

# *Precision QCD for the Tevatron and LHC*

Keith Ellis

`ellis@fnal.gov`

Fermilab, CERN

# *$\beta$ function in perturbation theory*

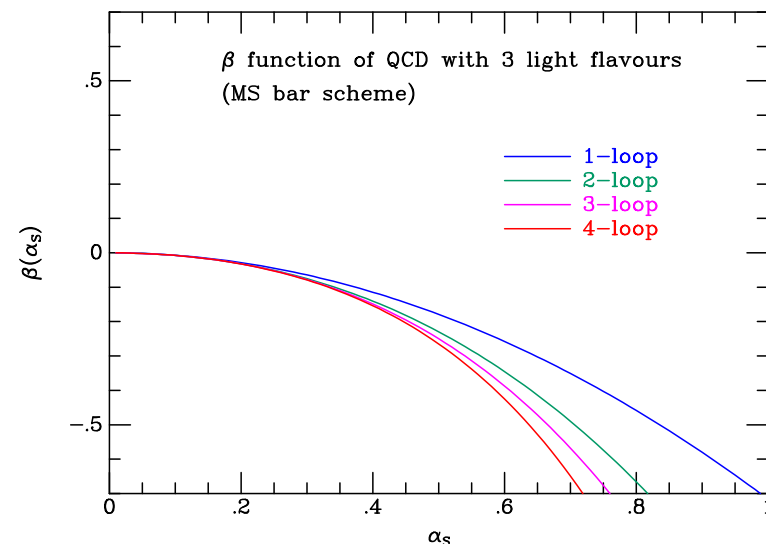
- Running of the QCD coupling  $\alpha_S$  is determined by the  $\beta$  function,
- The  $\beta$ -function of QCD is negative.

$$\beta(\alpha_S) = -b\alpha_S^2(1 + b'\alpha_S) + \mathcal{O}(\alpha_S^4)$$

$$b = \frac{(11C_A - 2n_{lf})}{12\pi}, \quad b' = \frac{(17C_A^2 - 5C_An_{lf} - 3C_Fn_{lf})}{2\pi(11C_A - 2n_{lf})},$$

where  $n_{lf}$  is number of “active” light flavors.  $b'$ , (Caswell, Jones)

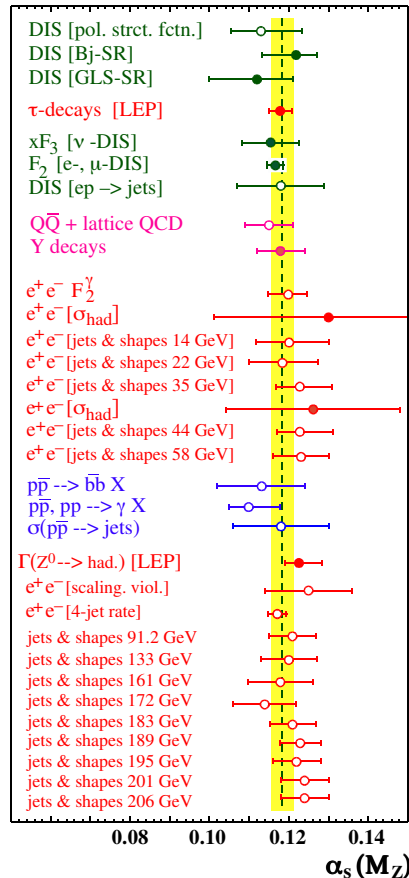
- $\beta$ -function now known up to four loops!



# Current experimental results on $\alpha_S$

Bethke, hep-ph/0407021

$$\alpha_S(M_Z) = 0.1182 \pm 0.0027, \overline{\text{MS}}, \text{NNLO}$$



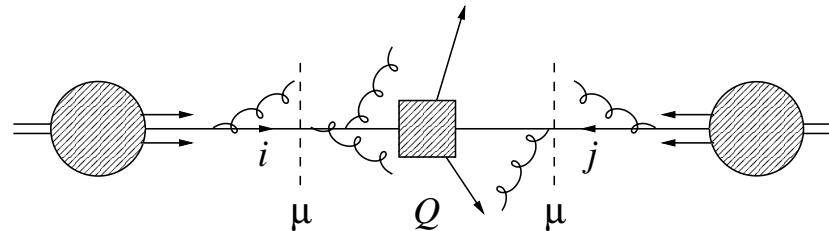
- $\alpha_S$  is large at current scales.
- Measurement  $\alpha_S$  is stable, ( $\alpha_S(M_Z) = 0.1182 \pm 0.0027$  in 2002).
- The decrease of  $\alpha_S$  is quite slow – as the inverse power of a logarithm.
- Higher order corrections are and will continue to be important.

# *The challenge*

- The challenge is to provide the most accurate information possible to experimenters working at the Tevatron and the LHC.
- Proton (anti)proton collisions give rise to a rich event structure.
- Complexity of the events will increase as we pass from the Tevatron to the LHC.
- The goals
  - ★ To provide physics software tools which are both flexible and give the most accurate representations of the underlying theories.
  - ★ To discover new efficient ways of calculating in perturbative QCD, (e.g. MHV amplitudes).

# Hadron-hadron processes

- In hard hadron-hadron scattering, constituent partons from each incoming hadron interact at short distance (large momentum transfer  $Q^2$ ).



- Form of cross section is

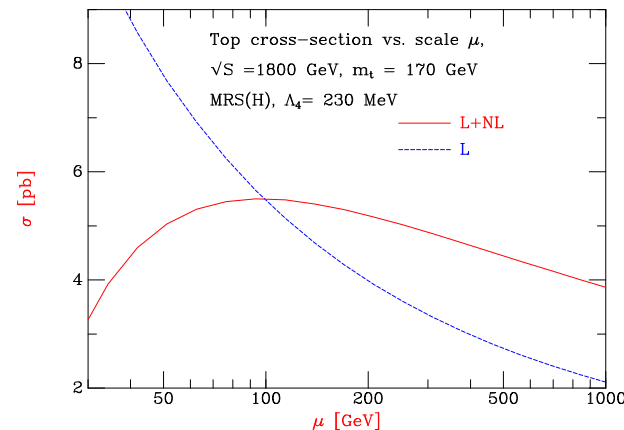
$$\frac{d\sigma}{dX} = \sum_{i,j} \sum_{\tilde{X}} \int dx_1 dx_2 f_i(x_1, \mu^2) f_j(x_2, \mu^2) \times \hat{\sigma}_{ij}^{\tilde{X}}(\alpha_S(\mu^2), Q^2, \mu^2) F(\tilde{X} \rightarrow X, \mu^2)$$

where  $\mu^2$  is factorization scale and  $\hat{\sigma}_{ij}$  is subprocess cross section for parton types  $i, j$  and  $X$  represents the hadronic final state.

## Hadron-hadron processes II

- Short distance cross section  $\hat{\sigma}_{ij}$  is calculable as a perturbation series in  $\alpha_S$ .
- Notice that factorization scale is in principle arbitrary: affects only what we call part of subprocess or part of initial-state evolution (parton shower), eg. if

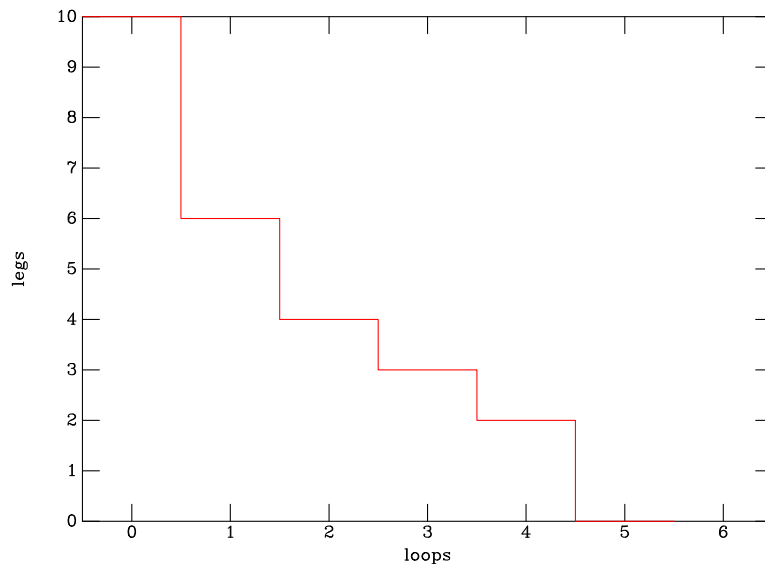
$$\sigma = q(x_1, \mu^2)q(x_2, \mu^2) \otimes [\alpha_S^2(\mu^2)f^{(0)} + \alpha_S^3(\mu^2)f^{(1)}], \quad \frac{d\sigma}{d\ln\mu^2} = O(\alpha_S^4)$$



- There are also interactions between spectator partons, leading to *soft underlying event* and/or *multiple hard scattering*. This an important issue, but I will not talk further about it.

# Many loops or many legs?

- For radiative corrections to hard processes the state of the art can calculate loops or legs, but not both.



- At LHC, trend is toward large numbers of legs.
- Most phenomenologically interesting processes involve vector bosons, leptons, missing energy, heavy flavours.
- Many processes can contribute to the same signature, argues for one (or several) unified approaches.
- NNLO desirable everywhere, but probably only available for a few specialized processes.
- For **LHC** theoretical effort should be given to multi-leg processes at one loop (NLO).

# Why NLO?

The benefits of higher order calculations are:-

- Less sensitivity to unphysical input scales (eg. renormalization and factorization scales)
- First prediction of normalization of observables at NLO
- Hence more accurate estimates of backgrounds for new physics searches.
- Confidence that cross-sections are under control for precision measurements.
- It is a necessary prerequisite for other techniques matching with resummed calculations, (eg. MC@NLO).
- More physics
  - ★ Parton merging to give structure in jets.
  - ★ Initial state radiation.
  - ★ More species of incoming partons enter at NLO.



# An experimenter's wishlist

Run II Monte Carlo Workshop

Single Boson	Diboson	Triboson	Heavy Flavour
$W+ \leq 5j$	$WW+ \leq 5j$	$WWW+ \leq 3j$	$t\bar{t}+ \leq 3j$
$W + b\bar{b} \leq 3j$	$W + b\bar{b}+ \leq 3j$	$WWW + b\bar{b}+ \leq 3j$	$t\bar{t} + \gamma+ \leq 2j$
$W + c\bar{c} \leq 3j$	$W + c\bar{c}+ \leq 3j$	$WWW + \gamma\gamma+ \leq 3j$	$t\bar{t} + W+ \leq 2j$
$Z+ \leq 5j$	$ZZ+ \leq 5j$	$Z\gamma\gamma+ \leq 3j$	$t\bar{t} + Z+ \leq 2j$
$Z + b\bar{b}+ \leq 3j$	$Z + b\bar{b}+ \leq 3j$	$ZZZ+ \leq 3j$	$t\bar{t} + H+ \leq 2j$
$Z + c\bar{c}+ \leq 3j$	$ZZ + c\bar{c}+ \leq 3j$	$WZZ+ \leq 3j$	$t\bar{b} \leq 2j$
$\gamma+ \leq 5j$	$\gamma\gamma+ \leq 5j$	$ZZZ+ \leq 3j$	$b\bar{b}+ \leq 3j$
$\gamma + b\bar{b} \leq 3j$	$\gamma\gamma + b\bar{b} \leq 3j$		single top
$\gamma + c\bar{c} \leq 3j$	$\gamma\gamma + c\bar{c} \leq 3j$		
	$WZ+ \leq 5j$		
	$WZ + b\bar{b} \leq 3j$		
	$WZ + c\bar{c} \leq 3j$		
	$W\gamma+ \leq 3j$		
	$Z\gamma+ \leq 3j$		

## A more realistic list

Les Houches workshop 2005

process ( $V \in \{Z, W, \gamma\}$ )	relevant for
★ <ol style="list-style-type: none"> <li>1. <math>pp \rightarrow V V \text{ jet}</math></li> <li>2. <math>pp \rightarrow t\bar{t} b\bar{b}</math></li> <li>3. <math>pp \rightarrow t\bar{t} + 2 \text{ jets}</math></li> <li>4. <math>pp \rightarrow V V b\bar{b}</math></li> <li>5. <math>pp \rightarrow V V + 2 \text{ jets}</math></li> <li>6. <math>pp \rightarrow V + 3 \text{ jets}</math></li> <li>7. <math>pp \rightarrow V V V</math></li> </ol>	$t\bar{t}H$ , new physics $t\bar{t}H$ $t\bar{t}H$ $\text{VBF} \rightarrow H \rightarrow VV$ , $t\bar{t}H$ , new physics $\text{VBF} \rightarrow H \rightarrow VV$ various new physics signatures SUSY trilepton

# *What is MCFM?*

- A parton-level event integrator for many processes
- Includes processes involving heavy quarks, vector and Higgs bosons, missing energy, with spin correlations in decay.
- Distributions of all variables are available.
- Most processes are included at NLO, with all the attendant benefits.
  - ★ reduced dependence on unphysical scales.
  - ★ better estimate of rates for physical processes.
  - ★ More than one parton in a jet, giving (primitive) structure to the jet.
  - ★ Better estimate than parton shower, for well separated jets, as required for the decays of heavy objects.
- Many processes included in a unified framework, allowing easy comparison

# MCFM overview

John Campbell and R.K. Ellis

- Parton level cross-sections predicted to NLO in  $\alpha_S$

$$p\bar{p} \rightarrow W^\pm / Z$$

$$p\bar{p} \rightarrow W^\pm + Z$$

$$p\bar{p} \rightarrow W^\pm + \gamma$$

$$p\bar{p} \rightarrow W^\pm + g^* (\rightarrow b\bar{b})$$

$$p\bar{p} \rightarrow W^\pm / Z + 1 \text{ jet}$$

$$p\bar{p}(gg) \rightarrow H$$

$$p\bar{p}(VV) \rightarrow H + 2 \text{ jets}$$

$$pp \rightarrow t + W$$

$$p\bar{p} \rightarrow W^+ + W^-$$

$$p\bar{p} \rightarrow Z + Z$$

$$p\bar{p} \rightarrow W^\pm / Z + H$$

$$p\bar{p} \rightarrow Z b\bar{b}$$

$$p\bar{p} \rightarrow W^\pm / Z + 2 \text{ jets}$$

$$p\bar{p}(gg) \rightarrow H + 1 \text{ jet}$$

$$p\bar{p} \rightarrow t + X$$

- ⊕ less sensitivity to  $\mu_R, \mu_F$ , rates are better normalized, fully differential distributions.
- ⊖ low particle multiplicity (no showering), no hadronization, hard to model detector effects

## References

- Calculation of the  $Wbb$  background to a  $WH$  signal at the Tevatron. R.K. Ellis, Sinisa Veseli, hep-ph/9810489.
- Vector boson pair production at the Tevatron, including all spin correlations of the boson decay products. J.M. Campbell, R.K. Ellis, hep-ph/9905386.
- Calculation of the  $Zbb$  and other backgrounds to a  $ZH$  signal at the Tevatron. J.M. Campbell, R.K. Ellis, hep-ph/0006304.
- Next-to-leading order corrections to  $W+2$  jet and  $Z+2$  jet production at hadron colliders. John Campbell, R.K. Ellis, hep-ph/0202176.
- Higgs Boson Production in Association with a Single Bottom Quark. J. Campbell, R.K. Ellis, F. Maltoni, S. Willenbrock, hep-ph/0204093.
- Next-to-Leading Order QCD Predictions for  $W+2$  jet and  $Z+2$  jet Production at the CERN LHC. J. Campbell, R.K. Ellis and D. Rainwater, hep-ph/0308195.
- Associated Production of a  $Z$  Boson and a Single Heavy Quark Jet. J. Campbell, R.K. Ellis, F. Maltoni, S. Willenbrock, hep-ph/0312024.
- Single top production and decay at next-to-leading order, J. Campbell, R.K. Ellis and F. Tramontano, hep-ph/0408158.
- Next-to-leading order corrections to  $WT$  production and decay, J. Campbell, and F. Tramontano, hep-ph/0506289.
- J. Campbell, R. K. Ellis, F. Maltoni and S. Willenbrock, Production of a  $Z$  boson and two jets with one heavy-quark tag, hep-ph/0510362.

## Shortcomings of MCFM

- No attachment of parton shower, (cf MC@NLO) Webber, Frixione ...), (but, NLO is a necessary prerequisite for MC@NLO)
- No hadronization model, so hard to model detector effects.
- No inclusion of pure QCD processes, such as  $gg \rightarrow gg, gg \rightarrow ggg, gg \rightarrow gggg$ , (cf NLOJet++) Nagy, Giele, Kilgore
- Weighted events

## MCFM v. 5.1

- MCFM v.5.1 released June 1st, 2006
- Available for download at <http://mcfm.fnal.gov>
- Processes added in NLO, ( $f \equiv q, \bar{q}, g$ , generic parton)

$$f + f \rightarrow W^{\pm} + t$$

$$f + b \rightarrow Z^0 + b + f$$

$$f + c \rightarrow Z^0 + c + f$$

- Processes added in LO

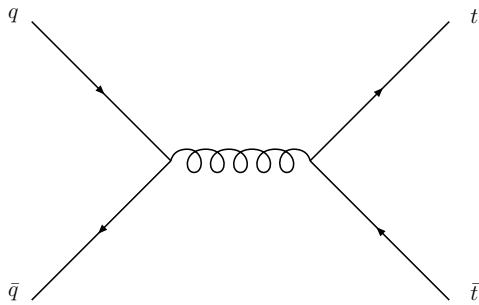
$$f + f \rightarrow Z^0(\rightarrow e^{-} + e^{+}) + c + c$$

$$f + f \rightarrow t\bar{t} + g$$

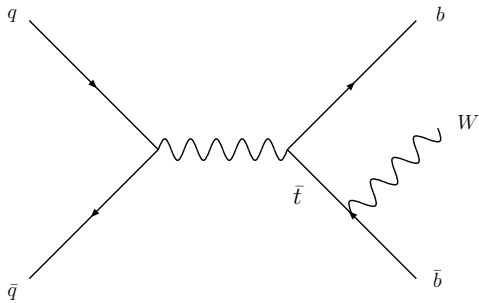
$$f + f \rightarrow H + f + f + f[\text{in heavy top limit}]$$

$$f + f \rightarrow W^{-}(\rightarrow e^{-} + \nu) + t + b[\text{massive } b]$$

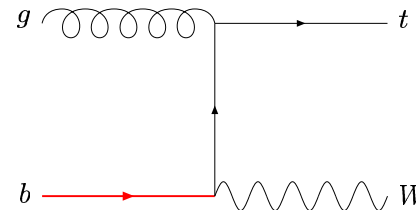
# Top production rates



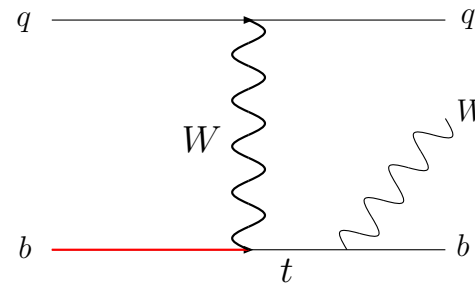
6 pb  
720 pb



0.8 pb  
10 pb



0.14 pb  
66 pb

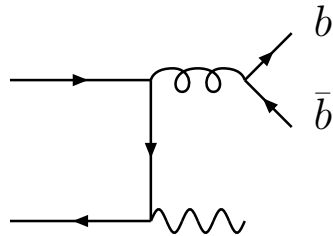


1.8 pb  
240 pb

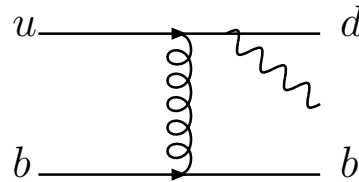
- All cross-sections are known to NLO (Tevatron / LHC)
- The total single top cross-section is smaller than the  $t\bar{t}$  rate by about a factor of two, at both machines



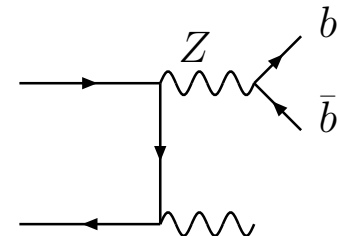
# Backgrounds for single top



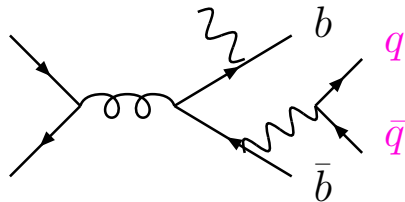
30



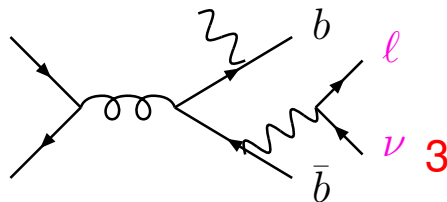
11



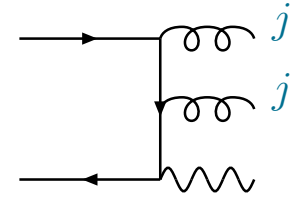
3



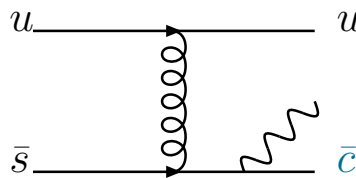
6



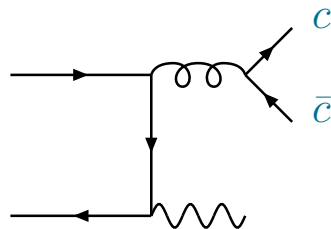
3



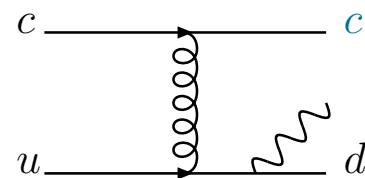
35



19



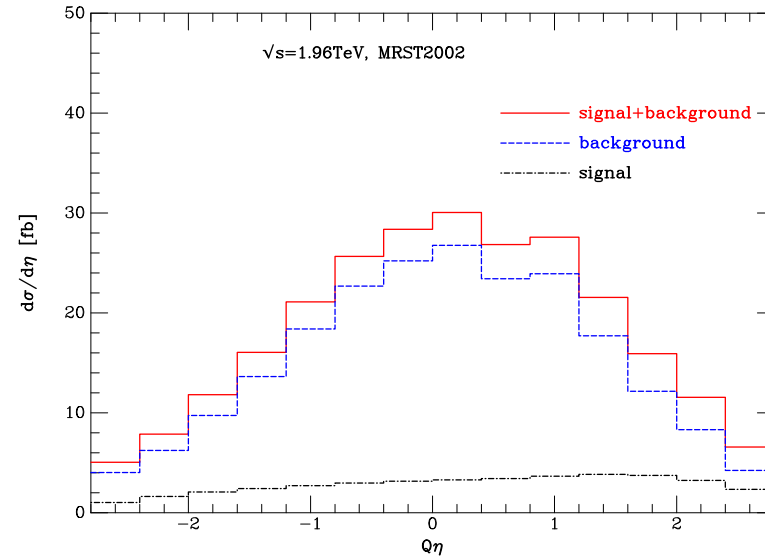
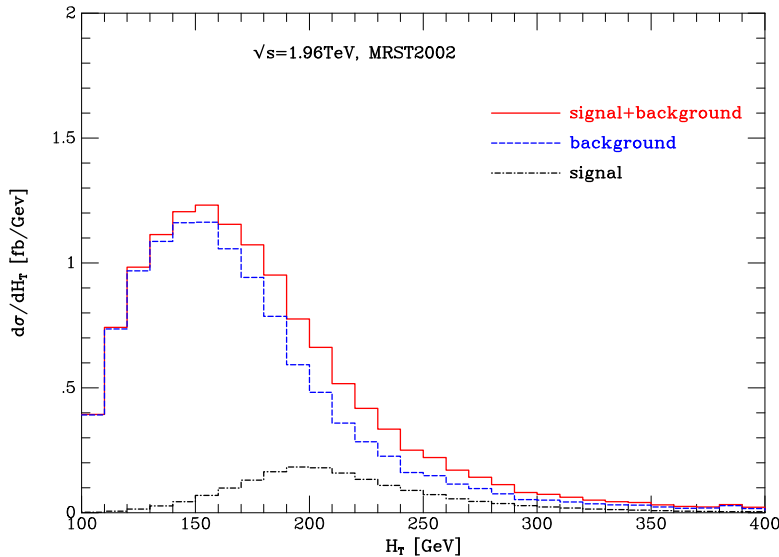
6



3

- Cross-sections in fb include nominal tagging efficiencies and mis-tagging/fake rates. Calculated with MCFM, most at NLO at  $\sqrt{S} = 2$  TeV.
- Rates are 7 fb and 11 fb for  $s$ - and  $t$ -channel signal

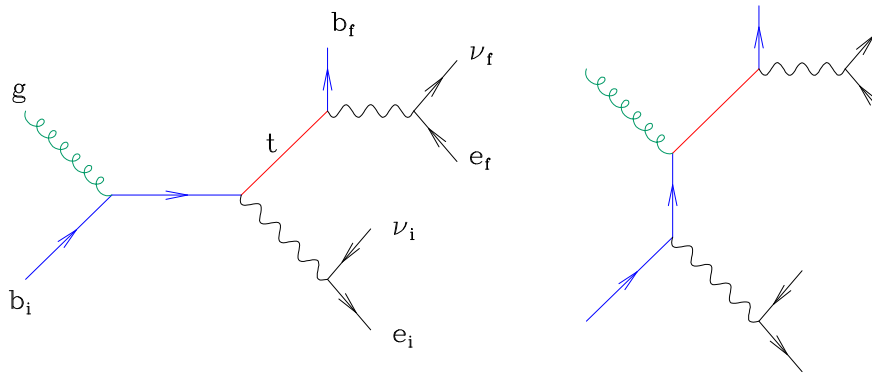
# Single top signal vs. backgrounds



- $H_T$  = scalar sum of jet, lepton and missing  $E_T$
- $Q_\eta$  is the product of the lepton charge and the rapidity of the untagged jet, useful for picking out the  $t$ -channel process
- Signal:Background (with our nominal efficiencies) is about 1 : 6.
- it will take  $1.5 \text{ fb}^{-1}$  to have evidence ( $3\sigma$ ) for single top from a single experiment at the Tevatron (Gresele, Moriond 2006).

# *Wt production*

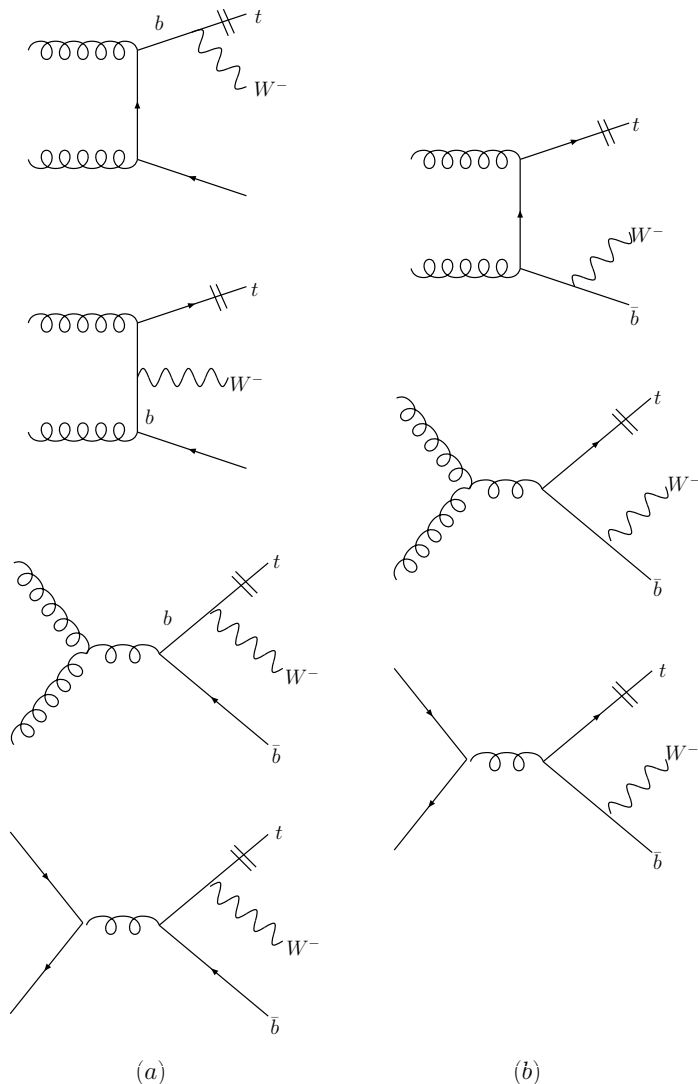
Campbell, Tramontano



- Rate depends on  $b$ -quark distribution.
- Top quark, (shown in red) is taken onshell, but all spin correlations are retained.
- Including real radiation we obtain both diagrams with and without a resonant  $\bar{t}$  propagator.
- The former are properly considered as contributions to  $t\bar{t}$  production, whereas the latter are contributions to single top production.

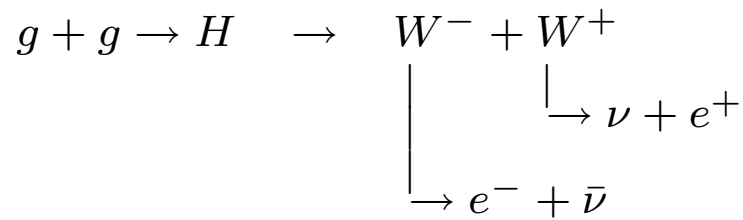
- The last of the single top processes.
- $Wt$  process important at LHC, negligible at Tevatron.

# Separation of $Wt$ and $t\bar{t}$ diagrams

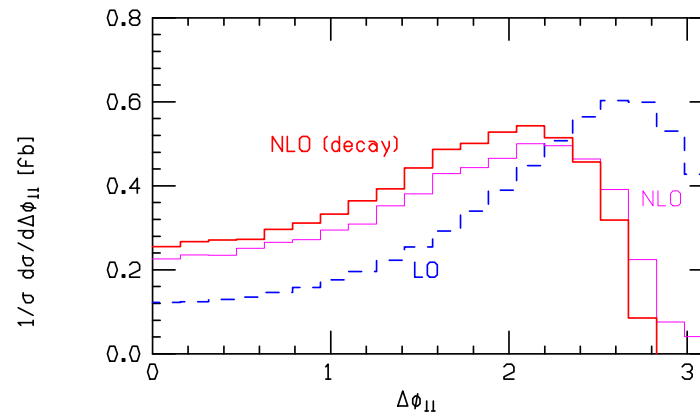
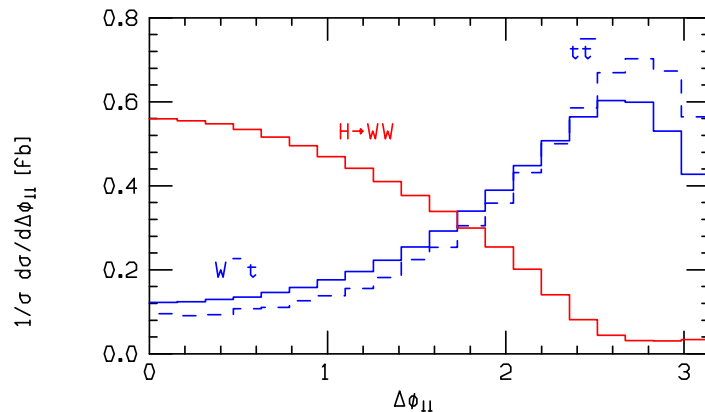


- diagrams (a) are "genuine" single top contributions, whereas diagrams (b) contain doubly resonant propagators.
- Apply a veto on the  $p_T$  of the additional  $\bar{b}$  quark which appears in NLO.
- Choose factorization scale  $\mu_F$  of the same order as the maximum  $p_T$  which is allowed.
- When the  $p_T > \mu_F$  doubly resonant diagrams dominate and a better description is obtained by using the  $t\bar{t}$  process.

# *$Wt$ background to $H \rightarrow WW^*$*



Process	$\sigma$ [fb]
$H \rightarrow WW(m_H = 155 \text{ GeV})$	58.1
continuum $WW$	270.5
$t\bar{t}$	43.9
$Wt$	40.1



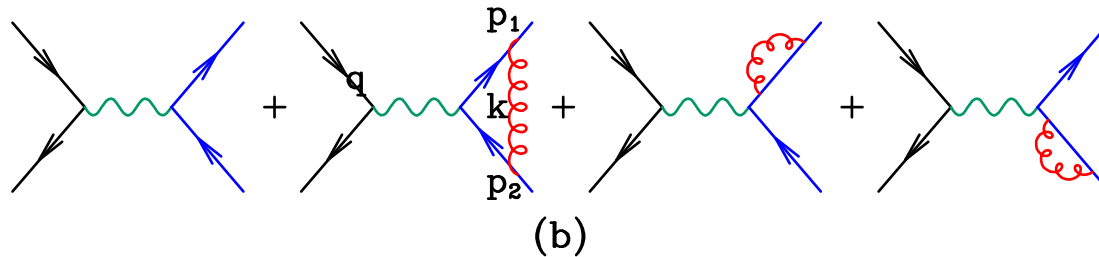
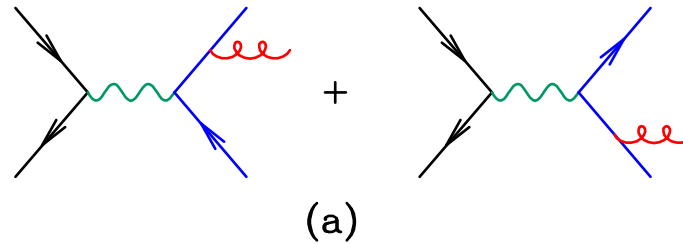
- $t\bar{t}$  and  $Wt$  backgrounds are of similar size.
- Shape of contribution of  $Wt$  process to Dittmar-Dreiner angle modified at NLO

## *Automatic NLO corrections*

- What is needed is an automatic procedure to calculate NLO corrections (MadLoop?).
- Current stumbling block is the calculation of virtual corrections.
- The virtual corrections contain singularities from the regions of collinear and soft gluon emission, (and in general also UV divergences).
- Divergences are normally controlled by dimensional regularization. A completely numerical procedure using, say, a gluon mass could cause problems with gauge invariance and is hence deprecated.

## Example: $e^+e^-$ total rate

- Consider the corrections to total  $e^+e^- \rightarrow q\bar{q}$  rate.



$$\sigma^{q\bar{q}g} = 2\sigma_0 \frac{\alpha_S}{\pi} H(\epsilon) \left[ \frac{2}{\epsilon^2} + \frac{3}{\epsilon} + \frac{19}{2} - \pi^2 + \mathcal{O}(\epsilon) \right].$$

- Soft and collinear singularities in real emission amplitudes (a) are regulated, appearing instead as poles at  $D = 4$ .

## *Virtual gluon contributions*

- Virtual gluon contributions (b): using dimensional regularization again

$$\sigma^{q\bar{q}} = 3\sigma_0 \left\{ 1 + \frac{2\alpha_S}{3\pi} H(\epsilon) \left[ -\frac{2}{\epsilon^2} - \frac{3}{\epsilon} - 8 + \pi^2 + \mathcal{O}(\epsilon) \right] \right\} .$$

- Adding real and virtual contributions, poles cancel and result is finite as  $\epsilon \rightarrow 0$ .  $R$  is an infrared safe quantity.

$$R = 3 \sum_q Q_q^2 \left\{ 1 + \frac{\alpha_S}{\pi} + \mathcal{O}(\alpha_S^2) \right\} .$$

- However the virtual corrections to  $W^+ \rightarrow u\bar{d}gggg$  are not so easily calculated.



## Historical perspective

We want to consider tensor integrals of the form

$$I^{\mu_1 \dots \mu_M} = \int \frac{d^D l}{i\pi^{D/2}} \frac{l^{\mu_1} \dots l^{\mu_M}}{d_1 d_2 \dots d_N}$$

where  $d_i = (l + \sum_{j=1}^{j=i} p_j)^2$  are the standard propagator factors.

Passarino and Veltman (1979) wrote a form factor expansion for one-loop integrals, with  $M \leq N$ ,  $N \leq 4$ . For example,

$$\int \frac{d^D l}{i\pi^{D/2}} \frac{l^\mu}{l^2(l+p_1)^2(l+p_1+p_2)^2} = C_1(p_1, p_2) p_1^\mu + C_2(p_1, p_2) p_2^\mu$$

Contracting with  $p_1$  and  $p_2$  and using the identities

$$l \cdot p_1 = \frac{1}{2}[(l+p_1)^2 - l^2 - p_1^2], l \cdot p_2 = \frac{1}{2}[(l+p_1+p_2)^2 - (l+p_1)^2 - p_2^2 - 2p_1 \cdot p_2]$$

## Historical perspective II

We derive a linear equation expressing  $C_1, C_2$  in terms of scalar integrals

$$\begin{pmatrix} 2p_1 \cdot p_1 & 2p_1 \cdot p_2 \\ 2p_2 \cdot p_1 & 2p_2 \cdot p_2 \end{pmatrix} \begin{pmatrix} C_1 \\ C_2 \end{pmatrix} = \begin{pmatrix} R_1 \\ R_2 \end{pmatrix}$$

where  $R_1 = [B_0(p_1 + p_2) - B_0(p_2) - p_1^2 C_0(p_1, p_2)]$

and  $R_2 = [B_0(p_1) - B_0(p_1 + p_2) - (p_2^2 + 2p_1 \cdot p_2) C_0(p_1, p_2)]$

$$C_0(p_1, p_2) = \int [dl] \frac{1}{l^2(l+p_1)^2(l+p_1+p_2)^2}, B_0(p_1) = \int [dl] \frac{1}{l^2(l+p_1)^2}$$

Solution involves the inverse of the Gram matrix,  $G_{ij} \equiv 2p_i \cdot p_j$

$$G^{-1} = \begin{pmatrix} +p_2 \cdot p_2 & -p_1 \cdot p_2 \\ -p_1 \cdot p_2 & +p_1 \cdot p_1 \end{pmatrix} / [2(p_1 \cdot p_1 p_2 \cdot p_2 - (p_1 \cdot p_2)^2)]$$

## *Historical perspective III*

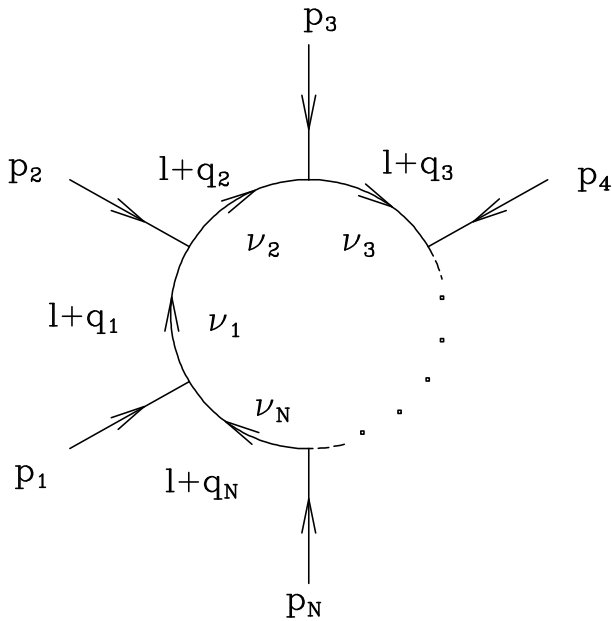
- M. Veltman wrote a CDC program for numerical evaluation of the formfactors in processes with only UV divergences, Utrecht (1979).
- He dealt with exceptional regions, (e.g. regions where the Gram determinant vanishes), by implementing parts of the program in quadruple precision.
- Translation and improvement by Van Oldenborgh (1990) and further work on interface by T. Hahn and M. Perez-Victoria (1998).

However this is not sufficient for our needs.

- We are interested in processes with more than 4 external legs.
- We are often interested in loop processes with collinear and soft singularities due to the presence of massless particles. These are most commonly (and elegantly) controlled by dimensional regularization.

# Recursion relations I

Define generalized scalar integrals



$$d_i \equiv (l + q_i)^2$$

$$q_i \equiv \sum_{j=1}^i p_j$$

$$q_N \equiv \sum_{j=1}^N p_j = 0,$$

$$I(D; \nu_1, \nu_2, \dots, \nu_N) = I(D; \{\nu_k\}_{k=1}^N) \equiv \int \frac{d^D l}{i\pi^{D/2}} \frac{1}{d_1^{\nu_1} d_2^{\nu_2} \dots d_N^{\nu_N}},$$

# Form-factor expansion

Davydchev

- For form factor expansion in terms of the  $q$ 's the coefficients are generalized scalar integrals in shifted dimensionalities
- e.g., the rank-1 and rank-2 tensor integrals with  $N$  external legs can be decomposed as

$$\begin{aligned} I^{\mu_1}(D; q_1, \dots, q_N) &= \sum_{i_1=1}^N I(D+2; \{1 + \delta_{i_1 k}\}_{k=1}^N) q_{i_1}^{\mu_1} \\ &= I(D+2; 2, 1, 1, \dots, 1) q_1^{\mu_1} + I(D+2; 1, 2, 1, \dots, 1) q_2^{\mu_1} \\ &+ \dots + I(D+2; 1, 1, 1, \dots, 2) q_N^{\mu_1} . \\ I^{\mu_1 \mu_2}(D; q_1, \dots, q_N) &= -\frac{1}{2} I(D+2; 1, 1, 1, \dots, 1) g^{\mu_1 \mu_2} \\ &+ 2 I(D+4; 3, 1, 1, \dots, 1) q_1^{\mu_1} q_1^{\mu_2} \\ &+ I(D+4; 2, 2, 1, \dots, 1) (q_1^{\mu_1} q_2^{\mu_2} + q_1^{\mu_2} q_2^{\mu_1}) + \dots \end{aligned}$$

## Recursion relations II

Using integration by parts methods we derive the basic recursion relation

$$\begin{aligned} & (\nu_l - 1) I(D; \{\nu_k\}_{k=1}^N) \\ &= - \sum_{i=1}^N S_{li}^{-1} I(D - 2; \{\nu_k - \delta_{ik} - \delta_{lk}\}_{k=1}^N) \\ & - b_l (D - \sigma) I(D; \{\nu_k - \delta_{lk}\}_{k=1}^N). \end{aligned}$$

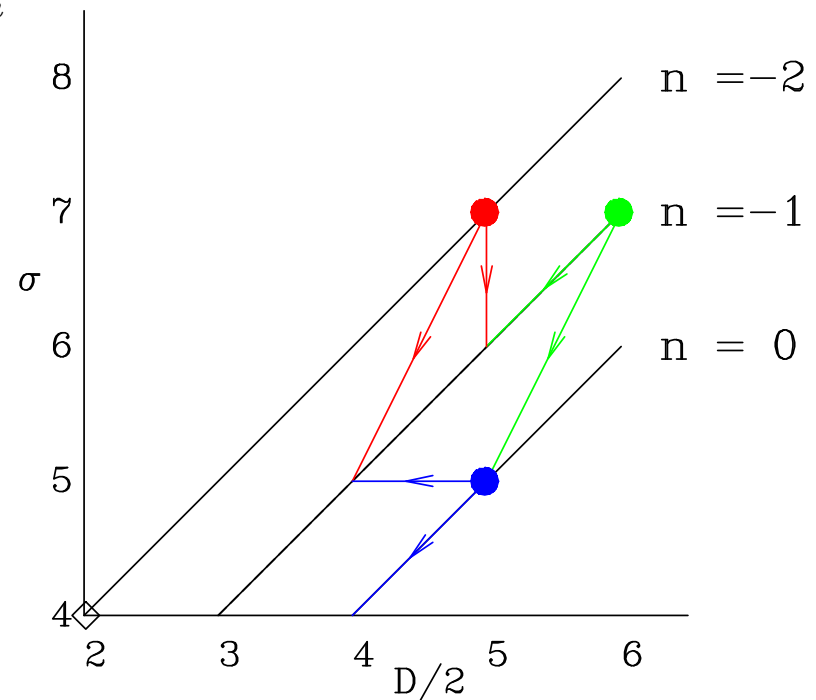
$$\sigma \equiv \sum_{i=1}^N \nu_i; \quad b_i \equiv \sum_{j=1}^N S_{ij}^{-1}; \quad B \equiv \sum_{i=1}^N b_i = \sum_{i,j=1}^N S_{ij}^{-1}.$$

The strategy is to reduce more complicated integrals to a set of simpler basis integrals which are known analytically.

Hence the method is seminumerical.

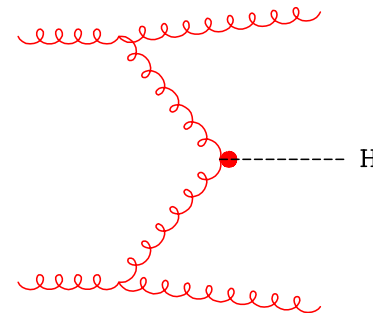
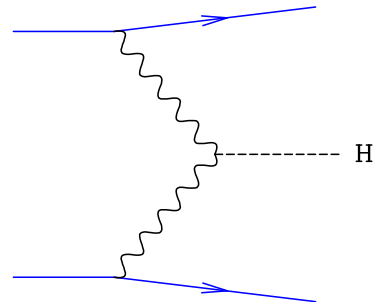
## Recursion relations (cont)

- Example: reduction of boxes,  $\sigma = \sum_i \nu_i$



- Using the basic identity (red lines) and other subsidiary identities (blue and green lines) one can always arrive at the basis integral, (four-dimensional box), denoted by a diamond, (or integrals with fewer external legs).

## *H+2 jet calculation*



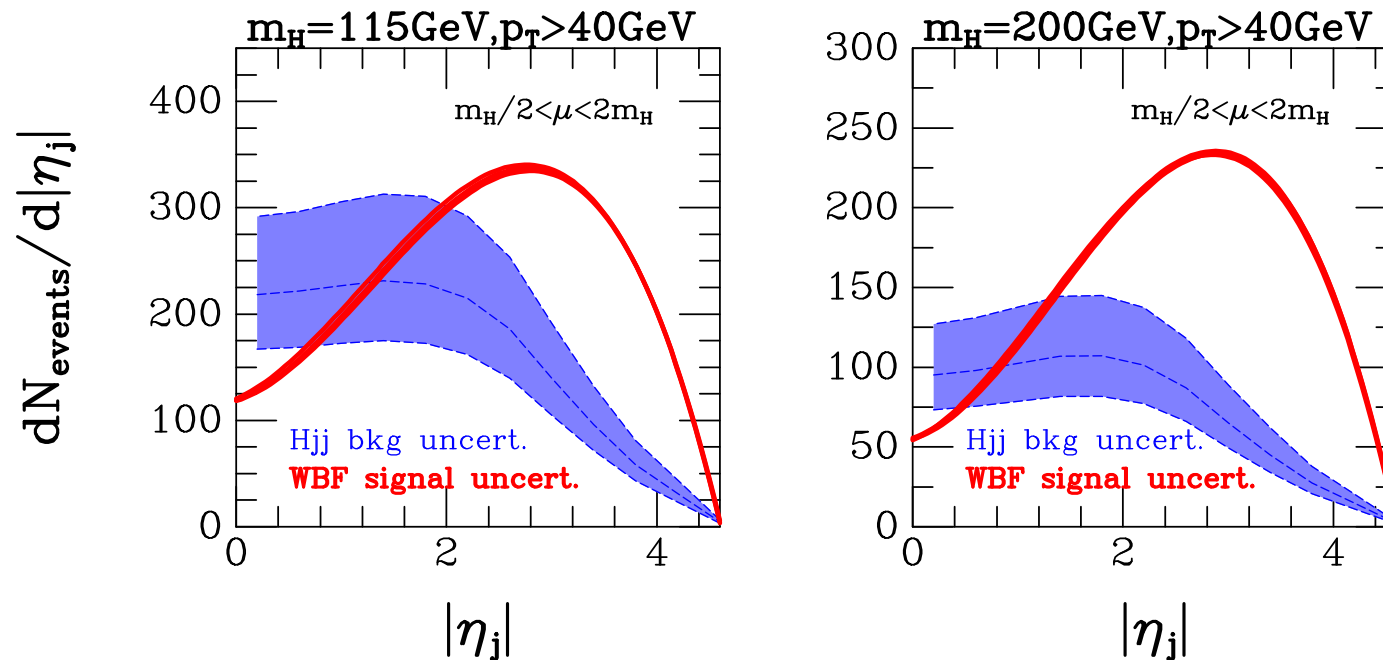
- NLO corrections to  $W$ -fusion mechanism already calculated by many authors.
- All the elements are in place for a full NLO Higgs + 2 jets calculation via gluon fusion mechanism
  - ★ Born level calculation Higgs + 4 partons
  - ★ Real calculation Higgs + 5 partons, Del Duca et al, Dixon et al, Badger et al
  - ★ Virtual calculation Ellis, Giele and Zanderighi, presented here
  - ★ Subtraction terms Campbell, Ellis and Zanderighi, in preparation



# Comparison of signal and “background”

- Large uncertainty in blue curves because NLO correction not included.

Berger, Campbell



# Proof of principle

Ellis, Giele, Zanderighi

Use the effective theory ( $m_t \rightarrow \infty$ ) for  $Hgg$  coupling

$$\mathcal{L}_{\text{eff}} = \frac{1}{4} A(1 + \Delta) H G_{\mu\nu}^a G^{a\mu\nu}.$$

$G_{\mu\nu}^a$  is the field strength of the gluon field and  $H$  is the Higgs-boson field,  $A = \frac{g^2}{12\pi^2 v}$  where  $g$  is the bare strong coupling and  $v$  is the vacuum expectation value parameter,  $v^2 = (G_F \sqrt{2})^{-1} = (246 \text{ GeV})^2$ .  $\Delta$  is a finite correction. Calculate virtual corrections to

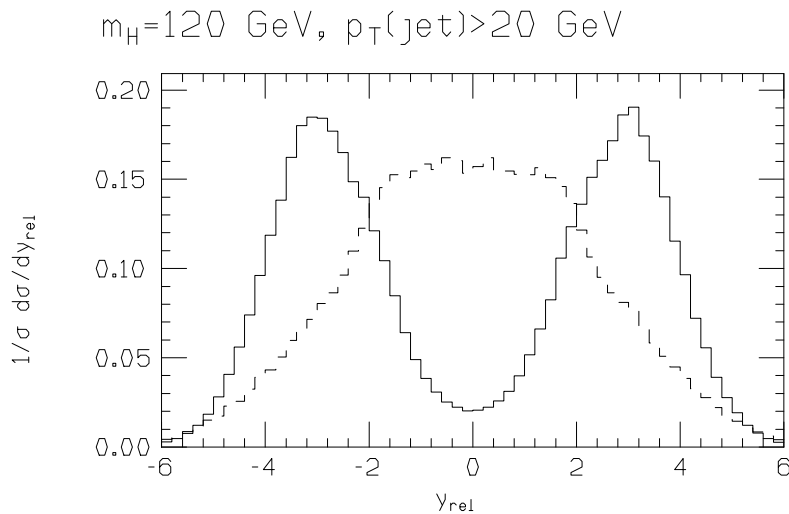
- A)  $H \rightarrow q\bar{q}q'\bar{q}'$ , (30 diagrams),
- B)  $H \rightarrow q\bar{q}q\bar{q}$ , (60 diagrams),
- C)  $H \rightarrow q\bar{q}gg$ , (191 diagrams),
- D)  $H \rightarrow gggg$ , (739 diagrams).

# Comparison of numerical and analytic results for $H \rightarrow \text{four partons}$

	$\frac{1}{\epsilon^2}$	$\frac{1}{\epsilon}$	1
$A_B$	0	0	12.9162958212387
$A_{V,N}$	-68.8869110466063	-114.642248172519	120.018444115458
$A_{V,A}$	-68.8869110466064	-114.642248172523	120.018444115429
$B_B$	0	0	858.856417157052
$B_{V,N}$	-4580.56755817094	-436.142317955208	26470.9608978350
$B_{V,A}$	-4580.56755817099	-436.142317955660	26470.9608978346
$C_B$	0	0	968.590160211857
$C_{V,N}$	-8394.44805516930	-19808.0396331354	-1287.90574949112
$C_{V,A}$	-8394.44805516942	-19808.0396331363	not known analytically
$D_B$	0	0	3576991.27960852
$D_{V,N}$	$-4.29238953553022 \cdot 10^7$	$-1.04436372655580 \cdot 10^8$	$-6.79830911471604 \cdot 10^7$
$D_{V,A}$	$-4.29238953553022 \cdot 10^7$	$-1.04436372655580 \cdot 10^8$	not known analytically

# Higgs+ 3 jets at LO

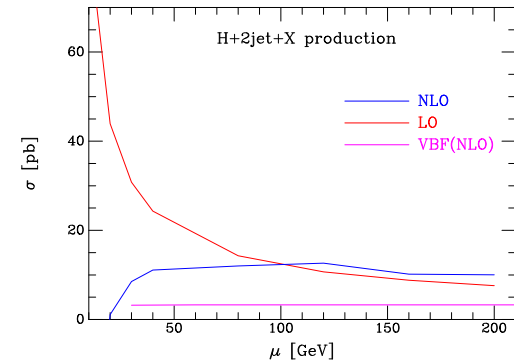
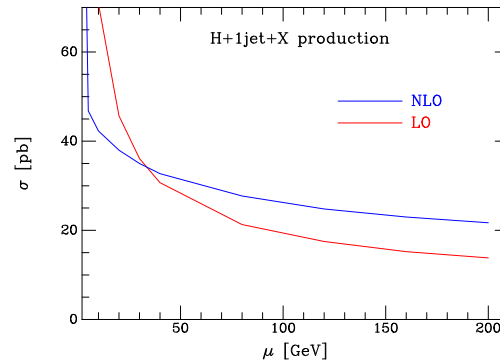
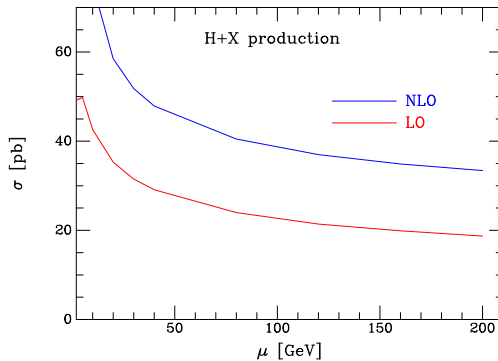
- Implementation of  $gg \rightarrow Hggg$  + other diagrams.
- Distribution of the rapidity of the third jet,  $y_{j_3}$  measured with respect to the rapidity average of the tagging jets.  $y_{rel} = y_{j_3} - (y_{j_1} + y_{j_2})/2$  cf, Del Duca, Frizzo, Maltoni



- $|y_{j_1} - y_{j_2}| > 4.2,$   
 $y_{j_1} \cdot y_{j_2} < 0,$   
 $m_{jj} > 600 \text{ GeV}$
- Rapidity of third jet in Vector-boson fusion (solid line) closer to tagging jets than in gluon fusion (dotted line).

## *H+2 jet results*

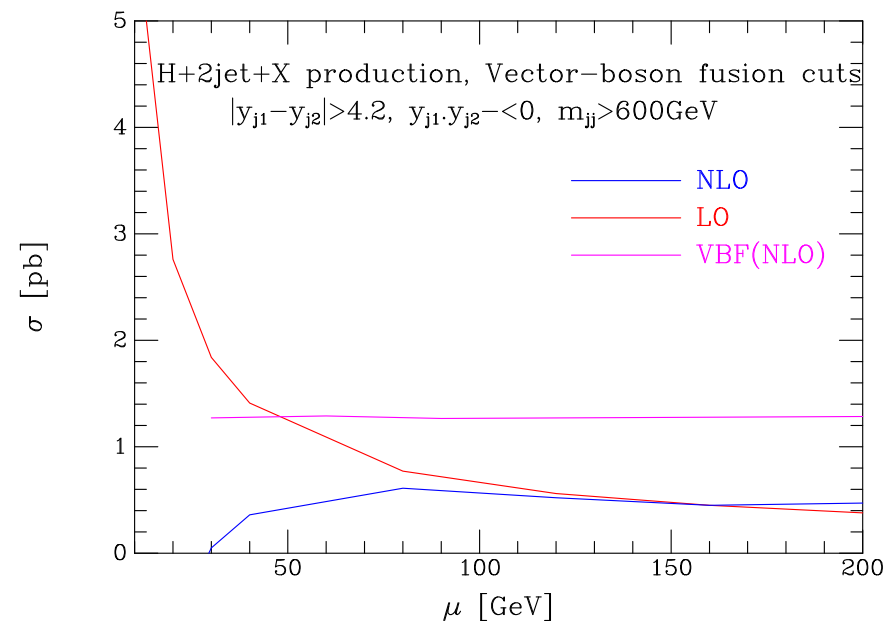
- Define jets with  $p_t(jet) > 20 \text{ GeV}$ ,  $|y_j| < 5$ ,  $R_{jj} > 0.6$
- We vary renormalization and factorization scale together.



- H + 0jet, H + 1 jet inclusive results from MCFMv5.0
- Our preliminary results indicate the Higgs + 2 jet inclusive rate is the better behaved at NLO than the rate for Higgs+X rate, or Higgs + 1 jet+X.
- Suggests that a relatively high scale  $\mu \sim m_H$  is appropriate for the Higgs.
- NNLO known for Higgs + X, Harlander+Kilgore, Anastasiou+Melnikov

## *H+2 jet results, continued*

- When we impose cuts to enhance vector boson fusion, (without central jet veto) we obtain a similar pattern
- Too early to comment on particular parton subprocesses, individual contributions, separated factorization and normalization scale dependence.



# Conclusions

- A serious program is underway to calculate NLO corrections to SM processes, relevant for LHC physics. MCFM is a beginning, but it is clearly not enough.
- Release of MCFM version 5.1, new processes,  $pp \rightarrow Wt$ ,  $pp \rightarrow Zbj$ , bug fixes, general housekeeping, (available at [mcfm.fnal.gov](http://mcfm.fnal.gov))
- Benefits of a unified approach are beginning to be seen. Calculation of signal and background in same program, e.g. for single top.
- Preliminary results for Higgs + 2 jets at NLO indicate
  - ★ a good prediction and stable result for H+2jets
  - ★ viability of seminumerical method