Status of gluon-fusion Higgs Production

Elisabetta Furlan
ETH Zürich

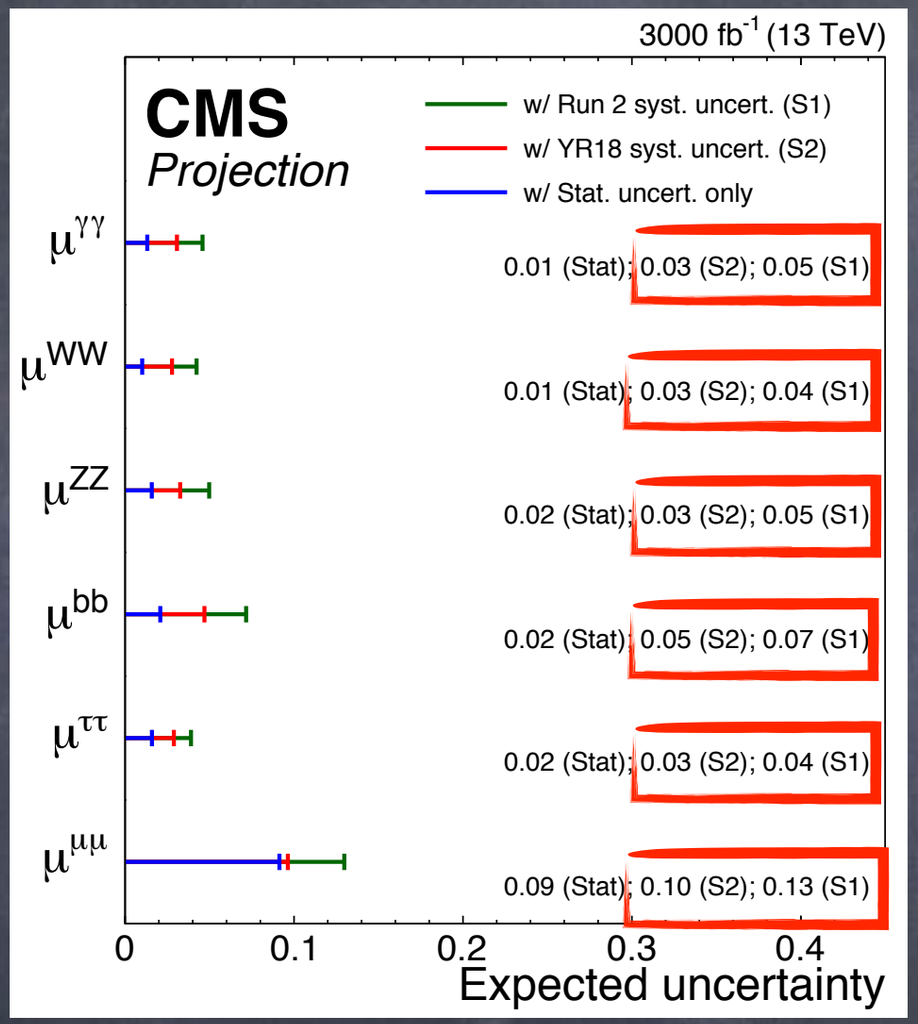
Higgs@LHC: where we are...

- LHC so far collected about 150 fb^{-1} of data → only 5% of the full expected dataset (3 ab^{-1})!
  ➡ great opportunities for
  - precision measures of the Higgs couplings ($\mathcal{O}$(few %)) → crucial to test the Higgs mechanism
  - detection of New Physics via rare decays
  - exploration of the Higgs potential (through double Higgs production)
  - ...

Higgs@LHC: where we are...

- LHC so far collected about 150 fb^{-1} of data → only 5% of the full expected dataset (3 ab^{-1})!
  ➡ great opportunities for
  - precision measures of the Higgs couplings ($\mathcal{O}$(few %)) → crucial to test the Higgs mechanism
  - detection of New Physics via rare decays
  - exploration of the Higgs potential (through double Higgs production)
  - ...

… and where we can go

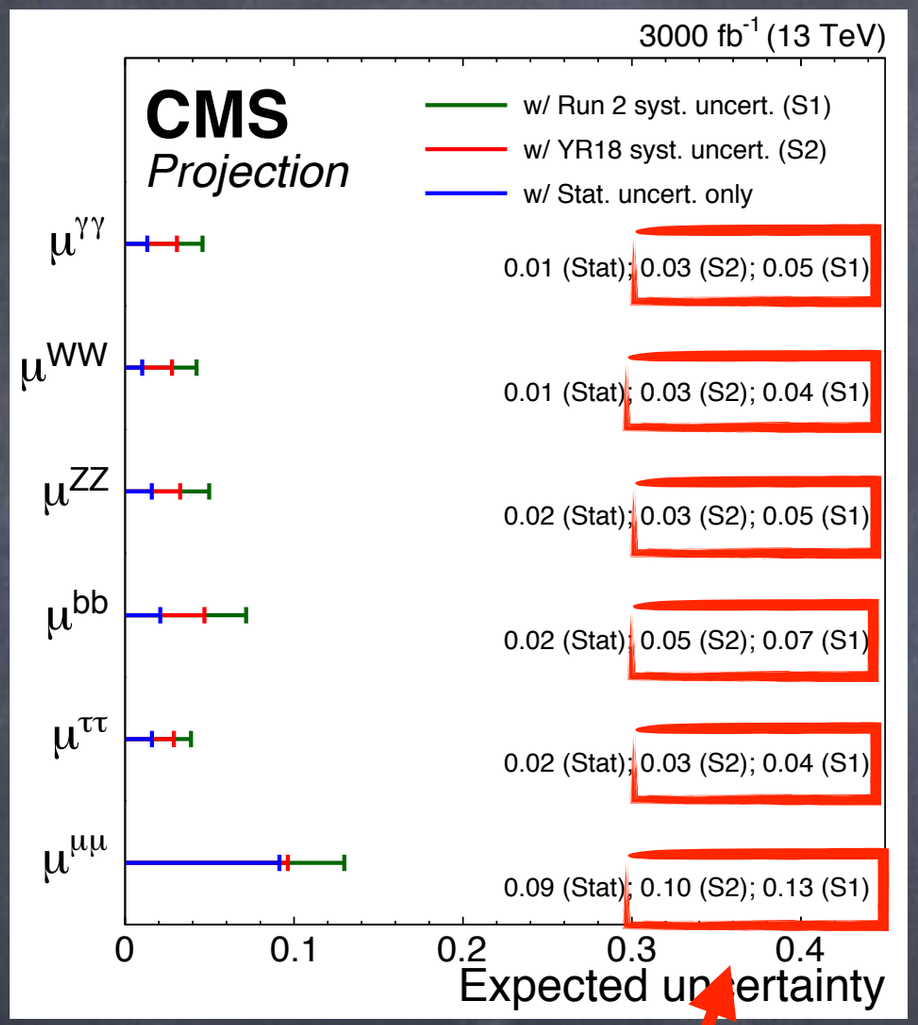


CMS PAS FTR-18-011

Prod. mode	Analysis	$\Delta\mu_{\text{sig}}$
ggF	Run 2, 80 fb^{-1}	$^{+0.070}_{-0.052}$
	HL-LHC S1	$^{+0.062}_{-0.056}$
	HL-LHC S2	$^{+0.030}_{-0.028}$
VBF	Run 2, 80 fb^{-1}	$^{+0.161}_{-0.101}$
	HL-LHC S1	$^{+0.087}_{-0.072}$
	HL-LHC S2	$^{+0.053}_{-0.050}$
VH	Run 2, 80 fb^{-1}	$^{+0.283}_{-0.144}$
	HL-LHC S1	$^{+0.124}_{-0.084}$
	HL-LHC S2	$^{+0.077}_{-0.062}$
$t\bar{t}H$	Run 2, 80 fb^{-1}	
	HL-LHC S1	$^{+0.156}_{-0.095}$
	HL-LHC S2	$^{+0.074}_{-0.051}$

ATL-PHYS-PUB-2018-054

… and where we can go



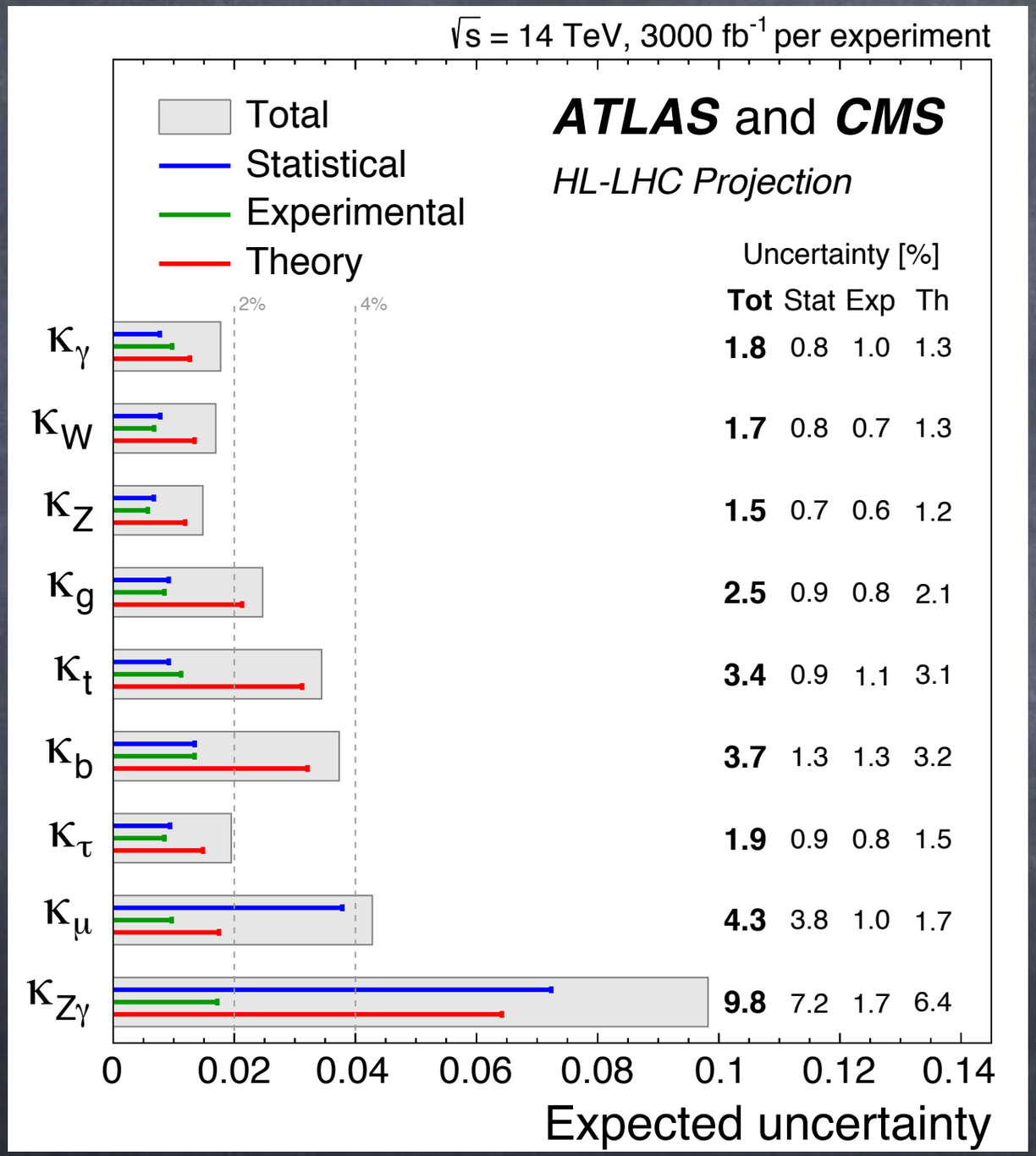
CMS PAS FTR-18-011

Prod. mode	Analysis	$\Delta\mu_{\text{sig}}$
ggF	Run 2, 80 fb^{-1}	$^{+0.070}_{-0.052}$
	HL-LHC S1	$^{+0.062}_{-0.056}$
	HL-LHC S2	$^{+0.030}_{-0.028}$
VBF	Run 2, 80 fb^{-1}	$^{+0.161}_{-0.101}$
	HL-LHC S1	$^{+0.087}_{-0.072}$
	HL-LHC S2	$^{+0.053}_{-0.050}$
VH	Run 2, 80 fb^{-1}	$^{+0.283}_{-0.144}$
	HL-LHC S1	$^{+0.124}_{-0.084}$
	HL-LHC S2	$^{+0.077}_{-0.062}$
$t\bar{t}H$	Run 2, 80 fb^{-1}	
	HL-LHC S1	$^{+0.156}_{-0.095}$
	HL-LHC S2	$^{+0.074}_{-0.051}$

ATL-PHYS-PUB-2018-054

Scenario 2: theory error halved w.r.t. its current value (S1)

… and where we can go



CERN-LPCC-2018-04

… and where we can go

- ➡ It is vital to reduce significantly (by at least 50%) the theoretical uncertainty, or it will become the main limiting factor in the interpretation of an important part of the HL – LHC data

The theory error

- on the branching ratios: well under control

decay channel	branching ratio	relative eror
$H \to \gamma\gamma$	2.27 x 10^{-3}	+1.73% -1.72%
$H \to ZZ$	2.64 x 10^{-2}	+0.99% -0.99%
$H \to W^+W^-$	2.15 x 10^{-1}	+0.99% -0.99%
$H \to \tau^+\tau^-$	6.26 x 10^{-2}	+1.17% -1.16%
$H \to b\bar{b}$	5.81 x 10^{-1}	+0.65% -0.65%
$H \to Z\gamma$	1.54 x 10^{-3}	+5.71% -5.71%
$H \to \mu^+\mu^-$	2.17 x 10^{-4}	+1.23% -1.23%

LHCHXSWG, for the CERN Yellow report 4

The theory error

- on the production mode

$\sqrt{s} = 13$ TeV	σ [pb]	$\delta\sigma^{theo}/\sigma$
ggH	48.5	+4.6% -6.7%
VBF	3.78	+0.4% -0.3%
WH	1.37	+0.5% -0.7%
⋮	⋮	⋮

LHCHXSWG, for the CERN Yellow report 4

The theory error

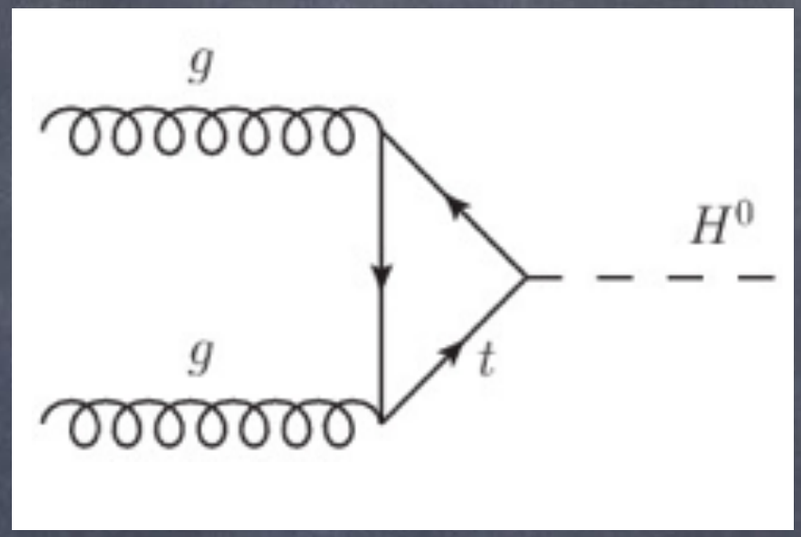
- gluon-fusion Higgs production is the main limiting factor!

The theory error

- ➡ gluon-fusion Higgs production is the main limiting factor!

Gluon-fusion Higgs production

- basic process (leading order in QCD)



- receives large higher-order corrections

1978 **LO** $\hat{\sigma}^{8TeV} = 9.6pb \pm 25\%$ Georgi et al

1991 **NLO** $\hat{\sigma}^{8TeV} = 16.7pb \pm 20\%$ Dawson; Djouadi, Spira, Zerwas; Graudenz, Spira, Zerwas

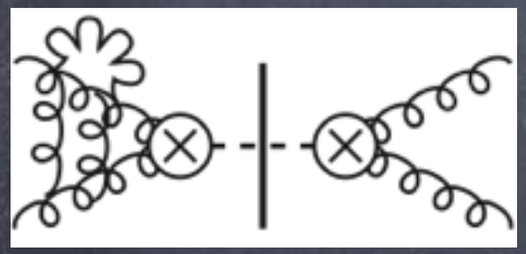
2002 **NNLO** $\hat{\sigma}^{8TeV} = 19.6pb \pm 9\%$ Harlander, Kilgore; Anastasiou, Melnikov

Gluon-fusion Higgs production

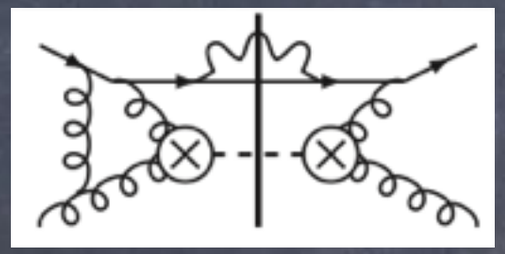
- currently known at N^3LO in QCD
  - astonishing result, as it requires the evaluation of hundreds of thousands of multi-loop, multi-scale diagrams!

Anastasiou, Duhr, Dulat, EF, Gehrmann, Herzog, Lazopoulos, Mistlberger, JHEP 05 (2016) 058

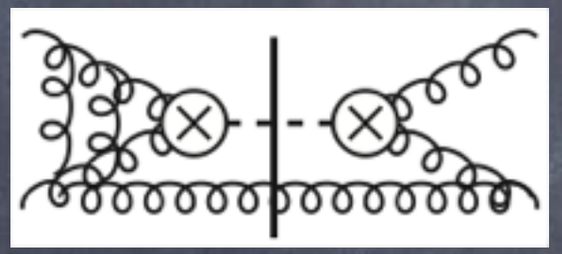
Mistlberger, JHEP 05 (2018) 028



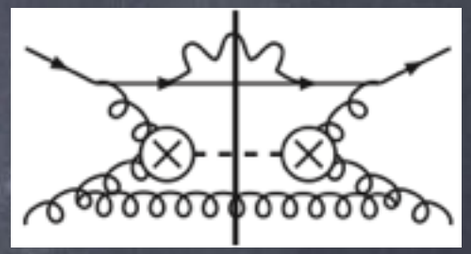
Baikov et al., Phys. Rev. Lett. 102, 212002 (2009); Gehrmann et al., JHEP 1006, 094 (2010)



Gehrmann et al., JHEP 1201, 056 (2012); Duhr et al., Phys. Lett. B 727, 452 (2013); Li et al., JHEP 1311, 080 (2013)



Anastasiou et al., JHEP 1312, 088 (2013); Kilgore, Phys. Rev. D 89 073008 (2014)



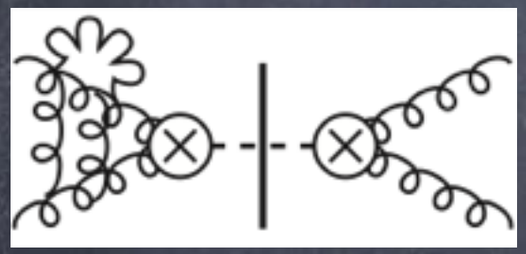
Anastasiou et al., JHEP 1307, 003 (2013)

Gluon-fusion Higgs production

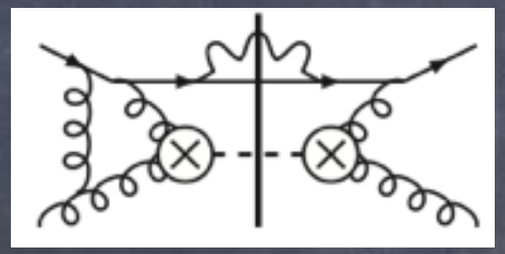
- currently known at N^3LO in QCD
  - astonishing result, as it requires the evaluation of hundreds of thousands of multi-loop, multi-scale diagrams!

Anastasiou, Duhr, Dulat, EF, Gehrmann, Herzog, Lazopoulos, Mistlberger, JHEP 05 (2016) 058

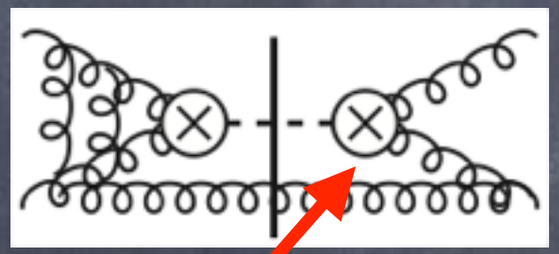
Mistlberger, JHEP 05 (2018) 028



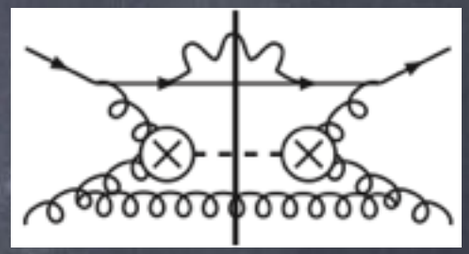
Baikov et al., Phys. Rev. Lett. 102, 212002 (2009); Gehrmann et al., JHEP 1006, 094 (2010)



Gehrmann et al., JHEP 1201, 056 (2012); Duhr et al., Phys. Lett. B 727, 452 (2013); Li et al., JHEP 1311, 080 (2013)

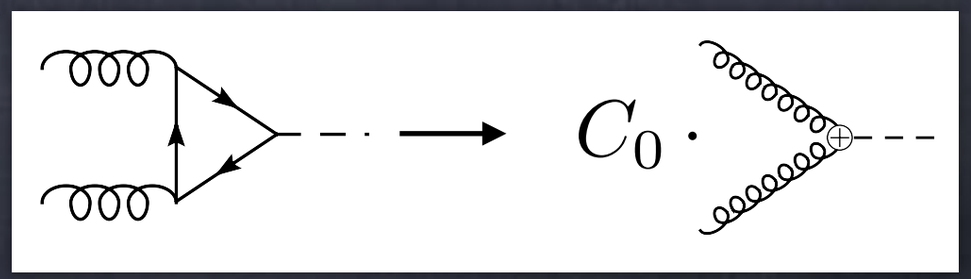


Anastasiou et al., JHEP 1312, 088 (2013); Kilgore, Phys. Rev. D 89 073008 (2014)



Anastasiou et al., JHEP 1307, 003 (2013)

heavy-quark effective theory (HQET): $m_t \to \infty$

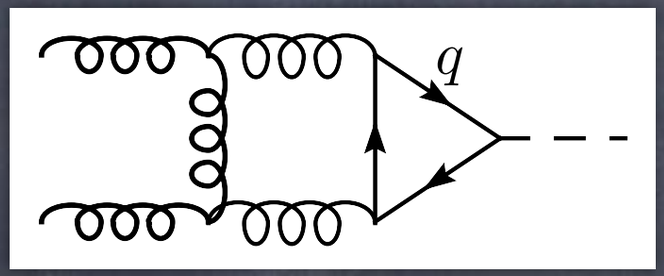


Gluon-fusion Higgs production

➡ currently known at N^{3}LO in QCD (in HQET)

with

➡ exact finite-mass effects of top, bottom and charm through NLO



Gluon-fusion Higgs production

➡ currently known at N^3LO in QCD (in HQET)

with

➡ exact finite-mass effects of top, bottom and charm through NLO

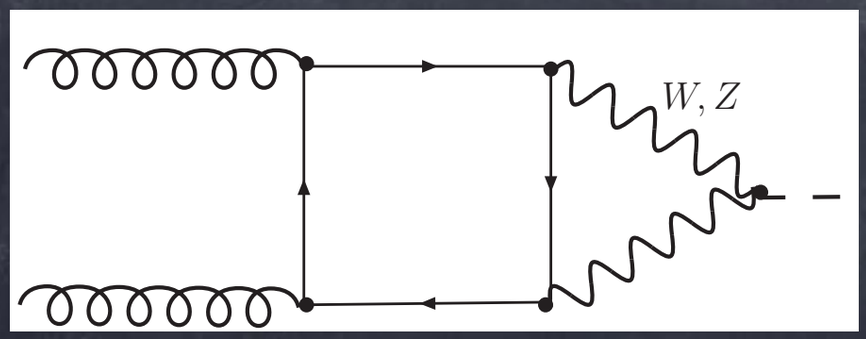
Graudenz et al., PRL 70, 1372 (1993); Spira et al., NP B 453, 17 (1995)

➡ $1/m_t^2$ series corrections around the infinte-mass approximation at NNLO

Harlander and Ozeren, JHEP 0911, 088 (2009); Pak et al., JHEP 1002, 025 (2010)

➡ two - loop electroweak corrections

Aglietti, et al.,PLB 595 (2004) 432-441; Actis et al., PLB 670 (2008) 12-17



Gluon-fusion Higgs production

➡ currently known at N^3LO in QCD (in HQET)

with

➡ exact finite-mass effects of top, bottom and charm through NLO

Graudenz et al., PRL 70, 1372 (1993); Spira et al., NP B 453, 17 (1995)

➡ $1/m_t^2$ series corrections around the infinte-mass approximation at NNLO

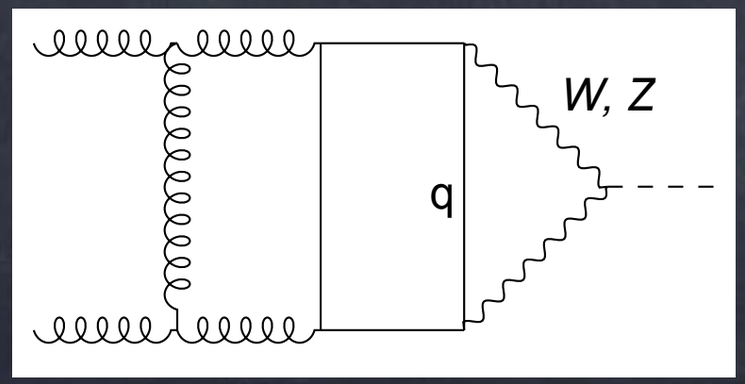
Harlander and Ozeren, JHEP 0911, 088 (2009); Pak et al., JHEP 1002, 025 (2010)

➡ two - loop electroweak corrections

Aglietti, et al.,PLB 595 (2004) 432-441; Actis et al., PLB 670 (2008) 12-17

➡ three loop QCD - electroweak corrections (heavy gauge-boson limit)

Anastasiou et al., JHEP 04 (2009) 003



Gluon-fusion Higgs production

- breakdown of the cross section

$$
\begin{aligned}
48.58\,\text{pb} = \quad & 16.00\,\text{pb} & & && (\text{LO, rEFT}) \\
& + 20.84\,\text{pb} & (+42.9\%) & && (\text{NLO, rEFT}) \\
& - \ 2.05\,\text{pb} & (-4.2\%) & && ((t,b,c), \text{ exact NLO}) \\
& + \ 9.56\,\text{pb} & (+19.7\%) & && (\text{NNLO, rEFT}) \\
& + \ 0.34\,\text{pb} & (+0.2\%) & && (\text{NNLO, } 1/m_t) \\
& + \ 2.40\,\text{pb} & (+4.9\%) & && (\text{EW, QCD-EW}) \\
& + \ 1.49\,\text{pb} & (+3.1\%) & && (\text{N}^3\text{LO, rEFT})
\end{aligned}
$$

Anastasiou, Duhr, Dulat, EF, Gehrmann, Herzog,
Lazopoulos, Mistlberger, JHEP 05 (2016) 058

Gluon-fusion Higgs production

- breakdown of the theory error

σ	$\delta(\text{PDF})$	$\delta(\alpha_s)$	$\delta(\text{scale})$	$\delta(\text{trunc})$	$\delta(\text{PDF-TH})$	$\delta(\text{EW})$	$\delta(tbc)$	$\delta(1/m_t)$	
48.58	± 0.90	$^{+1.27}_{-1.25}$	$^{+0.10}_{-1.15}$	± 0.18	± 0.56	± 0.49	± 0.40	± 0.49	pb
	± 1.86	$^{+2.61}_{-2.58}$	$^{+0.21}_{-2.37}$	± 0.37	± 1.16	± 1	± 0.83	± 1	%

Anastasiou, Duhr, Dulat, EF, Gehrmann, Herzog,
Lazopoulos, Mistlberger, JHEP 05 (2016) 058

$$\sigma = 48.58\,\text{pb}^{+2.22\,\text{pb}\,(+4.56\%)}_{-3.27\,\text{pb}\,(-6.72\%)}(\text{theory}) \pm 1.56\,\text{pb}\,(3.20\%)(\text{PDF}+\alpha_s)$$

Gluon-fusion Higgs production

- room for improvement!

σ	δ(PDF)	$\delta(\alpha_s)$	δ(scale)	δ(trunc)	δ(PDF-TH)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	
48.58	$\pm$0.90	$^{+1.27}_{-1.25}$	$^{+0.10}_{-1.15}$	$\pm$0.18	$\pm$0.56	$\pm$0.49	$\pm$0.40	$\pm$0.49	pb
	$\pm$ 1.86	$^{+2.61}_{-2.58}$	$^{+0.21}_{-2.37}$	$\pm$0.37	$\pm$ 1.16	$\pm$ 1	$\pm$0.83	$\pm$ 1	%

Anastasiou, Duhr, Dulat, EF, Gehrmann, Herzog,
Lazopoulos, Mistlberger, JHEP 05 (2016) 058

➡ if we manage to get under control these calculations, we achieve our aim of halving the theory error on ggH!

Gluon-fusion Higgs production

- room for improvement!

σ	δ(PDF)	$\delta(\alpha_s)$	δ(scale)	δ(trunc)	δ(PDF-TH)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	
48.58	$\pm$0.90	$^{+1.27}_{-1.25}$	$^{+0.10}_{-1.15}$	$\pm$0.18	$\pm$0.56	$\pm$0.49	$\pm$0.40	$\pm$0.49	pb
	$\pm$ 1.86	$^{+2.61}_{-2.58}$	$^{+0.21}_{-2.37}$	$\pm$0.37	$\pm$ 1.16	$\pm$ 1	$\pm$0.83	$\pm$ 1	%

✓ Mistlberger, JHEP 05 (2018) 028

Gluon-fusion Higgs production

- room for improvement!

σ	δ(PDF)	$\delta(\alpha_s)$	δ(scale)	δ(trunc)	δ(PDF-TH)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	
48.58	$\pm$0.90	$^{+1.27}_{-1.25}$	$^{+0.10}_{-1.15}$	$\pm$0.18	$\pm$0.56	$\pm$0.49	$\pm$0.40	$\pm$0.49	pb
	$\pm$ 1.86	$^{+2.61}_{-2.58}$	$^{+0.21}_{-2.37}$	$\pm$0.37	$\pm$ 1.16	$\pm$ 1	$\pm$0.83	$\pm$ 1	%

- work in progress
  - exact three-loop amplitude
  - full cross section in the opposite regime of massless gauge bosons $\rightarrow$ results in the two limits within 0.6% of each other!

Bonetti, Melnikov, Tancredi, PRD 97 (2018) 056017

Anastasiou, del Duca, EF, Mistlberger, Moriello, Schweizter, Specchia, JHEP 03 (2019) 162

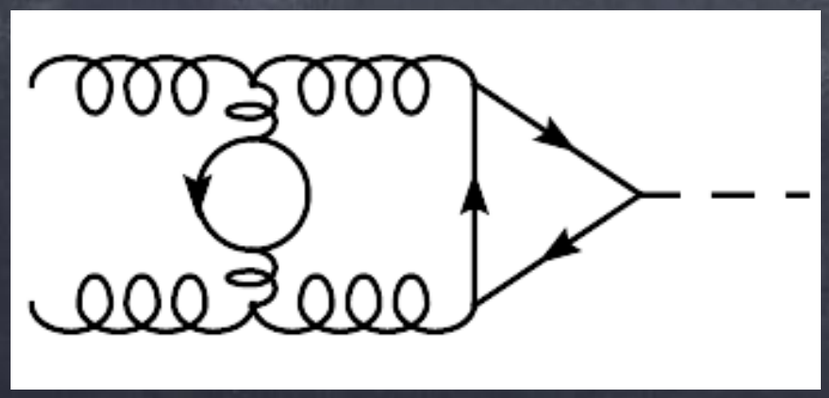
Gluon-fusion Higgs production

- room for improvement!

σ	δ(PDF)	$\delta(\alpha_s)$	δ(scale)	δ(trunc)	δ(PDF-TH)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	
48.58	$\pm$0.90	$^{+1.27}_{-1.25}$	$^{+0.10}_{-1.15}$	$\pm$0.18	$\pm$0.56	$\pm$0.49	$\pm$0.40	$\pm$0.49	pb
	$\pm$ 1.86	$^{+2.61}_{-2.58}$	$^{+0.21}_{-2.37}$	$\pm$0.37	$\pm$ 1.16	$\pm$ 1	$\pm$0.83	$\pm$ 1	%

- available: study of the contribution from light quarks at NNLO

Caola, Lindert, Melnikov, Monni, Tancredi, Wever, JHEP 09 (2018) 35

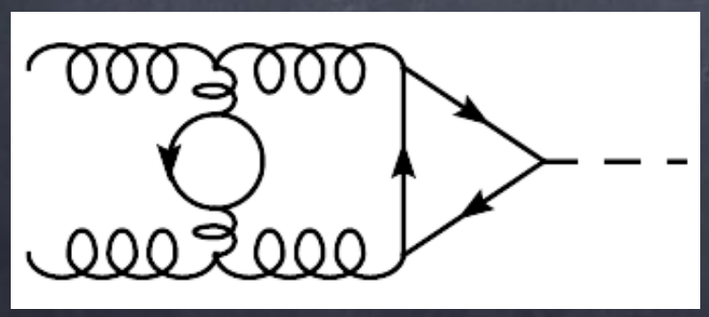


Gluon-fusion Higgs production

- room for improvement!

σ	δ(PDF)	$\delta(\alpha_s)$	δ(scale)	δ(trunc)	δ(PDF-TH)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	
48.58	$\pm$0.90	$^{+1.27}_{-1.25}$	$^{+0.10}_{-1.15}$	$\pm$0.18	$\pm$0.56	$\pm$0.49	$\pm$0.40	$\pm$0.49	pb
	$\pm$ 1.86	$^{+2.61}_{-2.58}$	$^{+0.21}_{-2.37}$	$\pm$0.37	$\pm$ 1.16	$\pm$ 1	$\pm$0.83	$\pm$ 1	%

- same calculation:



+ other 500 diagrams
+ radiation

→ new classes of multiloop integrals that depend on multiple mass scales

Outlook

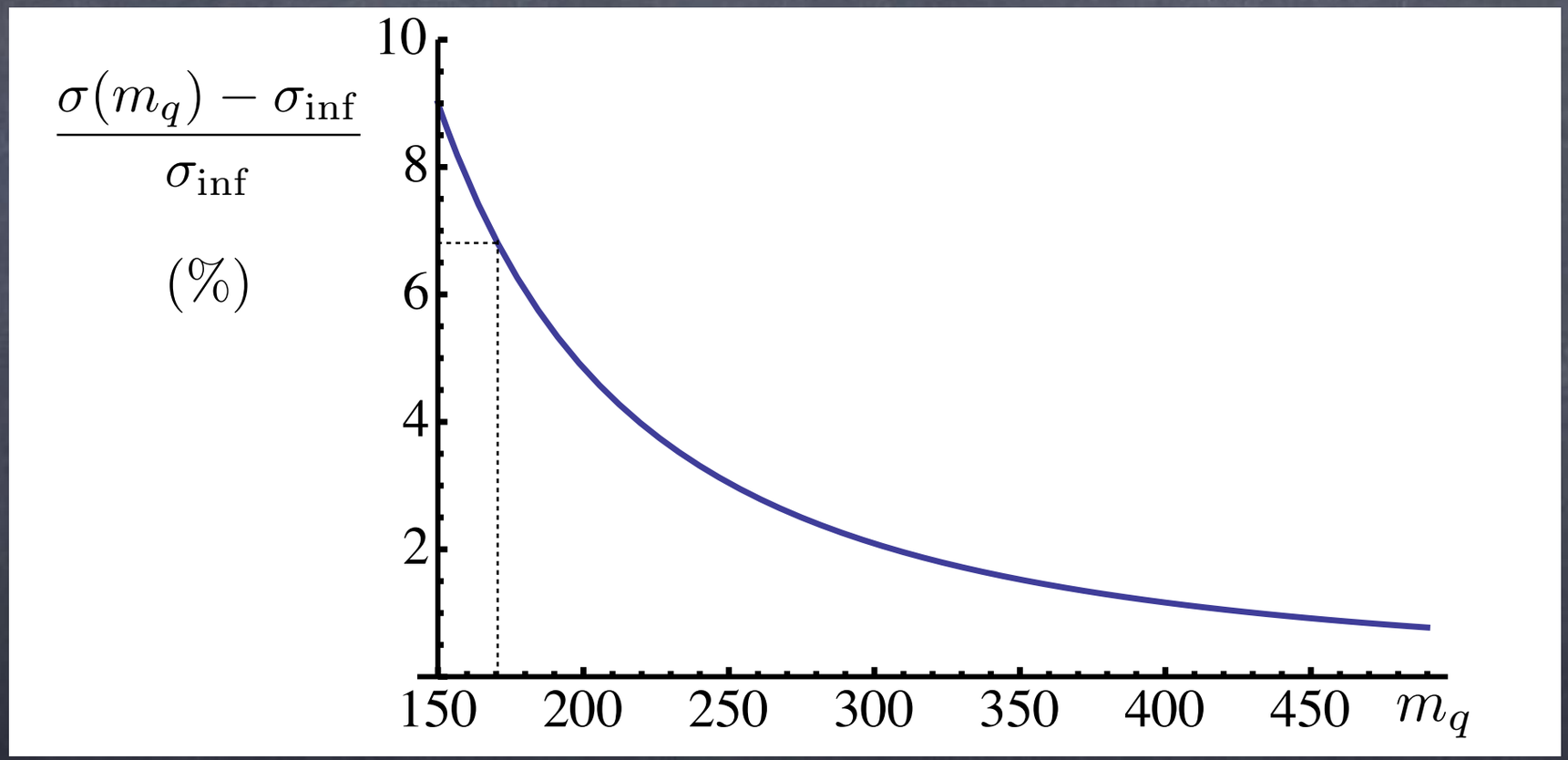
- The calculation of the gluon-fusion Higgs production cross section at N^3LO is a milestone result
  - phenomenological impact
  - completely new classes of integrals
- still room for improvement
  - ➡ an additional reduction of the theory error by 50% (“S2”) is achievable
  - ➡ break through the barrier of three–loop calculations with full mass dependance!

Stay tuned, lots of new developments coming up!

Finite mass effects

(top quark)

- How good is the heavy-top approximation?
  - at LO



Finite mass effects

(top quark)

- at NLO, "improve" the EFT result by rescaling it with the exact LO cross section:

$$\sigma_{EFT}^{NLO} = 34.66 \text{ pb}$$
$$\sigma_{ex}^{NLO} = 36.60 \text{ pb}$$

0.65%

$$\sigma_{EFT,r}^{NLO} = R_{LO} \times \sigma_{EFT}^{NLO} = 36.84 \text{ pb}$$

$$R_{LO} = \frac{\sigma_{exact}^{LO}}{\sigma_{EFT}^{LO}} \simeq 1.06$$

$\sqrt{S}$	13TeV
m_h	125GeV
PDF	`PDF4LHC15_nnlo_100`
$a_s(m_Z)$	0.118
$m_t(m_t)$	162.7 $(\overline{MS})$
$m_b(4.18GeV)$	4.18 $(\overline{MS})$
$m_c(3GeV)$	0.986 $(\overline{MS})$
$\mu = \mu_R = \mu_F$	62.5 $(= m_h/2)$

Finite mass effects

(top quark)

- rescale NNLO and N^{3}LO cross sections, computed in the EFT, by R_{LO}

- at NNLO, include known m_H/m_t corrections

$$gg \sim +0.8\%$$

$$qg \sim -0.1\%$$

Harlander, Ozeren; Pak, Rogal, Steinhauser; Mantler, Marzani

- tiny effect ➜ confirms the validity of the rescaled EFT
- the error due to unknown top-mass effects at NNLO is estimated as

$$\delta(1/m_t) \sim \pm 1\%$$

Harlander, Ozeren; Pak, Rogal, Steinhauser; Mantler, Marzani

Full NLO mass effects

(top, bottom, charm quark)

- The full dependance of the Higgs production cross section on the quark mass is known exactly through NLO

Spira, Djouadi, Graudenz, Zerwas ; Harlander, Kant; Aglietti, Bonciani, Degrassi, Vicini.

- include it for top, bottom and charm quarks

$\sigma^{NLO}_{ex;t}$ $\sigma^{NLO}_{ex;t+b}$ $\sigma^{NLO}_{ex;t+b+c}$

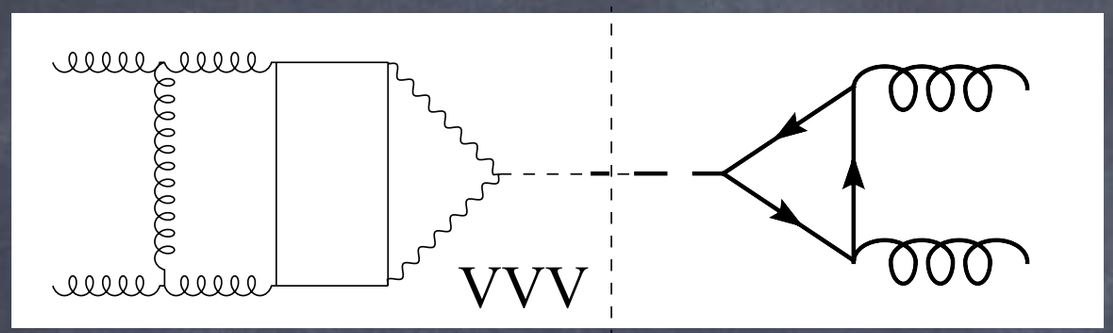
0.65% 5.1% 5.6% on $\sigma^{NLO}_{EFT,r}$

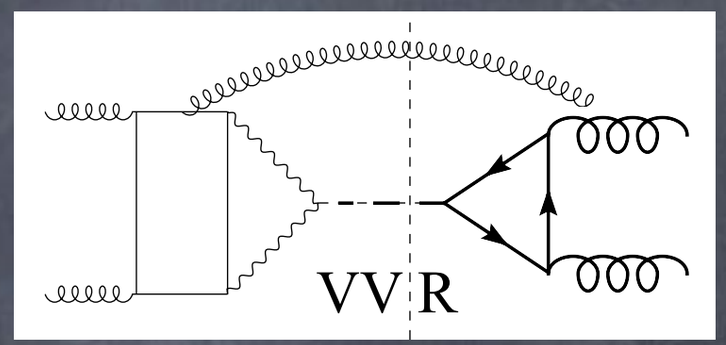
- estimate the error from unknown light-quark effects at NNLO as

$$\delta(tbc) = \pm \left| \frac{\delta\sigma^{NLO}_{ex;t} - \delta\sigma^{NLO}_{ex;t+b+c}}{\delta\sigma^{NLO}_{ex;t}} \right| \delta\sigma^{NNLO}_{EFT+\frac{1}{m_t}} \simeq \pm 0.31\,\text{pb} \quad (\pm 0.6\%)$$

NLO QCD-EW corrections

- contributions:





Bonetti, Melnikov, Tancredi, PRD 97 (2018) 056017

Anastasiou, Del Duca, EF, Mistleberger, Moriello, Schweitzer, Specchia, in preparation

Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- estimate of unknown higher order corrections, obtained by varying the factorisation and renormalisation scales around the central value ($m_H/2$) by a factor of 2

Anatomy of the N³LO uncertainty

σ	$\delta(\text{scale})$	$\delta(\text{PDF-TH})$	$\delta(\text{trunc})$	$\delta(\text{EW})$	$\delta(tbc)$	$\delta(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- error introduced computing the N³LO cross section using NNLO PDFs
- estimated from the analogous relative error one obtains at NNLO using NLO instead of NNLO PDFs

Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- the 2016 result was computed as an expansion around the threshold production of an Higgs boson, with additional radiation being soft
- a finite number of terms (37) was kept in this expansion, and an estimate on the convergence of the series was derived

Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- the new prediction

$$\sigma = 48.68\ \text{pb}\ ^{+2.07\ \text{pb}}_{-3.16\ \text{pb}}$$

  does not rely on the threshold approximation

- it is consistent with the previous result

- it eliminates the “truncation error”

Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- both due to the unknown exact-mass effects at NNLO

Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW)	$\delta(tbc)$	$\delta(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

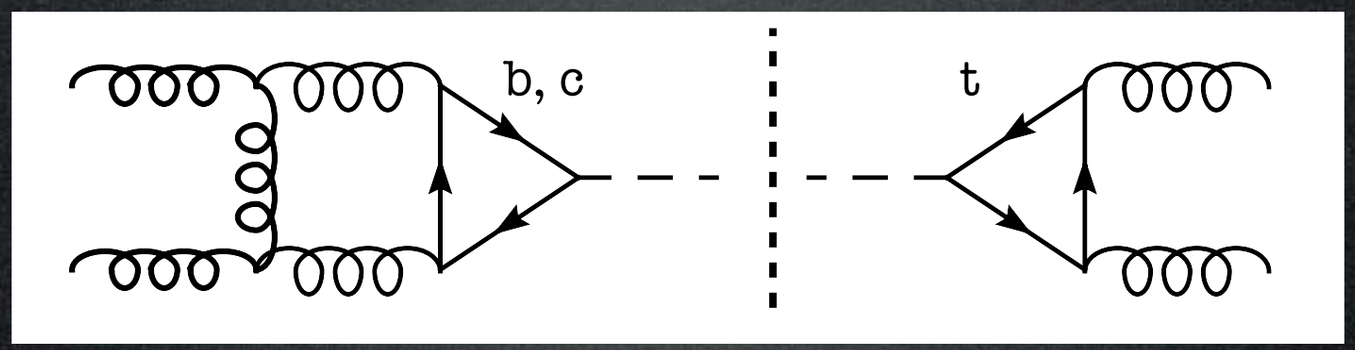
- for the top quark, leading finite-mass corrections compute as a $1/m_t$ expansion

Harlander and Ozeren, JHEP 0911, 088 (2009); Pak et al., JHEP 1002, 025 (2010)

Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW	$\delta(tbc)$	$(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- also light quarks, in particular the bottom, are important at this level of accuracy, due to the interference with the LO top loop



Anatomy of the N³LO uncertainty

σ	δ(scale)	δ(PDF-TH)	δ(trunc)	δ(EW	$\delta(tbc)$	$(1/m_t)$	$\delta\sigma^{tot}$	
48.58	$^{+0.10}_{-1.15}$	± 0.56	± 0.18	± 0.49	± 0.40	± 0.49	$^{+2.22}_{-3.27}$	pb
	$^{+0.21}_{-2.37}$	± 1.16	± 0.37	± 1	± 0.83	± 1	$^{+4.56}_{-6.72}$	%

- also light quarks, in particular the bottom, are important at this level of accuracy, due to the interference with the LO top loop

$$\delta\sigma^{NLO}_{(t,b,c)} = -2.05 \ \text{pb}\,(-4.2\%)$$