

# Double Higgs production at the LHC and Beyond

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# HH production processes

Several production channels  
but tiny cross section in the SM

◆ leading: **gluon fusion**

$$\sigma_{14\text{TeV}}^{\text{GF}} \simeq 40 \text{ fb}$$

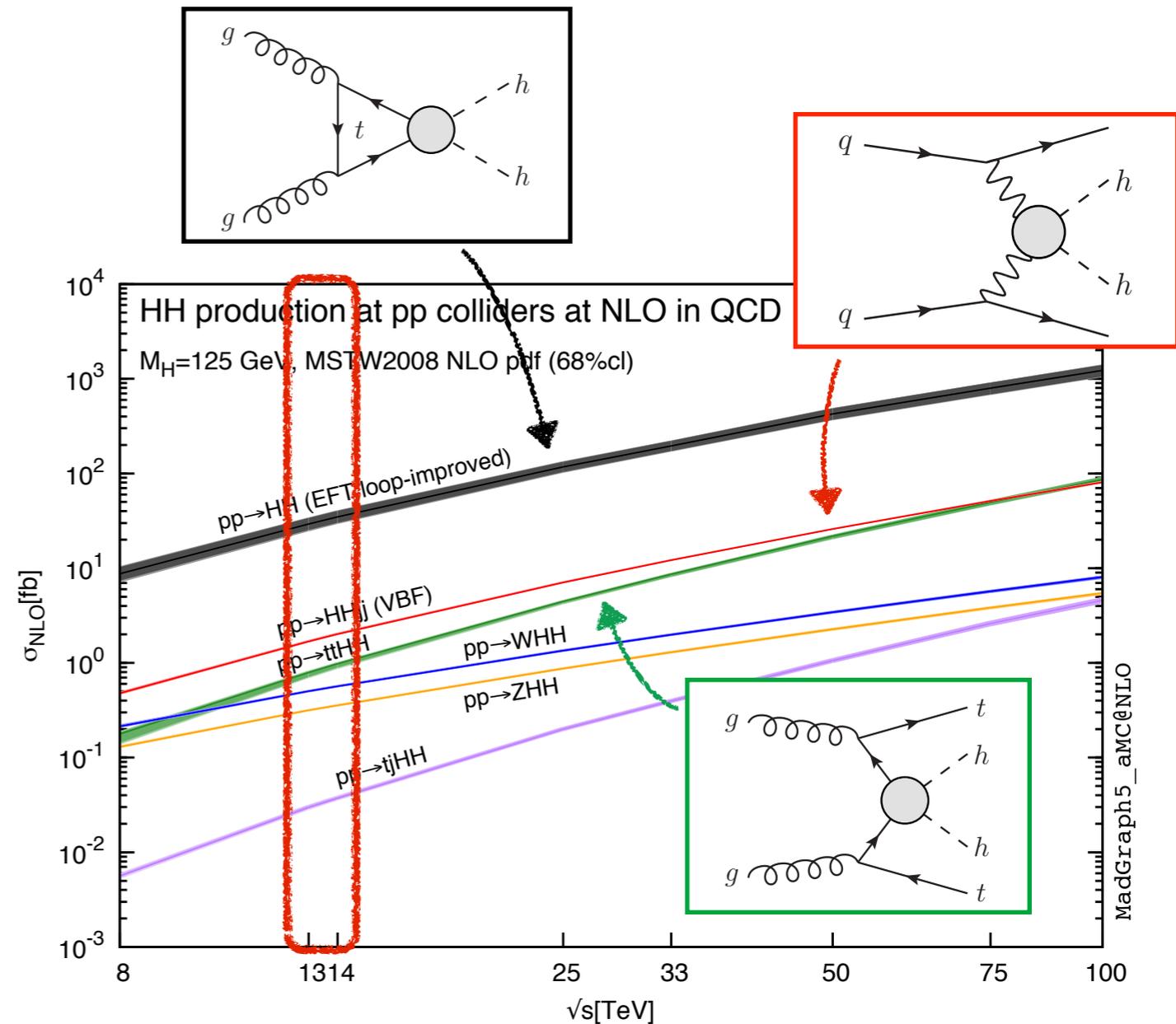
◆ potentially interesting:

• **vector boson fusion (VBF)**

$$\sigma_{14\text{TeV}}^{\text{VBF}} = 1.94^{+2.3\%}_{-2.6\%} (\text{scale}) \text{ fb}$$

• **ttHH** production

$$\sigma_{14\text{TeV}}^{\text{ttHH}} = 0.949^{+1.7\%}_{-4.5\%} (\text{scale}) \text{ fb}$$



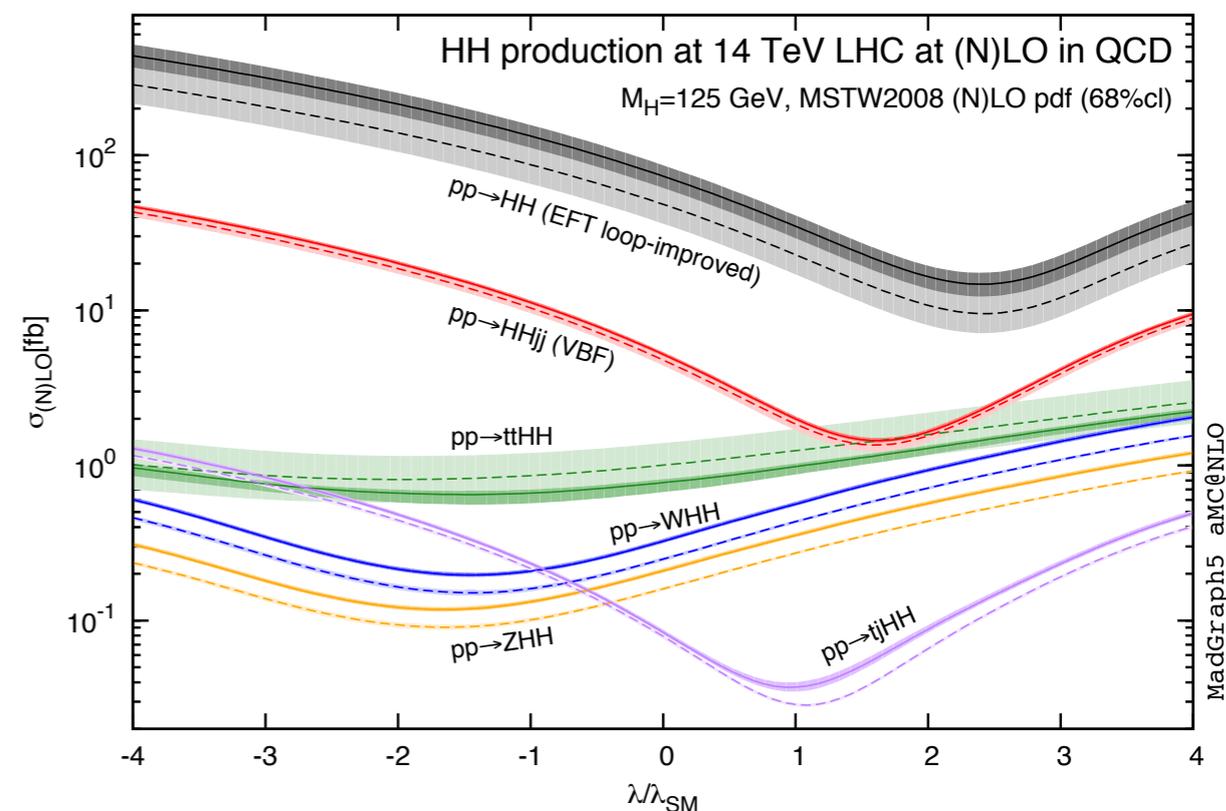
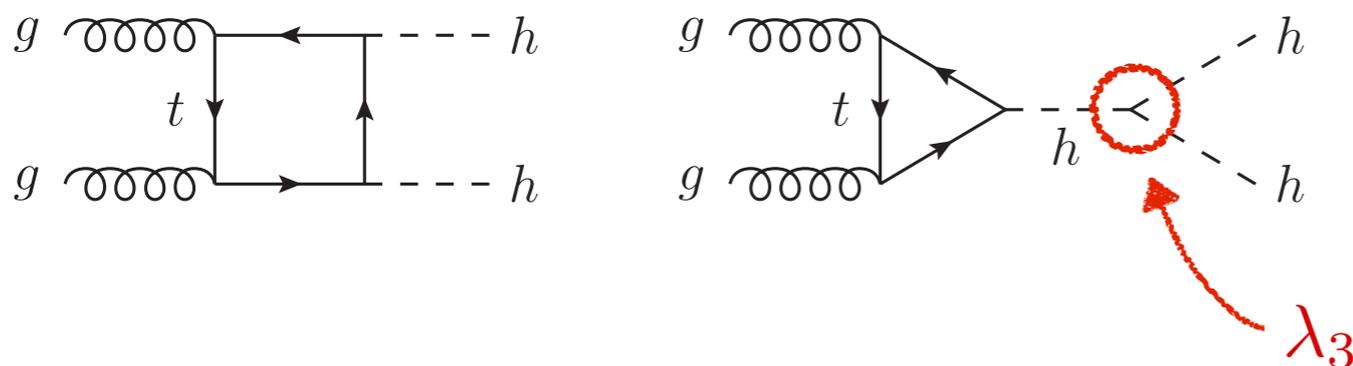
# Why double Higgs?

Obvious answer: directly accessing the Higgs potential!

$$\mathcal{L} = -\frac{1}{2}m_h^2 h^2 - \lambda_3 \frac{m_h^2}{2v} h^3 - \lambda_4 \frac{m_h^2}{8v^2} h^4$$

Significant dependence in the production rates

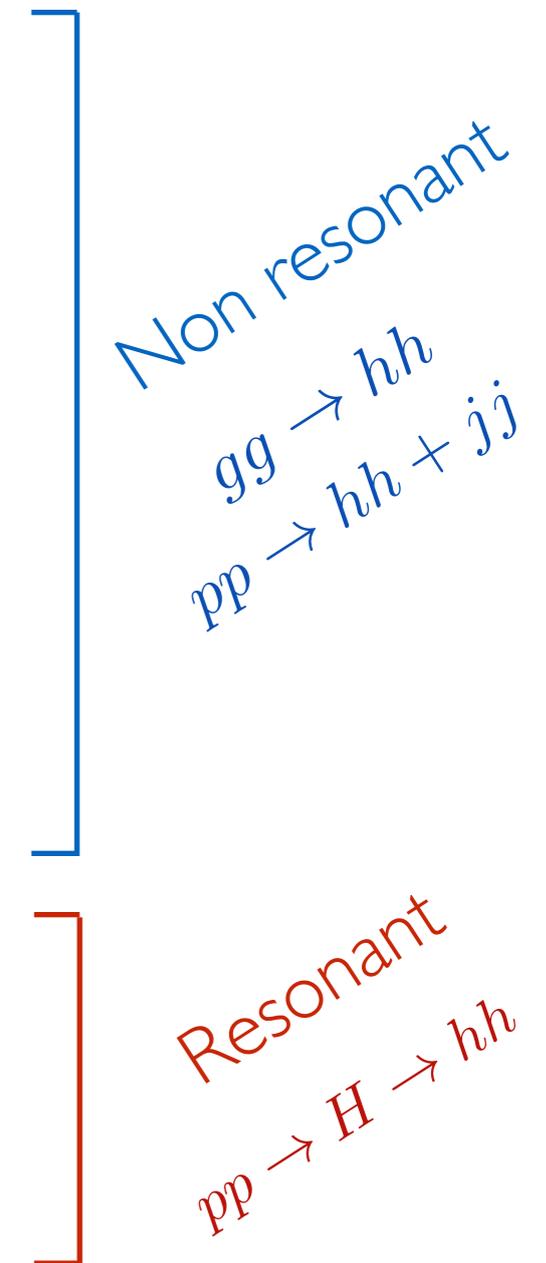
- ♦ in gluon fusion destructive interference



# Why double Higgs?

## Less obvious answers:

- ♦ extract **non-linear couplings** not accessible in single Higgs
- ♦ alternative measurement of **single-Higgs vertices**
- ♦ probe the **strength of EWSB dynamics** at high energy  $E \gg m_h$
- ♦ explore **extended Higgs sectors**



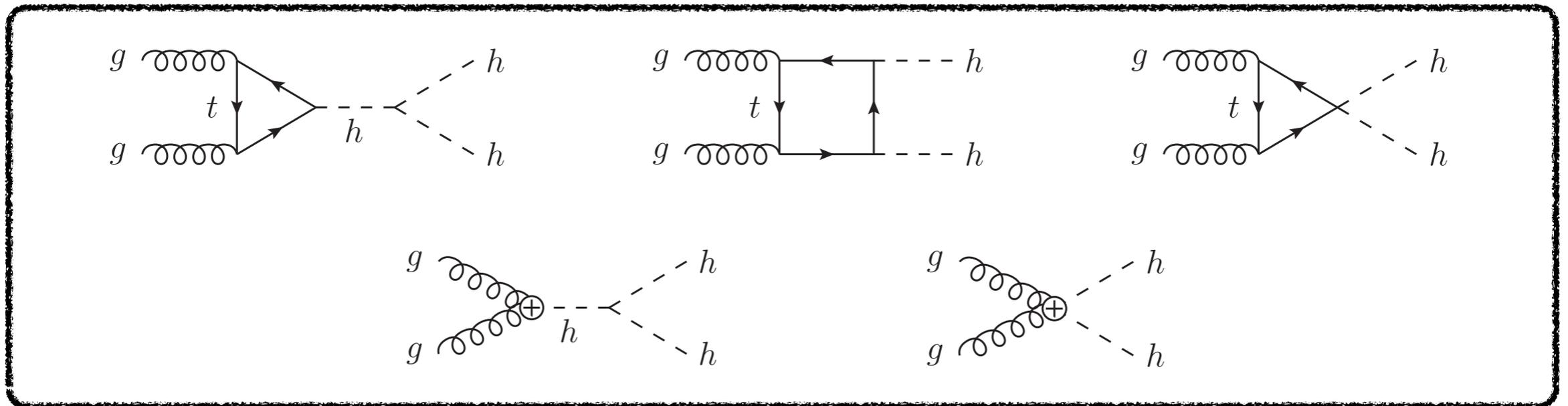
# **Non-resonant processes**

*The Gluon Fusion channel*

# The Higgs effective Lagrangian

Several vertices contribute to double Higgs production in GF

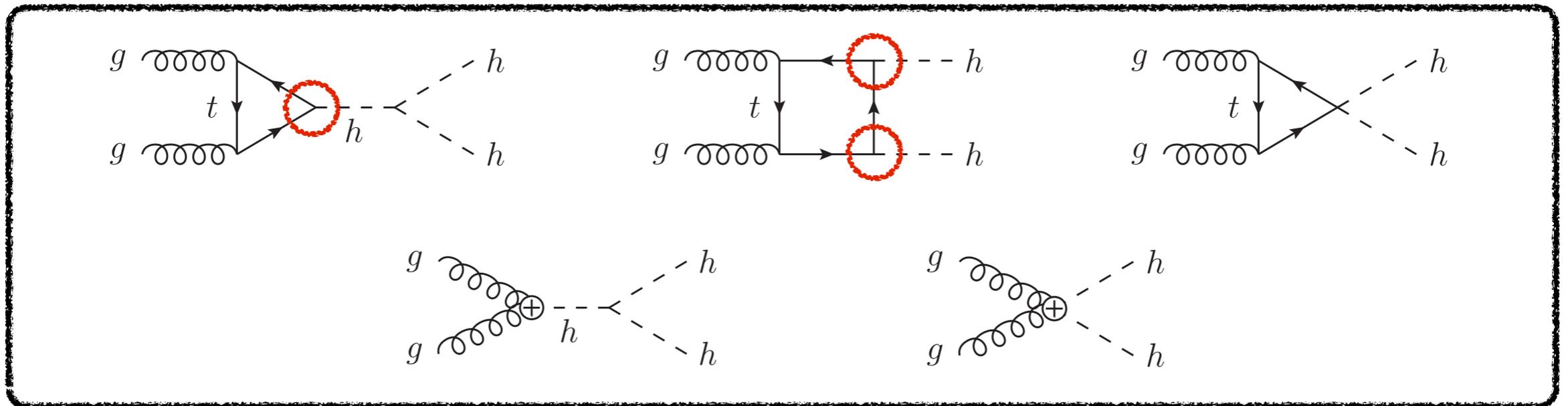
$$\mathcal{L} \supset -m_t \bar{t}t \left( c_t \frac{h}{v} + c_{2t} \frac{h^2}{2v^2} \right) - \lambda_3 \frac{m_h^2}{2v} h^3 + \frac{g_s^2}{4\pi^2} \left( c_g \frac{h}{v} + c_{2g} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu}$$



# Modified single Higgs couplings

Several vertices contribute to double Higgs production in GF

$$\mathcal{L} \supset -m_t \bar{t}t \left( c_t \frac{h}{v} + c_{2t} \frac{h^2}{2v^2} \right) - \lambda_3 \frac{m_h^2}{2v} h^3 + \frac{g_s^2}{4\pi^2} \left( c_g \frac{h}{v} + c_{2g} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu}$$

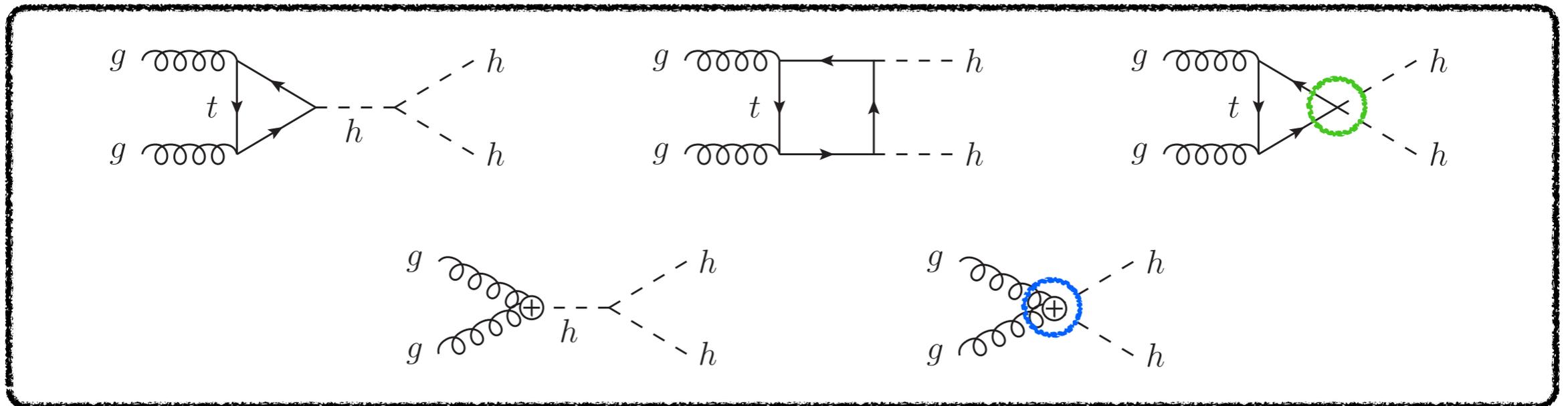


- ◆ modifications of the single Higgs couplings can affect HH production (eg.  $\bar{t}th$ )

# Non-linear Higgs couplings

Several vertices contribute to double Higgs production in GF

$$\mathcal{L} \supset -m_t \bar{t}t \left( c_t \frac{h}{v} + \underbrace{c_{2t}}_{\text{green}} \frac{h^2}{2v^2} \right) - \lambda_3 \frac{m_h^2}{2v} h^3 + \frac{g_s^2}{4\pi^2} \left( c_g \frac{h}{v} + \underbrace{c_{2g}}_{\text{blue}} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu}$$



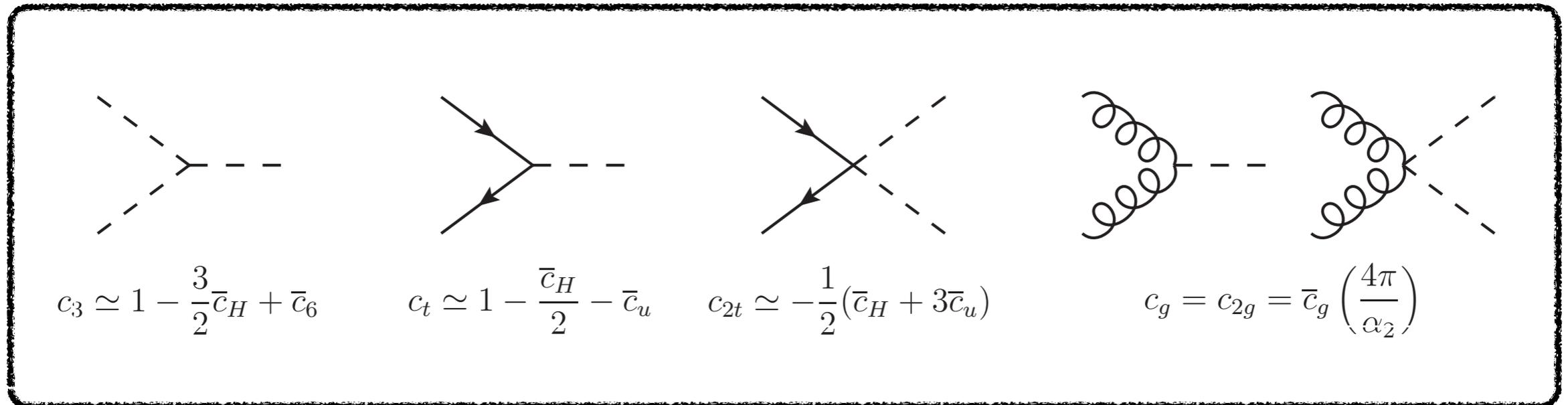
- ♦ modifications of the single Higgs couplings can affect HH production (eg.  $\bar{t}th$ )
- ♦ some vertices can be probed independently only in HH processes (eg.  $\bar{t}thh$ ,  $h^2 G_{\mu\nu} G^{\mu\nu}$ )

# Parametrization for a doublet Higgs

If the Higgs is part of an SU(2) doublet the number of independent operators is reduced

Buchmuller and Wyler; ...  
Giudice et al.; Grzadkowski et al.

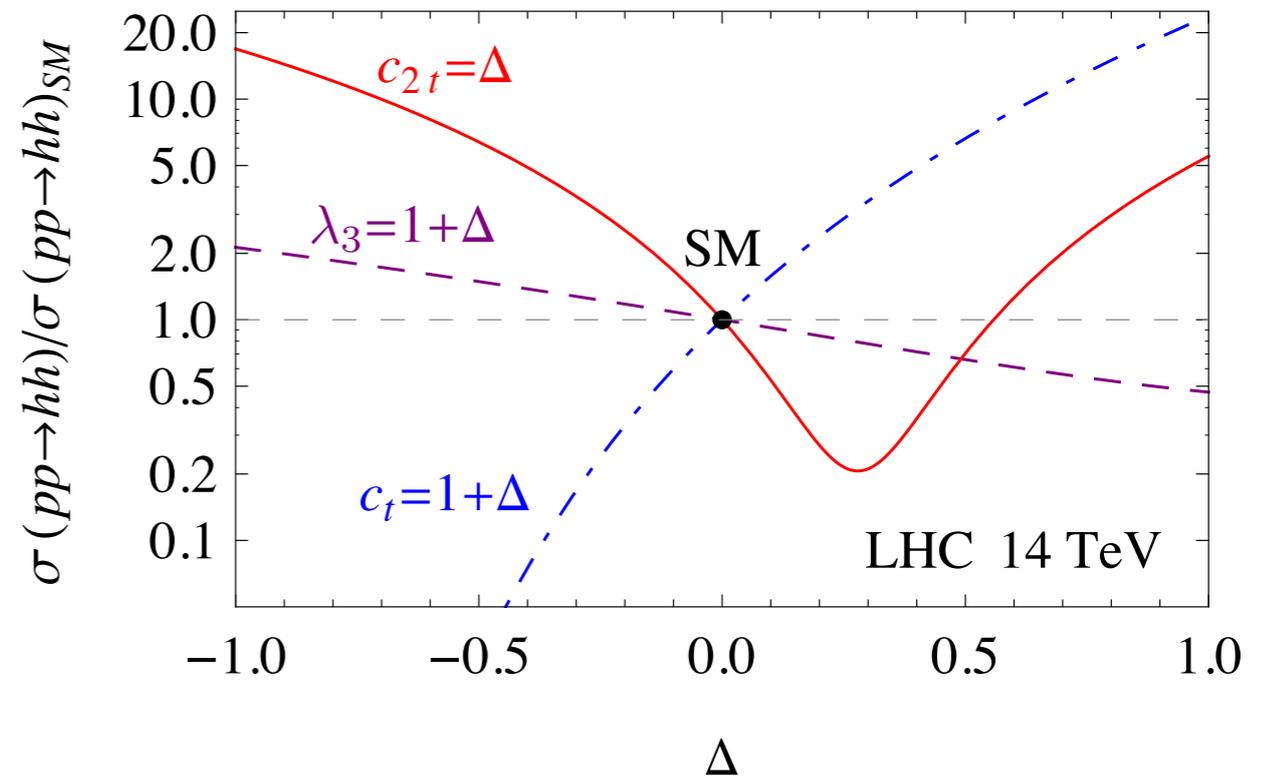
$$\mathcal{L} \supset \frac{\bar{c}_H}{2v^2} [\partial_\mu (H^\dagger H)]^2 + \frac{\bar{c}_u}{v^2} y_u H^\dagger H \bar{q}_L H^c u_R - \frac{\bar{c}_6}{v^2} \frac{m_h^2}{2v^2} (H^\dagger H)^3 + \frac{\bar{c}_g}{m_w^2} g_s^2 H^\dagger H G_{\mu\nu} G^{\mu\nu}$$



◆ requires an additional expansion in Higgs powers

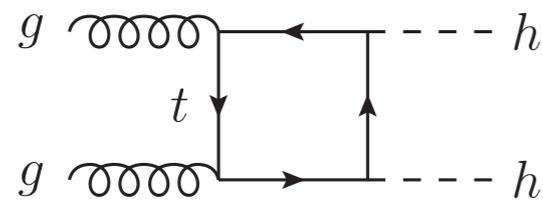
# Dependence on Higgs couplings

- ◆ mild dependence on  $\lambda_3$ 
  - effects mostly at threshold
- ◆ strong dependence on top couplings  $c_t$  and  $c_{2t}$ 
  - affect peak and tail of  $m_{hh}$
- ◆ Shape analysis could disentangle the various interactions

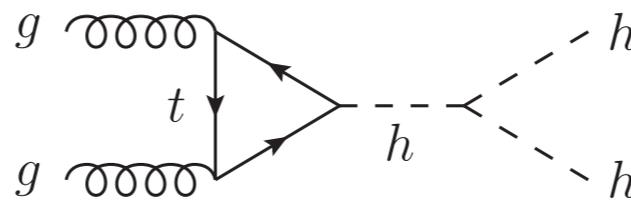


In many BSM scenarios **modifications to all Higgs couplings** arise simultaneously and have comparable size

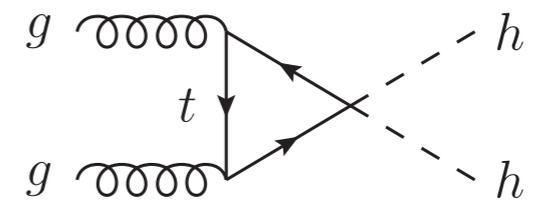
# Behaviour of amplitudes



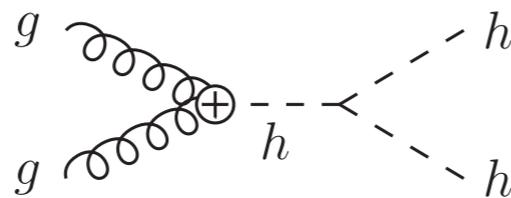
$$\sim c_t^2 \times \text{const.}$$



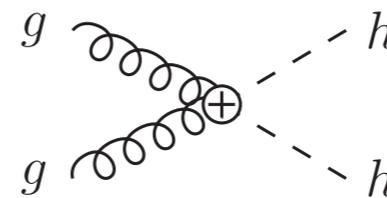
$$\sim c_t c_3 \times \frac{m_h^2}{\hat{s}} \log^2 \left( \frac{m_t^2}{\hat{s}} \right)$$



$$\sim c_{2t} \times \log^2 \left( \frac{m_t^2}{\hat{s}} \right)$$



$$\sim c_g c_3 \frac{\alpha_s}{4\pi} \times \text{const.}$$



$$\sim c_{2g} \frac{\alpha_s}{4\pi} \frac{\hat{s}}{v^2}$$

- ◆ Different behaviour at high energy  $\sqrt{\hat{s}} = m_{hh} \gg 2m_h$
- ◆ Dependence on Higgs trilinear suppressed in the tail
  - events at threshold more sensitive to Higgs trilinear,
  - events at large  $m_{hh}$  more important to determine the other operators

# Final states

GF is the hh production channel with highest cross section

$$\sigma_{14\text{TeV}}^{\text{SM}} \simeq 39.5 \text{ fb}$$

Full LO: Glover, van der Bij '88

Full NLO: Borowka, Greiner et al. '16

Approximate NNLO + NNLL: De Florian, Mazzitelli '13, '15;

Grigo, Melnikov, Steinauser '14; Grigo, Hoff, Steinauser '15;

Shao, Li, Wang '13

Many final states with reasonable number of events at HL-LHC

♦ golden channel:  $b\bar{b}\gamma\gamma$

- small number of events
- clean final state (small bkg)
- can access total cross section

♦ other modes:

$$b\bar{b}\tau^+\tau^-, \quad b\bar{b}WW^*, \quad b\bar{b}b\bar{b}$$

- larger cross section
- large bkg
- may be useful to probe tail of distribution (boosted jet techniques)

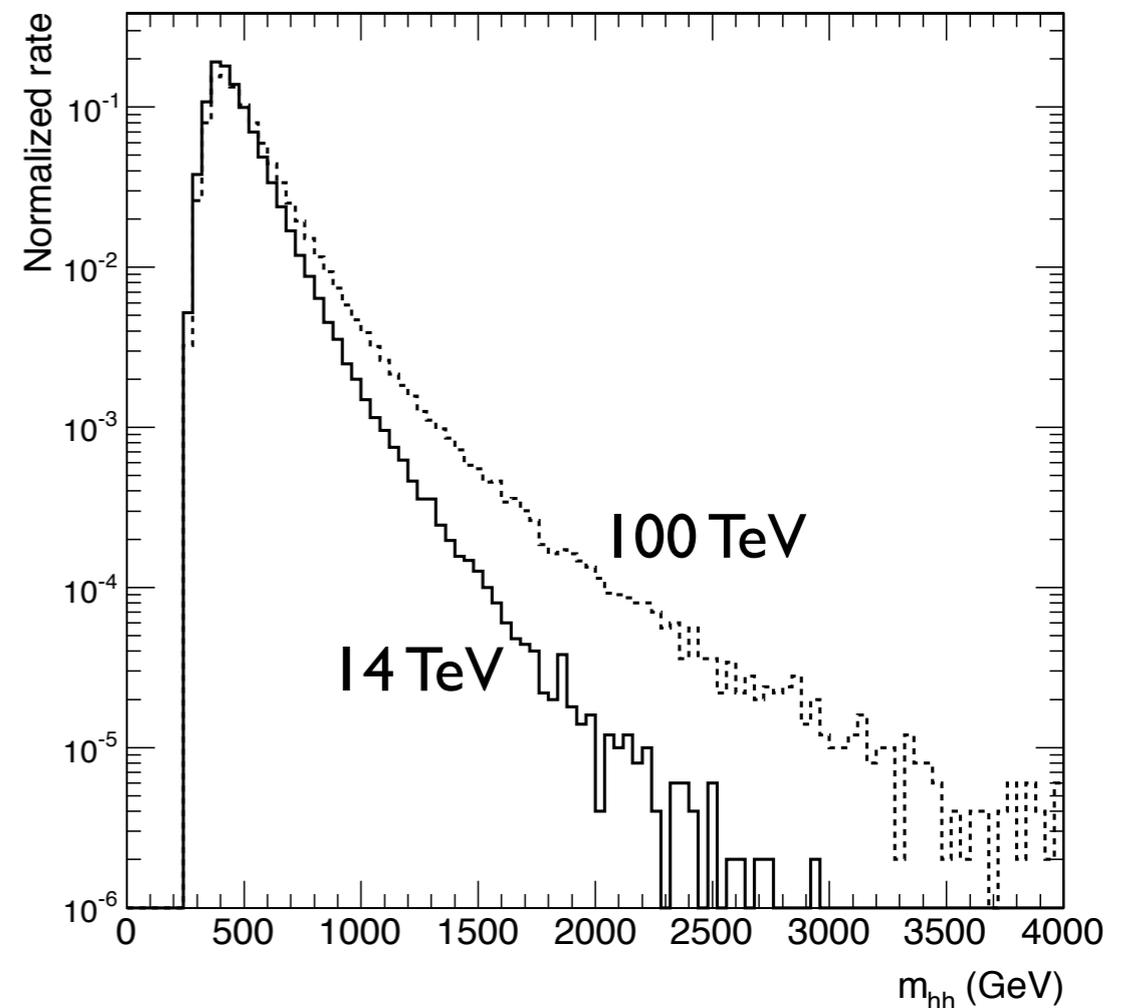
decay channel	BR	events ( $3 \text{ ab}^{-1}$ )
$b\bar{b}b\bar{b}$	33%	40000
$b\bar{b}WW^*$	25%	31000
$b\bar{b}\tau^+\tau^-$	7.3%	8900
$ZZb\bar{b}$	3.1%	3800
$WW^*\tau^+\tau^-$	2.7%	3300
$ZZWW^*$	1.1%	1300
$b\bar{b}\gamma\gamma$	0.26%	320

# Gluon Fusion at 100 TeV

- ◆ huge increase in cross section ( $\sim 40$  times 14 TeV)

$$\sigma_{100\text{TeV}}^{\text{SM}} \simeq 1400 \text{ fb}$$

- ◆ similar shape at threshold and around the peak
- ◆ significant increase in the high  $m_{hh}$  tail



# (Partial) List of theoretical analyses

- $hh \rightarrow b\bar{b}\gamma\gamma$

Baur, Plehn, Rainwater hep-ph/0310056

Baglio, Djouadi, Grober, Mullheitner, Quevillon et al. 1212.5581

Yao 1308.6302

Barger, Everett, Jackson, Shaughnessy 1311.2931

Azatov, Contino, Panico, Son 1502.00539

Kling, Plehn, Schichtel 1607.07441

- $hh \rightarrow b\bar{b}\tau^+\tau^-$

Baur, Plehn, Rainwater hep-ph/0304015

Dolan, Englert, Spannowsky 1206.5001

Baglio, Djouadi, Grober, Mullheitner, Quevillon et al. 1212.5581

Barr, Dolan, Englert, Spannowsky 1309.6318

Goertz, Papaefstathiou, Yang, Zurita 1410.3471

- $hh \rightarrow b\bar{b}WW^*$

Dolan, Englert, Spannowsky 1206.5001

Baglio, Djouadi, Grober, Mullheitner, Quevillon et al. 1212.5581

Papaefstathiou, Yang, Zurita 1209.1489

- $hh \rightarrow b\bar{b}b\bar{b}$

de Lima, Papaefstathiou, Spannowsky 1404.7139

- comprehensive study at 100 TeV:

Contino et al., "Physics at a 100 TeV pp collider: Higgs and EW symmetry breaking studies", 1606.09408

*The Golden Channel  $b\bar{b}\gamma\gamma$*

# The Higgs trilinear at HL-LHC

Tiny cross section:  $\sigma_{\text{SM}}(HH \rightarrow b\bar{b}\gamma\gamma) \simeq 0.1 \text{ fb}$

Main backgrounds:

	events after selection	(CMS analysis FTR-15-002) see also ATLAS: PHYS-PUB-2014-019, PHYS-PUB-2015-46
resonant	$ZH$	3.4
	$t\bar{t}H$	1.6
	$b\bar{b}H$	0.8
non resonant	$b\bar{b}\gamma\gamma$	10.4
	$b\bar{b}j\gamma$	6.3
	$jj\gamma\gamma$	2.1
	$b\bar{b}jj$	1.1
	$t\bar{t}\gamma$	1.2
	<hr/>	
	total	24.8

signal events: 9.0  
**Only  $\mathcal{O}(1)$  determination  
of  $\lambda_3$  is possible**

◆ Some improvement possible with multivariate techniques

Kling, Plehn, Schichten '16

$$\frac{\lambda}{\lambda_{\text{SM}}} \in [0.4, 1.7] \quad \text{at } 68\% \text{ CL}$$

# Prospects at 100 TeV

Sizeable cross section:  $\sigma_{\text{SM}}(HH \rightarrow b\bar{b}\gamma\gamma) \simeq 3.6 \text{ fb}$

Main backgrounds:

events after selection with  $20 \text{ ab}^{-1}$

(Contino et al. 1606.09408)

see also Kling, Plehn, Schichten '16

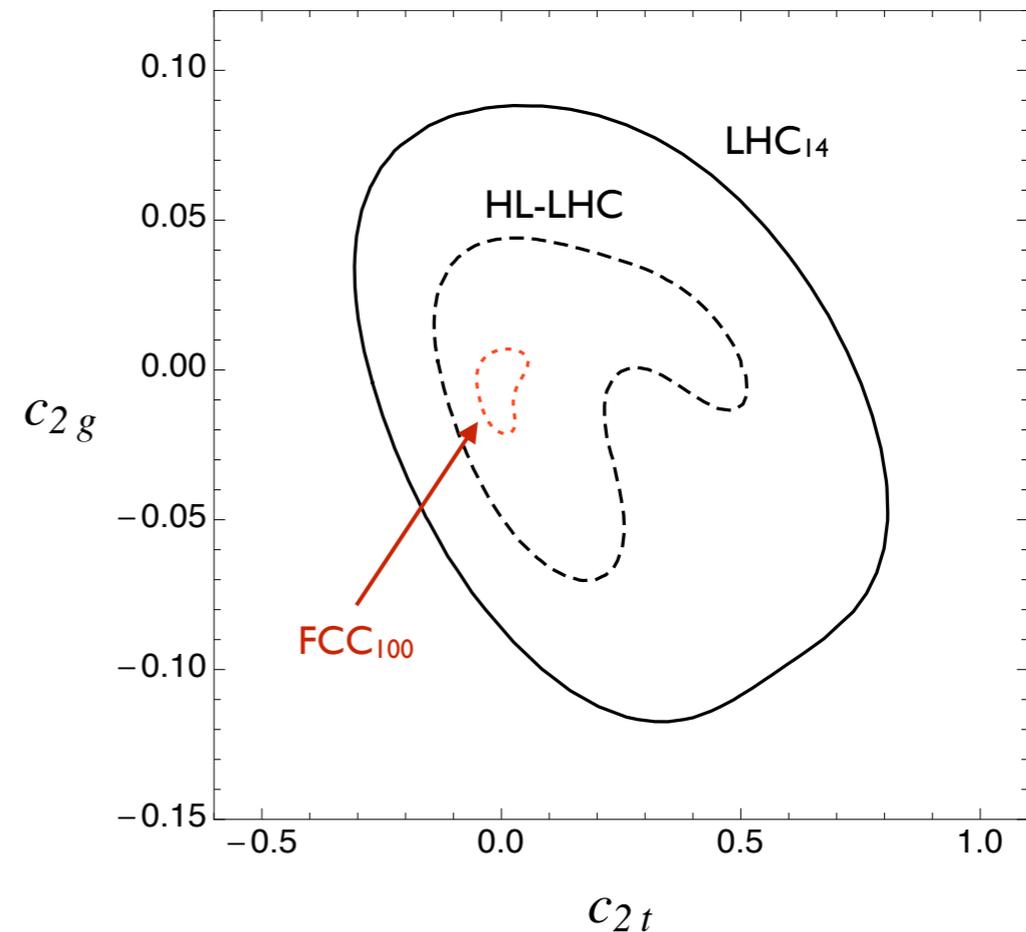
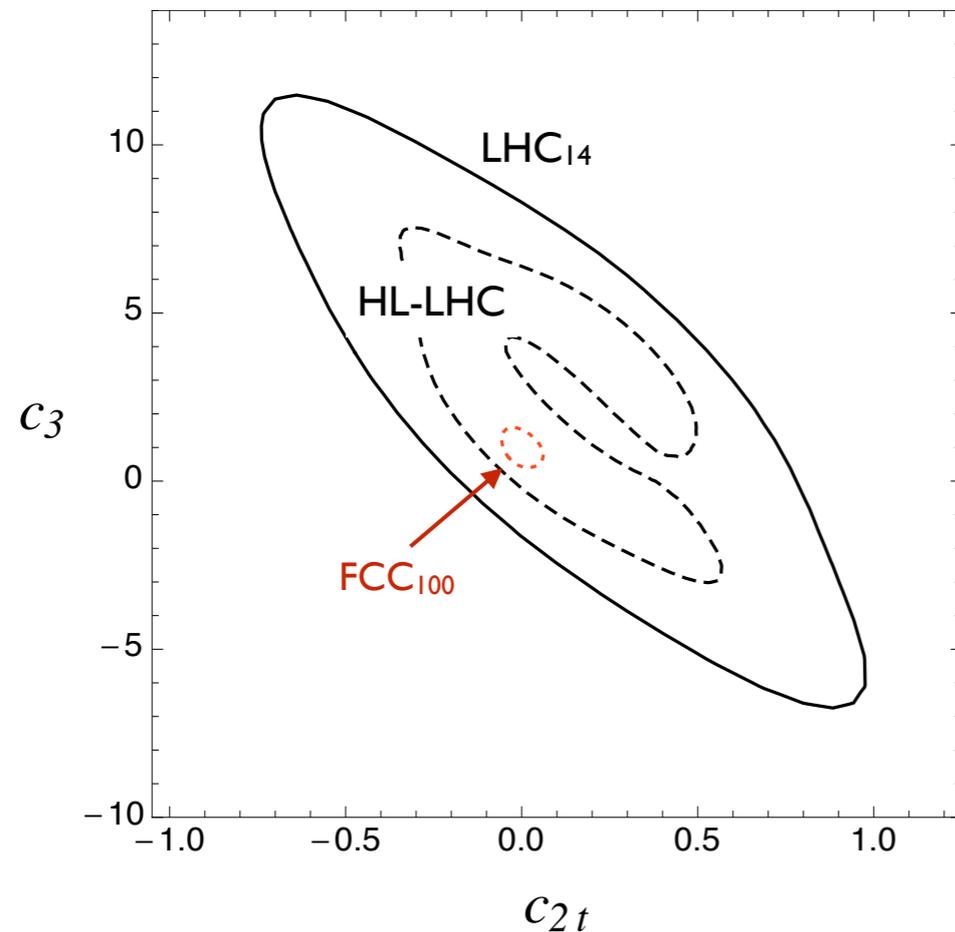
res.	$t\bar{t}H$	3250
	$b\bar{b}j\gamma$	9300
non res.	$jj\gamma\gamma$	3250
	$b\bar{b}\gamma\gamma$	2000
	total	<hr/> 17800

signal events: 7400

- ◆ Good precision on **SM cross section**:  $\sim 2\%$  at 68% CL
- ◆ Good determination of **Higgs trilinear**:  $\sim 4.5\%$  at 68% CL

# Fit to non-linear Higgs couplings

Determination of  $c_3$ ,  $c_{2t}$  and  $c_{2g}$

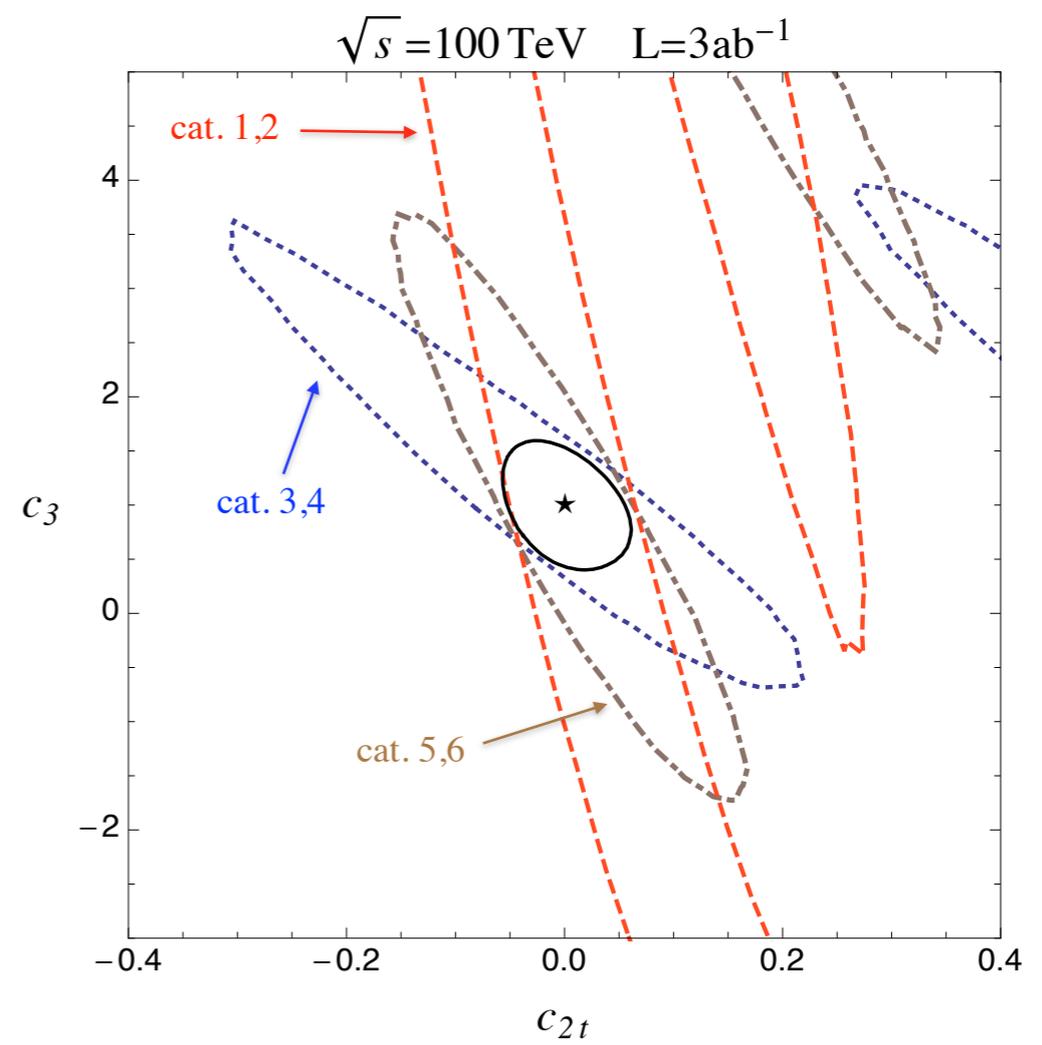
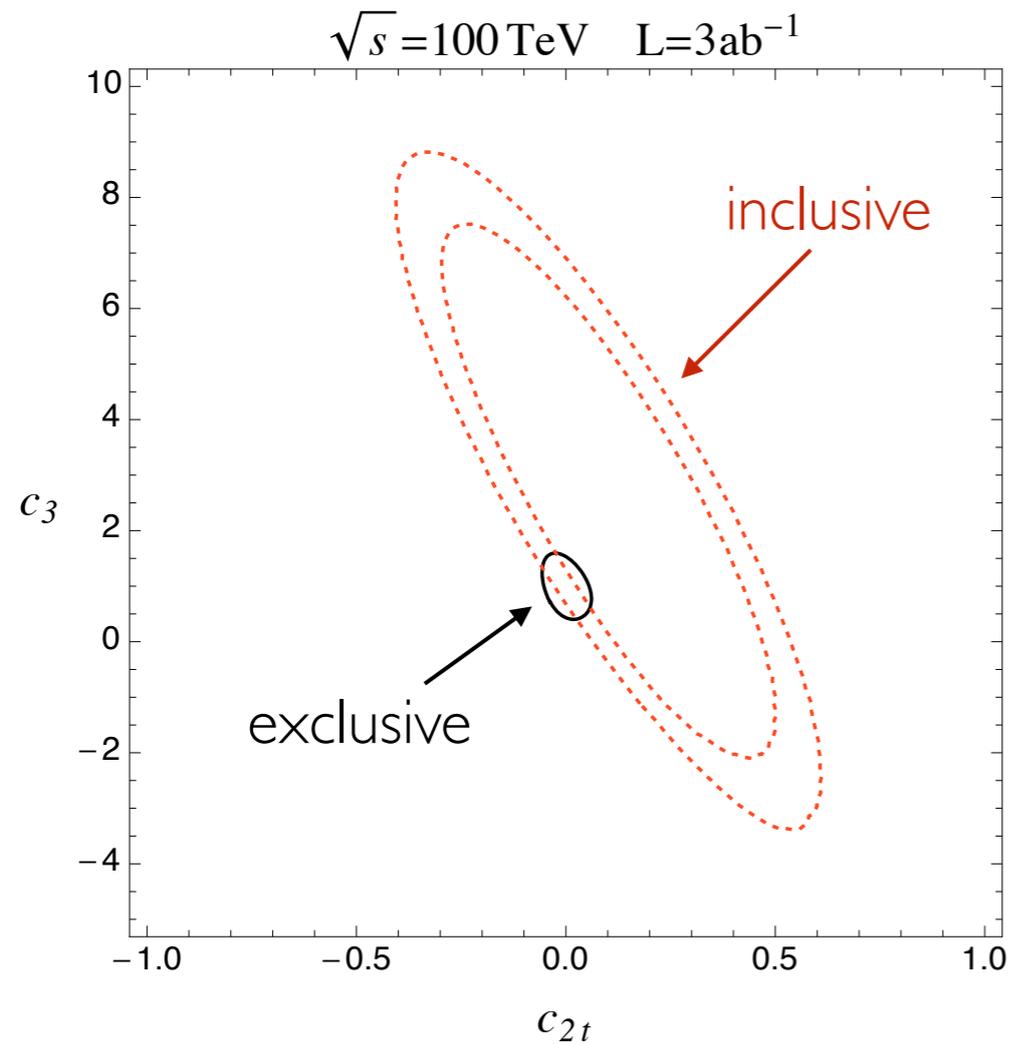


- ◆ Correlation between Higgs trilinear and top couplings
- ◆ Good precision on contact interactions to top and gluons

benchmark scenarios:

<b>LHC<sub>14</sub></b>	$\sqrt{s} = 14 \text{ TeV}$ ,	$L = 300 \text{ fb}^{-1}$
<b>HL-LHC</b>	$\sqrt{s} = 14 \text{ TeV}$ ,	$L = 3 \text{ ab}^{-1}$
<b>FCC<sub>100</sub></b>	$\sqrt{s} = 100 \text{ TeV}$ ,	$L = 3 \text{ ab}^{-1}$

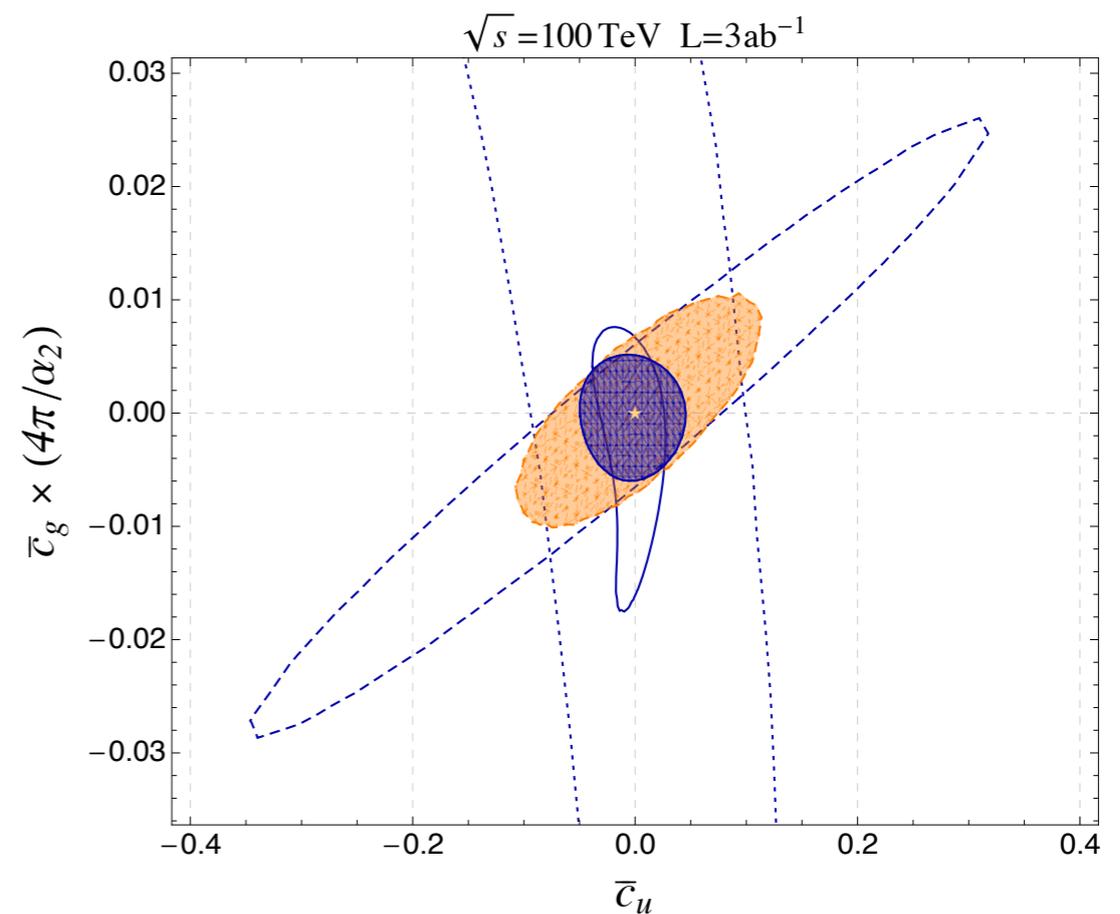
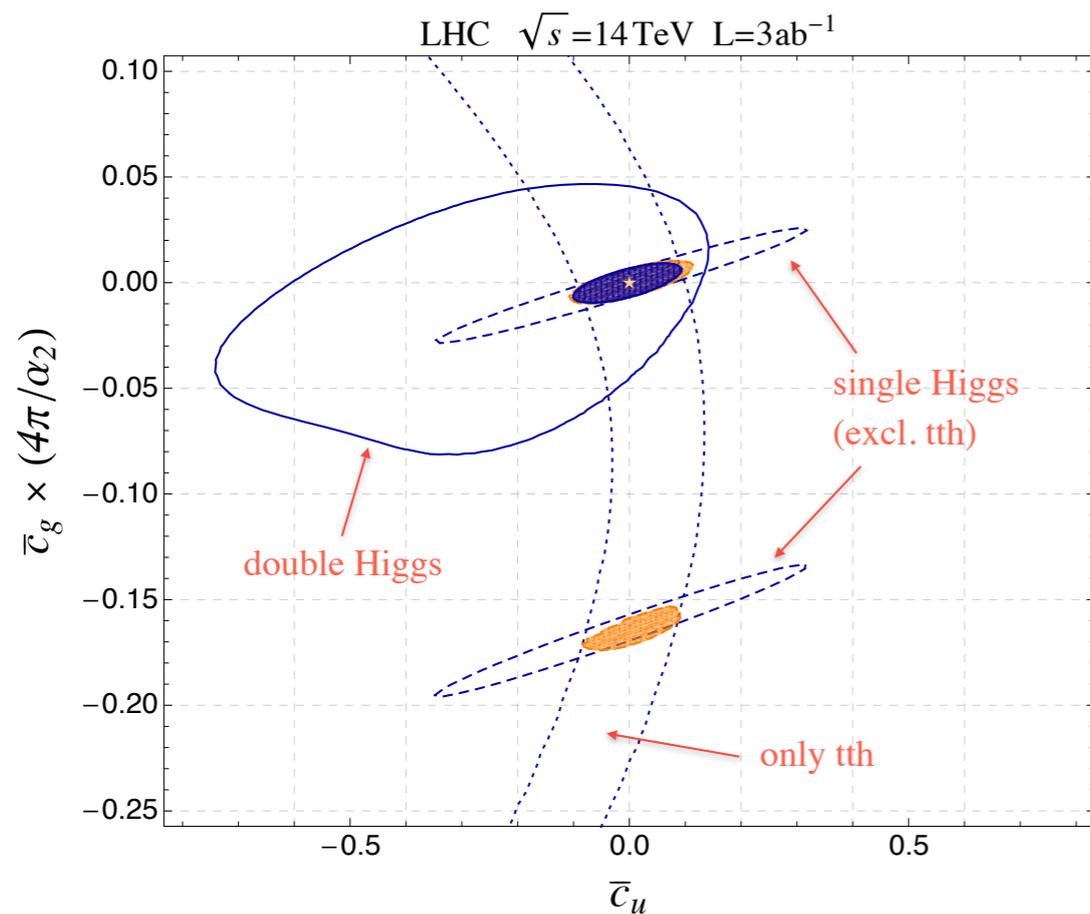
# Exclusive vs inclusive analysis



**Exclusive analysis** is crucial at FCC<sub>100</sub>

category	1	2	3	4	5	6
$m_{hh}$ [GeV]	250 - 400	400 - 550	550 - 700	700 - 850	850 - 1000	1000 -

# Operators in the Higgs doublet basis



- ◆ Double Higgs measurement can resolve the degeneracy in  $c_g$
- ◆ At FCC<sub>100</sub> can be competitive with  $t\bar{t}h$  for the determination of the top Yukawa  $\bar{c}_u$  (if precision from single Higgs similar to the LHC one)

orange region: single Higgs incl.  $t\bar{t}h$

blue region: single + double Higgs

# **Non-resonant processes**

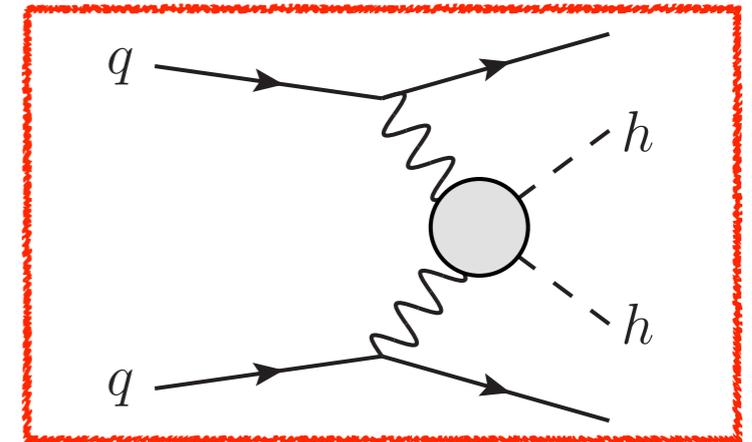
## *The Vector Boson Fusion channel*

*results from Contino, Rojo, work in progress (courtesy of R. Contino)*

# Testing the strength of EWSB

VBF can test perturbative unitarization

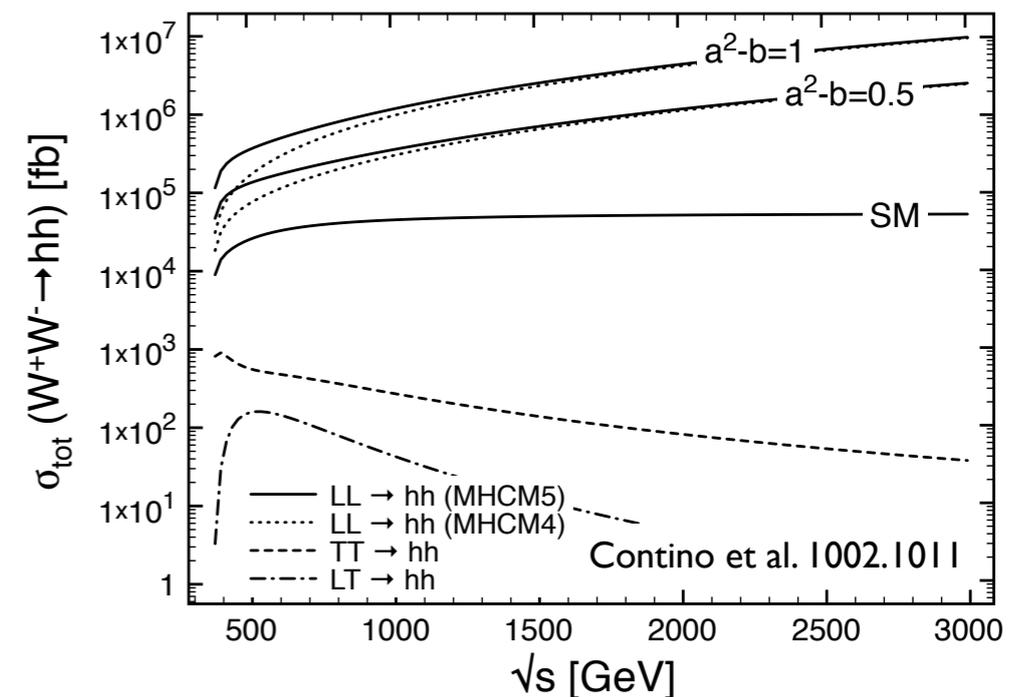
$$\mathcal{L} \supset \left( m_W^2 W_\mu^2 + \frac{m_Z^2}{2} Z_\mu^2 \right) \left( 1 + 2c_V \frac{h}{v} + c_{2V} \frac{h^2}{v^2} \right)$$



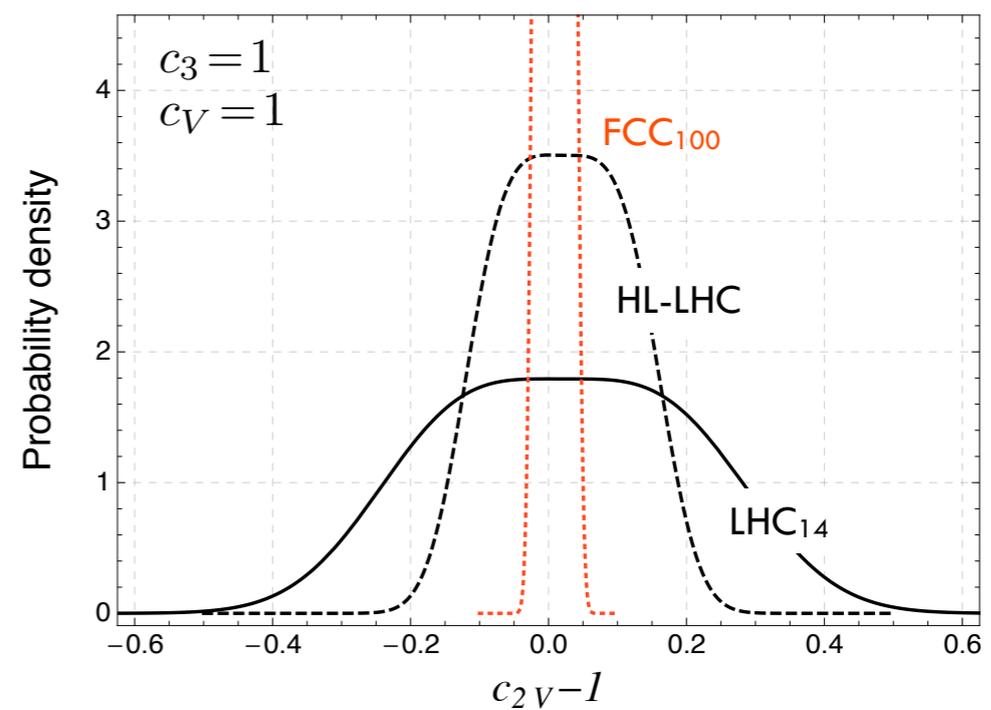
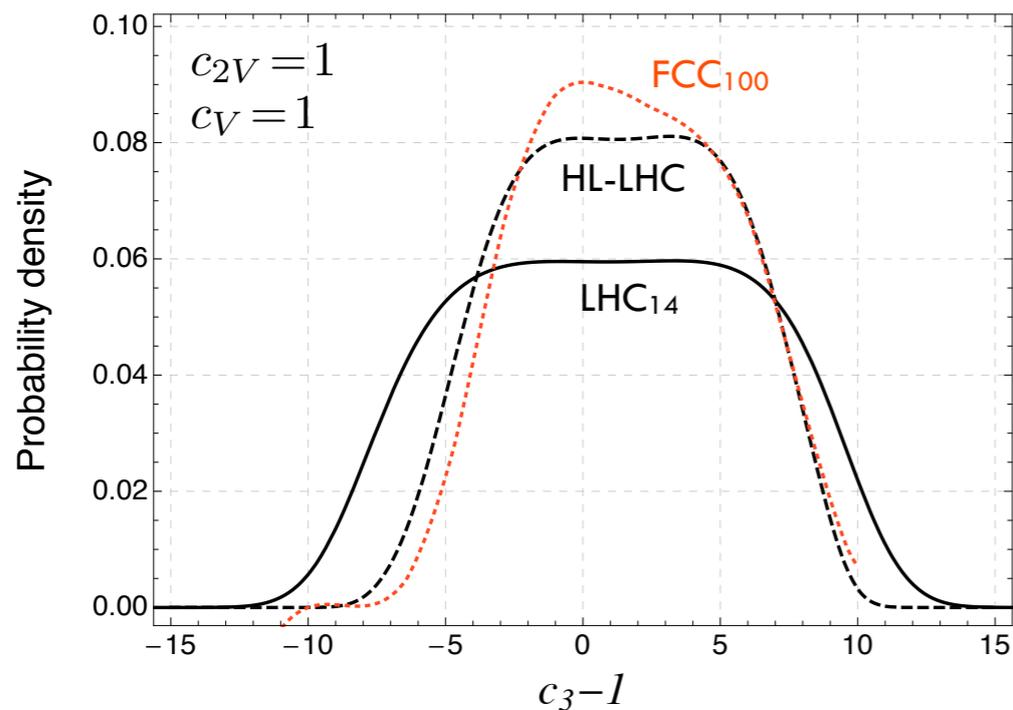
- ◆ Cross section grows at high  $m_{hh}$  if the couplings are modified (in the SM  $c_V = c_{2V} = 1$ )

$$\sim \frac{\hat{s}}{v^2} (c_V^2 - c_{2V})$$

$$\sim \frac{m_h^2}{v^3} \lambda_3 c_V$$



# Higgs couplings from VBF



Best channel:  $hh \rightarrow 4b$

- ♦ huge background, sensitive only if deviations much larger than SM
- ♦ poor precision on Higgs trilinear (not competitive with GF)
- ♦ FCC<sub>100</sub> can provide good bounds on  $\Delta c_{2V} \equiv c_{2V} - 1$

68% probability intervals  
on  $\Delta c_{2V}$

LHC <sub>14</sub>	HL-LHC	FCC <sub>100</sub>
[-0.18, 0.22]	[-0.08, 0.12]	[-0.01, 0.03]

# **Resonant processes**

*Scalar Singlet production*

# Additional scalar singlet

Extensions of the Higgs sector are quite common in BSM scenarios

Additional **singlet**  $\phi$  is often present (eg. NMSSM, Twin Higgs, ...)

*results taken from Buttazzo, Sala, Tesi, I505.05488  
see also references therein*

- ◆ Couplings controlled by the mixing with the Higgs

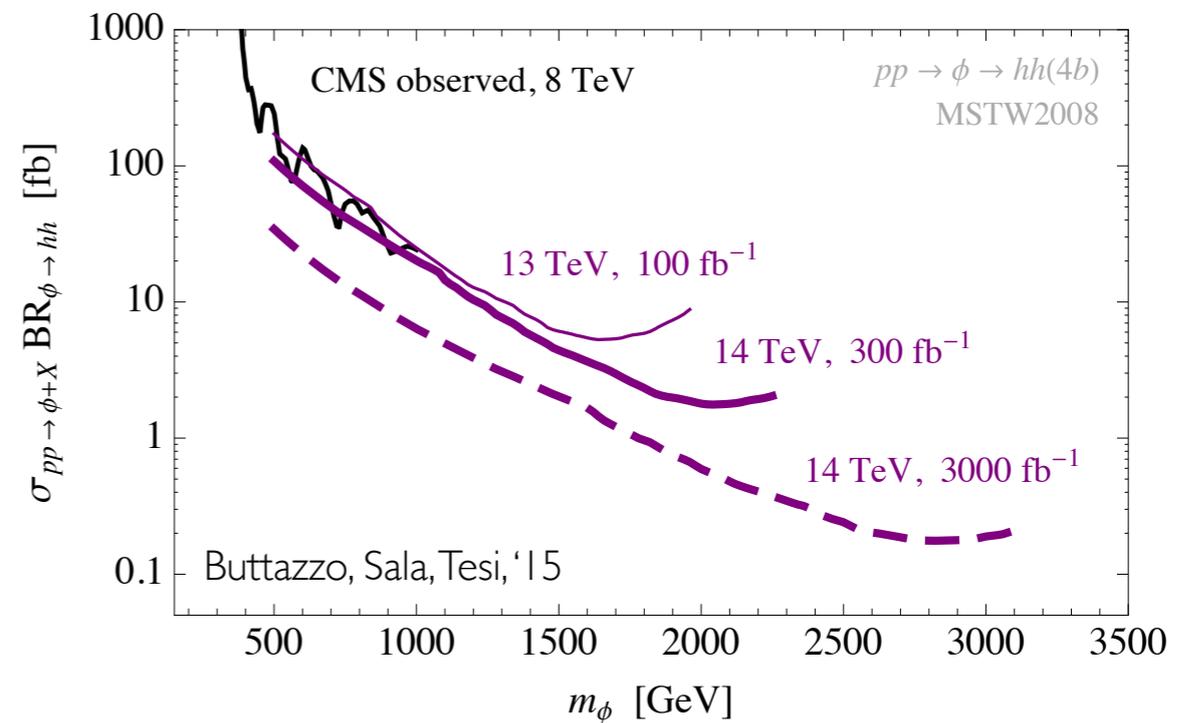
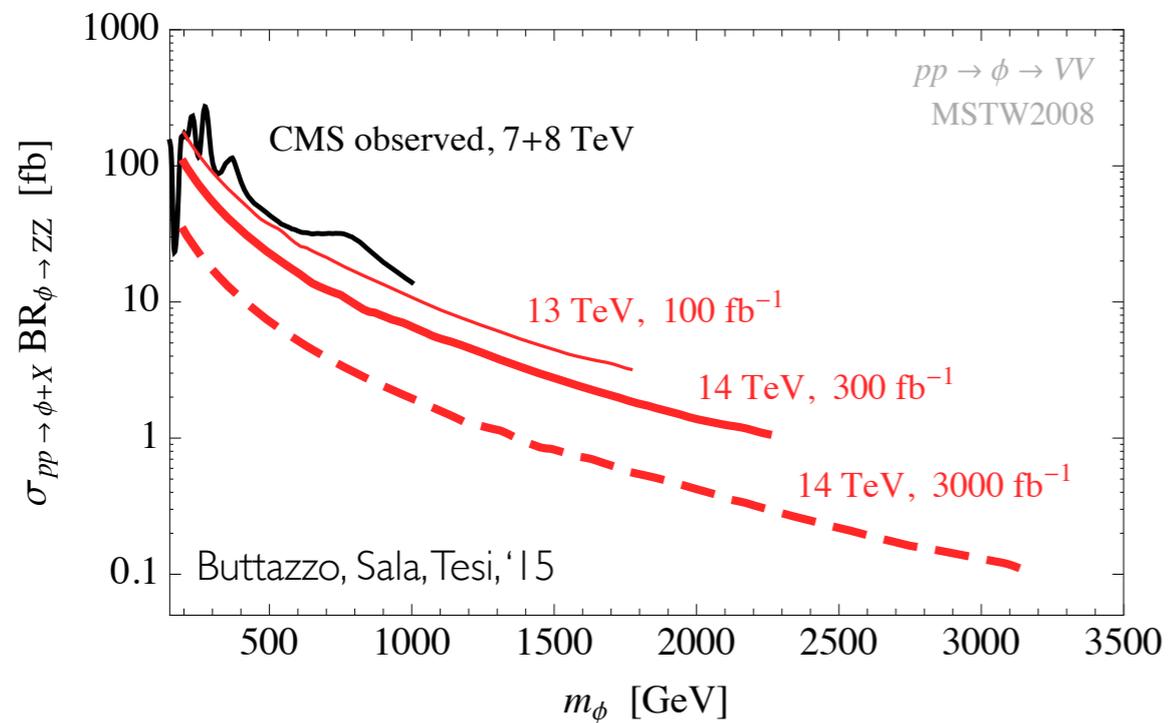
$$\begin{array}{ll} \text{couplings to SM} & \frac{g_{\phi ff}}{g_{hff}^{\text{SM}}} = \frac{g_{\phi VV}}{g_{hVV}^{\text{SM}}} = \sin \gamma = \left( \frac{M_{hh}^2 - m_h^2}{m_\phi^2 - m_h^2} \right)^{1/2} \\ \text{coupling to the Higgs} & g_{\phi hh} \end{array}$$

- ◆ Main decay channels

$$\text{BR}(\phi \rightarrow hh) = \text{BR}(\phi \rightarrow ZZ) = \frac{1}{2} \text{BR}(\phi \rightarrow WW) = \frac{1}{4}, \quad \text{for } m_\phi \gg m_W$$

# Direct searches

Direct searches can exploit the  $VV$  and  $hh$  channels

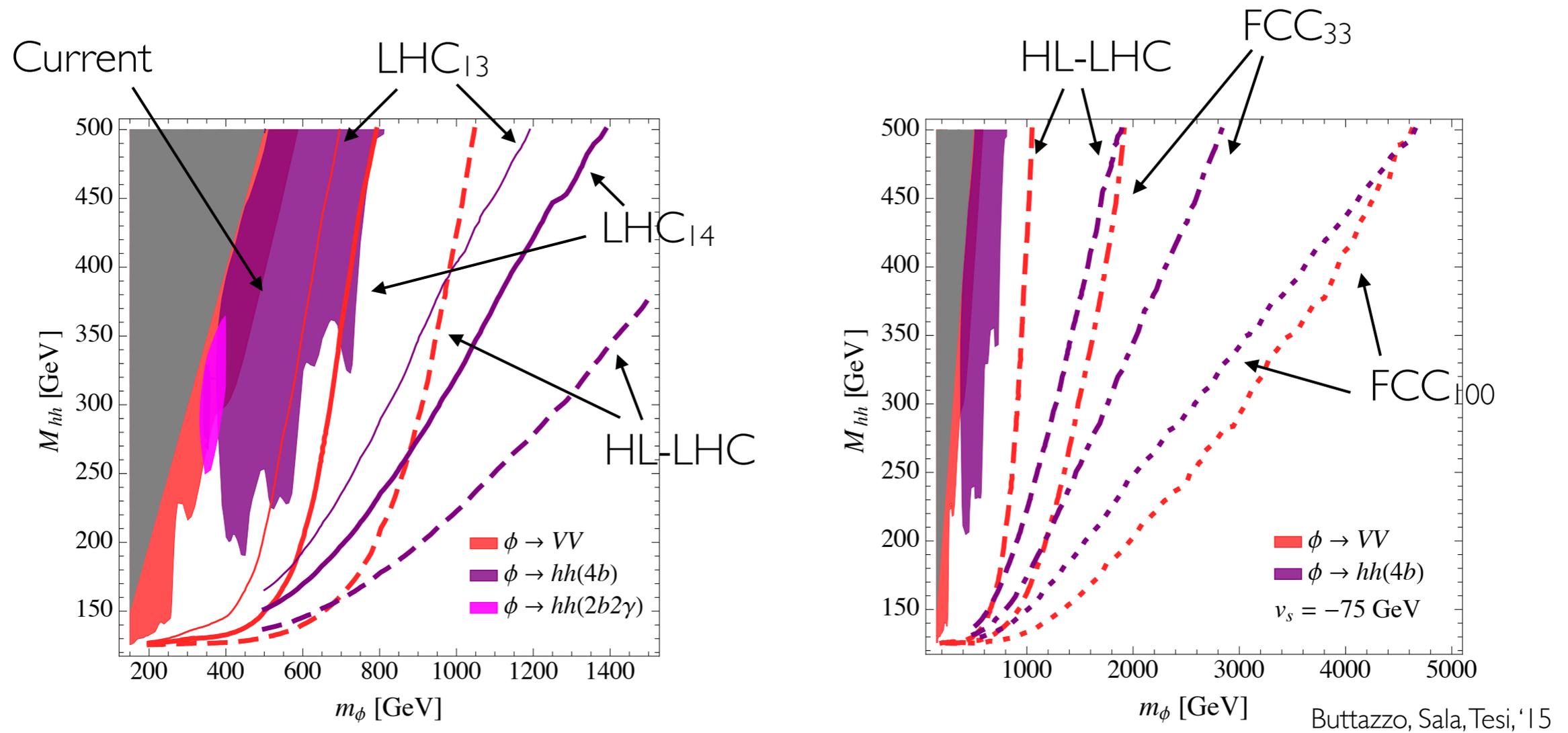


Current experimental analyses in the  $\phi \rightarrow hh(4b)$  channel

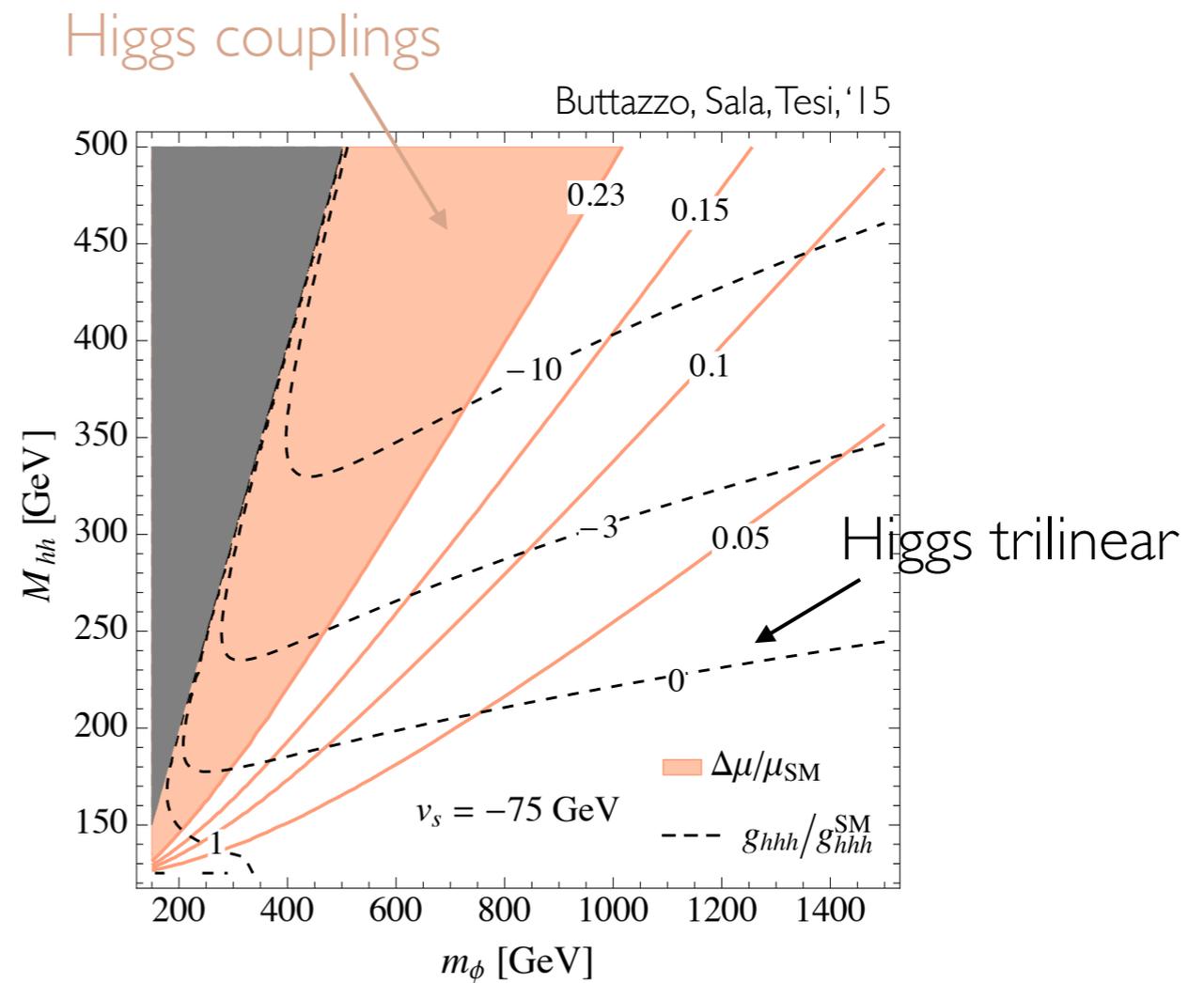
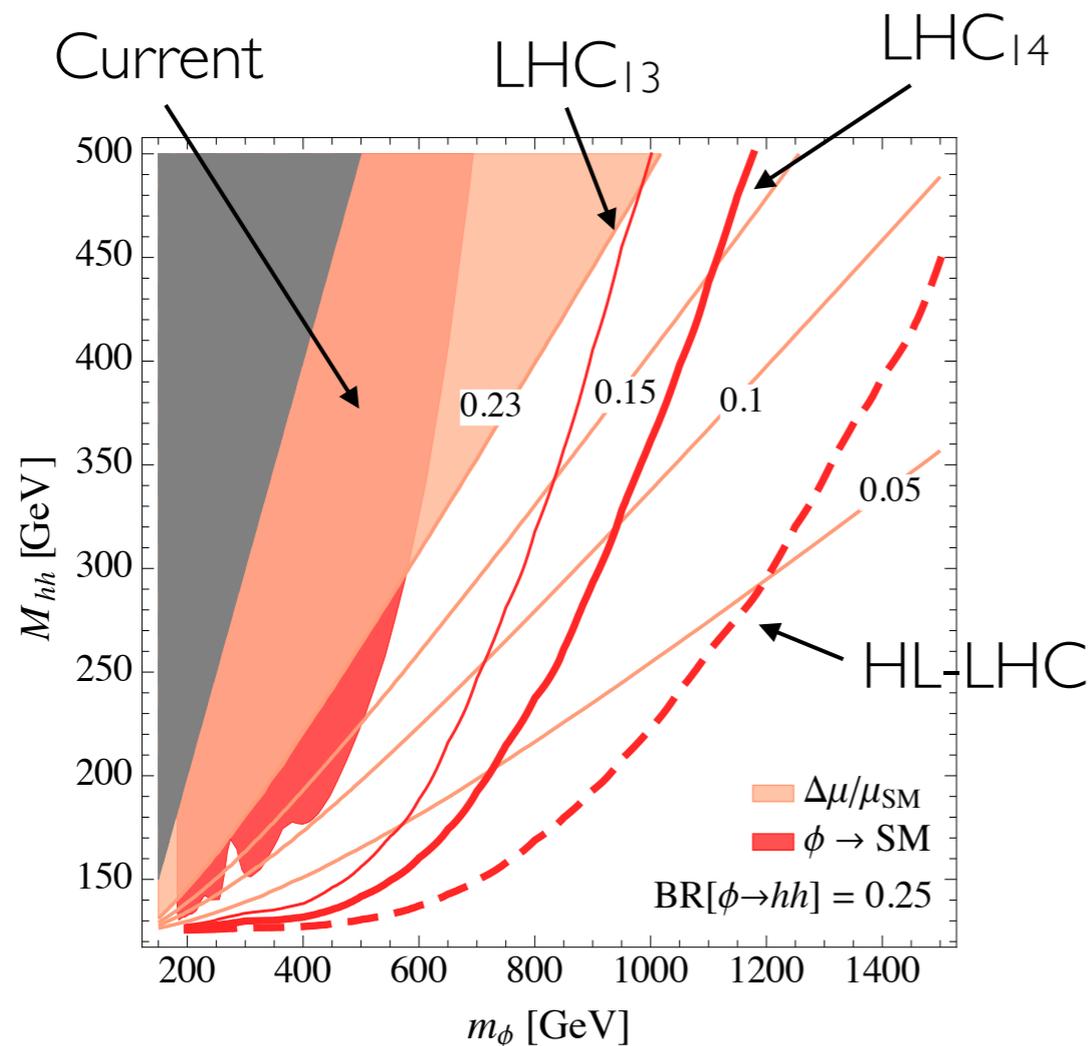
8 TeV	ATLAS	CONF-2014-005
	CMS	1503.04114
13 TeV	ATLAS	CONF-2016-049

# Reach of direct searches

In some regions of the parameter space, the  $\phi \rightarrow hh(4b)$  channel give the best reach



# Deviations in the Higgs couplings



- ◆ Direct searches can be competitive with indirect constraints from Higgs couplings deviations
- ◆ Sizeable deviations in the Higgs trilinear coupling expected

# **Conclusions**

# Conclusions

Double Higgs production can give access to a rich landscape of phenomena both in the SM and Beyond

## ◆ **Non-resonant** processes

- probe Higgs potential (in particular Higgs trilinear)
- access non-linear Higgs couplings
- test the strength of EWSB at high energy
- small cross section:
  - limited precision at LHC
  - good prospects at future high energy colliders (eg. FCC<sub>100</sub>)

## ◆ **Resonant** processes

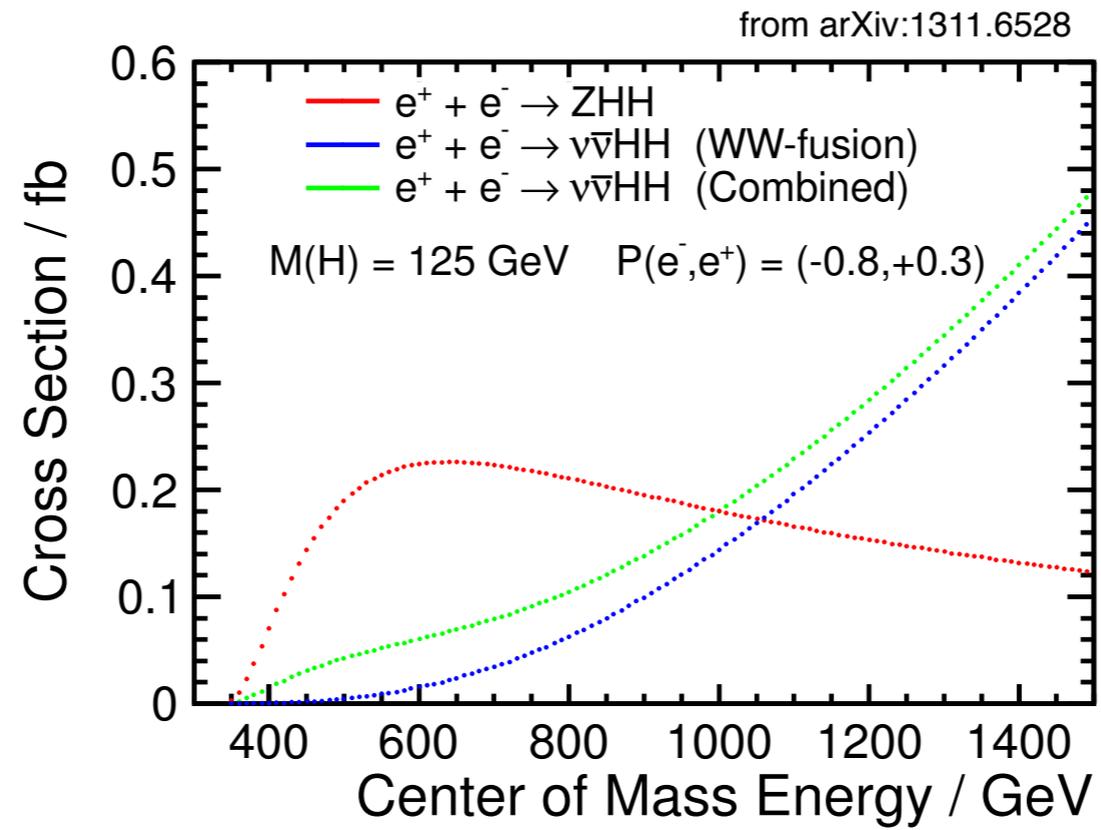
- test extended Higgs sectors
- good reach possible at HL-LHC

**Backup**

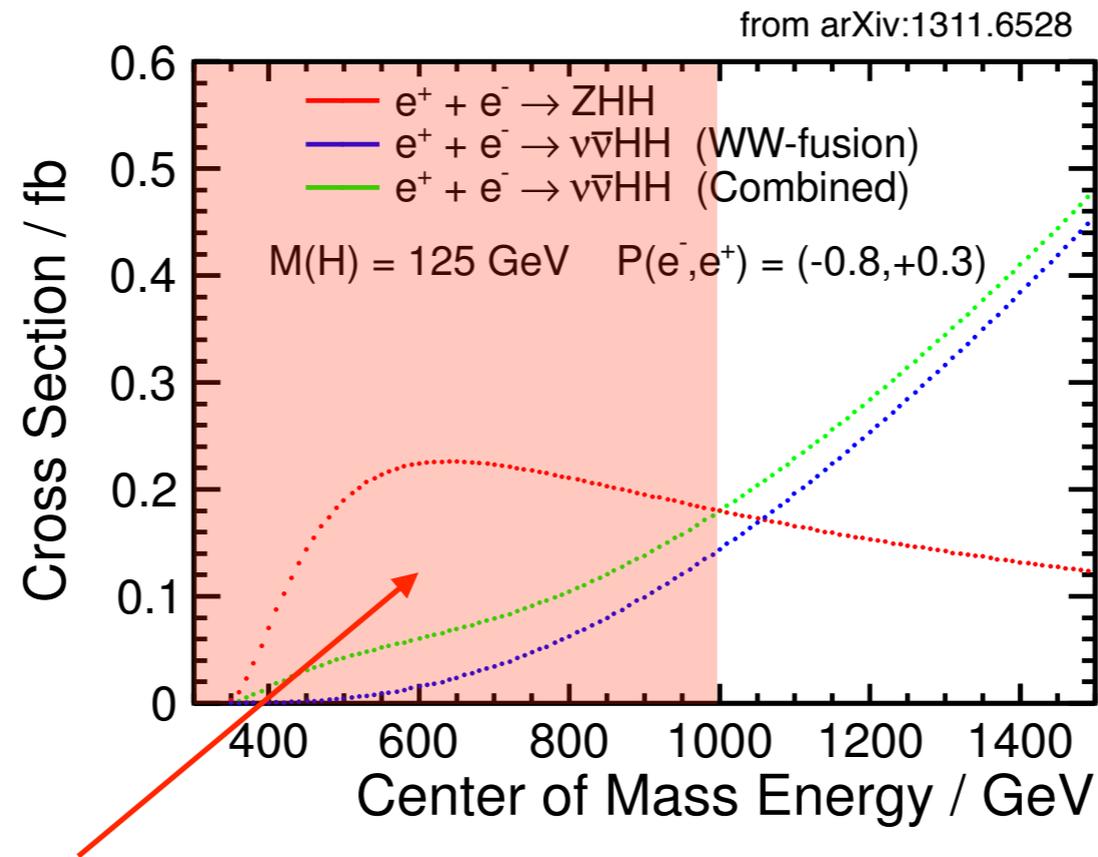
# **Non-resonant processes**

*Double Higgs at  $e^+e^-$  Colliders*

# Main production channels

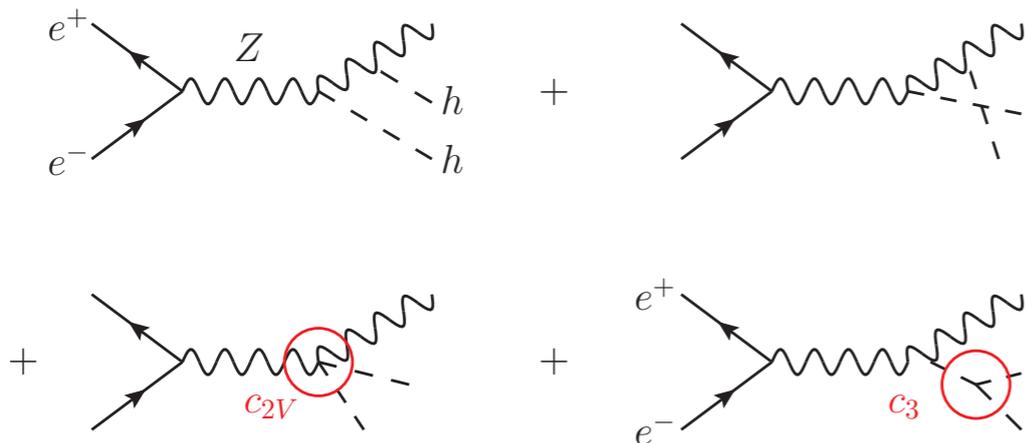


# Main production channels

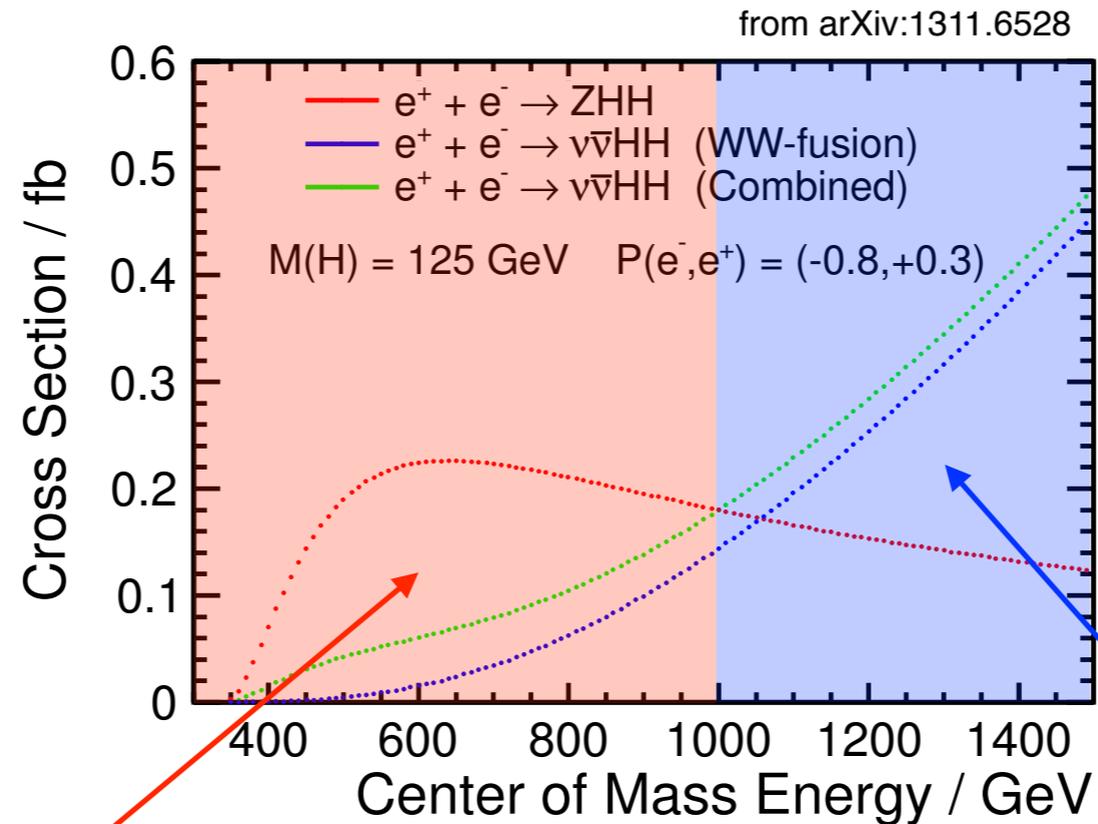


## Double Higgs-strahlung (DHS)

dominant below 1 TeV

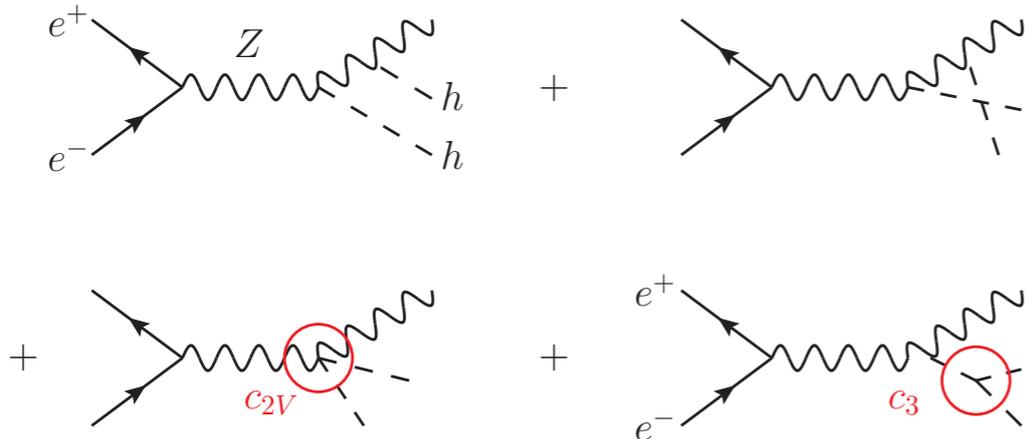


# Main production channels



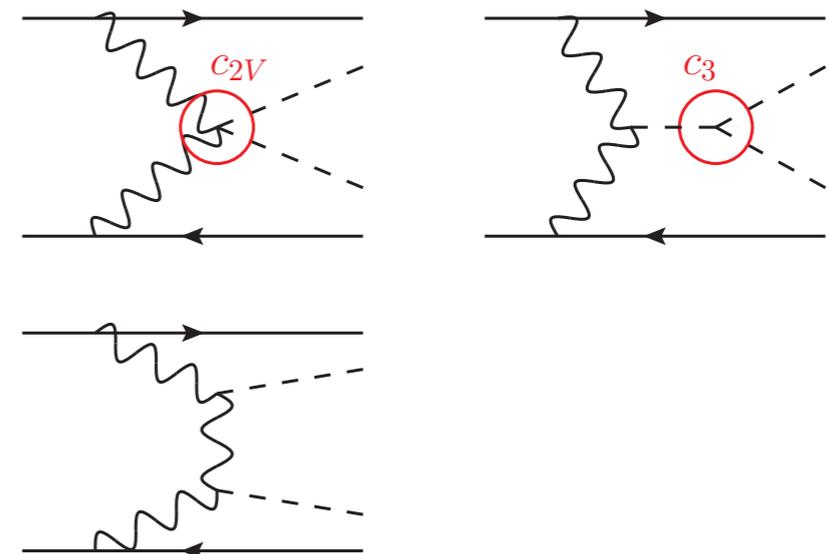
## Double Higgs-strahlung (DHS)

dominant below 1 TeV



## Vector Boson Fusion (VBF)

dominant above 1 TeV



# Expected precision on $c_3$ and $c_{2V}$

	COM energy	Precision	Process	Reference
<b>ILC</b>	500 GeV [ $L = 500 \text{ fb}^{-1}$ ]	$\Delta c_3 \sim 104\%$	DHS	ILC TDR, Volume 2, arXiv:1306.6352
	1 TeV [ $L = 1 \text{ ab}^{-1}$ ]	$\Delta c_3 \sim 28\%$	VBF	ILC TDR, Volume 2, arXiv:1306.6352
		$\Delta c_{2V} \sim 20\%$	DHS	Contino et al., JHEP 1402 (2014) 006
<b>CLIC</b>	1.4 TeV [ $L = 1.5 \text{ ab}^{-1}$ ]	$\Delta c_3 \sim 24\%$	VBF	Roloff (CLICdp Coll.), talk at LCWS14
		$\Delta c_{2V} \sim 7\%$		
	3 TeV [ $L = 2 \text{ ab}^{-1}$ ]	$\Delta c_3 \sim 12\%$		
		$\Delta c_{2V} \sim 3\%$		

FCC<sub>100</sub> allows for better precision

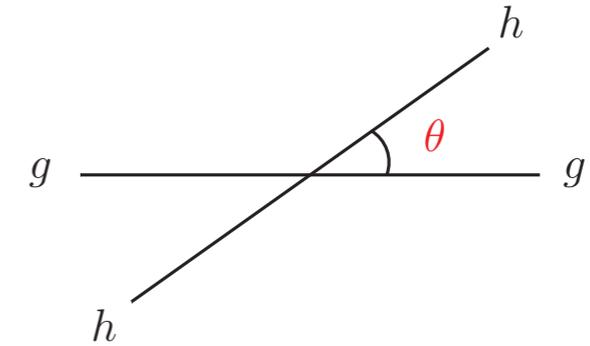
- ♦ higher energy reach (useful for  $\Delta c_{2V}$ )
- ♦ higher luminosity at threshold (useful for Higgs trilinear)

# **Gluon Fusion channel**

*Angular dependence*

# The angular distribution

The signal is also characterised by the angle between the Higgs pair and the beam axis in the c.o.m. frame

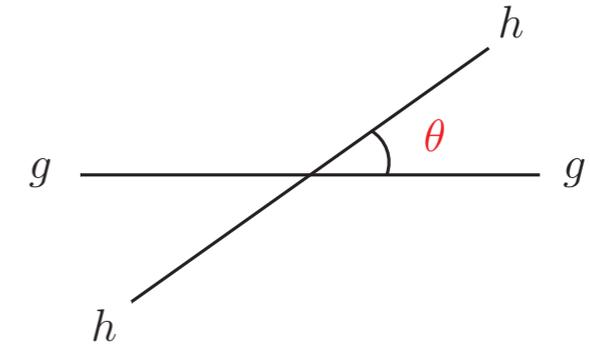


Scattering due to two partial waves  $J_z = 0$  and  $J_z = \pm 2$

$$\frac{d\sigma}{d\cos\theta} \sim \text{const.} \quad (J_z = 0) \qquad \frac{d\sigma}{d\cos\theta} \sim \sin^2\theta \quad (J_z = \pm 2)$$

# The angular distribution

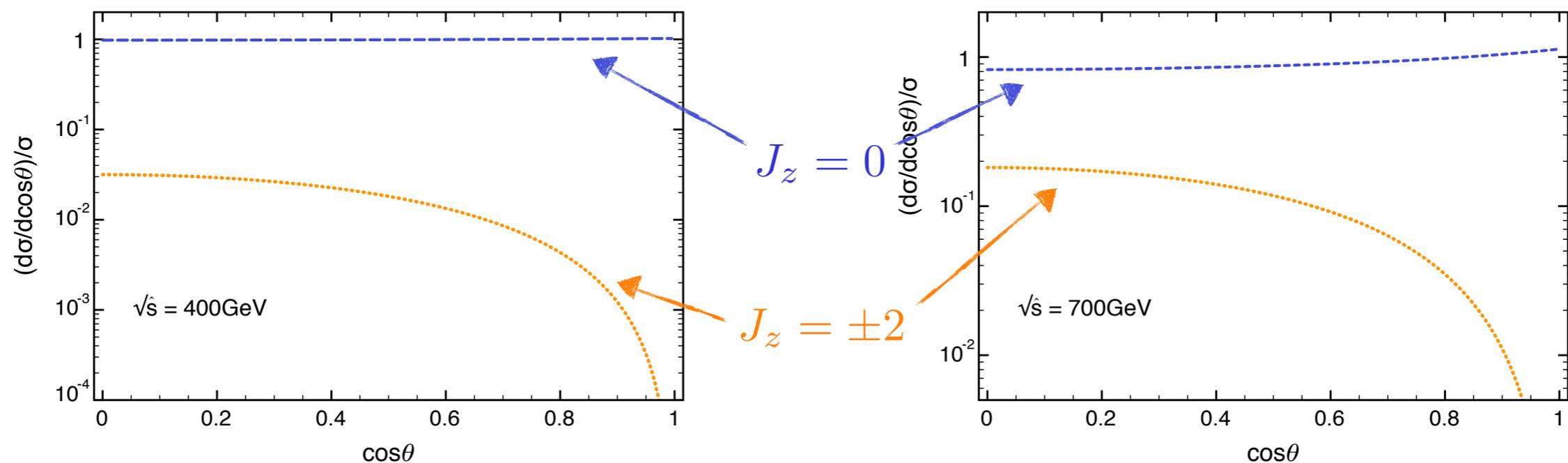
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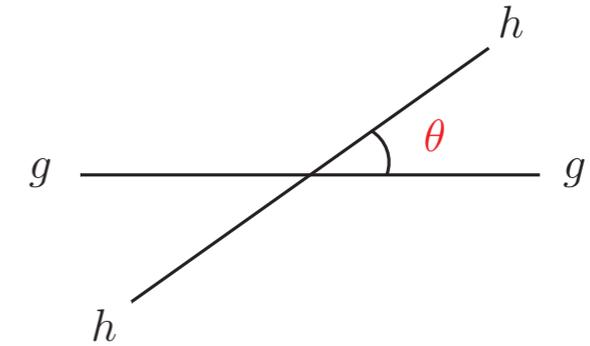
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- ♦ in the SM the  $J_z = \pm 2$  amplitude comes only from the box diagram and is quite suppressed



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- ♦ in the SM the  $J_z = \pm 2$  amplitude comes only from the box diagram and is quite suppressed
- ♦ the BSM diagrams coming from dim. 6 operators only generate contributions with  $J_z = 0$ 
  - ➔ angular analysis not useful to disentangle NP effects  
(possible exception dim. 8 operators, extremely hard at LHC)