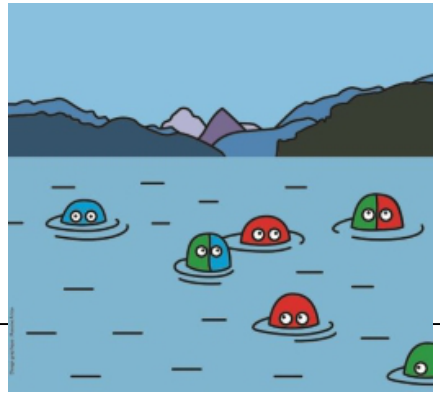
The statistical hadronization model for heavy quarks and a model intercomparison for quarkonium production in Pb-Pb collisions

A. Andronic - University of Münster

- The statistical hadronization model for charm quarks
- ...and beauty quarks
- Model intercomparison for quarkonium production in Pb-Pb collisions (EMMI RRTF - Quarkonium, 16-20.12.2019)
  ...revived 2022



The statistical (thermal) model

grand canonical partition function for specie (hadron) i :

$$\ln Z_i = \frac{V g_i}{2\pi^2} \int_0^\infty \pm p^2 \mathrm{d}p \ln[1 \pm \exp(-(E_i - \mu_i)/T)]$$

$g_i = (2J_i + 1)$ spin degeneracy factor; T temperature;
$E_i = \sqrt{p^2 + m_i^2}$ total energy; (+) for fermions (–) for bosons
$\mu_i = \mu_B B_i + \mu_{I_3} I_{3i} + \mu_S S_i + \mu_C C_i$ chemical potentials

μ ensure conservation (on average) of quantum numbers, fixed by "initial conditions"

i) isospin: $\sum_i n_i I_{3i} / \sum_i n_i B_i = I_3^{tot}/N_B^{tot}, \quad N_B^{tot} \sim \mu_B$
I_3^{tot}, N_B^{tot} isospin and baryon number of the system (=0 at high energies)

ii) strangeness: $\sum_i n_i S_i = 0$

iii) charm: $\sum_i n_i C_i = 0$.

SHM for charm (SHMc)

pQCD production, "throw in": $N_{c\bar{c}} = 9.6 \rightarrow g_c = 30.1$ $(I_1/I_0 = 0.974)$

LHC, central collisions

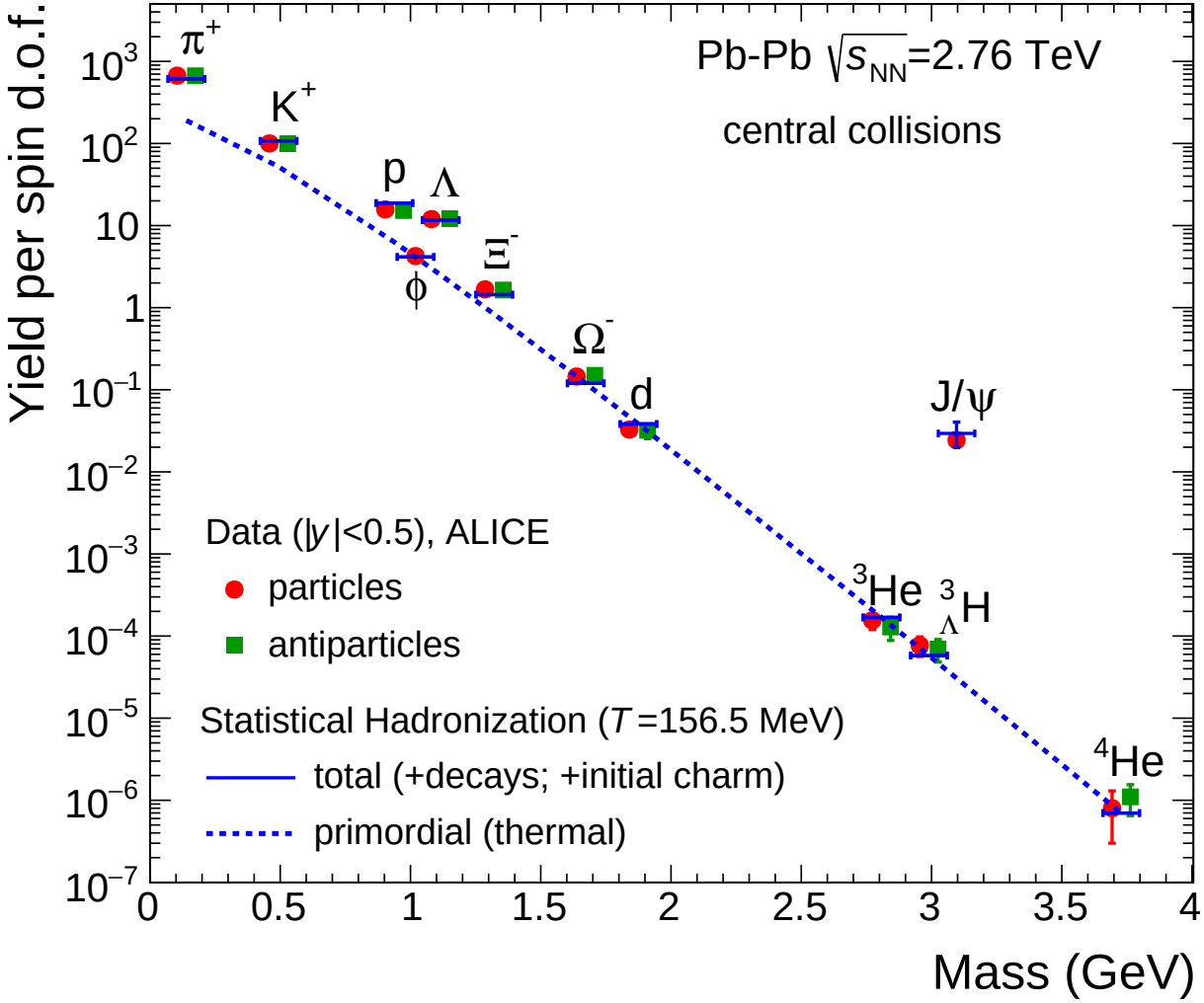
assume:

- full (99%) thermalization of $c, \bar{c}$ ("mobility" in V$\simeq$4000 fm^3)

- full color screening (Matsui-Satz)

Braun-Munzinger, Stachel, PLB 490 (2000) 196

Model predicts all charm chemistry ($\psi(2S)$, $X(3872)$)



π, $K^{\pm}$, K^0 from charm included in the thermal fit (0.7%, 2.9%, 3.1% for T=156.5 MeV)

PLB 797 (2019) 134836

SHMc: method and inputs

Braun-Munzinger, Stachel, PLB 490 (2000) 196, NPA 690 (2001) 119

- Thermal model calculation (grand canonical) T,μ_B: $\rightarrow n_X^{th}$

- $N_{c\bar{c}}^{dir} = \frac{1}{2} g_c V (\sum_i n_{D_i}^{th} + n_{\Lambda_i}^{th}) + g_c^2 V (\sum_i n_{\psi_i}^{th} + n_{\chi_i}^{th})$

- $N_{c\bar{c}} << 1 \rightarrow$ Canonical (Cleymans, Redlich, Suhonen, Z. Phys. C51 (1991) 137):

Gorenstein, Kostyuk, Stöcker, Greiner, PLB 509 (2001) 277

$$N_{c\bar{c}}^{dir} = \frac{1}{2} g_c N_{oc}^{th} \frac{I_1(g_c N_{oc}^{th})}{I_0(g_c N_{oc}^{th})} + g_c^2 N_{c\bar{c}}^{th} \quad \rightarrow g_c(N_{part}) \text{ (charm fugacity)}$$

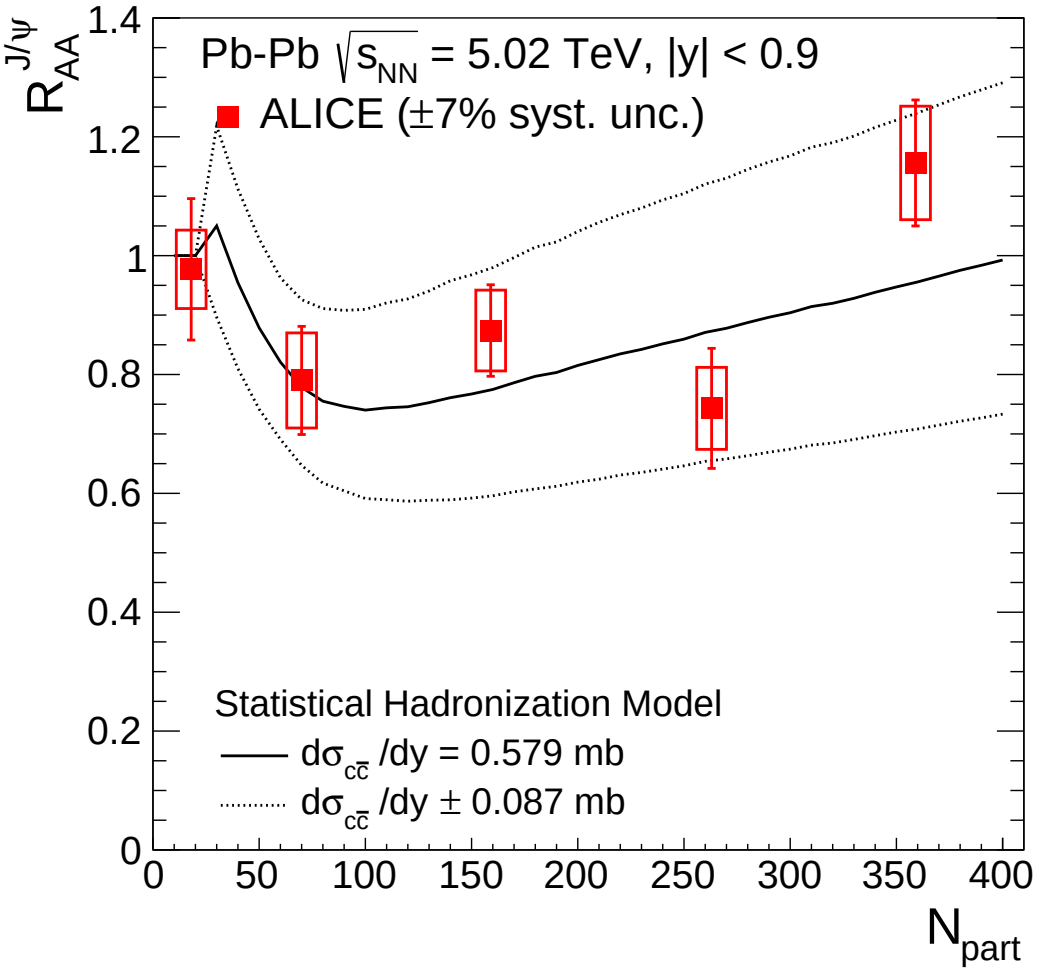
Outcome: $N_D = g_c V n_D^{th} I_1/I_0 \quad N_{J/\psi} = g_c^2 V n_{J/\psi}^{th}$

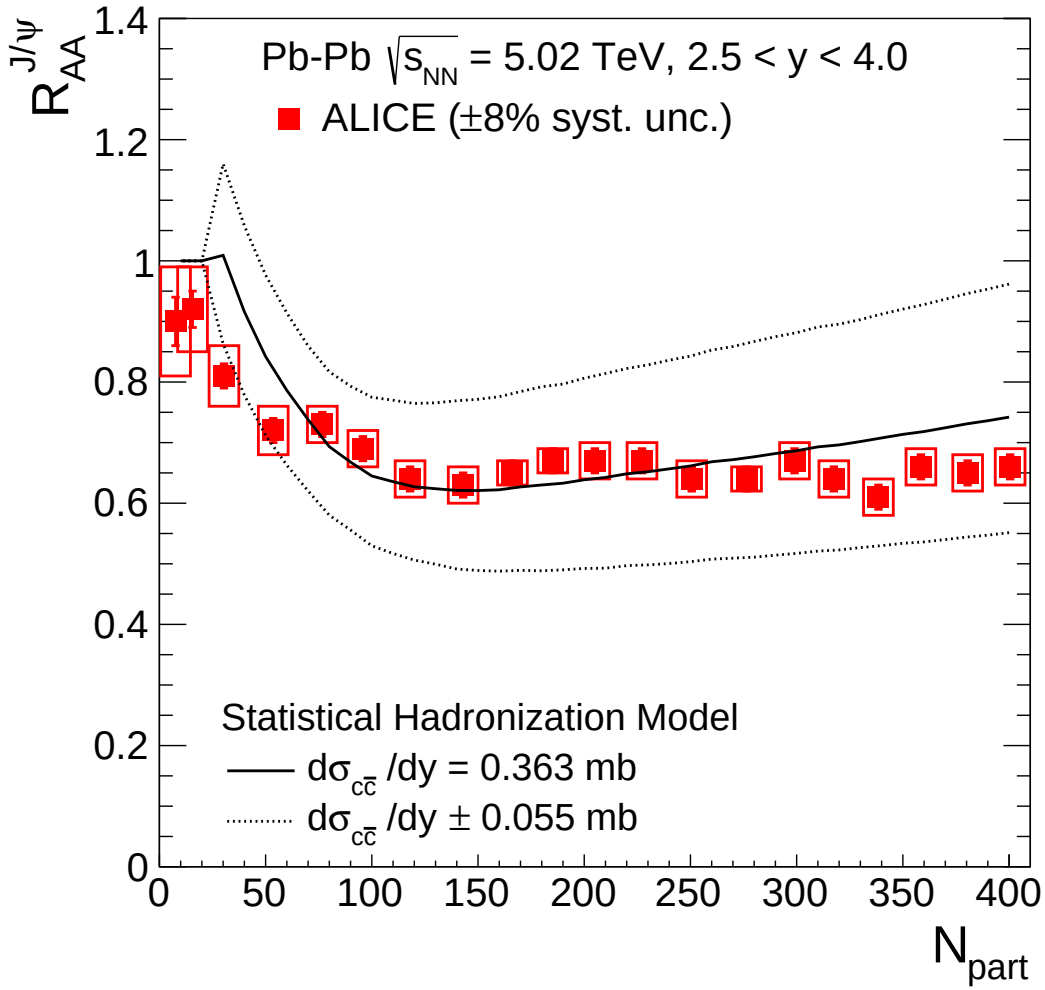
Inputs: T, μ_B, $\quad V_{\Delta y=1} (= (\mathrm{d}N_{ch}^{exp}/\mathrm{d}y)/n_{ch}^{th})$, $\quad N_{c\bar{c}}^{dir}$ (exp. or pQCD)

Assumed minimal volume for QGP: V_{QGP}^{min}=200 fm^3

SHMc and charmonium data at the LHC

full thermalization of c quarks in QGP, hadronization at chemical freeze-out

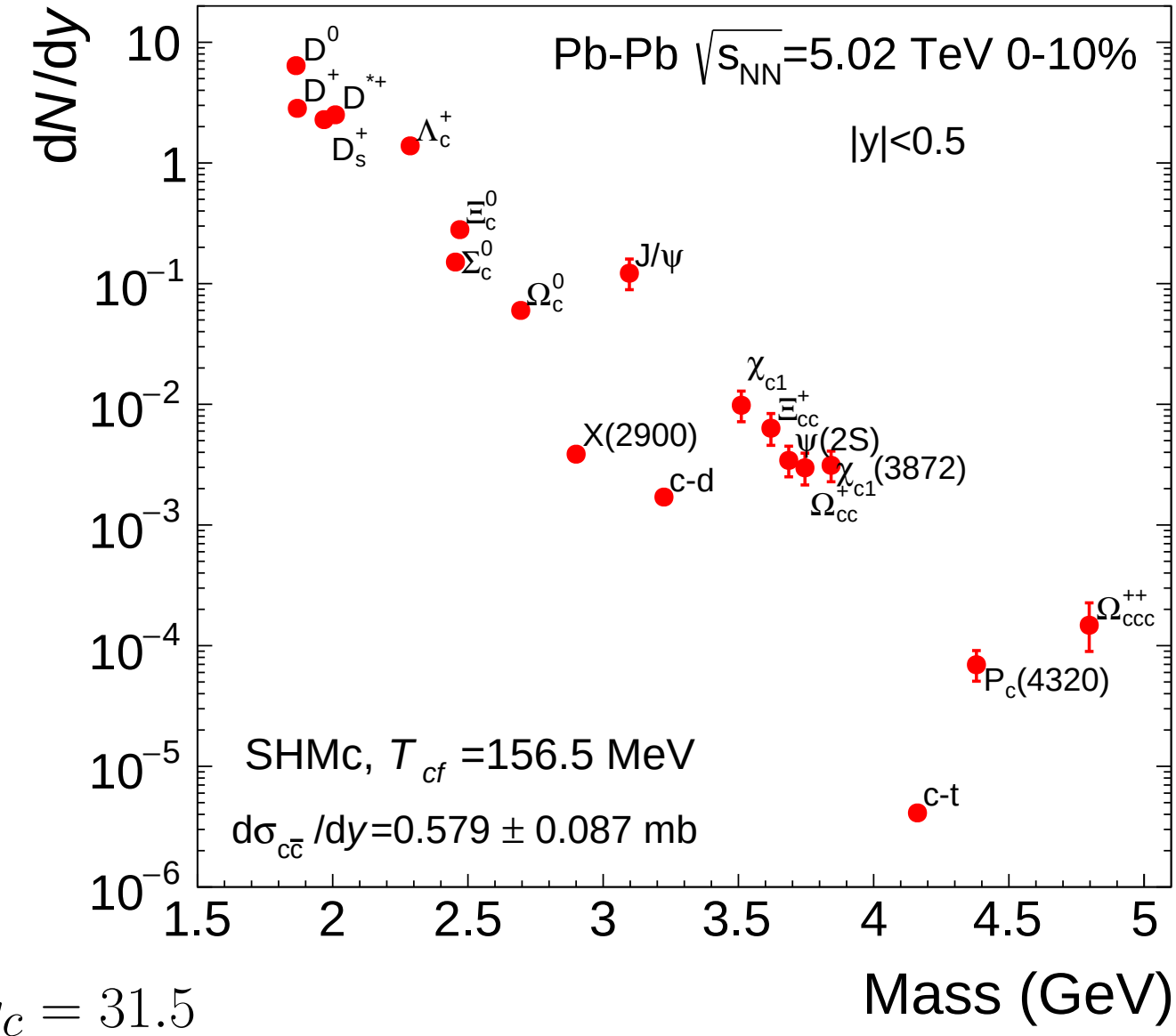




$\mathrm{d}\sigma_{c\bar{c}}/\mathrm{d}y$ via normalization to D^0 in Pb–Pb 0-10%, ALICE, arXiv:2110.09420

$\mathrm{d}N/\mathrm{d}y$ = 6.82±1.03 ($|y| < 0.5$; FONLL for y=2.5-4; assuming hadronization fractions in data as in SHMc)

SHMc: the full charm zoo



$$T_{cc}^+ \simeq 0.9 \cdot \chi_{c1}(3872)$$

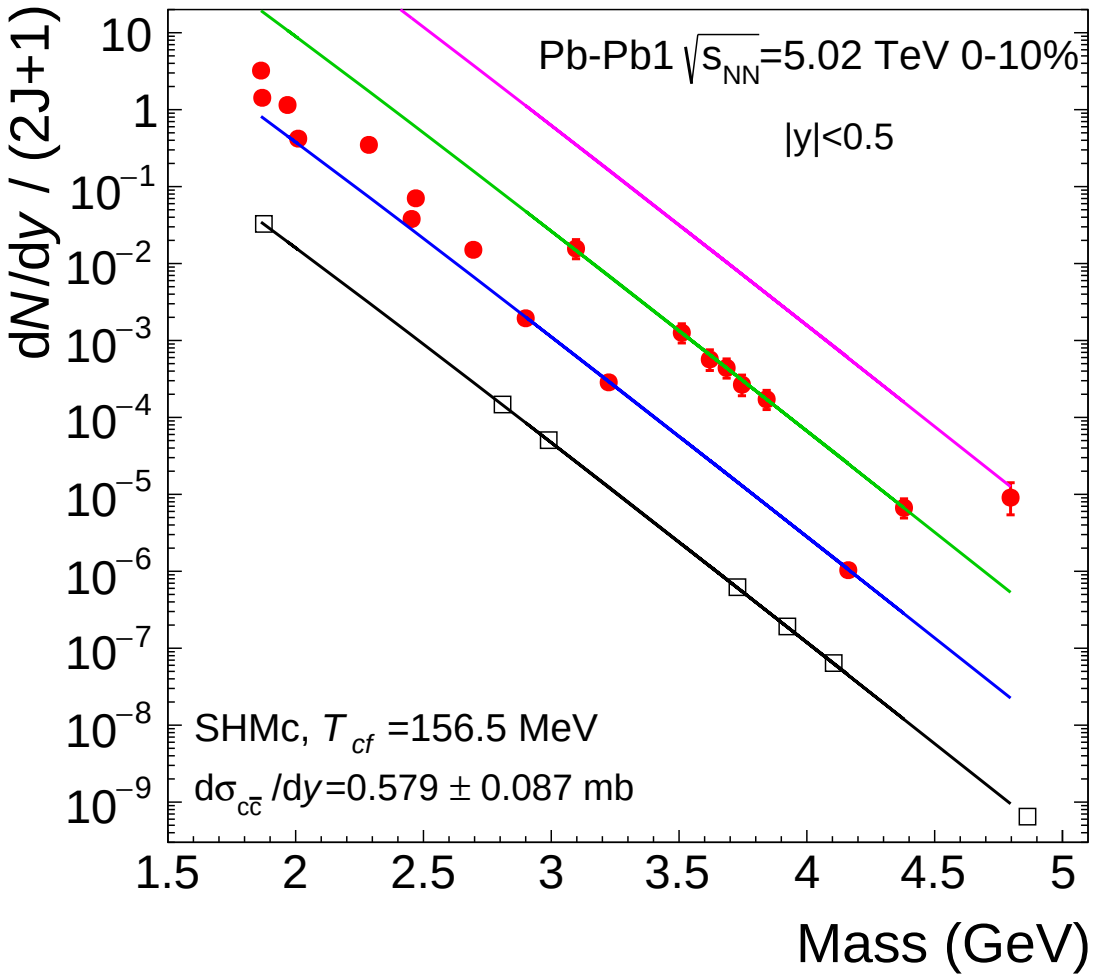
$$X(6900) \sim 10^{-8}$$

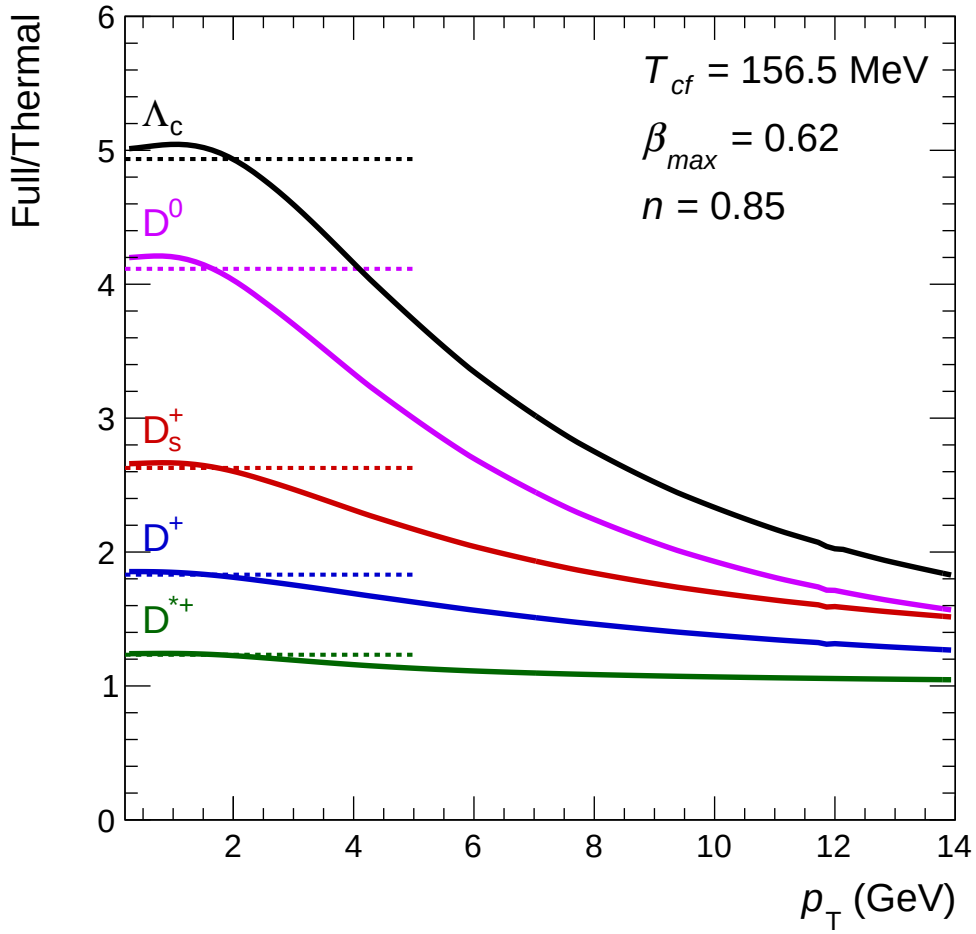
$$\frac{\mathrm{d}N_{c\bar{c}}}{\mathrm{d}y} = 13.8$$

$$\rightarrow g_c = 31.5$$

The power of the model: predicting the full suite of charmed hadrons

Full charm predictions for the LHC





Charm-hadron spectrum as in PDG: 55 c-mesons, 74 c-baryons (part.+antipart.)

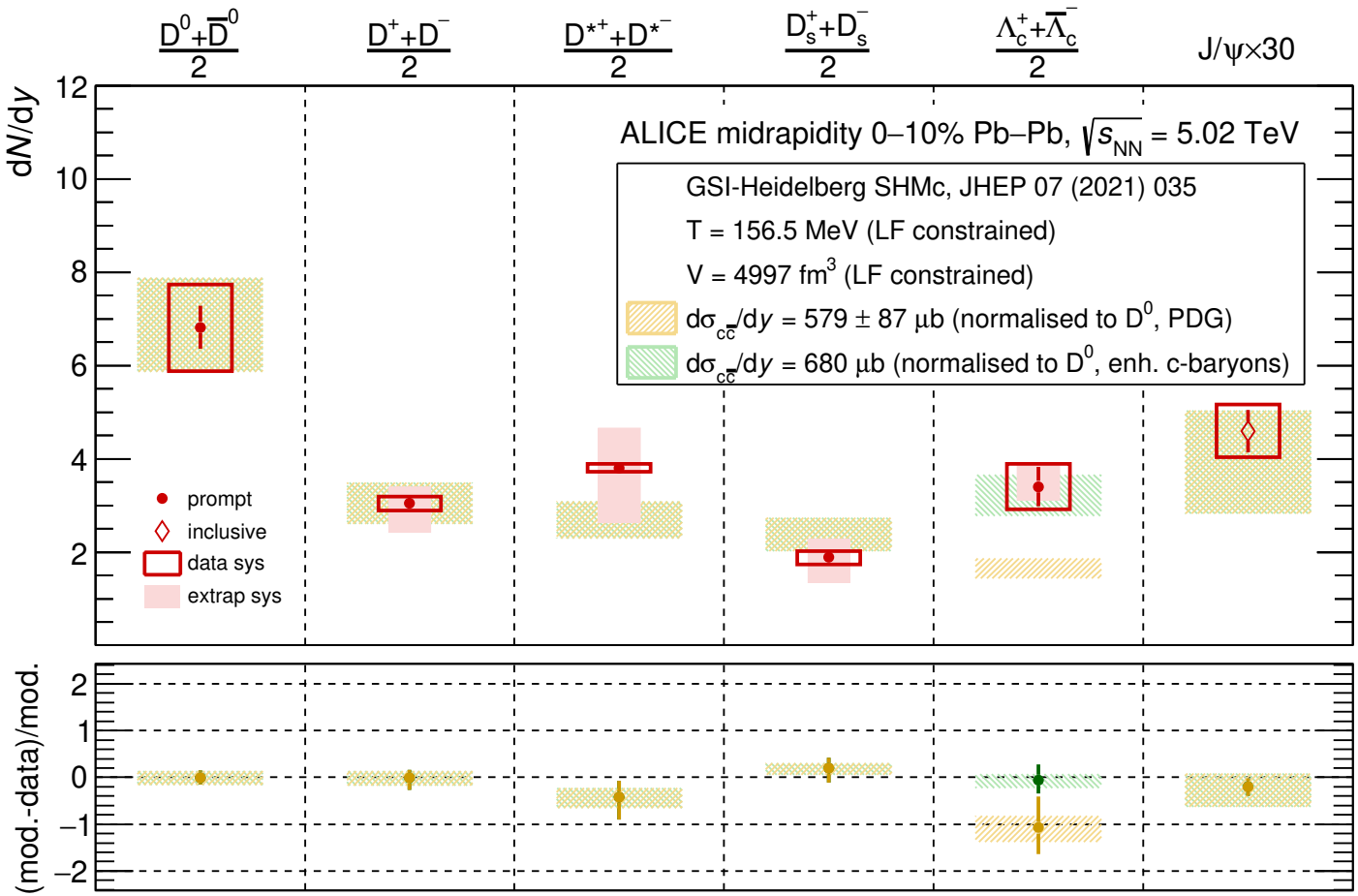
JHEP 07 (2021) 035

...large, but may not be complete

Modified charm-hadron spectrum

...ad-hoc: *tripled* the excited charm-baryon states, enhanced $\mathrm{d}\sigma_{\mathrm{c\bar{c}}}/\mathrm{d}y$ by 19%

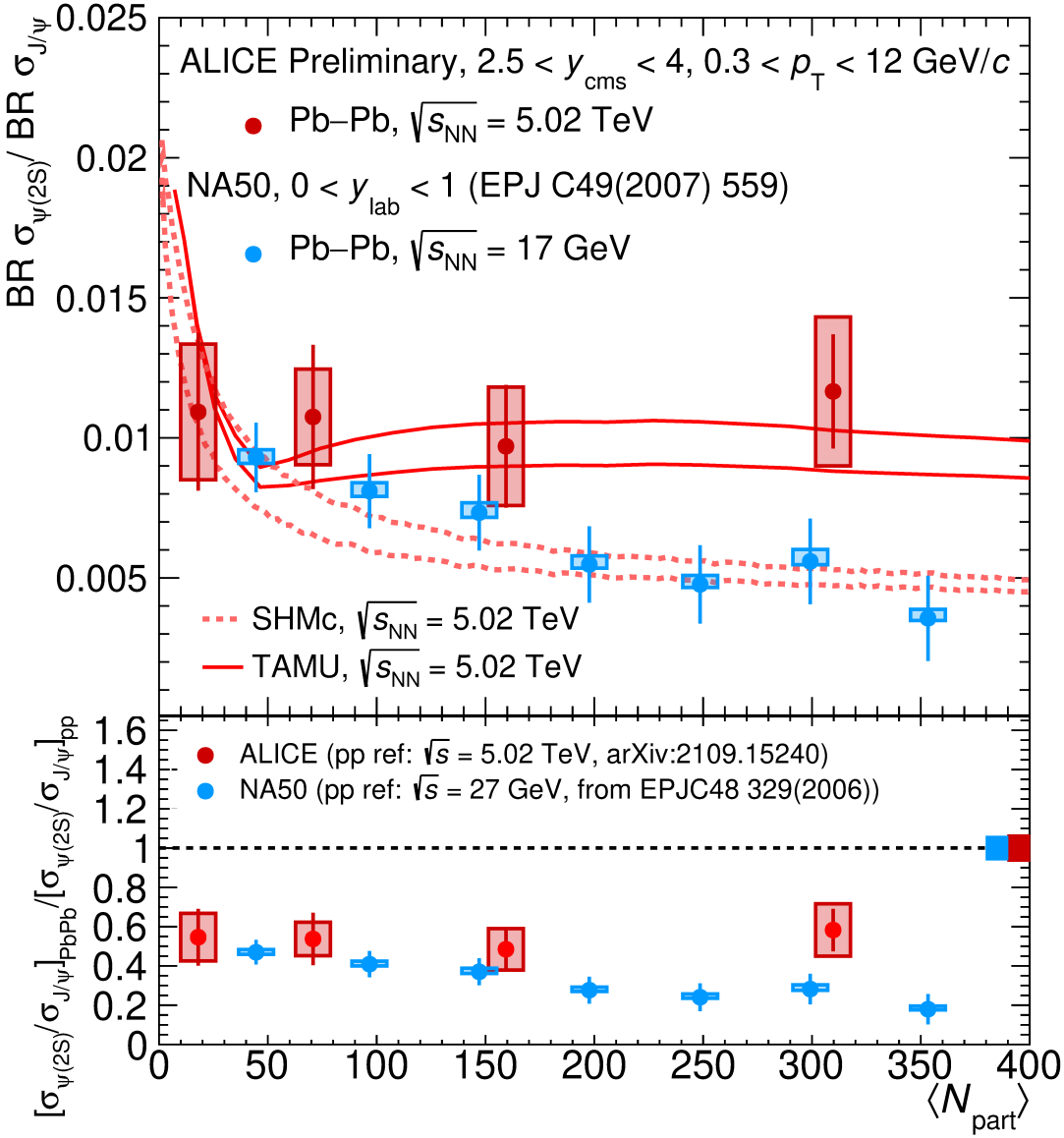
RQM: He,Rapp, PLB 795 (2019) 117; LQCD, Bazavov et al., PLB 737 (2014) 210



ALICE (QM'22 talk, L. Vermunt)

leaves the mesonic sector unaffected, for the commensurately larger $\sigma_{c\bar{c}}$

$\psi(2S)/J/\psi$ at the LHC

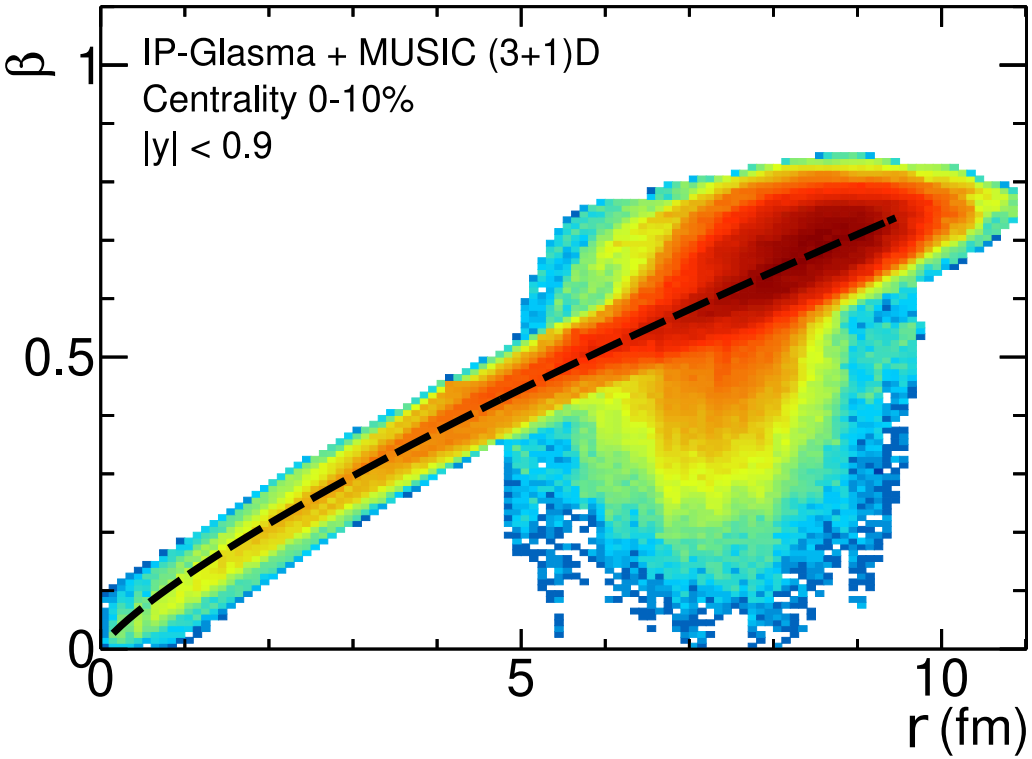


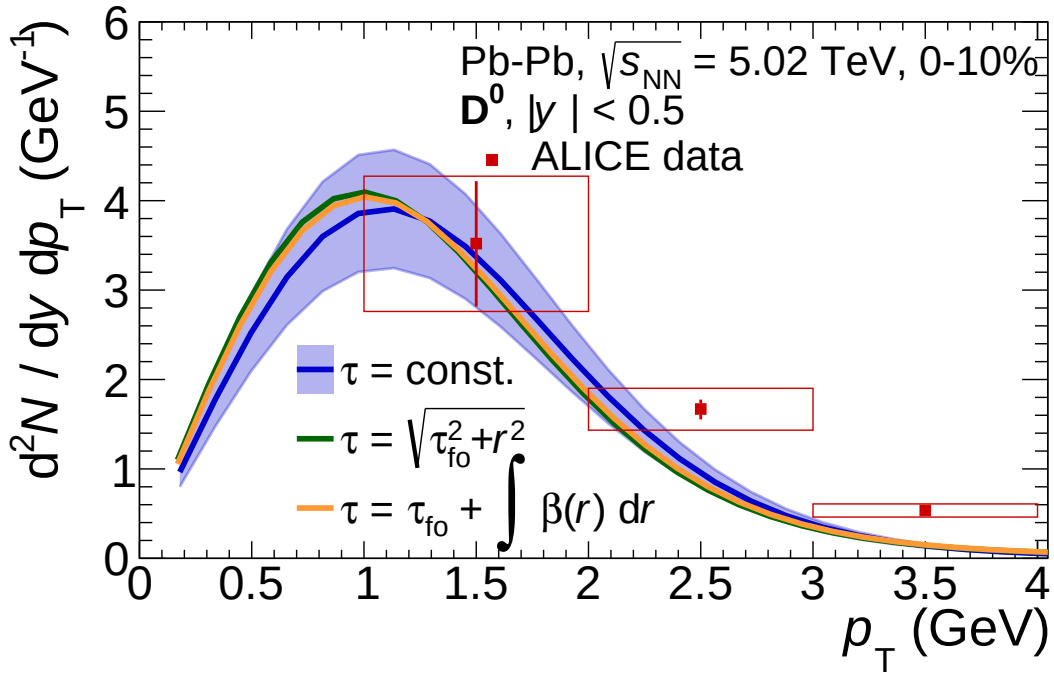
ALI-PREL-523330

In SHMc uncertainty only due to nuclear-corona ($\sigma_{c\bar{c}}$ cancels out completely)

SHMc: p_T dependence

full hydrodynamic flow (T=156.5 MeV, β_{max}=0.62), param. via blast-wave

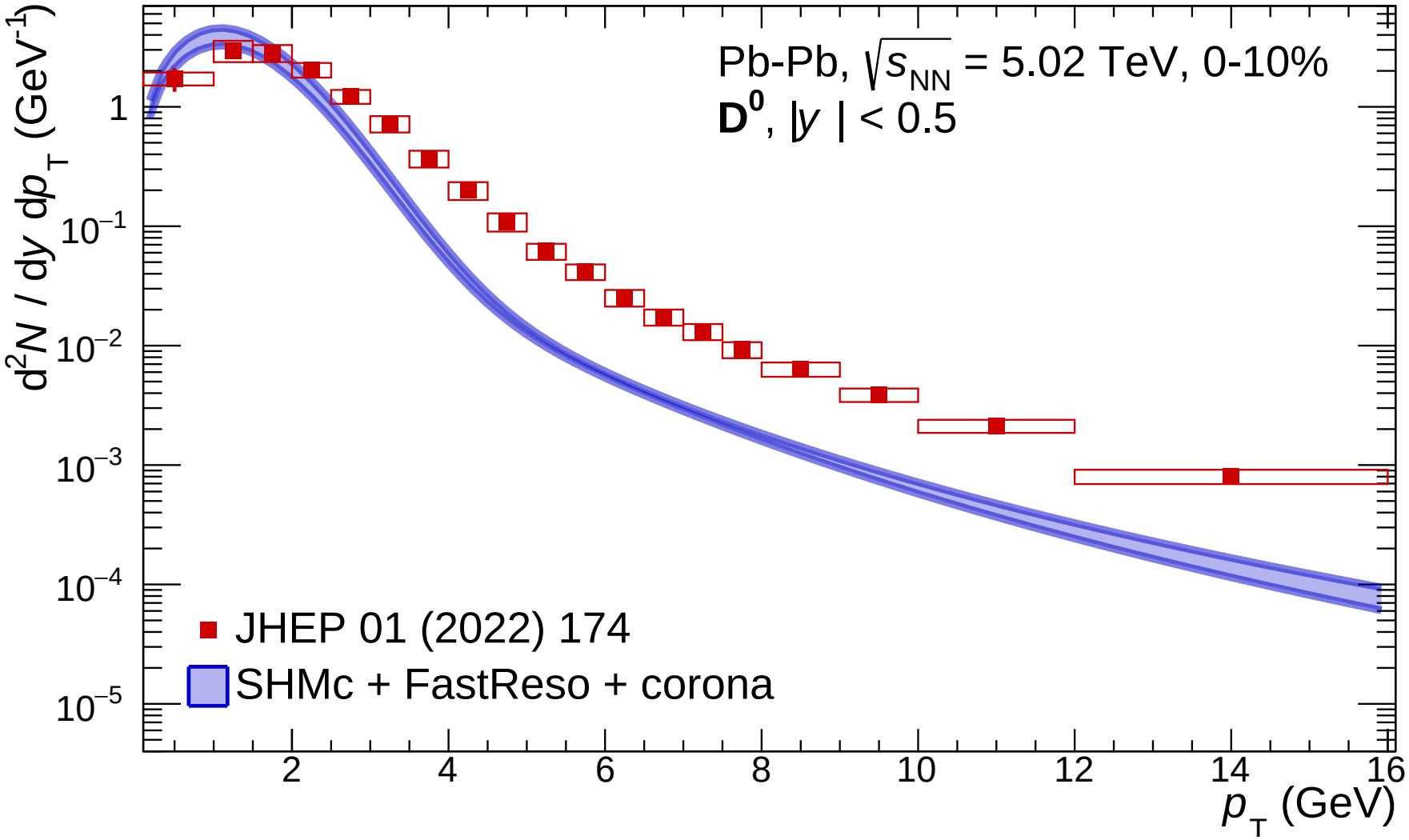




$$\frac{\mathrm{d}^2N}{2\pi p_\mathrm{T} dp_\mathrm{T} dy} = \frac{2J+1}{(2\pi)^3}\int \mathrm{d}\sigma_\mu p^\mu f(p) = \frac{2J+1}{(2\pi)^3}\int_0^{r_\mathrm{m}} \mathrm{d}r\ \tau(r) r \left[K_1^\mathrm{eq} - \frac{\partial\tau}{\partial r} K_2^\mathrm{eq}\right]$$

$$K_1^\mathrm{eq}(p_\mathrm{T}, u^r) = 4\pi m_\mathrm{T} I_0\left(\frac{p_\mathrm{T} u^r}{T}\right) K_1\left(\frac{m_\mathrm{T} u^\tau}{T}\right),\ K_2^\mathrm{eq}(p_\mathrm{T}, u^r) = 4\pi p_\mathrm{T} I_1\left(\frac{p_\mathrm{T} u^r}{T}\right) K_0\left(\frac{m_\mathrm{T} u^\tau}{T}\right)$$

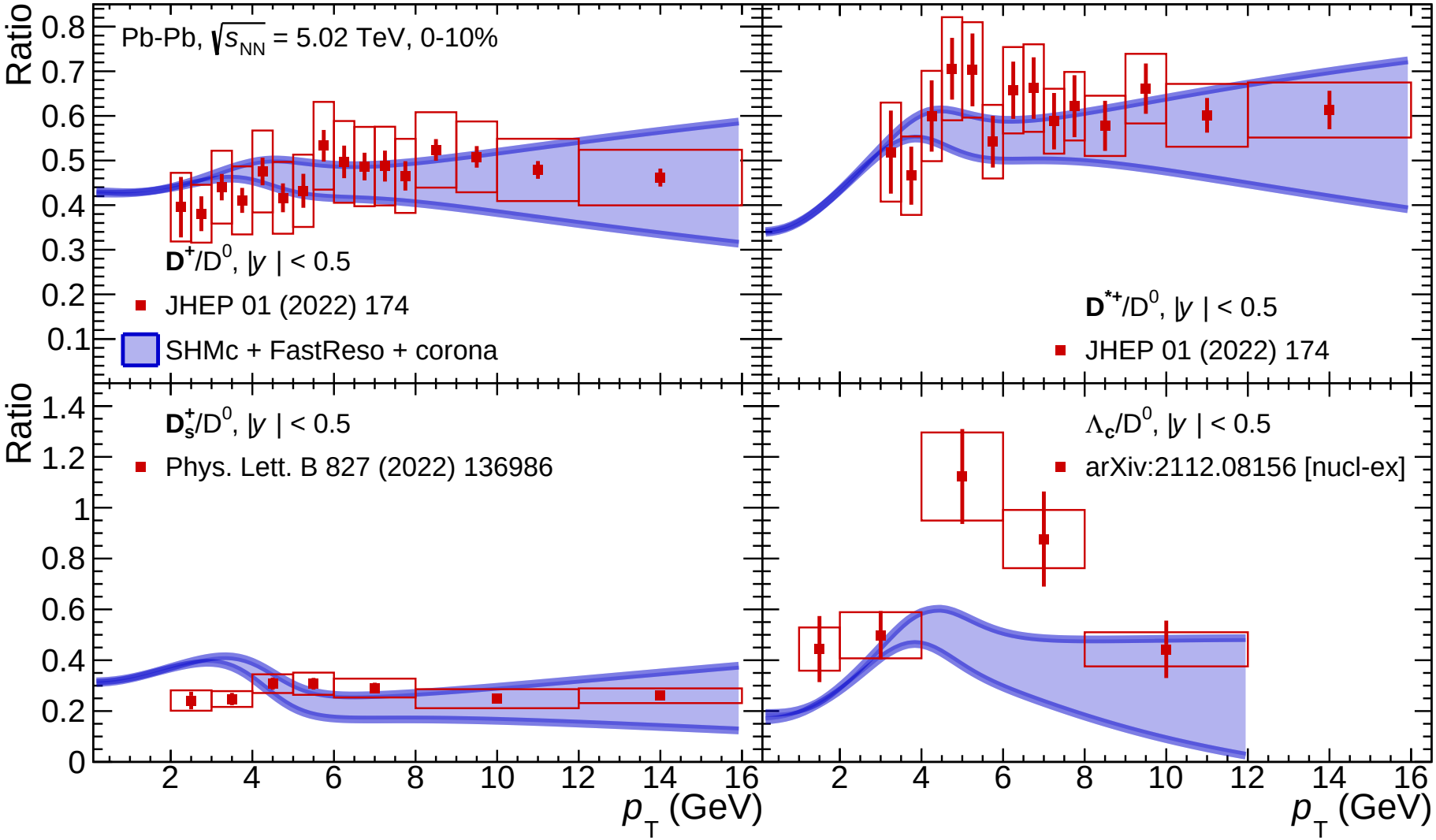
SHMc: p_T dependence



SHMc: low $\mathbf{p_T}$; high p_T: only nuclear-corona contribution (incl. uncert.)

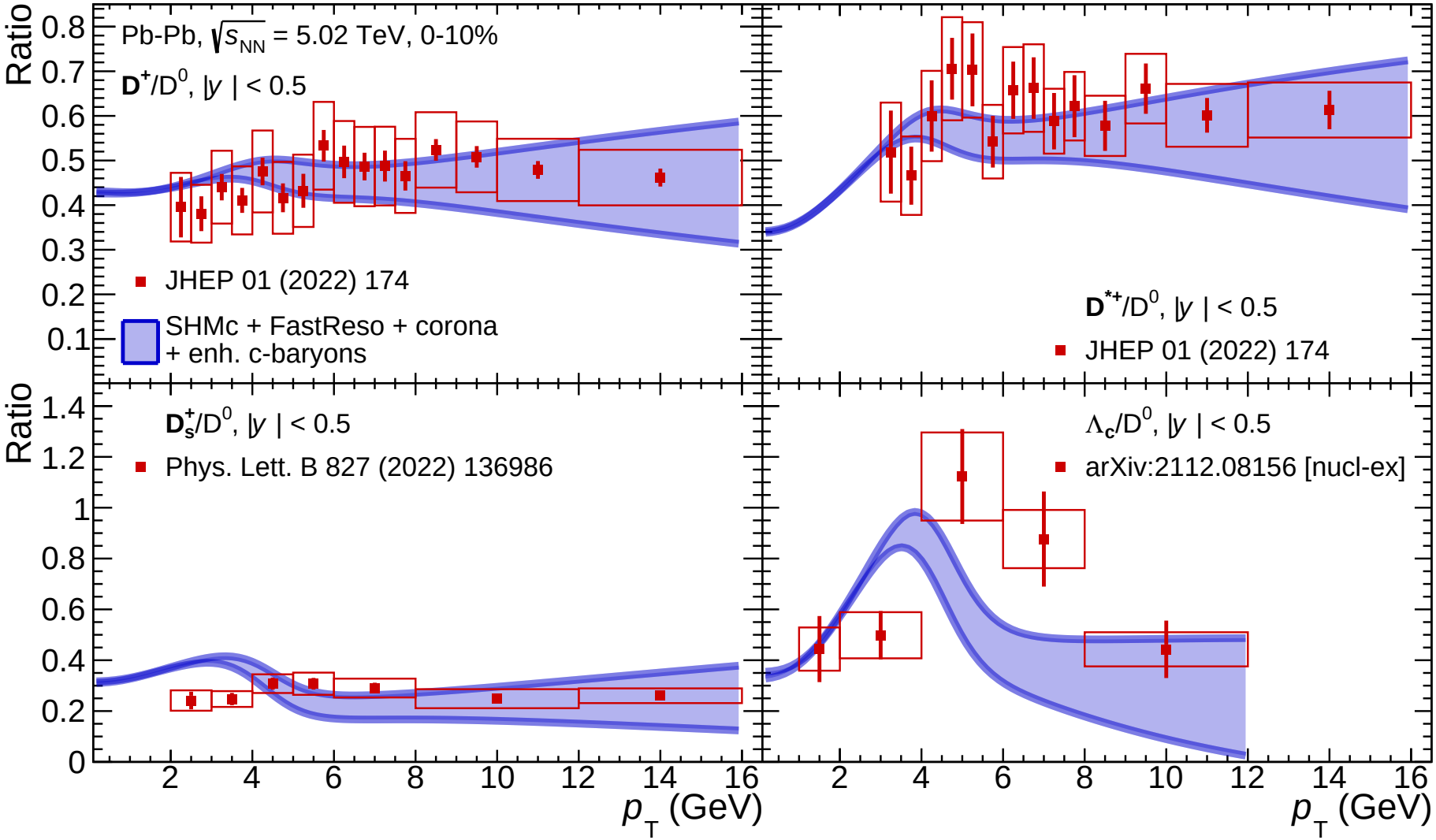
AA et al., JHEP 07 (2021) 035; ALICE, JHEP 01 (2022) 174

Ratios to D^0



Charm-hadron spectrum: PDG

Ratios to D^0

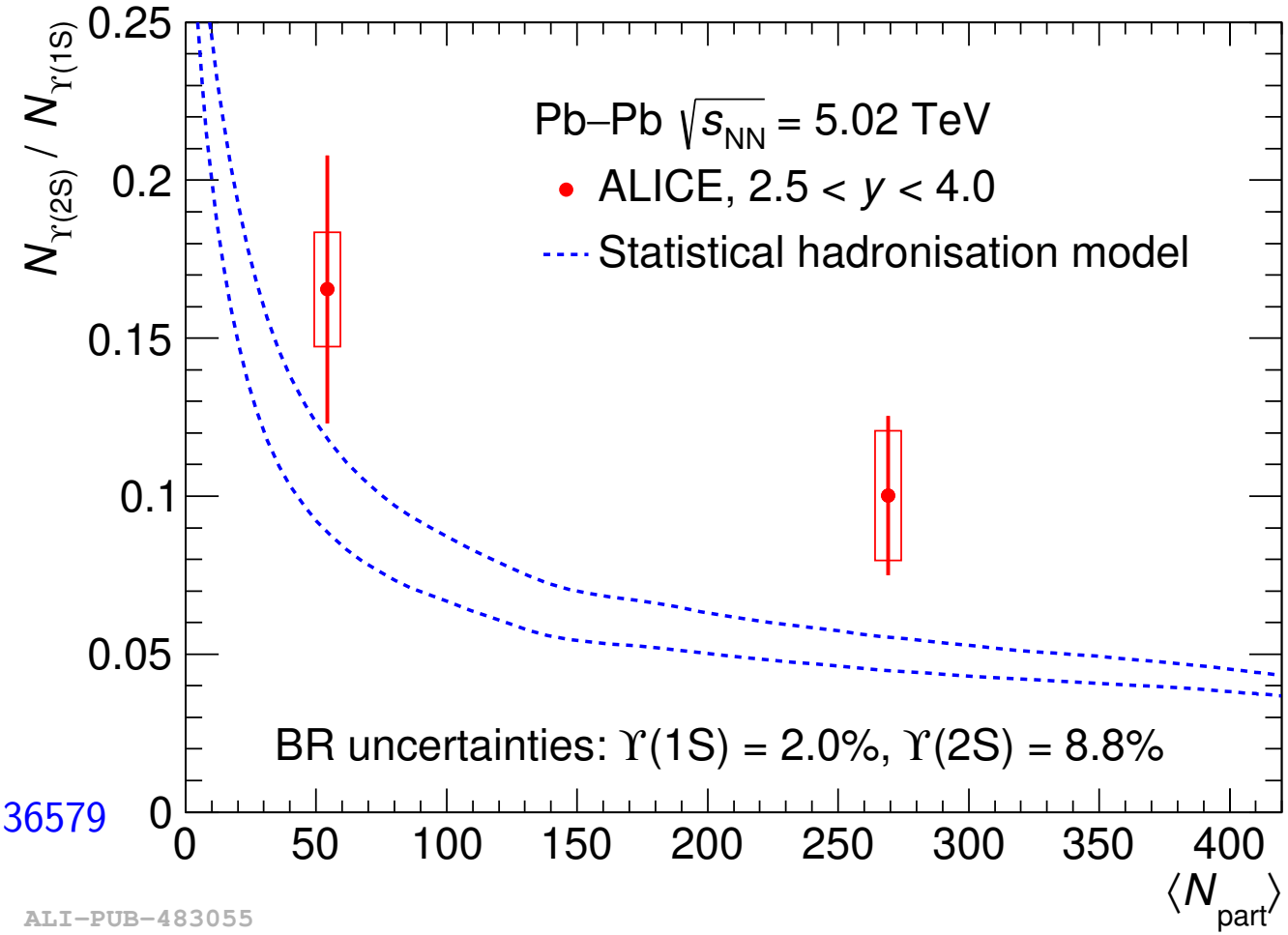


Charm-hadron spectrum: enhanced c-baryons (tripled excited states)

...and on to beauty (at the LHC)

Beauty is expected (R_{AA}, v_2 data) to be less thermalized compared to charm

The beauty-hadron spectrum is less well known (PDG: 48 b-mes, 46 b-bar total)



ALICE,

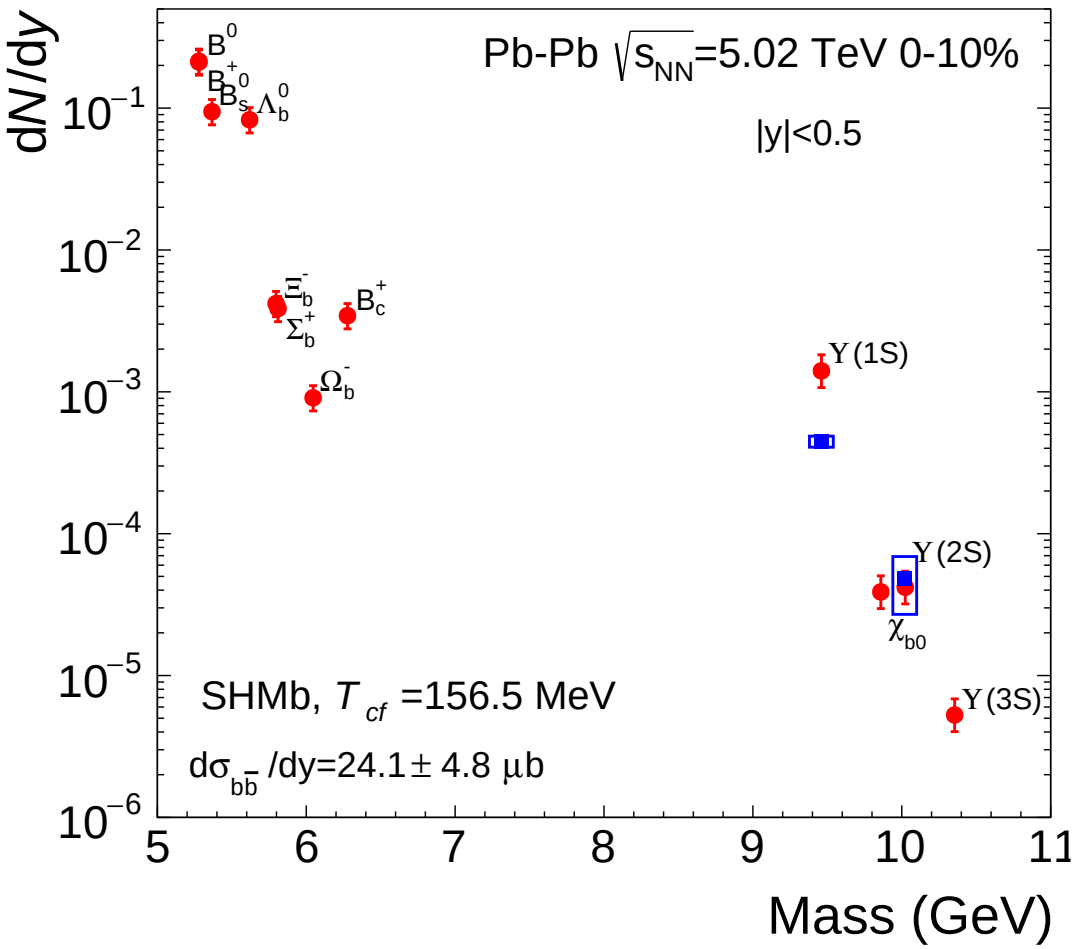
PLB 822 (2021) 136579

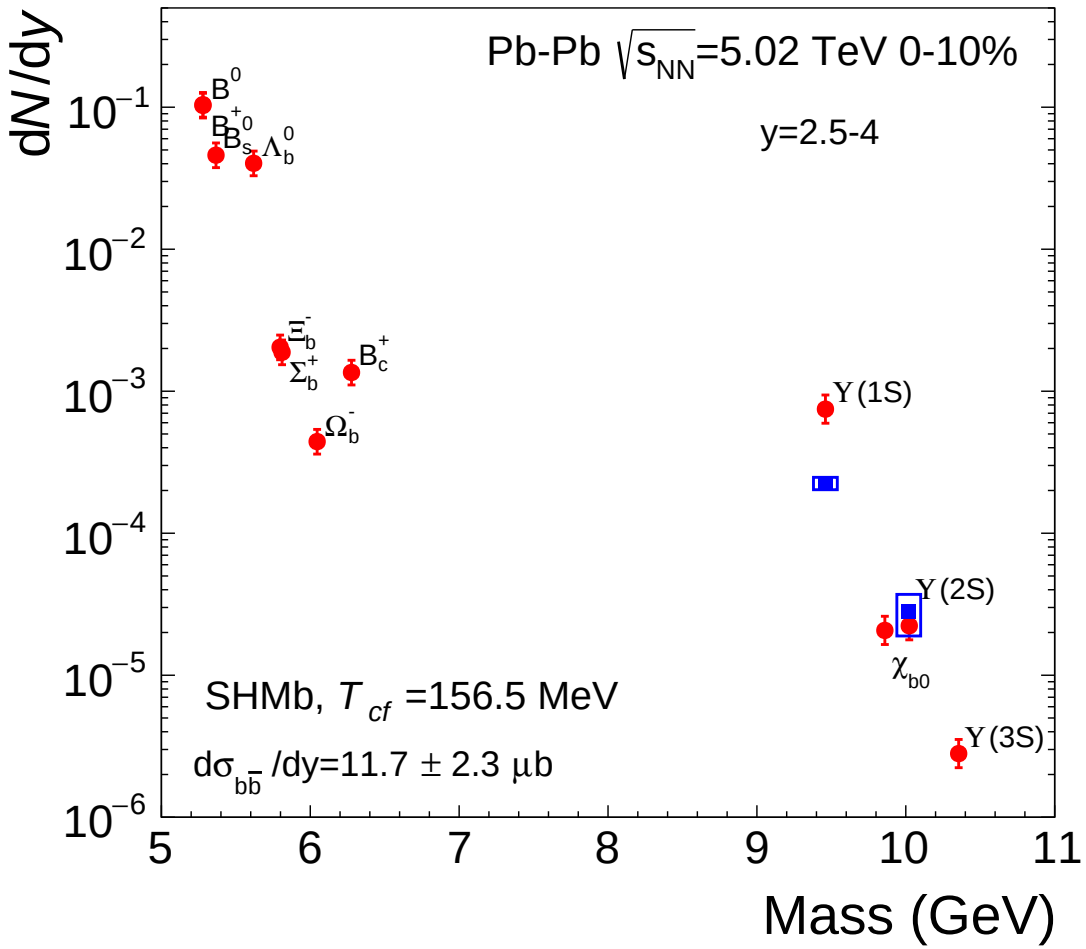
Color screening may not destroy all ϒ mesons in QGP

Uncertainty band determined by nuclear-corona

The limiting case: full beauty thermalization

A. Andronic





$$g_b = 1.05 \cdot 10^9 \quad (\frac{\mathrm{d}N_{b\bar{b}}}{\mathrm{d}y} = 0.57)$$

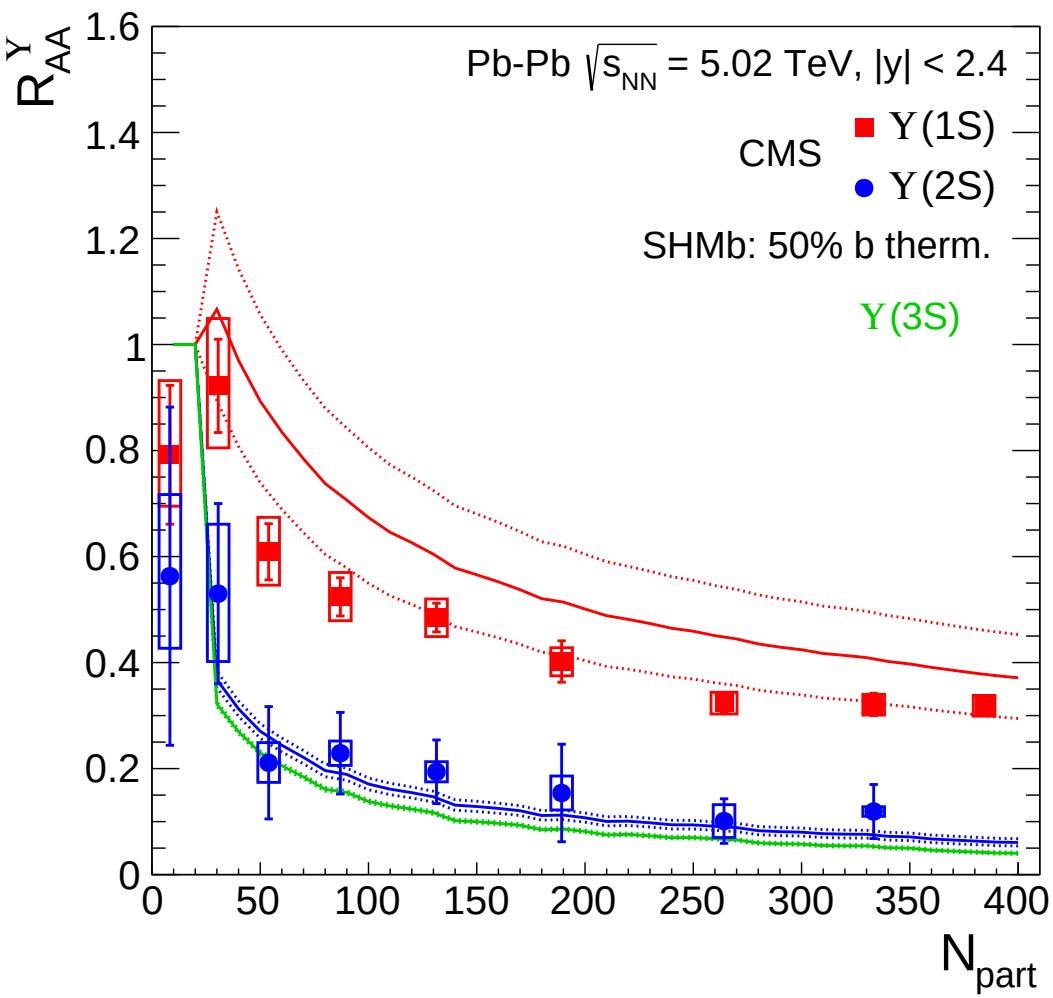
$$B_c : \; 3.44 \cdot 10^{-3}$$

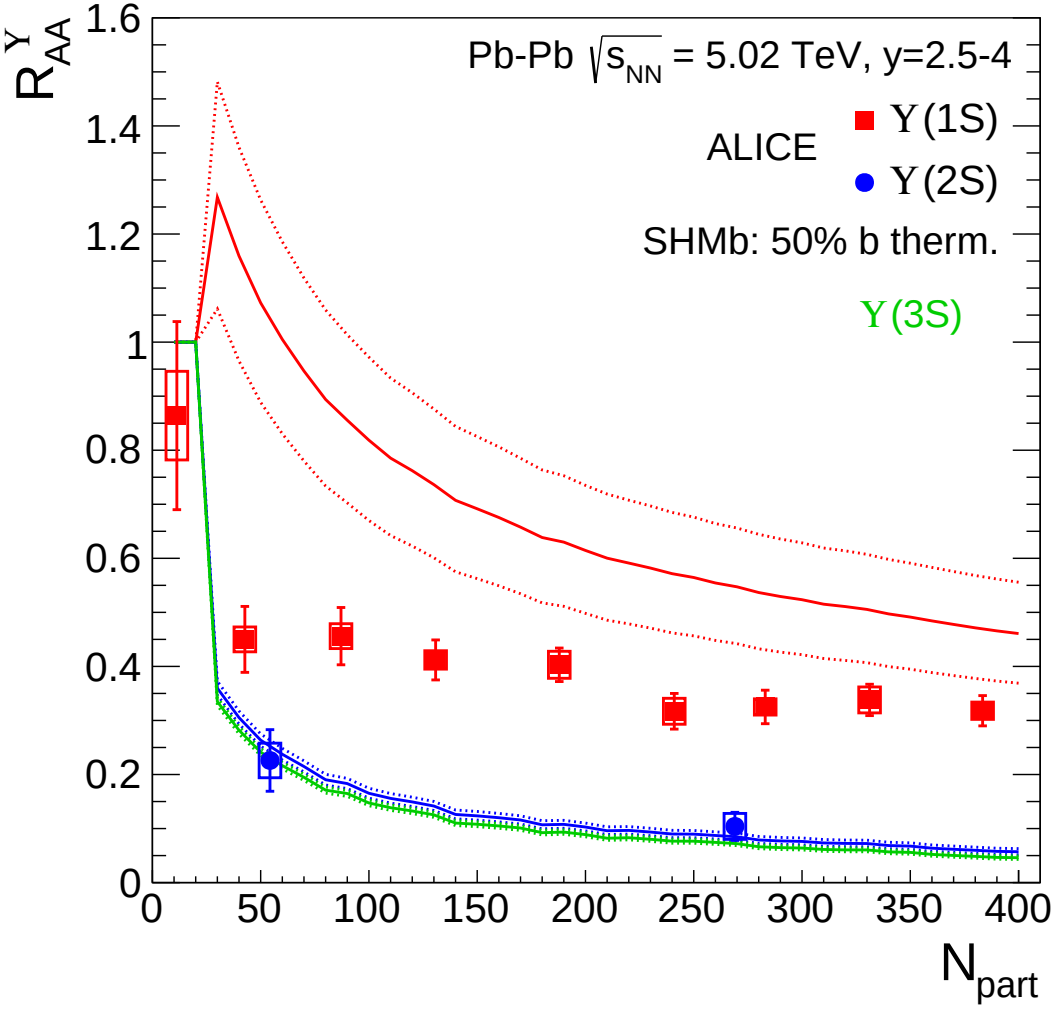
$$g_b = 0.86 \cdot 10^9 \quad (\frac{\mathrm{d}N_{b\bar{b}}}{\mathrm{d}y} = 0.28)$$

$$B_c : \; 1.36 \cdot 10^{-3}$$

Blue: Υ data (CMS, ALICE): calc. based on R_{AA} and pp (would be nice to include in publications $\mathrm{d}N/\mathrm{d}y$)

R_{AA}, 50% $b\bar{b}$ thermalized



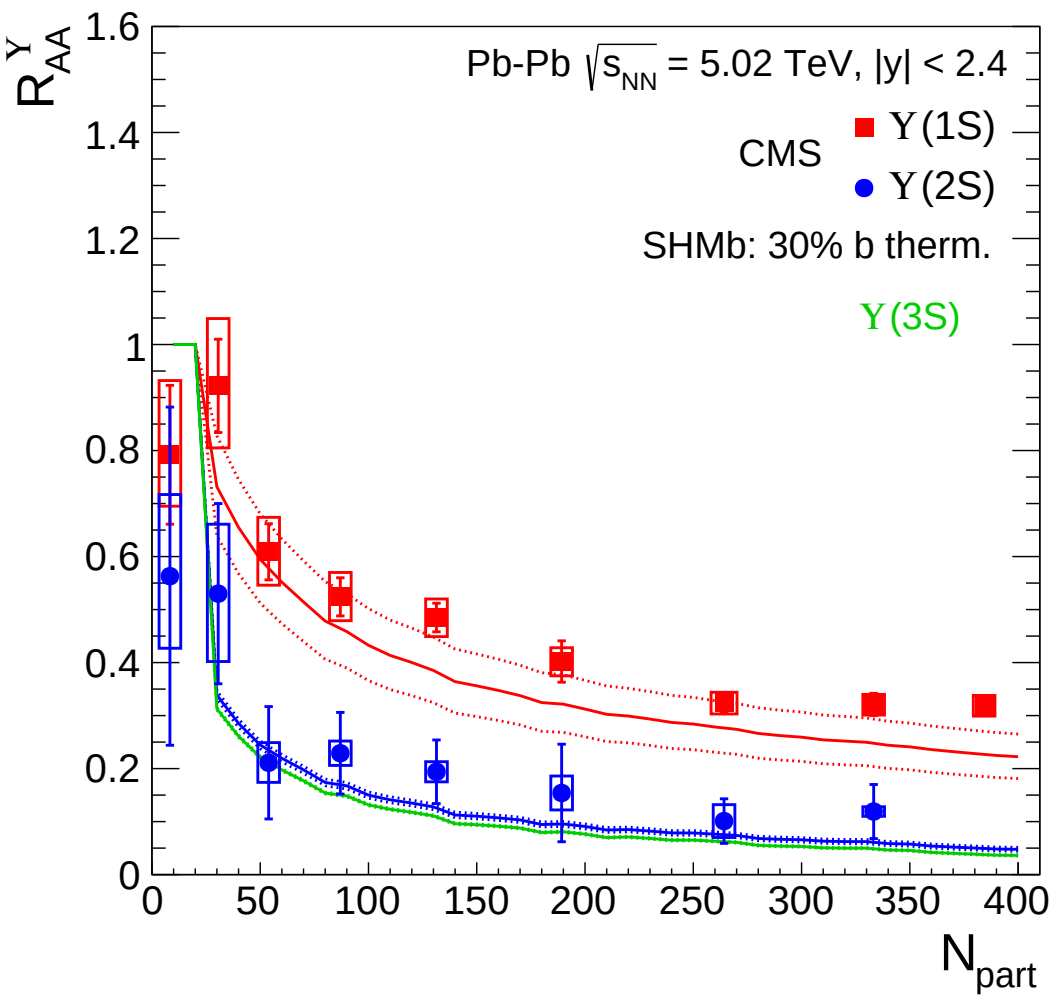


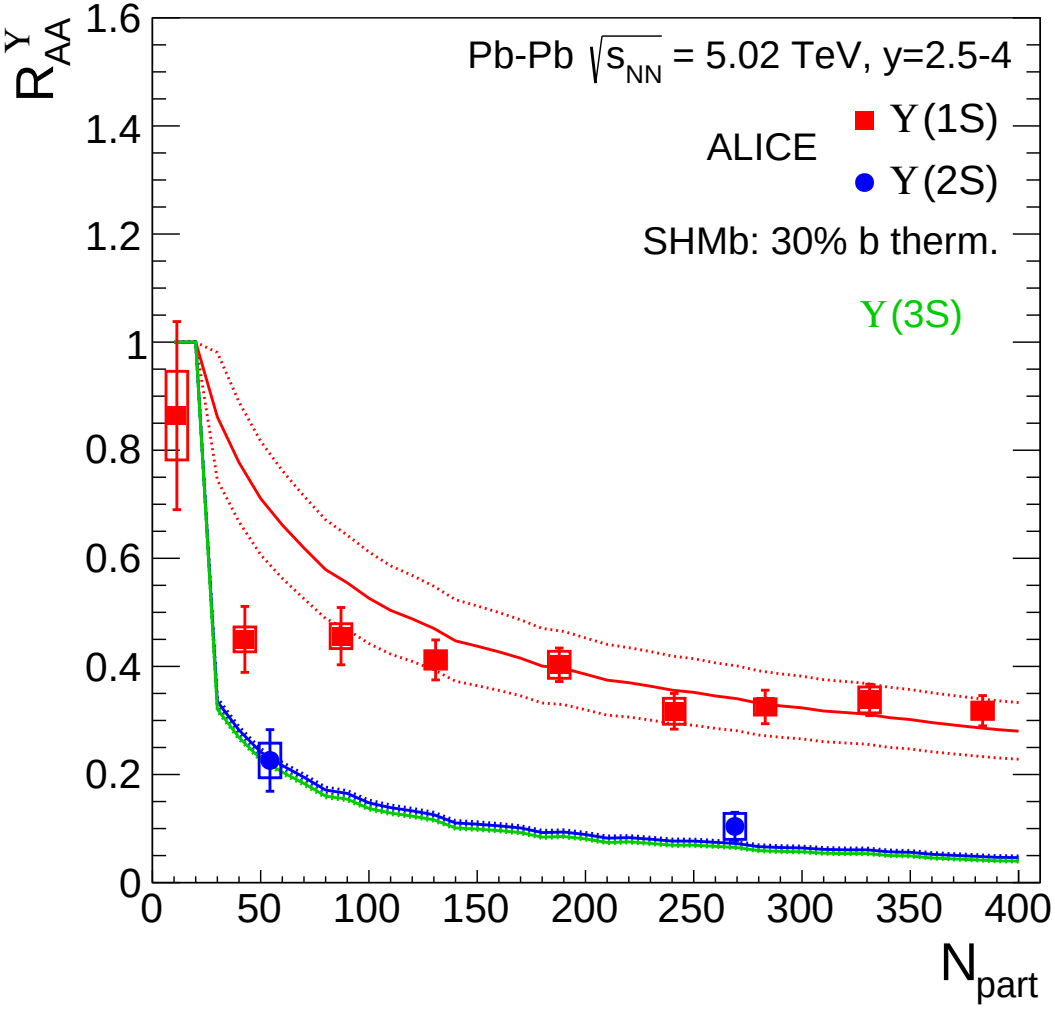
CMS, PRL 120 (2018) 142301

ALICE, PLB 822 (2021) 136579

What does non-thermalized beauty produce? (no room for it in SHMb)

R_{AA}, 30% $b\bar{b}$ thermalized



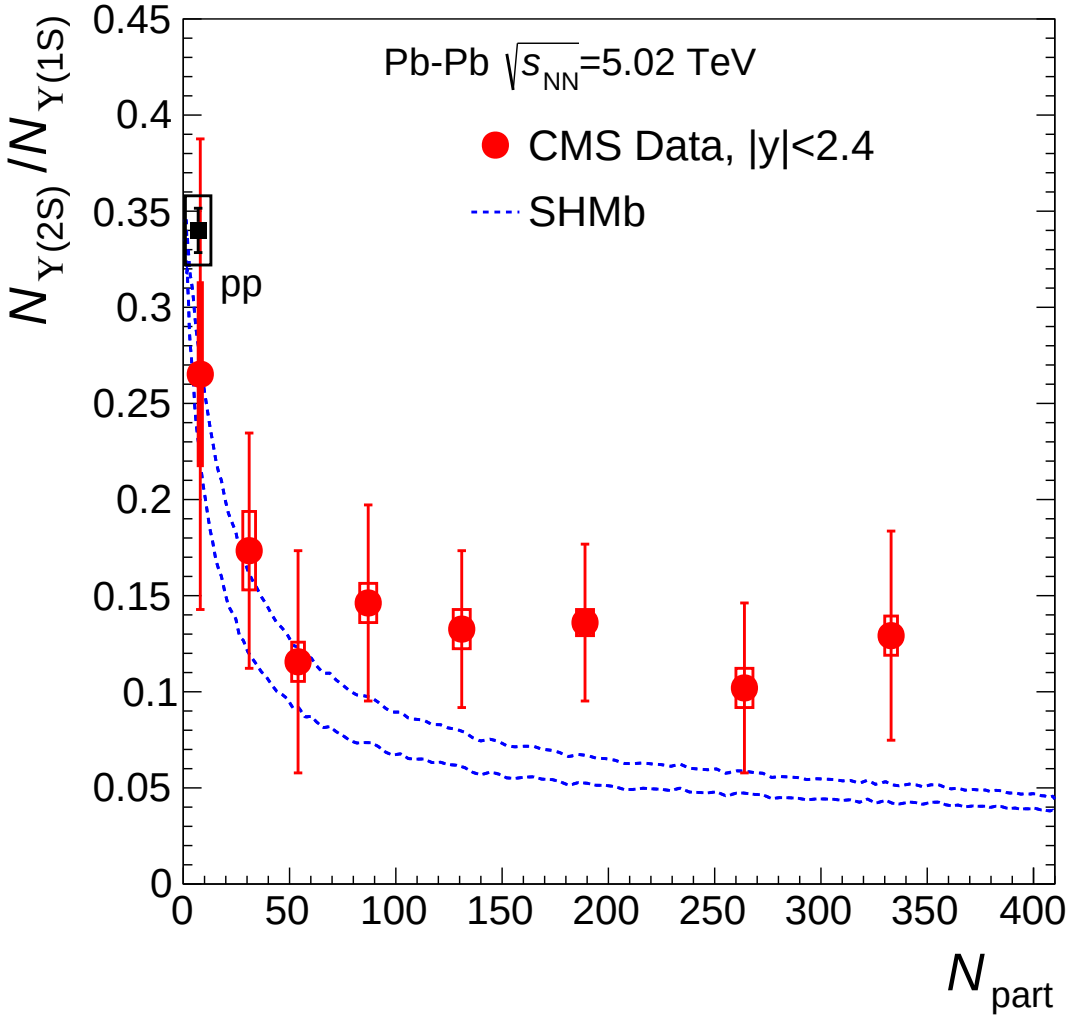


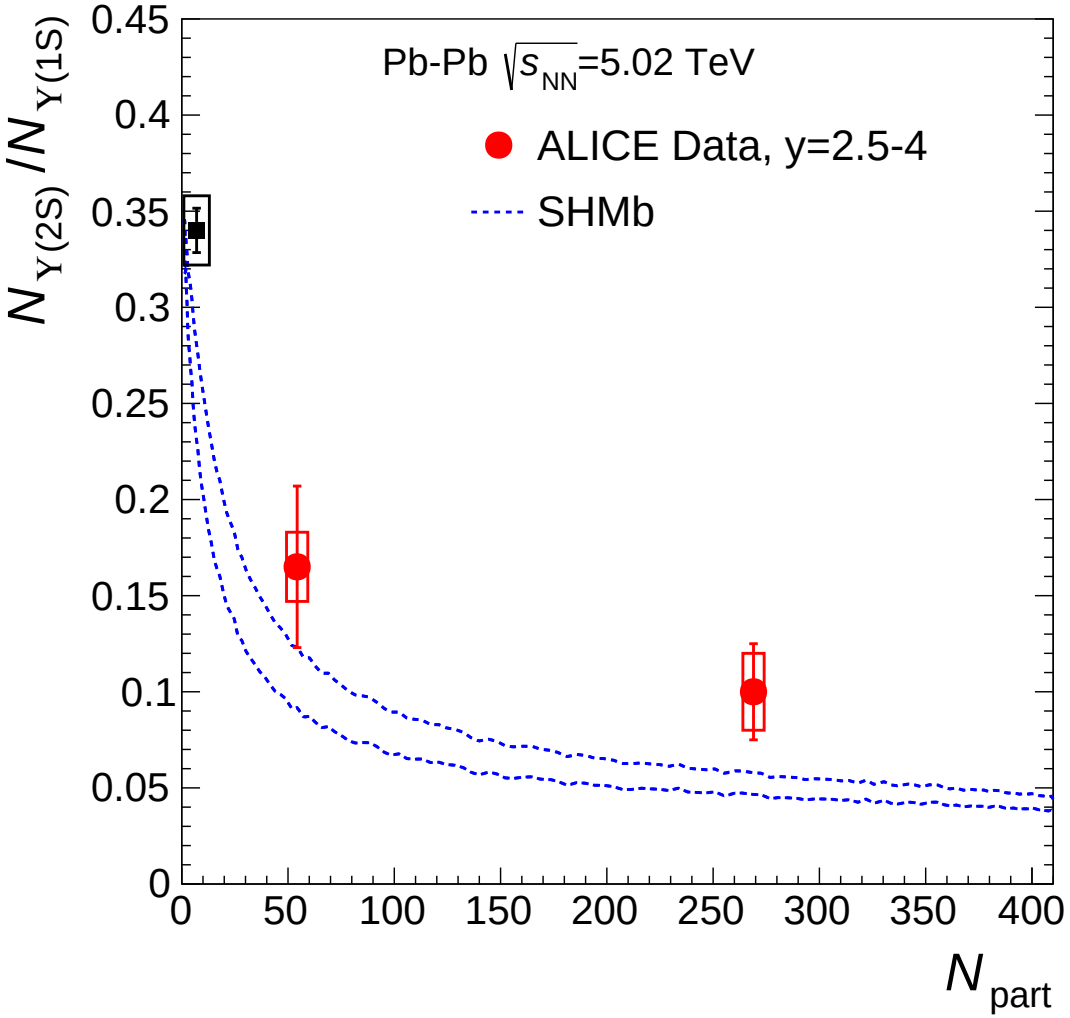
CMS, PRL 120 (2018) 142301

ALICE, PLB 822 (2021) 136579

What does non-thermalized beauty produce? (no room for it in SHMb)

$\Upsilon(2S)/\Upsilon(1S)$ ratio (100% b thermalization)





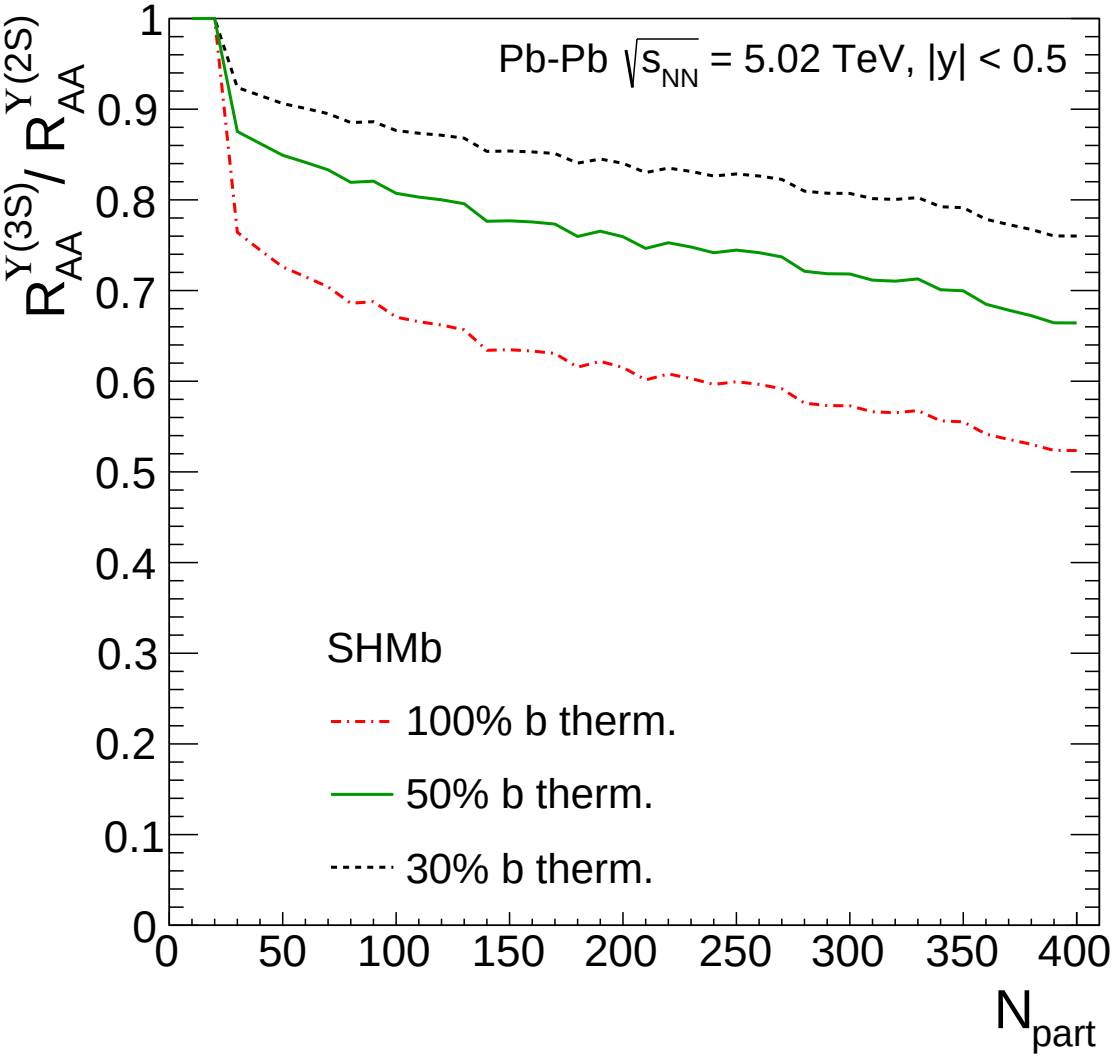
CMS, PRL 120 (2018) 142301

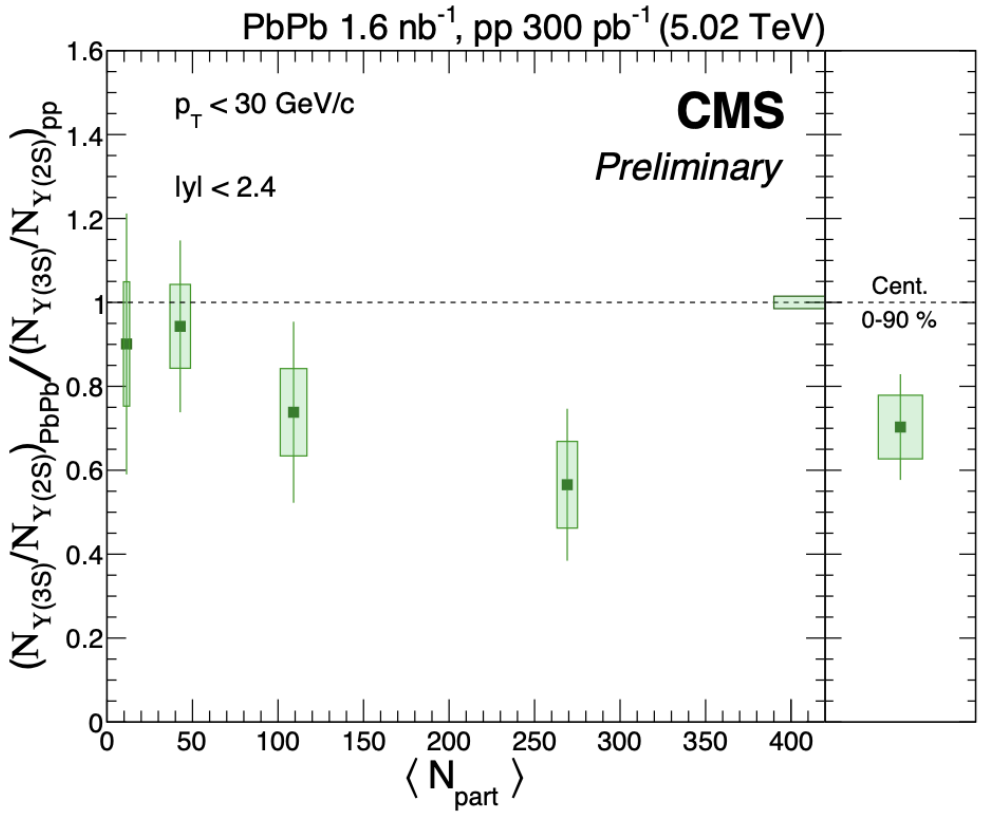
ALICE, PLB 822 (2021) 136579

ALICE pp: $\Upsilon(2S)/\Upsilon(1S) = 0.5 \pm 0.1$, arXiv:2109.15240

SHMb uncert.: nuclear-corona (fraction)

$\Upsilon(3S)/\Upsilon(2S)$ R_{AA} ratio



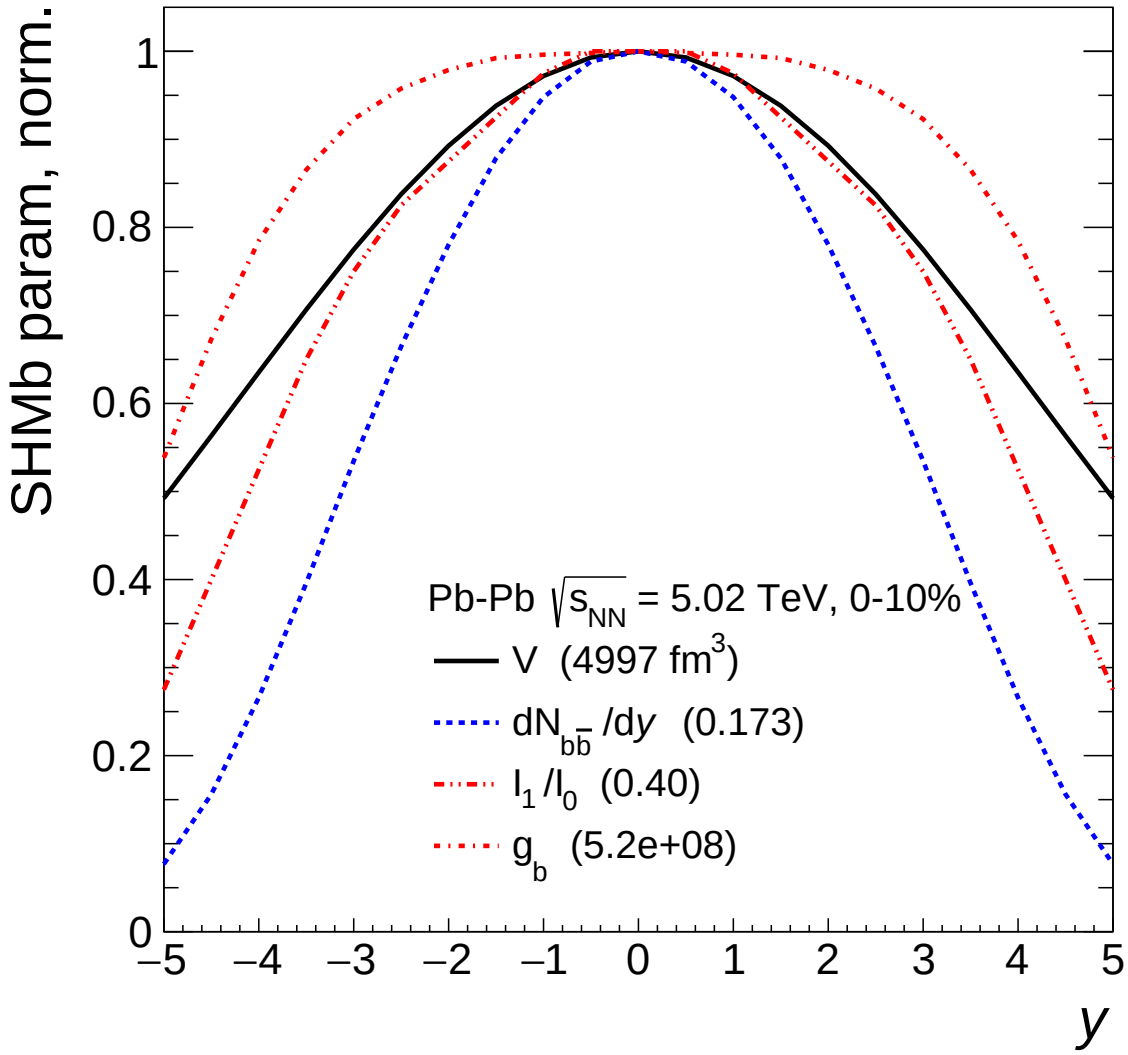


CMS, QM'22, HIN-21-007

The $\Upsilon(3S)/\Upsilon(2S)$ R_{AA} ratio is quite sensitive to the degree of b thermalization

SHMb parameters

NB: none is a free parameter, except the 30% b thermalization fraction



Summary / Conclusions: charm

In the (our) statistical hadronization model:

- The hadronization is a rapid process in which all quark flavors take part concurrently
- All charmonium and open charm states are generated exclusively at hadronization (chemical freeze-out) ...full color screening

The model is very successful in reproducting the J/ψ and open charm data

A handle for hadronization T with a mass scale well above T

"The competition":

the kinetic model, continuous J/ψ destruction and (re)generation in QGP

(only up to 2/3 of the J/ψ yield (LHC, central collisions) originates from deconfined c and $\bar{c}$ quarks)

Discriminating the two pictures implies providing an answer to fundamental questions related to the fate of hadrons in a hot deconfined medium.

A precision ($\pm$10%) measurement of $\mathrm{d}\sigma_{c\bar{c}}/\mathrm{d}y$ in Pb-Pb (Au-Au) collisions needed for a stringent test

(within reach with the upgraded detectors at the LHC and RHIC)

Summary / Conclusions: beauty

- Full beauty thermalization seems not realized in nature
  ...with 30-50% of beauty quarks fully thermalized we can explain the Υ data
  ...but this fraction is (significantly) dependent on the b-hadron spectrum

- What does non/partially-thermalized beauty produce?
  no Υ because strong coupling with the medium destroys the b-$\bar{b}$ correlation?
  ...related: is there non-screened bottomonium at all? (...or maybe just $\Upsilon(1S)$?)

- Another difficulty: $R_{AA}^{Y(1S)}(p_T)$ is flat (we would predict a bump), v_2 is small

similar to Reygers et al., PRC 101 (2020) 064905

forthcoming LHC data will (hopefully) clarify these questions (...in a while)

inspite (because:) of its simplicity SHM provides for all more sophisticated models a meaningful (powerful) limit to check (worth even if not fully realized in nature:)

EMMI Rapid Reaction Task Force - Quarkonium, 16-20.12.2019 - GSI Darmstadt

TAMU: Du, Liu, Rapp, Phys. Lett. B 796 (2019) 20
Tsinghua: PRC 86 (2012) 034906, PLB 697 (2011) 32
Santiago: E. Ferreiro at al., PLB 731 (2014) 57, JHEP 10 (2018) 094
Kent State Univ.: Kroupa, Strickland, Rothkopf, PRD 97 (2018) 016017
Duke: X. Yao et al., JHEP 01 (2021) 046
Nantes: S. Delorme et al., EPJ Web Conf. 259 (2022) 12001
Saclay: J.-P. B;aizot, M. Escobedo, PRD 104 (2021) 054034
pNRQCD: N. Brambilla et al., JHEP 08 (2022) 303
(quantum: JHEP 05 (2021) 136)
...

Homework

...restricted set, to make it more realistic to achieve it

Pb–Pb, $\sqrt{s_{NN}}$=5.02 TeV

- R_{AA} calculations vs. N_{part}, p_T ...*no feed down*
- Reaction rates vs. temperature
- $T(\tau)$ ...central cell
- A brief description of your main relevant inputs, e.g., cold-nuclear-matter effects (shadowing, nuclear absorption, Cronin), ccbar cross section $\mathrm{d}N_{c\bar{c}}/\mathrm{d}y$ (vs. pT), hot matter suppression/regeneration mechanisms (QGP and/or hadronic matter), dissociation temperature (if applicable), in-medium potential, input (reference) pT spectrum of quarkonia, etc.

Topical days - charges

Day-2: *Inelastic Quarkonium Reaction Rates*

Identify and qualitatively understand differences in charmonium and bottomonium reaction rates as used in transport models, scrutinize differences in calculating them, quantify their dependence on external parameters (momentum, temperature, binding energy, medium constituents) and develop criteria toward a more uniform framework for calculating them.

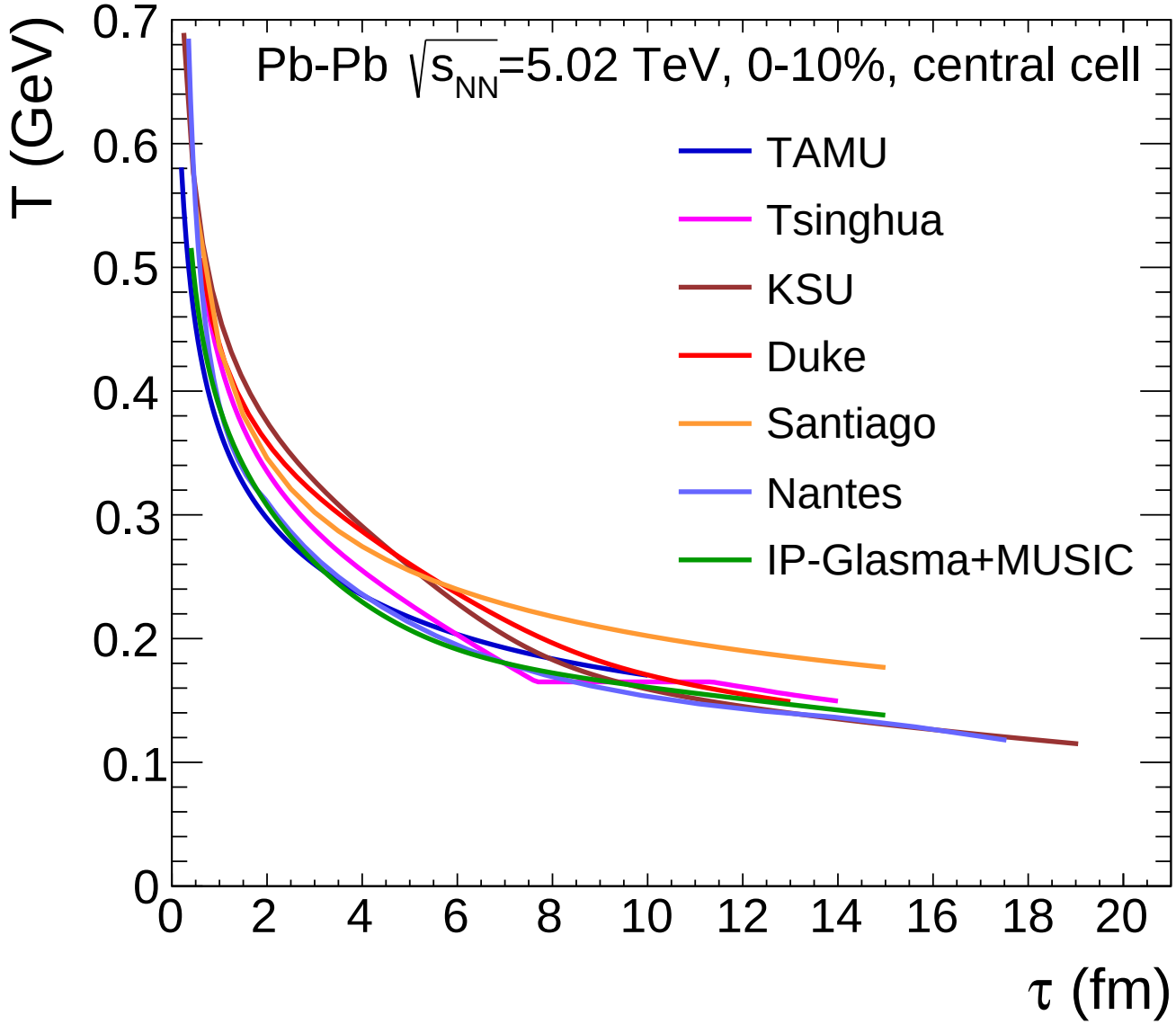
Day-3: *Quarkonium equilibrium limits and properties in hot matter*

Assess the equilibrium limit of quarkonium abundances in QGP and hadronic matter, as a key transport parameter, with critical ingredients such as the in-medium potential, Debye mass and heavy-quark masses, and how the knowledge from lattice QCD on those can be implemented in the models (using, e.g., EFT, T-matrix, potential models etc.).

Day-4: *Off-equilibrium effects in transport evolution*

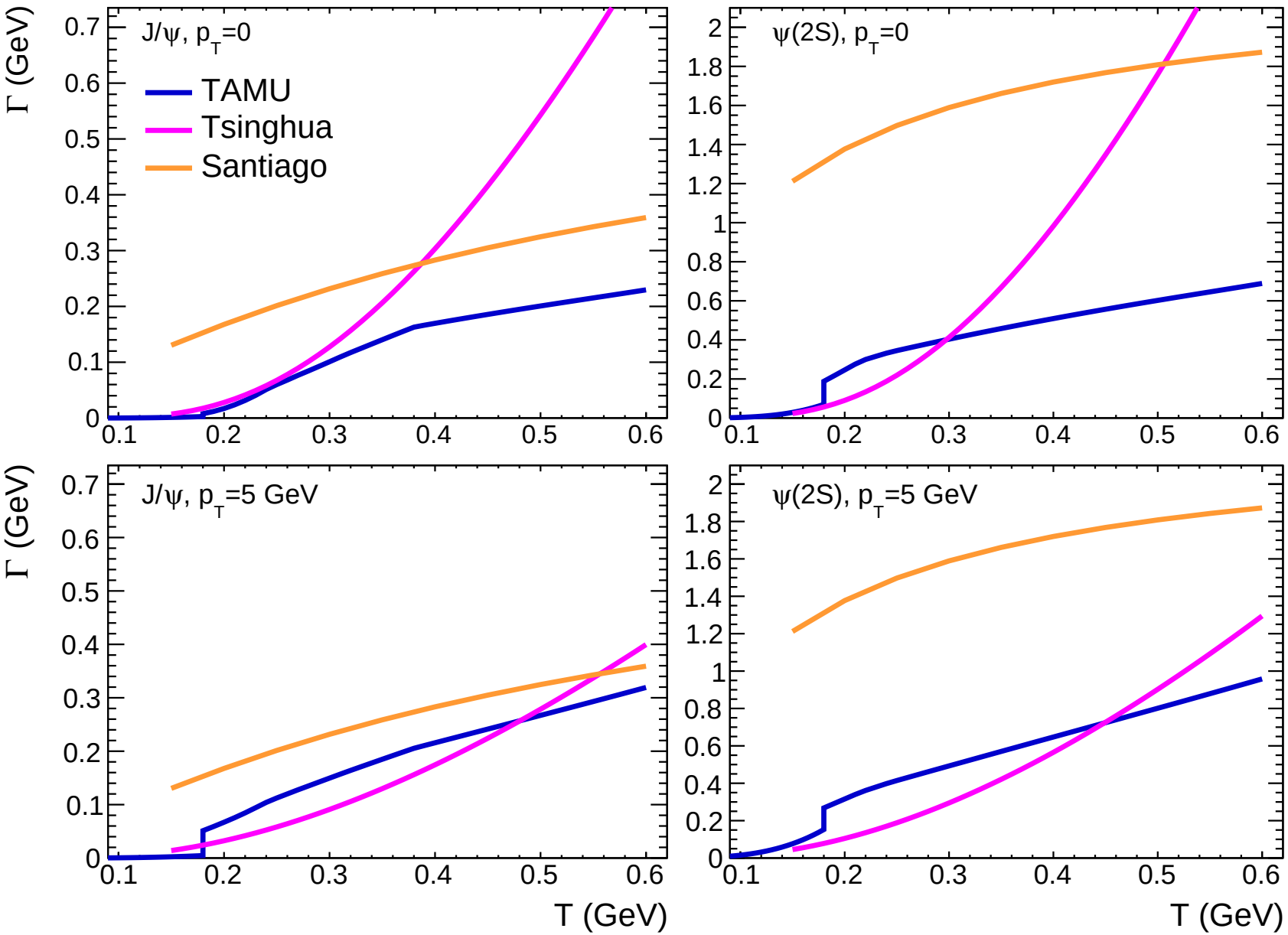
Identify off-equilibrium effects that are not encoded in the (equilibrium) transport parameters discussed during day-2 and -3 (e.g., incomplete thermalization of single heavy-quark distributions, anisotropies of the bulk medium, quantum coherence and its dissipation including initial formation time effects, equilibration of singlet vs octet channels, adiabatic limit etc.), how they are implemented and quantitatively affect the predictions for quarkonium observables in AA collisions.

Temperature

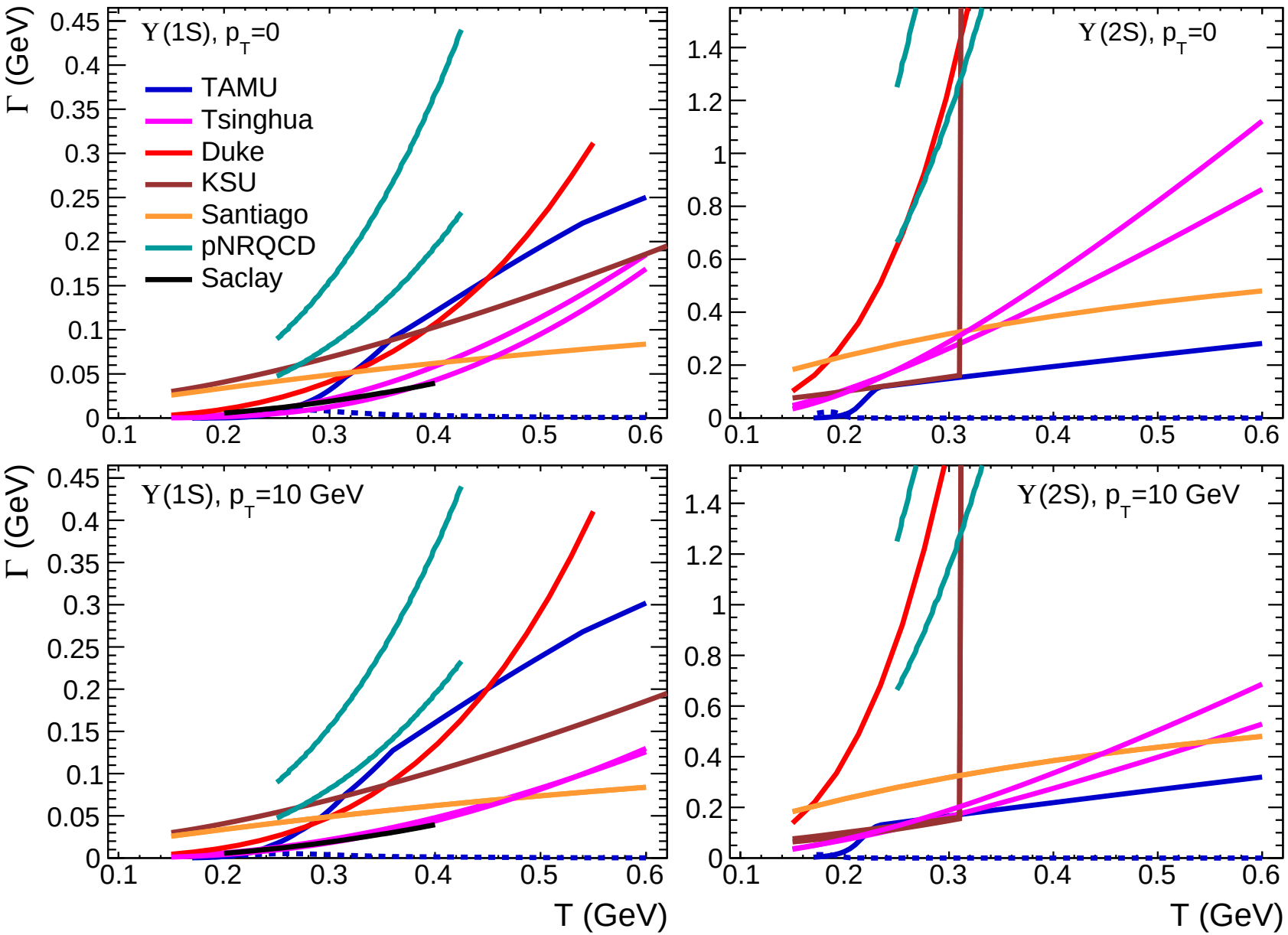


Santiago: 1-D Bjorken; SHM: IP-Glasma+MUSIC

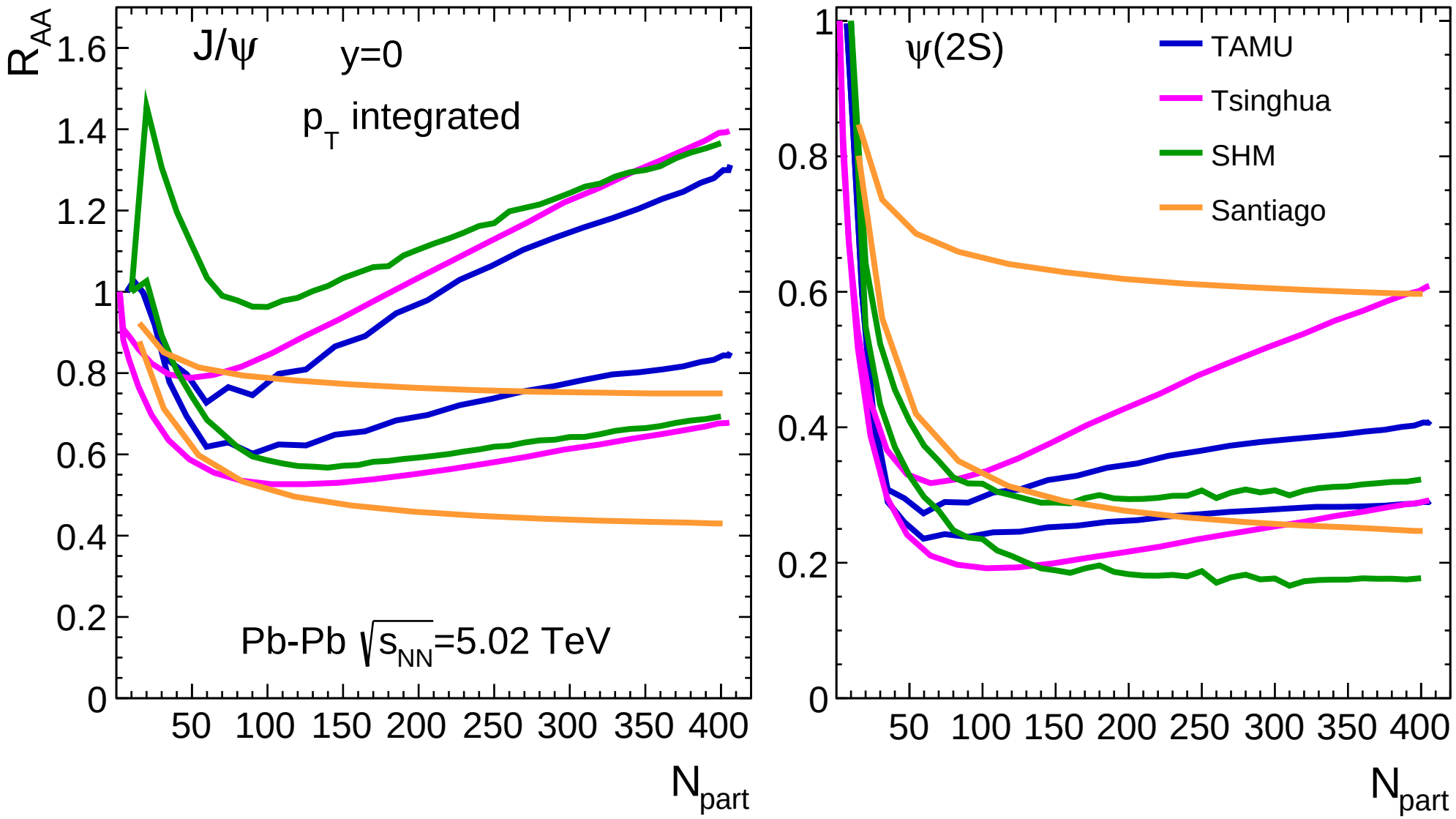
Reaction rates, ψ



Reaction rates, Υ

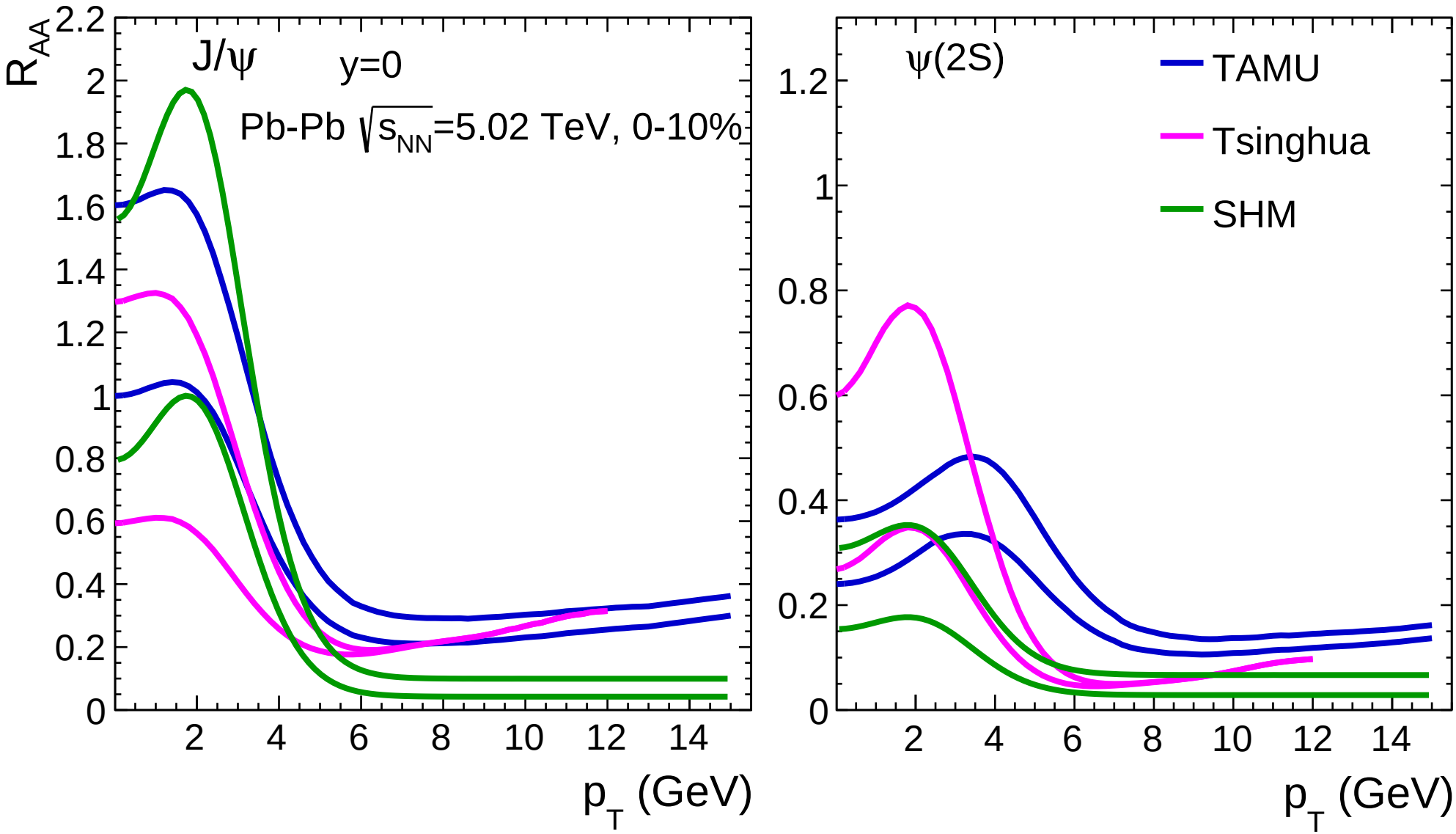


R_{AA}, ψ

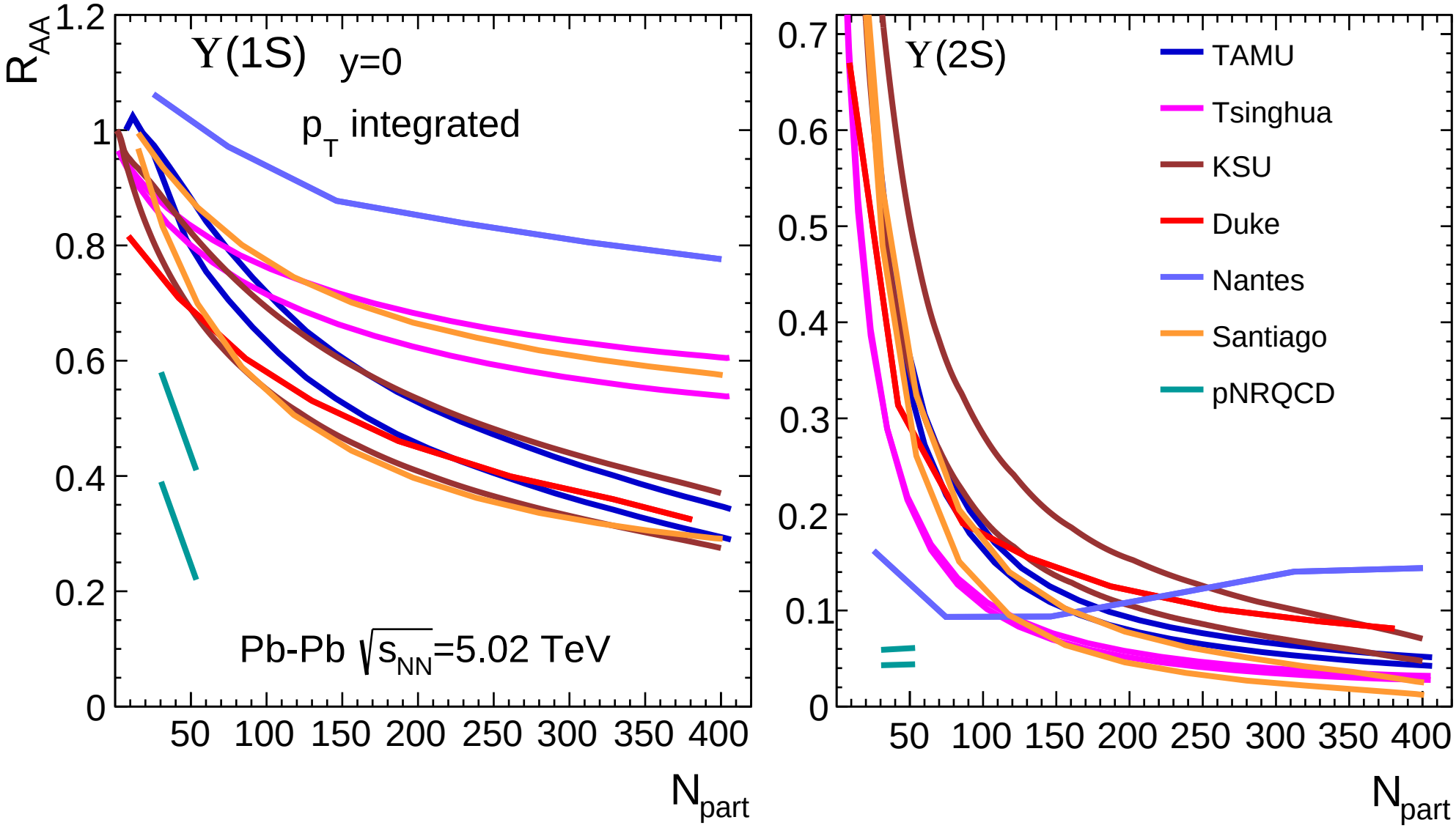

R_AA
J/ψ
y=0
p_T integrated
Pb-Pb √s_NN=5.02 TeV
N_part
ψ(2S)
TAMU
Tsinghua
SHM
Santiago
N_part

R_{AA}, ψ

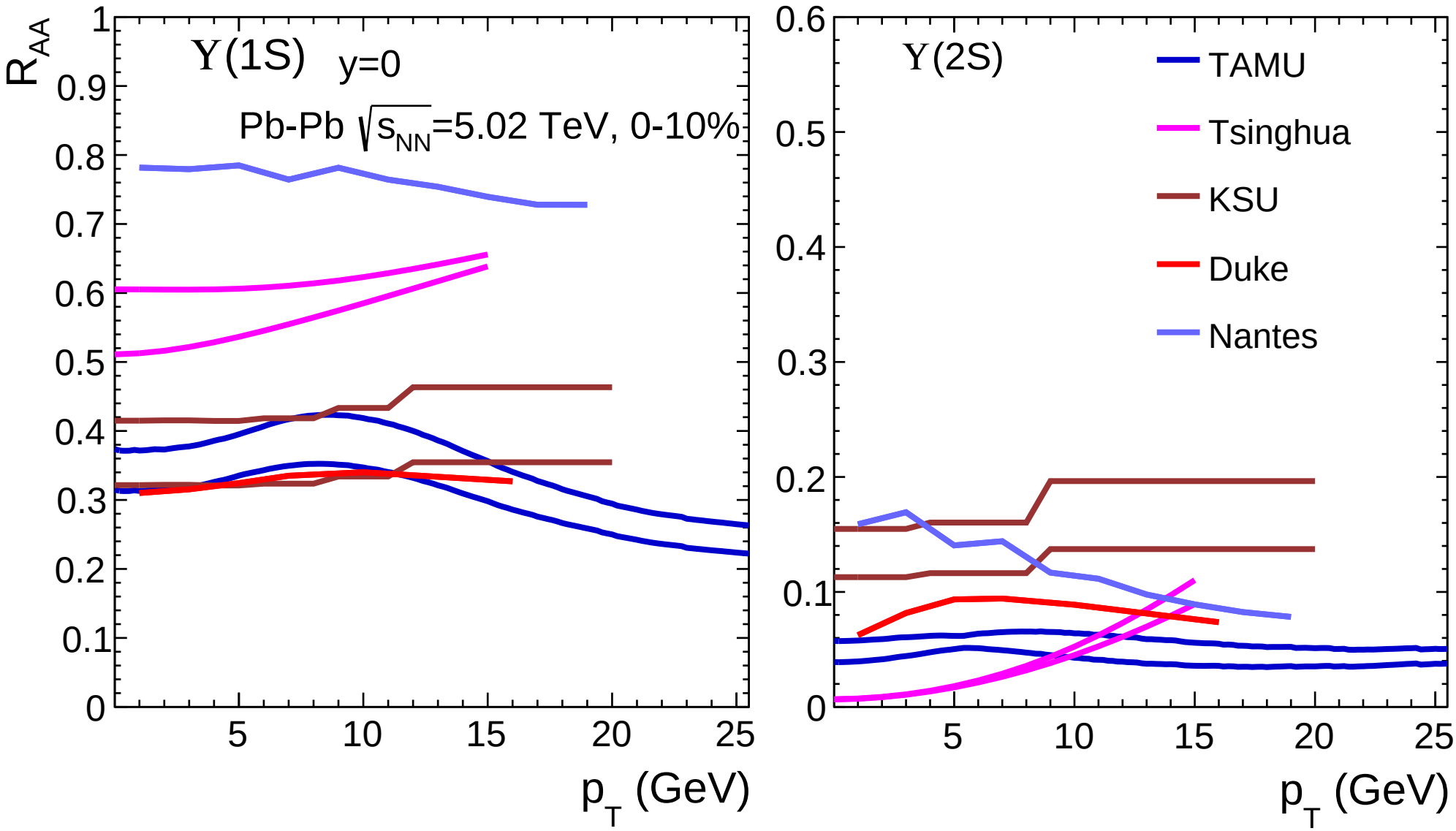
A. Andronic



R_{AA}, Υ


R_AA
Υ(1S) y=0
p_T integrated
Pb-Pb √s_NN=5.02 TeV
N_part
Υ(2S)
TAMU
Tsinghua
KSU
Duke
Nantes
Santiago
pNRQCD
N_part

R_{AA}, Υ


R_{AA}
Υ(1S) y=0
Pb-Pb $\sqrt{s_{NN}}$=5.02 TeV, 0-10%
Υ(2S)
TAMU
Tsinghua
KSU
Duke
Nantes
p_T (GeV)
p_T (GeV)

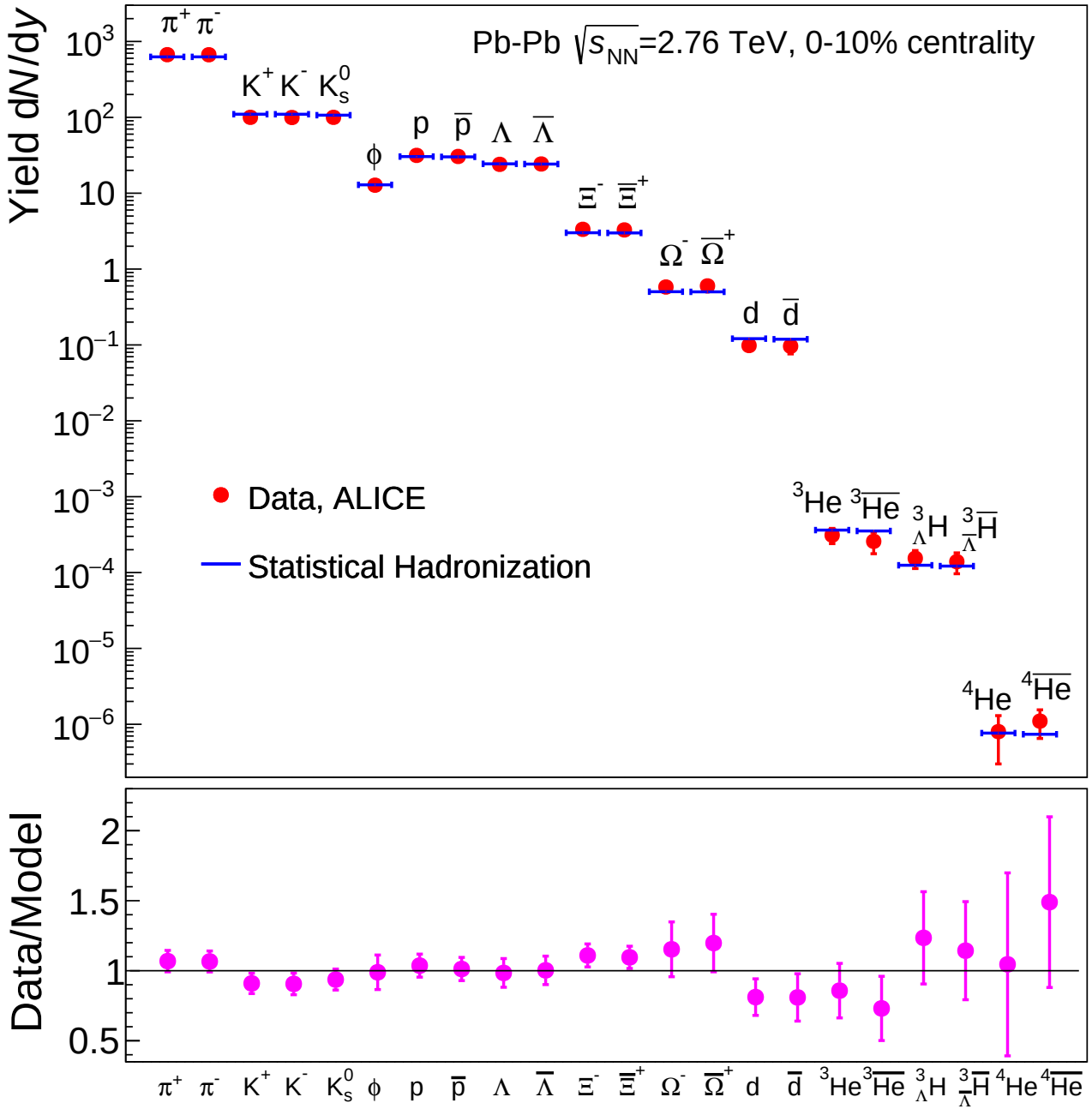
EMMI RRTF - Conclusions

"it's not easy"

we revived the RRTF (2022)
...with the aim to converge on the model intercomparison (in a writeup)

Extra slides SHM

Thermal fit – LHC, Pb–Pb, 0-10%



matter and antimatter produced in equal amounts

$T_{CF} = 156.6 \pm 1.7$ MeV
$\mu_B = 0.7 \pm 3.8$ MeV
$V_{\Delta y=1} = 4175 \pm 380$ fm^3

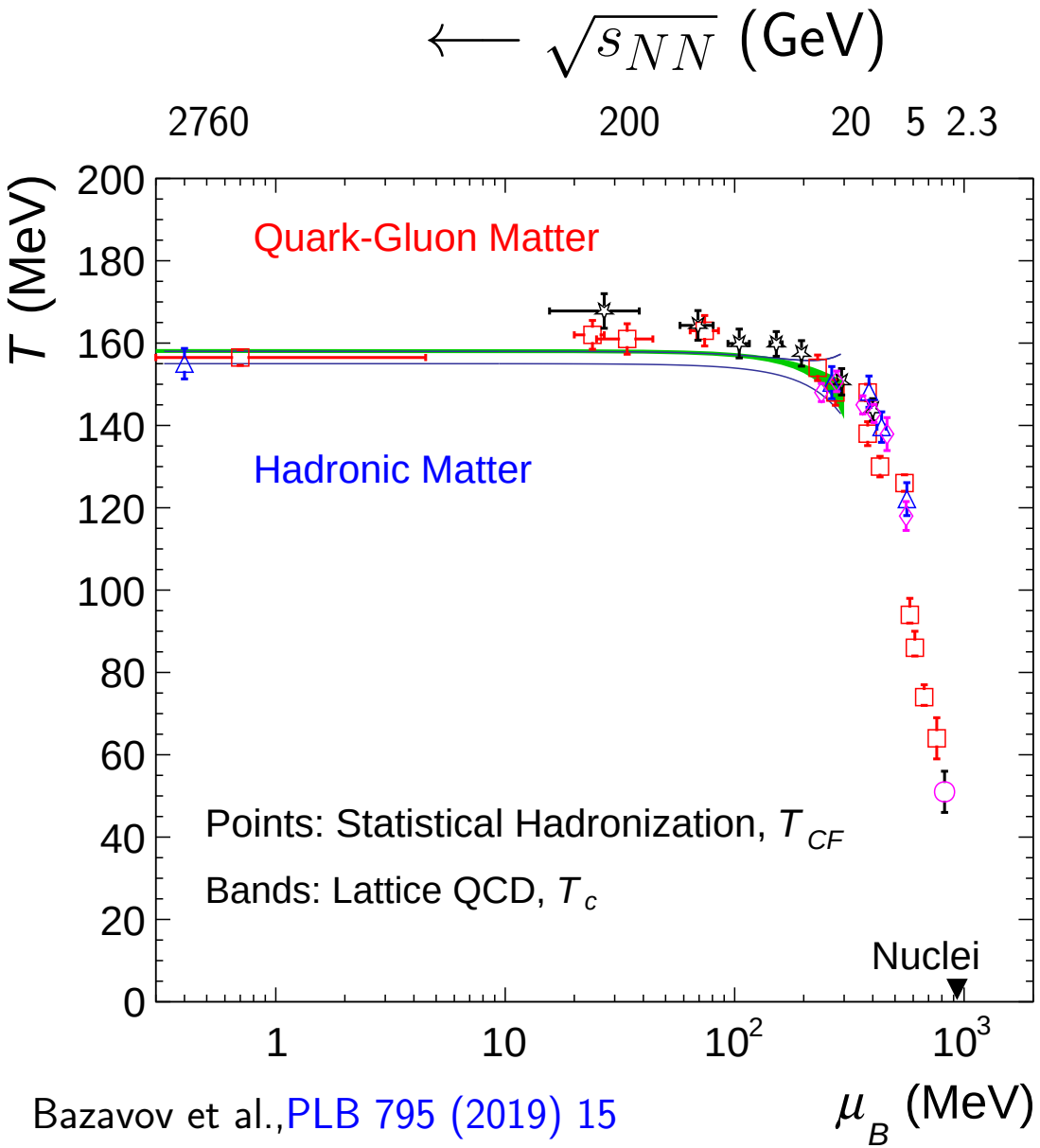
$\chi^2/N_{df} = 16.7/19$

S-matrix treatment

remarkably, loosely-bound objects are also well described ($^3_\Lambda$H with 25% B.R.)

hadronization as bags of quarks and gluons?

The phase diagram of QCD



Bazavov et al., PLB 795 (2019) 15
Borsanyi et al., PLB 370 (2014) 99

at LHC, remarkable "coincidence" with Lattice QCD results

at LHC ($\mu_B \simeq 0$): purely-produced (anti)matter ($m = E/c^2$), as in the Early Universe

$\mu_B > 0$: more matter, from "remnants" of the colliding nuclei

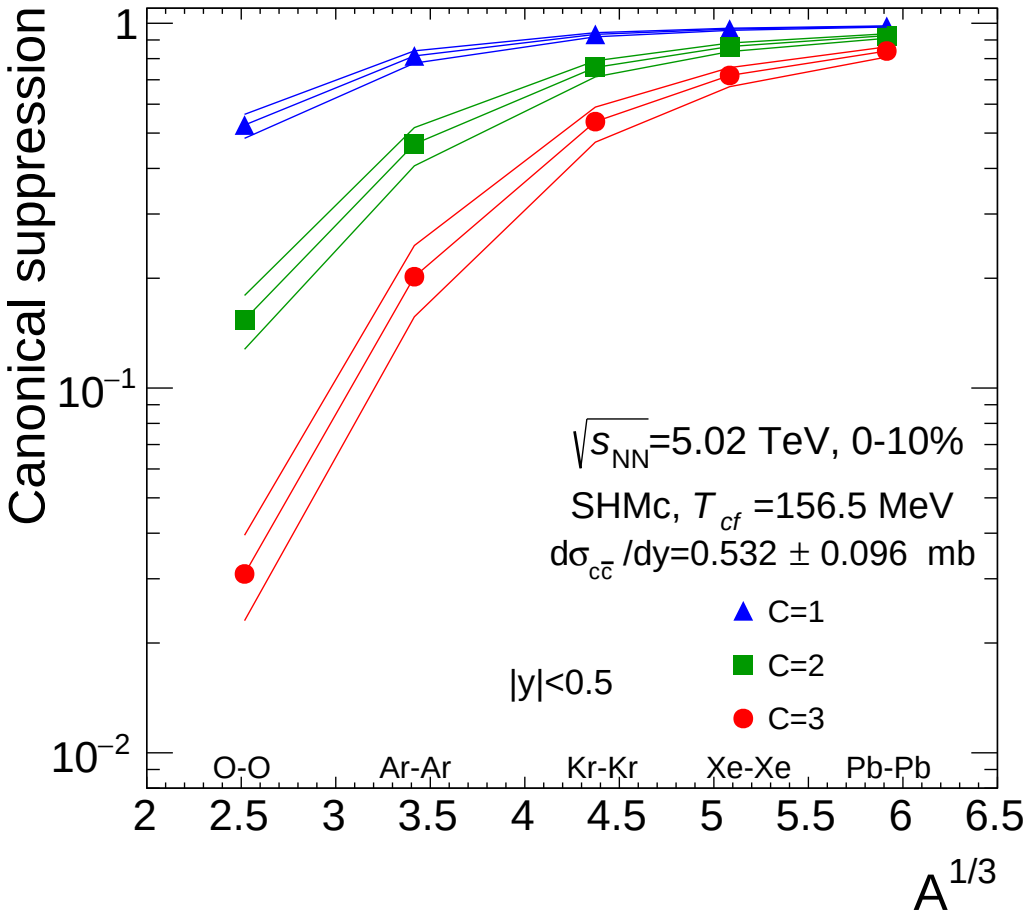
$\mu_B \gtrsim 400$ MeV: *the critical point awaiting discovery*

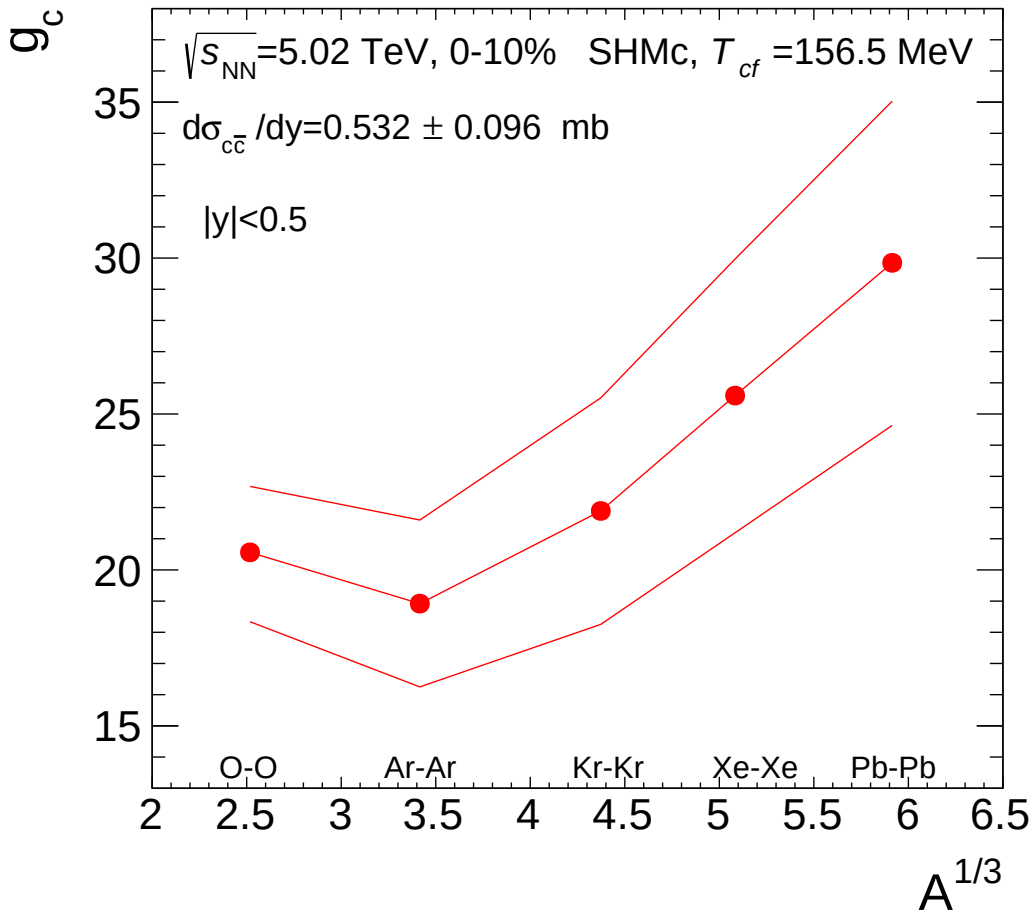
(RHIC BES / FAIR)

see refs. in Nature 561 (2018) 321

points: independent analyses of same data → "model/code uncert." are small

SHMc: system dependence (central, 0-10%)

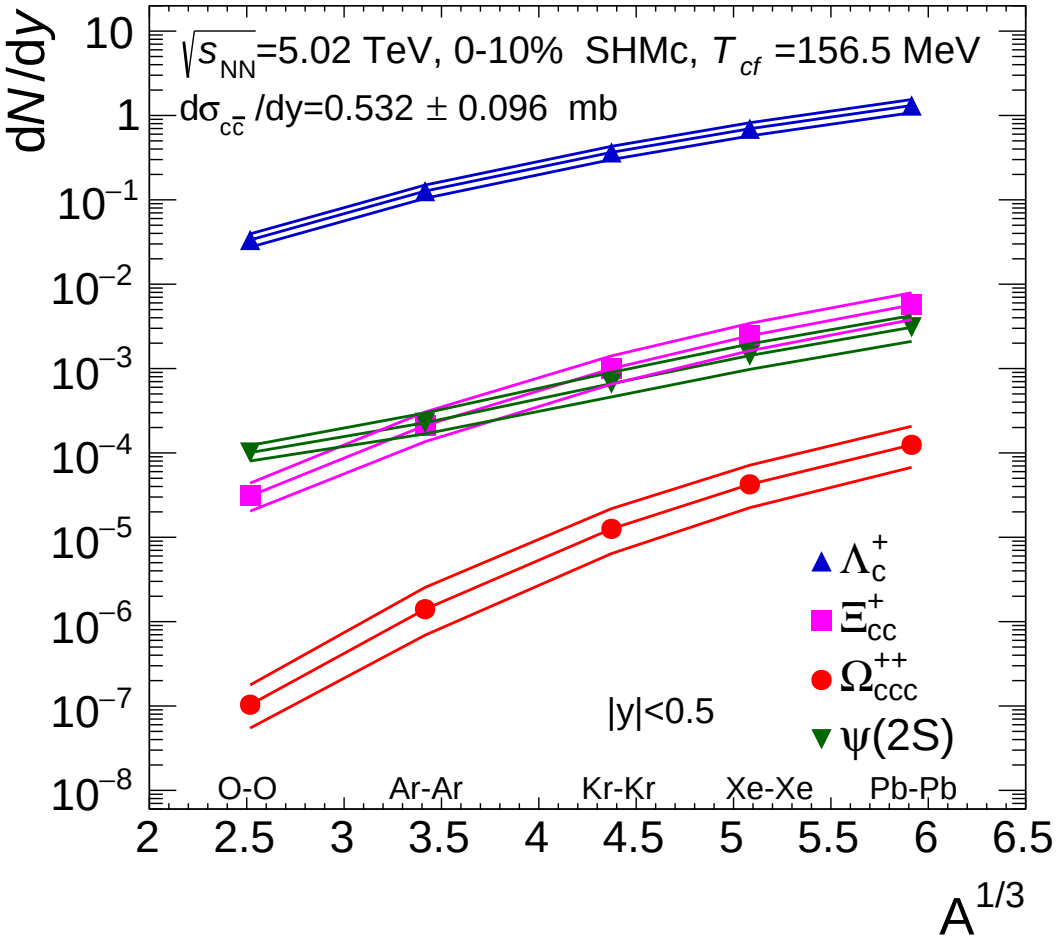


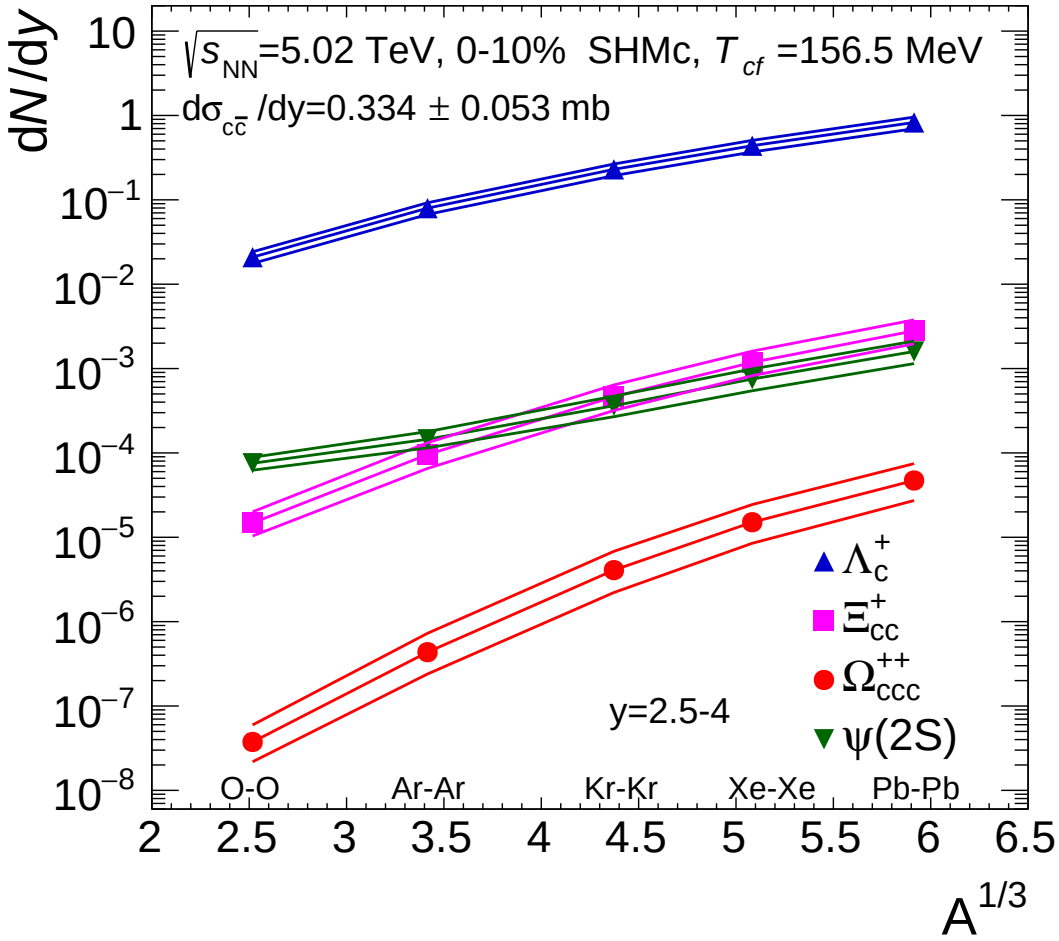


Strong canonical suppression for light systems (for multi-charm hadrons)

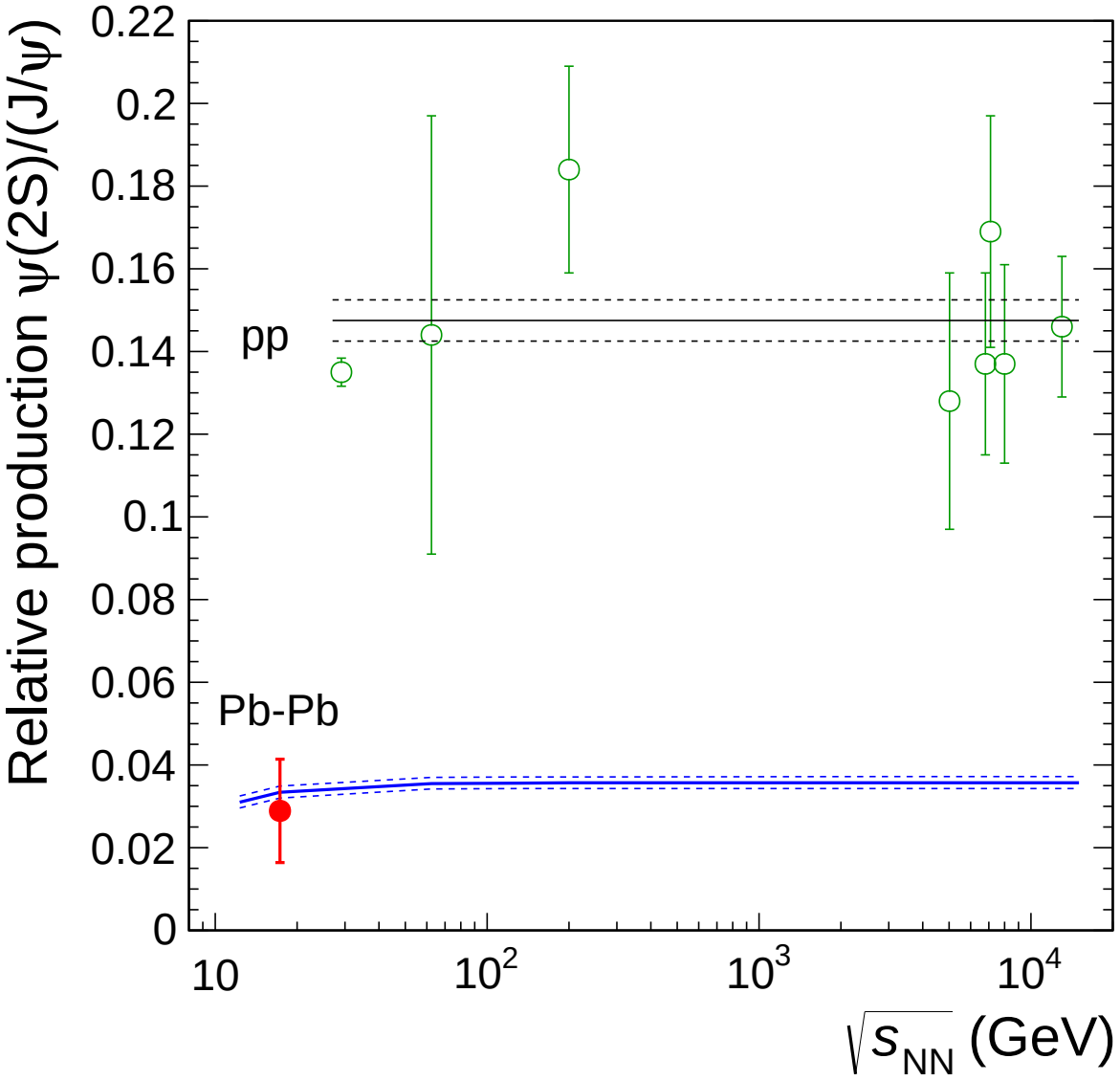
SHMc: system dependence (central, 0-10%)

A. Andronic





IF charm thermalizes (fully) also at lower energies



...SHMc is easy to be extended to lower energies

AA, Braun-Munzinger, Redlich, Stachel,

PLB 659 (2008) 149

..litmus test: $\psi(2S)$ ($+v_2$, R_{AA})

SHMc works (was proposed) at SPS

Braun-Munzinger, Stachel, PLB 490 (2000) 196

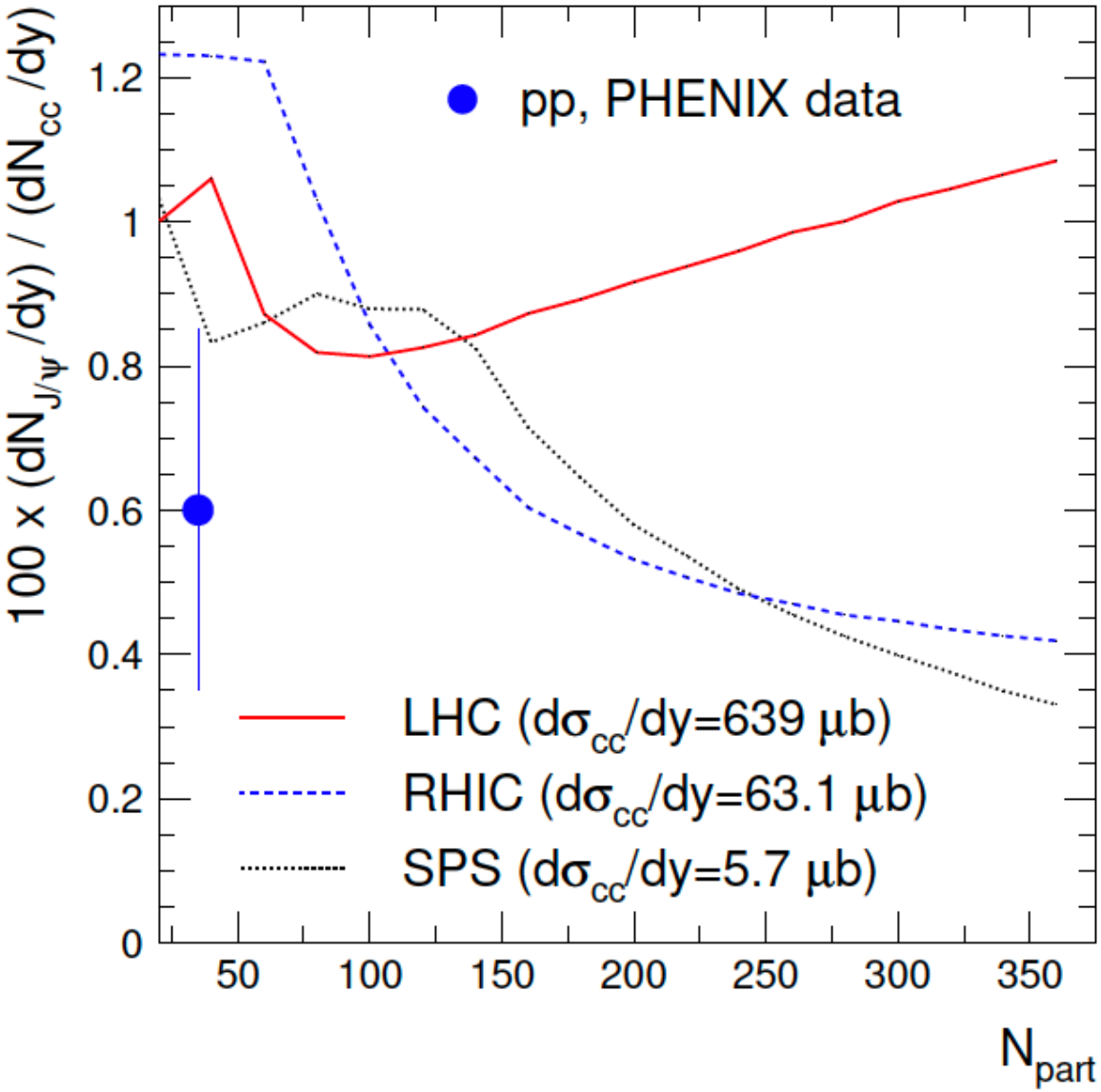
for D, stat. hadronization is a simpler act, may be at work in pp and in e^+e^-

PLB 678 (2009) 350

The measurement in Pb–Pb at LHC is a central goal for Run 3,4 (YR, WG5 HL-LHC)

J/ψ production relative to charm

...an observable with similar features as R_{AA}



NPA 789 (2007) 334

(see also: Satz, Adv.HEP 2013 (2013) 242918)

- similar values at RHIC and SPS

  ...with differences in fine details

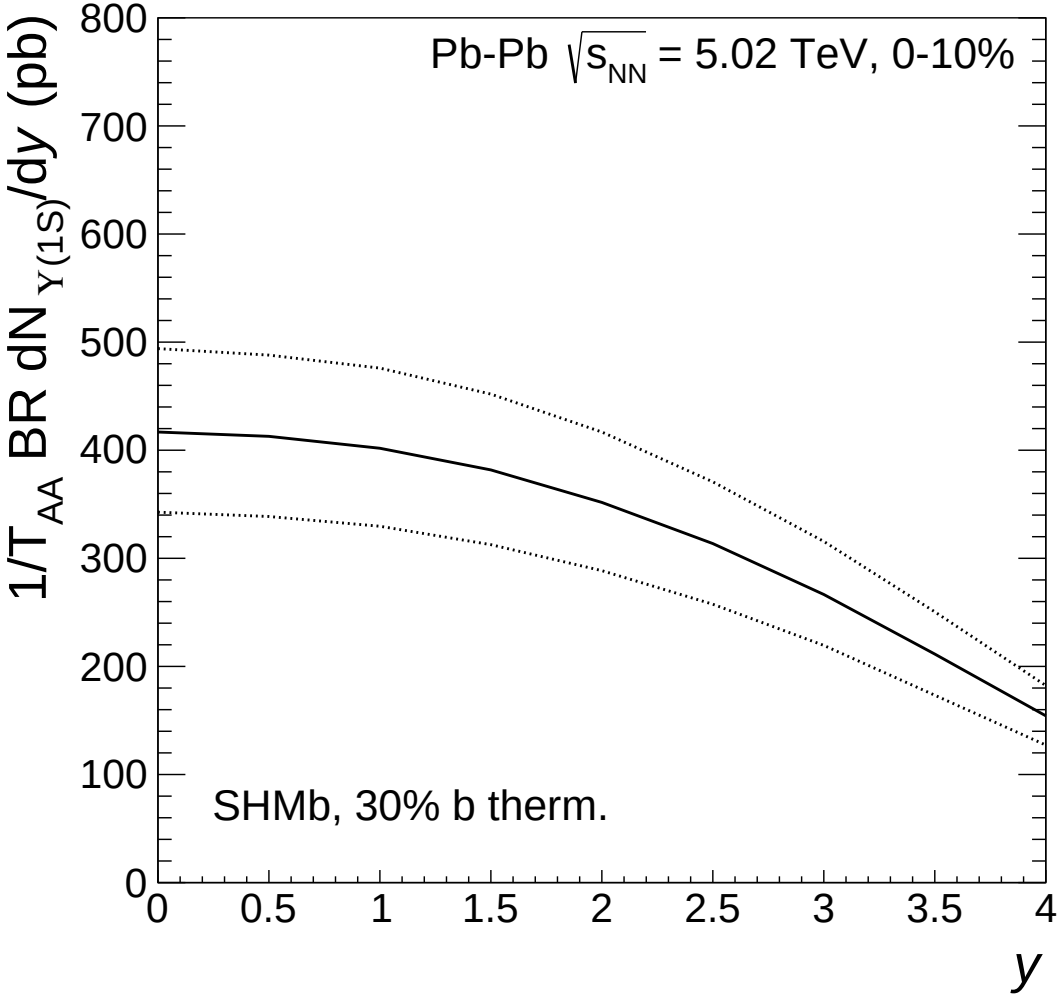
  ...determined by canonical suppression of open charm

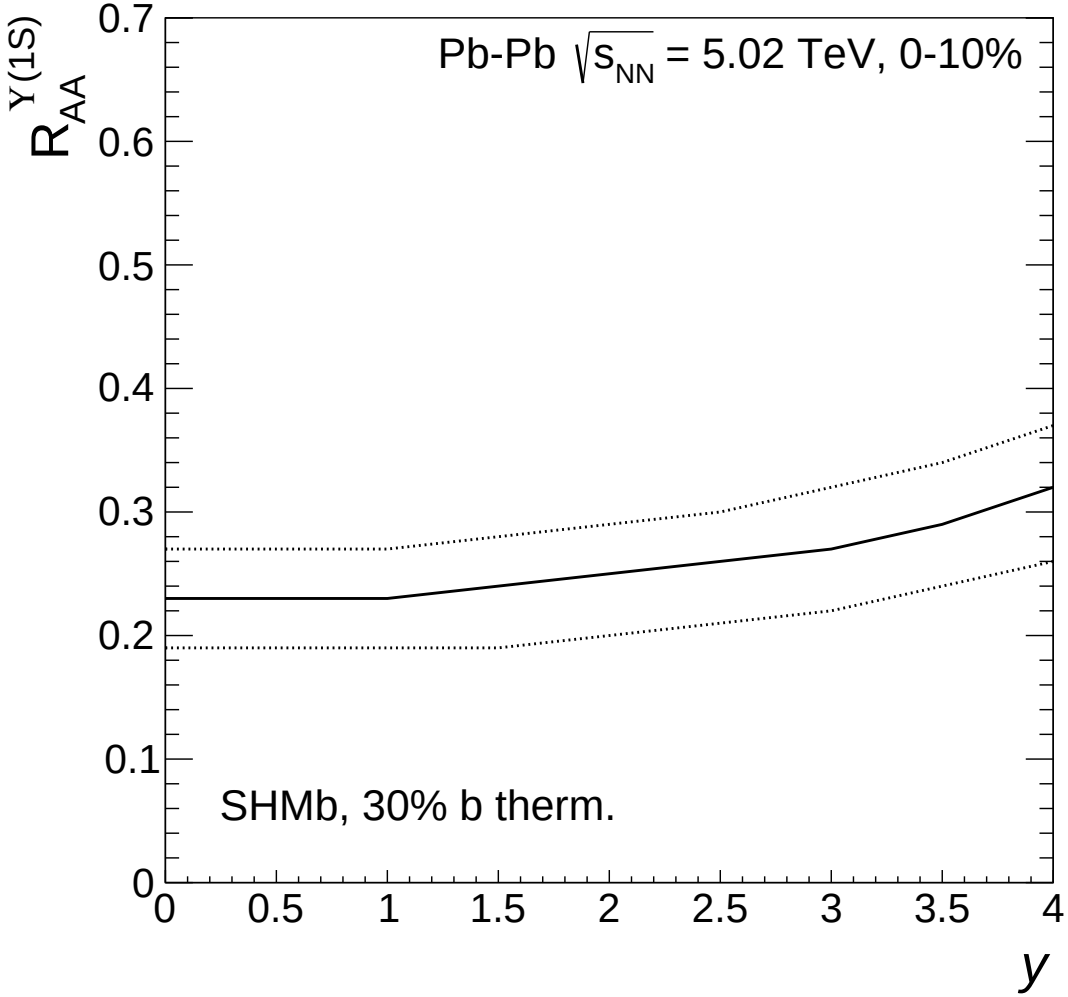
  same features in RHIC BES data (talk, K.Smith)

- enhancement-like at LHC

  can. suppr. lifted, quadratic term dominant

Rapidity dependence $\Upsilon(1S)$, 30% $b\bar{b}$ thermalized



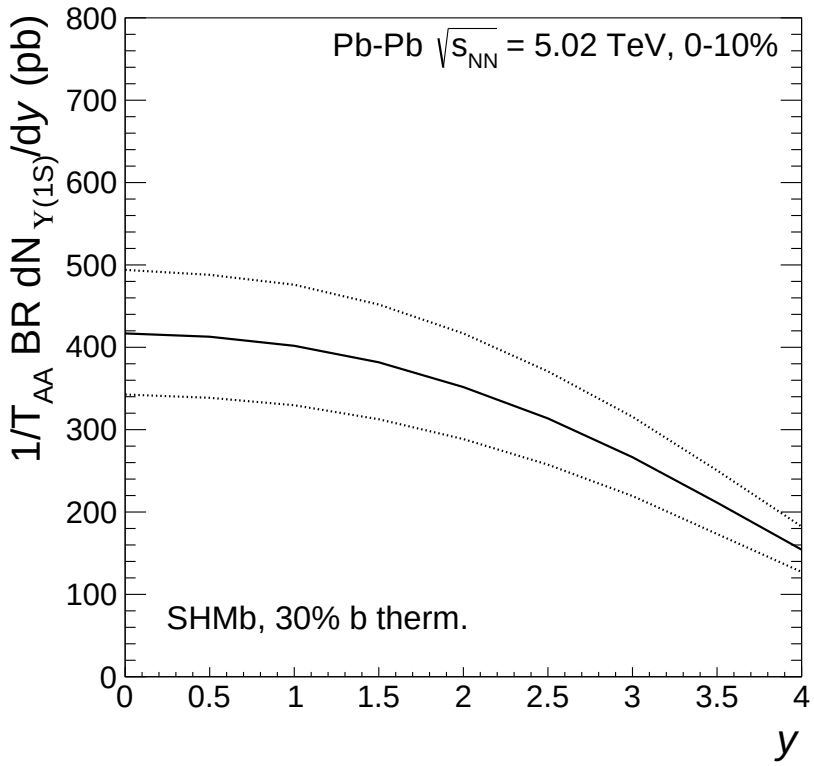


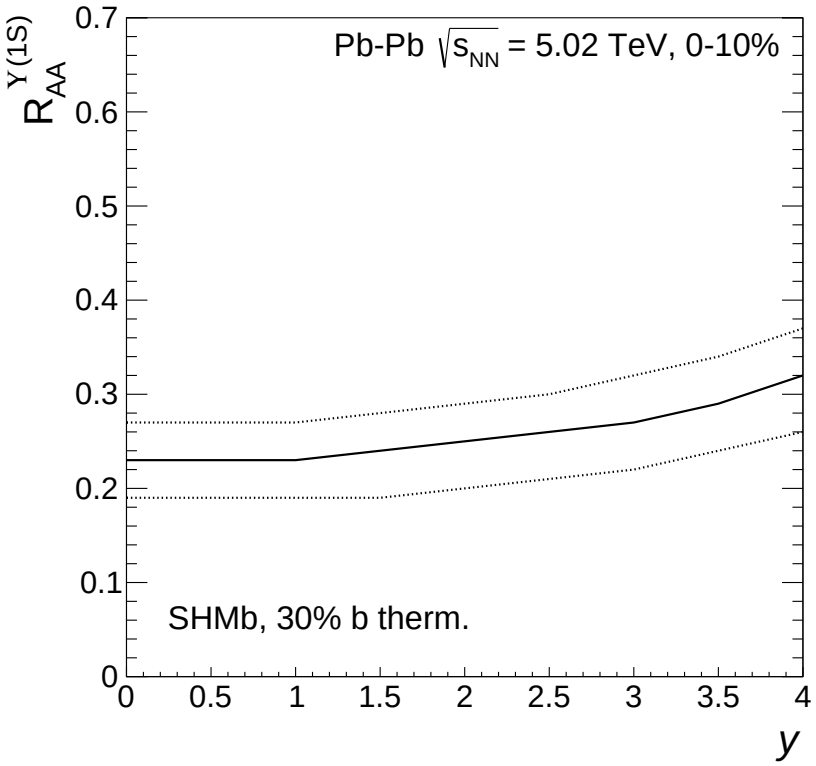
Data available only centrality-integrated ...is 0-10% (or 0-20%) doable?

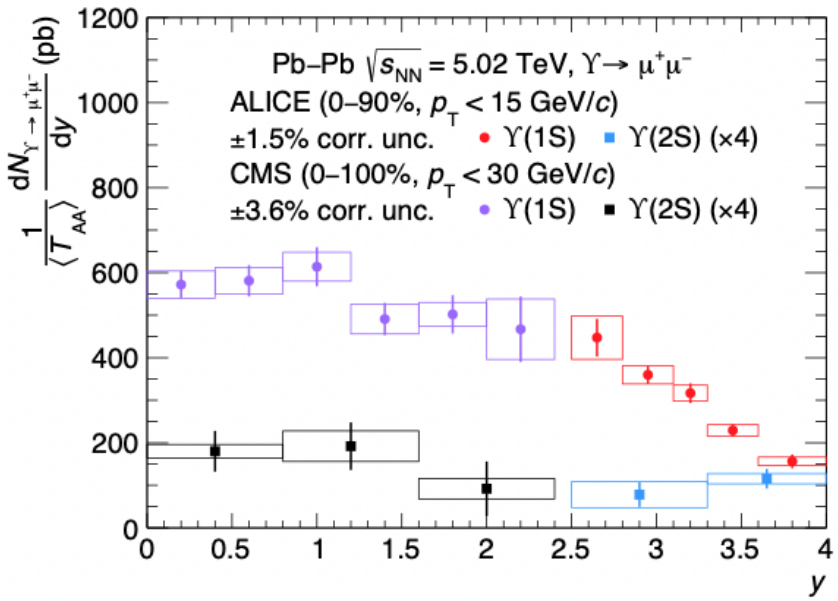
CMS, PRL 120 (2018) 142301; ALICE, PLB 822 (2021) 136579

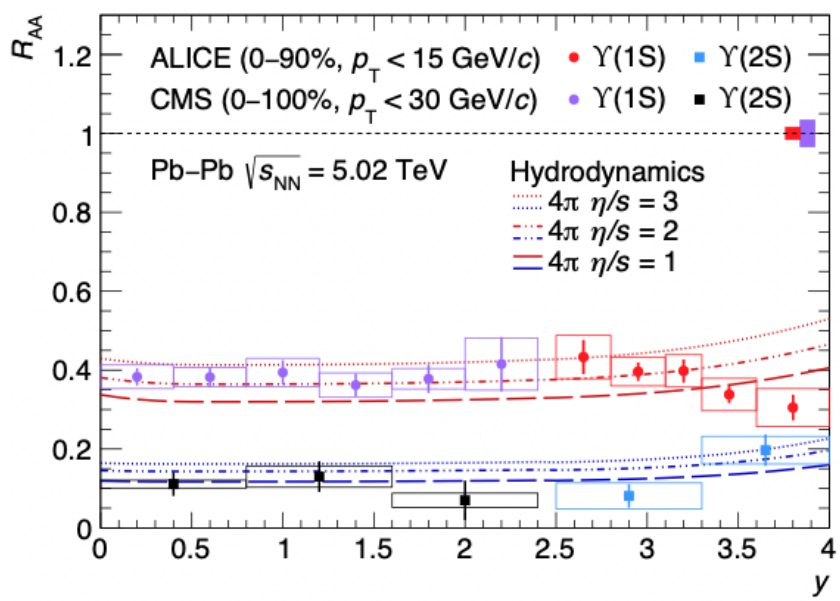
Rapidity dependence $\Upsilon(1S)$, 30% $b\bar{b}$ thermalized

A. Andronic









ALICE, PLB 822 (2021) 136579, CMS, PRL 120 (2018) 142301