

Beam Dynamics study by using  
Genetic Algorithms  
and  
the ELI-np case

*Alberto Bacci – INFN-Milano*

# Outline

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## □ Genetic Algorithms (GAs) introduction

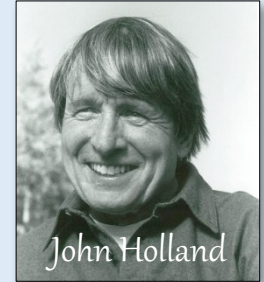
- Historical notes
- Hints on *What are* & *Why use GAs*
- *Where: Genetic Algorithms in Beam Dynamics Optimization*

## □ GAs applied to Beam-Lines Optimization

- From *Beam-Lines* to *Chromosomes*
- Following *Genetic Laws: Fitness, Reproduction, Mutations, ...*
- E.G.: *SPARC* beam line *Optimization* in *Thomson* case

## □ The GIOTTO code

- The *Data-Based DB*
- Inputs & Outputs
- *Fitness* function (or *Idoneity*) *definition*
- Optimizations & Statistics on *Specific Cases*:
  - ✓ *Ultra short bunches by Hybrid Velocity Bunching*
  - ✓ *Comb bunches distributions*
- *Eli-np Case: The reference Working Point & Statistic*



❖ 1970 John Holland - schemata theorem

❖ 1975 J. Holland *publication*: “Adaptation in Natural and Artificial Systems: An Introductory Analysis with Application to Biology, Control, and Artificial Intelligence”.  
*The Seminal work*

❖ 1975 K. De Jong (J. Holland’s student), Thesis: “An analysis of the behavior of a class of genetic adaptive systems”. *Broad applicability of GAs*

❖ 1989 David Goldberg *Book*: “Genetic Algorithms in Search, Optimization, and Machine Learning”

It deals with the topic at high level and is considered a **milestone in GAs story**. It reports techniques like Multi Objective GA (MOGA), today very current.

## □ Introduction: What & Why

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### What are Genetic Algorithms (GAs)

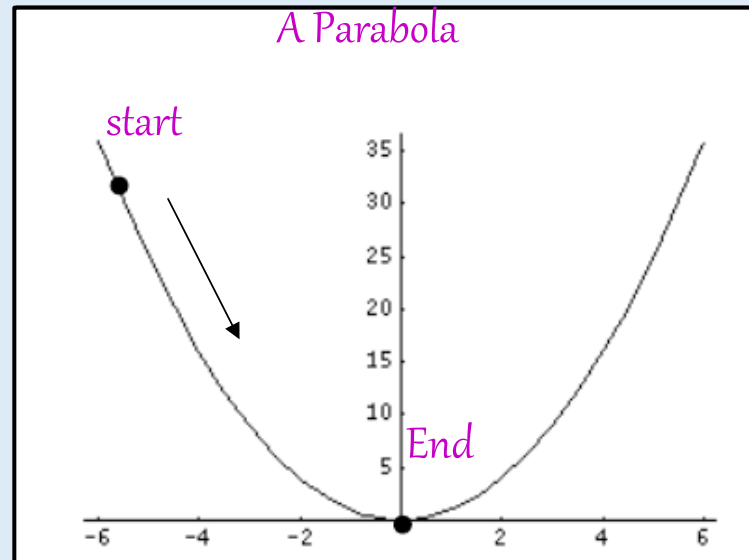
Searching procedures based on *natural selections* (genetic laws)

### Why choosing GAs versus other techniques ...

A basic answer:

*Newton-Raphson* methods (and **many variants**) are *based on local information*.

The Scan moves in direction of “local maxima” or “local minima”



## Why Genetic Algorithms \*\*

Despite, *Newton-Raphson* methods can overcome the local solutions issue by some tricks ...

**GAs are:**

- *naturally able* to manage the local solution issue
- *naturally parallelizable*
- usable with a *minimum mathematical effort*

*And*, by empiric results,

*show strong capability to manage problems where other methods fail*

Genetic Algorithm Optimization  
Applied to Electromagnetics:  
A Review

Daniel S. Weile and Eric Michielssen, *Member, IEEE*

IEEE TRANSACTIONS ON ANTENNAS AND PROPAGATION, VOL. 45, NO. 3, MARCH 1997

\*\* pros and cons in literature

## □ Where: Genetic Algorithms (GAs) in Beam Dynamics Optimization -1

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GAs give strong advantages ...

➤ in multi-dimensional problems with variables strongly non linear correlated

A main example :

➤ Space Charge & its non-linear nature: correlates low energy beam-line parameters

➤ Also frozen beams (space charge off): Other complex situations

Example (1) Thomson/Compton Sources (e.g. SPARC\_lab, STAR, ThomX, ELI-np, Munich Compact Light Source) which ask for :

For the spectral density: 1) very low DE/E, 2) low Emit

For the photon flux : 3)  $Q_{\text{bunch}}$  as high as possible

**Example (2) Ultra short e-beams** (e.g. SPARC\_lab, LCLS, REAGE, XFEL, EUPRAXIA, ... ):

- **Femtosecond light pulses (FEL/X-FEL)**, Atoms in chemical reactions, phase-transition, *Photosynthesis Water Splitting* : timescale 1-100 fs [2014 “first snapshots of water splitting” by LCLS; ScienceDaily; Nature]
- **Plasma Wave Acceleration**:  $\lambda_{\text{plasma}}$  order of 30-600 fs . The **Witness** much shorter, the **Driver** (pwfa) comparable to  $\lambda_{\text{plasma}}$
- **Femtosecond Electron Diffraction (FED)**  
*Molecular or atomic motion movies*: phase transitions, ..., . Timescale: few 10s of fs.  
Relativistic case:  $E_b \approx 5\text{MeV}$ ,  $Q_b \approx 100\text{fC}$ ,  $\varepsilon_{\text{tr}} < 0.1\text{ mm-mrad}$ ,  $\sigma_z < 30\mu\text{m}$  (100fs)
- **THz radiation (by CoTrRad)**  
0.1 up to tens THz is of great interest for both *longitudinal electron beam diagnostics* (fs scale) and *spectroscopy* in pump-and-probe experiments ...

*Genetic Algorithms  
applied to Beam-Line Optimization*

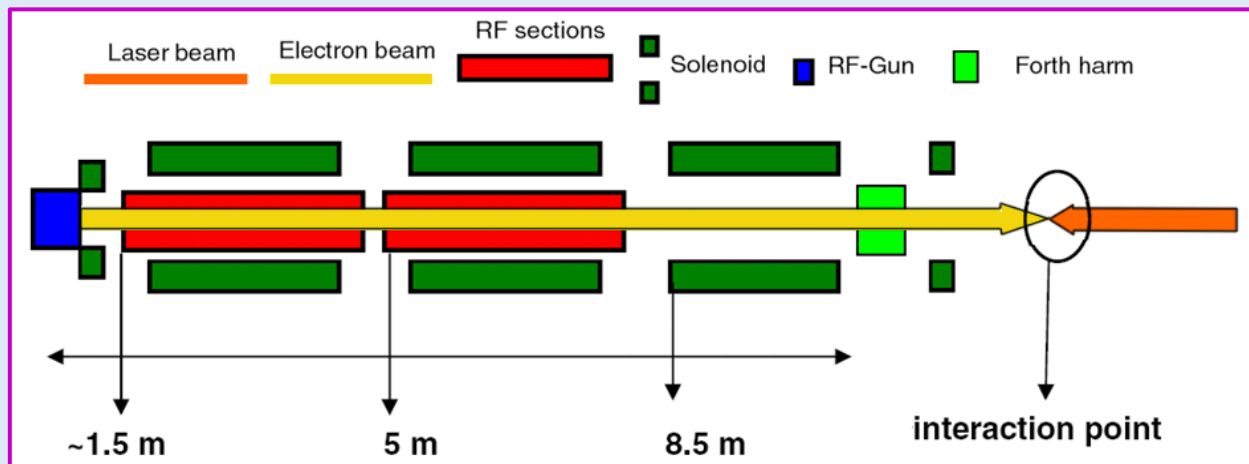


# From Beam-Lines to Chromosomes

Genetic Laws work on Chromosomes ==> Chromosomes are made of genes (parameters)

Beam-Line = Parameters Array ==> One Chromosome

A Beam-Line



=

Chromosome	
Gene	Reference case
$dE_g / dz (MV/m)$	120
$\phi_g (^\circ)$	0
$B_g (T)$	0.2707
$dE_1 / dz (MV/m)$	13.4
$\phi_1 (^\circ)$	-30
$B_1 (T)$	0.12
$z_1 (m)$	1.322
$dE_2 / dz (MV/m)$	6.55
$\phi_2 (^\circ)$	88
$B_2 (T)$	0.1145
$z_2 (m)$	5
$B_3 (T)$	0.1145
$z_3 (m)$	8.5
$\phi_{IH} (^\circ)$	180
$z_{IH} (m)$	11.7

# Following Genetic Laws: Fitness Function

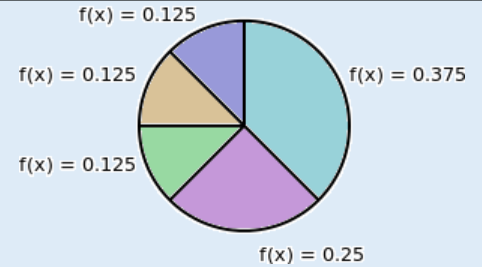
Gene	Reference case
$dE_g / dz (MV/m)$	120
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$\phi_2 (^\circ)$	88
$B_2 (T)$	0.1145
$z_2 (m)$	5
$B_3 (T)$	0.1145
$z_3 (m)$	8.5
$\phi_{\text{max}} (^\circ)$	180
$z_{\text{max}} (m)$	11.7

Starts from random generation

Rules to pass generation  $\rightarrow$  in generation:

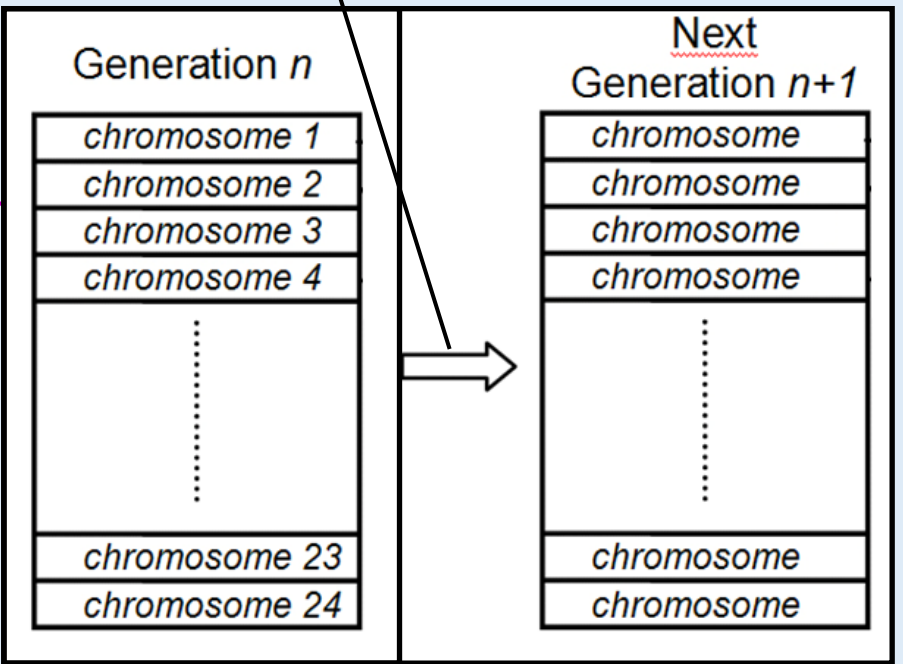
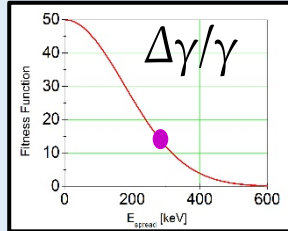
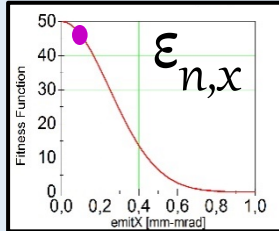
- Selection: *bluffed* Roulette wheel
- Mutations

.... & others methods & tricks. *The rule*: closest to Nature, best performances



Chromosomes Must be sorted by a Fitness function 

$$\text{runner} \approx 50 \cdot e^{-\left(\frac{eimtX}{0.35}\right)^2} + 50 \cdot e^{-\left(\frac{E_{\text{spread}}}{250}\right)^2}$$

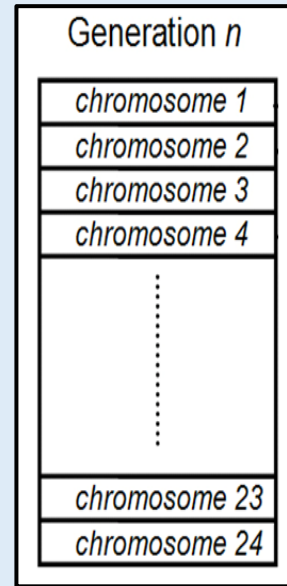
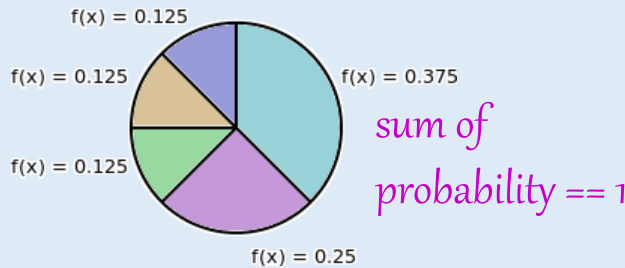


# ➤ Following Genetic Laws: Reproduction & Mutation

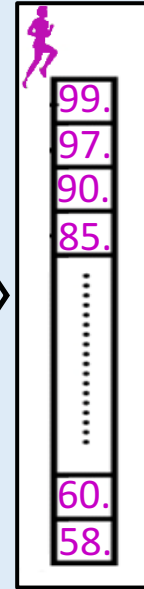
Chromosome Sorting by 

$$0 < \text{runner} < 100$$

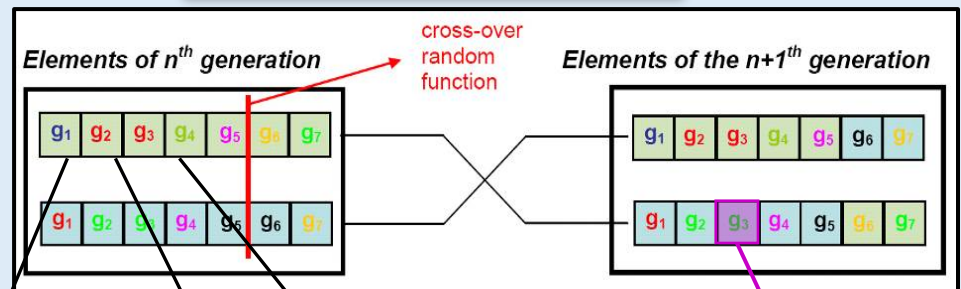
By the Roulette Wheel: **two** Chromosomes



Tracking code

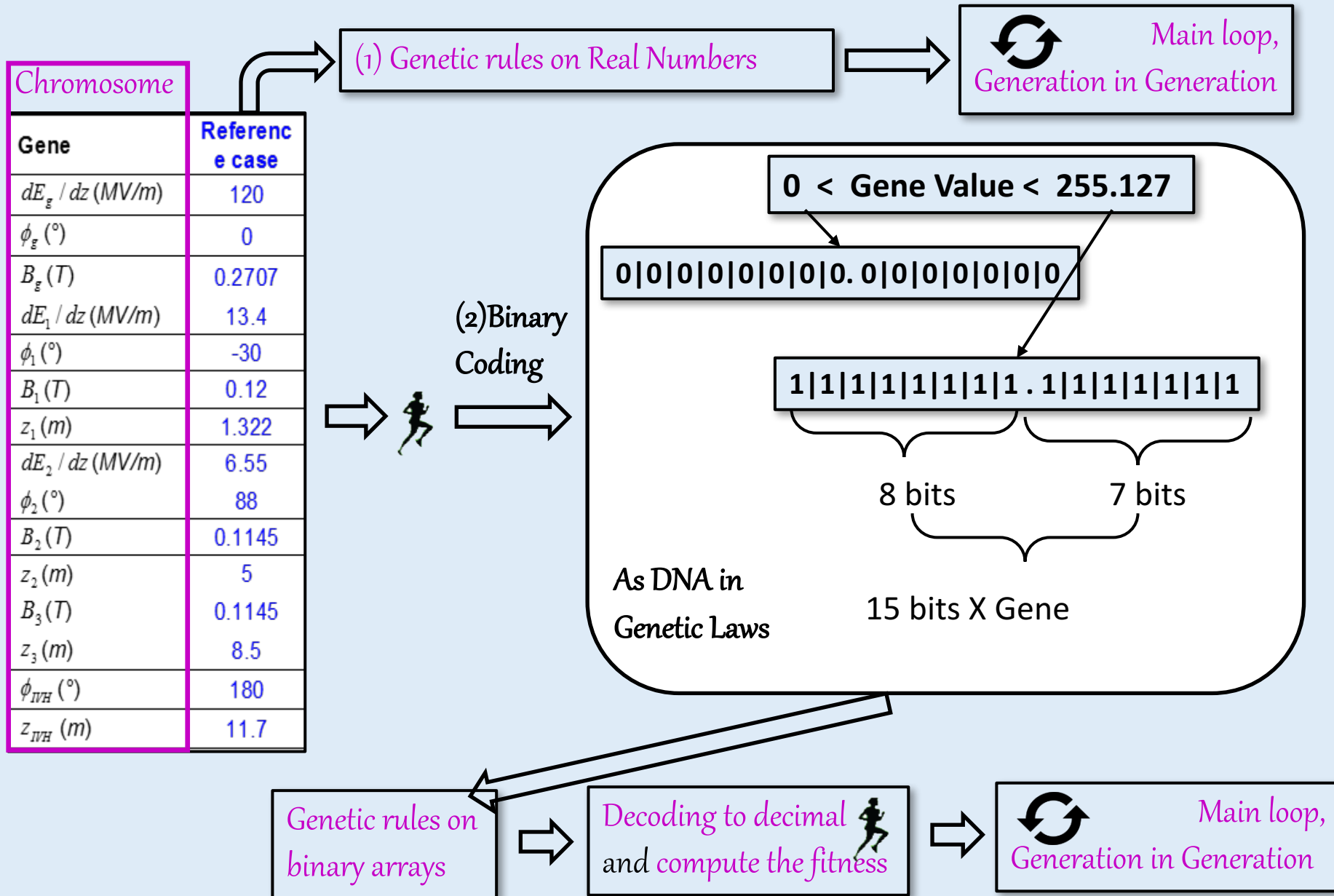


Chromosomes reproduction



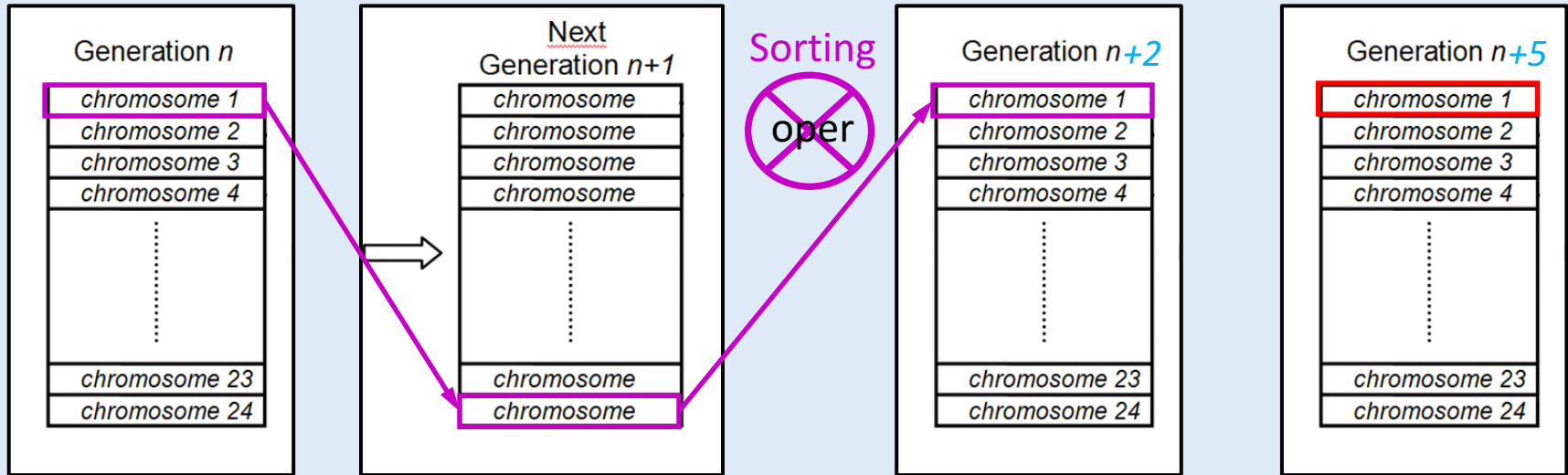
*Gun gradient*  
*Gun  $\Phi$  injection*  
 *$B_z$  intensity*  
*first solenoid*

➤ Following Genetic Laws: **Real coding (1)** and **binary coding (2)**



## ➤ Following Genetic Laws: Elitism

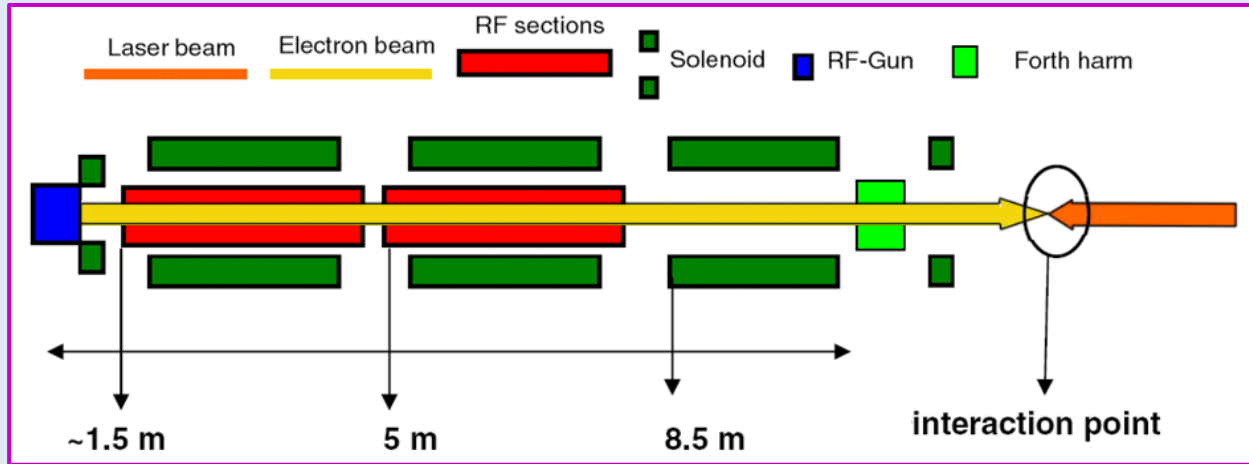
Concluding: *the elitism*



Nowadays “**quasi-classic**” optimization techniques

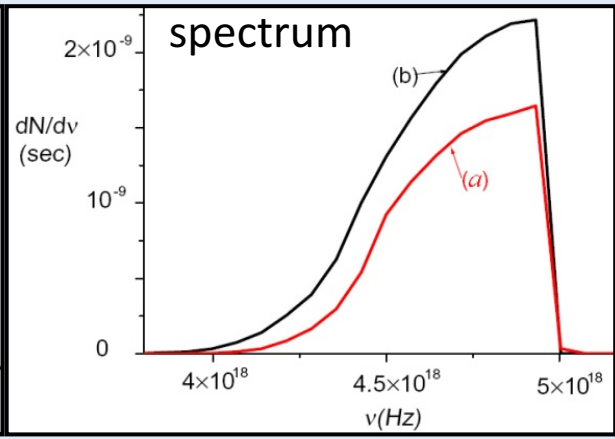
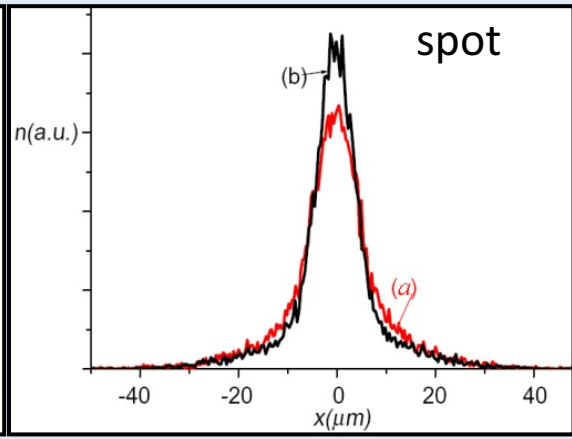
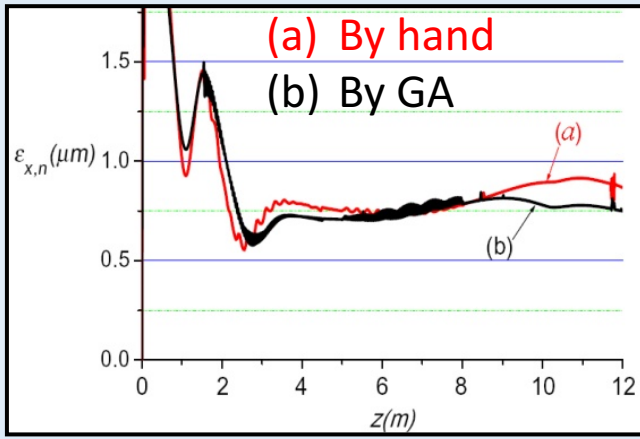
- *elitism*
- *advanced mutation operators*
- *hill climbing*
- *regeneration from best solutions*
- *... ..*
- *& parallelization quasi-mandatory*

➤ E.G.: SPARC beam line Optimization in Thomson case



Old Kind of Fitness Function

$$F_{fitness} = \frac{1}{\epsilon_{x,n} \cdot \frac{\Delta\gamma}{\gamma}}$$



“MAXIMIZING THE BRIGHTNESS OF AB ELECTRON BEAM BY MEANS OF A GENETIC ALGORITHM”

The  
GIOTTO code

# GIOTTO - Genetic Interface for Optimising Tracking with Optics

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- ❖ WAS BORN in 2008; Language: Fortran 90/95
- ❖ USE for Optimization of Generic Code's Parameters or for Statistical (Jitters) Analysis
- ❖ INPUTS based on NameList & on two internal DataBase
- ❖ CAN easily Drive different codes:  
Now: ASTRA's Generator, ASTRA, QFluid (Plasma acceleration, A. Rossi modifications)
- ❖ Current Version (Ver. 10.0):  
Linux 64 bit; Windows 64 – (compilers gfortran or INTEL fortran)  
Parallelized with OPEN-MPI (Linux), MS-MPI or INTEL MPI (Windows)  
Used @ PSI (S. Bettoni) and tested at Desy-Pitz
- ❖ Code and Documentations:  
URL: <http://pcfasci.fisica.unimi.it/Pagine/GIOTTO/GIOTTO.htm> (server down, pardon!)  
Exist an User manual for version 8.5 2012 (needs updates)



# GIOTTO — Genetic Interface for Optimising Tracking with Optics

From 2008 up to day, the code is **grew in power** and **capability**

Optimization techniques: **elitism**; **advanced mutation operators**; hill climbing; ant colony **regeneration from best solutions**

 **user freely defined by Astra outputs:**

**Targets: bunch PosZ or Time, En, En<sub>spread</sub>, SigZ, Xemit, sigX, divergX, Yemit, ...**

## Important GIOTTO's features:

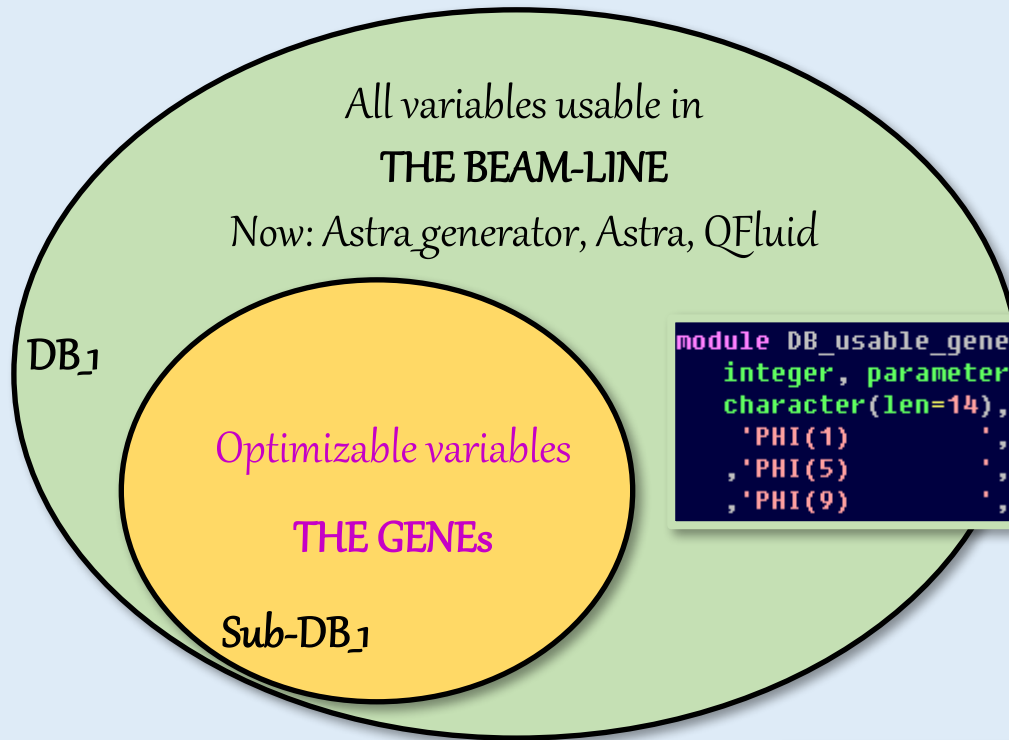
Every **NameList's variables** can be used as a **GENE** (optimizable) & **Any code working with NameList** is directly importable in GIOTTO.

ASTRA e.g. : **Phi(1)...**Phi(50), **MaxE(1:50)**, **MaxB(1:50)**, **sig\_x (laser cathode)** ,**sig\_clock (Laser @ cathode)**, ..., ... (no limit on the number)

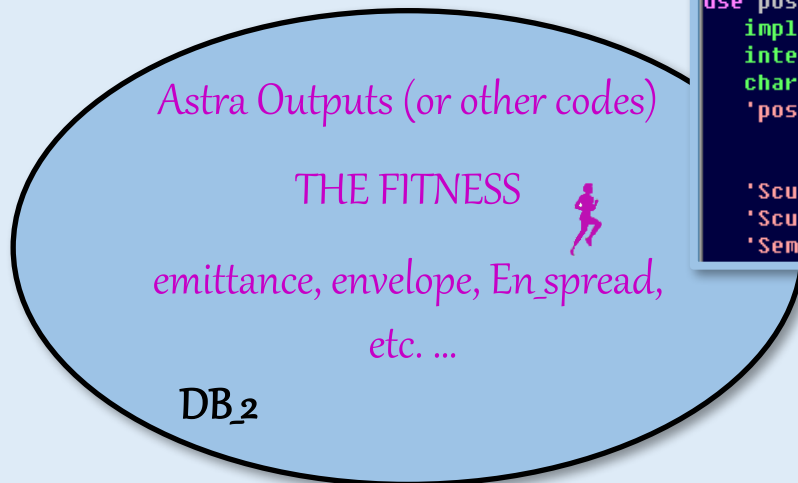
Constraints freely defined by the user (under test)

Switch from **Optimizations** to **Statistical analysis** is really **EASY**

**Jitters sampling interval: Uniform** or **Gaussian**



```
module DB_usable_gene
integer, parameter :: DB_extension=269
character(len=14),dimension(DB_extension) :: DB_genes=(&  !da inseri
'PHI(1)      ','PHI(2)      ','PHI(3)      ','PHI(4)      '&
','PHI(5)      ','PHI(6)      ','PHI(7)      ','PHI(8)      '&
','PHI(9)      ','PHI(10)     ','PHI(11)     ','PHI(12)     '&
```



```
module charge_rpn_idon  !rpn reverse polish notation
use post_processors
implicit none
integer,parameter,private :: DB_out_dim=107
character(len=10),dimension(DB_out_dim),private :: DB_out=(&
'posZ      ','time      ','En      ','sigZ      ','DEn      ','emitZ
','Xmed      ','sigX      ','divergX    ','emitX
','Ymed      ','sigY      ','divergY    ','emitY
','Scurr(1)  ','Scurr(2)  ','Scurr(3)  ','Scurr(4)  ','Scurr(5)  ','&
','Scurr(6)  ','Scurr(7)  ','Scurr(8)  ','Scurr(9)  ','Scurr(10) ','&
','SemitX(1) ','SemitX(2) ','SemitX(3) ','SemitX(4) ','SemitX(5) ','&
```

## ➤ GIOTTO's INPUT FILE

GINxx.xx.ini is divided in two parts:

- 1) One **NameList** (&GA) giving all the directive to GIOTTO
- 2) Three **keyNames** defining: **CONSTRAINTS**, **FITNESS** and **GENES**

```
1) {
&GA
Astra_in='Astra_23_Jan2014.exe','pls-start.in'
....
.....
/

=====From here Key_Names=====
===== (lines after one blank-record are comments) =====
=====

2) {
[constr01]
sigZ En * sqr emitZ sqr sigX * / 5300 * 1 >

[constr02]
sigZ En * sqr emitZ sqr sigX * / 6300 * 10 >

[idoneity] !must be used the Reverse Polish Notation
emitX 2.5 / sqr -1. * exp 50 *
sigZ 0.150 / sqr -1. * exp 50 * +
sigX 2.5 / sqr -1. * exp 50 * +

!Gene(i)___Delta___JoinGenes(i:i+N)___u-uniform___g-gaussian___JoingSign
[genes]
sig_clock    0.2E-3    1      u    1  0.0 0
SIG_x        0.02     1      u    1  0.0 0
MaxB(1)      0.08     1      u    1  0.0 0
MaxB(2)      0.08     1      u    1  0.0 0

```

# ➤ GIOTTO's INPUT FILE: &GA NameList

```
&GA
Astra_in='Astra_23_Jan2014.exe', 'pls-start.in'
Gener_in='generator Mar2013.exe', 'generator-start1.in'
Genes_number=7 !max value is 40
pop_size=8 !must to be a multiple of the nodes numbers
generations_number=410

keepADistribution=.false. !".f." start from "Gener_in", ".t." from Distribution
keepInParameters=.true.
!".t." the chrom in the first gen; ".f." All rnd, the chrom as central values

!*****Turn on and Control the constraints
constraints=.false. !if "true" turn-on constraints-----
minimumZ=1.0 !this is valid for all constraints
constr_number=2 !max number of constraints is 10
constr_name='[constr01]', '[constr02]'
lower_Zbound=1.6,5.0,16.0 !intervals where the constraint is valid
upper_Zbound=25.0,25.0,25.0

!*****Post processor for COMB bunch distributions*****
LaserComb=.false. !if true Gener_in is a generator input with SPIKES namelist--
!if "true" uses "ID_bunch_LC" for the spikes analysis and compute the Fitness--
LaserComb_PostPro=.false.
PostPro_in_index=0012

!*****Forced Optimization Process*****
step_OP_forced=25
variation_x100=5.0 !Best Cromosom Variation %. Every "step_OP_forced"-----
!-----variation in % is halved----untill "step_OP_forced" X "Step2Start_x100"---
Step2Start_x100=4

!*****Statistical Analysis*****
statistic=.false.
Runs_Number=360 !must be a multiple of the pop_size
/
```

Usually few variables are used

Under developing (it slows down heavily GIOTTO)

Optimization Rarely needs changes

Fitness & Genes

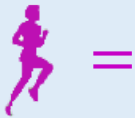


# ➤ GIOTTO: FITNESS FUNCTION

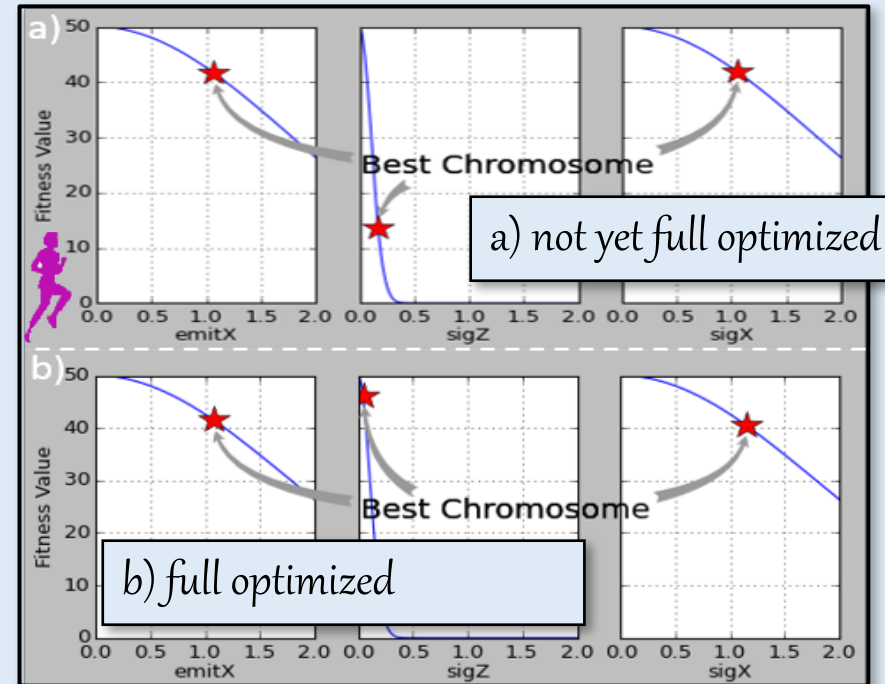
```
[idoneity] !must be used the Reverse Polish Notation
emitX 2.5 / sqr -1. * exp 50 *
sigZ 0.150 / sqr -1. * exp 50 * +
sigX 2.5 / sqr -1. * exp 50 * +
```

Reverse Polish Notation: Operands Follow Operands

- 3 4 + = 7
- Stack based operation
- Does not need brackets



$$50 \cdot e^{-\left(\frac{\text{emitX}}{2.5}\right)^2} + 50 \cdot e^{-\left(\frac{\text{sigZ}}{0.15}\right)^2} + 50 \cdot e^{-\left(\frac{\text{sigX}}{2.5}\right)^2}$$



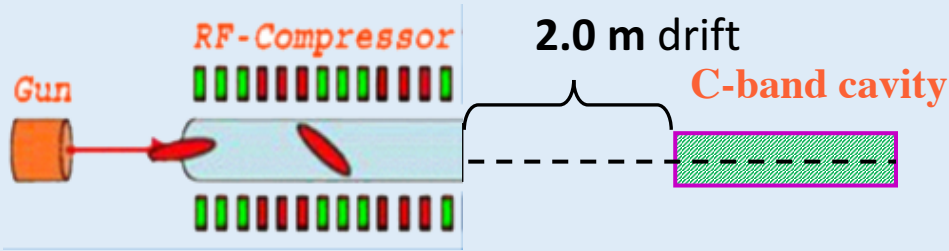
Fitness Function strategy to Cope with Multi Objectives Problems (MO):

- One Single Criterium per Equation piece (Objectives Wights)
- To be close to the Goal mean close to the Gaussian Curve Top
- The 'Far region' (referring to optimization) has to be on the maximum Gaussin slope
- change the FF in real time (ander implementation)

GIOTTO

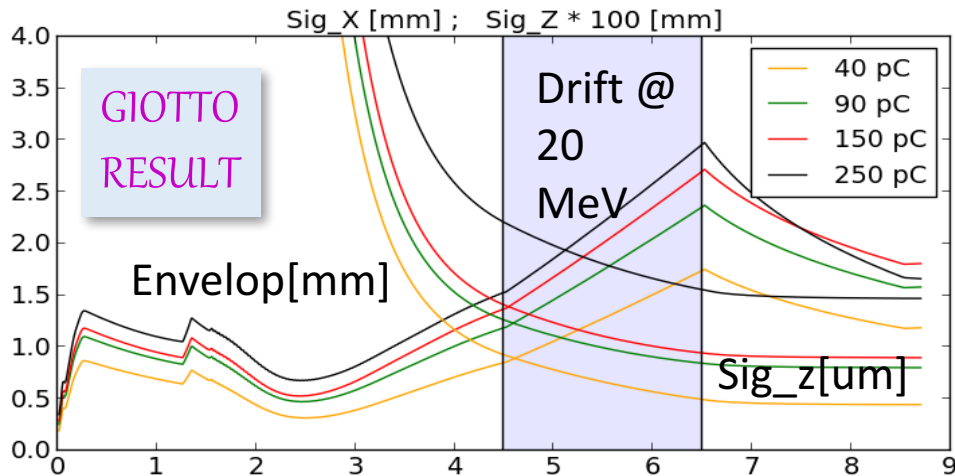
*Optimization &  
Statistical analysis*

# Beam-Line Optimization for: *ultra short*, *ultra cold*, High *brightness* bunches



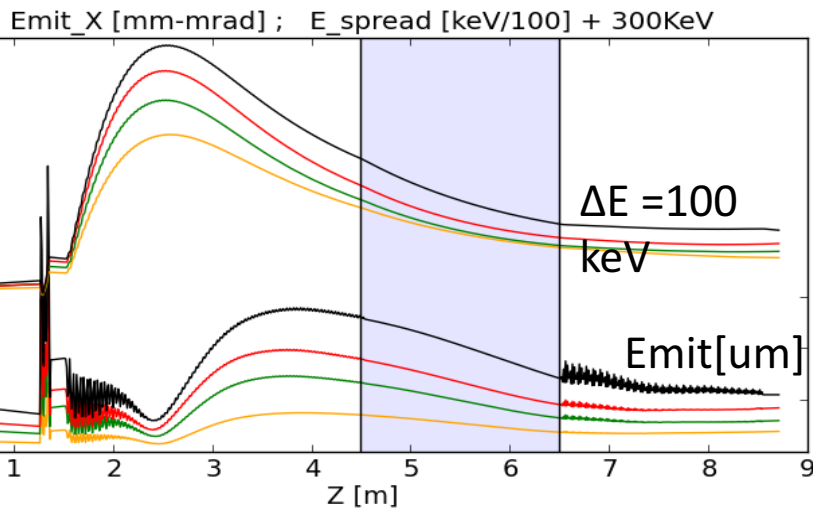
## GOALS:

- Low *Emittance*
- Low *Energy Spread*
- femptosec. *Sig\_Z*



## A Beam-Line studied with:

- *Experience*
- *An Ad hoc GIOTTO use*



## GENES in the Optimization:

- Gun:
  - (1) Phase & (2) Solenoid ( $B_z$ )
- TW cavity (RF- Compressor):
  - (3) Phase & (4) Solenoids
- C-band cavity: (5) Phase



# GIOTTO OUTPUT: RISULTATI.TXT



```
[idoneity] !must be used the Reverse
emitX 1.2 / sqr -1. * exp 100 *
sigZ 0.016 / sqr -1. * exp 400 * +
DEn 200.0 / sqr -1. * exp 50 * +
```

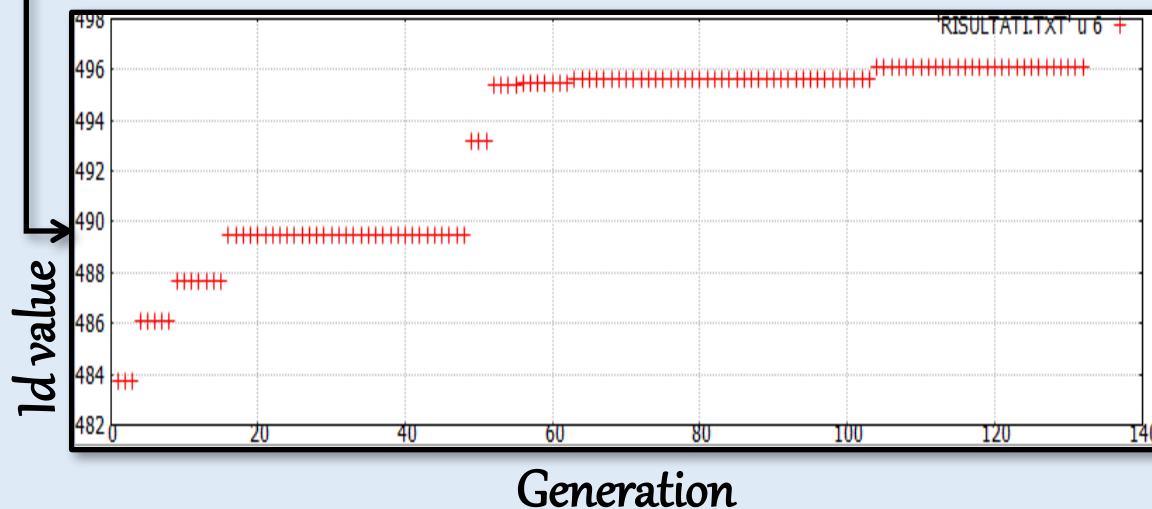
GENES

```
[genes]
MaxB(1) 0.003 1 u 1 0.0 0
MaxB(2) 0.01 1 u 1 0.0 0
Phi(1) 1.2 1 u 1 0.0 0
Phi(2) 1.5 1 u 1 0.0 0
Phi(3) 1.5 1 u 1 0.0 0
```

## RISULTATI.TXT

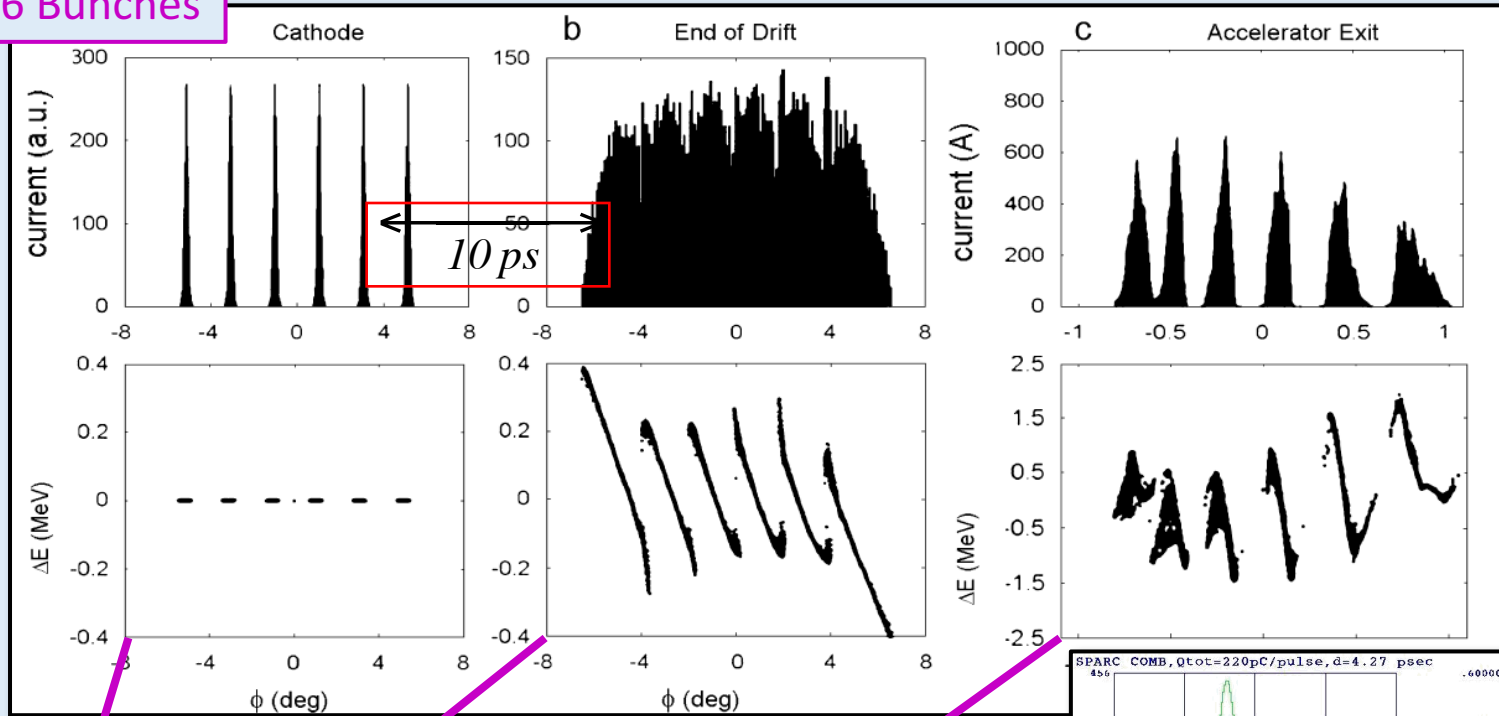
	MAXB(1)	MAXB(2)	PHI(1)	PHI(2)	PHI(3)	***id_best***	***id_worst***	Emit emitX	sigZ sigZ	$\Delta E$ DEn
1										
2	3.33234E-01	5.76714E-02	2.34351E+00	1.91001E+02	-8.48726E+01	4.83694E+02	7.83022E+01	5.79140E-01	5.08770E-03	7.80340E+01
3	3.33234E-01	5.76714E-02	2.34351E+00	1.91001E+02	-8.48726E+01	4.83694E+02	1.72762E+02	5.79140E-01	5.08770E-03	7.80340E+01
4	3.33234E-01	5.76714E-02	2.34351E+00	1.91001E+02	-8.48726E+01	4.83694E+02	3.32879E+02	5.79140E-01	5.08770E-03	7.80340E+01
5	3.33234E-01	5.76714E-02	2.18337E+00	1.90543E+02	-8.50834E+01	4.86096E+02	3.06747E+02	6.46100E-01	4.62500E-03	7.56980E+01
6	3.33234E-01	5.76714E-02	2.18337E+00	1.90543E+02	-8.50834E+01	4.86096E+02	3.27456E+02	6.46100E-01	4.62500E-03	7.56980E+01
7	3.33234E-01	5.76714E-02	2.18337E+00	1.90543E+02	-8.50834E+01	4.86096E+02	2.90264E+02	6.46100E-01	4.62500E-03	7.56980E+01
8	3.33234E-01	5.76714E-02	2.18337E+00	1.90543E+02	-8.50834E+01	4.86096E+02	2.92544E+02	6.46100E-01	4.62500E-03	7.56980E+01
9	3.33234E-01	5.76714E-02	2.18337E+00	1.90543E+02	-8.50834E+01	4.86096E+02	3.01542E+02	6.46100E-01	4.62500E-03	7.56980E+01
10	3.33234E-01	5.76714E-02	2.34351E+00	1.90543E+02	-8.50834E+01	4.87645E+02	4.29286E+02	6.16760E-01	4.63930E-03	7.69790E+01
11	3.33234E-01	5.76714E-02	2.34351E+00	1.90543E+02	-8.50834E+01	4.87645E+02	4.31203E+02	6.16760E-01	4.63930E-03	7.69790E+01
12	3.33234E-01	5.76714E-02	2.34351E+00	1.90543E+02	-8.50834E+01	4.87645E+02	4.40076E+02	6.16760E-01	4.63930E-03	7.69790E+01
13	3.33234E-01	5.76714E-02	2.34351E+00	1.90543E+02	-8.50834E+01	4.87645E+02	4.40076E+02	6.16760E-01	4.63930E-03	7.69790E+01

Best Chromosome of the Generation N.5

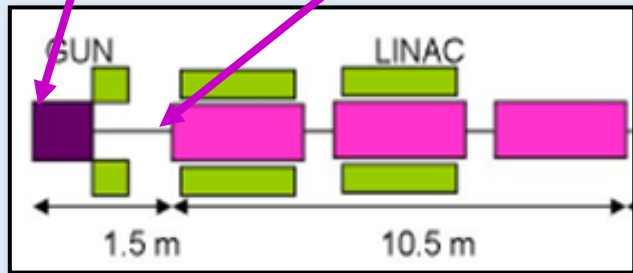
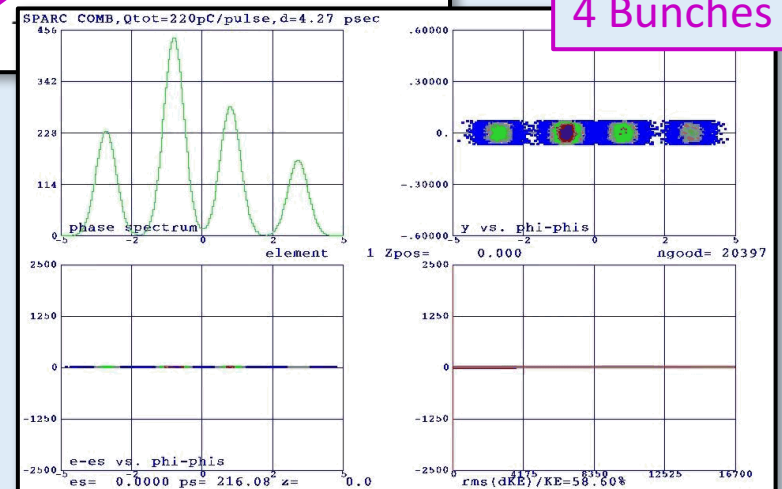


# Beam-Line STATISTIC for Laser Comb (ECHO Bunch Generations)

6 Bunches



4 Bunches



- P.O.Shea et al., Proc. of 2001 IEEE PAC, Chicago, USA (2001) p.704.
- M. Ferrario. M. Boscolo et al., Int. J. of Mod. Phys. B, 2006 (Taipei 05 Workshop)

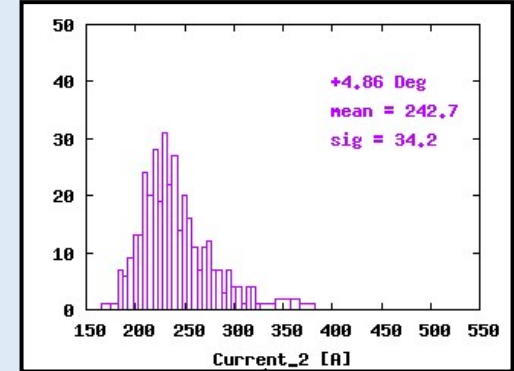
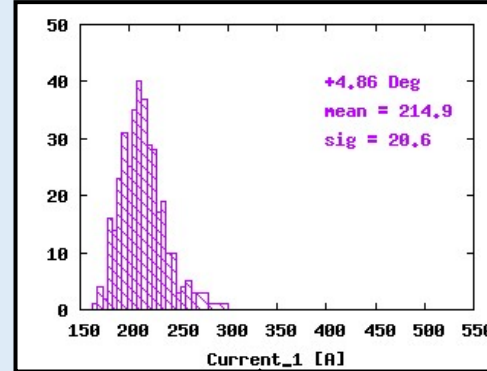
# Beam-Line STATISTIC for Laser Comb – TWO Bunches case : Current Statistic

```

!*****Statistical Analysis*****
statistic=.true.
Runs_Number=360      !must be a multiple of the pop_size
!*****
    
```

```

[genes]
phi(1)  0.9    1    g    1
phi(2)  0.9    1    g    1
    
```



bacci@pcsimul2:~/Doc\_Lavoro/08\_SPARC/03\_LaserComb/02\_Simulazioni/05\_Giotto/02b\_Titti\_comparison/02\_result\_p5

360 cases

5	posZ	time	En	sigZ	DEn	emitZ	zXEpMed	Xmed
6	12.0000000	40.1020012	127.5899963	0.1931200	315.2000122	49.8079987	181.1999969	-0.0012153
7	12.0000000	40.0989990	127.5899963	0.1988300	287.4100037	47.6329994	158.7799988	-0.0011859
8	12.0000000	40.1010017	127.5999985	0.1907200	329.6600037	51.0439987	192.4600067	-0.0012634
9	12.0000000	40.0989990	127.5899963	0.2004300	282.3500061	47.5709991	152.9400024	-0.0012552
10	12.0000000	40.0999985	127.5899963	0.2022500	275.6199951	47.2900009	145.9199982	-0.0012090
11	12.0000000	40.0970001	127.6399994	0.1682500	445.8599854	58.4290009	279.6300049	-0.0011903

sigX	divergX	emitX	xXxpMed	Ymed	sigY	divergY	emitY
0.1552100	0.0777850	1.6316000	0.0655140	0.0003971	0.1546800	0.0778750	1.6328000
0.1575600	0.0799780	1.5186000	0.0701300	0.0004734	0.1574000	0.0801450	1.5223000
0.1577300	0.0770300	1.7099000	0.0637480	0.0002847	0.1572100	0.0771520	1.7097000
0.1560300	0.0800730	1.4665999	0.0707510	0.0005361	0.1559900	0.0802450	1.4737000
0.1585100	0.0807810	1.4794000	0.0716900	0.0005785	0.1585100	0.0810230	1.4844000
0.1906800	0.0691680	2.5023999	0.0452270	0.0004415	0.1896900	0.0691130	2.5088999
0.1604000	0.0805670	1.5329999	0.0712300	0.0005018	0.1602400	0.0807310	1.5175000

yXypMed	Scurr01	Scurr02	SemtX01	SemtX02	SemtY01	SemtY02	Sdist01	Sdist02
0.0655090	216.6100006	234.6699982	1.0002000	1.6055000	1.0131000	1.5854000	0.0003813	0.0000000
0.0702470	227.5399933	218.2200012	1.0061001	1.6256000	1.0204000	1.6002001	0.0003928	0.0000000
0.0638020	209.6300049	244.7700043	1.0125999	1.7193000	1.0254000	1.7012000	0.0003765	0.0000000
0.0708450	230.9100037	215.6799927	0.9868600	1.6118000	1.0041000	1.5850000	0.0003960	0.0000000
0.0718970	234.2200012	212.6699982	1.0067000	1.6318001	1.0206000	1.6045001	0.0003997	0.0000000
0.0446640	170.4299927	359.5400085	1.0303000	1.6545000	1.0482000	1.6513000	0.0003305	0.0000000

GIOTTO  
*and the ELI-NP case*

## Beam Dynamic features

Electron Linac design to drive bright Compton back-scattering gamma-ray sources

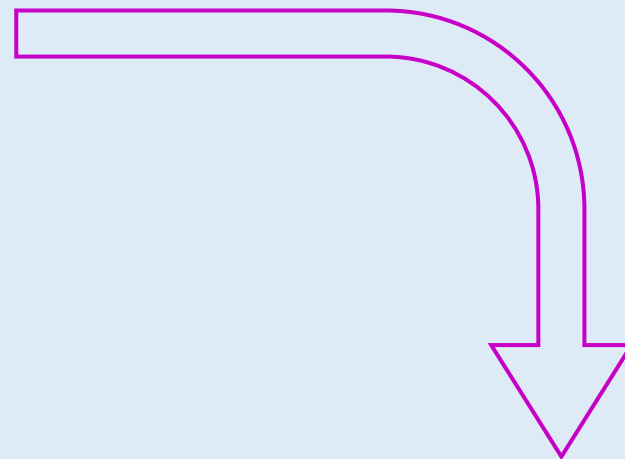
A. Bacci, D. Alesini, P. Antici, M. Bellaveglia, R. Boni et al.

J. Appl. Phys. 113, 194508 (2013); **online:** <http://dx.doi.org/10.1063/1.4805071>

## The Peculiar Gamma Ray Source features

Photon energy	<i>MeV</i>	0.2-19.5
Spectral Density	<i>ph/sec.eV</i>	$0.8\text{-}4\cdot 10^4$
Bandwidth (rms)	%	$\leq 0.5$
# photons per shot within FWHM bdw.		$\leq 2.6\cdot 10^5$
# photons/sec within FWHM bdw.		$\leq 8.3\cdot 10^8$
Source rms size	<i><math>\mu\text{m}</math></i>	10 - 30
Source rms divergence	<i><math>\mu\text{rad}</math></i>	25 - 200
Peak Brilliance ( $N_{ph}/\text{sec}\cdot\text{mm}^2\cdot\text{mrad}^2\cdot 0.1\%$ )		$10^{20}$ - $10^{23}$
Radiation pulse length (rms, <i>psec</i> )		0.7 - 1.5
Linear Polarization	%	> 99
Macro rep. rate	<i>Hz</i>	100
# of pulses per macropulse		$\leq 32$
Pulse-to-pulse separation	<i>nsec</i>	16

In next page,  
how to reach these parameters



## The Emittance

Maximization of electron density into transverse phase space :

==> means ==> very low emittance~ **0.4 mm-mrad**

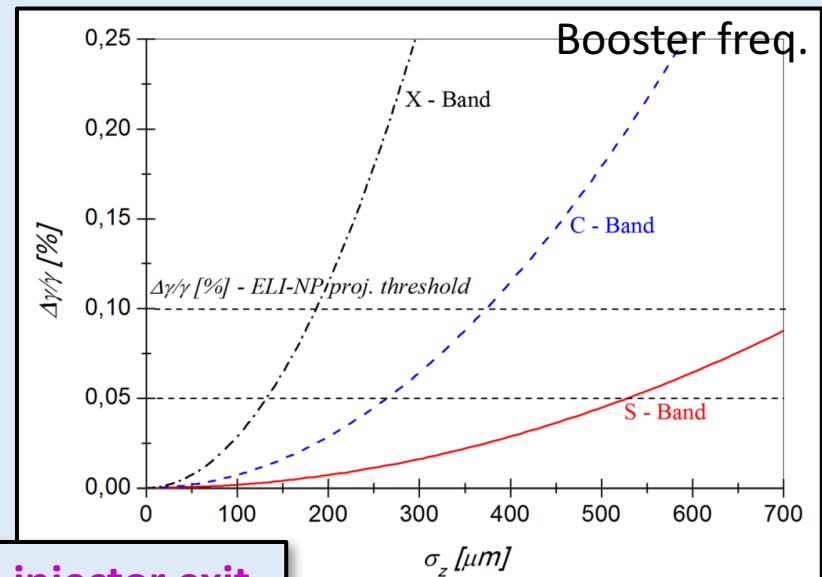
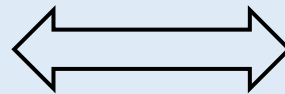
$$\eta \equiv \frac{Q_b}{\epsilon_n^2}$$

## The Energy Spread

Minimization of the energy spread: the **source spectral density** require  $\Delta\gamma/\gamma < 0.1\%$ , we have chosen a **conservative threshold of 0.05 %**

Energy Spread by **RF curvature**:

$$\frac{\Delta\gamma}{\gamma_{rms}} \approx 2 \left( \pi f_{RF} \frac{\sigma_z}{c} \right)^2$$

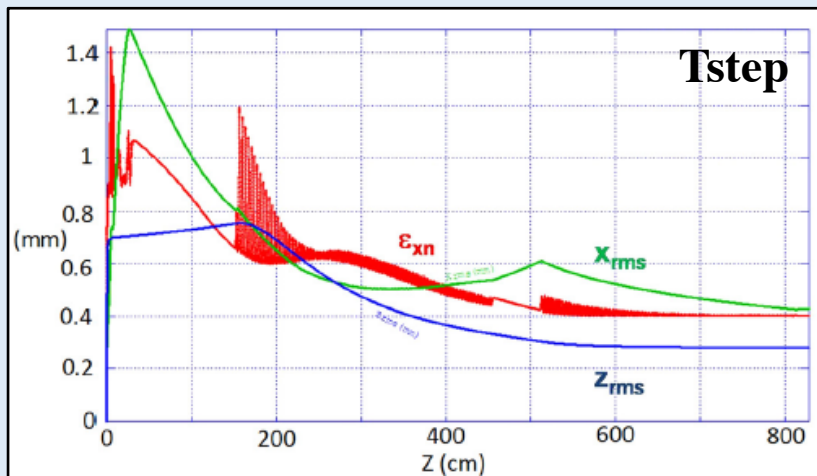
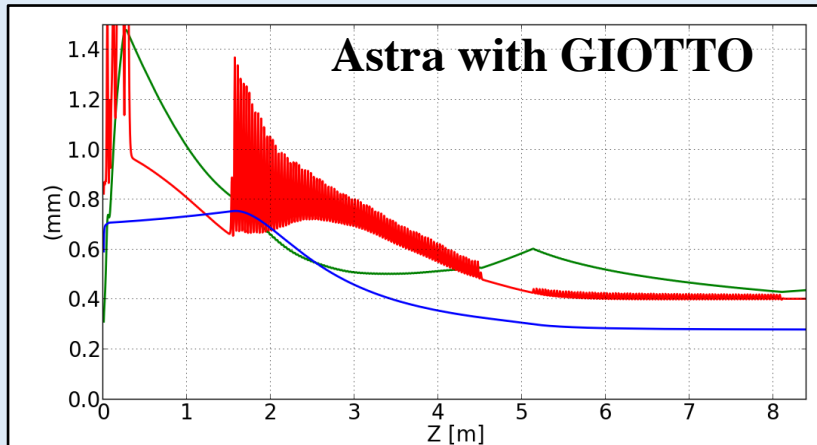


**σ<sub>z</sub> < 280 μm @ the injector exit**

# Result: GIOTTO optimization on merit factors ( booster's injector)

## Comparison using **Tstep** (a Parmela heir) & **Astra** codes

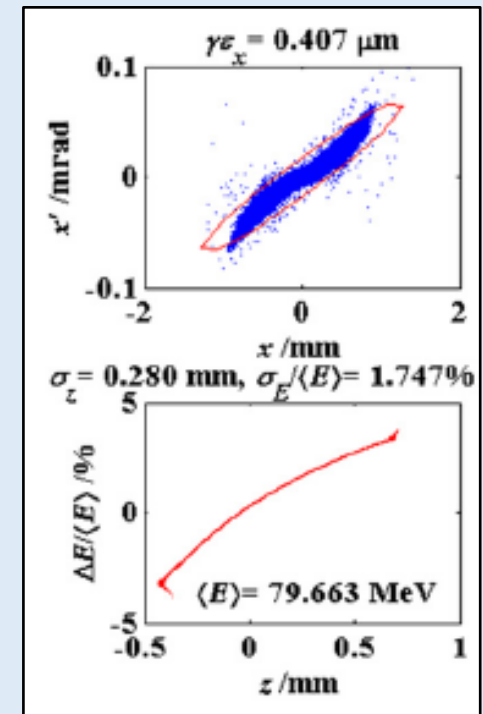
- 1) A space charged dominated region needs a double check
- 2) Astra gives the possibility to use Giotto (**Giotto improves 30-60 %**)



**Astra**

$\gamma\epsilon = 0.4 \mu m$   
 $\langle E \rangle = 79.8 MeV$   
 $\sigma_z = 0.279 mm$   
 $\sigma_E / \langle E \rangle = 1.65\%$

**Tstep**



Injector jitters analysis

a full S<sub>2</sub>E:

Injector → C Booster →  $\gamma$ -Source

Astra → Elegant → Cain



## ELI-NP booster's Injector Jitters (9 parameters)

### Jitters kept in Consideration in GIOTTO:

#### RF:

- 200 fs Phase (overestimated): (1) Gun & (2,3) TW cavities (S- band)
- 2‰ in pick field: (4) Gun & (5,6) TW cavities (S- band)

#### laser:

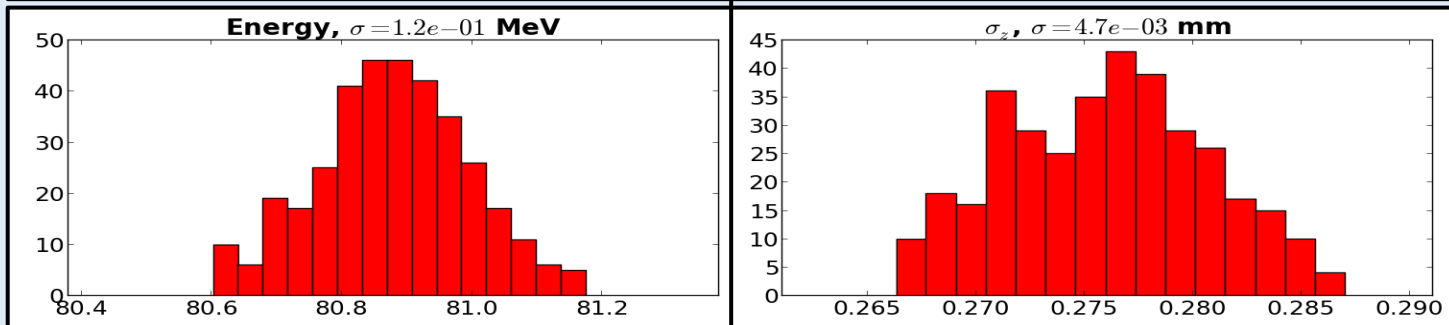
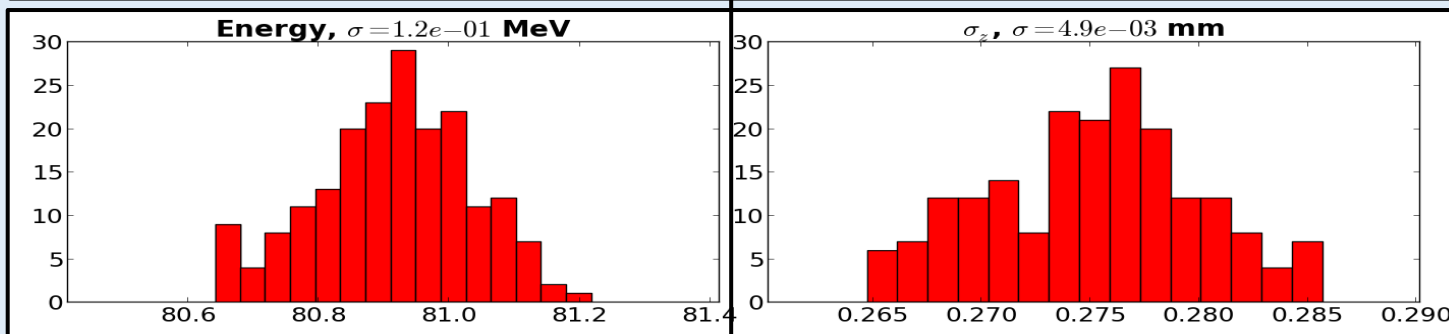
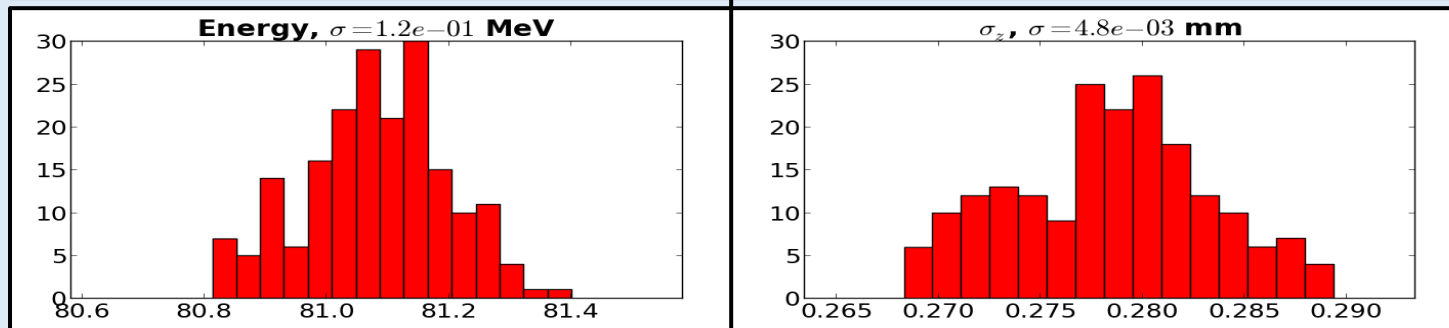
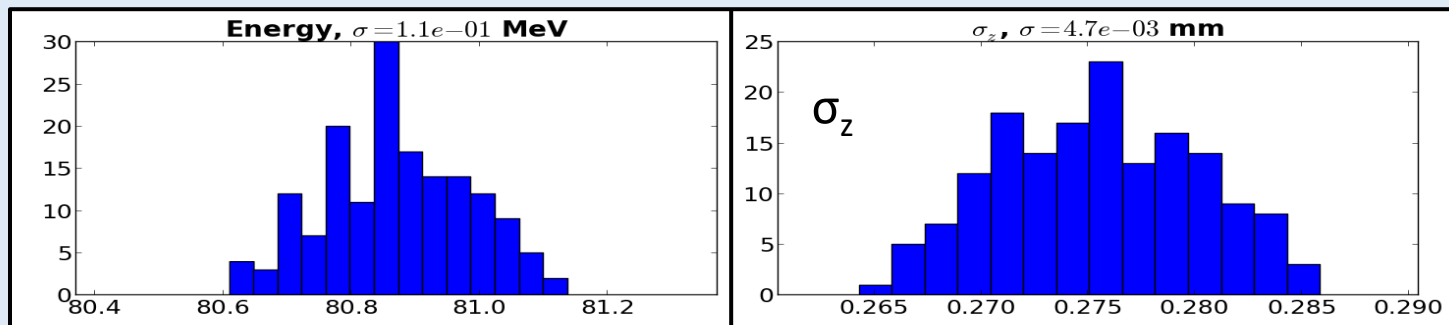
- (7) 200 fs arrival time
- (8) 20  $\mu\text{m}$  pointing instabilities (on cathode)
- (9) 5% energy fluctuation (Charge fluctuation)

### Different Machines:

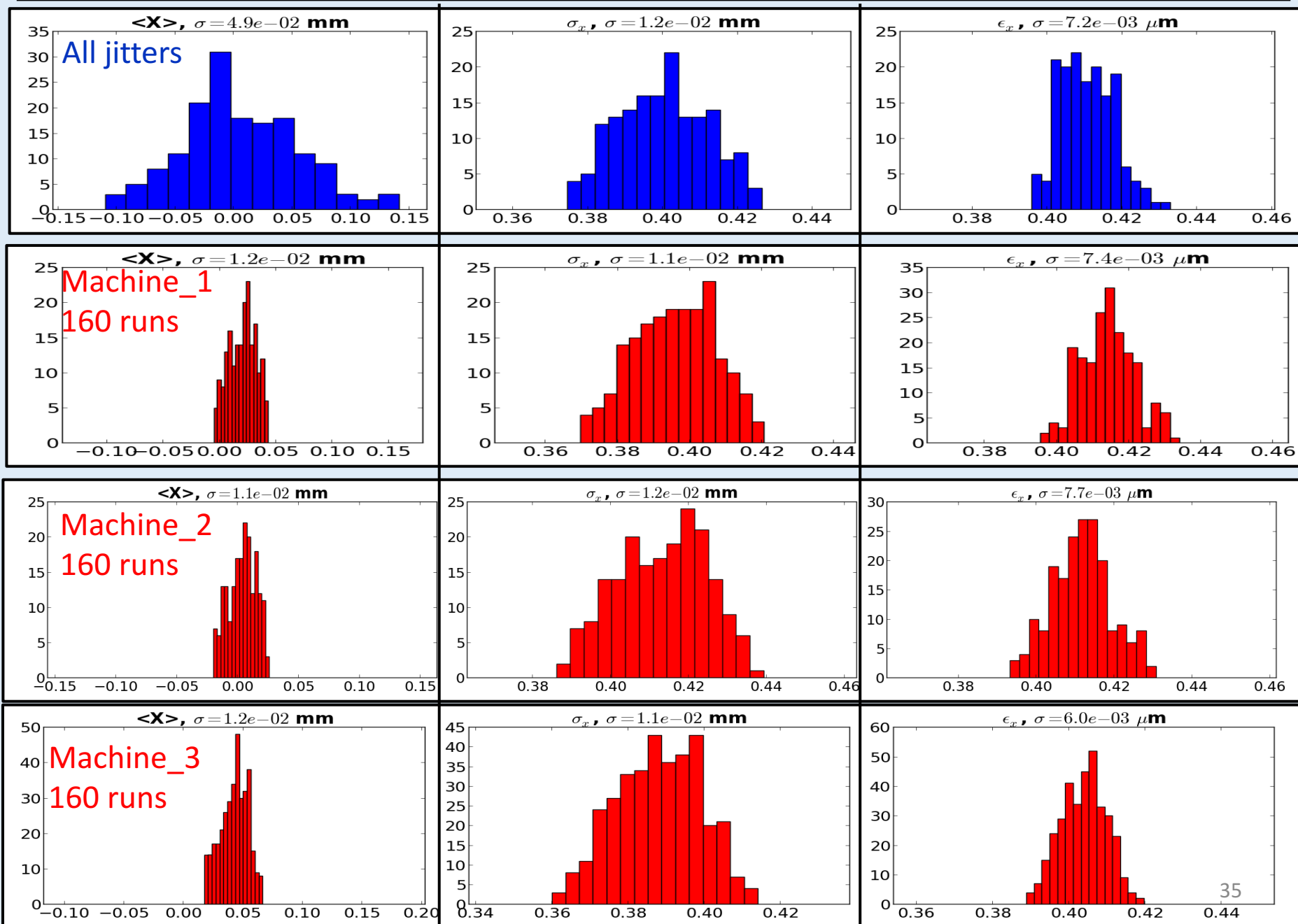
+/- 70  $\mu\text{m}$  as misalignments for: RF Cavities, Gun Solenoid, TW Solenoid

Uniform distributions Jitters; a very conservative choice

# ELI-NP Injector Jitters Analysis – Energy & Bunch length



# ELI-NP Injector Jitters Analysis – Centroid, Envelope, Emittance



## In Conclusion

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Genetic Algorithms show **great promise** in the **Beam Dynamics** optimization and **problem solution**.

GIOTO has been applied successfully to:

- refine known beam lines, with improvements around 20-40 % (in the performances)
- have been used to find completely new schemes, as in case of the hybrid velocity bunching

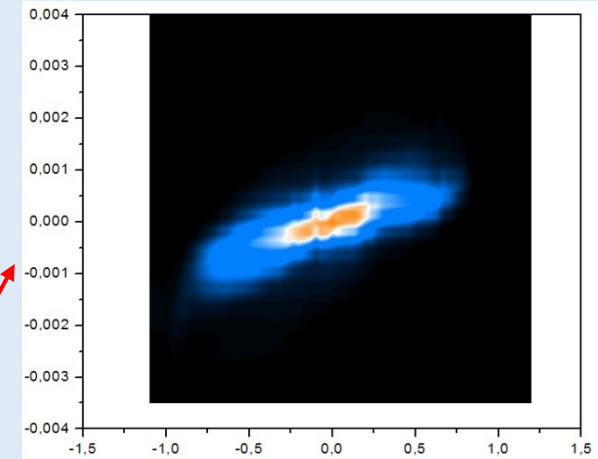
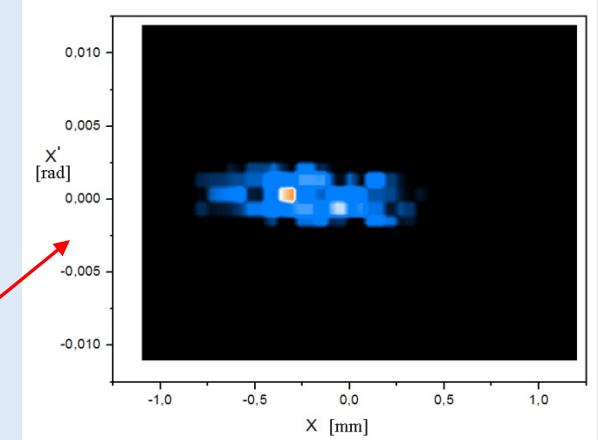
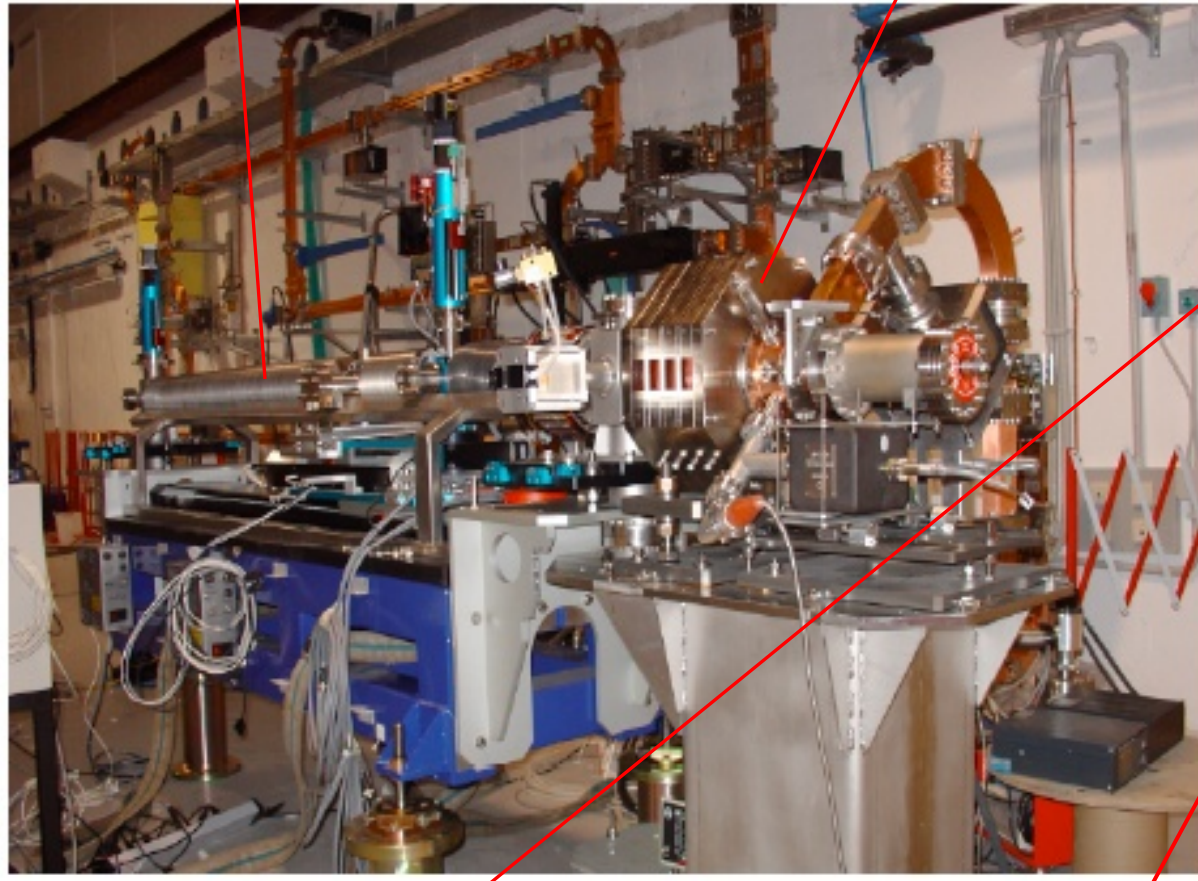
Thanks for your attention

Demand of EXTREME HIGH QUALITY electron beams doesn't stop and often it makes necessary to cope with strong space charge

Beam-Line optimization is Nowadays really a critical issue

Emittanzometro

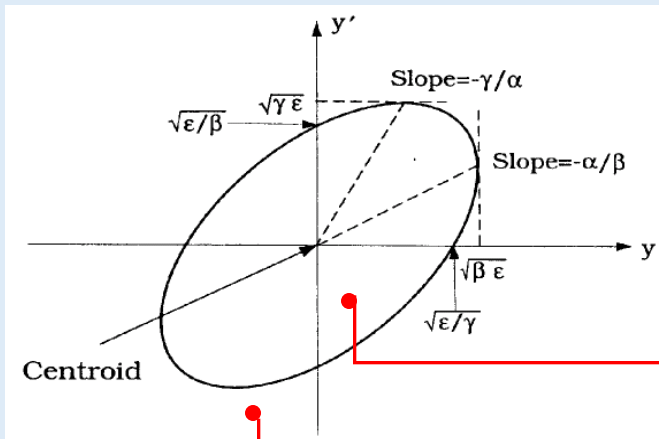
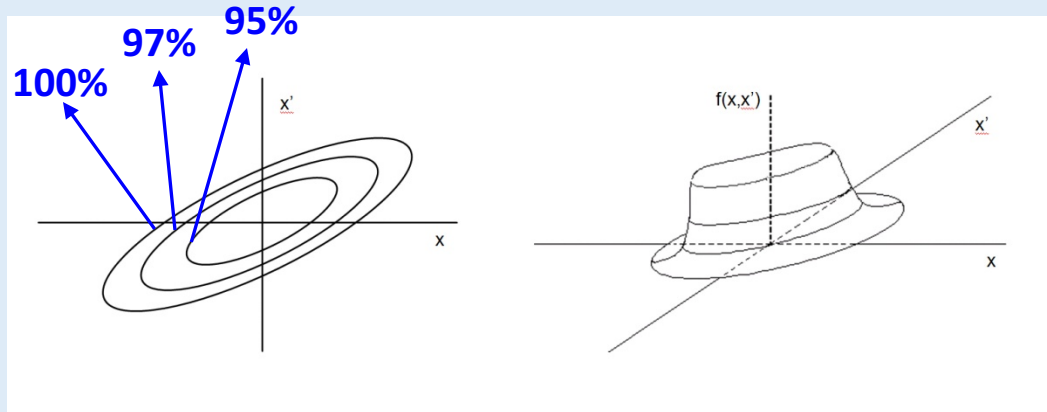
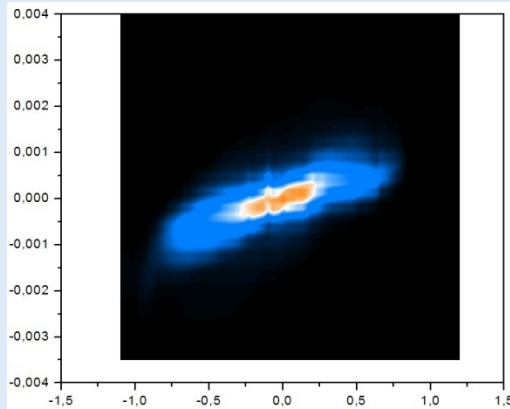
RF-Gun 1.6 S-band 120 MV/m



Emittanzometro's data are handled by a **dedicate algorithm** that return an **intensity matrix** PhaseSpace.txt (successively **interpolated** to increase the definition)

# Emittance in Real Beam

Since real beams usually do **not have well defined boundaries**, a method for calculating the emittance, is to **choose a specific density contour**, in the phase space, that represents from the **50% (worst cases)** up to the **98-99% (best cases)** of the whole bunch charge (or integrated intensity). Within this density contour and under certain conditions, such emittance satisfies the Liouville's theorem and thus is conserved



$$\gamma x^2 + \beta y^2 + 2\alpha xy = \epsilon$$

$$\gamma\beta - \alpha^2 = 1$$

$$\epsilon = \frac{\text{area}}{\pi}$$

GMESA normalization

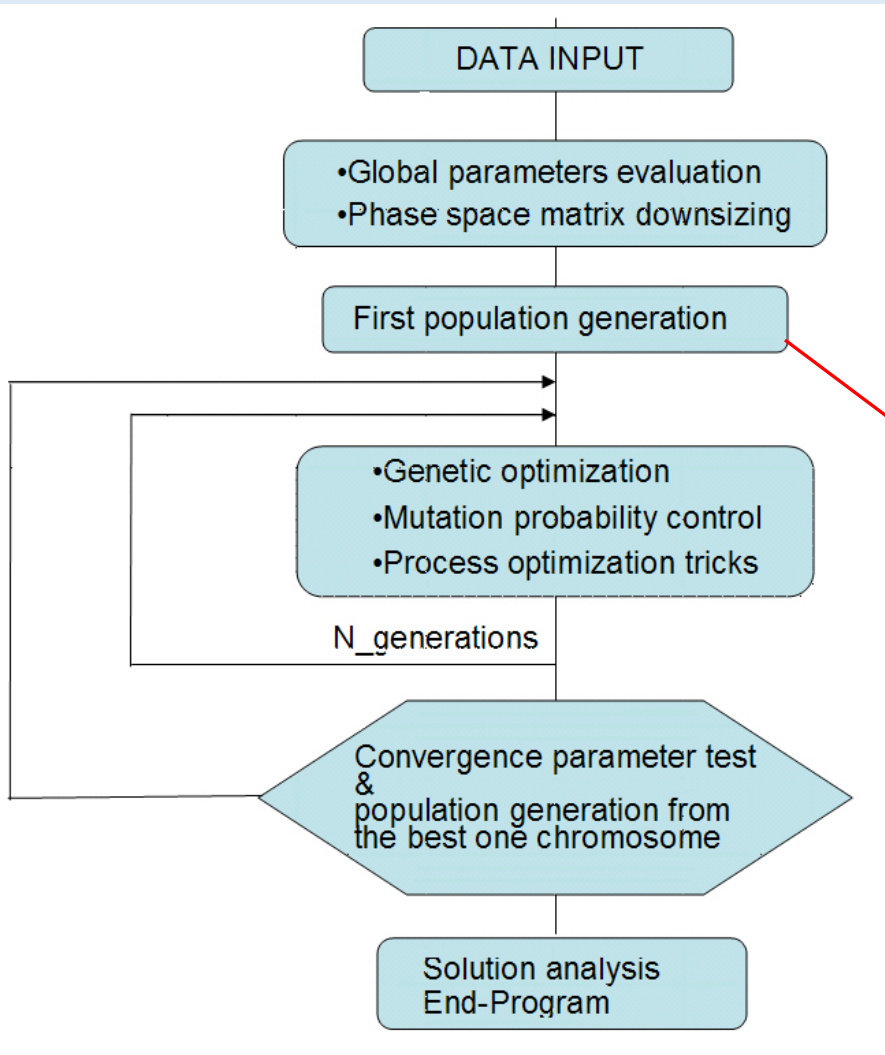
$$gx^2 + by^2 + 2axy = 1$$

$$gb - a^2 = \frac{1}{\epsilon^2}$$

$$g = \frac{\gamma}{\epsilon}, \quad b = \frac{\beta}{\epsilon}, \quad a = \frac{\alpha}{\epsilon}$$

$$gx^2 + bx'^2 + 2axx' < 1$$

$$gx^2 + bx'^2 + 2axx' > 1$$



The diagram shows an ellipse in a 2D phase space with axes  $y$  and  $y'$ . The centroid is marked with a red circle. The ellipse is defined by the equation  $gx^2 + by^2 + 2axy = 1$ . The parameters are given as  $g = \frac{\gamma}{\epsilon}$ ,  $b = \frac{\beta}{\epsilon}$ , and  $a = \frac{\alpha}{\epsilon}$ . The slopes of the major and minor axes are  $\text{Slope} = -\gamma/\alpha$  and  $\text{Slope} = \alpha/\beta$  respectively. The axes are labeled with  $\sqrt{\epsilon/\beta}$ ,  $\sqrt{\gamma\epsilon}$ ,  $\sqrt{\beta\epsilon}$ , and  $\sqrt{\epsilon/\gamma}$ .

Below the ellipse, a chromosome is shown with 25 genes. The first gene is  $c$  (green), followed by  $g$  (red),  $b$  (red),  $a$  (green),  $g$  (green),  $b$  (green), and  $a$  (green). The remaining 18 genes are represented by dots. The chromosome is divided into three segments: 1 (genes  $g, b, a$ ), 2 (genes  $g, b, a$ ), and 8 (genes  $g, b, a$ ).

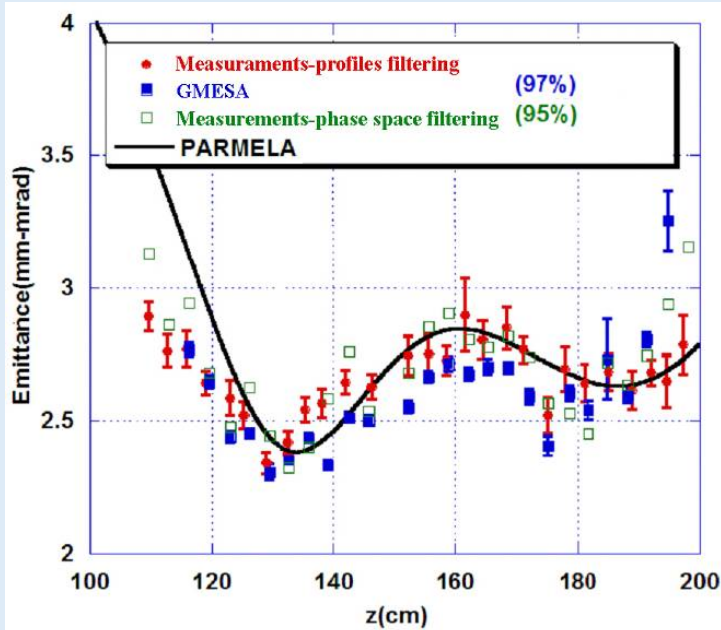
Below the chromosome, three square plots show the sampling of the ellipse. The first plot shows a dense, uniform sampling of the ellipse. The second plot shows a sparse, non-uniform sampling. The third plot shows a uniform random sampling of the ellipse.

The space phase ellipse's sampling is a thorny issue as uniformity and dimension. A shuffled uniform random generator is used.

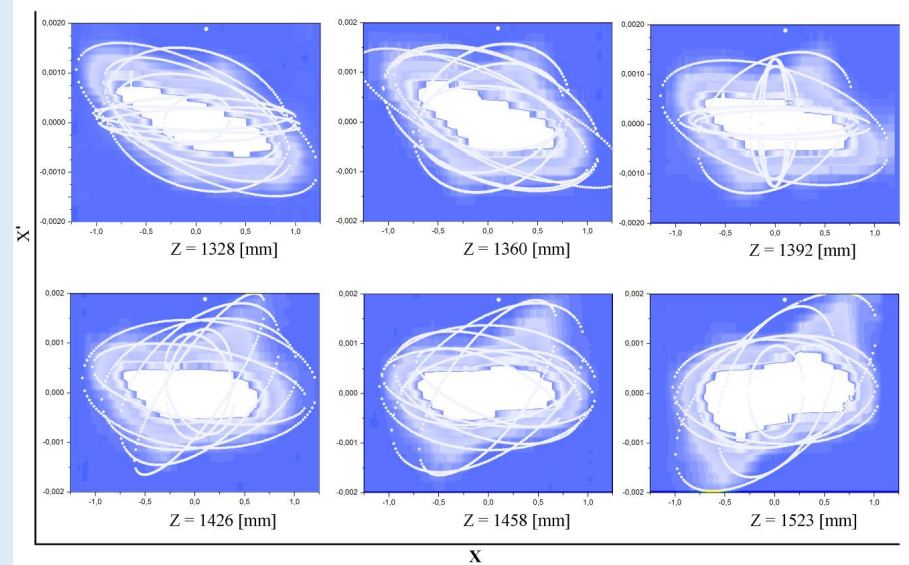
$$F_{fitness} = \frac{I}{A_d}$$

# Data analysis at SPARC - *Some relevant results*

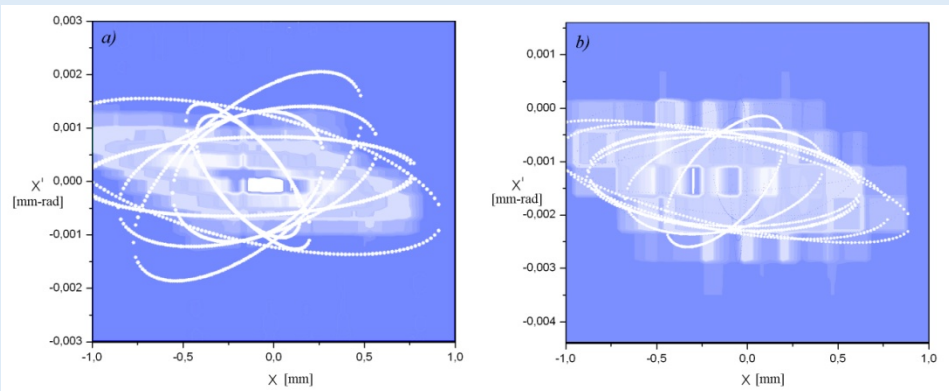
One of the more **significant curve** - analyzed also with two other methods - that shows a strongly marked **double minimum**



Some phase space of the emittance curve



From first tests the code seemed to be able to analyze the rough phase space images, not yet interpolated



## An output file

Coordinate del centro dell'ellissi:  
 $X\_c = 3.67236547E-02$   $X'\_c = 7.84265576E-05$   
 Emittanza rms al 100% della matrice centrata in 0,0= 2.23044437E-04  
 Emittanza rms al 100% della matrice centrata in  $X\_c, Y\_c = 2.23232026E-04$

EQ. ELLISSE 1 :  
 $2.01641560 * X^2 + 2 * 296.490082 * X * X' + 2428111.25 * X'^2 = 1$   
 $\gamma = 2.01641560$   $\gamma\text{-normalizzato} = 9.19580809E-04$   
 $\beta = 2428111.25$   $\beta\text{-normalizzato} = 1107.33350$   
 $\alpha = 296.490082$   $\alpha\text{-normalizzato} = 1107.33350$   
 emittanza analitica = 4.56047273E-06

EQ. ELLISSE 8 :  
 $1.98872209 * X^2 + 2 * -296.490082 * X * X' + 863863.063 * X'^2 = 1$   
 $\gamma = 1.98872209$   $\gamma\text{-normalizzato} = 1.55765051E-03$   
 $\beta = 863863.063$   $\beta\text{-normalizzato} = 676.613770$   
 $\alpha = -296.490082$   $\alpha\text{-normalizzato} = 676.613770$   
 emittanza analitica = 7.83241936E-06

Percentuale della carica raccolta= 97.0004120 %  
 Emittanza rms unione dell'ellissi - [massima stima] - non normalizzata = 2.09415637E-06 [mm-mrad]  
 Emittanza rms senza l'Area\_buio - [minima stima] - non normalizzata = 2.06715064E-06 [mm-mrad]  
 Area\_Intensita'\_nulla = 2.27432990 [% dell'Area numerica totale]  
 Area numerica= 5.23847807E-05 Emittanza numerica  $A\_num/\pi = 1.66745926E-05$  [mm-mrad]



