

- Higgs pair production:
Measurement of triple Higgs coupling → reconstruction of Higgs potential
- Hierarchy problem
→ in Composite Higgs models: Higgs mass generated dynamically through loops of SM fermions and gauge bosons
→ Higgs mass is naturally light

- SILH: Effective low-energy description, only the Higgs couplings to the SM fields are modified and depend on $\xi = \frac{v^2}{f^2}$ with $\xi \in [0, 1]$
[Giudice, Grojean, Pomarol, Rattazzi]
- Completion for large values of ξ : 5D theory on AdS spacetime $\rightarrow$ holographic interpretation in terms of 4D strongly coupled field theories
- Higgs boson as a pseudo Nambu-Goldstone boson [Kaplan, Georgi, Galison, Dugan; Dimopoulos, Preskill; Banks] of a global symmetry $G = SO(5) \times U(1)_X$ which is broken down to
 - $O(4) \times U(1)_X$ on IR-brane
 - $SU(2)_L \times U(1)_Y$ on UV-brane
- G is explicitly broken by couplings of SM fields to strong sector
 $\rightarrow$ loops of SM fermions and gauge bosons generate Higgs potential
- MCHM₅: Fermions in fundamental representation of $SO(5)$

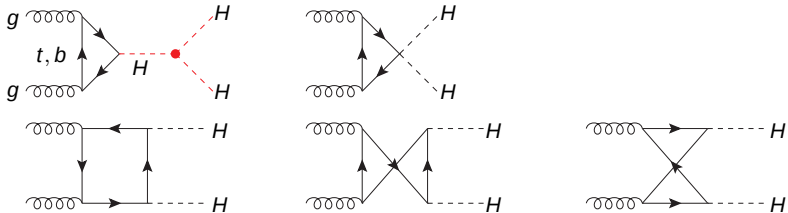
HVV	$\sqrt{1-\xi}$
$HHVV$	$1-2\xi$
HHH	$\frac{1-2\xi}{\sqrt{1-\xi}}$
$Hf\bar{f}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$

New coupling: $g_{HHf\bar{f}} = \frac{m_f}{v^2} 4\xi$

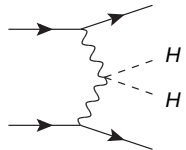
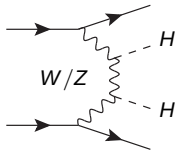
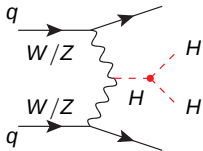
In SM limit $\xi \rightarrow 0$ the new coupling vanishes.

- Higgs self-couplings are necessary to investigate Higgs potential.
- In multi-Higgs-production Higgs self-couplings can be measured.
- Most important processes in SM at the LHC:
 - Gluon fusion
 - Vector boson fusion
 - Double Higgs-strahlung

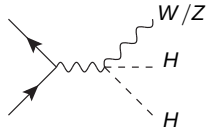
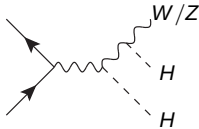
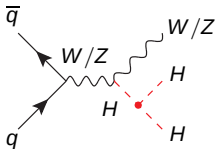
Gluon fusion:

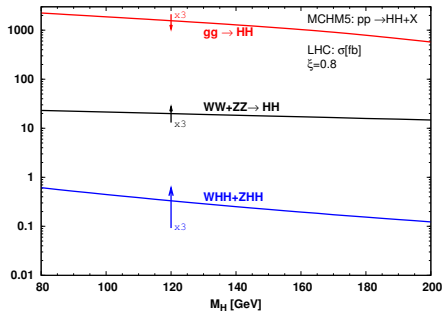
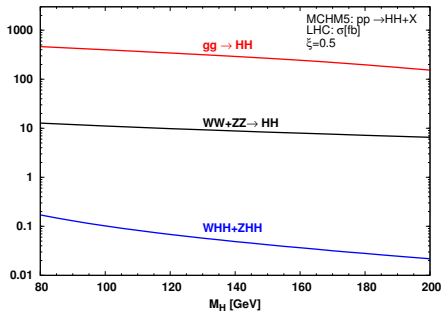
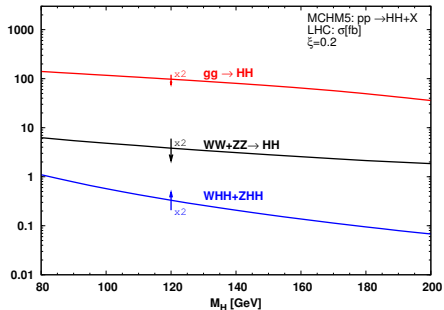
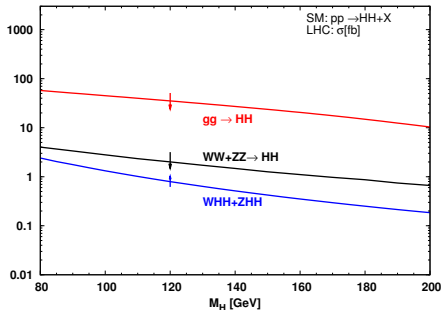


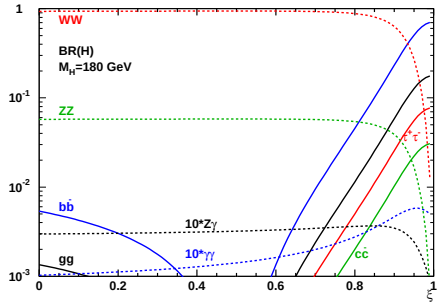
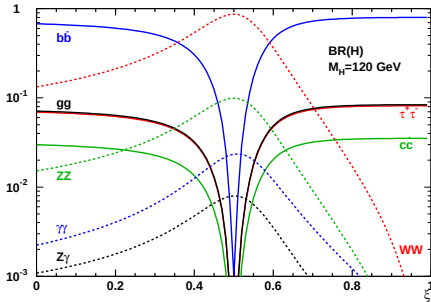
Vector boson fusion:



Double Higgs-strahlung:







HVV	$\sqrt{1-\xi}$
$Hf\bar{f}$	$\frac{1-2\xi}{\sqrt{1-\xi}}$

Sensitivities on $\lambda_{HHH} \neq 0$ in gluon fusion

In SM: $HH \rightarrow b\bar{b}\gamma\gamma$ for low Higgs masses and $HH \rightarrow W^+W^-W^+W^-$ for Higgs masses above the gauge boson threshold have best prospects

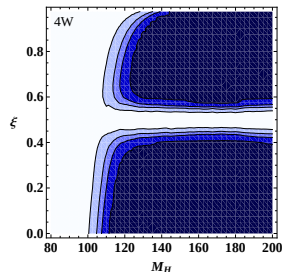
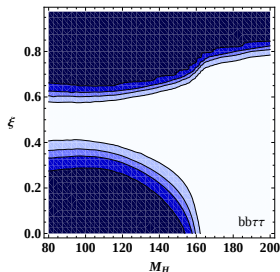
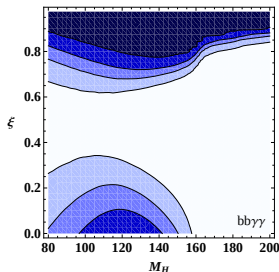
[Baur, Plehn, Rainwater]

Assumption: EWSB is realized in the framework of MCHM (ξ can be measured with accuracy of $\sim 20\%$ [Bock, Lafaye, Plehn, Rauch, Zerwas, Zerwas])

Criterion:

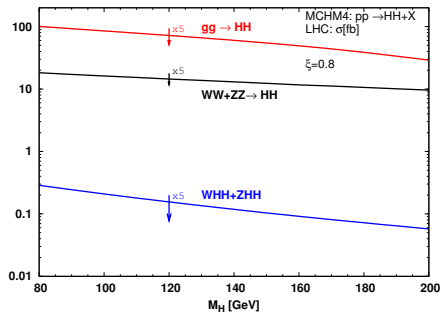
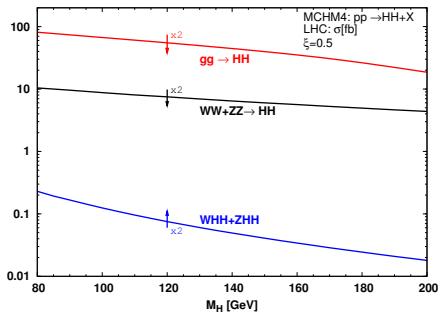
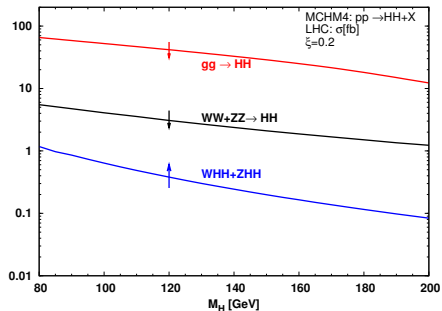
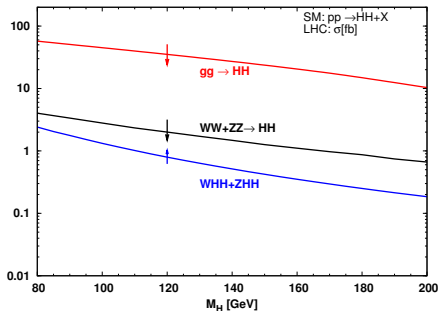
$$S + \beta\sqrt{S} < S_{\lambda_{HHH}=0} \quad \text{or} \quad S - \beta\sqrt{S} > S_{\lambda_{HHH}=0} \quad (\beta = 1, 2, 3, 5)$$

MCHM₅ for $\int \mathcal{L} = 300 \text{ fb}^{-1}$:



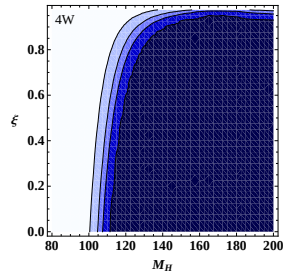
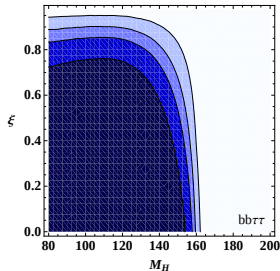
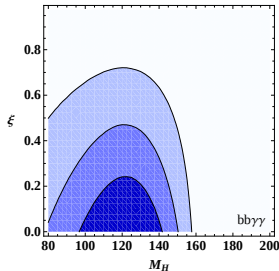
- Sensitivity areas present ideal case $\rightarrow$ for a full analysis: Detector properties and background processes must be investigated
- But e.g. for the $4W$ final state with $W^+W^-W^+W^- \rightarrow (jjl^\pm\nu)(jjl^\pm\nu)$:
In SM: For $150 \text{ GeV} \leq M_H \leq 200 \text{ GeV}$ a vanishing triple Higgs coupling can be excluded at 95% C.L. for 300 fb^{-1} [Baur,Plehn,Rainwater]
- Dominating background ($\mathcal{O}(\alpha_s\alpha^3)$)
 - $\rightarrow$ no Higgs in intermediate state
 - $\rightarrow$ leading background processes are the same as in SM
- But: Signal cross section is larger than in the SM!

- Composite Higgs models are an interesting alternative to the SM
- Cross sections for Higgs pair production via gluon fusion and vector boson fusion are enhanced compared to the SM for all ξ
- Cross section for Higgs pair production via double Higgs-strahlung is reduced compared to the SM
- Branching ratios in MCHM₅ are changed compared to the SM and depend on ξ .
- Prospects of measuring non-vanishing λ_{HHH} for large Higgs masses in $W^+W^-W^+W^-$ decay channel good, for low Higgs masses $b\bar{b}\tau^+\tau^-$ might be possible
- Measuring λ_{HHH} with higher precision might be possible for higher luminosities.



Sensitivity on $\lambda_{HHH} \neq 0$ in gluon fusion

MCHM₄ for $\int \mathcal{L} = 300 \text{ fb}^{-1}$:



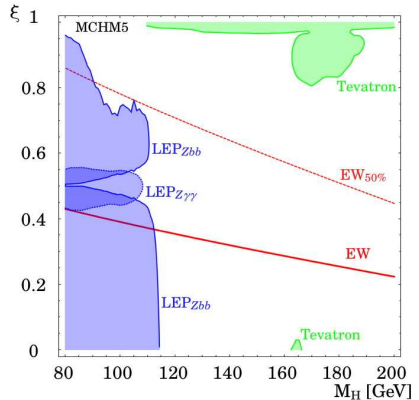
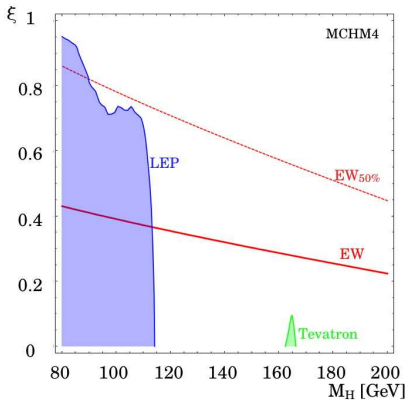


Figure: See [Espinosa,Grojean, Mühlleitner; arXiv:1003.3251]
 For constraints in a model with partially composite top, see [Anastasiou, Furlan, Santiago; Gillioz]

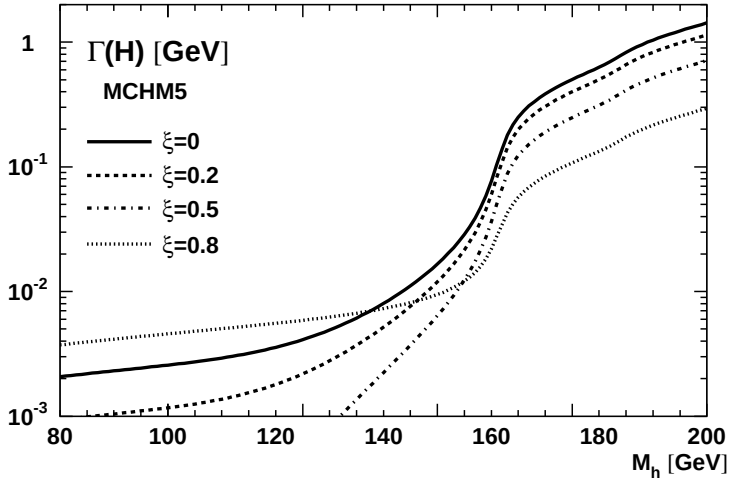
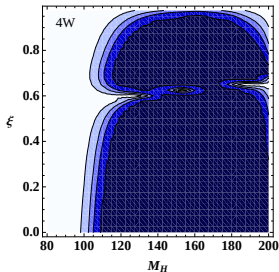
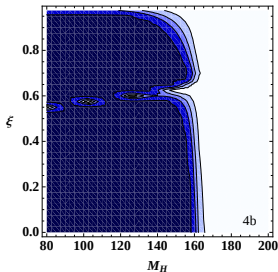


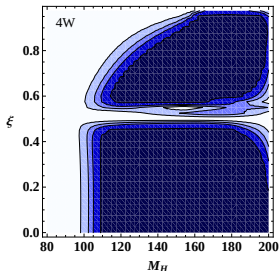
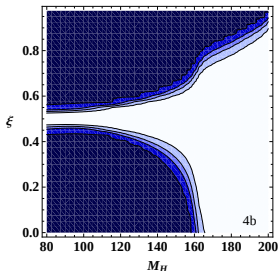
Figure: See [\[Espinosa, Grojean, Mühlleitner\]](#)

Double Higgs-strahlung at the ILC ($\sqrt{s} = 0.5$ TeV, $\int \mathcal{L} = 500 \text{ fb}^{-1}$)

MCHM₄:

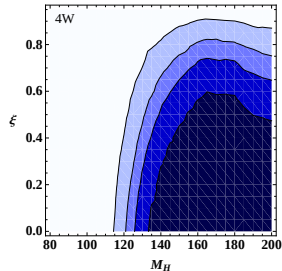
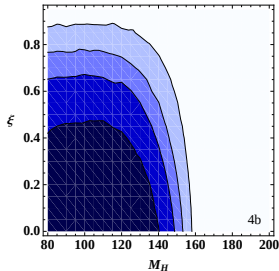


MCHM₅:

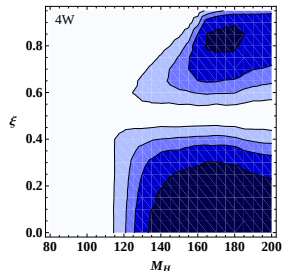
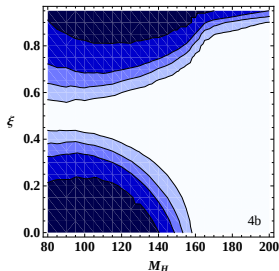


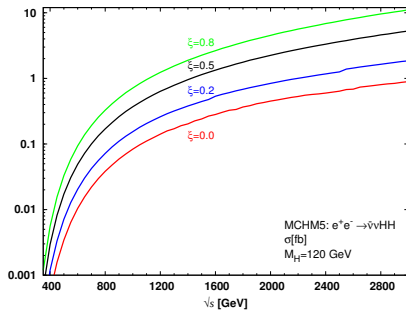
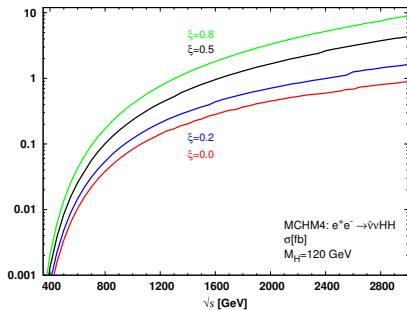
W boson fusion at the ILC ($\sqrt{s} = 0.5$ TeV, $\int \mathcal{L} = 500 \text{ fb}^{-1}$)

MCHM₄:



MCHM₅:





$$\mathcal{M} \xrightarrow{s \rightarrow \infty} -\sqrt{2}G_F s \xi$$

New kinetic terms $\rightarrow$ field redefinition

$$\Phi = \frac{v}{\sqrt{2}} \begin{pmatrix} 0 \\ \frac{1}{v} \left(H - \frac{c_H \xi}{2} \left(H + \frac{H^2}{v} + \frac{H^3}{3v^2} \right) \right) + 1 \end{pmatrix}$$

$\rightarrow$ redefinition of Higgs and fermion masses and vacuum expectation value

$$\frac{v^2}{2} = \frac{\mu^2}{2\lambda} \left(1 - \frac{3}{4} c_6 \xi \right) = \frac{(246 \text{ GeV})^2}{2} .$$

$$m_f = \frac{1}{\sqrt{2}} y_f v \left(1 + \frac{\xi}{2} c_y \right) ,$$

$$\frac{M_H^2}{2} = \frac{(\sqrt{2\lambda}v)^2}{2} \left(1 - c_H \xi + \frac{3}{4} c_6 \xi \right) .$$

$$g_{HVV} = g_{HVV}^{SM} \left(1 - \frac{c_H}{2} \xi \right)$$

$$g_{Hff} = g_{Hff}^{SM} \left(1 - \xi \frac{c_H}{2} + \xi c_y \right)$$

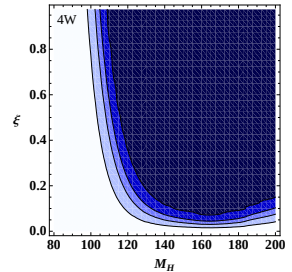
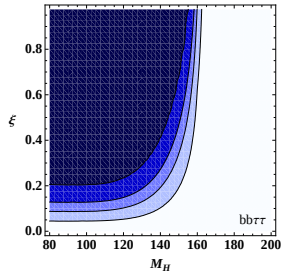
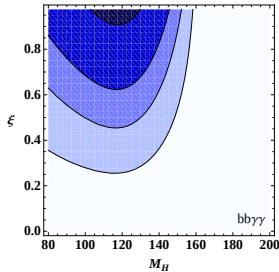
$$g_{HHH} = g_{HHH}^{SM} \left(1 + \xi c_6 - \xi \frac{3c_H}{2} \right)$$

$$\text{with } g_{HWW}^{SM} = g M_W \text{ and } g_{HZZ}^{SM} = \frac{g M_Z}{2}$$

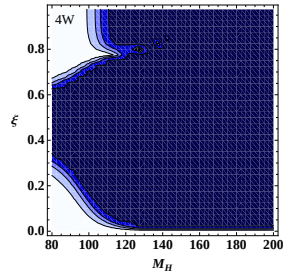
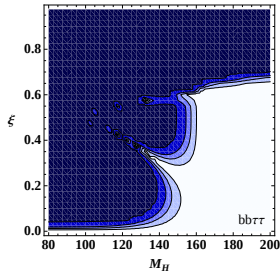
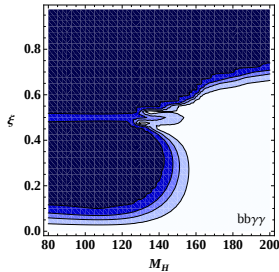
$$\text{with } g_{Hff}^{SM} = \frac{g m_f}{2 M_W}$$

$$\text{with } g_{HHH}^{SM} = \frac{3 g M_H^2}{2 M_W}$$

Can the MCHM₄ be distinguished from the SM for $\int \mathcal{L} = 300 \text{ fb}^{-1}$?

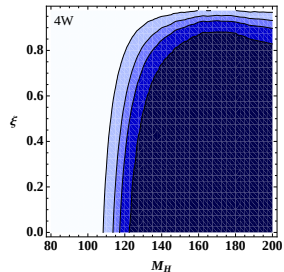
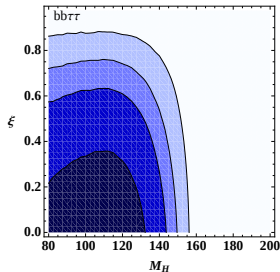
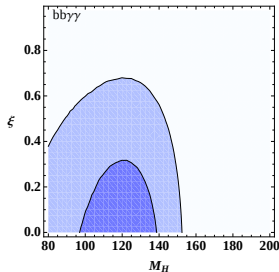


Can the MCHM₅ be distinguished from the SM for $\int \mathcal{L} = 300 \text{ fb}^{-1}$?



Can λ_{HHH} be measured with 30% precision in MCHM₄?

$\int \mathcal{L} = 3000 \text{ fb}^{-1}$ for $b\bar{b}\gamma\gamma$, $\int \mathcal{L} = 600 \text{ fb}^{-1}$ for $b\bar{b}\tau^+\tau^-$ and $4W$



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