

# Prompt $\eta_c$ hadroproduction, theoretical aspects

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# Outline

1. Why  $\eta_c$  ?
2. High-energy instability of the NLO cross section
3. High-Energy Factorization  $\Rightarrow$  resummation of  $\ln 1/z$
4. Reproducing NLO results at  $z \rightarrow 0$  from HEF, prediction for NNLO,
5. Matching HEF and NLO CPM calculations

# Do we understand anything about quarkonium production?

Understanding of hadronisation of the  $Q\bar{Q}$ -pair ( $Q = b, c$ ) into heavy quarkonium turned-out to be challenging theoretical/phenomenological problem. Do we understand which states of the  $Q\bar{Q}$ -pair are important?

**For some processes – yes!** The importance of the **color-singlet**  $Q\bar{Q}$ -state has been established:

- ▶ Photoproduction of prompt  $J/\psi$  at  $z < 0.9$  and not too small.
- ▶ Bulk of the double prompt hadroproduction of  $J/\psi$

and (somewhat unexpectedly...)

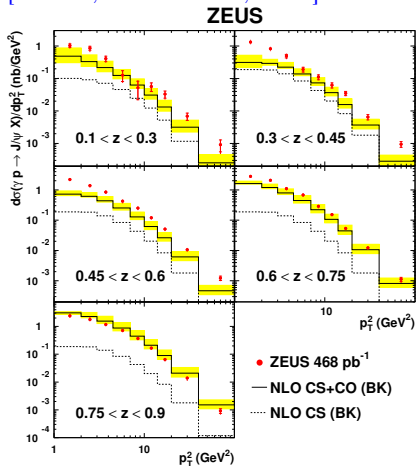
- ▶ Prompt  $\eta_c$  hadroproduction

Probability (=LDME) of hadronisation of the color-singlet  $Q\bar{Q}$ -pair to the physical state is  $\propto |R^{(')}(r=0)|^2$ , which is relatively well constrained, in comparison to CO LDMEs. **No free parameters!?**

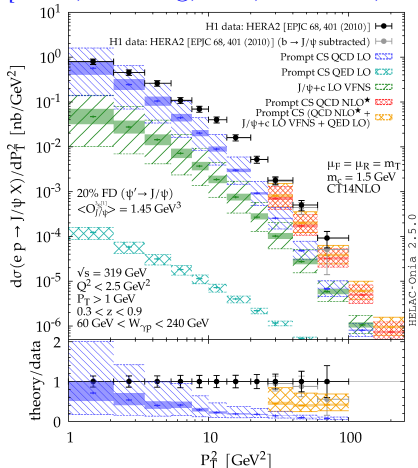
# Prompt $J/\psi$ photoproduction

Production of the  $c\bar{c} \left[ {}^3S_1^{(1)} \right]$ -state contributes up to a half of the cross section at “moderate” values of  $z = (p_{J/\psi} P)/(q_\gamma P)$ . As it should, no surprises here!

[Kniehl, Butenschön, 2012]



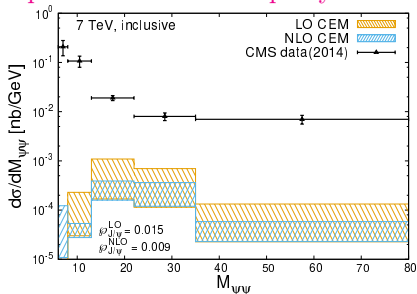
[Flore, Lansberg, Shao, Yedelkina, 2020]



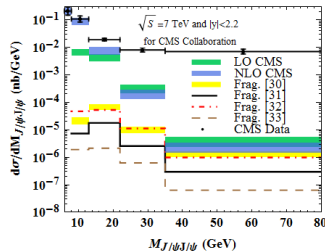
# Double prompt $J/\psi$ hadroproduction

NRQCD: “Double production of  $c\bar{c} \left[ {}^3S_1^{(1)} \right]$ -states dominates.”

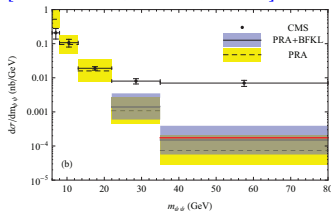
CEM: “All color, spin and  $L$ -states of  $c\bar{c}$  with  $M_{c\bar{c}} < 2m_D$  are created equal and hadronise equally...”



[Lansberg, Shao, Yamanaka, Zhang, Noûs, 2020]



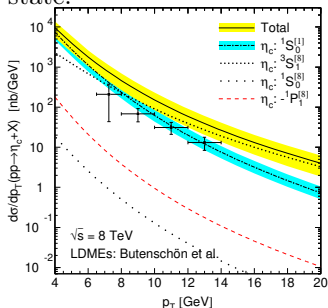
[Sun, Han, Chao, 2016]



[He, Kniehl, M.N., Saleev, 2019]

# Is $^1S_0^{(1)}$ -dominance in $\eta_c$ -production a bug or a feature?

The  $\eta_c$  hadroproduction was found to be dominated by the  $c\bar{c} \left[ ^1S_0^{(1)} \right]$  state:



[Butenschön, He, Kniehl, 2015]

This is a problem for NRQCD factorization, because roughly the same contribution of color-octet states as for  $J/\psi$  was expected.

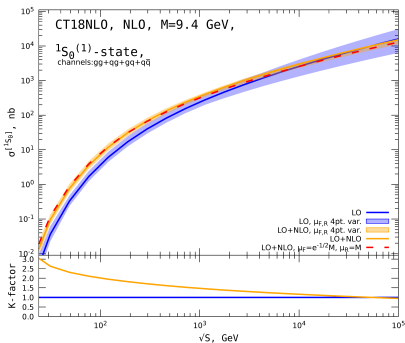
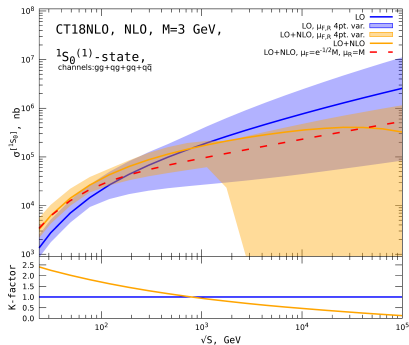
- Color-octet LDMEs for  $\eta_c$  are related (up to  $v^2$  corrections) to LDMEs of  $J/\psi$  by *heavy-quark spin symmetry* (long wavelength gluons do not “see” heavy quark spin). Strong HQSS violation?

- HQSS is quite “good” symmetry, manifests itself e.g. in hadron spectrum as closeness of  $D$  and  $D^*$  ( $B$  and  $B^*$ ) masses.

- **My speculation:** HQSS maybe inapplicable to production, because  $m_Q$  is not the largest scale in the problem. There is a lot of “soft” gluons with  $m_{c,b} \ll E_g \ll p_T$ .

# Is NLO QCD prediction for $\eta_c$ production perturbatively stable?

If we want to calculate the  $p_T$ -**integrated** total or  $y$ -differential cross section, then **NO**:



## Why?

**Collinear factorization** for total CS for the state  $m = 2S+1$   $L_J^{(0)}$ :

$$\sigma^{[m]}(\sqrt{S}) = \int_{z_{\min}}^1 \frac{dz}{z} \mathcal{L}_{ij}(z, \mu_F) \hat{\sigma}_{ij}^{[m]}(z, \mu_F, \mu_R),$$

where  $i, j = q, \bar{q}, g$ ,  $z = M^2/\hat{s}$  and *partonic luminosity*:

$$\mathcal{L}_{ij}(z, \mu_F) = \int_{-y_{\max}}^{+y_{\max}} dy \tilde{f}_i\left(\frac{M}{\sqrt{S}z}e^y, \mu_F\right) \tilde{f}_j\left(\frac{M}{\sqrt{S}z}e^{-y}, \mu_F\right),$$

with  $\tilde{f}_j(x, \mu_F)$  – momentum density PDFs.

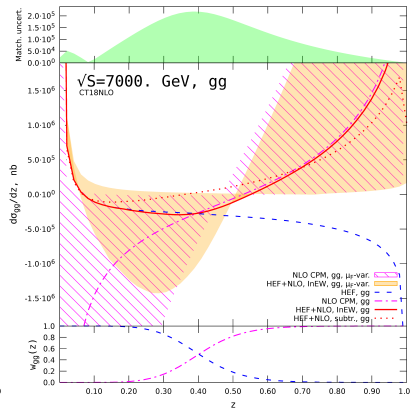
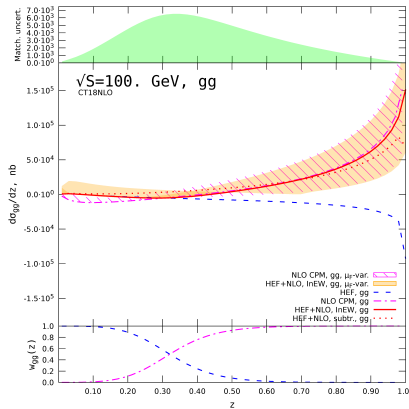
NLO coefficient function [Kuhn, Mirkes, 93'; Petrelli *et.al.*, 98'] in the  $z \rightarrow 0$  limit

$$\hat{\sigma}_{ij}^{[m]} = \sigma_{\text{LO}}^{[m]} \left[ A_0^{[m]} \delta(1-z) + C_{ij} \frac{\alpha_s(\mu_R)}{\pi} \left( A_0^{[m]} \ln \frac{M^2}{\mu_F^2} + A_1^{[m]} \right) + O(z\alpha_s, \alpha_s^2) \right],$$

where  $C_{gg} = 2C_A = 2N_c$ ,  $C_{qg} = C_{gq} = C_F = (N_c^2 - 1)/(2N_c)$ ,  $C_{q\bar{q}} = 0$  and  $A_1^{[m]} < 0$ .



# Why?

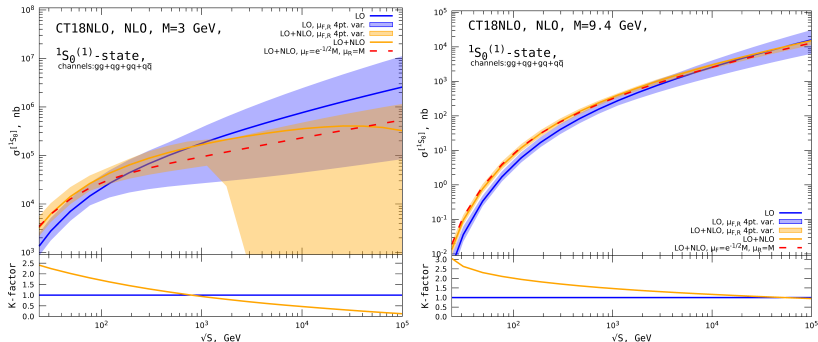


## Optimal $\mu_F$ choice?

It is natural to choose  $\mu_F$  such a way, that the negative  $A_1^{[m]}$  is cancelled [Lansberg, Ozelik, 2020]:

$$\hat{\mu}_F = M \exp \left[ \frac{A_1^{[m]}}{2A_0^{[m]}} \right],$$

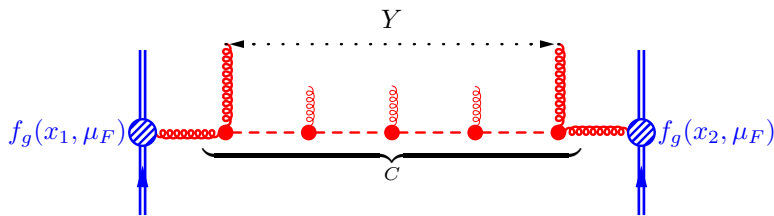
is equivalent to resummation of **some of the** terms  $\propto \alpha_s^n \ln^{n-1} \frac{1}{z}$  (more on this later). The result (red curve):



Is the systematic resummation of  $\propto \alpha_s^n \ln^{n-1} \frac{1}{z}$  possible?

# High-Energy factorization in a nutshell

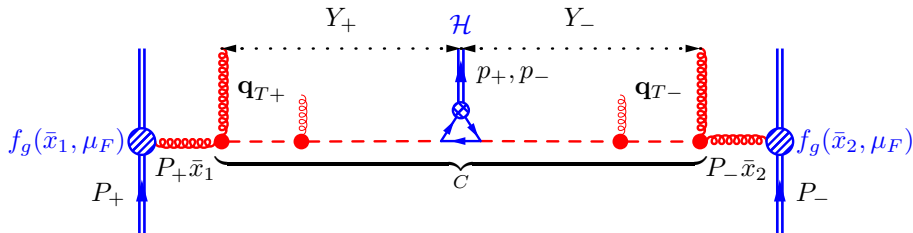
Reminder: Müller-Navelet dijet production ( $p_T$  of both jets is fixed):



Hard-scattering coefficient  $C$  contains higher-order corrections  $\propto (\alpha_s Y)^n$  (LLA) or  $\alpha_s (\alpha_s Y)^n$  (NLLA), which can be resummed at leading power w.r.t.  $e^{-Y}$  using [Balitsky-Fadin-Kuraev-Lipatov \(BFKL\)](#)-formalism.

# High-Energy factorization in a nutshell

High-Energy Factorization [Collins, Ellis, 91'; Catani, Ciafaloni, Hautmann, 91',94']:



Using the same formalism one can resum corrections to  $C$  enhanced by

$$Y_{\pm} = \ln \left( \frac{\mu_Y}{|\mathbf{q}_{T\pm}|} \frac{1 - z_{\pm}}{z_{\pm}} \right) \simeq \ln \frac{\mu_Y}{|\mathbf{q}_{T\pm}|} + \ln \frac{1}{z_{\pm}}, \text{ in LP w.r.t. } \frac{|\mathbf{q}_{T\pm}|}{\mu_Y} \frac{z_{\pm}}{1 - z_{\pm}}$$

in inclusive observables (e.g. inclusive quarkonium production). Here

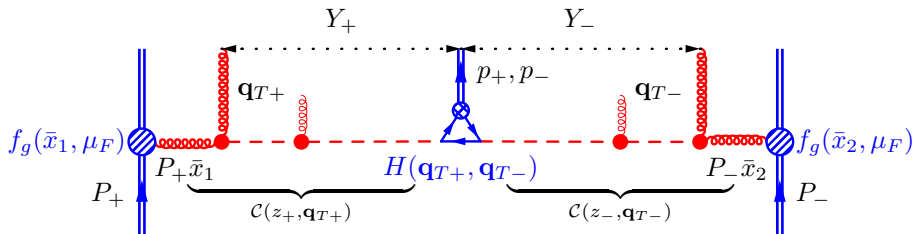
$$z_+ = \frac{p_+}{P_+ \bar{x}_1}, \quad z_- = \frac{p_-}{P_- \bar{x}_2} \text{ and } \mu_Y = p_+ e^{-y_H} = p_- e^{y_H},$$

e.g.  $\mu_Y^2 = m_{\mathcal{H}}^2 + \mathbf{p}_T^2$ . Connection with

$$z = \frac{M^2}{\hat{s}} = \frac{M^2}{M_T^2} z_+ z_-.$$

# High-Energy factorization in a nutshell

High-Energy Factorization [Collins, Ellis, 91'; Catani, Ciafaloni, Hautmann, 91',94']:



- ▶ Collinear divergences from additional emissions are subtracted inside UPDF.
- ▶ New coefficient function  $H$  depends on  $x_{1,2}$  as well as  $\mathbf{q}_{T\pm}$  ( $k_T$ -factorization).
- ▶ Factorization with single type of factors  $\mathcal{C}$  and  $H$  is proven at LL and NLL approximation [Fadin *et.al.*, early 2000s], and known to be violated at N<sup>2</sup>LL. Factorization with several types of  $\mathcal{C}$  and  $H$  should be introduced then.

## Resummed coefficient function

$$\begin{aligned}\hat{\sigma}_{ij}^{[m], \text{ HEF}}(z, \mu_F, \mu_R) &= \int_{-\infty}^{\infty} d\eta \int_0^{\infty} d\mathbf{q}_{T1}^2 d\mathbf{q}_{T2}^2 \mathcal{C}_{gi} \left( \frac{M_T}{M} \sqrt{z} e^{\eta}, \mathbf{q}_{T1}^2, \mu_F, \mu_R \right) \\ &\times \mathcal{C}_{gj} \left( \frac{M_T}{M} \sqrt{z} e^{-\eta}, \mathbf{q}_{T2}^2, \mu_F, \mu_R \right) \int_0^{2\pi} \frac{d\phi}{2} \frac{H^{[m]}(\mathbf{q}_{T1}^2, \mathbf{q}_{T2}^2, \phi)}{M_T^4},\end{aligned}$$

The coefficient functions  $H^{[m]}$  are known at LO in  $\alpha_s$  [Hagler *et.al*, 2000; Kniehl, Vasin, Saleev 2006] for  $m = {}^1S_0^{(1,8)}, {}^3P_J^{(1,8)}, {}^3S_1^{(8)}$ .

## LLA evolution w.r.t. $\ln 1/z$

In the LL( $\ln 1/z$ )-approximation, the  $Y = \ln 1/z$ -evolution equation for *collinearly un-subtracted*  $\tilde{\mathcal{C}}$ -factor has the form:

$$\tilde{\mathcal{C}}(x, \mathbf{q}_T) = \delta(1-z)\delta(\mathbf{q}_T^2) + \hat{\alpha}_s \int_x^1 \frac{dz}{z} \int d^{2-2\epsilon} \mathbf{k}_T K(\mathbf{k}_T^2, \mathbf{q}_T^2) \tilde{\mathcal{C}}\left(\frac{x}{z}, \mathbf{q}_T - \mathbf{k}_T\right)$$

with  $\hat{\alpha}_s = \alpha_s C_A / \pi$  and

$$K(\mathbf{k}_T^2, \mathbf{p}_T^2) = \delta^{(2-2\epsilon)}(\mathbf{k}_T) \frac{(\mathbf{p}_T^2)^{-\epsilon}}{\epsilon} \frac{(4\pi)^\epsilon \Gamma(1+\epsilon) \Gamma^2(1-\epsilon)}{\Gamma(1-2\epsilon)} + \frac{1}{\pi(2\pi)^{-2\epsilon} \mathbf{k}_T^2}.$$

It is convenient to go from  $(z, \mathbf{q}_T)$ -space to  $(N, \mathbf{x}_T)$ -space:

$$\tilde{\mathcal{C}}(N, \mathbf{x}_T) = \int d^{2-2\epsilon} \mathbf{q}_T e^{i\mathbf{x}_T \mathbf{q}_T} \int_0^1 dx x^{N-1} \tilde{\mathcal{C}}(x, \mathbf{q}_T),$$

because:

- ▶ Mellin convolutions over  $z$  turn into products:  $\int \frac{dz}{z} \rightarrow \frac{1}{N}$
- ▶ Large logs map to poles at  $N=0$ :  $\alpha_s^{k+1} \ln^{\textcolor{red}{k}} \frac{1}{z} \rightarrow \frac{\alpha_s^{k+1}}{N^{\textcolor{red}{k+1}}}$
- ▶ All *collinear divergences* are contained inside  $\mathcal{C}$  in  $\mathbf{x}_T$ -space.

# Collinear divergences

Exact (up to terms  $O(\epsilon)$ ) solution for  $\tilde{\mathcal{C}}$  can be obtained [Catani, Hautmann, 94]. It contains *collinear divergences*, which can be removed (absorbed into PDFs) in the  $\overline{MS}$ -scheme to all orders in  $\alpha_s$ :

$$Z_{\text{coll.}}^{-1} = \exp \left[ -\frac{1}{\epsilon} \int_0^{\hat{\alpha}_s S_\epsilon \mu_F^{-2\epsilon}} \frac{d\alpha}{\alpha} \gamma_{gg}(\alpha, N) \right], \quad S_\epsilon = \exp [\epsilon (\ln 4\pi - \gamma_E)],$$

$$\tilde{\mathcal{C}}(N, \mathbf{x}_T) = Z_{\text{coll.}}^{-1} \mathcal{C}(N, \mathbf{x}_T, \mu_F)$$



## Exact LL solution

In  $(N, \mathbf{q}_T)$ -space, subtracted  $\mathcal{C}$ , which resums all terms  $\propto (\hat{\alpha}_s/N)^n$  has the form:

$$\mathcal{C}(N, \mathbf{q}_T, \mu_F) = R(\gamma_{gg}(N, \alpha_s)) \frac{\gamma_{gg}(N, \alpha_s)}{\mathbf{q}_T^2} \left( \frac{\mathbf{q}_T^2}{\mu_F^2} \right)^{\gamma_{gg}(N, \alpha_s)},$$

where  $\gamma_{gg}(N, \alpha_s)$  is the solution of [Jaroszewicz, 82]:

$$\frac{\hat{\alpha}_s}{N} \chi(\gamma_{gg}(N, \alpha_s)) = 1, \text{ with } \chi(\gamma) = 2\psi(1) - \psi(\gamma) - \psi(1 - \gamma),$$

where  $\psi(\gamma) = d \ln \Gamma(\gamma) / d\gamma$  - Euler's  $\psi$ -function. The first few terms:

$$\gamma_{gg}(N, \alpha_s) = \underbrace{\frac{\hat{\alpha}_s}{N}}_{\text{DLA}} + \underbrace{2\zeta(3) \frac{\hat{\alpha}_s^4}{N^4} + 2\zeta(5) \frac{\hat{\alpha}_s^6}{N^6} + \dots}_{\text{LLA}}$$

The function  $R(\gamma)$  is

$$R(\gamma_{gg}(N, \alpha_s)) = 1 + O(\alpha_s^3).$$

## Doubly-logarithmic approximation

Taking the LO result for  $\gamma_{gg}(N, \alpha_s) \rightarrow \boxed{\gamma_N = \frac{\hat{\alpha}_s}{N}}$  we obtain:

$$\boxed{\mathcal{C}_{\text{DL}}(N, \mathbf{q}_T, \mu_F) = \frac{\gamma_N}{\mathbf{q}_T^2} \left( \frac{\mathbf{q}_T^2}{\mu_F^2} \right)^{\gamma_N},}$$

which resums  $\left( \frac{\hat{\alpha}_s}{N} \ln \frac{\mathbf{q}_T^2}{\mu_F^2} \right)^n \leftrightarrow \hat{\alpha}_s^n \ln^n \left( \frac{\mathbf{q}_T^2}{\mu_F^2} \right) \ln^{n-1} \left( \frac{1}{z} \right)$ .

In  $(z, \mathbf{q}_T)$ -space it is [\[Blümlein, 94'\]](#):

$$\mathcal{C}_{\text{DL}}(z, \mathbf{q}_T, \mu_F) = \frac{\hat{\alpha}_s}{\mathbf{q}_T^2} \begin{cases} J_0 \left( 2 \sqrt{\hat{\alpha}_s \ln \frac{\mu_F^2}{\mathbf{q}_T^2} \ln \frac{1}{z}} \right), & |\mathbf{q}_T| < \mu_F, \\ I_0 \left( 2 \sqrt{\hat{\alpha}_s \ln \frac{\mathbf{q}_T^2}{\mu_F^2} \ln \frac{1}{z}} \right), & |\mathbf{q}_T| > \mu_F, \end{cases}$$

where  $J_0/I_0$  is the Bessel function of the first/second kind.

**This approximation should be used with standard LO, NLO, NNLO PDFs, because DGLAP evolution is taken at fixed order (LO, NLO, NNLO).**

# Does this work?

The resummation has to reproduce the  $A_1^{[m]}$  NLO coefficient when expanded up to NLO in  $\alpha_s$ . And it does. We have performed expansion up to NNLO:

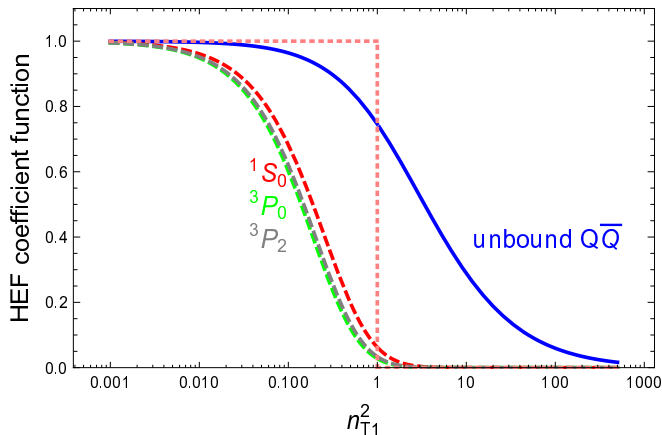
State	$A_0^{[m]}$	$A_1^{[m]}$	$A_2^{[m]}$	$B_2^{[m]}$
$^1S_0$	1	<b>-1</b>	$\frac{\pi^2}{6}$	$\frac{\pi^2}{6}$
$^3S_1$	0	1	0	$\frac{\pi^2}{6}$
$^3P_0$	1	<b><math>-\frac{43}{27}</math></b>	$\frac{\pi^2}{6} + \frac{2}{3}$	$\frac{\pi^2}{6} + \frac{40}{27}$
$^3P_1$	0	$\frac{5}{54}$	$-\frac{1}{9}$	$-\frac{2}{9}$
$^3P_2$	1	<b><math>-\frac{53}{36}</math></b>	$\frac{\pi^2}{6} + \frac{1}{2}$	$\frac{\pi^2}{6} + \frac{11}{9}$

for e.g.

$$\hat{\sigma}_{gg}^{[m], \text{HEF}}(z \rightarrow 0) = \sigma_{\text{LO}}^{[m]} \left\{ A_0^{[m]} \delta(1-z) + \frac{\alpha_s}{\pi} 2C_A \left[ A_1^{[m]} + A_0^{[m]} \ln \frac{M^2}{\mu_F^2} \right] \right. \\ \left. + \left( \frac{\alpha_s}{\pi} \right)^2 C_A^2 \ln \frac{1}{z} \left[ 2A_2^{[m]} + B_2^{[m]} + 4A_1^{[m]} \ln \frac{M^2}{\mu_F^2} + 2A_0^{[m]} \ln^2 \frac{M^2}{\mu_F^2} \right] + O(\alpha_s^3) \right\},$$

## Connection with $\hat{\mu}_F$

The HEF resummation **would be equivalent** to the  $\hat{\mu}_F$  prescription, if the HEF CF  $H^{[m]}(\mathbf{q}_{T1}^2, \mathbf{q}_{T2}^2 = 0)/M_T^4$  was  $\propto \theta(\hat{\mu}_F^2 - \mathbf{q}_{T1}^2)$ . But it is not:



# Matching with NLO of CF

The HEF works only at  $z \ll 1$ , misses power corrections  $O(z)$ , while NLO CF is exact in  $z$ , but only NLO in  $\alpha_s$ . **We need to match them.**

- ▶ Simplest prescription: just subtract the overlap at  $z \ll 1$ :

$$\sigma_{\text{NLO+HEF}}^{[m]} = \sigma_{\text{LO CF}}^{[m]} + \int_{z_{\min}}^1 \frac{dz}{z} \left[ \check{\sigma}_{\text{HEF}}^{[m],ij}(z) + \hat{\sigma}_{\text{NLO CF}}^{[m],ij}(z) - \hat{\sigma}_{\text{NLO CF}}^{[m],ij}(0) \right] \mathcal{L}_{ij}(z),$$

- ▶ Or introduce **smooth weights**:

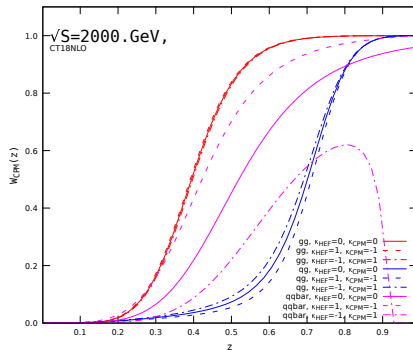
$$\sigma_{\text{NLO+HEF}}^{[m]} = \sigma_{\text{LO CF}}^{[m]} + \int_{z_{\min}}^1 dz \left\{ \left[ \check{\sigma}_{\text{HEF}}^{[m],ij}(z) \frac{\mathcal{L}_{ij}(z)}{z} \right] w_{\text{HEF}}^{ij}(z) + \left[ \hat{\sigma}_{\text{NLO CF}}^{[m],ij}(z) \frac{\mathcal{L}_{ij}(z)}{z} \right] (1 - w_{\text{HEF}}^{ij}(z)) \right\},$$

# Inverse error weighting method

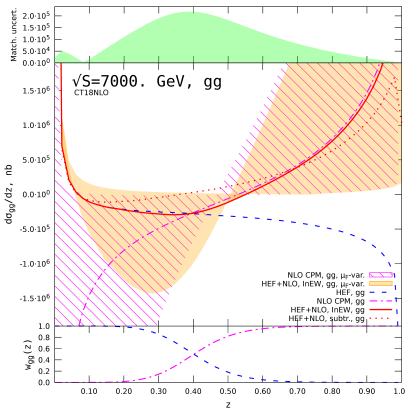
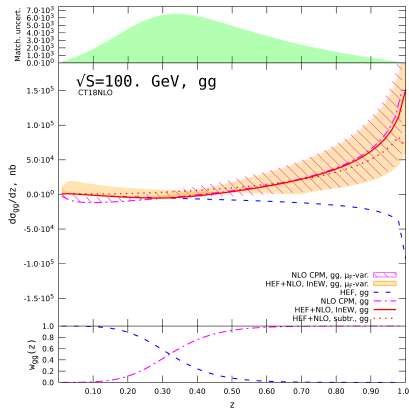
In the InEW method [Echevarria, *et.al.*, 2018] the weights are calculated from **estimates of the error** of each contribution:

$$w_{\text{HEF}}^{ij}(z) = \frac{[\Delta\sigma_{\text{HEF}}^{ij}(z)]^{-2}}{[\Delta\sigma_{\text{HEF}}^{ij}(z)]^{-2} + [\Delta\sigma_{\text{CF}}^{ij}(z)]^{-2}},$$

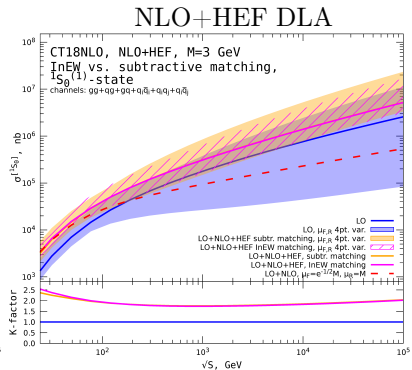
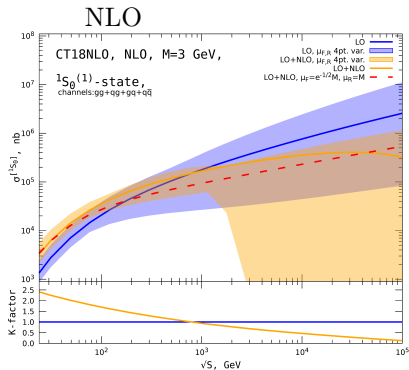
- For  $\Delta\sigma_{\text{CF}}$  we take the  $\alpha_s^2 \ln \frac{1}{z}$  term obtained from HEF  $+O(\alpha_s^2)$ -term which we vary.
- For  $\Delta\sigma_{\text{HEF}}$  we take the  $\alpha_s O(z)$  part of the NLO CF result  $+O(\alpha_s^2)$ -term which we vary.



# Matching plots

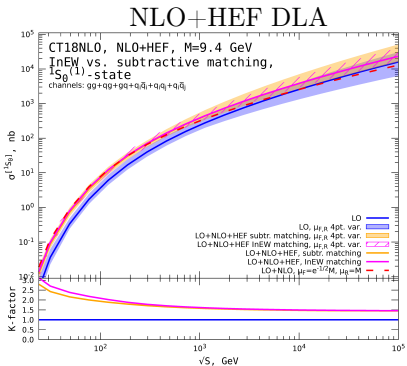
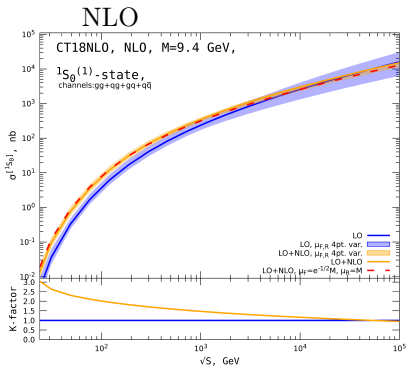


# Matched results for $\eta_c$

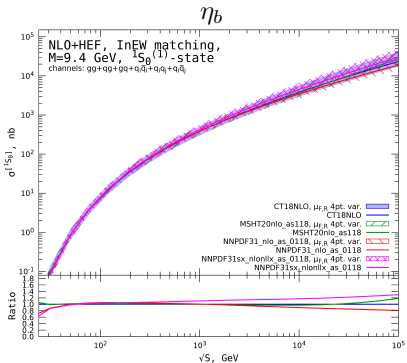
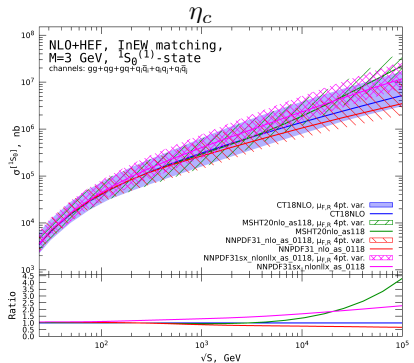




# Matched results for $\eta_b$



# The PDF dependence



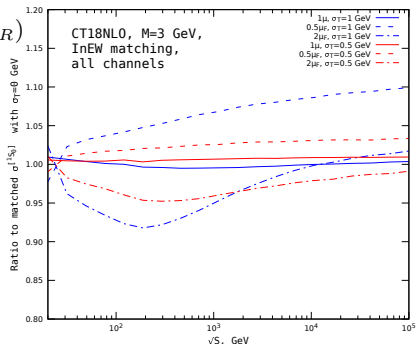
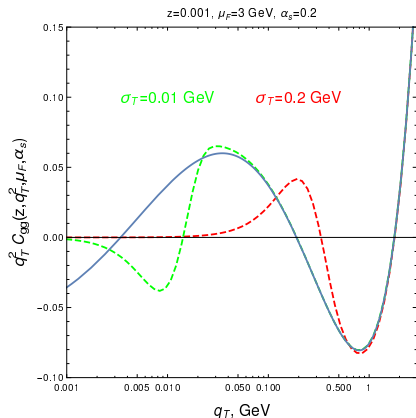
## Intermediate conclusions

- ▶ The high-energy instability of the NLO cross section is related with lack of the  $\alpha_s^n \ln^{n-1} \frac{1}{z}$  corrections in  $\hat{\sigma}(z)$  at  $z \ll 1$ .
- ▶ The HEF at DLA is the formalism to solve this problem if the standard fixed-order PDFs are to be used.
- ▶ Matching between NLO CF (finite  $z$ ) and HEF ( $z \ll 1$ ) has to be performed, but there is no strong sensitivity to matching procedure.
- ▶ Scale-uncertainty is reduced, the  $K$ -factor is flat at high energy. But the uncertainty of NLO CF+DLA HEF calculation is still too large.
- ▶ NLO CF+NLL HEF calculation is in progress.
- ▶ Future plans:  $y$ -distributions, production of  $\chi_{cJ}$ , photoproduction...

# Higher-twist effects

Convolution of  $\mathcal{C}$ -factor with the Gaussian in  $\mathbf{k}_T$ :

$$\int \frac{d^2 \mathbf{k}_T}{\pi \sigma_T^2} \exp \left[ -\frac{\mathbf{k}_T^2}{\sigma_T^2} \right] C_{gg}^{\text{DLA}}(z, (\mathbf{q}_T + \mathbf{k}_T)^2, \mu_F, \mu_R)$$



The correction is  $O(\sigma_T^2/M^2)$ , so it is **higher twist effect**.

# Photoproduction case

$$\sigma_{\gamma p} = \int dx f_i(x, \mu_F) \hat{\sigma}_{i\gamma}(\eta),$$

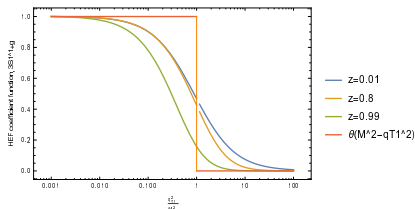
where  $\boxed{\eta = \frac{\hat{s}}{M^2} - 1}$  with  $\hat{s} = S_{\gamma p} x$ . Resummed partonic cross section:

$$\hat{\sigma}_{i\gamma}^{\text{HEF}}(\eta) = \frac{1}{2zM^2} \int_{1/z}^{1+\eta} \frac{dy}{y} \int_0^\infty d\mathbf{q}_T^2 C_{gi} \left( \frac{y}{\eta+1}, \mathbf{q}_T^2, \mu_F, \mu_R \right) \mathcal{H}(y, \mathbf{q}_T^2),$$

where  $\mathcal{H}$  is the integral of the HEF coefficient function for the process:

$$R(\mathbf{q}_T) + \gamma(q) \rightarrow c\bar{c} \left[ {}^3S_1^{(1)} \right] + g(k),$$

over the PS of the gluon.

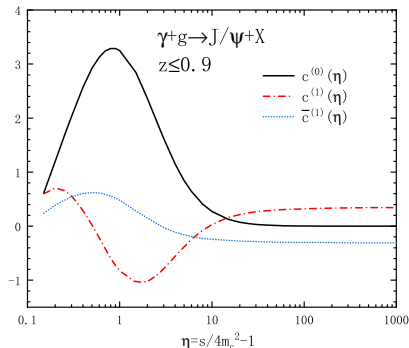


# Asymptotics $\hat{\sigma}(\eta \rightarrow \infty)$

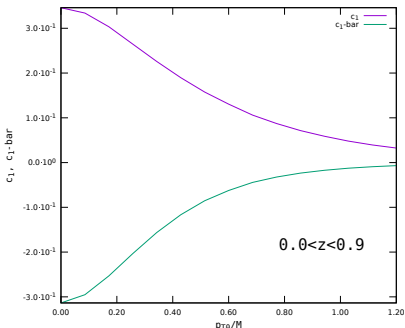
[Kraemer, 1995]:

$$\hat{\sigma}_{i\gamma} \propto c_{i\gamma}^{(0)}(\eta) + 4\pi\alpha_s \left[ c_{i\gamma}^{(1)}(\eta) + \bar{c}_{i\gamma}^{(1)}(\eta) \ln \frac{\mu_F^2}{m_c^2} + \frac{\beta_0}{8\pi^2} c_{i\gamma}^{(0)}(\eta) \right]$$

Numerical NLO result



$c^{(1)}$  and  $\bar{c}^{(1)}$  at  $\eta \rightarrow \infty$  from HEF as function of  $p_{T\min}^{J/\psi}$



Thank you for your attention!