

# **Polarization issues in Novosibirsk c-tau factory**

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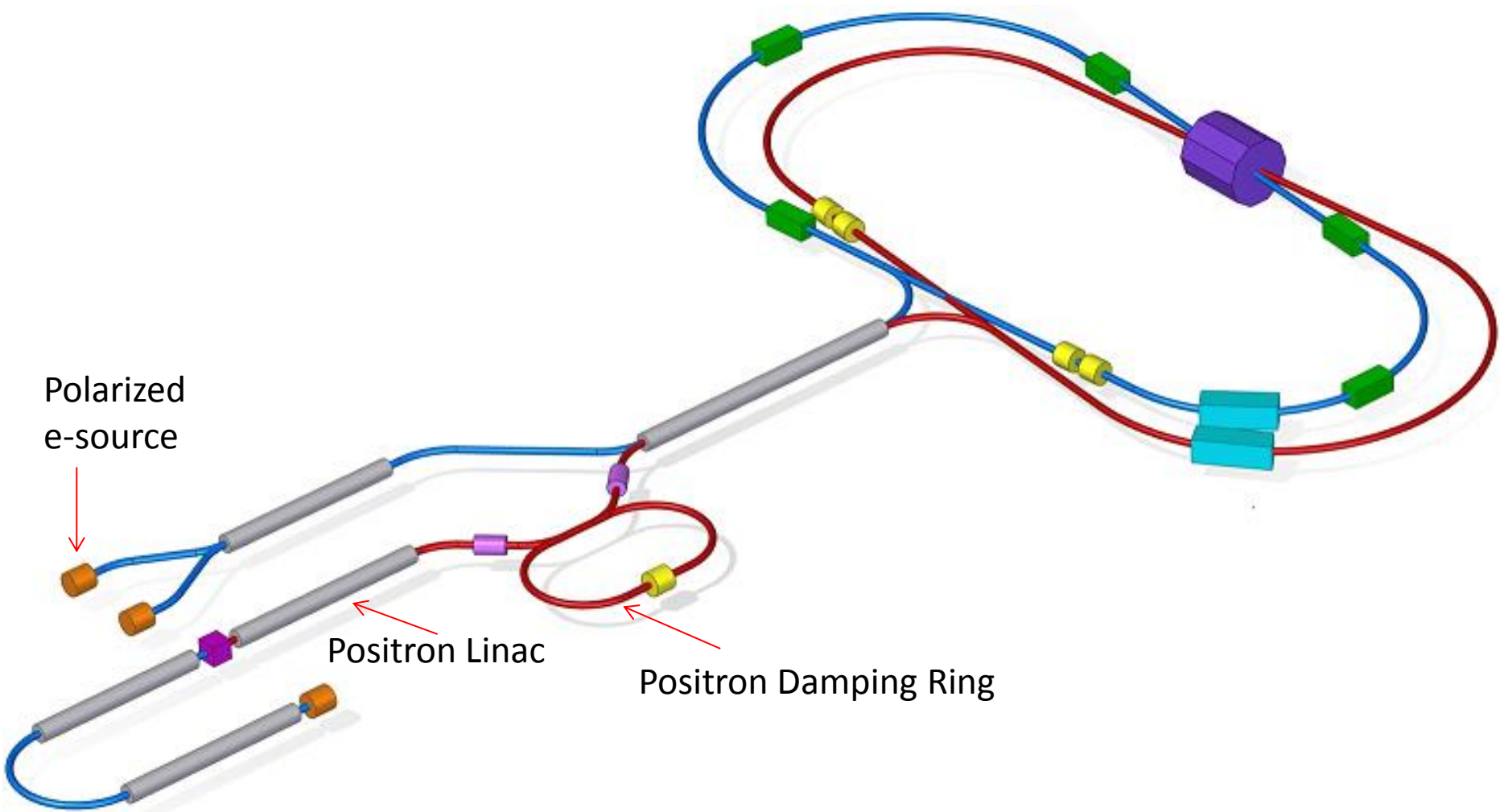
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# Outline

- C-tau complex with the longitudinally polarized electrons.
- Siberian Snakes Concept.
- Radiative self-polarization processes. Formulae Derbenev - Kondratenko.
- Few options with different number of snakes.
- Results and conclusion.

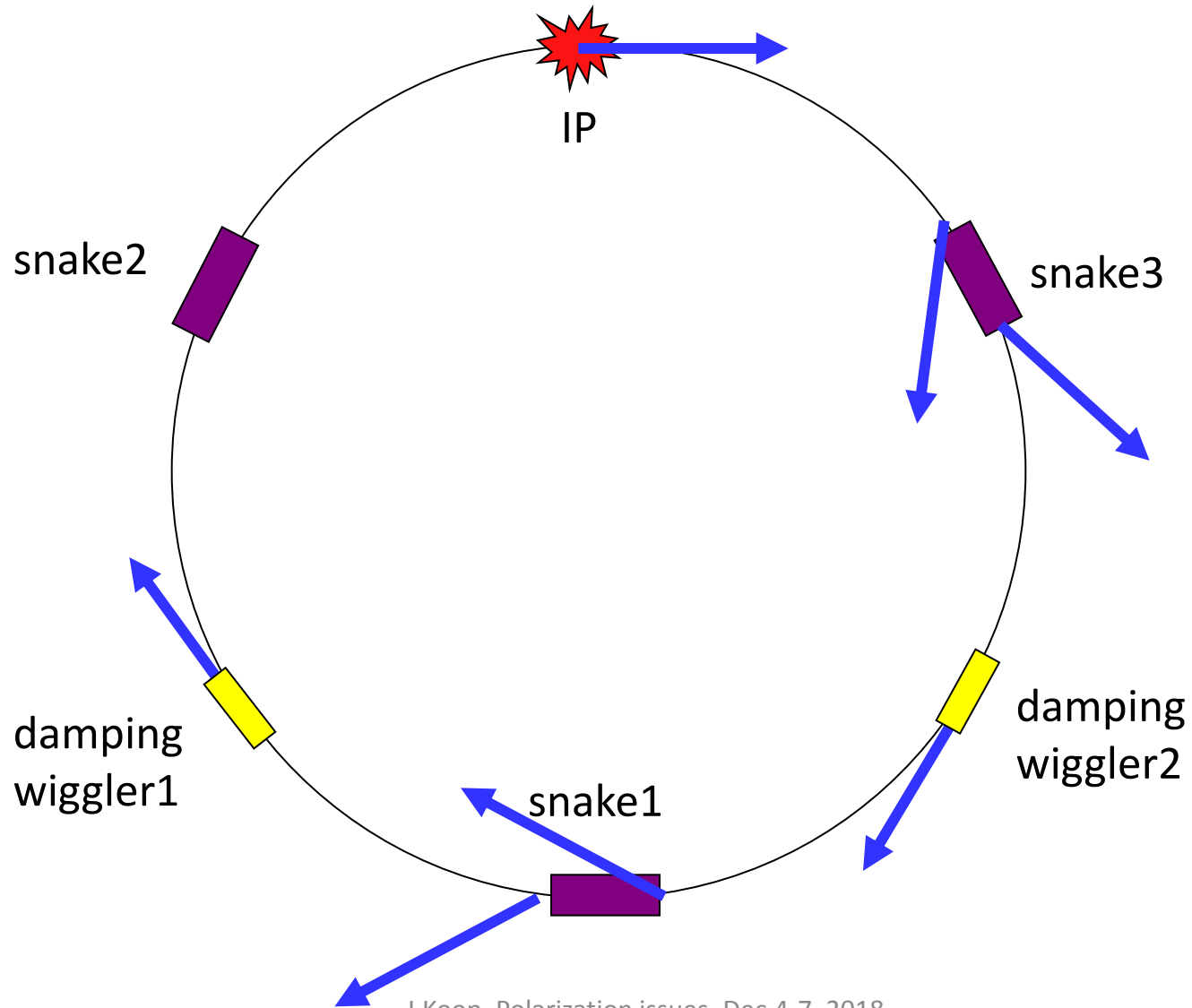
# Novosibirsk c-tau complex layout



# The Novosibirsk c-tau factory parameters

Beam Energy	1.0 – 3.0	GeV
Circumference	522	m
Crossing angle	60	mr
Emittances, $\epsilon_x / \epsilon_y$	4.8 / 0.025	nm
Number of bunches	270	
Number of particles/bunch	$9 \cdot 10^{10}$	
Total current	2.2	A
Beta function, $\beta_x / \beta_y$	50 / 0.5	mm
Sigma, $\sigma_x / \sigma_y$	15/0.1 (3 GeV)	mkm
Luminosity	$0.9 - 2.8 \cdot 10^{35}$	$\text{cm}^{-2}\text{s}^{-1}$

# Polarization scheme with 3 snakes (arc=120° +2 damping wigglers in the arc's middle )

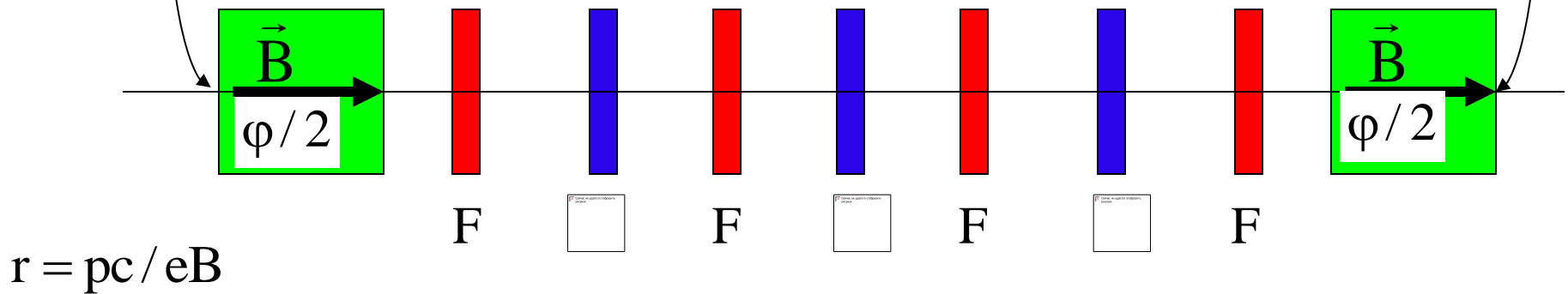


# Transparent spin rotator (partial snake)

To decouple x,y-motions should be  $T_x = -T_y$  (Litvinenko, Zholentz,1980)

$$T_x = \begin{pmatrix} -\cos \varphi & -2r \sin \varphi \\ (2r)^{-1} \sin \varphi & -\cos \varphi \end{pmatrix} \text{ - for the spin transparency!}$$

(Koop et al., SPIN2006)

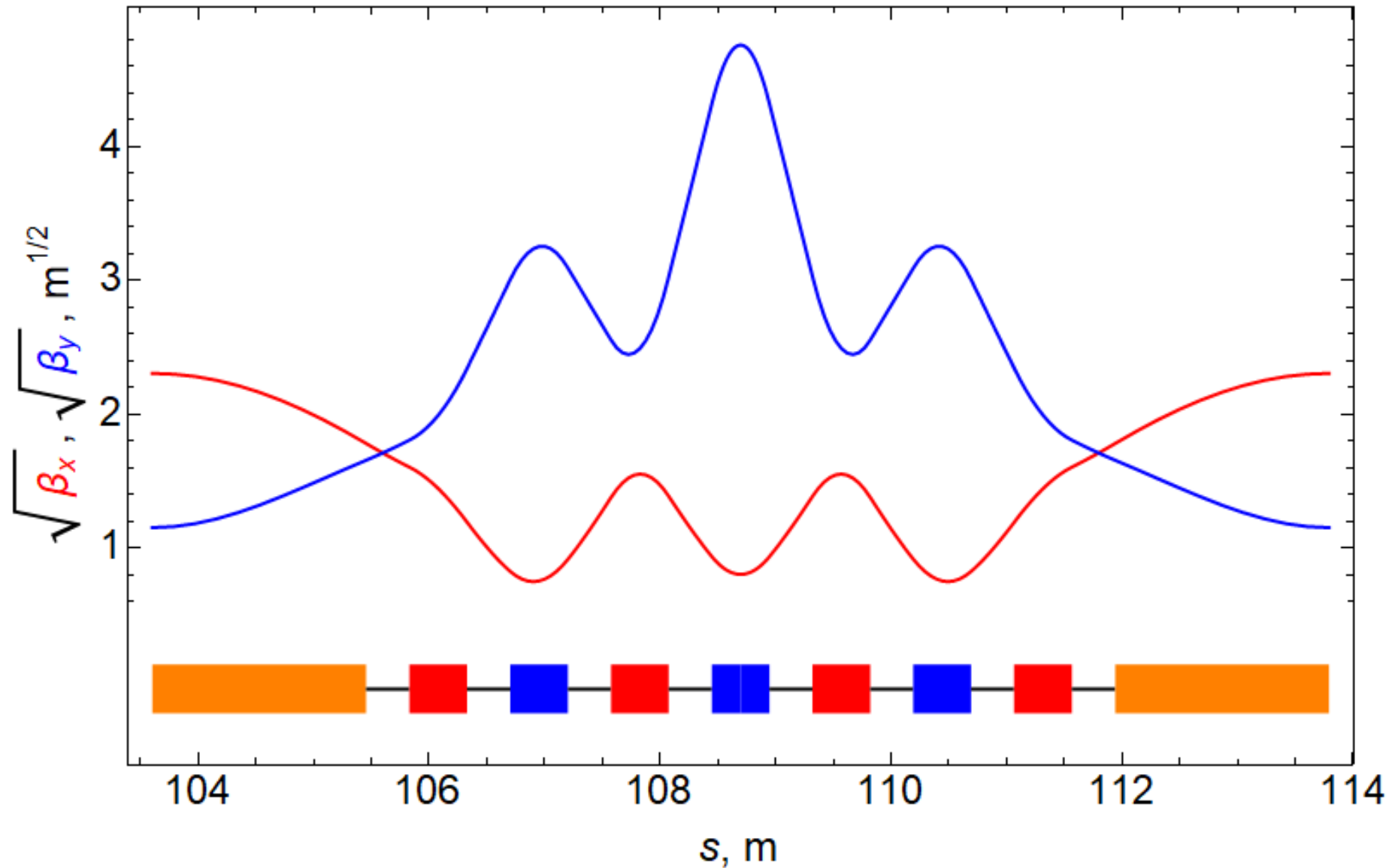


Two solenoids rotate spin by the angle  $\varphi$

All quads don't need to be skewed!

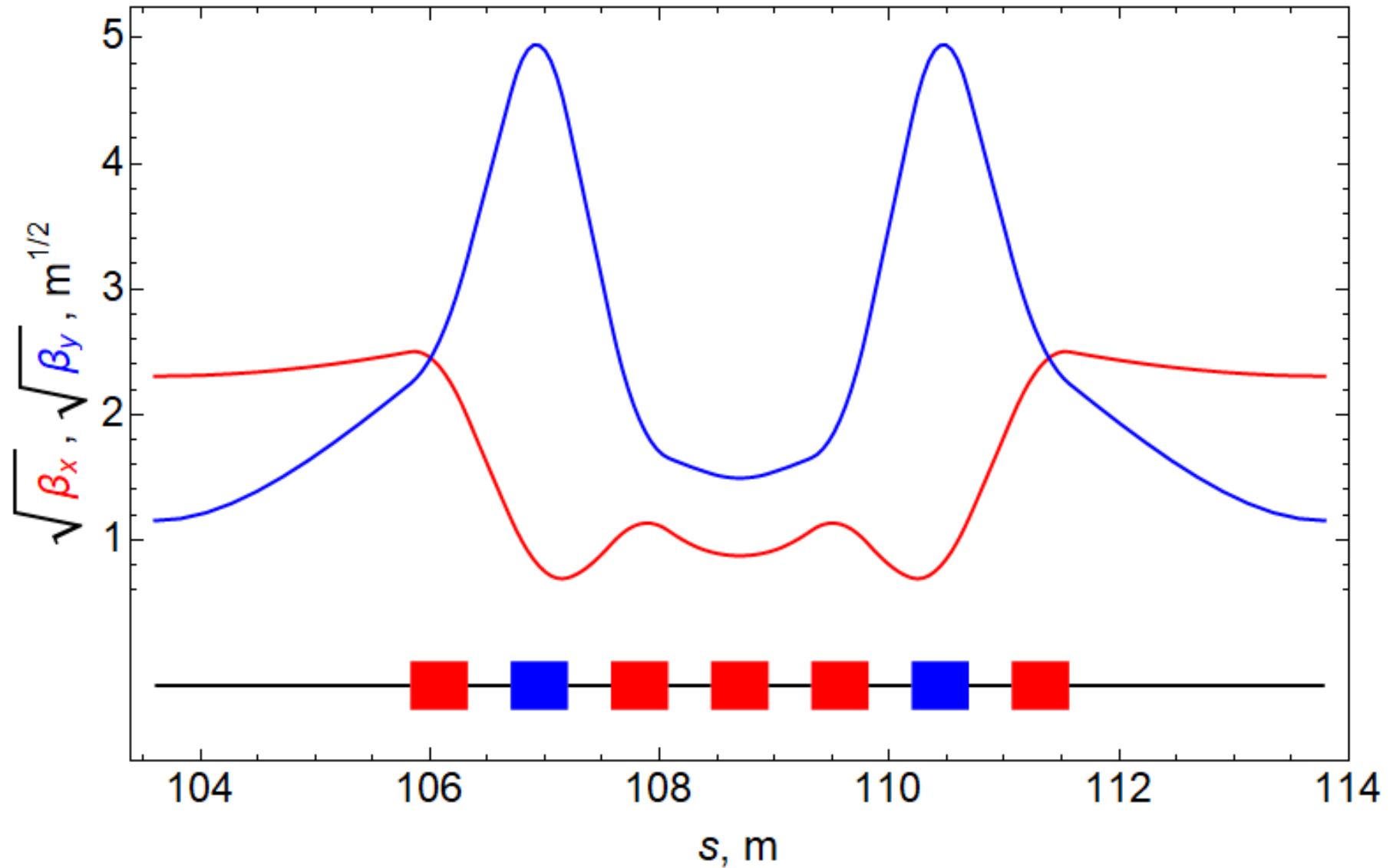
# 180° spin rotators, in places 1, 2, 3

Floquet functions of snakes №1, №2 and №3



# Equivalents of $180^\circ$ spin rotator, drifts 1, 2, 3

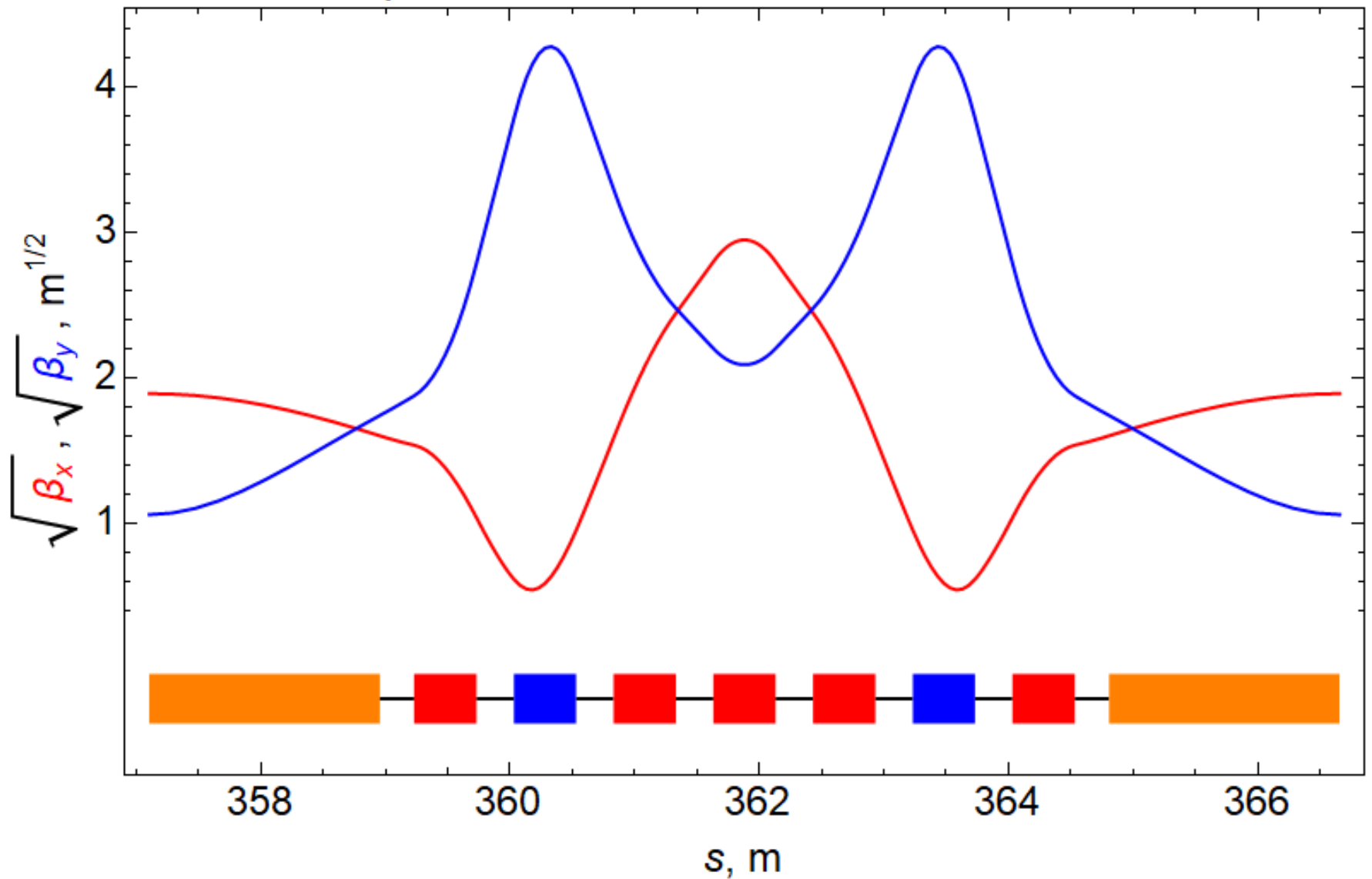
Floquet functions of snakes №1, №2 and №3, solenoids off





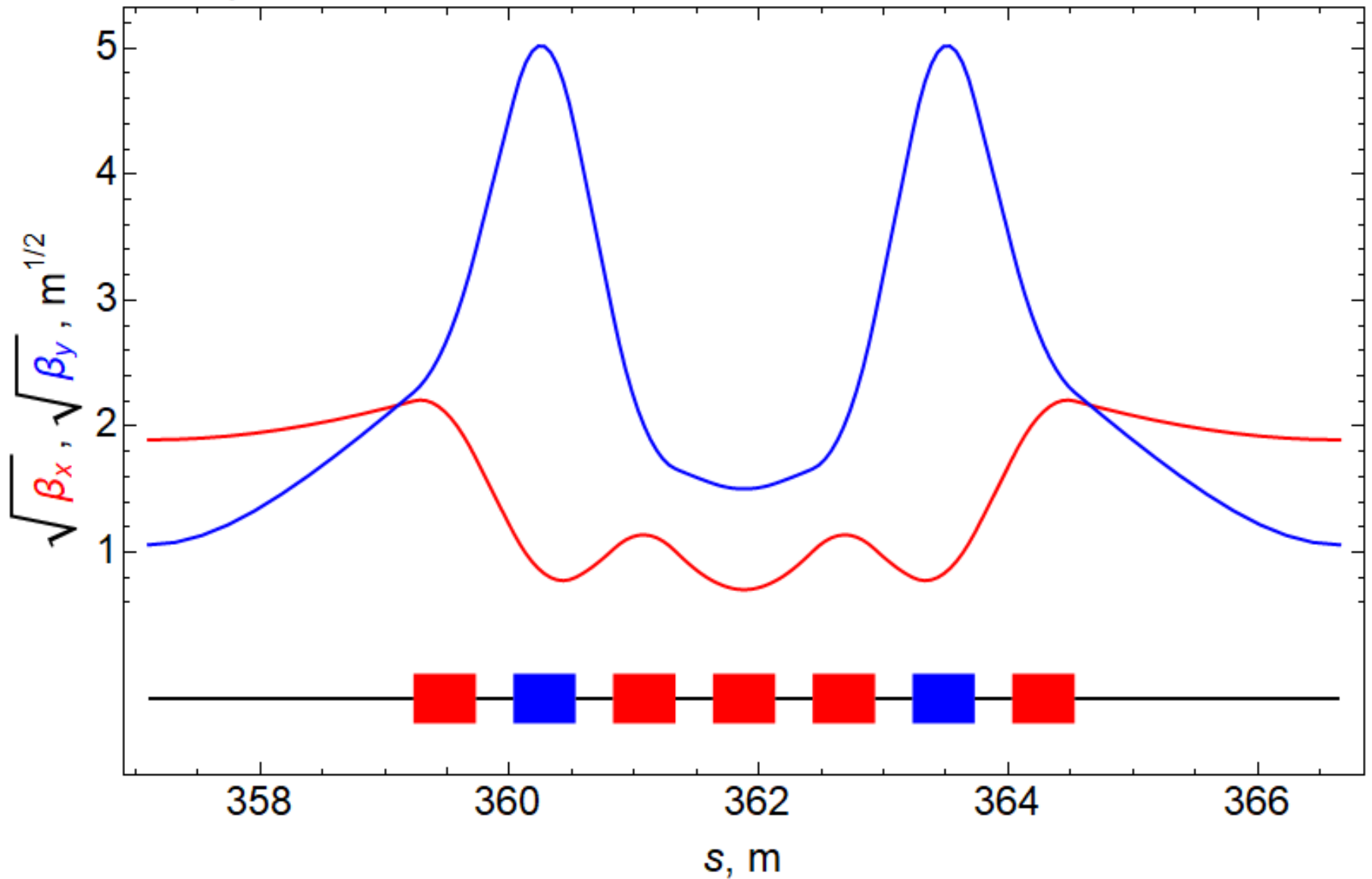
# 180° spin rotators, in places 4 and 5

## Floquet functions of snakes №4 and №5



# Equivalents of spin rotators, drifts 4 and 5

Floquet functions of snakes №4 and №5, solenoids off



# Depolarization time in presence of snakes

$$\tau_p^{-1} = \frac{5\sqrt{3}}{8} \lambda_e r_e c \gamma^5 \left\langle \left| \mathbf{K}^3 \right| \left( 1 - \frac{2}{9} (\vec{n}\vec{v})^2 + \frac{11}{18} \vec{d}^2 \right) \right\rangle$$

Here  $\mathbf{K} = \rho^{-1}$ ,  $|\vec{v}| = 1$

$$\vec{d} = \gamma \frac{\partial \vec{n}}{\partial \gamma} \text{ is}$$

the spin – orbit  
coupling vector

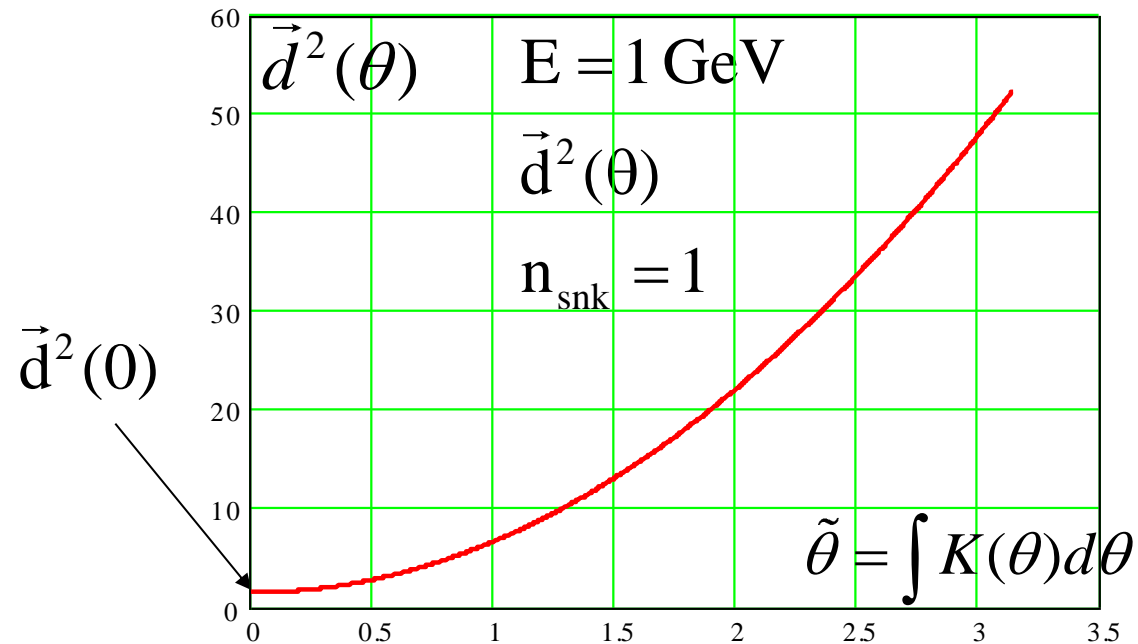
Spin transparency cancels  
the betatron contribution to  $\vec{d}$ :

$\vec{d} = \vec{d}_\gamma + \vec{d}_\beta$ , then:

$$\vec{d}^2(0) = \frac{\pi^2}{4} \sin^2 \frac{\pi v}{n_{\text{snk}}}$$

$$\langle \vec{d}^2 \rangle = \vec{d}^2(0) + \frac{\pi^2}{3} \frac{v^2}{n_{\text{snk}}^2}$$

Placing damping wigglers  
in minimum of  $|\vec{d}|$  weakens  
depolarizing effects of SR



# Self-polarization in presence of snakes

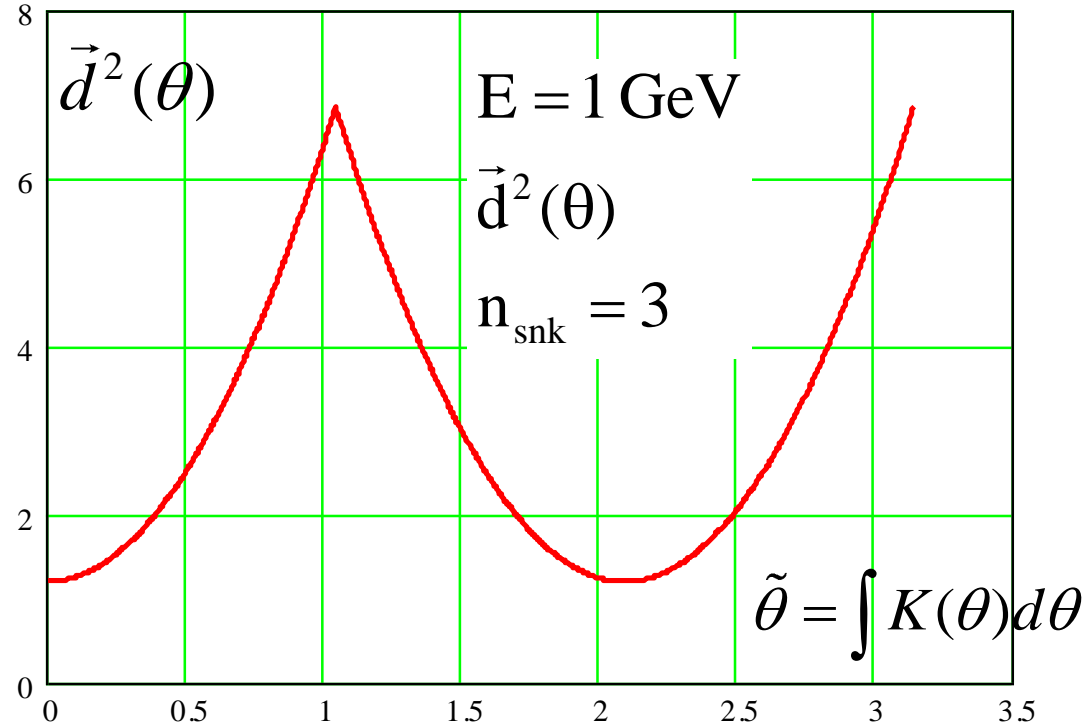
$$\zeta_p = \frac{8}{5\sqrt{3}} \cdot \frac{(\pi/2) \sin(\pi\nu / n_{\text{snk}}) \langle \mathbf{K}_B^3 + \mathbf{K}_W^3 \rangle}{\langle \mathbf{K}_B^3 + |\mathbf{K}_W|^3 \rangle 7/9 + \left[ \langle \mathbf{K}_B^3 d^2(\theta) \rangle + |\mathbf{K}_W|^3 d^2(0) \right] 11/18}$$

$$\mathbf{K}_W \equiv \rho_W^{-1}$$

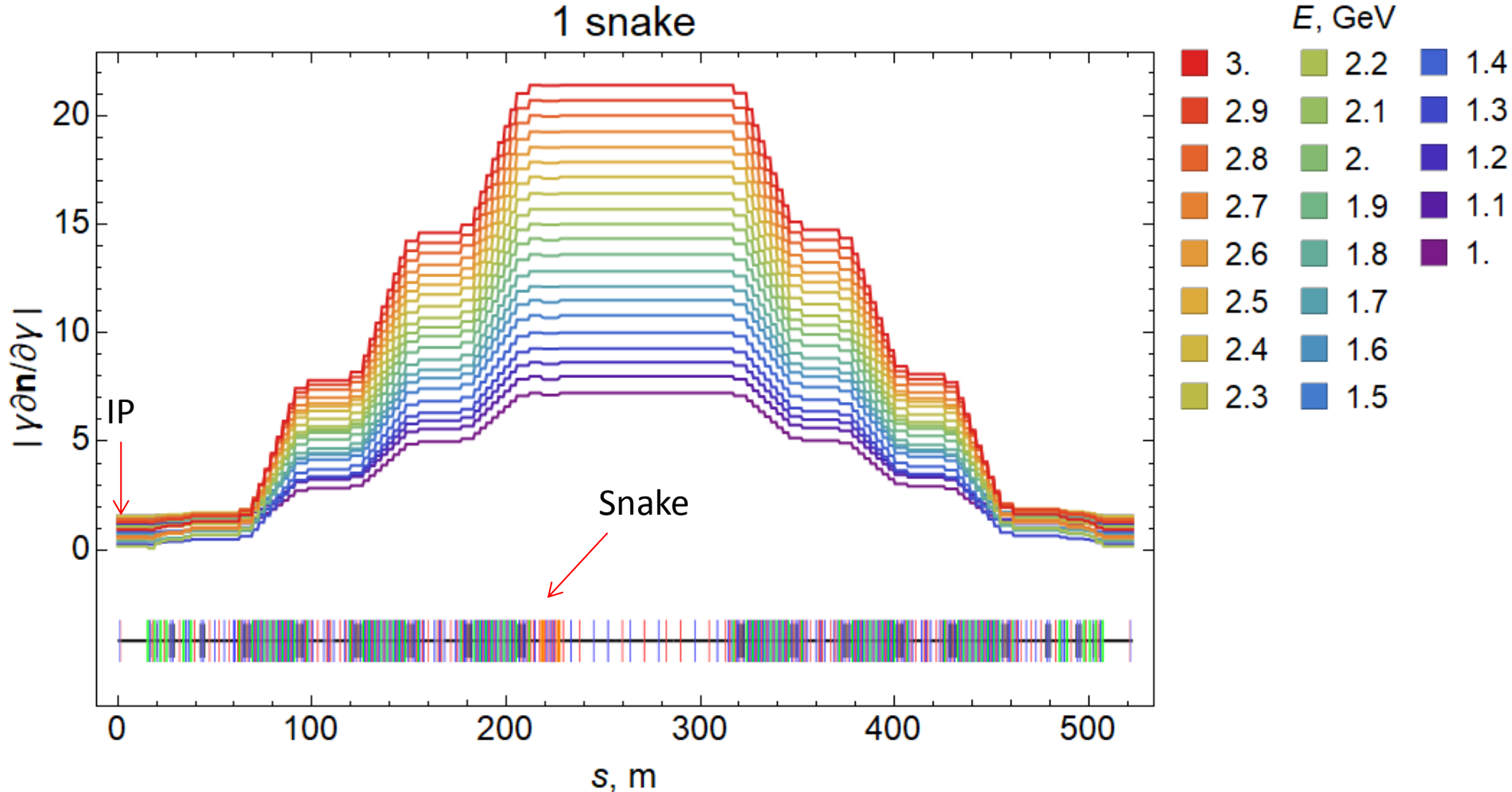
Symmetric wigglers do not contribute to the nominator, but asymmetric will do. That can be used to polarize the positron beam.

$$\vec{d}^2(0) = \frac{\pi^2}{4} \sin^2 \frac{\pi\nu}{n_{\text{snk}}}$$

$$\langle \vec{d}^2 \rangle = \vec{d}^2(0) + \frac{\pi^2}{3} \frac{\nu^2}{n_{\text{snk}}^2}$$

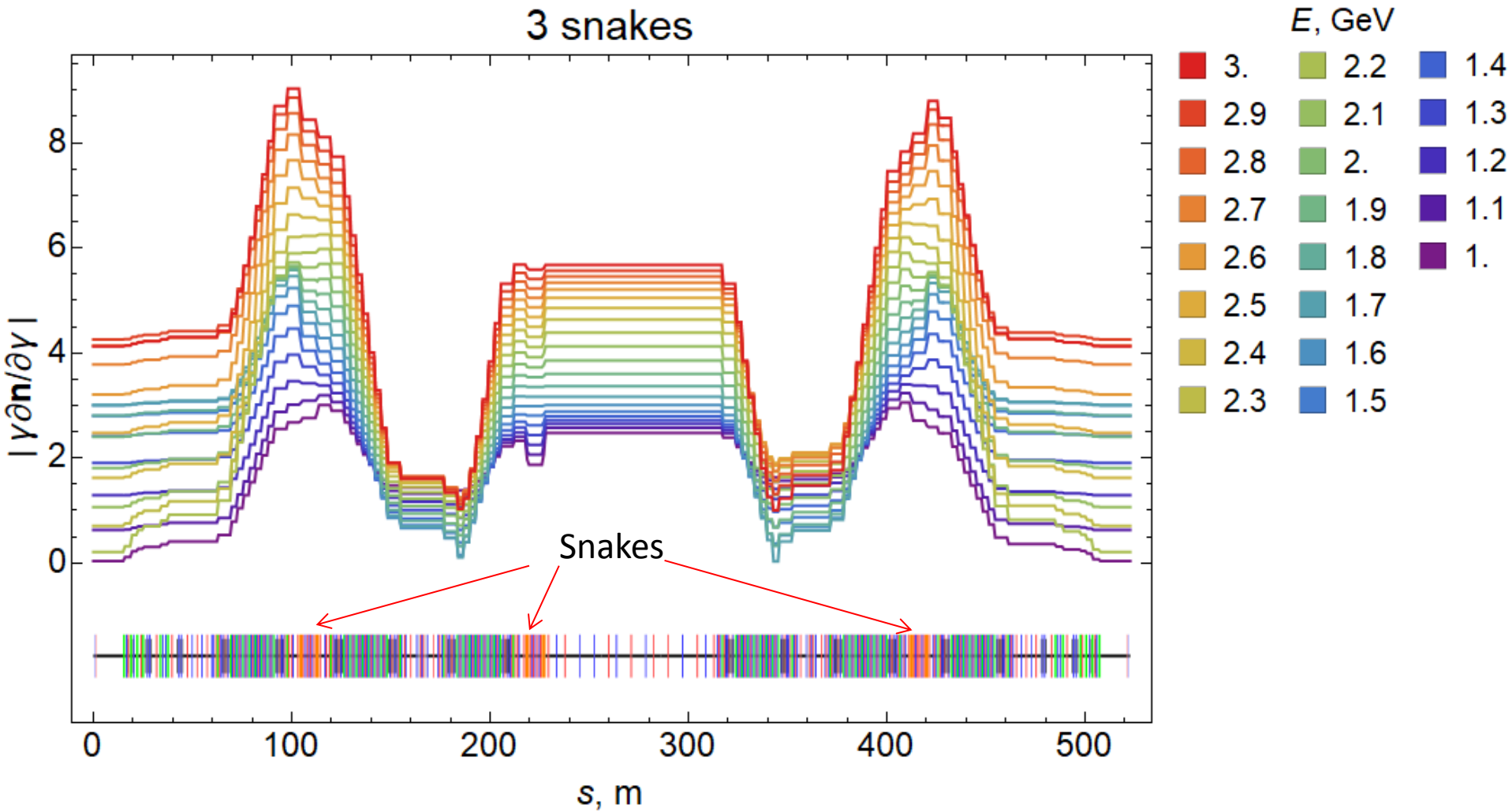


# Module of Spin-Orbital Function, 1 Snake

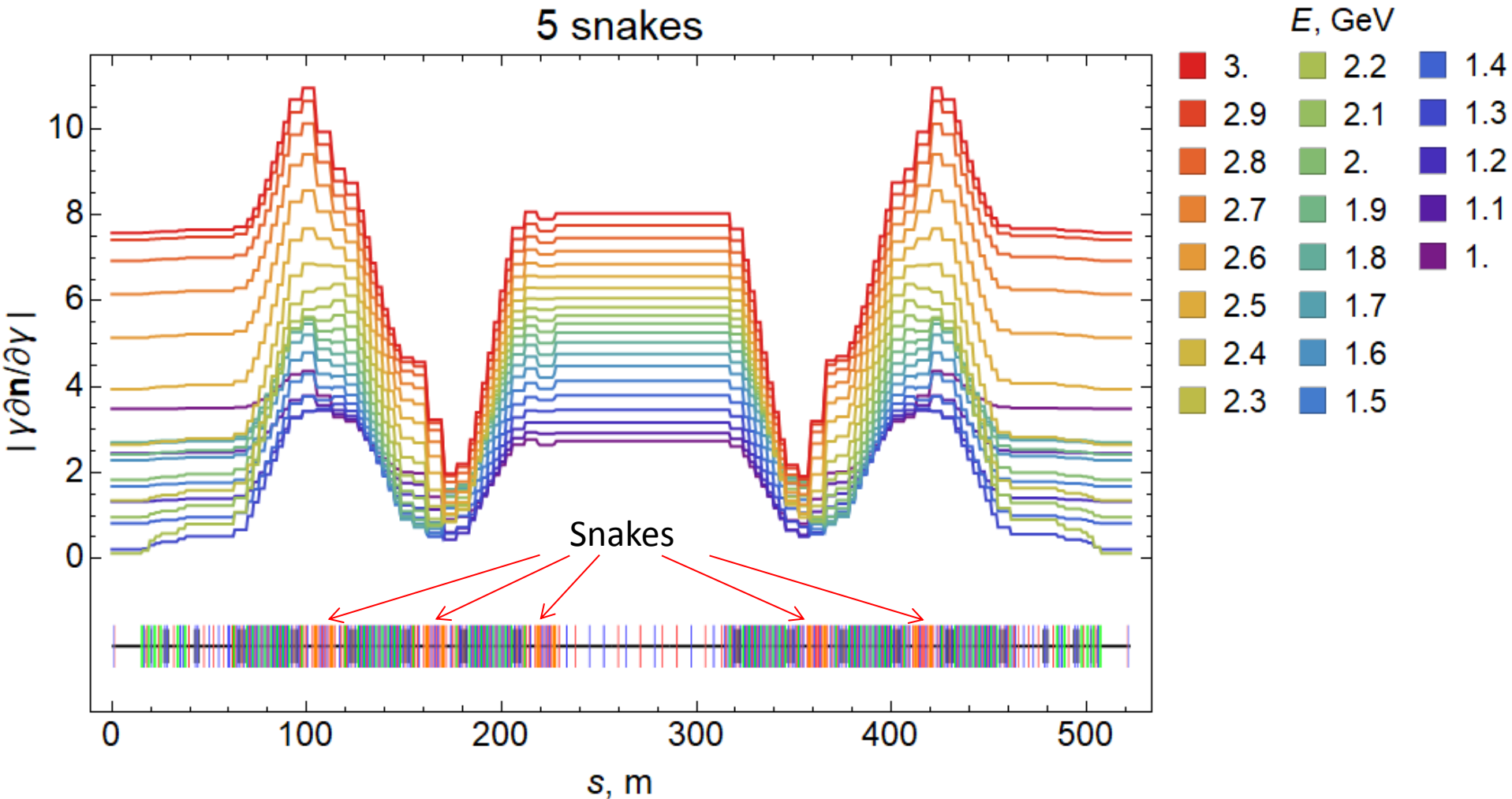


Here the Spin-Orbital coupling function  $d=|\gamma d\vec{n}/dy|$  was calculated by the code ASPIRRIN, written in 90-th by V. Ptitsyn and updated later on by S.R. Mane.

# Module of Spin-Orbital Function, 3 Snakes

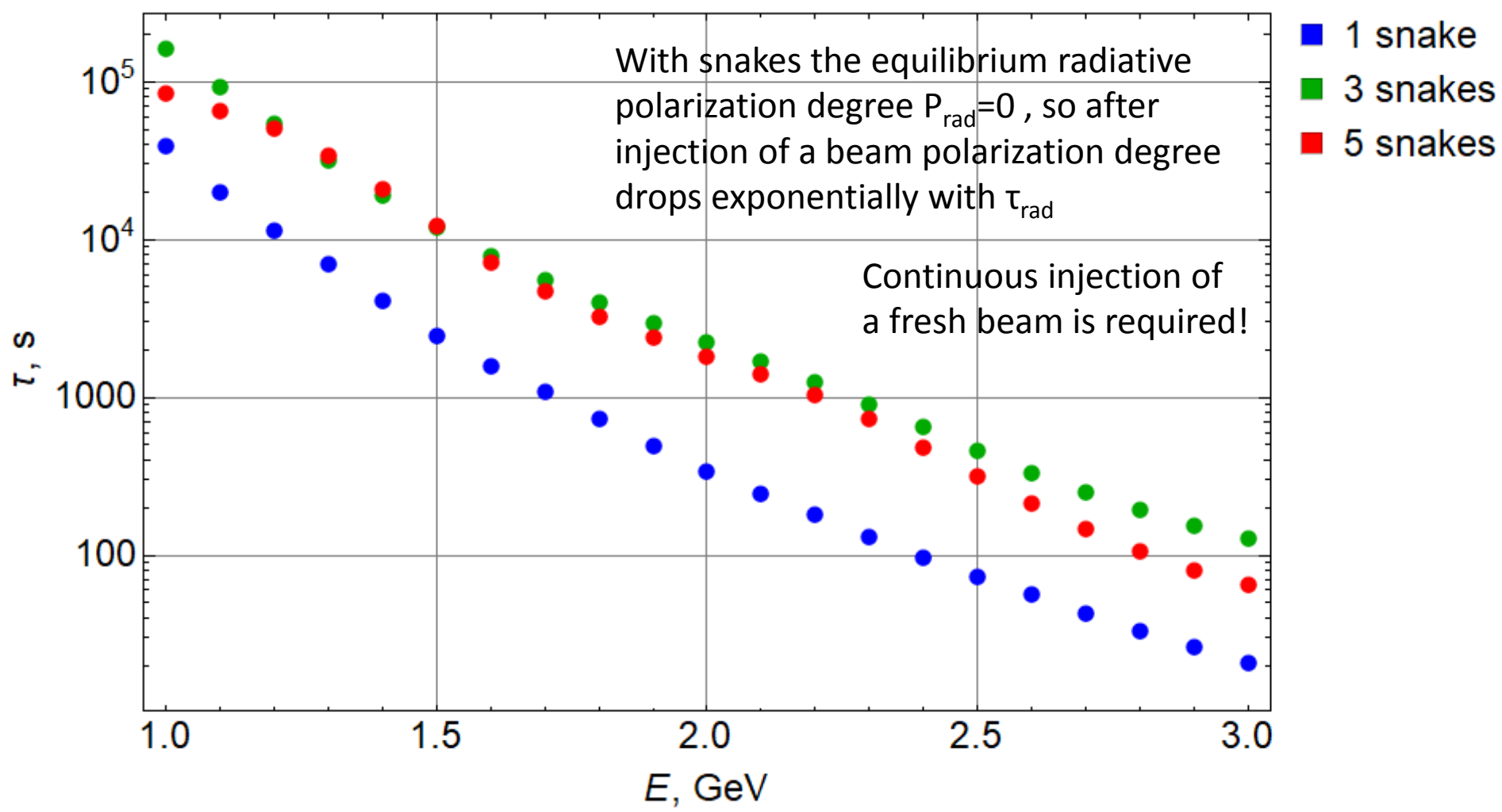


# Module of Spin-Orbital Function, 5 Snakes



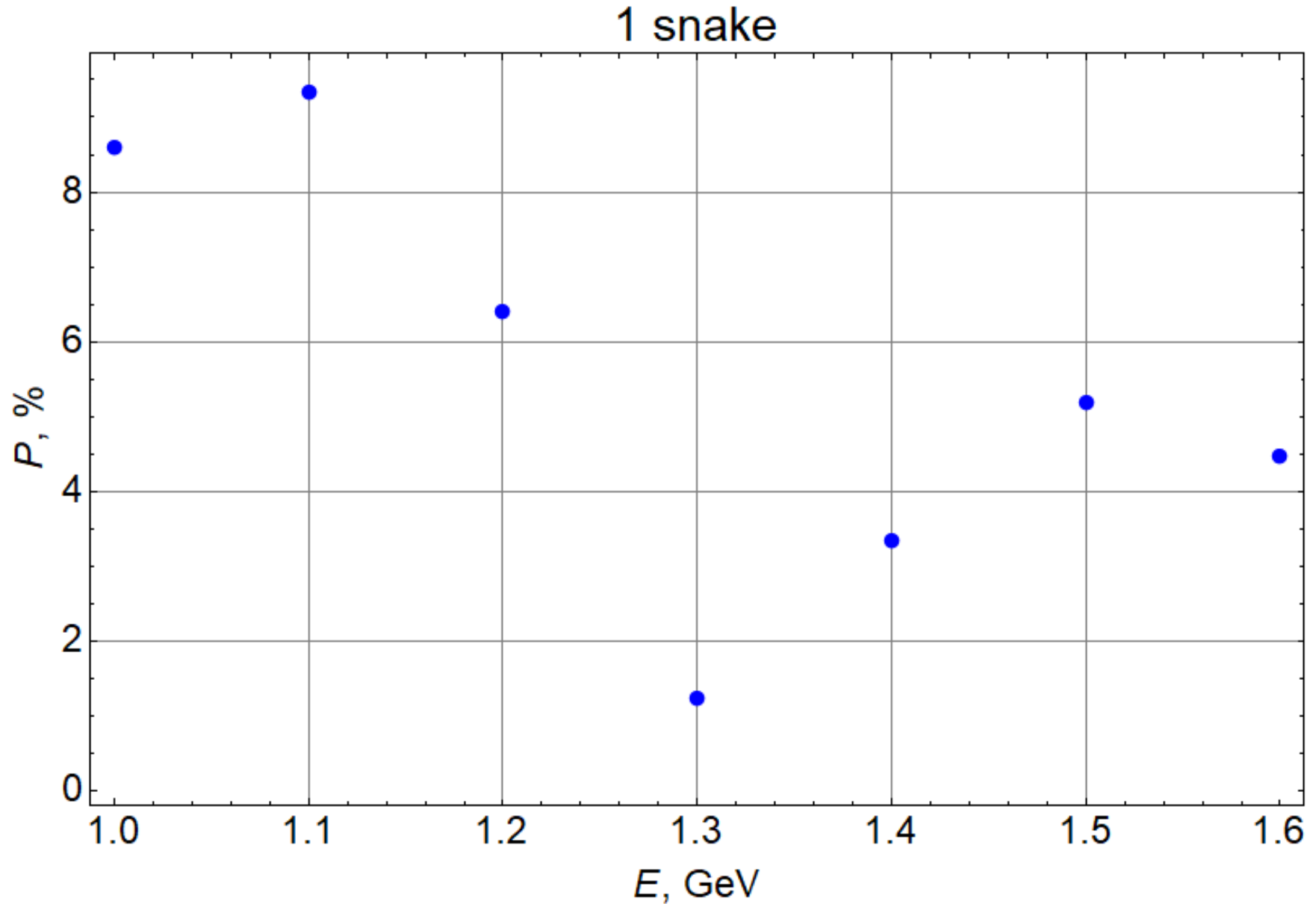
Arc's angles between snakes are chosen not optimal for 5 snakes. Therefore maximums of d-function are much higher than what was expected for their uniform distribution.

# Radiative polarization relaxation time, $\tau_{\text{rad}}$

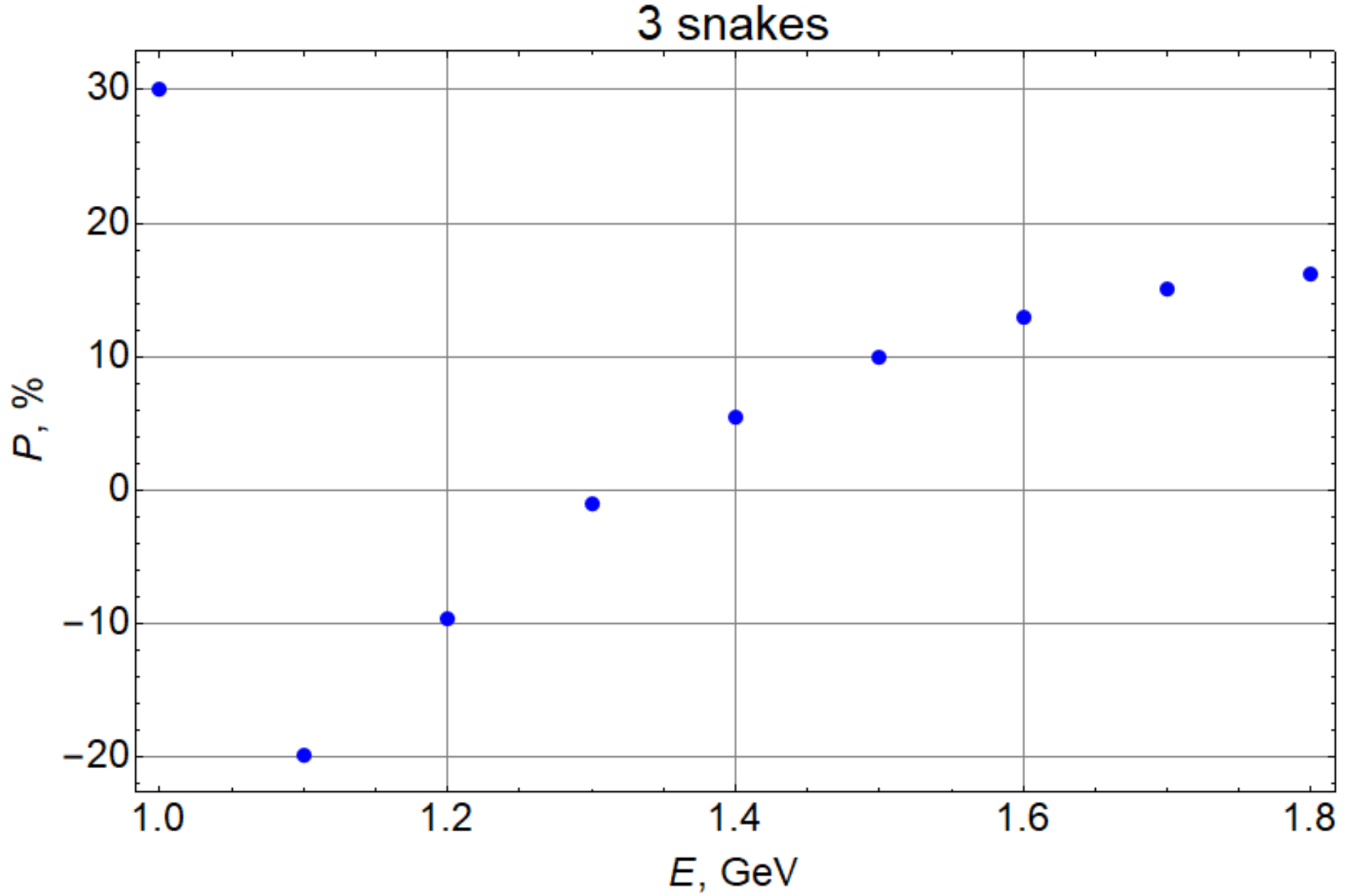




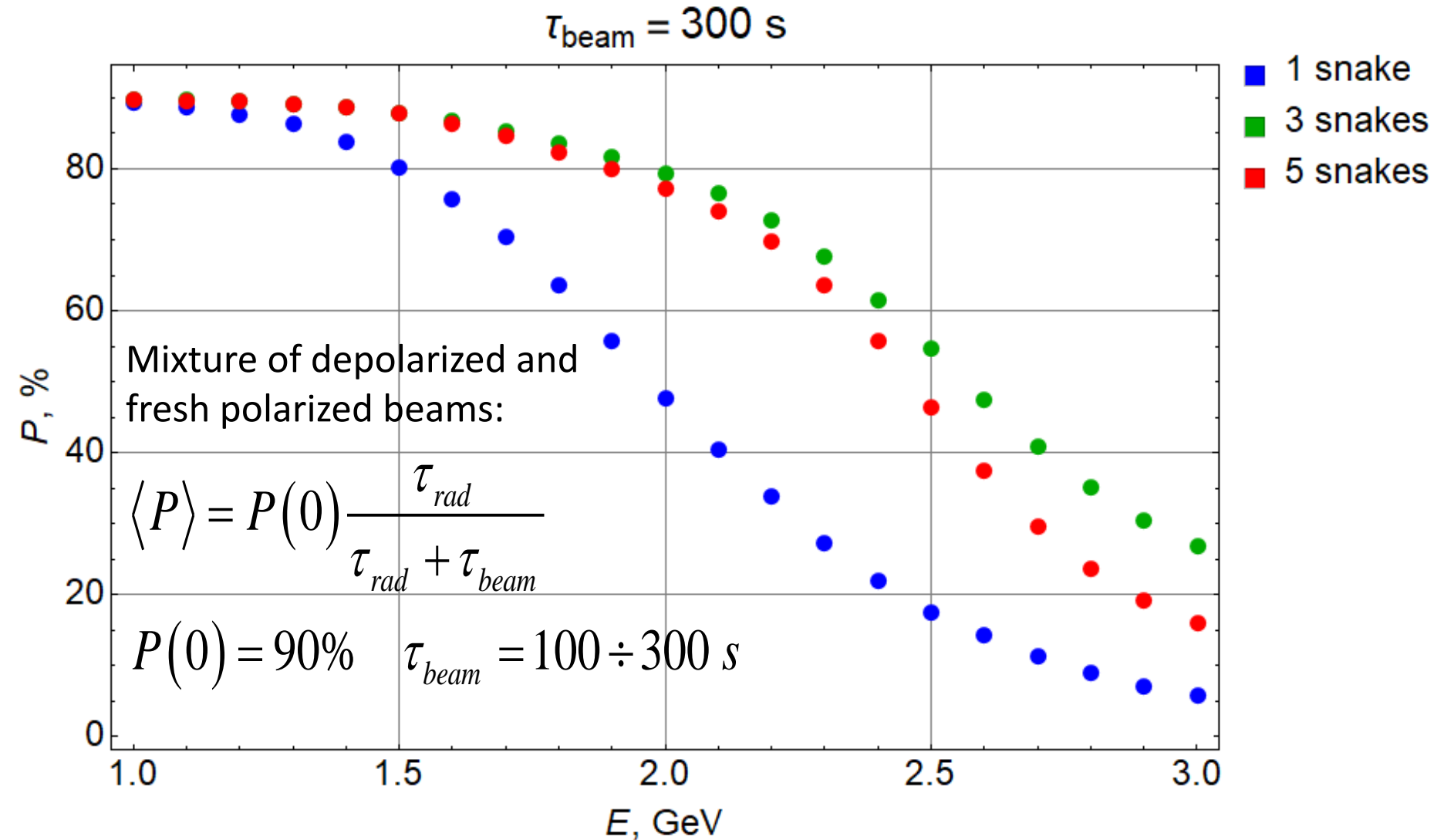
# Radiative equilibrium polarization, $P_{\text{rad}}$ , 1 snake



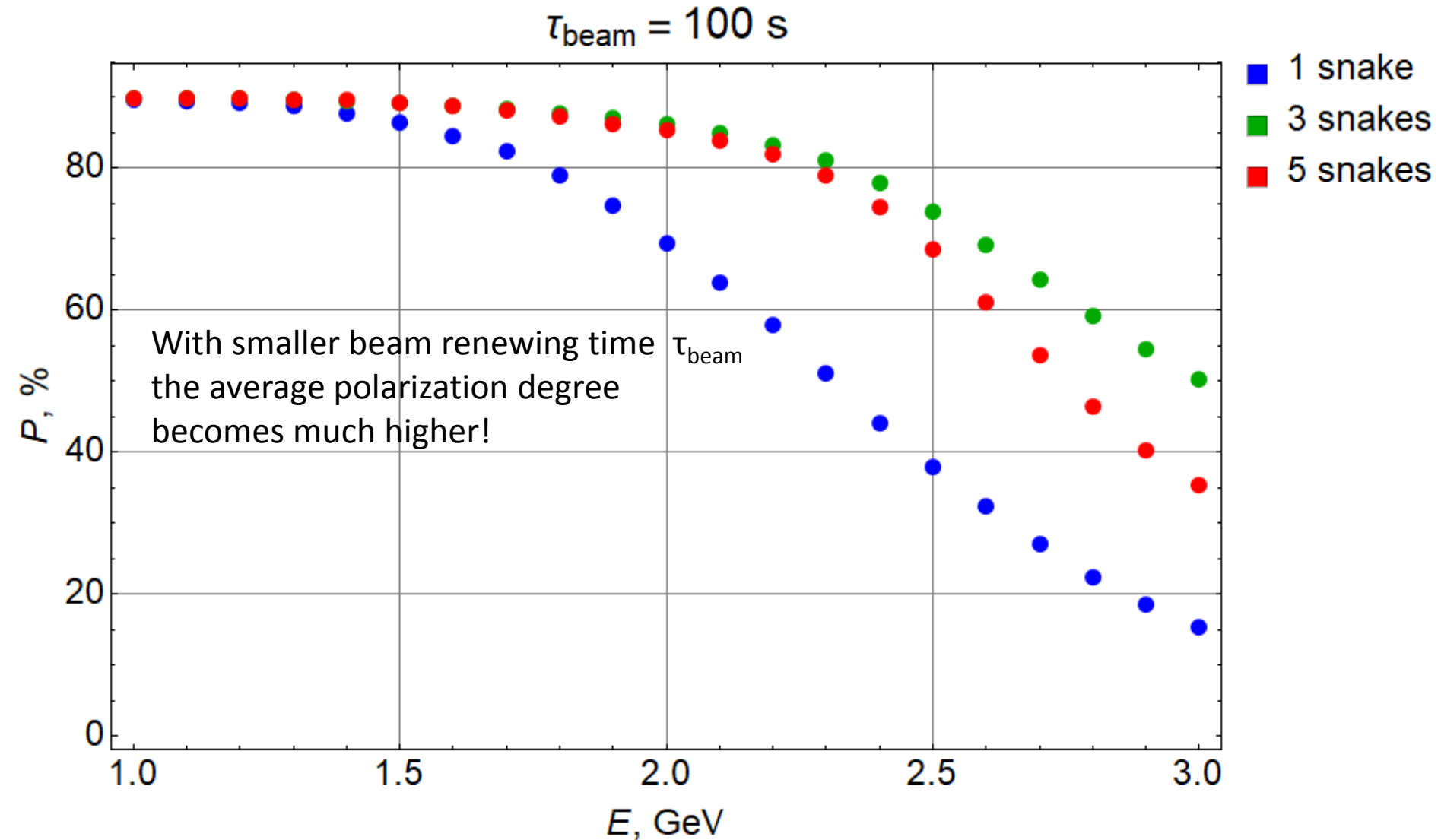
# Radiative equilibrium polarization, $P_{\text{rad}}$ , 3 snakes



# Polarization degree overview, if $\tau_{\text{beam}} = 300 \text{ s}$



# Polarization degree overview, if $\tau_{\text{beam}} = 100$ s



# Conclusion

- 1 snake provides up to 80% - 90% of the longitudinal polarization at  $E < 1.5$  GeV. This option can be considered as a first stage for polarization program.
- 3 snakes provide sufficiently high polarization degree, about 75-90% in the energy range  $E < 2.5$  GeV and only about 50% at 3 GeV. Currently this is the main scenario because it fulfills the main physics program requirements.
- 5 snakes option requires different optimization of a ring layout to place snakes equally by the velocity rotation angle. Now not under consideration.
- No preferable sign of the polarization. This helps to fight with systematic errors, caused by the detection efficiency asymmetries.
- Tolerances on the quads gradient integrals and the solenoid field integrals are in a range of few percent.