

ISR studies at flavour factories

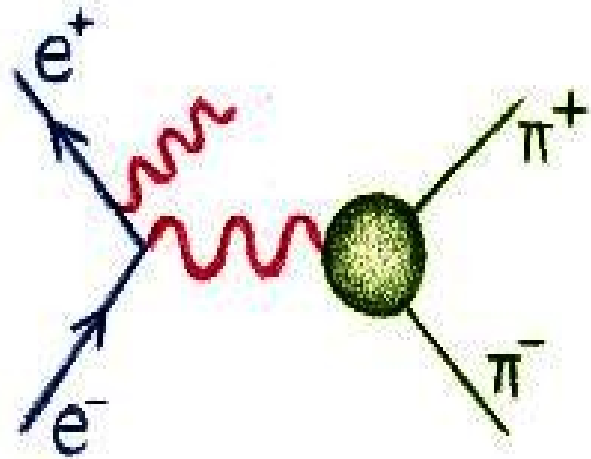
Germán Rodrigo



**Factory Workshop,
9-11 May 2007, Paris**

radiative return

The way to get the hadronic cross section at a fixed energy machine



Photon radiated off the initial e^+e^- (**ISR**) reduces the effective energy of the collision ($s \Rightarrow Q^2$)

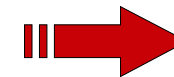
$$d\sigma(e^+e^- \rightarrow \text{hadrons} + \gamma) = H(Q^2, \theta_\gamma) d\sigma(e^+e^- \rightarrow \text{hadrons})$$

✓ Large luminosities of flavour factories:

❖ **KLOE @ DAPHNE**

❖ **CLEO-C @ CESR**

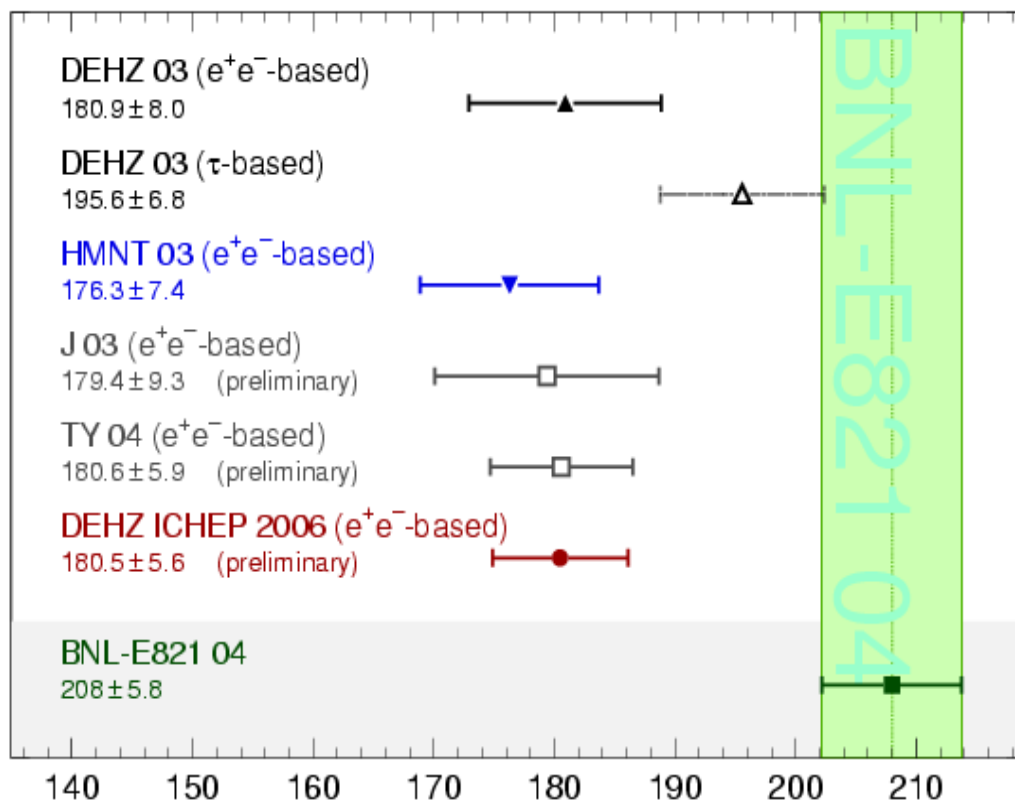
❖ **BaBar @ PEP-II and BELLE @ KEK-B**



compensate factor α/π from photon radiation

✓ High precision measurement of $R(s)$ over the full range of energies, from threshold up to \sqrt{s} **in an homogeneous data set**

$(g-2)_\mu$



$a_\mu - 11\,659\,000 \quad (10^{-10})$

$$a_\mu^{had, LO} = \left(\frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^{\infty} \frac{ds}{s^2} K(s) R(s)$$

$$\Delta \alpha_{had}(m_Z^2) = -\frac{\alpha m_Z^2}{3\pi} \int_{4m_\pi^2}^{\infty} \frac{ds}{s} \frac{R(s)}{s - m_Z^2 - i\eta}$$

Davier (TAU06) (x 10⁻¹¹)

$$a_\mu^{BNL} = 11\,659\,2080 \pm 63$$

$$a_\mu(e^+e^-) = 11\,659\,1805 \pm 44_{had} \pm 35_{|b|} \pm 2_{QED+EW} (56)$$

$$a_\mu^{had, LO} = 6909 \pm 44$$

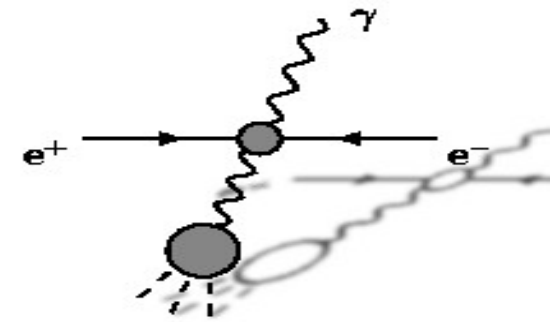
$$a_\mu^{|b|} = 120 \pm 35$$

$$a_\mu^{exp} - a_\mu^{SM} = 273 \pm 83 (3.3 \sigma)$$

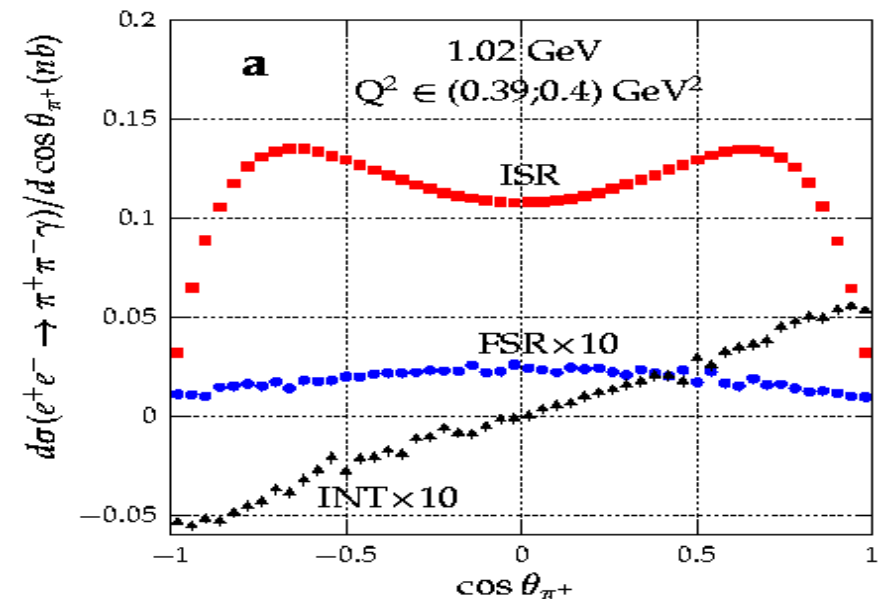
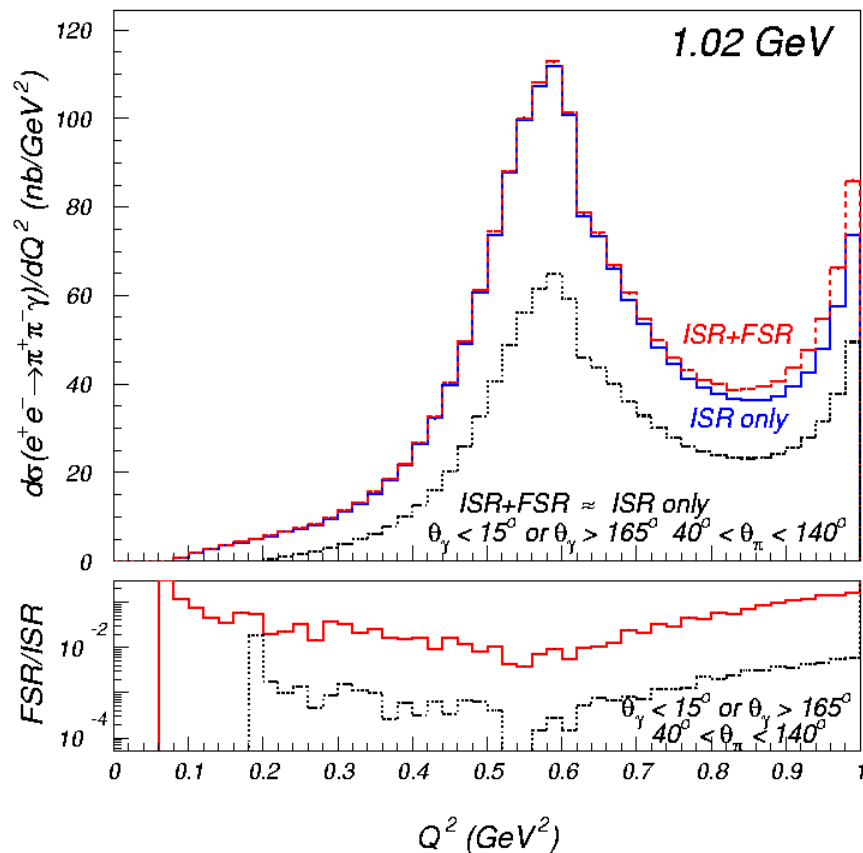
FSR

suppressed at **B-factories**:

very hard photons for low hadronic invariant masses



DAPHNE: ISR dominates for untagged photons (small angle), but suppress threshold tail tagged photons (large angle) FSR 10-20%



$$A_{FB}(Q^2) = \frac{N(\theta_{\pi^+} > \pi/2) - N(\theta_{\pi^+} < \pi/2)}{N(\theta_{\pi^+} > \pi/2) + N(\theta_{\pi^+} < \pi/2)}(Q^2)$$

$$A_C(\theta_\pi) = \frac{N(\pi^+) - N(\pi^-)}{N(\pi^+) + N(\pi^-)}(\theta_\pi)$$

radiative phi decays

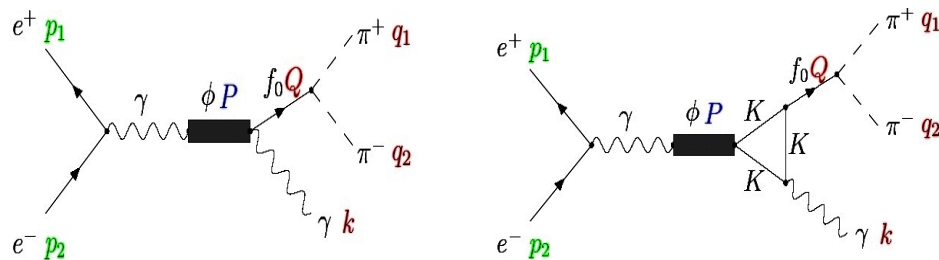
Czyż, Grzelinska, Kühn, PLB611(05)116,
KLOE PLB634(05)148

$e^+ e^- \rightarrow \phi \rightarrow \pi^+ \pi^- \gamma$ pollutes
the extraction of $\sigma(e^+ e^- \rightarrow \pi^+ \pi^-)$
close to the phi mass

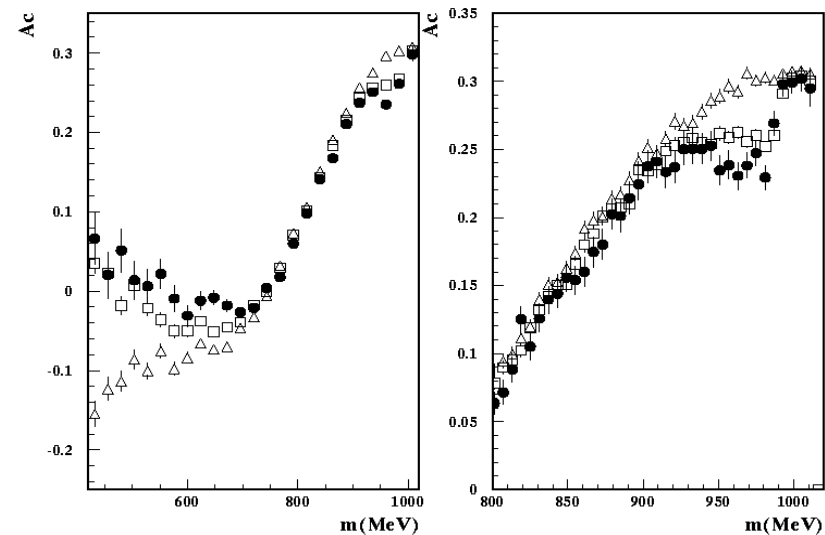
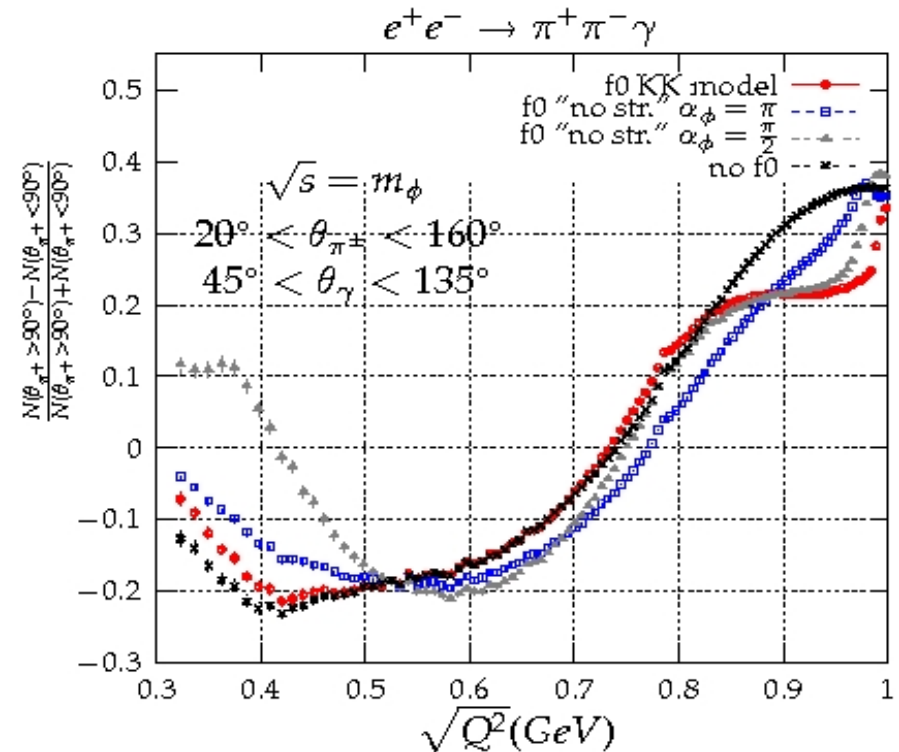
charge asymmetry allows to discriminate
between different models of the radiative
decay

$$\phi \rightarrow \pi^+ \pi^- \gamma, \pi^0 \pi^0 \gamma,$$

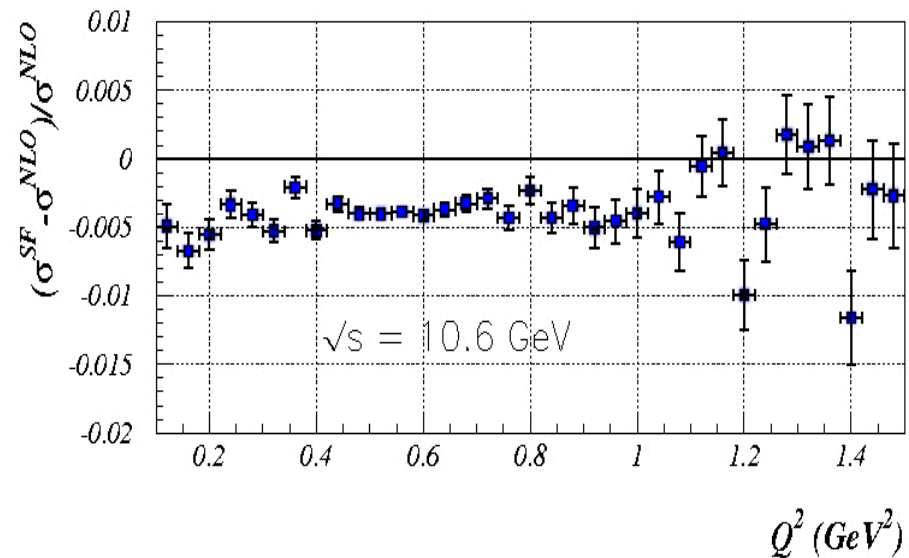
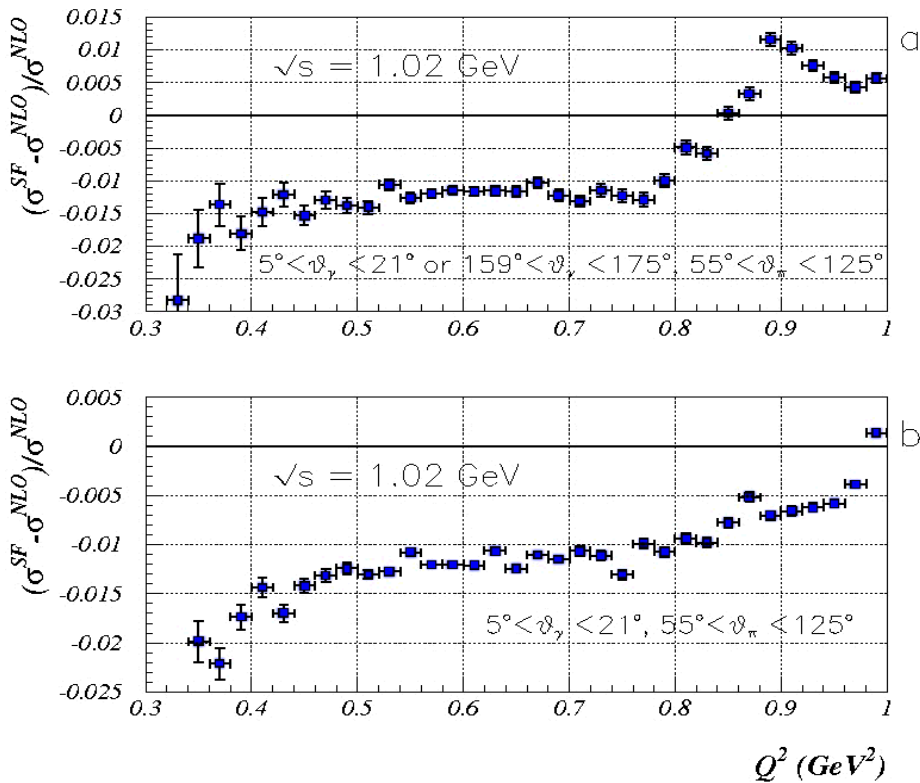
$$\phi \rightarrow (f_0(980) + f_0(600)) \gamma \rightarrow \pi \pi \gamma$$



other contributions (beyond sQED + VMD
+ radiative phi decays) might be
important in the threshold region
[Pancheri, Shekhovtsova, Venanzoni]



NLO vs SF



LL: EVA [Binner, Melnikov, Kühn]

EVA4 π [Czyż, Kühn]

- resums big logs $L = \text{Log}(s/m_e^2)$ to all orders
- Extra collinear emission integrated out: no momentum conservation
- Untagged photon: double counting

NLO: PHOKHARA

- LL+subleading terms (1%)
- Full angular dependence
- Momentum conservation
- Tagged or untagged photons
- ISR accuracy 0.5% (conservative)
- (goal: 0.1-0.2% by adding LL two-loop)**



PHOKHARA

radiative return at meson factories

Physics

Electron--positron annihilation into hadrons plus an energetic photon from initial state radiation (ISR) allows the hadronic cross-section to be measured over a wide range of energies at high luminosity meson factories [[DAPHNE](#), [CESR](#), [PEP-II](#), [KEK-B](#)].

Content

PHOKHARA is a Monte Carlo event generator which simulates this process at the next-to-leading order (NLO) accuracy. This includes virtual and soft photon corrections to one photon emission events and the emission of two real hard photons.

Downloads

VERSION 6.0 (December 2006): Lambda pair production added as new hadronic channel : $e^+e^- \rightarrow \Lambda (\rightarrow n^- p) \bar{\Lambda} (\rightarrow n^+ \bar{p}) \gamma$.

- manual [[Postscript](#), [PDF](#)], source [[uencoded](#)]

Forthcoming features

- Full one-loop radiative corrections for muon production
- Simulation of narrow resonances (J/ψ and $\psi(2S)$)
- Simulation of other exclusive hadronic channels
- FSR for three pion production

PHOKHARA 6.0 (December 2006)

Fixed order radiative corrections: NLO accuracy

Hadronic channels

$$\pi^+ \pi^-$$

$$\mu^+ \mu^-$$

$$2\pi^0 \pi^+ \pi^-, 2\pi^+ 2\pi^-$$

$$p \bar{p}, n \bar{n}$$

$$\pi^0 \pi^+ \pi^-, K^+ K^-, K^0 \bar{K}^0$$

$$\Lambda(\rightarrow \pi^- p) \bar{\Lambda}(\rightarrow \pi^+ \bar{p})$$

+ *radiative phi decays*

background and normalization

Pauli and Dirac Form Factors

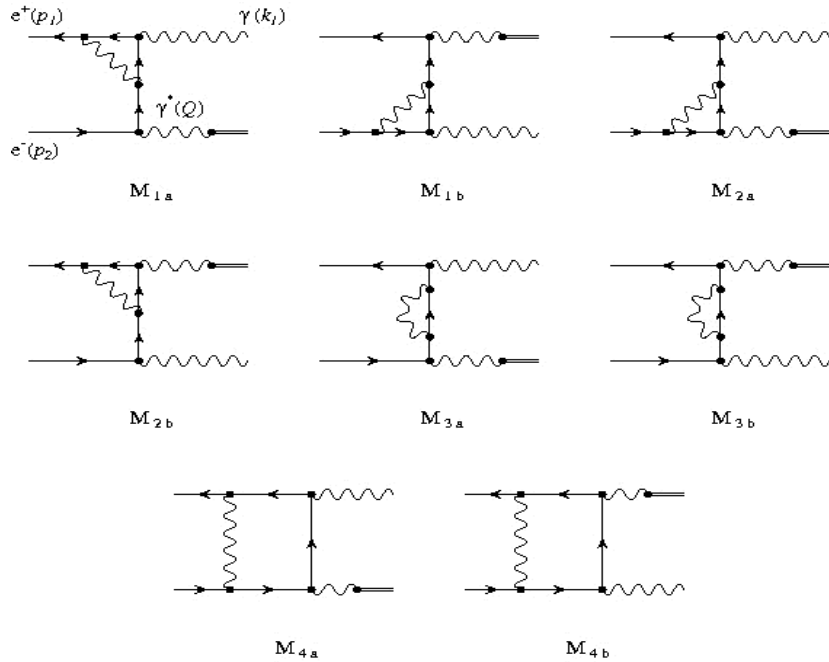
new channels

Tagged or untagged photons

Modular structure:

easy replacement of hadronic form factors

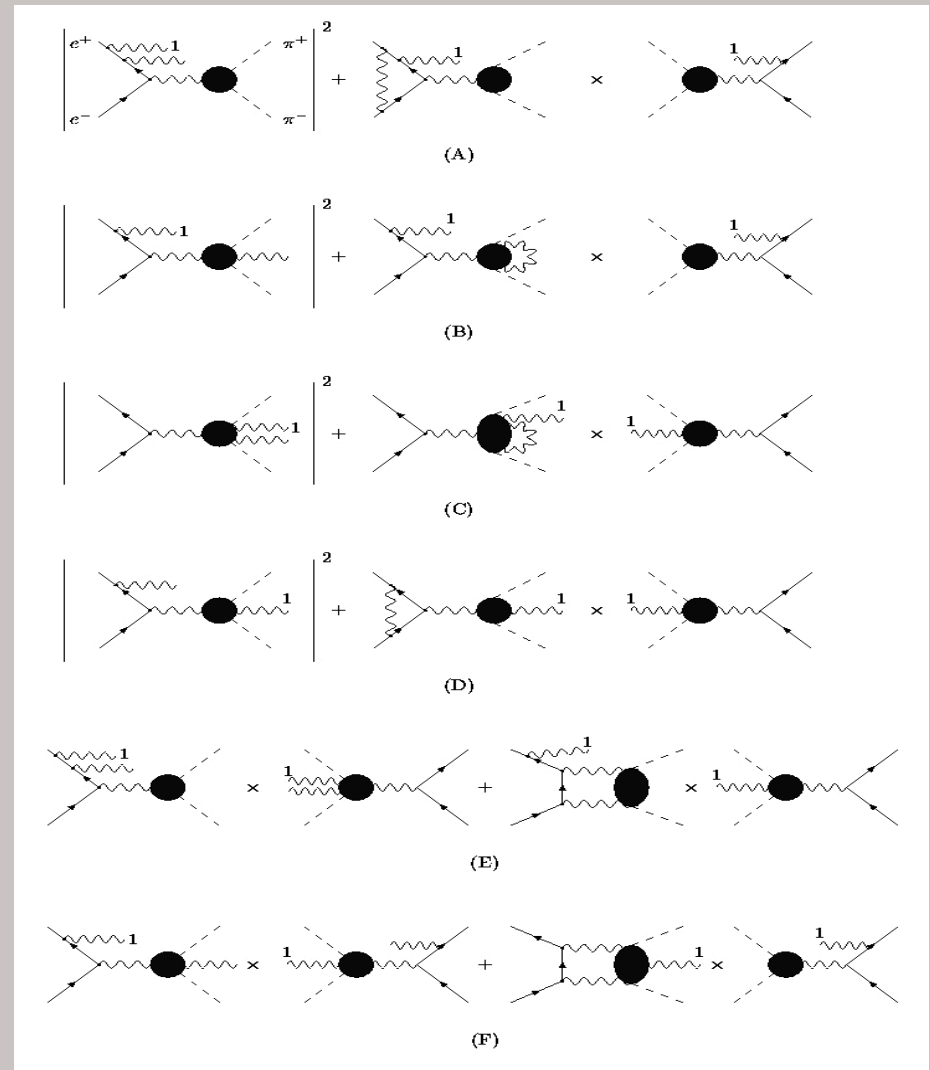
NLO



ISR virtual+soft corrections
to $e^+e^- \rightarrow \text{hadrons} + \gamma$
factorizable

$$\sigma = \int L_{ISR}^{\mu\nu} H_{\mu\nu}$$

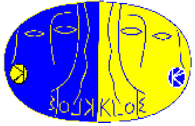
independent of the hadronic
channel



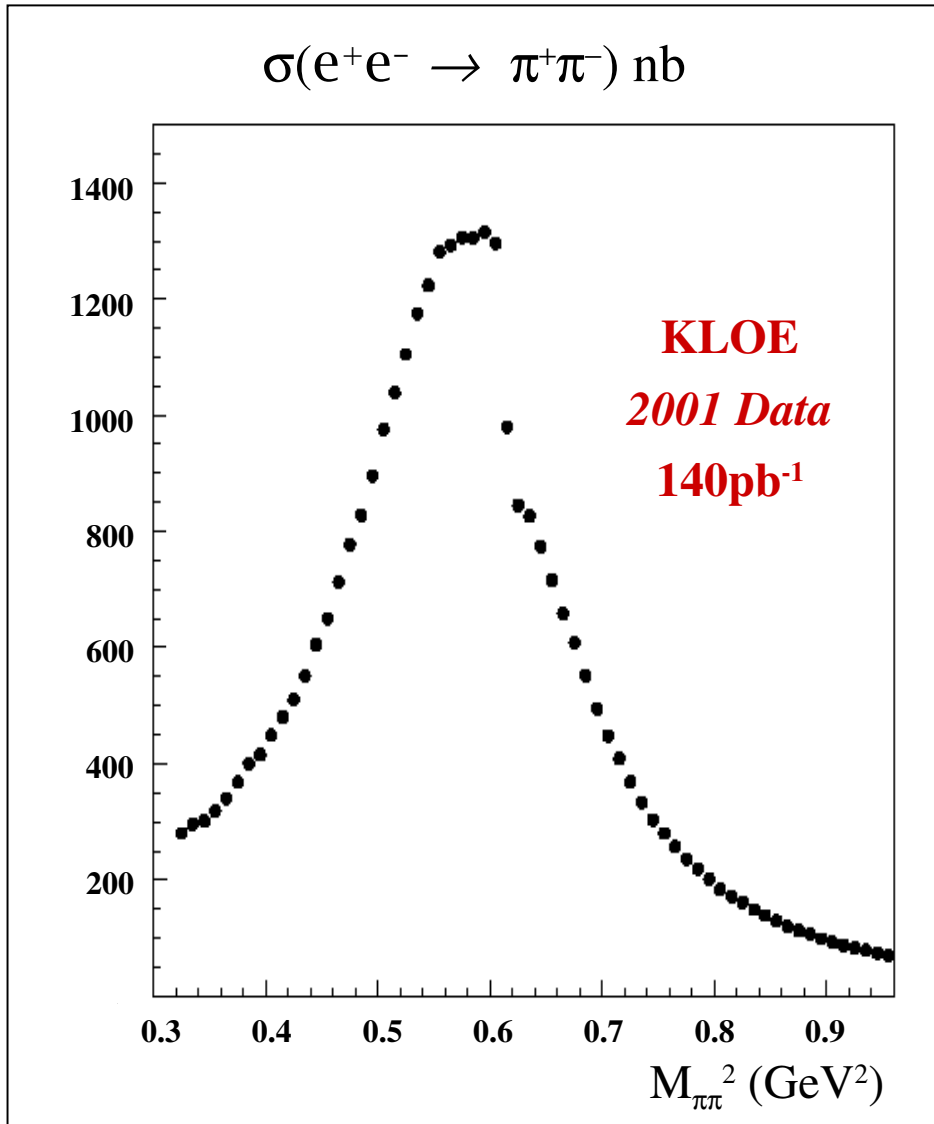
FSR @ NLO dominated by simultaneous emission
of one photon from FSR and another one from ISR
(+ virtual corrections)

PHOKHARA includes at present gauge invariant
sets of *amplitudes* which lead to infrared-finite
charge-even combinations for $\pi^+\pi^-$, KK and $\mu^+\mu^-$

pion form factor



Phys. Lett. B606 (2005) 12



Statistical error negligible (1.5 Million events)
total systematic error 1.3%

ongoing analysis at large and small
photon angles with systematics below 1%

nucleon form factors

Dirac (F_1) and Pauli (F_2) form factors

$$J_\mu = -ie \bar{u}(q_2) \left(F_1^N(Q^2) \gamma_\mu - \frac{F_2^N(Q^2)}{4m_N} [\gamma_\mu, Q] \right) v(q_1)$$

Electric and magnetic Sachs FF

$$G_M^N = F_1^N + F_2^N, \quad G_E^N = F_1^N + \frac{Q^2}{4m_N^2} F_2^N$$

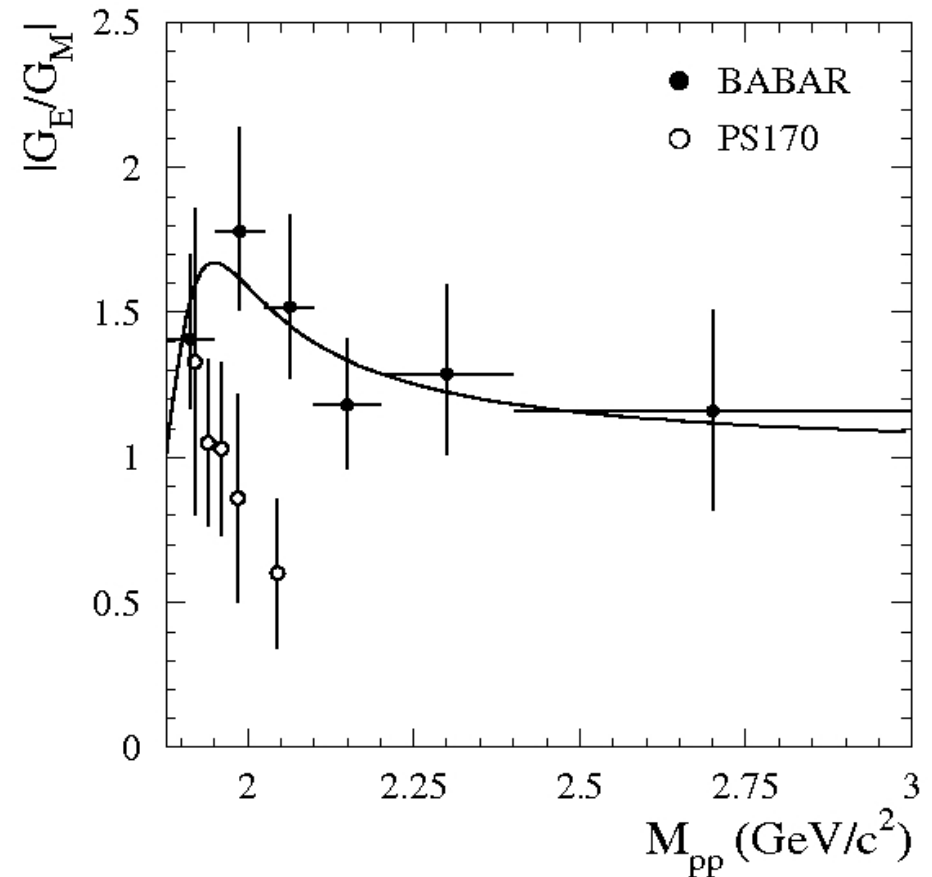
at threshold $|G_M| = |G_E|$

disagreement in the space-like region on the ratio G_E/G_M between Rosenbluth and recoil polarization methods

radiative return in the **time-like** region

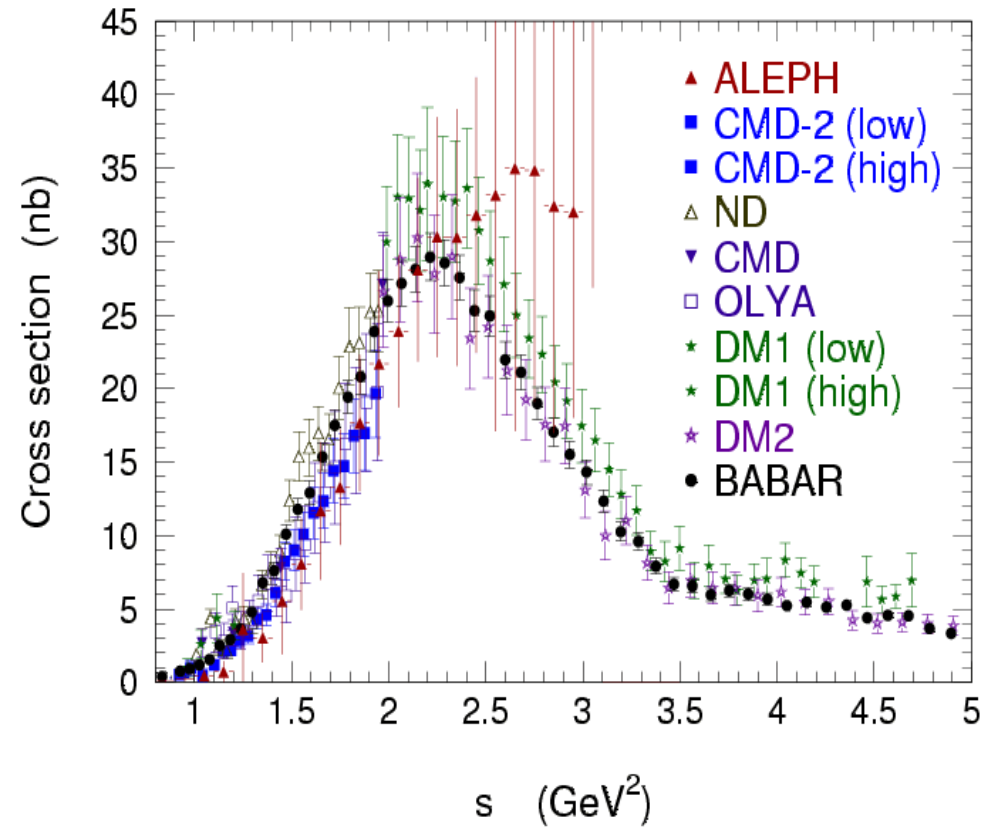
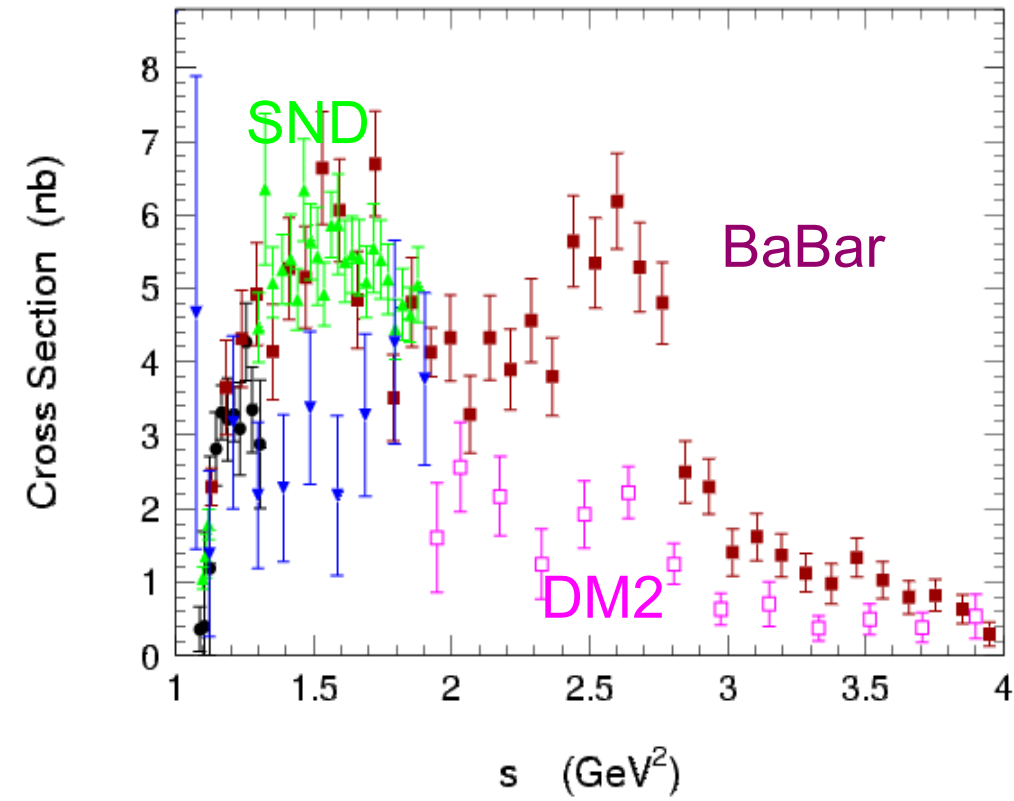
[Czyż, Kühn, Nowak, GR EPJC35(04)527]

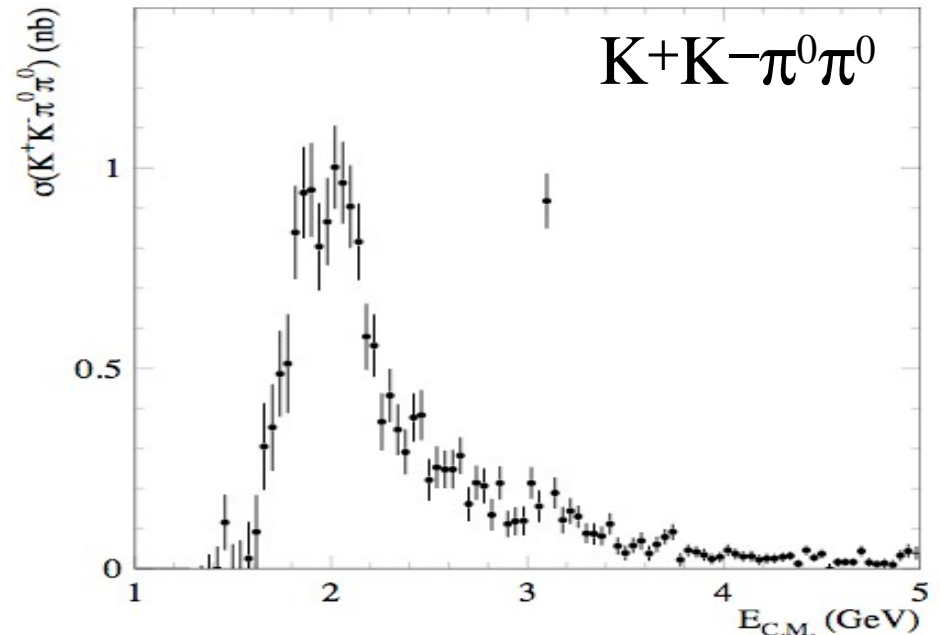
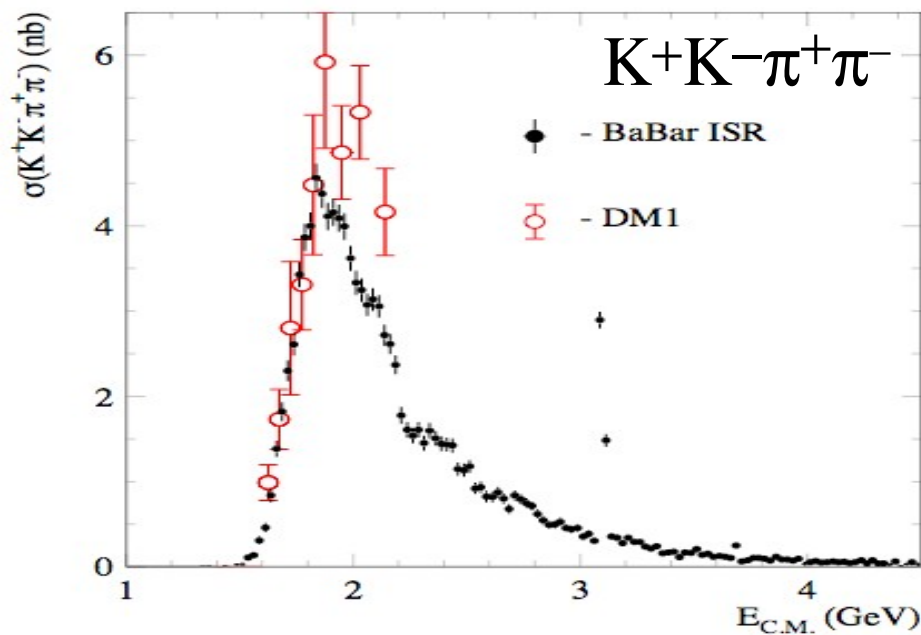
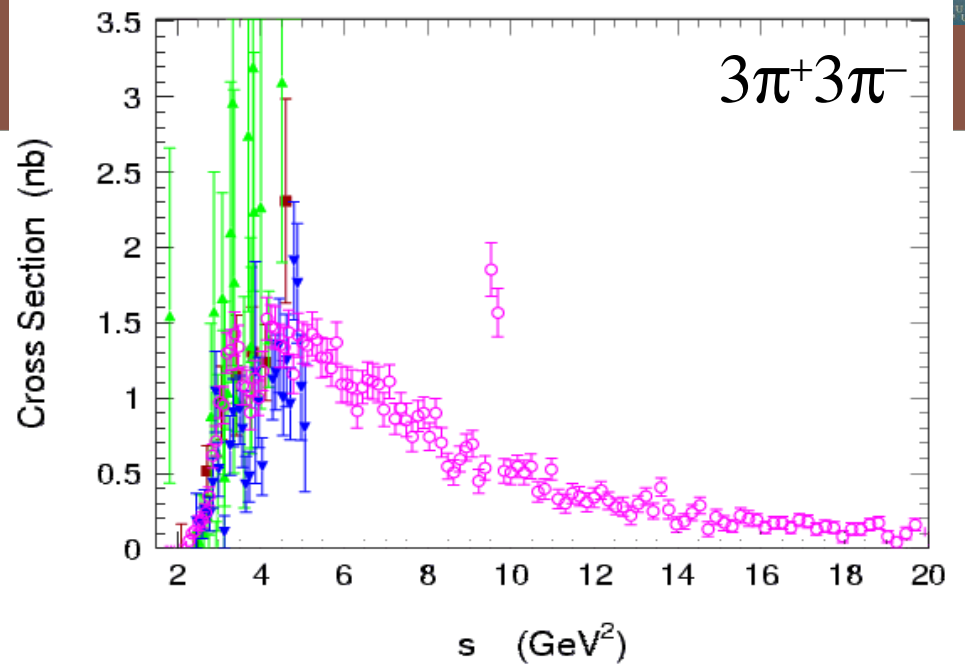
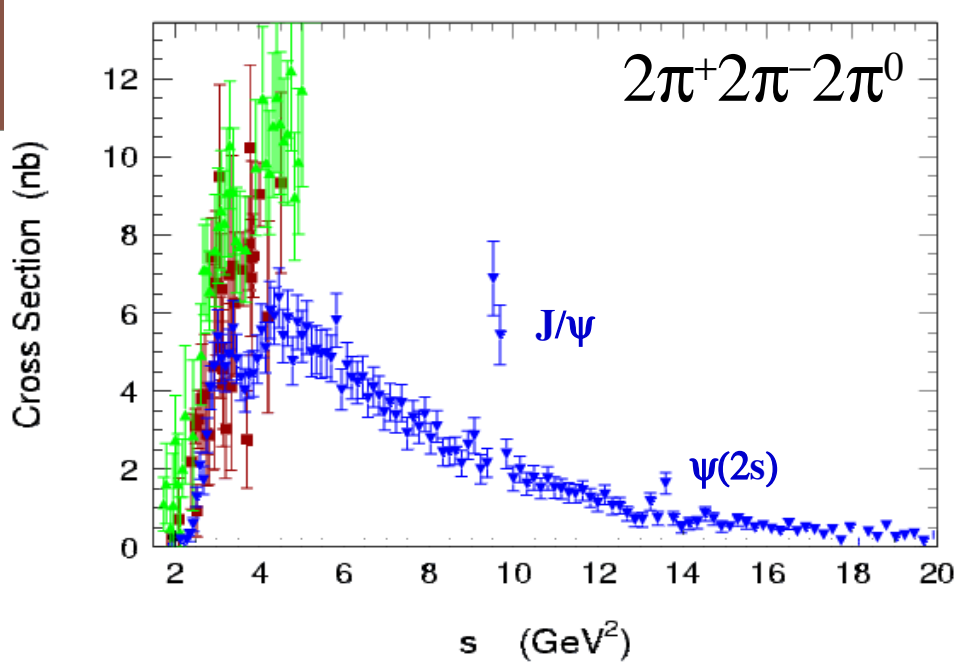
relative phase between G_E and G_M requires access to Nucleon spin



$\pi^+\pi^-\pi^0$

$2\pi^+2\pi^-$



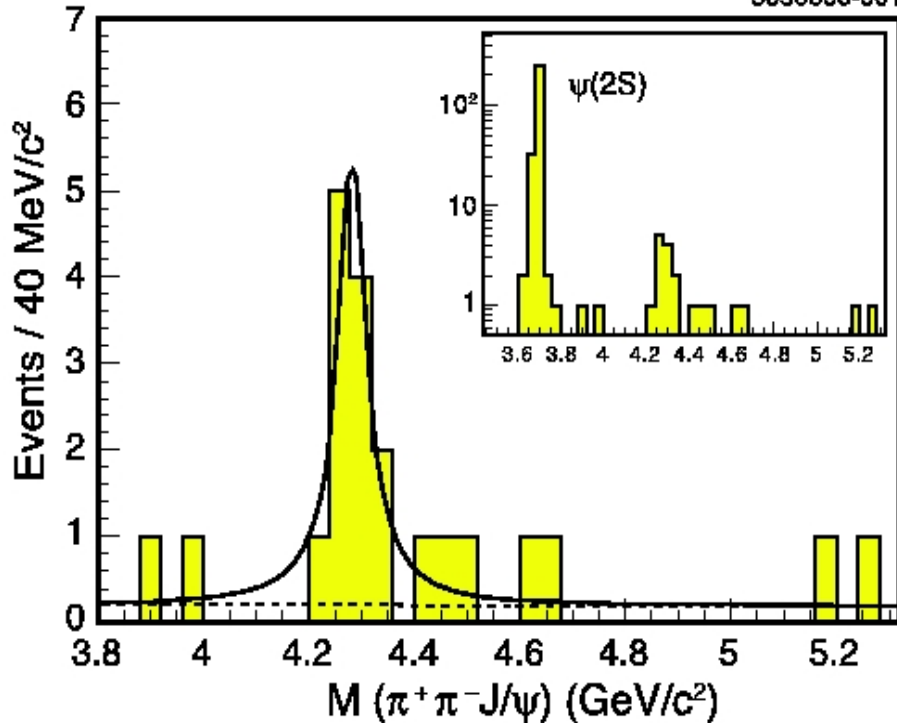


errors are statistical only
 systematic errors 5-15% (25% for $K^+K^-K^+K^-$)

Y(4260) resonance

CLEO PRD74(2006)091104

3850606-001



$$M_{Y(4260)} = 4284^{+17}_{-16} (stat) \pm 4 (syst) \text{ MeV}$$

$$\Gamma_{Y(4260)} = 73^{+39}_{-25} (stat) \pm 5 (syst) \text{ MeV}$$

New vector resonance with $J^{PC}=1^{--}$

First reported by BaBar
PRL95(2005)142001

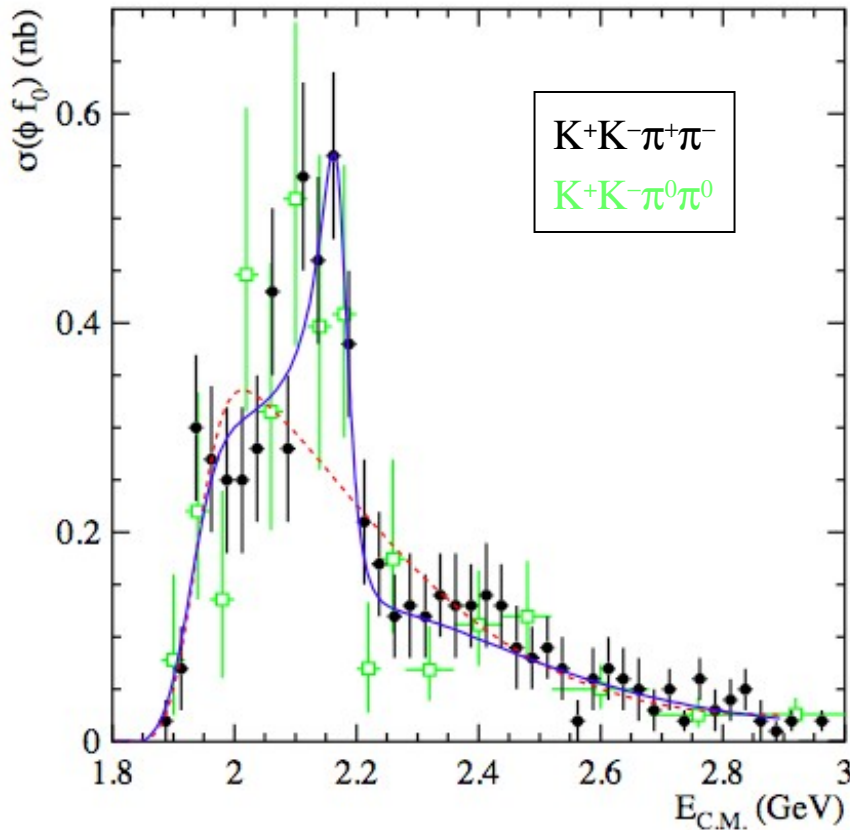
$$M_{Y(4260)} = 4259 \pm 8 (stat)_{-6}^{+2} (syst) \text{ MeV}$$

$$\Gamma_{Y(4260)} = 88 \pm 23 (stat)_{-4}^{+6} (syst) \text{ MeV}$$

no evidence in $e^+e^- \rightarrow p\bar{p}\gamma$
BaBar PRD73(2006)012005

Theoretically challenging (not predicted by theoretical calculations of charmonium spectra)

A structure at 2175 MeV in $e^+e^- \rightarrow \Phi f_0(980)$



BaBar PRD74(2006)091103

another vector resonance
with $J^{PC}=1^{--}$

$$M_X = 2175 \pm 10 \pm 15 \text{ MeV}$$

$$\Gamma_X = 58 \pm 16 \pm 20 \text{ MeV}$$

No $Y(4260)$ signal

- **radiative return:** not only hadronic cross-section and $(g-2)_\mu$ but also valuable information on hadronic physics
- **statistics** is not an issue at flavour factories (Super B) but **systematics**
- Many exclusive channels at **B-factories at 5-15% accuracy and new resonances**
- for measurements aimed at **few %**
NLO event generators (PHOKHARA) are mandatory
J/Ψ and Ψ(2S) simulations coming soon