Particle acceleration in winds of star clusters

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NGC 2237-9 The Rosette Nebula



Where does PeV particles come from?

In spite of big efforts of the last years, the origin of CRs is still unclear The SNR paradigm is the most accepted scenario but

- issue concerning the chemical abundances (e.g. ²⁰Ne/²²Ne) [see Prantzos, 2012, A&A 538] •



problem in reaching the maximum energy close to ~PeV for protons [see Cristofari, Blasi, Amato 2020]

Galactic CR protons should be accelerated up to ~PeV to explain the knee in the CR spectrum

> It is worth exploring other possible candidates for the production of cosmic rays

Stellar winds represent the second most powerful source



Luminosity of stellar winds

[Cesarsky & Montmerle, 1983; Seo, Kang & Ryu, 2018]

Power in stellar winds

$$P_{SW} = \int_{M_{\min}}^{M_{\max}} \xi(M) \mathscr{L}_{w}(M) \tau_{s}(M) \, dM$$

 $M_{\rm min} = 0.08 M_{\odot}; M_{\rm max} = 110 M_{\odot}$

Initial mass function

Wind kinetic luminosity

$$\mathscr{L}_w = \frac{1}{2} \dot{M} v_w^2$$

Star main sequence lifetime $\left(\frac{M}{M_{\odot}}\right)^{-2.5}$

$$\tau_s(M) \simeq \tau_\odot \left(\frac{1}{M} \right)$$

Power in SN explosion

$$P_{SN} = E_{SN} \int_{M_s}^{M_{max}} \xi(M) \, dM$$
$$E_{SN} = 10^{51} \, \text{erg/s}$$
$$M_s \simeq 8 \, M_{\odot}$$



 $\xi(M) = \frac{dN}{dM} \propto M^{-2.35}$ [Salpeter, 1955]

Mass loss rate $\dot{M} = 9.6 \times 10^{-15} \left(\frac{L}{L_{\odot}}\right)^{1.45} \left(\frac{M}{M_{\odot}}\right)^{0.16} \left(\frac{R}{R_{\odot}}\right)^{0.01}$ [Nieuwenhuijzen & de Jager, 1990] Stellar wind speed $v_w \gtrsim v_\infty = \sqrt{2GM/R_s}$

Ratio: $\approx 0.2 \in [0.06, 3]$

Stellar wind power can be comparable with the SN Power but there are numerous uncertainties

(I am neglecting the role of WR stars)





Hints from CR chemical composition

- **In the CR spectrum the** ²²Ne/²⁰Ne ~ 5 times the Solar value
- The only place where ²²Ne is overabundant is the stellar external layers of massive stars
- * In past this argument was used in favour of CR acceleration in super bubbles [Higdon & Lingenfelter 2003; Bings et al 2003, 2008] but in fact the average ²²Ne/²⁰Ne in SB is roughly Solar (enriched by winds but also by SN ejecta) [Prantzos, 2012]
- * Stellar rotation can mix the outer layers \Rightarrow ²²Ne enrichment of stellar wind ⇒ preferential acceleration of stellar wind material can solve the problem
- **From abundances of CR species**, Tatischeff et al. MNRAS 508, (2021) inferred that ~6% of (low energy) CR should come from SW material
- * Uncertainties due to several factors (e.g. element mixing in stellar layers, ionisation level, etc.)





Different role of stellar winds

WINDS FROM SINGLE STARS Pros.

- [Cesarsky & Montmerle, 1983]
- Long-living systems (age ~ Myr)
- Large size (bubble can reach several tens of pc)
- Cons.
 - Small velocity ($v_w \leq 3000 \text{ km/s}$)
 - Small mass ejecta: $\dot{M} \lesssim 10^{-6} M_{\odot} \,\mathrm{yr}^{-1}$

• Small magnetic field in the free wind region \rightarrow large diffusion coefficient \rightarrow small E_{max} FROM MASSIVE YOUNG STELLAR CLUSTERS

- * #stars $\gtrsim 10^3 \Rightarrow \dot{M} \gtrsim 10^{-4} M_{\odot} \,\mathrm{yr}^{-1}$



Winds from massive stars inject into the Galaxy a kinetic energy comparable to SNRs

* presence of strong wind turbulence \Rightarrow possibility to generate magnetic turbulence



Massive stellar clusters detected in gamma-rays

Recently, several young massive stellar clusters have been associated with gamma-rays sources

Name	log M/M _{sun}	r _c /pc	D/kpc	age/Myr	<i>L</i> _w / 10 ³⁸ erg s ⁻¹	Reference
Westerlund 1	4.6 ± 0.045	1.5	4	4-6	10	Abramowski A., et al., 2012, A&A, 537, A114
Westerlund 2	4.56 ±0.035	1.1	2.8 ± 0.4	1.5-2.5	2	Yang, de Oña Wilhelmi, Aharonian, 2018, A&A, 611, A77
Cyg. OB2	4.7±0.3	5.2	1.4	3-6	2	Ackermann M., et al. 2011, Science, 334, 1103
NGC 3603	4.1 ± 0.10	1.1	6.9	2-3	?	Saha, L. et al 2020, ApJ, 897, 131
BDS 2003	4.39	0.2	4	1	?	Albert A., et al., 2020, arXiv:2012.15275
W40	2.5	0.44	0.44	1.5	?	Sun, XN. et al. 2020, A&A, 639, A80
30 Dor (LMC) NGC 2070/RCM 136	4.8-5.7 4.34-5	multiple sub-clusters	50	1 5	?	H. E. S. S. Collaboration et al., 2015, Science, 347, 406



OBSERVATIONS: Cygnus OB2





Fermi-LAT Ackermann et al. (2011) Science 334

OBSERVATIONS: Westerlund 1





OBSERVATIONS: Westerlund 2

HESS collaboration, A&A 525 A46 (2011)





Spitzer/IRAC mosaic J1023-575(HESS; white) J1023.3-5747 (Fermi-LAT; magenta) cyan cross: pusar

- Compatible size in GeV and TeV range
- ✤ Spectral slope ~2 @ *E* < TeV; 2.6 @ *E* > TeV
- PWN contribution disfavoured
- Most promising accelerator in the FoV is Westerlund 2
- Total gamma-ray luminosity ~0.2% of mechanical * wind energy





Possible acceleration mechanisms

Young Stellar clusters (no SNRs)

- Termination shock of single stars
- **Collective wind termination shock** [GM et al. 2021]

Superbubbles (Winds+SNRs)

- DSA in enhanced turbulence [Parizot et al. 2004]
- Multiple primary shocks [Klepach et al. 2000]
- Multiple primary and secondary shocks [Bykov & Toptygin 1982, Bykov & Fleishman 1992]
- Acceleration by turbulence [Bykov & Toptygin 1993]

* Wind-wind collision [Reimer, Pohl, Reimer (2006); Bykov, Gladilin & Osipov (2013); Vieu, Gabici & Tatischeff (2020)]

Turbulence + multiple shocks [Parizot et al. 2004; Ferrand & Markowith 2010; Vieu, Gabici & Tatischeff ICRC 2021]



The wind-bubble system

The stellar wind blow a hot bubble in the ISM [Weaver et al., 1977, ApJ 218]

- The hot bubble spend the majority of its life (~few Myr) the in * adiabatic phase
- The shocked ISM collapse to a thin shell ($t_{cool} \sim 10^4 yr$)
- The termination shock is almost stationary *

Bubble radius:

$$R_b \simeq 55 \text{ pc} \left(\frac{\dot{M}}{10^{-4}M_{\odot}/yr}\right)^{1/5} \left(\frac{v_w}{1000 \text{ km/s}}\right)^{2/5} \left(\frac{\rho_0/m_p}{\text{ cm}^{-3}}\right)^{-1/5}$$

Radius of termination shock:

$$R_s \simeq 20 \text{ pc} \left(\frac{\dot{M}}{10^{-4}M_{\odot}/yr}\right)^{3/10} \left(\frac{v_w}{1000 \text{ km/s}}\right)^{1/10} \left(\frac{\rho_0/m_p}{\text{ cm}^{-3}}\right)^{-3/10}$$

$$u_{ts} \simeq v_w \sim 2000 - 3000 \,\mathrm{km/s}$$





ISM

6

8

Cluster compactness

In general a large scale termination shock is generated if the cluster is compact enough, such that $R_{\text{cluster}} \ll R_{\text{ts}}$

60

40

20

-20

-40

y (pc)

$$R_{\rm ts} = \sqrt{\frac{L_w}{2\pi v_w P_{\rm bubble}}}$$

From the model by Chevalier & Clegg (1985)

$$R_{\rm ts} \simeq 20 \text{ pc} \left(\frac{\dot{M}}{10^{-4}M_{\odot}/yr}\right)^{\frac{3}{10}} \left(\frac{v_w}{1000 \text{ km/s}}\right)^{\frac{1}{10}} \left(\frac{\rho_0/m_p}{\text{ cm}^{-3}}\right)^{-\frac{3}{10}} \left(\frac{t_{\rm age}}{\text{ Myr}}\right)^{\frac{2}{5}}$$

Powerful clusters should easily produce a large scale termination shock



Particle acceleration at the termination shock

Time-stationary transport equation in spherical geometry:

Arbitrary diffusion coefficient D(r,p)

Injection only at the termination shock

 $Q(r,p) \propto \delta(p-p_{\rm ini}) \,\delta(r-R_s)$

• Wind velocity profile: $u(r) = \begin{cases} u_1 = v_w & \text{for } r < R_s, \\ \frac{u_1}{\sigma} \left(\frac{R_s}{r}\right)^2 & \text{for } R_s < r < R_b, \\ 0 & \text{for } r > R_b; \end{cases}$

With respect to SNRs the geometry is "reversed"







Solution of the transport equation

Time-stationary transport equation in spherical geometry:

$$\frac{\partial}{\partial r} \left[r^2 D(r,p) \frac{\partial f}{\partial r} \right] - r^2 u(r) \frac{\partial f}{\partial r} + \frac{d \left[r^2 u \right]}{dr} \frac{p}{3} \frac{\partial f}{\partial p} + r^2 \frac{d^2 r^2}{dr} + r^2 \frac{d^2 r^2}{dr} + r^2 \frac{d^2 r^2}{dr} \frac{d^2 r^2}{dr$$

Boundary conditions:

- 1. No net flux at the cluster center:
- 2. Matching the Galactic distribution: $f(r \rightarrow \infty, p) = f_{gal}(p)$
- The equation is solved in regions (1, 2) and (3) and than matched at R_s and *R*_b using the flux conservation
- For generic expression of D(r,p) and u(r) the solution is not analytical, but can be expressed in an implicit form that can be solved by iterations.



Diffusion coefficient

Time-stationary transport equation in spherical geometry:

$$\frac{\partial}{\partial r} \left[r^2 D(r,p) \frac{\partial f}{\partial r} \right] - r^2 u(r) \frac{\partial f}{\partial r} + \frac{d \left[r^2 u \right]}{dr} \frac{p}{3} \frac{\partial f}{\partial p} + r^2 \frac{d^2 r^2}{dr} + r^2 \frac{d^2 r^2}{dr} + r^2 \frac{d^2 r^2}{dr} \frac{d^2 r^2}{dr} + r^2 \frac{d^2 r^2}$$

Wind-wind collision and non-stationarity can produce high level of HD turbulence

Assuming that a fraction η_B of kinetic wind energy is converted into magnetic energy

$$\frac{\delta B}{4\pi} 4\pi r^2 v_w = \frac{1}{2}$$

The type of turbulent cascade can result into different diffusion coefficients

 $D_{\text{Kol}}(E) = \frac{v}{3} r_L(\delta B)^{1/3} L_c^{2/3}$ $D_{\text{Kra}}(E) = \frac{v}{3} r_L (\delta B)^{1/2} L_c^{1/2}$ $D_{\text{Bohm}}(E) = \frac{v}{3} r_L (\delta B)$



*L*_c is the injection scale of turbulence, assumed of the order of the cluster size (~pc)

Bohm diffusion can be realised if there are multiple injection scales











Standard power-law,
for plane shocks
$$S = \frac{3u_1}{u_1 - u_2}$$

$$f_s(p) = s \frac{\eta_{\text{inj}} n_1}{4\pi p_{\text{inj}}^3} \left(\frac{p}{p_{\text{inj}}}\right)^{-s} e^{-\Gamma_1(p)} e^{-\Gamma_2(p)}$$

Where:

$$\Lambda_1(\xi, p) = -\frac{2}{3} \int_0^{\xi} f_1(\xi', p) \frac{d \ln(p^3 f_1)}{d \ln p} \xi' d\xi' \quad \blacksquare$$

*p*_{max} due to the upstream: the effective plasma speed decreased reducing the energy gain

Non-linear term: f_s depends on f_1 (upstream)



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Where:

$$\Gamma_1(p) = s \int_{p_{\text{inj}}}^p \frac{\Lambda_1(1,p')}{f_s(p')} dp' \qquad \longrightarrow \qquad \Gamma_1(p) \gg 1 \Rightarrow p \gg p_{\max 1} : \frac{D_1(p_{\max 1})}{u_1} = R_s$$

1

$$\Lambda_1(\xi, p) = -\frac{2}{3} \int_0^{\xi} f_1(\xi', p) \frac{d \ln(p^3 f_1)}{d \ln p} \xi' d\xi' \quad \blacksquare$$

$$\Gamma_2(p) = s \frac{u_2}{u_1} \int_{p_{\text{inj}}}^p \frac{dp'/p'}{e^{\alpha_2(p',R_b)} - 1} \quad \longrightarrow \quad \Gamma_2(p) \gg 1$$

 p_{max} due to the upstream: the effective plasma speed decreased reducing the energy gain

Non-linear term: f_s depends on f_1 (upstream)

 $\Rightarrow p \gg p_{\max 2} : \int_{R}^{n_{b}} \frac{u(r)dr}{D(p_{\max})} = 1$

 p_{\max} due to the escape from the downstream



Impact of diffusion coefficient

shape and effective maximum energy

Typical values for massive stellar clusters

 $\begin{cases} \dot{M} = 10^{-4} M_{\odot} \text{ yr}^{-1} \\ v_w = 3000 \text{ km/s} \\ L_{CR} = 0.1 L_w \\ \eta_B = 0.1 \end{cases}$

PeV energies can be reached in very powerful stellar clusters if the diffusion is close to *Bohm*

For fixed values of all parameters, the diffusion coefficient has a strong impact on the cutoff



Determining the diffusion properties inside the bubble is fundamental



Solution: spatial profile of CR distribution

Region 1 (cold wind):

$$f_1(\xi, p) = f_s(p) \exp\left\{-\int_{\xi}^1 \alpha_1 \left[1 + \frac{\Lambda_1(\xi', p)}{\xi'^2 f_1(\xi', p)}\right] d\xi\right\}$$

Region 2 (shocked wind): $f_{2}(\xi, p) = f_{s}(p) e^{\alpha_{2}} \frac{1 + \beta \left[e^{\alpha_{2}(1) - \alpha_{2}(\xi)} - 1 \right]}{1 + \beta \left[e^{\alpha_{2}(1)} - 1 \right]} + f_{gal}(p) \frac{\beta \left[e^{\alpha_{2}(\xi)} - 1 \right]}{1 + \beta \left[e^{\alpha_{2}(1)} - 1 \right]}$

Region 3 (unperturbed ISM): $f_3(\xi, p) = f_2 \left(\frac{R_b}{R_s}, p \right) \frac{1}{\xi} + f_{gal}(p) \left(1 - \frac{1}{\xi} \right)$

where:
$$\left(\xi = \frac{r}{R_s}; \alpha_1(\xi, p) = \frac{u_1 R_s}{D_1(\xi, p)}; \alpha_2(\xi, p) = \frac{u_2 R_s}{D_2(p)} \left(1 - \frac{1}{\xi}\right); \beta(p) = \frac{D_{\text{gal}}(p) R_s}{u_2 R_b^2};$$



Solution: spatial profile of CR distribution

• For $r < R_s$ the distribution is suppressed except when $E \gtrsim E_{max}$ * Distribution inside the bubble is flat for $E \ll E_{\text{max}}$ * $\neq 1/r$ inferred from FermiLAT data by Aharonian et al., 2019, Nat. Astr.3, 561 • For $E \leq 100 GeV$ the distribution outside the bubble is larger than the one inside it possible signature in the gamma-ray emission (to be investigated)





Source of turbulence: Colliding winds in binaries

- Colliding wind binaries show evidence of particle acceleration
- Turbulence injection on scale comparable to stellar distance due to stellar orbital motion





3D simulation of WR+O colliding wind binaries [Parkin & Grosset, 2011

[Bosh-Ramon, Brrkov & Perucho, A&A 2015]

VLBA 3.6 cm observation of WR 140



Possible role of self-generated magnetic field

Similarly to what is thought to happen for SNR shocks, streaming CRs could amplify the turbulent magnetic field ahead of the shock through resonant or non-resonant modes

Resonant modes

$$\left(\frac{\delta B_{\text{res}}}{B_1}\right)^2 \simeq \frac{\pi}{2} \frac{\xi_{\text{CR}}}{p_{\text{max}}/m_p c} \frac{v_w}{v_A} = \frac{\pi}{2} \frac{\xi_{\text{CR}}}{p_{\text{max}}/m_p c} \frac{1}{\sqrt{2\eta_B}}$$

Non-resonant modes Allowed to grow only if energy density in CR current > energy density of pre-existing magnetic field

$$\eta_B \lesssim \frac{6\,\xi_{\rm CR}}{\log(p_{\rm max}/m_p c)} \frac{v_w}{c} \sim 10^{-4}$$





CR self-amplification is not efficient



Conclusions

Context:

- could contribute to the bulk of Galactic component of cosmic rays.
- * Where those particles are accelerated? Method:
- space-dependent wind velocity and space- and energy-dependent particle diffusion.

Results:

- close to Bohm.
- The spatial profile of the accelerated particles is almost flat in the bubble



* We investigated the spectrum of protons accelerated at the termination shock of stellar winds, developing a technique to solve the transport equation in spherical symmetry able to account for

* The maximum energy can reach the PeV for very massive stellar cluster under the assumption that few percent of the wind kinetic energy is converted into magnetic turbulence and that diffusion is



Acceleration in super-bubbles

- Simultaneous presence of stellar winds and SNe
- Acceleration by multiple repeated shocks
- Fermi II order acceleration by turbulence *



[e.g Higdon & Lingenfelter 2003, Parizot et al. 2004]







Particle acceleration due to multiple shocks and turbulence

For example in the model by Bykov & Toptigyn (1992) the particle spectrum is

$$f_p(p) \propto \begin{cases} \left(\frac{p}{p_i}\right)^{-3}, & \text{for } p_i$$

Collective reacceleration occurs below $p^* \simeq p_i e^{t/t_{ch}}$ where $t_{ch} = l_c/u_T$

Maximum value of *p*^{*} determined from energy equipartition

$$W_{\rm cr} < W_{\rm th} \Rightarrow p_* < m_p c \eta^{-1} (u/c)^2 \approx 1 \,{\rm GeV}/c \frac{10^{-5}}{\eta} \left(\frac{1}{10^{-5}}\right)^{-5}$$

[Bykov & Fleishman 1992]

A general feature of acceleration models including turbulence and multiple shocks is the hard spectrum (\leq 3) below some characteristic energy







From Bykov & Fleishman 1992



Particle acceleration due to multiple shocks and turbulence

- Time dependent model accounting for winds, SNRs and turbulence.
- The intermittency of SN explosion produces a large variation of CR content in SBs
- * Maximum energy dominated by SNR; turbulence affects only $E \leq 1 \text{ GeV}$
- Particle escape from the super bubble results in steep spectra ~ $E^{-2.2}$



CR spectra at various times for a typical cluster of 100 massive stars (left), and 500 massive stars (center). The right panel displays the average escaping fluxes.

[Vieu, Gabici & Tatischeff, ICRC 2021]





Shell fragmentation



[Lancaster et al., ApJ 914, 89 (2021)] [Lancaster et al., ApJ 914, 90 (2021)]



*

Rayley-Taylor instability between dense ISM and low density bubble produces a fragmentation of the shocked ISM shell.

- Fragmentation enhances the cooling rate
 - The bubble effective size is reduced
- Dense clouds are located inside the bubble
 - gamma-ray emission possible also from the bubble interior
- What is the effect on CR diffusion?

3D Hydrodynamic $\mathscr{L}_w/M_* = 10^{34} \text{erg s}^{-1} M_{\odot}^{-1}$ simulations

 $M_{\rm cloud} = 10^5 M_{\odot}$ $t_{age} = 2.23 Myr$ $R_{\rm cloud} = 20\,{\rm pc}$



Open questions

- Which is the main acceleration mechanism?
 - wind-wind collisions
 - turbulent acceleration
 - wind termination shocks
- * Which is the maximum possible energy of accelerated particles?
 - strong dependence on magnetic field strength and turbulence power
- Study of turbulence
 - which observations?
 - need of specific numerical simulations
 - role of realistic environments (fragmentation; cooling)
- •
- * the stellar clusters population?

Chemical composition: Can CR from stellar winds help to account for anomalous CR chemical composition? Can stellar winds significantly contribute to Galactic CRs? Which is the total contribution integrated over

