

HELAC-Onia

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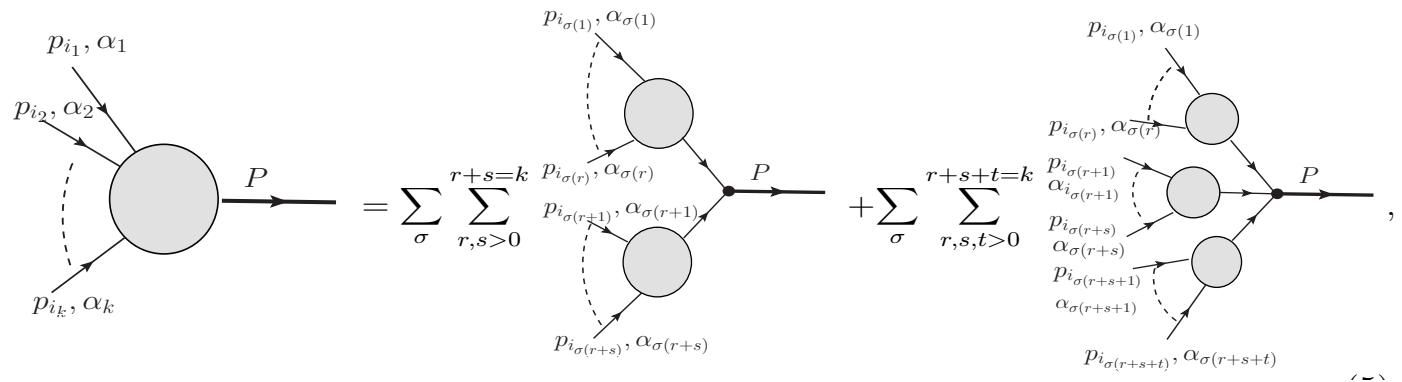
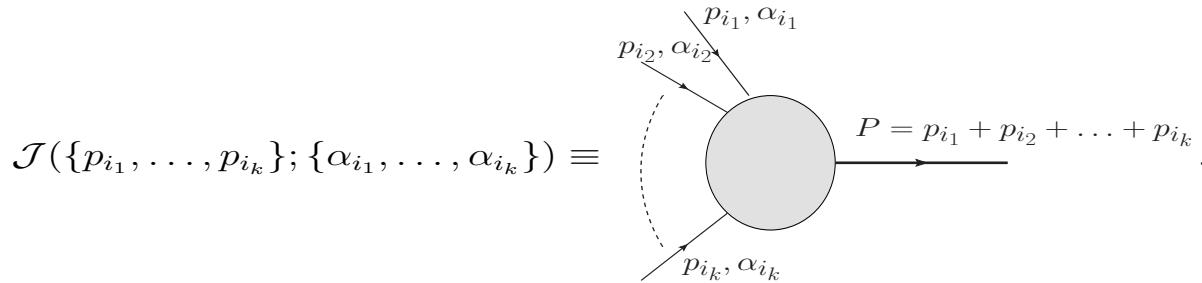
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HELAC-Onia framework

HELAC-Onia in a nutshell

- **HELAC** generates the QCD and EW amplitudes at the **partonic** level based on Dyson-Schwinger equations. *A. Kanaki, C.G.Papadopoulos (2000)*
C.G.Papadopoulos, M.Worek (2006)
- **PHEGAS** generates **partonic** level events with multi-channel techniques. *C.G.Papadopoulos (2000)*
- **Onia** generates **hadronic** (or **quarkonium**) level helicity amplitudes and physical observables based on the factorization of non-relativistic quantum chromodynamics.

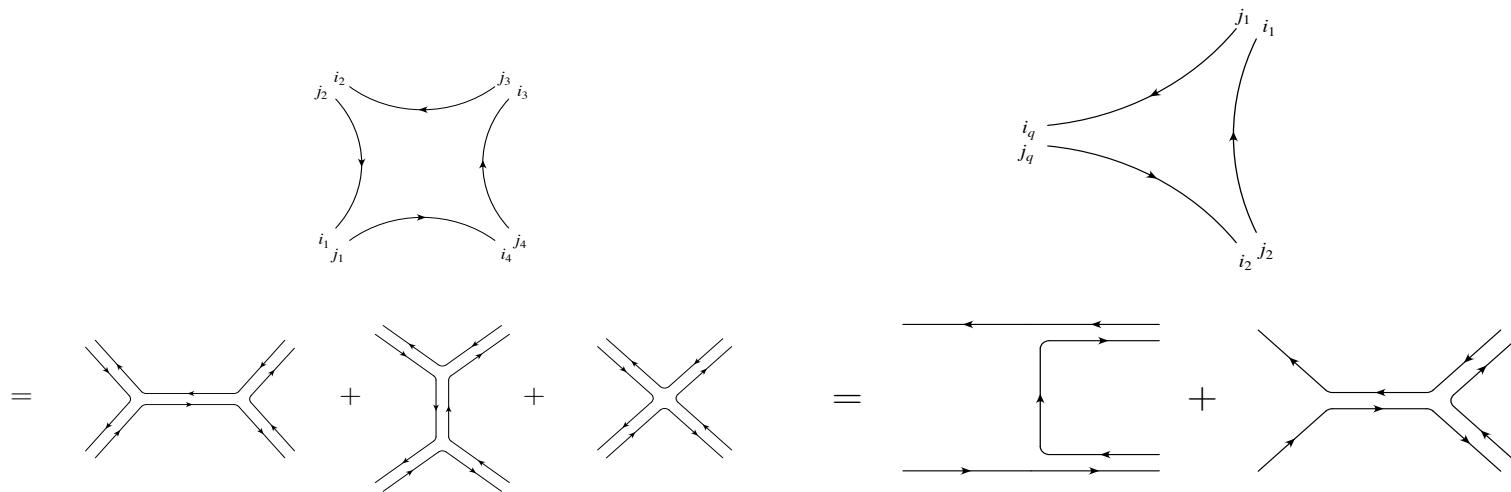
recursion relation



Generalization of Berends-Giele recursion relation !!!

color decomposition

- N particle amplitudes can be decomposed as $A_N = \sum C_i A_N^i$, where $C_i = \delta_1^{\sigma_i(1)} \delta_2^{\sigma_i(2)} \dots \delta_n^{\sigma_i(n)}$ ($n \leq N$) . The final color matrix is $M_{ij} = \sum C_i C_j$, and the final square of amplitudes is $A_N A_N^* = \sum_{i,j} M_{ij} A_N^i A_N^{j*}$ (color flow basis).
- For illustration: 1) $g g > g g$ 2) $q q^\sim > g g$



Quarkonium amplitudes

- In NRQCD factorization,

$$\sigma(pp \rightarrow Q + X) = \sum_{i,j,n} \int dx_1 dx_2 f_{i/p}(x_1) f_{j/p}(x_2) \hat{\sigma}(ij \rightarrow Q\bar{Q}[n] + X) \langle \mathcal{O}_n^Q \rangle,$$

- Projection method is used to constrain the spin and color quantum number of heavy quark pair in its short distance coefficient.
- P-wave currents are introduced in order to calculate helicity amplitudes of P-wave fock states.

More technical details are presented in arXiv:1212.5293

What could HELAC-Onia do ?

- Multi heavy quarkonium, including Bc system, production at the pp(p^\sim) and e+e- colliders.
- Multi P-wave heavy quarkonium production at the pp(p^\sim) and e+e- colliders.
- Fully differential distributions calculations.
- Spin density matrix elements in helicity frame, Collins-Soper frame, Gottfried-Jackson frame and target frame.
- EW particles with complex mass scheme and jets with inclusive kT clustering procedure.
- LHE files can be generated with modified PHEGAS.



First step to full NLO automation !!!

Benchmark processes

[arXiv:1212.5293](https://arxiv.org/abs/1212.5293)

- B_c meson production at the LHC.
- Charmonium production at B factories. Single charmonium and double charmonium production.
- Double quarkonia production at hadron colliders.
- Hadroproduction of quarkonia in association with a heavy quark pair.
- Spin density matrix and polarization.

Application

How to use HELAC-Onia?

- 1.Specify input parameters in user.inp following the format in default.inp.
- 2.Provide process information in process.inp.
- 3.Compile with the command line:
 > make
- 4.Run with the command line:
 > ./Helac-Onia
- 5.If one wants to remove the output files, object files and executable files, run the command line:
 > make clean

An example

- If we want to calculate

$$e^- e^+ \rightarrow \eta_c (^1 S_0^{[1]}) ggg$$

- Specify the process information in process.inp:

6 ← Total number of external legs nhad=6

2 -2 441001 35 35 35 ← Ids for the process

nhad ← comments

... ←

An example

- Choose input parameters in user.inp:

```
colpar 3 # 1=pp,2=ppbar,3=e+e-
energy 10.6d0 # cms energy
qcd 4 # qcd and qed
alphasrun 0 # running alphas (1) or not (0)
cmass 1.5d0 # mass of charm quark
# e+e- cutoff
cutoffe 1.0d-10 # cutoff (e+e- case)
minenl 0d0 # minimum lepton energy
minenq 0d0 # minimum quark energy
minangll 0d0 # minimum angle l-l
minanglq 0d0 # minimum angle l-q
minangqq 0d0 # minimum angle q-q
minmqqe 0d0 # minimum mass q-q (e+e-)
unwgt T # unweighting on/off
alphas2 0.26d0 # fixed value of alphas
alphaem 0.00729927d0 # alphaem value
```

```
preunw 10000 # n. of pre-unw events
unwevt 100000 # n. of unw events
nmc 100000 # number of MC interation
nopt 10000 # opti parameteter
nopt_step 10000 # opti parameter
optf 1 # opti parameter
maxopt 8 #opti parameter
noptlim 100000 # opti parameter
iopt 1 # opti parameter
alimit 0 # lower limit of alpha(i) in mul-cha
gener 0 # 0 PHEGAS 1 RAMBO 3 VEGAS
ranhel 3 # MC over helicities
ptdisQ F # don't calculate pt distribution
Scale 0 # 0=fixed scale
FScaleValue 5.3d0 # the value of fixed scale
LDMEmc1S01 0.0645d0 # 0.387/2/Nc
```

An example

- Run ./Helac-Onia. Two useful output files generated:
RESULT_eebaretac1ggg.out,sampleebaretac1ggg.lhe
(only when unwgt=1 and gener=0).

RESULT_eebaretac1ggg.out

```
...
average estimate : 0.373070D-05
          +/- 0.200429D-07
variance estimate: 0.401719D-15
          +/- 0.559955D-17
out of      100000      100001 points have been used
and      100001 points resulted to =/= 0 weight
whereas      0 points to 0 weight
```

total sigma (nb) = 0.373070D-05 +/- 0.200429D-07

% error: 0.537244D+00

lwri: number of points have used 8931.000000000000
The Timing Consuming in Phase Space Integration is:
0 h; 4 m; 11 s; 38 centi s

sampleebaretac1ggg.lhe

```
<LesHouchesEvents version="1.0">
<!--
File generated with HELAC_PHEGAS_ONIA
-->
<init>
11 -11 5.300000E+00 5.300000E+00 -1 -1 \
-1 -1 3 1 3.7306977547E-03 2.004293 \
5975E-05 1.0000000000E+00 81
</init>
<event>
...
```

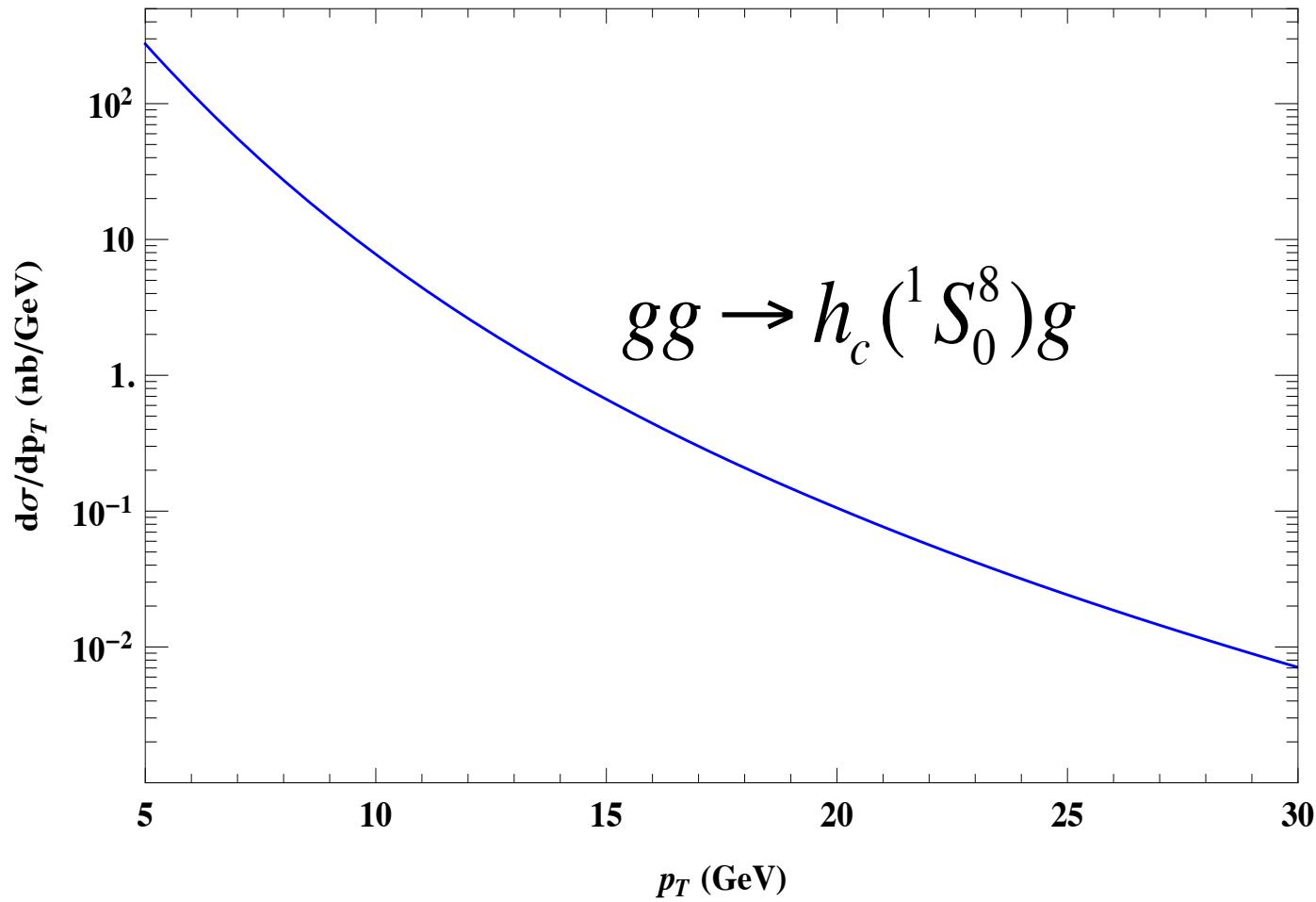
ηc and hc

- From above example, it is quite easy for one to calculate ηc and hc production rate at the LHC. The fock states up to $O(v^7)$ for ηc are ${}^1S_0^{[1/8]}, {}^3S_1^{[8]}, {}^1P_1^{[8]}$, and for hc are ${}^1S_0^{[8]}, {}^1P_1^{[1]}$.
- For example, I recalculated the dominant sub-channel $gg \rightarrow h_c({}^1S_0^8)g$ use the the same input parameters (except using **CTEQ6L1**) as in arXiv:0904.0726 (others see C.-F.Qiao's talk),

$$m_c = 1.78 \text{GeV}, \mu = \sqrt{4m_c^2 + p_T^2}, |\eta(h_c)| < 2.2,$$

$$\langle O^{h_c}({}^1S_0^{[8]}) \rangle = 9.8 \times 10^{-3} \text{GeV}^3, \text{CTEQ6L1}$$

ηc and hc



Close words

- The program is available at
<http://helac-phegas.web.cern.ch/helac-phegas> .
- If you have any questions about HELAC-Onia,
please don't hesitate to contact me:
erdiesshaw@gmail.com
- **Thanks for your attention !!!**