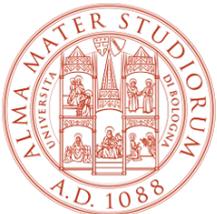


A last chance for kinetic mixing: explaining $(g-2)_\mu$ with semi-visible dark photons

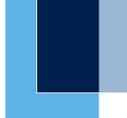
A. Abdullahi, M. Hostert, **D. Massaro**, S. Pascoli

Invisibles22 Workshop

20/06/2022



ALMA MATER STUDIORUM
UNIVERSITÀ DI BOLOGNA



UCLouvain

FNAL measurement

FNAL confirmed $(g-2)_\mu$ discrepancy with SM

$$\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = (251 \pm 59) \times 10^{-11}$$

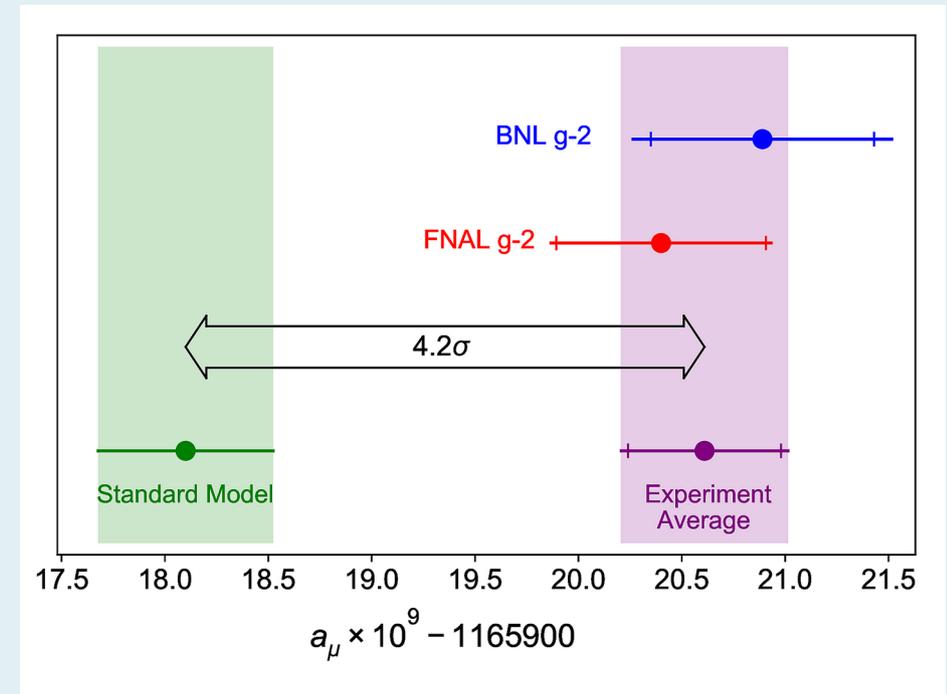
4.2 σ

Hints for new physics?

Not too far out of reach

$$\Delta a_\mu \propto \frac{g^2}{16\pi^2} \frac{m_\mu^2}{\Lambda^2} \Rightarrow \frac{\Lambda}{g} \approx \mathcal{O}(10^2) \text{ GeV}$$

*Recent comparison of Lattice Results for Leading Order Hadron Vacuum Polarization would reduce the significance to 2.9 σ . [Cè et al. (2022), arXiv:2206.06582]



[B. Abi et al. Phys. Rev. Lett. 126.14 (2021), p. 141801]

Semi-visible dark photon

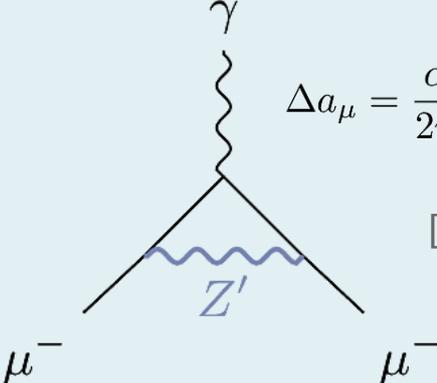
Dark U(1)' with Z' boson + dark Heavy Neutral Fermions ψ_i .

$$\mathcal{L} \supset \frac{\varepsilon}{2} B^{\mu\nu} X_{\mu\nu}$$

Kinetic mixing

Already constrained by visible
and invisible Z' searches

Positive contribution to a_μ


$$\Delta a_\mu = \frac{\alpha}{2\pi} \varepsilon^2 \int_0^1 dz \frac{2m_\mu^2 z(1-z)^2}{m_\mu^2(1-z)^2 + m_{Z',z}^2}$$

[M. Pospelov. Phys. Rev. D 80
(2009), p. 095002]

Semi-visible dark photon

Dark U(1)' with Z' boson + dark Heavy Neutral Fermions ψ_i .

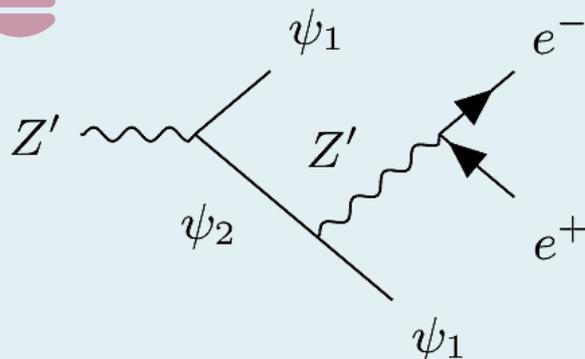
$$\mathcal{L} \supset \frac{\varepsilon}{2} B^{\mu\nu} X_{\mu\nu}$$

Kinetic mixing

Already constrained by visible and invisible Z' searches



Semi-visible final states



Positive contribution to a_μ

$$\Delta a_\mu = \frac{\alpha}{2\pi} \varepsilon^2 \int_0^1 dz \frac{2m_\mu^2 z(1-z)^2}{m_\mu^2(1-z)^2 + m_{Z',z}^2}$$

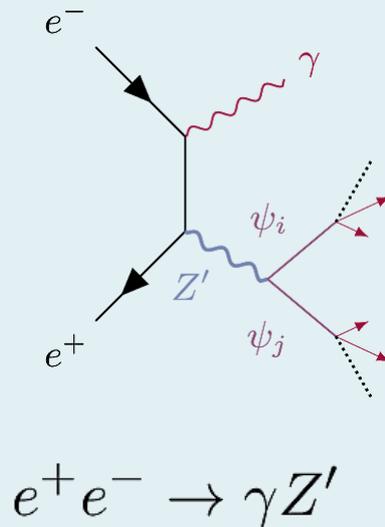
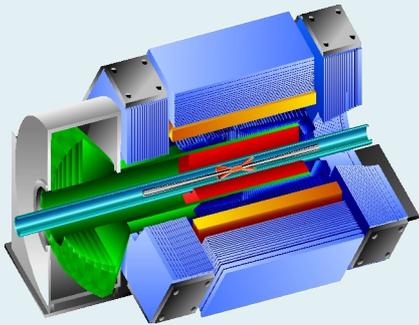
[M. Pospelov. Phys. Rev. D 80 (2009), p. 095002]

- **Missing energy:** evade visible constraints
- **Visible final states:** evade invisible constraints

[E. Izaguirre et al. Phys. Rev. D 96.5 (2017), p. 055007]
 [G. Mohlabeng. Phys. Rev. D 99.11 (2019), p. 115001]

Main constraints

BaBar monophoton



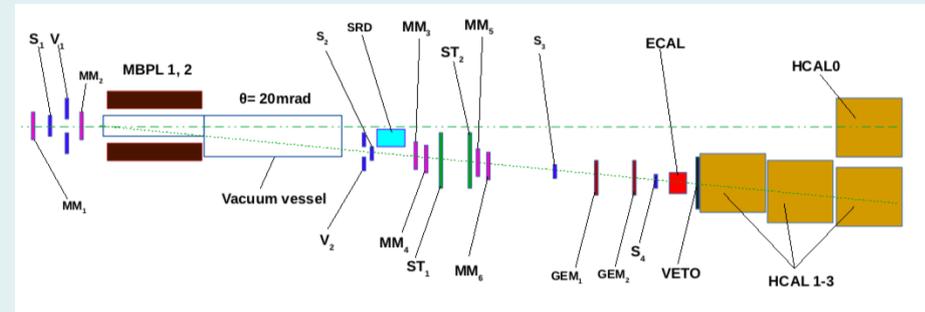
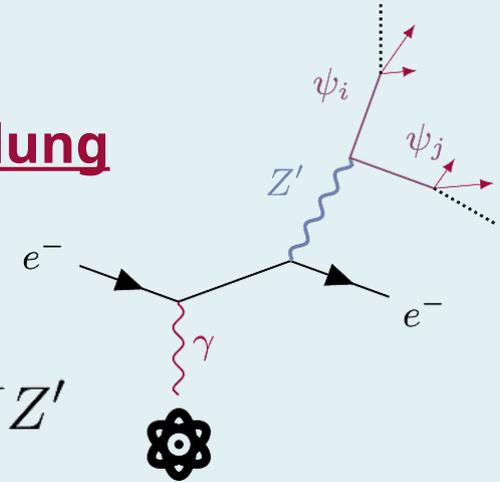
Monophoton + missing energy

Are semi-visible Z' viable?

- ☑ Simulate production of semi-visible Z' in BaBar and NA64 detector
- ☑ Apply selection criteria
- ☑ Recast the bound

$$\epsilon_{\text{bound}} = \epsilon_{\text{new}} \sqrt{P^{\text{inv}}(\epsilon_{\text{new}}, m_{Z'})}$$

NA64 Z' bremsstrahlung



Missing energy events with dark photon produced in electron bremsstrahlung

The NA64 simulation

Process: $e^- N \rightarrow e^- N Z'$

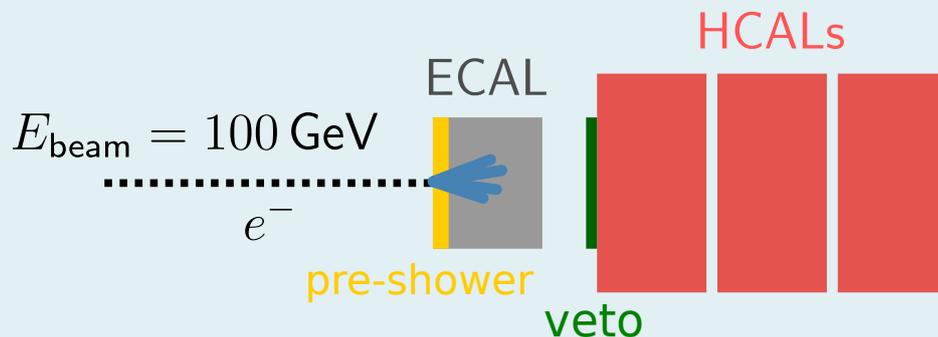
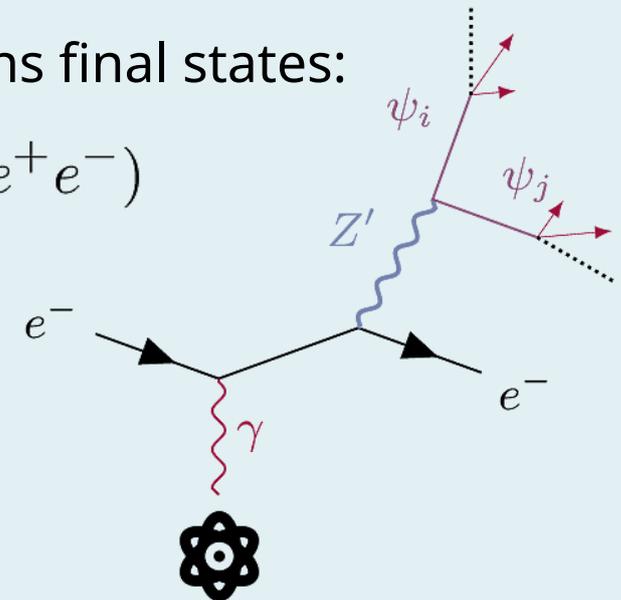
- ☑ Generate $O(10^5)$ events for given $m_{Z'}$ and ε
- ☑ Apply **veto criteria** and compute new P^{inv}

Z' decays instantly to HNL, producing pairs of leptons final states:

$$Z' \rightarrow (\psi_i \rightarrow \psi_k e^+ e^-) (\psi_j \rightarrow \psi_l e^+ e^-)$$

Recast: solve $\varepsilon_{\text{NA64}} = \varepsilon \sqrt{P^{\text{inv}}(\varepsilon, m_{Z'})}$

where
$$P^{\text{inv}}(\varepsilon, m_{Z'}) = 1 - \frac{N_{\text{veto}}(\varepsilon, m_{Z'})}{N(\varepsilon, m_{Z'})}$$



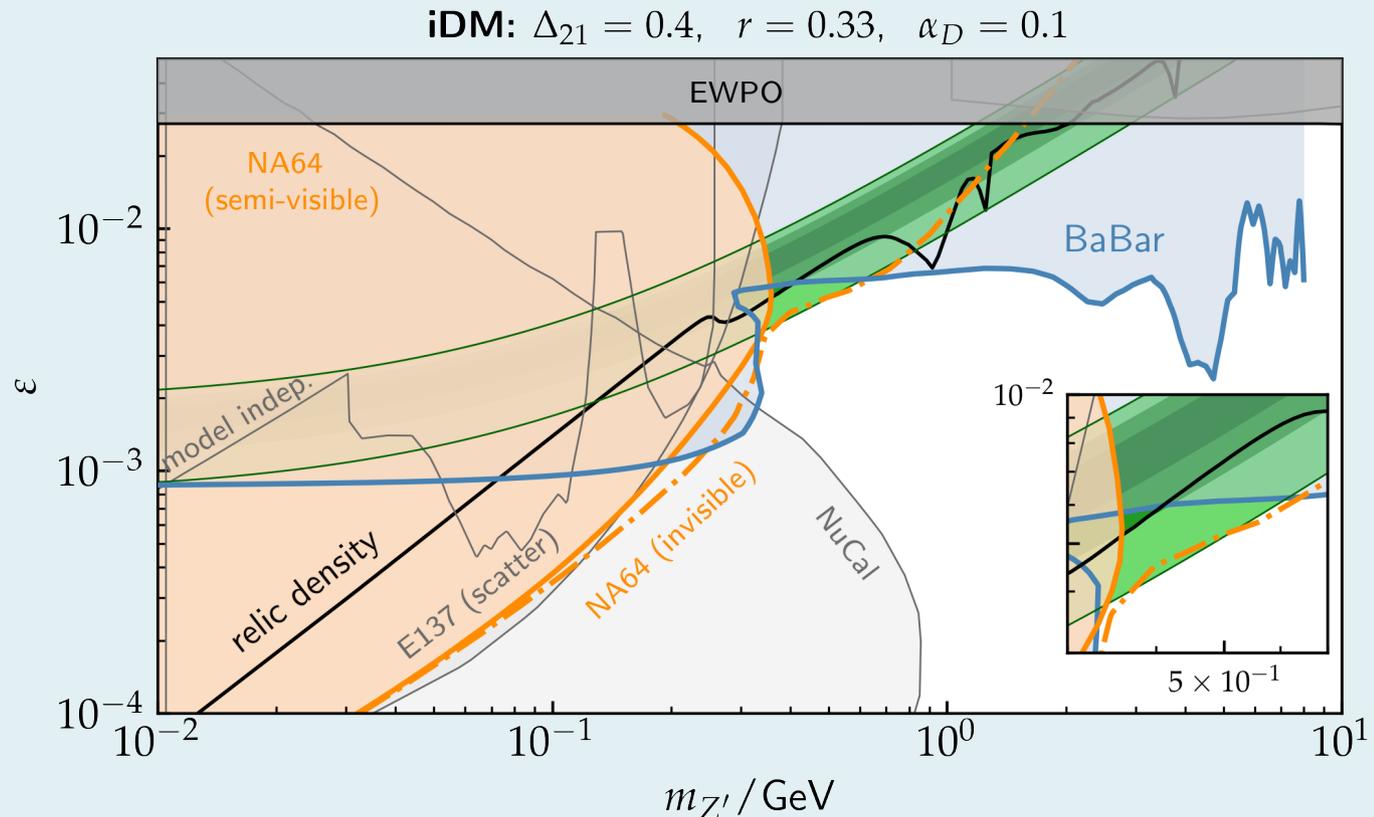
$e^+ e^-$ pairs deposit energy in the calorimeters or in the veto, so new events are vetoed according cut conditions.

Model 1: inelastic dark matter (iDM) with one pseudo-Dirac pair

$$\mathcal{L} \supset g_D \bar{\psi}_1 \not{Z}' \psi_2$$

- After diagonalisation, lightest state ψ_1 is DM, with ψ_2 decaying semi-visibly
- DM relic abundance from co-annihilations

**Minimal iDM is
almost excluded**



Model 2: iDM with several pseudo-Dirac pair

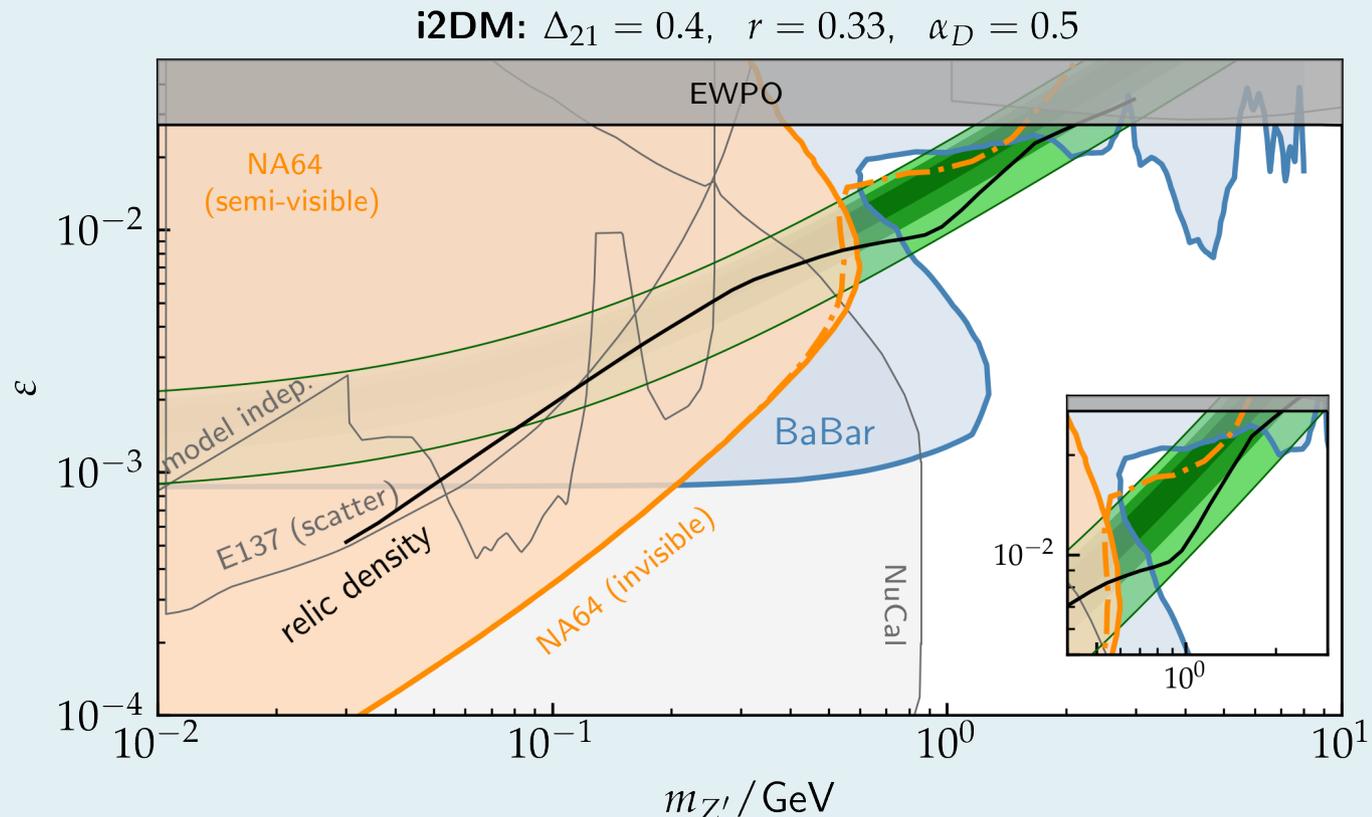
$$\mathcal{L} \supset g_D \theta^2 \bar{\psi}_1 Z' \psi_1 + g_D \theta \bar{\psi}_2 Z' \psi_1 + g_D \bar{\psi}_2 Z' \psi_2$$

- After diagonalisation: light neutral state ψ_1 and heavier state ψ_2 more strongly coupled to dark force with small mixing ϑ

Tip: inject more visible final states

- $Z' \rightarrow \psi_1 \psi_1$
- $Z' \rightarrow \psi_1 \psi_2$
- $Z' \rightarrow \psi_2 \psi_2$

Modified iDM allowed



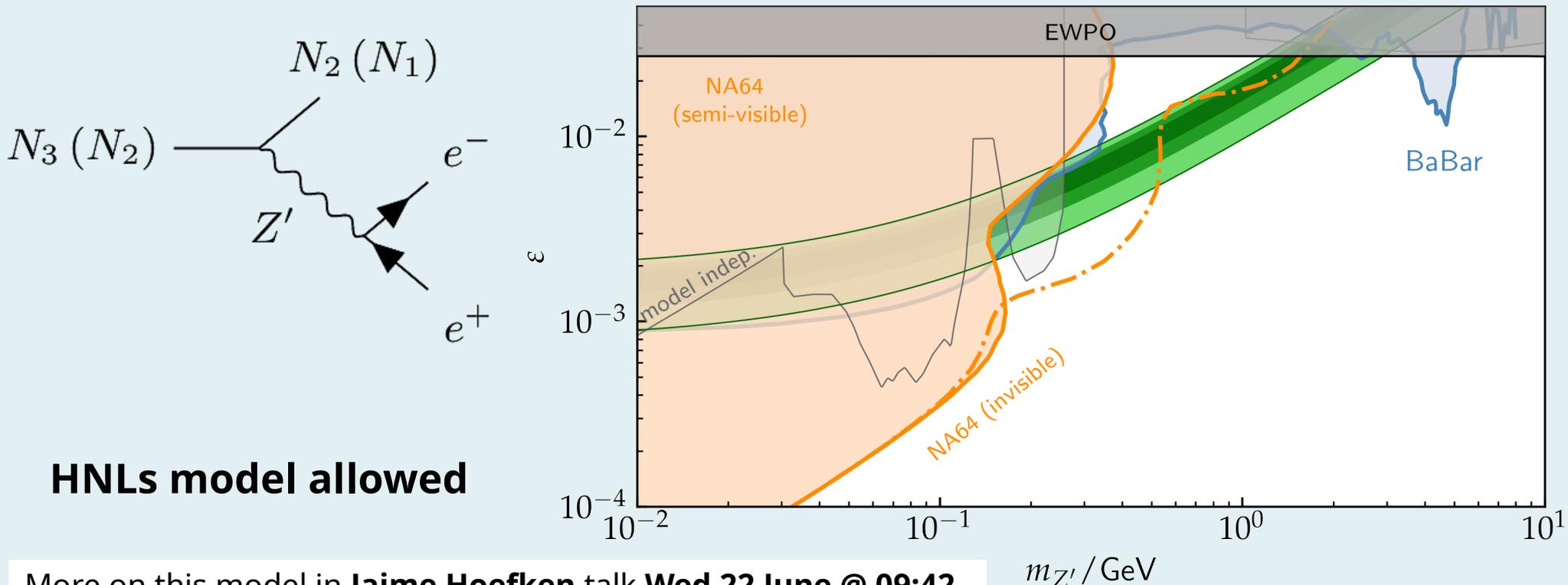
*Relic density courtesy of authors of [A. Filimonova et al. JHEP 06 (2022), p. 048].

Model 3: HNLs

$$\mathcal{L} \supset g_D V_{ij} \bar{N}_i \not{Z}' N_j + \text{h.c.}$$

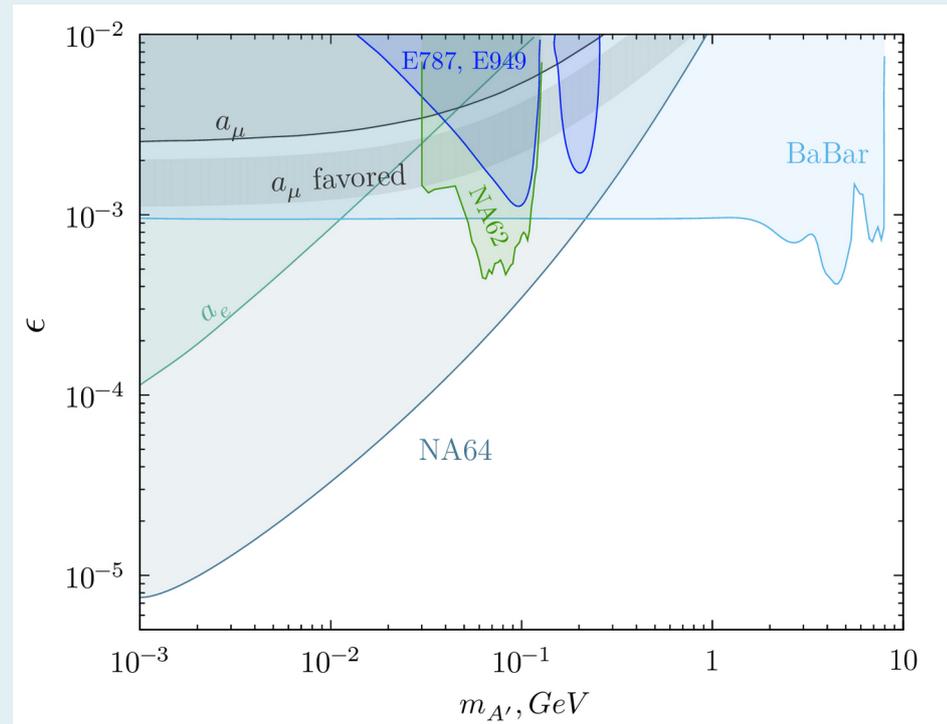
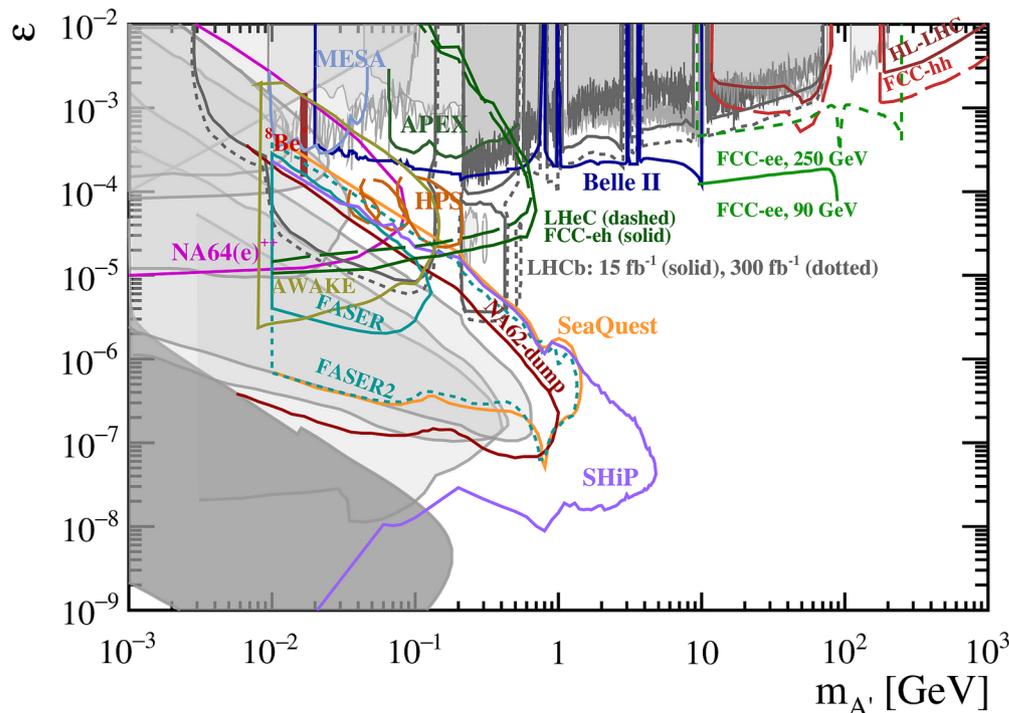
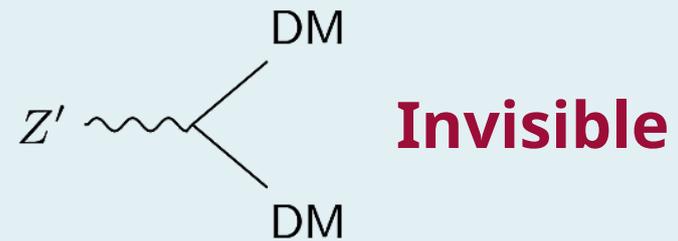
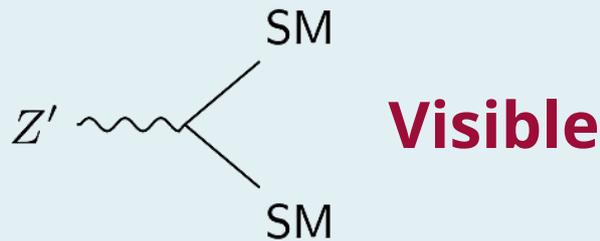
- After diagonalisation: we obtain 3 HNLs, interacting by V_{ij}
- BPs and model: [A. Abdullaoui et al. Phys. Lett. B 820 (2021), p. 136531]

HNL: $\Delta_{32} = 0.77$, $\Delta_{21} = 0.85$, $r = 0.15$, $\alpha_D = 0.75$



Backup slides

Dark photon decay modes



[M. Fabbrichesi et al. (2020). arXiv: 2005.01515]

[D. Banerjee et al. Phys. Rev. Lett. 123.12 (2019), p. 121801]

Visible decays in SM final states are **excluded** by colliders in resonance searches

Invisible decays **fully excluded** by BaBar and NA64

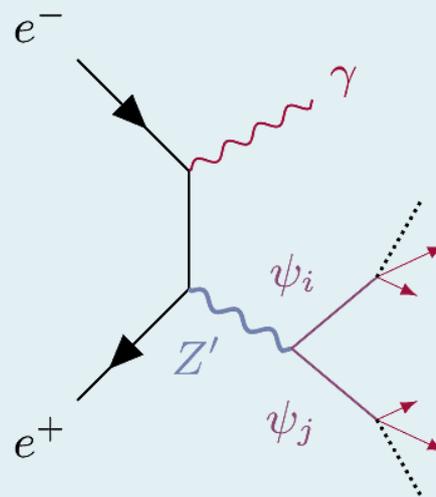
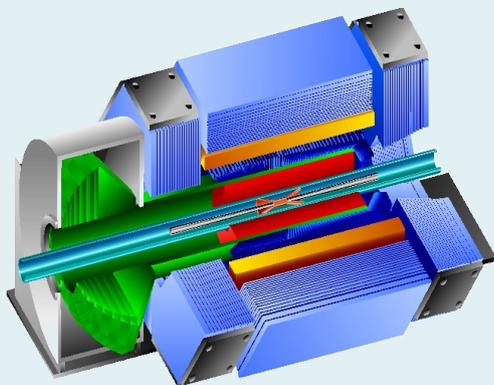
The BaBar simulation: generation

Process: $e^+e^- \rightarrow \gamma Z'$

- ☑ Generate $O(10^6)$ events for given $m_{Z'}$ and ϵ
- ☑ Apply primary selection cut on monophoton CM angle
- ☑ Apply veto criteria and compute new P^{inv}

Z' decays instantly to HNL, producing pairs of leptons final states:

$$Z' \rightarrow (\psi_i \rightarrow (\psi_k \rightarrow \dots)e^+e^-) (\psi_j \rightarrow (\psi_l \rightarrow \dots)e^+e^-)$$



Events containing visible final states are vetoed

The BaBar simulation: veto criteria

Veto criteria: if decays happen in instrumented region of detector then veto event if both

(1) Energy of lepton tracks exceeds BaBar detection threshold

(1) $\theta_{\text{sep}} > 10^\circ : E_{\pm} > 100 \text{ MeV}$ well separated pairs

(2) $\theta_{\text{sep}} < 10^\circ : E_+ + E_- > 100 \text{ MeV}$ overlapping pairs

(2) Wide polar angle to avoid electrons escaping along the beam pipeline

$$17^\circ < \theta_{\text{pol}} < 142^\circ$$

Recast: solve $\varepsilon_{\text{BaBar}} = \varepsilon \sqrt{P^{\text{inv}}(\varepsilon, m_{Z'})}$

$$\text{where } P^{\text{inv}}(\varepsilon, m_{Z'}) = 1 - \frac{N_{\text{veto}}(\varepsilon, m_{Z'})}{N(\varepsilon, m_{Z'})}$$

The NA64 simulation: veto criteria

Analysis 1: “invisible”

[Phys. Rev. Lett. 123.12 (2019), p. 121801]

HNLs decays can be prompt, thus depositing energy in the ECAL. Produced pairs can also be intercepted by the veto.

1. Pre-shower cut $E_{\text{tot}} \notin [0.5, 10]$ GeV

2. ECAL cut: $E_{\text{tot}} > 50$ GeV

E_{tot} is the sum of the main electron energy + the deposited energy by any other e^+e^- pair produced in the ECAL.

3. Check for pairs leaking out of the ECAL.

Veto cut: $E_{\pm}(x_{\text{veto}}) > 10$ MeV

4. HCAL cut: $E_{\pm} > 1$ GeV

Analysis 2: “semi-visible”

[Eur. Phys. J. C 81.10 (2021), p. 959]

Same analysis cuts applied also to other models in addition to the inelastic dark matter model:

1. Any e^+e^- pair triggering an activity before HCAL 2 is vetoed.

2. Max 1 e^+e^- pair in HCAL.

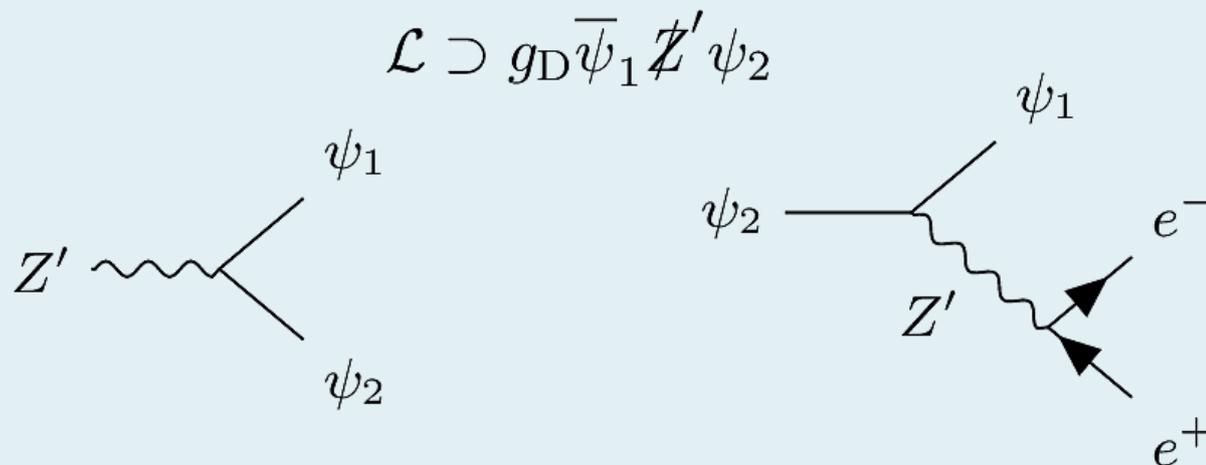
Assumptions:

- e^+e^- sufficiently overlapped: sum energies
- Neglect *leakage* of particles from transversal dimension of detector: everything is sufficiently *forward*

Model 1: inelastic dark matter (iDM) with one pseudo-Dirac pair

$$\mathcal{L} \supset \frac{1}{2} \begin{pmatrix} \overline{\psi_L} & \overline{\psi_R^c} \end{pmatrix} \begin{pmatrix} \mu_L & m_D \\ m_D & \mu_R \end{pmatrix} \begin{pmatrix} \psi_L^c \\ \psi_R \end{pmatrix} + \text{h.c.}$$

- $\mu_L \approx \mu_R \ll m_D$: on-diagonal couplings suppressed
- After diagonalisation, lightest state ψ_1 is DM, with ψ_2 decaying visibly
- DM relic abundance from co-annihilations



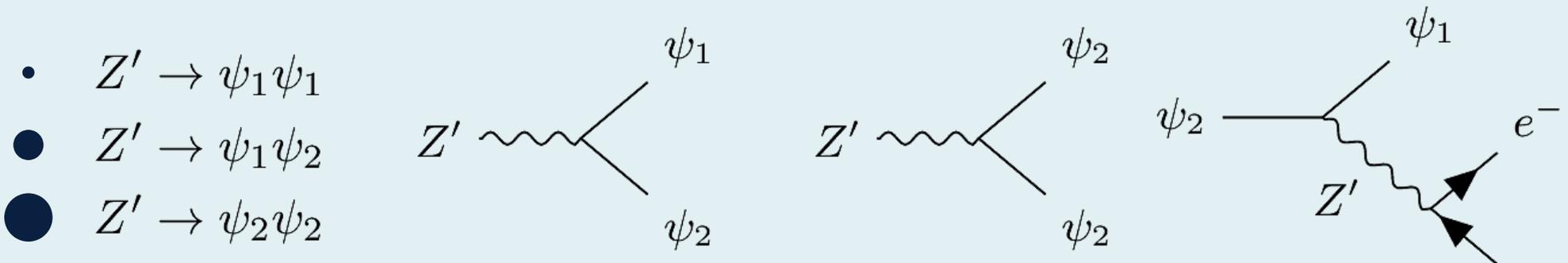
- Proposed in [G. Mohlabeng. Phys. Rev. D 99.11 (2019), p. 115001], where the study assumed BaBar energy threshold of 60 MeV (optimistic, we used 100 MeV, which is the same used in BaBar selection criteria)

Model 2: iDM with several pseudo-Dirac pair

$$\mathcal{L} \supset (\eta_L \quad \chi_L) \begin{pmatrix} M_1 & M_L \\ M_R & M_2 \end{pmatrix} \begin{pmatrix} \eta_R \\ \chi_R \end{pmatrix} + \text{h.c.}$$

- neutral (η) and U(1)' charged (χ) pseudo-Dirac pairs
- After diagonalisation: light neutral state ψ_1 and heavier state ψ_2 more strongly coupled to dark force with small mixing ϑ

$$\mathcal{L} \supset g_D \theta^2 \bar{\psi}_1 \not{Z}' \psi_1 + g_D \theta \bar{\psi}_2 \not{Z}' \psi_1 + g_D \bar{\psi}_2 \not{Z}' \psi_2$$



- ψ_1 can not be dark matter, unless secluded annihilations
- If not DM, then must decay (e.g. mixing w/ SM ν).

Model 3: HNLs

[A. Abdullahi et al. Phys. Lett. B 820 (2021), p. 136531]

$$\mathcal{L} \supset (\bar{N} \quad \bar{\psi}_L \quad \bar{\psi}_R^c) \begin{pmatrix} M_N & \Lambda_L & \Lambda_R \\ \Lambda_L^T & 0 & M_X \\ \Lambda_R^T & M_X^T & 0 \end{pmatrix} \begin{pmatrix} N^c \\ \psi_L^c \\ \psi_R \end{pmatrix} + \text{h.c.}$$

- With neutral state N and $U(1)'$ -charged fermions
- After diagonalisation we obtain 3 HNLs, interacting by V_{ij} (in principle they can mix also with SM ν).

$$\mathcal{L} \supset g_D V_{ij} \bar{N}_i Z' N_j + \text{h.c.}$$

