MSSM Higgs Mass

(The Effective Field Theory approach)

Javier Pardo Vega (SISSA / ICTP)

based on: JP and Giovanni Villadoro

[arXiv:1504.05200]

Higgs Hunting Orsay, France, July 30-August 01, 2015

Higgs mass constraint on SUSY

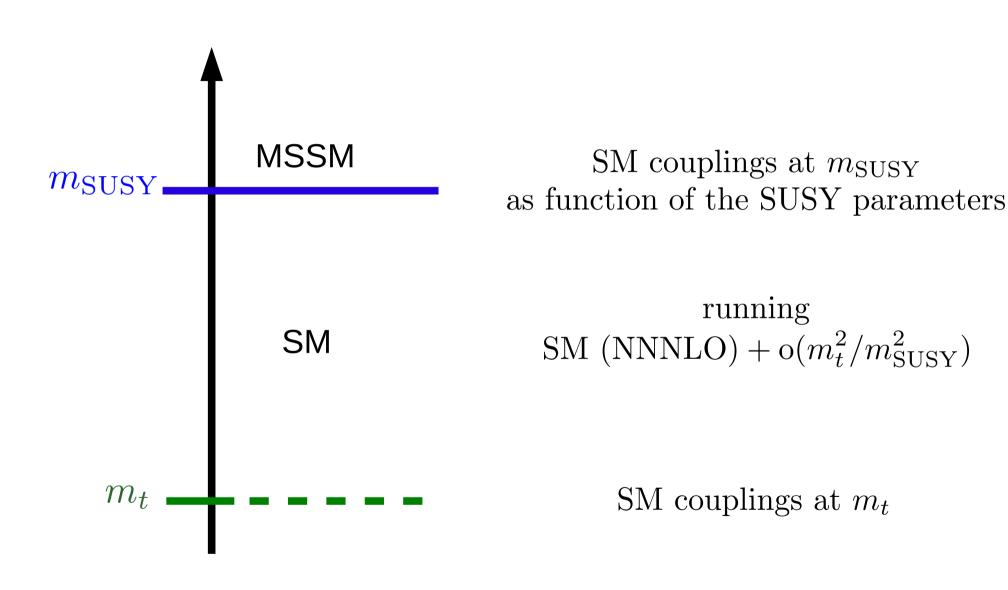
$$m_h^2 \approx m_Z^2 \cos^2 2\beta + \frac{3}{2\pi^2} \frac{m_t^4}{v^2} \left[\ln \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} - \frac{X_t^4}{12m_{\tilde{t}}^4} \right] + \dots$$
 tree-level RG logarithm stop mixing contribution

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 tree-level RG logarithm stop mixing contribution

It is important to calculate the Higgs mass with high precision.

Effective Field Theory calculation



Mathematica Package Susy

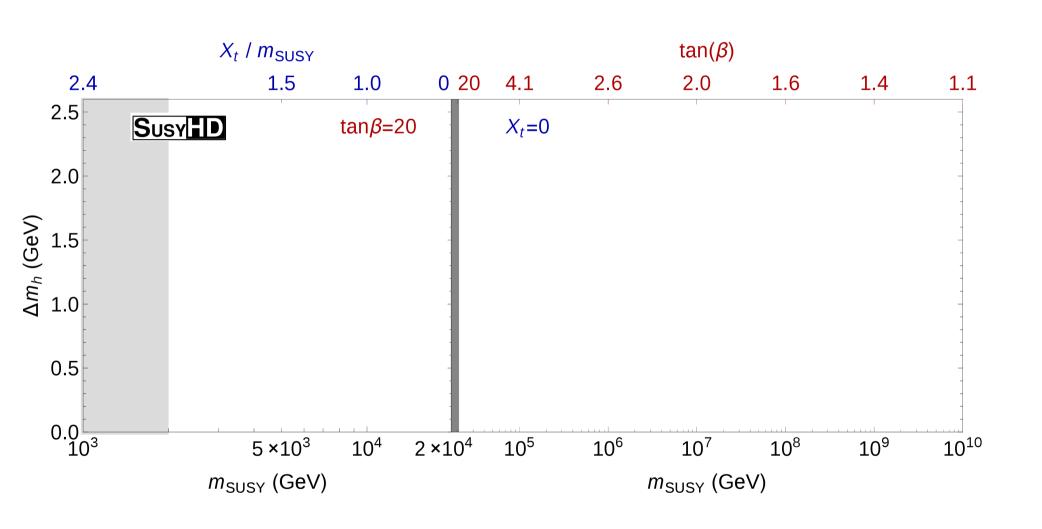


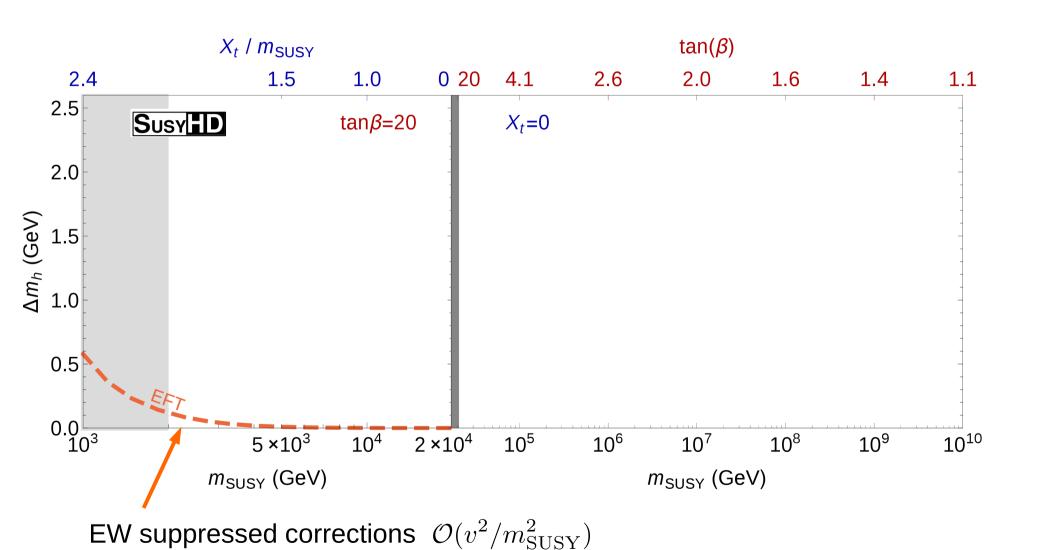
http://www.ictp.it/~susyhd

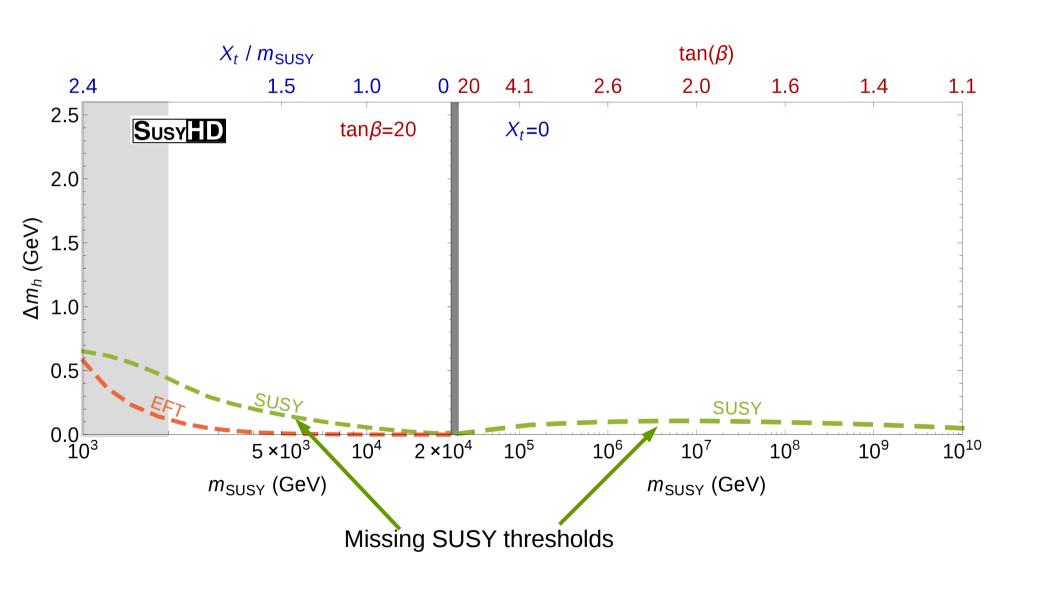
- SetSMparameters $[M_t, \alpha_s]$
- MHiggs [$\{\tan \beta, M_1, M_2, M_3, \mu, A_t, m_{Q_3}, m_{U_3}, m_{D_3}, m_{Q_2}, m_{U_2}, m_{D_2}, m_{D_3}, m_{D_3}$ $\{m_{Q_1}, m_{U_1}, m_{D_1}, m_{L_3}, m_{E_3}, m_{L_2}, m_{E_2}, m_{L_1}, m_{E_1}, m_A\}$
- $\Delta MHiggs[\{...\}]$

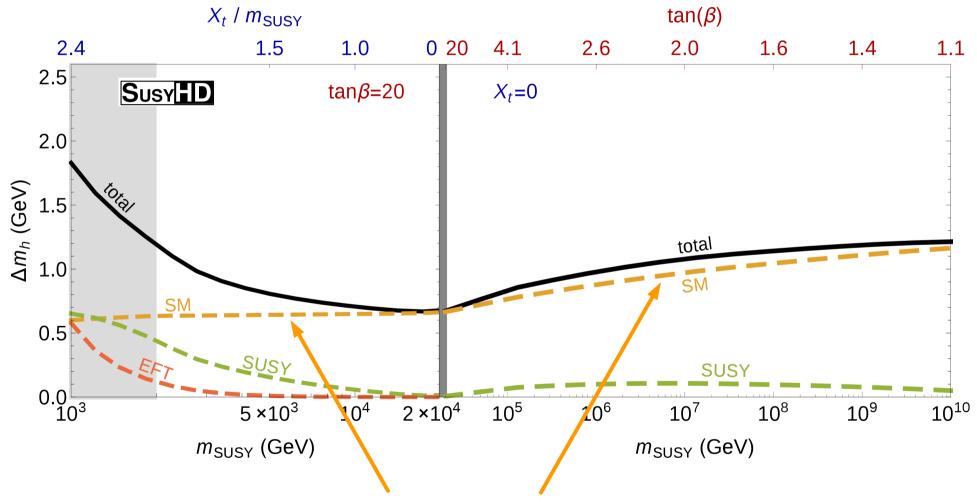
- Interpolated solution of the SM RGEs $\lambda(m_t) = F\left(\lambda(Q), \ln \frac{Q}{m_t}\right)$
- Fast program, Higgs mass can be used as a constraint.

```
In[1]:= << SUSYHD
     SUSYHD v1.0.2 (2015)
     Javier Pardo Vega and Giovanni Villadoro
     http://www.ictp.it/~susyhd
In[2]:= Mh := MHiggs[{tb, m0, At}]
     \Delta Mh := \Delta MHiggs[\{tb, m0, At\}]
ln[4]:= tb := 20; m0 := 2000; At := \sqrt{6} m0;
      {Mh, \DeltaMh}
Out[5]= \{125.467, 1.23442\}
In[6]:= Timing[Mh]
Out[6]= \{0.008000, 125.467\}
ln[7] := SetSMparameters[173.34 + 0.76 \times 2, 0.1184];
      \{Mh, \Delta Mh\}
Out[8]= \{126.767, 1.2656\}
```

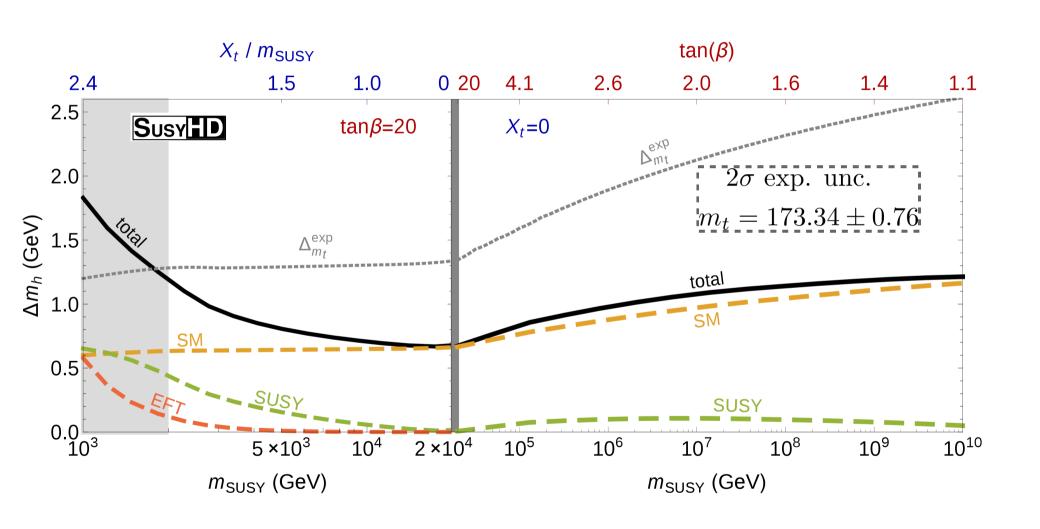




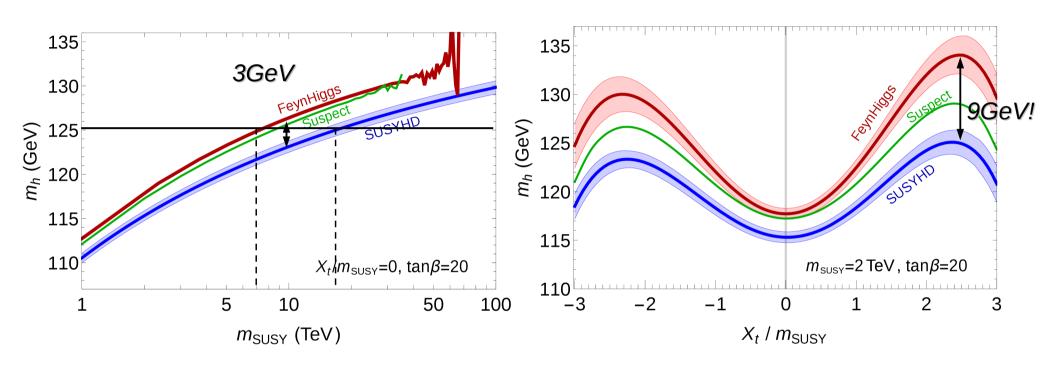




Matching of the SM couplings at the EW scale and their running (SM RGEs)



Comparison with existing computations

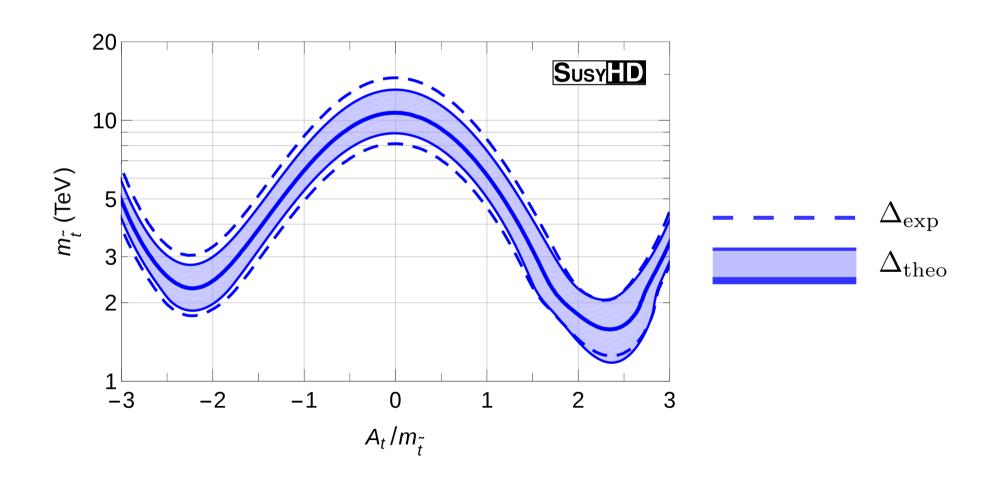


High sensitivity to the determination of the running top Yukawa

$$m_t^{\overline{\rm MS}}(M_t) = 173.34 - 8.00 - 1.90 - 0.59 - 0.21 \text{ GeV}$$
1 loop 2 loop 3 loop 4 loop

Where is SUSY?

 $\tan \beta = 20, \mu = 300 \text{ GeV}, \text{ other sparticles } m = 2 \text{ TeV}$



[Dine, Nir and Shirman '96] [Rattazzi and Sarid '96]

$$\mu\,, \qquad \Lambda = rac{F}{M}\,, \qquad M\,, \qquad N$$

[Dine, Nir and Shirman '96] [Rattazzi and Sarid '96]

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fixed by m_Z

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$$\mu$$
, $\Lambda = \frac{F}{M}$, M , N

fixed by m_Z fixed by m_h

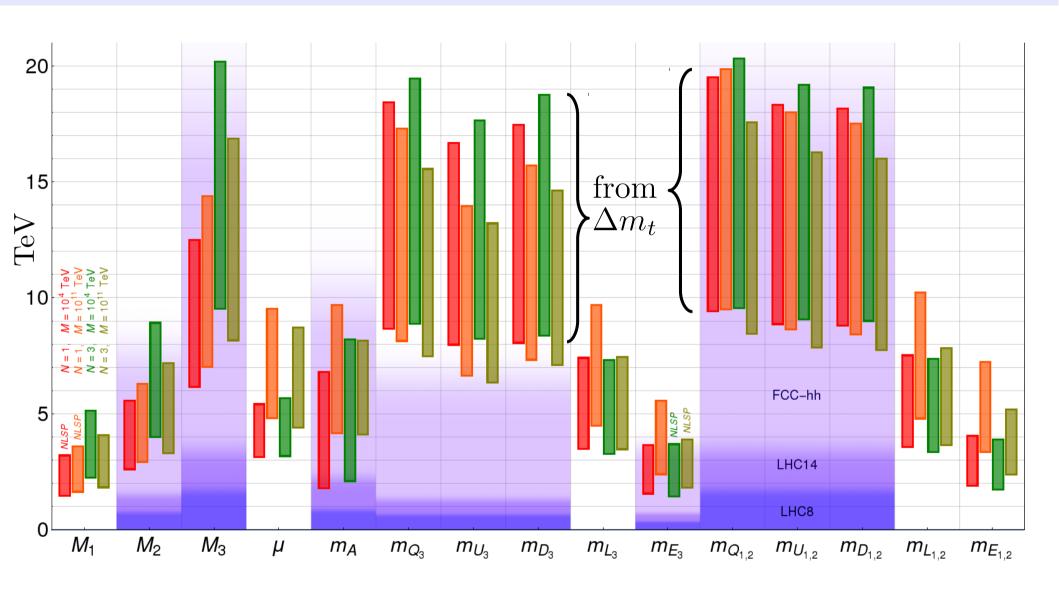
[Dine, Nir and Shirman '96] [Rattazzi and Sarid '96]

$$\mu$$
, $\Lambda = \frac{F}{M}$, M , N

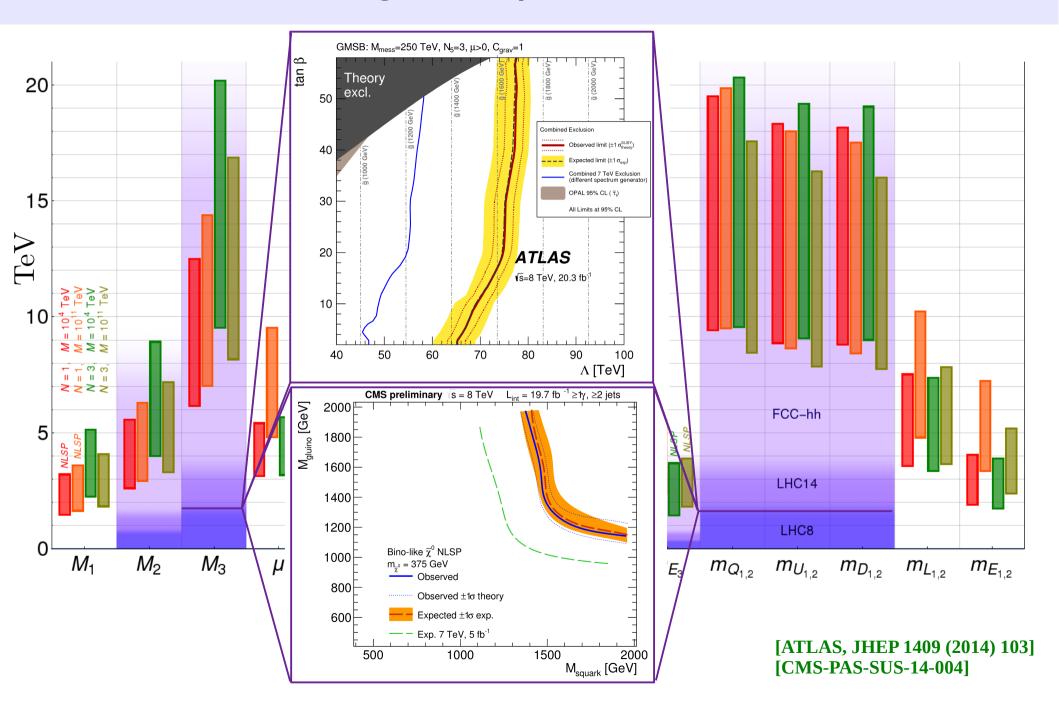
fixed by m_Z fixed by m_h

- **▲** No FCNC
- $B\mu$, $A \text{loop suppressed} \rightarrow \text{large } \tan \beta \sim 50$
- No EDM
- Gauge coupling unification

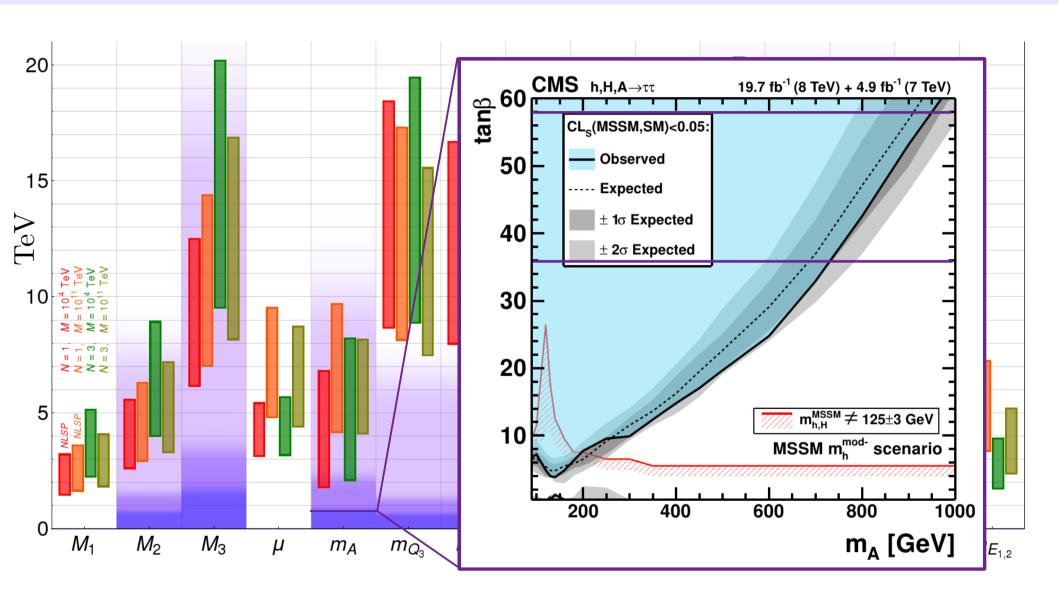
Predicting the spectrum of MGM



Predicting the spectrum of MGM

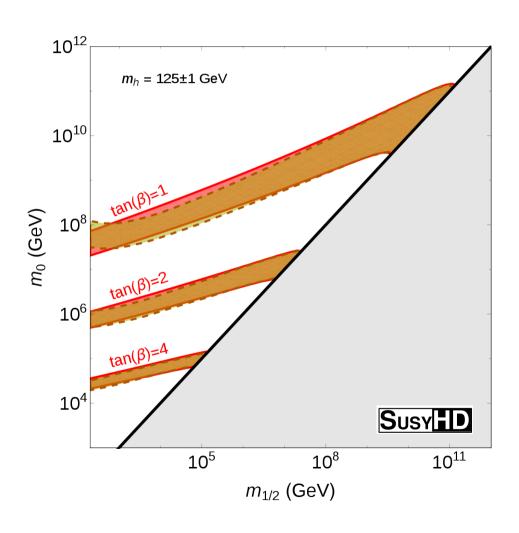


Predicting the spectrum of MGM

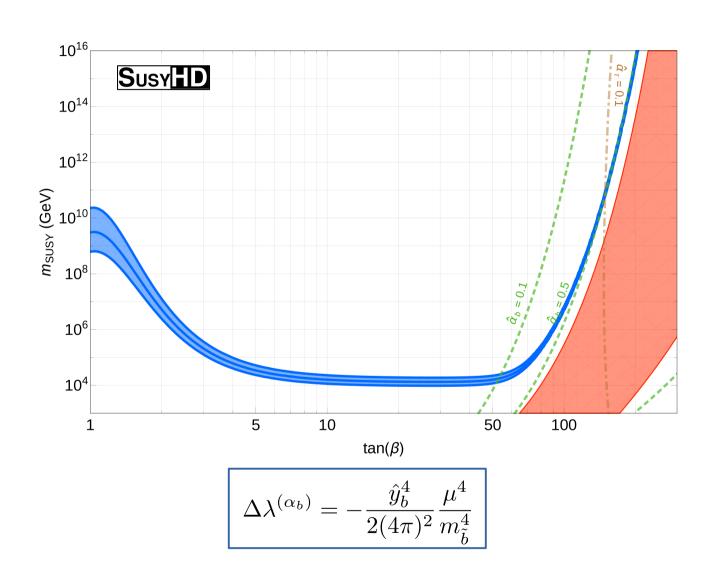


Thanks for your attention!

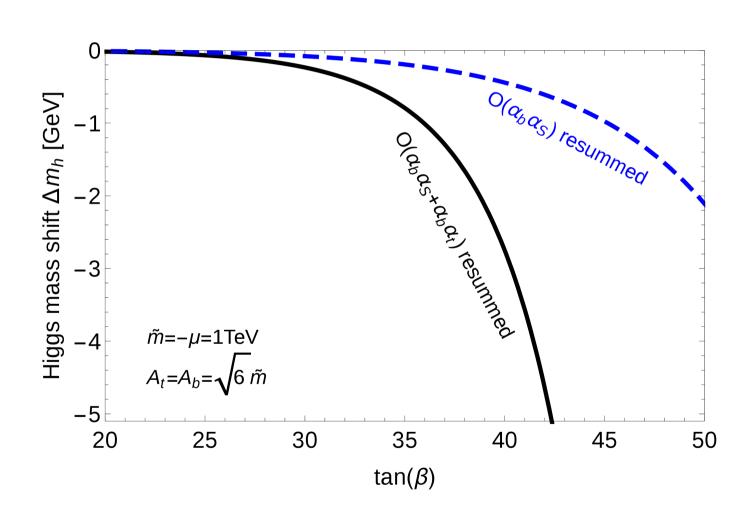
High-Scale and Split EFT calculations



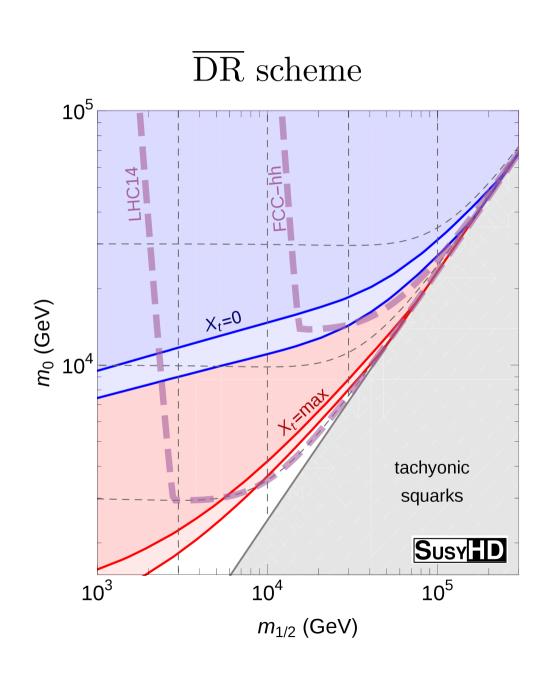
$\tan \beta$ – enhanced corrections



$\tan \beta$ – enhanced corrections (sbottom sector)



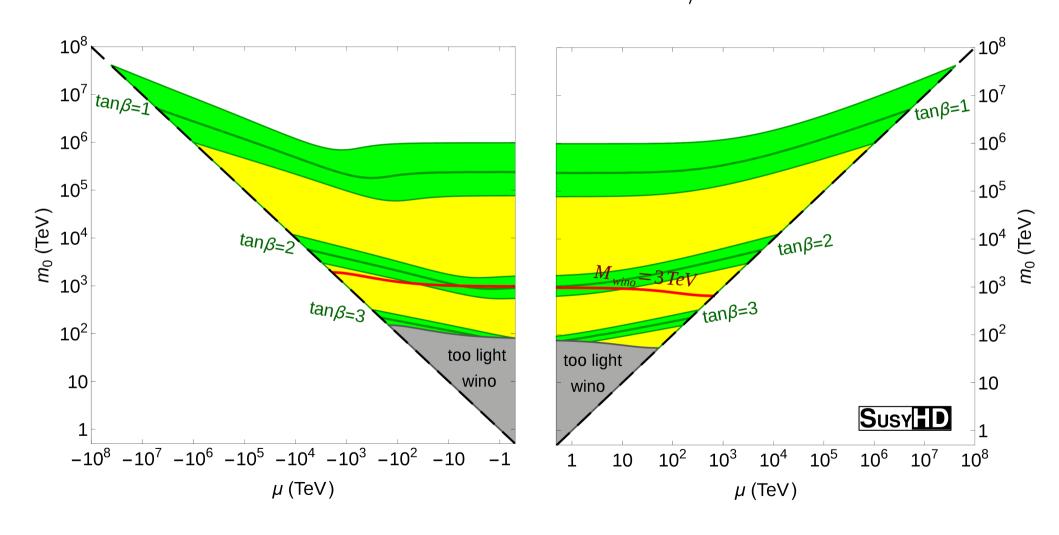
Where is SUSY?



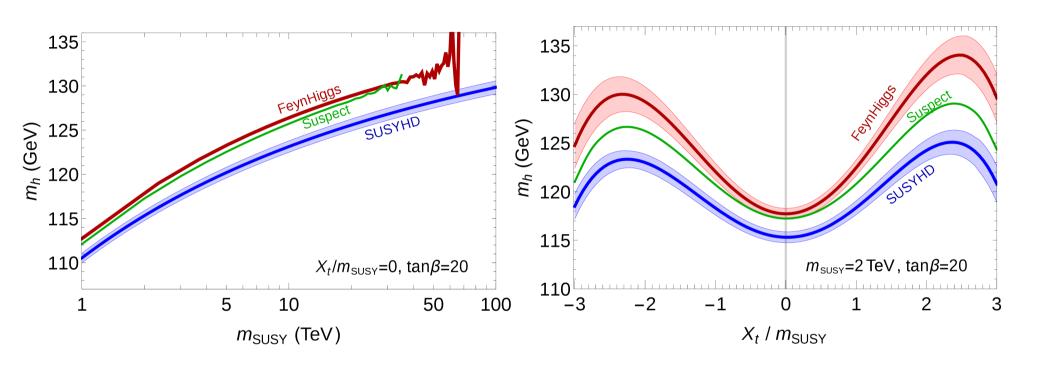
Parameter Space of Anomaly Mediation

[Giudice et. al., hep-ph/9810442, 9901378]

Independent parameters: $m_0 = m_{3/2}, \mu, \tan \beta$



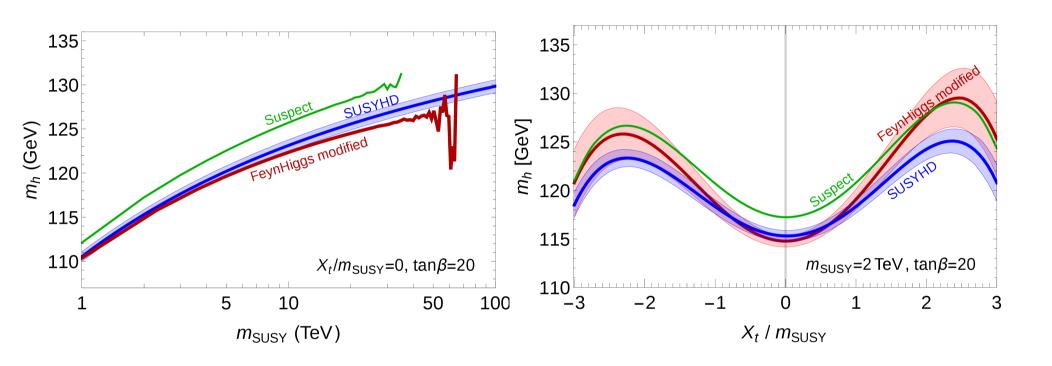
Comparison with existing computations



High sensitivity to the determination of the running top Yukawa

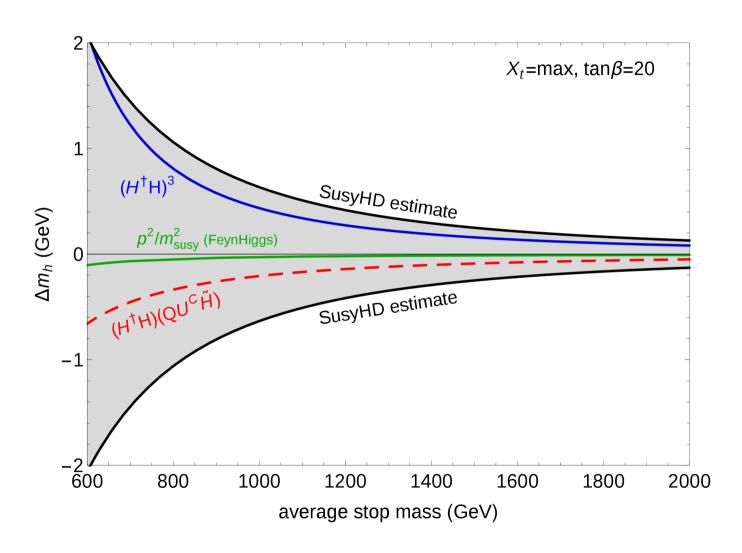
$$m_t^{\overline{\rm MS}}(M_t) = 173.34 - 8.00 - 1.90 - 0.59 - 0.21 \text{ GeV}$$
1 loop 2 loop 3 loop 4 loop

Comparison with existing computations



Changing the value of the running top Yukawa

Estimating the EFT uncertainty



We focus on the contribution from the stops (at maximal mixing)

Small contributions to a longstanding effort

[Pierce, Pokorski, Rosiek, Dabelstein, Zhang, Espinosa, Quiros, Hempfling, Hoang, Hahn, Heinemeyer, Hollik, Weiglein, Brignole, Slavich, Zwirner, Degrassi, Martin, Giuice, Strumia, Wagner, Carena, and many many others]

In particular, we use the results from:

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hep-ph/9912516 (matching bottom Yukawa MSSM) hep-ph/0003246, hep-ph/0105096 (two loop EP contribution to m_h^2) 1108.6077 (2-loop Split RGEs) 1307.3536 (3-loop SM RGEs, matching EW scale) 1407.4081 (SUSY thresholds in the EFT approach) and many others...
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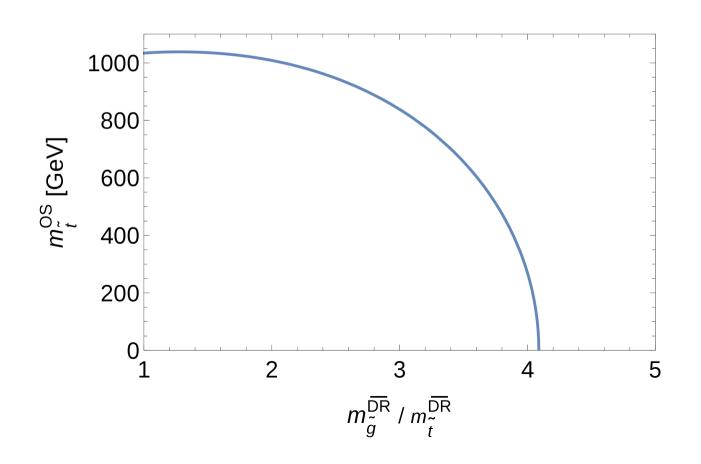
- Re-computation $\mathcal{O}\left(\alpha_t\alpha_s\right)$ SUSY threshold to λ
- Obtain $\mathcal{O}\left(\alpha_t^2\right)$ correction for degenerate scalars
- Include $\tan \beta$ —enhanced corrections (sbottom and stau sectors)
- Estimate of theoretical uncertainties in the EFT calculation
- Computation in both $\overline{
 m DR}$ and OS schemes
- Mathematica Package SusyHD

Conversion \overline{DR} – OS squark masses

$$\delta m^2 = (m^2)^{\overline{DR}} - (m^2)^{OS} = \text{Re}\,\hat{\Pi}\,(m^2)$$

 $\hat{\Pi}(m^2)$: self-energy of the particle

[Degrassi, Slavich, Zwirner, arXiv: 0105096]



Possible Improvements

- Reduce experimental uncertainty of the top mass
- Calculation of missing SM thresholds and RGEs

$$\Delta \lambda^{(\alpha_t \alpha_s^2)}, \quad \beta(\lambda)^{(\alpha_t \alpha_s^3)}, \quad \beta(y_t)^{(\alpha_s^4)}$$

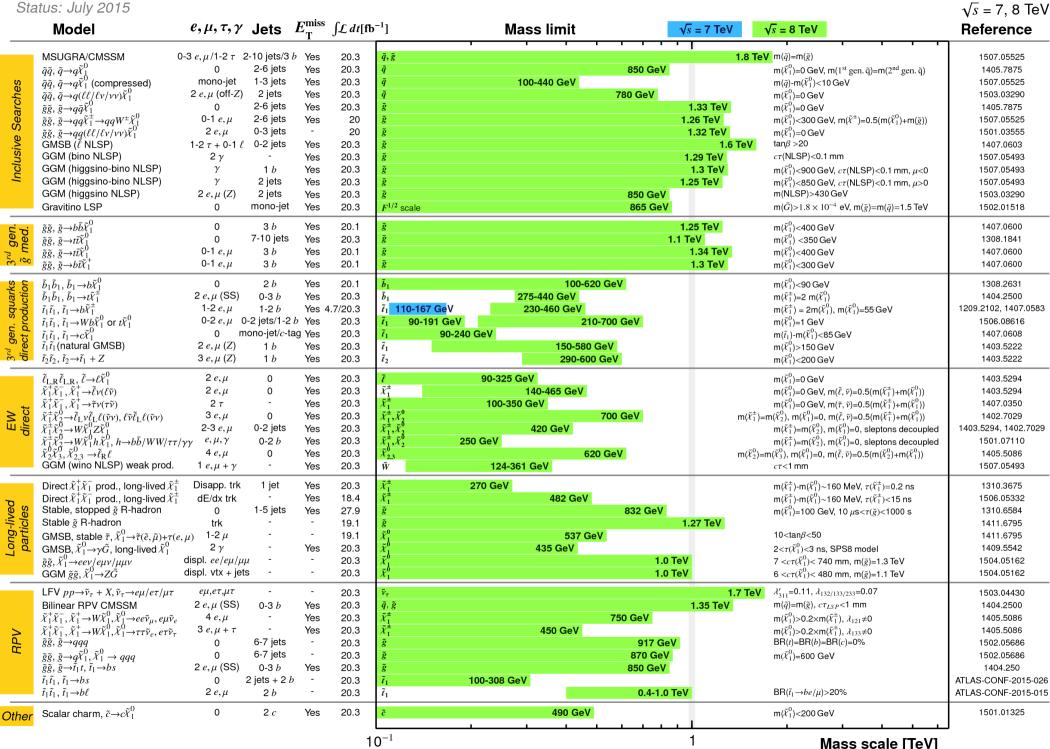
- Include $\mathcal{O}(v^2/m_{\mathrm{SUSY}}^2)$ corrections in the EFT expansion
- Calculation of SUSY thresholds

$$\mathcal{O}(\alpha_t^2)$$
 general, $\mathcal{O}(\alpha_t \alpha, \alpha_s \alpha), \mathcal{O}(\alpha_b \alpha_s, \alpha_b \alpha_t, \alpha_b^2), \mathcal{O}(\alpha_t \alpha_s^2)$

- In the code:
 - run the MSSM parameters or integrate with spectrum calculators
 - further optimization

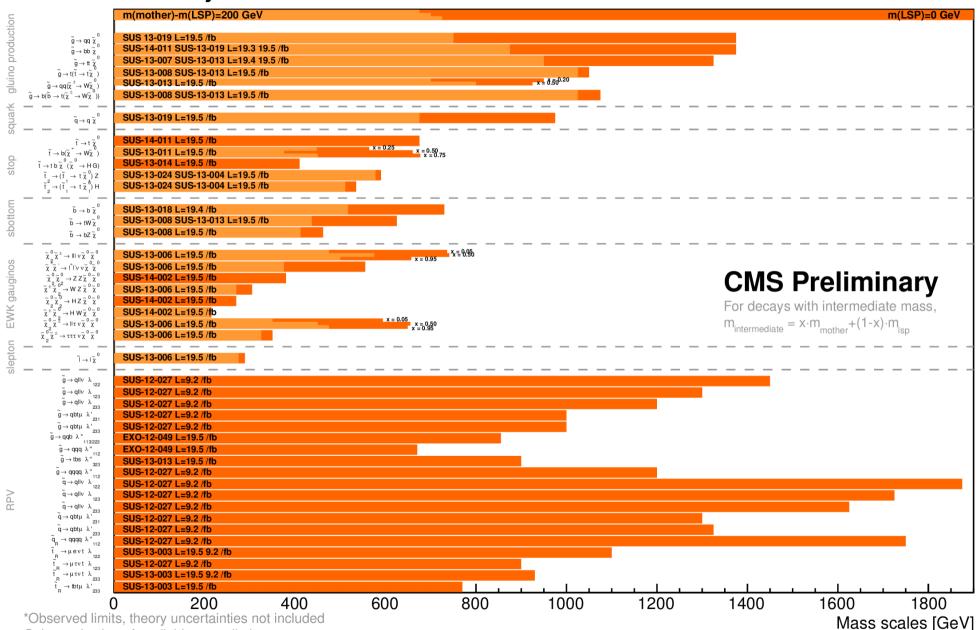
ATLAS SUSY Searches* - 95% CL Lower Limits

ATLAS Preliminary





ICHEP 2014



Only a selection of available mass limits

Probe *up to* the quoted mass limit