

# Dynamical Formation of a Magnetic Impurity

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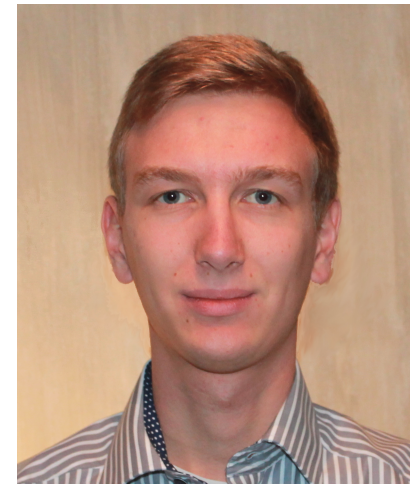
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F. Pollmann

Paris, September 13, 2021



European Research Council

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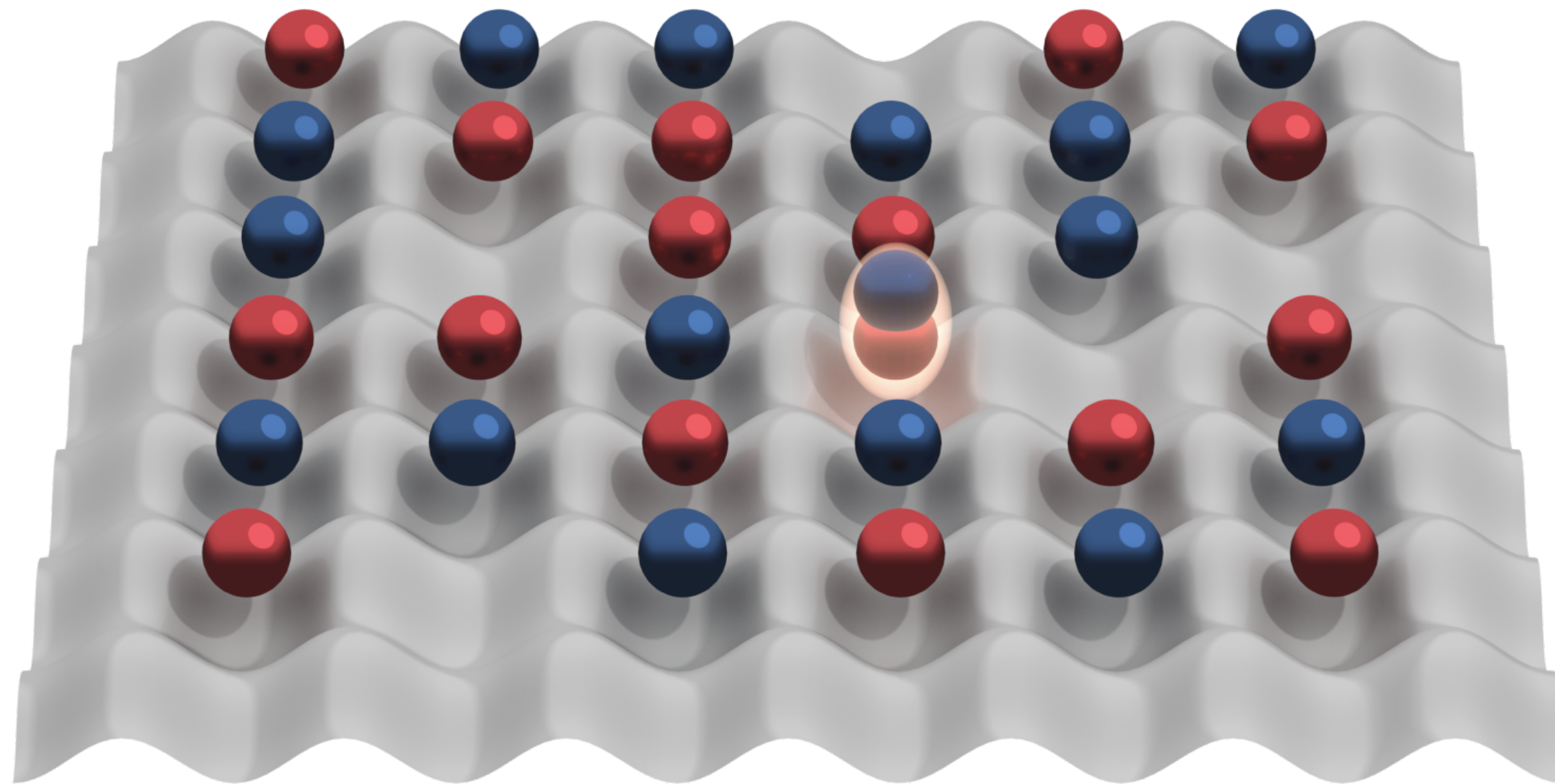


# Fermi-Hubbard model

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} (c_{i,\sigma}^\dagger c_{j,\sigma} + h.c.) + U \sum_i (\hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow})$$

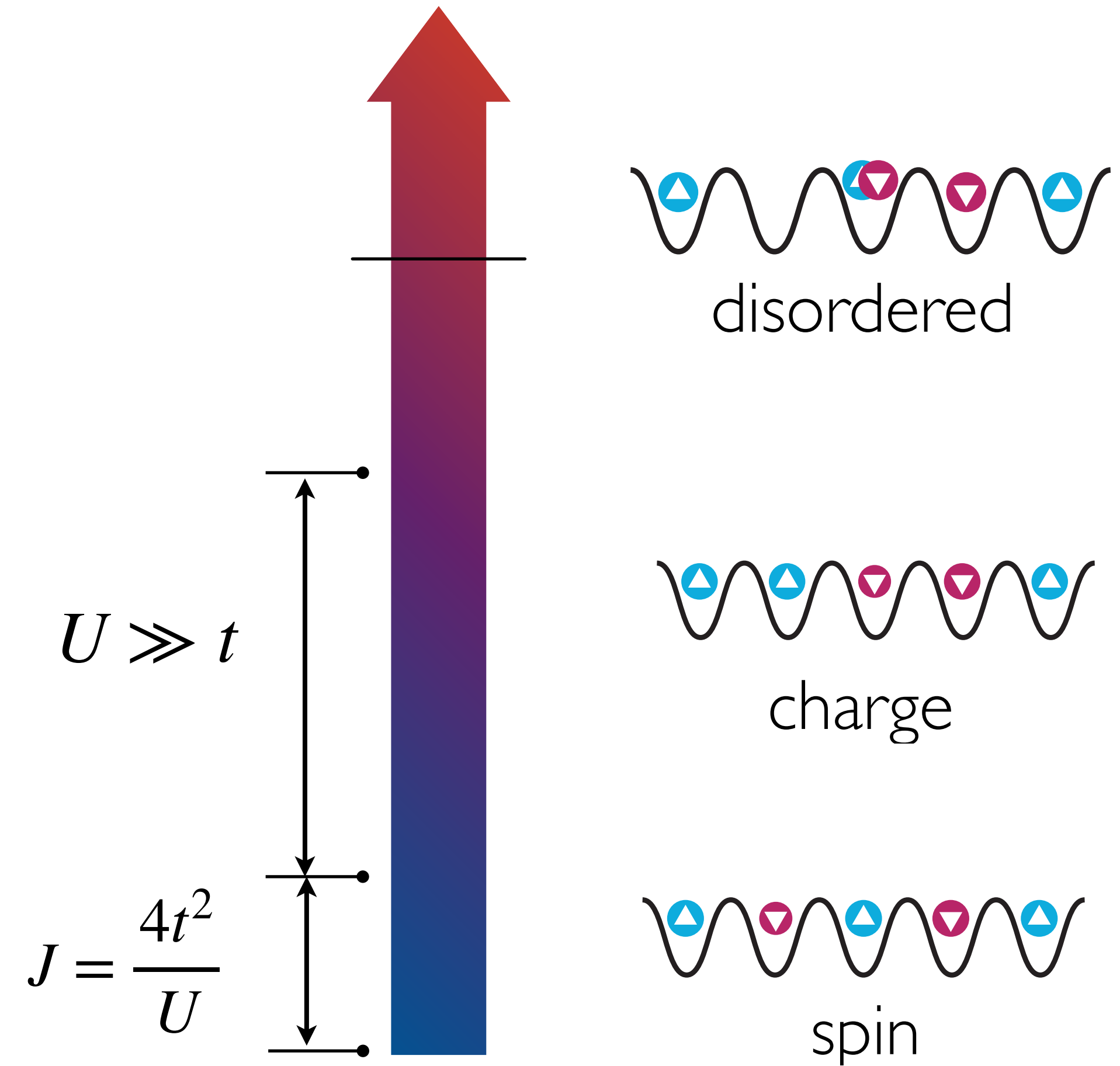
hopping

interactions



[Chiu et al., Science, 2019]

temperature

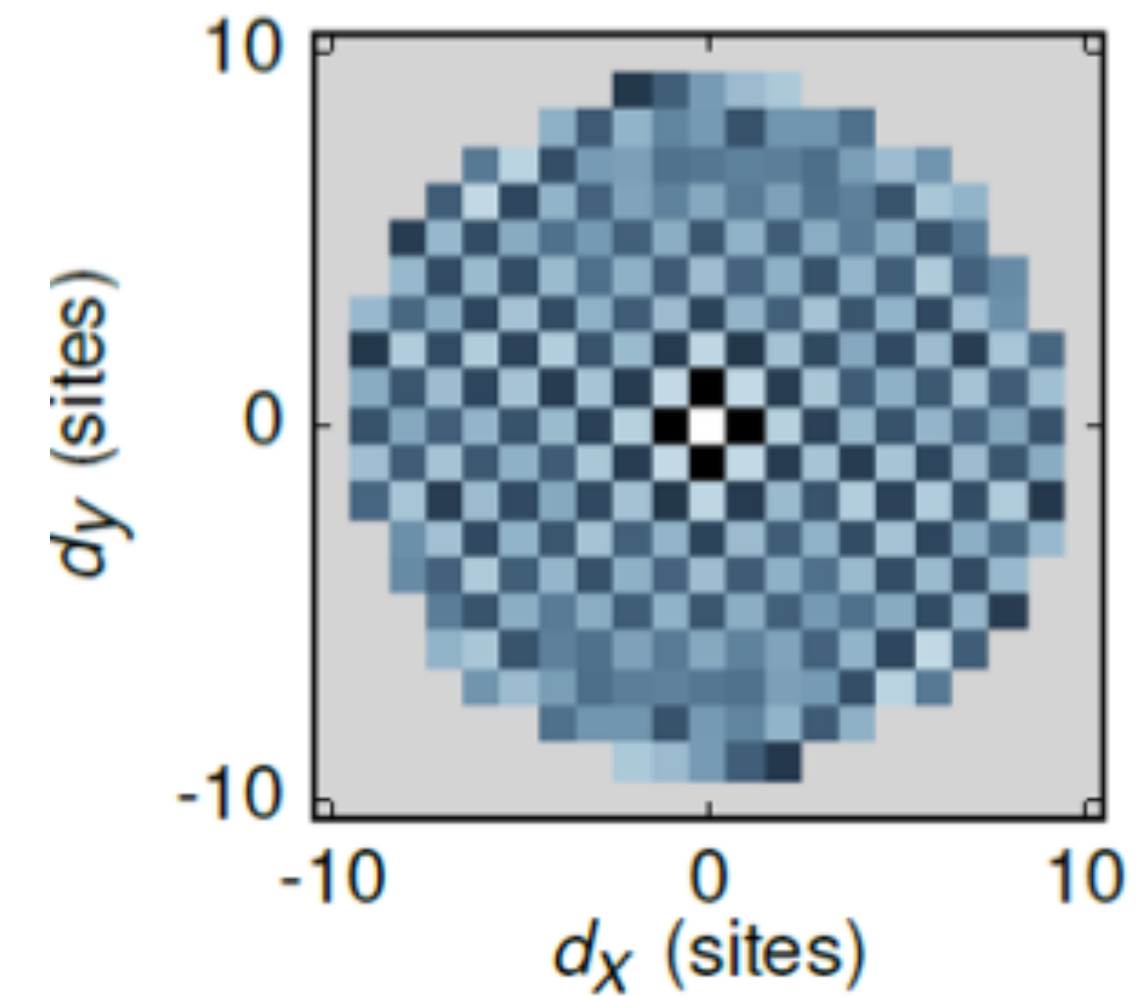
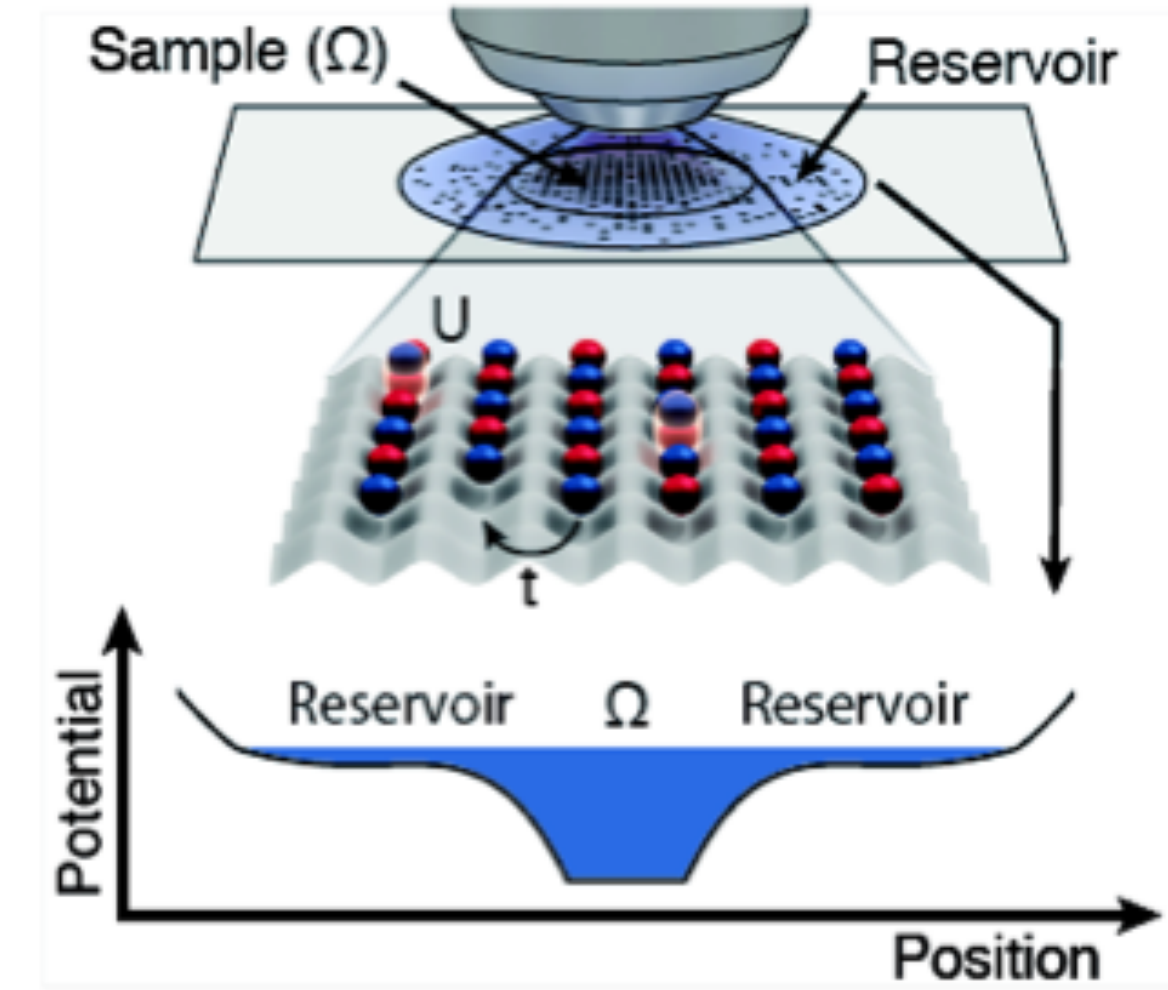
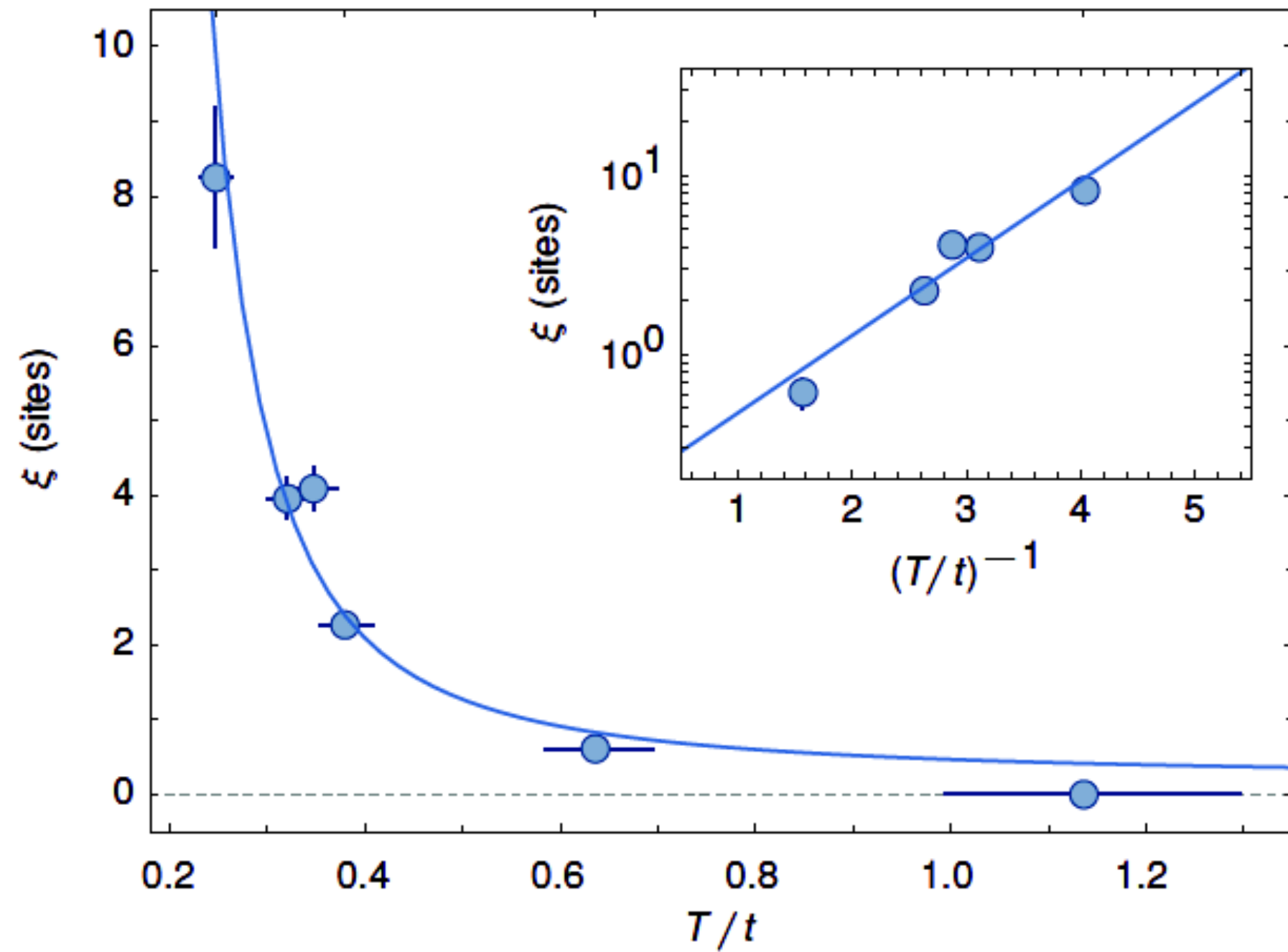




# Anti-ferromagnetic correlations

Correlation length diverges with decreasing temperature

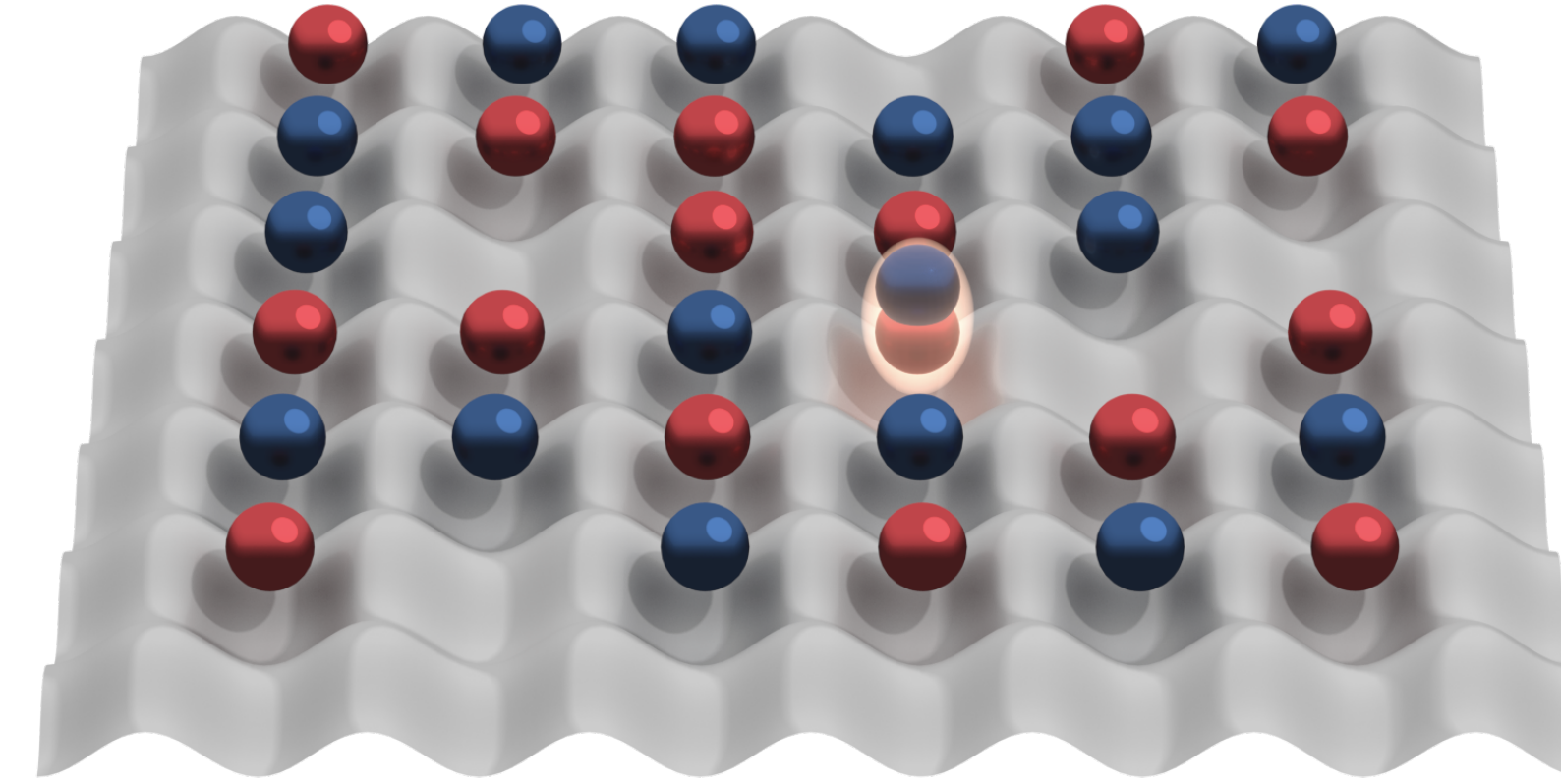
$$\xi(T) \sim e^{2\pi\rho_s/T}$$



# Strong Interactions

Strong interactions ( $t \gg J = 4t^2/U$ )  $\longrightarrow$  **tj-Model**


- Local configurations
-  spin down
  -  spin up
  -  hole




[Chiu et al., Science, 2019]

no double occupancies

$$\hat{\mathcal{H}}_{t-J} = -t \hat{\mathcal{P}} \left[ \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + \text{h.c.} \right] \hat{\mathcal{P}} + J \sum_{\langle i,j \rangle} \left( \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_j - \frac{1}{4} \hat{n}_i \hat{n}_j \right)$$



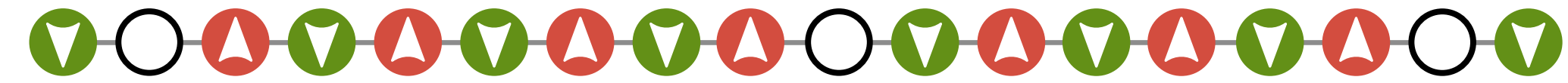
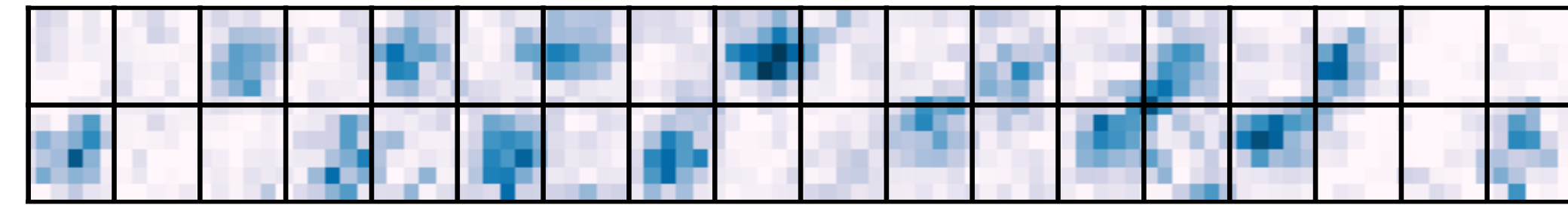


# Hole doping in 1D - a parton picture

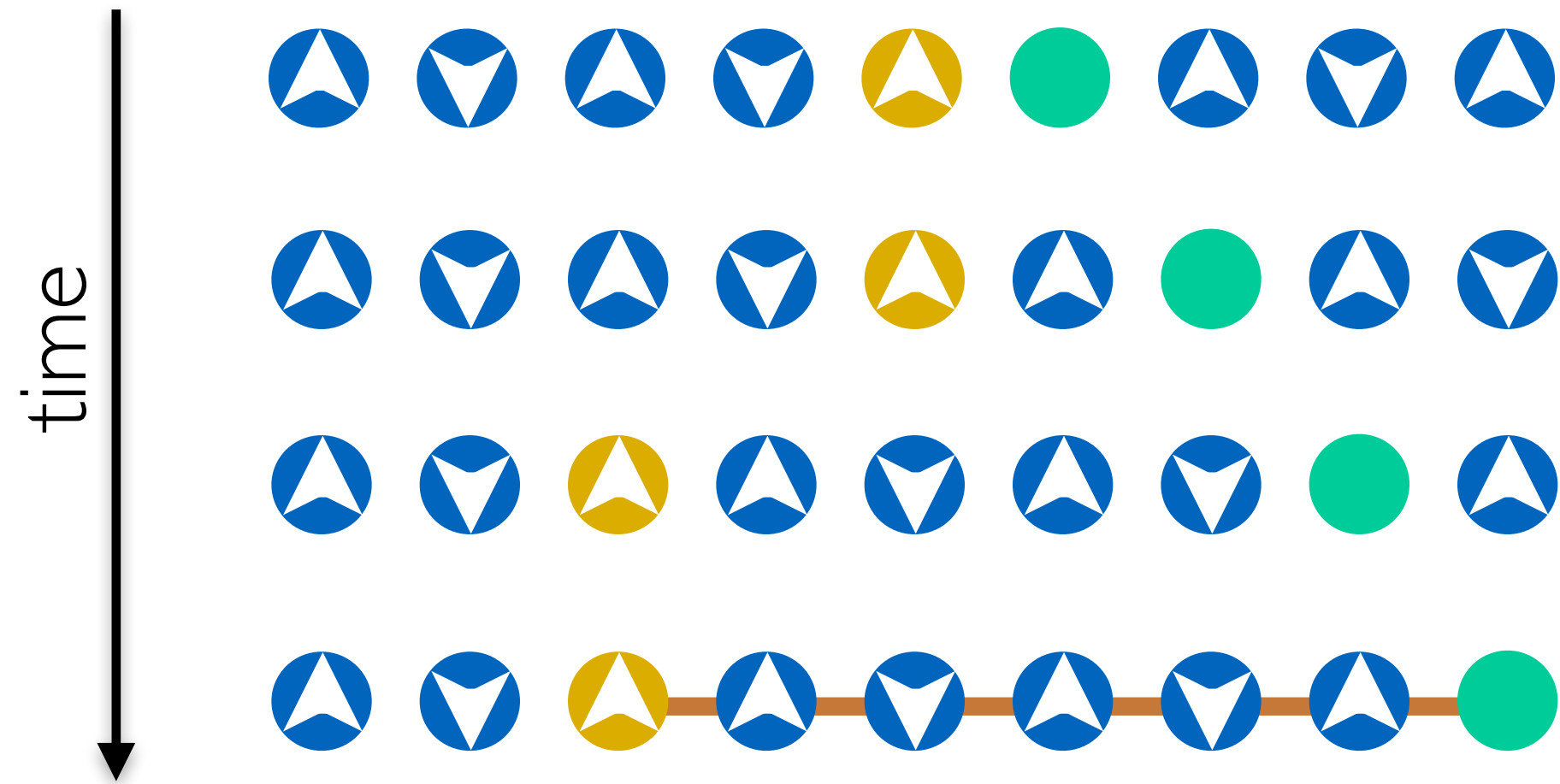


Spinon: fractional spin excitation  $S = 1/2$

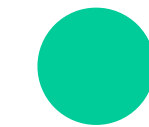
Chargon: keeps relative spin orientation



[Hilker et al., Science, 2017]



spinon



chargon

Spin-charge separation: deconfined spinons and chargons ( $t \gg J = 4t^2/U$ )

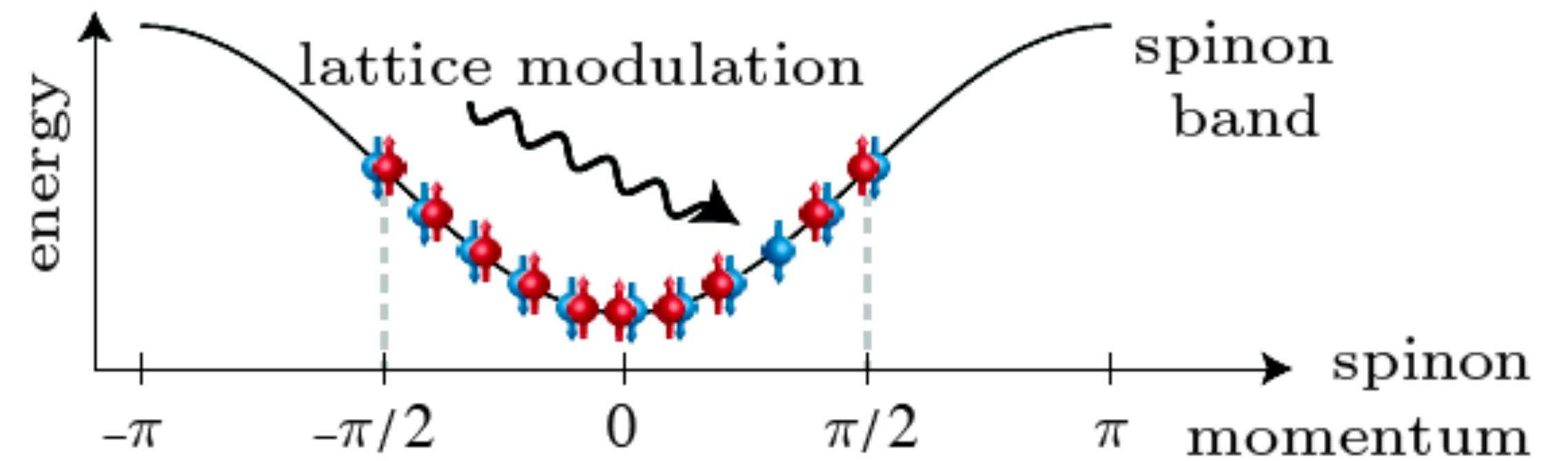
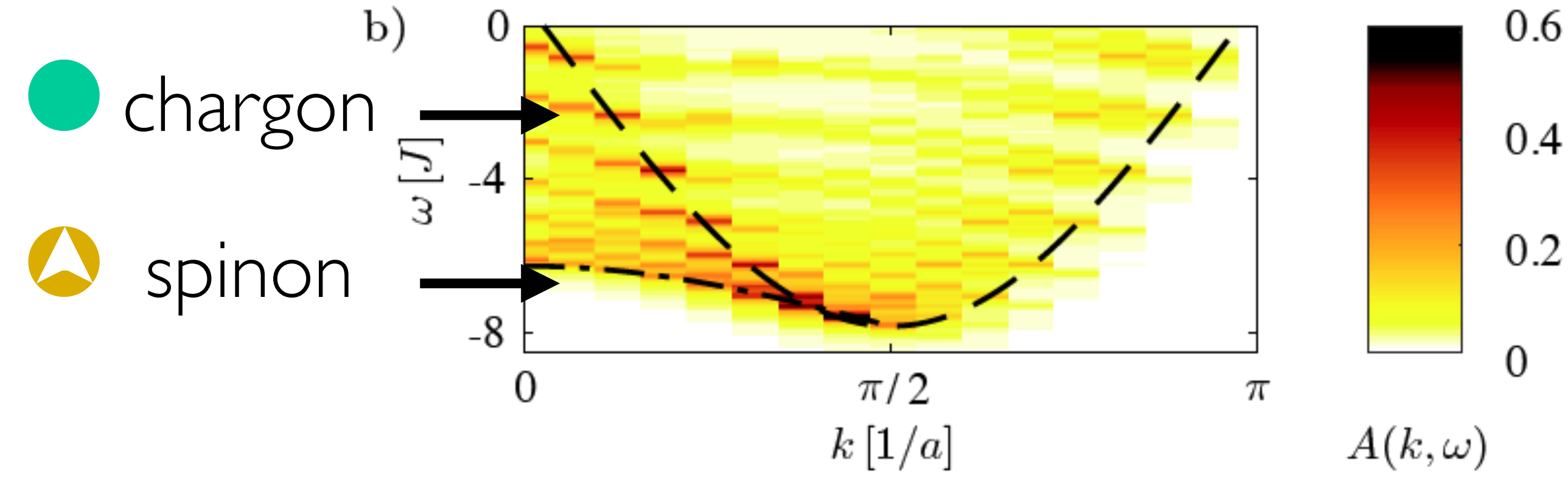
# Manifestation of spin-charge separation

Single-hole spectral function (ARPES)

$$A(k, \omega) = A_{\text{spinon}} * A_{\text{holon}} = \int d\omega_h dk_h A_{\text{holon}}(k_h, \omega_h) A_{\text{spinon}}(k - k_h, \omega - \omega_h)$$

Asymmetry of spectral weight around  $\pi/2$ :

- Parton description of ground state
- Hole: create chargon and remove spinon

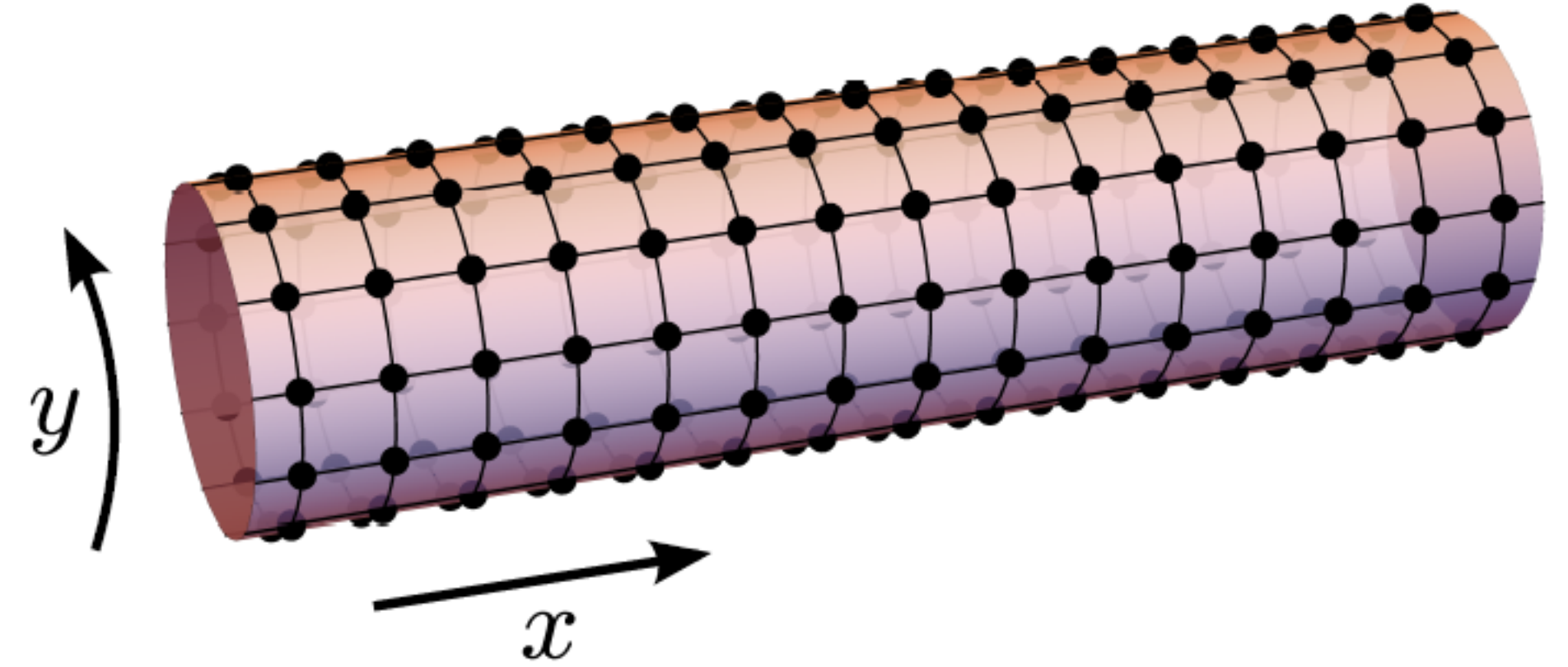
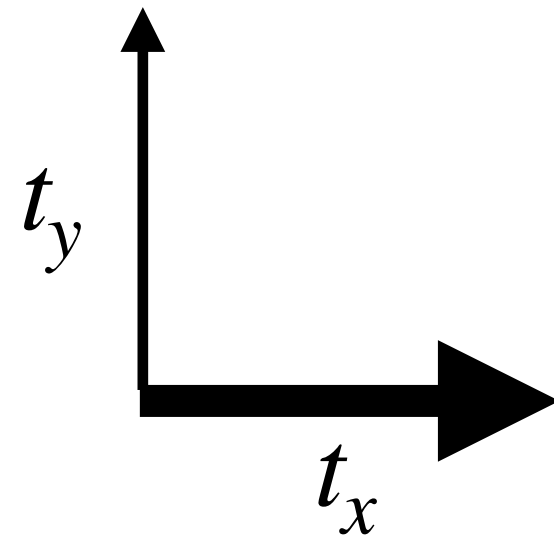
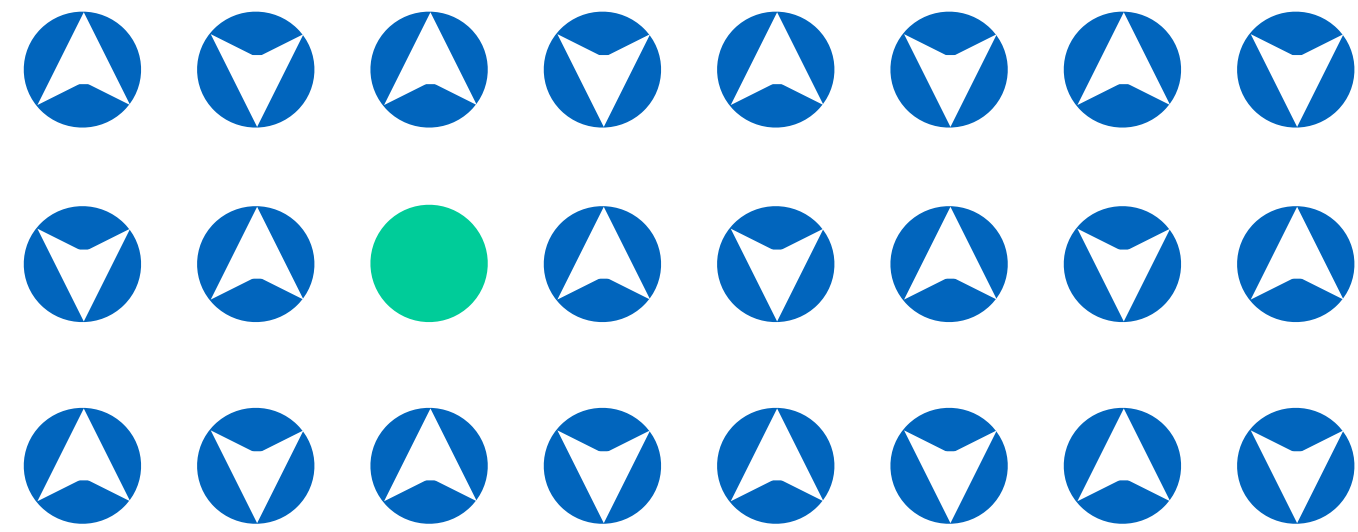


[Bohrdt, et al. Phys. Rev. B 2018]  
cf. [Szczepanski, et al., Phys. Rev. B 1990], ...

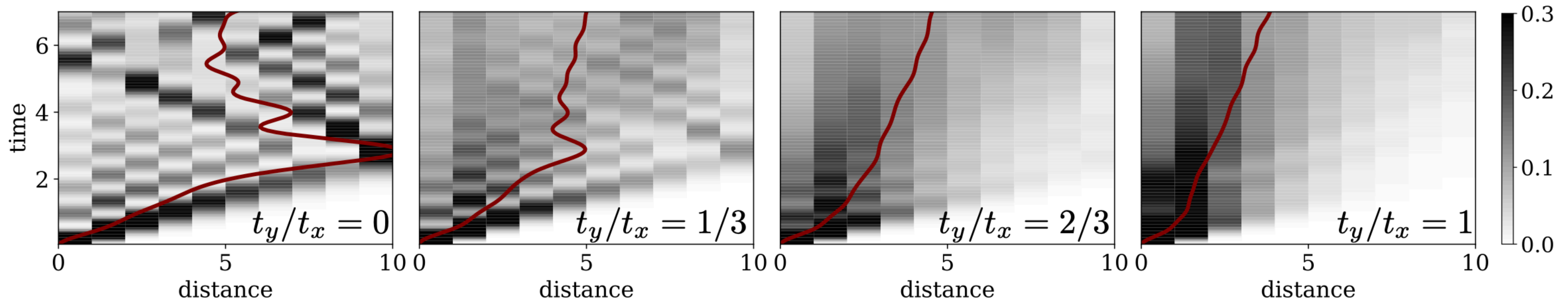


# Dimensional crossover

Numerical calculation: MPS on cylinders



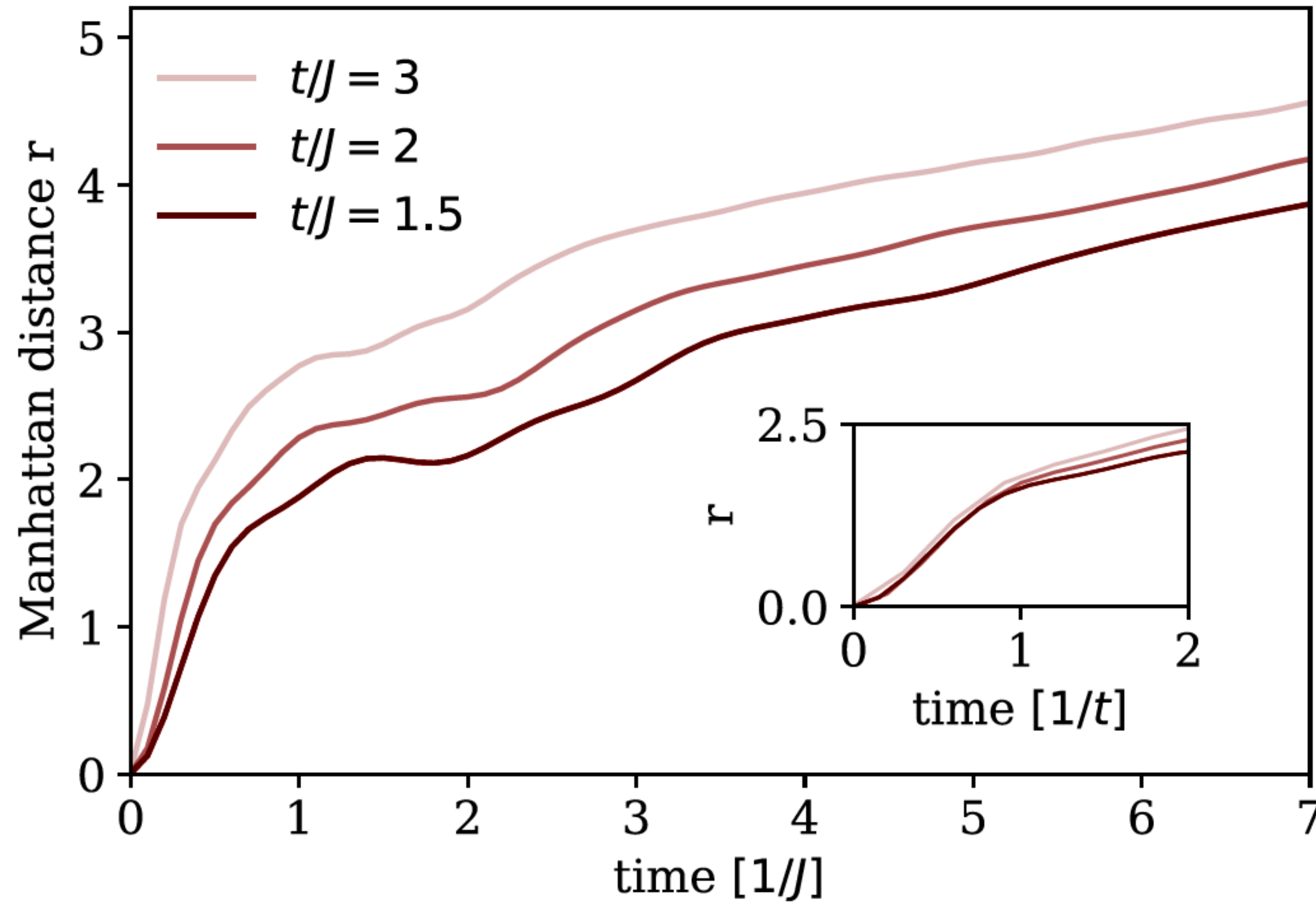
[2D DMRG: M. Zaletel et al., PRB 91 2015]



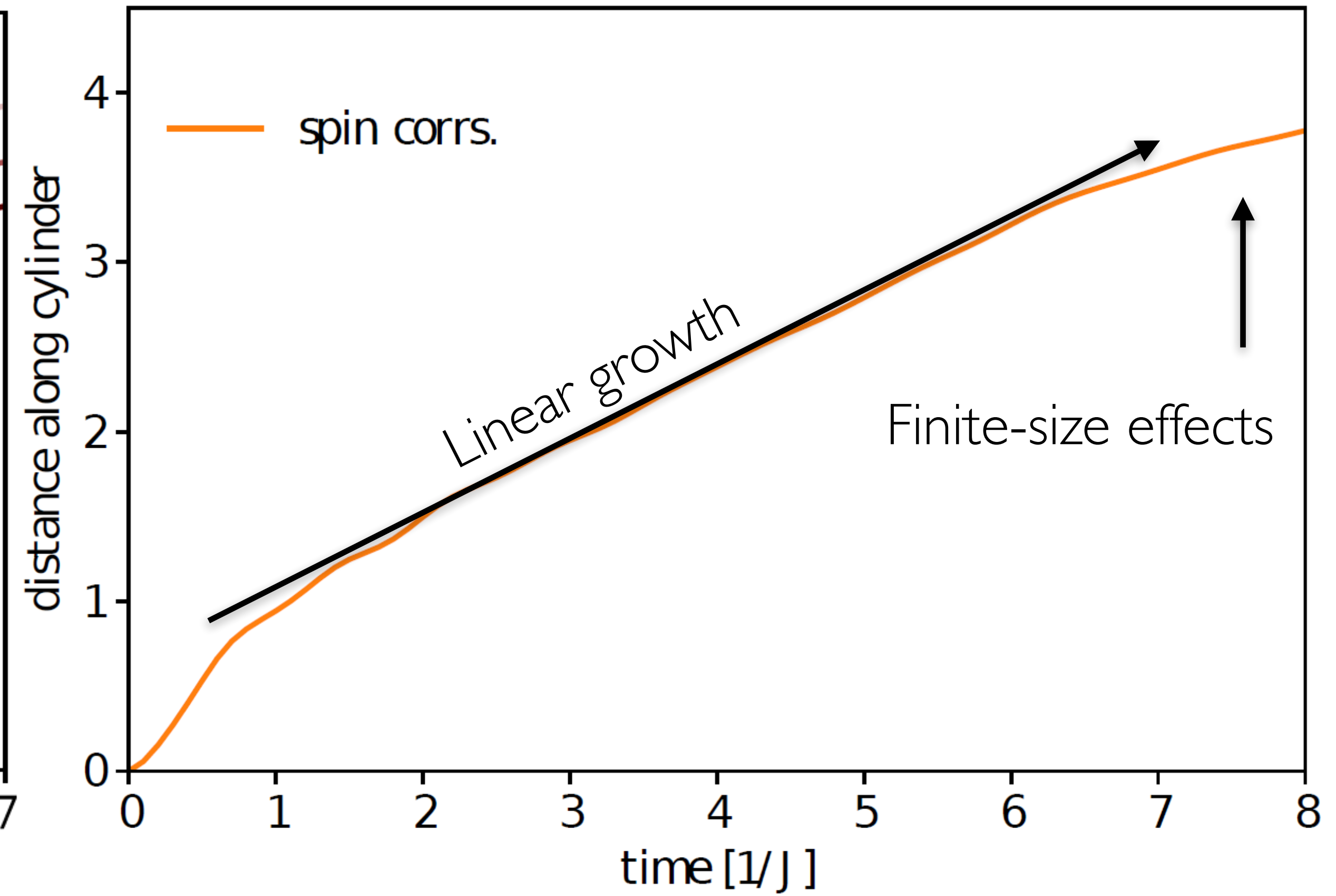
[Bohrdt, Grusdt, MK, NJP 2020]

# Isotropic hopping $t_x = t_y$

Position of hole



Local spin-correlations



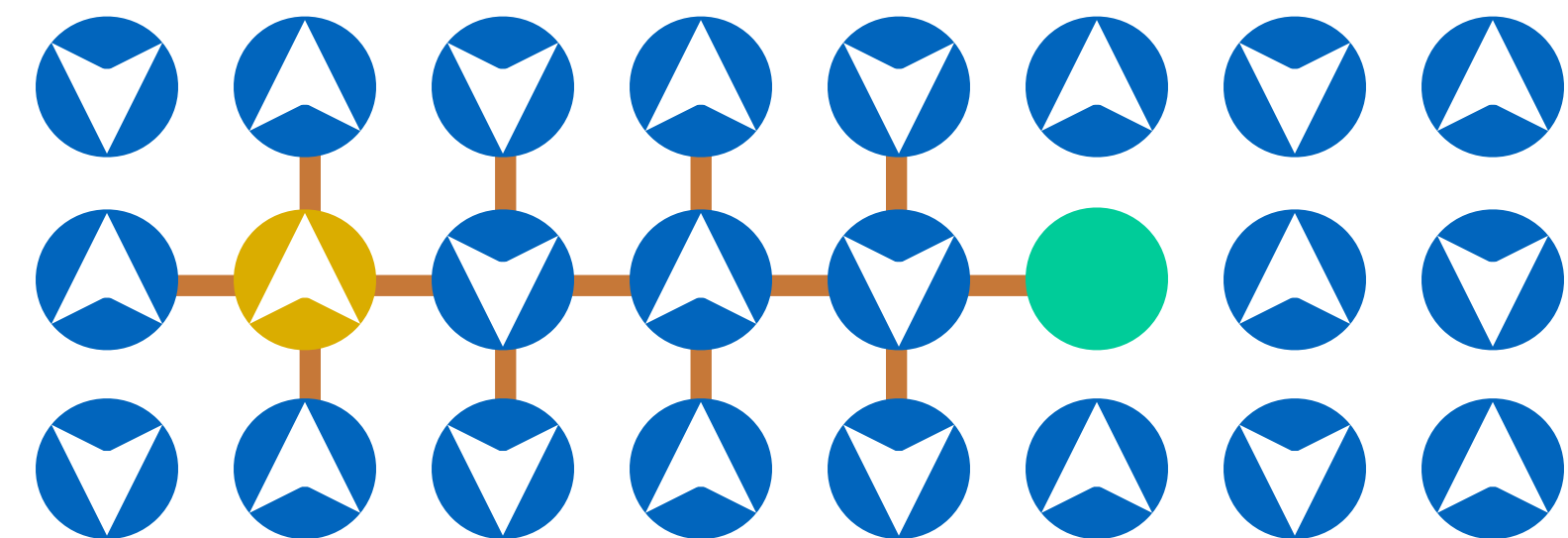
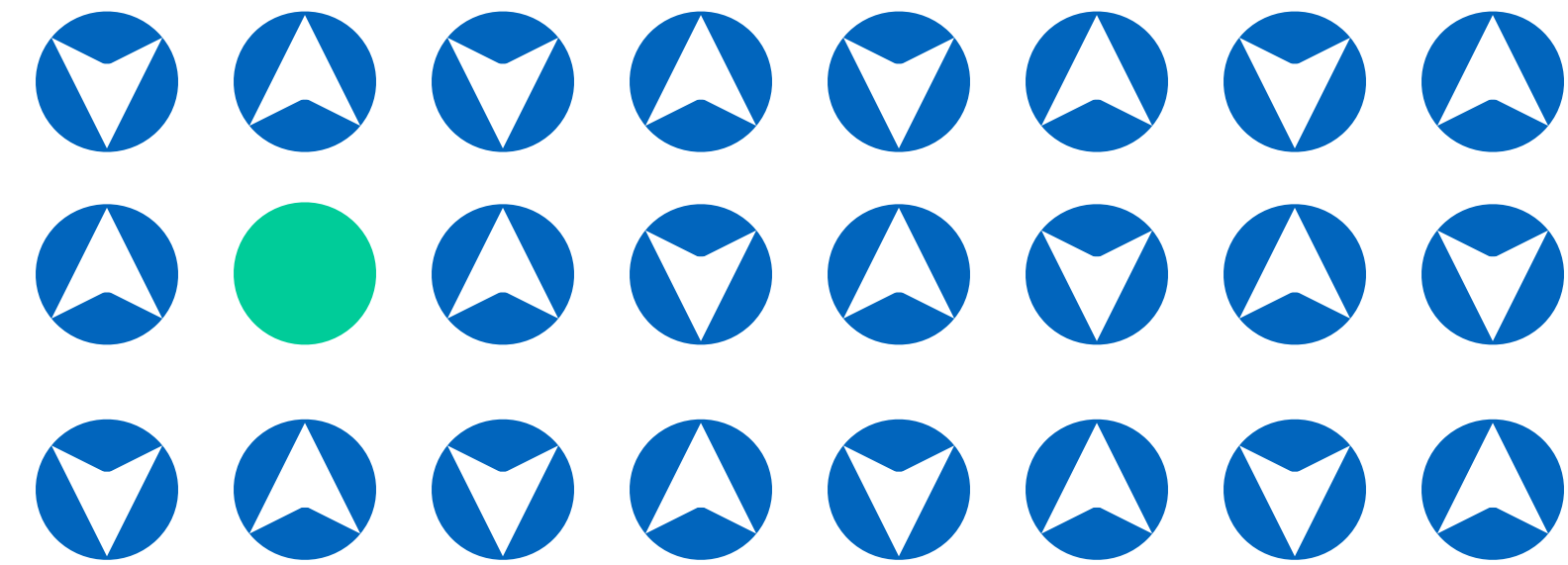


# Parton formalism in 2D

- Fractional spin excitation  $S = 1/2$
- Chargon distorts 2D Néel state
- Chargon bound to spinon at the end of a string

$$E \sim J\ell$$

Competition: hopping vs. bound state energy  
 → emergent length scale



[Beran, Poilblanc, Laughlin, Nucl. Phys. B, 1996]  
 [Grusdt, et al. PRX 2018]

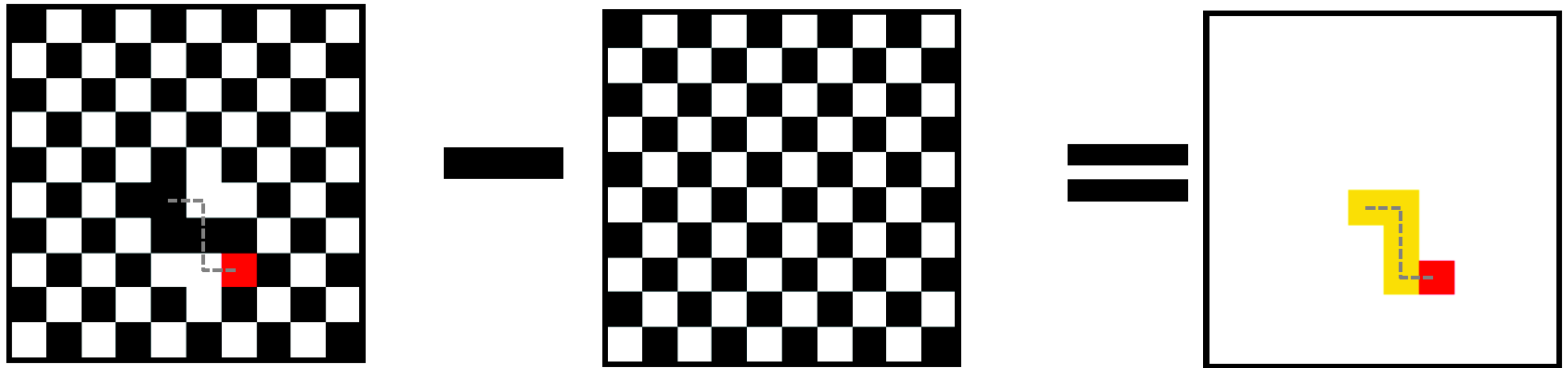
# Quantum many-body wave function

$$|\Psi\rangle = |\text{red dot, red arrow, green line, grey dot}\rangle + |\text{grey dot, red arrow, red dot}\rangle + |\text{grey dot, green line, red arrow, red dot}\rangle + |\text{grey dot, red arrow, red dot, red arrow}\rangle + \dots$$

averaging  
→



# Detecting strings (approximately)

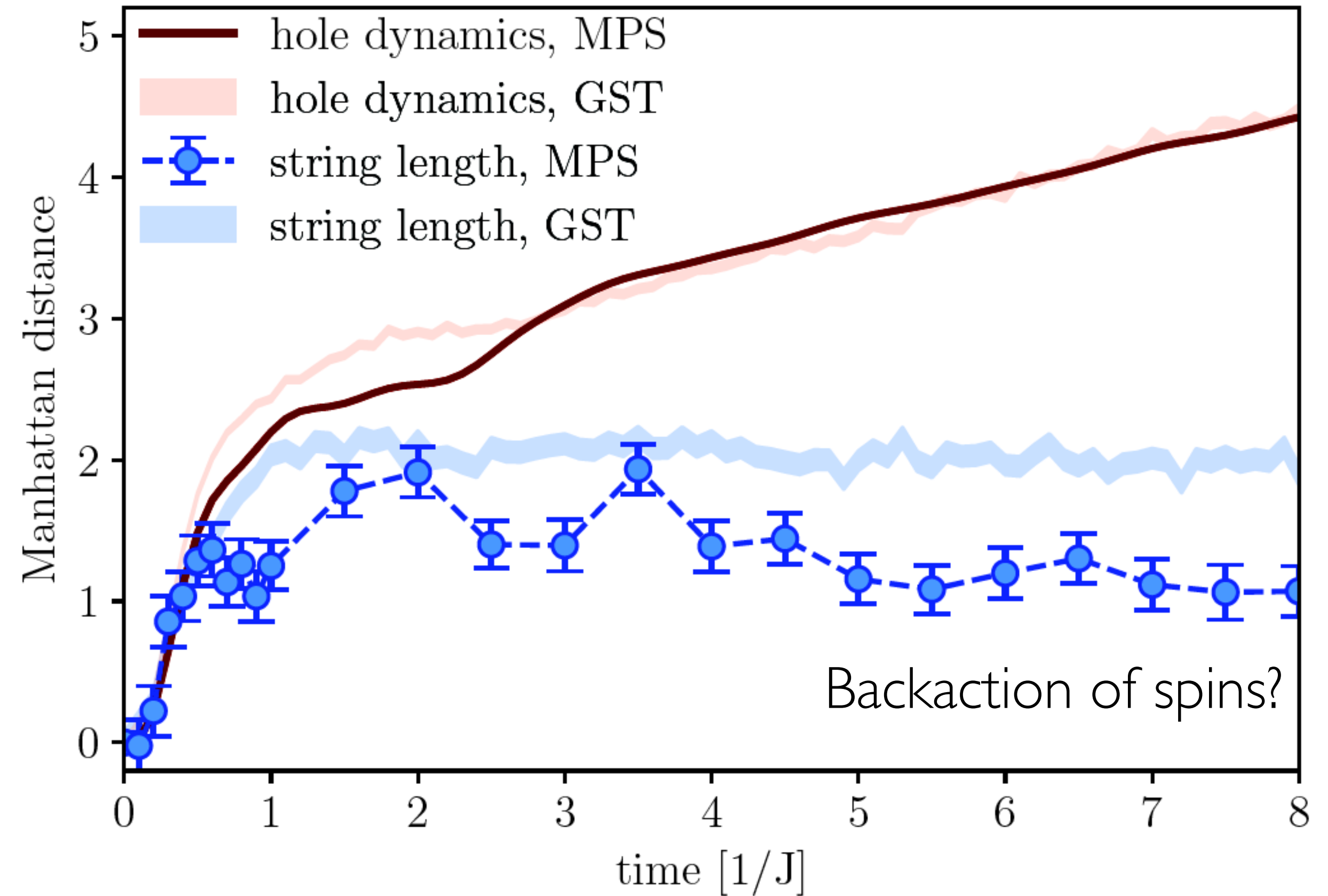


[Chiu, Ji, Bohrdt, et al. Science 2019]  
c.f. [Ho, PNAS 2020]



# Interpretation of our numerical results

1. Free chargon motion — creation of a string
2. Confinement — saturation of string length
3. Free center-of-mass motion by spinon

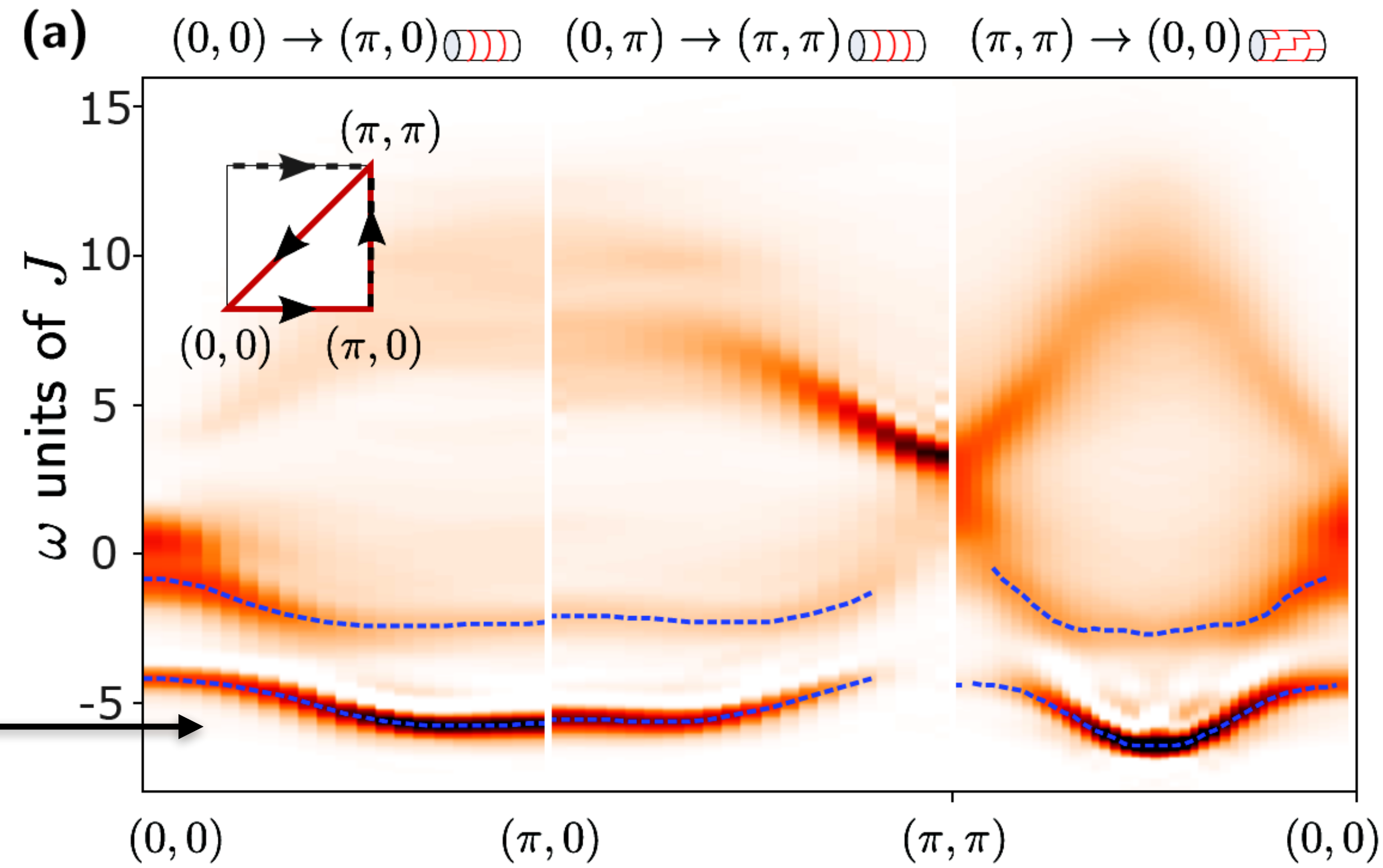


# Parton theory for ARPES

$$A(\omega, \mathbf{k})|_{\text{bound}} = \int d\nu A_s(\omega - \nu, \mathbf{k}) A_c(\nu).$$

- Momentum dependence due to spinon
- Structure factor: two spinons

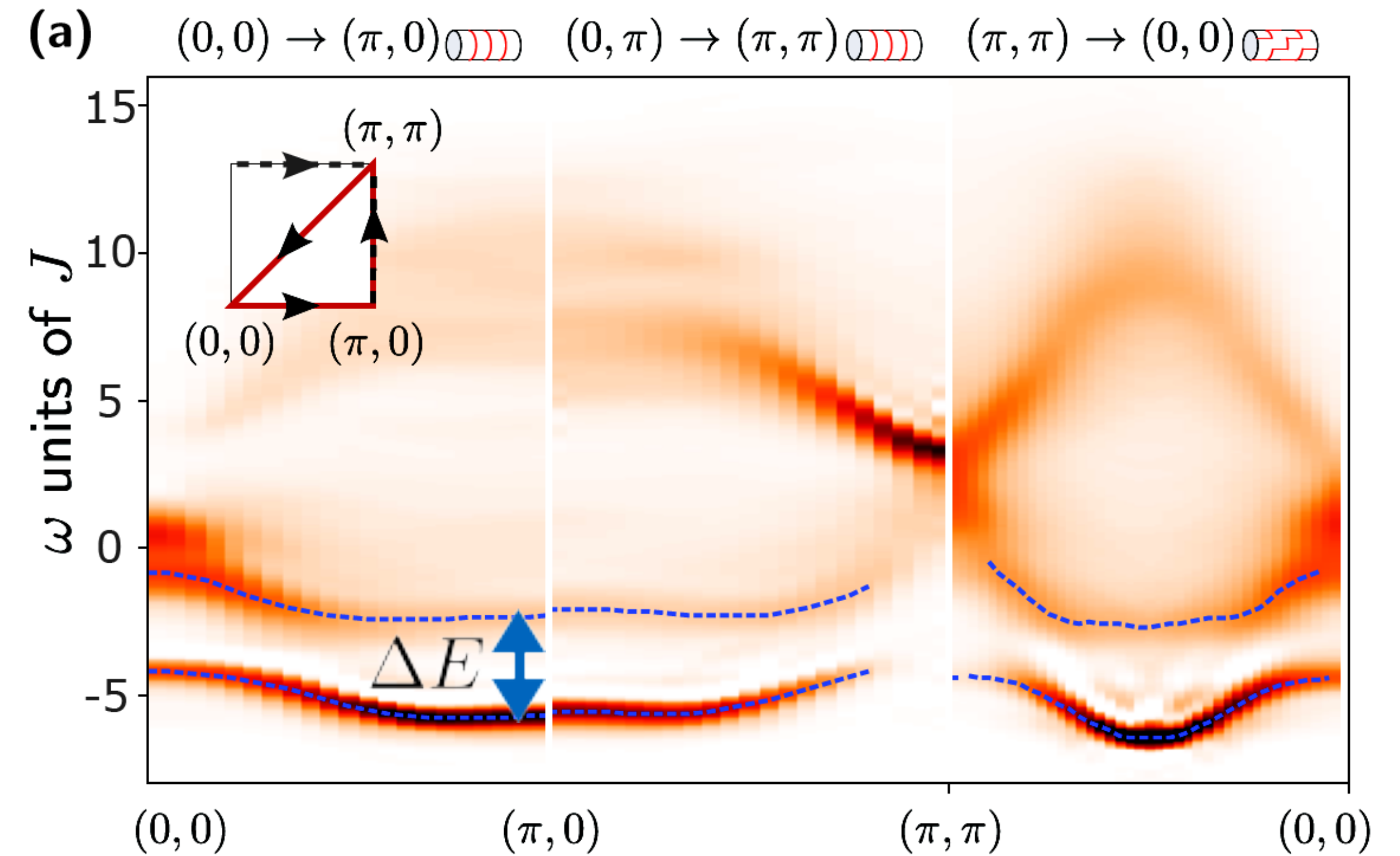
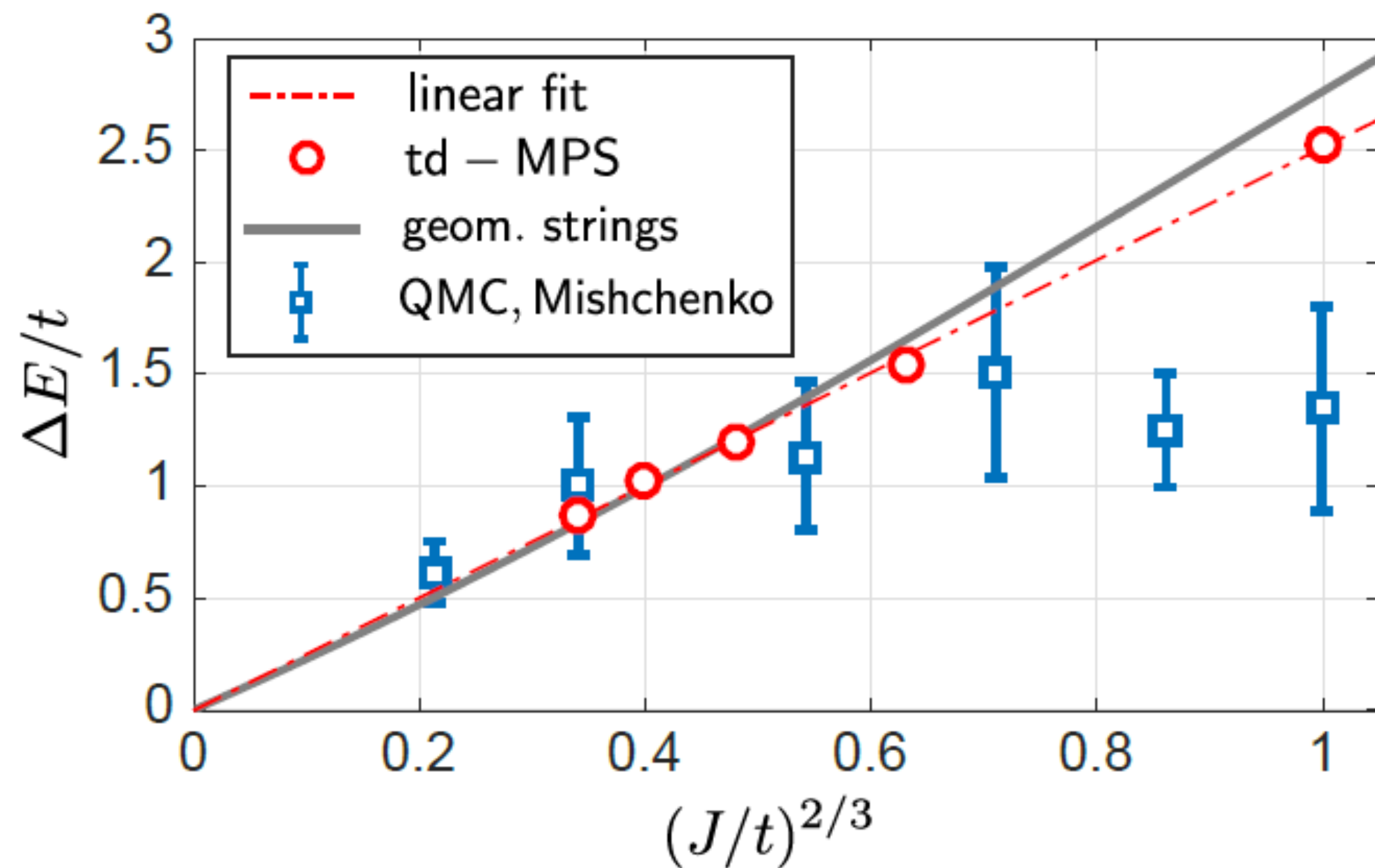
magnetic polaron



# Vibrational excitations

Geometric string leads to linear confinement

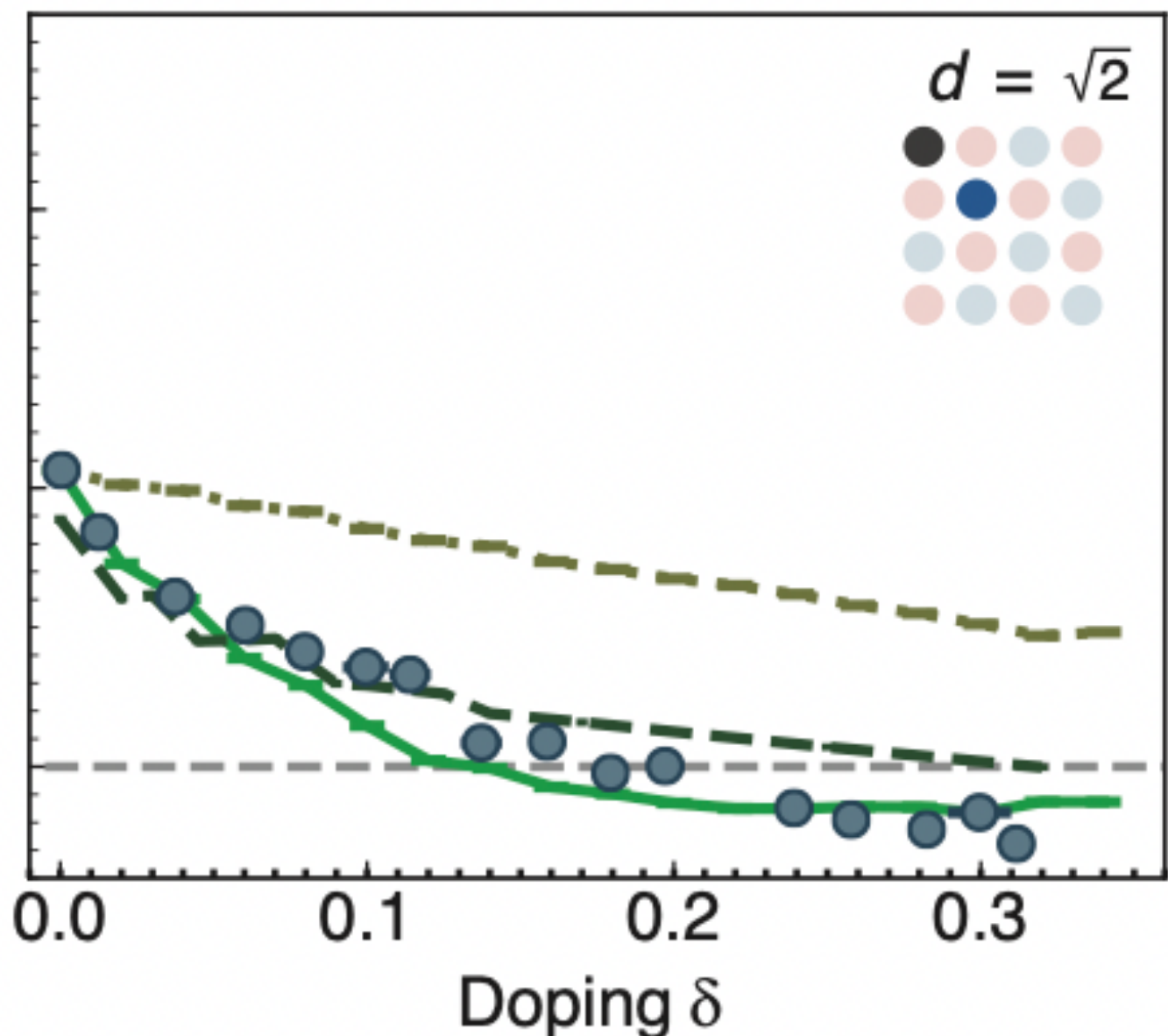
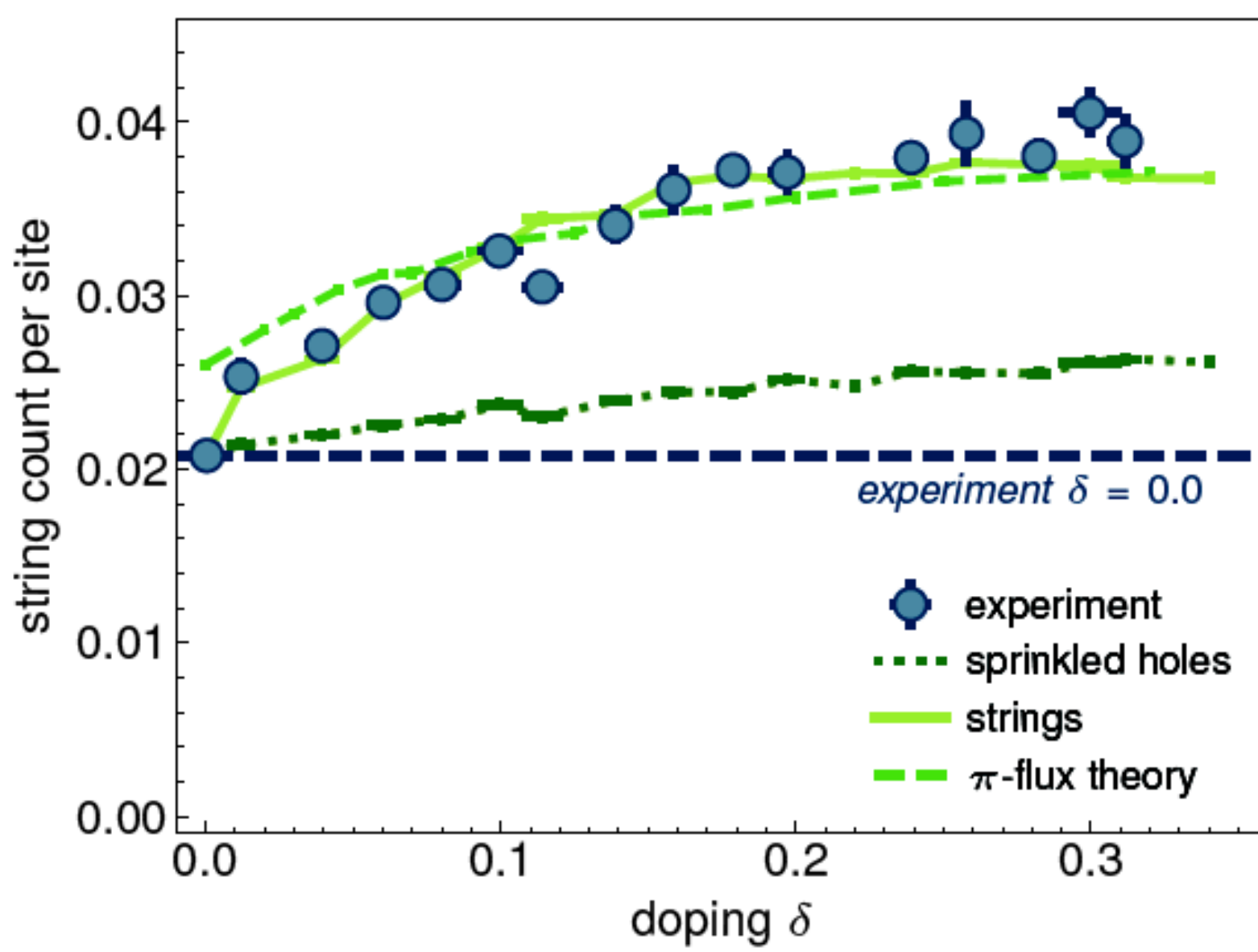
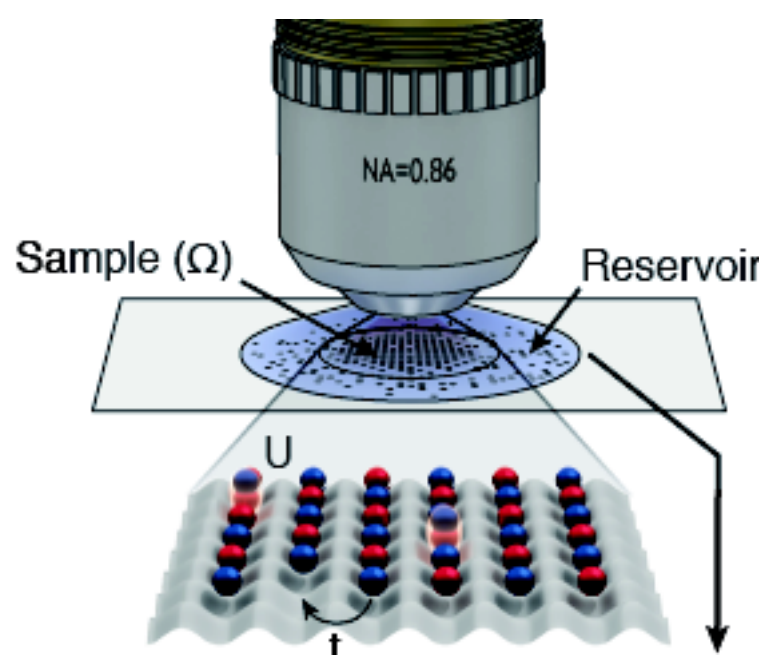
- Vibrational mode  $\Delta E \sim (J/t)^{2/3}$
- Approximately constant gap for all  $k$



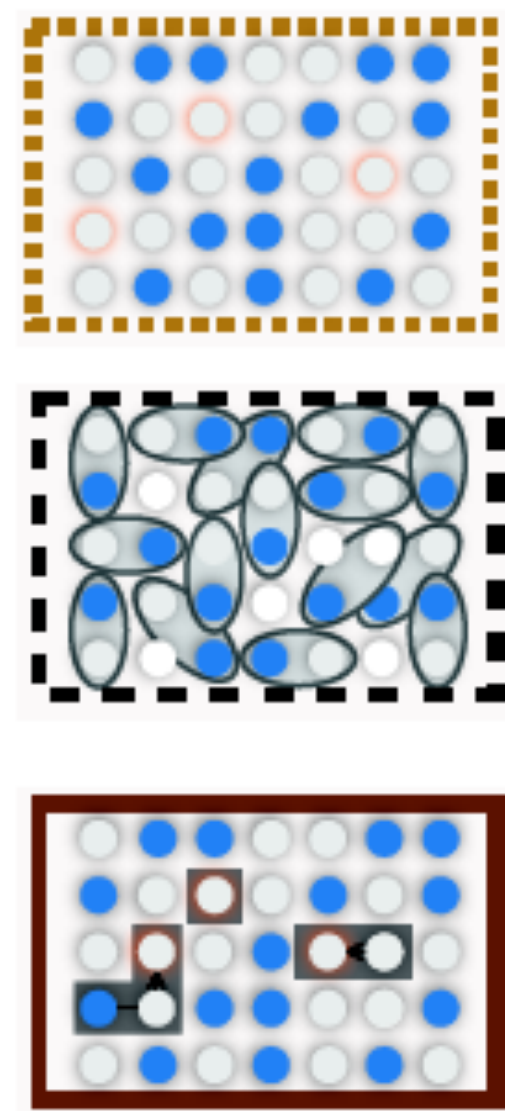


# String patterns in the doped Hubbard model

Christie S. Chiu<sup>1</sup>, Geoffrey Ji<sup>1</sup>, Annabelle Bohrdt<sup>2,1,3</sup>, Muqing Xu<sup>1</sup>, Michael Knap<sup>2,3</sup>, Eugene Demler<sup>1</sup>, Fabian Grusdt<sup>1,3</sup>, Markus Greiner<sup>1\*</sup>, Daniel Greif<sup>1</sup>



- sprinkling
- $\pi$ -flux theory (1 fit parameter)
- geometric string theory (no fit parameter)

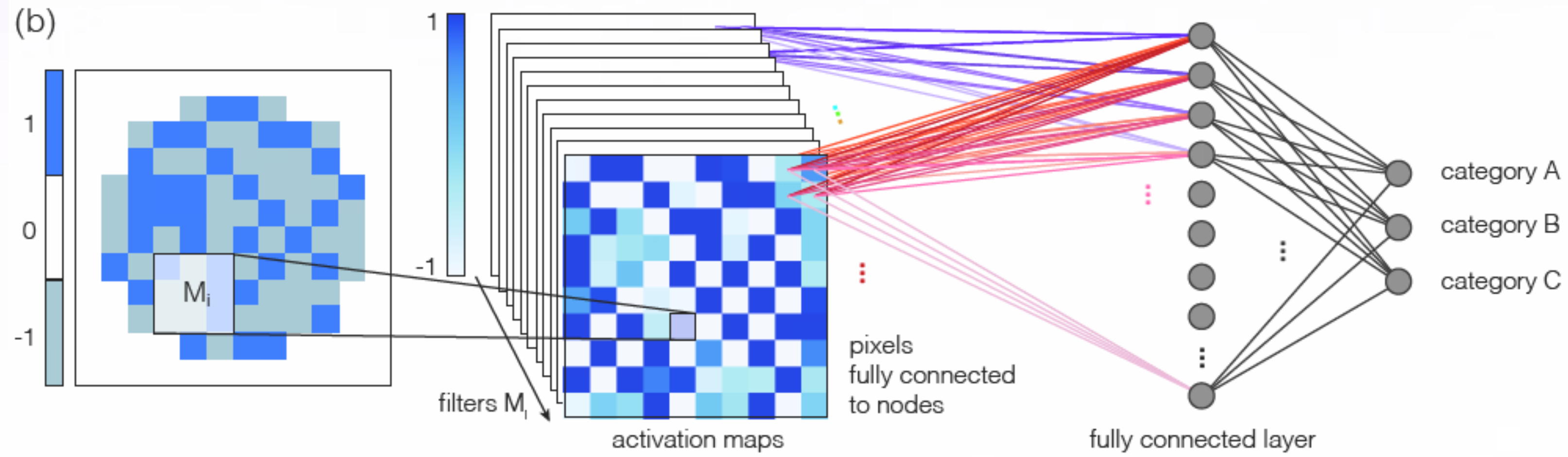


[Chiu, Ji, Bohrdt, et al. Science 2019]

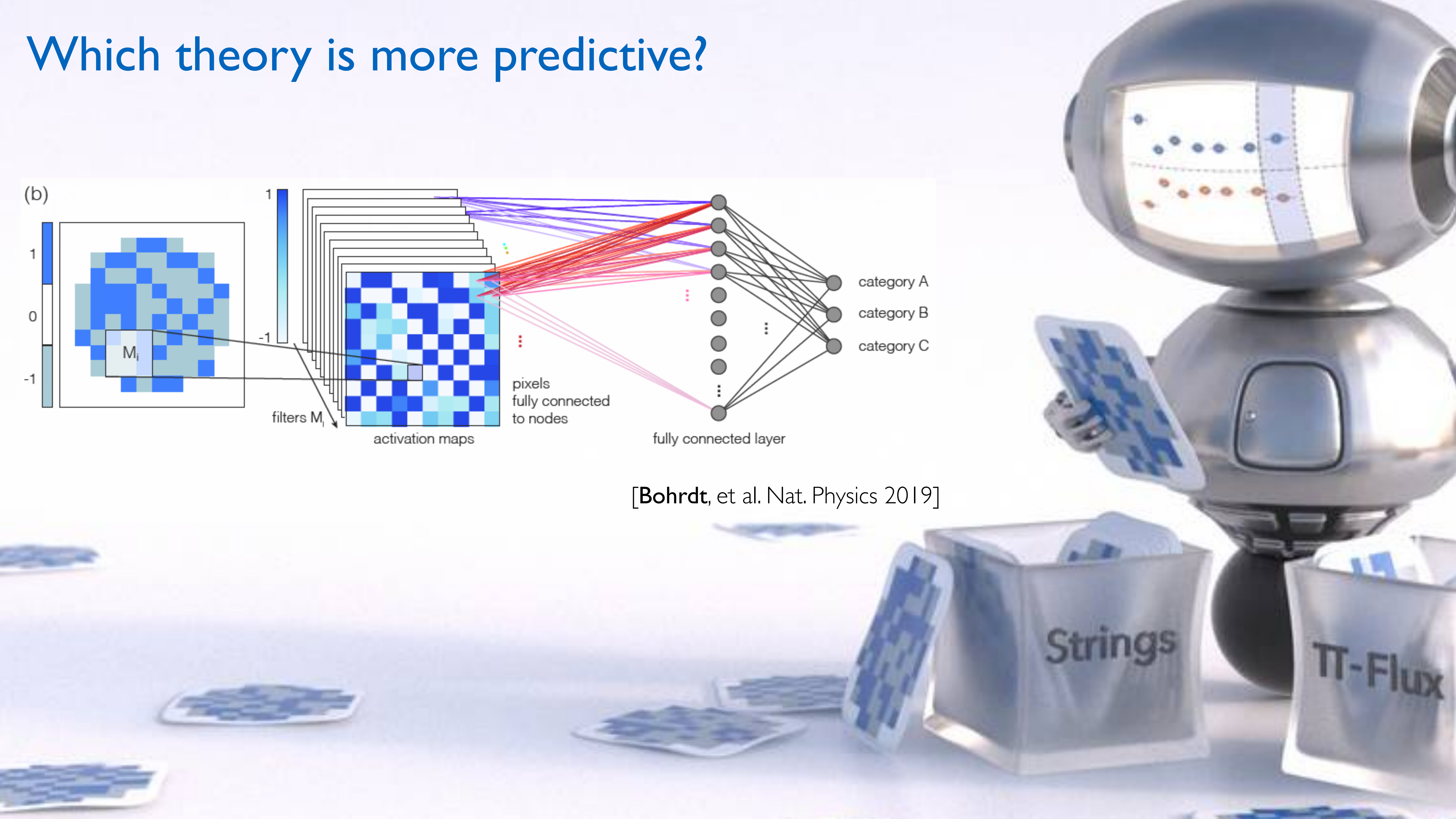
“The theoretical problem is so hard  
that there isn’t an obvious criterion for right.”  
— Steve Kivelson, Science 314 (2006)



# Which theory is more predictive?

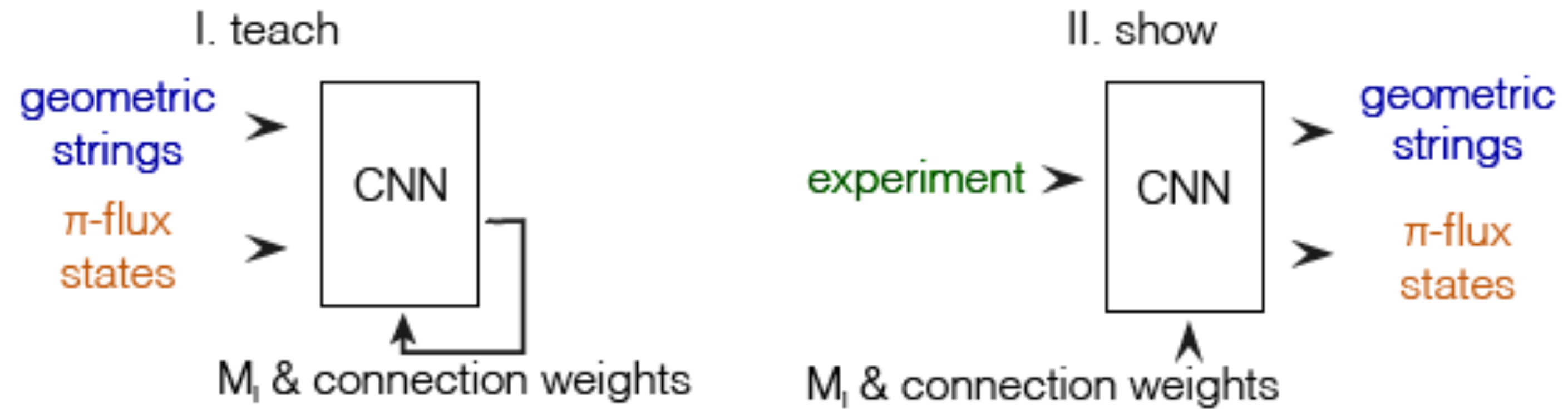
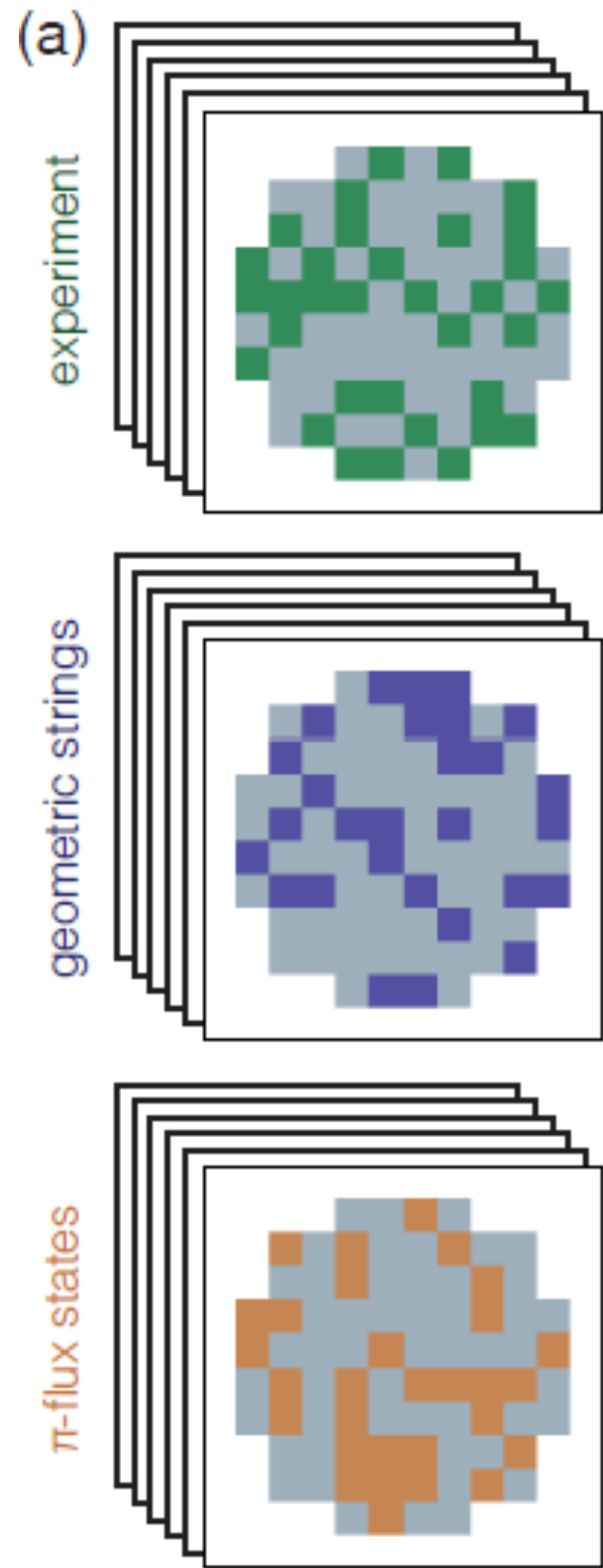


[Bohrdt, et al. Nat. Physics 2019]

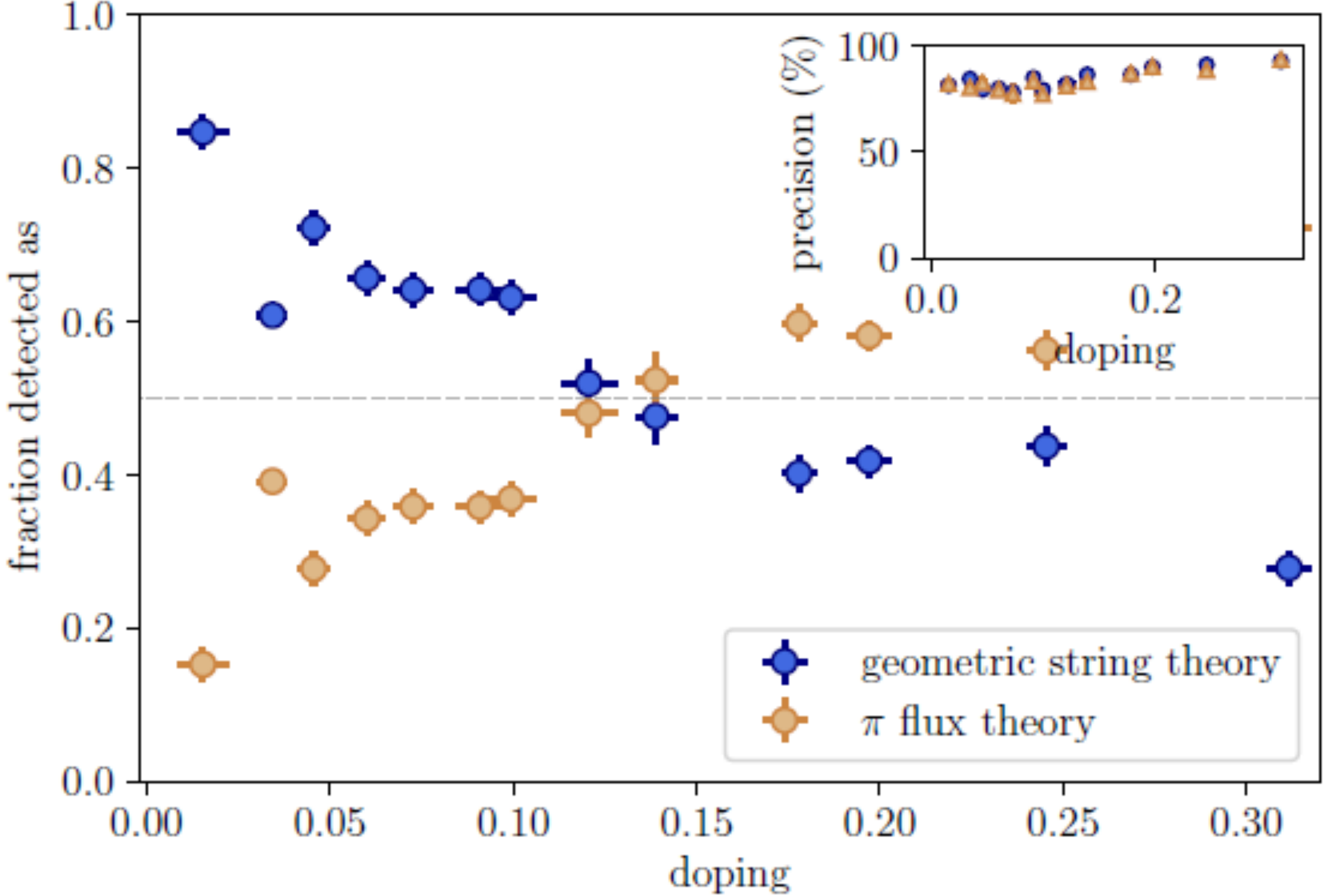




# Learning from theoretical predictions



# Classifying experimental data



[Bohrdt, et al. Nat. Physics 2019]

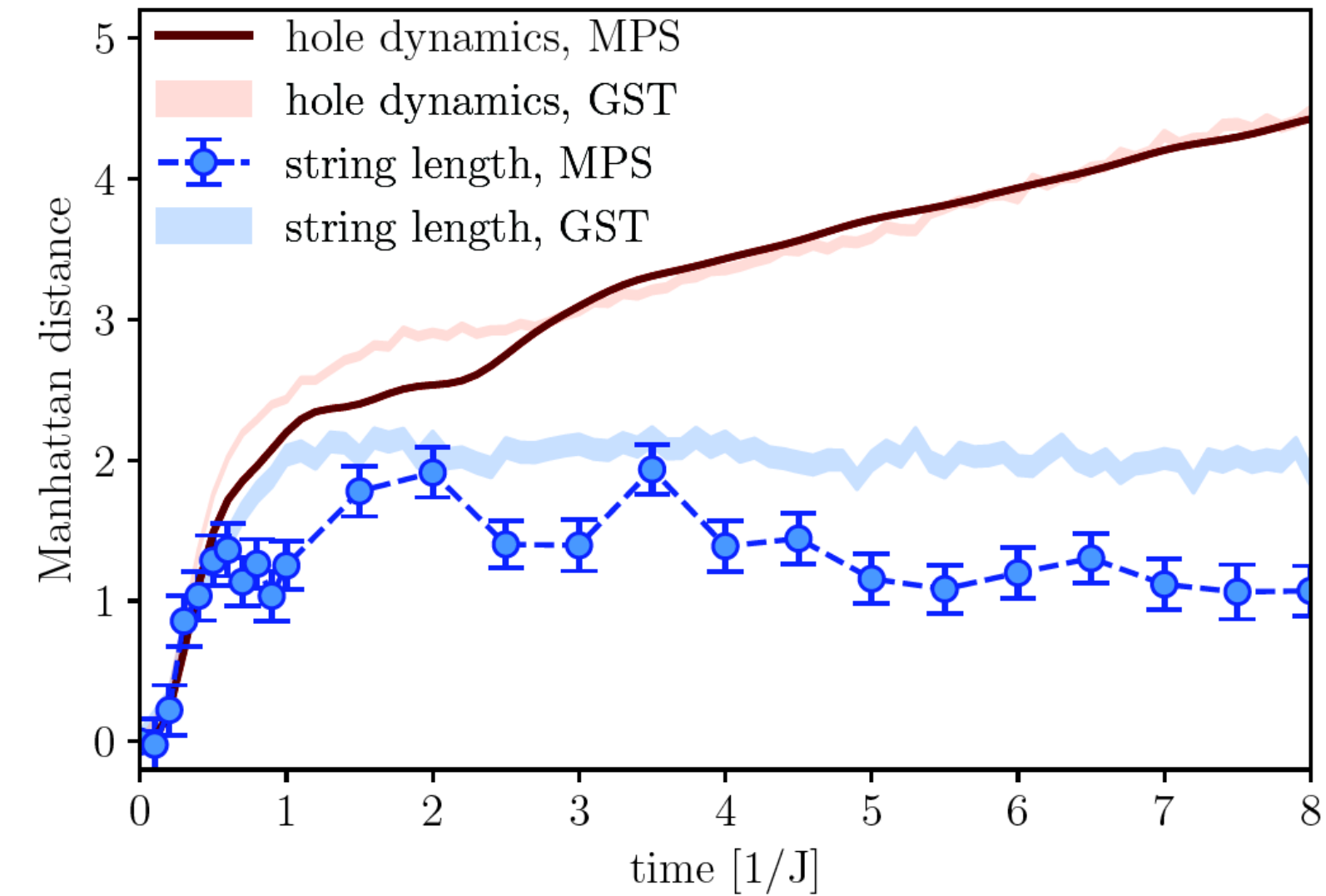
# Summary and Outlook

Parton picture: useful interpretation of hole in AFM

Neural Networks: a new route to analyze snapshots

Many open questions:

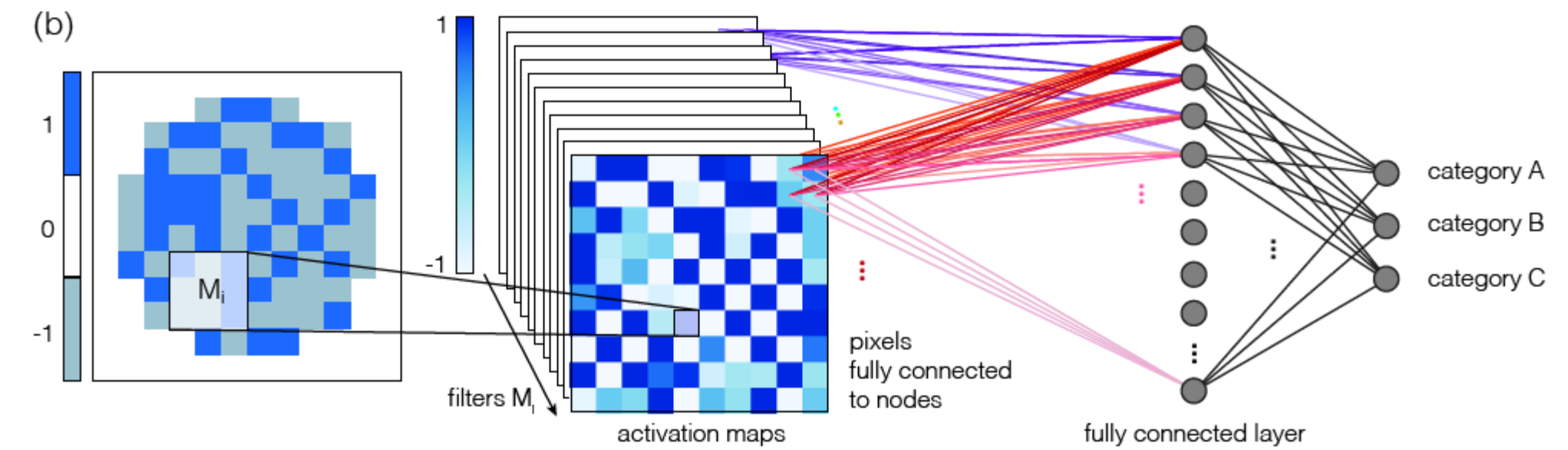
- Finite temperature?
- Dynamics of multiple holes?
- Frustrated quantum magnets?



[Bohrdt, Grusdt, MK, NJP 2020]

[Bohrdt, et al. PRB 2020]

[Bohrdt, et al. PRB 2018]



[Bohrdt, et al. Nat. Physics 2019]

[Chiu, Ji, Bohrdt, et al. Science 2019]