

# Relic density at one-loop with neutralino/chargino coannihilation

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## RELIC DENSITY OF DARK MATTER

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- PLANCK : 2% precision



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⇒ RADIATIVE CORRECTIONS ARE IMPORTANT



## RELIC DENSITY

$$\Omega_{DM} h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma(\chi\chi \rightarrow SM)v \rangle}$$



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## PRECISION

- Need to know precisely  $\sigma \Rightarrow$  **one-loop** calculations
- Parameters **reconstruction** at the LHC/LC
- Check the underlying cosmological **scenario**



# SOME PREVIOUS WORK AT 1-L IN SUSY

## EW + QCD corrections

$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow \gamma\gamma, Z\gamma, gg$  : processes only possible at one-loop order

(Boudjema, Semenov, Temes)[hep-ph :0507127]

$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow ZZ, W^+W^-$  (Baro, Boudjema, Semenov)[hep-ph :0710.1821, Phys.Lett B660(2008) 550]

$\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow \tau^+\tau^-, b\bar{b}$  (Baro, Boudjema, Semenov)[hep-ph :0710.1821, Phys.Lett B660(2008) 550]

Co-annihilation with  $\tilde{t}$  (Baro, Boudjema, Semenov)[hep-ph :0710.1821, Phys.Lett B660(2008) 550]

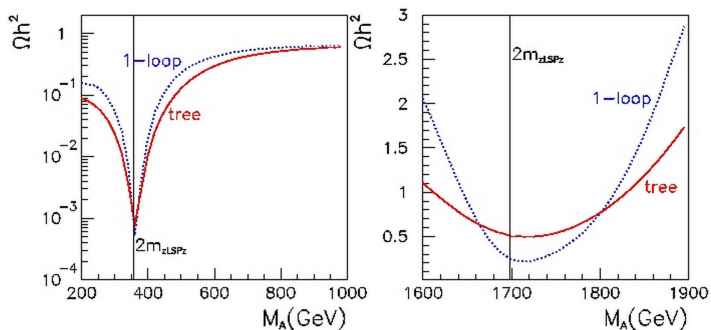
## QCD corrections

Co-annihilation with  $\tilde{t}$  (Freitas)[Phys.Lett. B652 (2007) 280]



# Example with MicrOMEGAs

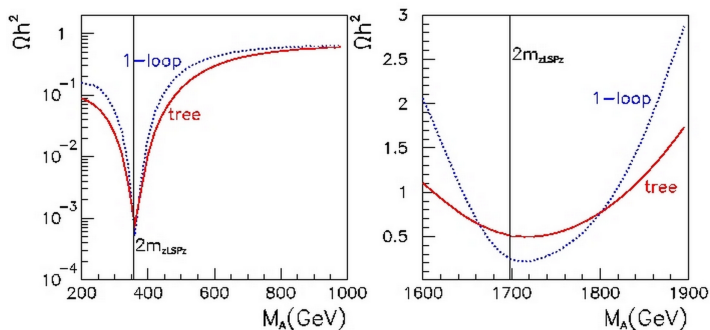
With one-loop effective lagrangian :





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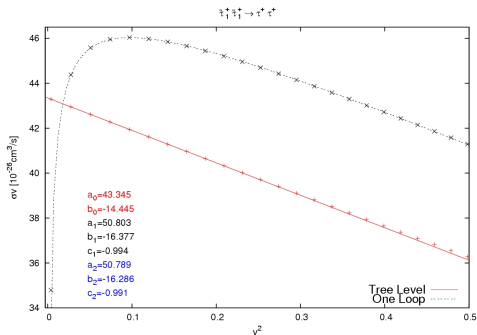
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⇒ EXCLUSION OF MODELS AT ONE-LOOP

# Example with **SloopS**

With **full** one-loop electroweak corrections :



$$\langle \sigma v \rangle \simeq a + b \langle v^2 \rangle$$

$$a = s - \text{wave coefficient}$$

$$b = p - \text{wave coefficient}$$



# PRESENT STUDY : COANNIHILATION WITH CHARGINOS/NEUTRALINOS

- It is already known that calculating the relic density including **coannihilation** effects can significantly change the results.
- Regions of parameters difficult to probe (in mSUGRA) in colliders are regions where coannihilation comes into account for the relic density.
- Coannihilation can be important for **Higgsino-like**, **mixed** or **gaugino-like** neutralino.
- It should be included in calculation whenever  $|\mu| \lesssim 2|M_1|$
- Can push the relic density **in** or **out** the cosmologically interesting region, as one-loop calculations do.



# BATTLE PLAN

To deal with radiative corrections we need :



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Loop Integrals to handle **Gram determinant** when  $v \rightarrow 0$

To deal with **IR** and **collinear divergencies**  $\rightarrow$  include bremsstrahlung.





# INPUT PARAMETERS IN CHARGINO/NEUTRALINO SECTOR

## AT TREE-LEVEL...

- The 4x4 neutralino mass matrix is defined as :

$$Y = \begin{pmatrix} M_1 & 0 & -c_\beta s_W M_Z & s_\beta s_W M_Z \\ 0 & M_2 & c_\beta c_W M_Z & -s_\beta c_W M_Z \\ -c_\beta s_W M_Z & c_\beta c_W M_Z & 0 & -\mu \\ s_\beta s_W M_Z & -s_\beta c_W M_Z & -\mu & 0 \end{pmatrix}$$

- The 2x2 chargino mass matrix is :

$$X = \begin{pmatrix} M_2 & \sqrt{2} s_\beta M_W \\ \sqrt{2} c_\beta M_W & \mu \end{pmatrix}$$



# INPUT PARAMETERS IN CHARGINO/NEUTRALINO SECTOR

## AND AT ONE-LOOP

- The 4x4 neutralino CT mass matrix is defined as :

$$\delta Y = \begin{pmatrix} \delta M_1 & 0 & \delta Y_{13} & \delta Y_{14} \\ 0 & \delta M_2 & \delta Y_{23} & \delta Y_{24} \\ \delta Y_{13} & \delta Y_{23} & 0 & -\delta\mu \\ \delta Y_{14} & \delta Y_{24} & -\delta\mu & 0 \end{pmatrix}$$

- The 2x2 CT chargino mass matrix is :

$$\delta X = \begin{pmatrix} \delta M_2 & \sqrt{2}s_\beta M_W \left( \frac{1}{2} \frac{\delta M_W^2}{M_W^2} + c_\beta^2 \frac{\delta t_\beta}{t_\beta} \right) \\ \sqrt{2}c_\beta M_W \left( \frac{1}{2} \frac{\delta M_W^2}{M_W^2} - s_\beta^2 \frac{\delta t_\beta}{t_\beta} \right) & \delta\mu \end{pmatrix}$$



- With this sector we can determine  $M_1, M_2, \mu$  and the corresponding counter-terms  $\delta M_1, \delta M_2, \delta \mu$
- Remaining counter-terms are determined in the gauge and higgs sector ( $\delta\alpha$  (defined with  $\alpha(0)$ ),  $\delta M_W^2, \delta s_W^2, \delta t_\beta$ ).
- To determine it we trade these parameters to **physical observables** (input parameters like masses)
- Different choice of input parameters (chargino/neutralino sector) :



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⇒ **DIFFERENT PREDICTIONS**  
(different  $\delta M_1, \delta M_2, \delta \mu$ )



# SOME REMARKS

- For general purpose the first input scheme is **well adapted** :
  - only diagonalisation of a  $2 \times 2$  matrix
  - for a mSUGRA type model we can reconstruct easily the fundamental parameters (provided that  $M_1 \ll M_2 \ll |\mu|$ )





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  - only diagonalisation of a  $2 \times 2$  matrix
  - for a mSUGRA type model we can reconstruct easily the fundamental parameters (provided that  $M_1 \ll M_2 \ll |\mu|$ )
- But some **drawbacks** :
  - $\delta' s \propto \frac{1}{\mu^2 - M_2^2}$
  - $\tilde{\chi}_2^0$  gets a correction at one-loop  $\Rightarrow$  care must be taken if it's on an external leg
- For calculation of relic density at one-loop the 2<sup>nd</sup> input scheme is better suited in case of **coannihilation** between  $\tilde{\chi}_1^0$  and  $\tilde{\chi}_2^0$



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Only  $MH, A^0_{\tau\tau}$  are gauge independent



# OVERVIEW OF THE CALCULATION

⇒ MIXED CASE to have coannihilation channels

$$M_1 = 110 \text{ GeV}, M_2 = 127 \text{ GeV}, \mu = -245 \text{ GeV}$$

$$\tan \beta = 10, M_A = 600 \text{ GeV}$$

$$m_{\tilde{f}} = 600 \text{ GeV}, m_{\tilde{\chi}_1^0} = 106 \text{ GeV}$$

At tree-level :

- $\tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow W^+ W^-$  : 40%
- $\tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow W^+ W^-$  : 6%
- $\tilde{\chi}_1^0 \tilde{\chi}_1^+ \rightarrow W^+ Z$  : 5%
- $\tilde{\chi}_1^0 \tilde{\chi}_1^+ \rightarrow u \bar{d}$  : 9%
- $\tilde{\chi}_1^0 \tilde{\chi}_1^+ \rightarrow c \bar{s}$  : 9%

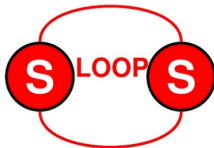




# OVERVIEW OF THE CALCULATION

At tree-level we have for process involving W's 7 diagrams

At one-loop we have  $\simeq 7000$  diagrams  $\rightarrow$  need for automation



A code for calculating one-loop diagrams including a **complete** and **coherent** renormalisation of the MSSM with an **OS scheme** (cf Nans Baro's talk).



# OVERVIEW OF THE CALCULATION

Using this program we calculated the one-loop cross section in the 2 schemes presented above :

- $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_1^+}, m_{\tilde{\chi}_2^+}$  (o1c1c2 scheme)
- $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^+}$  (o1o2c1 scheme)

And for both schemes we analyzed the  $t_\beta$  scheme dependence

For one-loop calculations several checks have to be done :

- UV finiteness
- IR safety (for process involving quarks we used the soft approximation to deal with  $g$  emission)
- gauge independence



To calculate the relic density we had to :

- use an approximation for thermal average :  
 $\langle \sigma_{ij} v_{ij} \rangle = a_{ij} + 6(b_{ij} - a_{ij}/4)/x \quad (x = m_{\tilde{\chi}_1^0}/T)$
- include coannihilation (Boltzmann factor  $\propto e^{-(m_{NLSP} - m_{LSP})}$ )

Our final formula is :

$$\Omega h^2 = \left( \frac{10}{\sqrt{g_*(x_F)} 24} x_F \right) \frac{0.237 \times 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}}{x_F J}$$

$$J = \int_{x_F}^{\infty} \langle \sigma v \rangle_{\text{eff}} dx / x^2$$

$$\langle \sigma v \rangle_{\text{eff}} = \sum_{ij} \frac{g_{i,\text{eff}} g_{j,\text{eff}}}{g_{\text{eff}}^2} \langle \sigma_{ij} v_{ij} \rangle$$



# THEORETICAL DIFFERENCES BETWEEN THE TWO SCHEMES

Tree-level masses(GeV) :

$$M_1 = 110, M_2 = 127, \mu = -245$$

$$m_{\chi_1^0} = 106.47, m_{\chi_2^0} = 119.34, m_{\chi_1^+} = 118.20, m_{\chi_2^+} = 274.06$$



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$m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_1^+}, m_{\tilde{\chi}_2^+}$

$$m_{\tilde{\chi}_1^+}, m_{\tilde{\chi}_2^+} \rightarrow M_2, \mu$$

$$m_{\tilde{\chi}_1^0} \rightarrow M_1$$



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$$m_{\tilde{\chi}_1^0} \rightarrow M_1$$

$\Rightarrow \mu$  is difficult to reconstruct  
in the 2<sup>nd</sup> scheme





# CORRECTED MASSES

$$m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_1^\pm}, m_{\tilde{\chi}_2^\pm}$$

Masses	$m_{\tilde{\chi}_1^0}$	$m_{\tilde{\chi}_2^0}$	$m_{\tilde{\chi}_3^0}$	$m_{\tilde{\chi}_4^0}$	$m_{\tilde{\chi}_1^\pm}$	$m_{\tilde{\chi}_2^\pm}$
TL (Gev)	106.474	119.345	258.291	269.471	118.203	274.061
1-L (Gev) $A_{\tau\tau}$		119.210	258.707	269.453		
1-L (Gev) $\overline{DR}$		119.264	258.594	269.506		
1-L (Gev) MH		119.448	258.211	269.686		

$$m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^\pm}$$

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TL (Gev)	106.474	119.345	258.291	269.471	118.203	274.061
1-L (Gev) $A_{\tau\tau}$			254.959	270.802		266.254
1-L (Gev) $\overline{DR}$			256.347	272.107		267.588
1-L (Gev) MH			261.068	276.545		272.125



# PRELIMINARY RESULTS

Table of result for  $\langle\sigma v\rangle$

$(\times 10^{-26} \text{ cm}^3/\text{s})$

$\chi_1^0 \chi_1^0 \rightarrow W^+ W^-$	Tree Level	ATT		$\overline{DR}$		MH	
		o1o2c1	o1c1c2	o1o2c1	o1c1c2	o1o2c1	o1c1c2
a	3.37	+24.6%	+6.8%	+23.1%	+12.8%	+18.7%	+30.6%
b	4.8	+18.8%	+4.2%	+18.8%	+8.3%	+12.5%	+25%
$\chi_1^0 \chi_2^0 \rightarrow W^+ W^-$							
a	32	+16.3%	+10%	+15.6%	+11.9%	+14.1%	+18.8%
b	26	+15.3%	+7.7%	+15.3%	+11.5%	+15.3%	+13.3%
$\chi_1^0 \chi_1^+ \rightarrow W^+ Z$							
a	13.5	+10.4%	+2.2%	+9.3%	+3.7%	+3.7%	+10.4%
b	4.3	+2.3%	-4.6%	+2.3%	-2.3%	+4.7%	+9.3%
$\chi_1^0 \chi_1^+ \rightarrow u \bar{d}$							
a	31.6	+15.5%	+7.3%	+14.9%	+9.8%	+12.3%	+15.7%
b	-12.3	+12.2%	+4.1%	+11.4%	+6.7%	+8.9%	+15.4%



# PRELIMINARY RESULTS

Table of result for  $\langle\sigma v\rangle$  with  $\alpha(0) \rightarrow \alpha(M_Z^2)$

$(\times 10^{-26} \text{ cm}^3/\text{s})$

$\chi_1^0 \chi_1^0 \rightarrow W^+ W^-$	Tree	ATT		$\overline{\text{DR}}$		MH	
	Level	o1o2c1	o1c1c2	o1o2c1	o1c1c2	o1o2c1	o1c1c2
a	3.82	+9.9%	-2.6%	+8.6%	+0%	+4.7%	+15.8%
b	5.4	+5.6%	-7.4%	+5.6%	-3.7%	+0%	+11%
$\chi_1^0 \chi_2^0 \rightarrow W^+ W^-$							
a	36.3	+2.5%	-3%	+1.9%	-1.4%	+0.6%	+4.7%
b	30	+0%	-6.7%	+0%	-3.3%	-3.3%	+2.7%
$\chi_1^0 \chi_1^+ \rightarrow W^+ Z$							
a	15.2	-2.3%	-9.2%	-3.3%	-7.9%	-3.7%	-2%
b	4.9	-10%	-16.3%	-10%	-14.3%	-8.2%	-4.1%
$\chi_1^0 \chi_1^+ \rightarrow u \bar{d}$							
a	35.8	+1.9%	-5.3%	+1.4%	-3.1%	-0.8%	+4.7%
b	-13.9	-0.7%	-7.9%	-1.4%	-5.6%	-3.6%	+2.2%



Correction to  $\Omega h^2$  with  $\alpha(0)$

	ATT		DR		MH	
	o1o2c1	o1c1c2	o1o2c1	o1c1c2	o1o2c1	o1c1c2
$\frac{\delta\Omega h^2}{\Omega h^2}$	-11.3%	-3.8%	-10.6%	-6.3%	-8.8%	-13.1%



Correction to  $\Omega h^2$  with  $\alpha(M_Z^2)$

	ATT		DR		MH	
	o1o2c1	o1c1c2	o1o2c1	o1c1c2	o1o2c1	o1c1c2
$\frac{\delta\Omega h^2}{\Omega h^2}$	+1.7%	+9.2%	+2.4%	+6.7%	+4.2%	-0.1%



# UNDERSTANDING THE CORRECTIONS

- With  $\alpha(0) \rightarrow \alpha(M_Z^2)$  we reabsorb  $\simeq 13\%$  of corrections
- The  $m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^+}$  scheme is sensitive to  $\delta t_\beta$  whereas the cross-section is not and conversely for the other scheme.
- **Constructive**/**Destructive** effect of the various  $\delta t_\beta/t_\beta$  contribution
- Most important channel is the exchange of the  $\tilde{\chi}_1^+$  (strong  $g_{\tilde{\chi}_1^+ \tilde{\chi}_1^0 W^+}$  coupling)
- Strong dependence of the tree-level cross-section with respect to  $M_2$  (compared to the one in  $\mu$ )



# CONCLUSION

- Complete one-loop renormalisation of MSSM and **modularity** with different schemes
- Full understanding of the **underlying physics** of the radiative corrections in the chargino/neutralino sector.
- Reconstruction of **fundamental parameters** at **one-loop**.
- Introduce **effective** couplings?
- Connection with **MicrOMEGAs**

