



HOM-damping studies of a 5-Cell Elliptical Superconducting Cavity for PERLE

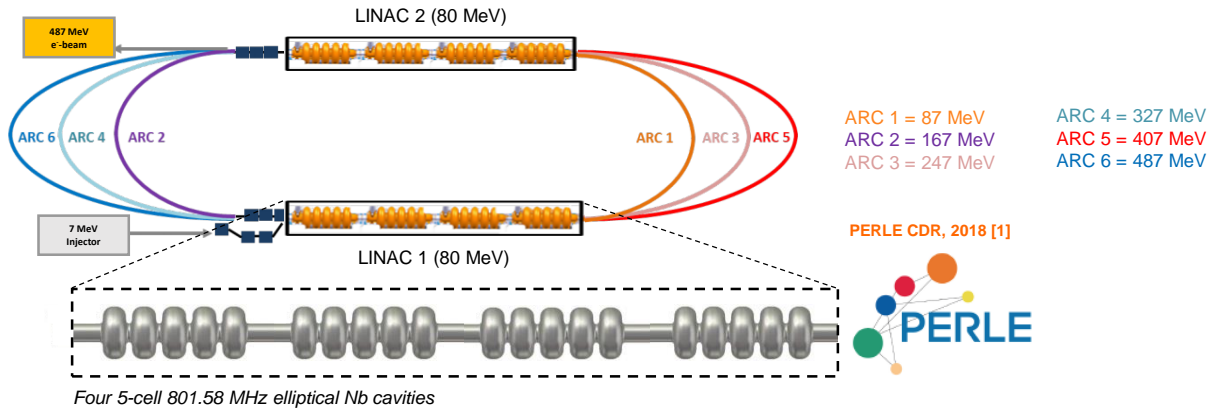
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Université Paris-Saclay

PERLE SRF Meeting, 03 December 2021

1. What is PERLE?
2. PERLE SRF Cavity – JLab design
3. HOM numerical simulations (CST Studio Suite[®])
4. 3D-Eigenmode/Wakefield simulations – JLab Case 1 Bare Cavity
5. HOM coupler power transmission studies and coupler optimization
6. HOM-damping studies
7. Future perspectives
8. Conclusions

- **PERLE** (**P**owerful **E**nergy **R**ecovery **L**inac for **E**xperiments): multi-turn ERL based on SRF technology to be studied and later host at **Orsay** (France).



Target Parameter [2]	Unit	Value
Injection energy	MeV	7
Electron beam energy	MeV	500
Normalized Emittance $\Upsilon_{e,x,y}$	mm-mrad	6
Average beam current	mA	20
Bunch charge	pC	500
Bunch length	mm	3
Bunch spacing	ns	25
RF frequency	MHz	801.58
Duty factor	CW (Continuous Wave)	

- 2 Linacs (Four 5-Cell 801.58 MHz SC cavities)
- 3 turns (160 MeV/turn): 3 passes 'up' to reach the maximum energy, 3 passes 'down' for energy recovery
- Maximum electron beam energy: 500 MeV

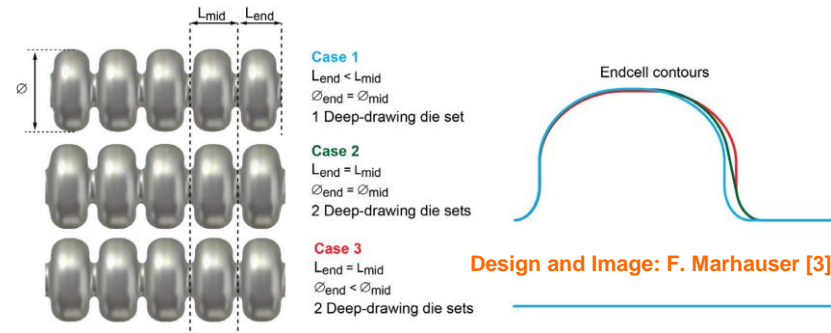
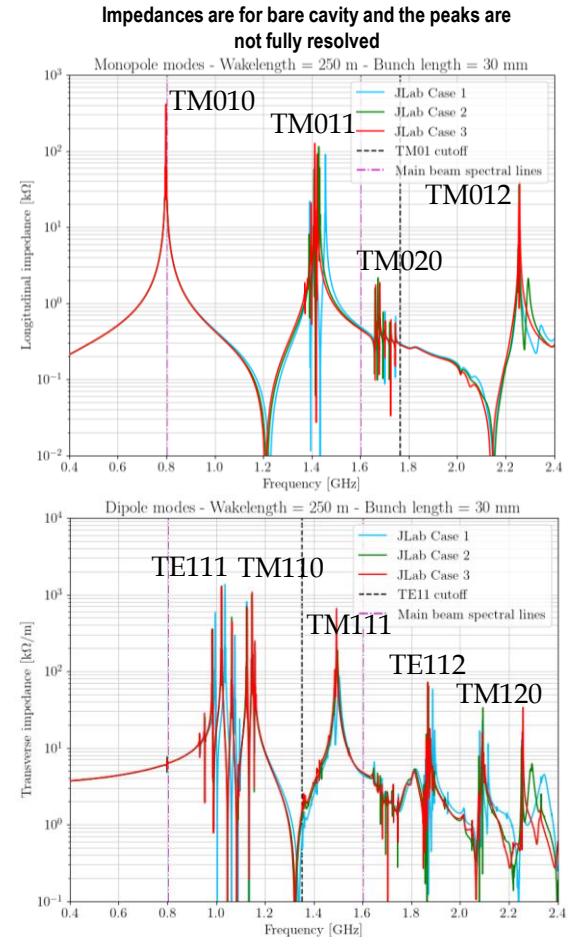
- **IJCLab** is today leading the PERLE project in the context of a collaboration between international partners:

- **Objective:** design and prototyping of a full **dressed SRF cavity** required in CW operation, with adequate HOM damping.
- First 801.58 MHz 5-cell elliptical Nb cavity already fabricated at **JLab** on October 2017 (**JLab Case 1 Cavity**)



Parameters*	JLab Case 1	JLab Case 2	JLab Case 3
Frequency [MHz]	801.58	801.58	801.58
Number of Cells	5	5	5
Material	Bulk Nb.	Bulk Nb.	Bulk Nb.
Temperature [K]	2.0	2.0	2.0
Cavity active length [mm]	917.911	935.536	935.536
Mid-cell length [mm]	187.107	187.107	187.107
End-cell length [mm]	178.295	187.107	187.107
R/Q [Ω]	524.25	520.63	522.70
(R/Q)/(cell number) [Ω]	104.85	104.13	104.54
Geometry Factor (G) [Ω]	274.505	201.490	278.112
$G^*(R/Q)$ [Ω^2]	143909.2	149901.7	145369.1
$(R/Q)*G/(cell\ number)$ [Ω^2]	28781.85	29980.35	29073.83
B_{pk}/E_{acc} (mid-cell) [mT/(MV/m)]	4.62	4.70	4.66
E_{pk}/E_{acc} (mid-cell) [-]	2.38	2.30	2.27
Iris radius [mm]	65	65	65
Beam Pipe radius [mm]	65	65	65
Mid-cell equator diameter [mm]	328	328	328
End-cell equator diameter [mm]	328	328	325
Wall angle [degree]	0	11.95	0
Cell-to-cell coupling of mid cells [%]	2.93	2.92	2.91
$k_{ }(\sigma_z = 3\text{ mm})$ [V/pC]	2.74	2.4	2.74
Cutoff TE11 [GHz]	1.35	1.35	1.35
Cutoff TM01 [GHz]	1.77	1.77	1.77

Note: $Q_{ext} \sim 10^7 \rightarrow 50\text{ kW}$ allows for sufficient margin during transients \rightarrow detuning $\sim 51.9\text{ Hz}$

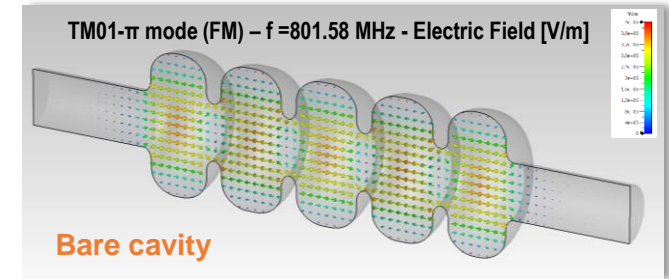


- **HOM-damping for ERLs** is a **challenge** due to the presence of many turns.

- **3D-Eigenmode simulations (bare and equipped cavity)**

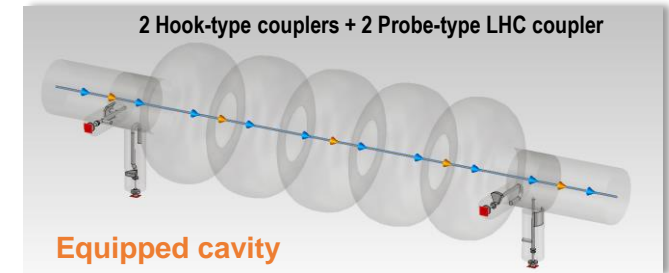
- Main RF parameters (table slide 4)
- Identification of dangerous **HOMs**
- **R/Q** and field distribution

All simulations were done
for JLab Case1 Cavity



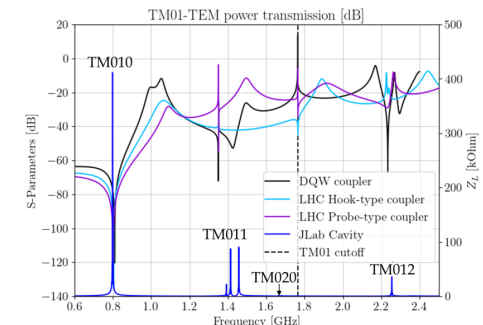
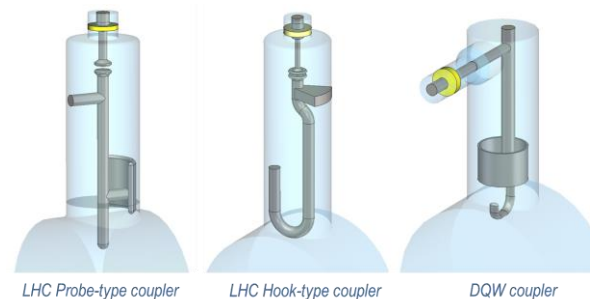
- **3D-Wakefield simulations (cavity-beam interaction)**

- Longitudinal impedance (Z_L [Ω])
- Transverse impedance (Z_T [Ω/m])



- **HOM-coupler power transmission**

- **S-parameter** [dB] calculation
- Coupler optimization (*recently started*)



*3D-Eigenmode simulations on equipped cavity (cavity + HOM coupler + PC) are still in progress

Longitudinal shunt impedance [Ω]

$$\frac{R}{Q_{||,n}} = \frac{|V_{||,n}(0,0)|^2}{\omega_n U_n}$$

Transversal shunt impedance [Ω/m]

$$\frac{R}{Q_{t,n}} = \frac{\frac{|V_{\perp x,n}(0,0)|^2}{\omega_n U_n} + \frac{|V_{\perp y,n}(0,0)|^2}{\omega_n U_n}}{r_0}$$

Longitudinal loss factor [V/pC]

$$k_{||,n} = \frac{\omega_n R}{4 Q_{||,n}}$$

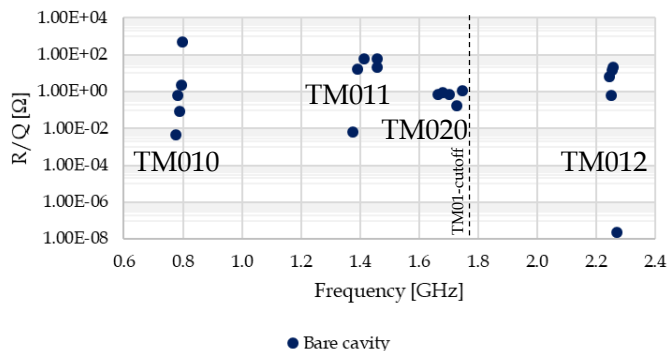
Transversal loss factor [V/(mm·pC)]

$$k_{t,n} = \frac{\omega_n^2 r_0 R}{c Q_{t,n}}$$

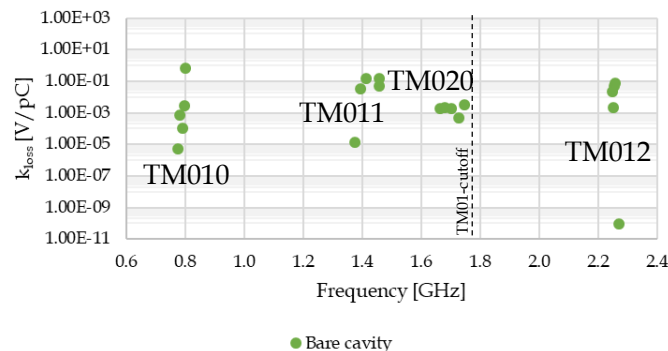
Wake length* [km]
(for $\sigma_{Cu}=5.80E+07 \Omega^{-1}m^{-1}$)

$$w_l = c\tau_n = c \frac{Q}{\omega_n}$$

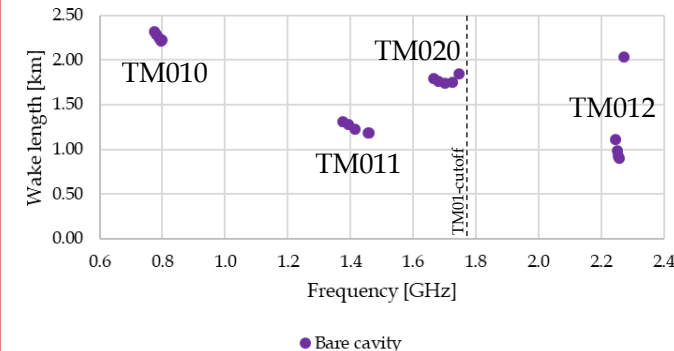
Monopole modes - R/Q - JLab cavity - Case 1



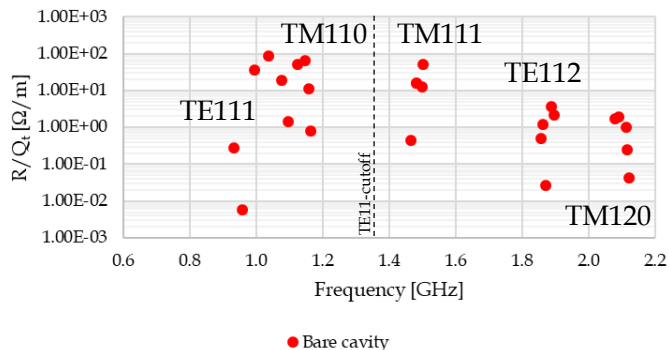
Monopole modes - Loss factor - JLab cavity - Case 1



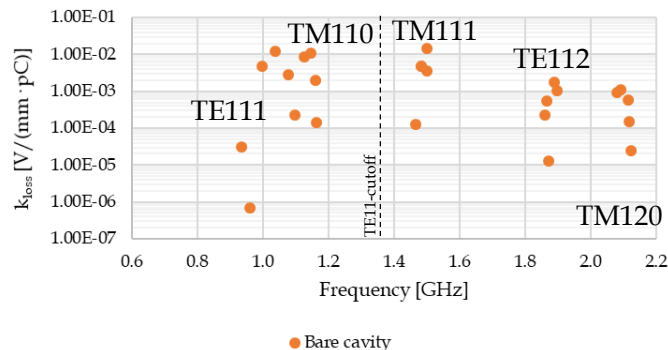
Monopole modes - Wake length - JLab cavity - Case 1



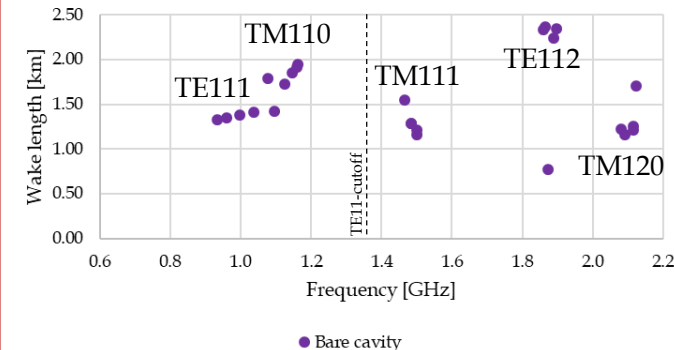
Dipole modes - R/Q_t - JLab cavity - Case 1

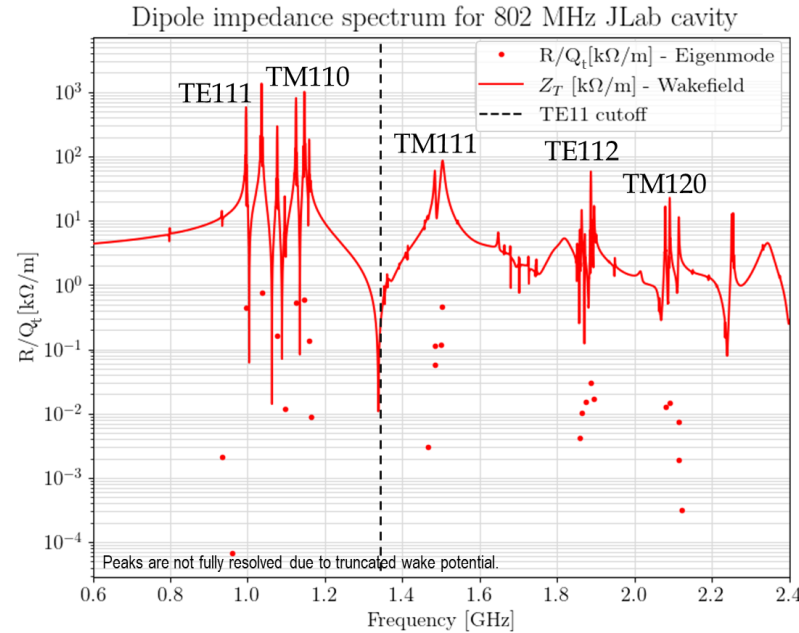
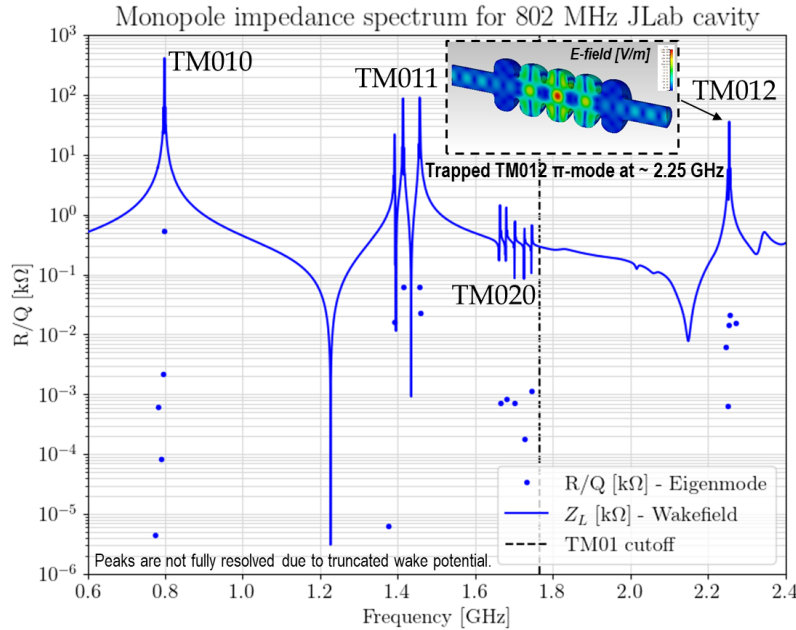


Dipole modes - Loss factor - JLab cavity - Case 1



Dipole modes - Wake length - JLab cavity - Case 1





TM monopole modes (like TM010, TM011, TM020, T012)

- E-field component along cavity axis
- Trapped mode can interact with the subsequent bunch
- Relative inefficient coupling of the TM012 π -mode to the beam tubes

TM dipole modes (like TM110, TM111, TM120)

- Strong longitudinal E-field component off axis.
- Possible deflection and subsequent beam resonant effect.

TE dipole modes (like TE111, TE112)

- Theoretically no longitudinal E-field component on and off axis.

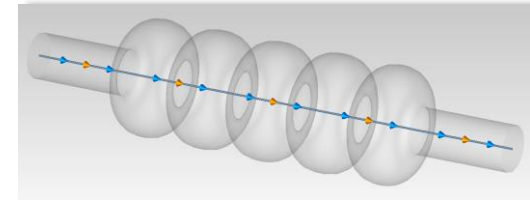
3D-Wakefield simulation:

Longitudinal impedance [Ω]

$$Z_L(\mathbf{r}, \omega) = \frac{1}{c} \int_{-\infty}^{\infty} w_L(\mathbf{r}, s) e^{-\frac{j\omega s}{c}} ds$$

Transverse impedance [Ω/m]

$$Z_T(\mathbf{r}, \omega) = \frac{-j}{r_0 c} \int_{-\infty}^{\infty} \mathbf{w}_T(\mathbf{r}, s) e^{-\frac{j\omega s}{c}} ds$$



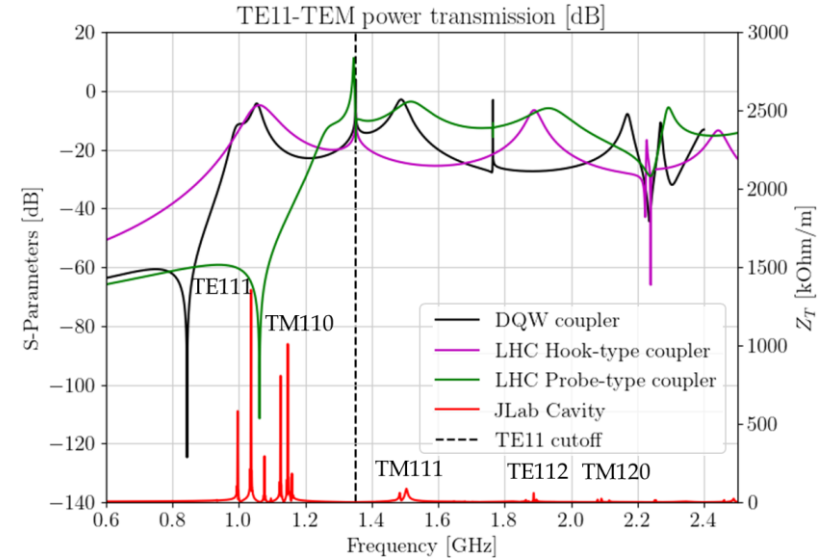
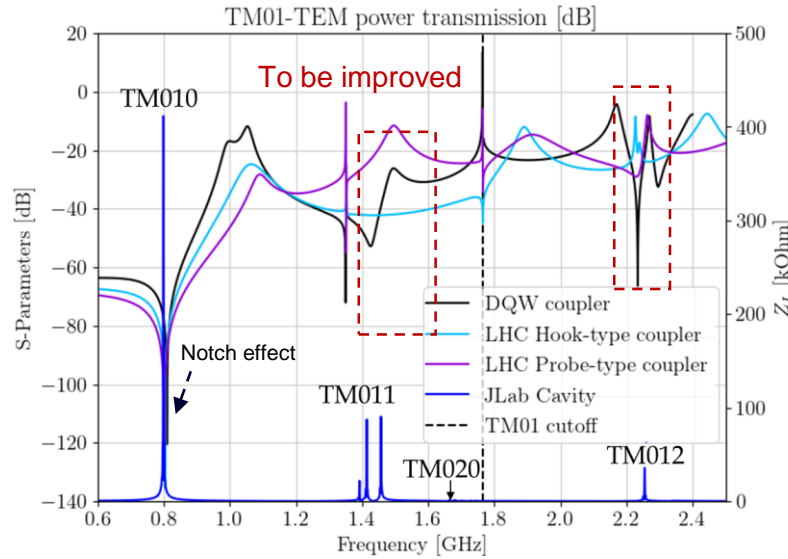
Wakefield simulation parameters JLab Case 1

Beam velocity β [-]	1
RMS bunch length [mm]	30
Wake length [m]	250
Number of samples [-]	1E+06

S-parameters [dB] simulation (frequency domain solver)

For a device with n ports

$$S = \begin{bmatrix} S_{11} & S_{12} & \dots & S_{1n} \\ S_{21} & S_{22} & \dots & \cdot \\ \cdot & \cdot & \dots & \cdot \\ S_{n1} & \cdot & \dots & S_{nn} \end{bmatrix} \begin{matrix} S_{ii} \text{ for reflected} \\ \text{power} \\ \\ S_{ij} \text{ for the} \\ \text{transmitted power} \end{matrix}$$

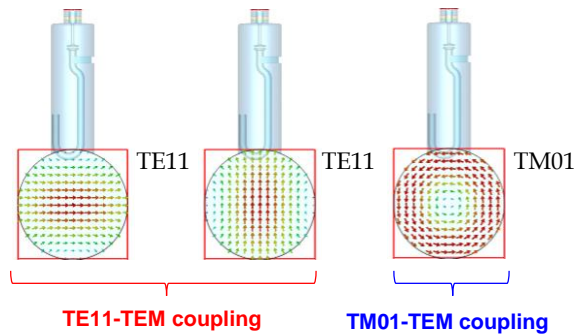


TM01-TEM transmission

- The notch effect of all couplers is tuned to 801.58 MHz for the monopole coupling.
- Couplers still need to be optimized to deliver a higher value of transmission for the TM011 and TM012 passband.

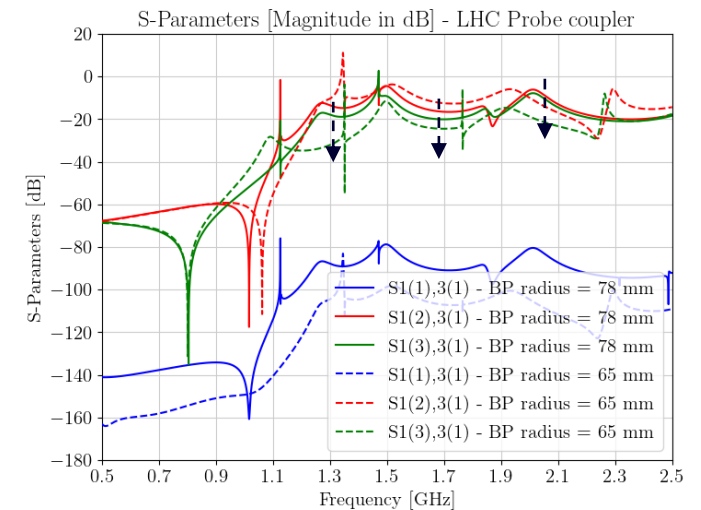
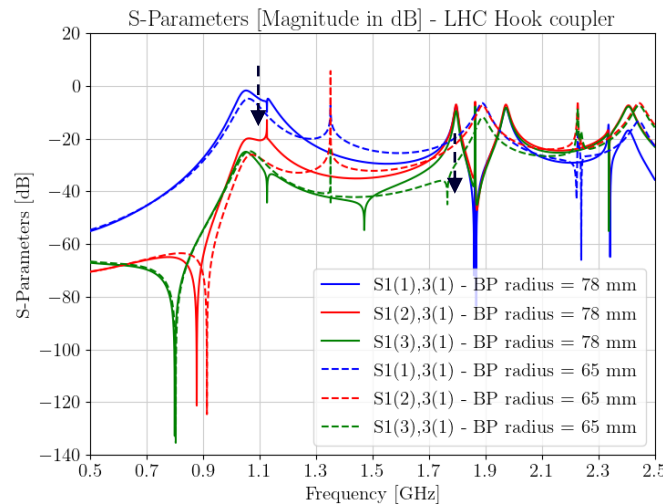
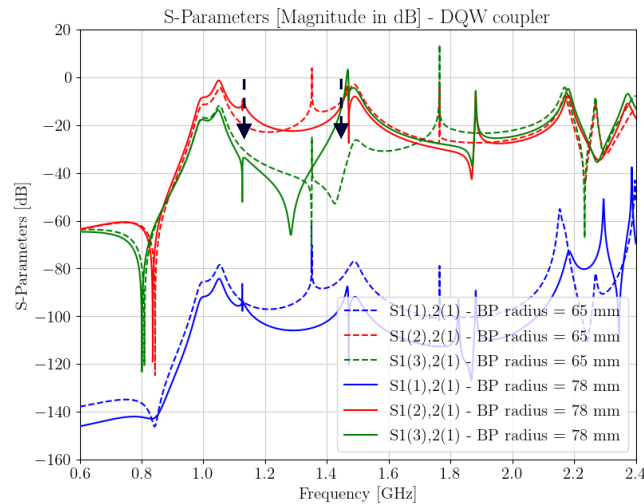
TE11-TEM transmission

- Hook coupler gives a higher transmission than DQW coupler for the TE111 and TM110 passband.



HOM coupler models used in our simulations were initially designed for a beam tube radius of $R=78$ mm (801.58 MHz Rostock University cavity).

- JLab 5-cell cavity has a 65 mm beam tube radius.
- S-curves are very sensitive to geometrical changes of couplers.
- Installation of current couplers in $R=65$ mm tubes: drop in performance in certain frequency ranges where HOMs need to be damped.



Optimization is needed: DQW coupler can assure a high transmission for both first higher order monopole and dipole passband.

CST Studio Suite

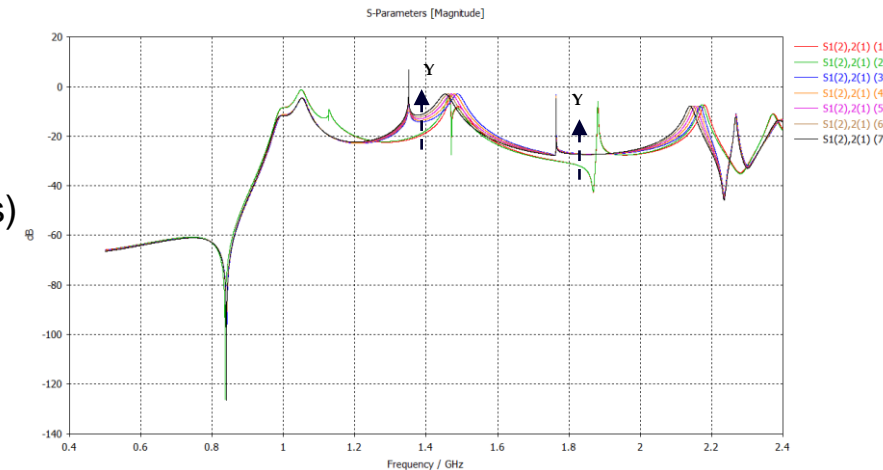
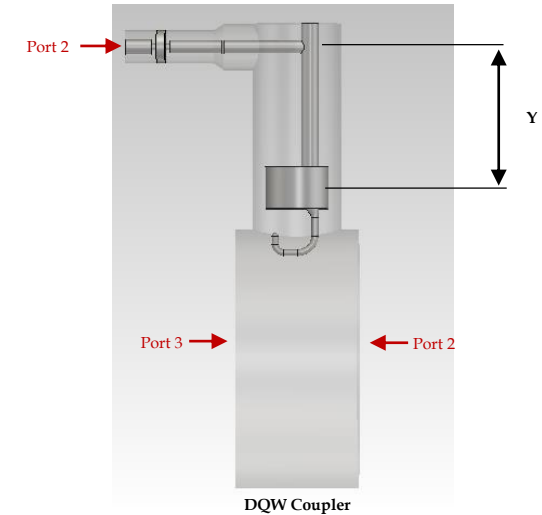
- Solver: Frequency domain solver
- Optimizer algorithm: Trust region framework, CMA evolution strategy...

STEP 1: parameter sweep analysis (one-parameter-at-a-time)

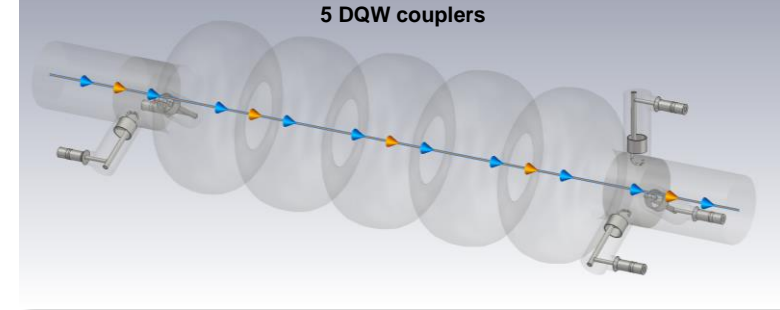
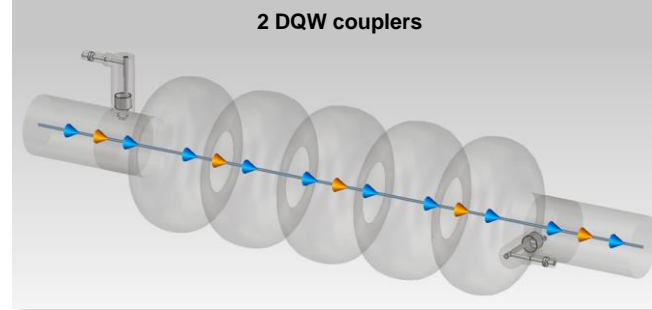
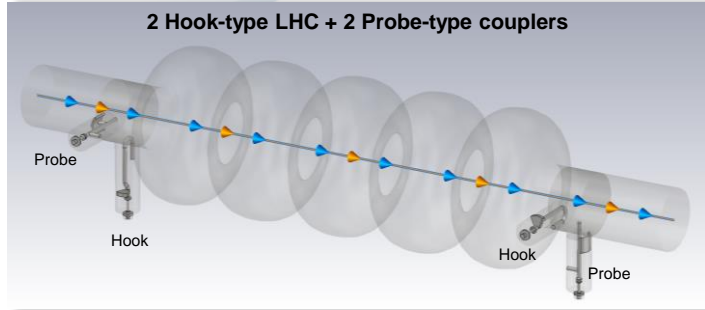
- Build a parametric geometry (max 40 parameters) of the HOM coupler
- Each parameter corresponds to a specific part of the HOM coupler equivalent circuit
- See the influence of each geometrical parameters on S-curves
- Find out which parameters play a more important role in changing S-curves

STEP 2: CST optimizer to fine-tune

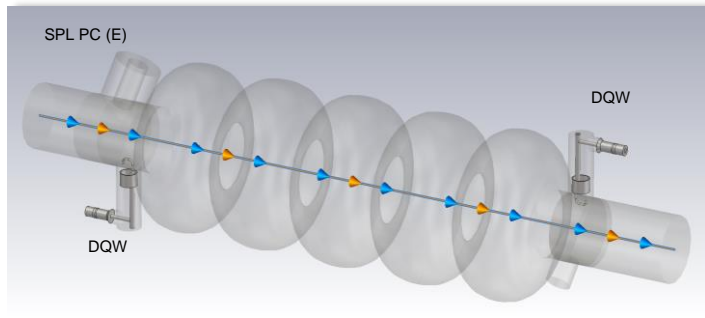
- Definition of the objective functions (minimization of the highest impedances)
- Optimization of multiple parameters at the same time (max 5 parameters).



5-cell cavity + HOM couplers

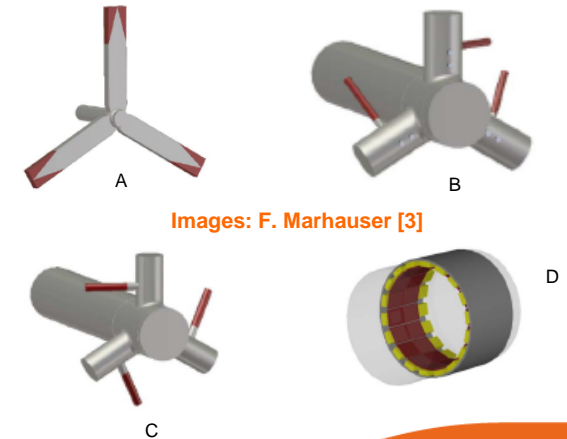


5-cell cavity + HOM couplers + SPL Power Coupler

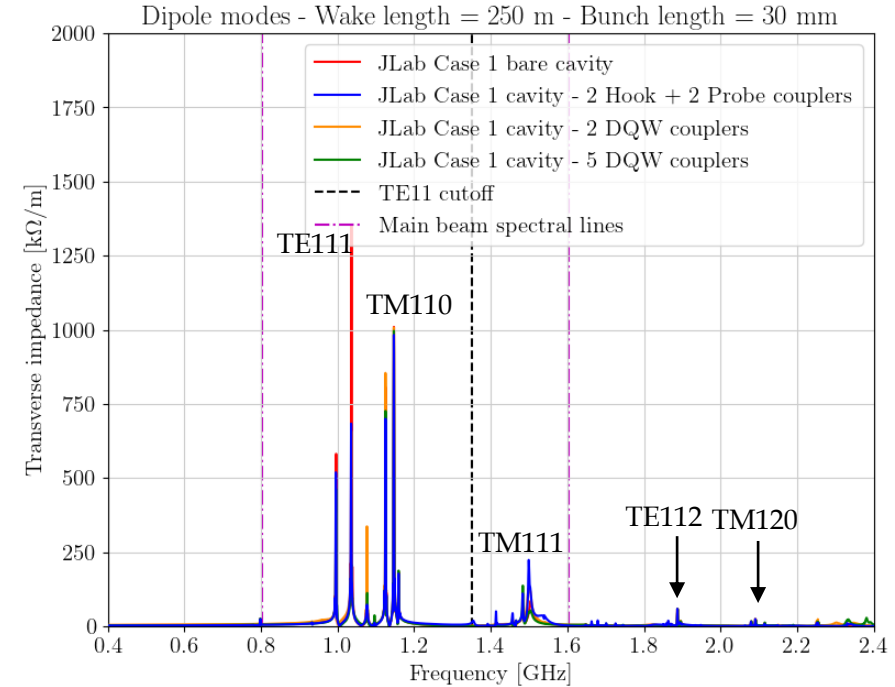
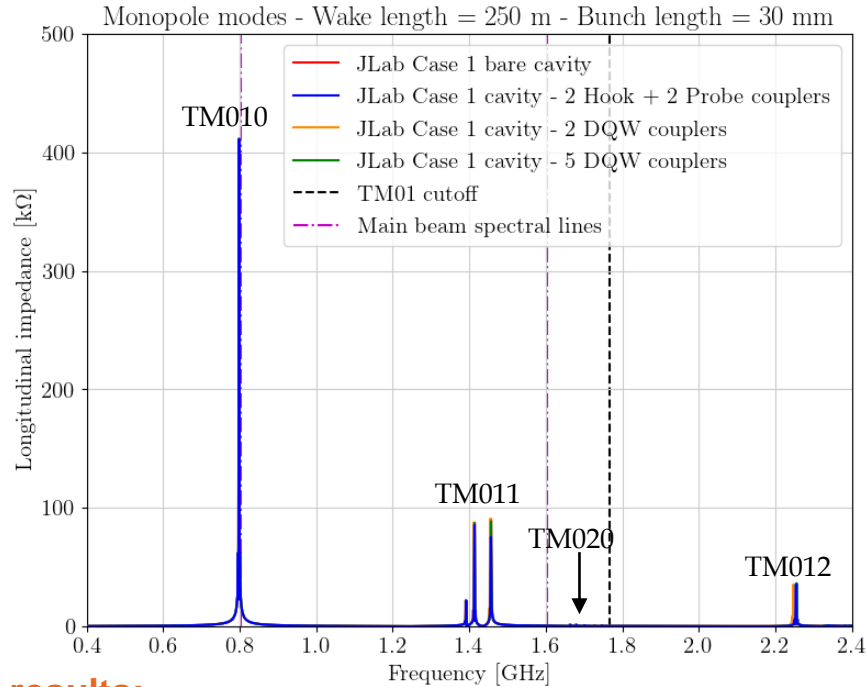


Other suitable HOM-damping schemes :

- Rectangular waveguide dampers (A)
- JLab-Type coaxial couplers (B)
- TESLA-Type coaxial couplers (C)
- Add absorbers in cavity-interconnecting beam tubes (D)
- Coupling through Fundamental Power Coupler (E)



- **Objective:** extract the energy of the dangerous HOMs from the cavity.



Preliminary results:

- 2 Hook + 2 Probe couplers configuration seems to provide a better damping than the DQW couplers configurations. However, DQW couplers have still to be optimized!
- Peaks are not fully resolved. **Extrapolated impedance spectra** need to be calculated (JLab's method) [9]
- **Trapped TM012 mode** was not damped in the investigated configurations (end-cells modification is needed)

Average HOM power deposited by the beam in the cavity

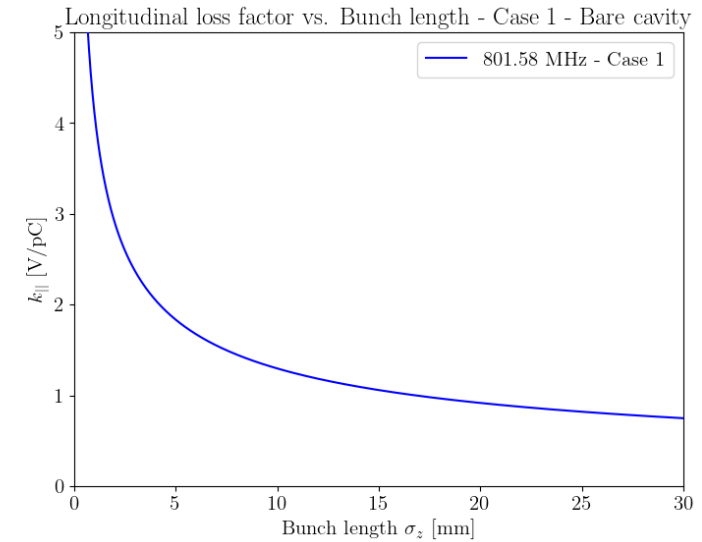
$$P_{HOM} = k_{||,HOM} Q_b I_0$$

If the main spectral line of the beam falls on the HOM resonance of the cavity, the voltage increases as well as the HOM power

$$P_{HOM} = \frac{R}{Q} Q_L I_0^2$$

Objective 1: estimate the HOM power once we will have the bunch spectrum of the beam available.

Objective 2: doing a thermal study on HOM couplers



RF and beam parameters	PERLE	PERLE @ Orsay
Q_b	320 pC	500 pC
I_0	15 mA	20 mA
σ_z	3 mm	3 mm
$k_{ }$	2.742 V/pC	2.742 V/pC
$k_{ ,0}$	0.657 V/pC	0.656 V/pC
P_{HOM} (1 pass)	10.009 W	20.862 W

Experimental activities:

- Cavity end-cell modifications (improve the damping of TM011 and TM012 mode)
 - Do we plan to do perform the modifications at JLab or at CERN, where and when (**Q1 2022**)?
 - Measurements on the cavity
- Tube modification to install HOM couplers
- Realization of the HOM couplers and installation on the cavity
- Integration of the PERLE cavity in the SPL cryomodule
- Thermal treatments (Nitrogen doping) on the cavity
- Integration of the SPL Power Coupler
- Test of the full dressed cavity on the vertical cryostat

- Eigenmode and wakefield analyses were carried-out in CST Studio Suite® to investigate on the HOM behavior of PERLE Cavity
- Potentially dangerous monopole and dipole HOMs were identified and classified until 2.4 GHz. A trapped monopole HOM was found at ~2.25 GHz
- HOM-damping scheme studies: 2 Hook + 2 Probe couplers configuration gives a better damping of both monopole and dipole HOMs than the two DQW coupler configurations. However, couplers need still to be optimized.

Future perspectives:

- Optimization of the cavity end-cells to improve the coupling of the TM₀₁₂ π -mode to the beam tubes
- Optimization of HOM couplers, and study of other HOM couplers (JLAB, TESLA)
- Thermal studies for HOM couplers (HOM power and dissipation)
- Planning of the experimental activities (CERN and JLab)

- [1] D. Angal-Kalinin et al., PERLE, Powerful Energy Recovery Linac for Experiments, CDR, *Journal of Physics G: Nuclear and Particle Physics*, 45(6):065003, 2018.
- [2] W. Kaabi, PERLE: A High-Power Energy Recovery Facility at Orsay, February 2021.
- [3] F. Marhauser, Next generation HOM-damping, *Superconductor Science and Technology*, 30(6):063002, 2017.
- [4] F. Marhauser, PERLE Cavity Design and Results and First Thoughts on HOM-Couplers, *PERLE HOM Coupler Meeting*, October 2019, CERN.
- [5] T. Wangler, RF Linear Accelerators, John Wiley & Sons, 2008.
- [6] CST Studio Suite manual, *CST Studio*, 2021.
- [7] F. Marhauser, Higher Order Modes (HOMs), SRF Hands-On Course at JLab, January 19-30, 2015, Newport News, VA.
- [8] R. Calaga and S.G. Zadeh, HOM Damping for PERLE, 2019.
- [9] F. Marhauser, Enhanced Method for Cavity Impedance Calculations, Proceedings of PAC09, Vancouver, BC, Canada, 2009.

Thank you for your attention!



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Backup slides

The **eigenmodes** of a resonator in a non-excited source-free and lossless medium are computed by solving the Helmholtz equations:

Helmholtz equations

$$\nabla^2 \underline{\mathbf{E}} + \omega^2 \mu \varepsilon \underline{\mathbf{E}} = 0$$

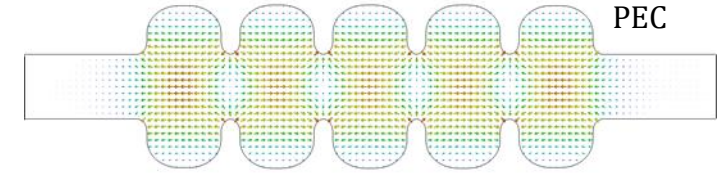
$$\nabla^2 \underline{\mathbf{H}} + \omega^2 \mu \varepsilon \underline{\mathbf{H}} = 0$$

Boundary conditions

$$\mathbf{n} \times \underline{\mathbf{E}} = 0 \quad \text{and} \quad \mathbf{n} \cdot \underline{\mathbf{H}} = 0 \quad \text{on} \quad \partial \Omega_{\text{PEC}}$$

$$\mathbf{n} \cdot \underline{\mathbf{E}} = 0 \quad \text{and} \quad \mathbf{n} \times \underline{\mathbf{H}} = 0 \quad \text{on} \quad \partial \Omega_{\text{PMC}}$$

TM01- π mode (FM) – $f = 801.58$ MHz



Assumption: PEC (Perfect Electric Conductor) on conducting walls (N_b) and interior domain of vacuum

Cavity-beam interaction: **wakefields** in time domain or **impedances** in frequency domain. The long-range wakefield commonly corresponds to the **high impedance peaks** and can lead to coupled-bunch instability issues.

Eigenmode simulations

Longitudinal shunt impedance [Ω]

$$\frac{R}{Q_{||,n}} = \frac{|V_{||,n}(0,0)|^2}{\omega_n U_n}$$

Transverse shunt impedance [Ω/m]

$$\frac{R}{Q_{t,n}} = \frac{|V_{\perp x,n}(0,0)|^2 + |V_{\perp y,n}(0,0)|^2}{\omega_n U_n r_0}$$

Wakefield simulations

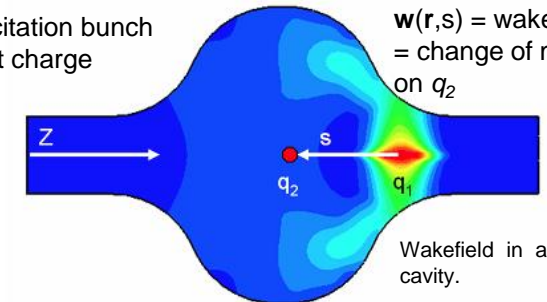
Longitudinal impedance [Ω]

$$Z_L(\mathbf{r}, \omega) = \frac{1}{c} \int_{-\infty}^{\infty} w_L(\mathbf{r}, s) e^{-\frac{j\omega s}{c}} ds$$

Transverse impedance [Ω/m]

$$\mathbf{Z}_T(\mathbf{r}, \omega) = \frac{-j}{r_0 c} \int_{-\infty}^{\infty} \mathbf{w}_T(\mathbf{r}, s) e^{-\frac{j\omega s}{c}} ds$$

q_1 = excitation bunch
 q_2 = test charge



$\mathbf{w}(\mathbf{r}, s)$ = wake potential
 = change of momentum
 on q_2

Wakefield in an elliptical cavity.

The energy left behind q_1 is called **wakefield**.

- $$P_{HOM} = k_{||,HOM} Q_b I_0$$

bunch charge \downarrow
 Q_b
 average beam current \uparrow

HOM power (1 pass)
- $$k_{||,HOM} = k_{||} - k_{||,0}$$

Total longitudinal loss (CST wakefield) \downarrow
 $k_{||}$
 Loss factor of FM (Fundamental Mode) \uparrow

Longitudinal loss factor
- $$k_{||}(\sigma_z) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} Z_{||}(\omega) e^{-(\omega\sigma_z/c)^2} d\omega$$

Longitudinal impedance (CST wakefield) \downarrow
- $$k_{||,0} = \frac{\omega_0}{4} \frac{R}{Q_{||,0}} e^{-(\omega_0\sigma_z/c)^2}$$

Geometric shunt impedance (Fundamental Mode) \uparrow

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