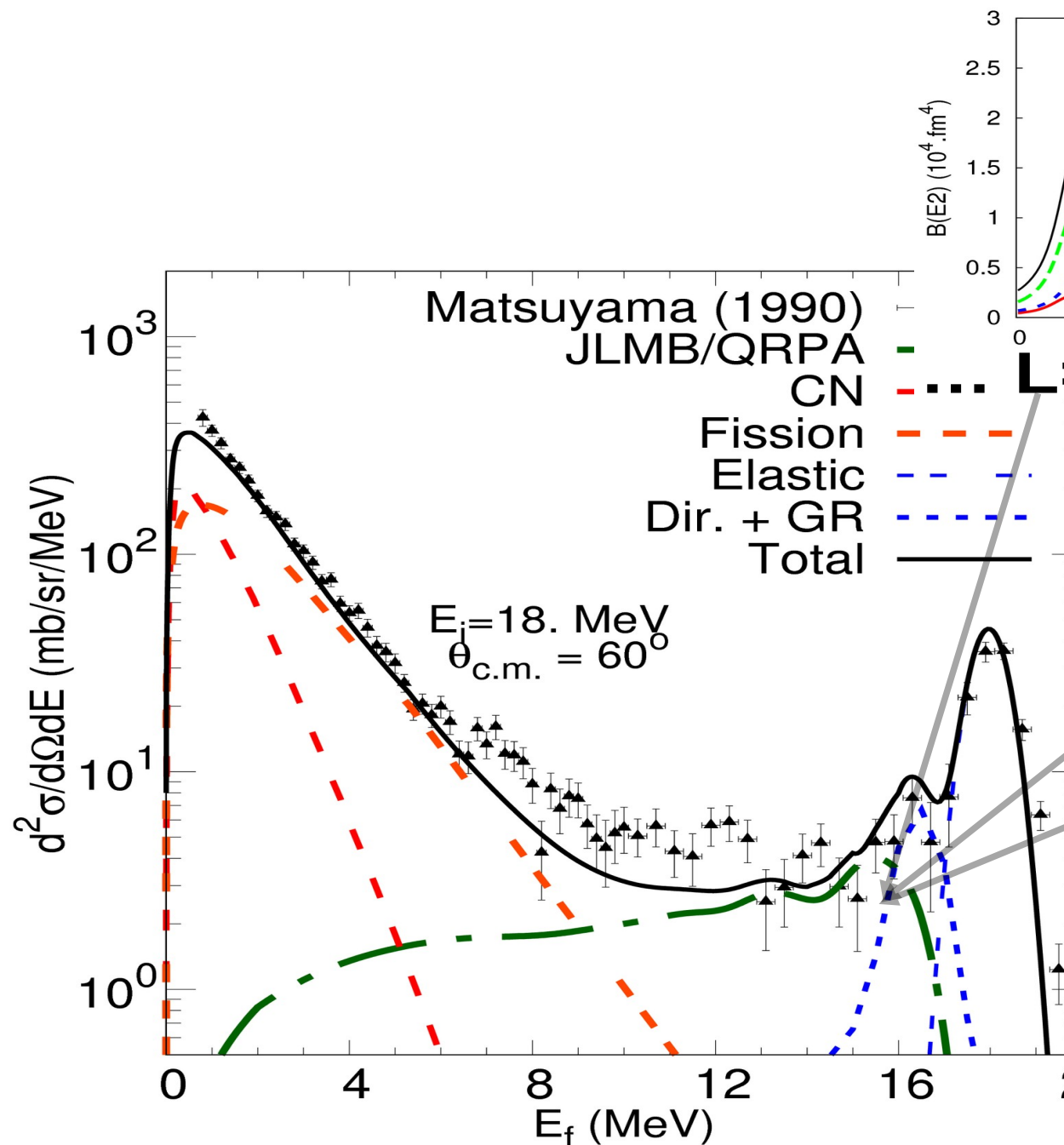
JLM – QRPA
potentials
Coupled channels

Target excited states : QRPA one-phonon + damping width



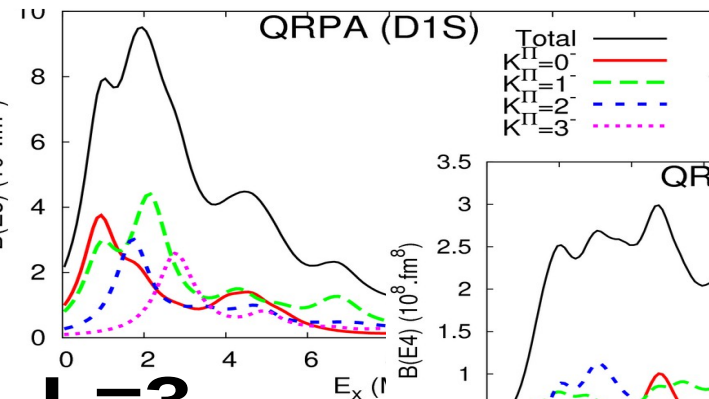
$^{238}\text{U}(n, xn)$



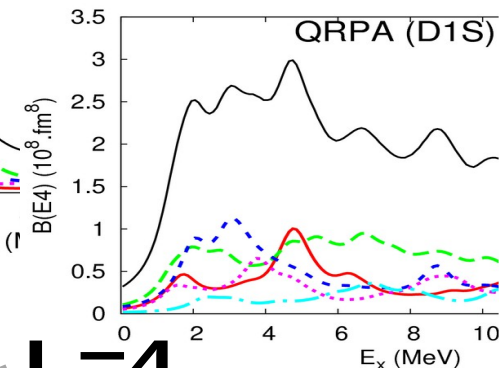


L=2

Transitions with angular momentum transfer L=0-8



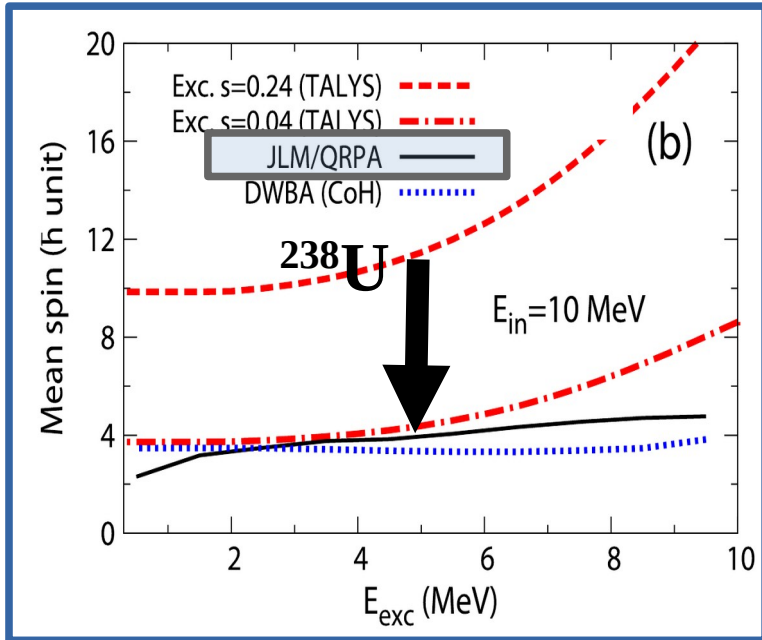
L=3



L=4 ...

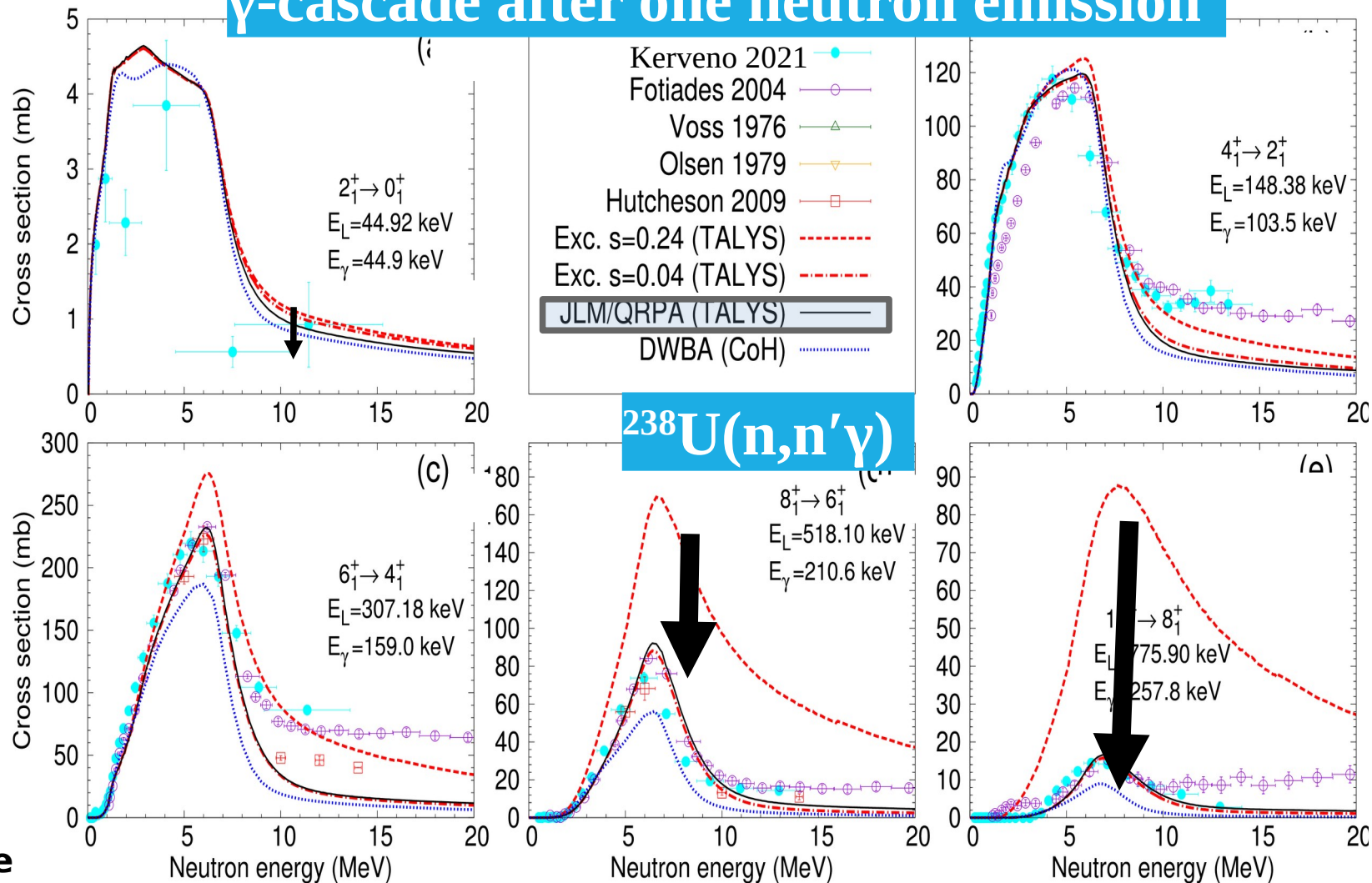
JLMB + QRPA :
collective excitations for $E_x = 1-6 \text{ MeV}$
→ do not need pseudo-states (still used to produce latest nuclear data libraries)
→ equivalent results for medium mass and heavy targets

Spin distribution of residual nucleus



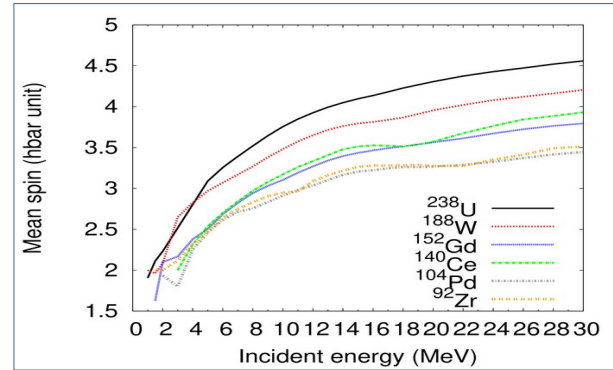
**Population of high spin levels
very sensitive to the mean value
of the spin distribution**

γ -cascade after one neutron emission



Spin distribution of residual nucleus

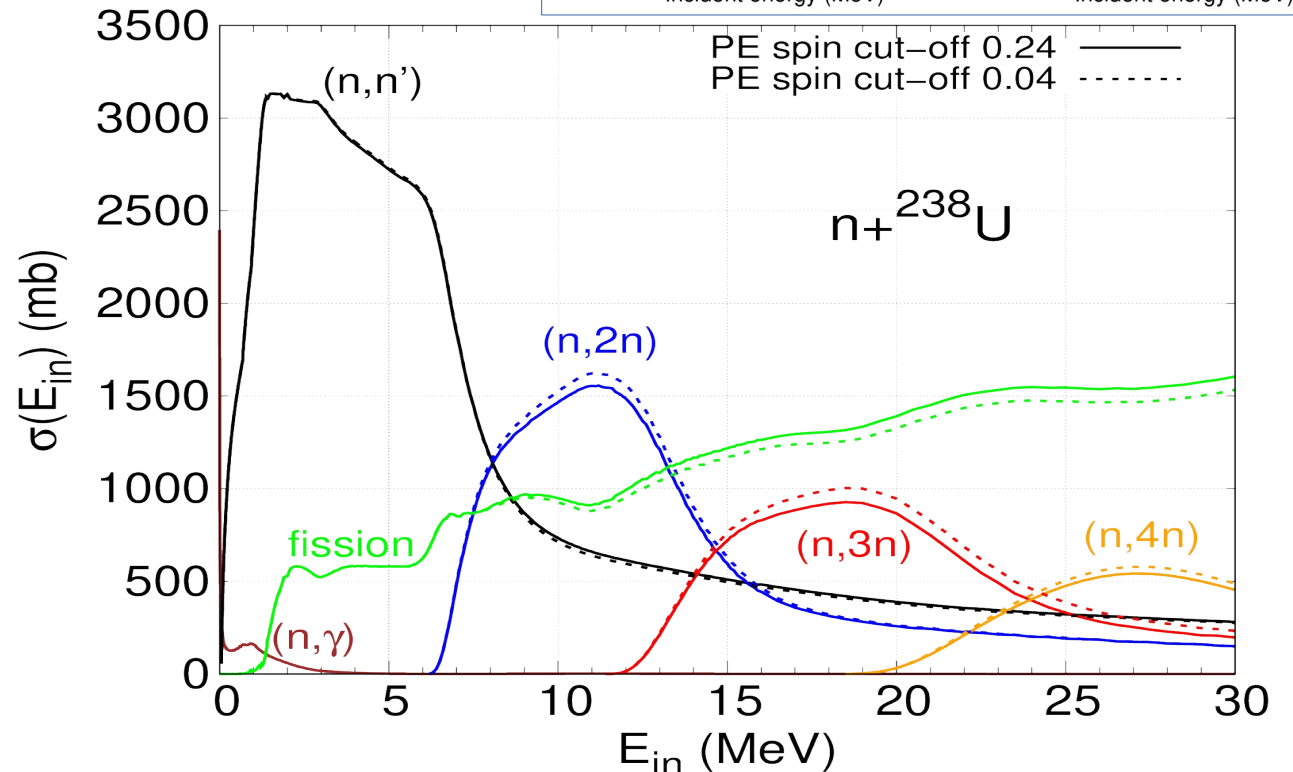
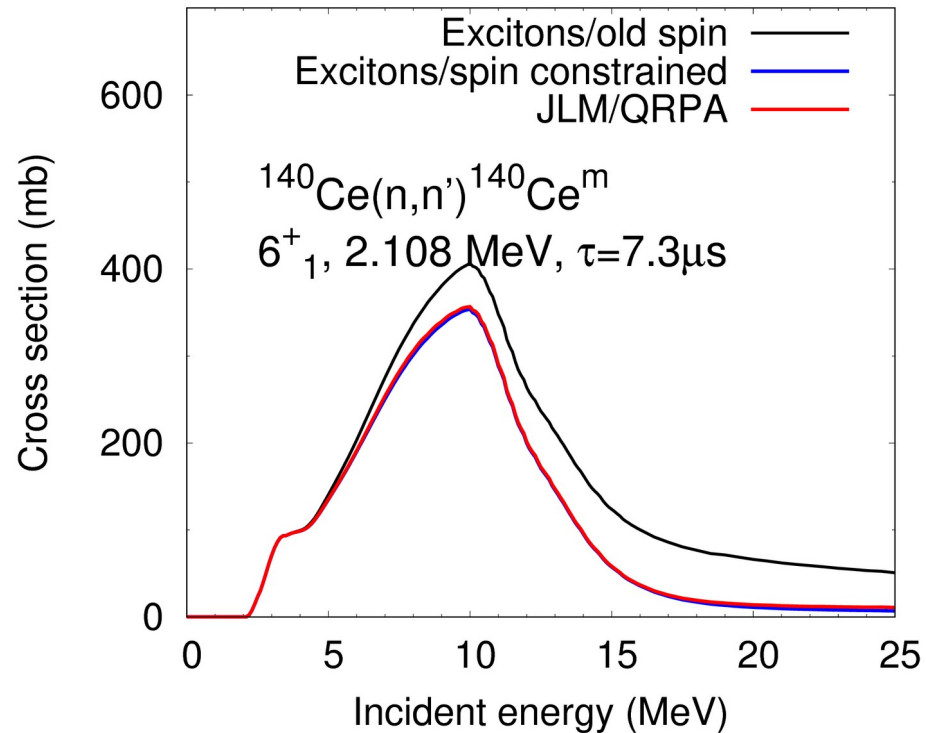
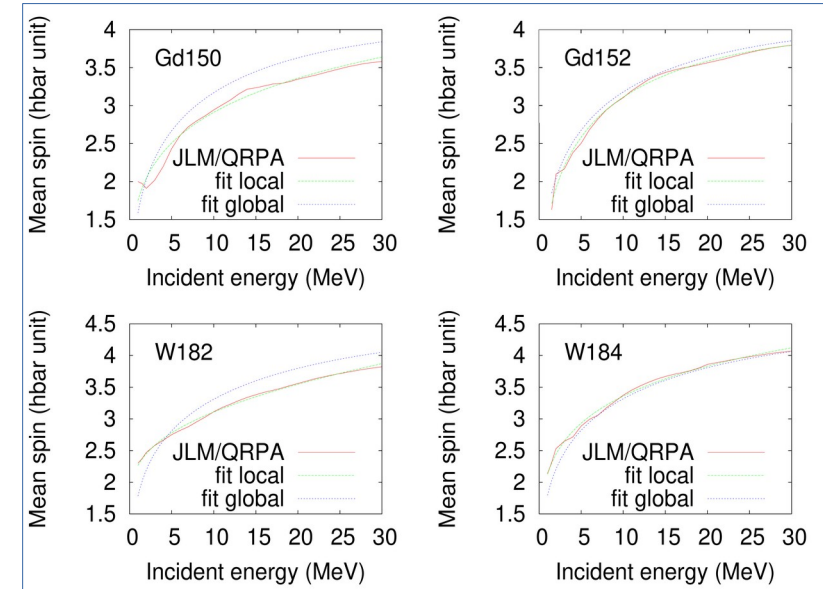
Systematics A=16-240 Constraints to spin-distributions for exciton pre-eq. model **TALYS ≥ 1.97**



$$x(A) = \alpha_x A^{\frac{1}{3}} + \beta_x, \text{ avec } x = a, b, c$$

$$\bar{J} = a(A)E_{in}^{\frac{1}{4}} + b(A)E_{in}^{\frac{3}{4}} + c(A)$$

$$x(A) = \alpha_x A^{\frac{1}{3}} + \beta_x, \text{ avec } x = a, b, c$$



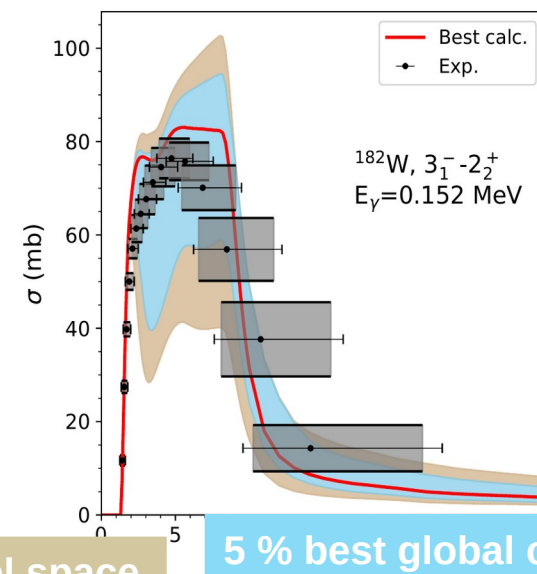
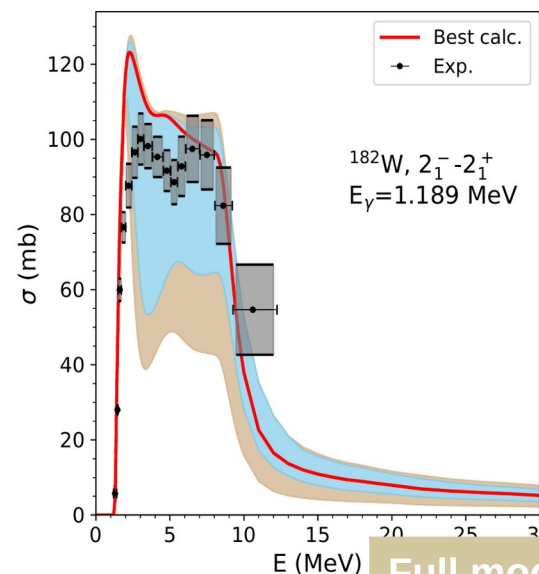
$^{182,184,186}\text{W} (n,n'\gamma) :$ 73 transitions measured G. Henning et al.

Global Modeling of Inelastic Processes Recent progress (implemented in TALYS / CoH)

- ✓ Microscopic inputs: LD, GSF, pre-equilibrium
- ✓ OMP, Engelbrecht–Weidenmüller transformation
- ✓ BR, Discrete levels extended into the continuum

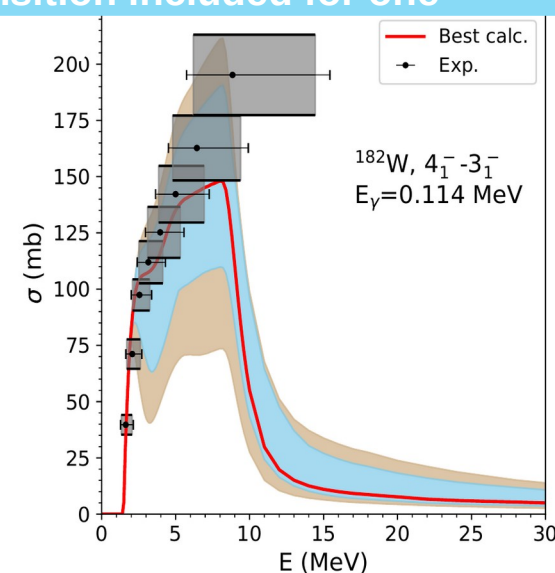
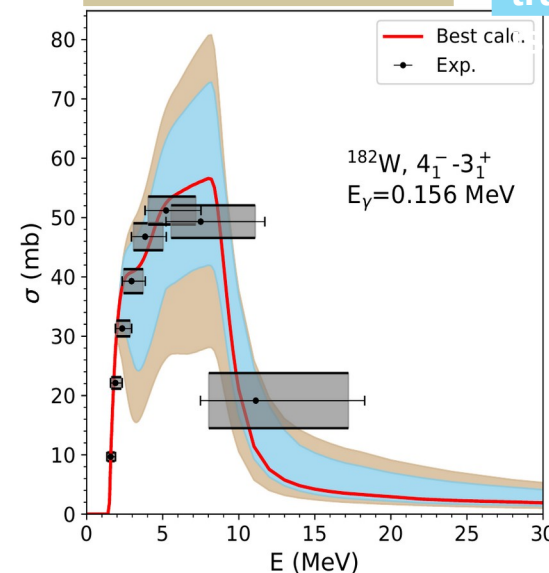
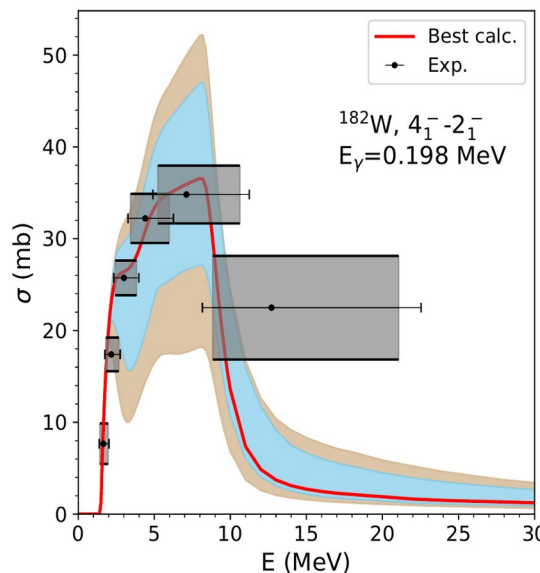
This study confirmed needs

- ✓ Inclusion of low-energy M1 upbend + scissors
- ✓ Reduced spin distributions (PE residual nucleus & LD)
- ✓ Extended discrete-level scheme



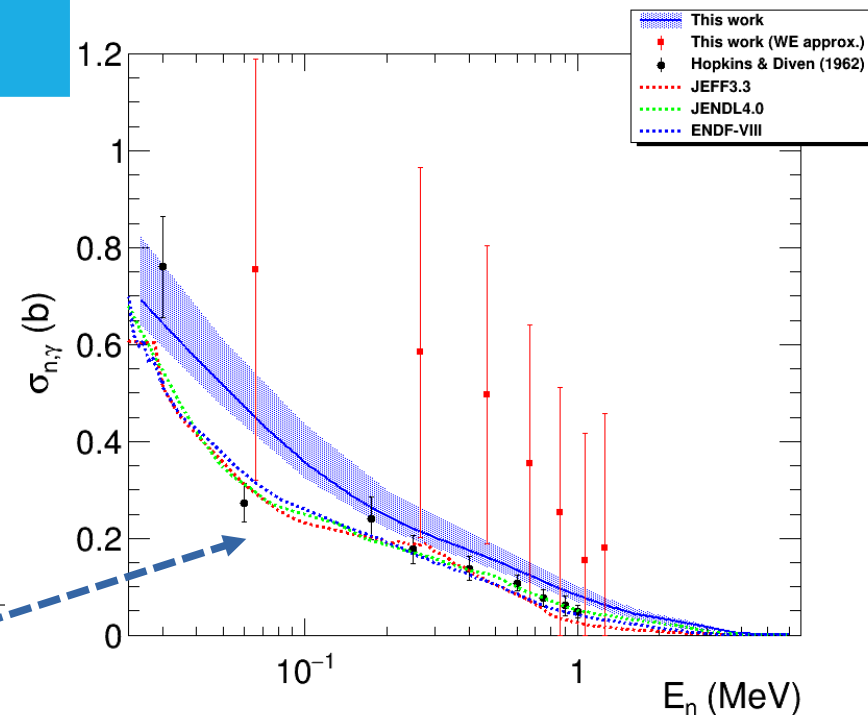
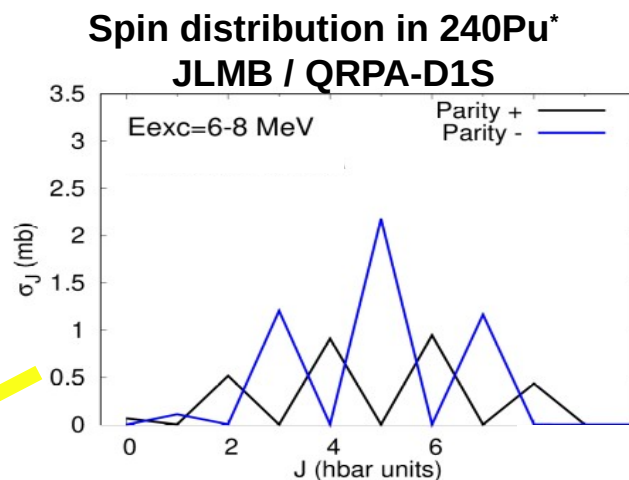
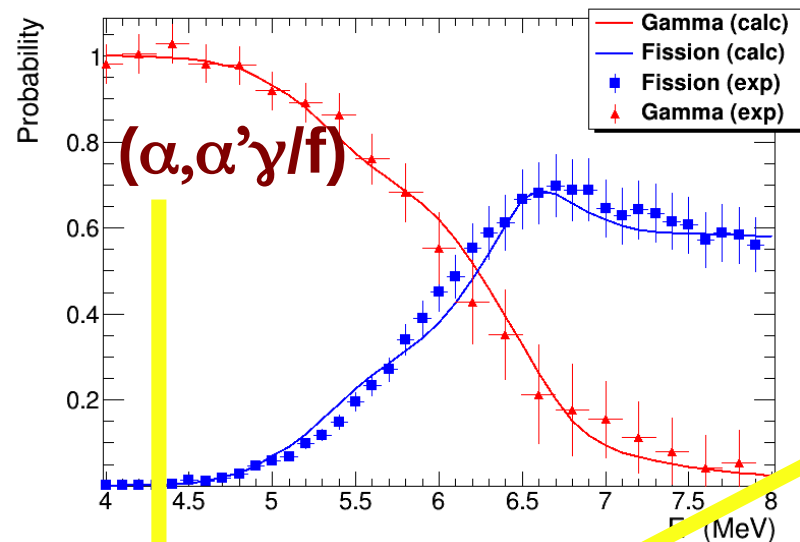
Full model space

5 % best global χ^2 (all transition included for one



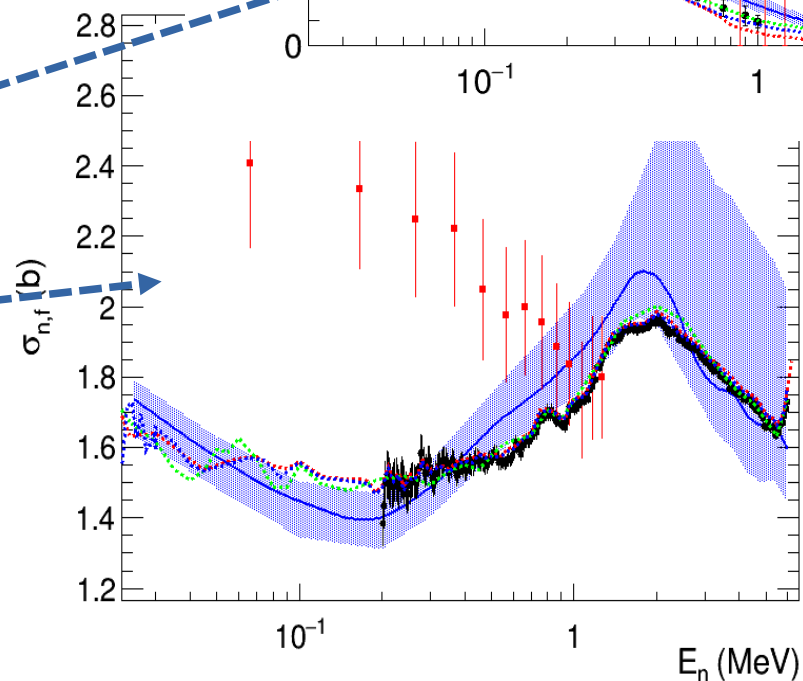
G. Henning et al., to be published in Phys. Rev. C (2026)

Surrogate studies: $^{240}\text{Pu}(\alpha, \alpha') \leftarrow \rightarrow ^{239}\text{Pu}(n, \gamma); (n, f)$



$$P_{\chi}(E^*) = \sum_{J^{\pi}} F(E^*, J^{\pi}) G_{\chi}(E^*, J^{\pi}) \text{ TALYS}$$

$$\sigma_{n,\chi}^A(E^*) = \sigma_{CN}^{A+1}(E^*) \sum_{J^{\pi}} S(E^*, J^{\pi}) G_{\chi}(E^*, J^{\pi})$$



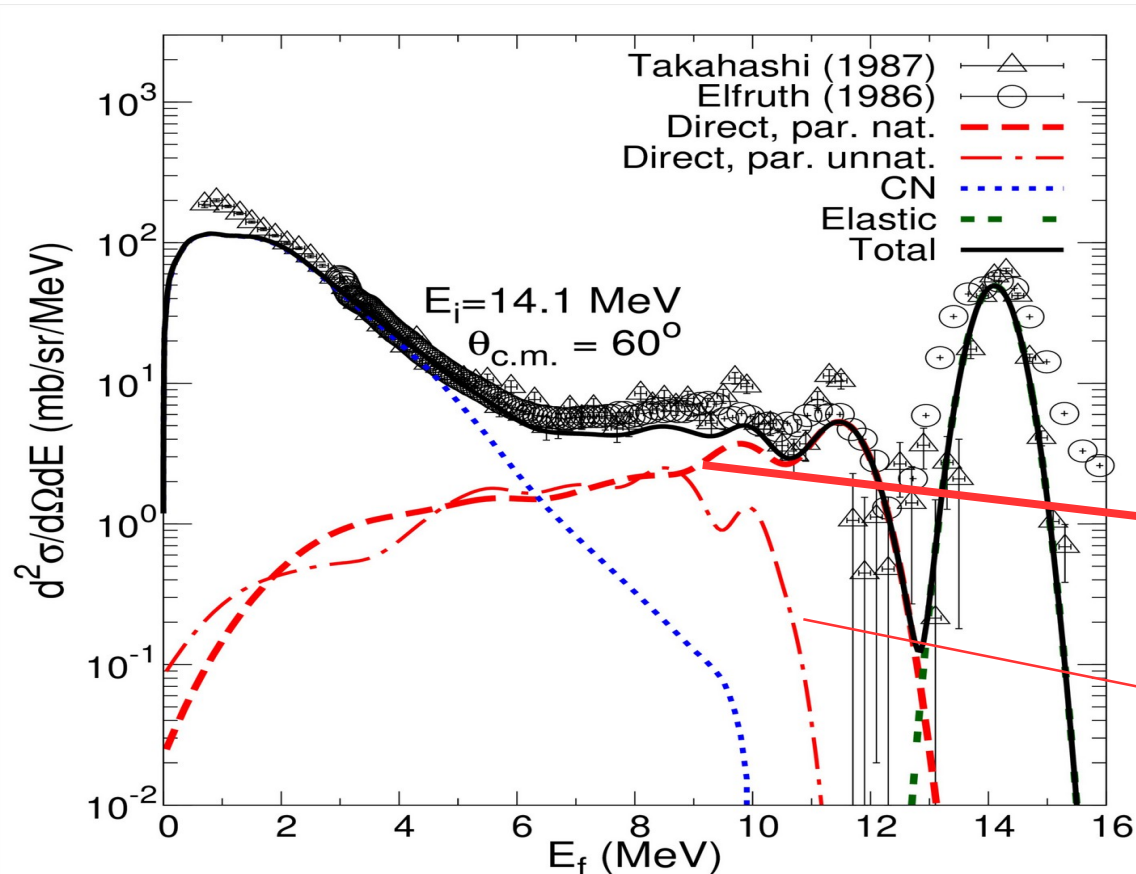
Direct/pre-eq (n,n') mechanism for spherical targets

Example:

$^{208}\text{Pb}(n,xn) \text{ ddx} :$

neutron emitted from

- **direct, pre-equilibrium (n,n')**
- **compound nucleus decay.**



Structure theory for

$^{208}\text{Pb}(n,n') :$

- RPA one-phonon excitations.

Reaction theory for

$^{208}\text{Pb}(n,n') :$

- **Spherical target**
→ weak coupling → DWBA.
- **One-step** process (one phonon).
- **Non-local** transition potentials
(M3Y interaction)
- **Two-body spin-orbit and tensor :**
generate **unnatural parity** transitions.

Natural parity : shape vibration (E1, E2, E3 ...).

Un-natural parity : vibration in the spin space (ex : scissors M1 mode) : **strong contribution to direct/pre-eq process.**

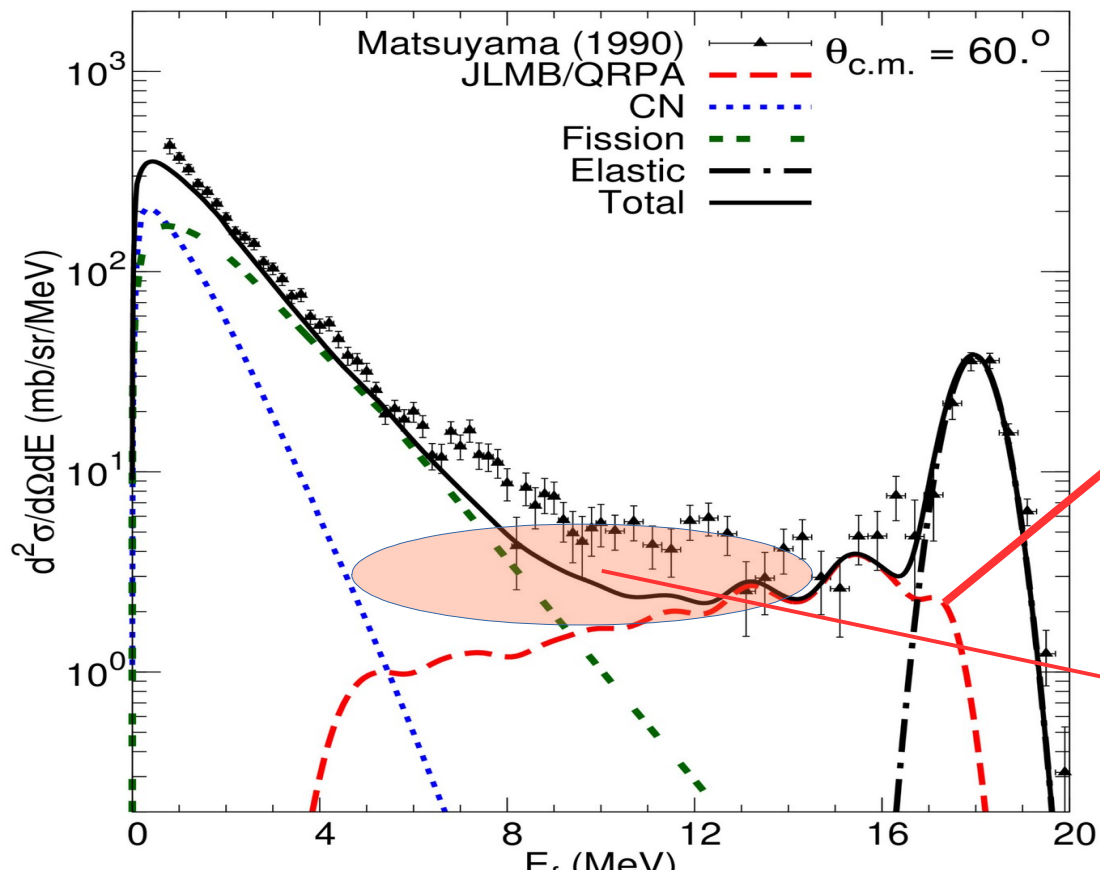
Direct/pre-eq (n,n') mechanism for deformed targets (actinides)

Example:

$^{238}\text{U}(n,xn) \text{ ddx} :$

neutron emitted from

- **direct, pre-equilibrium (n,n')**,
- compound nucleus decay,
- fission fragment decay.



Structure theory for $^{238}\text{U}(n,n')$

- QRPA one-phonon excitations + rotations.

Reaction theory for $^{238}\text{U}(n,n')$

- Strong channels couplings
→ Coupled channel (CC) framework.
- Uses **local** transition potentials (**JLM** interaction and CC code limitations).

Natural parity transitions.

Un-natural parity not included :

No two-body spin-orbit, no tensor in JLM :

→ cannot generate un-natural parity transitions

Missing xsecs :

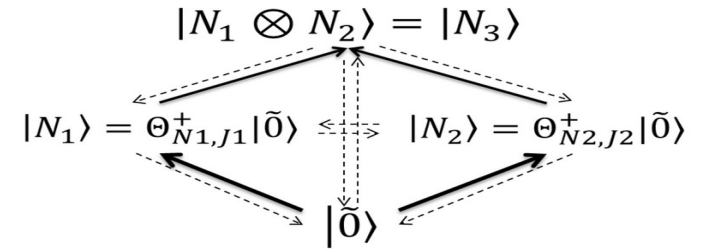
- un-natural parity ?
- Two-step process ?
- MSC ?

MSD two-step process, with 2-phonon RPA final states

One and two-step processes, $^{90}\text{Zr}(n,n')$

one-step : 1 ph or one-phonon

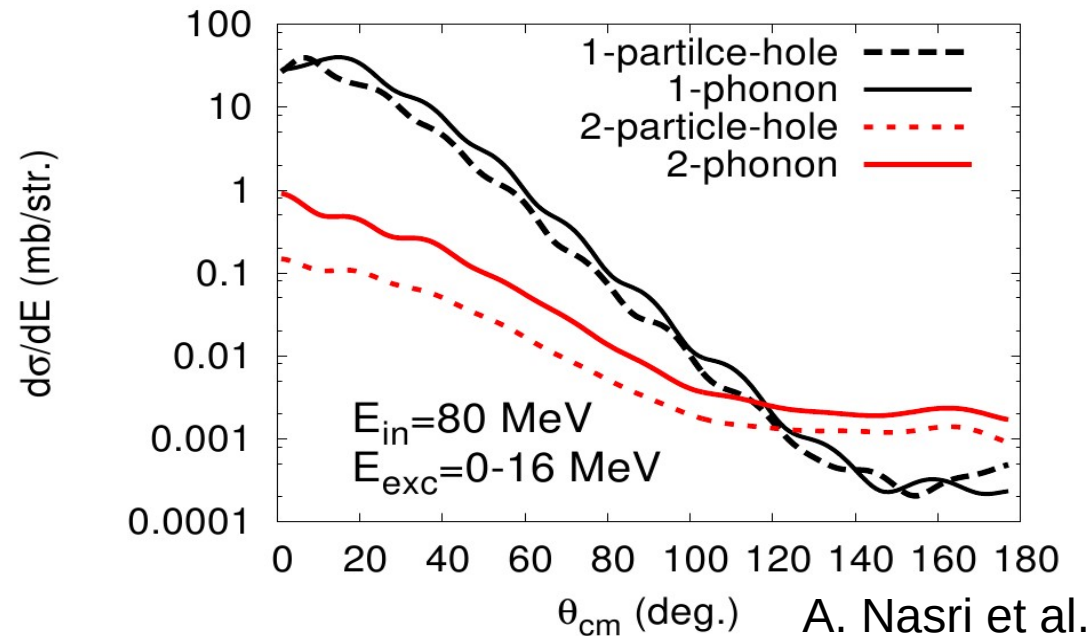
two-step : 2 ph (intermediate 1ph) or two-phonon (intermediate 1 phonon).



Approximations :

- ▶ interference between paths not considered,
- ▶ on-shell calculation for two-step,
- ▶ only central part of Melbourne g-matrix.

(No un-natural parity for now)

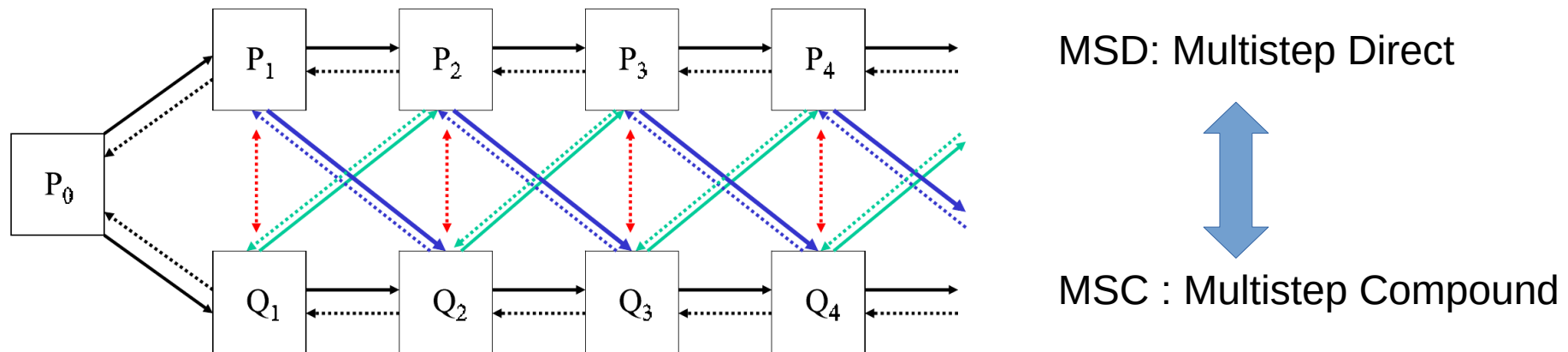


Two step : 2-phonon vs 2-particle-hole

- ▶ Collective enhancement with two-phonon.
- ▶ Quasi-Boson approximation : Pauli principle not respected.

Work in progress :MultiStep Compound

- The magnitude of the MSC contribution strongly depends on the specific implementation and underlying assumptions.
- Known to be strong for charge exchange
- Inelastic : Magnitude with respect to MSD need to be determined.
- Impact on spin-distributions of residual system.
- Implementation with new ingredients (LD...) – computing power to test approximations.



Principle, choice of unified/hybrid methods

Principle: one interaction/framework should, in spirit, cover natural and unnatural parity; requirement is comparable data quality in both channels.

→ **Broader scope:** this questioning also applies to using separate structure and reaction methods, and to competing mechanisms (one-step direct vs various multistep paths), where different ingredients may be required or optimal (structure inputs, effective interactions, continuum coupling).

Enforce uniformity if it degrades agreement with measurements ?

- Consistency is a goal, not a hard constraint; apply it with care and with a clear domain of validity.
 - But may reveal missing physics and/or compensating effect.

When to hybridize methods:

- Systematic underperformance after « honest retuning ».
- Physics-based rationale: missing spin–isospin response, tensor or spin–orbit dependence ...

Validation protocol and decision rule:

- Metrics (χ^2 ...) on a benchmark set : choice of NS method.
- Use various hybrids methods (ex for nat/unnat parity : Melbourne, xx-M3Y)

State of the art nuclear structure method, Relevant models, Developments

Effective / Chiral interactions : comparison when possible, choice depending on the system.

Small-amplitude vs large-amplitude

QRPA valid for small density-matrix oscillations (linear response, Matrix/QFAM ; S. Péru et al., J.P.Ebran et al.

Large collective motion → GCM → PGCM / 5DCH (J.P. Ebran et al. ; J. Libert et al. CEA/DAM)

QRPA typically excellent for giant resonances for most nuclei.

Rotations

Apply exact projection methods

Rotational approximation for well-deformed nuclei ($|\beta| \gtrsim 0.15$: actinides, rare earth ...) : applied with axially-deformed QRPA.

Complex excitations

In ^{16}O , low-lying 0^+ , 2^+ need $\sim 8p-8h$ → MPMH / configuration mixing (N. Pillet et al.)

Pre-equilibrium

MSD : Two-phonon couplings for 2-step pre-equilibrium (beyond QRPA)

QBA limitations → second-QRPA / SRPA-like extensions (to be developed)

MSC

New interactions (Gogny family)

D1S → D2 (finite-range in density dependence)

DG (D2-like + finite-range spin-orbit & tensor) (N. Pillet et al., CEA, DAM)

Exotic nuclei and coupling to the continuum : weak binding, halo systems, Strong N/Z asymmetry

Berggren basis / Gamow Shell Model (bound + resonant + scattering on equal footing).

Continuum HFB/RHB (DFT with explicit scattering channels) ; Continuum QRPA for collective response in weakly bound systems.

Not discussed : cluster, light nuclei.

Uncertainty Quantification and Propagation

Nuclear-structure inputs (work in progress with new Gogny interactions)

Parameterize D1S $\rightarrow$ D2 $\rightarrow$ DG variants (density dependence, spin-orbit, tensor, pairing).

Reactions

UQ for optical potentials and two-body effective interactions : JLM, Melbourne g -matrix, M3Y ...

Propagate to all channels: elastic, inelastic (one-step DWBA/CCBA; pre-equilibrium : multistep direct/compound)

Spectrum, angular distributions, total and partial cross sections

End-to-end workflow (structure $\rightarrow$ reaction) ; obviously not a unique protocole

Likelihood using the experiment's full covariance

Conclusions - Perspectives

- ✓ **Microscopic inelastic scattering model** based on **NM effective interaction** and **HFB+QRPA Gogny-based NS input** provides **good account of various inelastic processes**
 - **Improvement** in $(n,n'\gamma)$ and (n,xn) reactions modeling, **impact** on (n,xn) , fission
- ✓ Analysis of **large set of partial cross sections** : test **various aspects of modeling**
 - move towards **global improvement** of inelastic modeling.
- ✓ **Spin distributions** : input for analyses based on surrogate method.
- ✓ Input for exp. NS studies allows to **calibrate experiment**, and **extract NS informations** from measured cross sections.

► **Good predictive power, requires validated NS inputs and suitable NR formalism.** ◀

- ⇒ $(n,xn\gamma)$ data : analyses in progress ^{182,183,184,186}W, ²³⁸U ... - Application to ND evaluation process.
- ⇒ Improve/generalize UQ and propagation.
- ⇒ Recent implementation of deformed JLM in TALYS : global analysis EXFOR data.
- ⇒ Coupling rotational bands : systematics
- ⇒ Elastic/inelastic from MPMH, PGCM : ab-initio / effective forces.
- ⇒ Improve P-re-equilibrium model : two-steps and beyond MSD, review of MSC mechanism



→ JLM framework : V_{eff}

- + based Brueckner-Hartree-Fock in Nuclear matter
- + ad-hoc prescriptions :
 - * improved LDA (Gaussian form factors)
 - * spin-orbit
- + energy dependant parameters (remained close to unity) : fitted on set of el. and charge-exch exp. data for spherical and near-spherical nuclei (Bauge et al., Phys. Rev. C 2001)

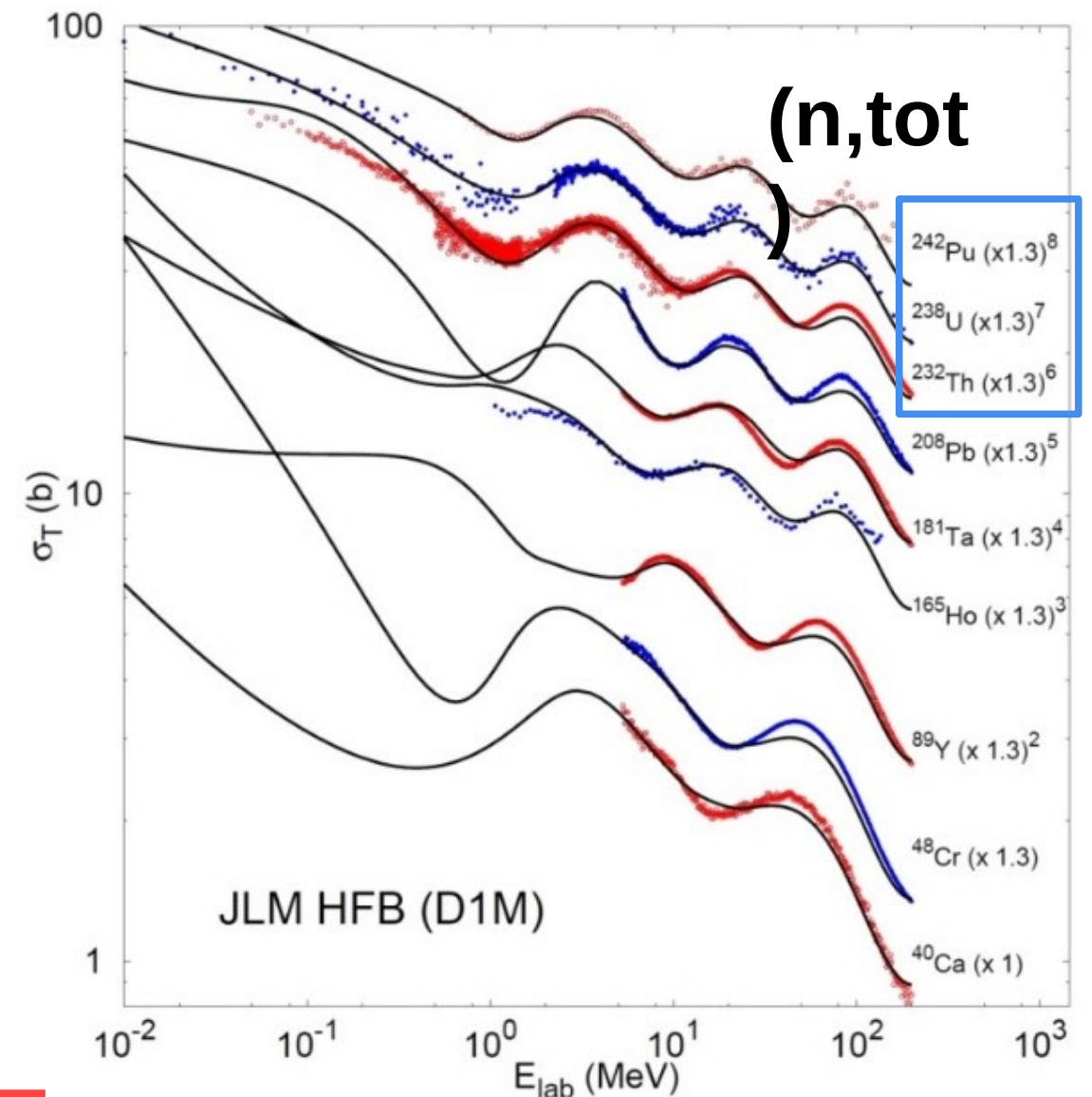
→ Good description :

- + total, elastic differential cross sections
 - *spherical*/deformed.
 - n,p, (dble folding : ^4He , ^{12}C)
- + inelastic cross sections for discrete/continuum excitations

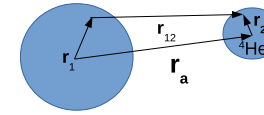
→ Input : needs accurate NS model : + mean field HF(B)
+ beyond mean field : (Q)RPA, MPMH, PGCM ...
+ shell model ...

→ predictive power, “validity domain” : Depends on NS Input, Limit of LDA, use adequate coupled channels framework.

*** Validation of NS input to reaction models ***



Double folding : $U(\mathbf{r}_\alpha) = \int d\mathbf{r}_1 \int d\mathbf{r}_2 \rho_A(\mathbf{r}_1) \rho_\alpha(\mathbf{r}_2) V(|\mathbf{r}_1 - \mathbf{r}_2|, \rho_1, \rho_2, E)$



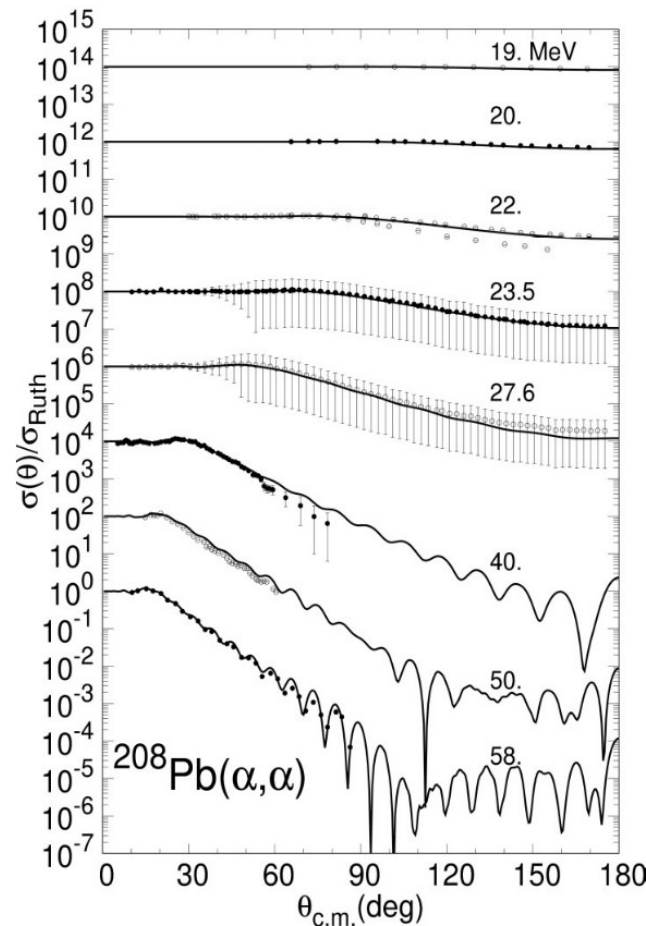
- Effective N-N interaction: JLM-B.
- Additional density-dependence
- Alpha frozen (not too high energy).

Hogenbrik et al., PLB 223, p.282 (1989)

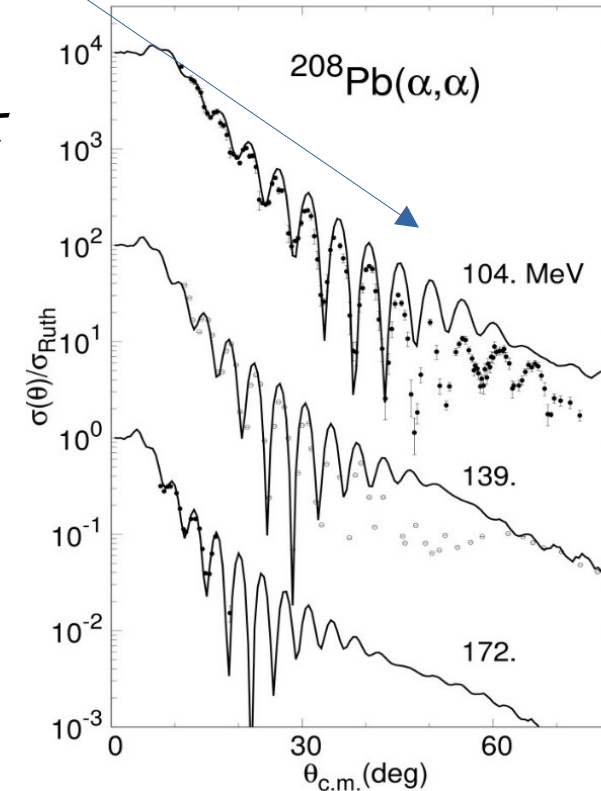
$$V(\rho_1, \rho_2, E) \equiv V_{JLM-B}(\rho_1, E)(1 - \beta \rho_2^2)$$

$$\rho_\alpha(r_2) = 0.4229 e^{-0.7014 r_2^2}$$

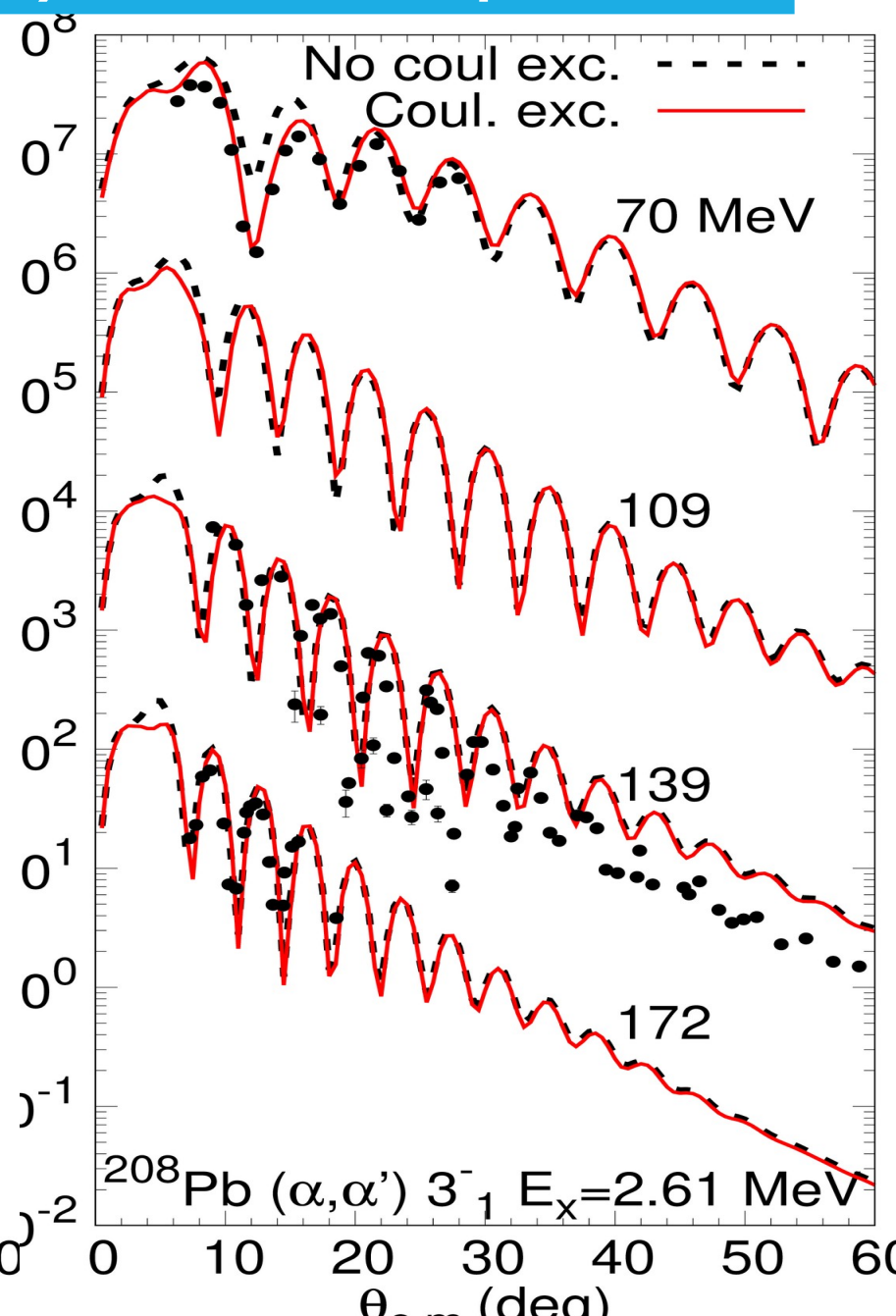
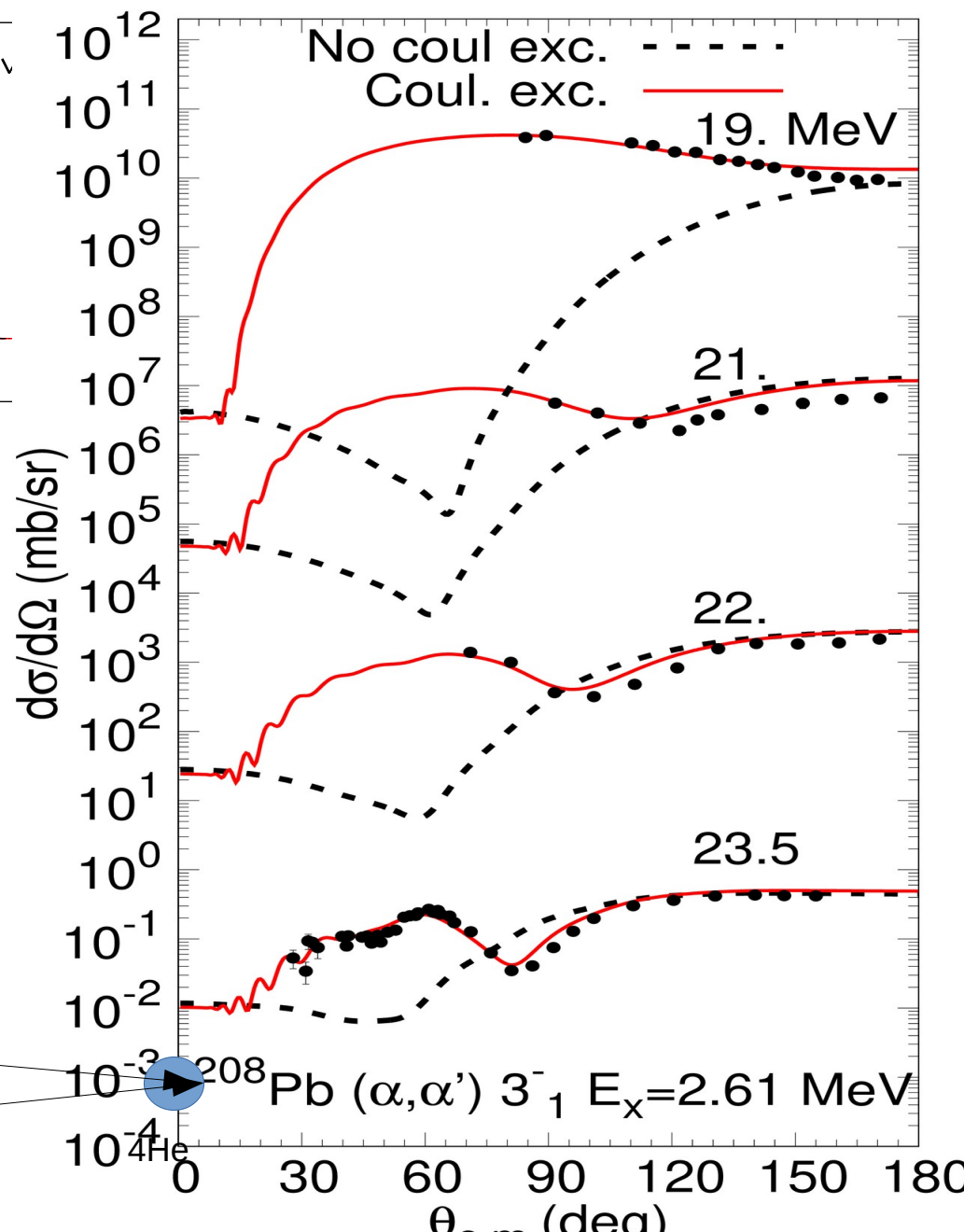
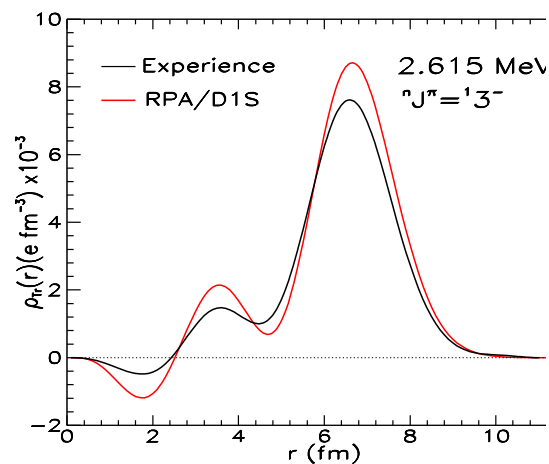
$$\beta_R = 0.4 \quad \beta_I = 0$$



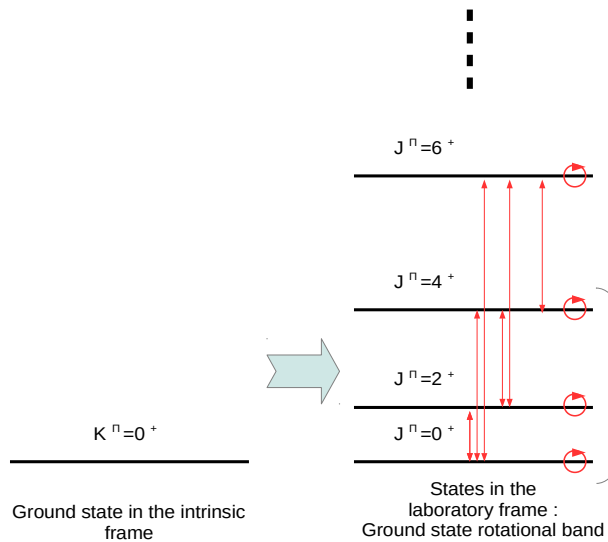
Matter densities RPA



$^{240}\text{Pu}(\alpha, \alpha')$: validation method for direct model : ii) inelastic on spherical



$^{240}\text{Pu}(\alpha, \alpha')$: validation
method for direct model :
iii) elastic + inelastic on
deformed



Coupled channels

