

TeV-PeV COSMIC-RAY ANISOTROPY AS A PROBE OF THE LOCAL INTERSTELLAR TURBULENCE

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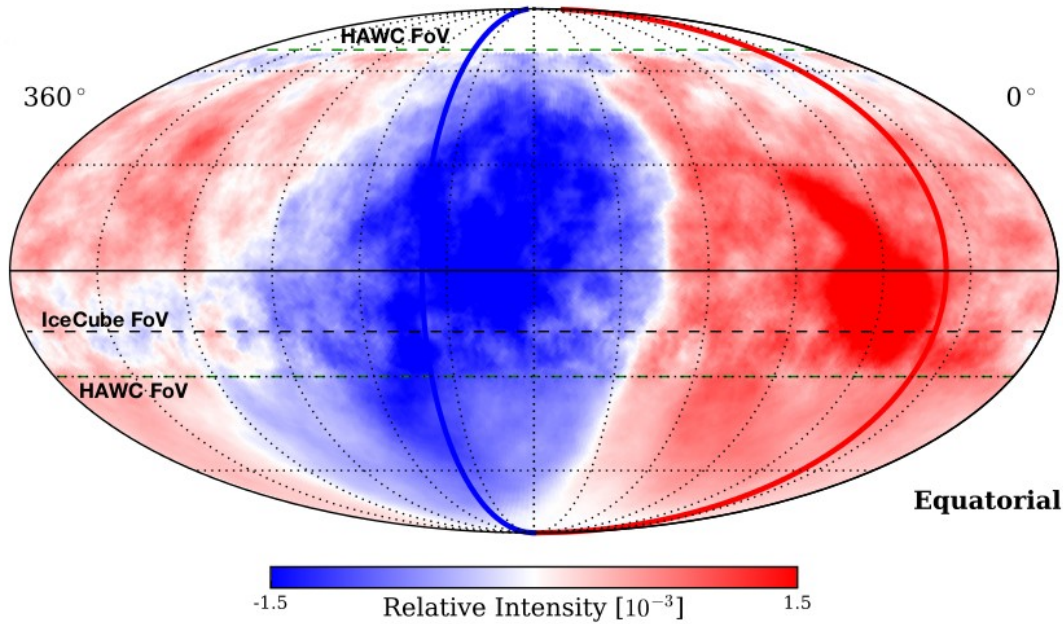
**GG, Brian Reville & Wenyi Bian (边稳懿), In Prep. (2021) –
*see also arXiv:1810.06396***

**GG & Kirk, ApJ 835, 258 (2017),
*arXiv:1610.06134***

**GG & Sigl, Phys. Rev. Lett. 109,
071101 (2012), *arXiv:1111.2536***

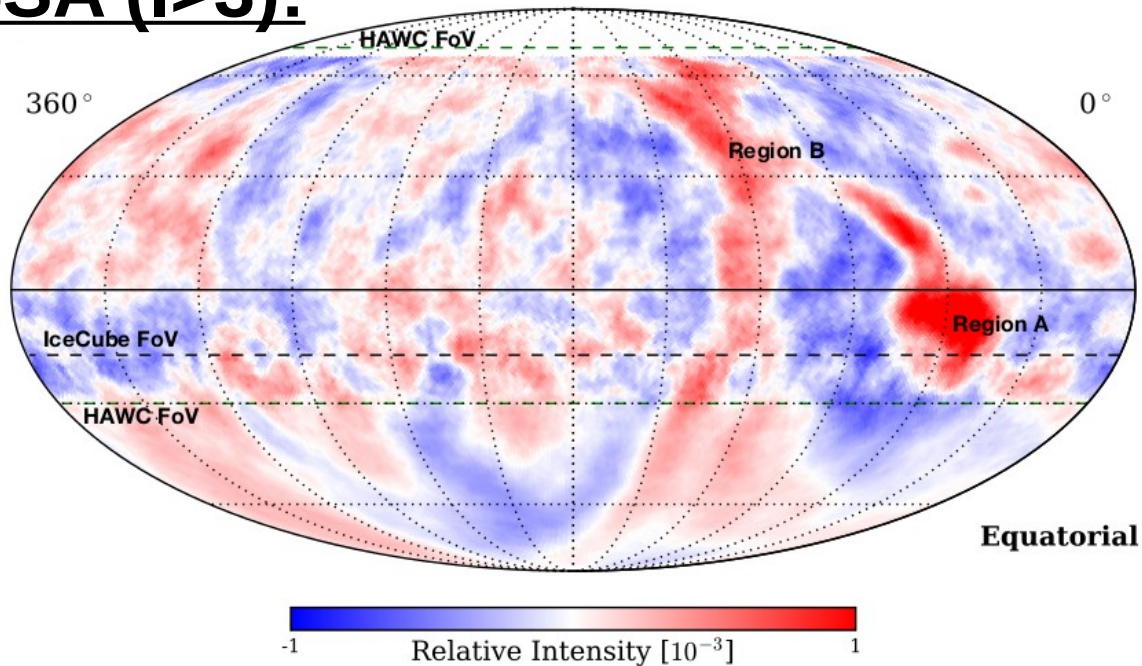


Large Scale Anisotropy (~0.1%) :



In the direction of field lines
SHAPE: NOT a dipole in general

SSA ($I > 3$):



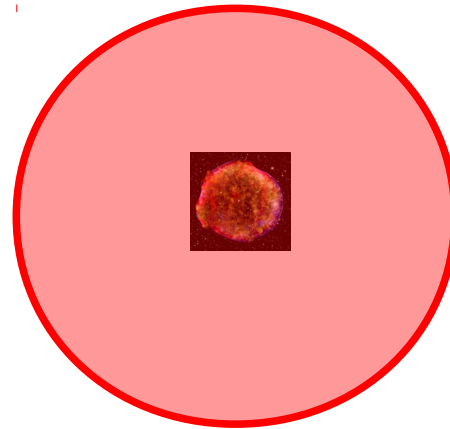
- Energy-dependent,
- No/Little time-dependence
- Amplitude: LSA/(few – 10)

CR Anisotropy



(Dipole) Anisotropy

→ **Direction**

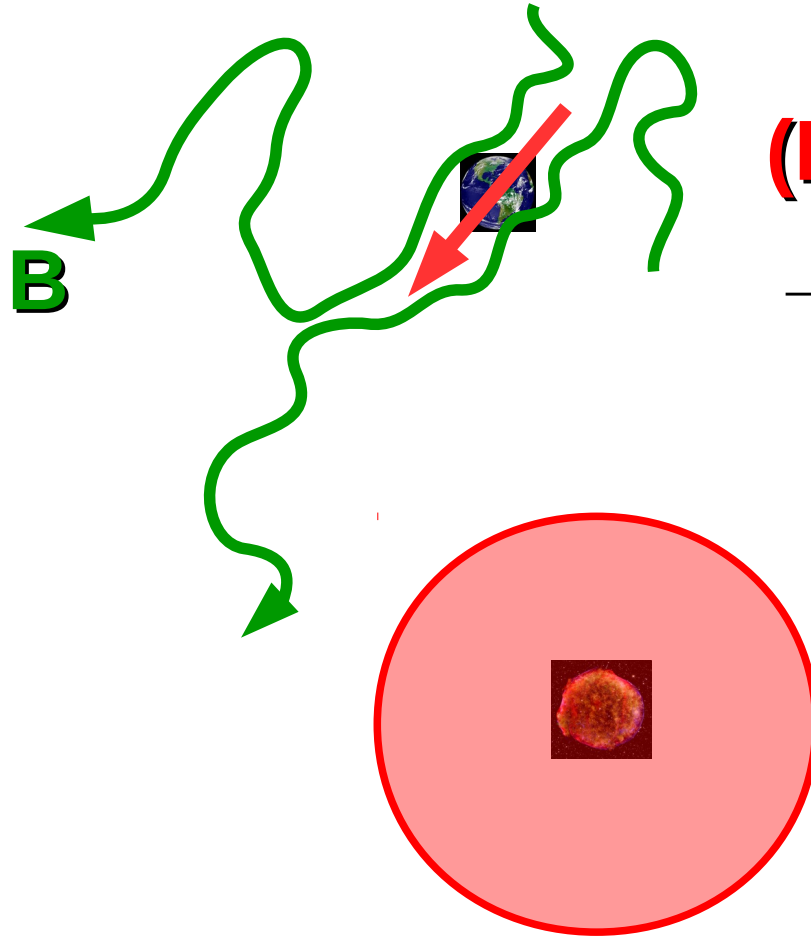


Amplitude

$$\delta(p) \simeq -\frac{3}{c_0} \frac{\mathbf{j}}{n} = \frac{3D(p)}{c_0} \frac{\nabla n}{n}$$

where $\mathbf{j}(\mathbf{r}, p) = -D(p)\nabla n$ is the CR current

CR Anisotropy



(Dipole) Anisotropy

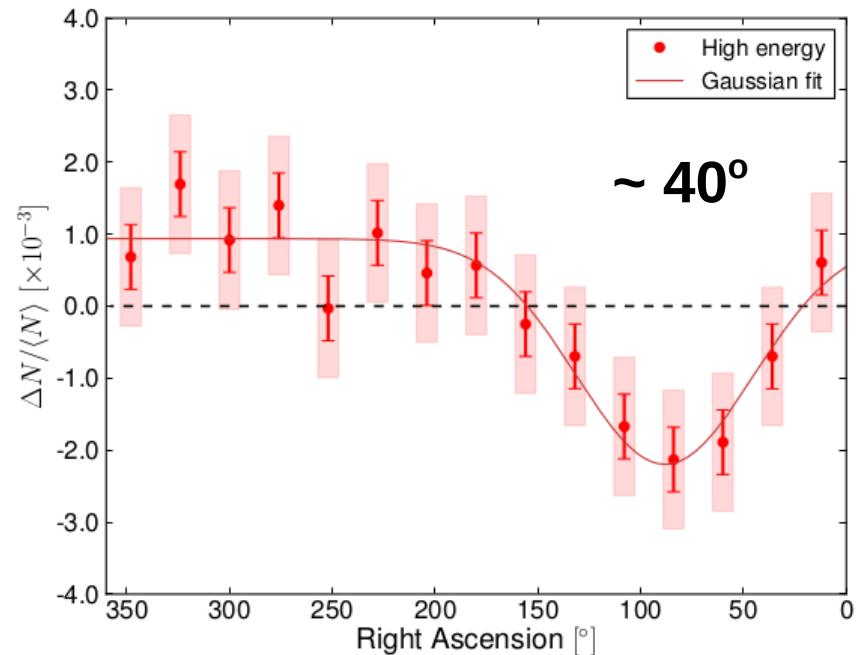
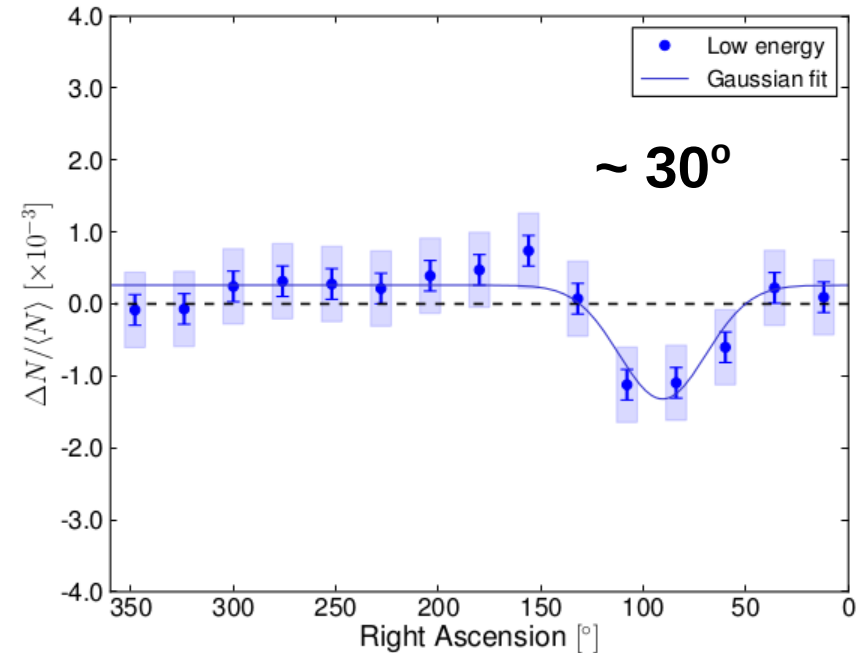
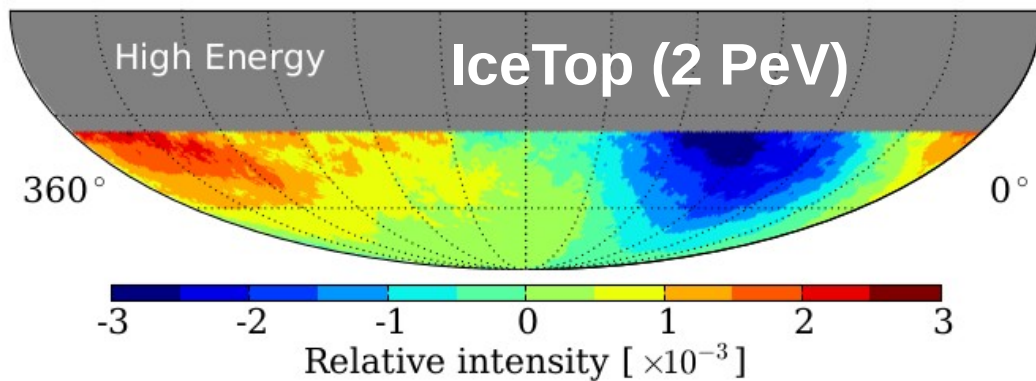
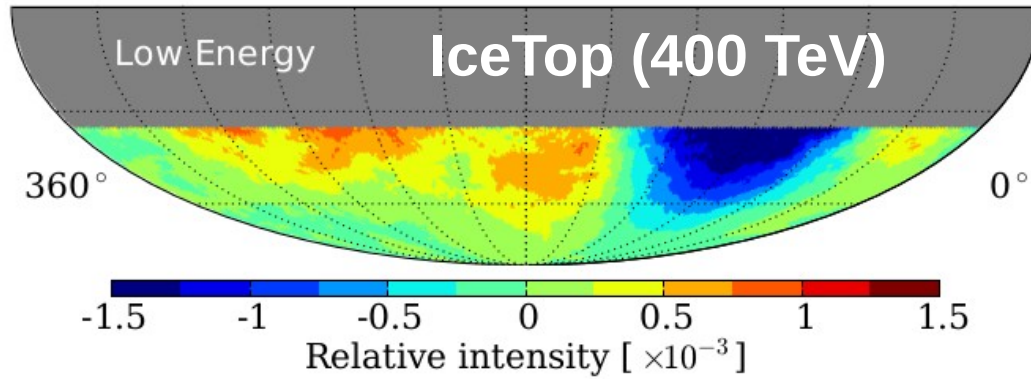
→ Direction B field

*cf. Schwadron et al.,
Science (2014)*

~ 180° flip at 100 TeV:
cf. Ahlers, PRL (2016)

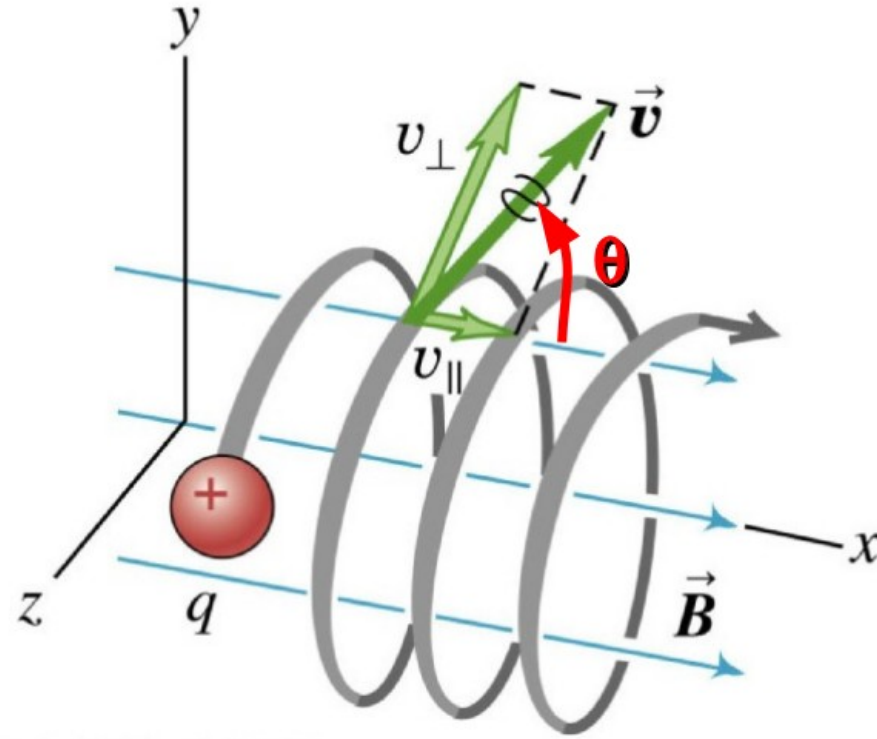
Observations (IceCube, IceTop)

Aartsen et al. (2013)



Also at 20 TeV...

Pitch-angle (θ) and gyrophase:

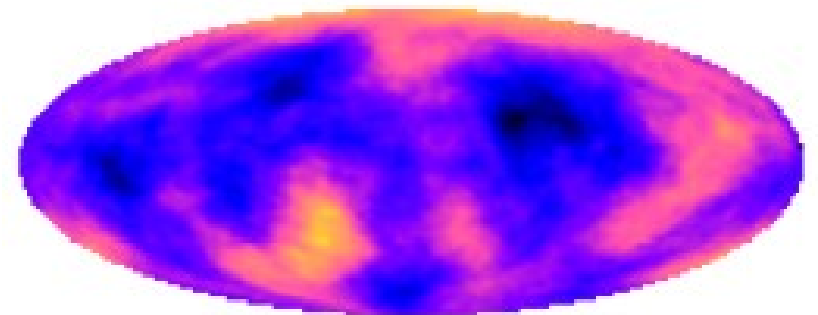
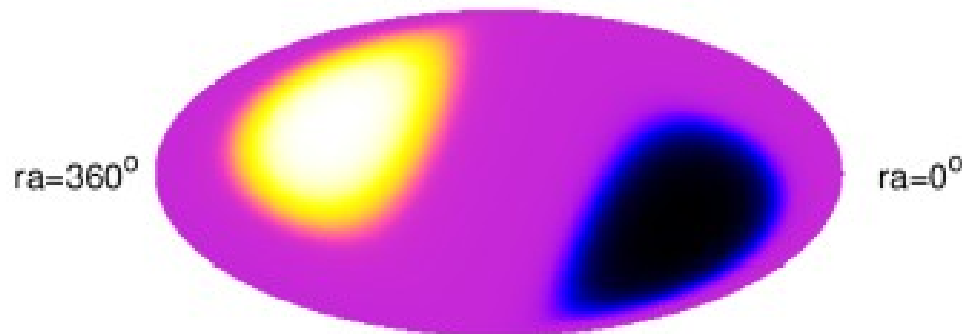


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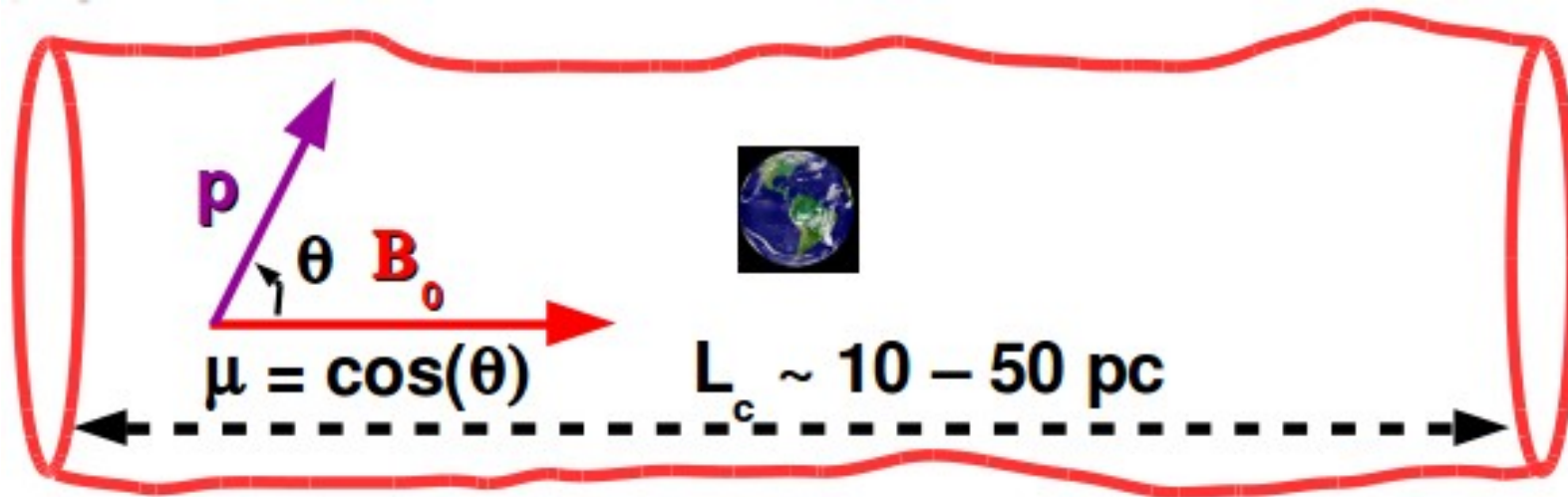
CRA = Large-scale

+

small-scales



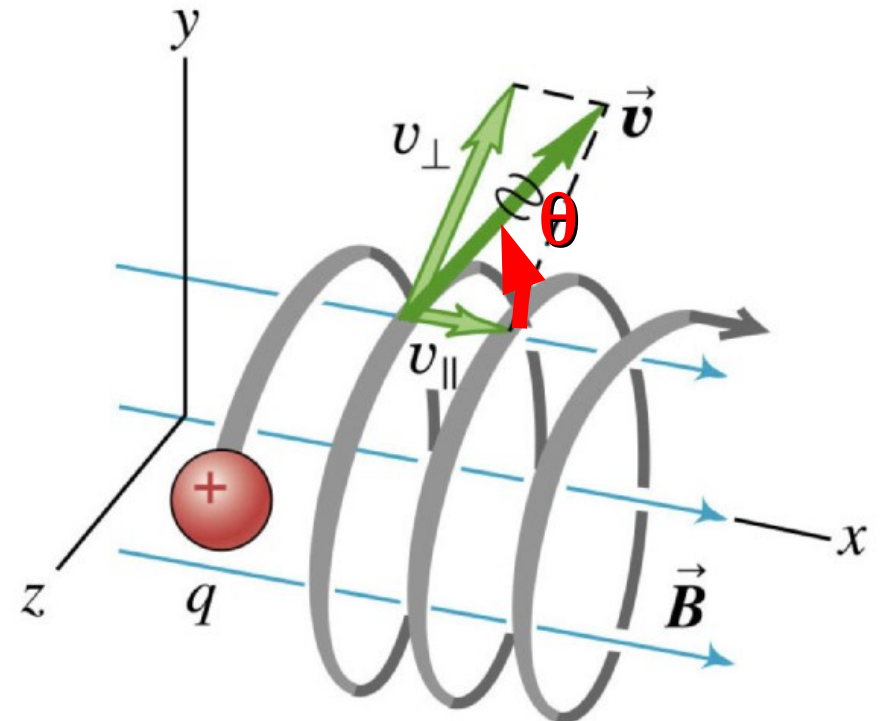
CR Anisotropy : Probe of turbulence



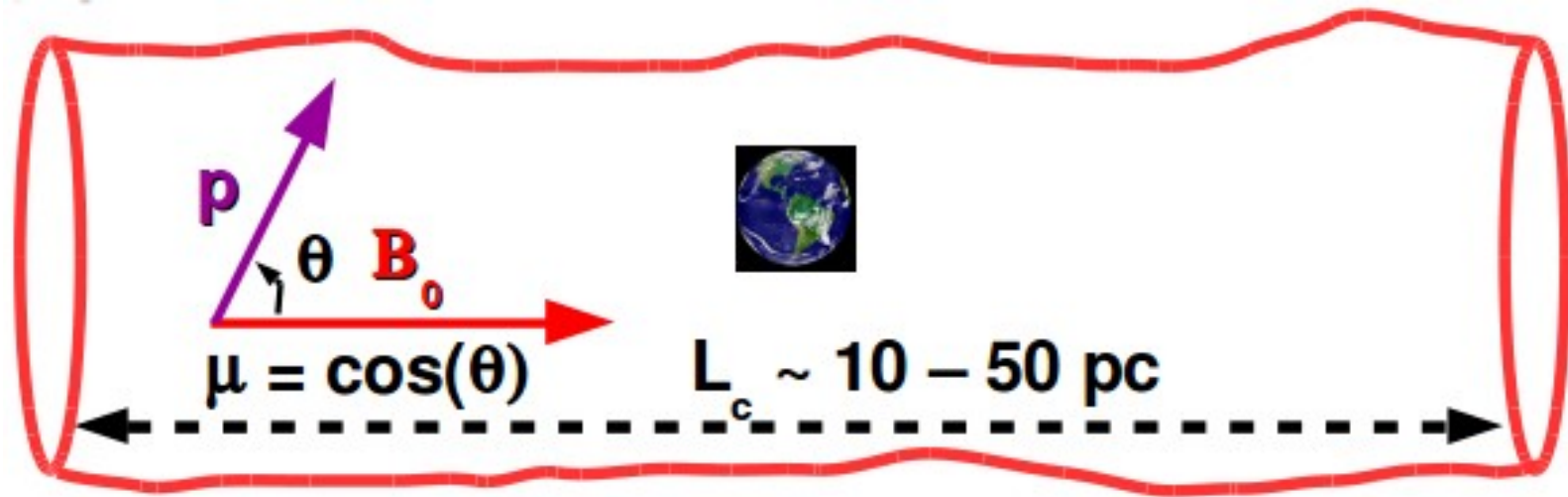
$$\mu v \frac{\partial f}{\partial x} = \frac{\partial}{\partial \mu} \left(D_{\mu\mu} \frac{\partial f}{\partial \mu} \right)$$

Pitch-angle diffusion

(gyrophase-averaged)



CR Anisotropy : Probe of turbulence



$$\mu v \frac{\partial f}{\partial x} = \frac{\partial}{\partial \mu} \left(D_{\mu\mu} \frac{\partial f}{\partial \mu} \right)$$

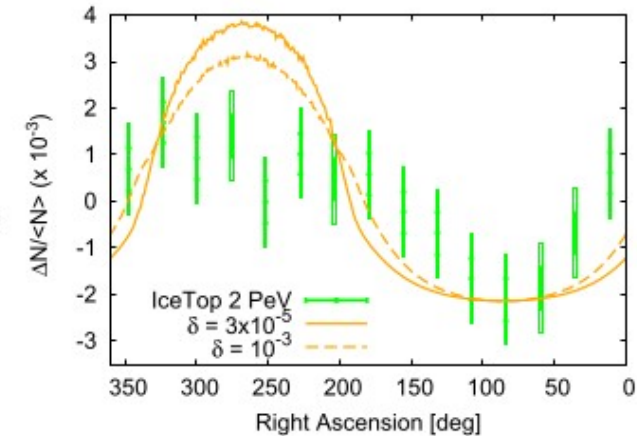
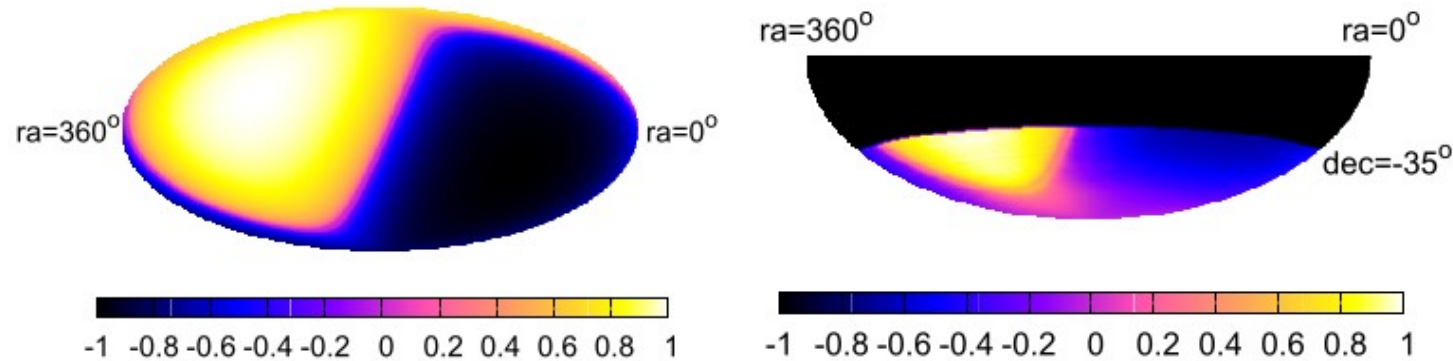
Aniso \propto

$$\int_0^\mu d\mu' \frac{1 - \mu'^2}{D_{\mu'\mu'}}$$

**NOT $1 - \mu^2$
in general !**

Case 1 : Fast modes & Narrow RF

No dependence of the *shape* on CR energy



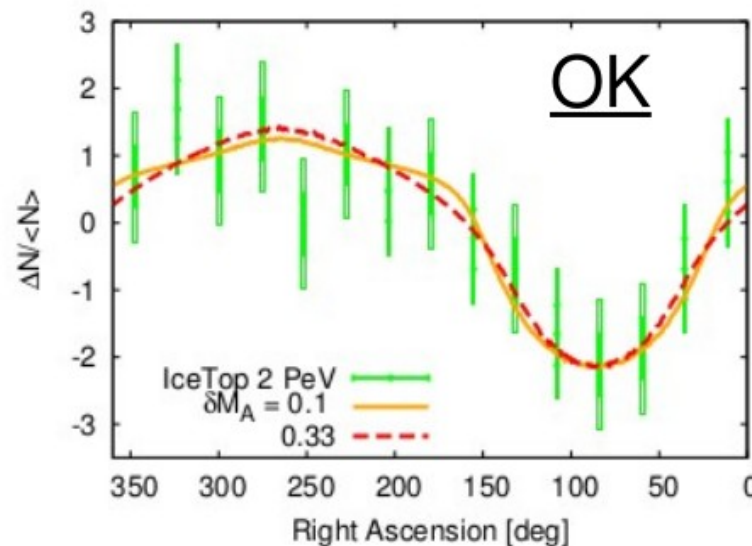
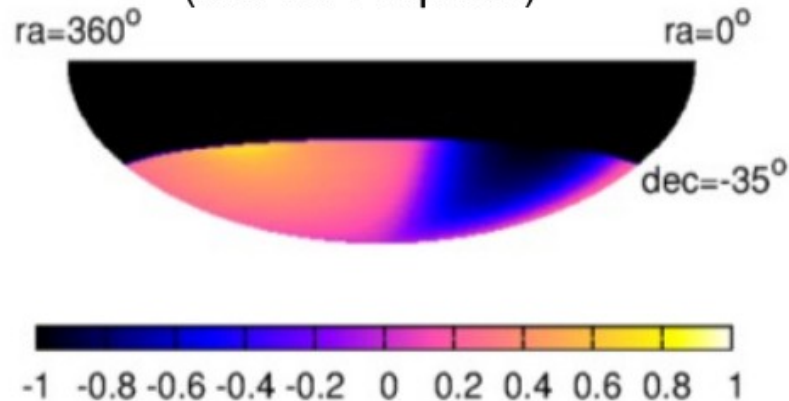
In general: Anisotropy too wide with narrow Res Fn =>

RULED OUT !

Case 2 : Fast modes & Broad RF

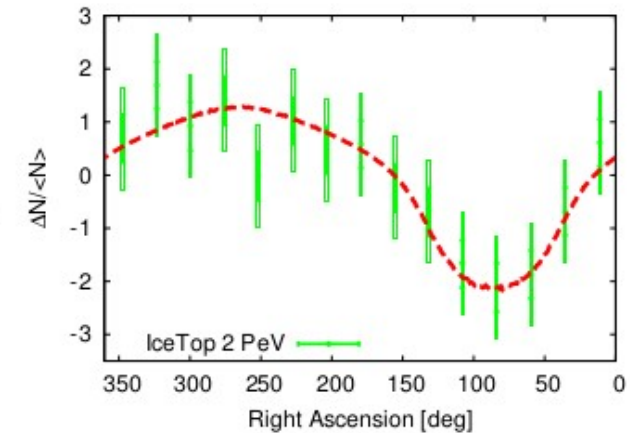
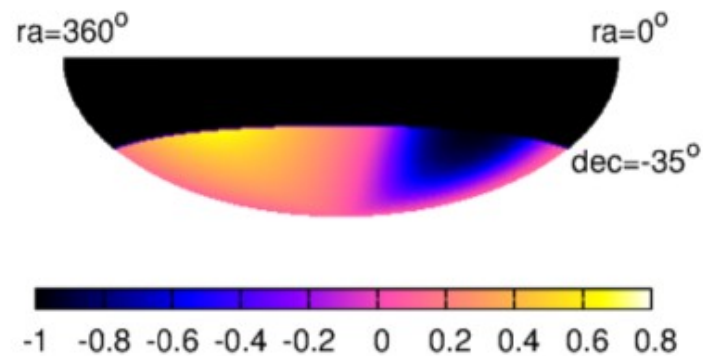
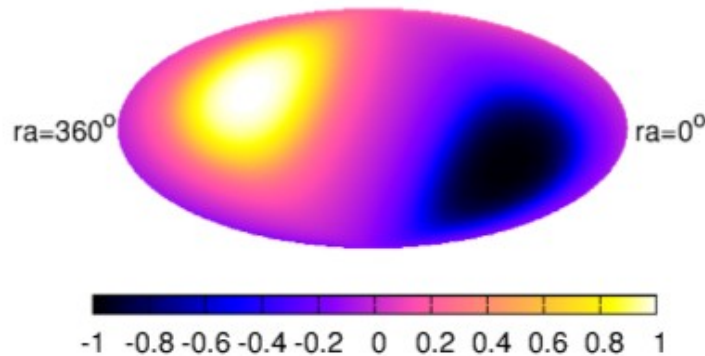
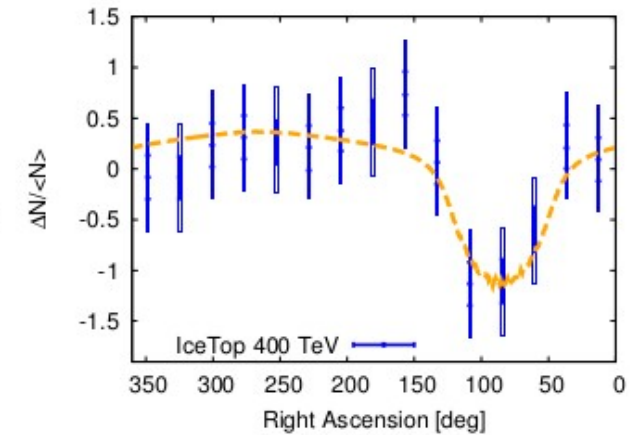
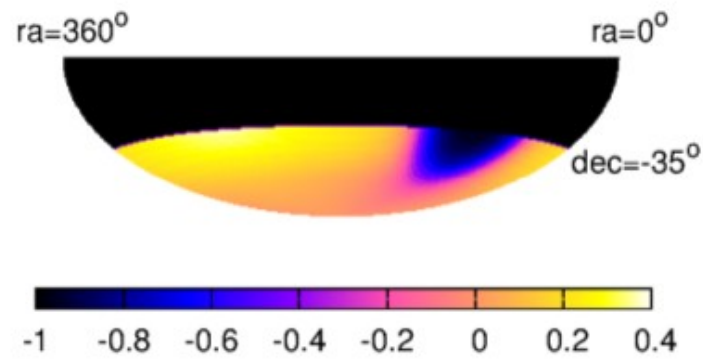
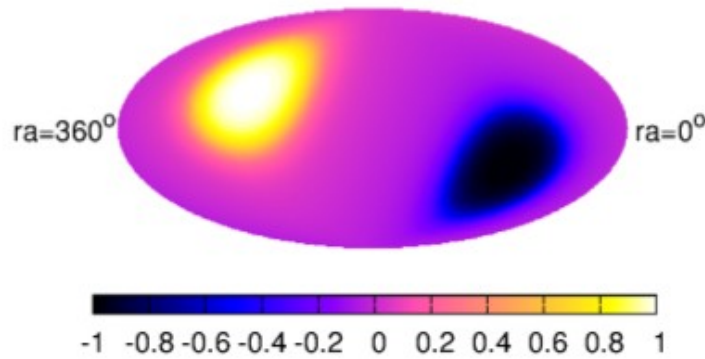
Can fit the 2 PeV data ! →

(but no-E dpdce)



Flattening in directions perpendicular to B field

Case 3 : GS – Exponential & Broad RF



Can fit well the 400 TeV and the 2 PeV data !

Energy-dependence reproduced for fixed turbulence parameters

First theoretical model to fit this data

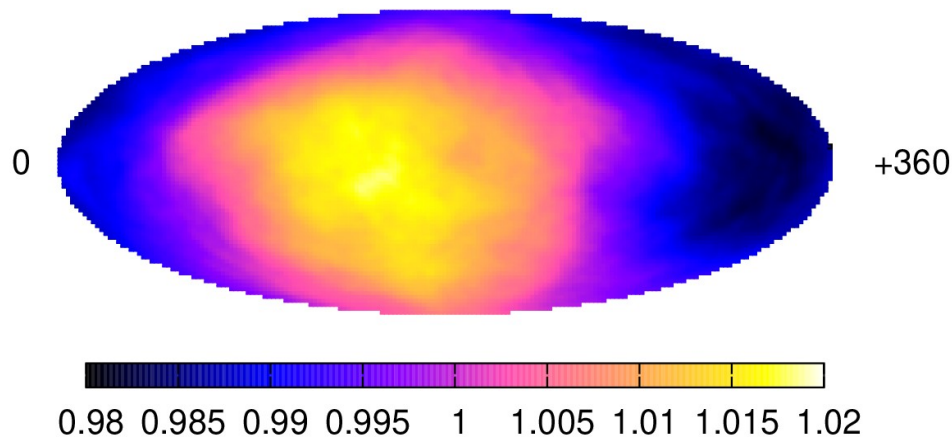
Change in shape with CR energy

- - -> $|\mathbf{k}|$ -dependent anisotropy in power spectrum?

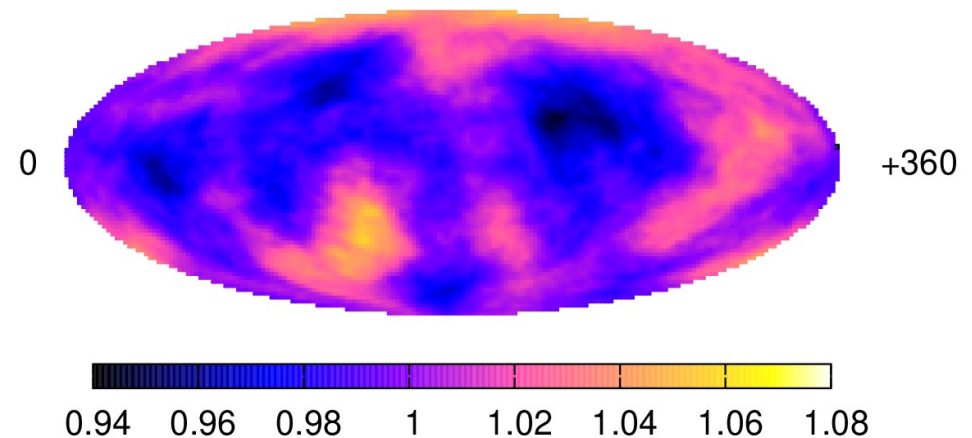
Small-scale aniso. & local turbulence

... What about the non-gyrotropic small scale anisotropies ?

90° smoothing

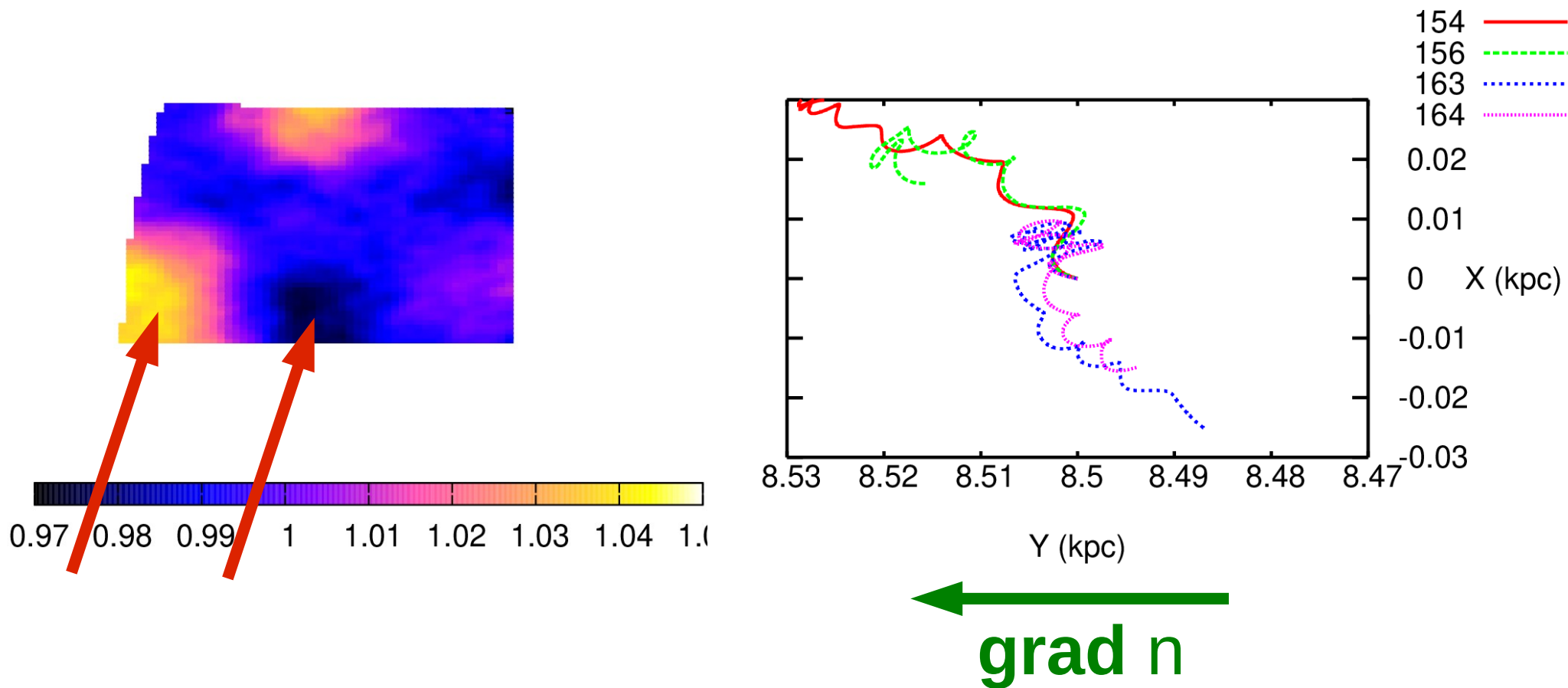


20° smoothing - {dipole}



GG & Sigl, PRL 109, 071101 (2012), *arXiv:1111.2536*

Local trajectories



→ SSA due to the local realization of the ISM turbulent field, within a CR MFP around Earth.

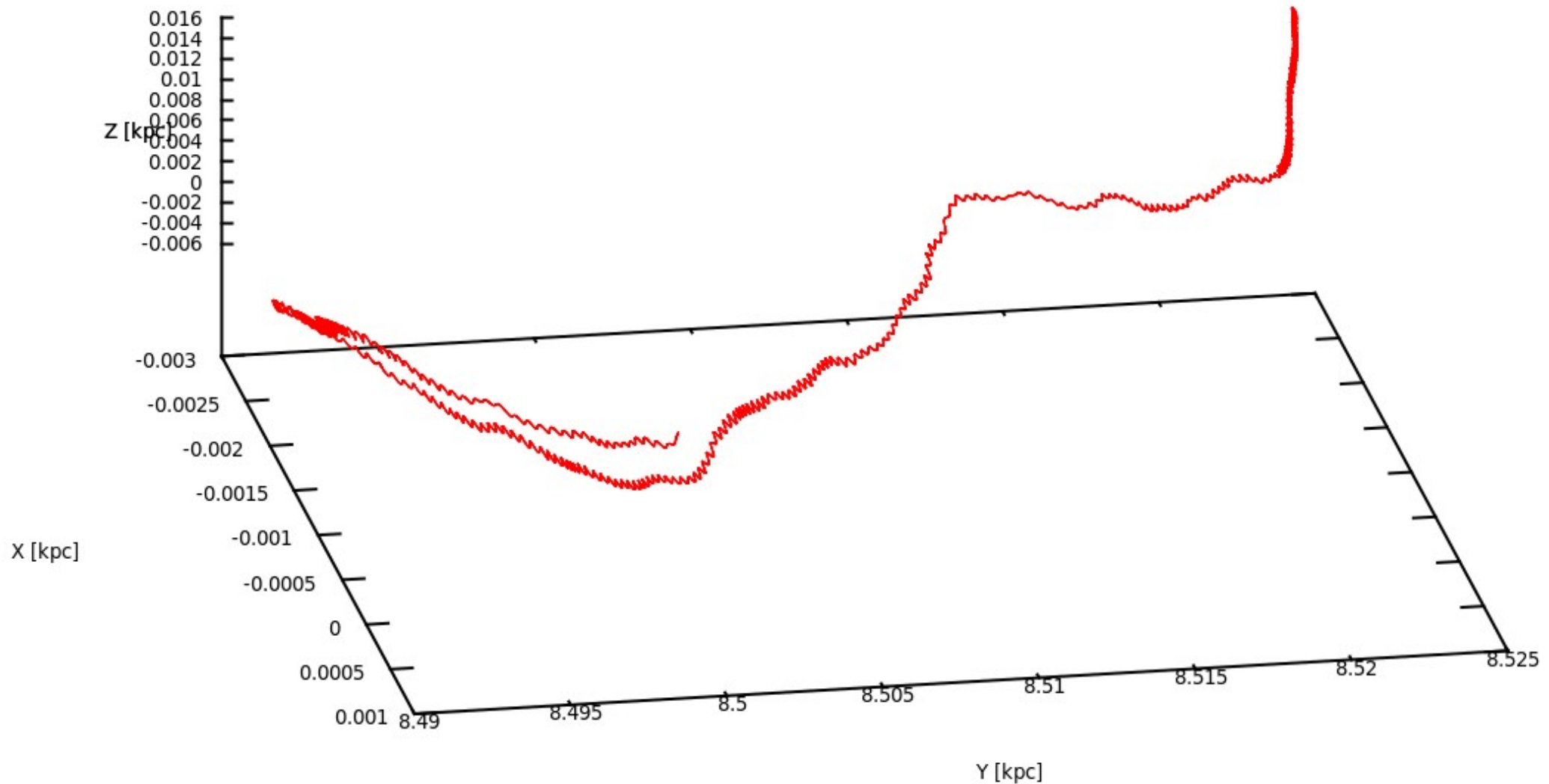
---> *Contain signatures of our very local environment.*

Numerical simulations down to 3 TeV

**GG, Reville & Bian, In Prep. (2021) – see also
*arXiv:1810.06396***

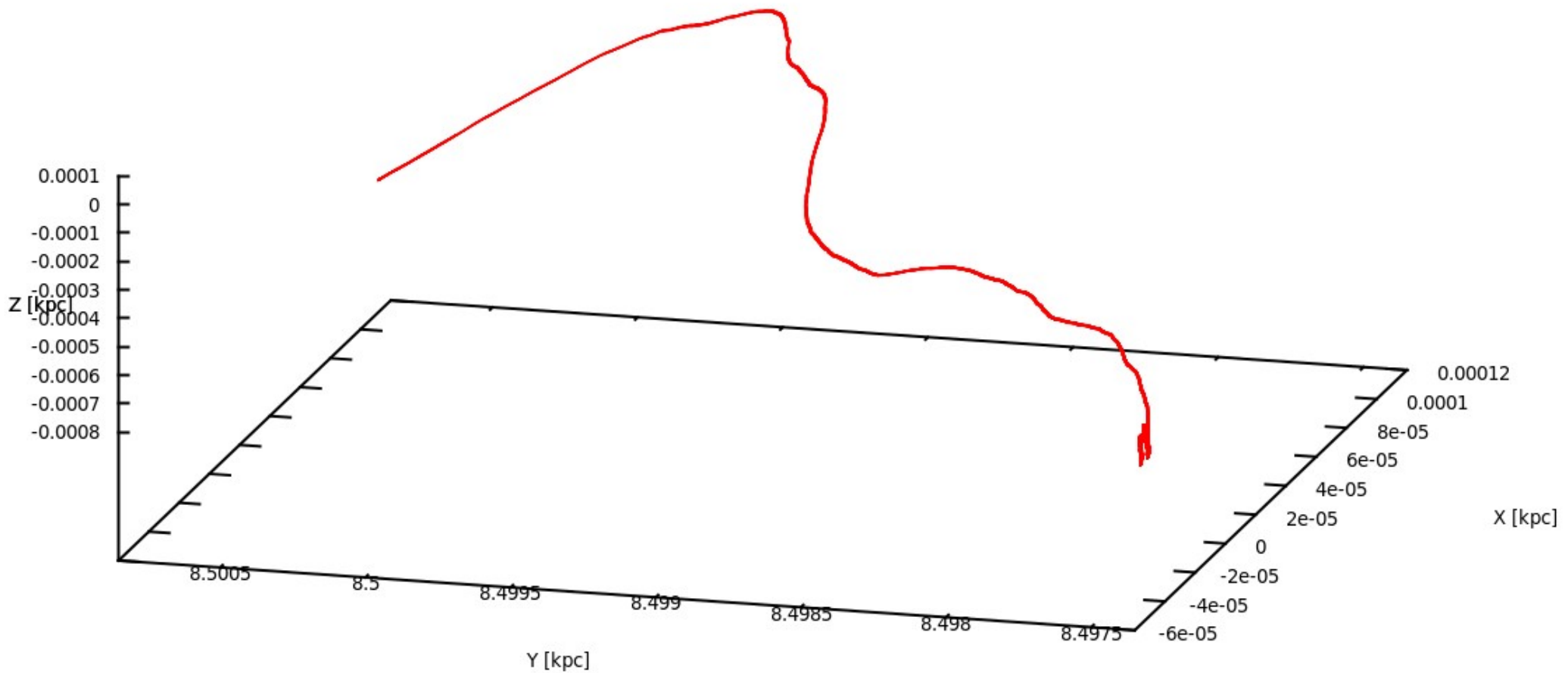
Individual CR trajectories

300 TeV, Kolmogorov, $L_{\text{max}} = 150 \text{ pc}$, $B_{\text{rms}} = 4 \mu\text{G}$.



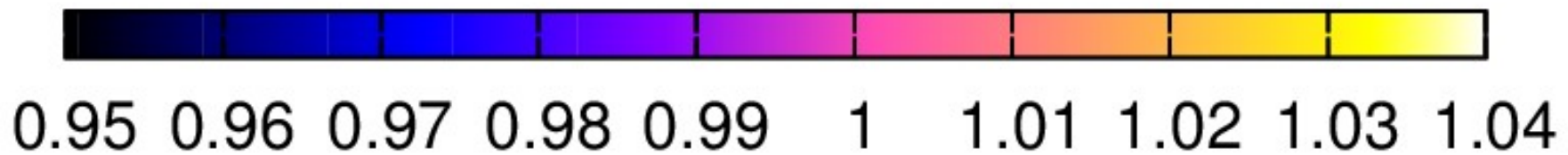
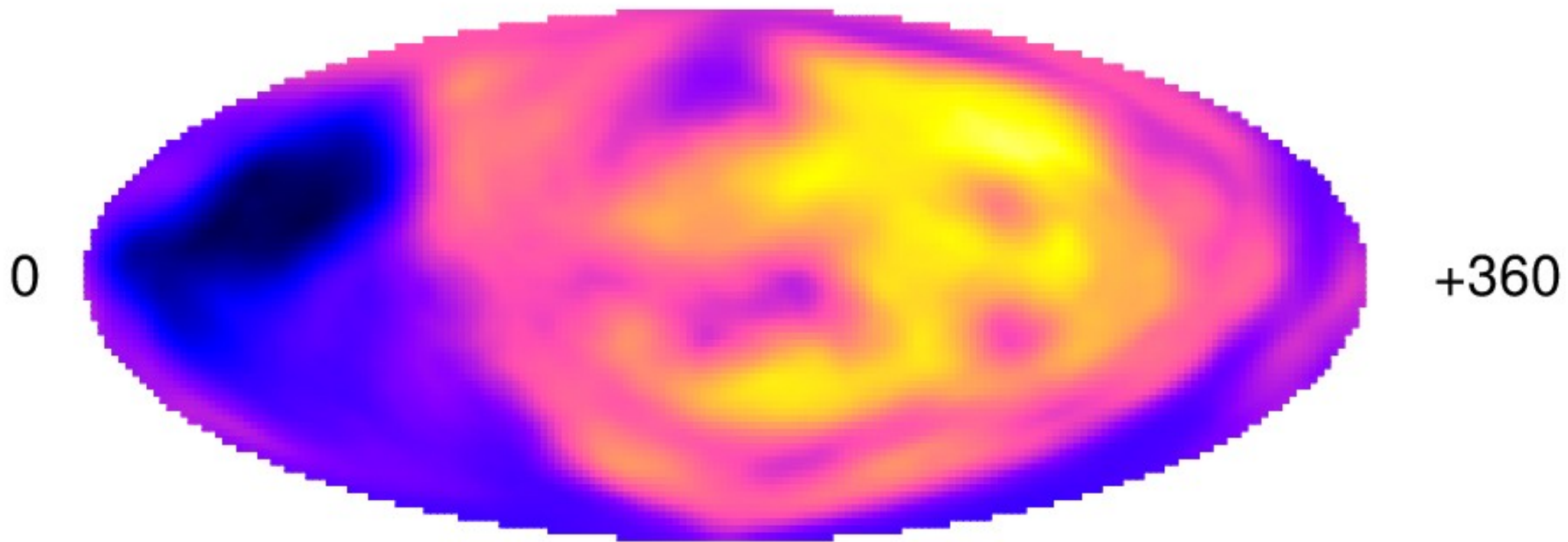
Individual CR trajectories

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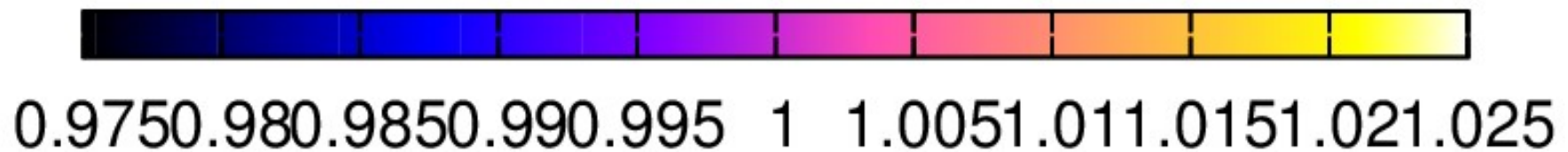
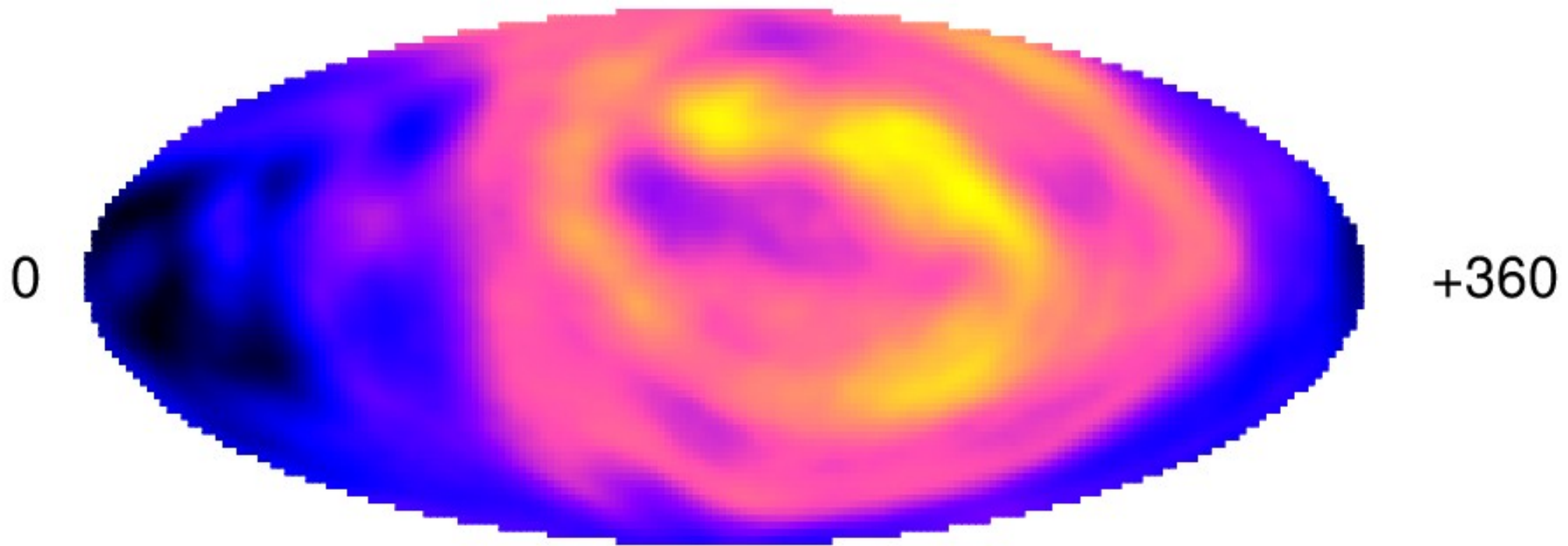
CR Anisotropy – Simulations

$E_{\text{CR}} = 3 \text{ PeV}$



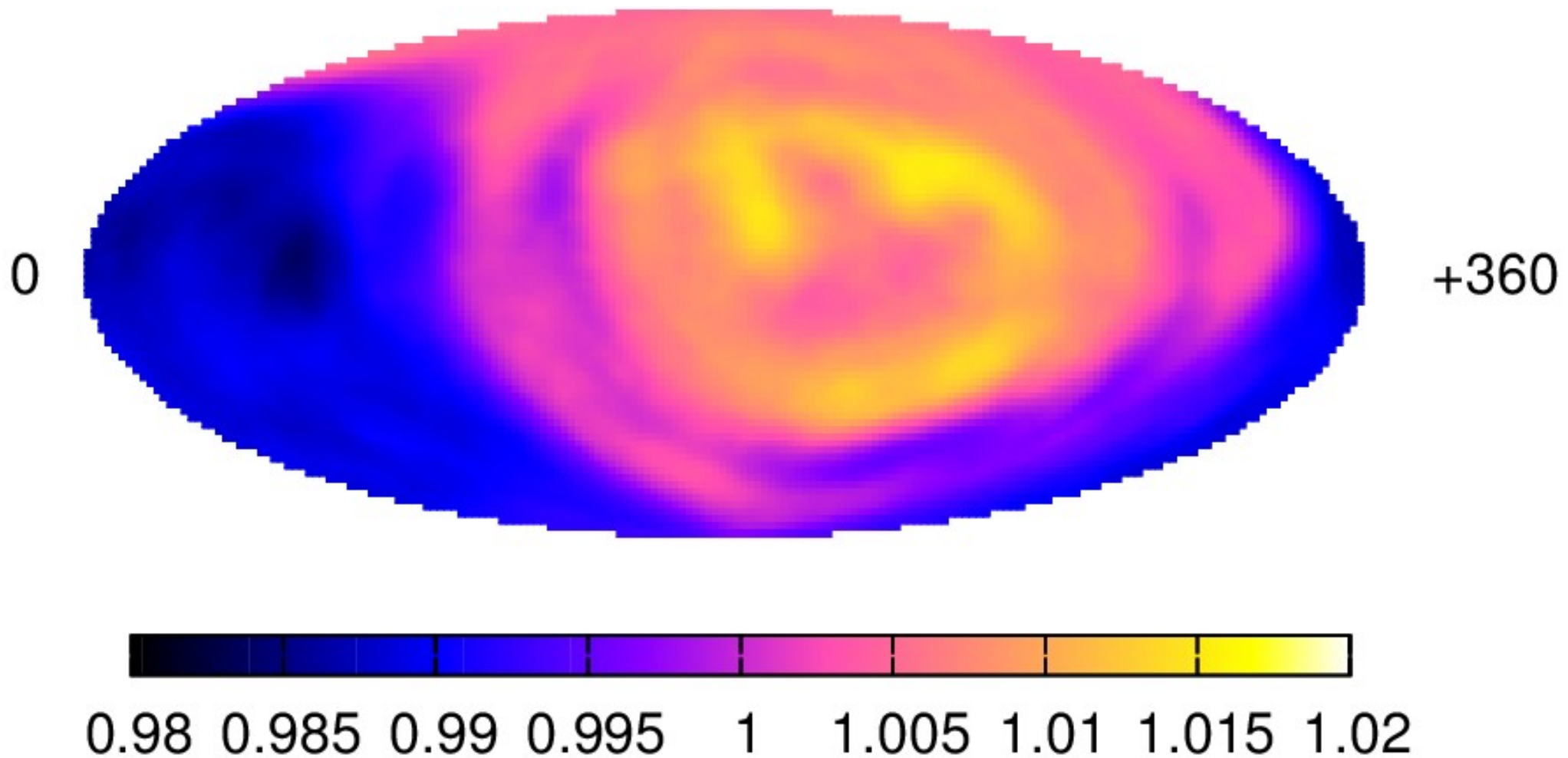
CR Anisotropy – Simulations

$E_{\text{CR}} = 1 \text{ PeV}$



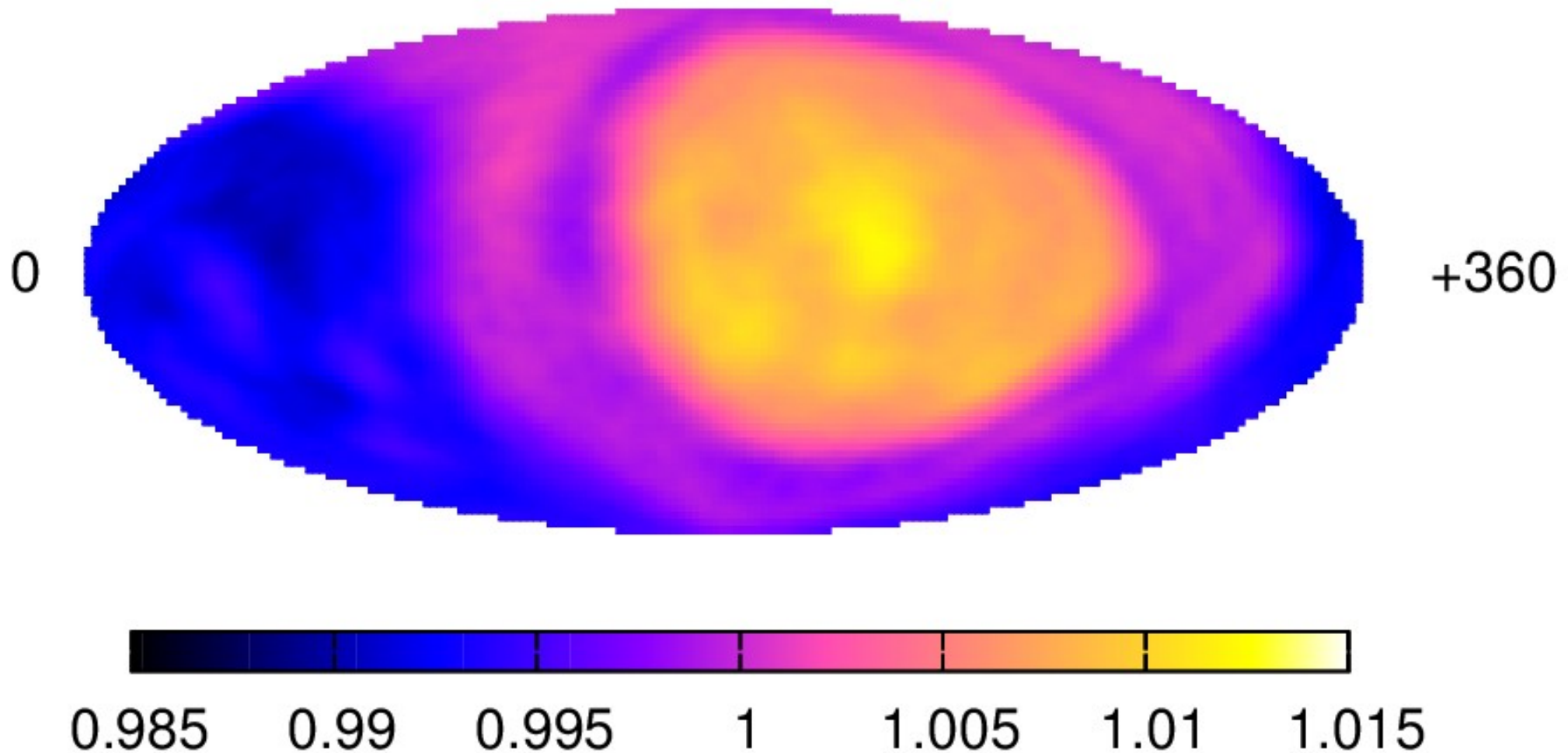
CR Anisotropy – Simulations

$E_{\text{CR}} = 300 \text{ TeV}$



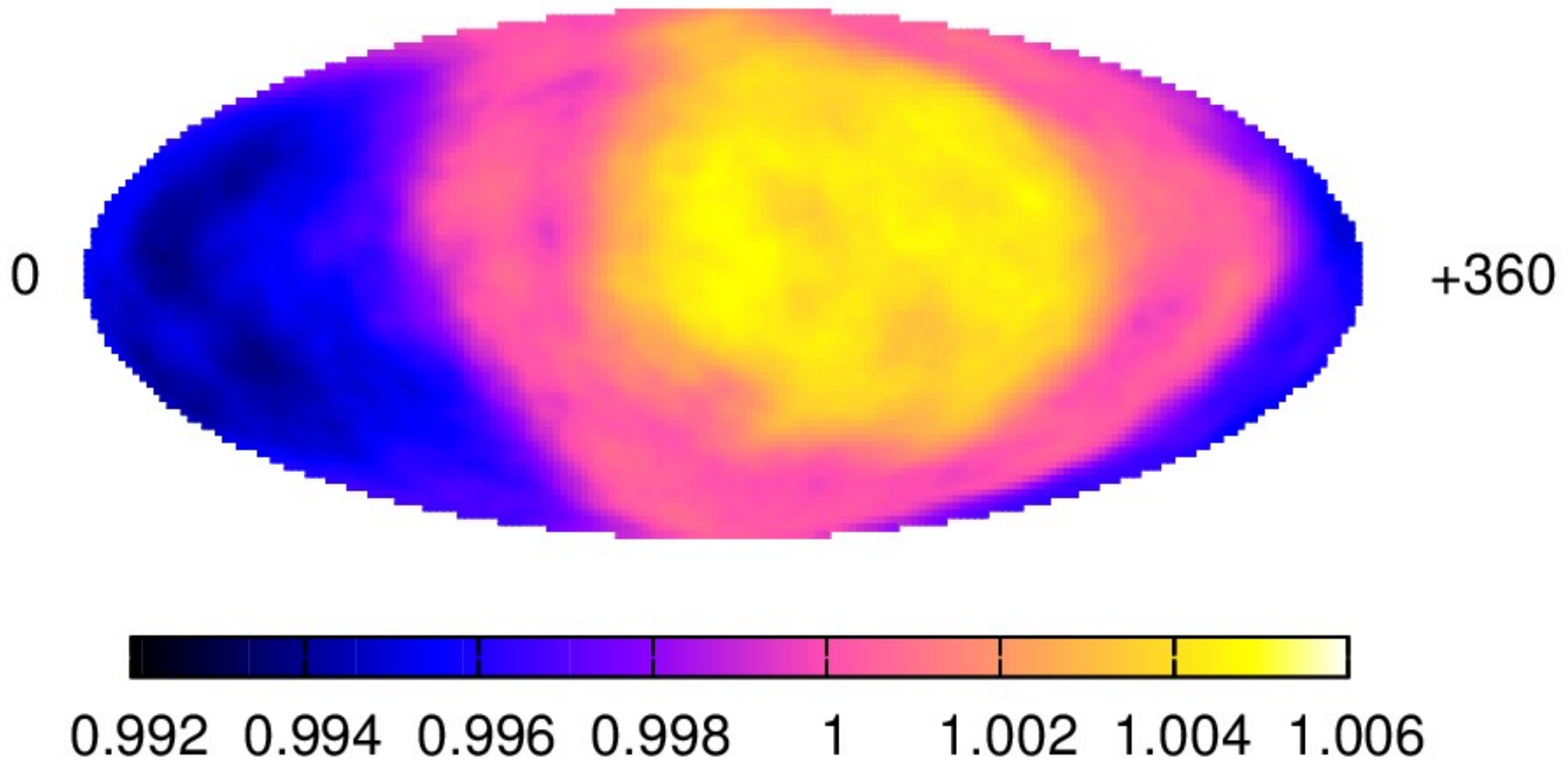
CR Anisotropy – Simulations

$E_{\text{CR}} = 100 \text{ TeV}$



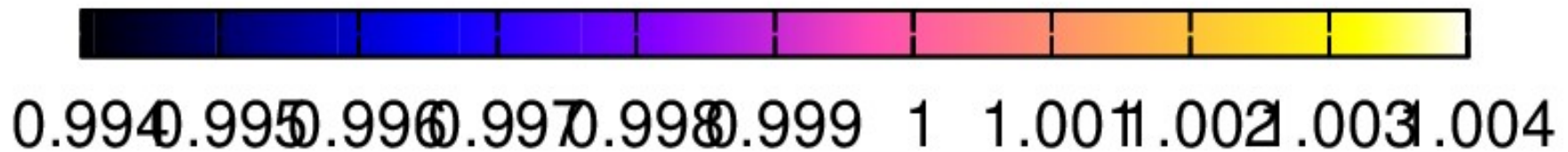
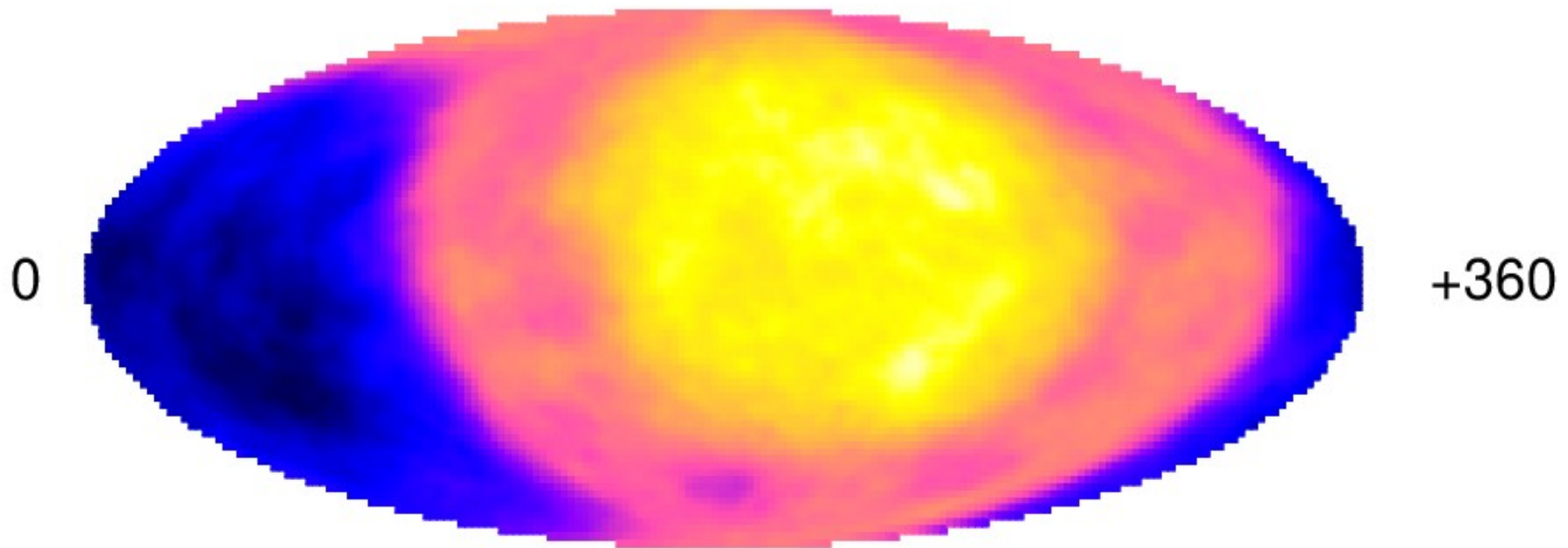
CR Anisotropy – Simulations

$E_{\text{CR}} = 30 \text{ TeV}$



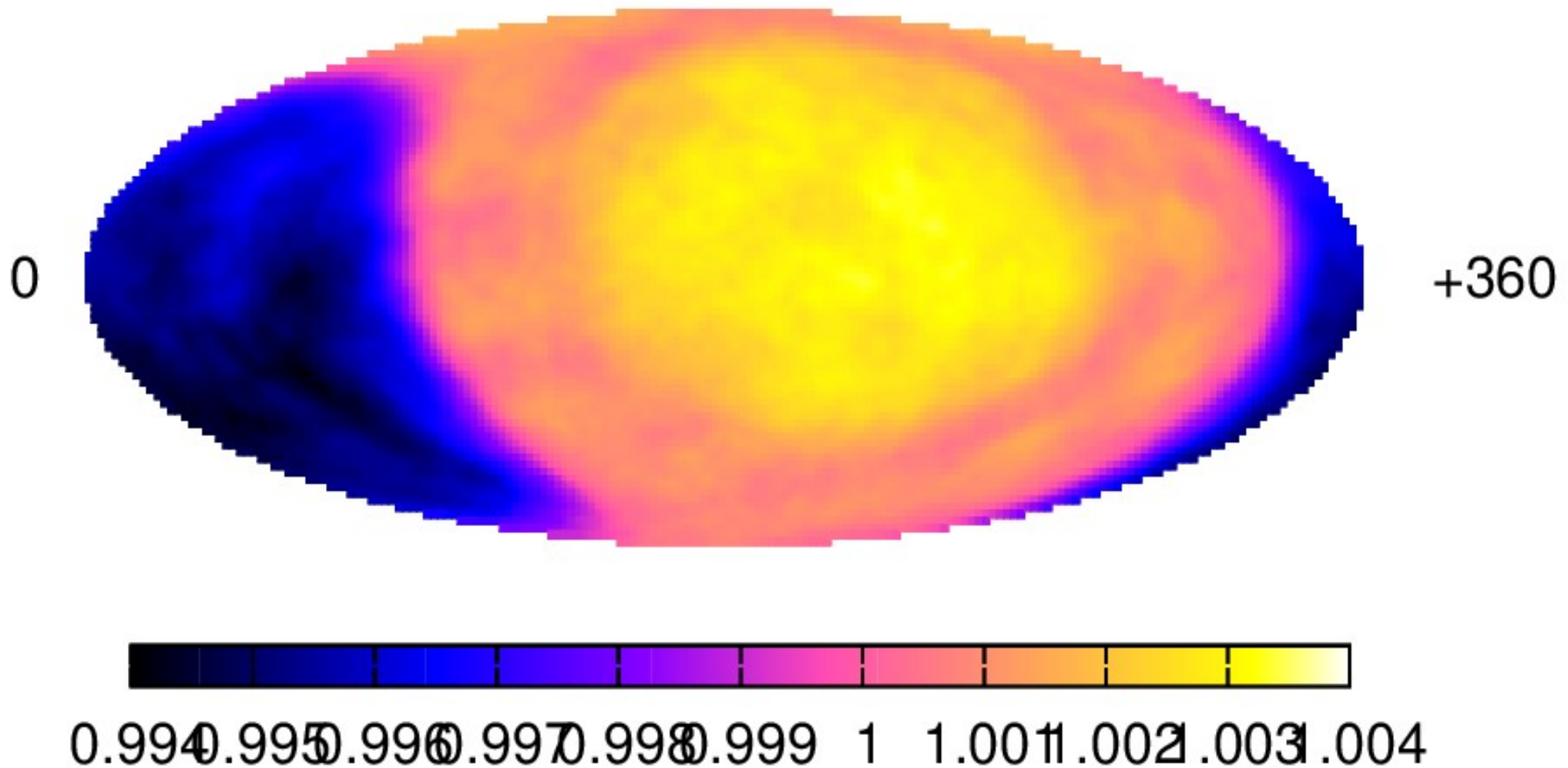
CR Anisotropy – Simulations

$E_{\text{CR}} = 10 \text{ TeV}$



CR Anisotropy – Simulations

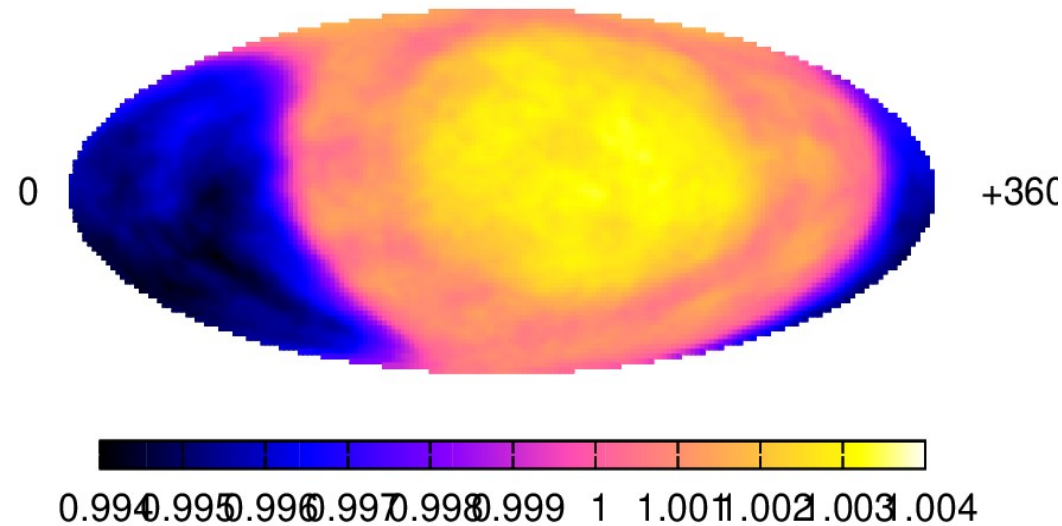
$E_{\text{CR}} = 3 \text{ TeV}$



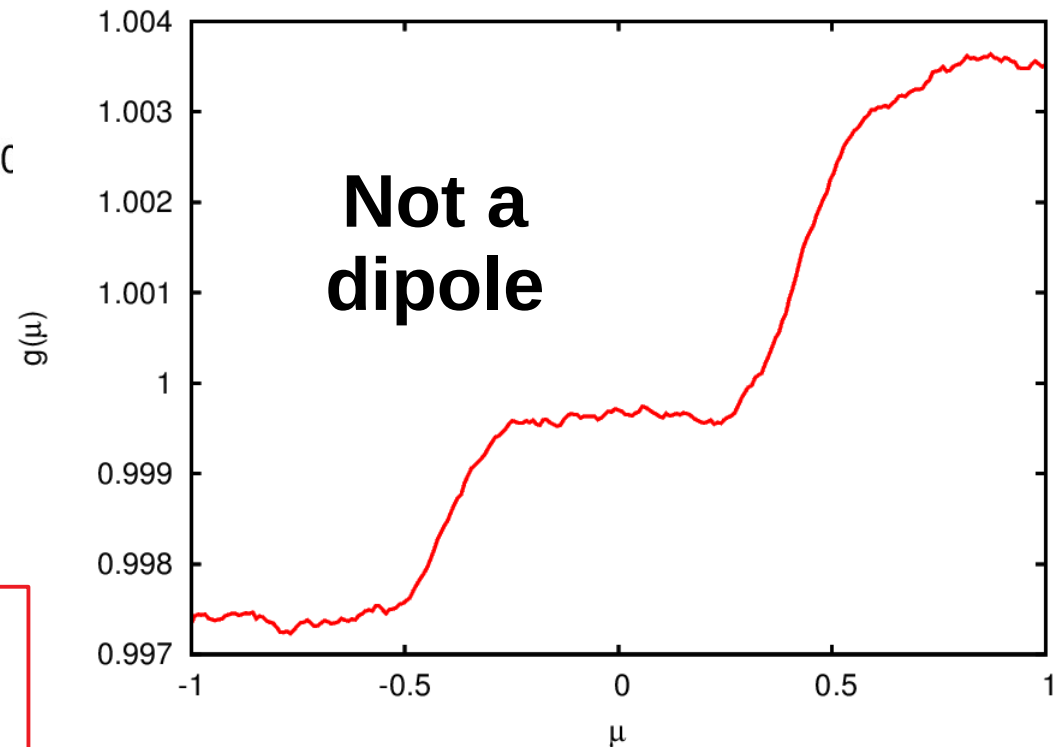
Simulations down to 3 TeV

First simulations that reach TeV energies with $L_{\max} = 150 \text{ pc}$

Kolmogorov, $B_{\text{rms}} = 4 \mu\text{G}$



Shape of the large-scale anisotropy:

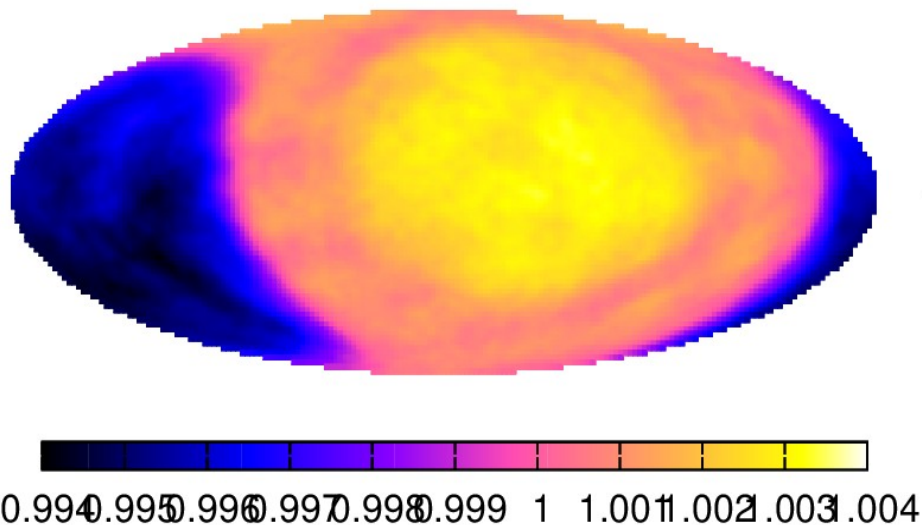


- LSA aligns with the direction of local magnetic field lines,
- **LSA not a dipole.**

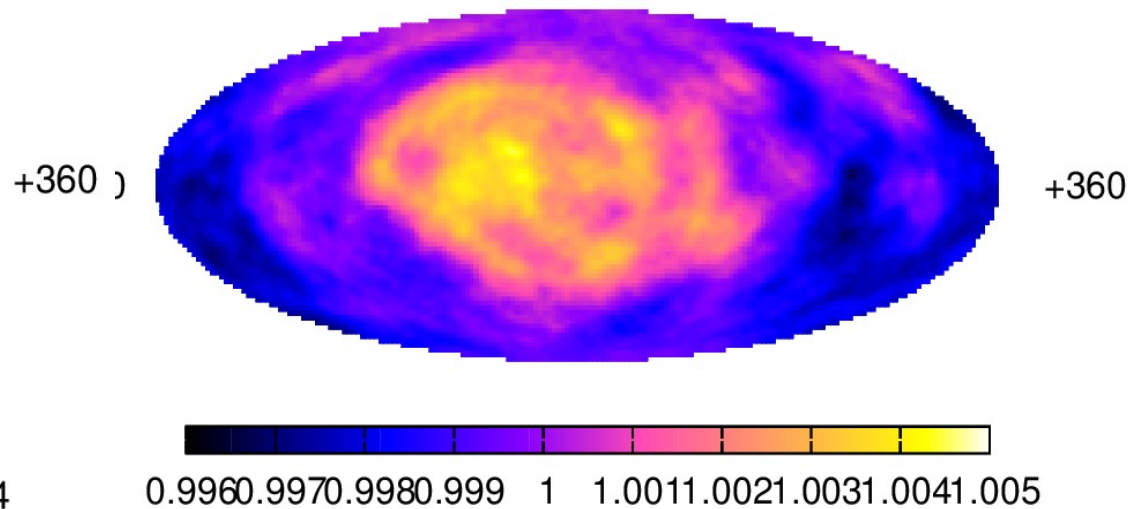
Simulations down to 3 TeV

First simulations that reach TeV energies with $L_{\text{max}} = 150 \text{ pc}$

Observer 1 (Low $\delta B/B$):



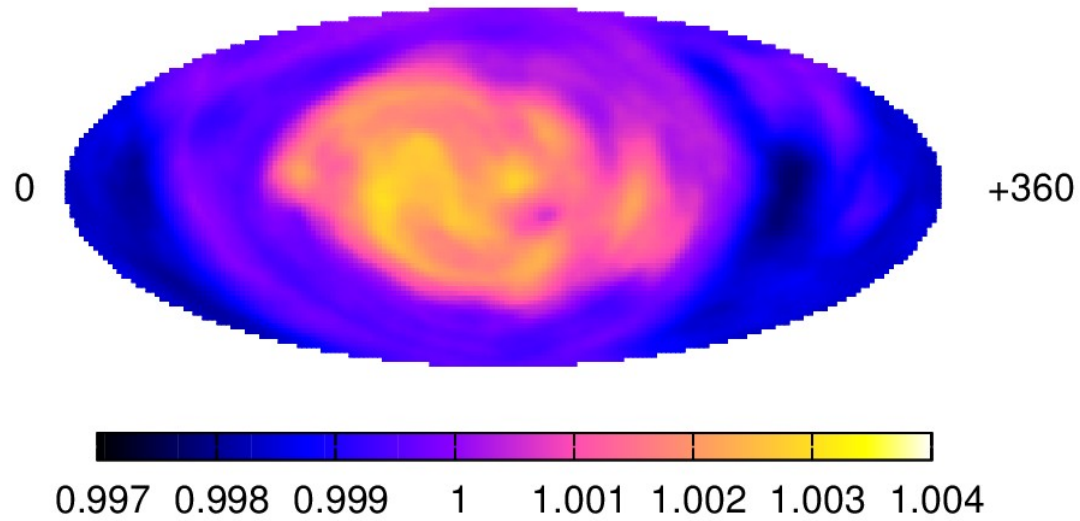
Observer 2 (High $\delta B/B$):



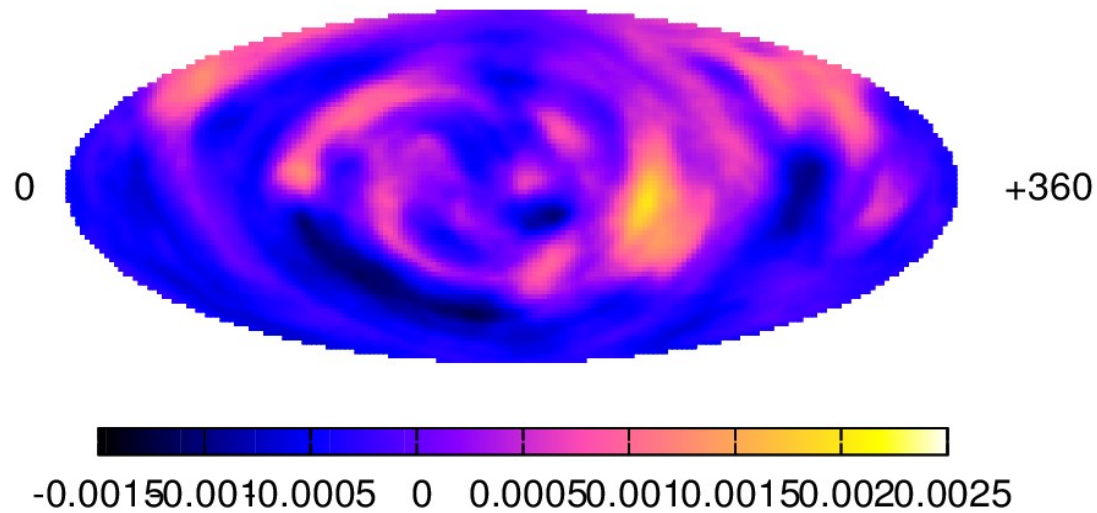
- “Non-gyrotropic”, smaller-scale anisotropies appear too,
- Ampl. SSA/LSA related to local $\delta B/B$ on gyroresonant scales.

(non-gyrotropic) small-scale anisotropies

Total
anisotropy

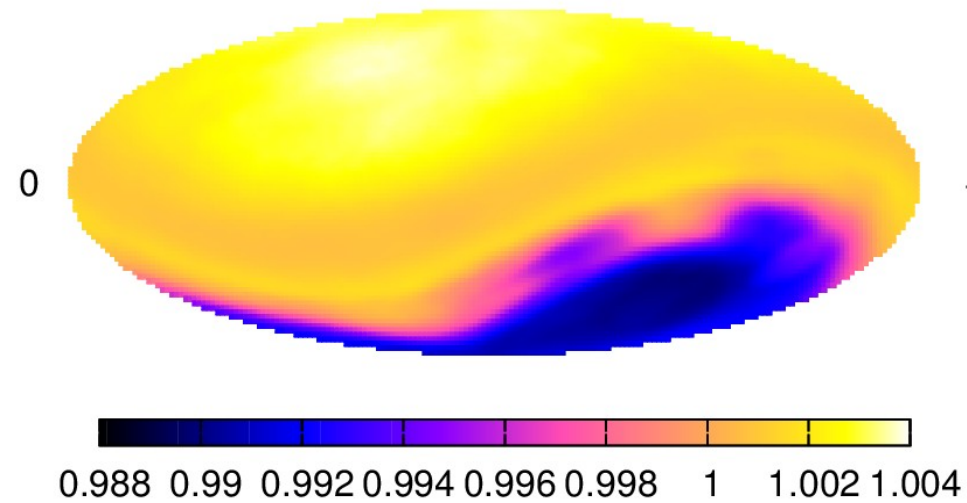


SSA

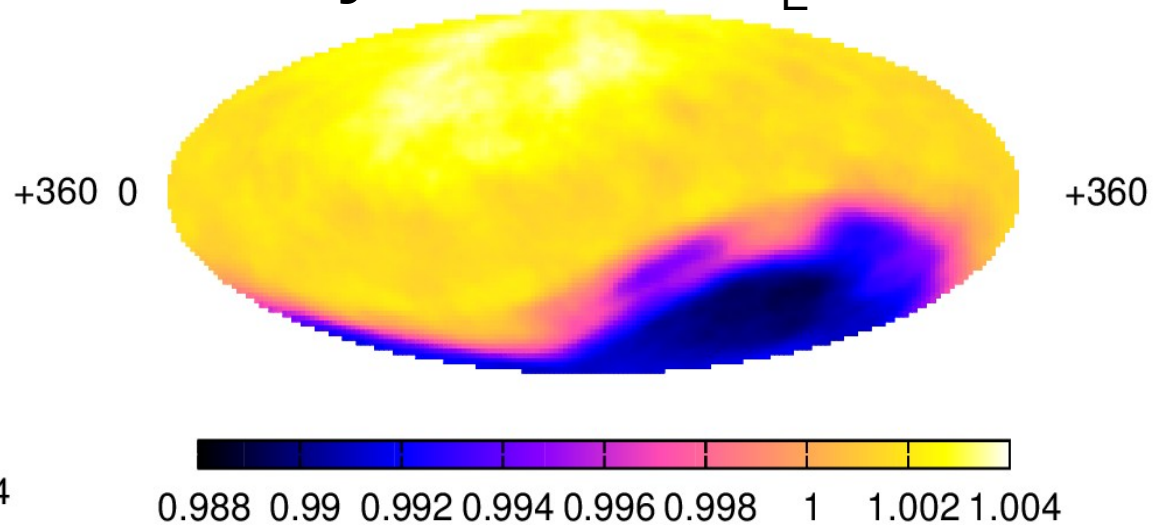


Time variability at 3 TeV

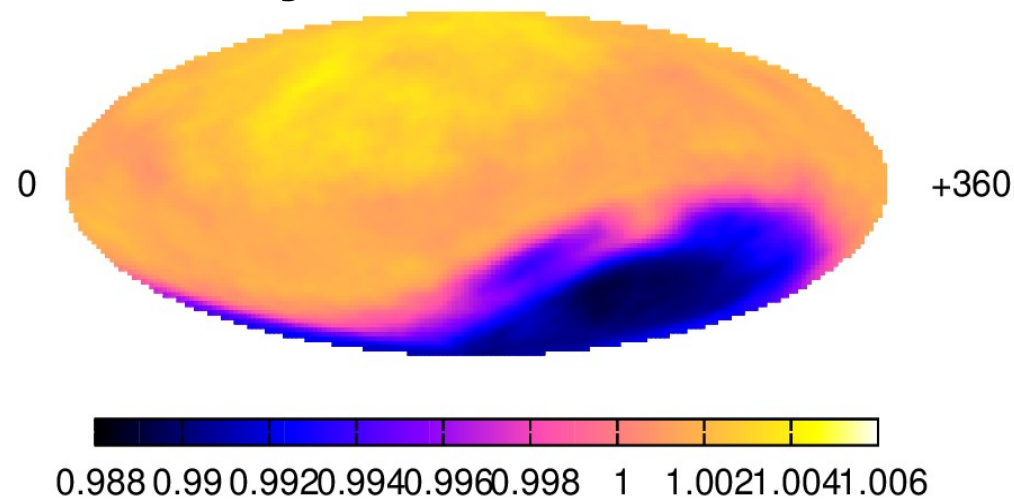
$\Delta t = 0$ yr



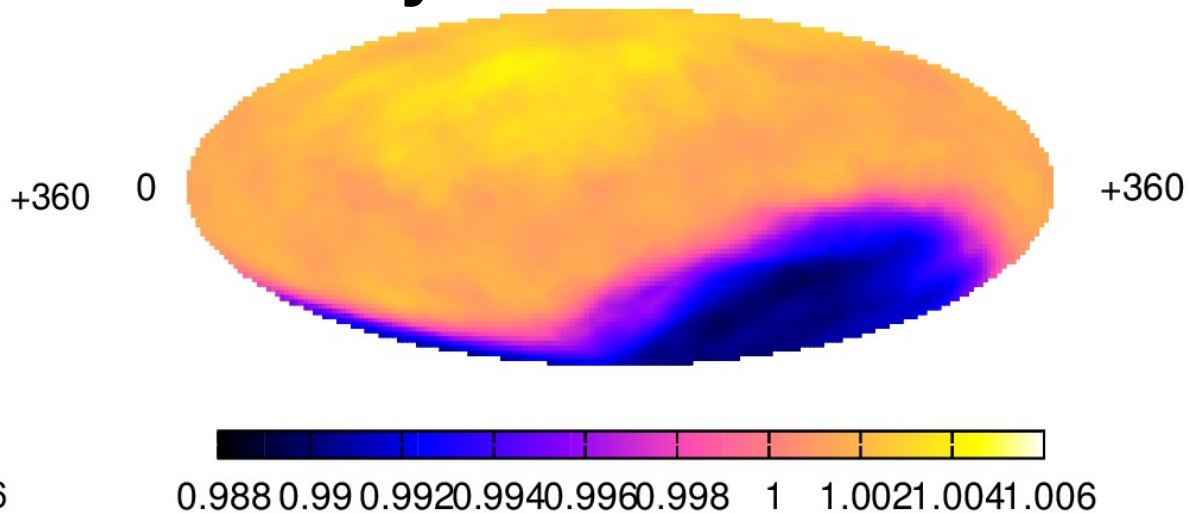
$\Delta t = 1$ yr



$\Delta t = 10$ yr



$\Delta t = 50$ yr



At $E \sim \text{TeV}$, SSA should vary on ~ 10 yr timescale

Conclusions

(1) Large-scale CR Anisotropy = New probe of local ISMFs and CR transport properties.

→ Aligns with local B field. Shape in μ contains crucial information on the properties of the local turbulence.

(2) Small Scales (non-gyrotropic) : Probe of the local realization of the ISM turbulent fields, within a CR MFP around Earth.

→ Relative amplitude with respect to large-scale CRA depends on local $\delta B/B$.

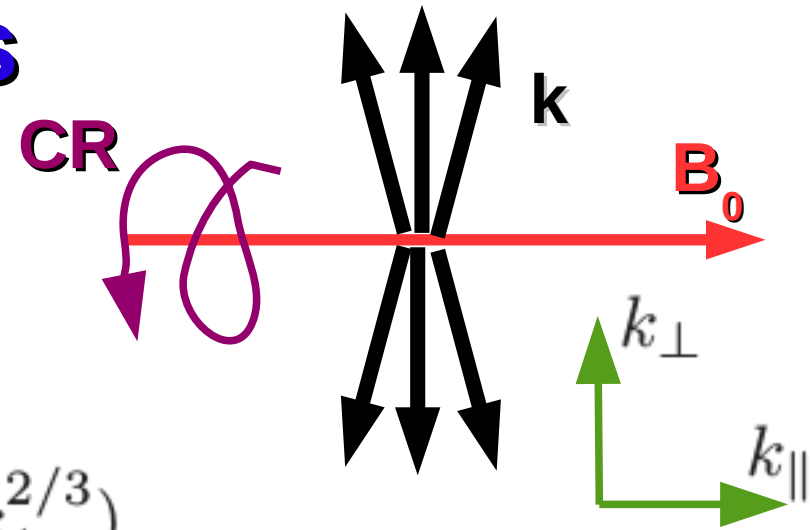
Conclusions

- LSA : Aligns with local B field lines. Gyrotropy assumption ~ OK at $E < \sim 100 \text{ TeV} - 1 \text{ PeV}$,
- LSA : Flattening in directions perpendicular to field lines. Shape in μ contains crucial information on the properties of the local turbulence,
- SSA : Do appear with the correct amplitude at TeV energies. Amplitude also depends on local $\delta B/B$.

Alfven (and Slow) modes

Goldreich & Sridhar (1995)

$$|k_{\parallel}| \lesssim |k_{\perp}|^{2/3} l^{-1/3}$$



(1) $\mathcal{I}_{A,S} = \mathcal{I}_{1,A,S} \propto k_{\perp}^{-10/3} h(k_{\parallel} l^{1/3} / k_{\perp}^{2/3})$

where $h(y) = 1$ if $|y| < 1$, and $h = 0$ otherwise (see Chandran (2000))

(2) MHD simulations of Cho & Lazarian (2002) :

$$\mathcal{I}_{A,S} = \mathcal{I}_{2,A,S} \propto k_{\perp}^{-10/3} \exp(-k_{\parallel} l^{1/3} / k_{\perp}^{2/3})$$

Fast magnetosonic modes

MHD simulations of Cho & Lazarian (2002) :

Isotropic with $\mathcal{I}_M(\mathbf{k}) \propto k^{-3/2}$

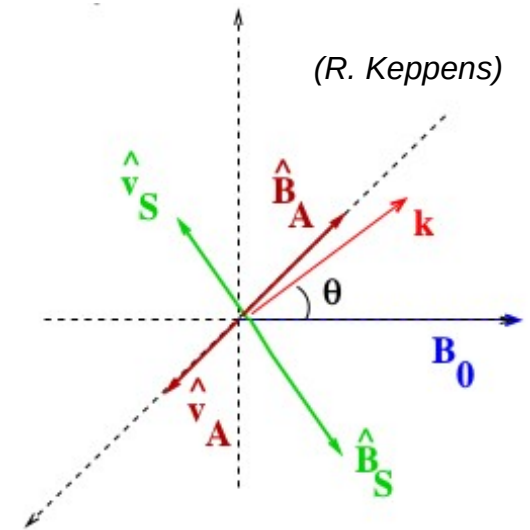
Pitch-angle diffusion coefficient

$$D_{\mu\mu} = \Omega^2 (1 - \mu^2) \int d^3k \sum_{n=-\infty}^{\infty} \left(\frac{n^2 J_n^2(z)}{z^2} \mathcal{I}_A(\mathbf{k}) + \frac{k_{\parallel}^2 J_n'^2(z)}{k^2} \mathcal{I}_{S,F}(\mathbf{k}) \right) \times R_n(k_{\parallel} v_{\parallel} - \omega + n\Omega),$$

where $\mathcal{I}_{A,S,F}$ respectively correspond to the normalized energy spectra of the Alfvén, slow and fast modes.

$z = k_{\perp} l \varepsilon \sqrt{1 - \mu^2}$, and Ω is the Larmor frequency.

$$\varepsilon = v / (l\Omega) = r_L / l$$



Resonance functions (RF)

(1) **NARROW:** RF dominated by Lagrangian correlation time (τ_w)

Chandran (2000)

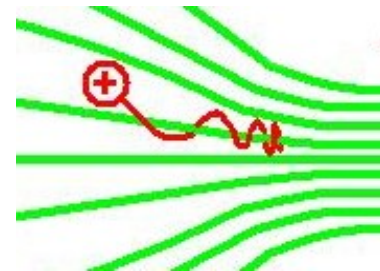
$$R_{n,1}(k_{\parallel}v_{\parallel} - \omega + n\Omega) = \frac{\tau_w^{-1}}{(k_{\parallel}v_{\parallel} - \omega + n\Omega)^2 + \tau_w^{-2}}$$

Lagr. corr. time for strong

aniso. incompr. MHD turb. $\rightarrow \tau_{A,S} = l^{1/3}/(v_A k_{\perp}^{2/3})$

$$\tau_F = l/(v_A \tilde{k}^{1/2}) \quad \tilde{k} = kl$$

(2) **BROAD:** Conservation of the adiabatic invariant v_{\perp}^2/B



Yan & Lazarian (2008)

$$\delta\mathcal{M}_A = \sqrt{\langle \delta B_{\parallel}^2 \rangle / B_0^2}$$

$$R_{n,2}(k_{\parallel}v_{\parallel} - \omega + n\Omega) = \frac{\sqrt{\pi}}{k_{\parallel}v_{\perp} \delta\mathcal{M}_A^{1/2}} \exp\left(-\frac{(k_{\parallel}v_{\parallel} - \omega + n\Omega)^2}{k_{\parallel}^2 v_{\perp}^2 \delta\mathcal{M}_A}\right)$$