

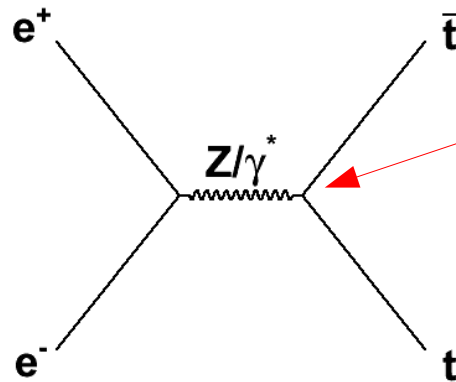
Top quark physics at lepton colliders

**Input from theorists +
further studies of $e^+e^- \rightarrow 6$ fermion composition**

IFIC-LAL, feb 2013

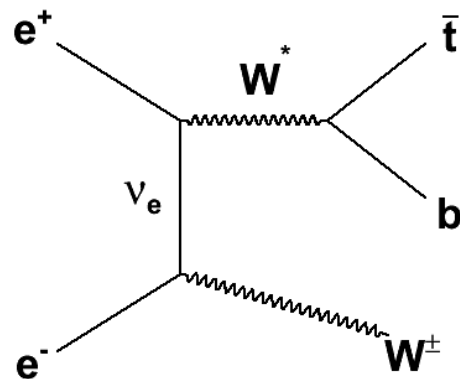
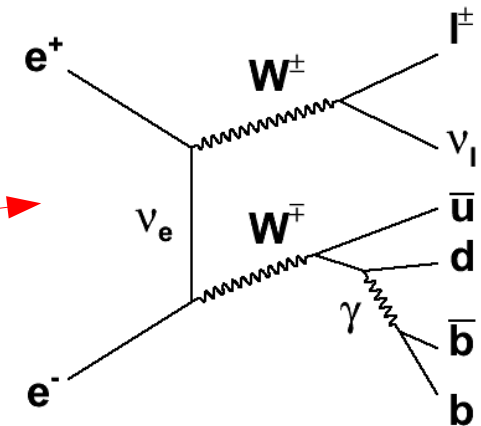
*M. Vos
(IFIC Valencia)*

Fundamental issues: The good, the bad and the ugly



This is the vertex we want to probe

This is a background we can reduce



This is a problem

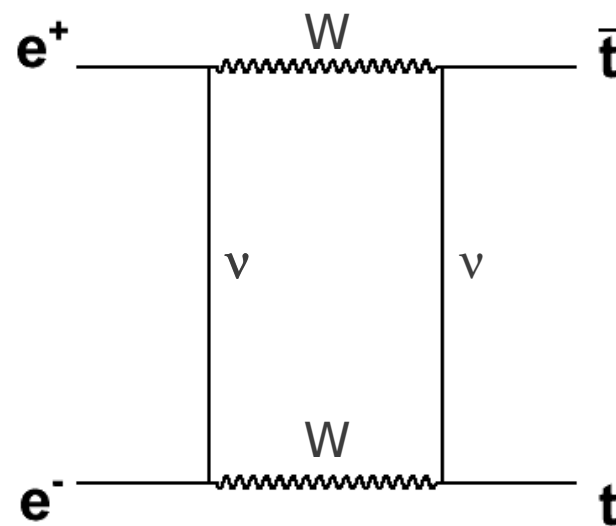
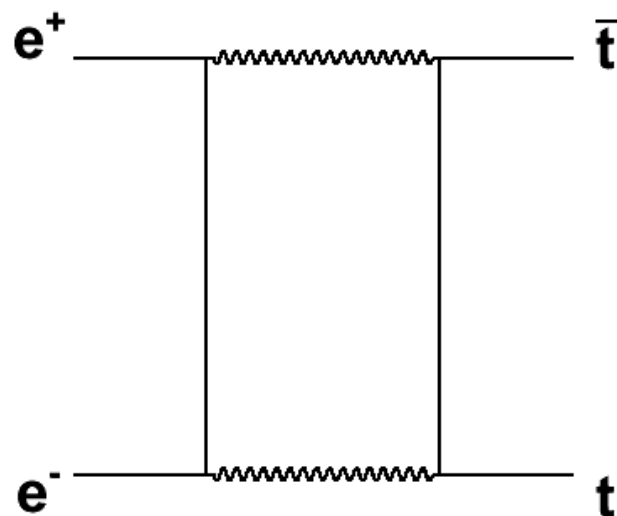
Fundamental issues...

German Rodrigo: at the next order further diagrams become important

These involve higher orders of the $t\bar{t}\gamma$ and $t\bar{t}Z$ vertices we're after... mixing the two sets of form factors for $t\bar{t}\gamma$ and $t\bar{t}Z$

And, unwanted (Wtb) vertices appear...

Is it sufficient to say that the anomalous couplings are small to make the couplings squared negligible?



Pedro Ruiz Femenia (a student of Toni Pich, and with some help from Germán Rodrigo) has evaluated the existing EW and QCD corrections, trying to come up with error estimates for the current state-of-the-art calculations...

Note that: the errors he estimates do not necessarily limit the ILC potential. Often, great progress can still be made at a relatively small cost (and will certainly be made as soon as the project is approved).

1/ Axial part (of the Z) not included in cross-section estimates. If needed, they can be included; they are available at N³LO.

2/ Results obtained last Friday. A cross-check is needed if we're to use any of these results.

3/ Pedro used a top quark mass $m_t=172$ GeV, defined in the on-shell scheme (pole mass).

Important sources:

Kiyo, Maier, Maierhöfer, P. Marquard, arXiv:0907.2120, 3 loops

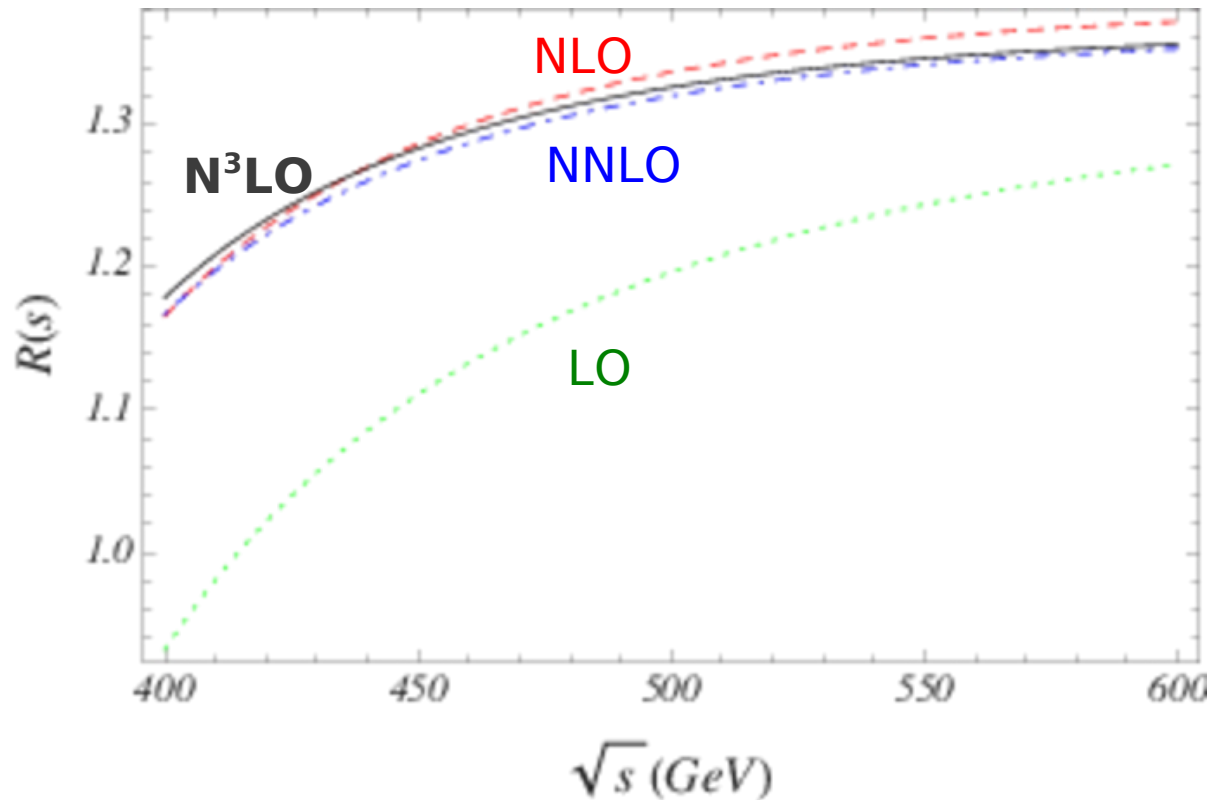
Hoang, Mateu, Zebarjad, Nucl. Phys. B 813 (2009) 349-369, 2-loops

Bernreuther, Bonciani et al., hep-ph/0604031

Theory input

QCD corrections to $e^+e^- \rightarrow t\bar{t} + X$, known up to $O(\alpha_s^3)$ (3-loops), in an expansion in m_t^2/q^2 with enough terms to be valid at $\sqrt{s} = 500$ GeV

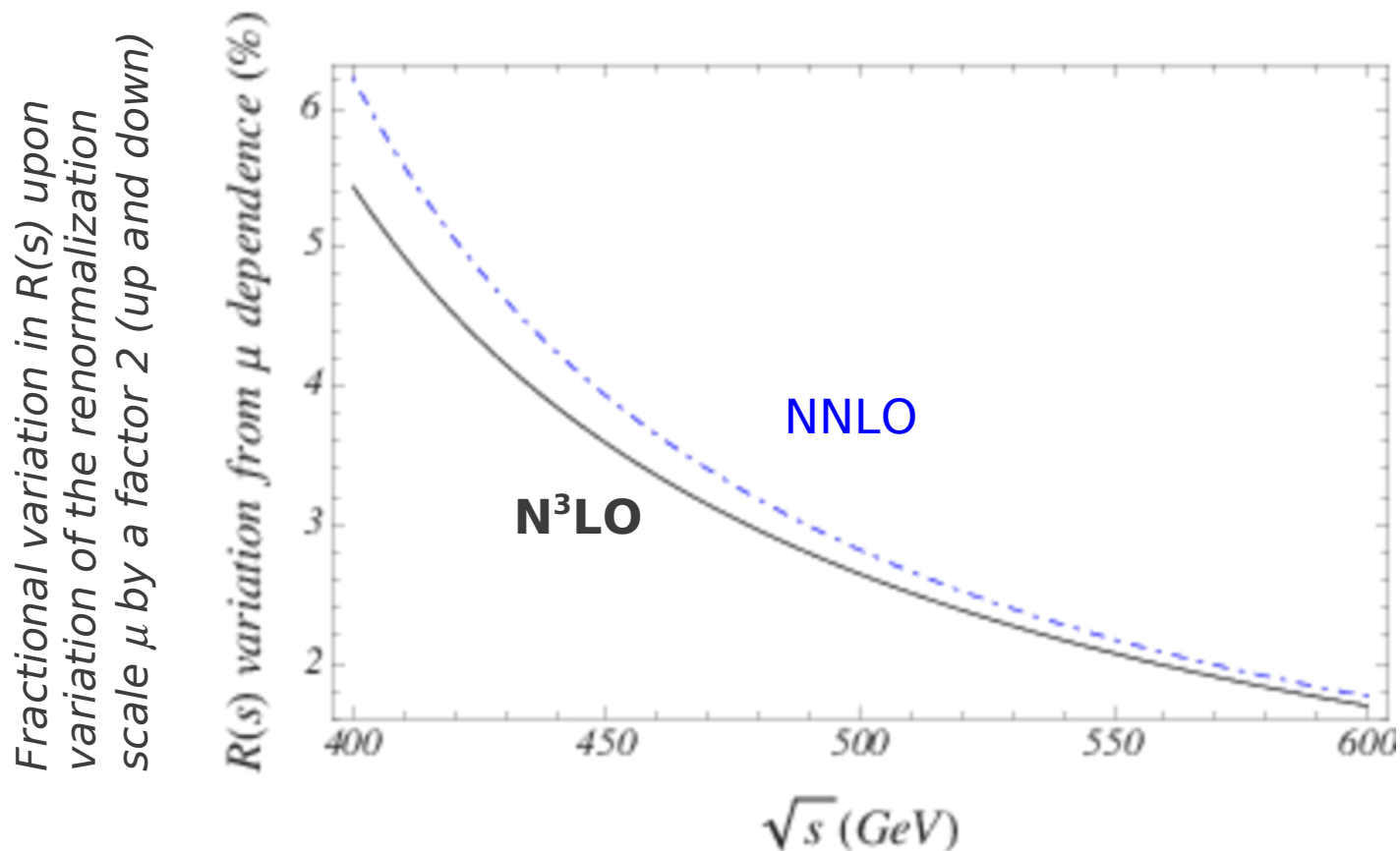
$R(s)$ = cross-section normalized to
x-sec for massless fermion



Theory input

Error estimate from scale variations: 2-3 %
(less if we run at larger center-of-mass energy)

Assigning this as the x-sec error would be very conservative...

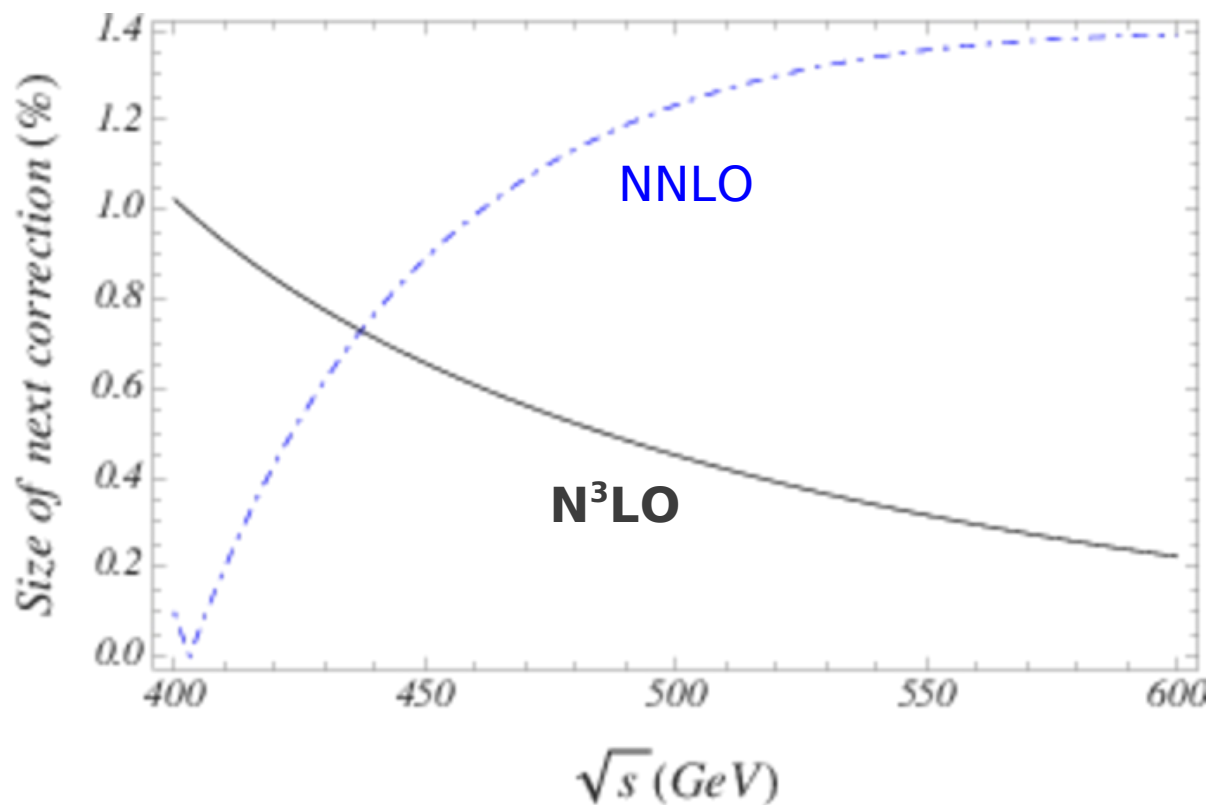


Theory input

Error estimate by comparing size of subsequent corrections in the perturbative series

LO → NLO: ~13 %
NLO → NNLO: ~1.5 %
NNLO → N³LO: ~0.5 %

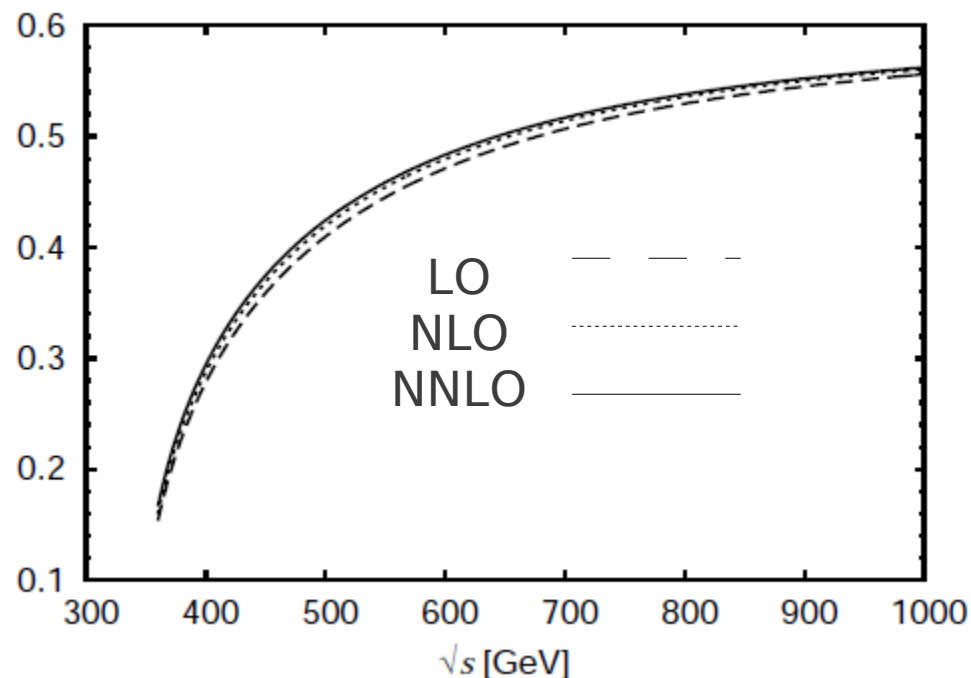
$$\frac{(R(s)^{\text{NNLO}} - R(s)^{\text{NLO}})/R(s)^{\text{NLO}}}{(R(s)^{\text{N}^3\text{LO}} - R(s)^{\text{NNLO}})/R(s)^{\text{NNLO}}}$$



Theory input

What about A_{FB} ?

Order α_s^2 results in
Bernreuther, Bonciani et
al., hep-ph/0604031



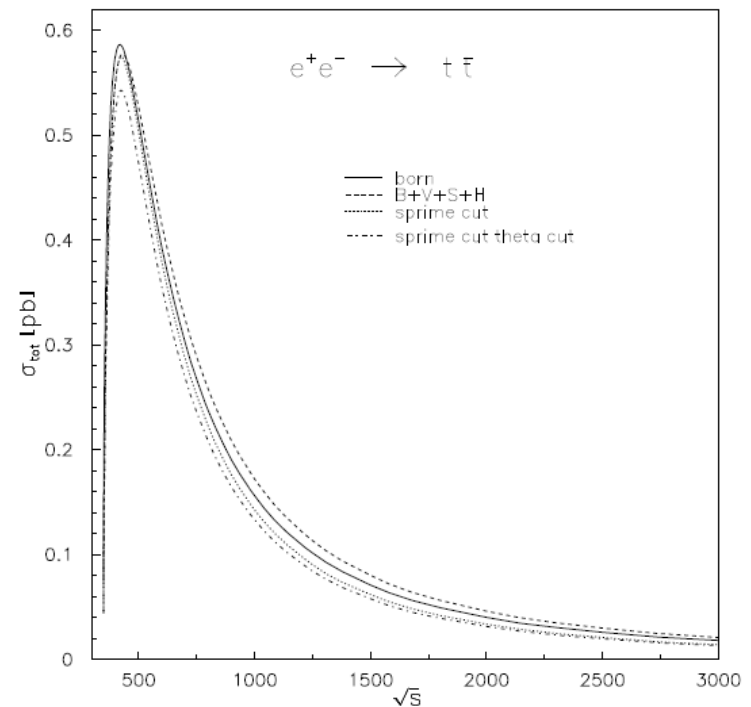
“... we conclude that the 2-parton QCD corrections to the lowest order asymmetry are moderate to small for $\sqrt{s} > 400$ GeV”

Scale variations yield $<1\%$ error @ NNLO

Theory input

EW correction to cross-section
are $\sim 3\%$ at $\sqrt{s} = 500$ GeV

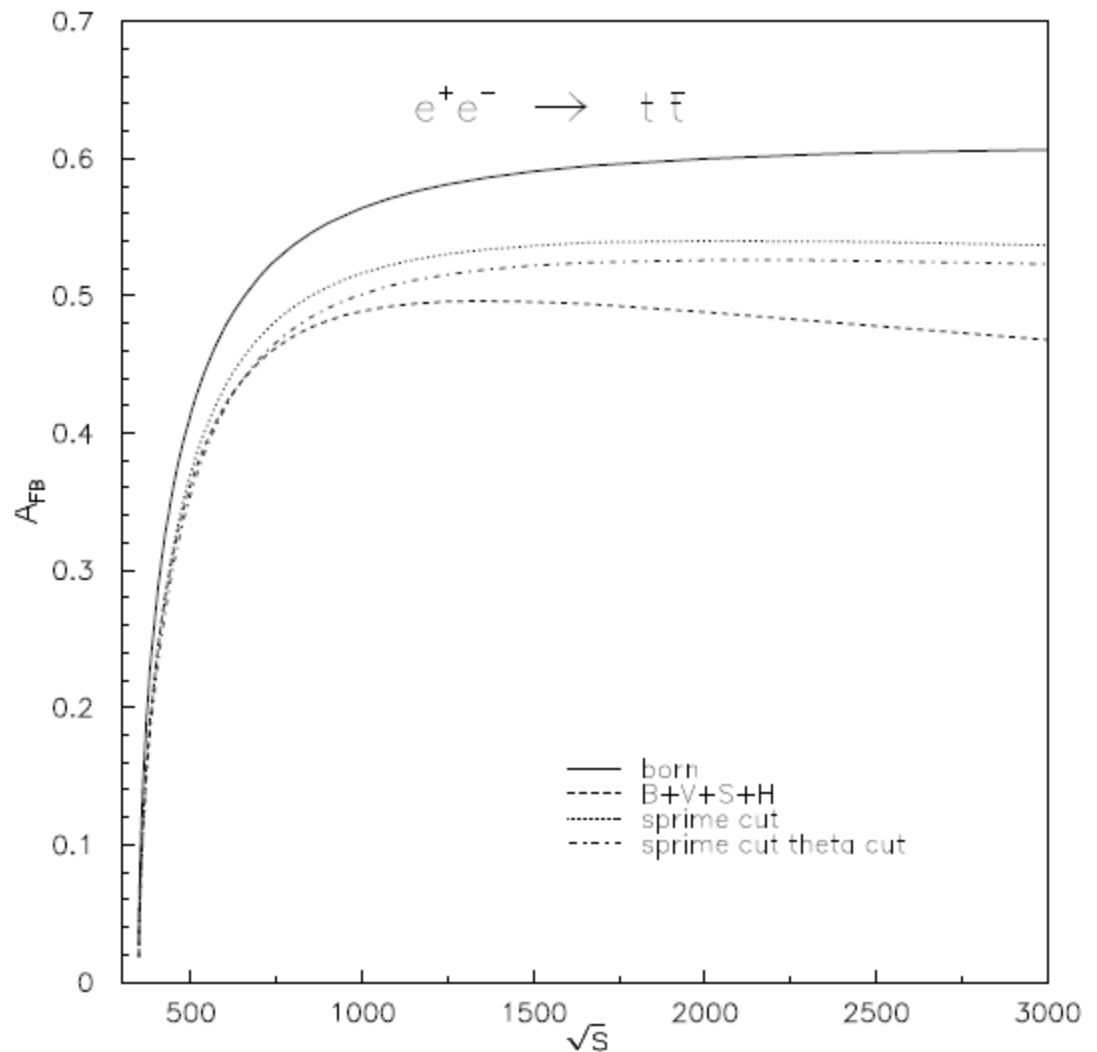
EW corrections from the decay
 $t\bar{t} \rightarrow bWbW \rightarrow$ six fermions
are expected to be order $\Gamma_t/m_t \sim 1\%$
Not calculated for e^+e^- , but they do
exist for (the more complicated
case of) hadron collider production



Electroweak corrections
Glover et al. hep/ph04010110
Fleischer et al. hep/ph0302259

Theory input

EW correction to forward-backward asymmetry are $\sim 20\%$ at $\sqrt{s} = 500$ GeV



Summarizing:

- Form factors are well-defined for LO. A more complex situation arises when interfering diagrams for the same six-fermion final states are considered, or higher orders are included...
- QCD calculations are available to α_s^3 . For x-sec and α_s^2 for A_{FB} .
 $A \sim$ rigorous error estimate yields acceptably small errors.
- Electroweak corrections are available. Effects are sizable, but expect next order correction to be much smaller... Contacted Jos Vermaseren to see if we can get an error estimate.
- Corrections to decay have been calculated, but not yet evaluated. Error order 1%.

Proposal: get Pedro Ruiz to write a section “Theory state-of-the-art”

Problem I

WHIZARD generates $e^+ e^- \rightarrow b \bar{b} l \nu j j$

Includes the good, the bad and the ugly
Interference taken into account

Unpolarized cross-sections according to MadGraph

tt production (2 diagrams) : 29 fb

6-fermion production (250 diagrams) : 30 fb

The Barklow criterion allegedly considers events with two on-shell top quarks only ($|m_{bW} - m_t| < 5 \Gamma_t$) $m_t = 174$, $\Gamma_t = 1.5...$

According to Nacho we discard:

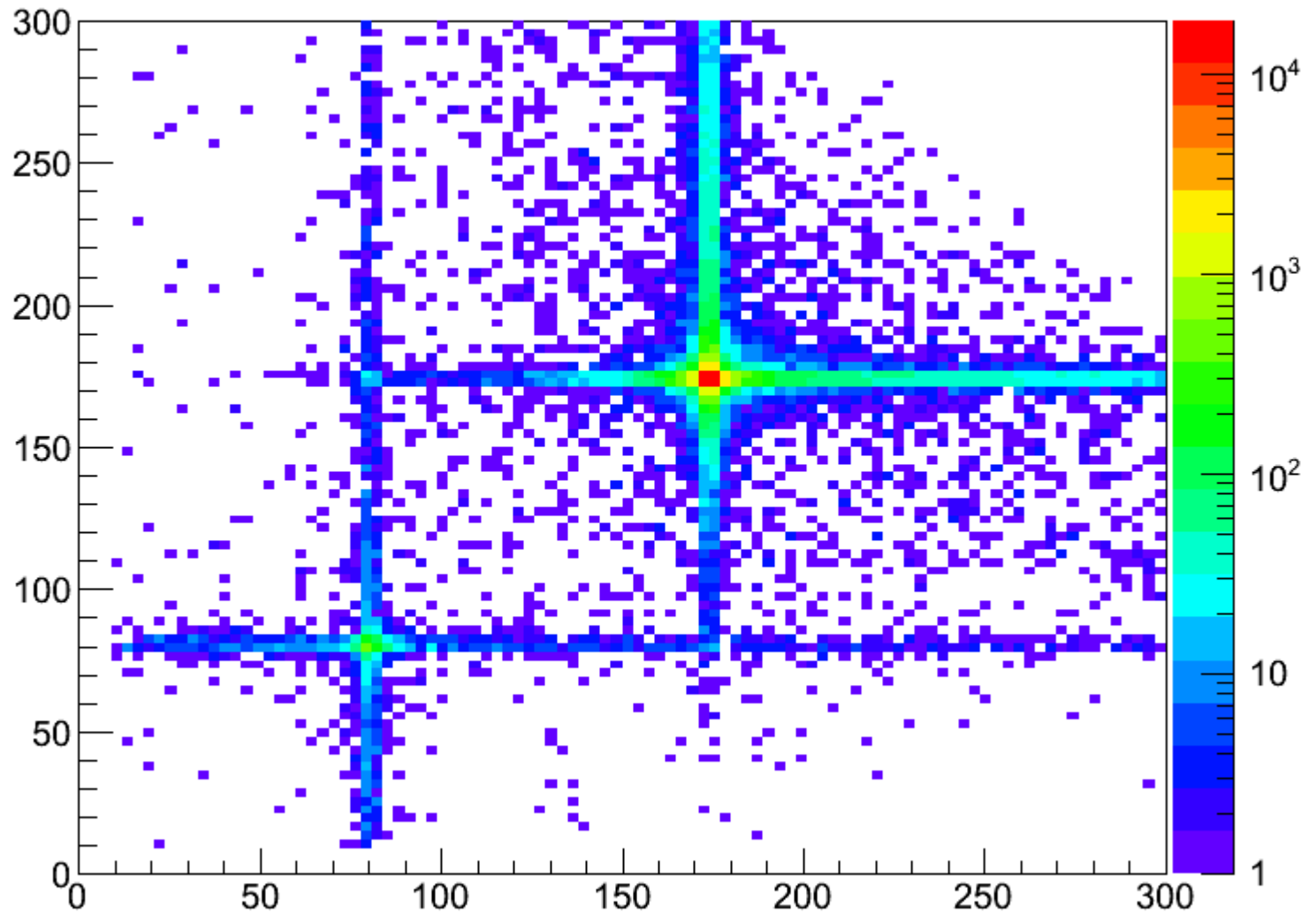
30 % of L-handed events

24 % of R-handed events

Disclaimer: what we call the Barklow criterion was never intended to be used as such by Tim Barklow!!!

Top candidate mass distributions

Running over 108.800 Left-handed events



Problem I

A practical issue: how do we define our $e^+e^- \rightarrow t\bar{t}$ sample?

Running over 108.800 Left-handed events

Apply criterion on N-tuple: $|m_{bW} - m_t| < 5 \Gamma_t$

Loose definition: $|m_{bW} - m_t| < 10 \Gamma_t$

Barklow/IsTTbarEvent: 75635 \rightarrow 69.5%

Mass criterion on N-tuple: 86721 \rightarrow 79.7%

Loose criterion: 93081 \rightarrow 85.6%

I create a cleaner criterion based on:

- the loose mass constraints
- energy of top and anti-top < 251 GeV
- E_b in top frame < 90 GeV

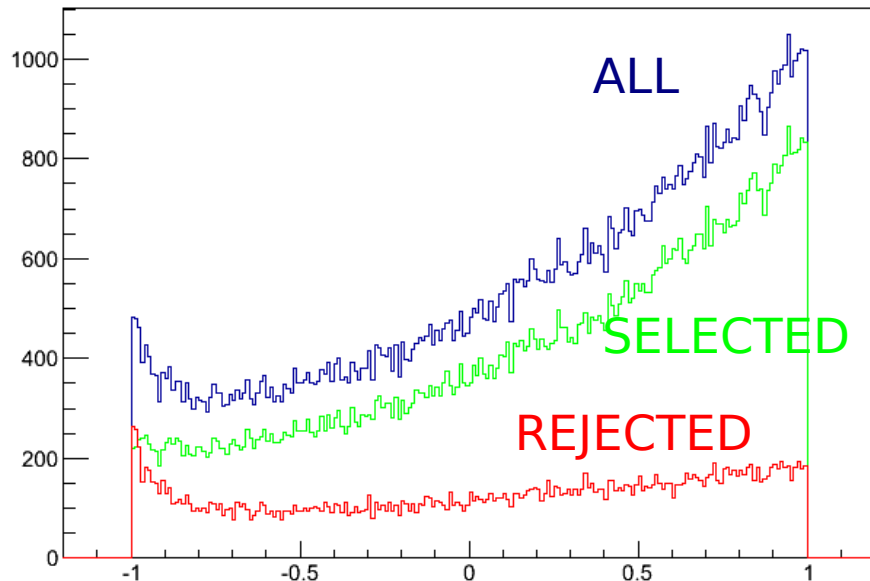
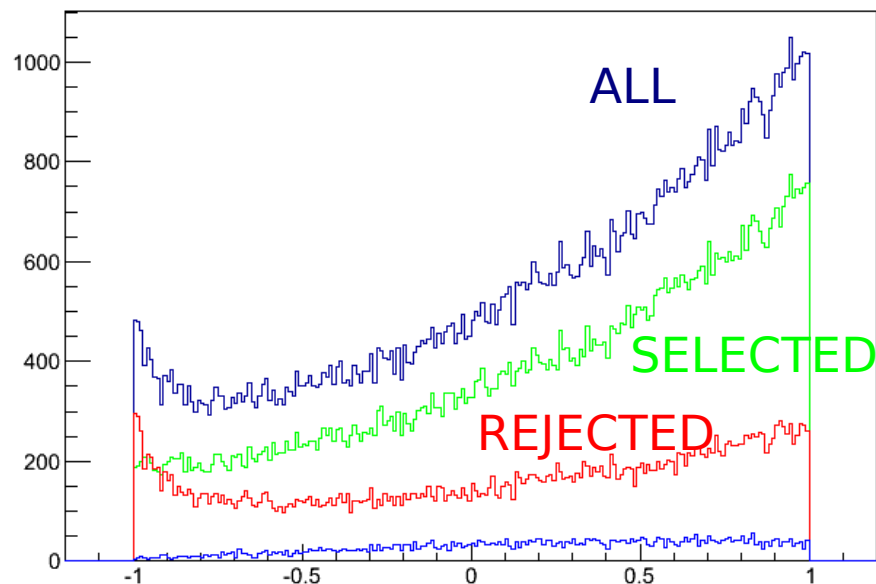
This select 76% of events

I find that the overlap with Barklow is imperfect... only 93% of events that meet the isTTbarEvent also make the new criterion \rightarrow is the sample contaminated with non- $t\bar{t}$ bar events?

FB asymmetry

Both criteria reject the background with the obviously wrong shape

Barklow accepts some more (light blue) and rejects some more



MadGraph unpolarized

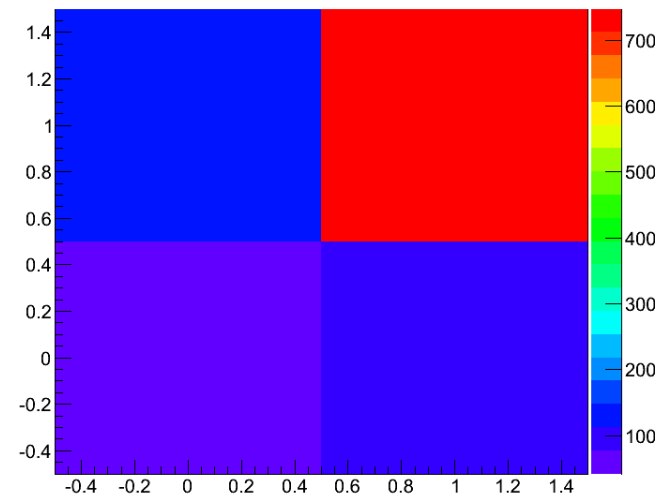
Ttbar : 75 %
Single top : 20 %
Others : 4.2 %

Not too dissimilar from
the previous results

On-shell
anti-top?

YES

NO



NO

YES

On-shell top?

Polarized x-sections

Unpolarized:

total	->	564.2 fb	
ttbar through gamma	->	422.5 fb	
ttbar through Z	->	96.1 fb	
WW* nu-exchange	->	24.7 fb	92%
WW* through Z	->	11.5 fb	
WW* through gamma	->	9.1 fb	

P: +30%, -80%

total	->	957.9 fb	
ttbar through gamma	->	669.3 fb	
ttbar through Z	->	208.2 fb	
WW* nu-exchange	->	58.3 fb	92%
WW* through Z	->	13.3 fb	
WW* through gamma	->	8.3 fb	

P: -30%, +80%

total	->	441.5 fb	
ttbar through gamma	->	376.2 fb	
ttbar through Z	->	32.5 fb	
WW* nu-exchange	->	3.4 fb	93%
WW* through Z	->	15.0 fb	
WW* through gamma	->	14.2 fb	

Strategy...

Attempts to disentangle single top and $t\bar{t}$ production seem to show this is difficult (maybe not impossible)

In any case the processes are entangled at the theory level by the interference term

Solution: measure and rate and differential distributions for the full six-fermion final state → compare this to prediction

Complicates matters:

- less experimental handles (top mass constraint)
- theory now depends on Wtb vertex in production as well
- definition of form factors

Problem II

François Richard: The gamma-gamma background is not innocuous since Jeremy finds that the top angular distribution suffers from the presence of this component for $P=-$.

Quoting the DBD:

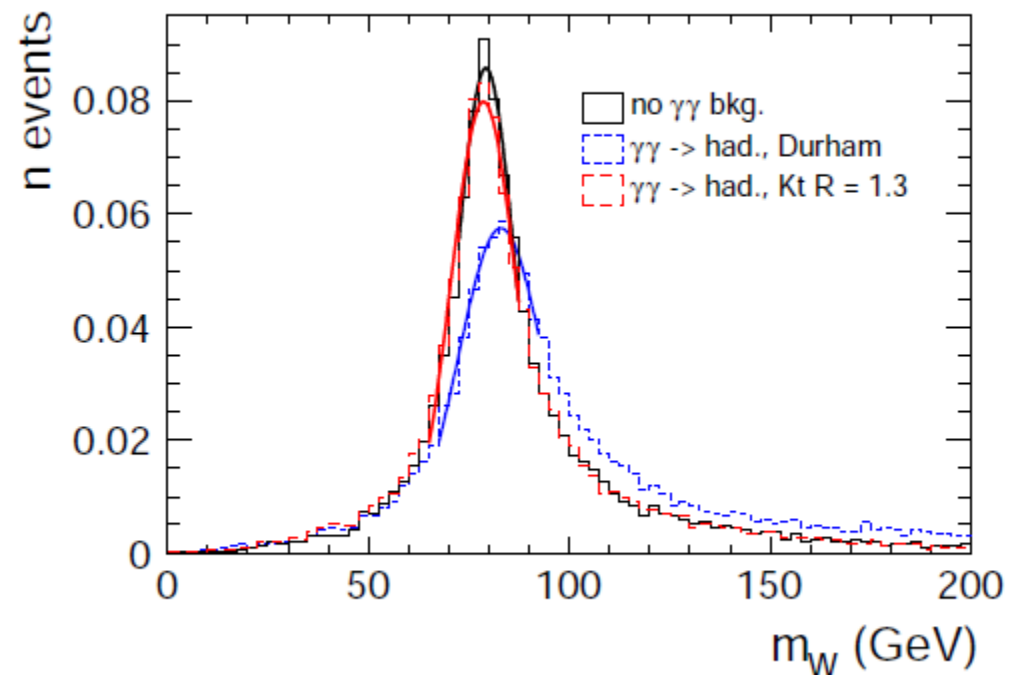
At lepton colliders exclusive jet algorithms, in which every particle is assigned to a jet have been favoured. However, at the ILC such algorithms work poorly [...] the large cross section for $\gamma\gamma \rightarrow \text{hadrons}$ implies that most interesting events will be accompanied by several unrelated “pile-up” events in the same bunch crossing.

Problem II: DBD solution

Still from the DBD:

This problem was studied at CLIC, where the pile-up conditions are much more challenging than at ILC. It was concluded that the use of inclusive algorithms, developed for hadron colliders, was well-suited to mitigate this problem.

Reconstructed di-jet
mass distribution in
 $e^+e^- \rightarrow W^+W^- \rightarrow l\nu q\bar{q}$.



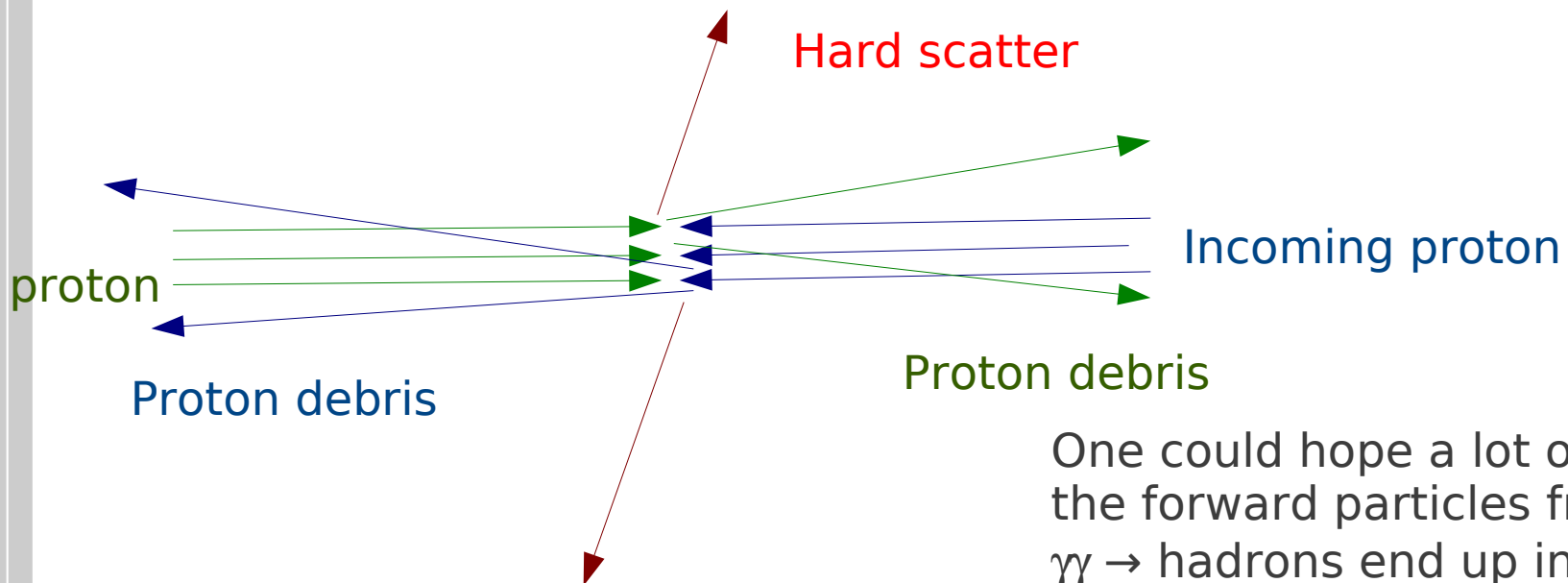
Problem II: discussion

The DBD actually uses three solutions in one go:

Exclusive jets \rightarrow inclusive jets

Durham without beam jets \rightarrow hadron collider algorithm

Distance criterion $\rightarrow k_t$

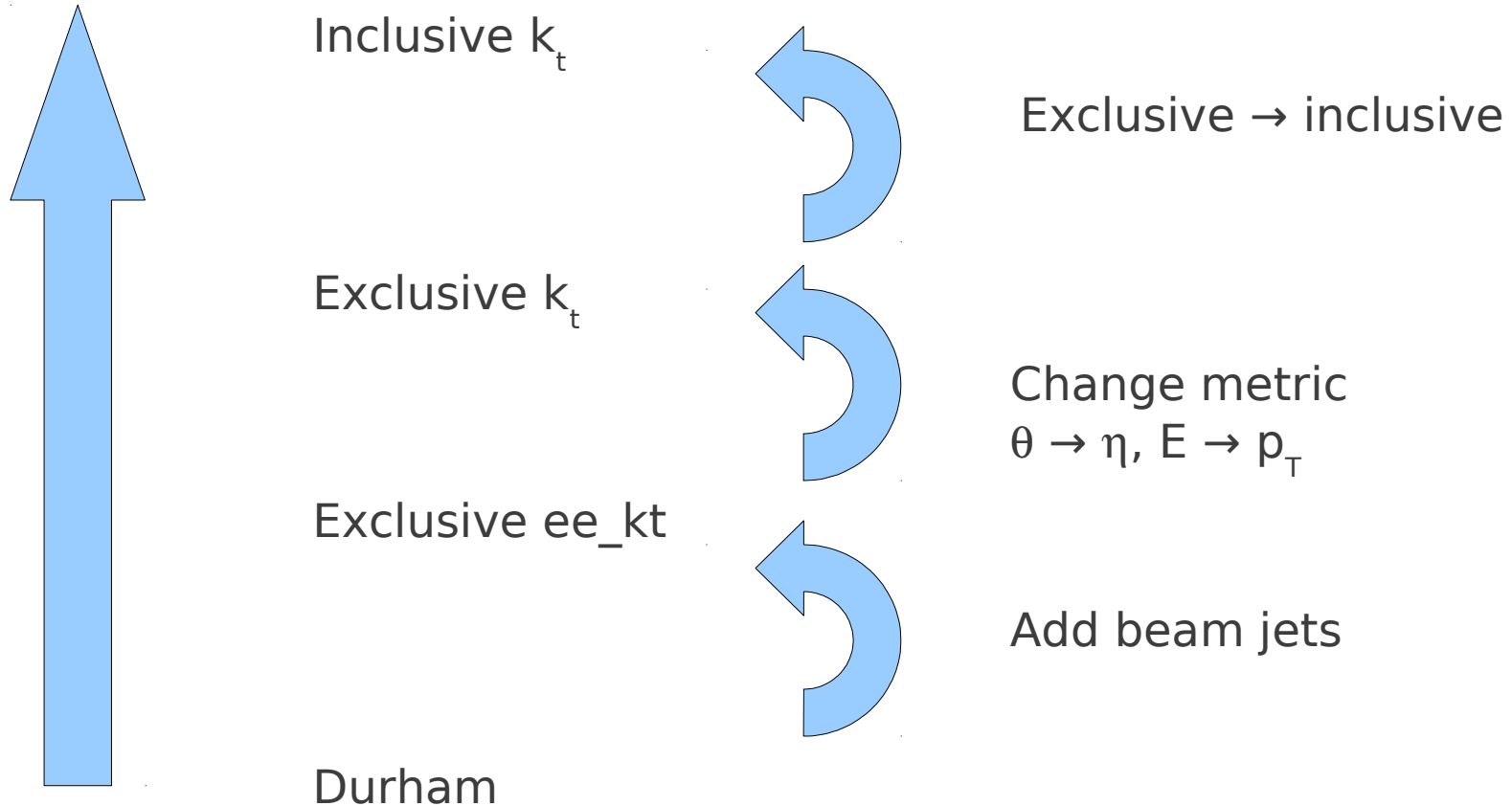


One could hope a lot of the forward particles from $\gamma\gamma \rightarrow$ hadrons end up in "beam jets"

See: FastJet user manual <http://arxiv.org/pdf/1111.6097.pdf>

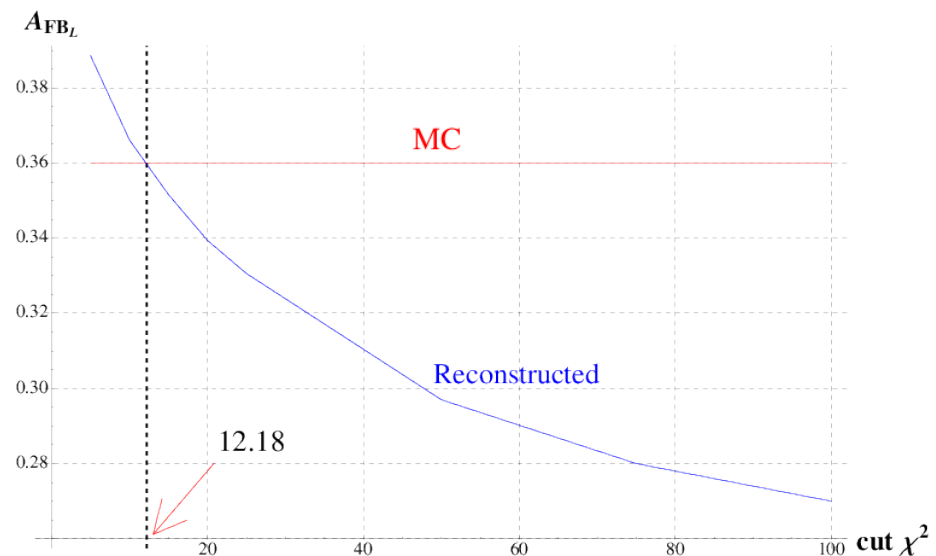
Problem II: inclusive vs. exclusive jet reco

Background resilience



Problem III

Nacho confirms the observation by François: there is a “lucky” value for The chi-squared cut



Some things that have kept us “honest” so far:

- we didn't know
- is the “lucky” chi-squared the same for both polarizations?

François proposes: What should be optimized is the differential agreement between the MC and the reconstructed angular distributions..

I'd like to know why this there is no plateau... Probably the χ^2 we find depends on the polar angle of the top quark. Is it related to problem II?

Backgrounds

$$\sigma(tt) \approx 600 \text{ fb at } 500 \text{ GeV}$$

$$L=500 \text{ fb}^{-1} \rightarrow N_{\text{total}} \sim 570 \text{ K}$$

Semileptonic $\sim 34\%$

Reducible backgrounds

WW \rightarrow no b quark

bb \rightarrow simple topology

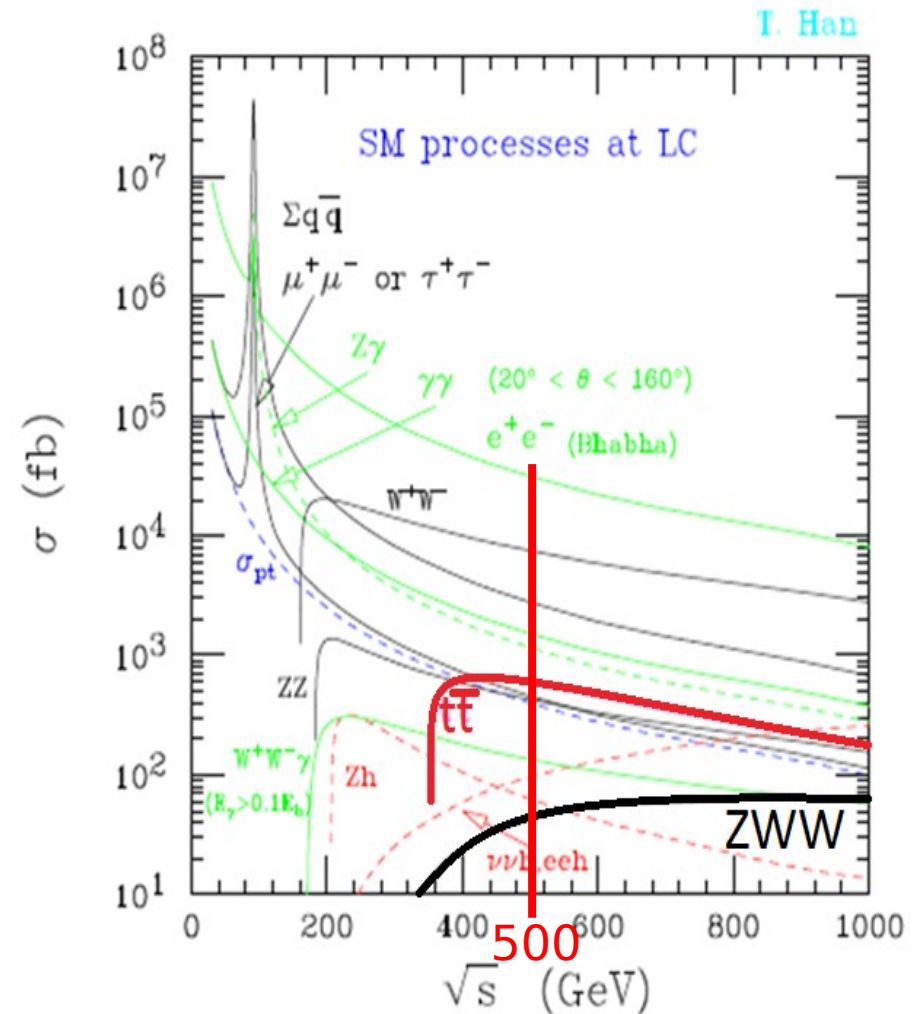
Other top decays (τ)

Irreducible:

Small but need to be subtracted

Other top decays (τ)

ZWW ($Z \rightarrow bb$) $\rightarrow 8 \text{ fb}$



Process	tt	bb	WW	ZZ	ZWW
$A_{\text{LR}} (\%)$	36.7	62.9	98.8	31.0	89

CP violating Form Factors

Nachtmann et al. gives the receipt used for the TESLA TDR

Toni Pich claims the Nachtmann paper is understandable

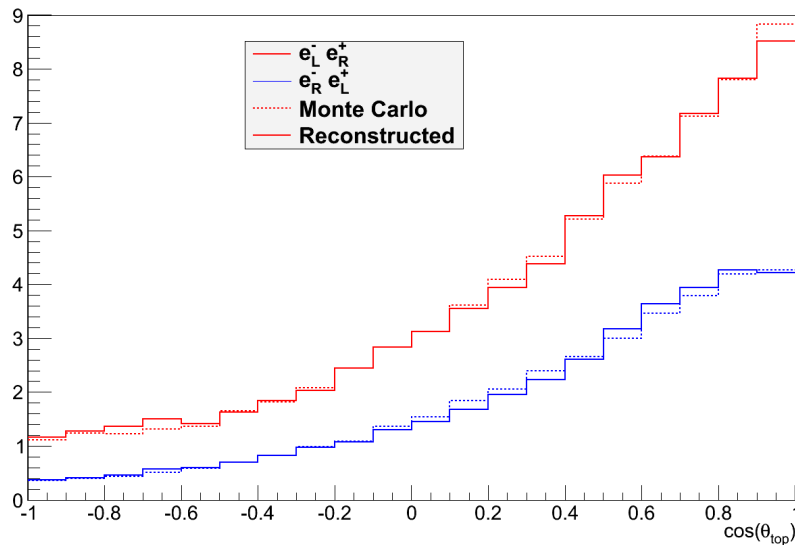
German Rodrigo has some orthogonal ideas

German Valencia (Iowa) has prepared a MadGraph UFO model that allows to generate events with an anomalous CP violating FF (electric dipole moment for the top quark) → unpacking later today

Try to reproduce TESLA numbers...

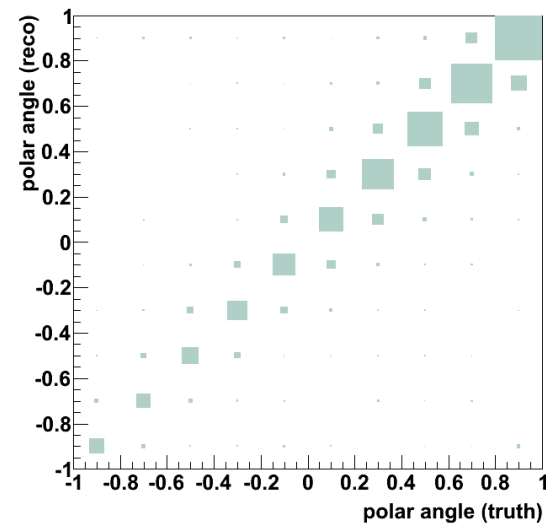
The FB asymmetry @ 1 TeV

Top direction



reco = truth within 2 %

ILC1000



Mapping OK

> 90 % of events is correctly reconstructed

Off-diagonal elements disappear

I'm also interested to explore how the sensitivity evolves with center-of-mass energy (250-3000 GeV)

Summary

Three immediate problems + two optional ones

Proposal:

Single top → MV

Kt vs Durham → Nacho

Chi-squared → Jeremy

Paper draft → Roman

Future directions:

- different center-of-mass energy
- CP violating observables