

Measurement of $K_{\mu 3}^0$ form factors with the NA48 detector

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Outline

- $K_{\ell 3}$ decays
- $|V_{us}|$ and CKM Unitarity
 - Experimental Inputs
 - Theory Inputs
- $K_{\mu 3}$ Decays and Physics beyond the SM
 - f_0 at the Callan-Treiman Point
 - Dispersive Parametrization for f_0
- The NA48 Detector
- $K_{\mu 3}$ Form Factor Analysis
- Comparison with other experimental results
- f_0 and the RHCs
- Summary

$K_{\ell 3}$ Decays – Introduction

- $s \rightarrow u$ transitions are involved in the semi-leptonic kaon decays

$$K^0 \rightarrow \pi^\pm \ell^\mp \nu_\ell \quad K^\pm \rightarrow \pi^0 \ell^\pm \nu_\ell \quad (\ell = \mu, e)$$

- These decays are known to be the “golden” modes to extract $|V_{us}|$ and one of the main playgrounds for low-energy theories such as ChPT
- $|V_{us}|$ and $|V_{ud}|$ are by far the most precisely known CKM matrix elements

⇒ Precision frontier in CKM studies: $\sigma_{|V_{ud}|}/|V_{ud}| \simeq 0.03\%$

$$\sigma_{|V_{us}|}/|V_{us}| \simeq 1\%$$

- **NEW** Precision test of SM and physics beyond it in $K_L \rightarrow \pi^\pm \mu^\mp \nu_\mu$ decays

⇒ Test the existence of right handed quarks coupled to the standard W

$K_{\ell 3}$ Decays – Introduction

- Only the vector part of the weak current contributes to the $K_{\ell 3}$ decays
 \Rightarrow Theoretically clean

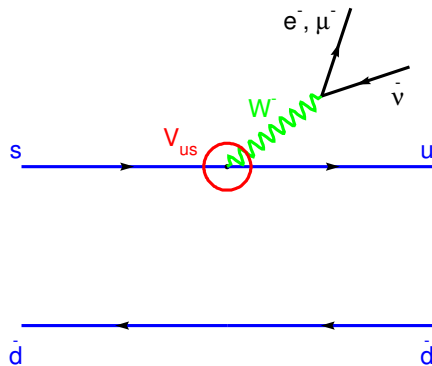
- The m.e. can be written in terms of two dimensionless form factors f_{\pm} :

$$\mathfrak{M} = G_F / \sqrt{2} |V_{us}| [f_+(t) (p_K + p_{\pi})^{\mu} + f_-(t) (p_K - p_{\pi})^{\mu}] \bar{u}_{\ell\mu} \gamma_{\mu} (1 - \gamma_5) u_{\nu\mu}$$

- t is the four-momentum squared transferred to the lepton system

$$t = q^2 = (p_{\ell} + p_{\nu})^2 = (p_K - p_{\pi})^2 = m_K^2 + m_{\pi}^2 - 2m_K E_{\pi}^*$$

- The form factors appear because the π and the K are not pointlike particles



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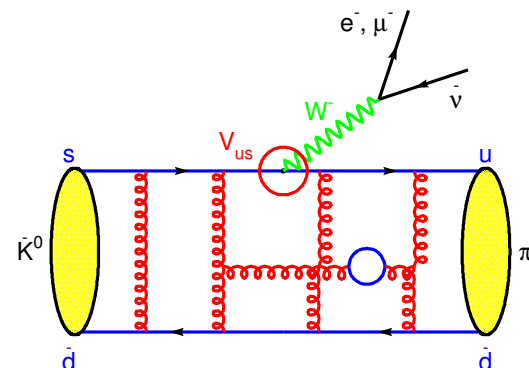
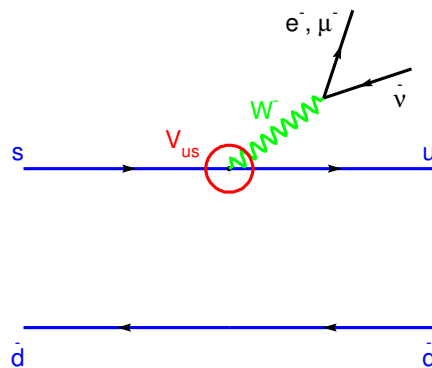
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Include the effects of the strong force using form factors

$K_{\ell 3}$ Decays – Form Factors

In the \mathfrak{M}^2 expression $f_-(t)$ is multiplied to a term $\propto m_\ell^2/m_K^2$

Need only f_+ to describe K_{e3} decays

f_- can be measured ONLY in $K_{\mu 3}$ decays

Describe $K_{\mu 3}$ decays using f_+ and f_0 instead of f_- :

$$f_0(t) = f_+(t) + \frac{t}{(m_K^2 + m_\pi^2)} f_-(t)$$

In the CM of the dilepton system:

$f_+(t)$ is related to $\vec{V}^{(\Delta S=1)}$ and describes 1^- transitions \rightarrow VECTOR f.f.

$f_0(t)$ is related to $V_0^{(\Delta S=1)}$ and describes 0^+ transitions \rightarrow SCALAR f.f.

$K_{\ell 3}$ Decays – Form Factors

Well known parametrizations of the form factors are: **Linear, Quadratic and Pole**

$$f_{+,0}(t) = f_+(0) \left(1 + \lambda_{+,0} t/m_\pi^2 \right) \quad \text{LINEAR}$$

$$f_{+,0}(t) = f_+(0) \left[1 + \lambda'_{+,0} t/m_\pi^2 + \frac{1}{2} \lambda''_{+,0} (t/m_\pi^2)^2 \right] \quad \text{QUADRATIC}$$

$$f_{+,0}(t) = f_+(0) \frac{m_{V,S}^2}{m_{V,S}^2 - t} \quad \text{POLE}$$

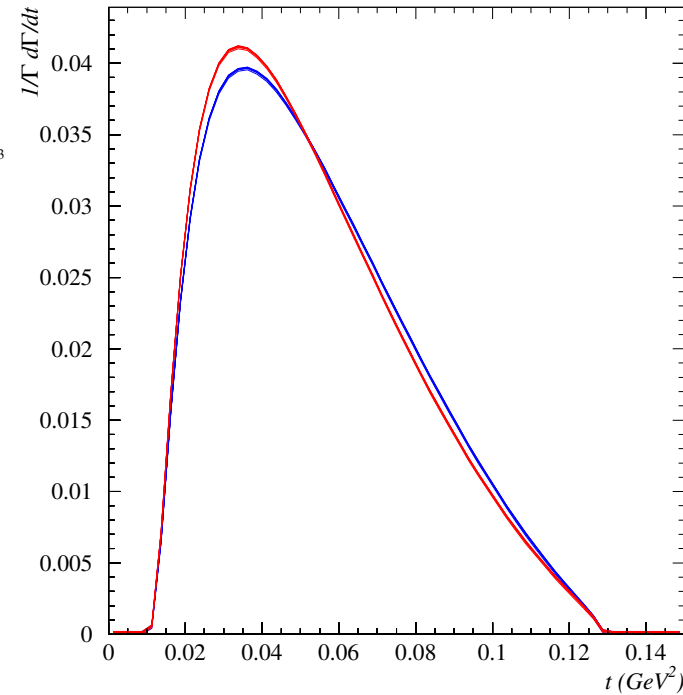
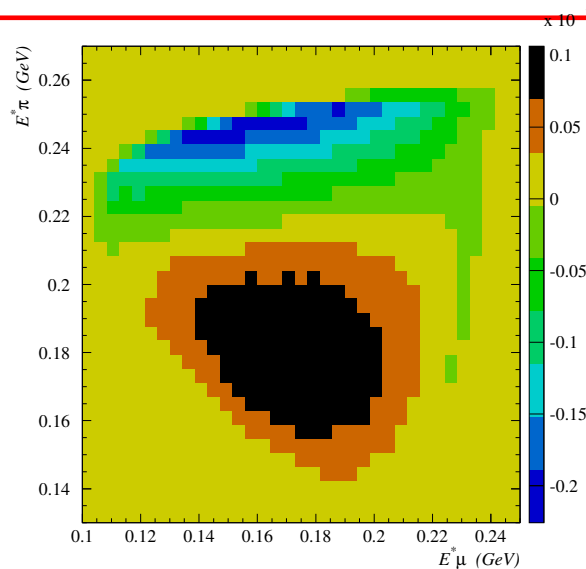
Linear & Quadratic \rightarrow Taylor expansions around $t = 0$

Experiments measure the normalized form factors: $\hat{f}(t) = f_{+,0}(t)/f_+(0)$

In the pole model the form factors acquire a physical meaning: they are related to the exchange of K^* resonances with spin-parity $1^-/0^+$ and mass m_V/m_S

- The vector form factor is dominated by $K^*(892)$
- One parameter fit: $\lambda'_{+,0} = \left(\frac{m_\pi}{m_{V,S}} \right)^2 \quad \lambda''_{+,0} = 2\lambda'_{+,0}$

$K_{\mu 3}$ Form Factors Measurement



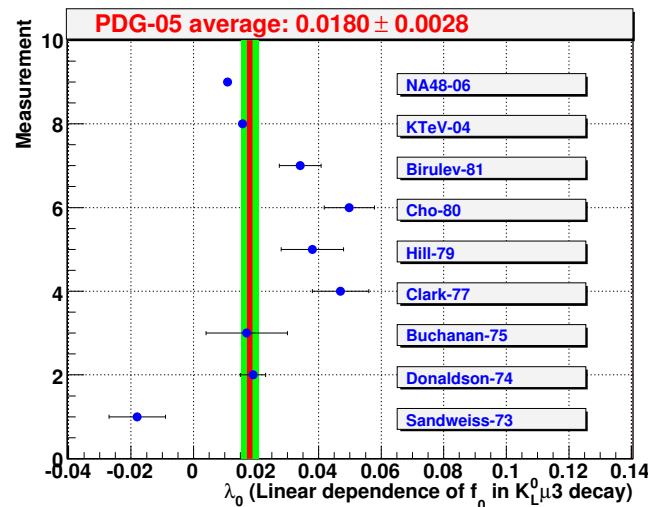
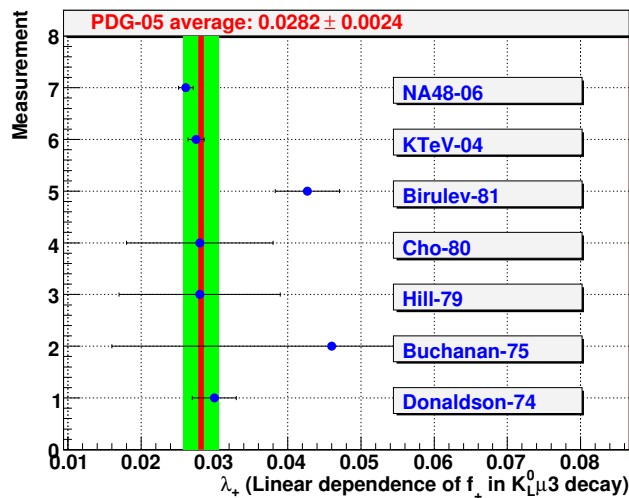
$$\lambda_+ = 0$$

$$\lambda_0 = 0$$

$$\lambda_+ = 0.0267$$

$$\lambda_0 = 0.0117$$

- After more than 50 years of investigations "reliable" results only nowadays
- σI_K^ℓ was the largest source of uncertainty for $|V_{us}|$



λ_0 has always been very hard to measure
Two ff and 4 parameters to fit in $K_{\mu 3}$

High correlations \rightarrow big errors

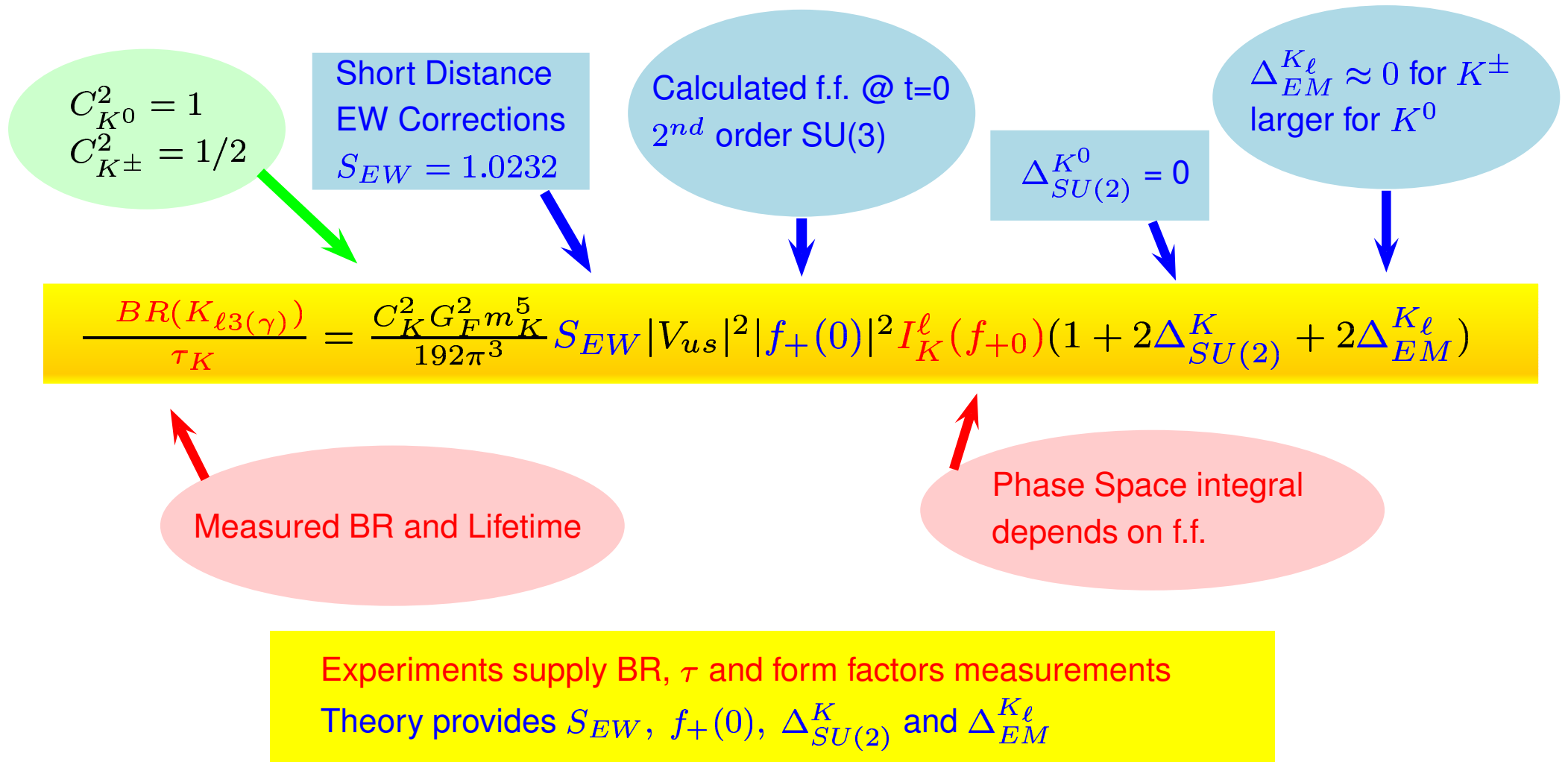
Direct measurement of λ_0' and λ_0''

\rightarrow Not possible (P. Franzini KAON07)

Importance of one parameter fit

$|V_{us}|$ and $K_{\ell 3}$ Decays – Master Formula

The master formula for the $K_{\ell 3}$ decay rates:



CKM Unitarity Test in the 1st Row

Test CKM unitarity using the 1st row:

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

($|V_{ub}| \simeq 10^{-3}$ can be neglected)

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 - \delta$$

PDG 2004

$$\delta = 0.0033 \pm 0.0015 \quad (2.3\sigma \text{ discrepancy})$$

Long standing problem...
CKM unitarity ?
Hint of new physics ?

2003 BNL 865 measures $BR(K^+ \rightarrow \pi^0 e^+ \nu_e) = 5.13(10)\%$
2.3 σ higher than PDG

The value for $|V_{us}|$ consistent with unitarity

Experimental Inputs

PDG04 used data mainly from experiments dating back to the seventies...

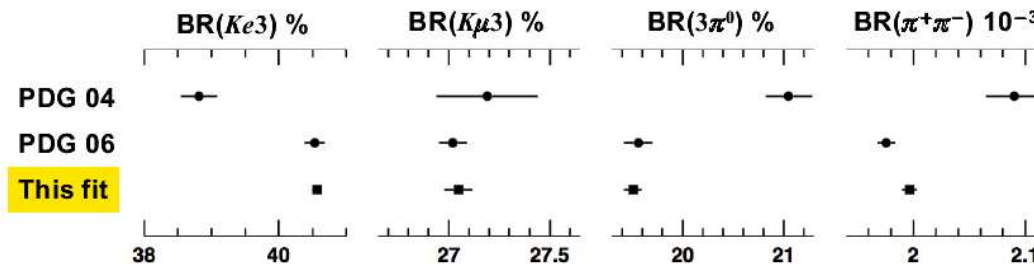
Much effort on the experimental side in these last 2-3 years !

KLOE	K_L	4 BRs, form factors, lifetime
	K_S	BR(K_{Se3}), charge asymmetry
	K^\pm	BR(K_{e3}), BR($K_{\mu3}$), lifetime
KTeV	K_L	main 6 BRs, form factors
ISTRA+	K^-	BR(K_{e3}), form factors
NA48	K_L	3 BRs, form factors
	K^\pm	BR(K_{e3}), BR($K_{\mu3}$)

A LOT OF WORK !

Experimental Inputs

- Much higher statistics than older experiments
- Radiative corrections
- Remarkable evolution of BRs
 - Confirm the increase of $\text{BR}(K_{e3}^+)$, as firstly reported by BNL E865
 - $\text{BR}(K_{e3})$ significantly increased, $\text{BR}(3\pi^0)$ and $\text{BR}(2\pi)$ significantly decreased



- Improved precision in form factors \rightarrow can use both e and μ results for $I_K^\ell(f_{+0})$
- Proper treatment of correlations between measurements

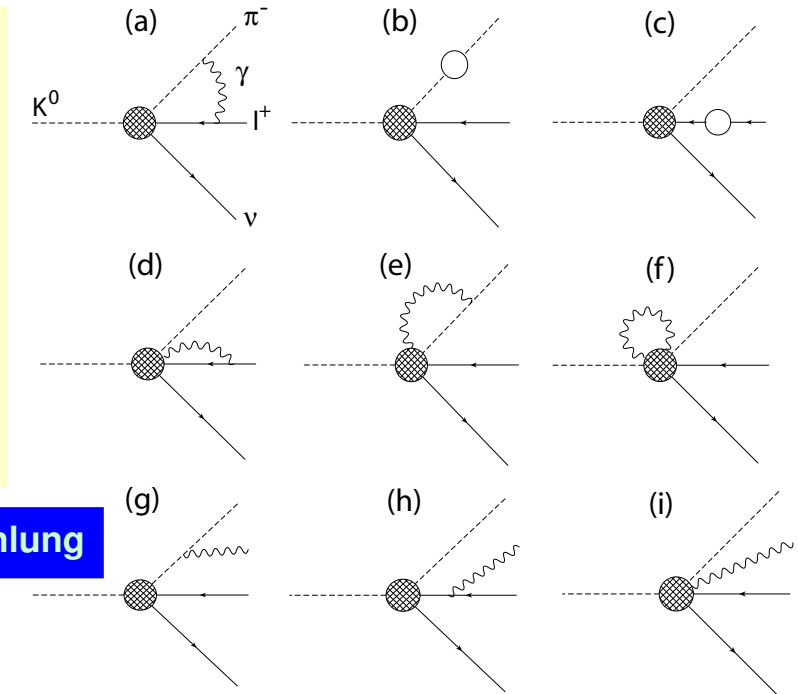
PDG 2006 has replaced, wherever possible, the old results with the new ones

$$\delta = 0.0008 \pm 0.0011$$

CKM unitarity "restored"...BUT...what about the theory inputs ?

Theory Inputs: $\Delta_{EM}^{K_\ell}$

Virtual Corrections



Inner-Bremsstrahlung

$\Delta_{EM}^{K_\ell}$ (%)	ChPT Cirigliano 02	ChPT Neufeld	Hadr. Model Andre 04
K_{e3}^0	$+0.52 \pm 0.10$	$+0.57 \pm 0.15$	$+0.65 \pm 0.15$
$K_{\mu 3}^0$		$+0.80 \pm 0.15$	$+0.95 \pm 0.15$
K_{e3}^+	$+0.03 \pm 0.10$	$+0.08 \pm 0.15$	
$K_{\mu 3}^+$		-0.12 ± 0.15	

- $\Delta_{EM}^{K_\ell}$ for full phase space
- Different estimate of $\Delta_{EM}^{K_\ell}$ agree within the quoted errors
- First estimate of $\Delta_{EM}^{K_{\mu 3}^+}$ from Neufeld removes dominant contribution to the error on $|V_{us}|f_+(0)$ for this mode
- Larger effect in K^0 decays, as expected from Coulomb interaction

Need common set of definitive values of $\Delta_{EM}^{K_\ell}$

Theory Inputs: $\Delta_{SU(2)}^{K^\pm}$

- Difference between K^0 and K^\pm due to the isospin breaking corrections

$$1 + \Delta_{SU(2)}^{K^\pm} = \frac{f_+^{K^+}(0)}{f_+^{K^0}(0)} \quad \Delta_{SU(2)}^{K^\pm} = (+2.31 \pm 0.22)\% \quad [\text{CHPT Cirigliano et al. (2002)}]$$

- ChPT to $O(p^4)$ relates $\Delta_{SU(2)}^{K^\pm}$ to ratios of quark masses

Quak mass ratios \rightarrow Predict $\Delta_{SU(2)}^{K^\pm}$

- Data and EM corrections are becoming precise enough to determine $\Delta_{SU(2)}^{K^\pm}$
- Turn it around and determine $\Delta_{SU(2)}^{K^\pm} \rightarrow$ Quark mass ratios
- Indeed the values of $|V_{us}|f_+(0)$ obtained from K^\pm and K^0 show a little difference...
- Use K^\pm results without isospin corrections and compare to K^0 mode

$$\rightarrow \Delta_{SU(2)}^{K^\pm} \approx 3\%$$

- If the data are OK this has consequences on the quark masses
- The underestimation of the isospin breaking corrections would result in an artificial increase of the extracted value of $|V_{us}|$

Theory Inputs: $f_+(0)$

Still dominant source of uncertainty on $|V_{us}|$

- In $SU(3)$ limit $f_+(0) = 1$
- Ademollo–Gatto theorem (1964) \Rightarrow only 2^{nd} order $SU(3)$ breaking effects

$$f_+(0) = 1 - \mathcal{O}[(m_s - m_u)^2]$$

- Two players in the game: ChPT and Lattice QCD
- The ChPT expansion of $f_+(0)$ reads:

$$f_+(0) = 1 + f_{p^4} + f_{p^6} + \dots$$

$$f_{p^4}$$

One-loop

$$f_{p^4} = -0.023 \text{ [Gasser \& Leutwyler (1985)]}$$

$$f_{p^6}$$

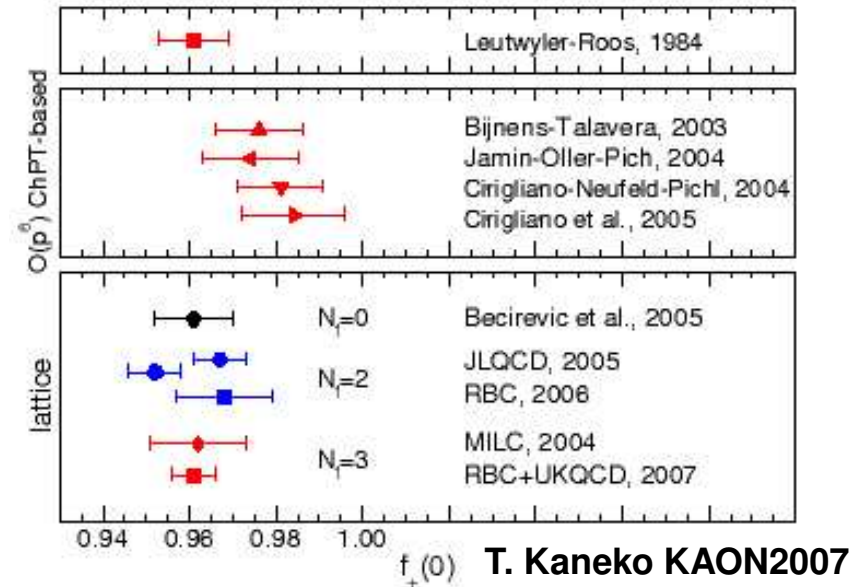
Two-loops

{ Quark model estimate [Leutwyler-Roos (1984)]
Analytic calculations [Bijnens-Talavera (2003)]
LECs can be constrained by λ'_0, λ''_0

Presently the L&R 84 value is the conventional choice used to extract $|V_{us}|$

$$f_+(0) = 0.961 \pm 0.008$$

Theory Inputs: $f_+(0)$



- Very promising activity in the field of the Lattice QCD
- Calculation of $f_+(0)$ with **1% accuracy is feasible**
- Work in progress towards fully "unquenched" calculations
- Major systematics
 - Interpolation in t : $f_+(t_{max}) \rightarrow f_+(0)$
 - Chiral extrapolation to physical masses
 $300 < m_\pi < 600$ MeV
- Lattice calculations generally agree with the LR value
- Not good agreement with analytic calculations

Meaningful extraction of $|V_{us}|$ only when $f_+(0)$ will be correctly determined

$K_{\mu 3}$ Decays and the Physics Beyond SM

New idea on $K_{\mu 3}$ decays [V. Bernard, M. Oertel, E. Passemar, J. Stern **PLB 638**(2006) 480]

A measurement of the value of the scalar form factor of the (neutral) $K_{\mu 3}$ decay at the Callan–Treiman point can provide a significant test of electro–weak coupling of right handed quarks to the standard W boson

- The Callan–Treiman low–energy theorem gives the value of $f_0(t)$ at the point $t = \Delta_{K\pi} = (m_K^2 - m_\pi^2)$

$$C = \hat{f}_0(\Delta_{K\pi}) = \frac{F_{K^+}}{F_{\pi^+} f_+(0)} + \Delta_{CT}$$

- Δ_{CT} evaluated at NLO in ChPT [Gasser and Leutwyler (1985)] ($m_u = m_d$)

$$\Delta_{CT} \simeq -3.5 \cdot 10^{-3}$$

- NNLO to be determined → **Should not change the order of magnitude**
- For K^\pm the effect of isospin breaking is **larger: $\Delta_{CT} \sim \text{few } 10^{-2}$**

$K_{\mu 3}$ Decays and the Physics Beyond SM

Scenario: Low Energy Effective Theory (LEET)

- Very high energy $E > \Lambda \rightarrow$ **New symmetries**
- $E < \Lambda$ not complete decoupling \rightarrow **High energy symmetries constrains the interactions at low energy**

The quark CC interaction is modified at NLO

- Existence of direct coupling of right handed quarks to W : ϵ
- Modifications of the left handed couplings: δ
- NO effects on leptonic CC
- Effective couplings for the vector and axial quark currents

$$\mathcal{V}_{eff}^{ij} = (1 + \delta)V_L^{ij} + \epsilon V_R^{ij} + \text{NNLO}$$

$$\mathcal{A}_{eff}^{ij} = -(1 + \delta)V_L^{ij} + \epsilon V_R^{ij} + \text{NNLO}$$

$i = u, c, t; j = d, s, b$. V_L, V_R left and right unitary flavour mixing matrices

$$\text{SM} \rightarrow \delta = \epsilon = 0$$

$$\mathcal{V}_{eff} = -\mathcal{A}_{eff} = V_{CKM}$$

$K_{\mu 3}$ Decays and the Physics Beyond SM

The presence of RHCs modifies the expression for C

With RHCs we do not measure directly the low energy QCD parameters but a combination of them and the non standard EW couplings

$$C = f_0(\Delta_{K\pi}) = \left| \frac{F_{K^+} \mathcal{A}_{eff}^{us}}{F_{\pi^+} \mathcal{A}_{eff}^{ud}} \right| \frac{1}{|f_+(0) \mathcal{V}_{eff}^{us}|} |\mathcal{V}_{eff}^{ud}| \left| \frac{\mathcal{A}_{eff}^{ud} \mathcal{V}_{eff}^{us}}{\mathcal{V}_{eff}^{ud} \mathcal{A}_{eff}^{us}} \right| + \Delta_{CT}$$
$$C = B_{exp} r + \Delta_{CT}$$

$$r = \left| \frac{\mathcal{A}_{eff}^{ud} \mathcal{V}_{eff}^{us}}{\mathcal{V}_{eff}^{ud} \mathcal{A}_{eff}^{us}} \right| = 1 + 2(\epsilon_S - \epsilon_{NS}) + \mathcal{O}(\epsilon^2) \neq 1$$

$$\epsilon_{NS} = \epsilon \operatorname{Re} \left(\frac{V_R^{ud}}{V_L^{ud}} \right), \quad \epsilon_S = \epsilon \operatorname{Re} \left(\frac{V_R^{us}}{V_L^{us}} \right)$$

Strengths of $\bar{u}d$ and $\bar{u}s$ RHCs

$K_{\mu 3}$ Decays and the Physics Beyond SM

To constrain the RHCs contributions compare the SM prediction for C ...

$$C_{SM} = \left| \frac{F_{K^+} V^{us}}{F_{\pi^+} V^{ud}} \right| \frac{1}{|f_+(0) V^{us}|} |V^{ud}| + \Delta_{CT}$$

0.27618(48)

Br $\frac{K_{l2}^+(\gamma)}{\pi_{l2}^+(\gamma)}$

Phys.Rev. D74:074009 (2006)

0.2169(9)

$\Gamma_{K_{l3}(\gamma)}$

PDG06

0.97377(27)

$0^+ \rightarrow 0^+$

PDG06

$$C_{SM} = 1.2399 \pm 0.0056 + \Delta_{CT}$$

$$\ln C_{SM} = 0.2151 \pm 0.0045 + \tilde{\Delta}_{CT} \quad (\tilde{\Delta}_{CT} = \Delta_{CT}/1.24)$$

... to a **DIRECTLY** measured value of C

Dispersive Parametrization for $f_0(t)$

To extract $\ln C$ use the new proposed parametrization of the scalar form factor

⇒ Connection between the experimentally accessible region of $f_0(t)$ and its value at the unphysical point $t = \Delta_{K\pi}$

The parametrization is based on a dispersive approach with a relation subtracted twice ($t = 0, t = \Delta_{K\pi}$)

$$f_0(t) = f_+(0) \exp\left[\frac{t}{\Delta_{K\pi}} (\ln C - G(t))\right]$$

$$G(t) = \frac{\Delta_{K\pi}(\Delta_{K\pi} - t)}{\pi} \int_{t_{\pi K}}^{\infty} \frac{dx}{x} \frac{\phi(x)}{(x - \Delta_{K\pi})(x - t - i\epsilon)}$$

ϕ phase of form factor → $f_0(t) = |f_0(t)| \exp(i\phi(t))$

One parameter describes simultaneously the slope and the curvature of the form factor

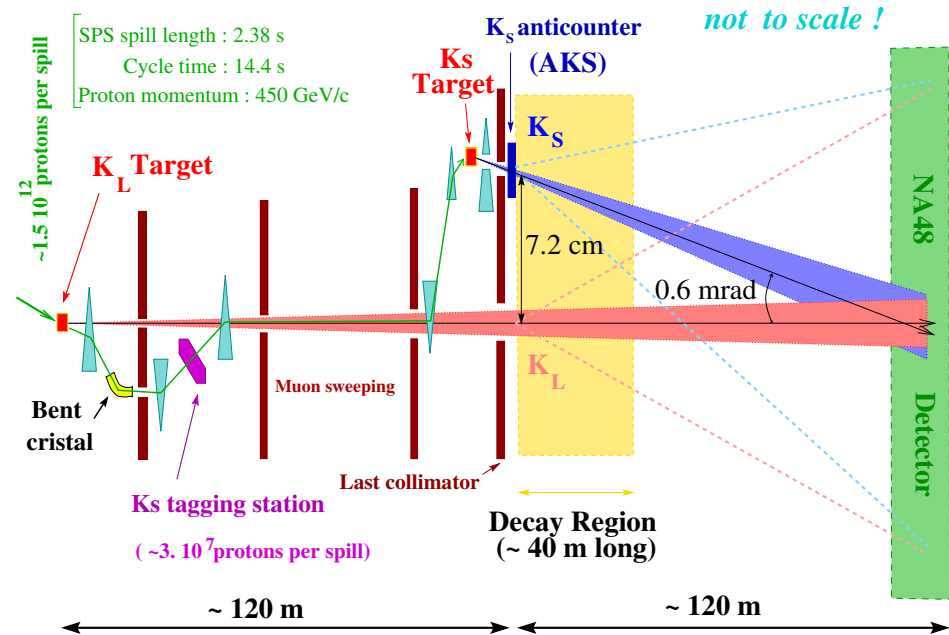
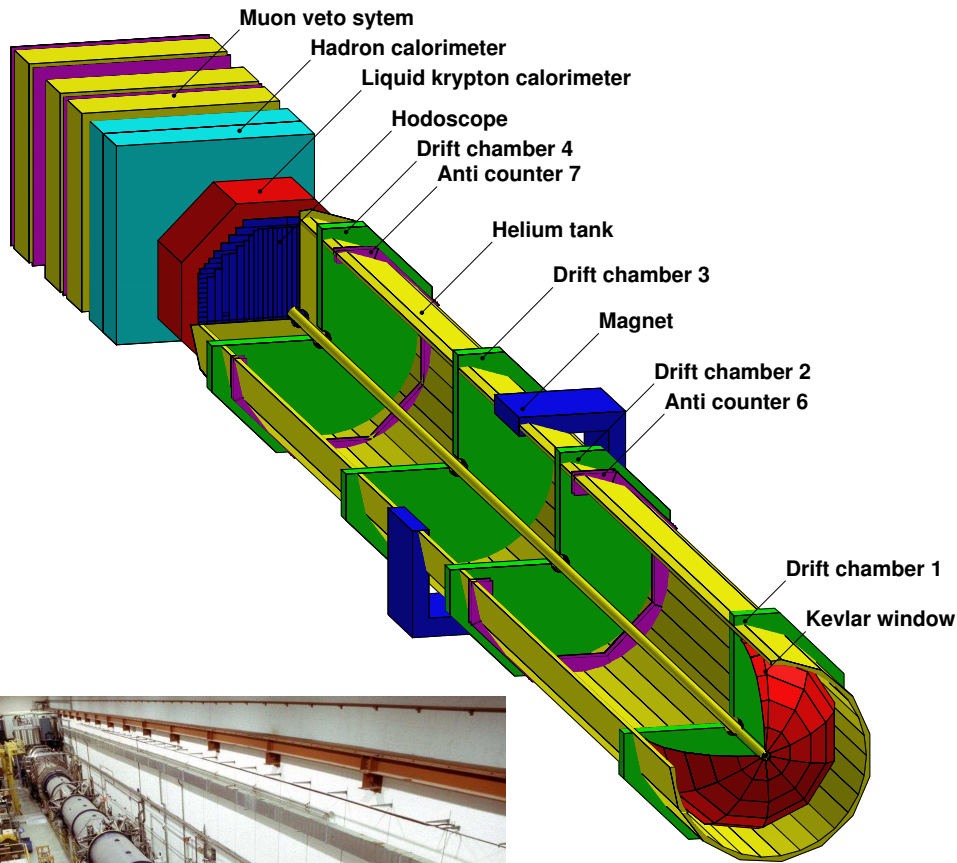
$$\begin{aligned} \lambda'_0 &= \frac{m_\pi^2}{\Delta_{K\pi}} [\ln C - G(0)] \\ \lambda''_0 &= \lambda'^2_0 - 2 \frac{m_\pi^4}{\Delta_{K\pi}} G'(0) = \lambda'^2_0 + (4.16 \pm 0.50) \times 10^{-4} \end{aligned}$$

New parametrization also for $f_+(t)$

$$f_+(t) = f_+(0) \exp\left[\frac{t}{m_\pi^2} (\Lambda_+ + H(t))\right]$$

Accurate polynomial approximations for the dispersive integrals $G(t)$ and $H(t)$

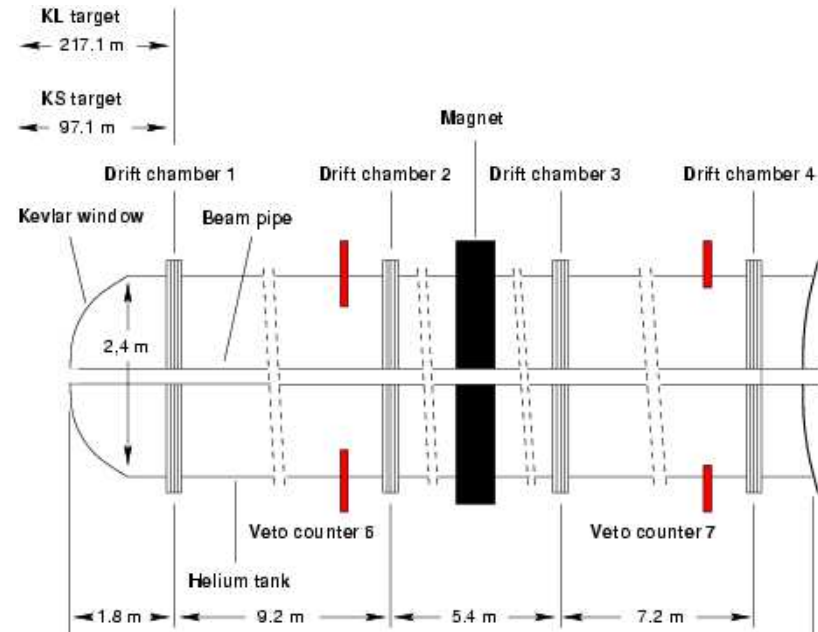
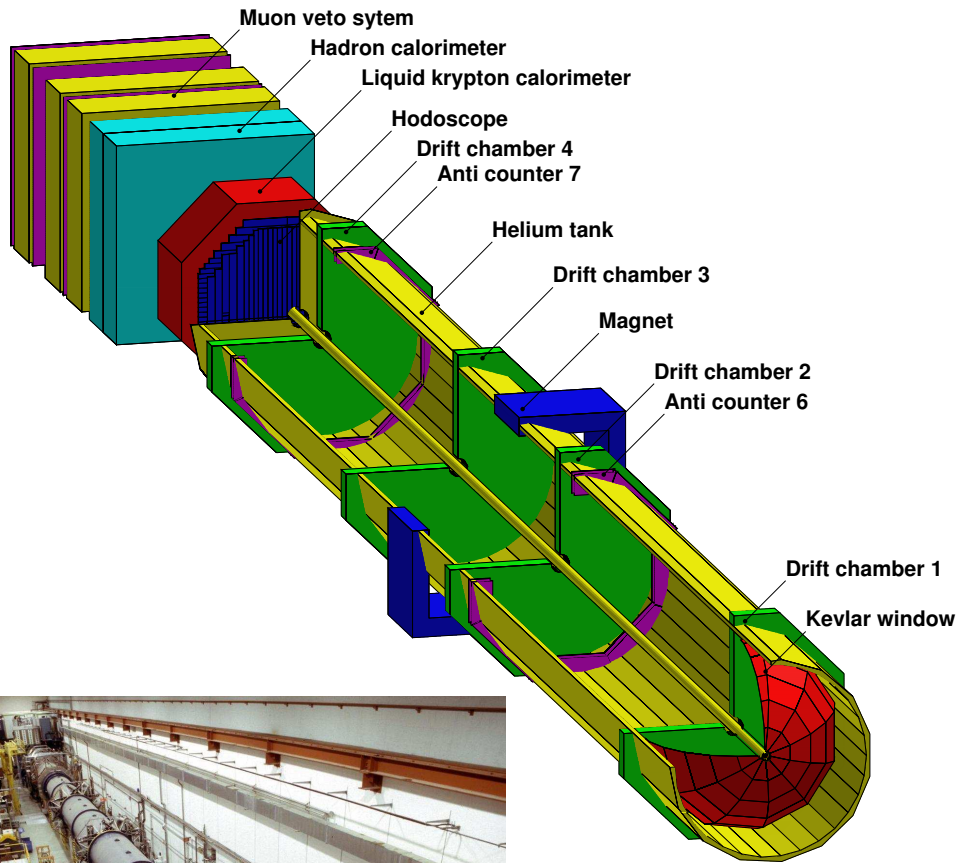
The NA48 Detector



K_L Beam

- 450 GeV/c p beam on Be target
- K_L target: 241 m from EM calo
- 126 m from decay region
- Useful p range: $70 < p_{K_L} < 170$ GeV/c
- Decay region 90 m (vacuum)

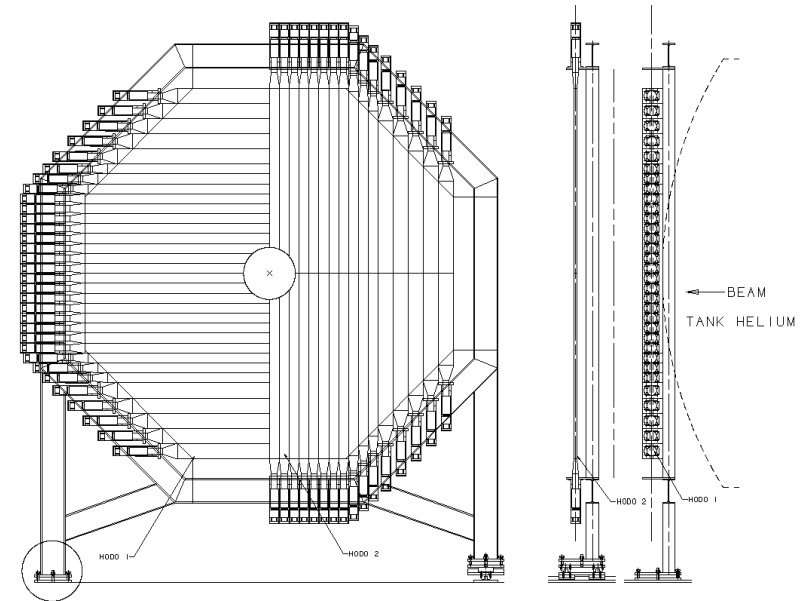
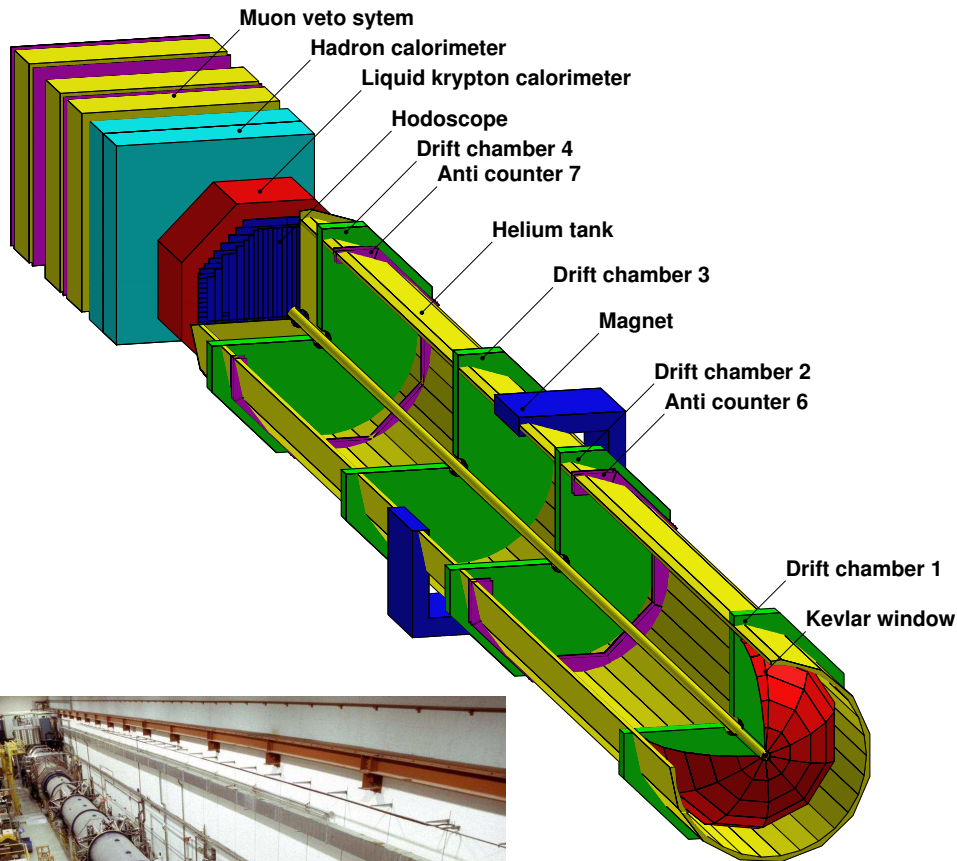
The NA48 Detector



Magnetic Spectrometer

- 4 drift chambers inside He tank
- Dipole magnet with 265 MeV/c p_T kick
- $\frac{\sigma_p}{p} (\%) = 0.48 \oplus 0.009 p \text{ (GeV/c)}$

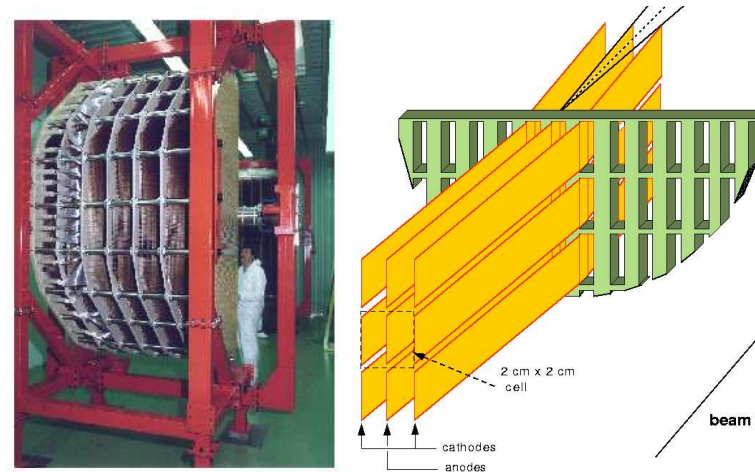
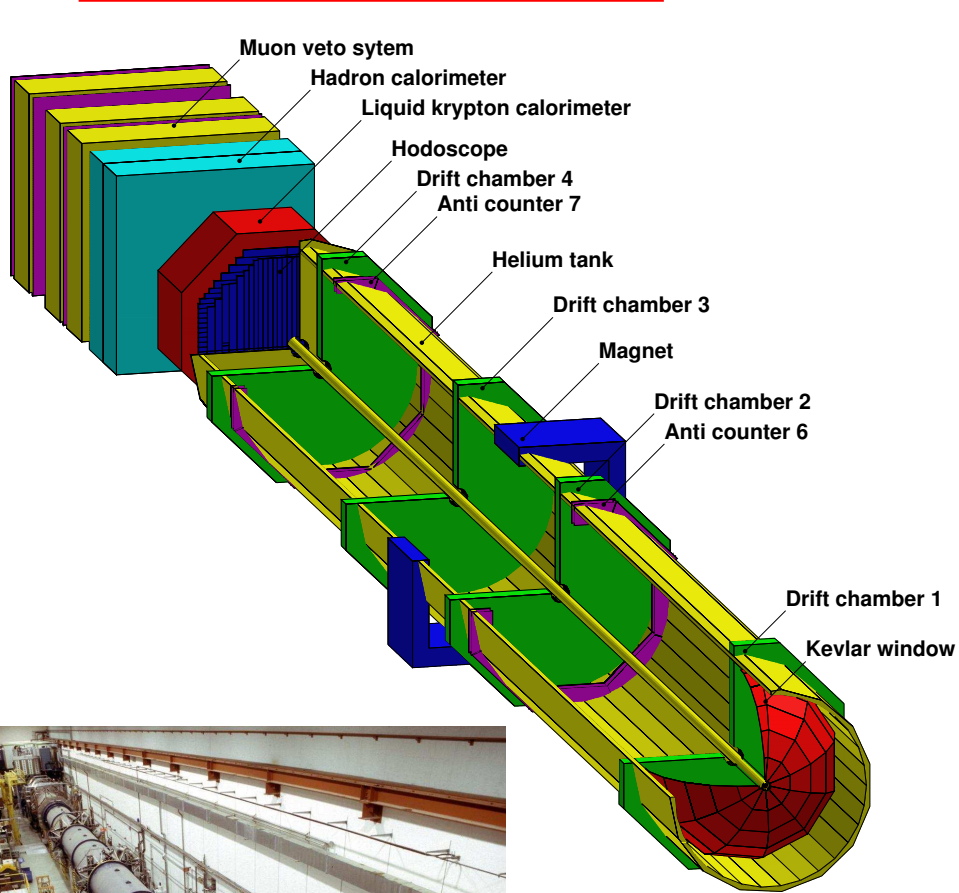
The NA48 Detector



Hodoscope

- Two \perp planes of scintillators
- Fast trigger
- Precise time measurement
- $\sigma_t \simeq 150$ ps

The NA48 Detector

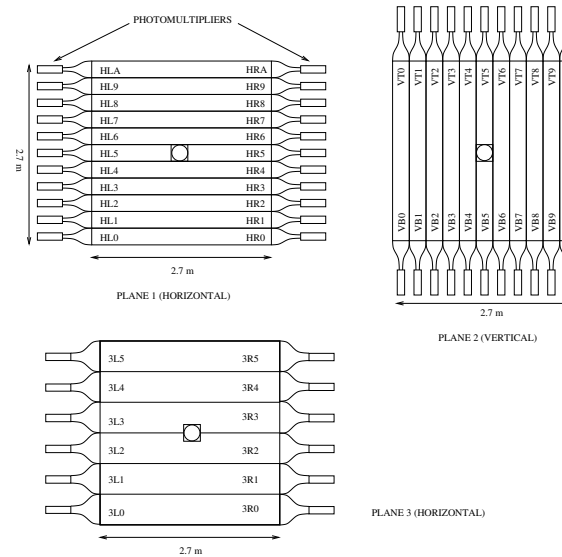
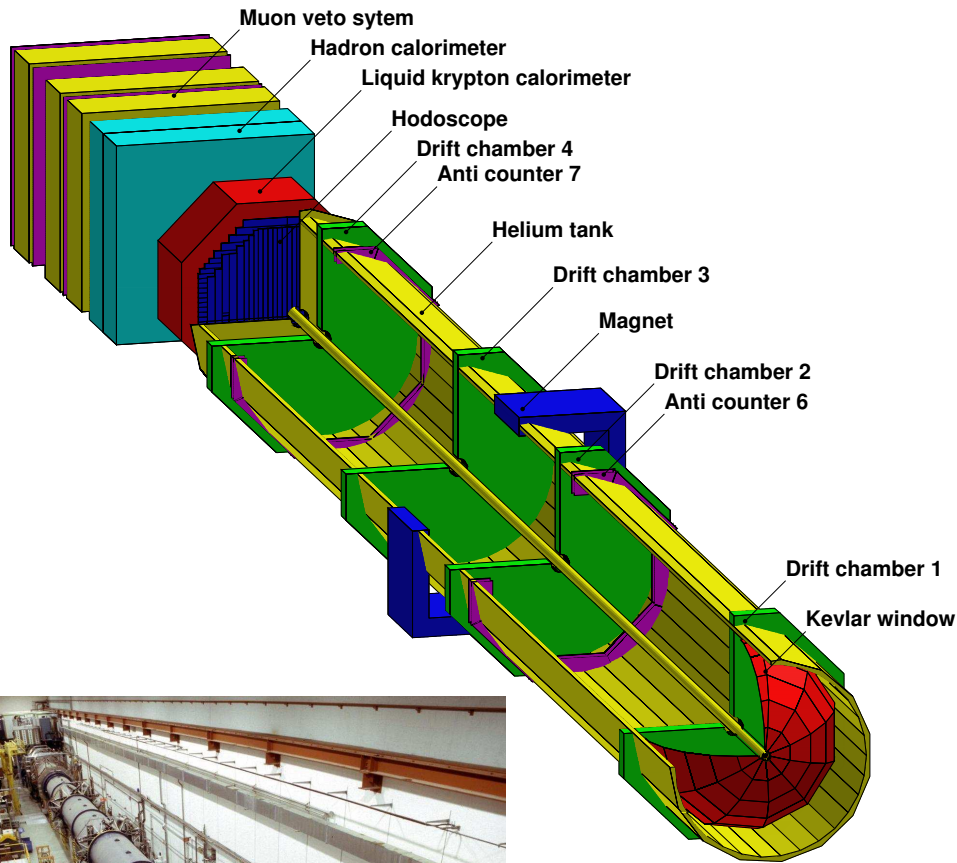


EM Calorimeter

- Liquid krypton
- 13248 cells of $2 \times 2 \text{ cm}^2$
- $\frac{\sigma_E}{E} (\%) = \frac{3.2}{\sqrt{E}} \oplus \frac{9.0}{E} \oplus 0.42 \text{ (GeV)}$



The NA48 Detector



Muon Counter

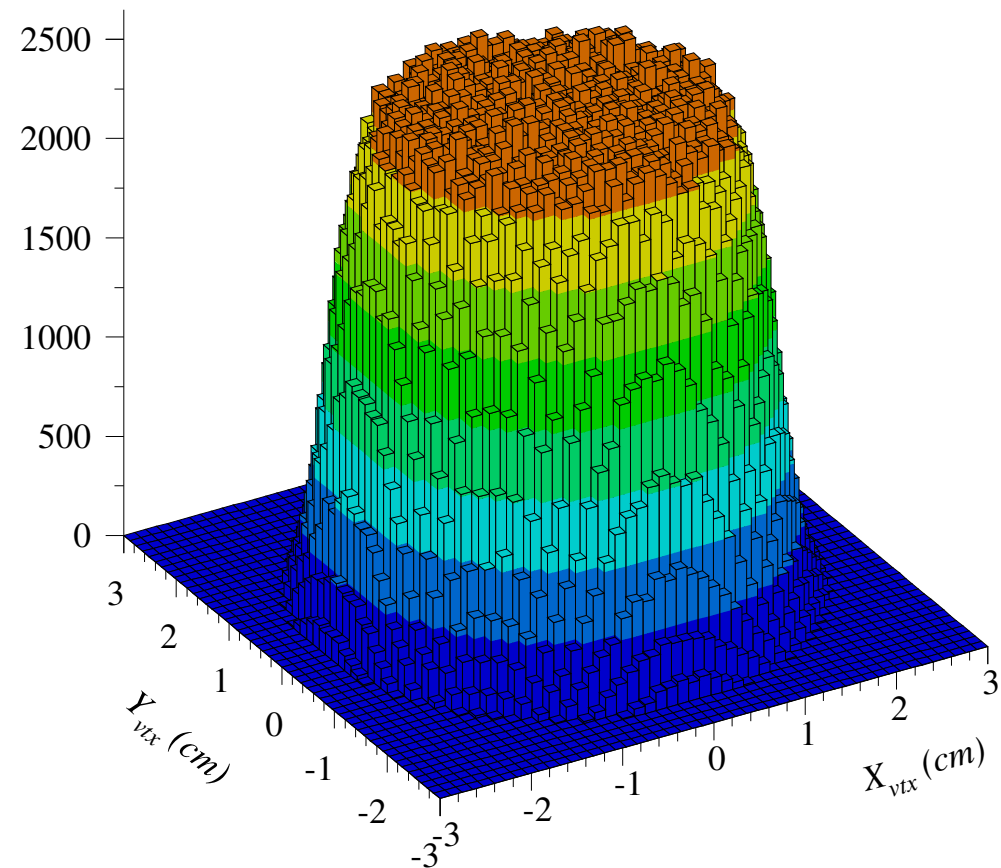
- 3 planes of scintillators
- 80 cm iron shield each
- 25cm × 25cm cells
- $\sigma_t \simeq 350$ ps

$K_{\mu 3}$ Event Selection

- K_L collected during 1999 ϵ'/ϵ data taking
- Special minimum bias run (2 days)
- K_L beam only
- 100 M events on tape

Event Selection

- Good vertex (Z, R, cda, 2 tracks \pm , Δ time)

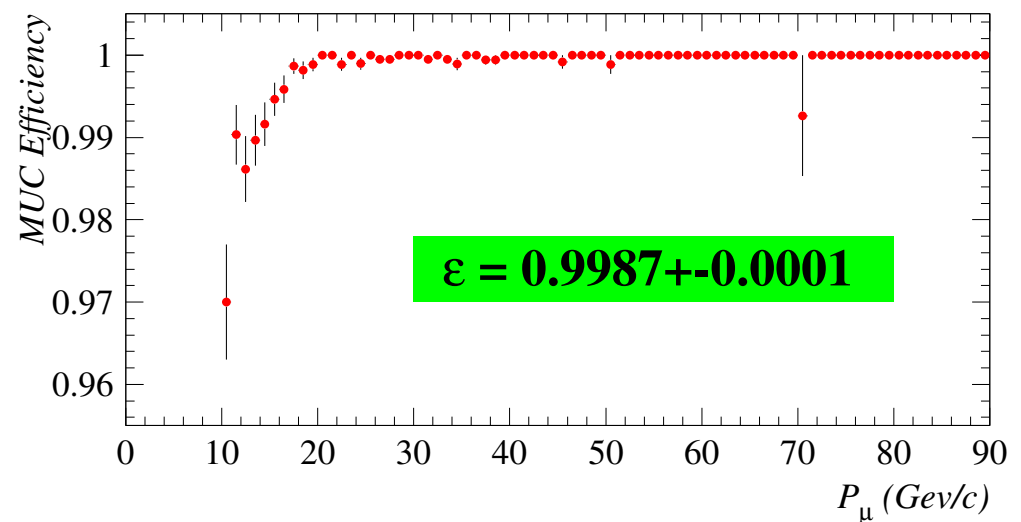
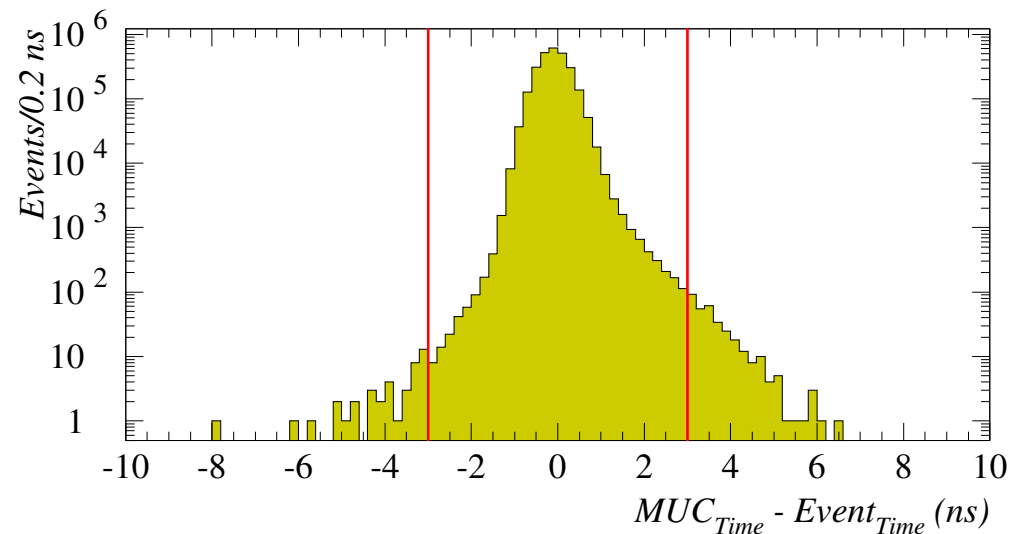


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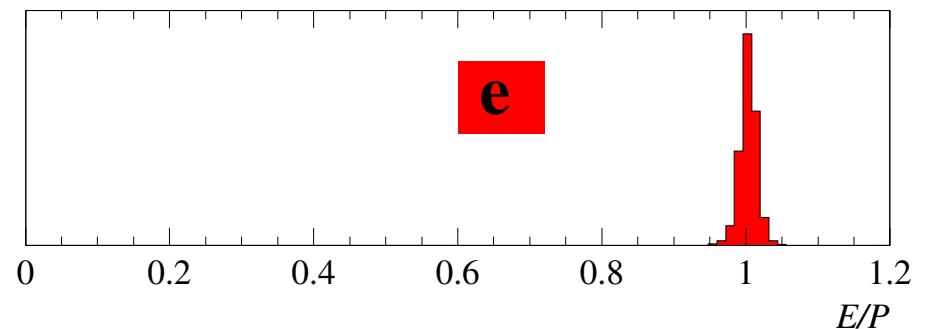
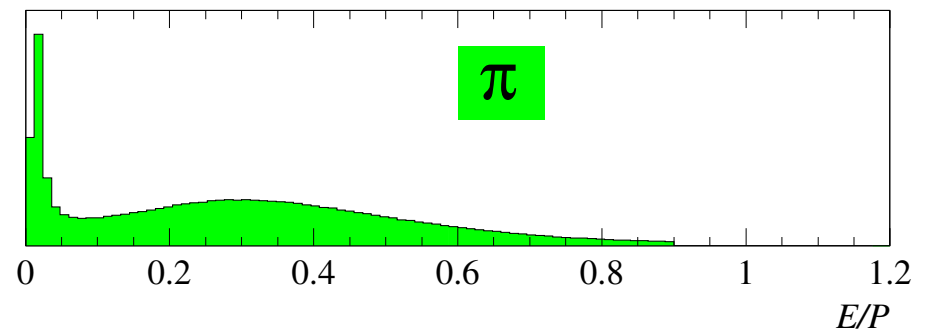
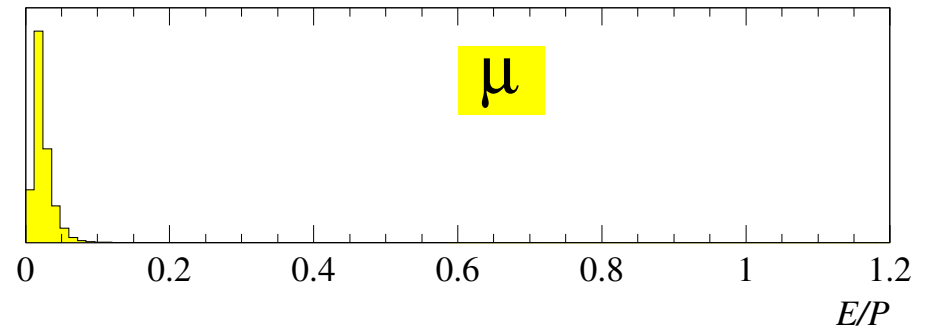


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Event Selection

- Good vertex (Z, R, cda, 2 tracks \pm , Δ time)
- μ id. (Hit in time in MUC)
- π id. ($E/p < 0.9$)

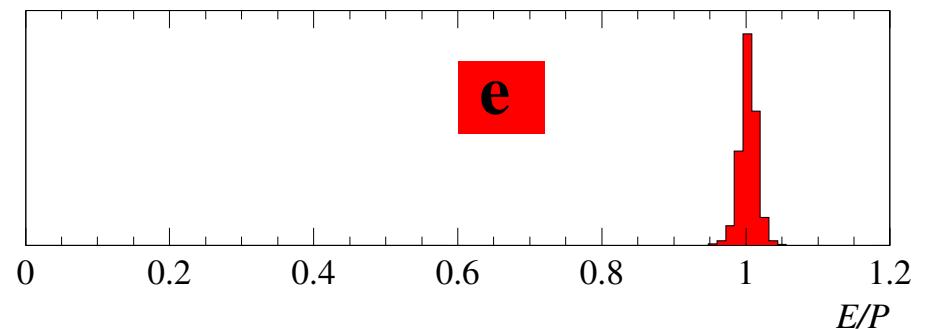
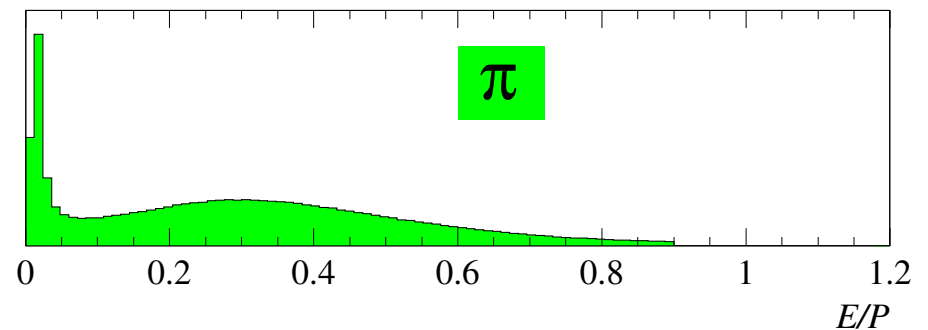
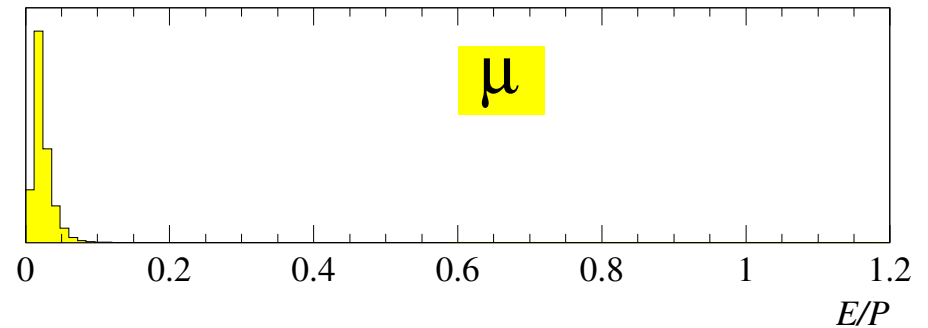


$K_{\mu 3}$ Event Selection

- K_L collected during 1999 ϵ'/ϵ data taking
- Special minimum bias run (2 days)
- K_L beam only
- 100 M events on tape

Event Selection

- Good vertex (Z, R, cda, 2 tracks \pm , Δ time)
- μ id. (Hit in time in MUC)
- π id. ($E/p < 0.9$)
- no e (against K_{e3})



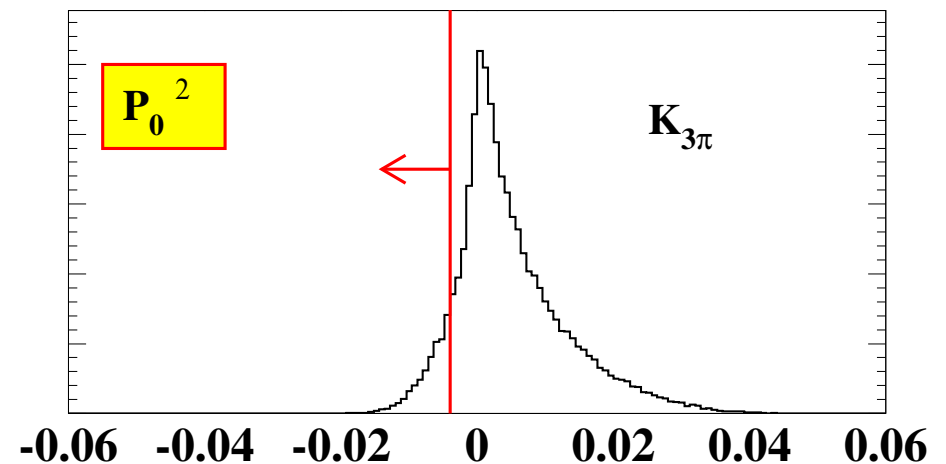
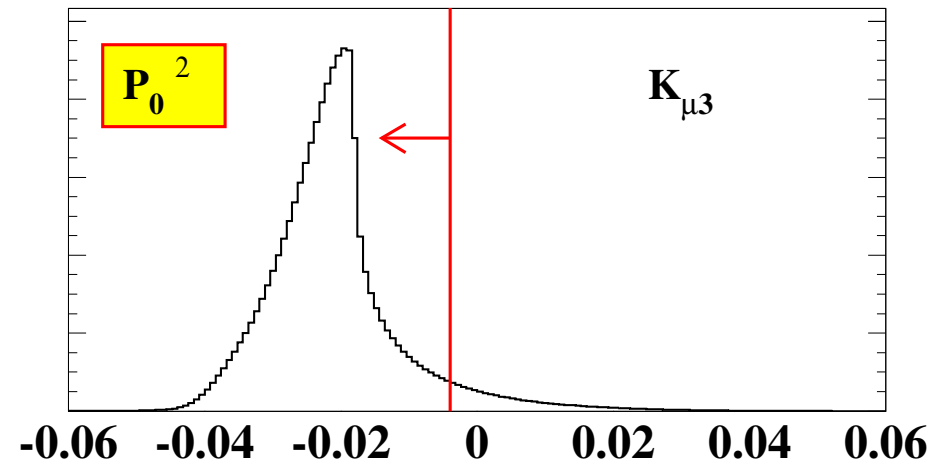
$K_{\mu 3}$ Event Selection

- K_L collected during 1999 ϵ'/ϵ data taking
- Special minimum bias run (2 days)
- K_L beam only
- 100 M events on tape

Event Selection

- Good vertex (Z, R, cda, 2 tracks \pm , Δ time)
- μ id. (Hit in time in MUC)
- π id. ($E/p < 0.9$)
- no e (against K_{e3})
- no $K_{3\pi}$ ($P_0'^2 < -0.004$ (GeV/c)²)

Selected 2.3×10^6 events



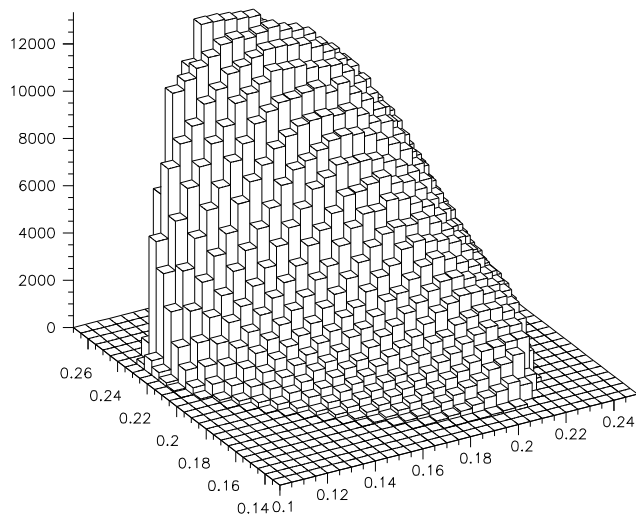
$K_{\mu 3}$ Form Factors Analysis

Dalitz Plot analysis: to extract the f.f. perform a fit to the DP density

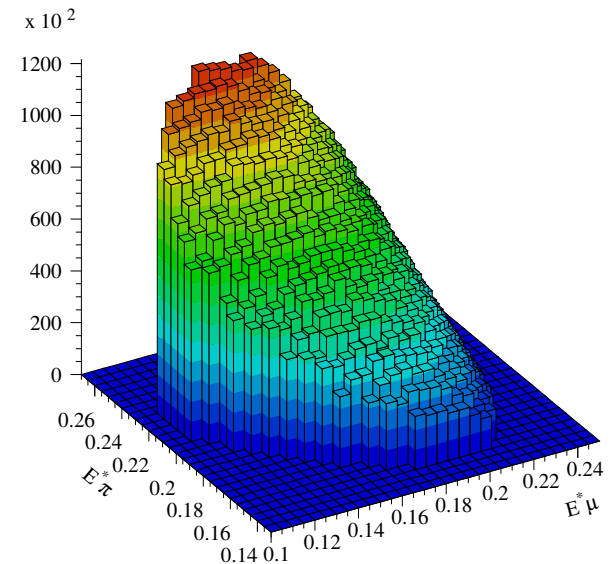
$$\rho(E_{\mu}^*, E_{\pi}^*) = \frac{d^2 N(E_{\mu}^*, E_{\pi}^*)}{dE_{\mu}^* dE_{\pi}^*} \propto A f_+^2(t) + B f_+(t) f_-(t) + C f_-^2(t)$$

E_{μ}^*, E_{π}^* are the energies of μ and π in the kaon CMS

A, B and C are kinematical terms



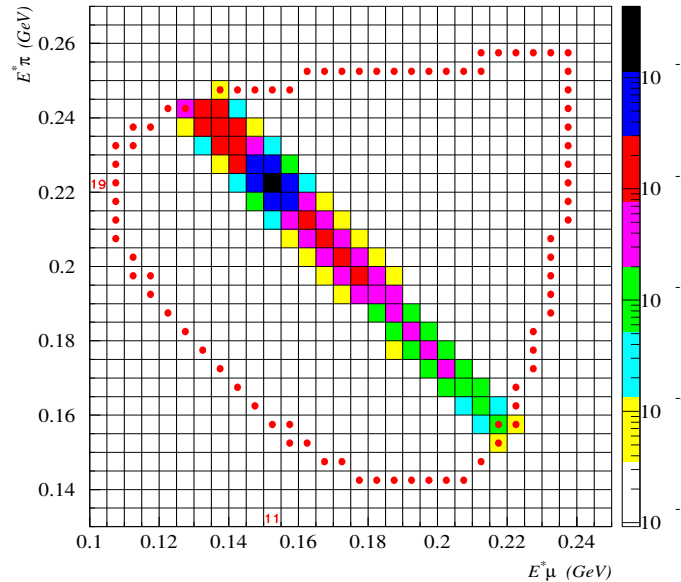
- Acceptance
- K_L energy ambiguity
- Radiative Corrections
- Background



K_L Energy Ambiguity

- The K_L energy is not known
- It cannot be determined unambiguously due to the undetected ν

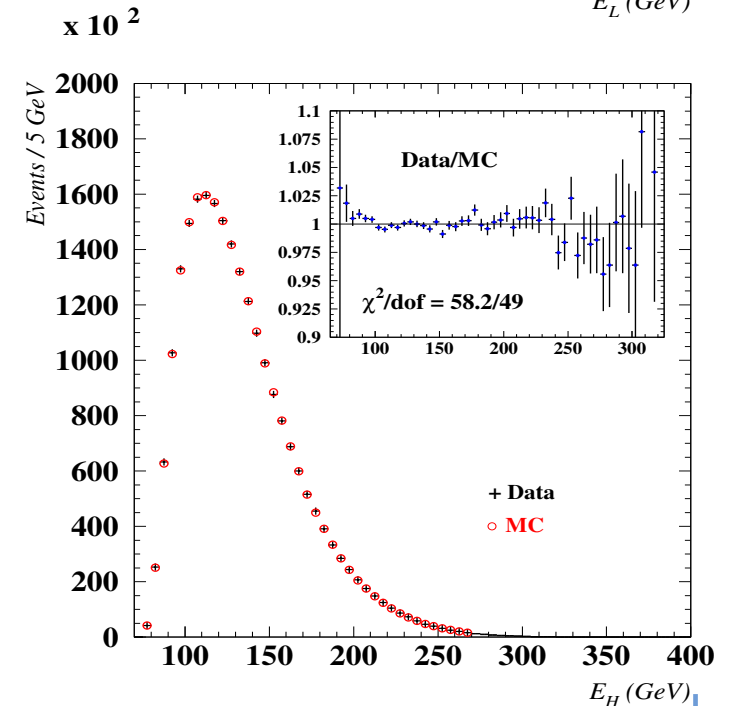
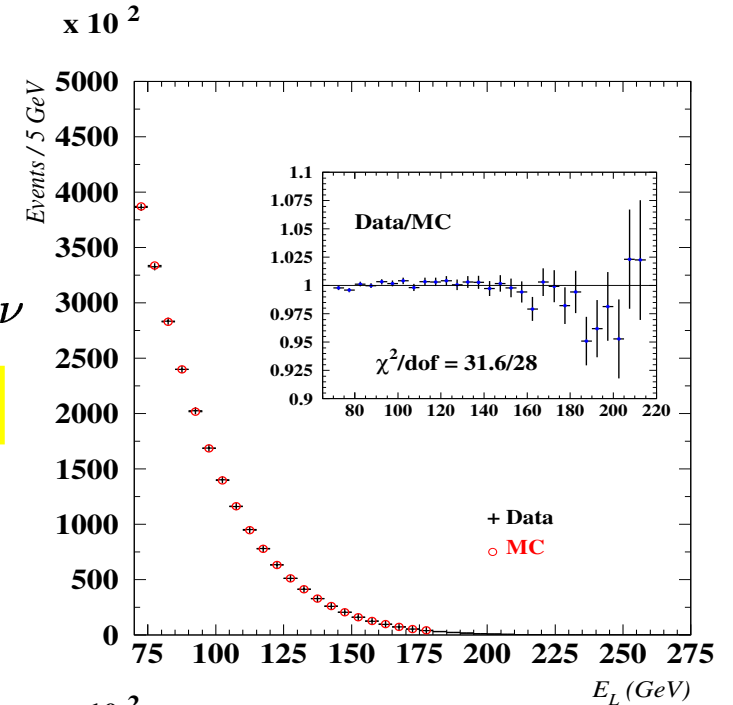
For every event there are two energy solutions E_L and E_H



Use the LOW solution

- 4×4 MeV² cells
- Correct solution in 61% of events
- 39% of events reconstructed in the same cell where generated

$$\epsilon = \frac{\rho(E_{\mu(Low)}^*, E_{\pi(Low)}^*)^{MC Rec}}{\rho(E_{\mu(TRUE)}^*, E_{\pi(TRUE)}^*)^{MC Gen}}$$



Radiative Corrections

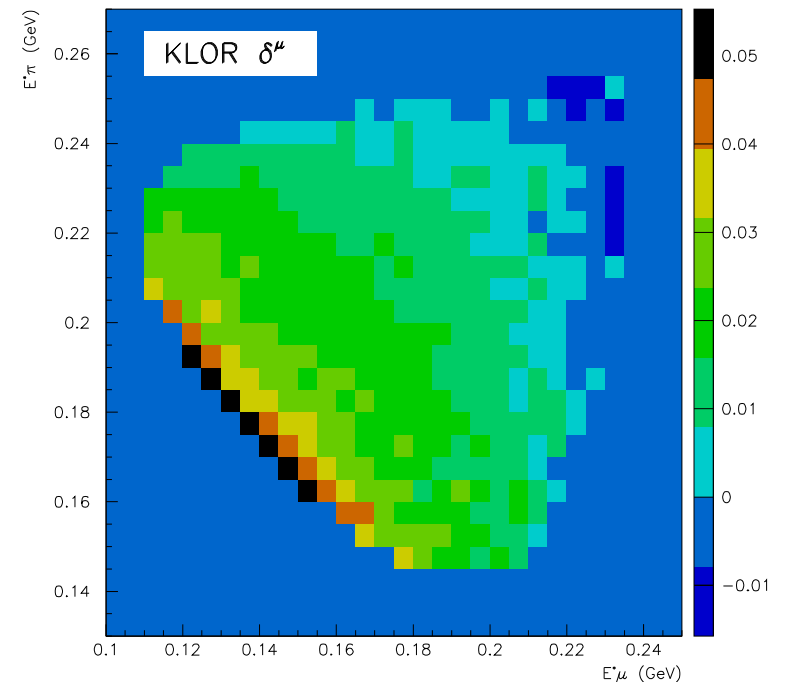
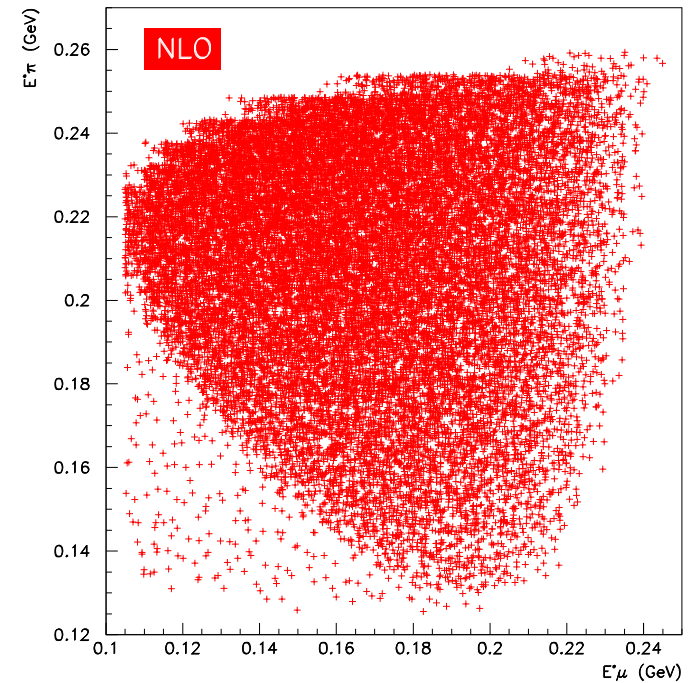
Simulation with KLOR
by T. Andre (hep-ph0406006v3)

Revisited version of the
phenomenological model
of Ginsberg (1966)

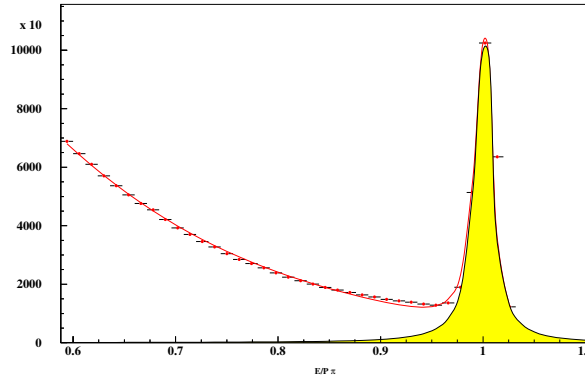
$$\Gamma_{K\mu 3}^{NLO} / \Gamma_{K\mu 3}^{BORN} = (1 + \delta_{EM}^{\mu})$$

$$\delta_{EM}^{\mu} = 2\Delta_{EM}^{K\mu} = (1.9 \pm 0.3)\%$$

- Small effect on the acceptance
- Significant distortions on the Dalitz plot



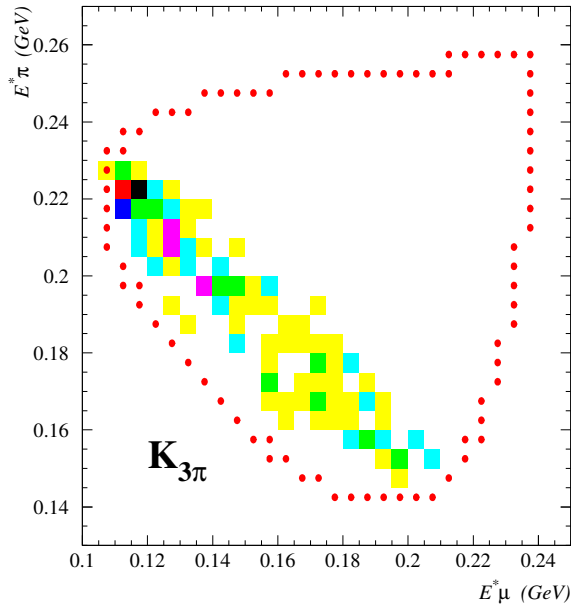
Background



$K_L \rightarrow \pi^\pm e^\mp \nu_e$
Removed by E/p cut

$$\mathcal{P}_{K_{e3}}^{cont} = (6.59 \pm 0.09) \times 10^{-4}$$

→ Negligible effect on f.f.



$K_L \rightarrow \pi^+ \pi^- \pi^0$
Removed by $P_0'^2$ cut

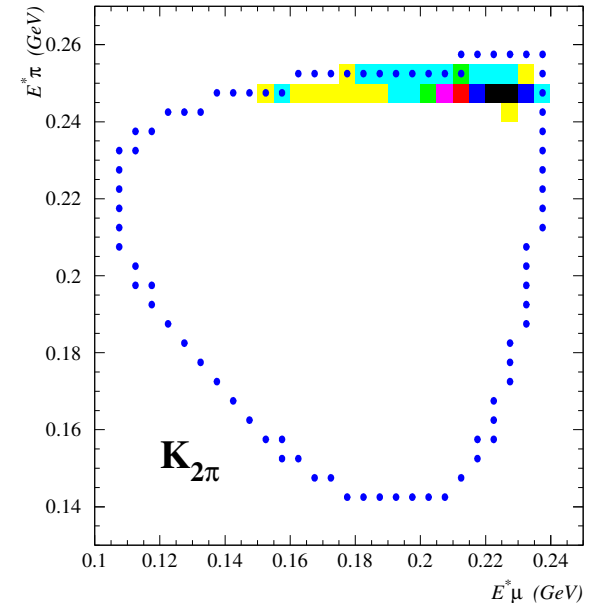
$$\mathcal{P}_{3\pi}^{cont} = (6.31 \pm 0.16) \times 10^{-4}$$

→ Small effect on f.f.

$K_L \rightarrow \pi^+ \pi^-$
Disfavoured by the small BR

$$\mathcal{P}_{2\pi}^{cont} = (5.63 \pm 0.16) \times 10^{-4}$$

→ Big effect on f.f.



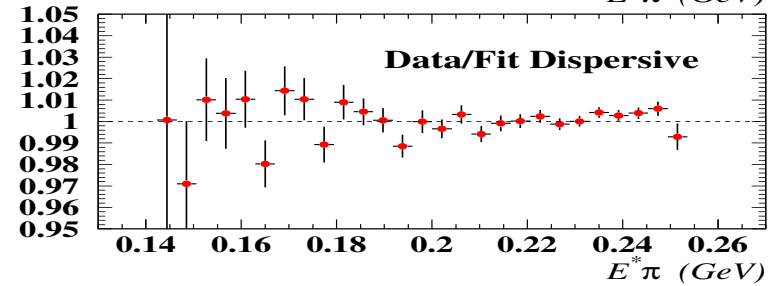
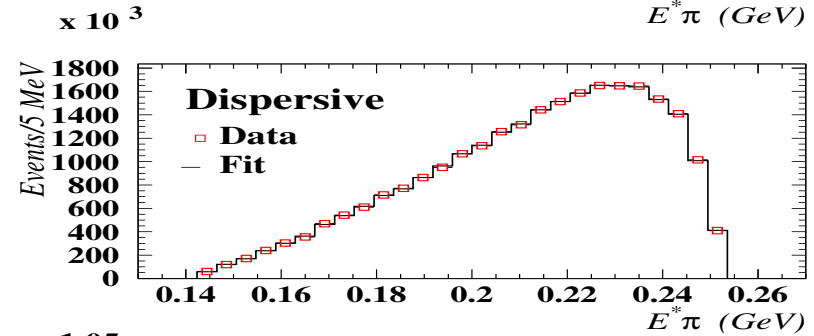
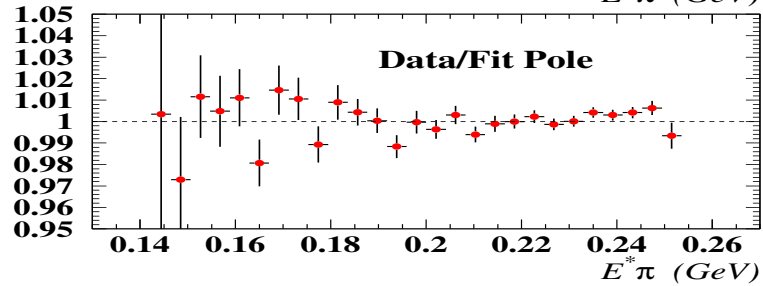
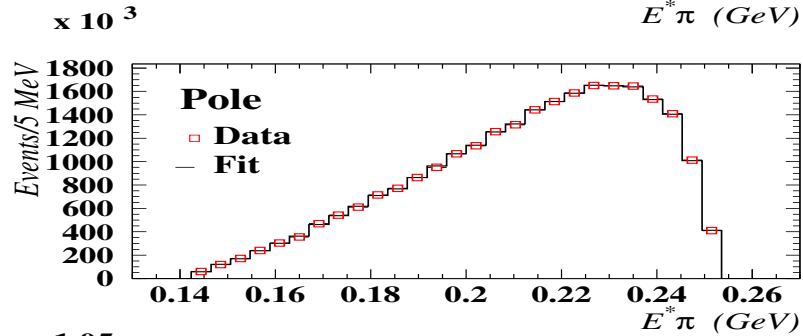
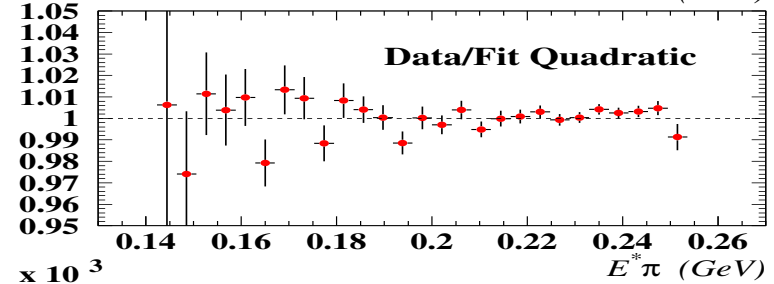
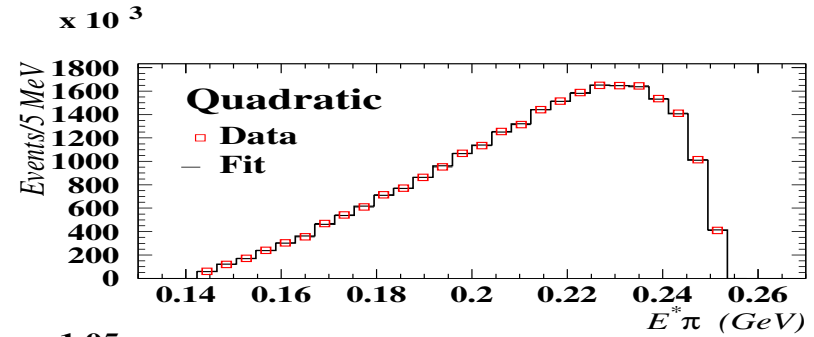
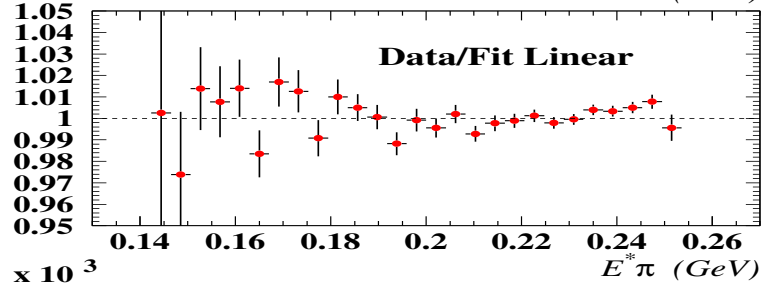
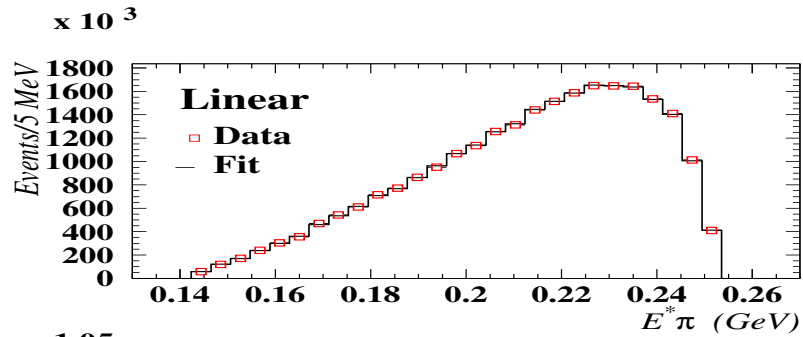
All of these sources
need a $\pi \rightarrow \mu$ decay

The NA48 Results for the $K_{\mu 3}$ Form Factor Slopes

Linear ($\times 10^{-3}$)		Quadratic λ_+ ($\times 10^{-3}$)	
λ_+	$= 26.7 \pm 0.6 \pm 0.8$	λ'_+	$= 20.5 \pm 2.2 \pm 2.4$
λ_0	$= 11.7 \pm 0.7 \pm 1.0$	λ''_+	$= 2.6 \pm 0.9 \pm 1.0$
χ^2/ndf	$= 604.0/582$	λ_0	$= 9.5 \pm 1.1 \pm 0.8$
		χ^2/ndf	$= 595.9/581$
Pole (MeV/c ²)		Dispersive ($\times 10^{-3}$)	
m_V	$= 905 \pm 9 \pm 17$	Λ_+	$= 23.3 \pm 0.5 \pm 0.8$
m_S	$= 1400 \pm 46 \pm 53$	$\ln C$	$= 143.8 \pm 8.0 \pm 11.2$
χ^2/ndf	$= 596.7/582$	χ^2/ndf	$= 595.0/582$

- Like other exp. we observe a quadratic term in the expansion of $f_+(t)$
- λ_0 is smaller than what recently reported

Data vs. Fit Comparison



Current Data on $K_{\ell 3}$ Form Factor Slopes

Using the quadratic fit results for comparison

	$\lambda'_+ \times 10^3$	$\lambda''_+ \times 10^3$	$\lambda_0 \times 10^3$	Events	Analysis	Ref.
KLOE	25.5 ± 1.8	1.4 ± 0.8		2.0×10^6 K_{e3}	t from K_S	PLB 632 (2006)
	Use K_{e3}	Use K_{e3}	15.6 ± 2.6	1.8×10^6 $K_{\mu 3}$	$E_\nu + K_{e3}$	Preliminary
KTeV	21.7 ± 2.0	2.9 ± 0.8		1.9×10^6 K_{e3}	t_\perp^π	PRD 70 (2004)
	17.0 ± 3.7	4.4 ± 1.5	12.8 ± 1.8	1.5×10^6 $K_{\mu 3}$	t_\perp^π	
ISTRA+	24.9 ± 1.7	1.9 ± 0.9		0.9×10^6 K_{e3}^-	$\rho(E_\mu, E_\pi)$	PLB 589 (2004)
	23.0 ± 6.4	2.3 ± 2.3	17.1 ± 2.2	0.9×10^6 $K_{\mu 3}^-$	$\rho(E_\mu, E_\pi)$	PLB 581 (2004)
NA48	28.0 ± 2.4	0.4 ± 0.9		5.6×10^6 K_{e3}	$\rho(t_l, t_h, E_\nu)$	PLB 604 (2004)
	20.5 ± 3.3	2.6 ± 1.5	9.5 ± 1.4	2.3×10^6 $K_{\mu 3}$	$\rho(E_\mu, E_\pi)_l$	PLB 647 (2007)

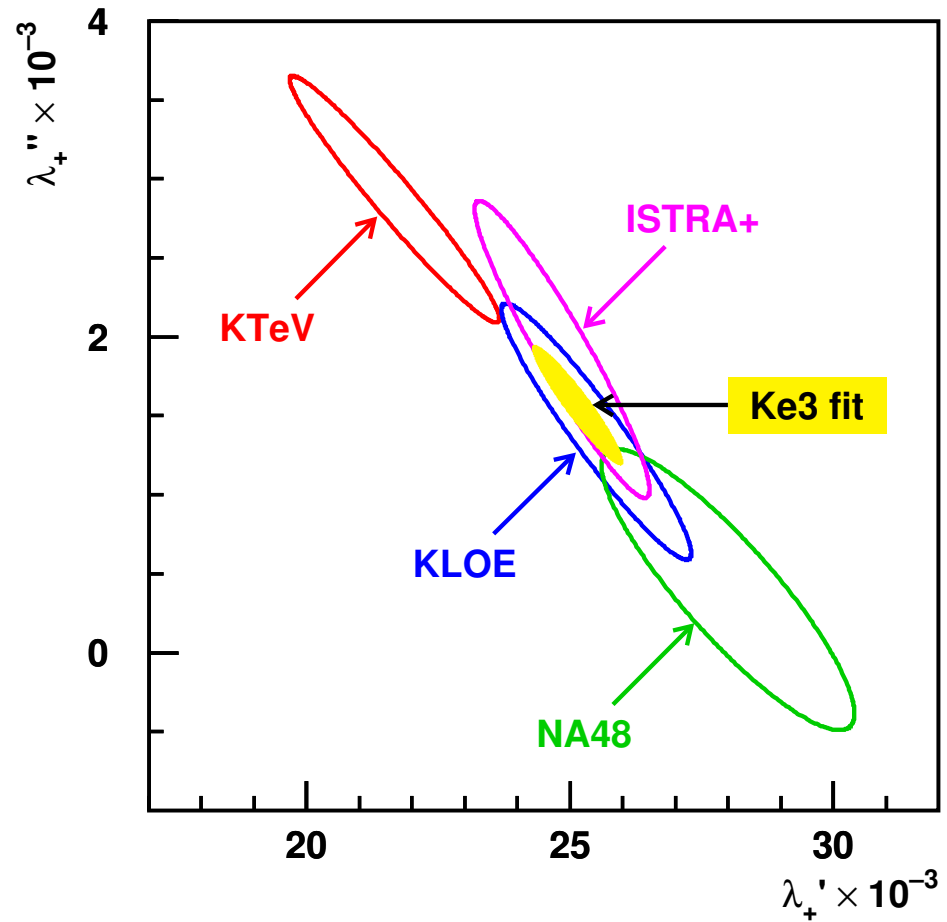
ISTRA+ Multiplied by $(m_{\pi^+}/m_{\pi^0})^2 = 1.069$. No systematic errors nor correlations given in the paper

K_ℓ Form Factor Slopes

K_{e3} slopes only

$$\lambda'_+ = (25.1 \pm 0.9) \times 10^3$$
$$\lambda''_+ = (1.6 \pm 0.4) \times 10^3$$

Correlation $\rho = -94.1\%$



(Ellipses = 1σ contour)

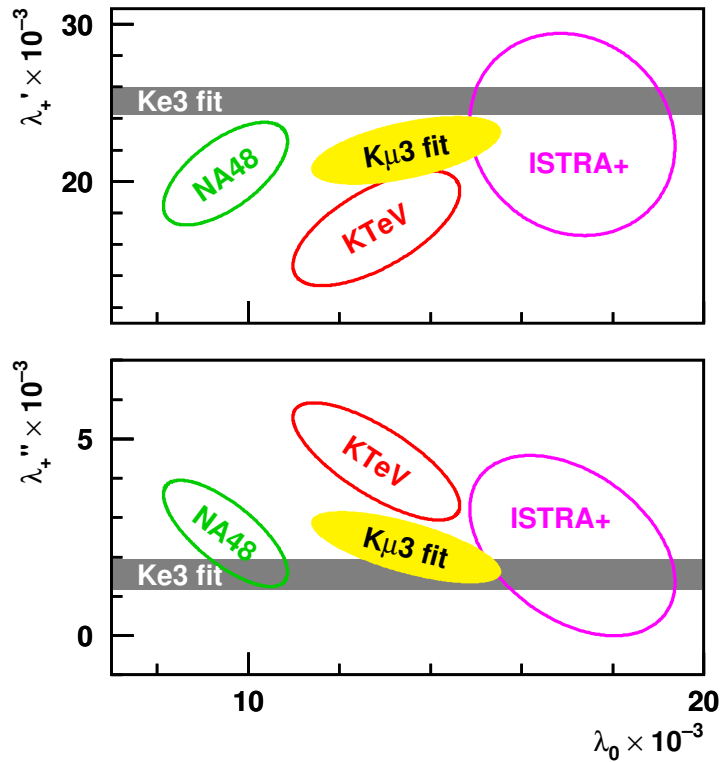
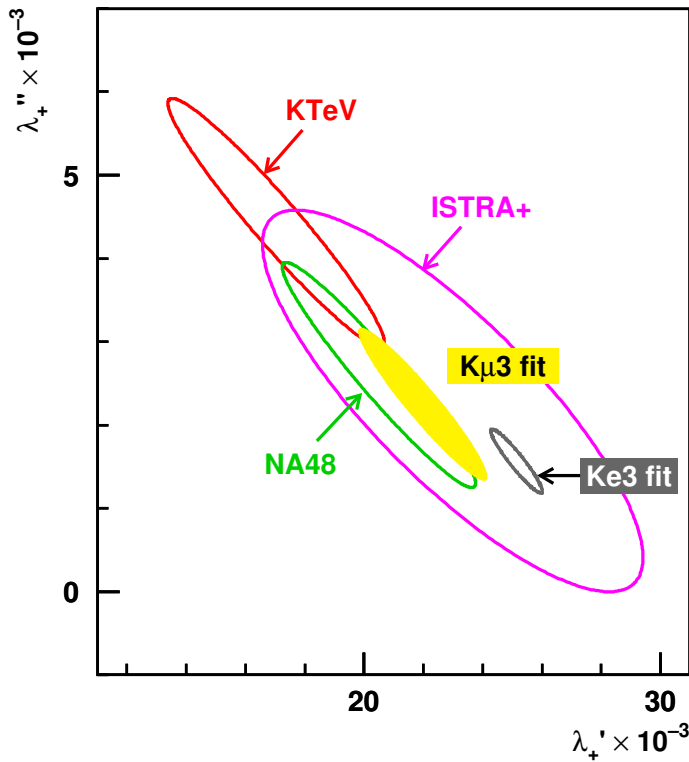
K_ℓ Form Factor Slopes

$K_{\mu 3}$ slopes only

$$\lambda'_+ = (22.1 \pm 2.2) \times 10^3$$

$$\lambda''_+ = (2.3 \pm 0.9) \times 10^3$$

$$\lambda_0 = (13.5 \pm 2.1) \times 10^3$$

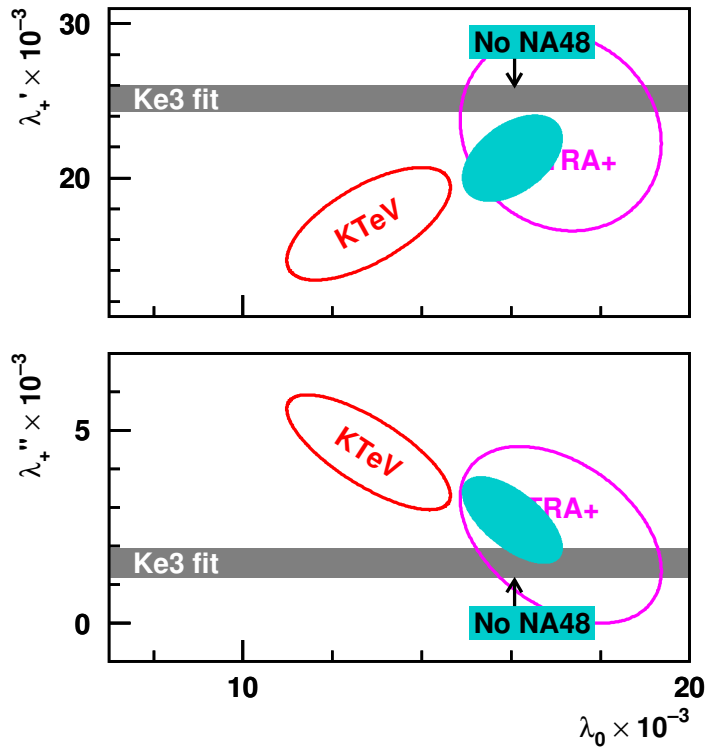
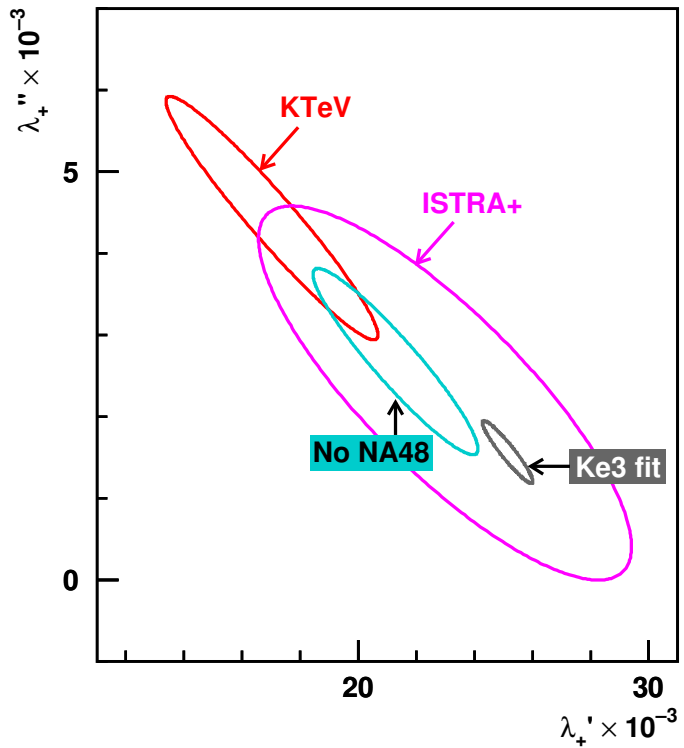


	λ'_+	λ''_+
λ'_+		-0.949
λ_0	0.540	-0.679

Agreement with K_{e3} poor, mostly driven by NA48 value on λ_0

K_ℓ Form Factor Slopes

Excluding NA48 $K_{\mu 3}$ from the fit



F_{net}^{flavi} fit to K_ℓ Form Factor Slopes

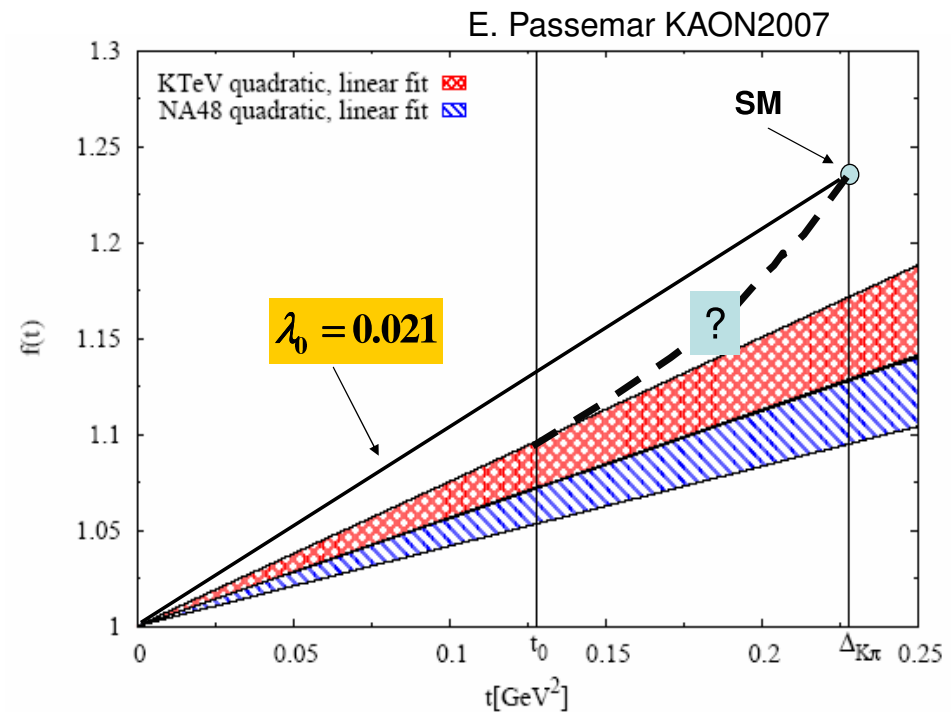
Slope Parameters $\times 10^3$				Integrals	
λ'_+	24.82	± 1.10	S=1.4	$I(K_{e3}^0)$	0.15454(29)
λ''_+	1.64	± 0.44	S=1.3	$I(K_{e3}^\pm)$	0.15889(30)
λ_0	13.38	± 1.19	S=1.9	$I(K_{\mu 3}^0)$	0.10209(31)
χ^2/ndf	53/13 (10^{-6})			$I(K_{\mu 3}^\pm)$	0.10504(32)

All Experiments

The rescaling of the errors and the change in λ_0 has anyway a negligible effect on $|V_{us}|$

λ_0 and the Callan–Treiman Point

- λ_0 is the slope of the power expansion of $f_0(t)$ around $t = 0$
- In order to satisfy the CT theorem a value of λ_0 bigger than what measured in any of the recent experiments is needed



- Curvature of the ff cannot be neglected going up to $\Delta_{K\pi}$

Use the new dispersive parametrization

f_0 and the RHCs

- NA48 has done the first direct measurement of $\ln C$ using the dispersive parametrization

$$\ln C = 0.1438 \pm 0.0080_{stat} \pm 0.0112_{syst}$$

- One parameter allows to extract slope and curvature of $f_0(t)$

$$\lambda'_0 = 0.0089 \pm 0.0012$$

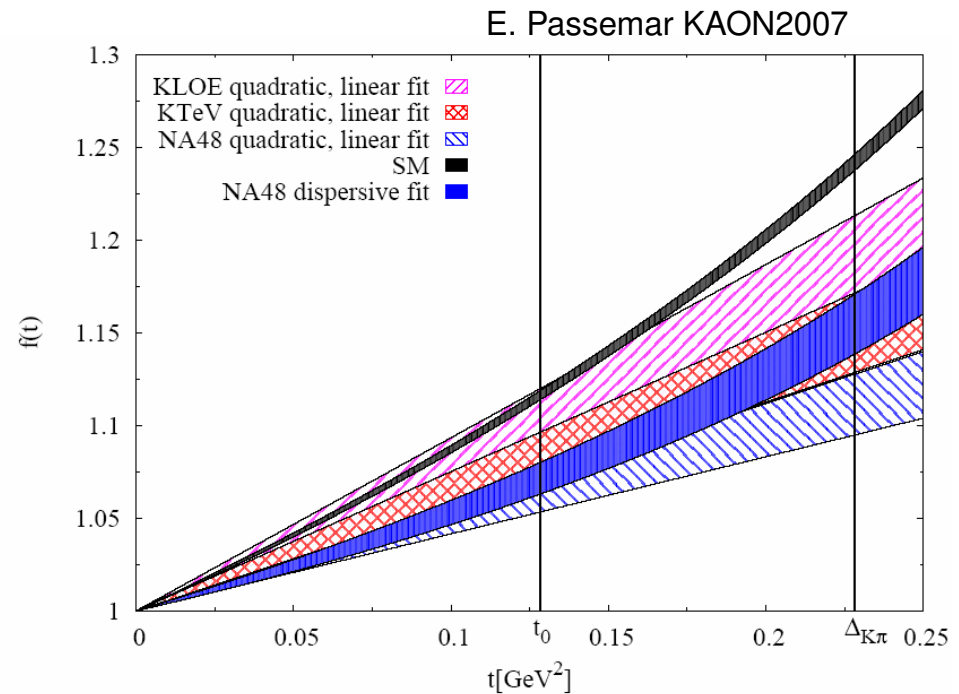
$$\lambda''_0 = (4.95 \pm 0.54)10^{-4}$$

- Big discrepancy with $\ln C_{SM}$

$$\ln C_{SM} = 0.2151 \pm 0.0045 + \tilde{\Delta}_{CT}$$

- Interpreted in terms of RHCs

$$\Delta(\epsilon) = 2(\epsilon_S - \epsilon_{NS}) + \tilde{\Delta}_{CT} = -0.071 \pm 0.014_{NA48} \pm 0.002_{theo} \pm 0.005_{ext}$$



f_0 and the RHCs

⇒ NA48 sees effect (5σ) in $K_{\mu 3}$ at the Callan-Treiman point

f_0 and the RHCs

⇒ NA48 sees effect (5σ) in $K_{\mu 3}$ at the Callan-Treiman point

Did one observe couplings
of right handed quarks to W ?

Jan Stern, IPN Orsay

Kaon 07, Frascati, May 21-25, 2007

V. Bernard, M. Oertel, E. Passemar, J. Stern : Phys.Lett. B638 (2006) 480
J. Hirn et J. Stern : Phys.Rev. D73 (2006) + in preparation

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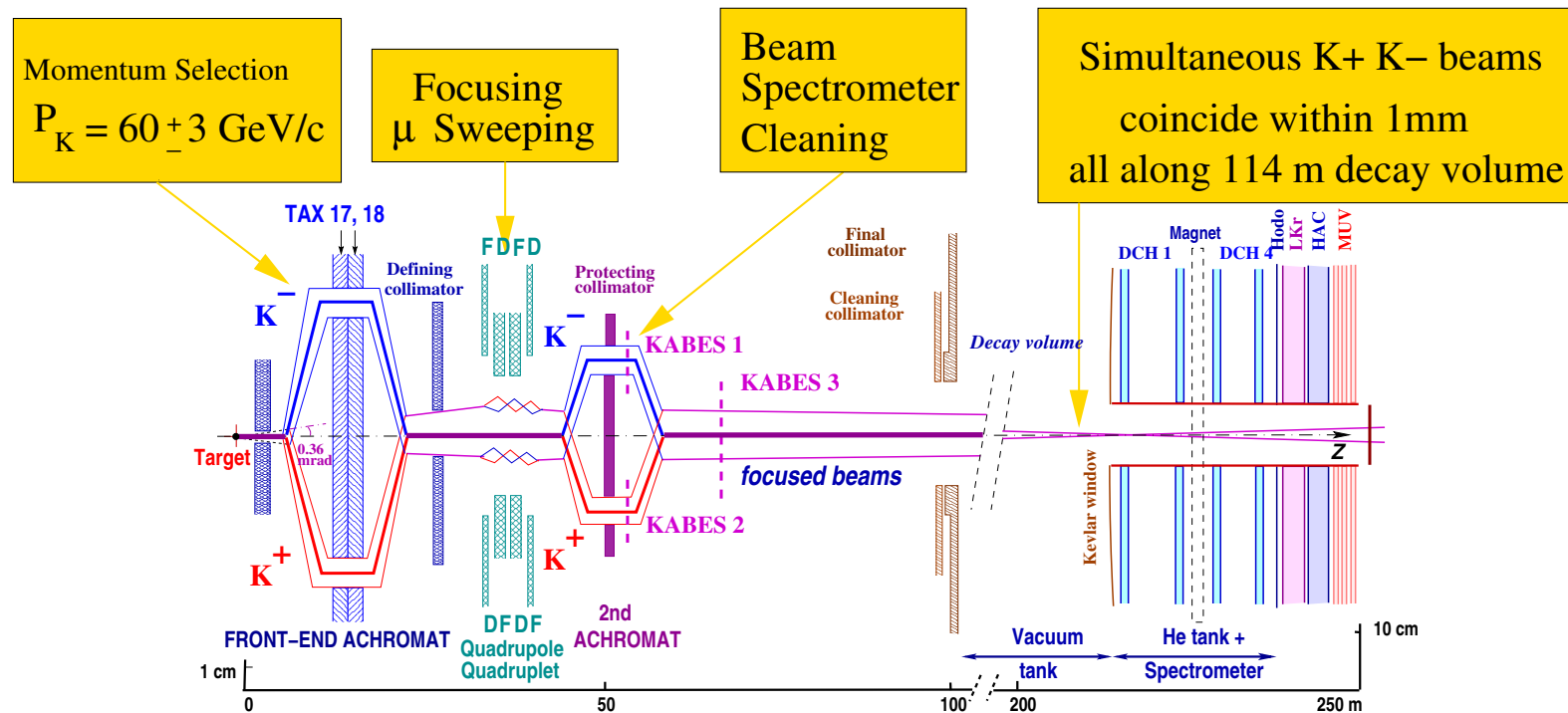
V. Bernard, M. Oertel, E. Passemar, J. Stern : Phys.Lett. B638 (2006) 480
J. Hirn et J. Stern : Phys.Rev. D73 (2006) + in preparation

- A good question ! ...No answer yet...
- No other experiment has performed yet a fit with the dispersive parametrization
- Other experiments disagree with NA48 in the slope λ_0 of the scalar form factor
- Data of other experiments need to be investigated

Situation to be clarified

$K_{\ell 3}^{\pm}$ Form Factors @ NA48/2

- K^{\pm} collected during 2003-2004 data taking NA48/2 Experiment
(Main purpose search for direct CP violation in $K^{\pm} \rightarrow 3\pi$ decays)
- Special low intensity ($\times 1/8$) minimum bias runs
- Simultaneous K^+ and K^- beams
- K^+ flux $\simeq 3.2 \times 10^6$; $K^+/K^- \simeq 1.78$ (production rate @target)



Summary

- $K_{\ell 3}$ decays & CKM unitarity

- Very intense activity in the last 3 years in the $K_{\ell 3}$ decays both on the exp and theory side
- $|V_{us}|$ is one of the best known CKM matrix element
⇒ Precision frontier in CKM studies: $\sigma|V_{us}f_+(0)| \sim 0.2\%$
- Dominant contribution to uncertainty on $|V_{us}|$ still from $f_+(0)$
- Slight difference between the values for $f_+(0)$ obtained with analytic calculations and Lattice QCD
- The LECs appearing in the ChPT $O(p^6)$ expansion could be determined by the slope and curvature of f_0
⇒ But they cannot be determined experimentally...
- Waiting the progresses of Lattice QCD...in the meanwhile use for $f_+(0)$ the LR value
- Differences in $|f_+(0)V_{us}|$ obtained in K^0 and K^\pm decays
⇒ Isospin correction underestimated by $\sim 1\%$?

Summary

- **$K_{\mu 3}$ decays & non SM physics**
 - The $K_{L\mu 3}$ decays can be used to test the existence of new physics
 - The value of f_0 at the Callan-Treiman point determines the amount of RHCs
 - New dispersive parametrization for f_0 (and f_+)
 - **The NA48 $K_{\mu 3}$ form factor analysis**
 - Big discrepancy w.r.t SM predictions for $\ln C$
 - No other experiment has performed a fit with the dispersive parametrization
 - The result of the scalar form factor however is controversial
- ⇒ Not possible to draw any conclusion yet, more experimental input is needed

Additional Material

Systematic Uncertainties

- Systematic and total uncertainty for the four form factor parametrizations analysed

	$\Delta\lambda_+$	$\Delta\lambda_0$	$\Delta\lambda'_+$ $\times 10^{-3}$	$\Delta\lambda''_+$	$\Delta\lambda_0$	Δm_V MeV/c ²	Δm_S	$\Delta\Lambda_+$ $\times 10^{-3}$	$\Delta \ln C$ $\times 10^{-3}$
Background	± 0.0	± 0.1	± 0.2	± 0.1	± 0.0	± 0	± 5	± 0.0	± 1.2
Acceptance	± 0.4	± 0.5	± 0.7	± 0.4	± 0.4	± 7	± 22	± 0.4	± 5.0
TRK_{dist} @ LKr	± 0.4	± 0.4	± 0.5	± 0.4	± 0.3	± 10	± 20	± 0.4	± 5.4
P_{MIN}	± 0.1	± 0.3	± 0.4	± 0.1	± 0.3	± 1	± 20	± 0.1	± 3.1
$P_\nu^* - P_{\nu T}$	± 0.2	± 0.2	± 0.5	± 0.2	± 0.2	± 6	± 10	± 0.2	± 2.2
K_L spectrum	± 0.2	± 0.4	± 0.0	± 0.0	± 0.3	± 4	± 20	± 0.2	± 4.1
HIGH solution	± 0.3	± 0.0	± 0.6	± 0.2	± 0.2	± 8	± 12	± 0.4	± 1.9
MUV reconstruction	± 0.1	± 0.1	± 0.1	± 0.0	± 0.1	± 2	± 5	± 0.2	± 0.8
Radiative corrections	± 0.2	± 0.4	± 2.0	± 0.7	± 0.3	± 2	± 20	± 0.1	± 4.3
Cell Size	± 0.3	± 0.3	± 0.5	± 0.3	± 0.3	± 5	± 20	± 0.2	± 4.0
Total Systematic	± 0.8	± 1.0	± 2.4	± 1.0	± 0.8	± 17	± 53	± 0.8	± 11.2
Statistical	± 0.6	± 0.7	± 2.2	± 0.9	± 1.1	± 9	± 46	± 0.5	± 8.0
Total Error	± 1.0	± 1.2	± 3.3	± 1.3	± 1.4	± 19	± 70	± 0.9	± 13.8

Data-MC Comparison

