

# Lepton Flavour Violation in the Littlest Higgs Model with T-Parity

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# Outline

*Based on:*

M. Blanke, A.J. Buras, BD, A. Poschenrieder, C. Tarantino

[JHEP 0705:013,2007]

- 1 **Sketching the Littlest Higgs Model with T-Parity**
- 2 **Lepton Flavour Violating Decays**
- 3 **Conclusions**

# Motivation: The Little Hierarchy Problem

## Naturalness

- Light Higgs  $\Rightarrow \Lambda \sim 1 \text{ TeV}$
- Higher-dimensional operators  $\Rightarrow \Lambda \geq 5 - 10 \text{ TeV}$

## How to solve this Tension?

## A Possible Solution

- Protection of the Higgs mass by an additional symmetry
- Introduction of new particles at the TeV scale
- A popular example: SUSY

# Central Ideas of Little Higgs Models

## Higgs as a Goldstone Boson

- The Higgs arises as a **Goldstone Boson** of a spontaneously broken, approximate global symmetry
- massless at tree level
- Higgs potential generated radiatively

Georgi, Pais '74; Georgi, Dimopoulos, Kaplan '84

+

## Collective Symmetry Breaking

- Global symmetry is only explicitly broken by **two or more** non-vanishing couplings
- Contributions to the Higgs mass involve at least two different couplings
- at one-loop level: logarithmical dependence on the cutoff

Arkani-Hamed, Cohen, Georgi, hep-ph/0105239, hep-th/0104005; Arkani-Hamed, Cohen, Gregoire, Wacker, hep-ph/0202089

# The Littlest Higgs Model (without T-Parity)

Spontaneous symmetry breaking of  $SU(5) \rightarrow SO(5)$

- Symmetry breaking takes places at **scale  $f$**
- $SU(5) \supset [SU(2) \otimes U(1)]^2 \supset [SU(2) \otimes U(1)]_{SM}$

## Particle Content

- **SM fields** (SM-fermions, SM-bosons)
- a **new (T-even) top partner** ( $T_+$ )
- **new heavy partners of EW gauge bosons** ( $W_H^\pm, Z_H, A_H$ )
- **10 scalars**
  - ▶ a light complex doublet  $\Rightarrow$  Higgs boson  $h$  with  $\langle h \rangle = v$
  - ▶ a heavy complex triplet  $\Rightarrow \Phi^P, \Phi^0, \Phi^\pm, \Phi^{\pm\pm}$  with  $\langle \Phi^0 \rangle \sim v^2/f$

# The Littlest Higgs Model with T-Parity

Electroweak precision observables imply  $f \sim 2-3\text{TeV}$

Cheng, Low, hep-ph/0308199, hep-ph/0405243

$\Rightarrow$

T-Parity

- $Z_2$  symmetry exchanging the  $[SU(2) \times U(1)]$  gauge factors
- SM particles and  $T_+$  are T-even
- all other new particles are T-odd

## Implications

- $f$  can be as low as  $\sim 500\text{GeV}$
- heavy photon  $A_H$  is a **dark matter candidate**
- need to introduce **mirror fermions**

(Note: T-Parity generally anomalous, Hill, Hill, 0705.0697)

# Ingredients for LFV in the LHT Model

Hubisz, Lee, Paz, hep-ph/0512169; Choudhury et al., hep-ph/0612327;  
Blanke, Buras, BD, Poschenrieder, Tarantino, hep-ph/0702136

## T-odd Sector

- **Mirror leptons**  $\begin{pmatrix} \nu_H^1 \\ \ell_H^1 \end{pmatrix}, \begin{pmatrix} \nu_H^2 \\ \ell_H^2 \end{pmatrix}, \begin{pmatrix} \nu_H^3 \\ \ell_H^3 \end{pmatrix}$
- to first order in  $v/f$ :  $m_{Hi}^\nu = m_{Hi}^\ell \sim \mathcal{O}(\text{TeV})$
- Heavy gauge bosons  $W_H^\pm, Z_H^0, A_H^0$
- contributions from T-even sector and  $\Phi$ 's negligible

Flavor mixing in the mirror sector  $\Rightarrow$  **New mixing matrices**  $V_{H\ell}$  and  $V_{H\nu}$

Mixing matrices are related by  $V_{H\nu}^\dagger V_{H\ell} = V_{PMNS}^\dagger$

$$\ell^j \longrightarrow \nu_H^i \quad \xrightarrow{W_H^\mu} \quad \frac{iq}{\sqrt{2}} (V_{H\ell})_{ij} \gamma^\mu P_L$$

# Why Study Lepton Flavor Violation?

Most famous LFV decay:  $\mu \rightarrow e\gamma$

SM + r.h. Dirac neutrinos  $\Rightarrow Br(\mu \rightarrow e\gamma)_{SM} \leq 10^{-54}$

Experimental upper bound (MEGA):

$$Br(\mu \rightarrow e\gamma)_{exp} < 1.2 \cdot 10^{-11}$$

(2007/2008:  $\mathcal{O}(10^{-13} - 10^{-14})$ ) (MEG)



# Why Study Lepton Flavor Violation?

Most famous LFV decay:  $\mu \rightarrow e \gamma$

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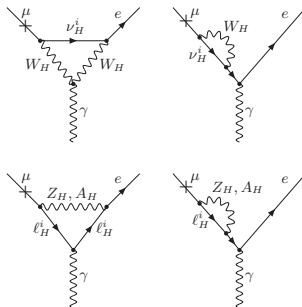
Experimental upper bound (MEGA):

$$Br(\mu \rightarrow e \gamma)_{exp} < 1.2 \cdot 10^{-11}$$

(2007/2008:  $\mathcal{O}(10^{-13} - 10^{-14})$ ) (MEG)

There is plenty of room for new physics!

For example:



# Experimental Status and Prospects

- $\mu^- \rightarrow e^- e^+ e^-$

$$Br(\mu^- \rightarrow e^- e^+ e^-)_{exp} < 1.0 \cdot 10^{-12}$$

- $\mu - e$  - conversion in nuclei (e.g. Ti)

$$R(\mu Ti \rightarrow e Ti)_{exp} < 4.3 \cdot 10^{-12}$$

- LFV  $\tau$  decays (BABAR & BELLE)

$$Br(\tau \rightarrow l\gamma, \tau \rightarrow l\{\pi, \eta, \eta'\}, \tau \rightarrow l_i l_j l_k)_{exp} < \mathcal{O}(10^{-8})$$

- $(g - 2)_\mu$

$$a_\mu^{exp} = 11659208.0(63) \cdot 10^{-10}$$

# Lepton Flavour Violating Decays in the LHT

## Calculated Processes

$$\mu \rightarrow e\gamma$$

$$\tau \rightarrow \mu\gamma$$

$$\tau \rightarrow e\gamma$$

$$\mu^- \rightarrow e^- e^+ e^-$$

$$\tau^- \rightarrow \mu^- \mu^+ \mu^-$$

$$\tau \rightarrow e^- e^+ e^-$$

$\mu$ -e-conversion  
in nuclei

$$K_L \rightarrow \mu e$$

$$B_{d,s} \rightarrow \mu e$$

$$B_{d,s} \rightarrow \tau e$$

$$B_{d,s} \rightarrow \tau \mu$$

$$\tau^- \rightarrow e^- \mu^+ e^-$$

$$\tau \rightarrow \mu^- e^+ \mu^-$$

$$\tau^- \rightarrow \mu^- e^+ e^-$$

$$\tau \rightarrow e^- \mu^+ \mu^-$$

$$(g-2)_\mu$$

$$K_L \rightarrow \pi^0 \mu e$$

$$\tau \rightarrow \ell P$$

$$(P = \pi, \eta, \eta')$$

- varied parameters:

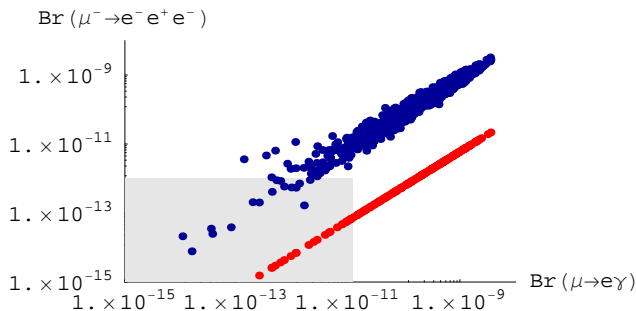
- ▶  $300 \text{ GeV} \leq m_{Hi} \leq 1.5 \text{ TeV}$
- ▶  $0 \leq \theta_{ij}^\ell \leq \pi$
- ▶  $0 \leq \delta_{ij}^\ell \leq 2\pi$
- ▶  $f = 1000 \text{ GeV}$  and  $f = 500 \text{ GeV}$

- several branching ratios can reach present experimental bounds

- $(g-2)_\mu$  negligible

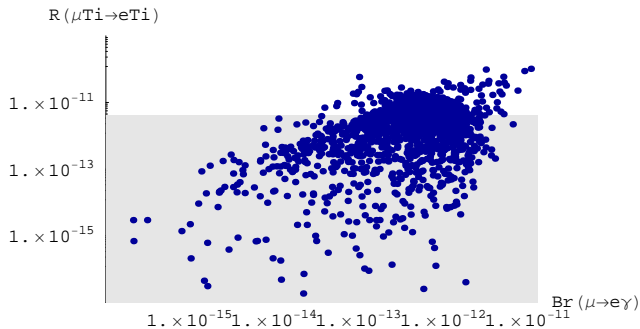
⇒ LHT can not explain tension between SM and experiment

$$\mu \rightarrow e\gamma \text{ vs. } \mu^- \rightarrow e^- e^+ e^-$$



- most points violate experimental bounds  
 $\Rightarrow$  **hierarchical  $V_{H\ell}$**  or **quasi-degenerate mirror leptons** required
- strong correlation between  $\text{Br}(\mu \rightarrow e\gamma)$  and  $\text{Br}(\mu^- \rightarrow e^- e^+ e^-)$
- **dipole contribution negligible - in contrast to the MSSM!**

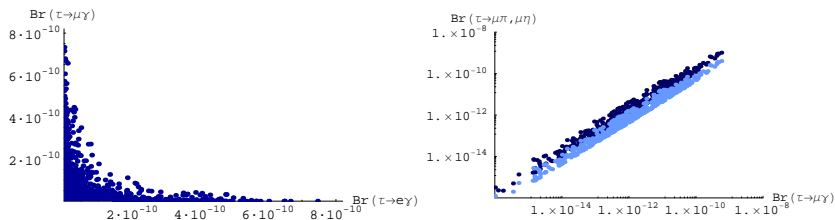
# $\mu$ -e-Conversion in Nuclei



- poses a strong experimental constraint
- many points close to experimental bound

⇒ **Chance of observation** at upcoming experiments (e.g. J-PARC)

# LFV $\tau$ Decays



( $f = 1000 \text{ GeV}$ )

- all  $\Delta L = 1$  decays considered can reach the experimental bounds (in particular for low values of  $f$ )
- even simultaneously, considerable values are possible
- again, there are interesting correlations
- powerful tool for LHT searches at SuperB-factories

# Correlations Allow a Distinction from the MSSM

**MSSM:** Dipole dominates in the absence of significant Higgs contributions

Ellis, Hisano, Raidal, Shimizu, hep-ph/0206110

Brignole, Rossi, hep-ph/0404211

Arganda, Herrero, hep-ph/0510405

Paradisi, hep-ph/0508054, 0601100

$$\frac{Br(\mu^- \rightarrow e^- e^+ e^-)}{Br(\mu \rightarrow e \gamma)} \simeq \frac{\alpha}{3\pi} \left( \log \frac{m_\mu^2}{m_e^2} - 2.7 \right)$$
$$\frac{Br(\tau^- \rightarrow \ell^- e^+ e^-)}{Br(\tau \rightarrow \ell \gamma)} \simeq \frac{\alpha}{3\pi} \left( \log \frac{m_\tau^2}{m_e^2} - 2.7 \right)$$
$$\frac{Br(\tau^- \rightarrow \ell^- \mu^+ \mu^-)}{Br(\tau \rightarrow \ell \gamma)} \simeq \frac{\alpha}{3\pi} \left( \log \frac{m_\tau^2}{m_\mu^2} - 2.7 \right)$$

**LHT:** Dipole negligible compared to boxes and  $Z^0$ -penguins

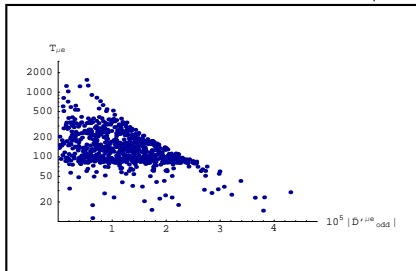
Blanke, Buras, BD, Poschenrieder, Tarantino, JHEP 0705:013,2007

⇒

very different pattern allows for a transparent distinction!

# Correlations in the LHT

- Dipole negligible  $\Rightarrow T_{ij} = \left| \frac{\bar{Y}_{j, \text{odd}}^{ij}}{\bar{D}'_{\text{odd}}{}^{ij}} \right|^2$  is strongly enhanced



boxes  
penguins  $\Rightarrow Y, Z$

electric dipole  $\Rightarrow D$

- ratios of Z and Y loop functions ( $a_{ij}, b_{ij}^k$ ) are  $\sim \mathcal{O}(1)$   
 $c_{ij} = c_{ij}(a_{ij}) \sim \mathcal{O}(0.1)$
- finally, ratios between branching ratios are e.g. given by

$$\frac{Br(\mu^- \rightarrow e^- e^+ e^-)}{Br(\mu^- \rightarrow e \gamma)} \simeq \frac{2\alpha}{3\pi} \frac{1}{\sin^4 \theta_W} T_{\mu e} C_{\mu e}$$

or

$$\frac{Br(\tau^- \rightarrow e^- e^+ e^-)}{Br(\tau^- \rightarrow e^- \mu^+ \mu^-)} \simeq 8 \frac{C_{\tau e}}{b_{\tau e}^\mu}$$

- ratios turn out to be mostly **parameter independent!**



# Ratios between Branching Ratios

ratio	LHT	MSSM (dipole)	MSSM (Higgs)
$\frac{Br(\mu^- \rightarrow e^- e^+ e^-)}{Br(\mu \rightarrow e \gamma)}$	0.4... 2.5	$\sim 6 \cdot 10^{-3}$	$\sim 6 \cdot 10^{-3}$
$\frac{Br(\tau^- \rightarrow e^- e^+ e^-)}{Br(\tau \rightarrow e \gamma)}$	0.4... 2.3	$\sim 1 \cdot 10^{-2}$	$\sim 1 \cdot 10^{-2}$
$\frac{Br(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{Br(\tau \rightarrow \mu \gamma)}$	0.4... 2.3	$\sim 2 \cdot 10^{-3}$	0.06... 0.1
$\frac{Br(\tau^- \rightarrow e^- \mu^+ \mu^-)}{Br(\tau \rightarrow e \gamma)}$	0.3... 1.6	$\sim 2 \cdot 10^{-3}$	0.02... 0.04
$\frac{Br(\tau^- \rightarrow \mu^- e^+ e^-)}{Br(\tau \rightarrow \mu \gamma)}$	0.3... 1.6	$\sim 1 \cdot 10^{-2}$	$\sim 1 \cdot 10^{-2}$
$\frac{Br(\tau^- \rightarrow e^- e^+ e^-)}{Br(\tau^- \rightarrow e^- \mu^+ \mu^-)}$	1.3... 1.7	$\sim 5$	0.3... 0.5
$\frac{Br(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{Br(\tau^- \rightarrow \mu^- e^+ e^-)}$	1.2... 1.6	$\sim 0.2$	5... 10
$\frac{R(\mu Ti \rightarrow e Ti)}{Br(\mu \rightarrow e \gamma)}$	$10^{-2} \dots 10^2$	$\sim 5 \cdot 10^{-3}$	0.08... 0.15

# Double-Ratios of Branching Ratios

Dipole operator logarithmically enhanced  $\Rightarrow$  breaks  $\mu \leftrightarrow e$  symmetry

- In the MSSM:  $\mu \leftrightarrow e$  symmetry strongly broken
- In the LHT:  $\mu \leftrightarrow e$  symmetry approximately conserved

$\Rightarrow$  Consider quantities of type

$$R_1 = \frac{Br(\tau^- \rightarrow e^- e^+ e^-)}{Br(\tau^- \rightarrow \mu^- \mu^+ \mu^-)} \frac{Br(\tau^- \rightarrow \mu^- e^+ e^-)}{Br(\tau^- \rightarrow e^- \mu^+ \mu^-)}$$

$$R_2 = \frac{Br(\tau^- \rightarrow e^- e^+ e^-)}{Br(\tau^- \rightarrow \mu^- \mu^+ \mu^-)} \frac{Br(\tau \rightarrow \mu \gamma)}{Br(\tau \rightarrow e \gamma)}$$

$$R_3 = \frac{Br(\tau^- \rightarrow e^- \mu^+ \mu^-)}{Br(\tau^- \rightarrow \mu^- e^+ e^-)} \frac{Br(\tau \rightarrow \mu \gamma)}{Br(\tau \rightarrow e \gamma)}$$

- In the MSSM:  $R_1 \simeq 20$ ,  $R_2 \simeq 5$ ,  $R_3 \simeq 0.2$ .
- In the LHT:  $0.8 \lesssim R_1 \lesssim 1.3$ ,  $0.8 \lesssim R_2 \lesssim 1.2$ ,  $0.8 \lesssim R_3 \lesssim 1.2$ .

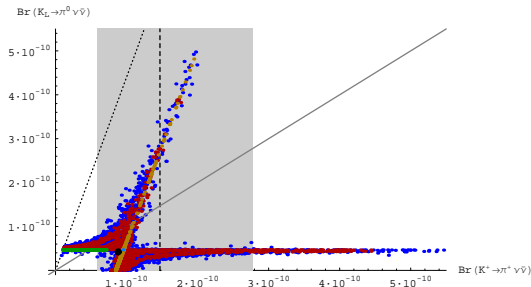
# Main Messages

- Contributions from mirror leptons dominate the SM background by more than 40 orders of magnitude
- LFV decays in the LHT can easily reach or even exceed present experimental bounds  
⇒ Chance of observation in upcoming experiments
- Signals of the LHT could show up in LFV decays even before the LHC starts!
- $(g - 2)_\mu$  negligible  $\Rightarrow$  a problem?
- Correlations between branching ratios allow for a clear distinction from the MSSM and other models

# A Reminder: (Quark-) Flavor Violation in the LHT

Blanke, Buras, Poschenrieder, Tarantino, Uhlig, Weiler, hep-ph/0605214

Blanke, Buras, Poschenrieder, Recksiegel, Tarantino, Uhlig, Weiler, hep-ph/0610298



## Upshot

- Large effects (up to factor 10 enhancements) in the K-system
- Smaller effects in the B-system (except for CP violating observables)

# Backup: Upper Bounds

decay	$f = 1000 \text{ GeV}$	$f = 500 \text{ GeV}$	exp. upper bound
$\mu \rightarrow e\gamma$	$1.2 \cdot 10^{-11} (1 \cdot 10^{-11})$	$1.2 \cdot 10^{-11} (1 \cdot 10^{-11})$	$1.2 \cdot 10^{-11}$
$\mu^- \rightarrow e^- e^+ e^-$	$1.0 \cdot 10^{-12} (1 \cdot 10^{-12})$	$1.0 \cdot 10^{-12} (1 \cdot 10^{-12})$	$1.0 \cdot 10^{-12}$
$\mu\text{Ti} \rightarrow e\text{Ti}$	$2 \cdot 10^{-10} (5 \cdot 10^{-12})$	$4 \cdot 10^{-11} (5 \cdot 10^{-12})$	$4.3 \cdot 10^{-12}$
$\tau \rightarrow e\gamma$	$8 \cdot 10^{-10} (7 \cdot 10^{-10})$	$1 \cdot 10^{-8} (1 \cdot 10^{-8})$	$9.4 \cdot 10^{-8}$
$\tau \rightarrow \mu\gamma$	$8 \cdot 10^{-10} (8 \cdot 10^{-10})$	$2 \cdot 10^{-8} (1 \cdot 10^{-8})$	$1.6 \cdot 10^{-8}$
$\tau^- \rightarrow e^- e^+ e^-$	$7 \cdot 10^{-10} (6 \cdot 10^{-10})$	$2 \cdot 10^{-8} (2 \cdot 10^{-8})$	$2.0 \cdot 10^{-7}$
$\tau^- \rightarrow \mu^- \mu^+ \mu^-$	$7 \cdot 10^{-10} (6 \cdot 10^{-10})$	$3 \cdot 10^{-8} (3 \cdot 10^{-8})$	$1.9 \cdot 10^{-7}$
$\tau^- \rightarrow e^- \mu^+ \mu^-$	$5 \cdot 10^{-10} (5 \cdot 10^{-10})$	$2 \cdot 10^{-8} (2 \cdot 10^{-8})$	$2.0 \cdot 10^{-7}$
$\tau^- \rightarrow \mu^- e^+ e^-$	$5 \cdot 10^{-10} (5 \cdot 10^{-10})$	$2 \cdot 10^{-8} (2 \cdot 10^{-8})$	$1.9 \cdot 10^{-7}$
$\tau^- \rightarrow \mu^- e^+ \mu^-$	$5 \cdot 10^{-14} (3 \cdot 10^{-14})$	$2 \cdot 10^{-14} (2 \cdot 10^{-14})$	$1.3 \cdot 10^{-7}$
$\tau^- \rightarrow e^- \mu^+ e^-$	$5 \cdot 10^{-14} (3 \cdot 10^{-14})$	$2 \cdot 10^{-14} (2 \cdot 10^{-14})$	$1.1 \cdot 10^{-7}$
$\tau \rightarrow \mu\pi$	$2 \cdot 10^{-9} (2 \cdot 10^{-9})$	$5.8 \cdot 10^{-8} (5.8 \cdot 10^{-8})$	$5.8 \cdot 10^{-8}$
$\tau \rightarrow e\pi$	$2 \cdot 10^{-9} (2 \cdot 10^{-9})$	$4.4 \cdot 10^{-8} (4.4 \cdot 10^{-8})$	$4.4 \cdot 10^{-8}$
$\tau \rightarrow \mu\eta$	$6 \cdot 10^{-10} (6 \cdot 10^{-10})$	$2 \cdot 10^{-8} (2 \cdot 10^{-8})$	$5.1 \cdot 10^{-8}$
$\tau \rightarrow e\eta$	$6 \cdot 10^{-10} (6 \cdot 10^{-10})$	$2 \cdot 10^{-8} (2 \cdot 10^{-8})$	$4.5 \cdot 10^{-8}$
$\tau \rightarrow \mu\eta'$	$7 \cdot 10^{-10} (7 \cdot 10^{-10})$	$3 \cdot 10^{-8} (3 \cdot 10^{-8})$	$5.3 \cdot 10^{-8}$
$\tau \rightarrow e\eta'$	$7 \cdot 10^{-10} (7 \cdot 10^{-10})$	$3 \cdot 10^{-8} (3 \cdot 10^{-8})$	$9.0 \cdot 10^{-8}$
$K_L \rightarrow \mu e$	$4 \cdot 10^{-13} (2 \cdot 10^{-13})$	$3 \cdot 10^{-14} (3 \cdot 10^{-14})$	$4.7 \cdot 10^{-12}$
$K_L \rightarrow \pi^0 \mu e$	$4 \cdot 10^{-15} (2 \cdot 10^{-15})$	$5 \cdot 10^{-16} (5 \cdot 10^{-16})$	$6.2 \cdot 10^{-9}$
$B_d \rightarrow \mu e$	$5 \cdot 10^{-16} (2 \cdot 10^{-16})$	$9 \cdot 10^{-17} (9 \cdot 10^{-17})$	$1.7 \cdot 10^{-7}$
$B_s \rightarrow \mu e$	$5 \cdot 10^{-15} (2 \cdot 10^{-15})$	$9 \cdot 10^{-16} (9 \cdot 10^{-16})$	$6.1 \cdot 10^{-6}$
$B_d \rightarrow \tau e$	$3 \cdot 10^{-11} (2 \cdot 10^{-11})$	$2 \cdot 10^{-10} (2 \cdot 10^{-10})$	$1.1 \cdot 10^{-4}$
$B_s \rightarrow \tau e$	$2 \cdot 10^{-10} (2 \cdot 10^{-10})$	$2 \cdot 10^{-9} (2 \cdot 10^{-9})$	—
$B_d \rightarrow \tau \mu$	$3 \cdot 10^{-11} (3 \cdot 10^{-11})$	$3 \cdot 10^{-10} (3 \cdot 10^{-10})$	$3.8 \cdot 10^{-5}$
$B_s \rightarrow \tau \mu$	$2 \cdot 10^{-10} (2 \cdot 10^{-10})$	$3 \cdot 10^{-9} (3 \cdot 10^{-9})$	—

# Backup: Full Particle Content

## T-even

- SM fermions, SM bosons, SM Higgs
- T-even top partner  $T_+$

## T-odd

vector-like mirror fermions:

$$\begin{pmatrix} u_H^1 \\ d_H^1 \end{pmatrix}, \begin{pmatrix} u_H^2 \\ d_H^2 \end{pmatrix}, \begin{pmatrix} u_H^3 \\ d_H^3 \end{pmatrix}$$
$$\begin{pmatrix} \nu_H^1 \\ \ell_H^1 \end{pmatrix}, \begin{pmatrix} \nu_H^2 \\ \ell_H^2 \end{pmatrix}, \begin{pmatrix} \nu_H^3 \\ \ell_H^3 \end{pmatrix}$$

- to order  $\mathcal{O}(v/f)$ : mass degenerate doublets
- masses of order  $\mathcal{O}(TeV)$

T-odd top partner  $T_-$

heavy gauge bosons:

$$W_H^\pm, Z_H^0, A_H$$

T-odd scalars:

$$\phi^\pm, \phi^{\pm\pm}, \phi^0, \phi_P^0$$

# Backup: Additional Parameters in the LHT

## Explicit Parameters of the LHT

Symmetry breaking scale  $f$   
mixing parameter  $x_L$

### mirror quarks

3 mirror quark masses  $m_{Hi}^q$

3 mixing angles  $\theta_{ij}^d$

3 mixing phases  $\delta_{ij}^d$

### mirror leptons

3 mirror quark masses  $m_{Hi}^\ell$

3 mixing angles  $\theta_{ij}^\ell$

3 mixing phases  $\delta_{ij}^\ell$

⇒ total of 20 new parameters

## Parameters from the Unknown UV-Completion

Some amplitudes are formally divergent ⇒  $\delta_{div}$

Formally, coefficients of higher dimensional operators have to be included

# Backup: Determination of Parameters

Discovery of heavy gauge bosons  
 $A_H, W_H^\pm, Z_H$

$\Rightarrow$

$f$

Discovery of heavy top partners  $T_\pm$

$\Rightarrow$

$x_L$

Discovery of mirror leptons

$\Rightarrow$

$m_{H1}^q, m_{H2}^q, m_{H3}^q$   
 $m_{H1}^\ell, m_{H2}^\ell, m_{H3}^\ell$

FCNC processes  
CP asymmetries

$\Rightarrow$

$\theta_{12}^d, \theta_{13}^d, \theta_{23}^d$   
 $\delta_{12}^d, \delta_{13}^d, \delta_{23}^d$

LFV processes

$\Rightarrow$

$\theta_{12}^\ell, \theta_{13}^\ell, \theta_{23}^\ell$   
 $\delta_{12}^\ell, \delta_{13}^\ell, \delta_{23}^\ell$