

# MC Tools and NLO Monte Carlos

or

## The Good, the Bad & the Ugly

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- what the talk is about
- the cutting edge in theory inputs
- matching & merging with parton showers
- where we are and where we (should/could/would) go

# motivation & introduction

## motivation: the need for (more) accurate tools

- to date no survivors in searches for new physics & phenomena  
(a pity, but that's what Nature hands to us)
- push into precision tests of the Standard Model  
(find it or constrain it!)
- statistical uncertainties approach zero  
(because of the fantastic work of accelerator, DAQ, etc.)
- systematic experimental uncertainties decrease  
(because of ingenious experimental work)
- theoretical uncertainties are or become dominant  
(it would be good to change this to fully exploit LHC's potential)

⇒ more accurate tools for more precise physics needed!

## motivation: aim of the exercise

- review the state of the art in precision simulations
- highlight missing or ambiguous theoretical ingredients
- suggest some further studies – experiment and theory

(celebrate success)

(acknowledge failure)

(...)

reminder: fixed-order and its limits

# the aftermath of the NLO (QCD) revolution

- establishing a wide variety of automated tools for NLO calculations

BLACKHAT, GoSAM, MADGRAPH, NJET, OPENLOOPS, RECOLA + automated IR subtraction methods (MADGRAPH, SHERPA)

- first full NLO (EW) results with such tools

- technical improvements still mandatory

(higher multis, higher speed, higher efficiency, easier handling, . . .)

- start discussing scale setting prescriptions

(simple central scales for complicated multi-scale processes? test smarter prescriptions?)

- steep learning curve still ahead: “NLO phenomenology”

(example: methods for uncertainty estimates beyond variation around central scale)

# the looming revolution: going beyond NLO

- $H$  in ggF at N<sup>3</sup>LO (Anastasiou, Duhr and others)
- explosive growth in NNLO (QCD)  $2 \rightarrow 2$  results

(apologies for any unintended omissions)

- $t\bar{t}$  (1303.6254; 1508.03585; 1511.00549)
- single- $t$  (1404.7116)
- $VV$  (1507.06257; 1605.02716; 1604.08576; 1605.02716)
- $HH$  (1606.09519)
- $VH$  (1407.4747; 1601.00658)
- $V\gamma$  (1504.01330)
- $\gamma\gamma$  (1110.2375; 1603.02663)
- $Vj$  (1507.02850; 1512.01291; 1602.06965)
- $Hj$  (1408.5325; 1504.07922; 1505.03893; 1508.02684)
- $jj$  (1310.3993)
- $WBF$  at NNLO and N<sup>3</sup>LO (1506.02660 and N<sup>3</sup>LO 1606.00840)
- different IR subtraction schemes:  
N-jettiness slicing, antenna subtraction, sector decomposition,



# challenging the revolution

- some technical issues at NNLO (and beyond)

(stability of automated NLO, robustness under integration, subtraction vs. slicing)

- more scales (internal or external) complicated – need integrals
- going to higher power of  $N$  often driven by need to include larger FS multiplicity – maybe not the most efficient method
- structural questions concerning convergence/importance
- limitations of perturbative expansion:
  - breakdown of factorisation at HO (Seymour et al.)
  - higher-twist: compare  $(\alpha_S/\pi)^n$  with  $\Lambda_{\text{QCD}}/M_Z$

(see Melnikov's talk last week)

matching @ (N)NLO

merging @ (N)LO

## prequel: parton showers vs. resummation calculations

- various schemes for various logs in analytic resummation
- concentrate on parton shower instead  $\longleftrightarrow$  compare with  $Q_T$  resummation

(transverse momentum of Higgs boson etc.)

- parametric accuracy by comparing Sudakov form factors:

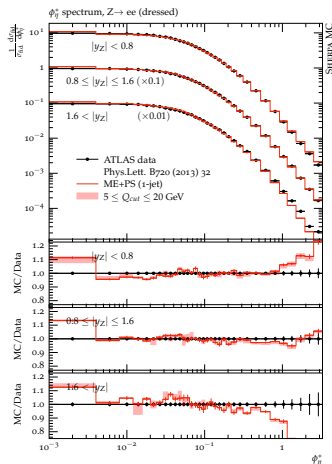
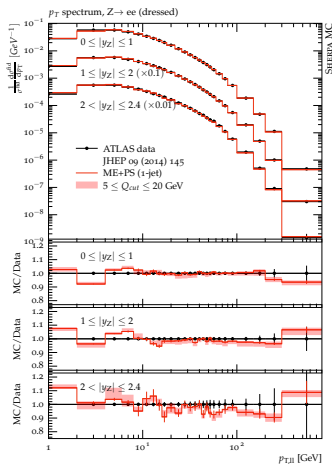
$$\Delta = \exp \left\{ - \int \frac{dk_{\perp}^2}{k_{\perp}^2} \left[ A \log \frac{k_{\perp}^2}{Q^2} + B \right] \right\},$$

where  $A$  and  $B$  can be expanded in  $\alpha_S(k_{\perp}^2)$

- showers usually include terms  $A_{1,2}$  and  $B_1$  (NLL)
- $A_2$  often realised by pre-factor multiplying scale  $\mu_R \simeq k_{\perp}$

# some parton shower fun with DY

(example of accuracy in description of standard precision observable)



# matching at NLO and NNLO

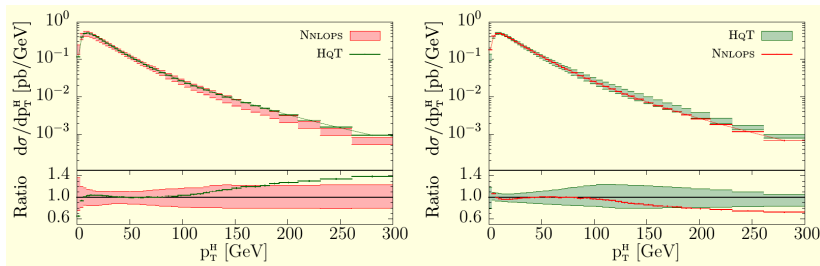
- avoid double-counting of emissions
- two schemes at NLO: MC@NLO and POWHEG
  - mismatches of  $K$  factors in transition to hard jet region
  - MC@NLO:  $\rightarrow$  visible structures, especially in  $gg \rightarrow H$
  - POWHEG:  $\rightarrow$ : high tails, cured by  $h$  dampening factor
  - well-established and well-known methods

(no need to discuss them any further)

- two schemes at NNLO: MINLO & UN<sup>2</sup>LOPS (singlets  $S$  only)
  - different basic ideas
  - MINLO:  $S + j$  at NLO with  $p_T^{(S)} \rightarrow 0$  and capture divergences by reweighting internal line with analytic Sudakov, NNLO accuracy ensured by reweighting with full NNLO calculation for  $S$  production
  - UN<sup>2</sup>LOPS identifies and subtracts and adds parton shower terms at FO from  $S + j$  contributions, maintaining unitarity
  - available for two simple processes only: DY and  $gg \rightarrow H$

# NNLOs for $H$ production: MINLO

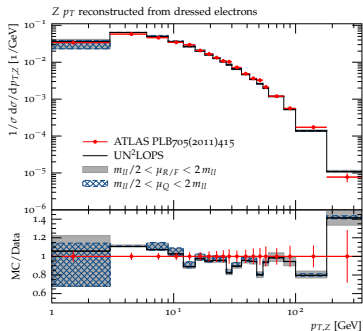
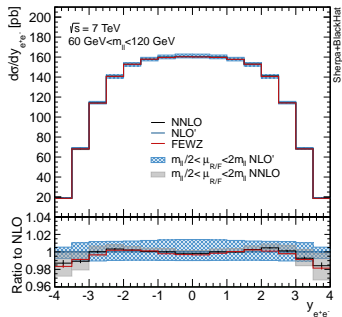
K. Hamilton, P. Nason, E. Re & G. Zanderighi, JHEP 1310



- also available for  $Z$  production

# NNLOs for $Z$ production: UN<sup>2</sup>LOs

S. Hoche, Y. Li, & S. Prestel, Phys.Rev.D90 & D91



- also available for  $H$  production

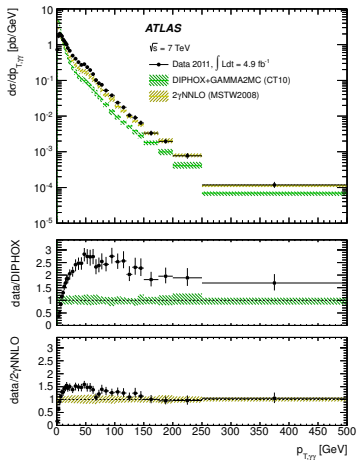
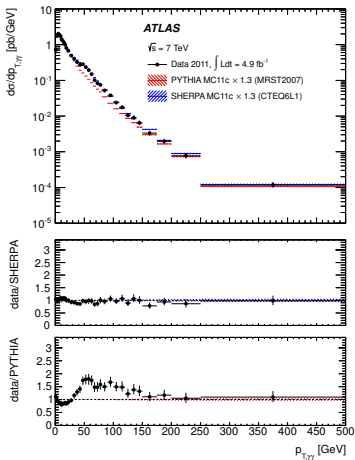
## NNLOs: shortcomings/limitations

- MINLO relies on knowledge of  $B_2$  terms from analytic resummation  
→ to date only known for colour singlet production
- MINLO relies on reweighting with full NNLO result  
→ one parameter for  $H$  ( $y_H$ ), more complicated for  $Z$ , ...
- UN<sup>2</sup>LOs relies on integrating single- and double emission to low scales and combination of unresolved with virtual emissions  
→ potential efficiency issues, need NNLO subtraction
- UN<sup>2</sup>LOs puts unresolved & virtuals in “zero-emission” bin  
→ no parton showering for virtuals (?)



# merging example: $p_{\perp, \gamma\gamma}$ in MEPS@LO vs. NNLO

(arXiv:1211.1913 [hep-ex])



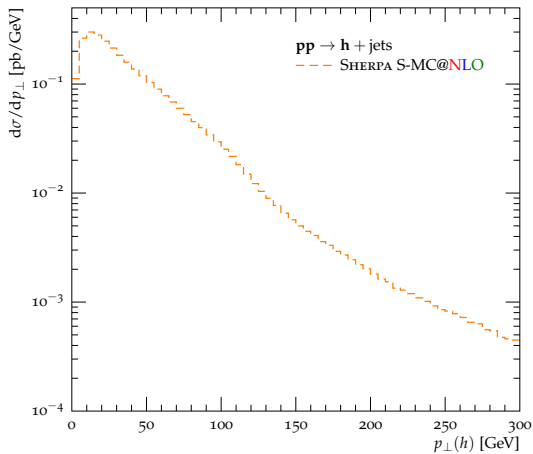
# multijet-merging at NLO

- sometimes “more legs” wins over more loops
- basic idea like at LO: towers of MEs with increasing jet multi (but this time at NLO)
- combine them into one sample, remove overlap/double-counting
- maintain NLO and LL accuracy of ME and PS
- this effectively translates into a merging of MC@NLO simulations and can be further supplemented with LO simulations for even higher final state multiplicities
- different implementations, parametric accuracy not always clear
- starts being used, still lacks careful cross-validation

(MEPs@NLO, FxFx, UNLOPs)

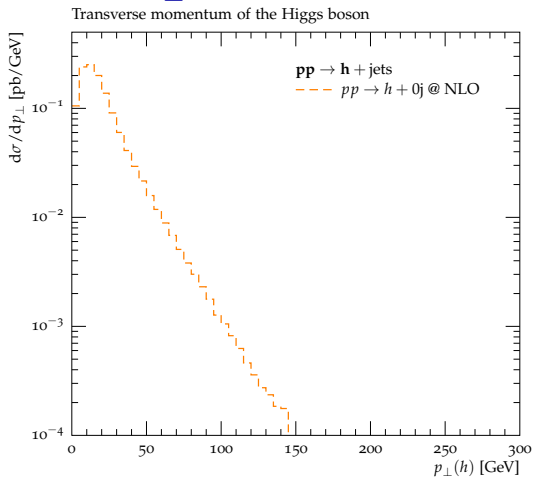
# illustration: $p_{\perp}^H$ in MEPS@NLO

Transverse momentum of the Higgs boson



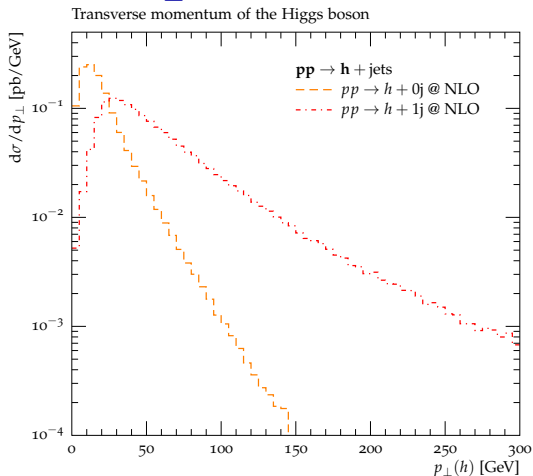
- first emission by MC@NLO

# illustration: $p_{\perp}^H$ in MEPS@NLO



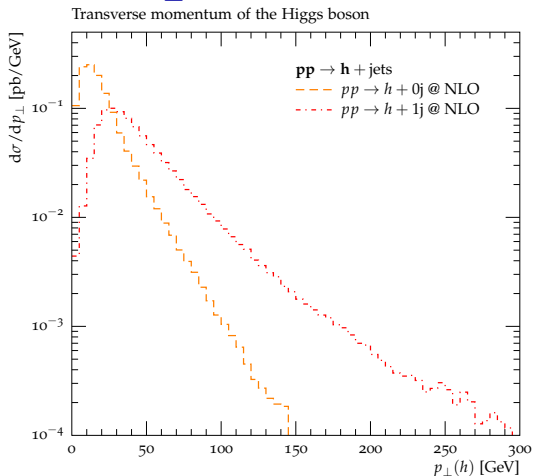
- first emission by MC@NLO, restrict to  $Q_{n+1} < Q_{\text{cut}}$

# illustration: $p_{\perp}^H$ in MEPS@NLO



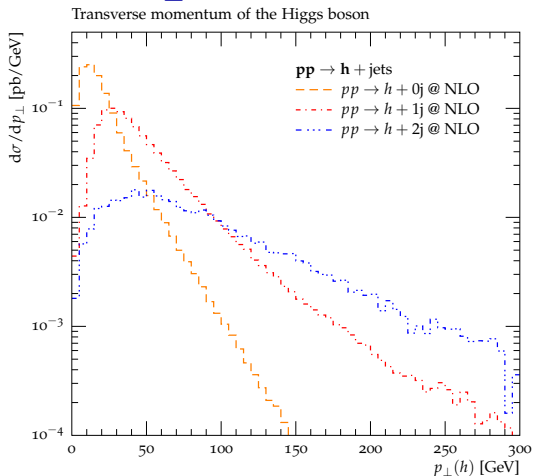
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- MC@NLO  $pp \rightarrow h + \text{jet}$  for  $Q_{n+1} > Q_{\text{cut}}$

# illustration: $p_{\perp}^H$ in MEPS@NLO



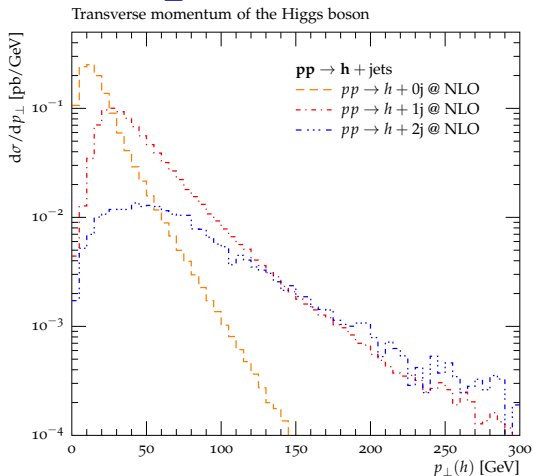
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- MC@NLO  $pp \rightarrow h + 2\text{jets}$  for  $Q_{n+2} > Q_{\text{cut}}$

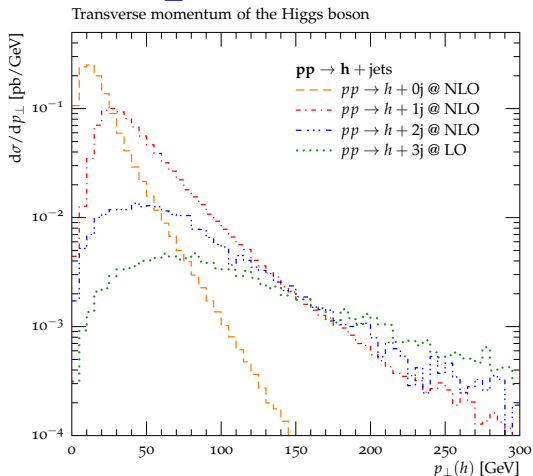
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- iterate

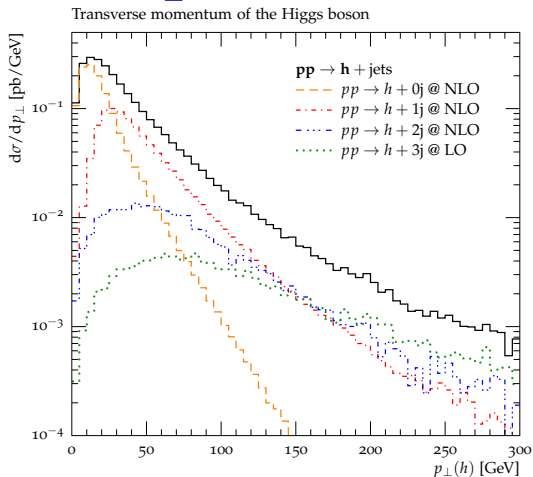


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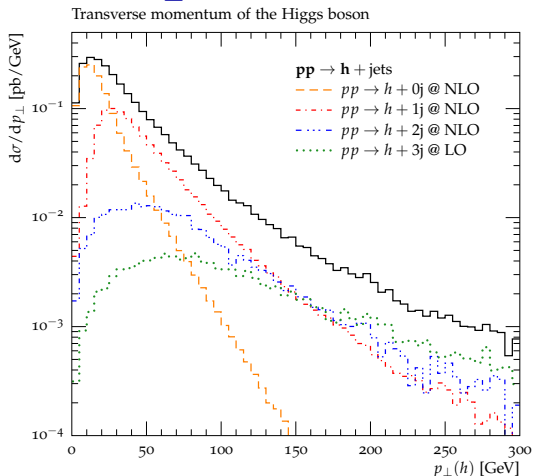
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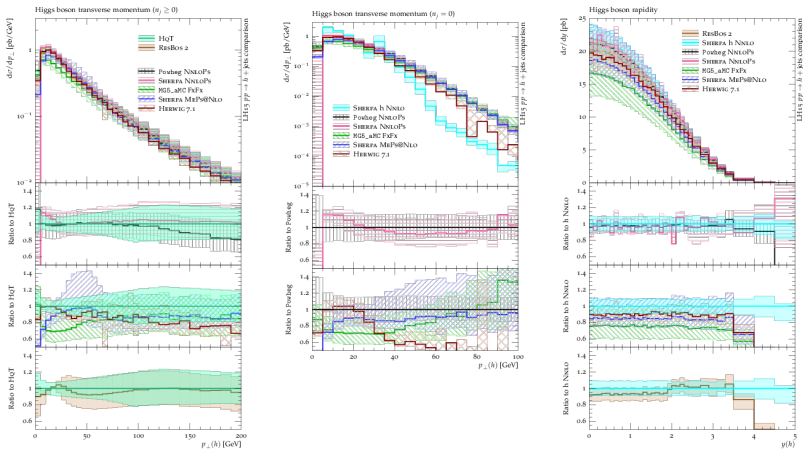
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- iterate
- sum all contributions

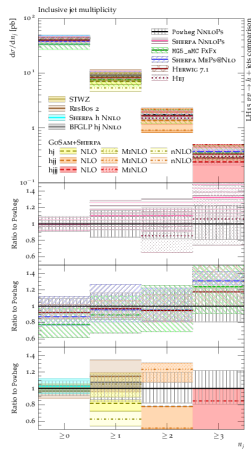
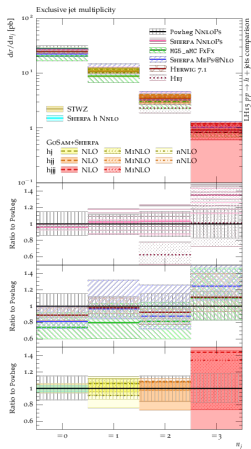
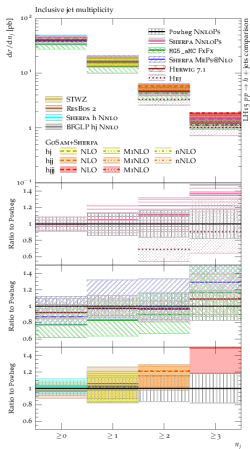
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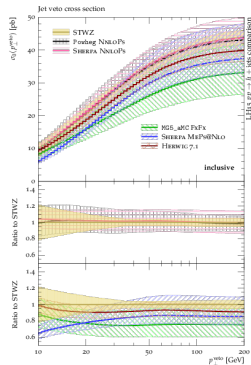
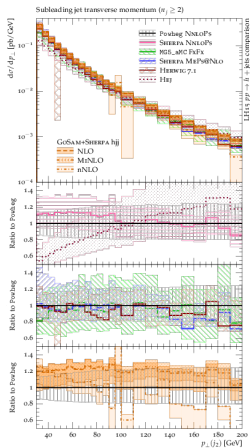
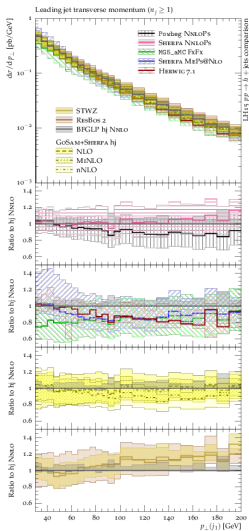


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- iterate
- sum all contributions
- eg.  $p_{\perp}(h) > 200$  GeV has contributions fr. multiple topologies

# results from various schemes in $H$ +jets through ggF

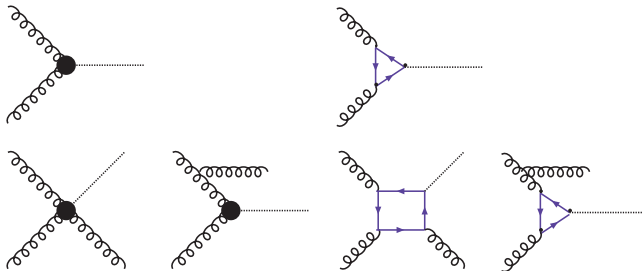






## aside: quark mass effects

- include effects of quark masses



- reweight NLO HEFT with LO ratio:

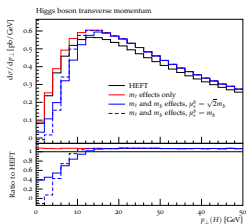
(reweight virtual with Born ratio, real with real ratio)

$$d\sigma_{\text{mass}}^{(\text{NLO})} \approx d\sigma_{\text{HEFT}}^{(\text{NLO})} \times \frac{d\sigma_{\text{mass}}^{(\text{LO})}}{d\sigma_{\text{HEFT}}^{(\text{LO})}}$$

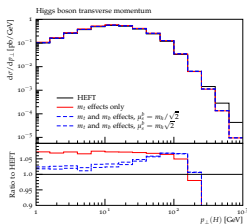
# $b$ -mass effects: playtime

- use LO multijet merging for  $tb$ -interference

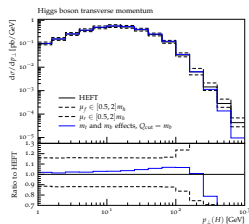
vary around  $\mu_Q = m_b$



vary around  $\mu_Q = m_h$   
with  $Q_{\text{cut}} = m_b$  fixed



vary  $\mu_{F,R}$





# limitations of full simulations

- lots of routinely used tools for large FS multis (4 and more) at NLO accuracy, but

→ not many detailed comparisons

(critical appraisals and learning curve in their phenomenological use still in infancy)

→ no standard way of estimating uncertainties (yet?)

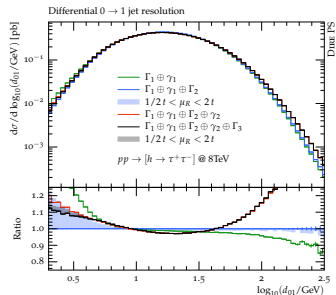
- to improve: description of loop-induced processes
- potentially important for new physics searches

- users of codes: higher orders tricky → training needed

(MC = black box attitude problematic - a new brand of pheno/experimenters needed?)

# a systematic uncertainty

- showering a source of uncertainty  
 → (N)LL only, scale variations?  
 (quite often just used as black box)
- maybe include higher orders?
- example right:  
 $\mu_R$  uncertainty in  $p_{\perp}^{(\text{emit})}$  in ggF



# limitations

## theory limitations/questions

- we have constructed lots of tools for precision physics at LHC
  - **but** we did not cross-validate them careful enough (yet)
  - **but** we did not compare their theoretical foundations (yet)
- will NNLO (or beyond) become as automated as NLO?
  - **or more precisely: when and how?**
- we also need unglamorous improvements on existing tools:
  - systematically check advanced scale-setting schemes (MINLO)
  - automatic (re-)weighting for PDFs & scales
  - scale compensation in PS is simple (implement and check)
- 4 vs. 5 flavour scheme → **really?**
- how about  $\alpha_S$ : range from 0.113 to 0.118

(yes, I know, but still - it still bugs me)

→ **is there any way to settle this once and for all (measurements?)**

## more theory uncertainties/issues?

- with NNLOs approaching 5% accuracy or better:
  - non-perturbative uncertainties start to matter:
    - PDFs, MPIs, hadronization, etc.
  - question (example): with hadronization tuned to quark jets (LEP)
    - how important is the “chemistry” of jets for JES?
    - can we fix this with measurements?
  - example PDFs: to date based on FO vs. data
    - will we have to move to resummed/parton showered?

(reminder: LO\* was not a big hit, though)
- $g \rightarrow q\bar{q}$  at accuracy limit of current parton showers:
  - how bad are  $\sim 25\%$  uncertainty on  $g \rightarrow b\bar{b}$ ?
  - can we fix this with measurements?

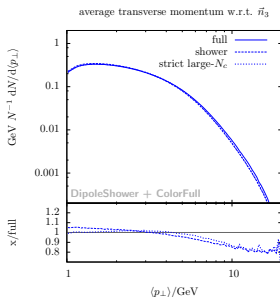
plan

# achievable goals in fixed order calculations: a roadmap (?)

- practical limitations/questions to be overcome:
  - dealing with IR divergences at NNLO: slicing vs. subtracting  
(I'm not sure we have THE solution yet)
  - how far can we push NNLO? are NLO automated results stable enough for NNLO at higher multiplicity?
  - matching for generic processes at NNLO?  
(MINLO or UN<sup>2</sup>LOs or something new?)
- NLO for loop-induced processes:
  - fixed-order starting, MC@NLO tedious but straightforward
- EW NLO corrections with tricky/time-consuming calculational setup
  - but important at large scales: effect often  $\sim$  QCD, but opposite sign
  - need maybe faster approximation for high-scales (EW Sudakovs)

# “curable” bottleneck: colours/spins in parton showers

- parton shower usually is spin-averaged, leading colour, (next-to) leading log
- start including next-to leading colour
  - (first attempts by Platzer & Sjodahl; Nagy & Soper)
- no big effects in  $e^-e^+ \rightarrow$  hadrons seen maybe more exclusive observables?
- aside: can also include spin-correlations important for EW emissions
  - (maybe relevant for ultra-high energies)
- HO being implemented at nth moment





## outlook

- will need precision for ballistics of smoking guns

