New microscopic model for production of J/psi and other charmonia in heavy ion collisions

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Diversity in the dissociation rate



EMMI RRTF on QUARKONIA (Dec 2019)

See <u>https://indico.gsi.de/event/9314/overview</u> and manuscript in preparation

Several motivations to go microscopic

- The in-medium quarkonia are not born as such. One needs to develop an initial compact state to fully bloomed quarkonia
- The dissociation-recombination reactions affecting quarkonia are not instantaneous.
- In dense medium, the notion of cross section should be replaced by the more rigorous open-quantum system approach
- Better suited for « from small to large »
- Extra complication: For RHIC and LHC : many c-cbar pairs !



Pioneering work of **Blaizot and Escobedo** for many c-cbar pairs (NRQCD) => mixed Fokker-Planck + gain/loss rates for color transitions; awaits for implementation in realistic conditions **4**

Conclusions

Charmonia in a transport model

Conclusions

Charmonia in a microscopic theory Several regimes / effects

Well identified formalisms (Quantum Master Equation, Boltzmann transport, Stochastic equations,...) in well identified regimes, but continuous evolution and no unique framework continuously applicable (to my knowledge)

Yet, still a need to define the equivalent of a formation – dissociation rate

Remler's formalism for dynamical coalescence

Generic idea : describe charmonia (Ψ) production using density matrix

$$P^{\Psi}(t) = \operatorname{Tr} \left[\hat{\rho}_{Q\bar{Q}}^{\Psi} \hat{\rho}_{N}(t) \right]$$

 $\hat{\rho}_{Q\bar{Q}}^{\Psi_{i}}=\sum_{i}|\Psi_{Q\bar{Q}}^{i}\rangle\langle\Psi_{Q\bar{Q}}^{i}|$

Single quarkonia density operator

"Just" looking at the initial stage brings interesting features:

Good reproduction of pp -> J/ ψ + x !!!

 N-body density matrix (bulk partons + many c and many cbar)

> Taesoo .S, J.Aichelin and E.Bratkovskaya , PRC 96. 014907 (2017)

considerable enhancement of primordial J/ ψ (in the **initial** state): **large off-diagonal contributions**

$\begin{aligned} \mathbf{A} \ & \text{bit of background} \\ P^{\Psi}(t) = \mathrm{Tr} \begin{bmatrix} \hat{\rho}_{Q\bar{Q}}^{\Psi} \hat{\rho}_{N}(t) \end{bmatrix} \\ \hat{\rho}_{Q\bar{Q}}^{\Psi_{i}} = \sum_{i} |\Psi_{Q\bar{Q}}^{i}\rangle \langle \Psi_{Q\bar{Q}}^{i}| \qquad \underbrace{\frac{\partial \rho_{N}(t)}{\partial t}}_{\partial t} = -i[H_{N}, \rho_{N}(t)] \end{aligned}$

Dealing with the dynamics ?

- The idea of the formalism goes back to Remler's work
- General scheme connecting composite-particle cross section and rates with time-dependent density operators
- Applied by Remler et al to the deuteron production in (low energy) AA collisions. The formalism is able to deal with many particles (nucleons -> deuterium)

E.A. Remler, ANNALS OF PHYSICS 136, 293-316 (1981)

[2020,...

Apply Remler formalism to quarkonia production in heavy ion collisions (Arrebato, Aichelin & Gossiaux, 2206.01308)

Lessons from the past : the direct calculation is not effective for codes based on "cascade approach" (for which members of a genuine fragment are found far apart in the final stage)

Use the identity $P^{\Psi}(t) = P^{\text{prim}}(t_0) + \int_{t_0}^t \Gamma^{\Psi}(t') dt'$

 Γ is The effective rate for quarkonia state creation (dissociation) in the medium : •

$$\Gamma^{\psi}(t) = \frac{dP^{\Psi}(t)}{dt} = \operatorname{Tr}\left[\hat{\rho}_{Q\bar{Q}}^{\Psi} \frac{d\hat{\rho}_{N}(t)}{dt}\right]$$

 $P^{\text{prim}}(t_0)$ is the production at initial time (*primordial*)

Then : Von Neumann equation + Hamiltonian composed of 2-body interactions

Total interaction of Q and Qbar with all light partons

Can be modelled resorting to Wigner transforms :

$$\begin{split} W^{\Psi}_{Q\bar{Q}}(r_{\rm rel},p_{\rm rel}) &= C e^{r_{\rm rel}^2 \sigma^2} \times e^{\frac{p_{\rm rel}^2}{\sigma^2}} & \text{Approx Wigner transform for } \Psi(\text{1S}) \\ W_N &= \Pi_i \hbar^3 \delta(x_i - x_{i0}(t)) \delta(p_i - p_{i0}(t)) & \text{Semi-classical approximation} \\ & \text{for N-body density} & \text{grade} \end{split}$$

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Conclusions

Remler formalism at work

Combining the expression of the Wigner's functions and substituting in the **effective rate equation** :

 $\Gamma^{\Psi}(t) = \sum_{i=1,2} \sum_{j\geq 3} \delta(t-t_{ij}) \int \frac{d^3 p_i d^3 x_i}{h^3} W^{\Psi}_{Q\bar{Q}}(p_1, x_1; p_2, x_2) \left[W_N(t+\epsilon) - W_N(t-\epsilon) \right]$

- The quarkonia production in this model is a three body process, the HQ (anti-quark) interact only by collision !!!
- The "details" of H_{int} between HQ and bulk partons are incorporated into the evolution of W_N after each collision / time step (nice feature for the MC simulation)
- $W_N(t+\epsilon)$ and $W_N(t-\epsilon)$ are NOT the equivalent of gain and loss terms in usual rate equation
- Dissociation and recombination treated in the same scheme

Then:
$$P^{\Psi}(t) = P^{\Psi}(t_0) + \int_{t_0}^t \Gamma(t') dt'$$

NB: Also possible to generate similar relations for differential rates

for D and B mesons production)

Interaction of HQ with the QGP are

carried out by EPOSHQ (good results

Extension of the Remler formalism

- Generalization to relativistic Wigner density (boosted quarkonium states)
- Extra source of Γ due to "local-T" basis evolution with time : Γ^{loc}
- Confining $Q\bar{Q}$ forces inside the MC evolution ; large impact on the # of close pairs... and correlated trajectories.

The dynamics of c-cbar correlation

- The c-cbar potential (« pot ») leads to a huge increase of the c-cbar at close distance at large times (not a random Poisson distribution)...
- ... Especially when the collisions with the QGP (« coll ») are switched ON as well

We do not have J/ ψ quasi particles in our approach, just correlated c-cbar trajectories

Conclusions

Results : J/ ψ production vs time

- Without interaction potential between c and cbar, the collisions with the medium manage to destroy the native J/ψ .
- With the interaction potential between c and cbar « on », one observes a steady rate of J/ ψ creation (reduction of Γ^{col} , increase of Γ^{local})... No adiabaticity, but no instantaneous formation either.

Conclusions

Results : J/ψ production vs p_T

- Equivalent pp production (the denominator of the R_{AA}) : c-cbar according to FONLL² without any correlation, then coalescence with the Wigner distribution.
- No feed-down from higher states (to be implemented)
- Acceptable for p_T < 5 GeV/c, but deviations for higher p_T.
- To investigate : more appropriate scheme for c-cbar production, including c-cbar correlation.

Results : J/ψ production vs p_T

- Dynamical recombination is quite effective at low $\ensuremath{p_{\text{T}}}$
- At higher p_T , we are missing J/ ψ as compared to the experimental value.
- Several possible reasons, under investigation... in terms of transport model : « as if the primordial was too much suppressed »

Conclusions

- V_2 excess as compared to experimental data (late formation of the J/ ψ due to binding potential under restoration)
- The « diagonal » contribution shows no difference wrt the full production, what is a bit conter-intuitive

- Most of the transport models have considered up to now that primordial charmonia can just be destroyed (with a small probability), but not deflected.
- In our approach, we have investigated the consequences of considering the opposite limit... with somehow too large v₂ resulting from this prescription...

Conclusions and Perspectives

- First move towards a microscopic approach based on individual c and cbar dynamics implementing some of the open quantum systems features for charmonia production in realistic HI conditions : dynamical coalescence
- Encouraging results, but still many issues
- Rooms for improvement :
 - Including color transparency (preliminary results can be shown this afternoon) and more generally color dynamics
 - More reliable treatment of the fully relativistic evolution of a Nbody coupled system (under construction)
 - \circ More realistic « initial state » for the c-cbar pairs, including correlations at intermediate p_T .

Back up

A central quantity: the decay rate Γ

Several approaches

pQCD view (Bhanot & Peskin), later on consolidated by NRQCD (Brambilla & Vairo)

QFT/Lattice QCD

Time correlator

$$\left|\mathcal{C}_{>}(t,\vec{r})\approx\langle\psi(t,\frac{\vec{r}}{2})\bar{\psi}(t,-\frac{\vec{r}}{2})\psi(0,0)\bar{\psi}(0,0)\rangle\right|$$

Satisfies Schroedinger equation with imaginary potential iW . Breakthrough by Laine et al. (2006)

$$\Gamma_{\Phi}(T) = -2\langle \Phi | W | \Phi \rangle$$

Prob survival
$$= \exp\left(-\int_{t_0}^{t_{\text{fin}}} \Gamma(T(t)) dt\right)$$

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Suppression of the bottomonium « candle »

- $b\bar{b}$ \Rightarrow Less shadowing
 - Less final state effect

Allows to probe the internal potential...

Suppression of the bottomonium « candle »

 $0.6_{\rm F}$ Real Part Binding Energy [GeV] Y(1s) Imaginary Part 0.5 0.4593 MeV 0.30.2 50 Me 0.1 04 200 400 500 T [MeV] 600 7000.2Binding Energy [GeV] Y(2s)120 MeV Real Part Imaginary Part 0<u>h</u> 200 400 500 T [MeV] 600 700 300 Resulting decay rate $\Gamma_{T} = -2 \text{ Im}[\text{E}_{\text{bind}}]$

Strickland et al.

 $b\bar{b} \Rightarrow \bullet$ Less shadowing

• Less final state effect

B. Krouppa, R. Ryblewski, and M Stickland, Phys. Rev. C 92, 061901(R) (2015).

... as well as QGP viscosity

Schematic summary of approaches

Initial quasi stationary Sequential Suppression

assumption (Matsui & Satz 86) Final quasi "instantaneous" Statistical Hadronisation assumption

(Andronic, Braun-Munzinger & Stachel)

Dynamical Models (aims at quantifying the degree of equilibration above Tc relying on kinetic rates and/or (in-medium) cross sections • Prob survival = $\exp\left(-\int_{t_0}^{t_{fin}} \Gamma(T(t))dt\right)$

(Rapp et alS : TAMU, Zhuang, Nantes,...)

Nowadays, all state-of-the art dynamical models include both suppression and recombinaison, although not always consistently

???

Quantum coherence

Picture behind transport theory :

Open heavy flavor and quarkonia assumed to be uncorrelated

Formed after some "formation time" τ_f (typically the Heisenberg time), usually assumed to be independent of the surrounding medium

Common belief in the transport community:

Quarkonia initially « formed » in QGP and survive with an *individual* survival probability

$$S(t) = e^{-\int_{\tau_f}^t \Gamma(T(t'))dt'}$$

Extra Motivations

Spectral density

David Lafferty, Alexander Rothkopf, Phys. Rev. D 101, 056010 (2020)

How justified is it to deal with the quantum evolution of such state with cross sections, meant to describe the reactions of asymptotic states ?

Quantum coherence

How to proceed ?

 J/ψ are *quantum* bound states => need for a formalism that preserves *quantum* properties... and continuous transitions between bound and unbound states

Passing to the Wigner representation:

$$\begin{split} W_{N}(\{r\},\{p\}) &= \int \Pi d^{3}y e^{ipy} \langle r - \frac{y}{2} | \hat{\rho}_{N} | r + \frac{y}{2} \rangle \\ \text{Direct space} & \text{Wigner space....} \\ \partial \rho_{N}(t) / \partial t &= -i \Sigma_{j} [K_{j}, \rho_{N}(t)] \\ -i \Sigma_{j > k} [V_{jk}, \rho_{N}(t)] & \partial W_{N}(t) / \partial t &= \langle \Sigma_{i} v_{i} \cdot \partial_{r} W_{N}(\mathbf{r}, \mathbf{p}, t) \rangle + \\ \langle \Sigma_{i \geq j} \Sigma_{n} \delta(t - t_{ij}(n)) \times \\ (W_{N}(\mathbf{r}, \mathbf{p}, t + \epsilon) - W_{N}(\mathbf{r}, \mathbf{p}, t - \epsilon)) \rangle \\ \text{One to one correspondance} \\ \text{... treated at the semi-classical level :} \end{split}$$

Wigner distribution 🗇 {trajectories in phase space}

 $\hat{U}_1 + \hat{U}_2, \hat{
ho}_N(t)$ can be modelized from the trajectories evolution in Wigner space

The effective rate for quarkonia state creation (dissociation) in the medium is

$$\Gamma^{\Psi}(t) = -iTr[\hat{\rho}^{\Psi}[\hat{U}_1 + \hat{U}_2, \hat{\rho}_N(t)]]$$

Working in the phase space through Wigner distribution $W^{\Psi_i}_{Q\bar{Q}} = \int d^3y e^{ipy} \langle r - \frac{y}{2} | \Psi^i \rangle \langle \Psi^i | r + \frac{y}{2} \rangle$

Quarkonia: Double Gaussian approximation $W^{\Psi}_{Q\bar{Q}}(r_{\rm rel}, p_{\rm rel}) = Ce^{r_{\rm rel}^2 \sigma^2} \times e^{\frac{p_{\rm rel}^2}{\sigma^2}} V$

Parameter: The Gaussian width $\sigma\approx$ 0.35 fm

$$[\frac{\hbar^2}{2\mu}\nabla^2 + V(r)]\Psi_{Q\bar{Q}}(r) = E_{Q\bar{Q}}\Psi_{Q\bar{Q}} \longrightarrow \langle r^2 \rangle \longrightarrow W^{\psi}$$

W_N : Semi-classical approach

$$W_N = \Pi_i \hbar^3 \delta(x_i - x_{i0}(t)) \delta(p_i - p_{i0}(t))$$

... but no explicit description of $W_{\rm N}$ required (as it appears in the trace)

and (less trivial) : generalisation at finite 4-velocity u; fully relativistic... to warrant orthogonality of states $Tr[W_{u}^{J/\psi}W_{v'}^{\psi'}] = 0$

Preliminary results for J/ ψ production in Pb-Pb

First answer to puzzle found in Song et al: the primordial production is killed rather fast by the « loss » rate.

Remler formalism for the QGP : last ingredient

<u>Combining the rate definition + VN equation</u>: $\Gamma^{\Psi}(t) = -iTr[\rho^{\Psi}[H_N, \rho_N(t)]]$ $\blacksquare H_N = H_{1,2} + H_{N-2} + U_1 + U_2$ 1 t] $car{c}$ Internal Hamiltonian In QGP, 2 body T-dependent effective potential => $\Gamma^{\Psi}(t) = -iTr[\rho^{\Psi}[H_N, \rho_N(t)]] = -iTr[\rho_N(t)[\rho^{\Psi}, H_N]]$ $[\rho^{\Psi}, H_{1,2}(T)] = 0$ $= -iTr[\hat{\rho}^{\Psi}(T)[\hat{U}_1 + \hat{U}_2, \hat{\rho}_N(t)]] \label{eq:constraint} \begin{array}{l} \text{One only preserves the structure of the} \\ \text{Remler } & \text{collisional rate } & \text{if one works in the} \end{array}$ « local » basis ρ^{Ψ} (T) !!! Accessible for T > T_{dissoc}^{Ψ} (=0.4 GeV for J/ ψ) Back to the rate : $\Gamma^{\Psi}(t) = \frac{dP^{\Psi}(t)}{dt} = \operatorname{Tr}\left[\hat{\rho}_{Q\bar{Q}}^{\Psi}\frac{d\hat{\rho}_{N}(t)}{dt}\right]$ $\mathbf{\Gamma} \mathbf{\Gamma} \mathbf{\Gamma} (t) = \operatorname{Tr} \left[\hat{\rho}_{Q\bar{Q}}^{\Psi}(T(t)) \frac{d\hat{\rho}_N(t)}{dt} \right] + \frac{dT}{dt} \operatorname{Tr} \left[\frac{\partial \hat{\rho}_{Q\bar{Q}}^{\Psi}(T)}{\partial T} \hat{\rho}_N(t) \right]$

New contribution to the rate (so-called « local rate »)

• "Minor problem" #1: Classical equations of motion are unstable (in the CM):

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• "Issue" : slicing the global time evolution (usual strategy in MC) is not compatible with passing to c.m. frame for each individual pair...

Generic need to store / describe the trajectory of particle 2 at a time $t_{lab} > t_{lab}^2$ if ones propagates particle 1 up to t_{lab}^2 by resorting to evolution in the c.m.

