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# ADAPTIVE MULTILEVEL SPLITTING FOR MONTE CARLO PARTICLE TRANSPORT

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PHENIICS DOCTORAL SCHOOL DAYS  
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# INTRODUCTION

PhD at CEA since october 1<sup>st</sup> 2014, directed by

**Cheikh DIOP** (CEA) and **Tony LELIÈVRE** (CERMICS-ENPC)

And supervised by

**Eric DUMONTEIL**

**Goal:** Adapt a mathematical Monte Carlo variance reduction technique to the field of particle transport. Applications to shielding simulations in the code TRIPOLI-4®.

## Monte Carlo particle transport

- Monte Carlo transport simulations
- Variance reduction

## Adaptive Multilevel Splitting

- The AMS algorithm
- Implementation

## Results

- Implementation validation
- Comparison between AMS and TRIPOLI-4®

## Conclusion

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# MONTE CARLO PARTICLE TRANSPORT

Goal of Monte Carlo particle transport simulations:

- Estimate a score (**flux**) in a volume of interest

How is it done?

- $n$  particles are simulated
- The  $i$ -th particle contribution to the score is stored as  $\hat{\phi}_i$
- We define the **average flux** and its associated variance:

$$\bar{\phi} = \frac{1}{n} \sum_{i=1}^n \hat{\phi}_i$$

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^n (\hat{\phi}_i - \bar{\phi})^2$$

If the attenuation is really strong:

- **Many particles will not reach the volume of interest**
- Their contributions will be null
- The variance or the computation time will explode

Variance reduction techniques:

- Modify the simulation behavior
- Reduce the variance **for a given computation time**

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# THE AMS METHOD: ALGORITHM

## AMS: Adaptive Multilevel Splitting

- Theory :

F.Cérou et A. Guyader. *Adaptive multilevel splitting for rare event analysis*.  
Stoch. Anal. Appl, 25(2):417-443, 2007.

- Application in molecular dynamics :

D.Aristoff, T.Lelièvre, C.G.Mayne et I.Teo. *Adaptive multilevel splitting in molecular dynamics simulations*. ESAIM:Proc., 48:215-225, 2015.



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AMS is a **population control algorithm**. It takes place at the end of the simulation

A free parameter:

- An **importance function** denoted  $I$ :

$$I: \mathbb{R}^6 \rightarrow \mathbb{R}$$

- Associates an **importance** value to any point of the phase space

## First step

- $n$  particles are simulated

## AMS iterations:

- Each particle **track** is given a **note** according to  $I$
- The less interesting particles is suppressed
- One of the remaining particles is splitted
- We get a new set of  $n$  particles:
  - $1$  new replica
  - $n-1$  particles that were not suppressed

# THE AMS METHOD

Stopping criterion:

- When the less interesting particle is in the volume of interest
- The total number of iterations is denoted  $N$
- The probability of reaching the volume of interest is estimated by:

$$\alpha = \left(1 - \frac{1}{n}\right)^N$$

An **unbiased** estimate of the score is computed using the last generated points and weighting the result by  $\alpha$

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# THE AMS METHOD: IMPLEMENTATION

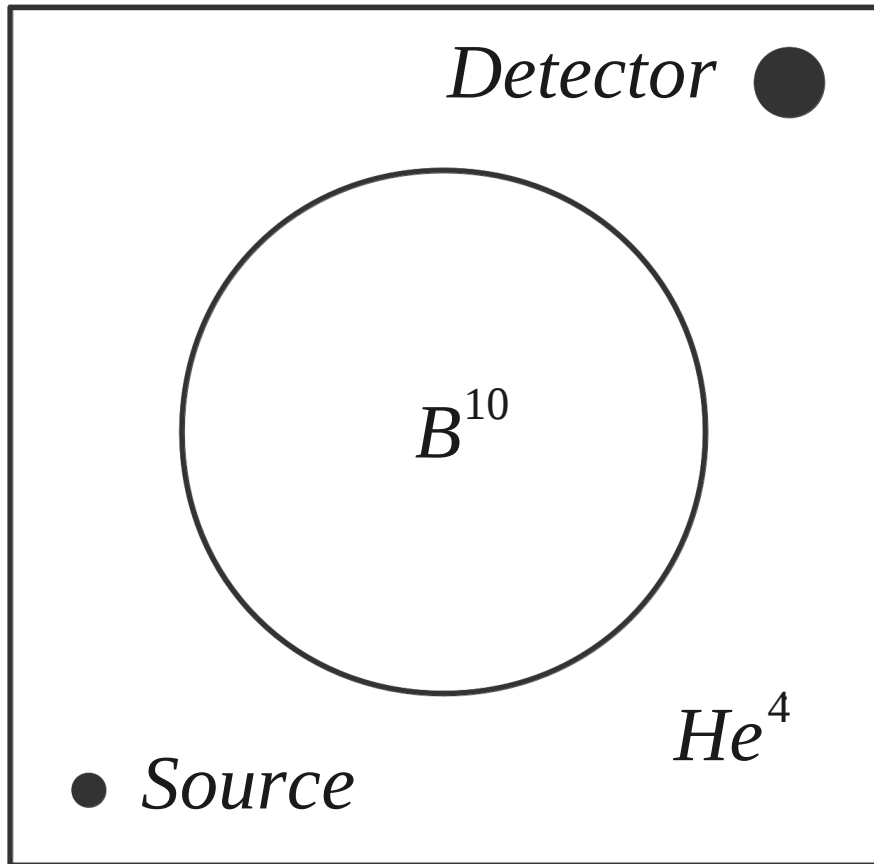
## TRIPOLI-4® :

- 3D continuous-energy Monte Carlo particle transport code
- Dedicated to shielding, reactor physics, criticality, safety and nuclear instrumentation
- Developed at **CEA Saclay** since the mid-60s

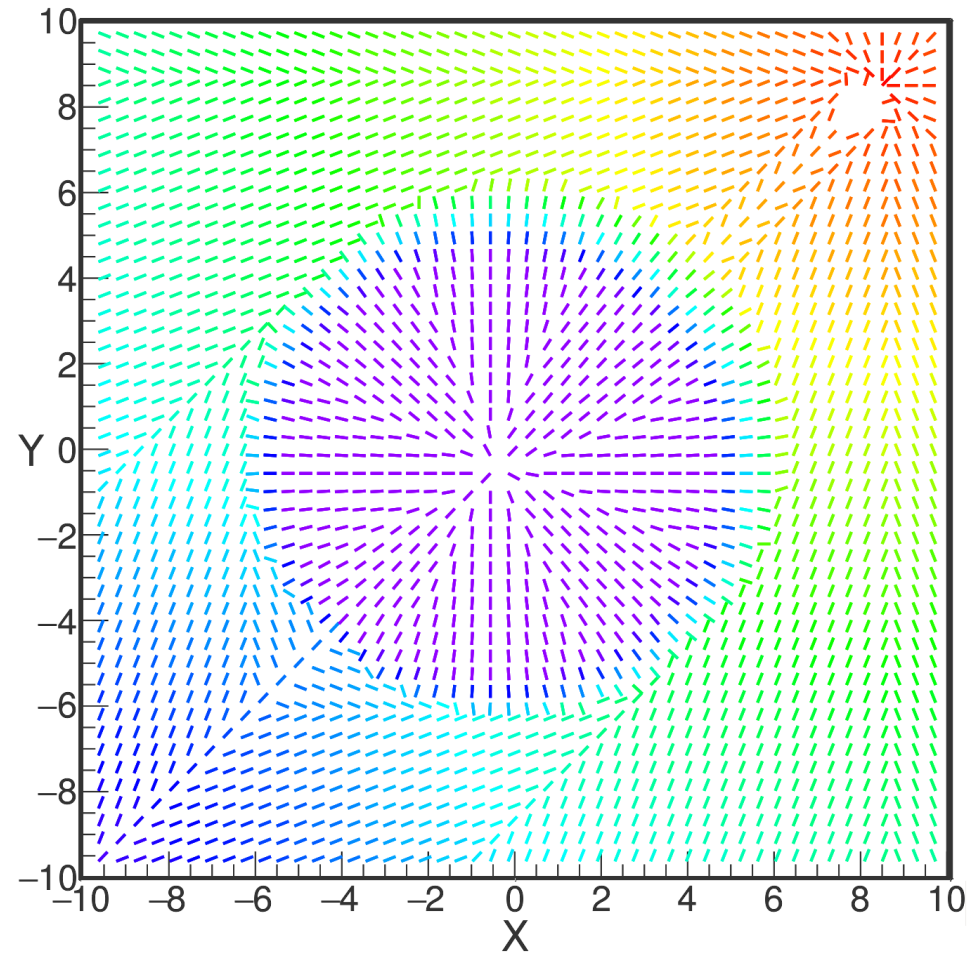
## Existing variance reduction technique:

- “Exponential transform”
- Also uses an **importance map**
- Has a module that estimates the importance from the geometry

# THE AMS METHOD



Example of geometry



Associated importance map

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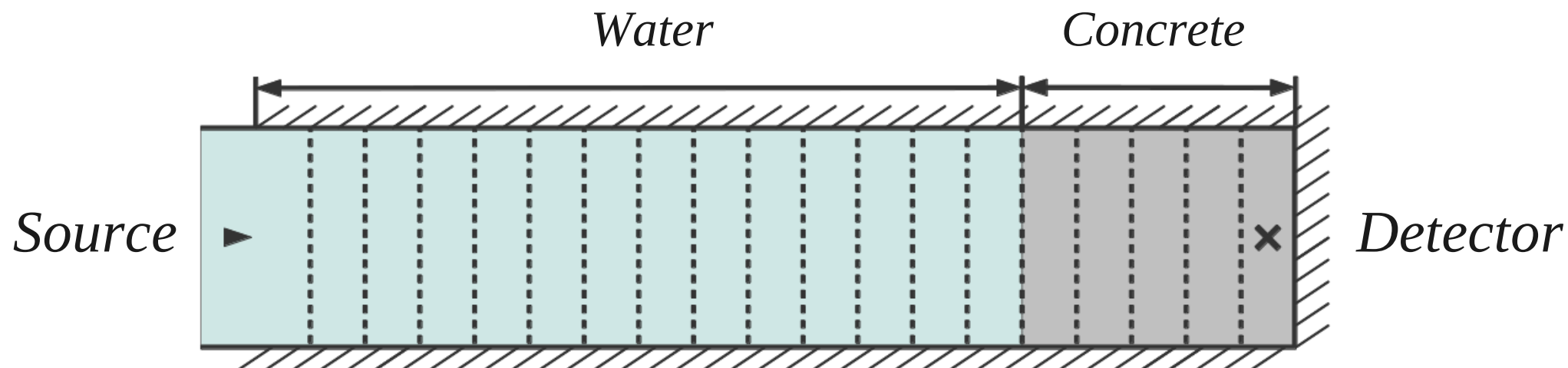


# RESULTS

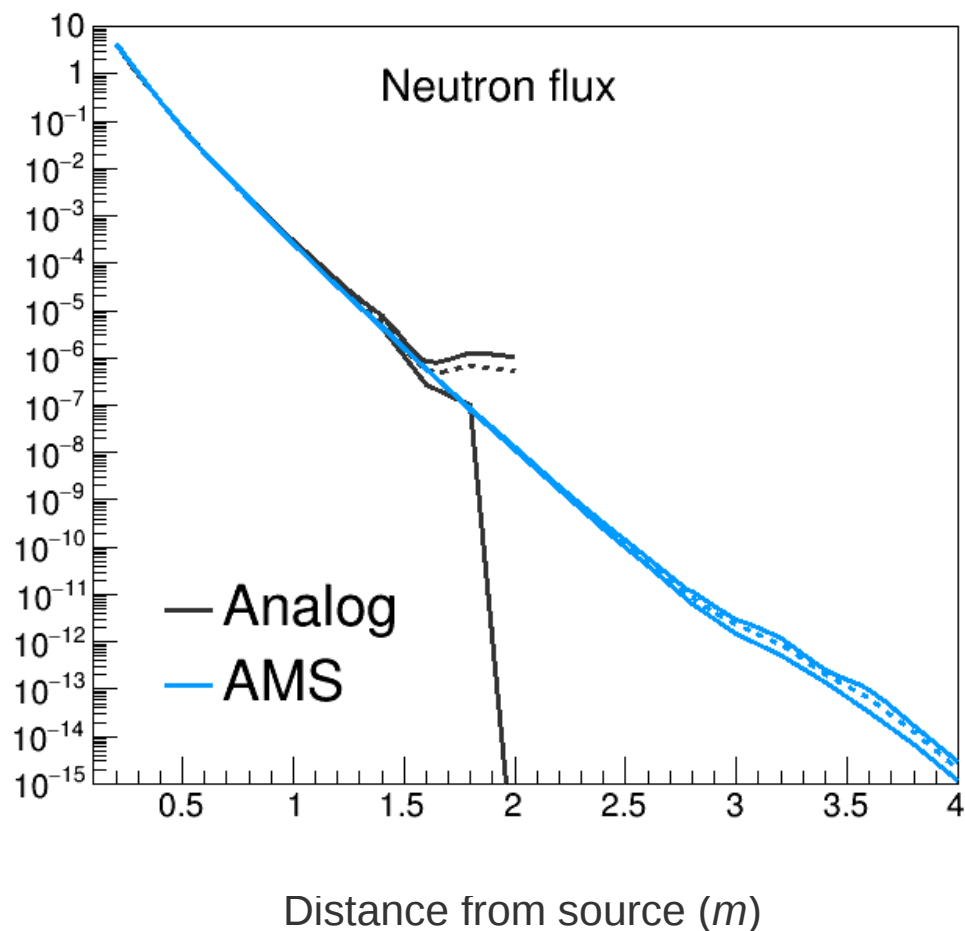


## Illustration of the variance reduction use:

- We want to estimate the neutron flux attenuation when traversing 3m of water and 1m of concrete
- The neutron source is mono-directional at the entrance of a box with perfect reflectors around it
- The flux is estimated every 20cm between the source and the detector



Neutron flux and associated standard deviation obtained with **AMS**, compared to an **analog** calculation (i.e. without variance reduction)

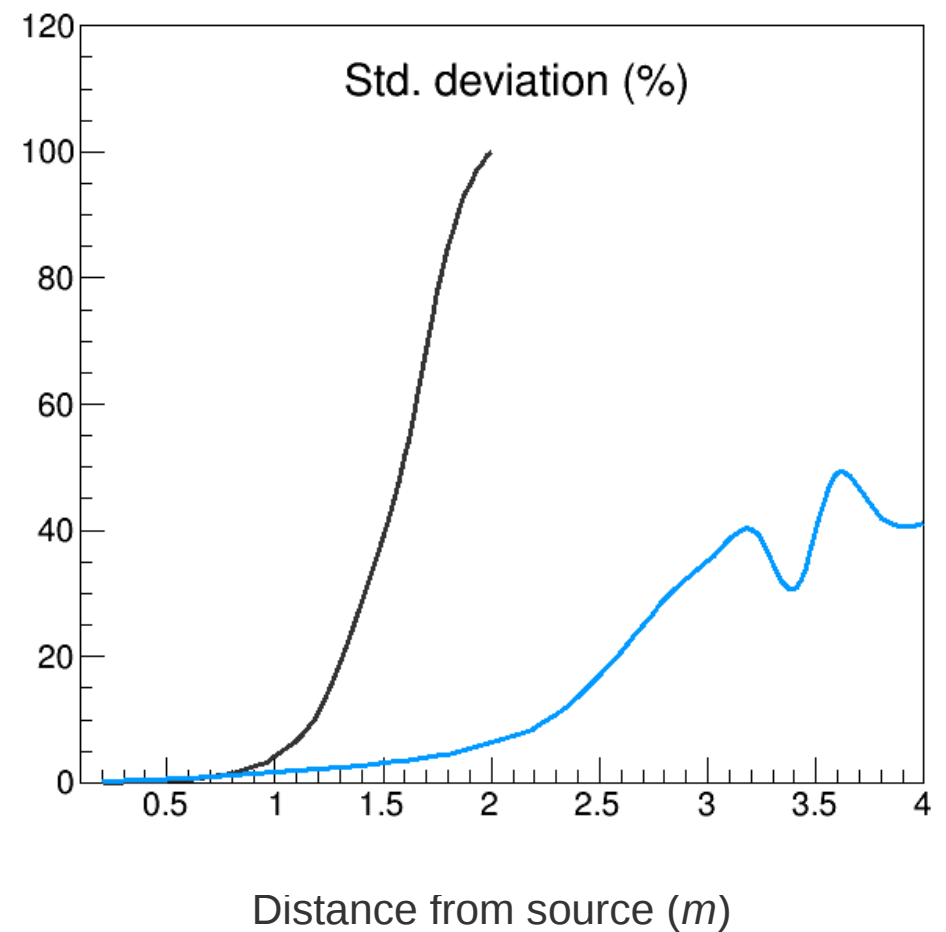
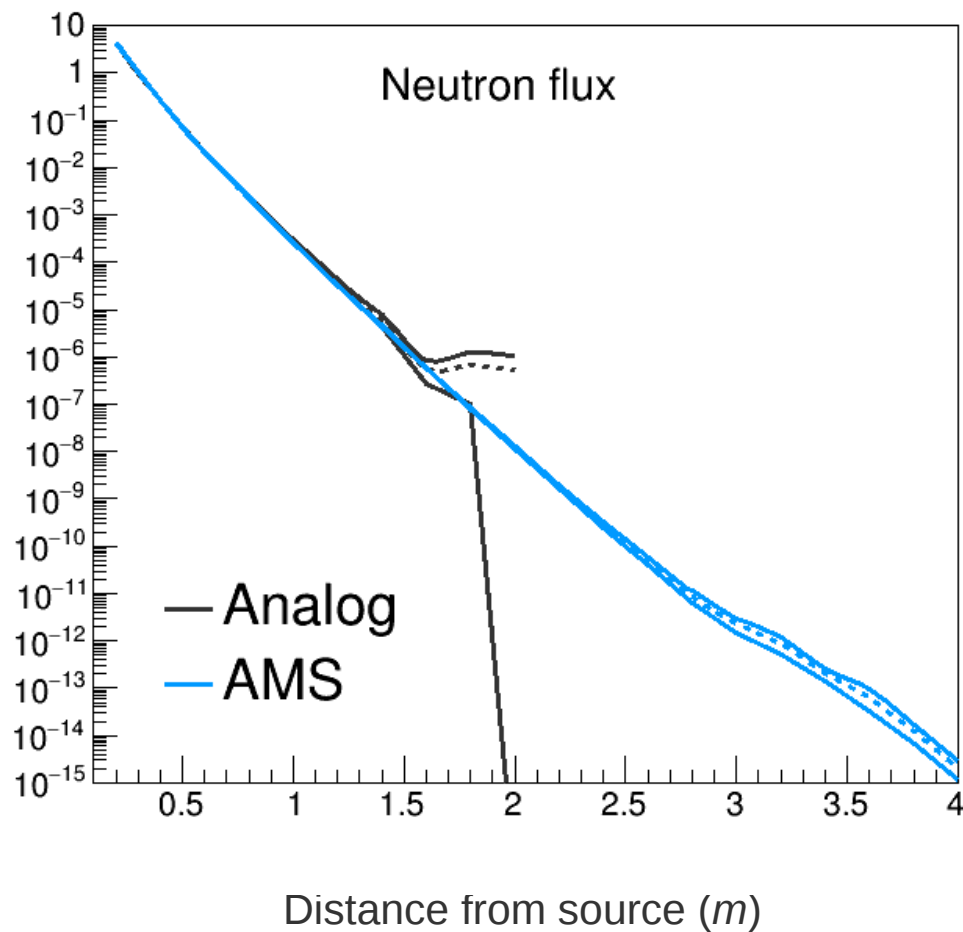


## OBSERVATIONS:

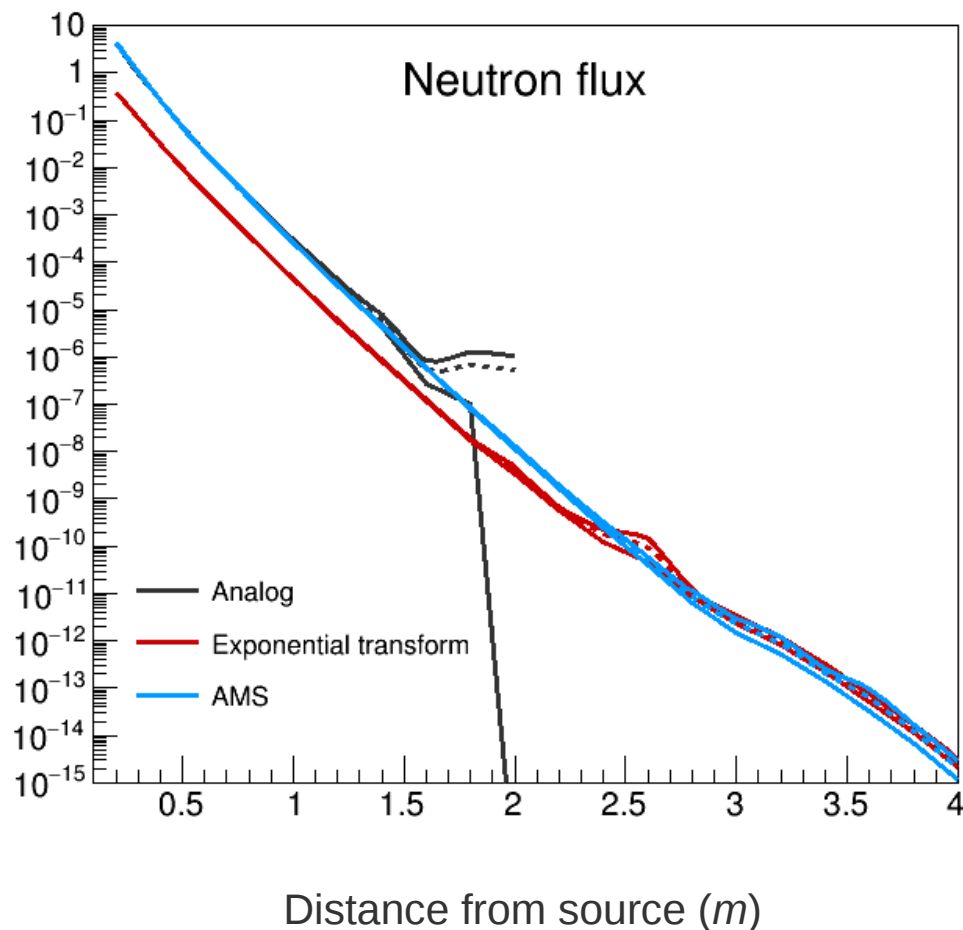
- **Very good accordance** with the reference near the source
- The analog simulation has **no results** deeper than 2m
- AMS is able to yield results **all the way** to the detector (and probably beyond)

# RESULTS

Neutron flux and associated standard deviation obtained with **AMS**, compared to an **analog** calculation (i.e. without variance reduction)



Neutron flux and associated standard deviation obtained with **AMS**, compared to an **analog** calculation and the **current variance reduction** method of TRIPOLI-4®

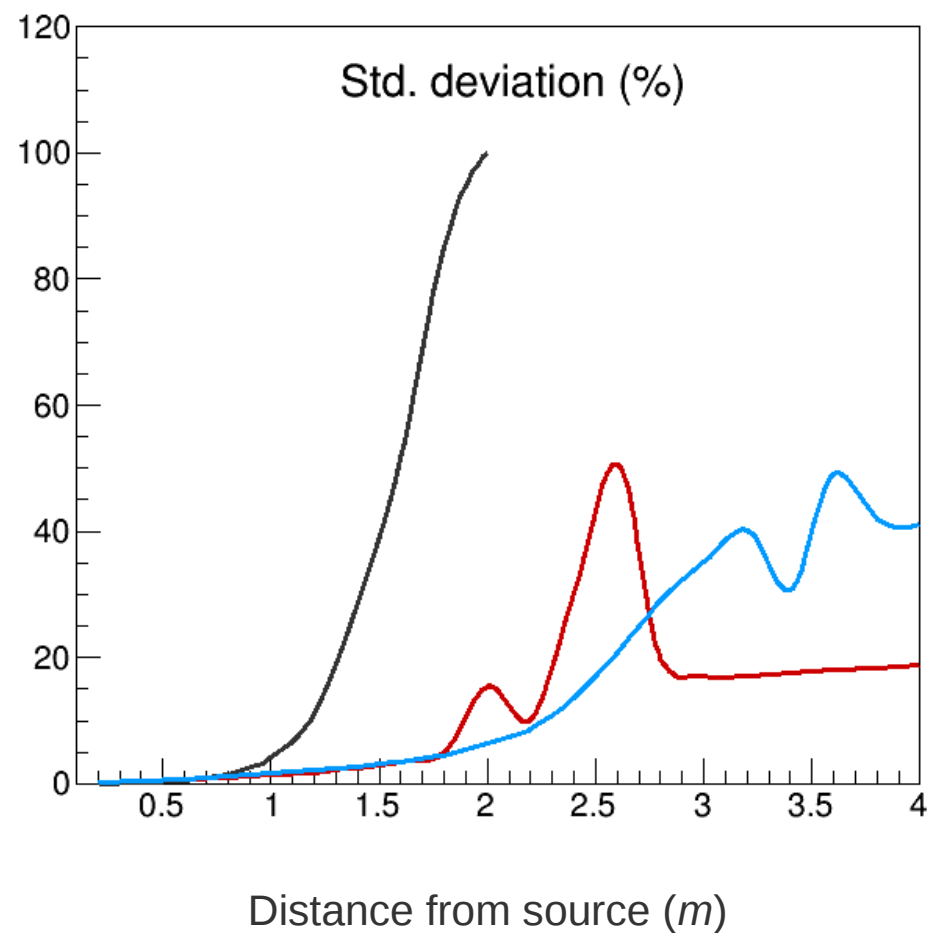
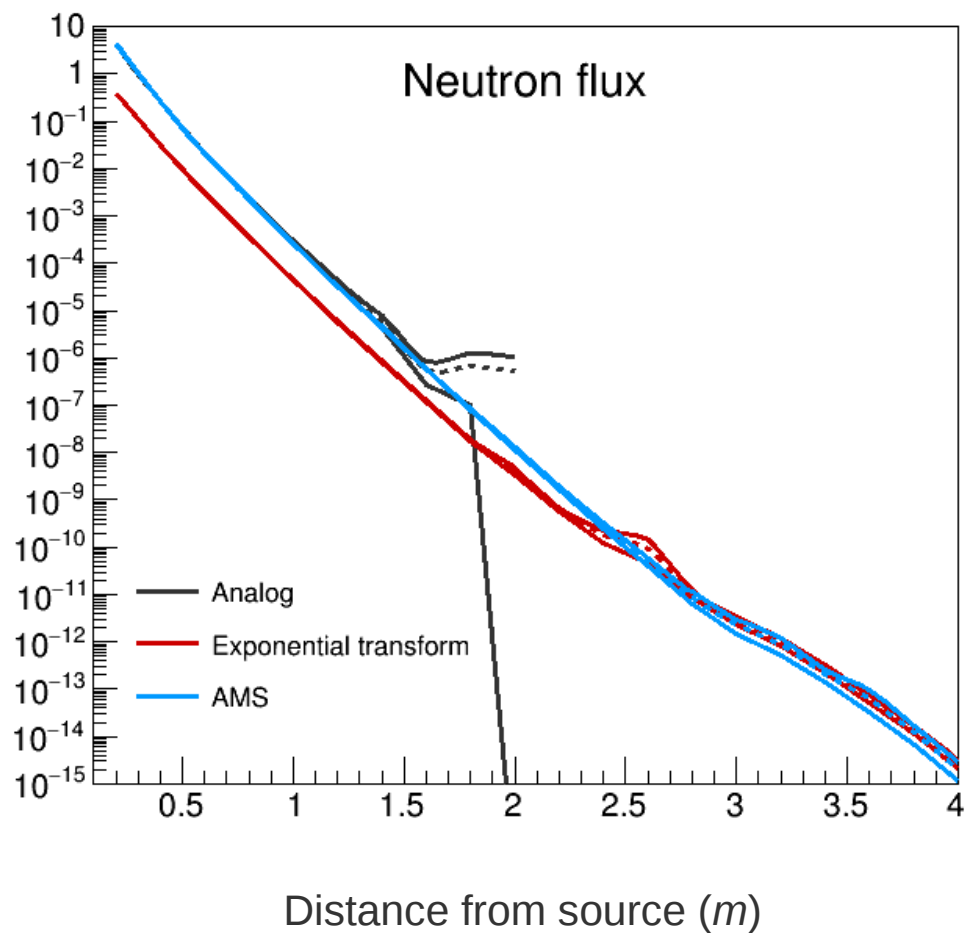


## OBSERVATIONS:

- Very good accordance between AMS and the exponential transform **near the detector**
- The exponential transform results away from the detector **can't be trusted**
- The importance map used to get results with exponential transform had to be **optimized**

# RESULTS

Neutron flux and associated standard deviation obtained with **AMS**, compared to an **analog** calculation and the **current variance reduction** method of TRIPOLI-4®



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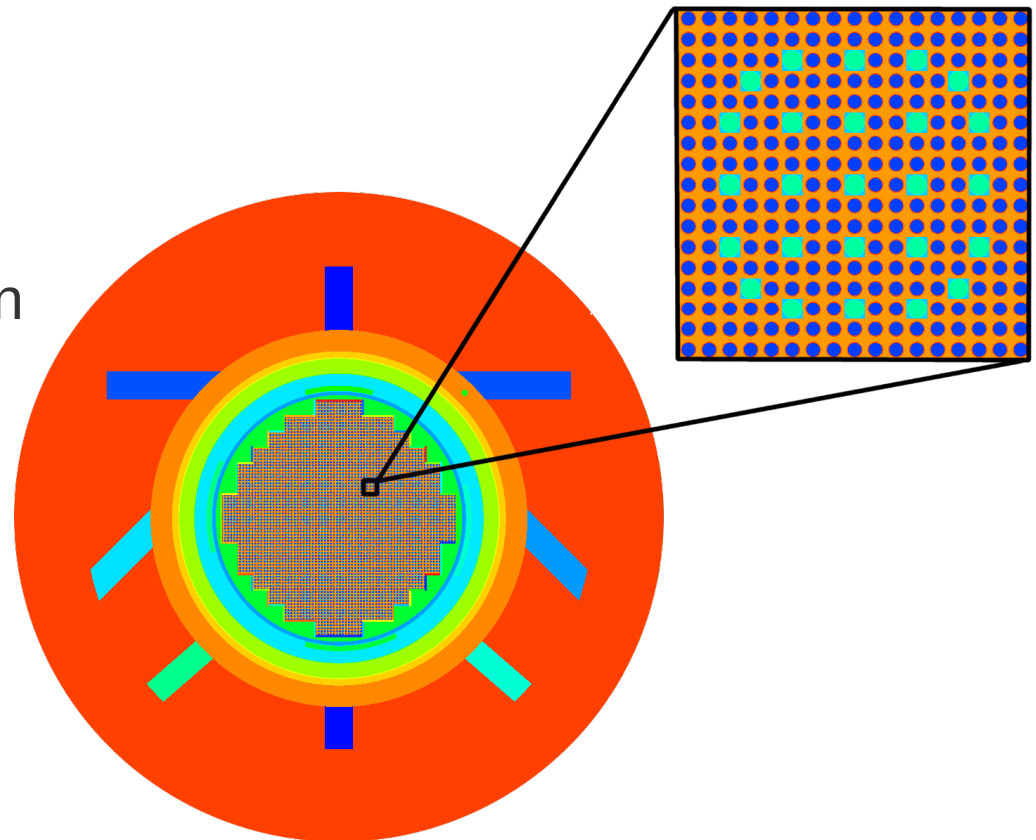
# CONCLUSION

## Implementation:

- The AMS implementation in TRIPOLI-4® is **over** and **stable**
- The method will be available in the developer's version of the code **soon**

## Testing:

- The AMS efficiency is tested in many problems, from **simple cases** to **full nuclear cores**



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