

WWU
MÜNSTER



A lattice QCD extraction of $B_s \rightarrow D_s^{(*)}$ form factors

Explorative study of the mass step-scaling method
with $N_f=2$

Based on [arXiv:2110.10061](https://arxiv.org/abs/2110.10061) (hep-lat)

Benoît Blossier, Pierre-Henri Cahue, Jochen Heitger, Simone LaCesa,
Jan Neuendorf* and Savvas Zafeiropoulos



The Form Factors

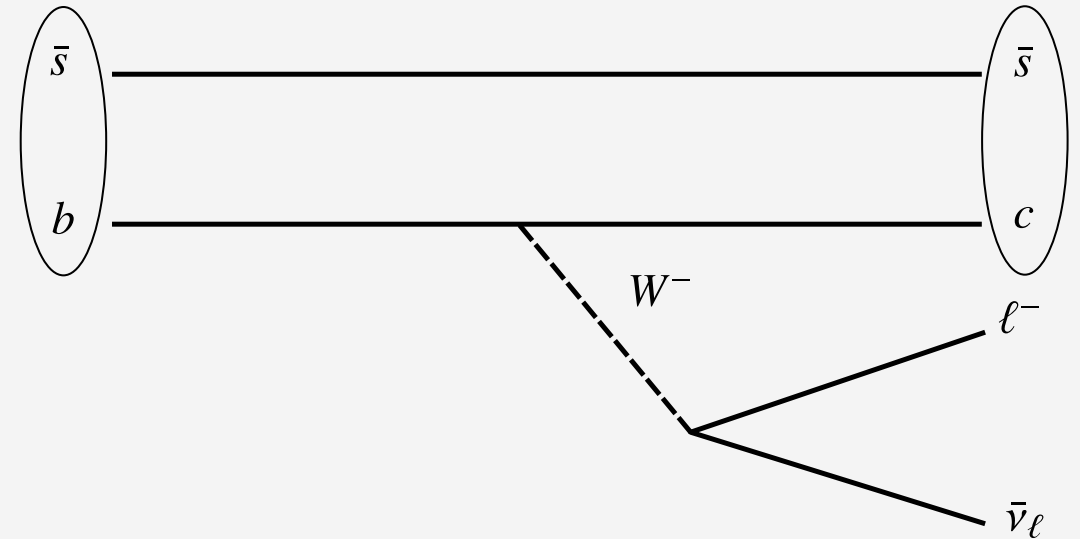
-Semileptonic decay.

-Strong and weak contributions.

$$\frac{d\Gamma_{B_s \rightarrow D_s}}{dw} \propto |V_{cb}|^2 \cdot |G(w)|^2$$

$$w = \frac{E_{D_s}}{m_{D_s}}$$

Can be extracted
from **Lattice QCD**.

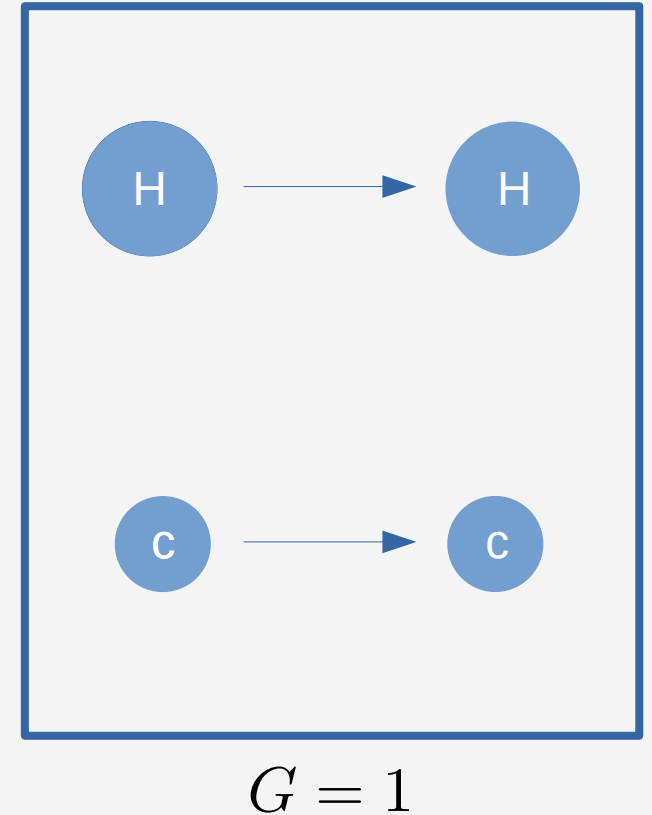
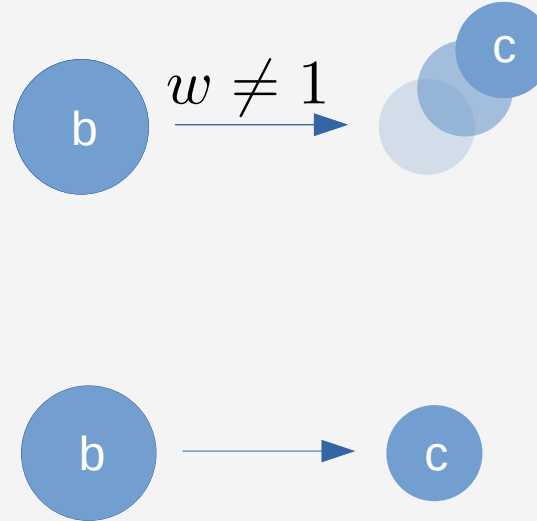


Schematic of the decay in question.

The Form Factors

- G only depends on w .
- We are interested in **zero recoil** ($w=1$)
- This is **not directly accessible** on the lattice.

$$\begin{aligned} &\langle D_s(k) | \bar{b} \gamma_\mu c | B_s(p) \rangle \\ &= A_\mu(p, k) G(w) + B_\mu(p, k) f_0(w) \end{aligned}$$

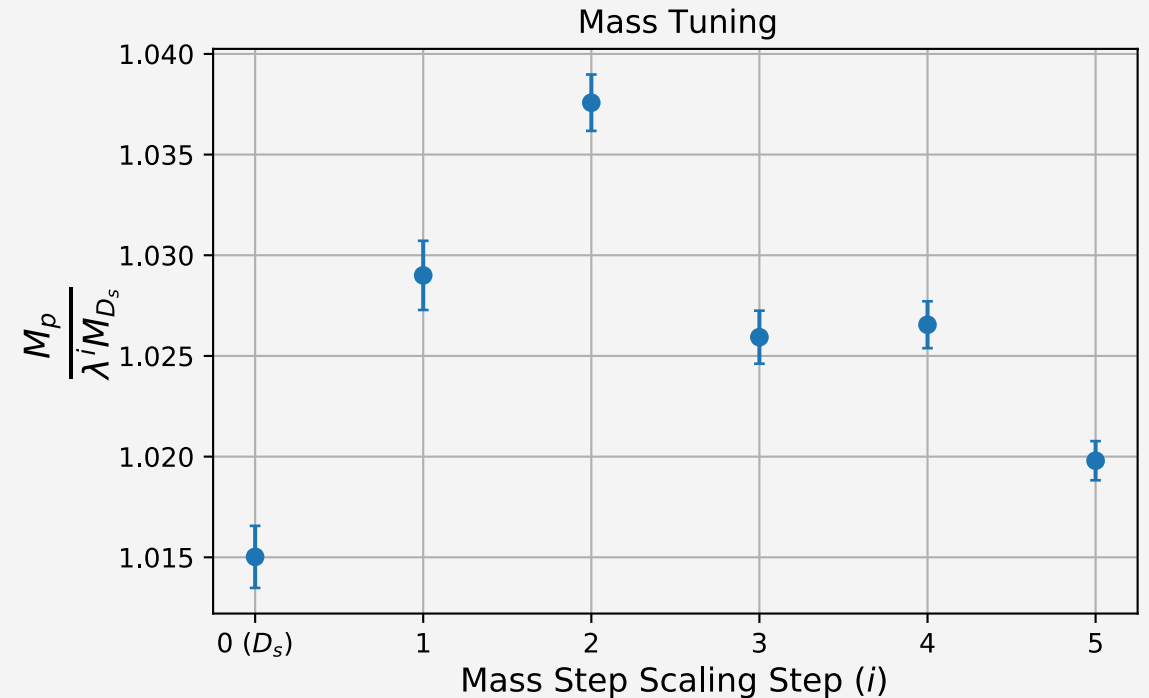


Mass Step-Scaling

- No measurements at b-scale (cutoff effects)
- Instead **extrapolation to B_s mass.**

$$m_{h_0s} = m_{D_s}$$

$$\frac{m_{h_{i+1}s}}{m_{h_i s}} = \lambda \quad \text{with} \quad \lambda = \sqrt[6]{\frac{m_{B_s}}{m_{D_s}}}$$



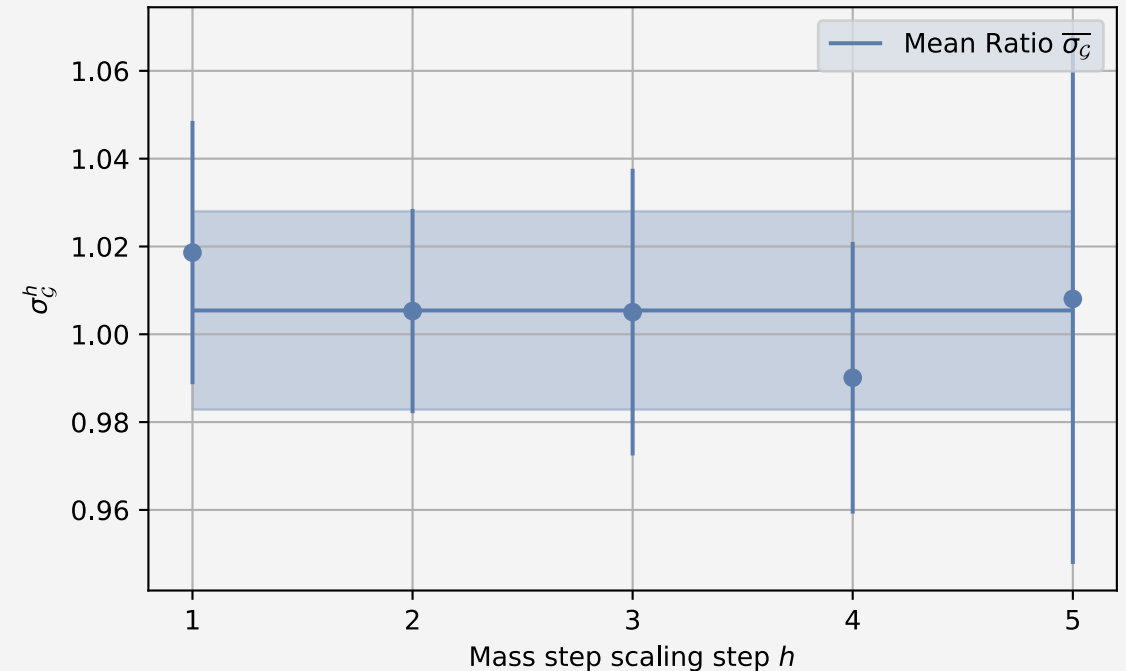
Example from one ensemble used in our analysis.

Mass Step-Scaling

-Only consider **ratios** of G 's between steps.

-Exploit $G=1$ for $D_s \rightarrow D_s$.

$$\begin{aligned}
 G^{B_s \rightarrow D_s}(w=1) &= G_{i=6}(1) \\
 &= \frac{G_6(1)}{G_5(1)} \cdot \frac{G_5(1)}{G_4(1)} \cdot \dots \cdot \frac{G_1(1)}{G_0(1)} \cdot G_0(1) \\
 &= \sigma_6 \cdot \sigma_5 \cdot \dots \cdot \sigma_1 \quad \text{with} \quad \sigma_i = \frac{G_i(1)}{G_{i-1}(1)}
 \end{aligned}$$



-Method used by M. Atoui et al. (arXiv: 1310.5238)

On the Lattice

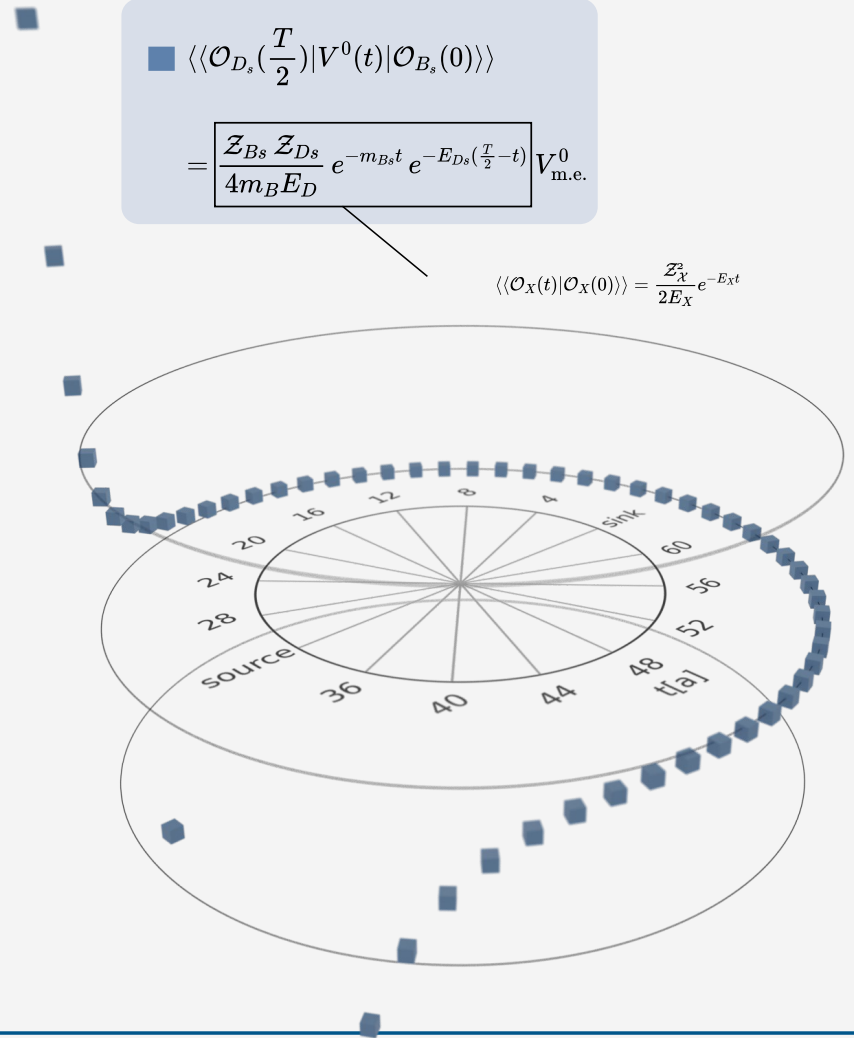
- Three point correlation function $\langle O_{H_2}(t_2)\Gamma(t_1)O_{H_1}(0) \rangle$
- Extract matrix element
- Twisted boundary conditions for (unquantized) momenta.

$$\Psi(x + L\vec{e}_i) = e^{i\theta_i} \Psi(x)$$

- 4x4 smeared sources.

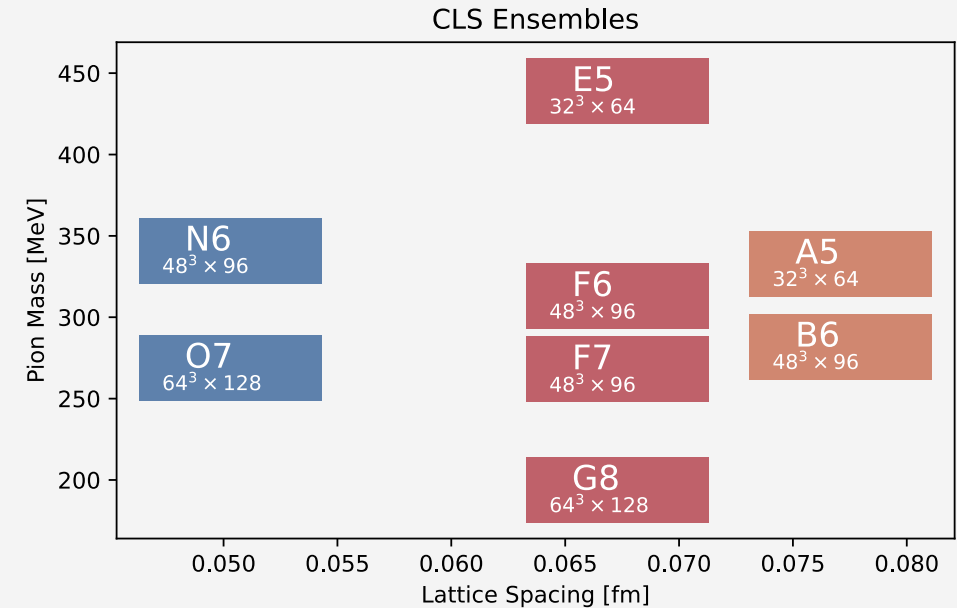
$$\begin{aligned} & \langle \langle \mathcal{O}_{D_s}(\frac{T}{2}) | V^0(t) | \mathcal{O}_{B_s}(0) \rangle \rangle \\ &= \frac{\mathcal{Z}_{B_s} \mathcal{Z}_{D_s}}{4m_B E_D} e^{-m_{B_s} t} e^{-E_{D_s}(\frac{T}{2}-t)} V_{\text{m.e.}}^0 \end{aligned}$$

$$\langle \langle \mathcal{O}_x(t) | \mathcal{O}_x(0) \rangle \rangle = \frac{\mathcal{Z}_x}{2E_x} e^{-E_x t}$$



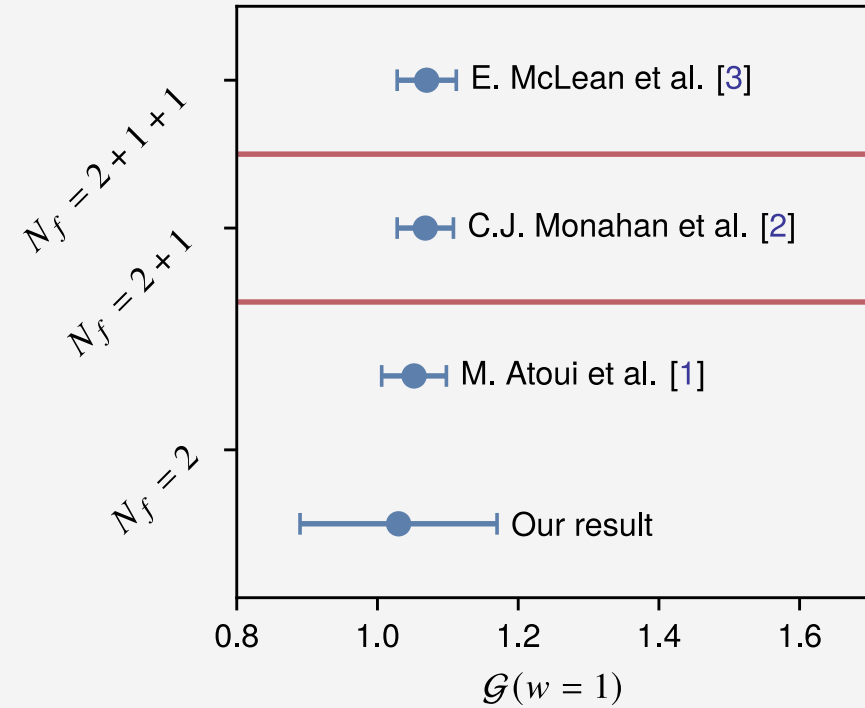
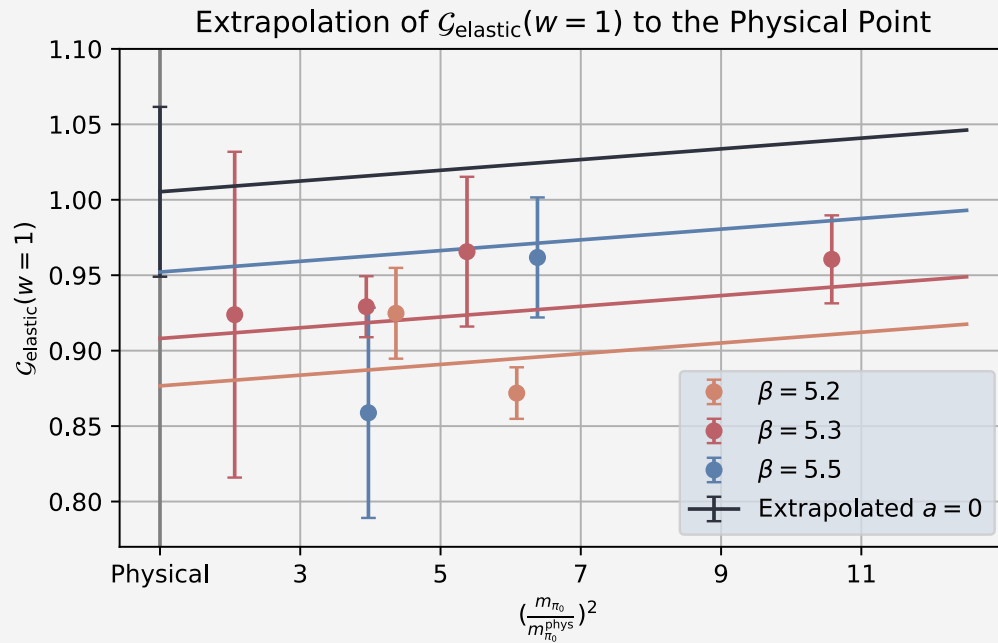
Analysis

- Get **ground state** projection.
- Masses** and amplitudes from **2pt correlators**.
- Extract **matrix element** and calculate G.
- Extrapolate to zero recoil (linear in $(w-1)$).
- Take ratios between masses.
- Extrapolate to the physical point.



Ensembles used in this analysis.

Results



- [1] M. Atoui, D. Becirevic, V. Morénas and F. Sanfilippo, *Lattice QCD study of $B_s \rightarrow D_s \ell \bar{\nu}_\ell$ decay near zero recoil*, *PoS LATTICE2013* (2014) 384, [1311.5071].
- [2] C. J. Monahan, H. Na, C. M. Bouchard, G. P. Lepage and J. Shigemitsu, *$B_s \rightarrow D_s \ell \nu$ Form Factors and the Fragmentation Fraction Ratio f_s/f_d* , *Phys. Rev. D* **95** (2017) 114506, [1703.09728].
- [3] E. McLean, C. T. H. Davies, J. Koponen and A. T. Lytle, *$B_s \rightarrow D_s \ell \nu$ Form Factors for the full q^2 range from Lattice QCD with non-perturbatively normalized currents*, *Phys. Rev. D* **101** (2020) 074513, [1906.00701].