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The MSSM Higgs sector  
&  $\Delta M_{B_{d,s}}$  for large  $\tan\beta$



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# Motivation and generalities

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- Exact SUSY → The quark-Higgs couplings are those of a 2HDM-II :

$$\mathcal{L}_{Yuk} = - \underbrace{\bar{d}_R^I \mathbf{Y}_d^{IJ}}_{\uparrow} H_d \cdot \underbrace{Q_L^J}_{\uparrow} + \bar{u}_R^I \mathbf{Y}_u^{IJ} H_u \cdot Q_L^J + h.c.$$

- When the Higgses acquire their VEV's :

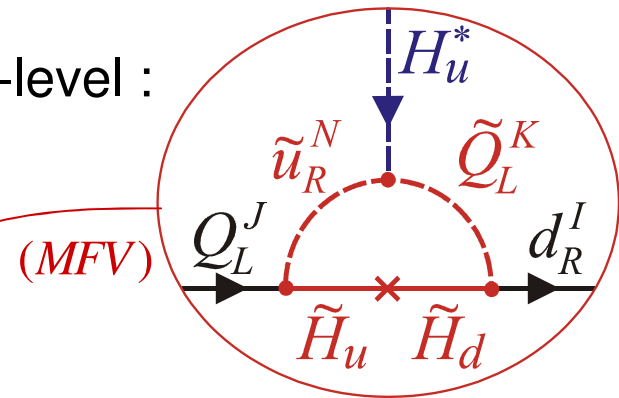
$$\left. \begin{array}{l} \text{Quark-Higgs vertices : } - \bar{d}_R^I \mathbf{Y}_d^{IJ} \underset{\downarrow v_d}{h_d^{0*}} d_L^J - \bar{u}_R^I \mathbf{Y}_u^{IJ} \underset{\downarrow v_u}{h_u^0} u_L^J + h.c. \\ \text{Quark mass terms :} \end{array} \right\} \text{aligned}$$

⇒ The quark – neutral Higgs vertices are flavour blind

# Motivation and generalities

- Soft SUSY-breaking  $\rightarrow$  2HDM-III structure at loop-level :

$$\mathcal{L}_{Yuk}^{eff} \supset - \bar{d}_R^I \left[ \mathbf{Y}_d H_d + \varepsilon_Y \mathbf{Y}_d \mathbf{Y}_u^\dagger \mathbf{Y}_u H_u^c \right]^{IJ} \cdot Q_L^J$$



- When the Higgses acquire their VEV's :

$$\left. \begin{array}{l} \text{Quark-Higgs vertices : } - \bar{d}_R^I \left[ \mathbf{Y}_d \underset{\downarrow v_d}{h_d^{0*}} + \varepsilon_Y \mathbf{Y}_d \mathbf{Y}_u^\dagger \mathbf{Y}_u \underset{\downarrow v_u}{h_u^{0*}} \right]^{IJ} d_L^J \\ \text{Quark mass terms :} \end{array} \right\} \text{disaligned!}$$

$\Rightarrow$  **Higgs-mediated FCNC** for large  $\tan\beta \equiv t_\beta = v_u/v_d$  :

[Babu, Kolda '99]

$$\mathcal{L}_{FCNC}^{Higgs} = \mathbf{K}^{IJ} \bar{d}_R^I d_L^J \left[ c_\beta h_u^{0*} - s_\beta h_d^{0*} \right] + \mathbf{K}^{JI*} \bar{d}_L^I d_R^J \left[ c_\beta h_u^0 - s_\beta h_d^0 \right]$$

(in quark mass eigenstate basis)

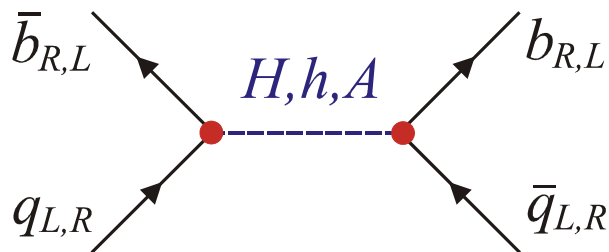
$$\mathbf{K}^{IJ} \sim \varepsilon_Y t_\beta^2 m_I / v$$

# Motivation and generalities

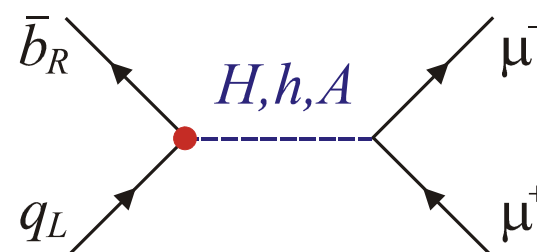
Rich phenomenology, especially in  $B$  physics!

Interesting signature within MFV :

$q = d, s$



← correlated →  
[Buras et al '02]



$\Delta M_{s(d)}$  decreased (unaffected)

$\mathcal{B}(B_q \rightarrow \mu^+ \mu^-)$  increased

- Clean (same dependence on  $F_{B_q}$  and  $V_{tq}$  in both observables)
- $\Delta M_q$  : a priori leading contribution from  $\bar{b}_R q_L \bar{b}_R q_L$  ( $\propto m_b^2$ ) .  
Vanishes if tree-level Higgs propagation [Babu, Kolda '99]
- Correlation obtained from  $\bar{b}_R q_L \bar{b}_L q_R$  ( $\propto m_b m_q$ )

**Look at all (sub-)leading contributions before concluding!**

# Outline

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*I.  $\Delta M_{d,s}$  anatomy*

*II. SUSY corrections to the Higgs potential*

*III.  $\Delta M_{d,s}$  versus  $B_{d,s} \rightarrow \mu^+ \mu^-$  and  $B^\pm \rightarrow \tau^\pm \nu$*

I.  $\Delta M_{d,s}$  anatomy

# Why the cancellation?

$$\Delta M_q^{(m_b^2)} \propto \begin{array}{c} \bar{b}_R \\ \nearrow \\ \text{---} H, h, A \text{---} \\ \searrow \\ q_L \\ m_b \end{array} \begin{array}{c} b_R \\ \nearrow \\ \text{---} H, h, A \text{---} \\ \searrow \\ \bar{q}_L \\ m_b \end{array} = 0 \quad [\text{Babu, Kolda '99}]$$

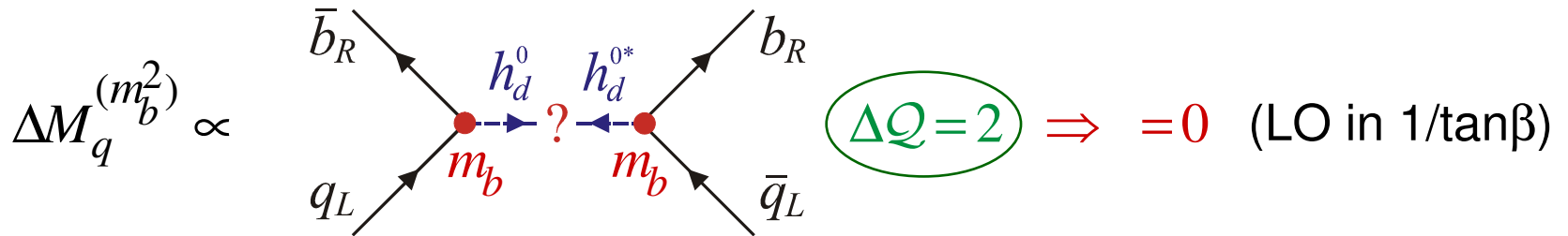
Sparticle masses  $\gg$  Higgs masses  $\Rightarrow$  effective 2HDM :

- $V^{(0)} = m_1^2 H_d^\dagger H_d + m_2^2 H_u^\dagger H_u + B\mu \{ H_u \cdot H_d + h.c. \}$   
 $+ \frac{\tilde{g}^2}{8} \left[ (H_d^\dagger H_d) - (H_u^\dagger H_u) \right]^2 + \frac{g^2}{2} (H_u^\dagger H_d) (H_d^\dagger H_u)$
- $\mathcal{L}_{\bar{b} \rightarrow \bar{q}}^{\text{Higgs}} = \kappa^{bq} \bar{b}_R q_L \left[ c_\beta h_u^{0*} - s_\beta h_d^{0*} \right] + \kappa^{qb*} \bar{b}_L q_R \left[ c_\beta h_u^0 - s_\beta h_d^0 \right]$

After SSB, for  $\tan\beta \rightarrow \infty$  (i.e.,  $v_d \rightarrow 0$ ), the theory is invariant under

$$U(1)_{PQ} : Q(H_d) = Q(d_R^I) = 1, \quad Q(\text{other}) = 0$$

# Why the cancellation?



Sparticle masses  $\gg$  Higgs masses  $\Rightarrow$  effective 2HDM :

- $V^{(0)} = m_1^2 H_d^\dagger H_d + m_2^2 H_u^\dagger H_u + B\mu \{ \cancel{H_u H_d} + h.c. \}$
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  - $\mathcal{L}_{\bar{b} \rightarrow \bar{q}}^{\text{Higgs}} = \kappa^{bq} \bar{b}_R q_L \left[ \cancel{c_\beta h_u^{0*}} - s_\beta h_d^{0*} \right] + \kappa^{qb^*} \bar{b}_L q_R \left[ \cancel{c_\beta h_u^0} - s_\beta h_d^0 \right]$
- $m_{12}^2 = s_\beta c_\beta M_A^2$ ,  
 $\tan\beta$ -suppressed  
 for fixed  $M_A$

After SSB, for  $\tan\beta \rightarrow \infty$  (i.e.,  $v_d \rightarrow 0$ ), the theory is invariant under

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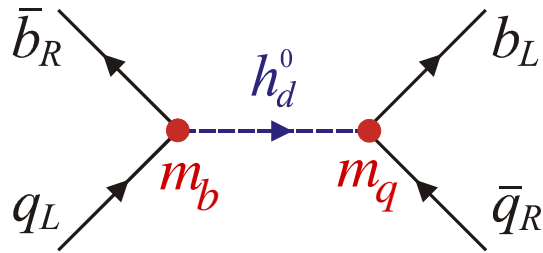
# What are the leading contributions?

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Look at all contributions with 1 suppression factor

# What are the leading contributions?

A/ Chirality flipped contribution ("LR")

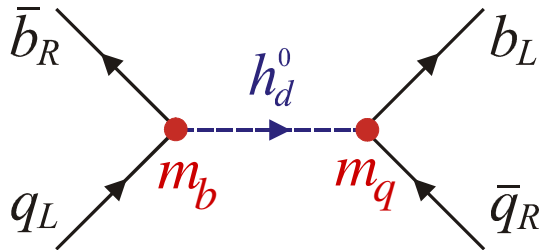


$$\Delta Q = 0 \quad \Rightarrow \quad \Delta M_q^{LR} \propto \frac{m_b \boxed{m_q}}{v^2} \quad \text{decreases } \Delta M_s$$

[Buras, Chankowski,  
Rosiek, Sławianowska '01]

# What are the leading contributions?

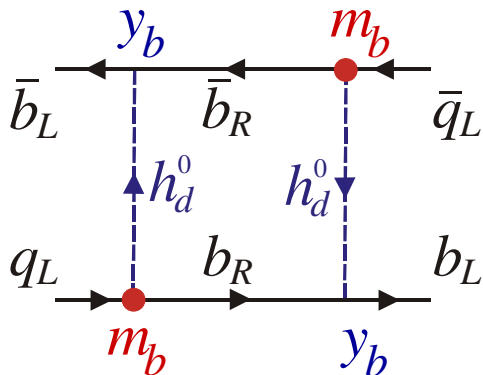
## A/ Chirality flipped contribution ("LR")



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[Buras, Chankowski, Rosiek, Sławianowska '01]

## B/ Weak scale loop contribution



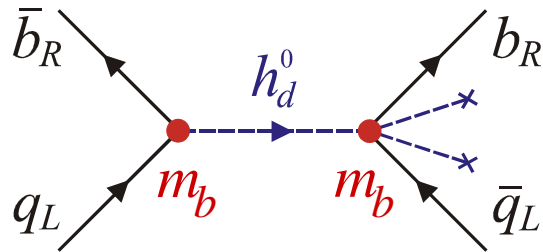
$$\Delta Q = 0 \quad \Rightarrow \quad \Delta M_q^{WS} \propto \frac{m_b^2}{v^2} \times \boxed{\frac{y_b^2}{16\pi^2}}$$

increases  $\Delta M_{d,s}$ , but numerically small

# What are the leading contributions?

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C/ Higher-dimension operator contribution

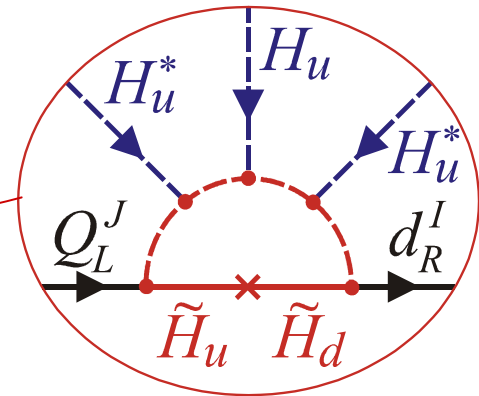


$\Delta Q = 2 \quad \Rightarrow \quad \Delta M_q^{\text{d6}} \propto \frac{m_b^2}{v^2} \times \boxed{\frac{v^2}{M_{\text{SUSY}}^2}}$

# What are the leading contributions?

Type of Higgs-FCNC resulting from HD operators?

$$\mathcal{L}_{Yuk}^{eff} \supset -\bar{d}_R^I \left[ \mathbf{Y}_d H_d + \varepsilon_Y \mathbf{Y}_d \mathbf{Y}_u^\dagger \mathbf{Y}_u H_u^c + \frac{1}{M_{SUSY}^2} \varepsilon_{6d} \mathbf{Y}_d \mathbf{Y}_u^\dagger \mathbf{Y}_u \mathbf{Y}_u^\dagger \mathbf{Y}_u (H_u^\dagger H_u) H_u^c \right]^{IJ} \cdot Q_L^J \quad (MFV)$$



Quark-Higgs int. :  $-\bar{d}_R^I \left[ \mathbf{Y}_d \underset{\downarrow v_d}{h_d^{0*}} + \varepsilon_{Y,6d} \mathbf{Y}_d \dots \mathbf{Y}_u \underset{\downarrow v_u}{h_u^{0*}} + \frac{v_u^2}{M_{SUSY}^2} \varepsilon_{6d} \mathbf{Y}_d \dots \mathbf{Y}_u \underset{\downarrow v_u}{h_u^0} \right]^{IJ} d_L^J$

Quark mass terms :

$$v_d \quad v_u \quad v_u$$

The only **tanβ-enhanced** effect in Higgs-FCNC comes from the modification of the rotation of the quark interaction eigenstates

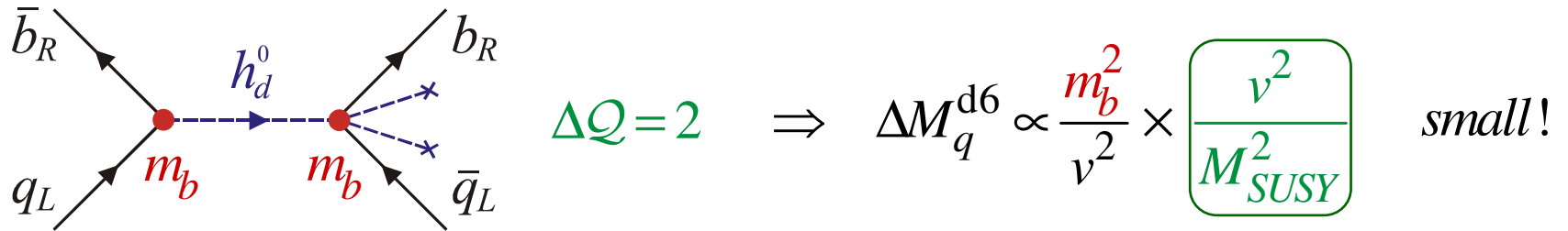
$$\Rightarrow \mathcal{L}_{\bar{b} \rightarrow \bar{q}}^{Higgs} = -(\kappa + \delta\kappa)^{bq} \underbrace{\bar{b}_R q_L h_d^{0*}}_{\text{PQ-conserving}} - (\kappa + \delta\kappa)^{qb*} \underbrace{\bar{b}_L q_R h_d^0}_{\text{loop not compensated by a large tan}\beta \text{ factor}} + O(1/t_\beta)$$

PQ-conserving

loop not compensated by a large tanβ factor

# What are the leading contributions?

## C/ Higher-dimension operator contribution



$\Delta Q = 2 \Rightarrow \Delta M_q^{\text{d6}} \propto \frac{m_b^2}{v^2} \times \frac{v^2}{M_{\text{SUSY}}^2} \quad \text{small!}$

# What are the leading contributions?

## C/ Higher-dimension operator contribution

$$\Delta Q = 2 \quad \Rightarrow \quad \Delta M_q^{\text{d6}} \propto \frac{m_b^2}{v^2} \times \frac{v^2}{M_{\text{SUSY}}^2} \quad \text{small!}$$

## D/ Corrections to Higgs masses/mixings ("RR")

$$\Delta Q = 2 \quad \Rightarrow \quad \Delta M_q^{\text{RR}} \propto \frac{m_b^2}{v^2} \times \text{SUSY loop in Higgs potential}$$

Corrections to the Higgs sector have already been extensively studied. However, contradictory statements about their effects on  $B - \bar{B}$  mixing are found in the literature. We thus go through them again in part II.

## II. SUSY corrections to the Higgs potential



# Matching MSSM $\rightarrow$ 2HDM

$V$  has the most general structure compatible with gauge symmetry :

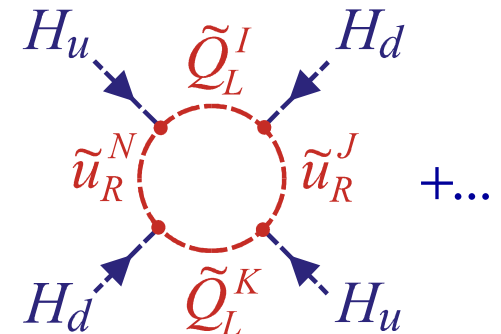
- $$V^{(1)} = m_{11}^2 H_d^\dagger H_d + m_{22}^2 H_u^\dagger H_u + \{ m_{12}^2 H_u \cdot H_d + h.c. \}$$

$$+ \frac{\lambda_1}{2} (H_d^\dagger H_d)^2 + \frac{\lambda_2}{2} (H_u^\dagger H_u)^2 + \lambda_3 (H_u^\dagger H_u) (H_d^\dagger H_d) + \lambda_4 (H_u^\dagger H_d) (H_d^\dagger H_u)$$

$$+ \left\{ \frac{\lambda_5}{2} (H_u \cdot H_d)^2 - \lambda_6 (H_d^\dagger H_d) (H_u \cdot H_d) - \lambda_7 (H_u^\dagger H_u) (H_u \cdot H_d) + h.c. \right\}$$

Ex:  $(MFV)$   $\lambda_5 = -\frac{3y_t^4}{8\pi^2} \frac{a_t^2 \mu^2}{M_{\tilde{t}_R}^4} L_1 \left( \frac{M_{\tilde{t}_L}^2}{M_{\tilde{t}_R}^2} \right) + \dots$

$$L_1(x) = \frac{-1}{(1-x)^2} - \frac{(1+x) \ln x}{2(1-x)^3}$$




Note: many refs! [*Haber, Hempfling '93*][*Carena, Espinosa, Quirós, Wagner '95*]...

We keep arbitrary flavour and CP structures, and propose a definition for  $\tan\beta$  in the effective 2HDM better suited to the large  $\tan\beta$  regime.

# WF renormalization and definition of $\tan\beta$

$$\mathcal{L}_{Kin} = Z_{uu}^r \partial_\mu H_u^\dagger \partial^\mu H_u + Z_{dd}^r \partial_\mu H_d^\dagger \partial^\mu H_d - \{ Z_{ud} \partial_\mu H_u \cdot \partial^\mu H_d + h.c. \}$$

$$\begin{pmatrix} H_u' \\ -H_d^c' \end{pmatrix} = \begin{pmatrix} 1 + (\delta Z_{uu}^r + i\delta H_{uu}^r)/2 & (\delta Z_{ud}^* + i\delta H_{ud}^*)/2 \\ (\delta Z_{ud} + i\delta H_{ud})/2 & 1 + (\delta Z_{dd}^r + i\delta H_{dd}^r)/2 \end{pmatrix} \begin{pmatrix} H_u \\ -H_d^c \end{pmatrix}$$



$m_1^2, m_2^2$  are renormalized such that the fields in the effective 2HDM (before redef.) stay at the minimum of the potential  $\Rightarrow v_{i,eff} = Z_{WF,ij} \cdot v_{j,tree}$

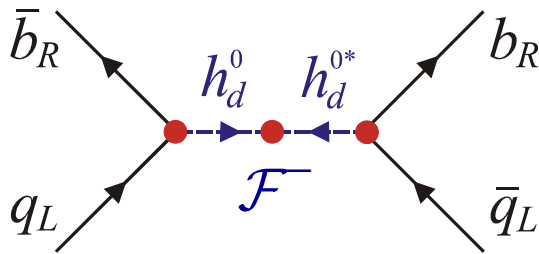
We exploit the **freedom to change the Higgs basis** to

- keep the vevs real and positive

- prevent  $\tan\beta$  from getting  $\tan\beta$ -enhanced corrections !

$$\begin{pmatrix} v_{u,eff} \\ v_{d,eff} \end{pmatrix} = \begin{pmatrix} 1 + \delta Z_{uu}^r/2 + i t_\beta^{-1} \delta Z_{ud}^i & \delta Z_{ud}^* \\ 0 & 1 + \delta Z_{dd}^r/2 \end{pmatrix} \begin{pmatrix} v_{u,tree} \\ v_{d,tree} \end{pmatrix}$$

# Corrections to Higgs masses and mixings



$$\mathcal{F} = \frac{s_{\alpha-\beta}^2}{M_H^2} + \frac{c_{\alpha-\beta}^2}{M_h^2} - \frac{1}{M_A^2} \simeq \left( -\lambda_5 + \lambda_7^2 / \lambda_2 \right) \frac{v^2}{M_A^4} \neq 0$$

+ Higgs **WF renormalization** in the effective FCNC vertices

## Earlier approaches

[Parry '06]: Corrections to  $\alpha, \beta, M_{h,H,A}$  using the FeynHiggs package

[Freitas, Gasser, Haisch '07]:  $\delta\mathcal{F} \propto \frac{M_h^2}{M_H^2 - M_h^2} \varepsilon_{GP}$  This pole singularity is not present in our result



There are many cancellations at play. These are built in in the effective Lagrangian approach. The non-vanishing of  $\mathcal{F}$  originates from the PQ-violating couplings  $\lambda_5$  and  $\lambda_7$  for large  $\tan\beta$ .

III.  $\Delta M_{d,s}$  versus  $B_{d,s} \rightarrow \mu^+ \mu^-$   
and  $B^\pm \rightarrow \tau^\pm \nu$ .

# Final formula

$$X = \frac{(\varepsilon_Y 16\pi^2)^2}{(1 + \tilde{\varepsilon}_3 \tan \beta)^2 (1 + \varepsilon_0 \tan \beta)^2} \frac{m_t^4}{M_W^2 M_A^2} \left[ \frac{\tan \beta}{50} \right]^4 \begin{cases} |V_{ts}| = 0.041; F_{B_s} = 0.24 \text{ GeV} \\ |V_{td}| = 0.0086; F_{B_d} = 0.20 \text{ GeV} \end{cases}$$

$$(\Delta M - \Delta M^{SM})_{\{s,d\}} = \begin{cases} -14 \text{ ps}^{-1} \\ \sim 0 \text{ ps}^{-1} \end{cases} X \begin{bmatrix} \frac{m_s}{0.06 \text{ GeV}} \end{bmatrix} \begin{bmatrix} \frac{m_b}{3 \text{ GeV}} \end{bmatrix} \begin{bmatrix} \frac{P_2^{LR}}{2.56} \end{bmatrix} \\ + \begin{cases} +4.4 \text{ ps}^{-1} \\ +0.13 \text{ ps}^{-1} \end{cases} X \frac{M_W^2 (-\lambda_5 + \lambda_7^2 / \lambda_2) (16\pi^2)}{M_A^2} \begin{bmatrix} \frac{m_b}{3 \text{ GeV}} \end{bmatrix}^2 \begin{bmatrix} \frac{P_1^{SLL}}{-1.06} \end{bmatrix}$$

Typically:  $M_{\tilde{q}} = \mu = a_{t,b} \Rightarrow \sim \frac{(y_t^4 + y_b^4)}{2} \frac{M_W^2}{M_A^2}$

(Moderate) effect for small  $M_A$ .

# Correlation to $B_q \rightarrow \mu^+ \mu^-$

$$\mathcal{B}(B_{\{s,d\}} \rightarrow \mu^+ \mu^-) = \left\{ \begin{array}{l} 3.9 \cdot 10^{-5} \\ 1.2 \cdot 10^{-6} \end{array} \right\} \times \frac{M_W^2}{M_A^2} \left[ \frac{\tan \beta}{50} \right]^2$$

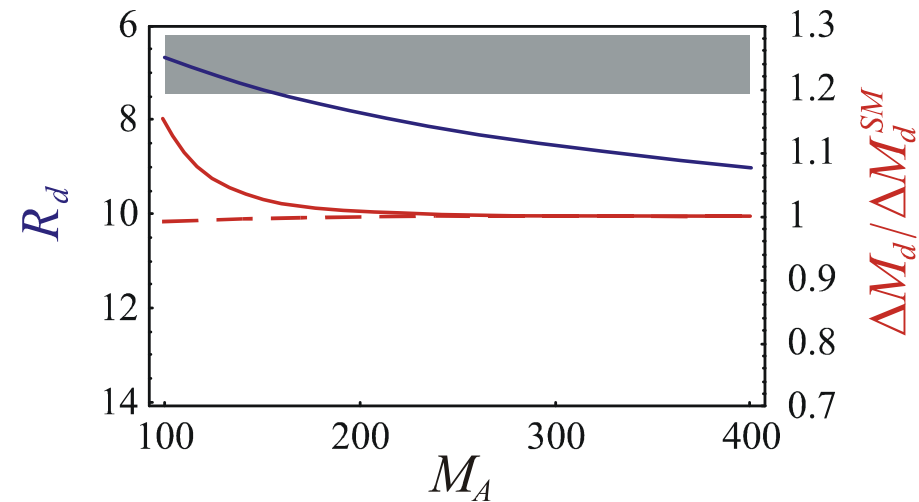
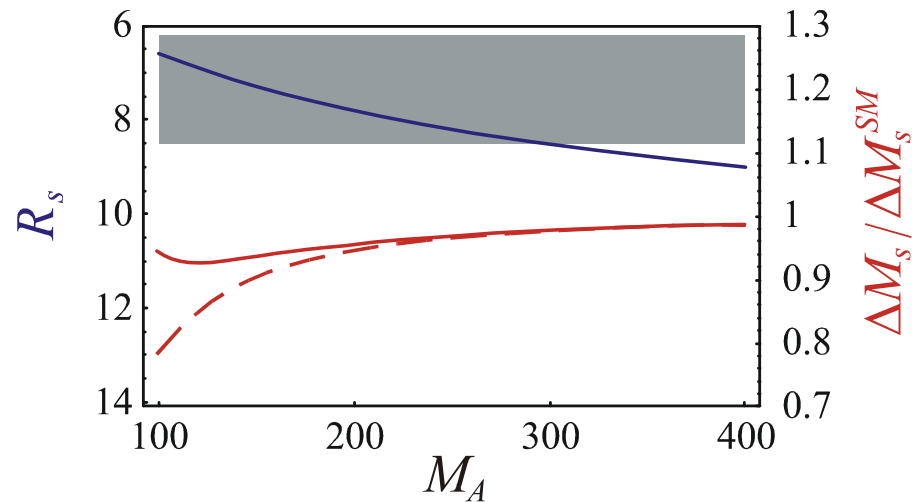
[Babu, Kolda '99]

[Chankowski, Sławianowska '01]

[Bobeth et al '01] [Huang et al '01]

[Buras et al '02][Isidori, Retico '01]

...



Plain:  $\Delta M_q = \Delta M_q^{SM+LR+RR}$

Dashed:  $\Delta M_q = \Delta M_q^{SM+LR}$

$$R_q \equiv \log_{10} \left[ \mathcal{B}(B_q \rightarrow \mu^+ \mu^-) / \Delta M_q (ps^{-1}) \right]$$

$\tan \beta = 40; M_{\tilde{q}} = M_2 = 1 TeV$

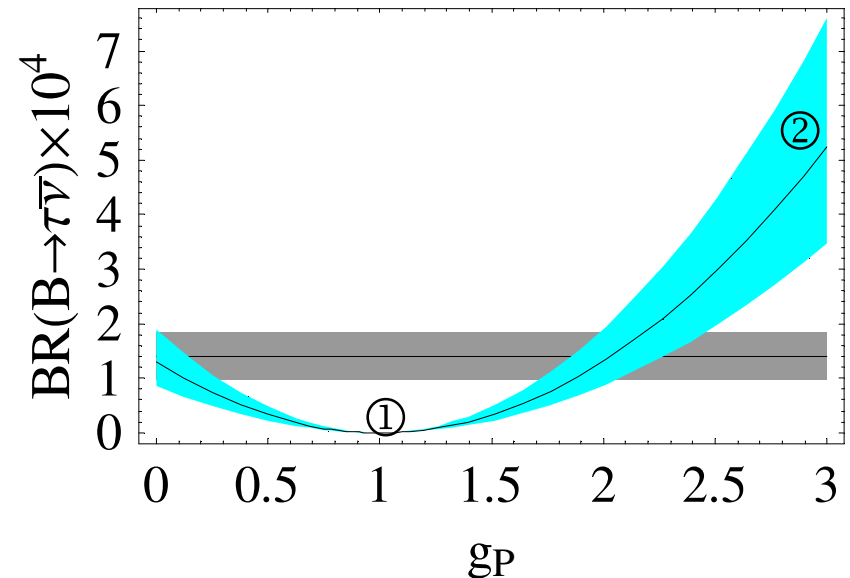
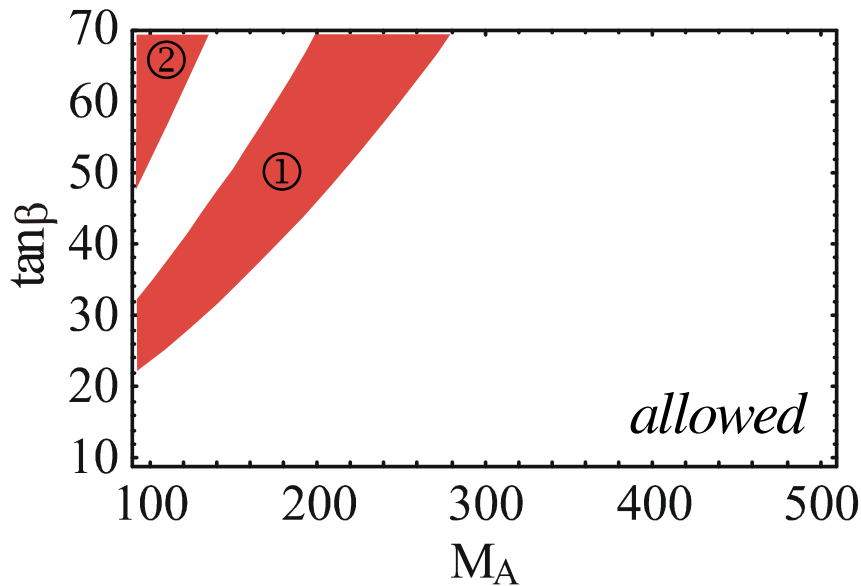
$a_{t,b} = 2 TeV; \mu = M_{\tilde{g}} = 1.5 TeV$

$M_1 = 0.5 TeV$

# The $B^\pm \rightarrow \tau^\pm \nu$ constraint

$$\mathcal{B}(B^\pm \rightarrow \tau^\pm \nu) = \mathcal{B}(B^\pm \rightarrow \tau^\pm \nu)_{SM} |1 - g_P|^2, \quad g_P \simeq \frac{M_B^2 \tan \beta^2}{M_{H^\pm}^2 (1 + \epsilon_0 \tan \beta)}$$

[Hou '93][Akeroyd, Recksiegel '03]...



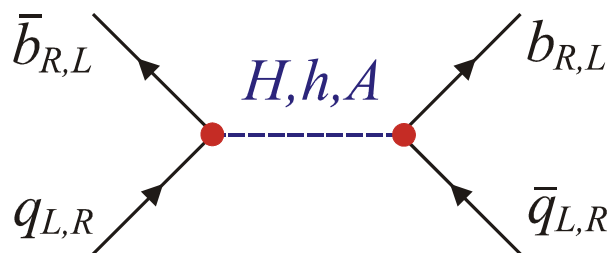
$\Rightarrow$  The precise measurements of  $\Delta M_{d,s}$  are best used as normalizations to avoid the large uncertainties related to  $V_{tq}$  and  $F_{B_q}$  when using  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$  and  $\mathcal{B}(B^\pm \rightarrow \tau^\pm \nu)$  to probe the MSSM with large  $\tan \beta$

# Conclusions



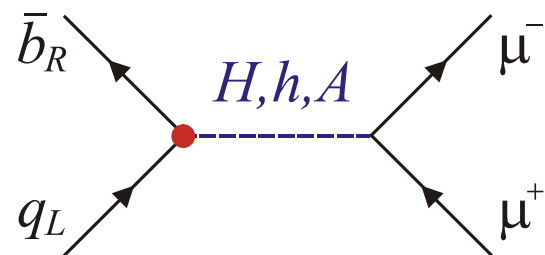
# Conclusions

- Systematic investigation of *all leading contributions* to  $\Delta M_q$  in the MFV-MSSM with large  $\tan\beta$  and heavy sparticles
- No new large effects are found. Still, *corrections to Higgs masses/mixings* can be relevant for *small*  $M_A$  ( $< 200$  GeV). They *add* to the SM contribution.
- Correlation to  $\mathcal{B}(B_q \rightarrow \mu^+ \mu^-)$  then becomes :



$\Delta M_s$  decreased (but less),  
 $\Delta M_d$  increased

← correlated →



$\mathcal{B}(B_q \rightarrow \mu^+ \mu^-)$  increased  
(as before)

- With all contributions under control: the present experimental bounds on  $\mathcal{B}(B_q \rightarrow \mu^+ \mu^-)$  *excludes a significant decrease (increase)* of  $\Delta M_s$  ( $\Delta M_d$ )