

Particle acceleration to extreme energies

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Usual suspects... twenty years ago...

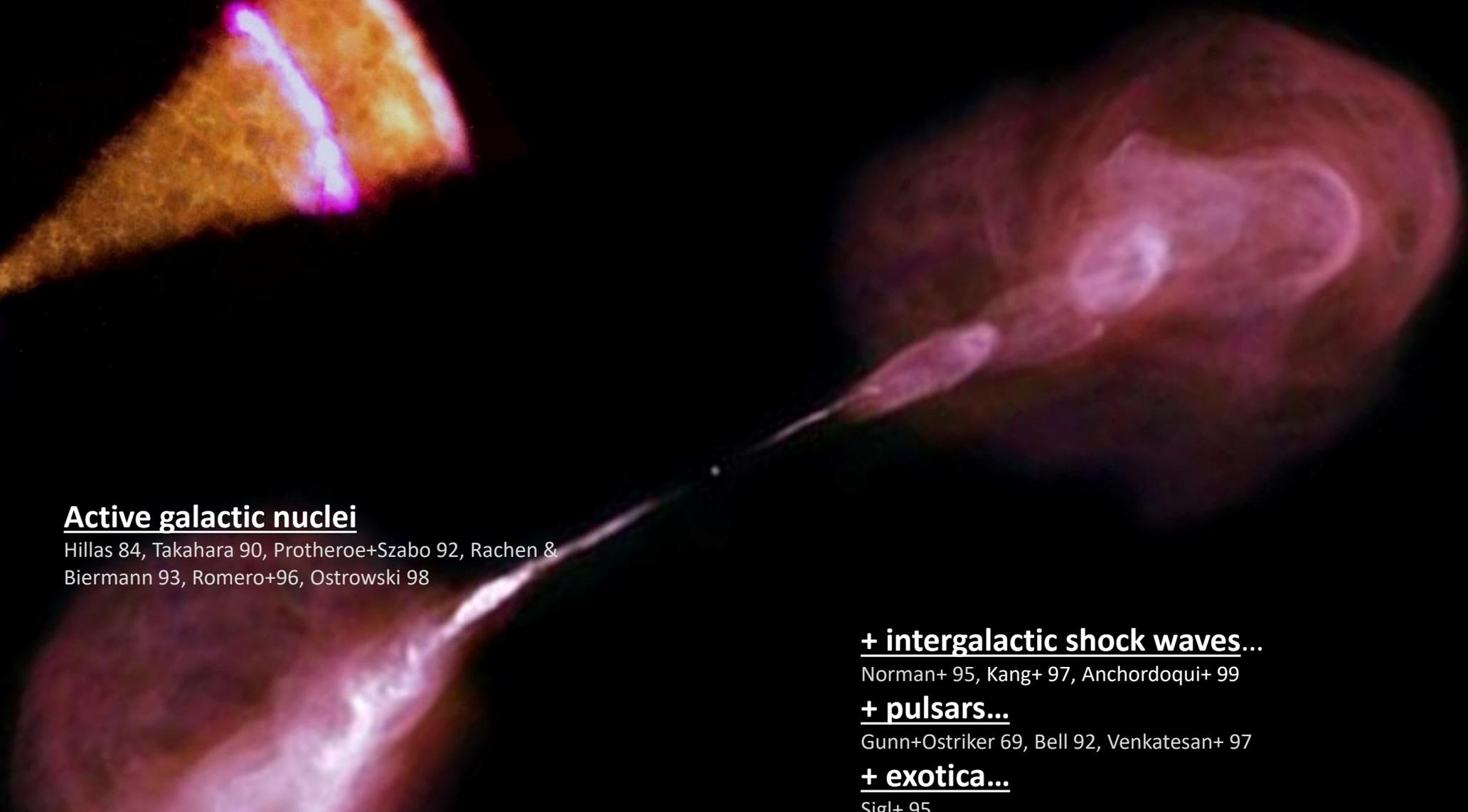
Gamma-ray bursts (scale x 10⁵)

Milgrom+Usov 95, Vietri 95, Waxman 95



Active galactic nuclei

Hillas 84, Takahara 90, Protheroe+Szabo 92, Rachen & Biermann 93, Romero+96, Ostrowski 98



+ intergalactic shock waves...

Norman+ 95, Kang+ 97, Anchordoqui+ 99

+ pulsars...

Gunn+Ostriker 69, Bell 92, Venkatesan+ 97

+ exotica...

Sigl+ 95

Usual suspects... now...

Powerful transients: high and low luminosity GRBs, relativistic SNe, fast spinning magnetars/pulsars...

High luminosity GRB:

Milgrom + Usov 95, Vietri 95, Waxman 95, Rachen + Meszaros 96, Gallant + Achterberg 99, Pelletier + Kersale 00, Dermer + Humi 01, Waxman 01, Scully + Stecker 02, Gialis + Pelletier 03, Waxman 04, Rieger + Duffy 06, Asano+ 09, 10, Razzaque+ 10, Giannios 10, Eichler + Pohl 11, Metzger+ 11, Baerwald+ 15, Globus+ 15, Asano + Meszaros 16, Samuelsson+ 19

Low-luminosity GRBs

/ Relativistic SNe:

Murase+ 06, Budnik+ 08, Wang+ 08, Liu+ 11, Chakraborti+ 11, Liu + Wang 12, Zhang + Murase 18, Zhang+ 18, Boncioli+ 19

Magnetar WNe/ Pulsar WNe :

Bell 92, Blasi+ 00, de Gouveia dal Pino + Lazarian 01, Arons 03, Vietri+ 03, Fang+ 13, Lemoine+ 15, Fang+ 18, Kirk + Giacinti 19

Blazar/Radio-galaxy jet+lobe:

Takahara 90, Rachen + Biermann 93, Ostrowski 98, Farrar + Piran 00, Tinyakov + Tkachev 01, Gorbunov+ 02, Lyutikov + Ouyed 07, Atoyan+Dermer 08, Gorbunov + 08, Dermer+ 09, Hardcastle+ 09, O'Sullivan+ 09, Dermer + Razzaque 10, Gopal-Krishna+ 10, Biermann+ deSouza 12, Murase+ 12, Ptuskin+ 13, Caprioli 15, Wang + Loeb 17, Eichmann+ 18, Liu+ 17, Resconi+ 17, Kimura+ 18, Matthews+ 18,19, Fang + Murase 18, Rieger 19

Active galactic nuclei:

AGN Core:

Protheroe + Szabo 92, Boldt + Ghosh 99, Levinson 00, Levinson + Boldt 00, Torres+ 02, Dempsey + Rieger 09, Istomin + Sol 09, Neronicov + 09, Rieger + Aharonian 09, Dutan + Caramazza 14, Moncada+ 17

+ intergalactic shock waves (clusters, starbursts)...

Norman+95, Kang+ 97, Anchordoqui+ 99, + 01, Murase+ 08, Kotera +09, Malkov +11, Anchordoqui 18, Romero+ 18

+ other transients: e.g. tidal disruption events...

Farrar+Piran14, Alves Batista + Silk 17, Biehl+18, Guepin+18

Connections to many (contemporaneous) fields of physics...

High-energy astrophysics:

e.g. the origin, dynamics, energy content and dissipative physics of (relativistic) jets...
e.g. environments of compact objects...

Experimental astroparticle physics:

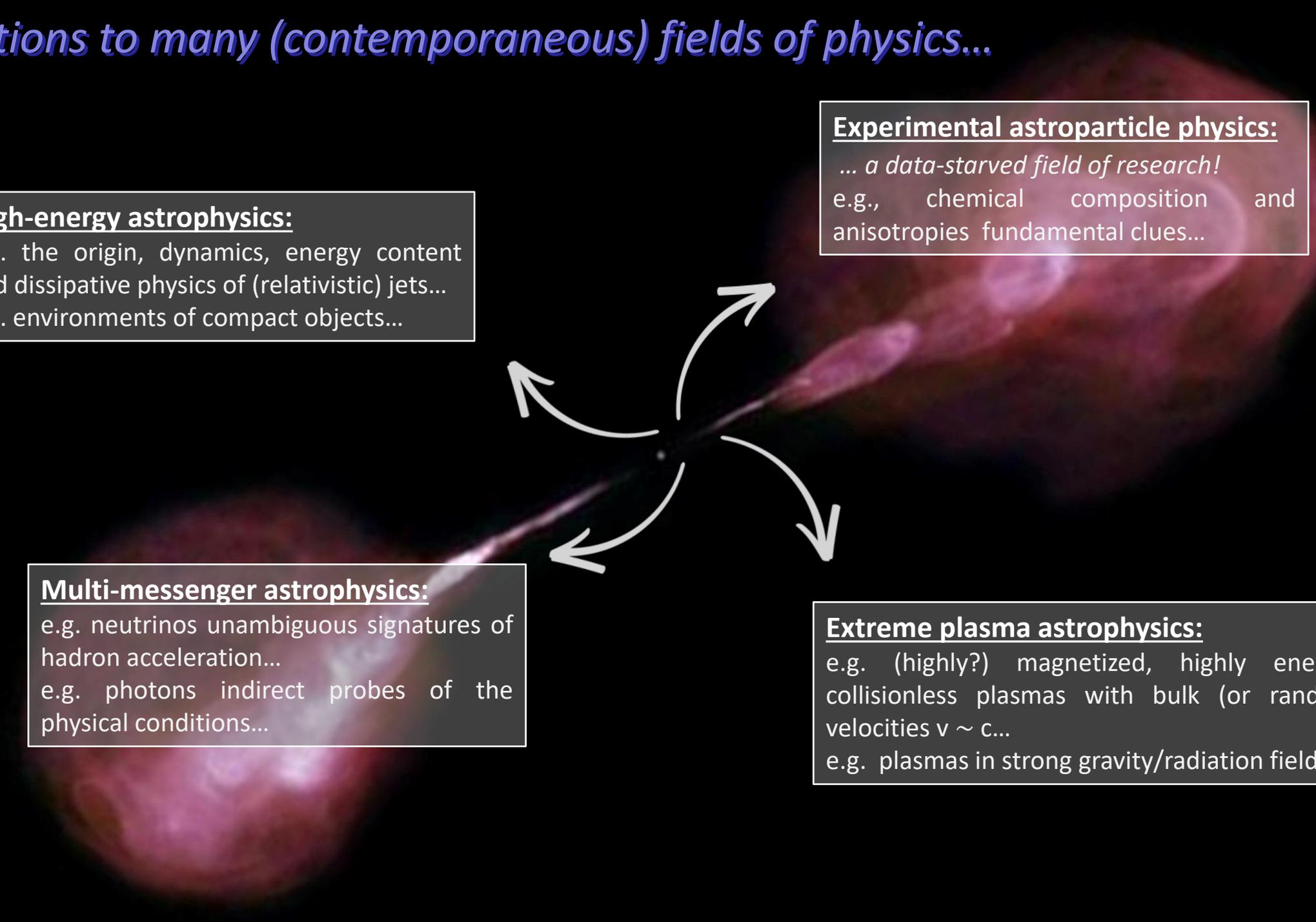
... a data-starved field of research!
e.g., chemical composition and anisotropies fundamental clues...

Multi-messenger astrophysics:

e.g. neutrinos unambiguous signatures of hadron acceleration...
e.g. photons indirect probes of the physical conditions...

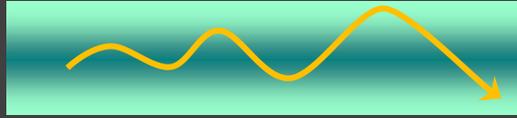
Extreme plasma astrophysics:

e.g. (highly?) magnetized, highly energetic collisionless plasmas with bulk (or random?) velocities $v \sim c$...
e.g. plasmas in strong gravity/radiation fields...

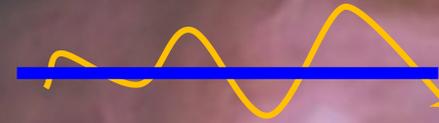


Various (more or less known) acceleration scenarios...

Shear acceleration



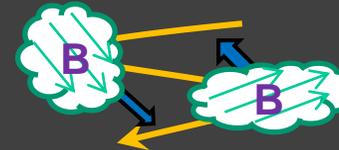
Shock acceleration



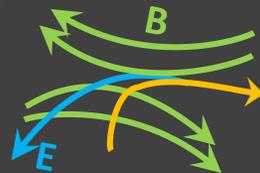
Linear acceleration in gaps



Turbulent acceleration



Reconnection

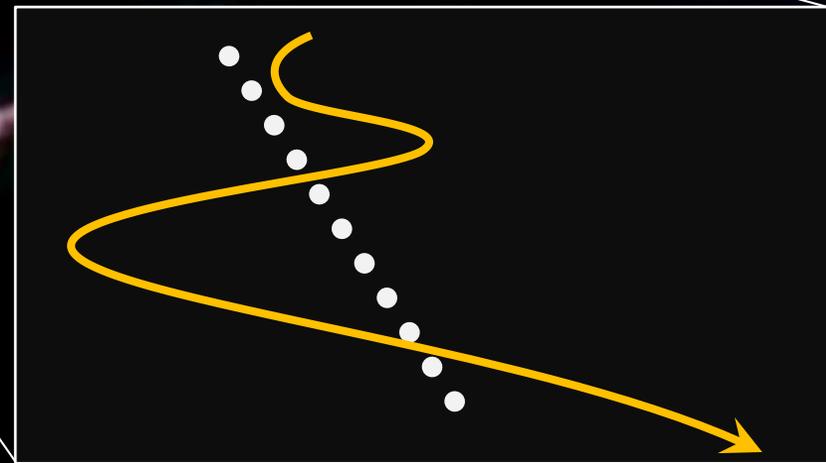
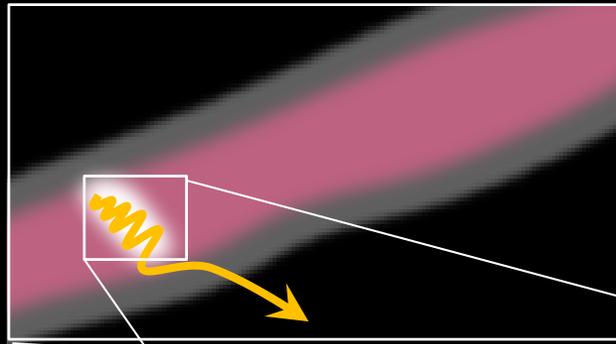


A challenge of scales...

Macroscopic scales: particle escape...

$$r_g = L : E = 10^{20} \text{ eV } Z B_{100\mu\text{G}} L_{\text{kpc}}$$

$\sim \mathcal{O}(10^{22} \text{ cm})$



$\sim \mathcal{O}(10^9 \text{ cm})$

Micro-scales: particle injection...

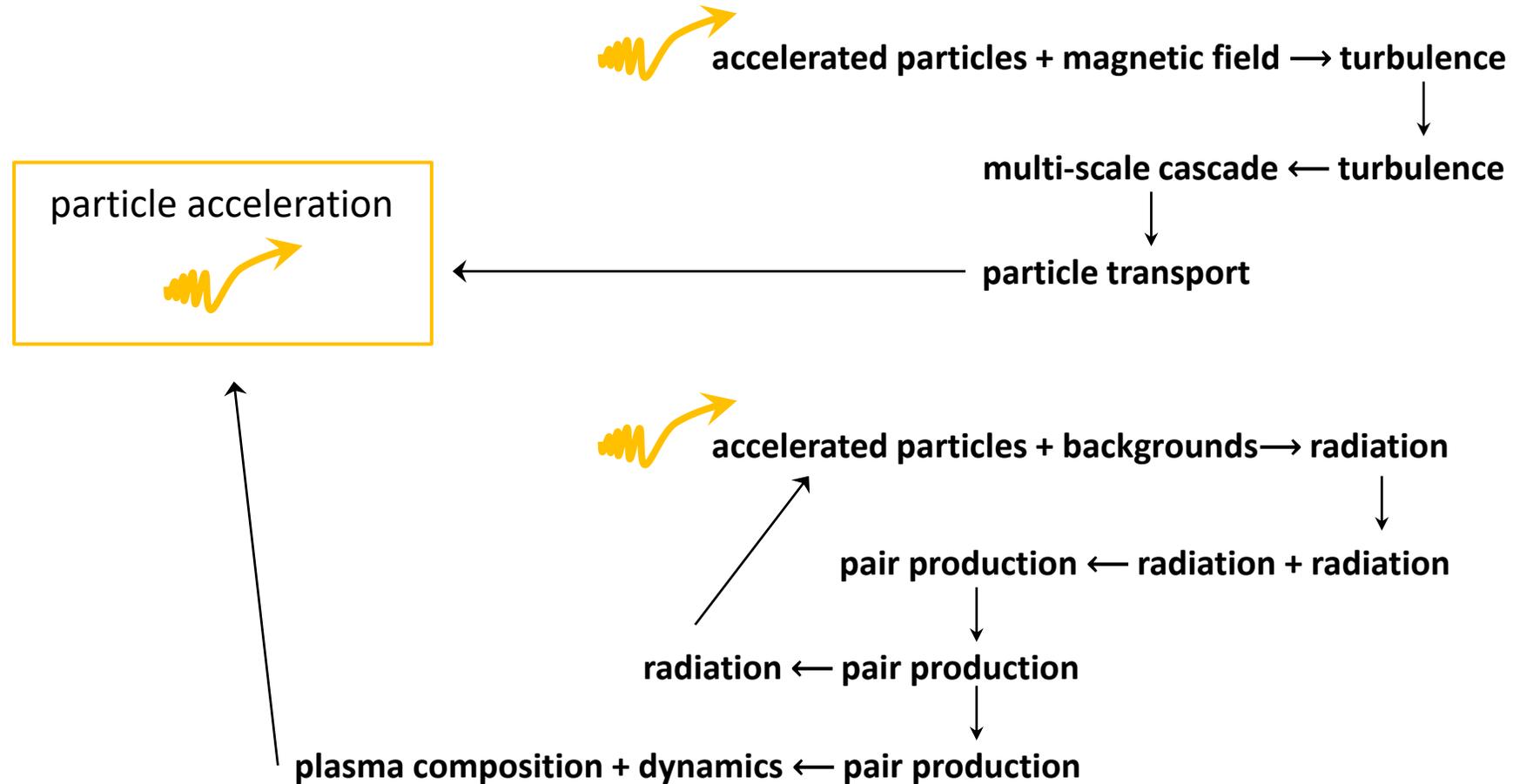
$$c/\omega_c \sim 10^8 \text{ cm } B_{100\mu\text{G}}$$

$$c/\omega_p \sim 10^7 \text{ cm } n_{\text{cm}^{-3}}^{1/2}$$

Particle acceleration as multi-scale, nonlinear process

... in many (most?) situations, accelerated particles feed back on the electromagnetic environment

⇒ need to go beyond the test particle description!



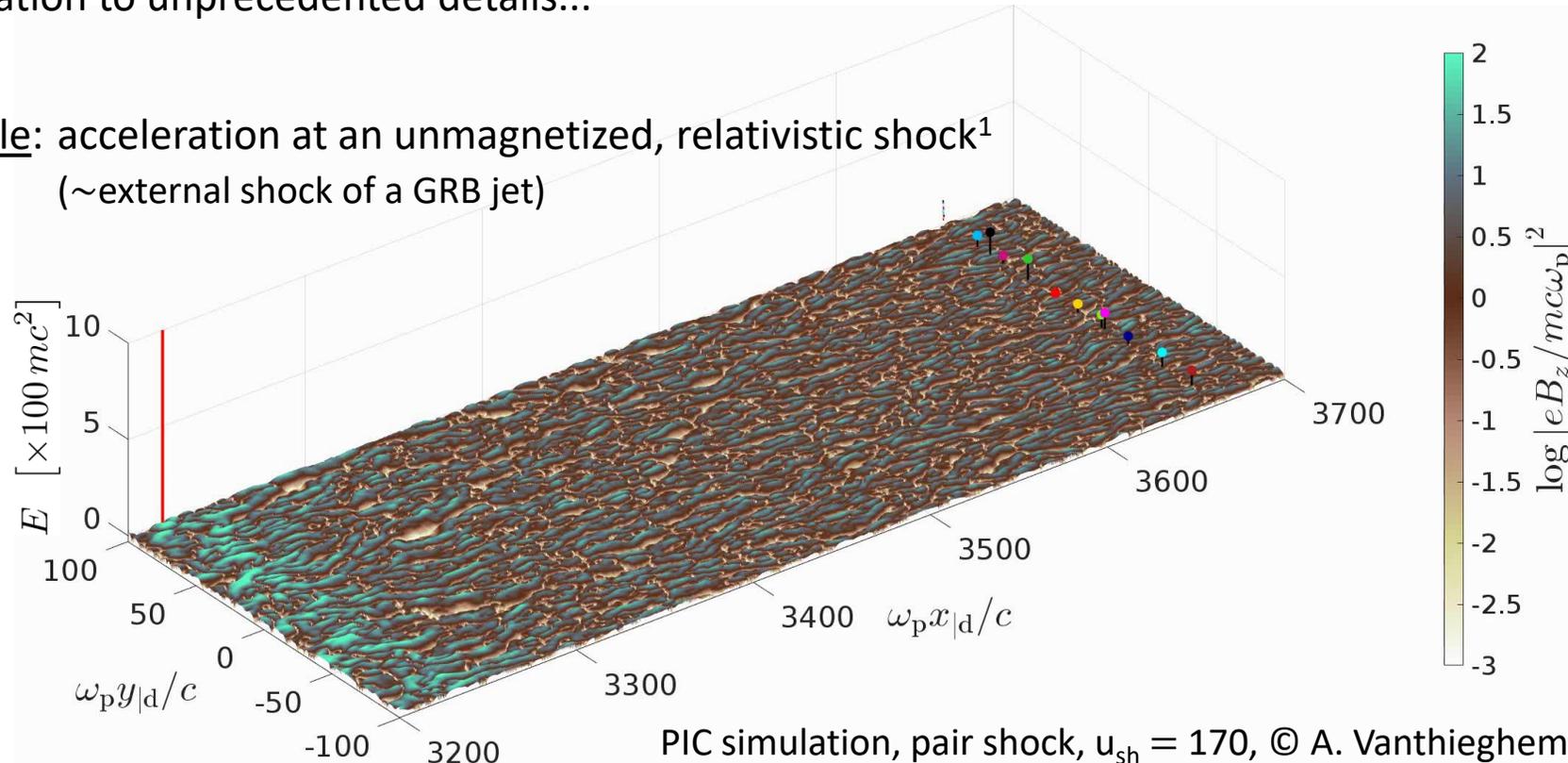
Particle acceleration as multi-scale, nonlinear process

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⇒ need to go beyond the test particle description!

... HPC numerical simulations (Monte Carlo, particle-in-cell, MHD+PIC, hybrid ...) allow to explore the physics of acceleration to unprecedented details...

example: acceleration at an unmagnetized, relativistic shock¹
(~external shock of a GRB jet)



magnetic field self-generated
by accelerated particles
on microscopic length scales

... an important caveat to keep in mind: ab initio simulations remain limited to small scales...

Particle acceleration to extreme energies

Outline:

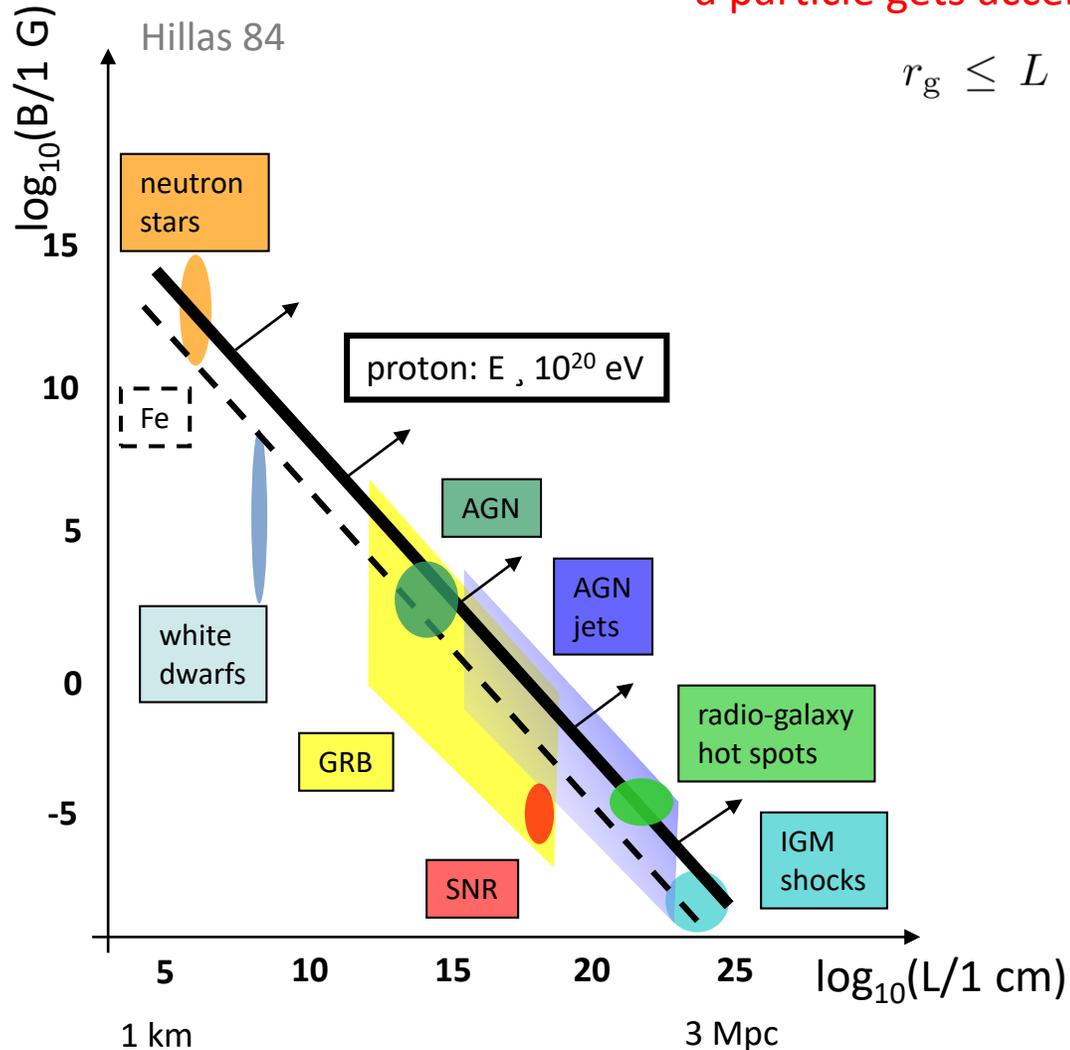
1. The view from phenomenology: top-down, from large to small scales
2. The view from microphysics: bottom-up, from first principles
3. Discussion: clues and issues

Acceleration – Hillas bound

a simple criterion: to find which object ***might*** be a source of UHE cosmic rays:

a particle gets accelerated as long as it is confined in the source:

$$r_g \leq L \Rightarrow E \leq 10^{20} \text{ eV } Z B_{\mu\text{G}} L_{100 \text{ kpc}}$$



1. necessary, but by no means sufficient (losses, age...)

E_{conf} : $r_g(E_{\text{conf}}) = L$, the best you can hope for...

\Rightarrow acceleration challenge: reach E_{conf}

2. watch out for relativistic effects

accelerators are likely relativistic sources...

A luminosity bound for acceleration in outflows

→ a generic model: acceleration in some relativistic outflow

write acceleration timescale (comoving frame): $t_{\text{acc}} = \mathcal{A} t_g$

$$t_g \equiv \frac{p}{eB} \text{ gyrotime, } t_{\text{scatt}} \text{ scattering timescale}$$

... comparing t_{acc} and age $t_{\text{dyn}} = R/(\beta\Gamma c)$ bounds the (magnetic) luminosity of the source to reach UHE:

$$t_{\text{acc}} \leq t_{\text{dyn}} \Rightarrow E_{\text{obs}} \leq \mathcal{A}^{-1} Z e B R / \beta$$

... magnetic luminosity of the source: $L_B = 2\pi R^2 \Theta^2 \frac{B^2}{8\pi} \Gamma^2 \beta c$

$$\Rightarrow L_{\text{tot}} \geq L_B \geq 10^{45} \dots \mathcal{A}^2 \left(\frac{E}{Z \times 10^{20} \text{ eV}} \right)^2 \text{ erg/s}$$

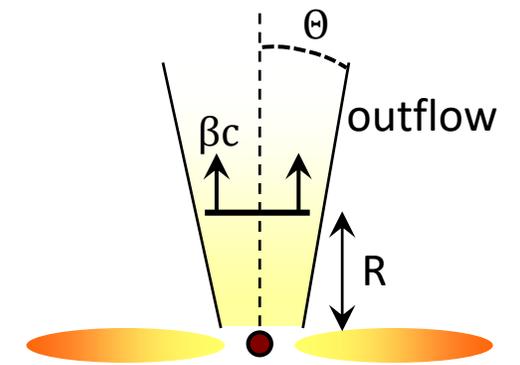
... some typical examples:

low lum. AGN: $L_{\text{bol}} \ll 10^{45}$ ergs/s

high lum. AGN: $L_{\text{bol}} \sim 10^{46}$ - 10^{48} ergs/s

Crab pulsar: $L_{\text{bol}} \sim 10^{39}$ ergs/s

high lum. GRBs: $L_{\text{bol}} \sim 10^{52}$ ergs/s



A luminosity bound for acceleration in outflows

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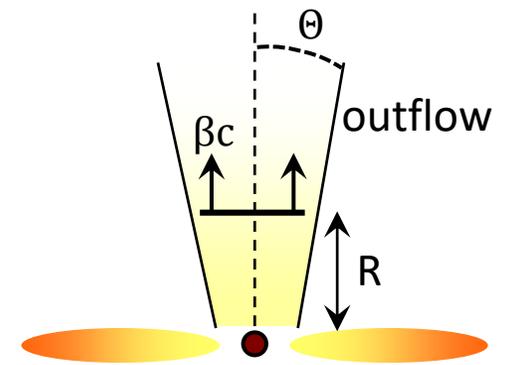
... comparing t_{acc} and age $t_{\text{dyn}} = R/(\beta\Gamma c)$ bounds the (magnetic) luminosity of the source to reach UHE:

$$L_{\text{tot}} \geq 10^{45} \dots \mathcal{A}^2 \left(\frac{E}{Z \times 10^{20} \text{ eV}} \right)^2 \text{ erg/s}$$

Note:

+ accounts for possible self-amplification of magnetic field by accelerated particles!

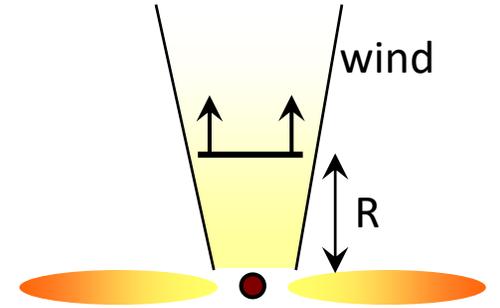
— assumes an outflow: not applicable to static sources, e.g. gaps or stochastic acceleration in lobes of radio-galaxies...



A luminosity bound for acceleration in outflows

→ a generic model: acceleration in some relativistic outflow

write acceleration timescale (comoving frame): $t_{\text{acc}} = \mathcal{A} t_L$



→ $\mathbf{A} \gg 1$ in most acceleration scenarios:

e.g. in Fermi-type, $\mathbf{A} \sim$ interaction time / energy gain

sub-relativistic Fermi I: $\mathcal{A} \gtrsim 1/\beta_{\text{sh}}^2$ (β_{sh} shock velocity/c)
(saturation: Bohm regime!)

sub-relativistic stochastic: $\mathcal{A} \gtrsim 1/\beta_A^2$ (β_A turb. velocity/c)

relativistic Fermi: $\mathcal{A} \sim t_{\text{scatt}}/t_g$ (TBD!)

relativistic reconnection: $\mathcal{A} \gtrsim 10$

→ **strong limit:** $L_{\text{tot}} \geq 10^{45} \dots \mathcal{A}^2 \left(\frac{E}{Z \times 10^{20} \text{ eV}} \right)^2 \text{ erg/s}$

A luminosity bound for acceleration in outflows

→ a generic model: acceleration in some relativistic outflow

write acceleration timescale (comoving frame): $t_{\text{acc}} = \mathcal{A} t_g$

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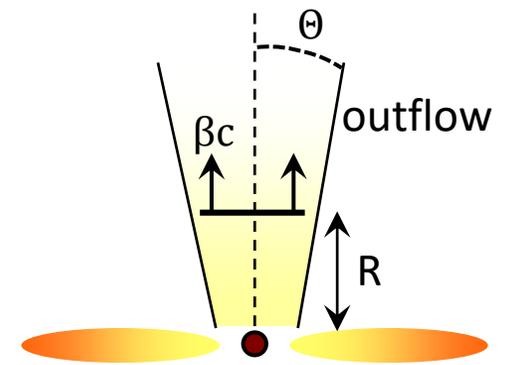
$$L_{\text{tot}} \geq 10^{45} \dots \mathcal{A}^2 \left(\frac{E}{Z \times 10^{20} \text{ eV}} \right)^2 \text{ erg/s}$$

→ a direct consequence: **chemical composition (Z) controls the phenomenology!**
(very few candidates for low Z, many more for high Z!)

+ to go further: $\dots \mathcal{A}^2 \propto \frac{t_{\text{scatt}}}{t_g} \begin{cases} u^2 & (u \gg 1) \\ 1/u & (u \ll 1) \end{cases}$ (u 4-velocity of outflow)

⇒ favors relativistic (mildly?) sources...

+ optimal acceleration to reach confinement energy: $t_{\text{acc}} \sim t_g$!



Top - down... some lessons learned...

Three critical properties of UHECR sources:

→ a large (apparent) source density¹:

$$\Delta t_{\text{magnetic}} \dot{n}_{\text{UHECR}} \text{ or } n_{\text{UHECR}} \gtrsim 10^{-5} / \text{Mpc}^3$$

→ a high output of cosmic rays²:

$$\dot{e}_{\text{UHECR}} \sim 10^{44} \text{ erg/Mpc}^3/\text{yr}$$

... a non-trivial constraint:

e.g. $L_{\text{UHE}}/L_{\gamma} \sim 10$ for HL GRBs...

e.g. $L_{\text{UHE}}/L \sim \mathcal{O}(1\%)$ for radio-galaxies...

→ a high magnetic luminosity:

$$L_{\text{tot}} \gtrsim 10^{45} \text{ erg/s} \dots \left(\frac{t_{\text{acc}}}{t_{\text{g}}} \right)^2 \left(\frac{E/Z}{10^{20} \text{ eV}} \right)^2$$

... leading contenders, for accelerating intermediate nuclei ($Z \sim 10$):

→ powerful radio-galaxies, $L \sim 10^{44} \text{ erg/s}$, $u \sim 1$...

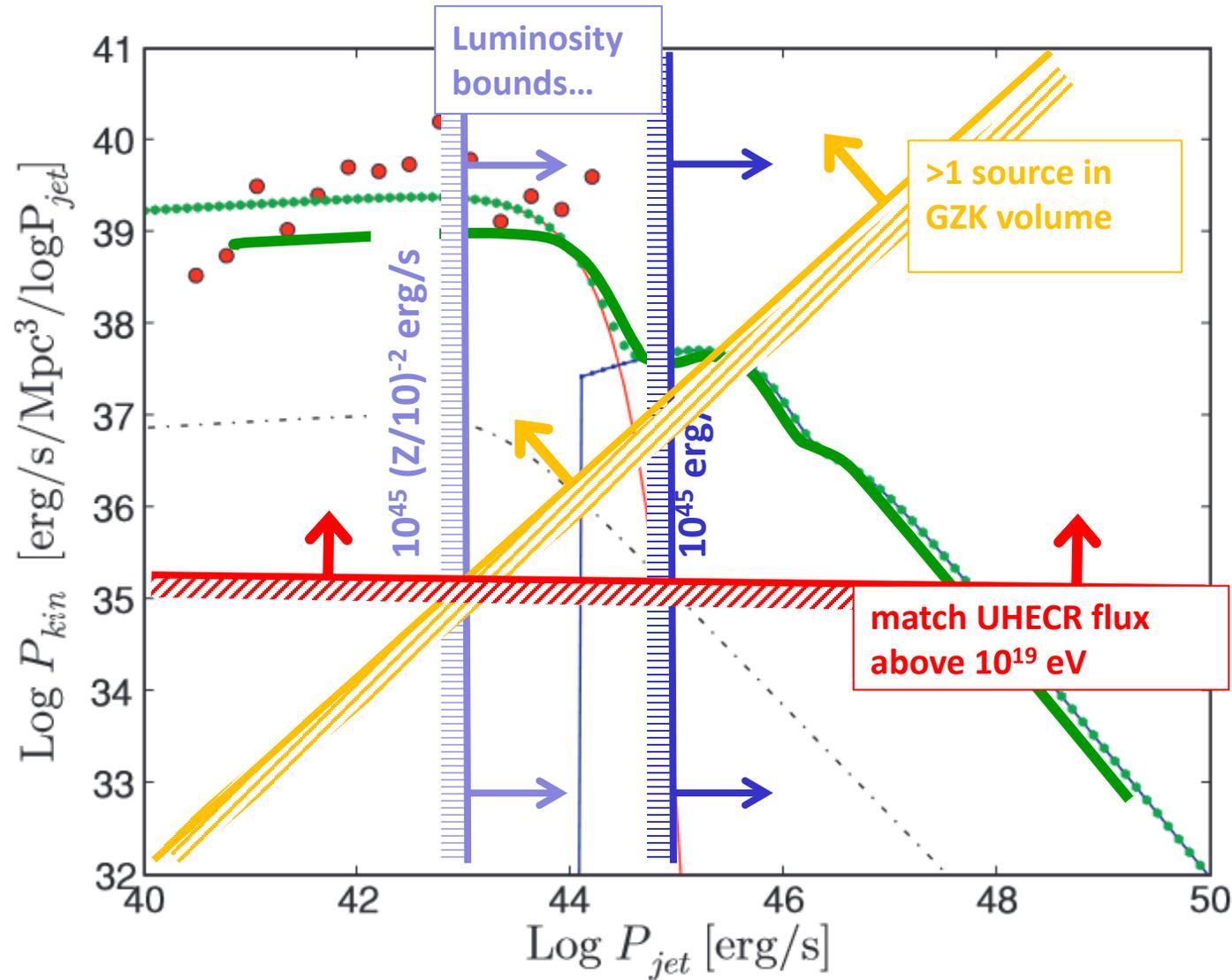
→ relativistic supernovae (LLGRB), $L \sim 10^{44} \text{ erg/s}$, $u \sim 1$...

... need extreme sources for accelerating light nuclei ($Z \sim 1$):

→ gamma-ray bursts, fast-spinning magnetar/pulsar wind nebulae...

→ most powerful FRII like radio-galaxies

The view from phenomenology... the radio-galaxy population...



Körding+ 07

... local radio-galaxies barely satisfy the luminosity bound: accelerate $Z \sim 10+$ nuclei?

Particle acceleration to extreme energies

Outline:

1. The view from phenomenology: top-down, from large scales to small scales

→ constraints from L_{tot} , n_{UHECR} , \dot{e}_{UHECR}

→ for minimal constraints, search for: $t_{\text{acc}} \sim t_{\text{g}}$ at UHE

2. The view from microphysics: bottom-up, from first principles

3. Discussion: clues and issues

Particle acceleration from first principles (?)

→ Lorentz force:
$$\frac{d\mathbf{p}}{dt} = q \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)$$

... but, $\mathbf{E} \leftrightarrow \mathbf{B}$ in a change of reference frame: rely on Lorentz scalars $\mathbf{E} \cdot \mathbf{B}$ and $\mathbf{E}^2 - \mathbf{B}^2$...

Acceleration à la Fermi: highly conducting plasma... $\mathbf{E} \cdot \mathbf{B} = 0$ and $\mathbf{E}^2 - \mathbf{B}^2 < 0$

→ **generic for UHECR?**

... corresponds to ideal Ohm's law $\mathbf{E} = -\mathbf{v}_p \times \mathbf{B} / c$... (on timescales \gg micro, comoving electric field is screened out)

→ **Fermi-type scenarios: magnetized turbulence, shear flows, shock waves**

"Linear" accelerators: non-MHD flows... $\mathbf{E} \cdot \mathbf{B} \neq 0$ or $\mathbf{E}^2 - \mathbf{B}^2 > 0$

→ acceleration can proceed unbounded along \mathbf{E} (or at least \mathbf{E}_{\parallel})...

→ **gaps in magnetospheres**

→ **reconnection**

Particle acceleration in electrostatic gaps

→ Gaps: regions where plasma density cannot screen out parallel electric fields, e.g. of rotating magnetospheres

... in gaps: acceleration as in linear accelerators,

$$E_{\max} \simeq q|\mathbf{E}|L_{\text{gap}} = q\Delta\phi \text{ (voltage drop)}$$

$$E_{\max} \sim 10^{19} \text{ eV } Z \frac{M_{\text{BH}}}{10^9 M_{\odot}} \frac{L_{\text{gap}}}{r_{\text{BH}}} \frac{B}{100 \text{ G}}$$

→ Motivations: observations of rapid flares from AGN, up to TeV energies¹

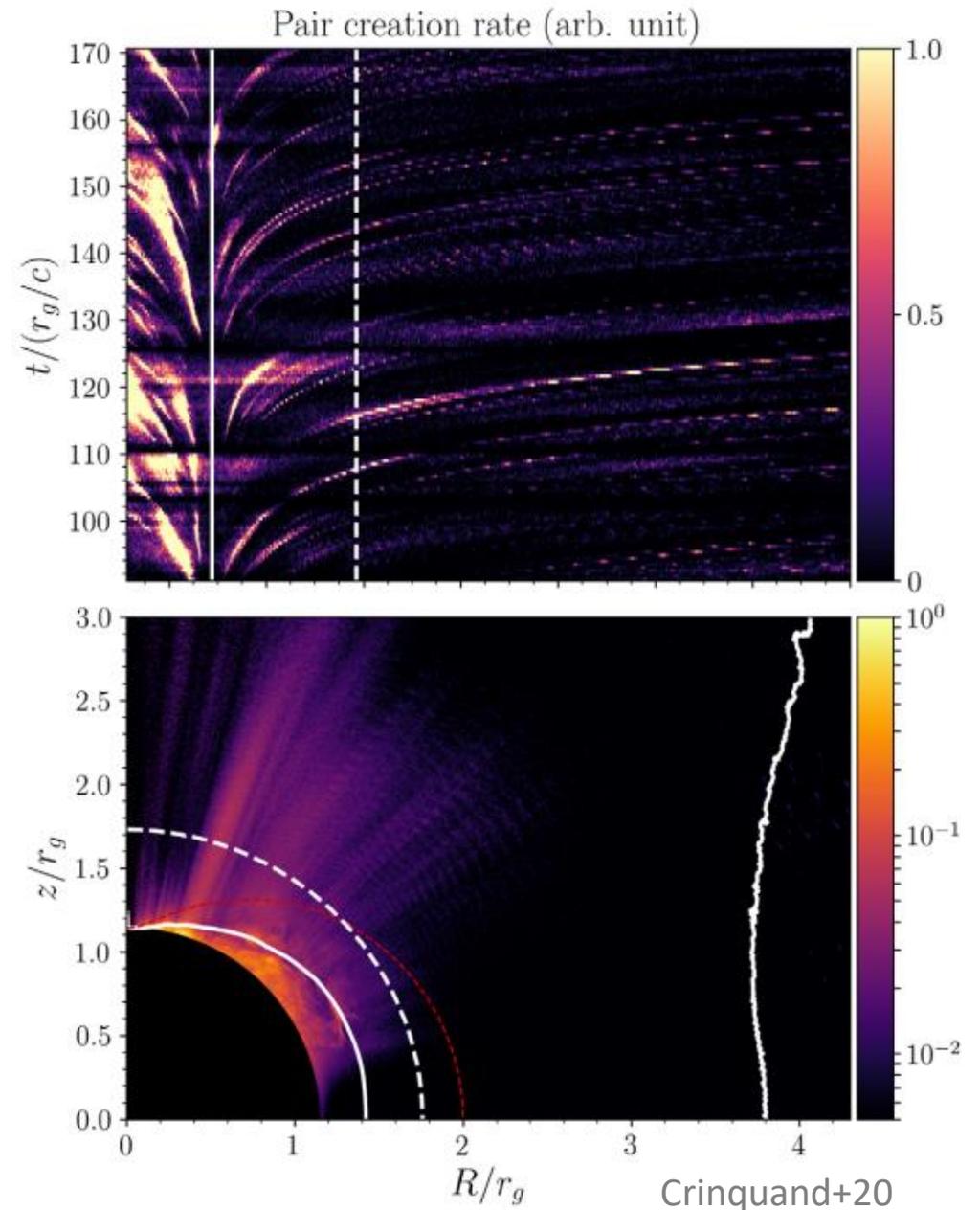
→ Issues/questions:

→ **value of L?**

(input from kinetic simulations of BH magnetospheres²)

→ **injection of hadrons in gaps?**³

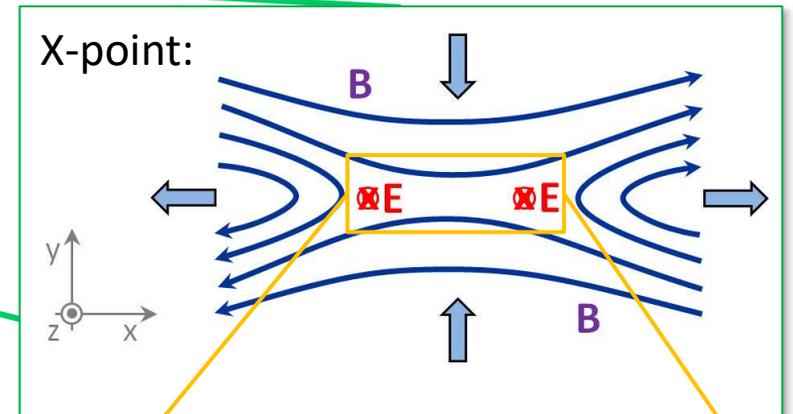
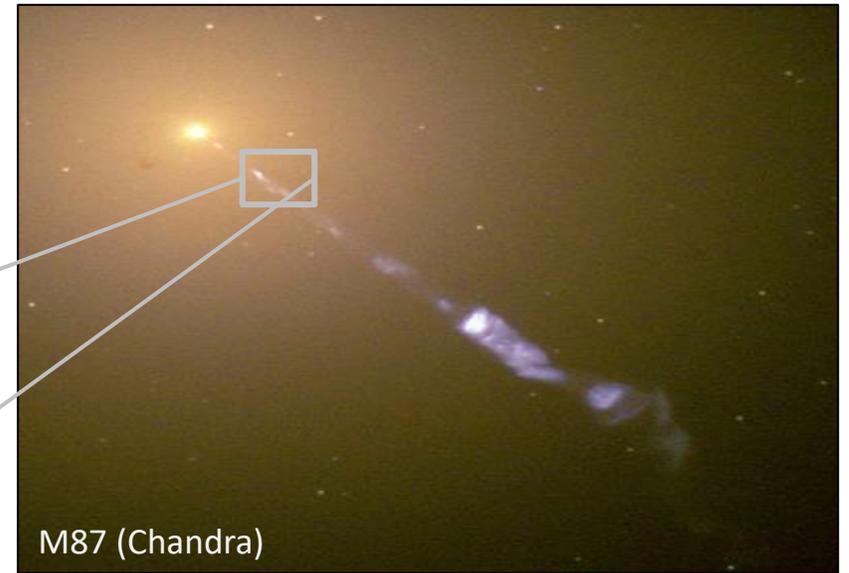
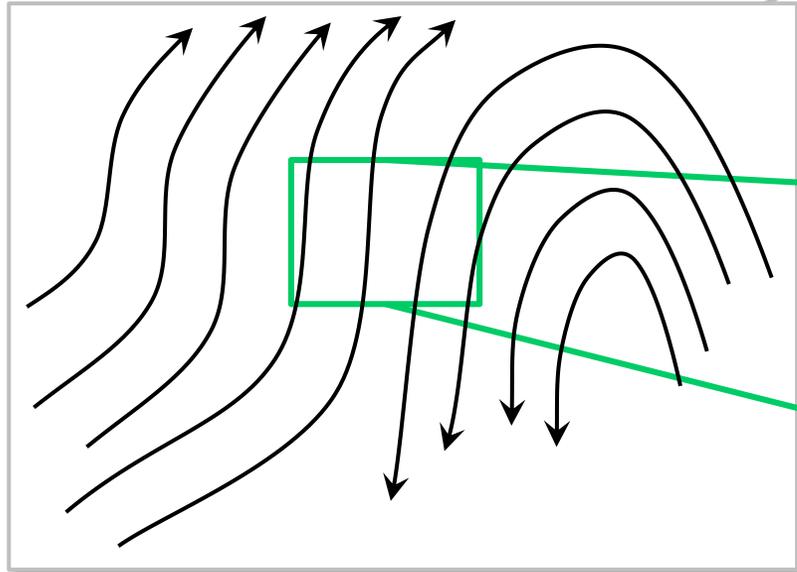
→ **energy losses/photodisintegration, maximal energy?**



Acceleration in reconnection regions

→ reconnection: dissipation of magnetic energy through interchange of field lines of opposite polarity

→ wrt UHECR: e.g. reconnection of tangled field in jets¹...



here: $E \cdot B \neq 0$ or $E^2 - B^2 > 0$
⇒ linear accelerator

Acceleration in reconnection regions

→ reconnection: dissipation of magnetic energy through interchange of field lines of opposite polarity

→ wrt UHECR: e.g. reconnection of tangled field in jets...

→ Lessons from kinetic HPC simulations¹:

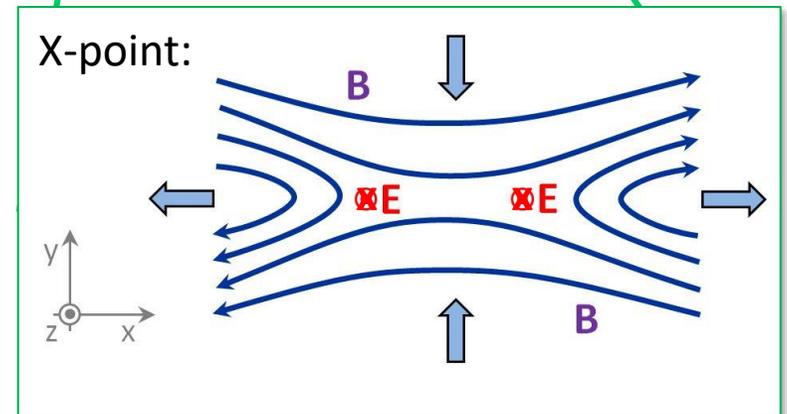
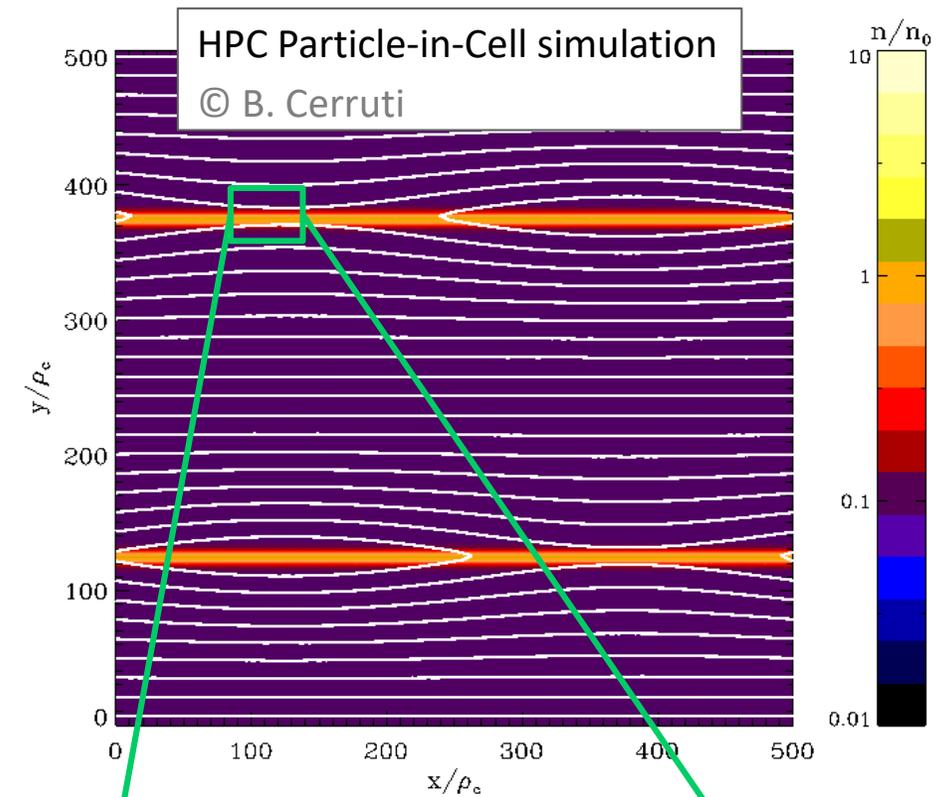
... **particle acceleration fast and efficient in relativistic (magnetically dominated) regime**

$$\text{magnetization } \sigma = \frac{\text{magnetic e. density}}{\text{plasma e. density}}$$

... particle acceleration through E_z at X-point

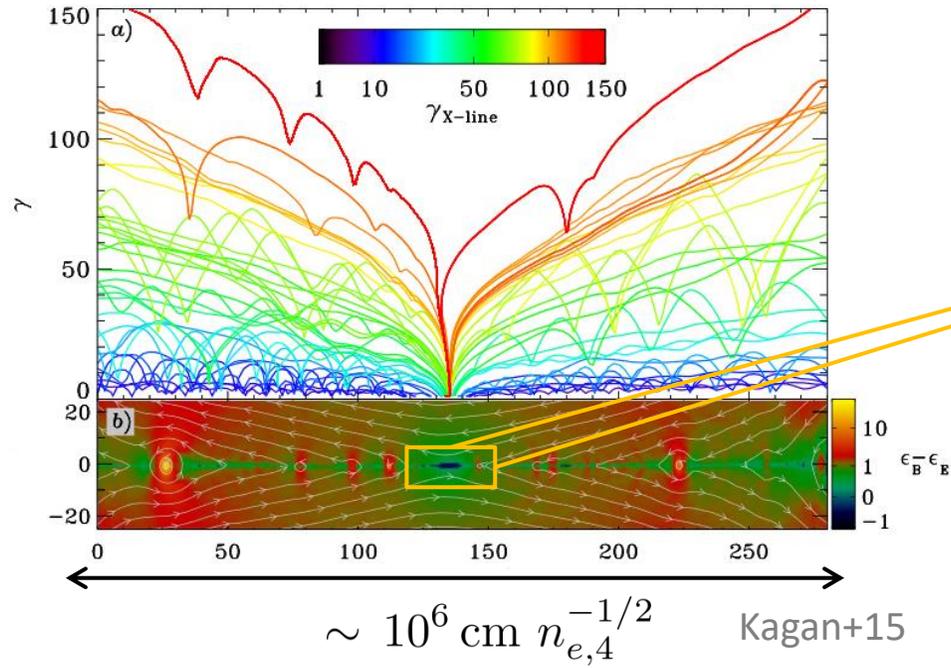
$$E_z = -\beta_{y,\text{in}} B_x \Rightarrow t_{\text{acc}} \simeq \frac{t_g}{\beta_{\text{in}}}$$

β_{in} “reconnection rate” determines t_{acc} at X-point, as large as 0.1 in relativistic regime...

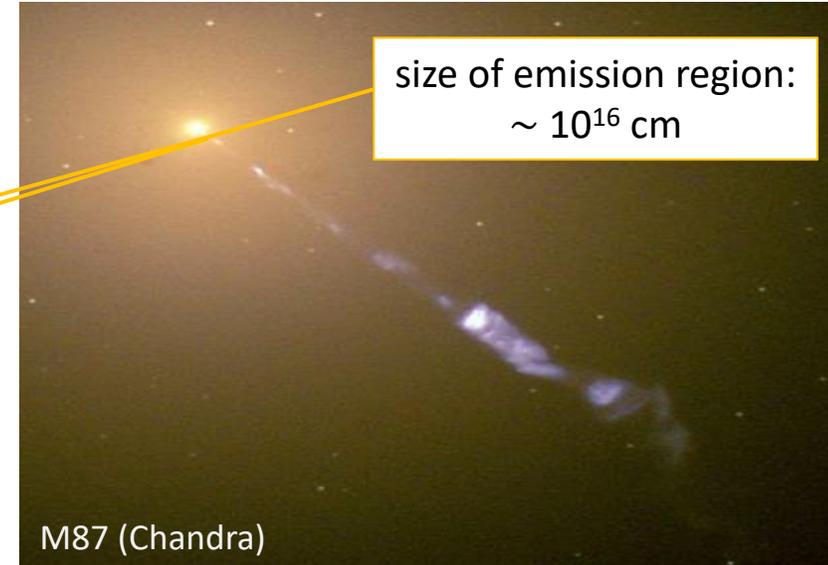


Acceleration in reconnection regions

from numerical simulations...



... to actual astrophysical objects!



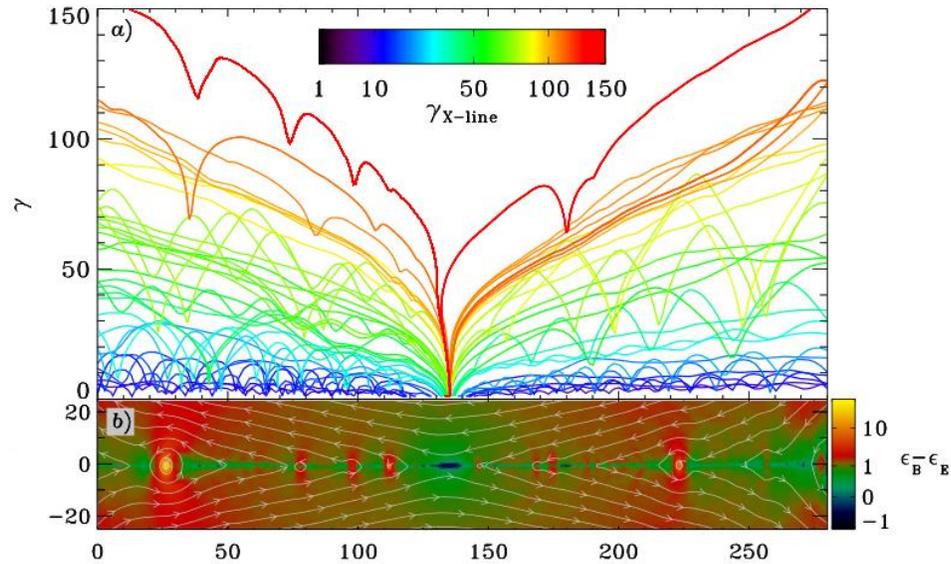
X-points are small scale features... unless magnetic field can confine particle in reconnection region, most of acceleration takes place through Fermi processes in surrounding velocity structures (turbulence?)...

... in practice: "confinement" limit $E_{\text{max}}/mc^2 \sim \text{a few} \times \sigma$

\Rightarrow requires huge magnetizations for direct acceleration to UHE at X-point

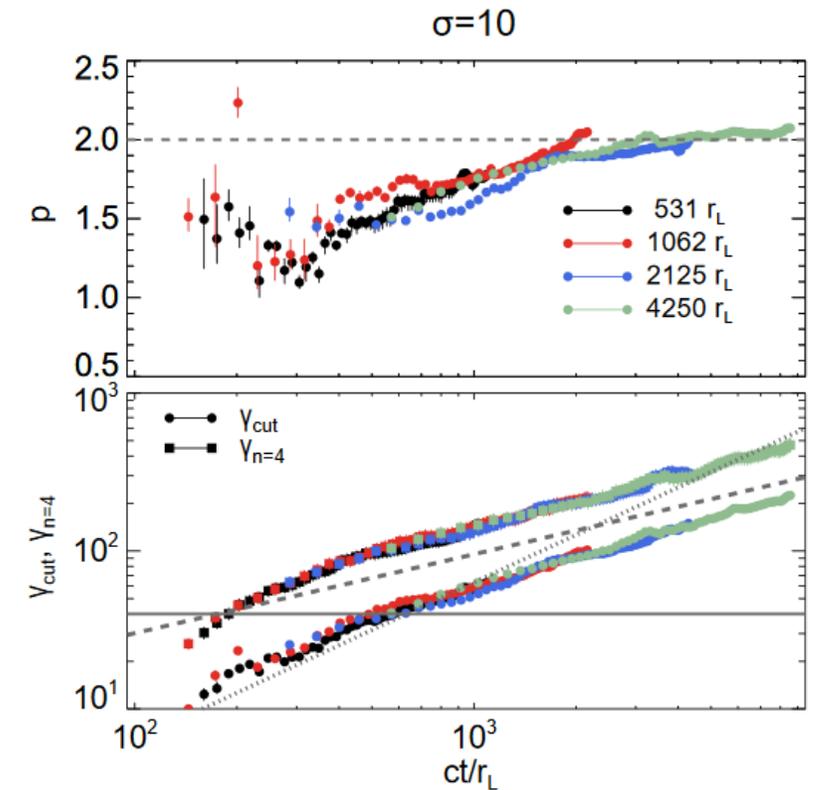
Acceleration in reconnection regions

→ acceleration proceeds in two stages^{1,2}:



(1) acceleration in dissipation regions...

- fast rate: $t_{\text{acc}} \sim 0.1 t_g$
- hard powerlaws with $p < 2$ if $\sigma \gtrsim 1$...
- ... but a cut-off¹ at Lorentz factor $\sim 4\sigma$ (escape!)



(2) acceleration in surrounding turbulence...

- softer powerlaws...
- slow acceleration²: $t_{\text{acc}} \propto t_g^2$...
- i.e. t_{acc} / t_g increases with energy: unlikely to reach UHECR...

(larger simulations needed to probe long term!)

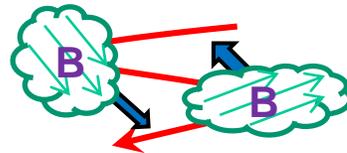
Fermi-type acceleration to UHE

→ Lorentz force: $\frac{dp}{dt} = q \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)$... what is the origin of \mathbf{E} ?

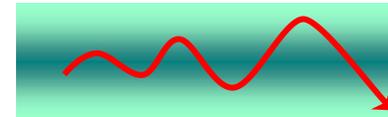
1. Acceleration à la Fermi: highly conducting plasma...

→ **large scale physics** (\leftrightarrow very high energies?): corresponds to ideal Ohm's law $\mathbf{E} = -\mathbf{v}_E \times \mathbf{B} / c \dots$

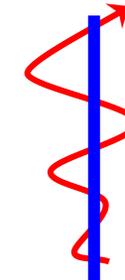
→ **Fermi-type scenarios: magnetized turbulence,**



shear flows,



shock waves

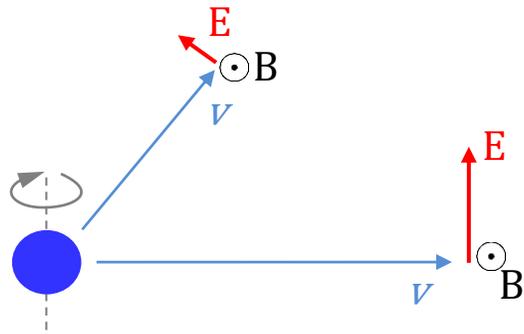


→ **two essential characteristics:**

1. E vanishes in local frame: **what truly matters is the spatial variation of the velocity field!**
 \Rightarrow classification of Fermi scenarios according to topology of velocity fields...
2. scattering is essential to explore E fields through cross- B transport: **need turbulence!**

Cross-B transport: magnetized rotators as extreme accelerators?

→ **magnetized rotator / unipolar inductor**: magnetized, highly conducting, rotating plasma, leading to a potential drop between the poles and the equator, due to the motional electric field $\mathbf{E} = -\mathbf{v} \times \mathbf{B} / c$ (← Fermi type acceleration)



at large distances: \sim radial wind + \sim azimuthal \mathbf{B}

e.g. in a fast rotating magnetar wind, voltage drop allows for¹

$$E_{\max} \sim 0.6 \times 10^{22} Z \left(\frac{B}{10^{15} \text{ G}} \right) \left(\frac{R}{10 \text{ km}} \right)^3 \left(\frac{P}{1 \text{ ms}} \right)^{-2} \text{ eV}$$

... key question: how to experience the voltage drop?
... incorporate turbulence in fast rotators?²

... transport across the magnetic field lines is the key limitation of Fermi acceleration processes!

... in most Fermi scenarios: $t_{\text{acc}} \propto t_{\text{scatt}}$

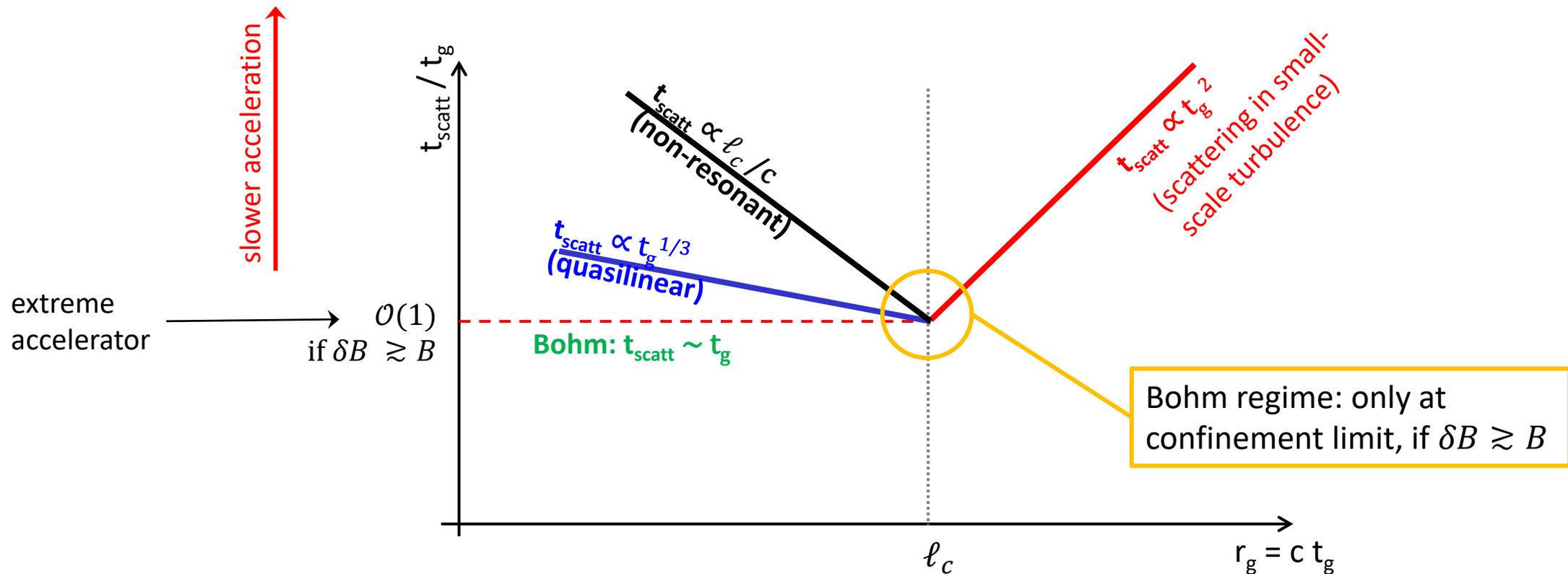
Fermi acceleration: the issue of scattering

→ generic scaling: $t_{\text{acc}} \simeq \frac{t_{\text{scatt}}}{\beta_E^2}$ (applies to original Fermi, shock, turbulence... here $\beta_E \lesssim 1$)

→ scattering timescale t_{scatt} : time it takes to deflect the particle by an angle of the order of unity,

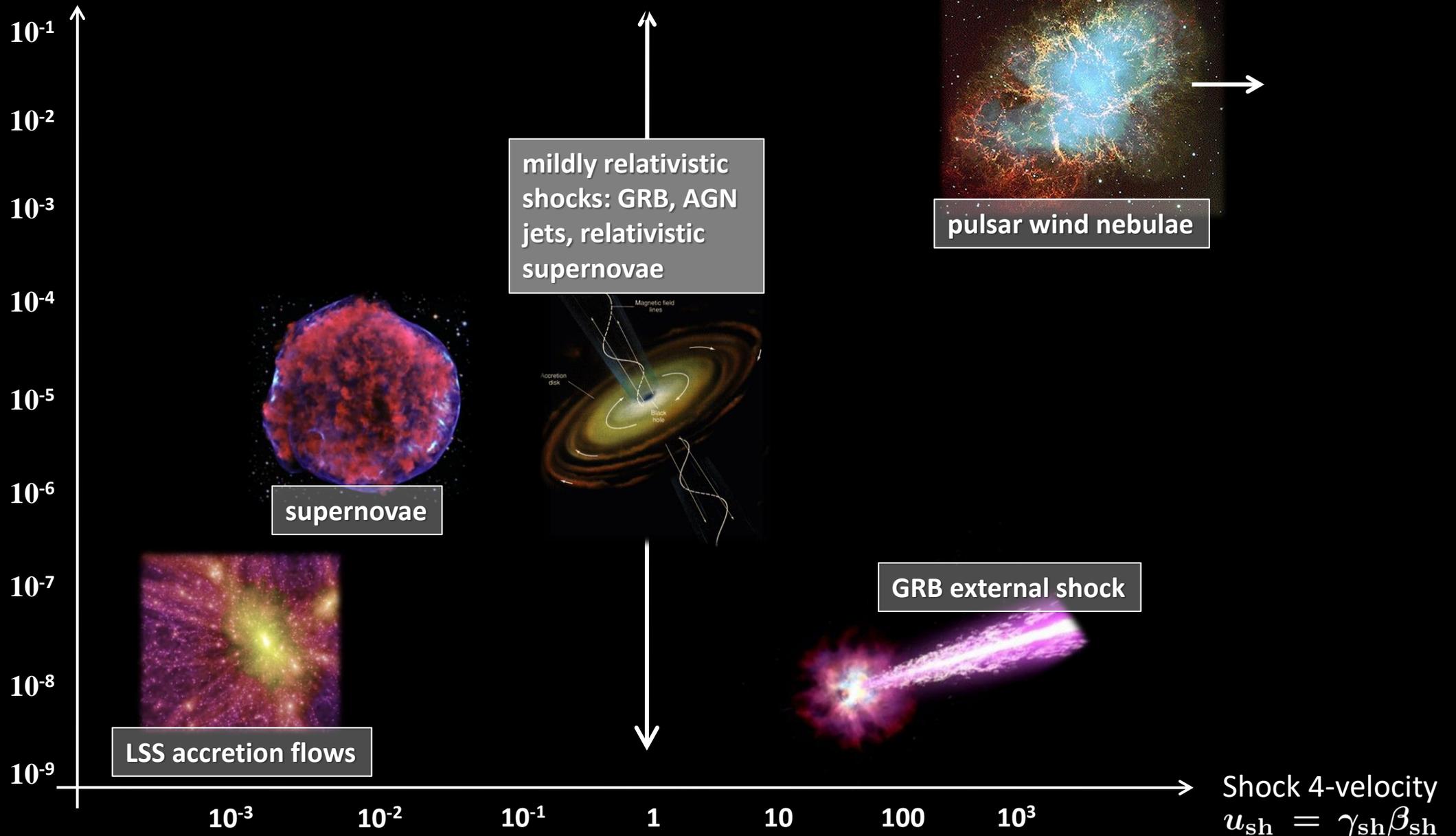
$$t_{\text{scatt}} \sim t_g^\alpha (\ell_c/c)^{1-\alpha} \quad (\ell_c \text{ coherence length scale of turbulence})$$

... in absence of specific information, **assume (too often!): $\alpha = 1$ Bohm regime**



The (HE) astrophysical shock landscape

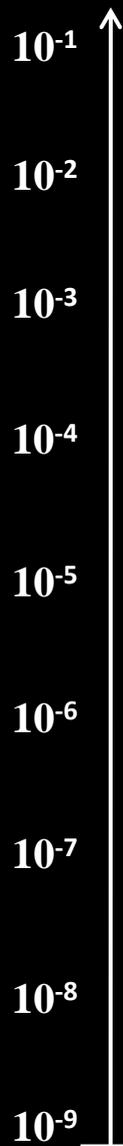
Shock magnetization $\sigma = u_A^2 / v_{sh}^2$



The (HE) astrophysical shock landscape

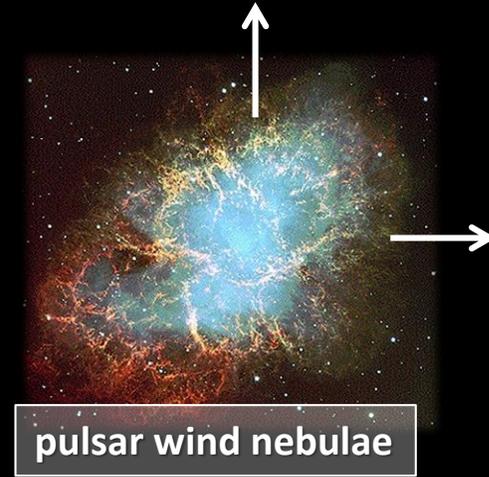
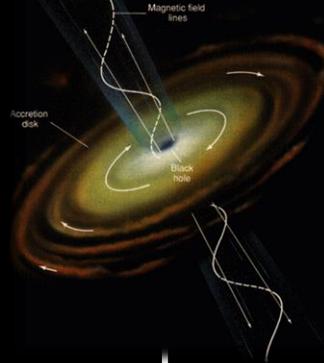
Shock magnetization

$$\sigma = u_A^2 / v_{sh}^2$$



sub-relativistic regime¹:
 acceleration is slow
 because of low shock
 velocity... $t_{acc} \propto 1/v_{sh}^2$
 e.g. $E_{max} \sim \text{PeV}$ for SNe

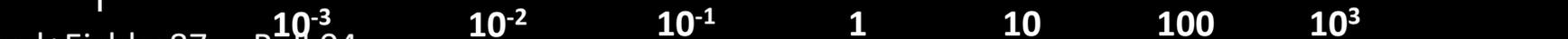
mildly relativistic
 shocks: GRB, AGN
 jets, relativistic
 supernovae



GRB external shock



Shock 4-velocity
 $u_{sh} = \gamma_{sh} \beta_{sh}$



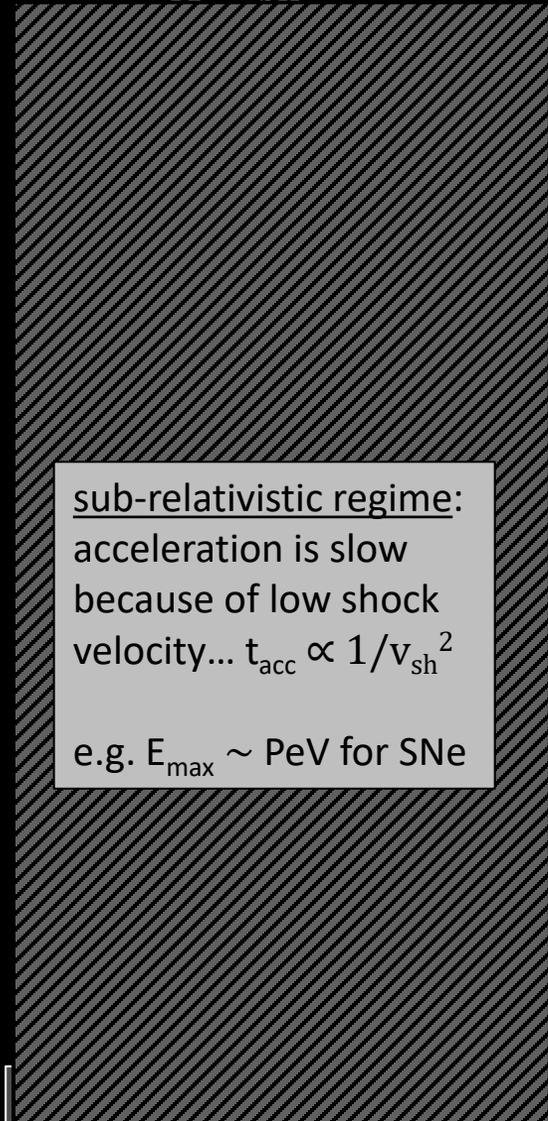
Refs.: 1. e.g. Blandford+Eichler87,... Bell 04, ...

The (HE) astrophysical shock landscape

Shock magnetization

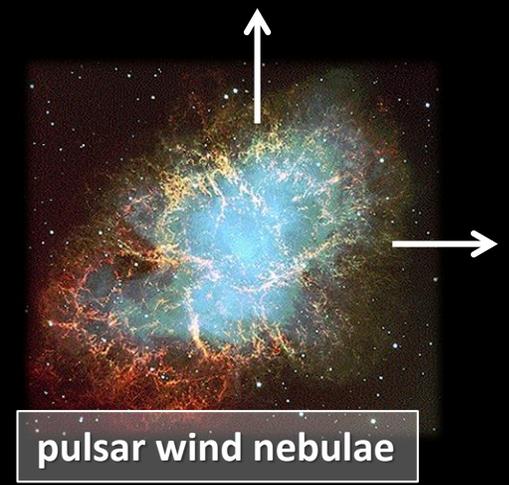
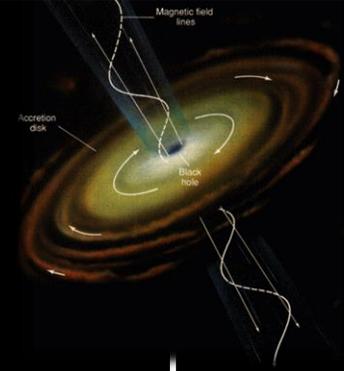
$$\sigma = u_A^2 / v_{sh}^2$$

10⁻¹
10⁻²
10⁻³
10⁻⁴
10⁻⁵
10⁻⁶
10⁻⁷
10⁻⁸
10⁻⁹

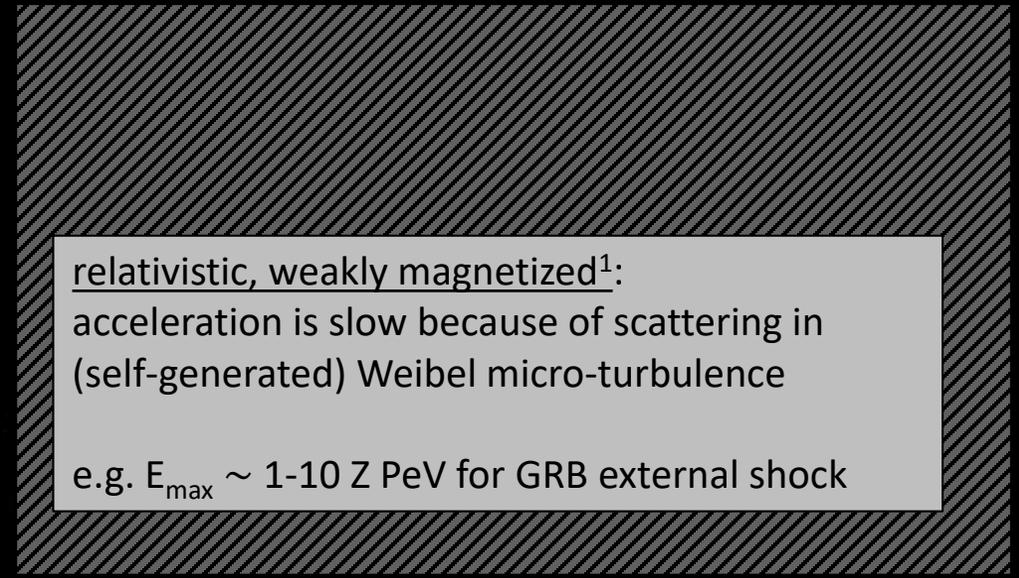


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e.g. $E_{max} \sim \text{PeV}$ for SNe

mildly relativistic
shocks: GRB, AGN
jets, relativistic
supernovae



pulsar wind nebulae



relativistic, weakly magnetized¹:
acceleration is slow because of scattering in
(self-generated) Weibel micro-turbulence
e.g. $E_{max} \sim 1-10 Z \text{ PeV}$ for GRB external shock

Shock 4-velocity $u_{sh} = \gamma_{sh} \beta_{sh}$

10⁻³ 10⁻² 10⁻¹ 1 10 100 10³

Refs.: 1. e.g. ML+06, Niemiec+06, Spitkovsky08, Sironi+Spitkovsky 09, ML+Pelletier 10, Eichler+Pohl11, Plotnikov+13, Sironi+13,...

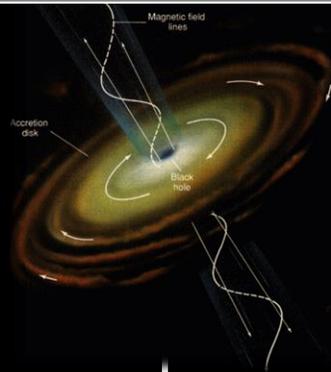
The (HE) astrophysical shock landscape

Shock magnetization $\sigma = u_A^2 / v_{sh}^2$

10⁻¹
10⁻²
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sub-relativistic regime:
acceleration is slow
because of low shock
velocity... $t_{acc} \propto 1/v_{sh}^2$
e.g. $E_{max} \sim$ PeV for SNe

mildly relativistic
shocks: GRB, AGN
jets, relativistic
supernovae



relativistic, magnetized¹:
acceleration is inhibited by external magnetic
field (superluminal shocks!)

caveat! Physics of PWNe²?
→ extreme accelerators with $t_{acc} \sim t_g$

relativistic, weakly magnetized:
acceleration is slow because of scattering in
(self-generated) Weibel micro-turbulence
e.g. $E_{max} \sim 1-10 Z$ PeV for GRB external shock



Shock 4-velocity

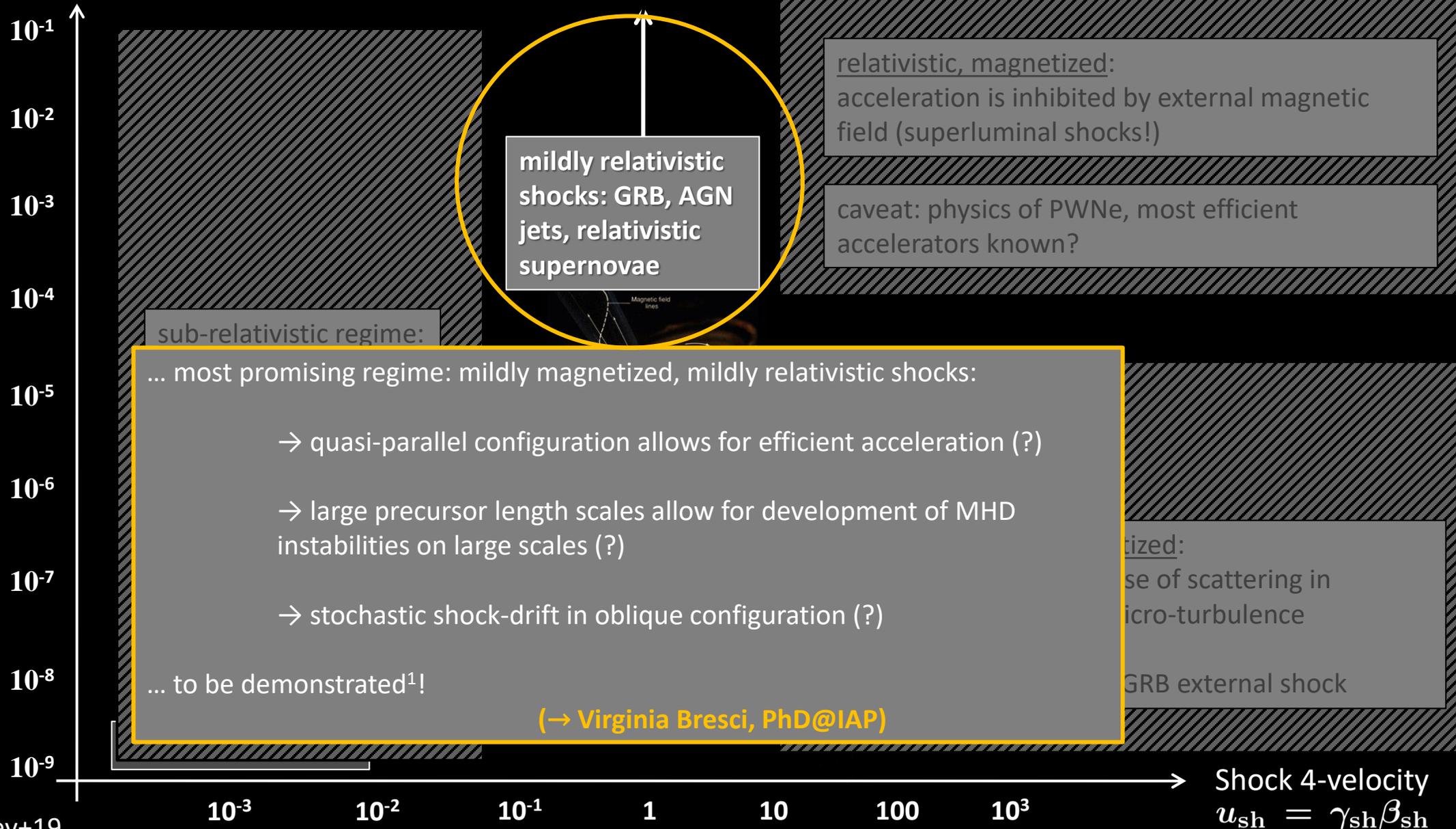
$u_{sh} = \gamma_{sh} \beta_{sh}$

Refs.: 1. e.g. ML+06, Niemiec+06, Sironi+Spitkovsky 09, ML+Pelletier 10, Sironi+11,13,...

2. e.g. Kirk+09, Amato15,...

The (HE) astrophysical shock landscape

Shock magnetization $\sigma = u_A^2 / v_{sh}^2$



Shear acceleration

→ Fermi shear acceleration: ... the electric field cannot be boosted away globally, particles gain energy by exploring the shear gradient...

... acceleration timescale:
(at $t_{\text{scatt}} \ll \Delta r$)

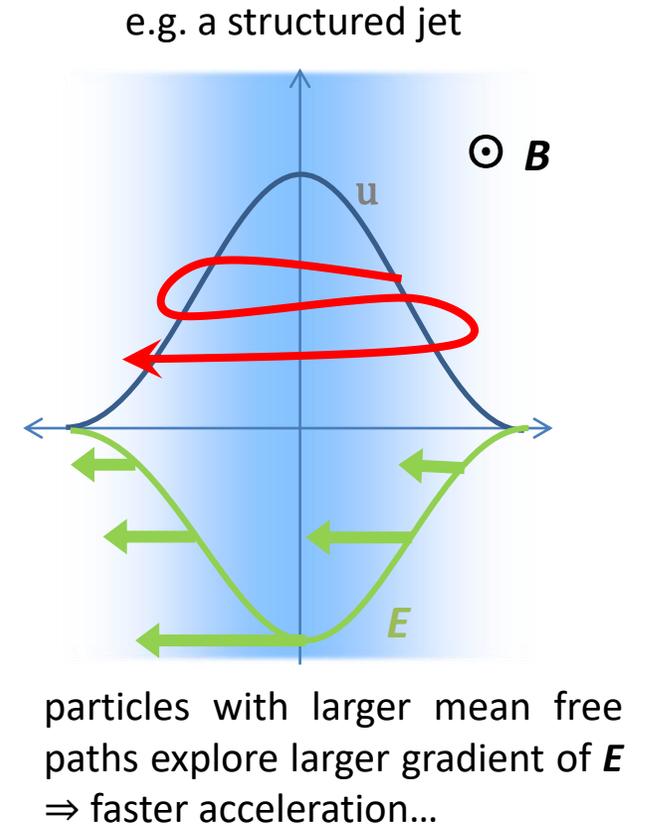
$$t_{\text{acc}} \sim \frac{\Delta r^2}{t_{\text{scatt}}} \frac{1}{\Delta u^2 / \gamma_u^2}$$

⇒ inefficient at low energies, since $t_{\text{scatt}} \uparrow p$,
requires a seed population of particles

... if $\ell_c \sim \Delta r$, at confinement energy $r_g \sim \Delta r$,
⇒ $t_{\text{scatt}} \sim r_g \sim \Delta r \Rightarrow t_{\text{acc}} \sim r_g$ for $\Delta u \sim u \sim 1$
⇒ optimal for (mildly?) relativistic shear!

⇒ reacceleration of a population of energetic CRs in mildly relativistic shear may reach confinement energy...

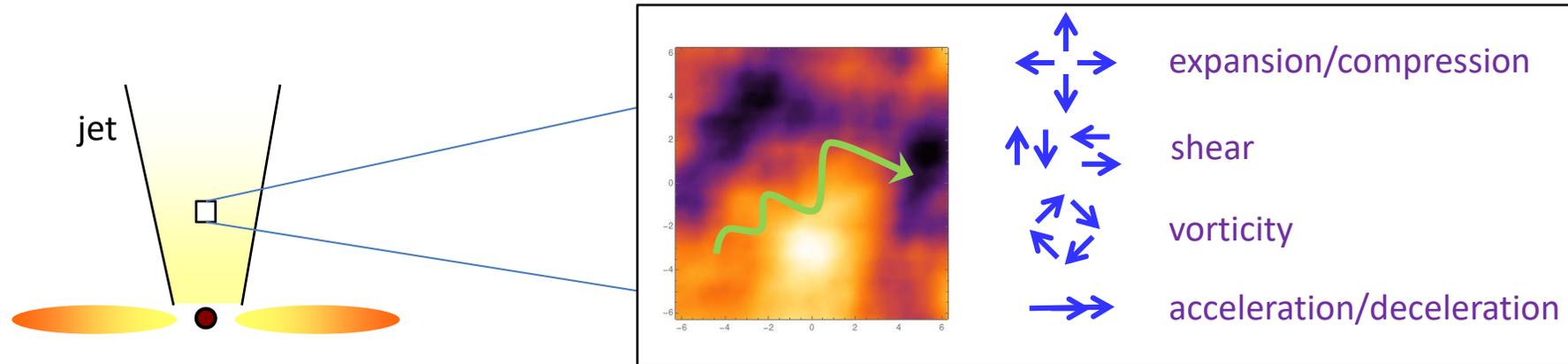
(note: efficient scattering needs $\delta B/B \sim 1$: how does turbulence impact shear acceleration?)



Generalized Fermi acceleration in a large-scale, turbulent flow

... particle random walks in structured (or random) MHD flow of (large) scale ℓ_c ...

... what truly controls acceleration is the velocity variation: \supset shear, compression etc.



\rightarrow **expect¹** $t_{\text{acc}} \sim \dots \frac{\ell_c}{\langle \delta u^2 \rangle}$ (note: δu is a 4-velocity! Fast in relativistic regime)

... slow at low energies ($t_{\text{acc}} \gg t_g$) ... but fast at high energies (where $c t_g \sim \ell_c$)

$\Rightarrow t_{\text{acc}} \sim t_g$ **appears possible at confinement energy**

Particle acceleration in magnetized turbulence

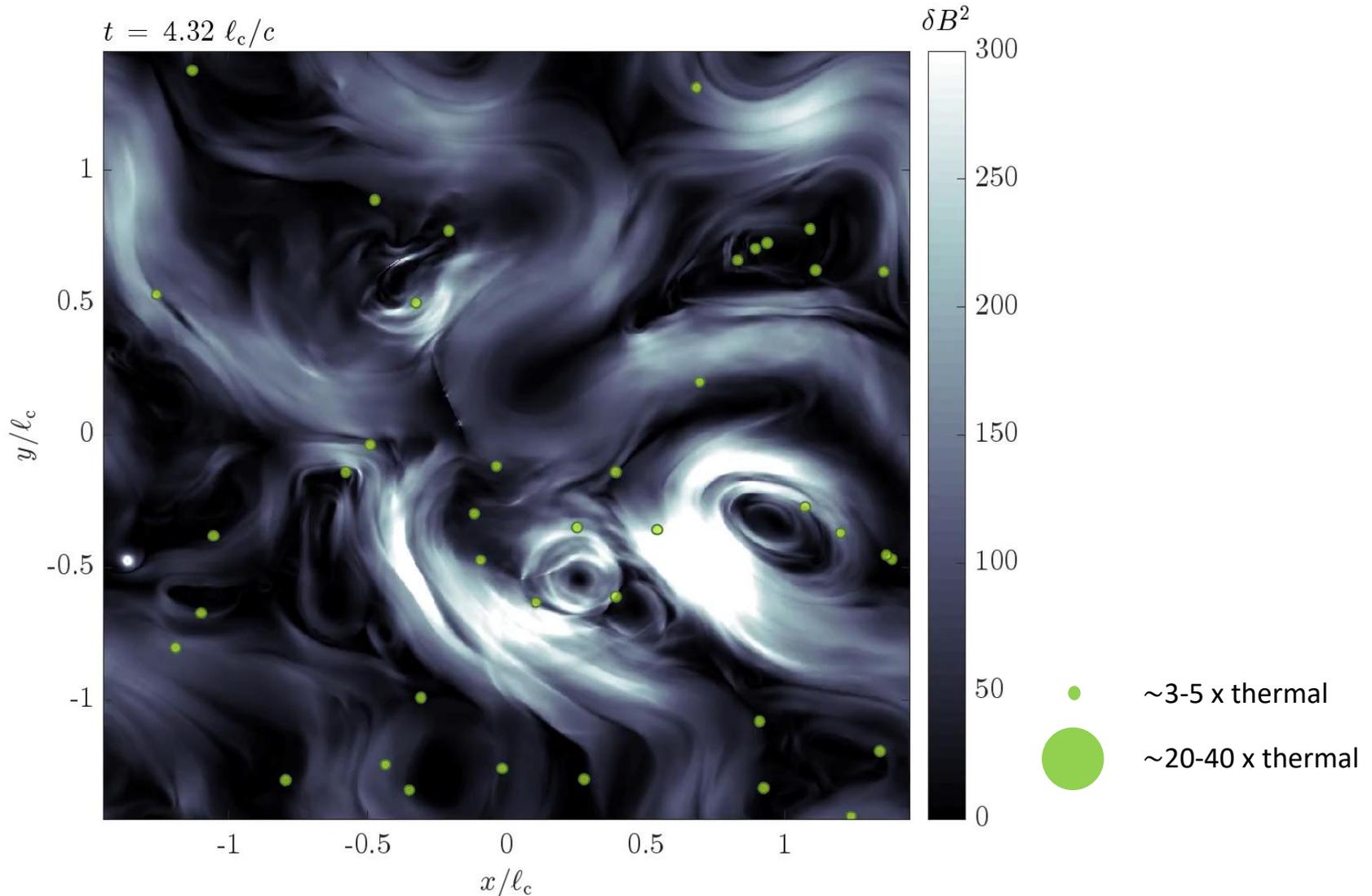
→ HPC kinetic simulations have started to probe particle acceleration in large-scale turbulence¹...

⇒ particle acceleration fast in relativistic regime $\sigma \gtrsim 1$ ($v_A \sim c$)

... acceleration timescale:

$$t_{\text{acc}} \sim \frac{c \ell_c}{\langle \delta u^2 \rangle} \sim \frac{\ell_c}{\sigma c}$$

ℓ_c : coherence scale,
 $\langle \delta u^2 \rangle \sim u_A^2 = \sigma$



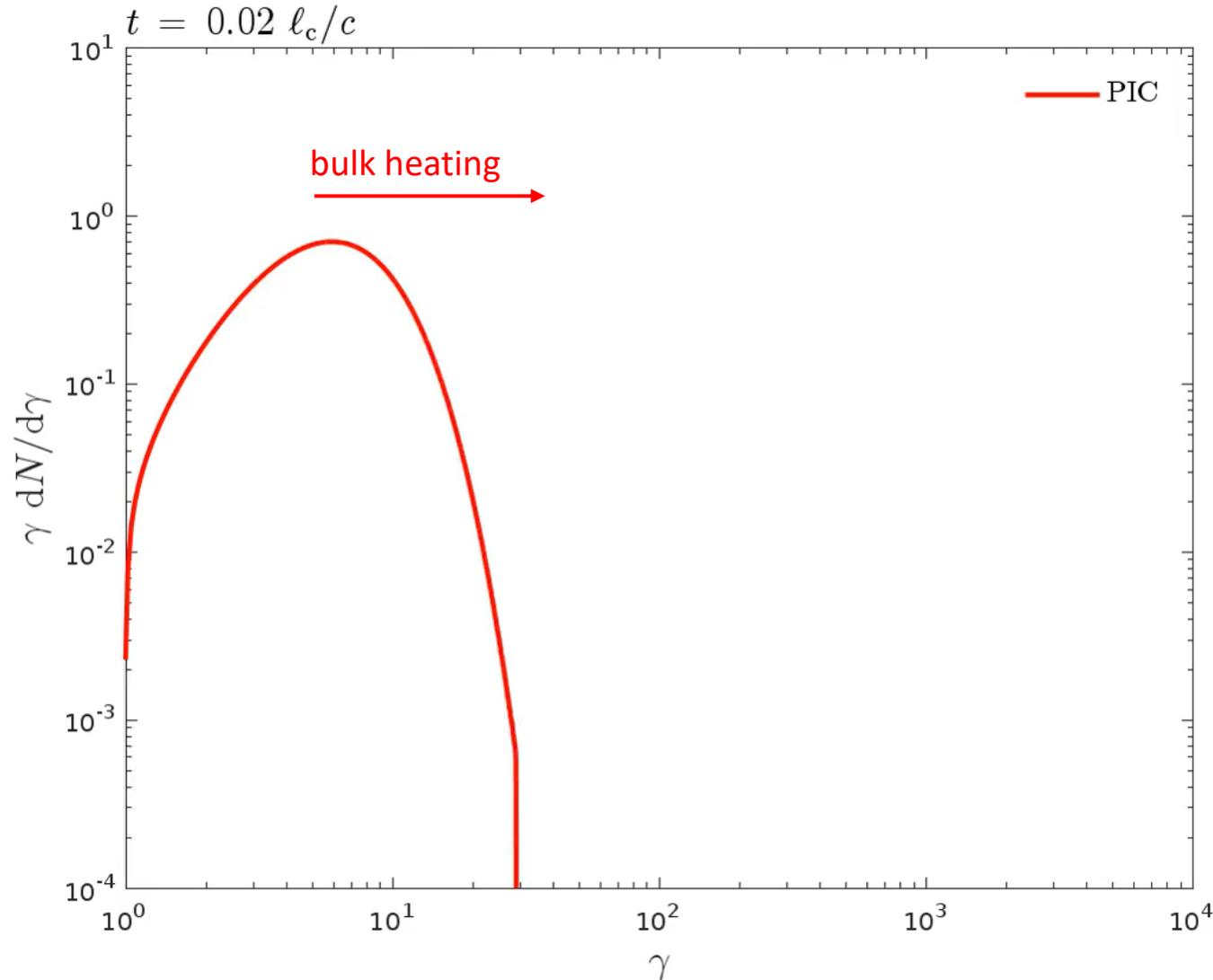
© V. Bresci, L. Gremillet, M. L.: 2D PIC, driven turb., e^+e^- , $10\,000^2$, $\delta B/B \sim 3$, $\sigma \sim 1$

Refs.: e.g. Zhdankin+17,18,19, Comisso+Sironi19,20, Wong+19,...

Spectra from stochastic acceleration

→ a surprise: turbulence produces powerlaw spectra (even in closed box!)

not the Maxwellian type distribution as expected from phenomenology!



Note: Fokker-Planck solution assumes infinite reservoir of energy!

In reality: turbulent/magnetic energy reservoir mostly converted to bulk heating... and into particle acceleration as a soft powerlaw...

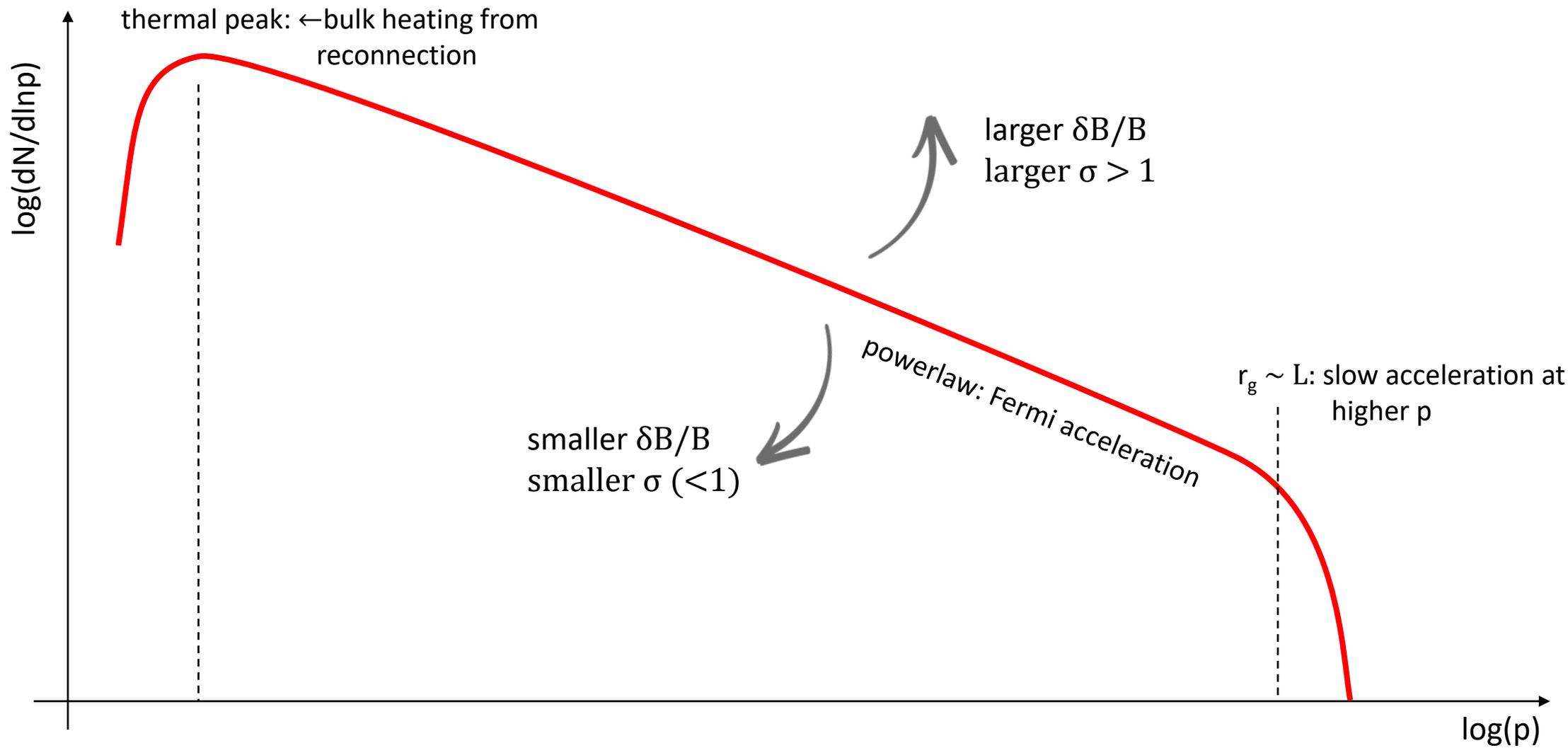
@ $\sigma \sim 1, \delta B/B \sim 1$:

$$\frac{dN}{dp} \propto p^{-s} \quad \text{and} \quad s \sim 3$$

Spectra from stochastic acceleration

→ a surprise: turbulence produces powerlaw spectra (even in closed box!)

not the Maxwellian type distribution as expected from phenomenology! (see ¹ for interpretation)



Refs.: 1. ML+Malkov 20, ML21

Particle acceleration to extreme energies

Summary:

1. The view from phenomenology: top-down, from large to small scales

- constraints from L_{tot} , n_{UHECR} , \dot{e}_{UHECR}
- for minimal constraints, search for: $t_{\text{acc}} \sim t_g$ at UHE

2. The view from microphysics: bottom-up, from first principles

- improved knowledge from kinetic numerical simulations (on small scales!)
- mildly relativistic shocks or shear, ($\sigma > 1$) turbulence equally interesting for UHE
- in mildly relativistic regime, a common trait: $t_{\text{acc}} \sim t_g$ at $r_g \sim \ell_c$

3. Discussion: clues and issues

Clues and issues: signatures from extreme Fermi accelerators

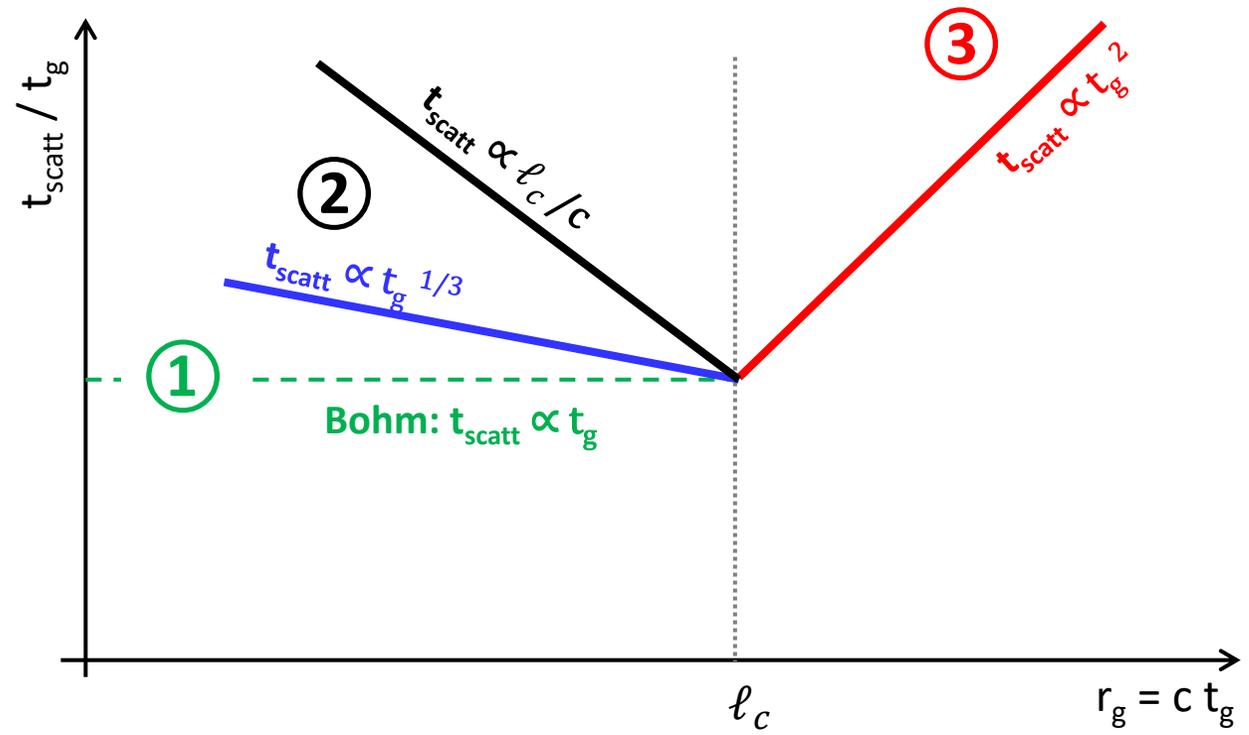
→ recall, no direct counterpart for transient sources ($\Delta t \gtrsim 10^5$ yr due to scattering in B fields)...
 ⇒ learn from modelling of astrophysical sources!

① : extreme accelerator if $\beta_E \sim 1$, synchrotron from e at radiation reaction limit:
 $t_{\text{acc}} \simeq \mathcal{A} t_L \Rightarrow \epsilon_{\text{syn,max}} \sim 100 \mathcal{A}^{-1} \text{ MeV}$
 (up to Lorentz boost)

② : non-extreme for e, but can reach confinement (Hillas) limit for ions if:

③ $\beta_E \sim 1, \ell_c \sim \text{source size}, \delta B \gtrsim B,$
 in absence of energy losses...

⇒ for e, signatures below gamma-domain, X-ray and below?



→ an accelerator that does not look extremal for leptons... may be extremal for ions if

$\beta_E \sim 1, \ell_c \sim \text{source size}, \delta B \gtrsim B$ (+ t_{acc} does not decrease with energy)

Clues and issues: signatures from extreme Fermi accelerators

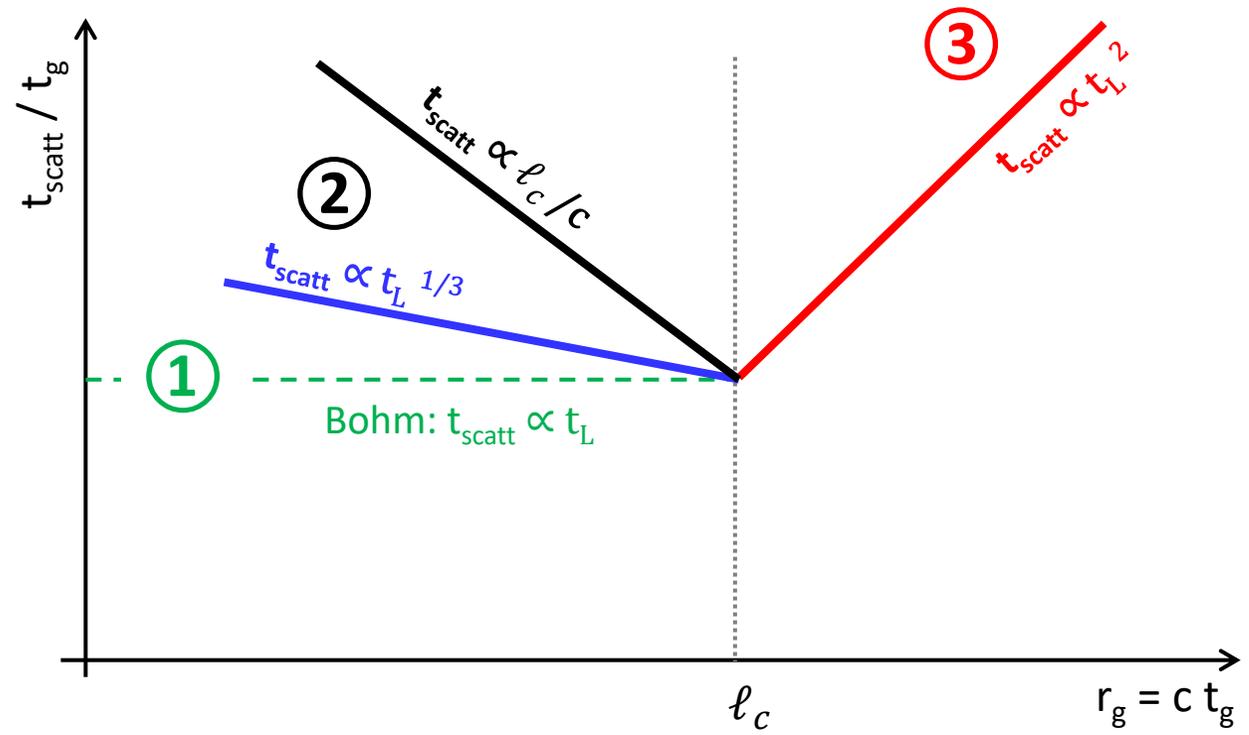
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③ 1, $\ell_c \sim$ source size, $\delta B \gtrsim B$, in absence of energy losses...

⇒ for e, signatures below gamma-domain, X-ray and below?



→ however, an extreme case: acceleration of fossil HE CR population in some large-scale flow
 ⇒ weak or no radiative signatures !?
 ⇒ search strategy: direct identification from arrival directions?

Clues and issues: the spectral slope $s \dots dN/dp \propto p^{-s}$

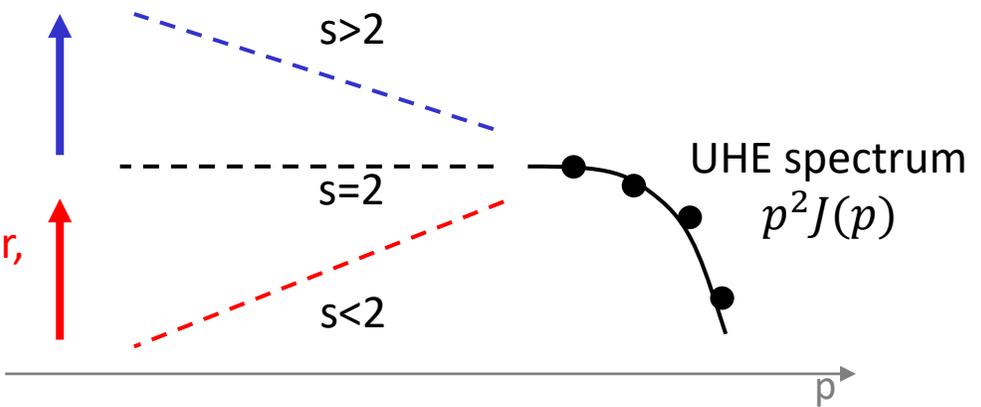
→ in acceleration scenarios, shock acceleration generically predicts $s \sim 2$...
 ... harder or softer indices are possible for other schemes (reconnection,... turbulence)

generic behavior: {
 high magnetization $\sigma > 1 \Rightarrow$ hard spectra
 low magnetization $\sigma < 1 \Rightarrow$ soft spectra

→ issue of energy conservation (!):

soft s requires more input / source,
 $L_{\text{UHECR}} \propto (E_{\text{UHE}}/E_{\text{min}})^{s-2}$

hard s requires a large initial energy reservoir,
 e.g. $\sigma \sim (E_{\text{UHE}}/E_{\text{min}})^{2-s}$



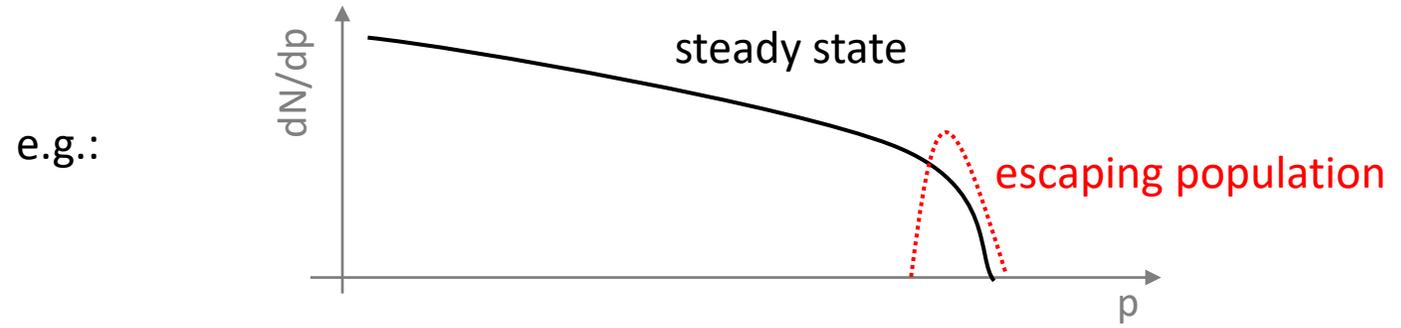
⇒ most conservative choice: $s \sim 2$ inside source (?)

Clues and issues: the spectral slope $s \dots dN/dp \propto p^{-s}$

→ in acceleration scenarios, shock acceleration generically predicts $s \sim 2 \dots$
 ... harder or softer indices are possible for other schemes (reconnection, ... turbulence)

generic behavior: $\left\{ \begin{array}{l} \text{high magnetization } \sigma > 1 \Rightarrow \text{hard spectra} \\ \text{low magnetization } \sigma < 1 \Rightarrow \text{soft spectra} \end{array} \right.$

→ however, recall that escape can remodel the spectrum¹: $\frac{dN_{\text{esc}}}{dt dp} = \frac{1}{t_{\text{esc}}(p)} \frac{dN}{dp}$ ($t_{\text{esc}} \sim L^2/t_{\text{scatt}}$)
 (+other effects: source population², interactions³...)
 ⇒ low E cut, or hard slope?



Refs.: 1. e.g. Ohira+10, ... 2. e.g. Kachelriess+Semikoz06 3. e.g. Globus+15, Unger+15, ...

Clues and issues: the chemical composition

→ chemical composition, or rigidity $E/(eZ)$ at a given energy, controls the phenomenology at ultra-high energies:

(1) sources of 10^{20}V are much more extreme than sources of 10^{18}V particles:

... e.g., a few candidate sources for 10^{20}eV protons vs *dozens* of candidate sources of 10^{20}eV iron...

(2) light particles leave stronger signatures of their sources:

... e.g., anisotropies at ultra-high energies with deflections of a few deg, vs large deflections for iron-like primaries

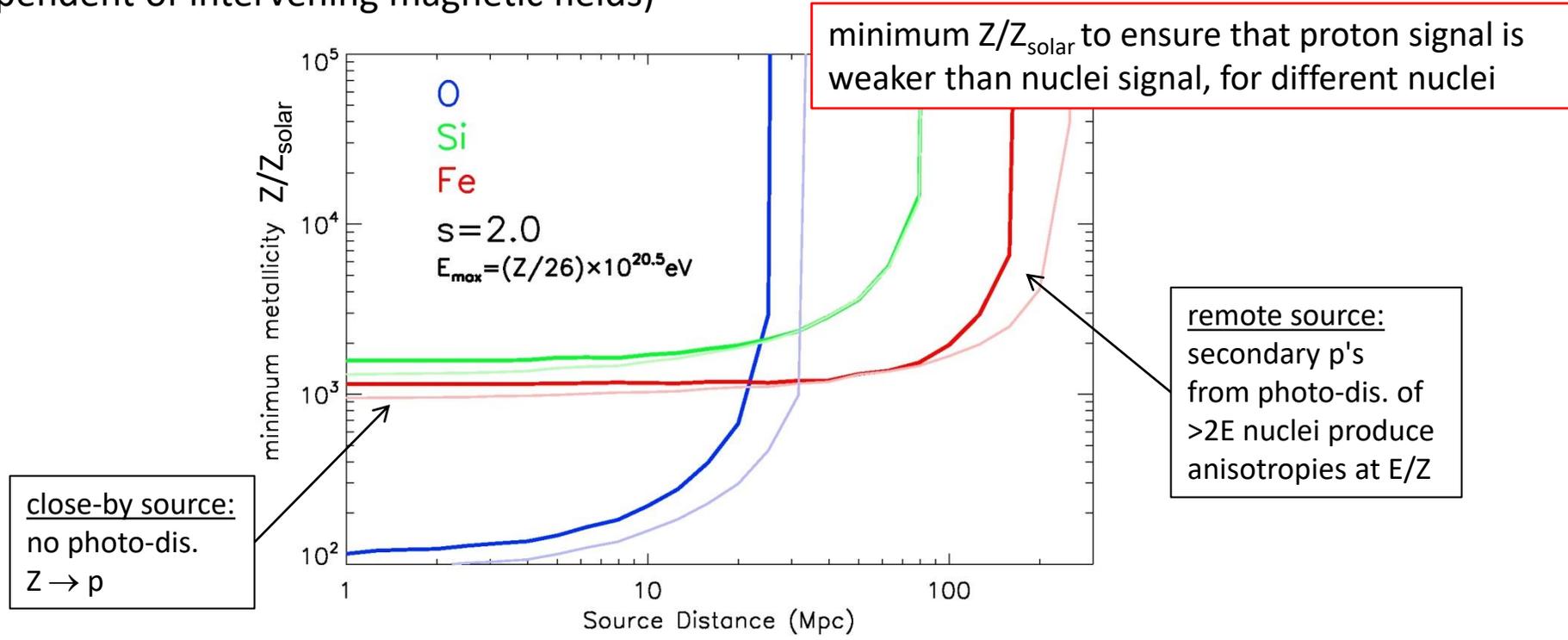
... e.g., secondary photons and neutrino signals

⇒ if light nuclei exist at GZK: search for extreme sources of *ultra-high rigidity* particles!

→ related issue: how to better constrain the composition: direct measurements, diffuse backgrounds?

Clues and issues: (small-scale) anisotropies at GZK

→ if anisotropic signal $>E$ is due to heavy nuclei, then one should detect a stronger anisotropy signal associated with protons of same magnetic rigidity at $>E/Z$ eV... **where are the accompanying protons?**¹
 (argument independent of intervening magnetic fields)



→ to assume that the anisotropies are produced by heavy nuclei thus requires a source metallicity:

if Fe at UHE: $Z > 1000 Z_{\text{solar}}$... if Si at UHE: $Z > 1600 Z_{\text{solar}}$... if O at UHE: $Z > 100 Z_{\text{solar}}$

... a clue on the source: ambient material from stellar collapse? or a fraction of protons at UHE?

Refs.: 1. ML + Waxman 09, Auger 11, Liu+13

Clues and issues: from microphysics to macrophysics

→ Numerical PIC simulations are ideal tools to reproduce ab initio the acceleration of particles in astrophysical sources...
however: they need to resolve the smallest length scale...

$$c/\omega_c \equiv \frac{m_e c^2}{eB} \sim 10^6 \text{ cm } B_{\text{mG}}^{-1}$$

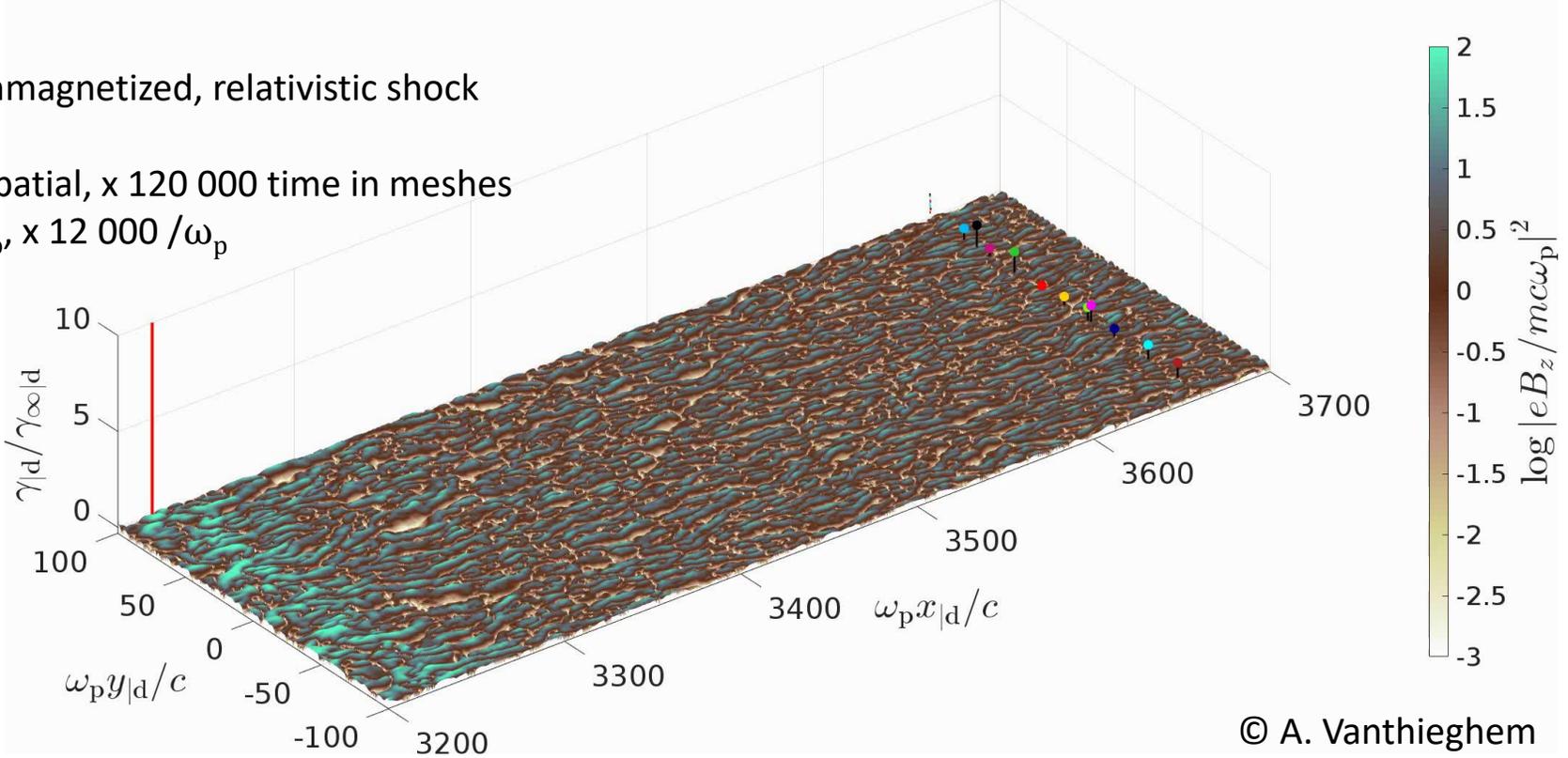
$$c/\omega_{pe} \equiv \left(\frac{m_e c^2}{4\pi n e^2} \right)^{1/2} \sim 10^6 \text{ cm } n_{1 \text{ cm}^{-3}}^{-1/2}$$

PIC simulation of an unmagnetized, relativistic shock

size: 120 000 x 2 000 spatial, x 120 000 time in meshes

12 000 x 200 c/ω_p , x 12 000 $/\omega_p$

cost: ~1 M CPUhr



→ strategy to bridge the gap between microscopic and macroscopic scales ?

Topics for discussion?

→ One accelerator, from injection at low E to UHE...

... or a sequence of accelerators, working in different energy ranges?

→ Consequences for radiative signatures? Search strategy?

→ Are there protons at UHE? ⇒ Search strategy/constraints for extreme accelerators?

→ Spectral slope: a clue on acceleration, escape or transport?

→ Theory side: making progress toward bridging the gap in scales: micro → macro?

→ ??