

Heavy-flavour meson and baryon production in high-energy nucleus-nucleus collisions

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INFN - Sezione di Torino

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Heavy-particle diffusion: physics motivation

Goal: getting access to the **microscopic properties of the background medium** in which the Brownian particle propagates

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$$\mathcal{N}_A = \frac{\mathcal{R}T}{6\pi a \eta D_s} \approx 5.5 - 7.2 \cdot 10^{23}$$

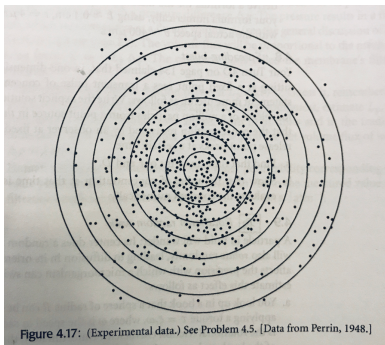


Figure 4.17: (Experimental data.) See Problem 4.5. [Data from Perrin, 1948.]

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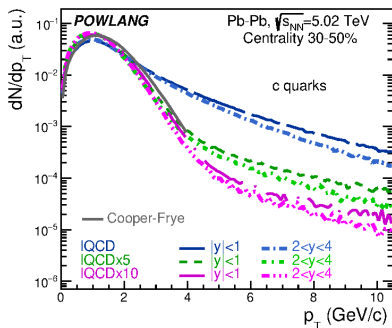
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- 100 years later: getting an estimate of similar accuracy of some transport coefficients, like e.g. the **momentum broadening**

$$\kappa = \frac{2T^2}{D_s}$$



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In HF studies in nuclear collisions the **nature of the Brownian particle changes** during its propagation through the medium

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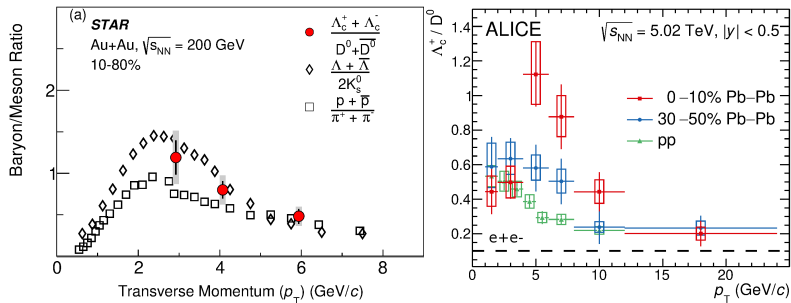
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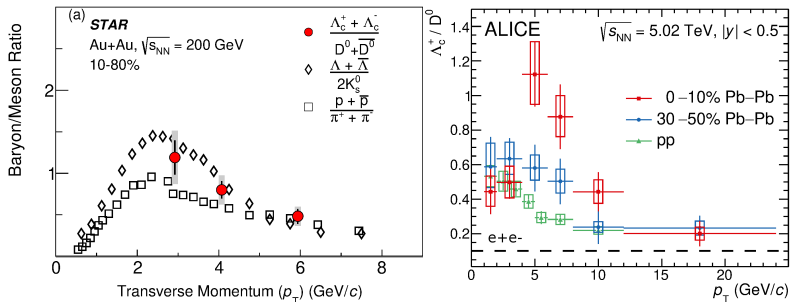
- possible thermal mass-shift (here neglected)
- **hadronization** (impossible to neglect)
 - source of systematic uncertainty in extracting transport coefficients;
 - an issue of interest in itself: how **quark \rightarrow hadron transition** changes **in the presence of a medium** (the topic of this talk)

HF hadronization: experimental findings



Strong **enhancement of charmed baryon/meson ratio**, incompatible with hadronization models tuned to reproduce e^+e^- data

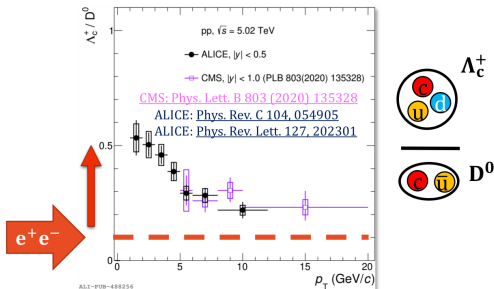
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- pattern similar to light hadrons
- baryon **enhancement observed also in pp collisions**: is a dense medium formed also there? **Breaking of factorization** description in pp collisions

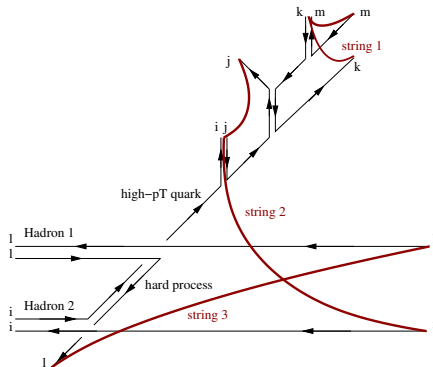
$$d\sigma_h \neq \sum_{a,b,X} f_a(x_1) f_b(x_2) \otimes d\hat{\sigma}_{ab \rightarrow c\bar{c}X} \otimes D_{c \rightarrow h_c}(z)$$

Hadronization models: common features

Grouping colored partons into color-singlet structures: strings (PYTHIA), clusters (HERWIG), hadrons (coalescence).

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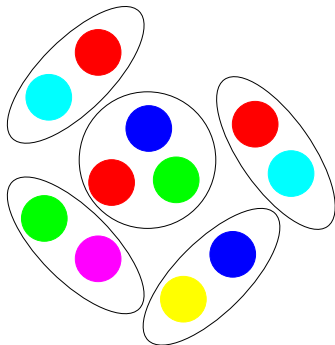
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- in “elementary collisions”: from the hard process, shower stage, underlying event and beam remnants;

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Grouping colored partons into color-singlet structures: strings (PYTHIA), clusters (HERWIG), hadrons (coalescence). Partons taken



- in “elementary collisions”: from the hard process, shower stage, underlying event and beam remnants;
- in heavy-ion collisions: from the hot medium produced in the collision. NB Involved **partons closer in space** in this case and this has deep consequence!

Our new hadronization model

Once a c quarks reaches a fluid cell at $T_H = 155$ MeV it is recombined with a light antiquark or diquark, assumed to be thermally distributed (for more details see [A.B. et al., 2202.08732 \[hep-ph\]](#)).

- 1 Extract the medium particle species according to its thermal weight

$$n \approx g_s g_l \frac{T_H M^2}{2\pi^2} K_2 \left(\frac{M}{T_H} \right)$$

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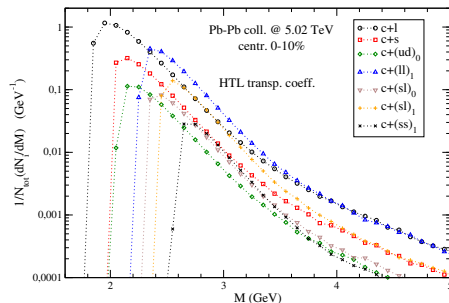
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 - Light clusters ($M_C < M_{\max}$) undergo **isotropic two-body decay** in their own rest frame, as in HERWIG;
 - Heavier clusters ($M_C > M_{\max}$) undergo string fragmentation into N hadrons, as in PYTHIA.

Cluster mass distribution

Species	g_s	g_l	M (GeV)	h_c
l	2	2	0.33000	D^0, D^+
s	2	1	0.50000	D_s^+
$(ud)_0$	1	1	0.57933	Λ_c^+
$(ll)_1$	3	3	0.77133	Λ_c^+
$(sl)_0$	1	2	0.80473	Ξ_c^0, Ξ_c^+
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$(ss)_1$	3	1	1.09361	Ω_c^0, Ξ_c^+

(masses taken from PYTHIA 6.4)

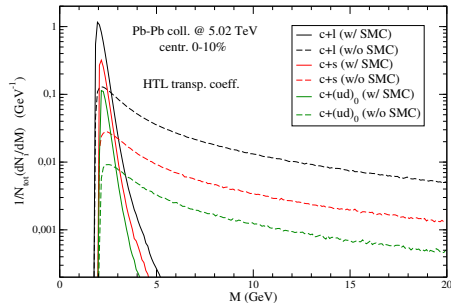


- Cluster mass distribution is steeply falling, most clusters are light and undergo a two-body decay $C \rightarrow h_c + \pi/\gamma$;
- This arises from Space-Momentum Correlation: charm momentum usually parallel to fluid velocity \rightarrow recombination occurs between quite collinear partons;

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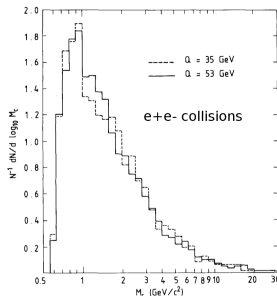
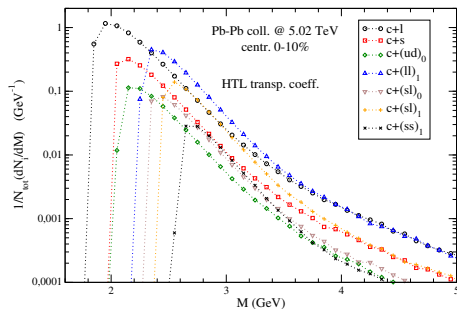
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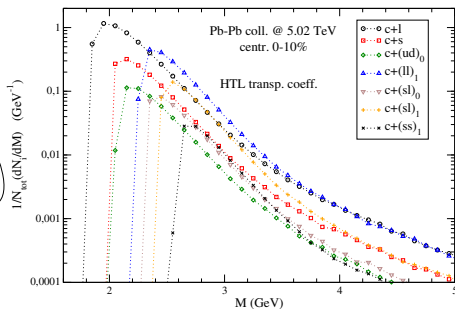
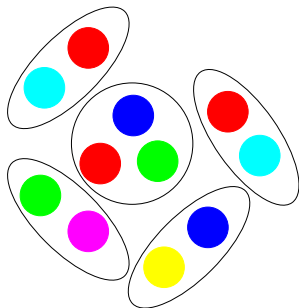
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- This arises from Space-Momentum Correlation: charm momentum usually parallel to fluid velocity \rightarrow recombination occurs between quite collinear partons;
- Cross-check: remove SMC by randomly selecting light parton from a different point on the FO hypersurface \rightarrow long high- M_c tail

On the suppression of high-mass clusters



Both in our model and in QCD event generators like e.g. HERWIG (B.R. Webber, NPB 238 (1984) 492) one gets a steeply falling M_C distribution due to preferential cluster formation between collinear partons

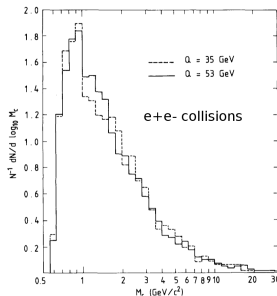
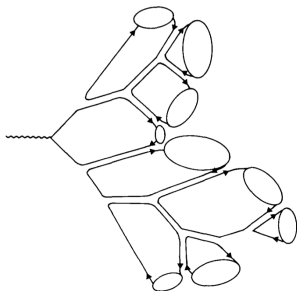
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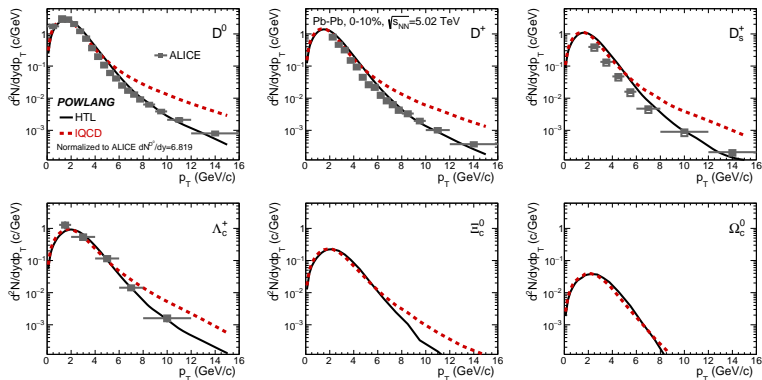
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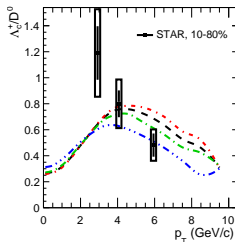
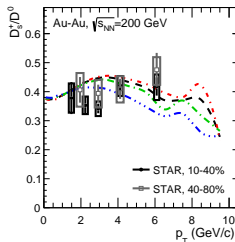
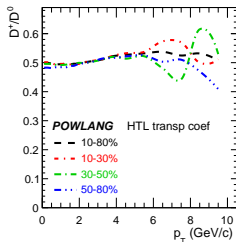
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- In Herwig, in e^+e^- collisions, this is due to the angular ordered parton shower (pre-confinement)

Results: charmed-hadron p_T -distributions



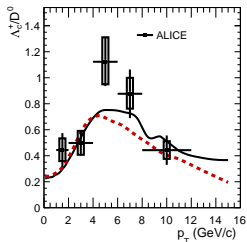
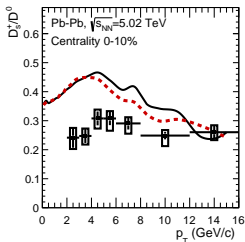
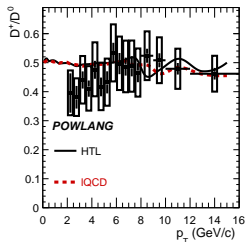
Charmed hadron p_T -spectra normalized to integrated D^0 -yield per event. At high p_T better agreement with experimental data for curves including momentum dependence of the transport coefficients (HTL curves)

Results: hadron ratios



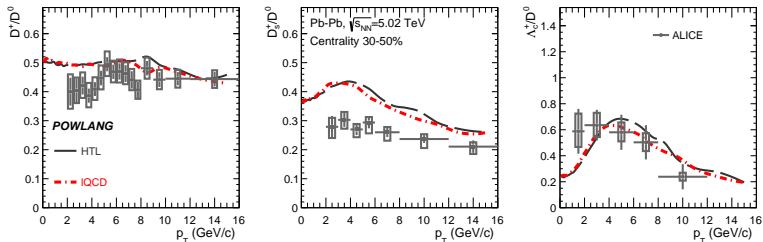
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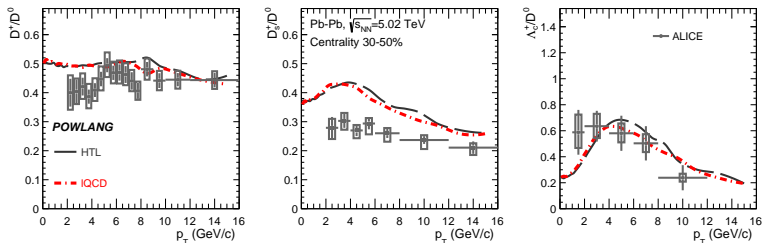
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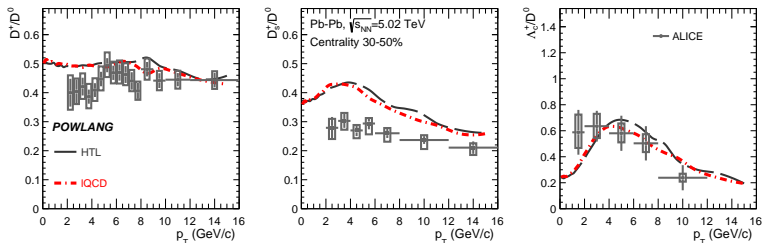
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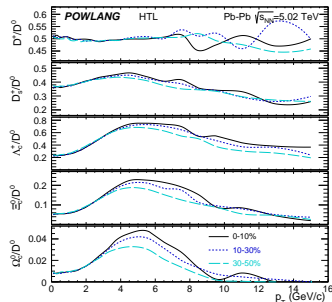
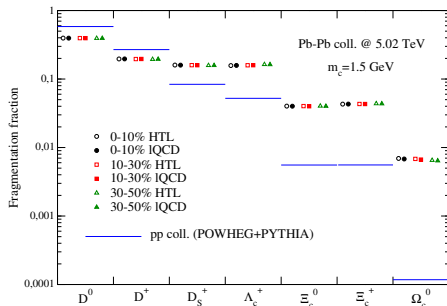
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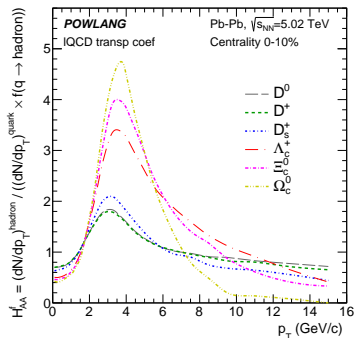
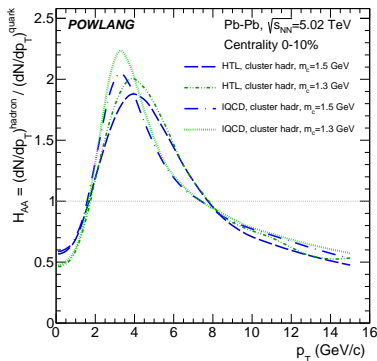
NB We have not attempted a tuning of the parameters to fit the data, e.g. quark and diquark masses taken from default values in PYTHIA

Results: fragmentation fractions



- FF's in AA collisions pretty independent from the centrality, leading simply to a reshuffling of the p_T -distribution (stronger radial flow of charmed baryons in central events);
- Strong enhancement of charmed baryon production wrt theoretical predictions by default tunings of QCD generators in pp collisions

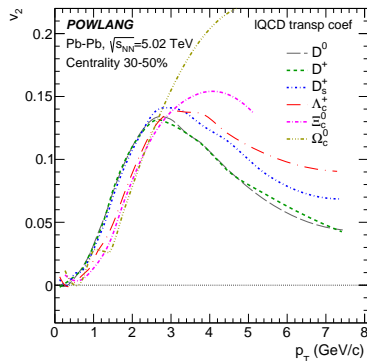
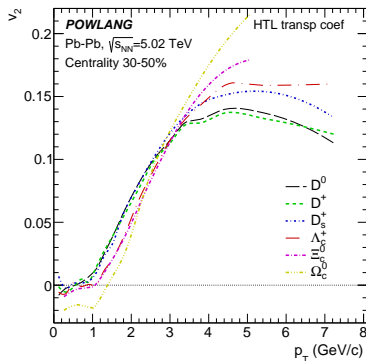
How much flow acquired at hadronization?



Big **enhancement** of charmed hadron production **at intermediate p_T**

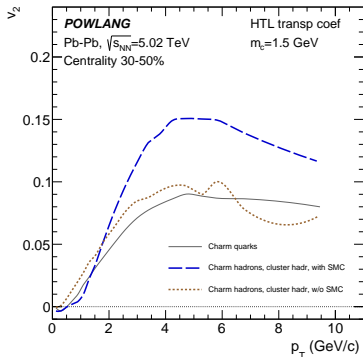
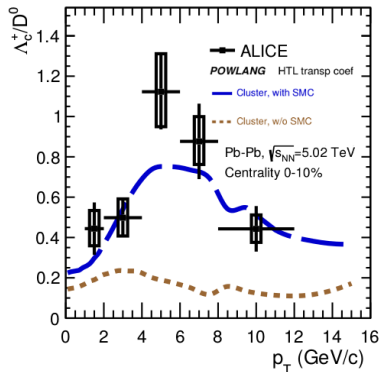
- **SMC** efficient mechanism to transfer flow from the fireball to the charmed hadrons;
- stronger signal for heaviest charmed baryons due to the **larger radial flow of the heaviest diquarks**

Results: elliptic flow



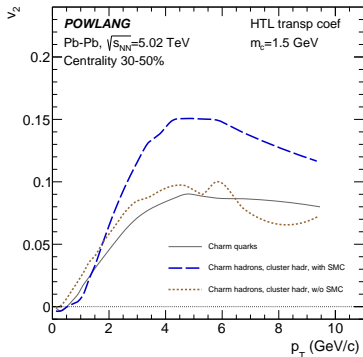
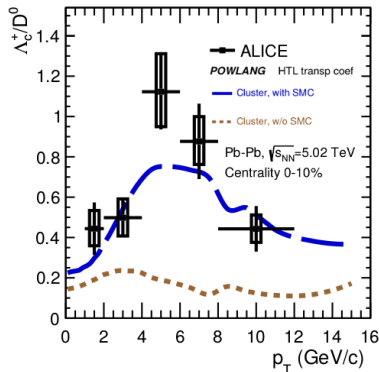
Two different bands for charmed mesons and baryons arising in our model from the higher mass of diquarks involved in the recombination process (mass scaling rather than quark-number scaling)

The role of SMC



Explore the role of SMC's combining the HQ with a thermal particle chosen from a different point on the FO hypersurface \rightarrow recombining partons no longer collinear, hence:

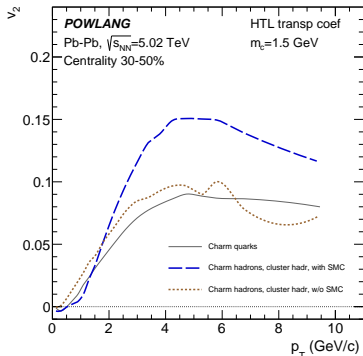
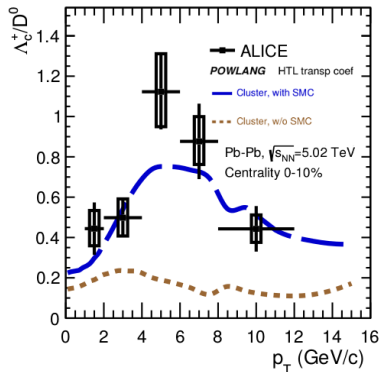
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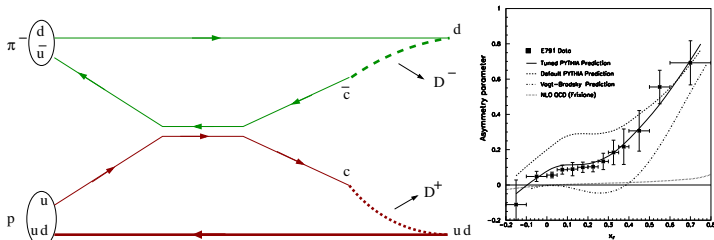
- No big enhancement of the charmed hadron v_2
- Larger invariant mass of the formed cluster \rightarrow fragmentation into a larger number of hadrons as a standard Lund string, with no modified HF hadrochemistry

Some comments

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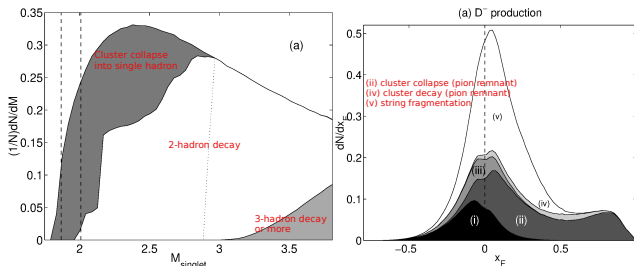


Second endpoint boosts the string along the direction of the beam-remnant (*beam-drag effect*), leading to an **asymmetry in the rapidity distribution of D^+/D^- mesons**

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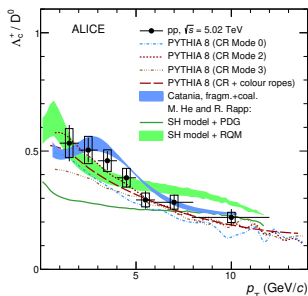


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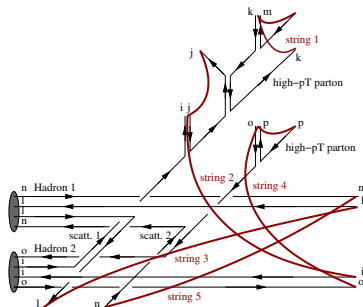
NB Small invariant-mass string can collapse into a single hadron: **non-universal flavor composition** (E. Norrbin and T. Sjostrand, EPJC 17 (2000) 137)!

On color-reconnections and pp collisions



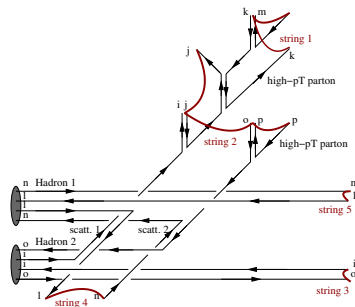
Charmed baryon enhancement in pp collisions can be accounted for in PYTHIA introducing the possibility of **color-reconnection** (CR).

On color-reconnections and pp collisions



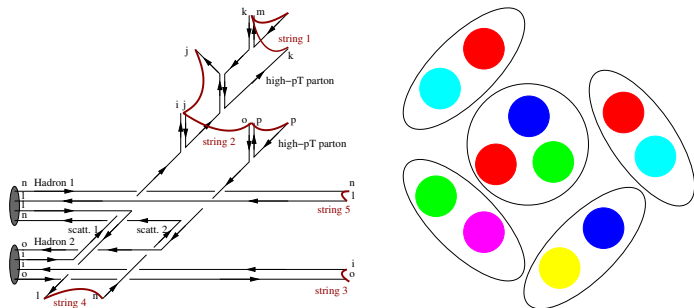
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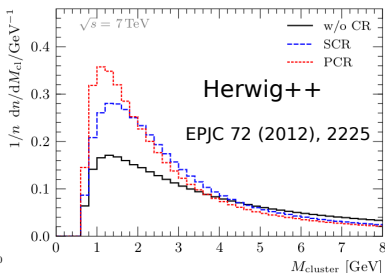
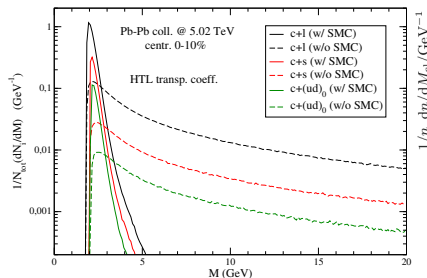
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- The **generalization** of the results **to the pp and pA case** is currently in progress.