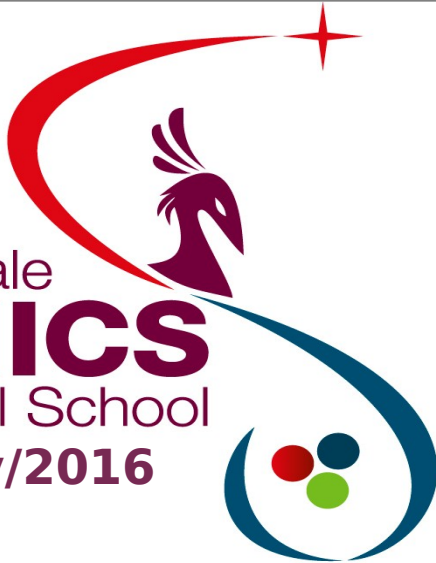




## Aspects of Nucleon form factors measurements:

- Phenomenological study of proton anti-proton annihilation into light meson pairs
- Contribution to ALPOM2 experiment



École Doctorale  
**PHENIICS**  
Doctoral School  
**11/ May/2016**

Supervisors: Egle Tomasi-Gustafsson

Dominique Marchand

Collaborators: Y. Bystritskiy

N. Piskunov

# Nucleon Form Factors (FFs)

## The electromagnetic FFs: GE and GM

- Inside structure of nucleon

Spatial distributions of charge and magnetization current inside the nucleon.

## How to measure?

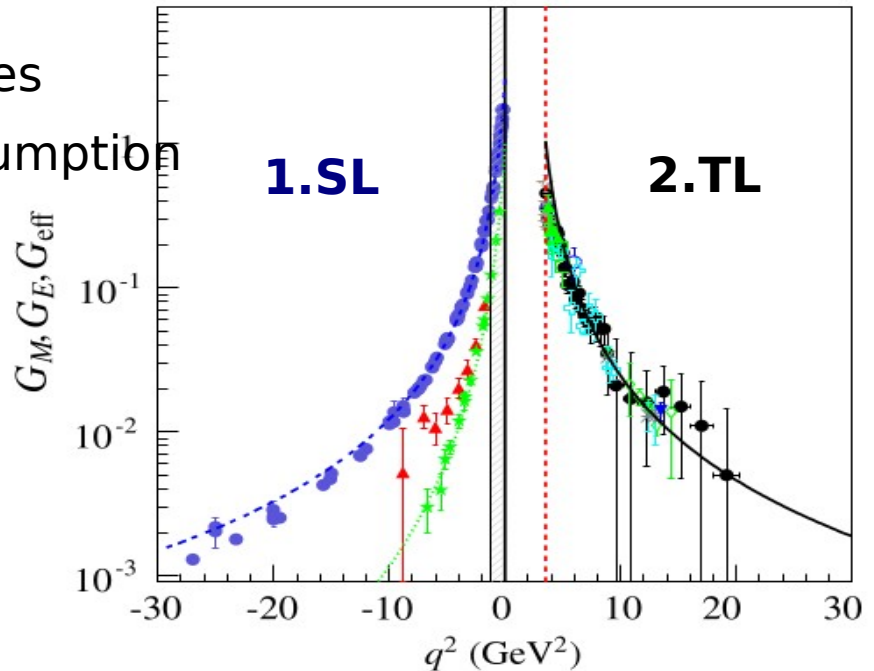
Can be approached from two sides within one photon exchange assumption

1.Space-like region (SL)

$$ep \rightarrow ep$$

2.Time-like region (TL)

$$p\bar{p} \rightarrow e^+ e^-$$
$$e^+ e^- \rightarrow p\bar{p}$$



# Content

---

*Time-like region ( $\bar{p} p \rightarrow e^+ e^-$ )*  
PANDA experiment

- Neutral particles

$$p\bar{p} \rightarrow \pi^0\pi^0, \eta\eta, \eta\pi^0$$

*Space-like region ( $e^- p \rightarrow e^- p$ )*  
Experiment preparation ALPOM2

- Experimental prediction for  $np \rightarrow np$  ( $pn$ )

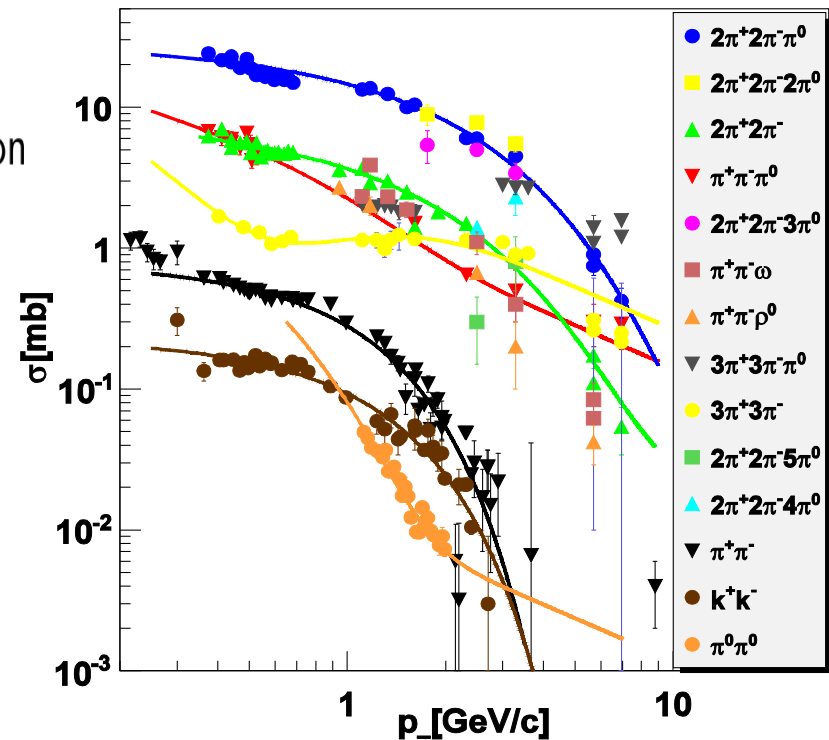
# Motivation of my work

- ▶ The reaction  $\bar{p}p \rightarrow e^+e^-$  allows to measure electromagnetic proton form factors.
- ▶ Important simulation work is under way.
- ▶ The reaction  $\bar{p}p \rightarrow \pi^+\pi^-$  is the main background :

- ▶ has a large cross section,
- ▶ contains information on the quark content of the proton
- ▶ allow to test different QCD models

Largest cross sections come from multi-pions

(5 > 4 > 2)



It is necessary to fully understand the process  $\bar{p}p \rightarrow \pi^+\pi^-$ .

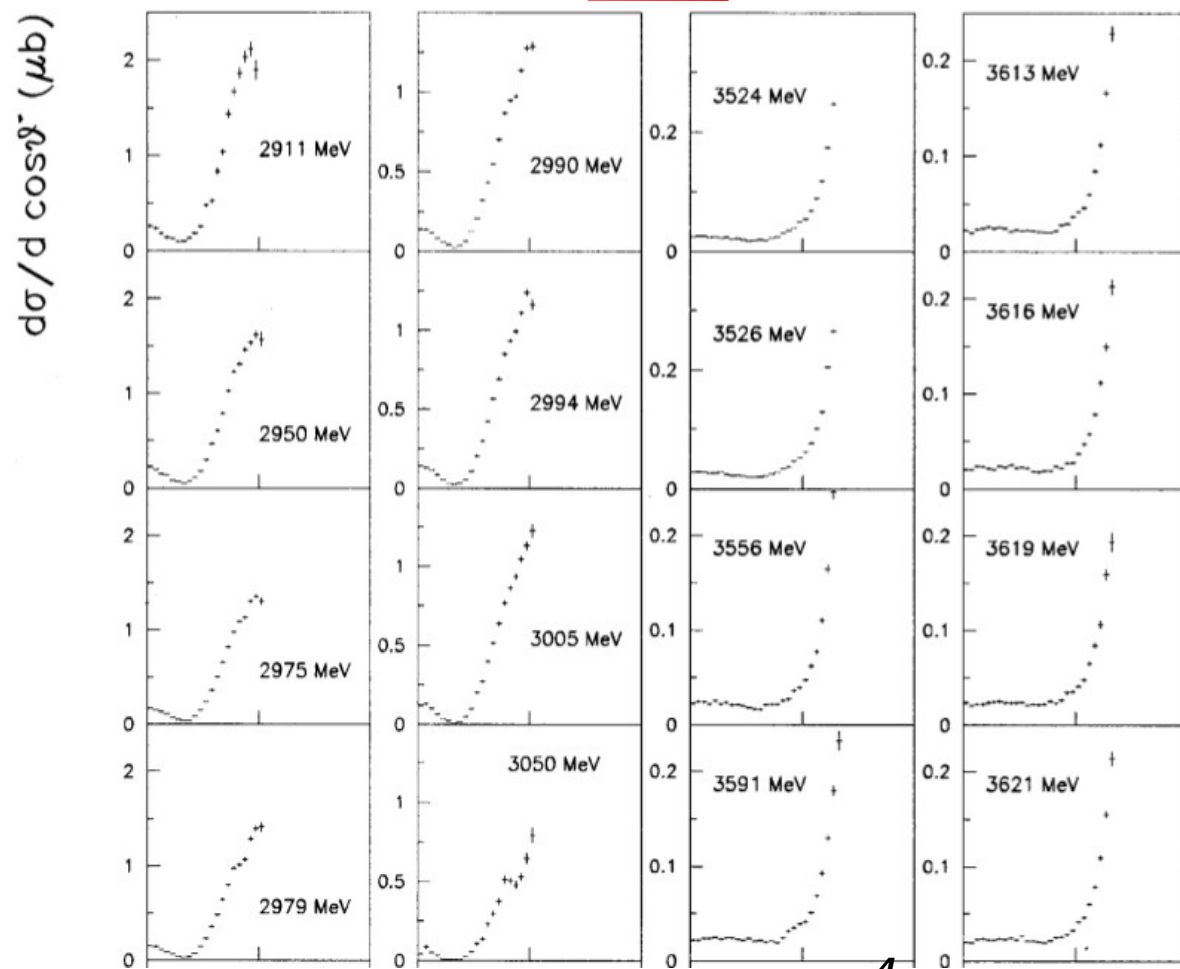
## ARTICLES

T. A. Armstrong, et al

## Two-body neutral final states produced in antiproton-proton annihilations at

$$2.911 \leq \sqrt{s} \leq 3.686 \text{ GeV}$$

$$p + \bar{p} \rightarrow \pi^0 + \pi^0, \quad \eta + \pi^0, \quad \eta + \eta, \quad \pi^0 + \gamma, \quad \gamma + \gamma$$



Energy under 2.911 GeV

Sum of resonances:

$$T_{L,J} = \sum_{i=1} \frac{G_i B_L(p) B_J(q) \exp(i\phi_i)}{M_i^2 - s - iM_i \Gamma_i}$$

We develop effective  
Lagrangian model based  
on  
s,t, u channel  
Feynman diagrams.

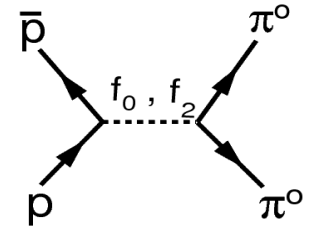
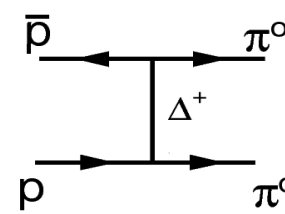
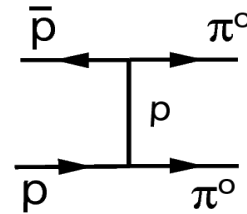
The aim is to reproduce all  
available data and make  
reliable predictions at  
higher energies.

Our model should work in  
Panda energy region

# Calculation $\bar{p}p \rightarrow \pi^0\pi^0$

## ➤ Differential cross section

$$\frac{d\sigma}{d\cos\theta} = \frac{1}{2^7\pi} \frac{1}{s} \frac{\beta_\pi}{\beta_p} |\overline{\mathcal{M}}|^2$$



## ✓ (e.g.) Nucleon exchange

- Vertex:  $-ig_{\pi NN}(i\gamma_5)(2\pi)^4$

- Propagator:  $\frac{i}{(2\pi)^4} \frac{\hat{q}_t + M_p}{q_t^2 - M_p^2}$

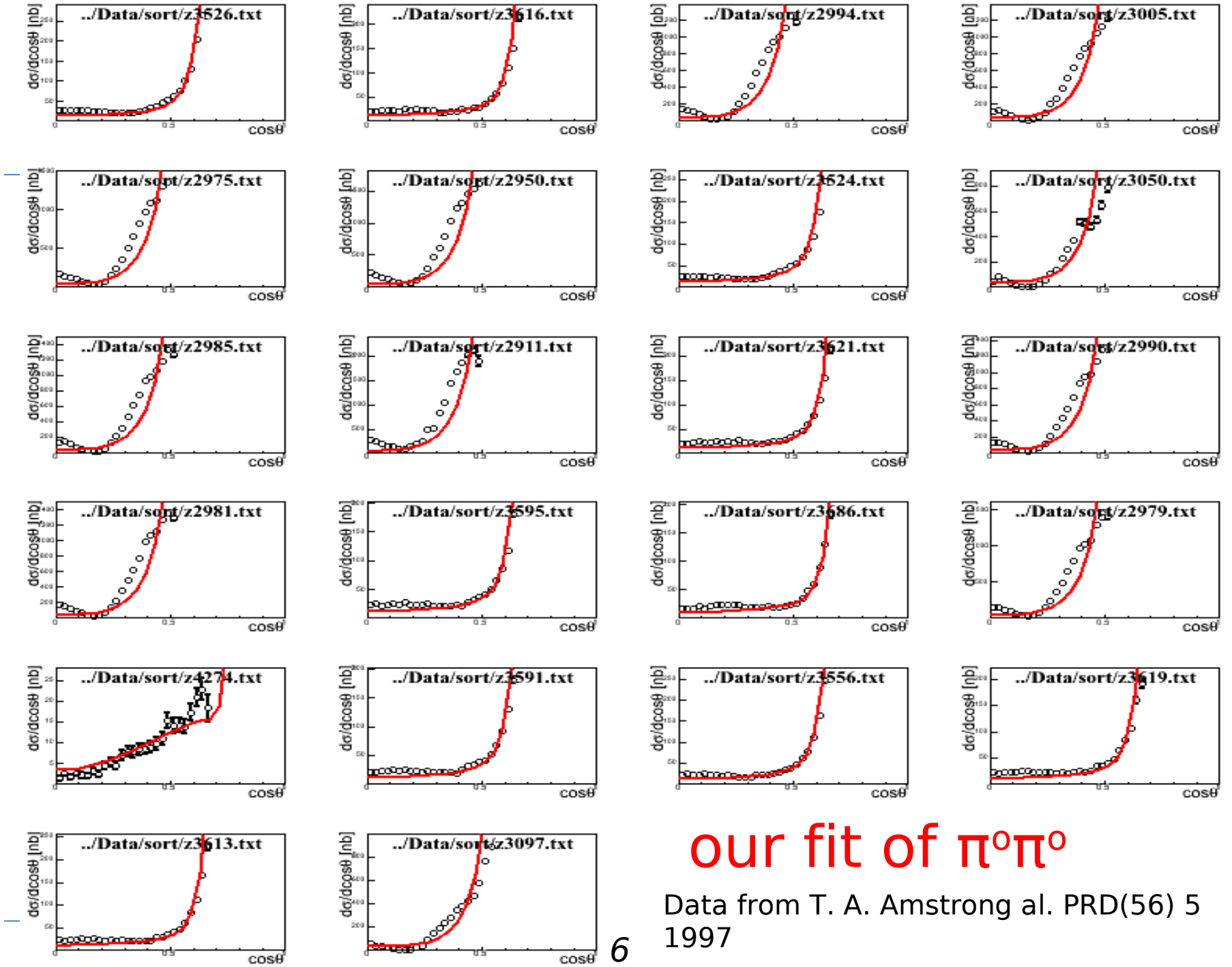
$$|\overline{\mathcal{M}}|^2 = \mathcal{M}_n A^*(a) = \frac{g_{\pi NN}^4}{(q^2 - M_p)^2} \text{Tr} [(\hat{p}_1 - M_p)(\hat{q} + M_p)^2(\hat{p}_2 + M_p)]$$

Add Regge factors and form factors

(compositeness of particles, absorption, ISI, FSI...)

$$R_N(t) = \left(\frac{s}{p_3}\right)^{\frac{1}{2} + p_2 \left(\frac{t - M_p^2}{M_p^2}\right)}$$

$$R_\Delta(u) = \left(\frac{s}{p_3}\right)^{\frac{3}{2} + p_4 \left(\frac{t - M_\Delta^2}{M_\Delta^2}\right)}$$



# our fit of $\pi^0\pi^0$

Data from T. A. Armstrong al. PRD(56) 5 1997

# Test of quark counting

PRL (1973) 31. 18.  
S. J. Brodsky, G. R. Farrar  
Scaling Laws at Large Transverse Momentum

LETTERE AL NUOVO CIMENTO (1973) 5 14  
V. A. Matveev et al.  
Automodelity in Strong Interactions.

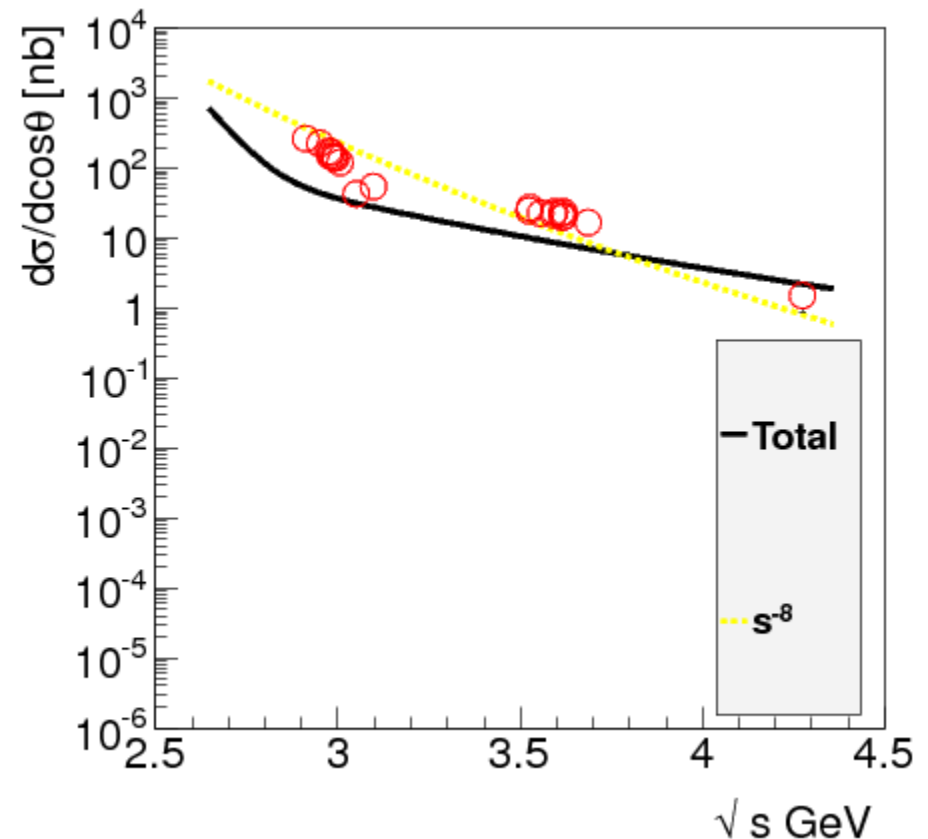
$$d\sigma/dt \sim s^{2-n} f(t/s)$$

n total number of leptons, photons  
and quark components

Reaction  $\bar{p}p \rightarrow \pi^0\pi^0$

$$n = n_i + n_f = 2 \times (3 + 2) = 10$$
$$2 - n = -8$$

$$d\sigma/dt \sim s^{-8} f(t/s)$$





# From pion to eta through SU(3)

Physics Letters B 471 (1999) 271–279

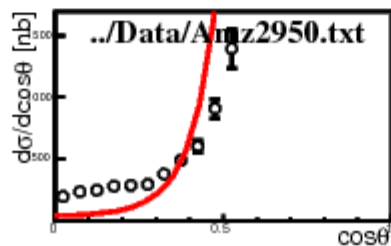
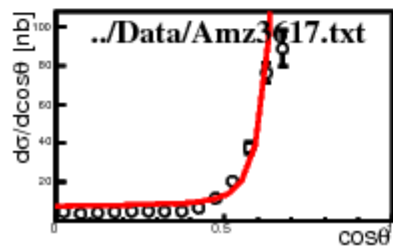
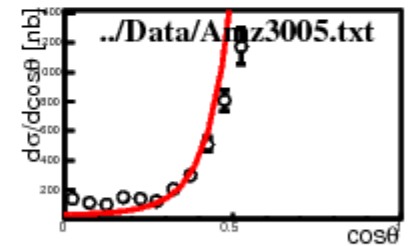
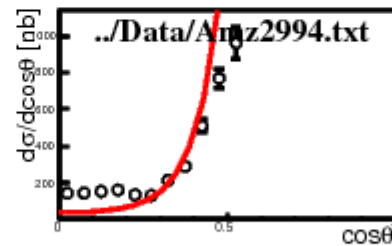
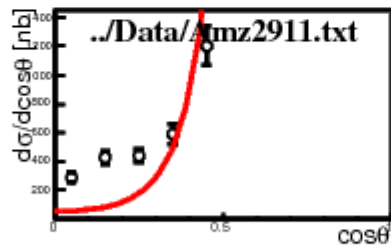
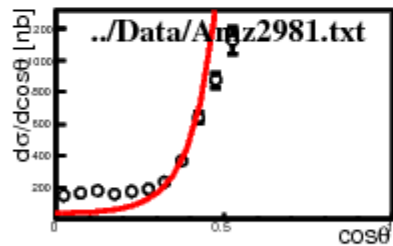
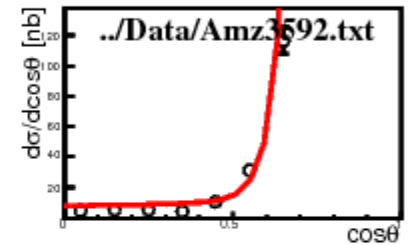
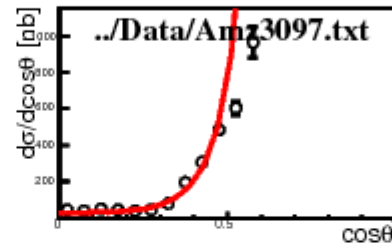
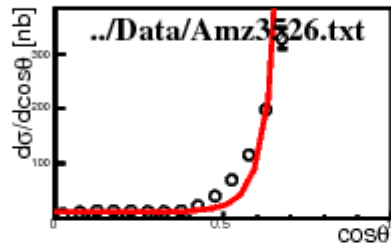
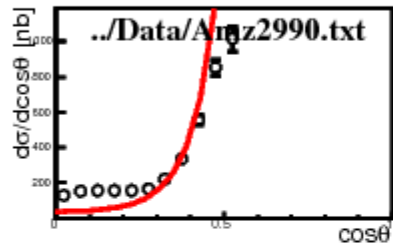
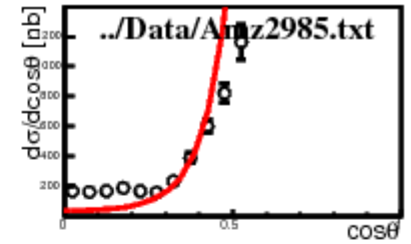
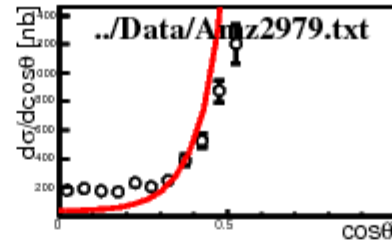
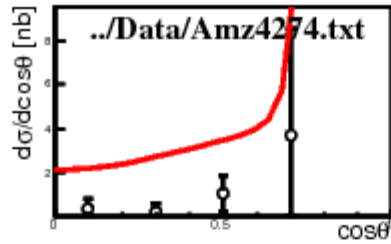
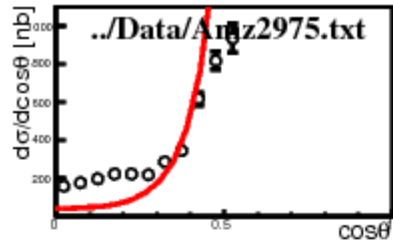
$\Pi$  and  $\eta$  mesons are pseudoscalar mesons.

The decay to  $\eta\eta$  can be described from  $\pi^0\pi^0$  using the well-known decomposition of singlet and octet states, where the mixing angle is  $\Theta \approx 40^\circ$

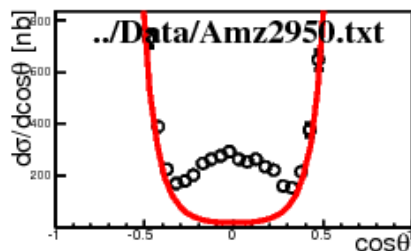
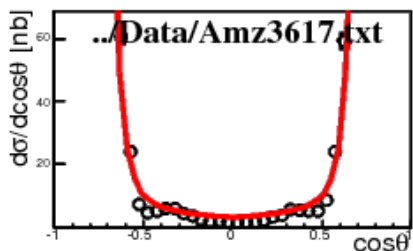
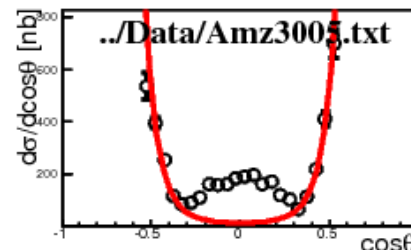
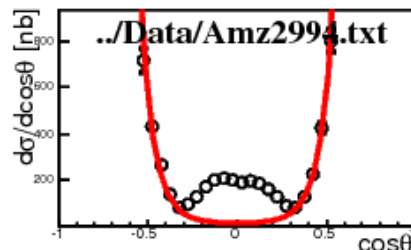
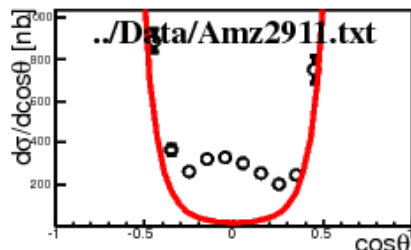
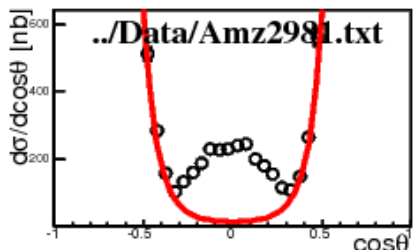
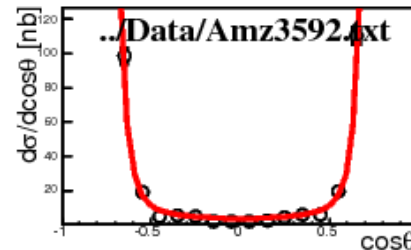
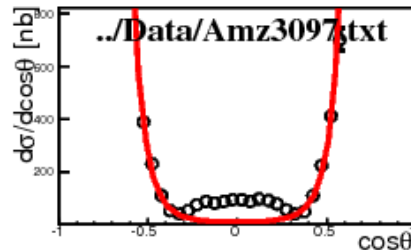
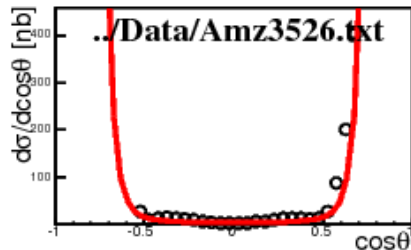
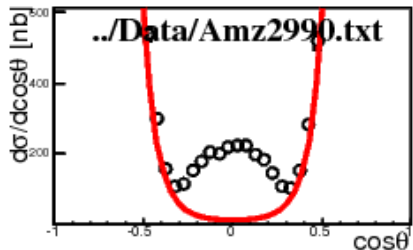
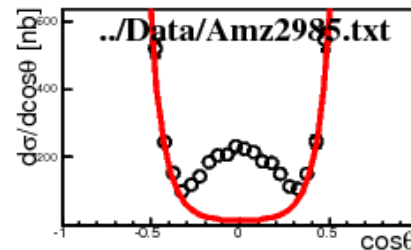
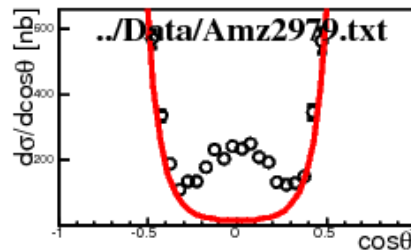
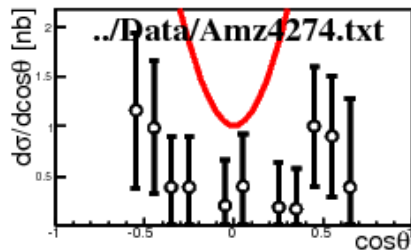
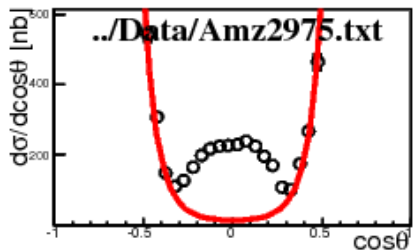
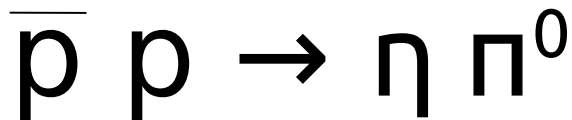
$$\eta \approx (u\bar{u} + d\bar{d})/\sqrt{2} + s\bar{s}$$
$$(u\bar{u} + d\bar{d})\sqrt{2} \leftarrow |q\bar{q}\rangle = \cos\Theta|\eta\rangle + \sin\Theta|\eta'\rangle$$
$$|s\bar{s}\rangle = -\sin\Theta|\eta\rangle + \cos\Theta|\eta'\rangle$$

$$f(\eta\eta) = f(\pi^0\pi^0) \cos^2\Theta$$

# $\bar{p} p \rightarrow \eta \eta$



T. A. Armstrong et al. PRD(56) 5 1997



T. A. Armstrong et al. PRD(56) 5 1997

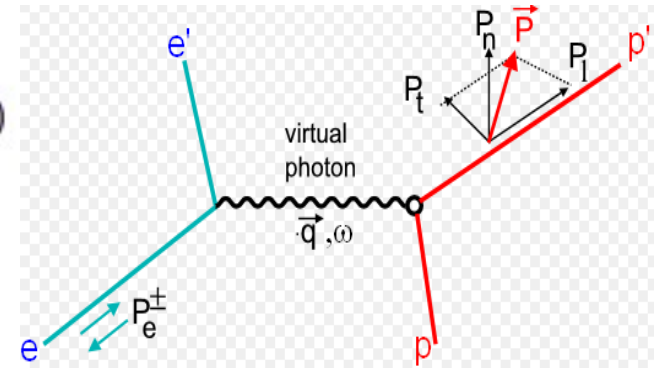
II part  
ALPOM2 experiment

# Hadron form factor measurement

*Polarized ep elastic scattering*

$$\frac{G_E}{G_M} = - \frac{P_t}{P_\ell} \frac{(E_e + E'_e)}{2M_p} \tan\left(\frac{\theta_e}{2}\right)$$

*1st step: measure the proton analyzing powers (Ay) in GeV region*

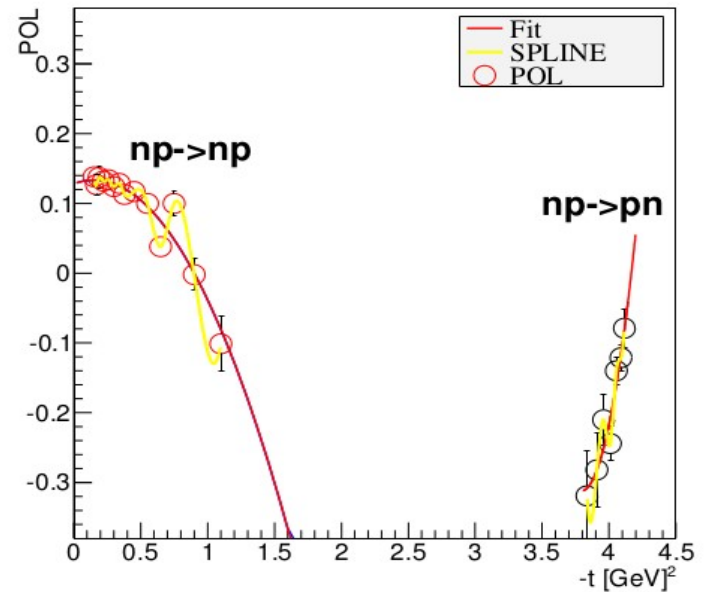


(Analyzing power is the Polarization of the beam)

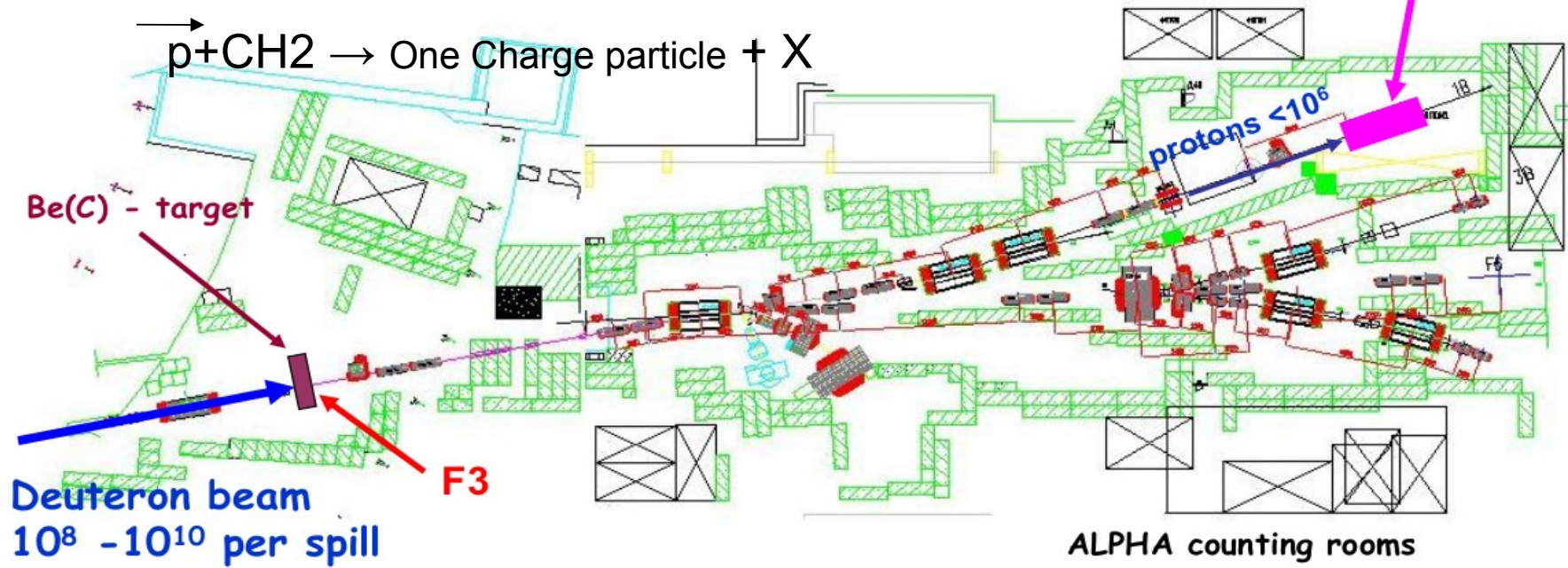
ALPOM2 (JINR- Dubna):

p+CH2 → One Charge particle + X

n p → p n (np)

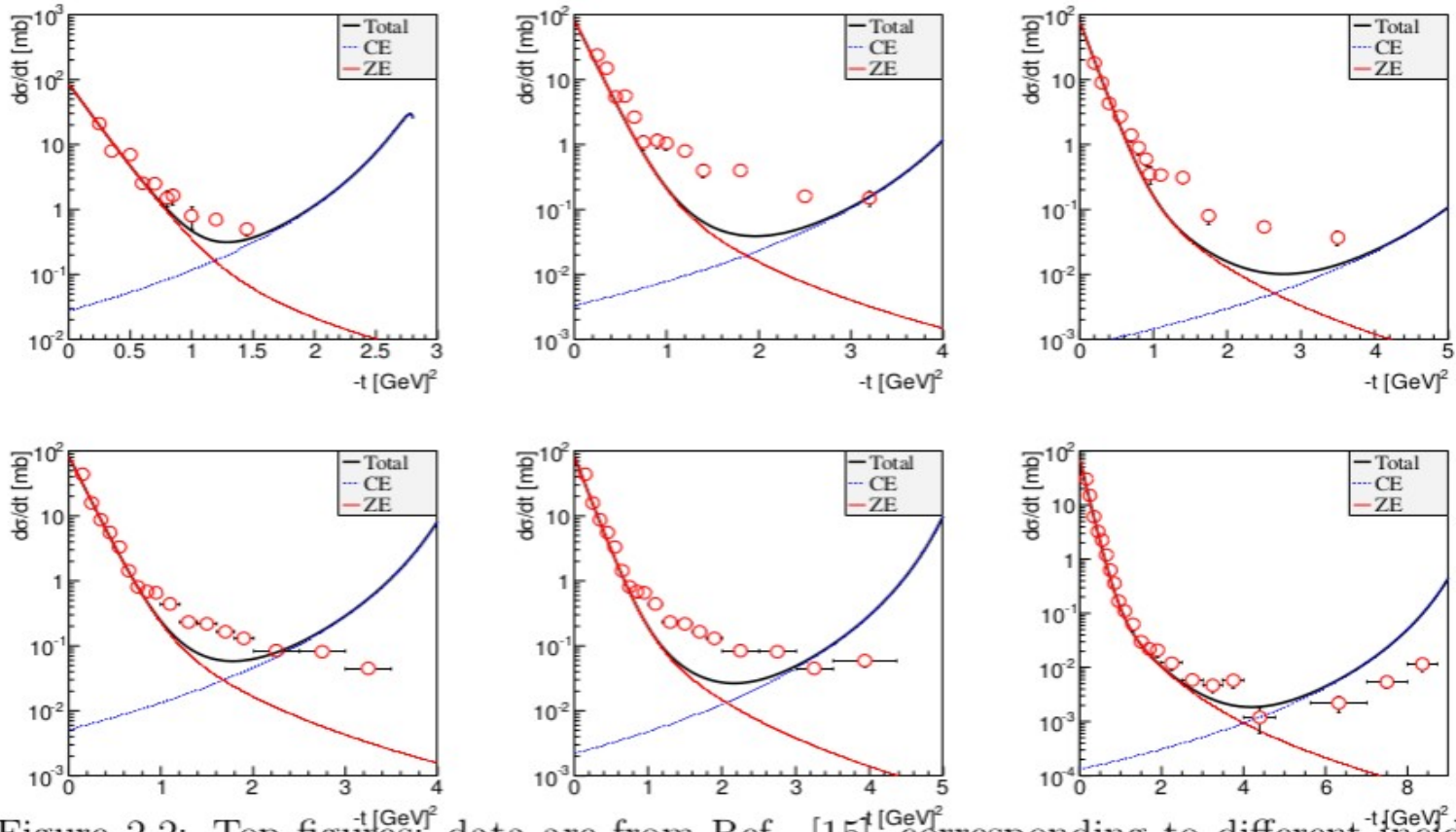


# Introduction of ALPOM2



- Polarized protons will be produced by the fragmentation of the polarized deuteron beam
- Protons interact with activated target CH<sub>2</sub>
- Through the drift chambers to reconstruct the trajectories
- Finally the particles will be detected by the hadron calorimeter

# Differential cross section of $np \rightarrow np(pn)$



Red circles are from experiment, and the red line represents Zero-exchange (ZE) and the blue line is Charge-exchange (CE).

$$\frac{d\sigma}{dt} = \frac{1}{64\pi s q^2} (|T_\pi(u) + T_\rho(u)|^2 + \frac{1}{4}|T_\pi(t) + T_\rho(t)|^2 + |T_P(t)|^2)$$

# Analyzing power and Figure of Merit

$$\mathcal{F}^2(\cos \theta) = A_y^2(\cos \theta) \cdot \frac{d\sigma/d\cos \theta}{\sigma_{tot}}$$

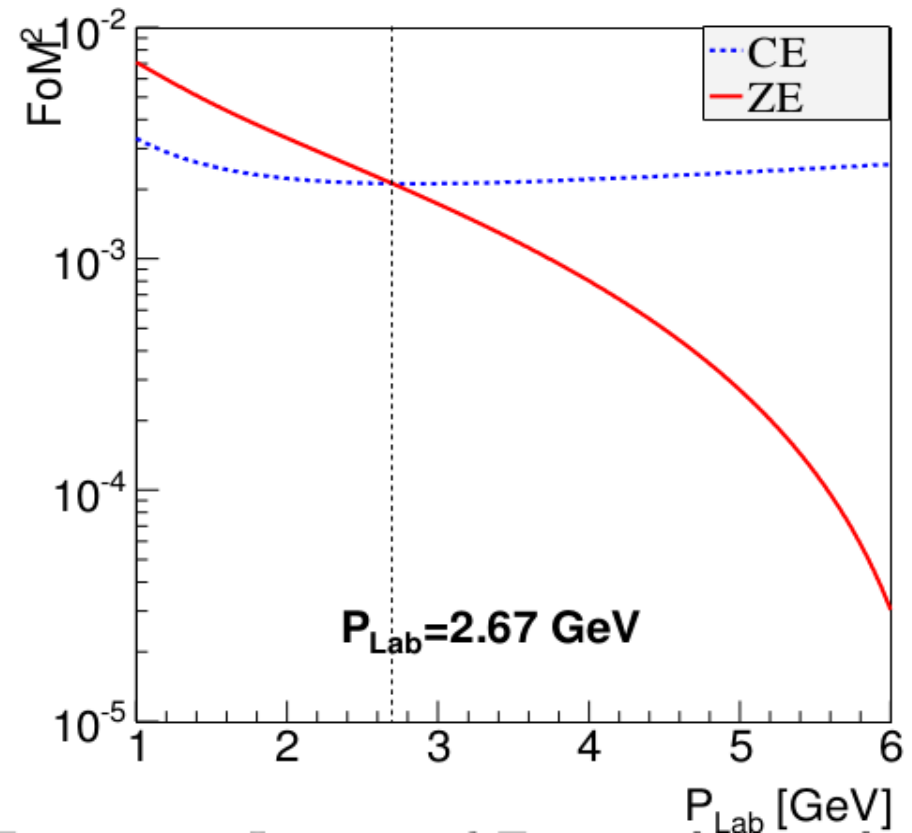
## The statistical error

$$\Delta P = \sqrt{\frac{2}{N_{inc} \mathcal{F}^2}}$$

*Figure of Merit considered both cross section and the analyzing power.*

*It can predict the statistical error when you know the experiment condition.*

*Also it can help to decide which energy which reaction to have better expected data.*





# Summary

---

I )We have built a promising model based on effective lagrangian to describe 2 meson production in  $p\bar{p}$  annihilation

- Parameters fixed on  $\pi^0\pi^0$
- neutral channel obtained from SU3 symmetry:  $\eta\eta, \eta\pi^0$
- Encouraging results on angular distributions and the expected  $s$  dependence have been obtained

II) Calculation of Figure of Merit for proton and neutron polarimetry at 7.5 GeV/c momentum and comparison of the elastic and charge exchange reactions  $np \rightarrow np(pn)$  for JLAB experiments.

# Perspectives

---

Optimize the parameters to improve charged pion description at small angles

Apply similar formalism to other channels:

$\gamma\gamma, \gamma\pi^0, KK$

## ***Goal:***

To build a generator based on our model

*Thank you!*

---