New Opportunities for Electroweak Baryogenesis





Marcela Carena Fermilab/Uchicago Higgs Hunting, September 13, 2022





The great success of the Higgs Boson

Its discovery and subsequent study of its properties at the LHC has provided a first portrait of the electroweak symmetry breaking mechanism

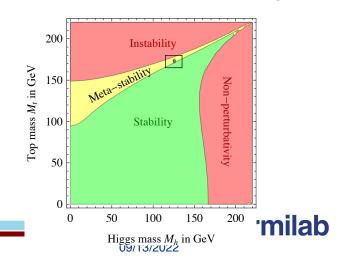
It ensures the calculability of the SM at high energies

It offers us a powerful tool for the exploration of fundamental questions in particle physics, e.g. Baryogenesis, Dark Matter, Inflation?

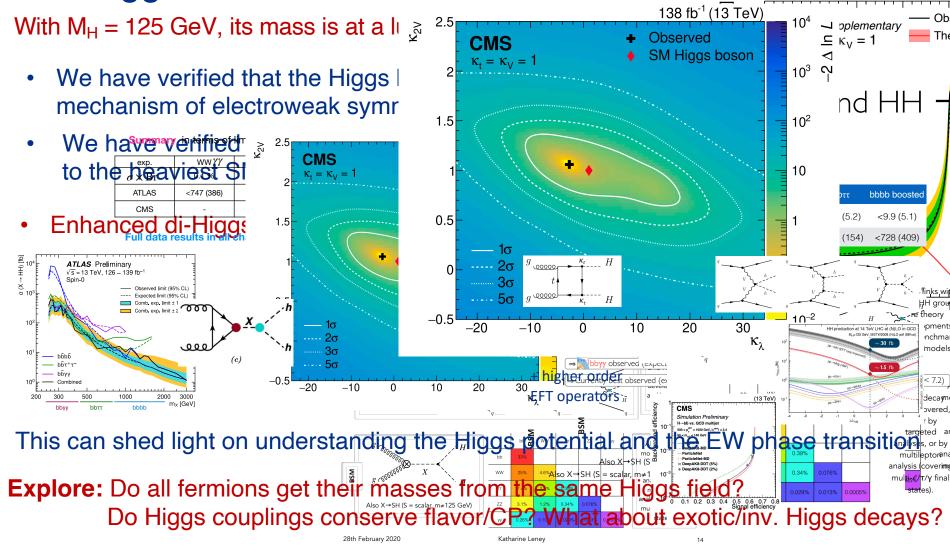
What is encoded in the Higgs potential? $V(\phi) = -m^2 |\phi|^2 + \lambda |\phi|^4$

$$V(\phi) = -m^2 |\phi|^2 + \lambda |\phi|^4$$

- What determines the values of the Higgs mass parameter and quartic coupling?
- Is there an explanation for the apparent metastability of the Higgs potential?
- Is it a part of a richer scalar potential?
- If so, what is the dynamics of the electroweak phase transition?



The Higgs boson: a lot to understand

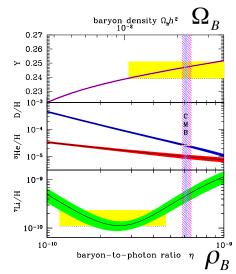


What is behind the EWSB mechanism: Radiative breaking? Compositeness?



The Mystery of our Asymmetric Universe

Precision Cosmology: information on baryon abundance



- Abundance of primordial elements
- Predictions from Big Bang Nucleosynthesis
- CMB

$$\eta = n_B / n_{\gamma} \approx 6.10^{-10}$$

What generated the small observed baryon-antibaryon asymmetry? Initial condition, or generated during the evolution of the universe?

Starting from a CPT conserving theory, the necessary Sakharov's conditions for baryogenesis are



- Baryon (or Lepton) number violation: if universe starts symmetric
- C and CP violation: treat baryon/anti-baryon differently (to remove antimatter)
- Out-of-thermal equilibrium: suppress inverse processes

All three requirements fulfilled in the SM – conditions are necessary but NOT sufficient to produced the OBSERVED asymmetry





Baryon Number Violation: Anomalous Processes

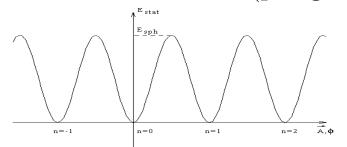
In the SM, Baryon Number conserved at classical level but violated at quantum level

- For gauge theories, one finds violation of classically preserved symmetries due to
- the quantization process paragraphics a: Weak Interaction Indexes For the chiral weak interactions, gauge symmetry preservation yields the non-indexes conservation of baryon and lepton currents

$$\frac{\simeq}{\partial_{\mu}j_{B,L}^{\mu}} \propto F_{\mu\nu}^{a} F_{\rho\delta}^{a} \epsilon^{\mu\nu\rho\delta} \frac{E^{\rho\sigma}}{\nu} = \frac{1}{2} \int_{0}^{\infty} dx \int_$$

$$\begin{split} & \Delta B = \Delta \cdot \Delta B = \Delta L = n \quad \text{(per generation)} \\ & \tilde{F}_{\mu\nu} = \frac{\epsilon_{\mu\nu\rho\sigma}}{2} F^{\rho\sigma} \qquad \text{If} \quad \int F_{\mu\nu} \tilde{F}^{\mu\nu} \neq 0 \implies \Delta Q_{B,L} \neq 0 \\ & \text{Anomalous processes violate both baryon and lepton number, hence violate B+L,} \end{split}$$

 $bu\underline{\mathsf{htpey}} preserve_{n} - \underbrace{\mathsf{lper}}_{per} proceed by the production of "sphalerons"$



$$E_{sph} \sim 8\pi v(T) / g$$

→ height of the barrier separating vacua with different baryon number Static configuration: middle point in the instanton tunneling





SM Baryon Number Violation at zero and finite Temperature

- At T = 0, B-violating sphaleron processes exponentially suppressed $\Gamma_{\Delta B \neq 0} \cong \exp(-2\pi/\alpha_{\rm W})$ with $S_{\rm inst} = 8\pi/\alpha_{\rm W}$
- At very high temperatures they are unsuppressed, $\Gamma_{\Delta B \neq 0} \propto T$
- At finite temperature they are Boltzmann suppressed

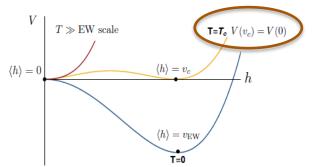
$$\Gamma_{\Delta B \neq 0} \cong \beta_0 \text{ T exp}(-E_{sph}(T)/T)$$
 with $E_{sph} \sim 8\pi \text{ v(T)/g}$

Klinkhammer and Manton'84; Arnold and Mc Lerran'88, Khlebnikov and Shaposhnikov '88

Baryon number generation at the Electroweak phase transition

Start from B = L = 0 at $T > T_c$

 In a first order EW phase transition, universe tunnels from h = 0 to h≠ 0 vacuum via bubble nucleation.





₹ Fermilab

Bubbles expand at near speed of light. Processes near the wall highly out of equilibrium



Effects of CPV and Baryon

r generation at the EWPT

- Start with B = L = 0 at T>Tc
 - Particles flow into the expanding and CPV implies that the wall exerts different forces on particles and antiparticles creating a chiral asymmetry

m>0

m>0

 \bigwedge m=0

• Outside the bubble, EW sphalerons allow a fraction "f" of the chira asymmetry in quarks to be shared with leptons → Sphalerons violate B+L, but conserve B-L

$$n_B - n_{\bar{B}} \propto \left[n_{t_R} - n_{t_R^c}\right] + (1 - f)\left[n_{t_L} - n_{t_L^c}\right] = f\Delta$$

A net baryon asymmetry is generated this way





Baryon Asymmetry Preservation

For a short period, EW sphalerons work to generate the desired baryon asymmetry; Then need to shut off quickly to prevent washout.

if $n_B = 0$ at T > Tc, independently of the source of baryon asymmetry

$$\frac{n_B}{s} = \frac{n_B(T_c)}{s} \exp\left(-\frac{10^{16}}{T_c(\text{GeV})} \exp\left(-\frac{E_{\text{sph}}(T_c)}{T_c}\right)\right)$$
<< 1 \rightarrow \text{v(T_c) /T_c \forall 1}

Recall:
$$\Gamma_{\Delta B \neq 0} \cong \beta_0 \text{ T exp}(-E_{sph}(T)/T)$$

If
$$\Gamma_{\Delta B \neq 0} \lesssim H \sim T^2 / M_{Pl}$$

B processes frozen

To preserve the baryon asymmetry demands a Strong First Order EWPT

Transition does not occur at T_c , but rather at T_n (bubble nucleation temp.) [$T_n < T_c$]

→ actual transition from false vacuum to real one requires S_{bounce}/T_n ~ 140





EW Baryogenesis in the SM fails

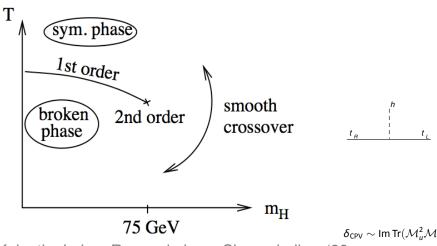
All three Sakharov's conditions could have been fulfilled

- Baryon number violation: Anomalous Processes/Sphalerons
- CP violation: Quark CKM mixing
- Non-equilibrium: At the Electroweak Phase Transition.

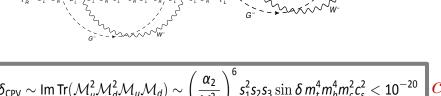
But

With the measured 125 GeV Higgs mass, lattice simulations show the EWPT is a cross over.

Contribution from CP violation (CKM) is highly suppressed $\frac{t}{t}$



High order loop effects needed to generate a complex contribution to the top quark mass



Kajantie, Laine, Rummukainen, Shaposhnikov '88 $\mathcal{M}_q = Y_q Y_q^{\dagger}$

 $\mathcal{M}_q = Y_q Y_q^{\dagger}$

Electroweak Baryogenesis demands new Physics/ New Scalars

Basic Questions:

- What was the mechanism that triggered electroweak symmetry breaking? (SM gives a simple parameterization, not an explanation)
- Does this mechanism involve an expanded "Higgs sector" with other scalar boson fields, new forces, new fermions, new sources of CP violation?
- Was the resulting phase transition strongly first order?
- Was there just one phase transition or a multi-step transition?
- Was there an electroweak phase transition at all?

The answers to these questions will inform whether electroweak baryogenesis is a viable explanation of the observed baryon excess in our universe



Higgs boson cousins may be the key to our Asymmetric Universe

To render the EWPT strongly first order and provide new sources of CPV Many BSM scenarios have been studied which allow for EWBG

- Singlet extensions of the SM
- Two Higgs doublet Models
- Supersymmetric models
- MSSM: light stop scenario, ruled out by Higgs precision
- NMSSM: through additional scalars, is an appealing possibility
 - Importance of computing nucleation temperature
 - EWBG possible but new scalar boson states are hard to probe at colliders due to alignment proximity (LHC information)
- Models with Dark CP violation and gauged lepton/baryon number
- Models with heavy Fermions
- Models of EW symmetry non-restoration/delayed restoration, with multiple singlets and possibly with an inert doublet



Finite temperature Higgs Potential: general considerations

Need to consider:
$$V(\phi,T) = V_0(\phi) + V_1^{CW}(\phi,0) + V_1(\phi,T)$$

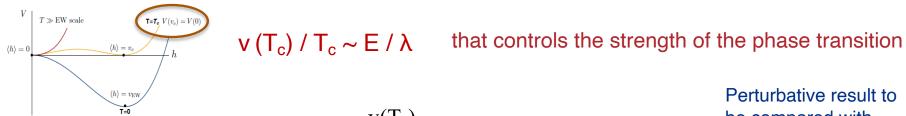
 V_1^{CW} yields renormalization scale independence, and $V_1(\phi,T)$ considers thermal contributions, e.g.

$$V_{1}(\phi,T) = \sum_{i=b,f} \left[\frac{n_{i}m_{i}^{2}(\phi)T^{2}}{48} - \frac{\eta_{i}m_{i}^{4}(\phi)}{64\pi^{2}} \log \left(\frac{m_{i}^{2}(\phi)}{T^{2}} \right) \right] - \sum_{b} \frac{m_{b}^{3}(\phi)T}{12\pi}$$
 For $m_{i}(\phi) < 2T$, with $\eta_{i} = n_{i}$ (-1)^{2S}

Review Standard Model example: \rightarrow V=D(T²-T₀²)H²+E_{SM}T H³ + $\frac{\lambda(T)}{2}$ H⁴

- D: contributions at one-loop proportional to the sum of the couplings of all bosons and fermions squared, responsible for symmetry restoration
- E: contributions from to the sum of the cube of all light boson particle couplings: $E_{SM} \approx \frac{2}{3} \left(\frac{2M_W^3 + M_z^3}{\sqrt{2}\pi v^3} \right)$

Defining T_c and requiring that $\langle \Phi(T_c) \rangle = v(T_c)$ is a minimum yields



Since
$$\lambda = m_H^2/v^2$$
 then $\frac{v(T_c)}{T_c} > 1$ implies $m_H < 40 \text{ GeV}$

Perturbative result to be compared with lattice computations yielding $m_H < 75 \text{ GeV}$



Finite temperature Higgs Potential: general considerations

Going beyond the Standard Model to allow for a first order phase transition, sufficiently strong, one needs to add new particles and look in the direction of the transition

$$V(\phi,T) = V_0(\phi,S, H_{BSM}) + V_1^{CW}(\phi, S, H_{BSM},0) + V_1(\phi, S, H_{BSM},T)$$

The scalar potential can have many fields

 Tree-level Effects New fields coupling directly with the Higgs, modifying the potential at tree level

$$\lambda
ightarrow \lambda_{ ext{eff}}$$

$$\lambda
ightarrow \lambda_{
m eff}$$
 [$E
ightarrow E_{
m eff}^{
m tree}$])

Zero Temperature loop effects

Modifying the potential through radiative corrections involving new particles

$$\lambda
ightarrow \lambda_{ ext{eff}}$$

Thermal effects

Modifying the thermal potential through thermal loops involving new particles

$$E \to E_{\mathrm{BSM}} \propto y_t^3$$

Higher order operators: if new particles heavy $\rightarrow V_{\text{eff}}$





Enhancing the EWPT strength through a singlet scalar

Scalar couples to the Higgs and affects the tree level potential

$$V_0(h,s) = -\frac{1}{2}\mu_h^2 h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2 s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2 + V_0^{\text{explicit}}(h,s)$$

We have separated out terms that explicitly break the Z_2 symmetry: $s \rightarrow -s$

The last case follows naturally in scenarios where, e.g., the singlet is the Higgs-like boson of a complex scalar in the dark sector that spontaneously breaks a dark gauge symmetry

→ Different thermal histories, with 1 or 2 step phase transitions and strong first order EWPT

To determine phase transition pattern requires finite temperature potential

$$V(h, s, T) \neq V_0(h, s) + V_{CW}(h, s; T) + V_T(h, s, T)$$

$$V^{\text{high-T}}(h, s, T) \approx \frac{1}{2}(-\mu_h^2 + c_h T^2)h^2 - ETh^3 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}(\mu_s^2 + c_s T^2)s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2 s^2$$

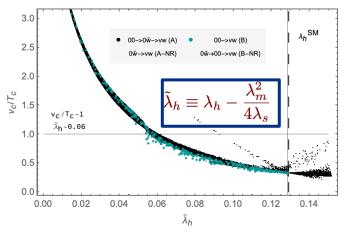


Exotic Higgs decays as a potent probe of viable EWBG models

The electroweak phase transition strength – Spontaneous Z₂ breaking scenario

$$rac{v_c}{T_c} = rac{2E}{ ilde{\lambda}_h} = rac{2E}{\lambda_h^{
m SM}} \Big[1 + \sin^2 heta \left(rac{m_H^2}{m_S^2} - 1
ight) \Big]$$



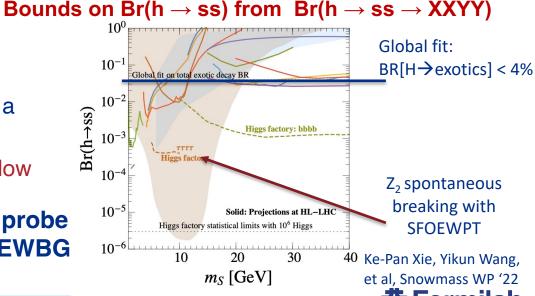


- Quartic mixing coupling proportional to mixing between mass eigenstates - strongly constrained by Higgs precision measurements $\rightarrow \sin \theta \lesssim 0.4$
- Strength of the EWPT enhanced for small m_S light singlet

10^{-1} Global fit on total exotic decay BR

- Sizeable s² IHI² coupling needed for a strongly 1st order EWPT
- → BR (H→SS) to be bounded from below

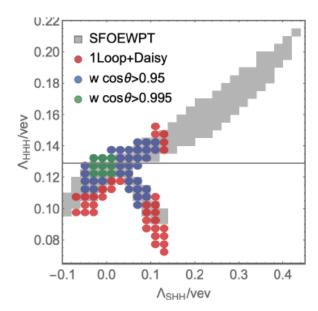
Exotic Higgs decays are a potent probe of Singlet extensions with viable EWBG

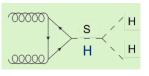


EWPT and Higgs Pair Production: Higgs Trilinear Coupling

Z₂ spontaneous Symmetry Breaking Scenario

M.C, Z. Liu, Y. Wang, '19

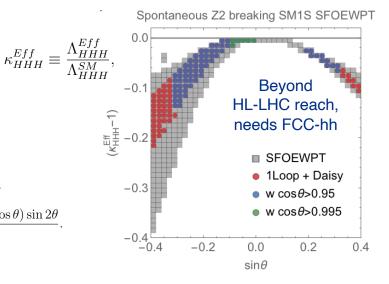




$$\Lambda_{HHH}^{\rm Eff} \simeq \frac{2}{3}\sin\theta\Lambda_{SHH} + \cos\theta\Lambda_{HHH}.$$

$$\Lambda_{HHH} = \frac{m_H^2 \left(-\sin^3 \theta + \tan \beta \cos^3 \theta \right)}{2 \tan \beta v}$$

$$\Lambda_{SHH} = \frac{(2m_H^2 + m_S^2)(\sin \theta + \tan \beta \cos \theta) \sin 2\theta}{4 \tan \beta v}.$$

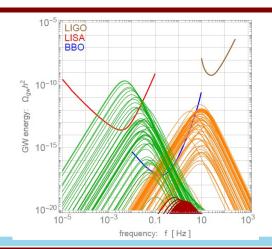


Gravitational Waves:

Bubble nucleation: expanding bubbles collide and produce stochastic GW through:

- sound waves propagation
- magnetohydrodynamic turbulence
- bubble collisions

Many parameters affect the GW signal



May be too weak to be probed after including all radiative corrections (red curves)

Further RG improvement may help

Fermilab



A SUSY example: the Next-to-Minimal Supersymmetric SM

A more extended Higgs sector: two Higgs doublets + a singlet

both charged under the EW gauge group

provides flexibility enhancing the PT strength

The NMSSM with the scalar potential

$$\begin{split} V_0 &= m_{H_d}^2 \left| H_d \right|^2 + m_{H_u}^2 \left| H_u \right|^2 + m_S^2 \left| S \right|^2 + \lambda^2 \left| S \right|^2 \left(\left| H_d \right|^2 + \left| H_u \right|^2 \right) + \left| \lambda H_u \cdot H_d + \kappa S^2 \right|^2 \\ &+ \left(\lambda A_\lambda S H_u \cdot H_d + \frac{\kappa}{3} A_\kappa S^3 + \text{h.c.} \right) + \frac{g_1^2 + g_2^2}{8} \left(\left| H_d \right|^2 - \left| H_u \right|^2 \right)^2 + \frac{g_2^2}{2} \left| H_d^\dagger H_u \right|^2 \end{split} \qquad \text{from Z3-NMSSM superpotential}$$

Without loss of generality, we consider the 3-dim. field space $\langle H_d \rangle = \begin{pmatrix} v_d \\ 0 \end{pmatrix}$ $\langle H_u \rangle = \begin{pmatrix} 0 \\ v_u \end{pmatrix}$ $\langle S \rangle = v_S$

CP even interaction states $\{H^{\text{SM}}, H^{\text{NSM}}, H^S\}$ \rightarrow CP even mass states $\{h_{125}, H, h_S\}$ Higgs basis

The EW vacuum
$$\langle H^{\mathrm{SM}} \rangle = v, \quad \langle H^{\mathrm{NSM}} \rangle = 0, \quad \langle H^{\mathrm{SM}} \rangle = v_S$$

After minimization conditions, replacing mass parameters by vev's and suppress mixing of HNMS and HS with HSM to be consistent with Higgs 125 GeV phenomenology

Parameter space:
$$\left\{v \equiv \sqrt{v_d^2 + v_u^2} \;,\; \tan\beta \equiv v_u/v_d \;,\; \mu \equiv \lambda v_S,\; \lambda,\; \kappa,\; A_\lambda,\; A_\kappa \right\} \rightarrow \left\{\left\{\mu,\; \tan\beta,\; \kappa,\; A_\kappa\right\}\right\}$$



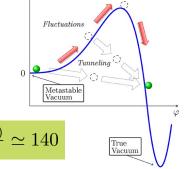
EWPT in the NMSSM - nucleation is more than critical

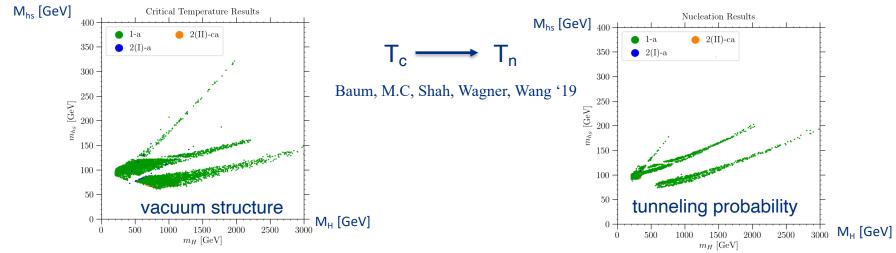
The vacuum structure gives little information about tunneling probability. V(x)

→ the higher the barrier, and the larger the distance between the minima, the lower the nucleation probability

The bubble nucleation rate per unit volume: $\Gamma/V \propto T^4 e^{-S_3/T}$

requiring the nucleation probability to be approx. one per Hubble volume and Hubble time leads to the nucleation condition





Collider and Dark Matter opportunities

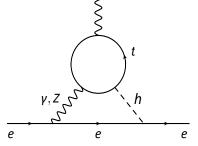
- Strong EWPT consistent with light to heavy non-SM-like Higgs boson and a singlet
- Despite light masses, these states are hard to probe at LHC (best: $H \rightarrow h_{125} + h_S$)
- The most promising dark matter scenario is a bino-like lightest neutralino



The challenge of new CPV sources for E Baryogenesis

The observed baryon asymmetry requires enew CPV sources that are in usually in tension with Electric Dipole Moment experimental bounds

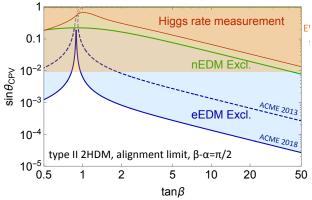
Electron EDM and the ACME experiment



on EDM measurement ==> $d_e < 1.1 \times 10^{-29} e \text{ cm}$

$$d_e < 1.1 imes 10^{-29} \, e \, ext{cm}$$
 ,

Most New Physics models of EWBG require $\sin \theta_{CPV} \ge 10^{-2}$



de Electron Prediction Can be suppressed if the CP violating fermion is a SM gauge singlet - doesn't couple to photons -

Shu, Y. Zhang, '13 Inoue, Ramsey-Musolf, Y. Zhang'14

Leading EDM arises at higher loops, naturally suppressed by one or two orders of magnitude below current limit for CPV sources of order one

How to transfer CP violation in the early universe?



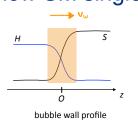
A new mechanism for EW Baryogenesis: Dark CP violation

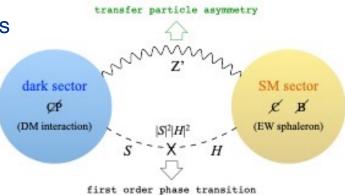
A model with gauged lepton number

MC, Quiros and Yue Zhang.19

- Higgs portal (sourcing CP violation & phase transition)
- Z' portal (for transfer of CP violation)

A dark fermion χ (DM) talks to the Higgs boson via a new SM singlet scalar S





EW sphalerons cannot touch the chiral charge asymmetries in the χ SU(2) singlet

new U(1) gauge boson Z' couples to the dark fermions and SM leptons and transfers CPV to SM sector

A varying mass m_{χ} along the z direction, together with the S vev, generates a chiral charge asymmetry in χ particles

This in turn generates a Thermal Equilibrium Asymmetry in SM leptons Sphaleron processes yield $\Delta N_L = \Delta N_B$

SU(2)_L anomalons, besides DM, must decouple from thermal number density A new scalar-Higgs interaction, $\lambda_{SH}|S|^2|H|^2$, can trigger strong first order EWPT

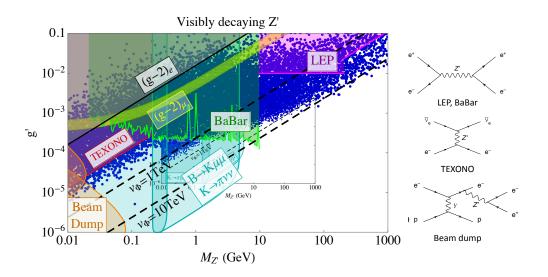




Dark CPV: Phenomenology

MC, Quiros and Yue Zhang'19 MC, Y-Y li, T. Ou, W. Wang, to appear

- Predicts the existence of a new force carrier Z', leptophilic $\Rightarrow Z'$ searches.
- Predicts very small EDM's, but can be at reach in next round of experiments
- Predicts a new Higgs portal scalar S, which could mainly decay into Z's.
- The χ particle qualifies to be a thermal dark matter candidate



13TeV, 36fb⁻¹ ● 3.0 HL-LHC O 2.5 γ_{SH} γ_{SH} 1.5 1.0 0.5 0.0 50 100 150 200 250 300 $m_a[GeV]$

Leptophilic Z': Target and Searches

LHC searches for long-lived scalars





Outlook: Electroweak Baryogenesis

An appealing mechanism to explain the matter-antimatter asymmetry:

It requires a strongly first order electroweak phase transition and additional CPV beyond the SM.

It may come with interesting new collider signatures and may even accommodate DM Gravitational wave signatures can be interesting probes of the nature of the phase transition at the reach of planned instruments

Some examples:

- Singlet extensions to the SM can enhance the EWPT, which exhibits rich thermal history and collider phenomenology.
- Extended Higgs sectors with large tree level barriers and multi dimensional field space: important differences between the critical temperature study versus the nucleation temperature study
- Baryogenesis generation with CPV in a dark sector can circumvent EDM current restrictions and provide a novel mechanism for EWBG in models with gauged lepton (or quark number), with CPV transmitted by a new force





Merci!

Extras

Simplest Case: A singlet extension of the Standard Model





Enhancing the EWPT strength through a Singlet extension

A singlet scalar that couples to the Higgs and affects the tree level potential

$$V_0(h,s) = -\frac{1}{2}\mu_h^2h^2 + \frac{1}{4}\lambda_hh^4 + \frac{1}{2}\mu_s^2s^2 + \frac{1}{4}\lambda_ss^4 + \frac{1}{4}\lambda_mh^2s^2 + \frac{1}{4}$$

- Generic Potential: Explicit Z2 breaking $\rightarrow V_0^{explicit}(h,s) = a_1h^2s + b_1s + b_3s^3$ Espinosa, Quiros '93, Profumo, Ramsey-Musolf, Shaughnessy '07, Choi, Volkas '93, Huang, Joglekar, Li, Wagner '16, Kozaczuk, Ramsey-Musolf, Shelton '19
- Z2 preserving (at T=0) $\rightarrow \langle (h,s) \rangle = (v_{\rm EW},0)$

Espinosa, Konstandin, Riva '11, Curtin, Meade, Yu '15, Barger, Chung, Long, Wang '12, Kozaczuk, Ramsey-Musolf, Shelton '19

Spontaneously Z₂ breaking $ightarrow \langle (h,s) \rangle \equiv (v_{\rm EW},w_{\rm EW})$ M.C, Liu Wang '19 In connection with a dark gauge symmetry, spontaneously broken by a dark Higgs vev.

Different thermal histories, with 1 or 2 step phase transitions and strong first order EWPT

→ Distinct rich phenomenolegy out Colliders (Higgs) provisions Higgs trilinear coupling, double Higgs production, direct new scalar searches, possible effects of CPV





09/13/2022

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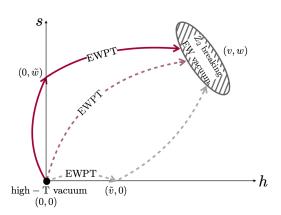


The SM singlet extension: EWPT paths for baryogenesis

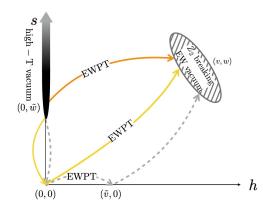
Is it possible that the EW symmetry or/and the Z_2 symmetry is/are Non-Restored (NR)?

- EW-NR demands many, many singlets (+ possibly an inert doublet) MC, Krauss, Liu, Wang '21
- Z₂-NR: Yes

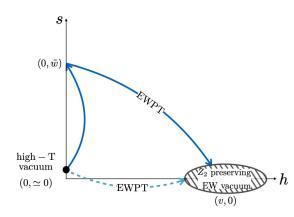
Solid lines: EWPT can be strongly first-order



Z₂ spontaneous breaking scenarios with symmetry restoration at high T



Z₂ spontaneous breaking scenarios without symmetry restoration at high T



Z2 preserving or explicit breaking scenarios

- The step where the EW symmetry is first broken is required to be strongly first-order.
- To enable a strongly first-order phase transition, the singlet should have significant couplings to the Higgs, to induce a sufficiently large deformation to the scalar potential in the early universe





EWPT with Spontaneous Z₂ Breaking: The full analysis

Tree-level Potential
$$V_0(h,s) = -\frac{1}{2}\mu_h^2h^2 + \frac{1}{4}\lambda_h h^4 + \frac{1}{2}\mu_s^2s^2 + \frac{1}{4}\lambda_s s^4 + \frac{1}{4}\lambda_m h^2s^2$$

Parameters
$$\{\mu_h^2, \mu_s^2, \lambda_h, \lambda_s, \lambda_m\} \longleftrightarrow \{v_{\text{EW}}, m_H, \tan \beta, m_S, \sin \theta\}$$

Thermal potential

$$V_T(h, s, T) = \frac{T^4}{2\pi^2} \left[\sum_{i=\{B\}} n_i J_B \left(\frac{m_i^2(h, s)}{T^2} \right) + \sum_{f=\{F\}} n_f J_F \left(\frac{m_f^2(h, s)}{T^2} \right) \right]$$

expanding the J_B and J_F functions in terms of small $\alpha = m^2/T^2$

$$J_B^{\text{high-T}}(\alpha) = \text{Re}\left[-\frac{\pi^4}{45} + \frac{\pi^2}{12}\alpha - \frac{\pi}{6}\alpha^{\frac{3}{2}} + \cdots\right],$$

$$J_F^{\text{high-T}}(\alpha) = \text{Re}\left[\frac{7\pi^4}{360} - \frac{\pi^2}{24}\alpha + \cdots\right].$$

$$V^{\text{high-T}}(h, s, T) \approx \frac{1}{2} (-\mu_h^2 + c_h T^2) h^2 - ETh^3 + \frac{1}{4} \lambda_h h^4 + \frac{1}{2} (\mu_s^2 + c_s T^2) s^2 + \frac{1}{4} \lambda_s s^4 + \frac{1}{4} \lambda_m h^2 s^2$$

One Loop Coleman-Weinberg potential and daisy resummation also considered

$$V_{\text{CW}}(h,s) = \frac{1}{64\pi^2} \left(\sum_{B} n_B m_B^4(h,s) \left[\log \left(\frac{m_B^2(h,s)}{Q^2} \right) - c_B \right] - \sum_{F} n_F m_F^4(h,s) \left[\log \left(\frac{m_F^2(h,s)}{Q^2} \right) - \frac{3}{2} \right] \right)$$

$$m_i^2(h,s) \to m_i^2(h,s,T) = m_i^2(h,s) + d_i T^2$$





EWPT with Spontaneous Z₂ Breaking: The full analysis

The electroweak phase transition strength

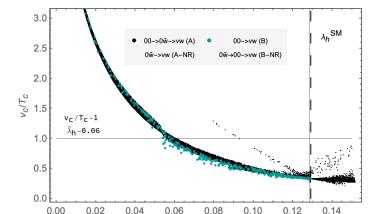
$$\frac{v_c}{T_c} = \frac{2E}{\tilde{\lambda}_h} = \frac{2E}{\lambda_h^{\rm SM}} \left[1 + \sin^2 \theta \left(\frac{m_H^2}{m_S^2} - 1 \right) \right]$$

Bare parameters

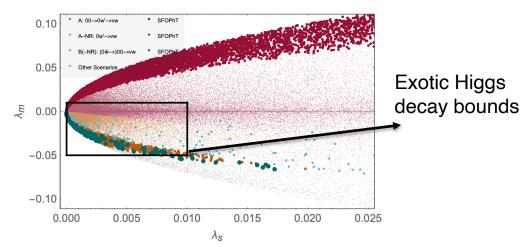
$$\tilde{\lambda}_h \equiv \lambda_h - \frac{\lambda_m^2}{4\lambda_s} \qquad \frac{v_c}{T_c} \propto \tilde{\lambda}_h^{-1}$$

Physical parameters

 $\sin \theta \lesssim 0.4$ bounded by Higgs precision measurements



Small m_S renders SFOPhT: light singlet



- Full one-loop effective potential with daisy resummation allows for all types of solutions shown in the thermal only analysis.
- Results robust against the Nucleation calculation

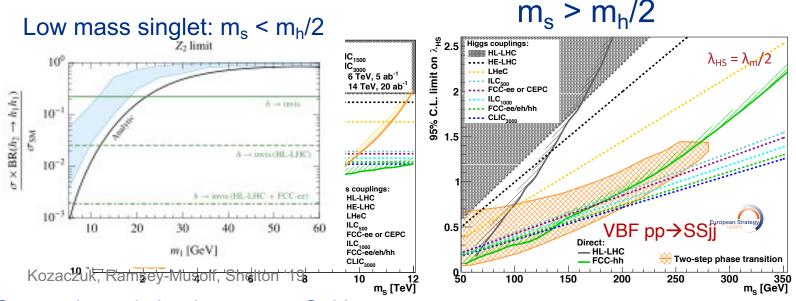




Phenomenology of SM plus Singlet models

- Z₂-symmetric (at T=0) scenario: Invisible Decays
- Requires sizeable s² IHI² coupling for a 2 step strongly 1st order EWPT, $[(0,0)\rightarrow(0,v_S)\rightarrow(v,0)]$, that calls for a careful treatment of perturbativity
- No S-H mixing S is stable (invisible decays)

Lower bound on BR(H) inv or pp →VSS (AP) pp →SSii (VBF)



Current bounds imply m_S < 20 GeV

EWBG scenario to be fully probed by full FCC or CLIC

Scenarios for EWBG based on EW symmetry non restoration can also be tested via Higgs invisible decays M.C, Krause, Z. Liu, Y Wang'21





Higgs Exotic Decay Phenomenology in Singlet models

If singlet sufficiently light → BR (H→SS) to be bounded from below for a strongly 1st order EWPT that demands significant S-H couplings

- → exotic Higgs decays are a potent probe of Singlet extensions with viable EWBG Specifics of the exotic Higgs decays depend on Z₂ symmetry realization
- Z₂ spontaneously breaking scenario
- ➤ Requires sizeable s² IHI² coupling for a strongly 1st order EWPT Only 3 parameters after defining Higgs mass and v.e.v
 - → quartic mixing coupling proportional to S-H mixing strongly constrained by Higgs precision measurements
 - → strength of the EWPT is enhanced for small m_S light singlet -
 - Z₂ explicitly breaking scenario
 - Not only the s² IHI² coupling is relevant for a strongly 1st order EWPT, but also terms in s³ and s IHI² play a role (more free parameters; quartic mixing coupling independent of S-H mixing)
 - ➤ A strong 1st order EWPT and a small amount of H-S mixing compatible with Higgs properties, with a looser lower bound on BR[H→SS]



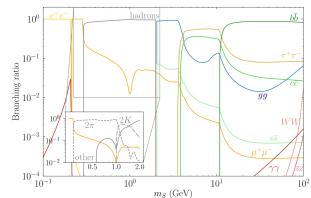


Probing Z₂ breaking Singlet Extensions via Higgs Exotic Decays

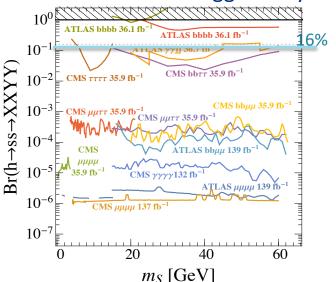
Currently: BR[H→ exotics] < 16%

H→ SS can lead to many final states with S inheriting Higgs-like hierarchical BR's, mediated through mixing

Final state dominated by h \rightarrow ss \rightarrow bbbb for m_s > 2m_b, and by jjjj, jjtt, and tttt for m_s < 10 GeV

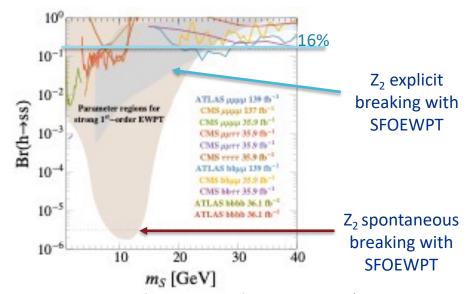


Bounds on exotic Higgs decays



Besides the 4b's final state, the rest involves at least a pair of EW states

Bounds on Br(h \rightarrow ss) from Br(h \rightarrow ss \rightarrow XXYY)



Ke-Pan Xie, Yikun Wang, et al, Snowmass WP '22



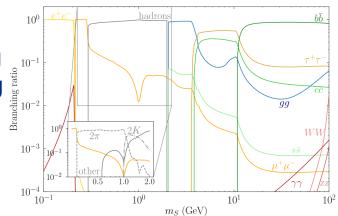
₹ Fermilab

Probing Z₂ breaking Singlet Extensions via Higgs Exotic Decays

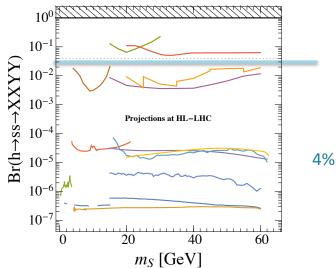
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H→ SS can lead to many final states with S inheriting Higgs-like hierarchical BR's, mediated through mixing

Final state dominated by h \rightarrow ss \rightarrow bbbb for m_s > 2m_b, and by jjjj, jj $\tau\tau$, and $\tau\tau\tau\tau$ for m_s < 10 GeV

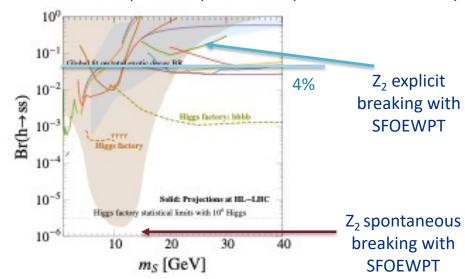


Bounds on exotic Higgs decays



Besides the 4b's final state, the rest involves at least a pair of EW states (same color coding)

Bounds on Br(h \rightarrow ss) from Br(h \rightarrow ss \rightarrow XXYY)



Ke-Pan Xie, Yikun Wang, et al, Snowmass WP '22



Extended Higgs sectors: a SUSY example

The Electroweak Phase Transition in the NMSSM





EWPT in the NMSSM: alignment limits and parameter space

Defining
$$\mathcal{M}_S^2$$
 in the in the Higgs basis $m_{h_{125}}^2 \simeq \mathcal{M}_{S,11}^2 = m_Z^2 \cos^2(2\beta) + \lambda^2 v^2 \sin^2(2\beta)$

To be consistent with the current Higgs phenomenology, the mass eigenstate h₁₂₅ needs to be dominantly composed of HSM - need to suppress mixing of HNMS and HS with HSM

$$\left|\mathcal{M}_{S,12}^2\right| \ll \left|\mathcal{M}_{S,22}^2\right| - \left|\mathcal{M}_{S,11}^2\right|, \quad \left|\mathcal{M}_{S,13}^2\right| \ll \left|\mathcal{M}_{S,38}^2 - \mathcal{M}_{S,11}^2\right|$$
 alignment without decoupling alignment without decoupling

The alignment conditions –without decoupling, imply $m_H, m_A, m_{H^\pm} \sim 2 \mu / \sin 2 eta$

$$\mathcal{M}_{S,12}^2 = 0 \quad \rightarrow \quad \lambda^2 = \frac{m_{h_{125}}^2 - m_Z^2 \cos(2\beta)}{2v^2 \sin^2 \beta}, \qquad \mathcal{M}_{S,13}^2 = 0 \quad \rightarrow \quad A_\lambda = \frac{2\mu}{\sin 2\beta} \left(1 - \frac{\kappa}{\lambda} \sin 2\beta \right)$$

For small to moderate tan β : $\lambda \sim 0.6 - 0.7$

The parameter space

$$\{v, \tan \beta, \mu, \lambda, \kappa, A_{\lambda}, A_{\kappa}\} \rightarrow \{\mu, \tan \beta, \kappa, A_{\kappa}\}$$





EWPT in the NMSSM: alignment limits and parameter space

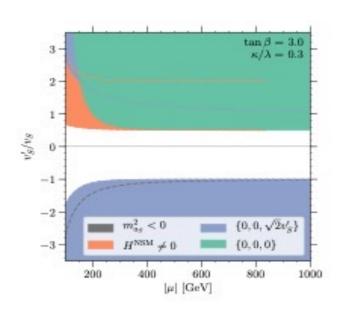
The parameter space

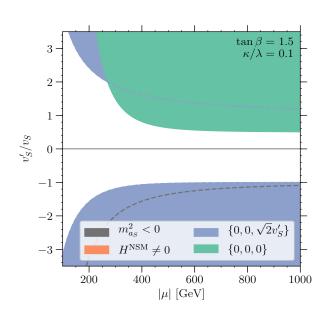
$$\left\{v, \, \tan\beta, \, \mu, \, \lambda, \, \kappa, \, A_{\lambda}, \, A_{\kappa}\right\} \quad \rightarrow \quad \left\{\mu, \, \tan\beta, \, \kappa, \, A_{\kappa}\right\} \quad \longrightarrow \quad \left\{\tan\beta, \, \mu, \, \frac{\kappa}{\lambda}, \, \frac{v_S'}{v_S}\right\}$$

- 125 GeV mass eigenstate without large radiative corrections $\tan \beta \lesssim 5$
- Avoid Landau poles (GUT) $\sqrt{\lambda^2 + \kappa^2} \lesssim 0.7$

 $v_S' \equiv -\left(\frac{\mu}{\lambda} + \frac{A_\kappa}{2\kappa}\right)$

- Avoid tachyonic masses, e.g. $m_{a_S}^2 \geq 0$
- Correct vacuum structure at zero temperature $\{H^{\text{SM}}, H^{\text{NSM}}, H^{\text{S}}\} = \{0, 0, 0\} \lor \left\{0, 0, \sqrt{2v_S'}\right\} \lor \left\{0, 0, \frac{\sqrt{2}\mu}{\lambda}\right\} \lor \left\{\sqrt{2}v, 0, \frac{\sqrt{2}\mu}{\lambda}\right\} \lor \cdots$







Baum, M.C Shah, Wagner, Wang '19



EWPT in the NMSSM - the effective potential

Radiative corrections (zero temperature)

Integrating out heavy degrees of freedom (sfermions, gluinos etc) are integrated out. A new operator by matching:

$$V_0^{ ext{eff}} = V_0 + rac{\Delta \lambda_2}{2} \left| H_u
ight|^4$$

 $V_0^{ ext{eff}} = V_0 + rac{\Delta \lambda_2}{2} \left| H_u \right|^4$ with $\Delta \lambda_2$ fixed by 125 GeV Higgs mass

Light degrees of freedom: CW potential

$$V_{1-\text{loop}}^{\text{CW}} = \frac{1}{64\pi^2} \sum_{i=P,F} (-1)^{F_i} n_i \widehat{m}_i^4 \left[\log \left(\frac{\widehat{m}_i^2}{m_t^2} \right) - C_i \right]$$

$$B = \left\{h_i, a_i, H^{\pm}, G^0, G^{\pm}, Z, W^{\pm}\right\}$$

$$F = \left\{\widetilde{\chi}_i^0, \widetilde{\chi}_i^{\pm}, t\right\}$$

Introducing counterterms to maintain boundary conditions

$$\delta \mathcal{L} = -\delta_{m_{H_d}^2} \left| H_d \right|^2 - \delta_{m_{H_u}^2} \left| H_u \right|^2 - \delta_{m_S^2} \left| S \right|^2 - \delta_{\lambda A_{\lambda}} \left(S H_u \cdot H_d + \text{h.c.} \right) - \frac{\delta_{\lambda_2}}{2} \left| H_u \right|^4$$

Finite temperature effective potential

$$V_1(T) = V_0^{\mathrm{eff}} + V_{\mathrm{1-loop}}^{\mathrm{CW}}(\widetilde{m}_i^2) + V_{\mathrm{1-loop}}^{T \neq 0}(\widetilde{m}_i^2)$$

with

$$V_{1-\text{loop}}^{T\neq 0} = \frac{T^4}{2\pi^2} \sum_{i=B,F} (-1)^{F_i} n_i J_{B/F} \left(\frac{\widetilde{m}_i^2}{T^2} \right)$$





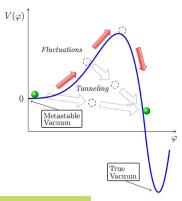
EWPT in the NMSSM - nucleation is more than critical

The phase transition proceeds by tunneling through the barrier separating local minima, the so-called bubble nucleation.

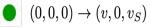
→ the higher the barrier, and the larger the distance between the minima, the lower the nucleation probability

The bubble nucleation rate per unit volume: $\Gamma/V \propto T^4 e^{-S_3/T}$

requiring the nucleation probability to be approx. one per Hubble volume and Hubble time leads to the nucleation condition



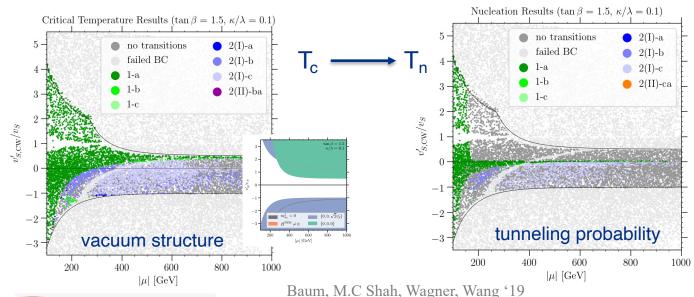
$$\frac{S_3(T_n)}{T_n} \simeq 140$$



$$(0,0,0) \to (0,0,\tilde{v}_S) \to (v,0,v_S)$$

$$(0,0,0) \to (0,0,\tilde{v}_S) \to (v,0,v_S)$$

$$(0,0,0) \to (\tilde{v},\tilde{v}_{\rm NSM},0) \to (v,0,v_S)$$



- Integer: # of steps
- Roman number:

Intermediate phase (I): singlet-only direction

- (II): EWS broken phase
- Lower case letter:

Strength of the EWPT

a: SFOEWPT

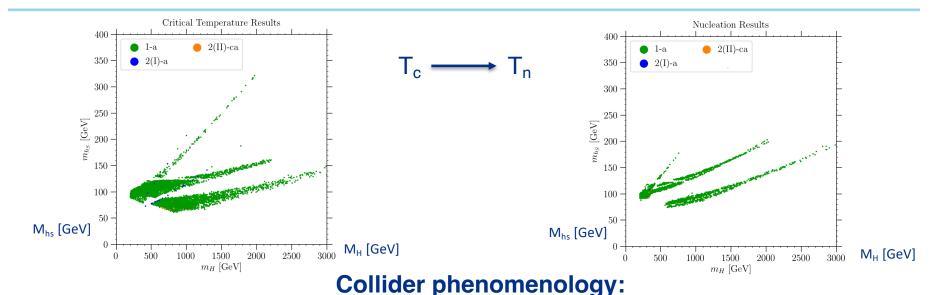
b: weakly 1st order

c: 2nd order





EWPT in the NMSSM: collider and dark matter pheno



- The SFOEWPT consistent with light to heavy non-SM-like Higgs boson and a singlet
- Despite the light masses, these states are hard to probe in colliders
 - Production of the singlet-like state suppressed due to small NSM component
 - Decay modes of the doublet-like states make it hard to be probed
 - Promising channels to probe: final states containing at least one singlet-like boson

Dark Matter:

- The most promising dark matter scenario is a bino-like lightest neutralino
 - Small interaction cross sections
 - well-tempered scenario for the correct relic density





Baryogenesis with Dark CP Violation:

A model with gauged lepton number



Dark CPV: The Higgs Portal

Sourcing CP Violation

MC, Quiros and Yue Zhang '19

The direct coupling between a SM gauge singlet fellow to the Higgs boson would be higher dimensional. To write a renormalizable theory introduce a new scalar S

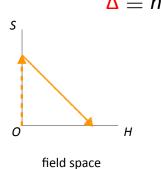
Scalar S - also SM singlet - couples to dark fermion (DM) $\mathcal{L} \sim \bar{\chi}_L(m_0 + yS)\chi_R + \text{h.c.}$

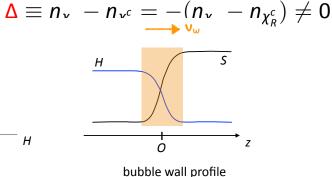
In the presence of a relative phase between m_0 and y, a chiral charge asymmetry in χ particles can be generated $\Delta \equiv n_{\chi_L} - n_{\chi_L^c} = -(n_{\chi_R} - n_{\chi_R^c}) \neq 0$

This requires m_{χ} to vary along the z direction, together with the S vev

A new EW phase transition

A new scalar-Higgs interaction, $\lambda_{\rm SH} |S|^2 |H|^2$, with $\lambda_{\rm SH} > 0$, can trigger strong first order EWPT





z is distance from bubble wall

Need at least $\delta V(S) = \mu_S^2 S^2$ to avoid CPV being redefined away

Espinosa, Konstandin, Riva, 1107.5441; MC, Y.Y Li, Ou and Wang, in prep.



Dark CPV: The role of the Z' Portal

EW sphalerons cannot touch the chiral charge asymmetries in χ because it is an SU(2) singlet — must transfer such CPV effect in other ways to the SM sector

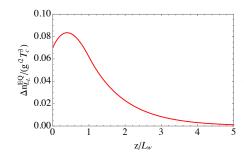
Introduce a new U(1) gauge boson couples to the dark fermions and SM leptons

If $q\chi_I \neq q\chi_R$ (required by anomaly cancellation), there is a net charge density, that generates a background for the Z'_0 component (static electric potential analogue).

Z' couples to SM leptons
$$g'Z'_{\alpha}\sum_{i=1}^{3}\left[\mathbf{q}_{L_{l_{i}}}\bar{L}_{L_{i}}\gamma^{\alpha}L_{L_{i}}+\mathbf{q}_{e_{R_{i}}}\bar{e}_{R_{i}}\gamma^{\alpha}e_{R_{i}}+\mathbf{q}_{v_{R_{i}}}\bar{v}_{R_{i}}\gamma^{\alpha}v_{R_{i}}\right] \\ +\mathbf{q}_{Q_{L_{i}}}\bar{Q}_{L_{i}}\gamma^{\alpha}Q_{L_{i}}+\mathbf{q}_{u_{R_{i}}}\bar{u}_{R_{i}}\gamma^{\alpha}u_{R_{i}}+\mathbf{q}_{d_{R_{i}}}\bar{d}_{R_{i}}\gamma^{\alpha}d_{R_{i}}\right]$$

The Z'_0 background generates a chemical potential for them.

This in turn generates a Thermal Equilibrium Asymmetry in SM leptons



$$\Delta n_{L_L}^{\rm EQ}(z) = \frac{2N_g T_c^2}{3} \mu_{L_L}(z) = \frac{2g' N_g T_c^2}{3} \langle Z_0'(z) \rangle$$





10

Dark CPV: Baryogenesis

• Solving the corresponding Boltzman equation , considering sphaleron rate suppressed inside the bubble wall, one generates a lepton asymmetry ΔN_L

$$\frac{\partial \Delta n_{L_L}(z,t)}{\partial t} = \Gamma_{\rm sph}(z-v_\omega t) \left[\Delta n_{L_L}^{\rm EQ}(z-v_\omega t) - \Delta n_{L_L}(z,t) \right] \longrightarrow \Delta n_{L_L} = \frac{\Gamma_0}{v_\omega} \int_0^\infty dz \, \Delta n_{L_L}^{\rm EQ}(z) e^{-\Gamma_0 z/v_\omega} \ .$$

 Γ_{sph} exponentially suppressed after the bubble wall has passed

• Sphaleron processes conserve B-L \rightarrow equal asymmetries are generated $\Delta N_L = \Delta N_B$

$$\eta_B = \frac{\Delta n_B}{s} \rightarrow \eta_B \simeq 0.9 \ 10^{-10} \ \text{as needed}$$

Crucial Condition: Non-vanishing lepton asymmetry depends on the EFT at EW scale having an anomalous lepton number, but a gauged U(1)_I should be anomaly free

Anomalons in a gauged U(1)_I

Particle	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)_{\ell}$
$ u_R^i$	1	1	0	1
$L_L' = (\nu_L', e_L')^T$	1	2	-1/2	q
e_R'	1	1	-1	q
χ_R	1	1	0	q
$L_R'' = (\nu_R'', e_R'')^T$	1	2	-1/2	$ q + N_g $
$e_L^{\prime\prime}$	1	1	-1	$ q + N_g $
χ_L	1	1	0	$q+N_g$

Z' couples to SU(2)_L current, governing L/B violating processes

$$\mathcal{J}^{\mu} = \sum_{i=1}^{N_g} \bar{L}_{L_i} \gamma^{\mu} L_{L_i} + q \bar{L}'_L \gamma^{\mu} L'_L + (q + N_g) \bar{L}''_R \gamma^{\mu} L''_R + \cdots$$

$$\partial_{\mu} \mathcal{J}^{\mu} \propto \operatorname{tr}(\ell \tau^{a} \tau^{b}) W^{a} \widetilde{W}^{b} \propto [N_{g} \times 1 + \mathbf{q} - (\mathbf{q} + N_{g})] \operatorname{tr}(W \widetilde{W}) = 0$$

$$\Delta n_{L,\mathrm{eff}}^{\mathrm{EQ}} = \Delta n_{L_L}^{\mathrm{EQ}} + \Delta n_{L_L'}^{\mathrm{EQ}} - \Delta n_{L_R''}^{\mathrm{EQ}} = \left[N_g \times 1 + \mathsf{q} - (\mathsf{q} + N_g) \right] \quad \frac{2}{3} T_c^2 g' \left\langle Z_0' \right\rangle$$

e.g. $I = e + \mu + \tau (N_g = 3)$

SU(2) anomalons must decouple from thermal number density

