

# Muon $g - 2$ theory: beyond the SM

Dominik Stöckinger, TU Dresden

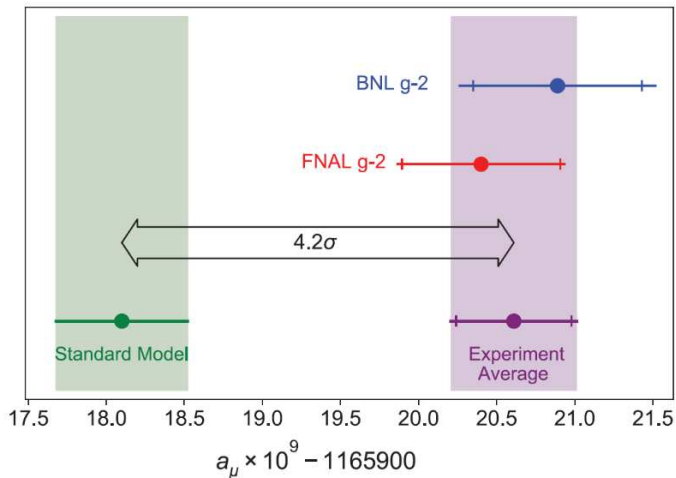
Paris GDR/IJCLab Virtual  $g-2$  breakfast, 19th May 2021

$(g_\mu - 2)/2 = a_\mu$  is among the most precise observables  
sensitive to all known (and unknown?) interactions

# Outline

- 1 Overview and SM theory
- 2  $g = 2$  and BSM — important general remarks
- 3 Examples of concrete models and constraints
- 4 General lessons and conclusions

# Finally: Fermilab Run 1 versus Theory Initiative SM value



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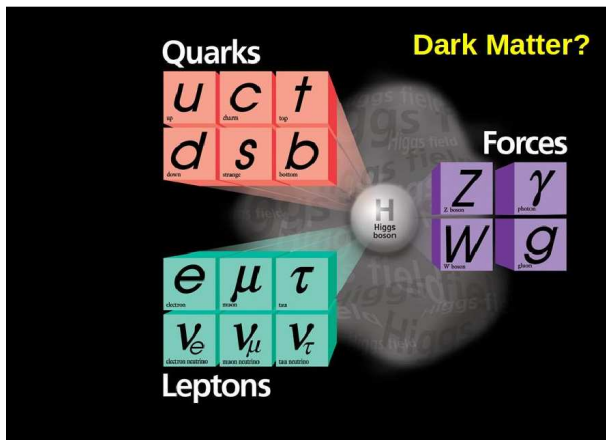
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- 1 Overview and SM theory
- 2  $g = 2$  and BSM — important general remarks
  - Simple, distinctive properties
  - Overview of contributions
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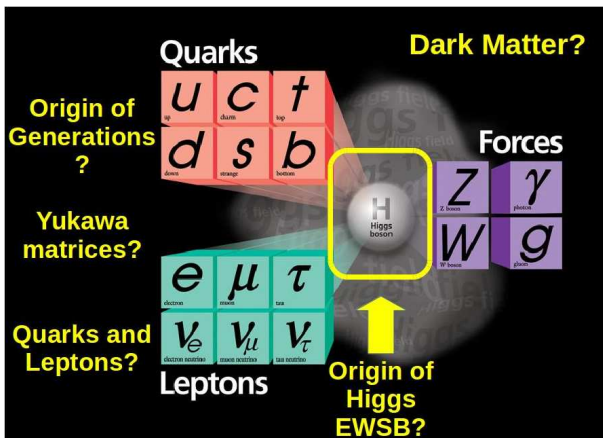
# Open questions require Beyond the Standard Model (BSM) physics



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- experimental clues needed!  $\rightsquigarrow g - 2!$   
not easy to explain!
- relevant and deep questions may be related to  $g - 2$

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# Discrepancy

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**Questions: Which models can(not) explain it?**

**Why is a single number so interesting?**

**“Why are you happy about a discrepancy?”**

- Very active area ( $> 70$  papers)
- Here: general remarks and examples from survey [2104.03691](#)

[Peter Athron, Csaba Balasz, Douglas Jacob, Wojciech Kotlarski, DS, Hyejung Stöckinger-Kim]

## Two important general points

discrepancy  $\approx 2 \times a_\mu^{\text{SM,weak}}$

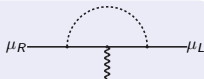
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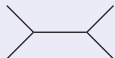
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loop-induced, CP- and Flavor-conserving, chirality-flipping



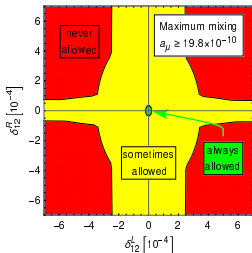
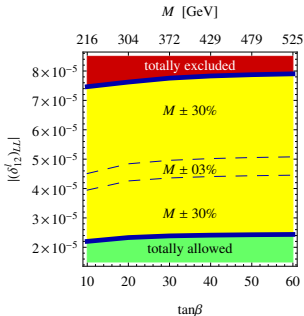
compare:



$b \rightarrow s\gamma$   
EDMs,  $B \rightarrow \tau\nu$   
 $\mu \rightarrow e\gamma$

EWPO

# Connection to CP and flavor (example)



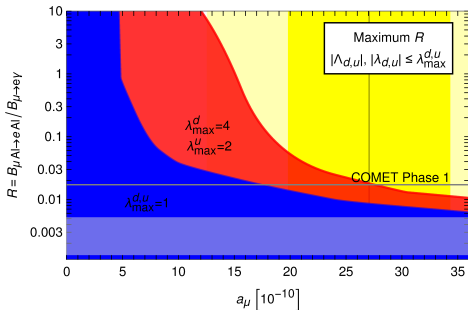
- given  $g - 2$ , derive upper limits on LFV parameters from  $\mu \rightarrow e\gamma$

MSSM:

[Kersten, Park, DS, Velasco-Sevilla '14]

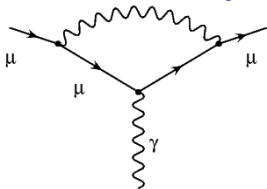
MRSSM:

[Kotlarski, DS, Stöckinger-Kim '19]



- MRSSM: large  $g - 2$  enforces special parameter space with restricted  $\mu \rightarrow e / \mu \rightarrow e\gamma$

# Connection to chirality flip, and structure of BSM



$$\mathcal{L}_{\text{eff}} = -\frac{Qe}{4m_\mu} a_\mu \times \bar{\psi}_L \sigma_{\mu\nu} \psi_R F^{\mu\nu}$$

But:

EW gauge invariant  $a_\mu$ -operator:

$$\bar{L} \sigma_{\mu\nu} \mu_R F^{\mu\nu} \langle H \rangle$$

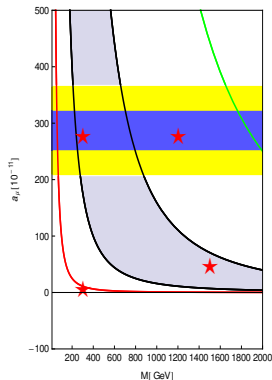
$$a_\mu \sim m_\mu \times \underbrace{(\text{some VEV}) \times (\mu_{L \leftrightarrow R}\text{-flipping param.})}_{\text{related to muon mass generation, potential enhancement!}} \times \frac{(\text{other couplings})}{M_{\text{typical}}^2}$$

$$m_\mu(\text{SM}) \sim (\text{SM Higgs-VEV}) \times (\text{muon Yukawa coupling})$$

Typical behaviour:  $\sim$  chirality flip ( $\rightsquigarrow$  Higgs!) and masses

$$a_\mu \sim \frac{m_\mu \times (\text{some VEV}) \times (\mu_{L \leftrightarrow R}\text{-flipping parameter})}{M_{\text{typical}}^2} \left[ \lesssim \frac{m_\mu^2}{M_{\text{typical}}^2} \text{ (no finetuning)} \right]$$

$$\Delta m_\mu \sim (\text{some VEV}) \times (\mu_{L \leftrightarrow R}\text{-flipping parameter})$$



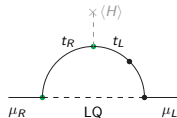
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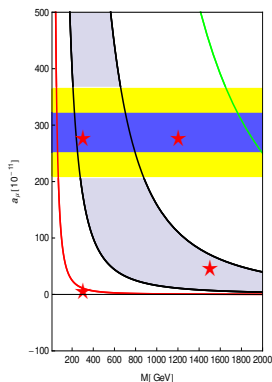
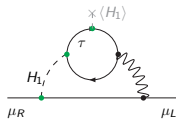
• EWSM:  $\alpha \frac{m_\mu^2}{M_W^2}$



• LQ:  $g_L g_R \frac{m_\mu m_t}{M_{LQ}^2}$



• 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$





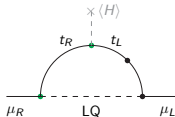
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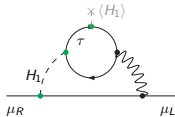
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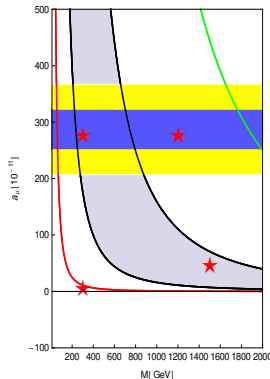
Can also involve Higgs couplings to  $b$ ,  $c$  or new particles.

Beware:  $\Delta m_\mu / m_\mu \sim g_L g_R m_t / m_\mu$  restricts couplings

- 2HDM:  $\alpha^2 \tan^2 \beta \frac{m_\mu^2}{M_H^2}$



Well motivated; many variants; many constraints



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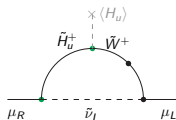
- EWSM:

$$\propto \frac{m_\mu^2}{M_W^2}$$



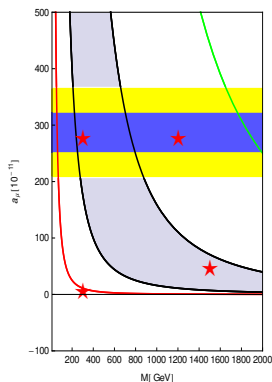
- SUSY:

$$\propto \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2} \frac{\mu}{M_{\text{SUSY}}}$$



- rad.  $m_\mu$

$$\sim \frac{m_\mu^2}{M_{\text{NP}}^2}$$



# Typical behaviour: $\sim$ chirality flip ( $\rightsquigarrow$ Higgs!) and masses

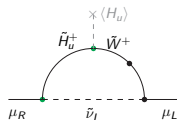
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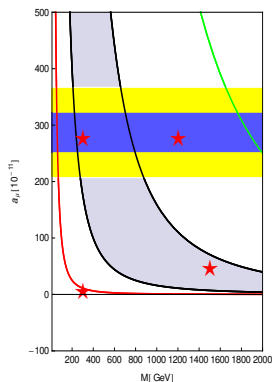
- SUSY:  $\propto \frac{m_\mu^2 \tan \beta}{M_{\text{SUSY}}^2} \frac{\mu}{M_{\text{SUSY}}}$

Well-motivated theory. Many other advantages



- rad.  $m_\mu \sim \frac{m_\mu^2}{M_{\text{NP}}^2}$

E.g. MSSM for  $\tan \beta \rightarrow \infty$  [Bach,Park,DS,Stöckinger-Kim'15]



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# There are many more examples. . .

## SUSY: **MSSM**, **MRSSM**

- **MSugra**. . . many other generic scenarios
- **Bino-dark matter**+some coannihil.+mass splittings
- **Wino-LSP**+specific mass patterns

## Two-Higgs doublet model

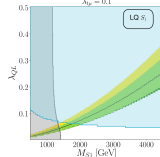
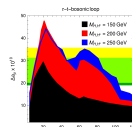
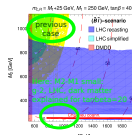
- **Type I, II, Y, Type X**(lepton-specific), flavour-aligned

## Lepto-quarks, vector-like leptons

- scenarios with muon-specific couplings to  $\mu_L$  and  $\mu_R$

## Simple models (one or two new fields)

- **Mostly excluded**
- light N.P. (**ALPs**, **Dark Photon**, **Light  $L_\mu - L_\tau$** )



Model	Mass	Spin	CP	Parity	Charge	Color	Notes
1	1.0	0	+	+	0	1	Standard Model
2	1.0	1	+	+	0	1	Standard Model
3	1.0	1	+	-	0	1	Standard Model
4	1.0	1	-	+	0	1	Standard Model
5	1.0	1	-	-	0	1	Standard Model
6	1.0	0	+	+	1	3	Standard Model
7	1.0	0	+	-	1	3	Standard Model
8	1.0	0	-	+	1	3	Standard Model
9	1.0	0	-	-	1	3	Standard Model
10	1.0	1	+	+	1	3	Standard Model
11	1.0	1	+	-	1	3	Standard Model
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26	1.0	1	+	+	3	3	Standard Model
27	1.0	1	+	-	3	3	Standard Model
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30	1.0	0	+	+	0	1	Standard Model
31	1.0	0	+	-	0	1	Standard Model
32	1.0	0	-	+	0	1	Standard Model
33	1.0	0	-	-	0	1	Standard Model
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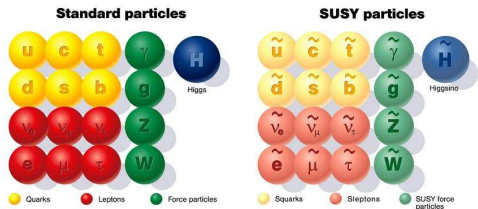
[Athron,Balazs,Jacob,Kotlarski,DS,Stöckinger-Kim, 2104.03691]

# Example BSM idea

- fundamental new QFT symmetry
- predicts Higgs potential/mass
- dark matter candidate
- **chirality flip enhancement**  $\rightsquigarrow g - 2$
- **viable (LHC)?**

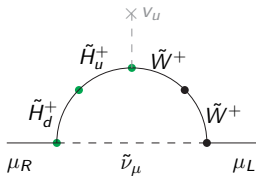
# Example BSM idea Minimal SUSY Standard Model

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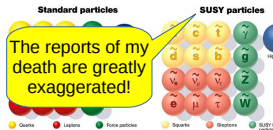
Superpartners and SUSY Higgs sector  $\rightsquigarrow \tan \beta = \frac{v_\mu}{v_d}$ , Higgsino mass  $\mu$

# MSSM can explain $g - 2$ and dark matter

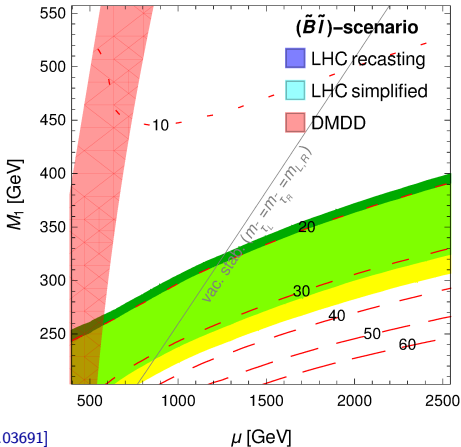


$$a_{\mu}^{\text{SUSY}} \approx 25 \times 10^{-10} \frac{\tan \beta}{50} \frac{\mu}{M_{\text{SUSY}}} \left( \frac{500 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

- “Dark matter mass” versus  $\mu$
- explains  $g - 2$  in large region (expands for  $\tan \beta \neq 40$ )
- DM explained by stau/slepton-coannihilation
- this automatically evades (current) LHC limits



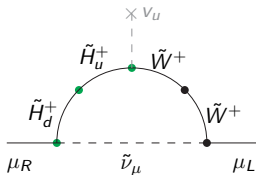
$m_{L,R} = M_1 + 50 \text{ GeV}, M_2 = 1200 \text{ GeV}, \tan \beta = 40$



[2104.03691]

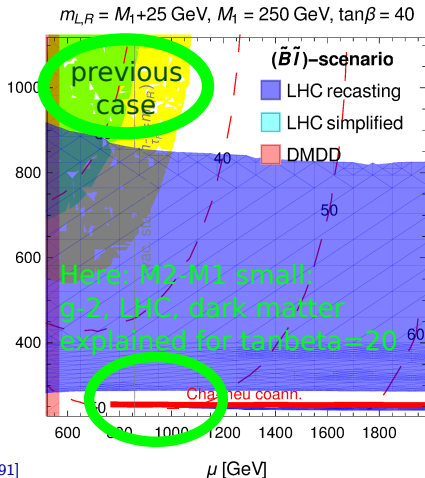
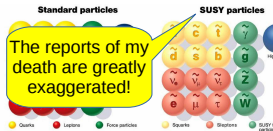


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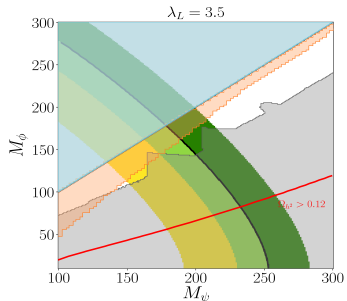
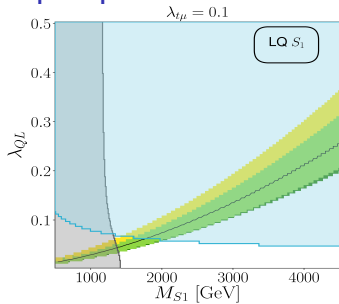
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- Strong LHC limits on  $M_2$
- DM also explained by Wino-coannihilation
- again evades (current) LHC limits



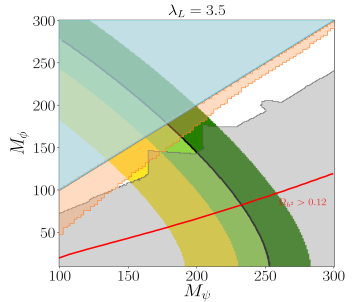
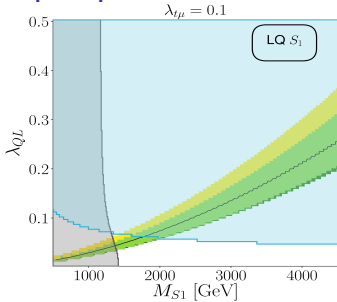
[2104.03691]

# Leptoquarks and Model L with 2 fields



[Athron,Balazs,Jacob,Kotlarski,DS,Stöckinger-Kim, 2104.03691 ]

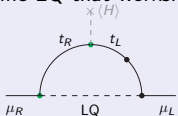
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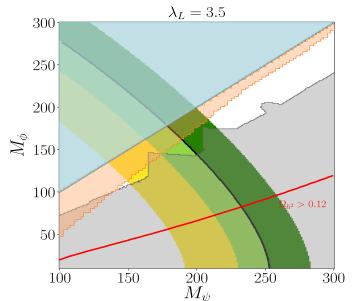
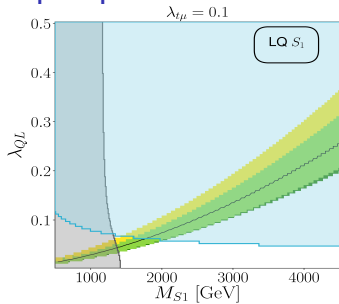
$$a_\mu \text{ from LQ (or VLL)} \quad \mathcal{L}_{S_1} = - (\lambda_{QL} Q_3 \cdot L_2 S_1 + \lambda_{t\mu} t_\mu S_1^*)$$

Specific LQ that works:



- Chiral enhancement  $\sim y_{\text{top}}, y_{\text{VLL}}$  versus  $y_\mu$
- LHC: lower mass limits
- Flavour constraints  $\rightsquigarrow$   
assume **only couplings to muons**
- Viable window above LHC (without  $m_\mu$ -finetuning)

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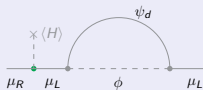


[Athron, Balazs, Jacob, Kotlarski, DS, Stöckinger-Kim, 2104.03691 ]

## $a_\mu$ from 2-field model L

- No chiral enhancement, need very large couplings
- LHC: lower mass limits
- Dark matter candidate, but incompatible with large  $a_\mu$

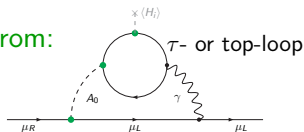
General result:  $a_\mu$  and DM require at least three new fields!



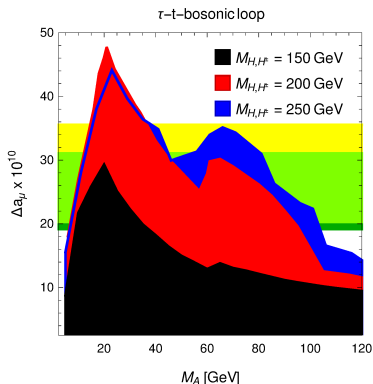
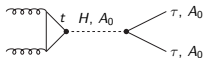
# BSM with smaller masses, hidden from colliders?

- Aligned 2-Higgs doublet model, rich new Higgs/Yukawa sectors

$a_\mu$  from:



LHC constraints:

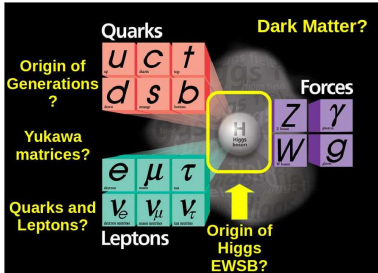


[2104.03691]

- can explain  $g - 2$
- need large new Yukawa couplings
- under pressure, testable at LHC, lepton colliders, B-physics

# Outline

- 1 Overview and SM theory
- 2  $g = 2$  and BSM — important general remarks
- 3 Examples of concrete models and constraints
- 4 General lessons and conclusions



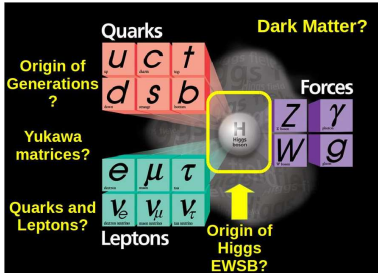
Window to muon mass generation mechanism?

Dark Matter? Hard to see in detectors

but could couple to muon  $\rightsquigarrow$  large effects possible!

many examples, but within simple models: need at least three new fields

generally: dark matter direct detection constraints important!



## Window to muon mass generation mechanism?

allows significant chiral enhancements,

but such models are constrained by collider, flavour etc

## Dark Matter? Hard to see in detectors

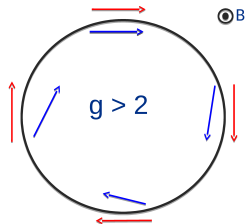
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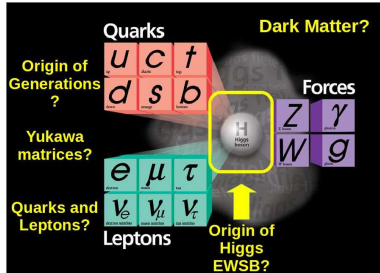
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(continuous spin rotation requires rest mass!)







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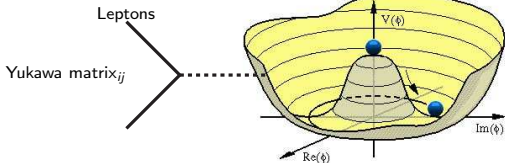
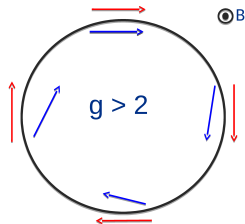
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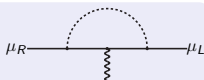
(changed by new physics?)

## Two important general points

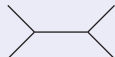
discrepancy  $\approx 2 \times a_\mu^{\text{SM,weak}}$

but: expect  $a_\mu^{\text{NP}} \sim a_\mu^{\text{SM,weak}} \times \left(\frac{M_W}{M_{\text{NP}}}\right)^2 \times \text{couplings}$

loop-induced, CP- and Flavor-conserving, chirality-flipping



compare:



$b \rightarrow s\gamma$   
EDMs,  $B \rightarrow \tau\nu$   
 $\mu \rightarrow e\gamma$

EWPO

**Questions: Which models can(not) explain it?**

**Why is a single number so interesting?**

**“Why are you happy about a discrepancy?”**

$\Rightarrow$  we might make significant progress!

# Summary of main points

discrepancy  $\approx 2 \times a_\mu^{\text{SM,weak}}$

but: expect  $a_\mu^{\text{NP}} \sim a_\mu^{\text{SM,weak}} \times \left(\frac{M_W}{M_{\text{NP}}}\right)^2 \times \text{couplings}$

$a_\mu$  is loop-induced, CP- and flavor-conserving and chirality-flipping

rather light, neutral (?) particles  $\rightsquigarrow$  Connection to dark matter?

Chirality flip enhancement  $\rightsquigarrow$  Window to muon mass generation? EWSB/generations?

## Which models can still accommodate large deviation?

Many (but not all) models!

but always: **experimental constraints!**

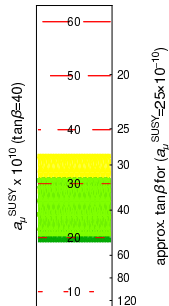
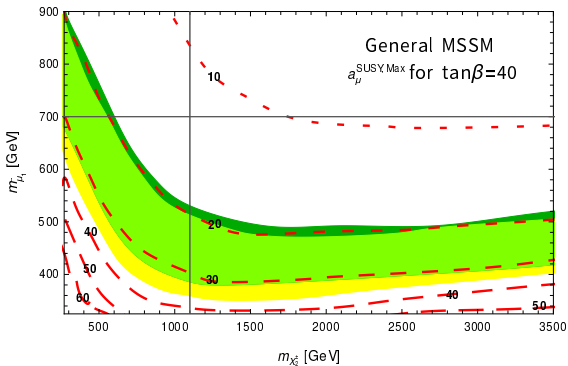
## Outlook:

- $g - 2 + \text{LHC, DM}$   $\rightsquigarrow$  constraints on BSM physics, great potential for future
- often chirality flips/new flavor structures/light particles  $\rightsquigarrow$  tests: Higgs couplings,  $B$ -physics, CLFV, EDM, light-particle searches,  $e^+e^-$ /muon collider

20 years after BNL... deviation confirmed ... very promising future!

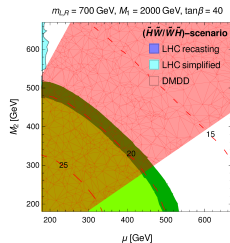
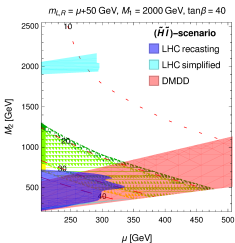
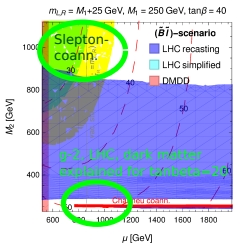
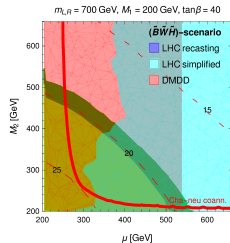
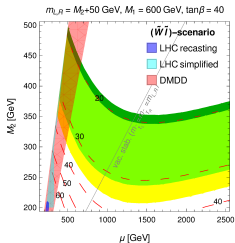
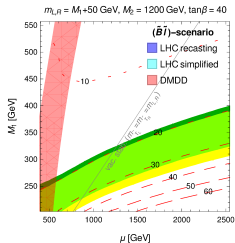
# Full MSSM overview in 7 plots

[Peter Athron, Csaba Balasz, Douglas Jacob, Wojciech Kotlarski, DS, Hyejung Stöckinger-Kim, 2104.03691]



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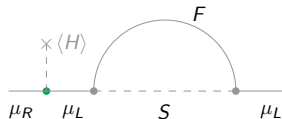
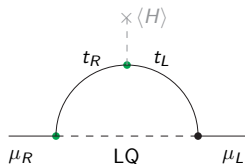


Summary: Bino-LSP:  $a_\mu$  and DM. Wino-/Higgsino-LSP:  $a_\mu$ . Both  $\chi_0 < \text{slepton}$ :  $\approx$ disfavoured.

DM+LHC  $\Rightarrow$  mass patterns! Coannihilation regions help! Specific cases excluded, e.g. Constrained MSSM



# One-field, two-field models (renormalizable, spin 0, 1/2)



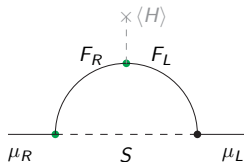
- many models: excluded
- very special models: chiral enhancement  
specific leptoquarks, specific 2HDM versions
- however, no dark matter

Model	Spin	$M(S) = M(S')$	Remark
101	0	$\frac{1}{2} \times \frac{1}{2}$	Excluded (see below)
102	0	$\frac{1}{2} \times \frac{1}{2}$	Excluded (see below)
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112	0	$\frac{1}{2} \times \frac{1}{2}$	Excluded (see below)
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149	1	$\frac{1}{2} \times \frac{1}{2}$	Excluded (see below)
150	1	$\frac{1}{2} \times \frac{1}{2}$	Excluded (see below)

- even more models: excluded
- no chirality flip
- few models: either  $a_{\mu}^{\text{BNL}}$  or dark matter

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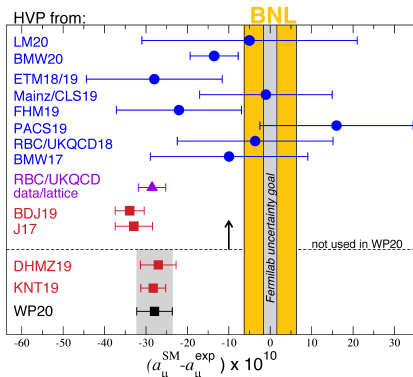
# Three-field models



- many models: viable, large chirality enhancements
- can explain  $a_\mu^{\text{BNL}}$  and LHC and dark matter

# Details on hadronic vacuum polarization

$a_\mu^{\text{HVP}}$ : Status of Hadronic Vacuum Polarisation contributions



## Lattice QCD + QED

- impressive progress, but...
- large spread between results
- tensions when looking at 'Euclidean time window' comparisons
- large systematic uncertainties (e.g. from non-trivial extrapolation to continuum limit, finite size)

## Dispersive/lattice hybrid

('window' method)

For WP20: **Dispersive data-driven**  
from DHMZ and KNT

TI White Paper 2020 value:

$$a_\mu^{\text{HVP}} = 6845 (40) \times 10^{-11}$$

- TI WP2020 prediction uses **dispersive data-driven** evaluations with **minimal model dependence**
- $a_\mu^{\text{HVP}}$  **value and error** obtained by **merging** procedure  $\Rightarrow$  accounts for tensions in input data and differences in data treatment & combination (going beyond usual  $\chi^2_{\text{min}}$  inflation)

Thomas Teubner

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