



DYTurbo interface for xFitter

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DYTurbo project

- Optimised version of DYNNLO, DYqT, DYRes with improvements in

Software	Numerical integration
Code profiling	Quadrature with interpolating functions
Loop vectorisation	Factorisation of integrals
Hoisting	Analytic integration
Loop unrolling	
Multi-threading	

- The main application is the measurement of the W mass at the LHC, Other applications: PDF fits including qt-resummation for cross-section predictions, $\sin^2\theta_w$, $\alpha_s(m_Z)$
- A few active developers (SC, Giancarlo Ferrera, Leandro Cieri, Manuel Der) and several users helping with testing, scripts, etc...
- Widely used in ATLAS, CMS, LHCb, primary usage are W,Z NNLO predictions

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Fast predictions for Drell-Yan processes including q_T -resummation

Installation instructions

Download the source code

- [dyturbo-1.1.tar.gz](#)

- Public code available on HEPForge (<https://dyturbo.hepforge.org/>)
- Original reference”
 - ➔ “DYTurbo: Fast predictions for Drell-Yan processes” Eur.Phys.J.C 80 (2020) 3, 251
- Recent developments:
 - ➔ “Drell–Yan lepton-pair production: q_T resummation at N3LL accuracy and fiducial cross sections at N3LO”, Phys.Rev.D 104 (2021) 11, L111503
 - ➔ “Fiducial perturbative power corrections within the q_T subtraction formalism”, arXiv:2111.14509

Drell-Yan cross section

- DYTurbo can compute the DY cross section at

Fixed order
with qt-subtraction

$$d\sigma_{(N)NLO}^V = d\sigma_{(N)NLO}^{\text{virt}} - d\sigma_{(N)LO}^{\text{CT(FO)}} + d\sigma_{(N)LO}^{V+\text{jet}}$$

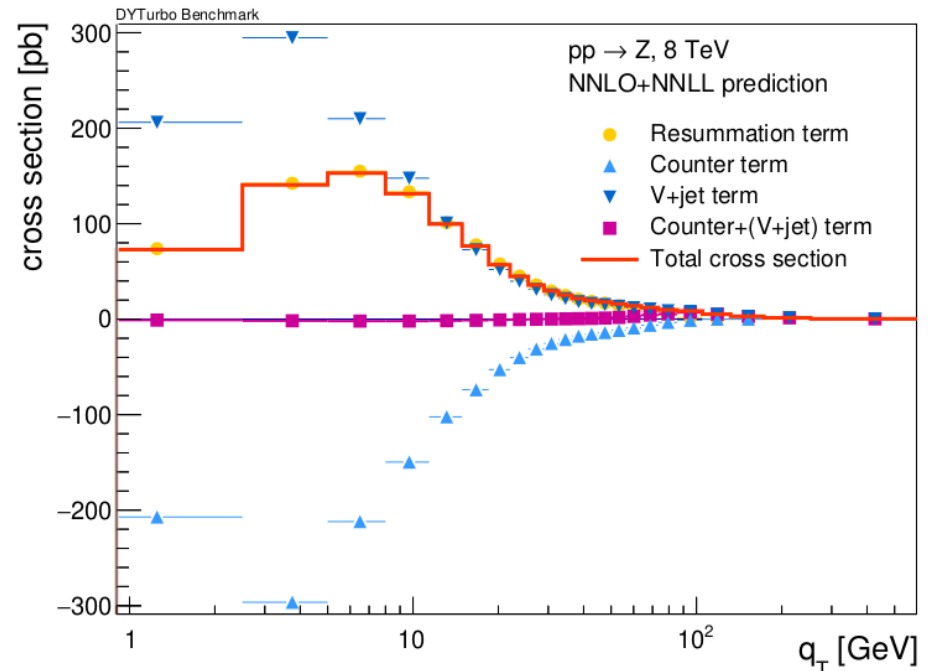
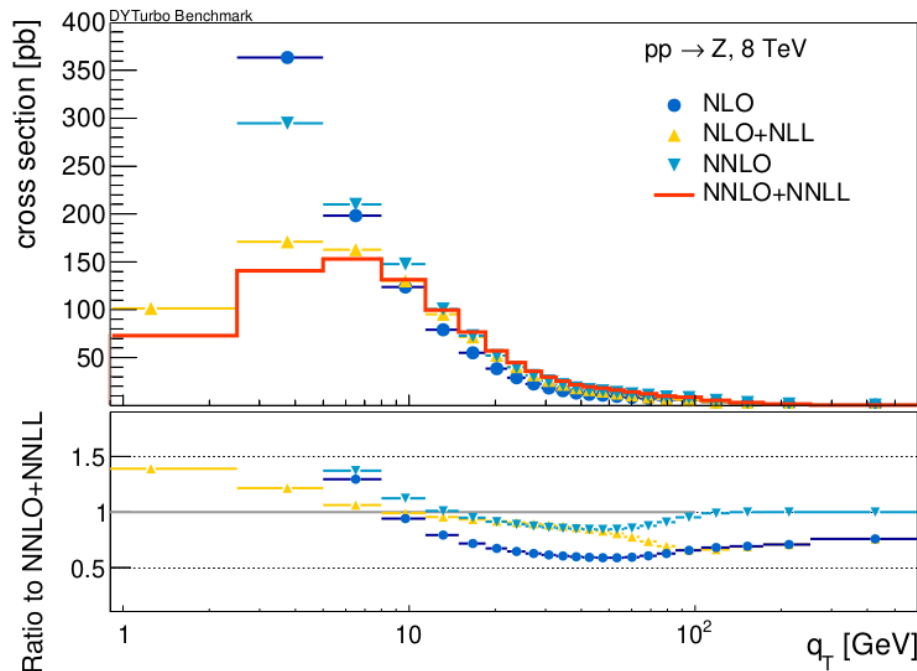
Fast predictions already implemented with NNLOJET + APPLfast

Fixed order
+qt-resummation

$$d\sigma_{(N)NLO+(N)NLL}^V = d\sigma_{(N)NLL}^{\text{res}} - d\sigma_{(N)LO}^{\text{CT(res)}} + d\sigma_{(N)LO}^{V+\text{jet}}$$

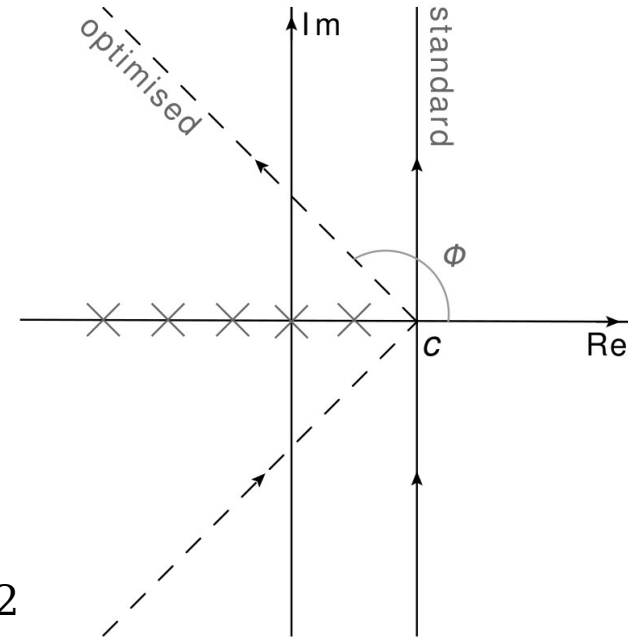
Main motivation for DYTurbo

b-space CdFG resummation formalism



Numerical integration improvements

- Fast x-space to Mellin-space integral transform of PDFs based on Gauss-Legendre quadrature, coefficients in Mellin space evaluated through their large-N expansion
- Acceptance corrections evaluated by factorising the integration over lepton-decay angular variables in the LO cross section



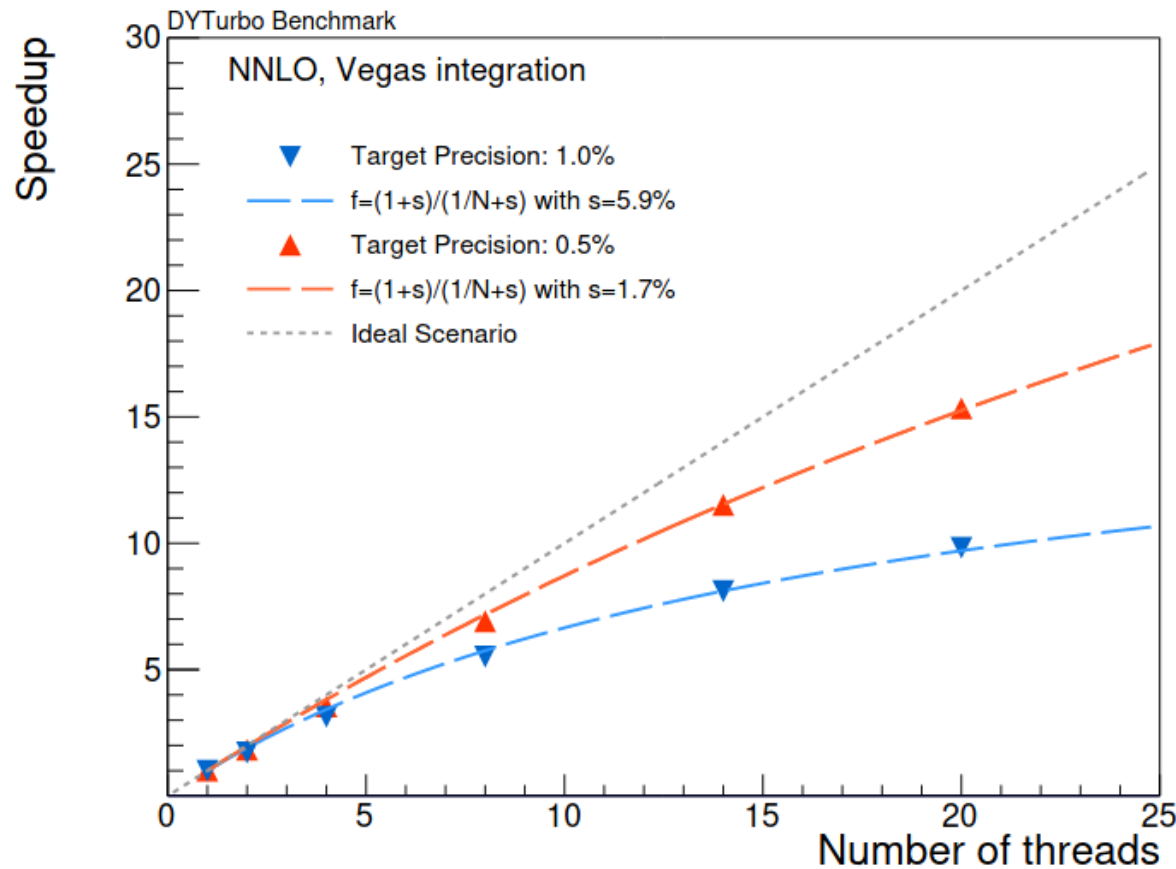
$$\sigma_{LO} = a + b \cos(\theta) + c \cos^2(\theta) \rightarrow a \theta_0 + b \theta_1 + c \theta_2$$

- Analytic integration over
$$\begin{cases} \theta_0 = \int d\Omega \Theta_K, \theta_1 = \int d\Omega \Theta_K \cos \theta_\ell, \\ \theta_2 = \int d\Omega \Theta_K \cos^2 \theta_\ell \end{cases}$$

$$\int dx x J_0(x) = x J_1(x) \quad \rightarrow \quad \int_{q_T^0}^{q_T^1} dq_T 2q_T \mathcal{W}(q_T, m) = \frac{m^2}{s} \int_0^\infty db \frac{1}{2} [q_T^1 J_1(bq_T^1) - q_T^0 J_1(bq_T^0)] \tilde{\mathcal{W}}(b, m)$$

Multithreading time performance

- Measured the performance of the multi-threading implementation

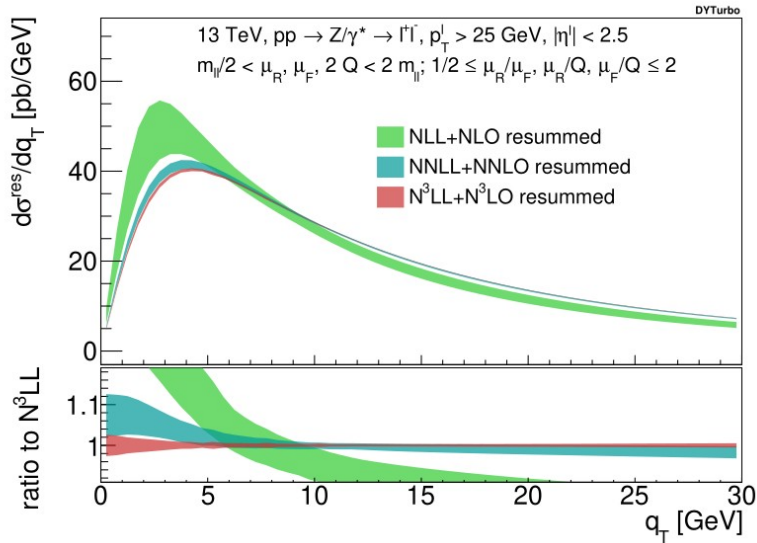


Good efficiency (~ 1) thanks to small overhead

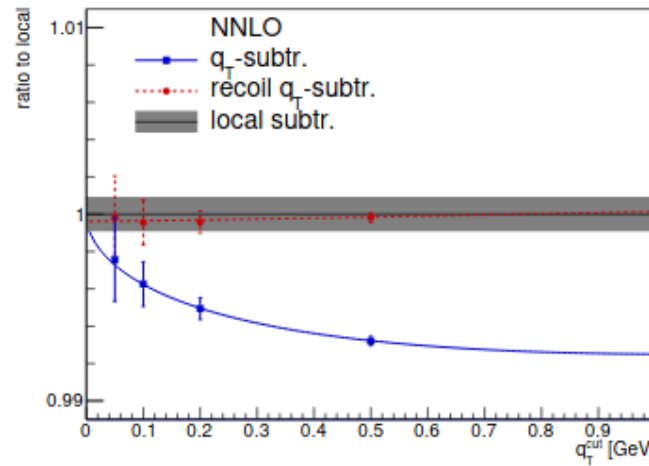
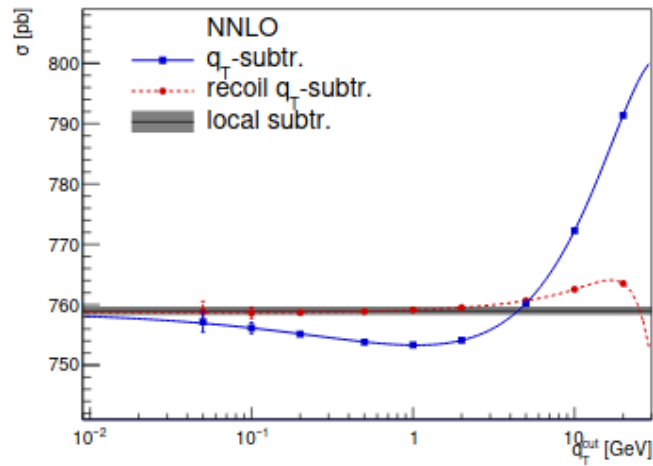
$s \sim 2-5\%$ is the nonparallelisable fraction

Larger gain from multi-threading when the required precision is higher

Recent DYTurbo results



- N3LL q_T resummation
- Fiducial power corrections
- N3LO fiducial cross sections (depend on the availability of external V+jet NNLO predictions)



Order	N ³ LO
q_T subtr. ($q_T^{\text{cut}} = 4$ GeV)	747.1 ± 0.7 pb
recoil q_T subtr.	745.7 ± 0.7 pb

xFitter interface

- DYTurbo-xFitter interface developed in two xFitter branches:
 - ➔ dyturbo-reaction
 - ➔ alphas-scan
- yaml settings currently include scales and non-perturbative parameters

```
# DYTurbo:
order: 2      # Perturbative order in QCD: 0 for LL, 1 for NLL+NLO, 2 for NNLL+NNLO, 3 for NNNLL+NNLO
muR: 1.       # Renormalization scale
muF: 1.       # Factorization scale
muRes: 1.     # Resummation scale
g1: 1         # Universal Gaussian non-perturbative form factor
g2: 0         # Q-dependent Gaussian non-perturbative form factor
g3: 0         # x-dependent Gaussian non-perturbative form factor
Q0: 1         # Reference scale at which the g2 contribution is zero
```

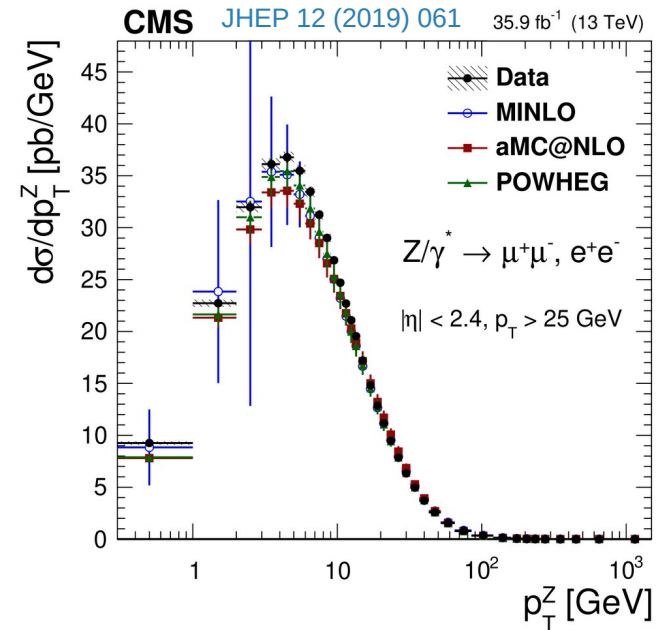
- Two main operational modes for Z/γ^*
 - ➔ Full-lepton phase space cross sections in p_T, y, m : DYTurbo can provide the full fixed order or resummed prediction
 - ➔ Fiducial phase space cross sections in p_T, y, m : include V+jet APPLgrid, DYTurbo computes the rest
- Lepton variables (for W) are possible, but currently rather slow

Measure $\alpha_s(m_Z)$ from semi-inclusive DY

Desirable features for a measurement of $\alpha_s(m_Z)$ [PDG]

- Large observable's sensitivity to $\alpha_s(m_Z)$ compared to the experimental precision
- High accuracy of the theory prediction
- Small size of non-perturbative QCD effects

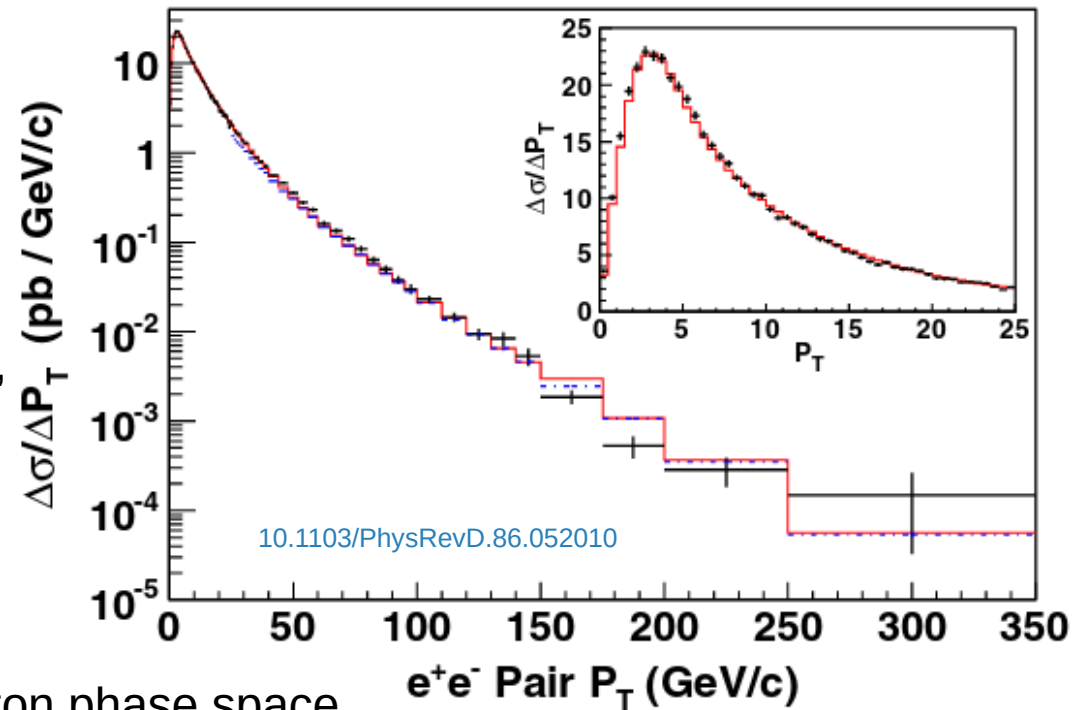
- Measuring $\Lambda_{\overline{\text{MS}}}$ from semi-inclusive (radiation inhibited) DY cross sections was first proposed in [Nucl. Phys. B 349 \(1991\) 635-654](#) (Catani, Marchesini, Webber), in the context of Monte Carlo parton showers
- Here we consider as semi-inclusive observable the Z p_T distribution in the Sudakov region



- Inclusive observables benefit from higher theory accuracy and smaller non-pQCD effects, but usually smaller experimental sensitivity to $\alpha_s(m_Z)$
- Exclusive observables have higher experimental sensitivity, but generally larger theory uncertainties
- Semi-inclusive observables may take benefits from both categories

CDF measurement of Z-boson p_T

- The CDF measurement of Z-boson p_T in full-lepton phase space is an ideal candidate for testing the $\alpha_s(m_Z)$ extraction, and the xFitter-DYTurbo interface



- The measurement is extrapolated to full-lepton phase space using measured angular coefficients

- $p\bar{p}$ collisions

→ reduced contribution from heavy-flavour-initiated production compared to pp collisions

$$\frac{d\sigma}{dpdq} = \frac{d^3\sigma}{dp_T dy dm} \sum_i A_i(y, p_T, m) P_i(\cos\theta, \phi)$$

$$\begin{aligned} b\bar{b} &\rightarrow Z: 0.4\% \\ c\bar{c} &\rightarrow Z: 1.3\% \end{aligned}$$

Theory predictions

- Theory predictions evaluated with DYTurbo: public code implementing CdFG qt-resummation in b-space

$$\frac{d\hat{\sigma}_{Fab}}{dq_T^2} = \frac{d\hat{\sigma}_{Fab}^{(\text{res.})}}{dq_T^2} + \frac{d\hat{\sigma}_{Fab}^{(\text{fin.})}}{dq_T^2}$$

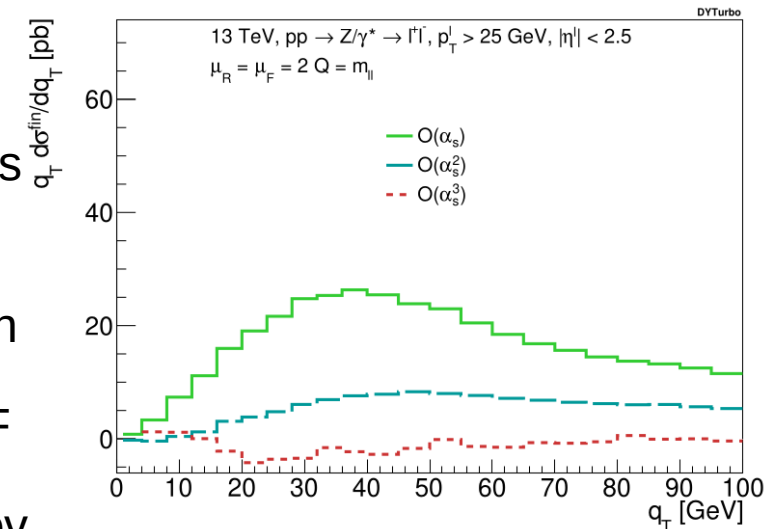
$$\frac{d\hat{\sigma}_V^{(\text{res.})}}{dq_T^2}(q_T, M) = \frac{M^2}{\hat{s}} \int_0^\infty db \frac{b}{2} J_0(bq_T) \mathcal{W}^V(b, M)$$

$$\mathcal{W}_N^V(b, M) = \mathcal{H}_N^V(\alpha_s) \times \exp\{\mathcal{G}(\alpha_s, L)_N\}, L = \log(M^2 b^2)$$

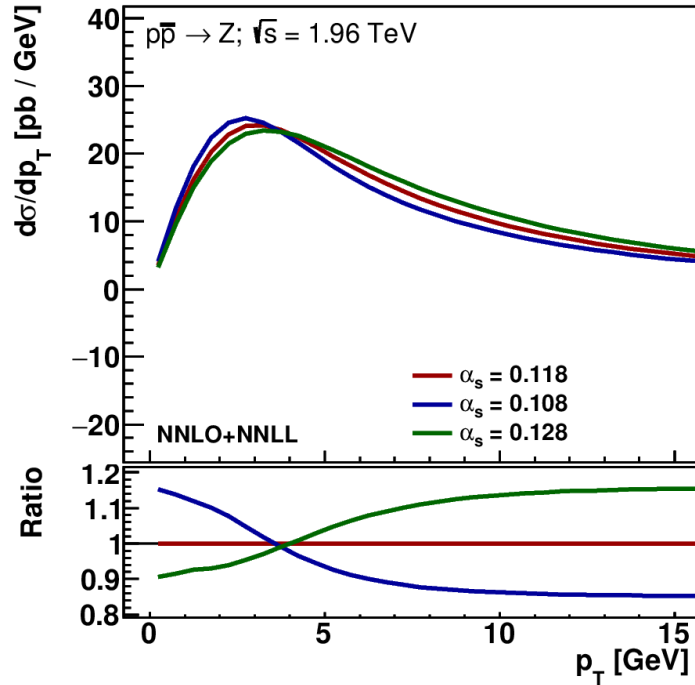
perturbative Sudakov form factor

Sensitivity to α_s

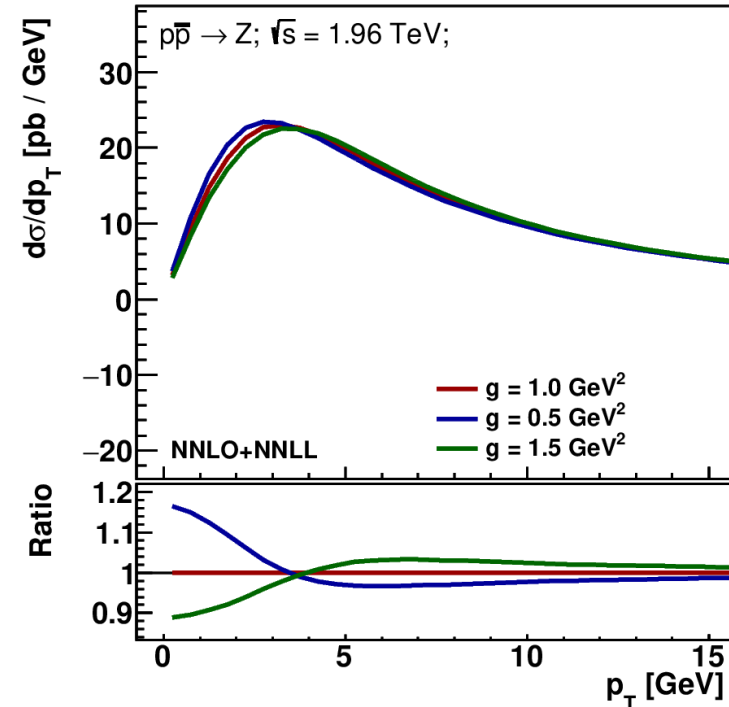
- N3LL accuracy in the Sudakov, N3LO accuracy in the hard coefficient H
- NNLO accuracy in the matching to fixed order at large p_T
→ missing $O(\alpha_s^3)$ terms have permille or subpermille effects in the region $p_T < 30$ GeV
- Consistent 4-loop running of α_s in all parts of the calculation
- PDFs evaluated at the hard scale and evolved with FFN 5F
- Non-perturbative effects modelled with a Gaussian Sudakov form factor governed by a parameter g



Sensitivity to $\alpha_s(m_Z)$



- The sensitivity of the Z-boson p_T distribution to $\alpha_s(m_Z)$ mainly comes from the position of the Sudakov peak
- Typical recoil scale:
 $\langle p_T \rangle \sim 10$ GeV



- The sensitivity of the Z-boson p_T distribution to the non-perturbative parameter g also comes from the position of the Sudakov peak
- The scale of the non-perturbative smearing is given by the primordial $\langle k_T \rangle$:
 $g \sim 0.6$ GeV² $\rightarrow \langle k_T \rangle \sim 1.5$ GeV

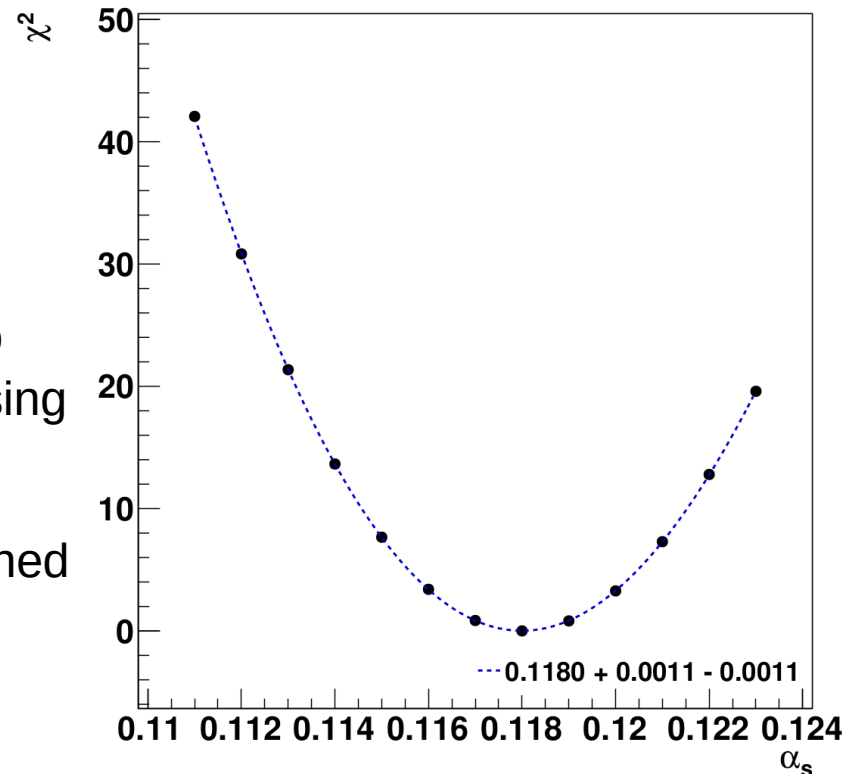
\rightarrow Possible to disentangle α_s , and g , thanks to their different scale

Methodology for the $\alpha_s(m_Z)$ determination

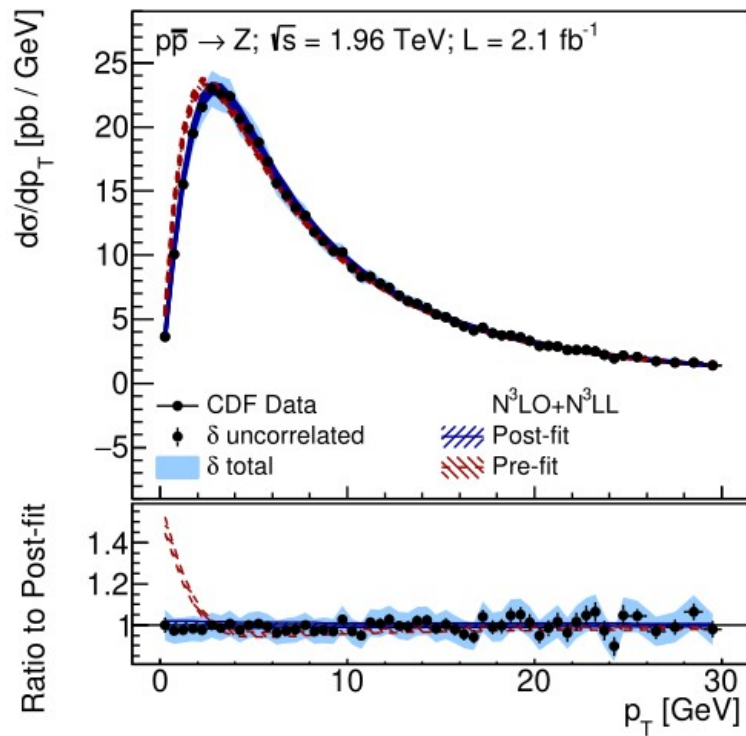
- DYTurbo interfaced to xFitter
- Evaluate $\chi^2(\alpha_s)$ with α_s variations as provided in LHAPDF
- Include experimental ($\beta_{j,\text{exp}}$) and PDF ($\beta_{k,\text{th}}$) uncertainties in the χ^2

$$\chi^2(\beta_{\text{exp}}, \beta_{\text{th}}) = \sum_{i=1}^{N_{\text{data}}} \frac{\left(\sigma_i^{\text{exp}} + \sum_j \Gamma_{ij}^{\text{exp}} \beta_{j,\text{exp}} - \sigma_i^{\text{th}} - \sum_k \Gamma_{ik}^{\text{th}} \beta_{k,\text{th}} \right)^2}{\Delta_i^2} + \sum_j \beta_{j,\text{exp}}^2 + \sum_k \beta_{k,\text{th}}^2$$

- At each value of $\alpha_s(m_Z)$ the $\beta_{k,\text{th}}$ terms explore the PDF space to find the best fit to the Z p_T data → equivalent to including the new dataset in the PDF without refitting, using profiling/reweighting [Eur.Phys.J.C 75 \(2015\) 9, 458](#)
- The non-perturbative form factor is added as unconstrained nuisance parameter ($\beta = 0$) i.e. left free in the fit
- Fit the region of Z $p_T < 30$ GeV



Fit results



Simultaneous fit of $\alpha_s(m_Z)$ and g

$$\alpha_s = 0.1187$$

$$\pm 0.0007 \text{ (exp. stat)}$$

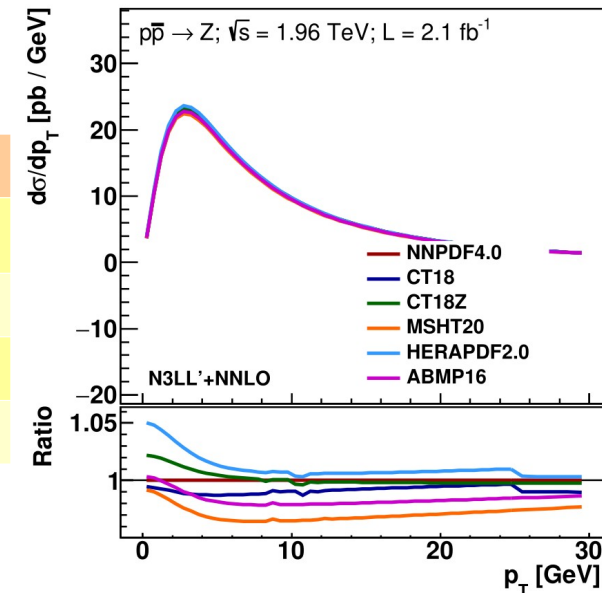
$$\pm 0.0002 \text{ (exp. syst)}$$

$$\pm 0.0004 \text{ (PDF)}$$

$$g = 0.66 \pm 0.05 \text{ (GeV}^2\text{)}$$

	NNPDF4.0	CT18	CT18Z	MSHT20	HERAPDF2.0	ABMP16
$\alpha_s(m_Z)$	0.1187	0.1186	0.1192	0.1178	0.1185	0.1178
PDF unc.	0.0004	0.0006	0.0005	0.0004	0.0004	0.0002
$g \text{ (GeV}^2\text{)}$	0.66	0.69	0.69	0.72	0.74	0.72
χ^2/dof	41/55	40/55	40/55	40/55	40/55	41/55

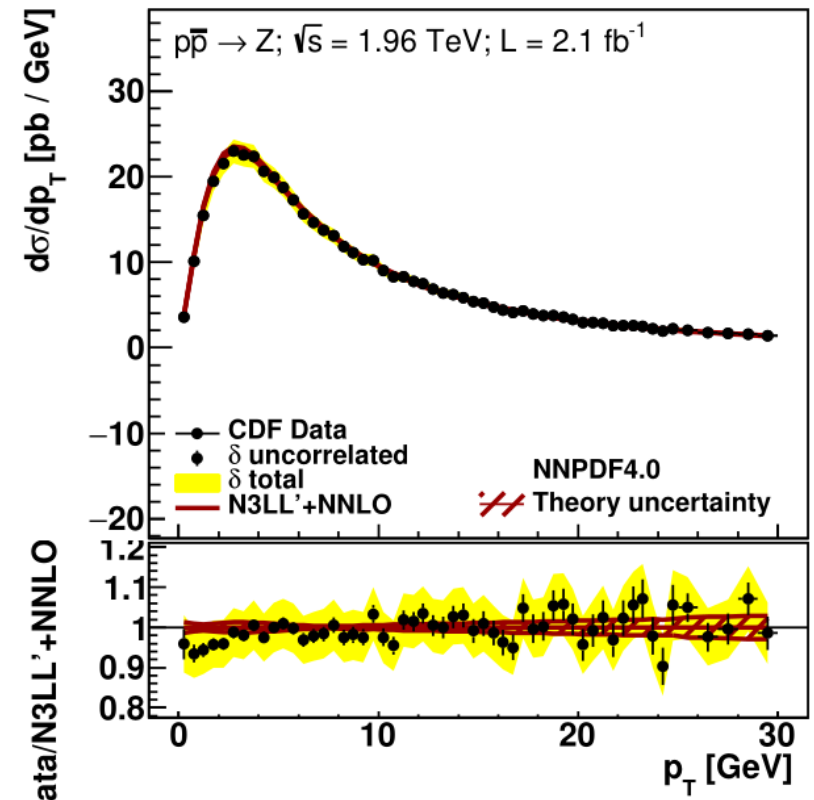
$$\alpha_s = 0.1185 \pm 0.0007 \text{ (PDF envelope)}$$



QCD scale variations

- Predictions depend on three QCD scales: renormalisation, factorisation, and resummation
- Uncertainty from the envelope of all possible combinations of $m_{\text{H}}/2 < \mu_{\text{R}}, \mu_{\text{F}}, \mu_{\text{RES}} < 2m_{\text{H}}$ with $0.5 < \mu_{\text{R}}/\mu_{\text{F}}, \mu_{\text{R}}/\mu_{\text{RES}}, \mu_{\text{F}}/\mu_{\text{RES}} < 2$

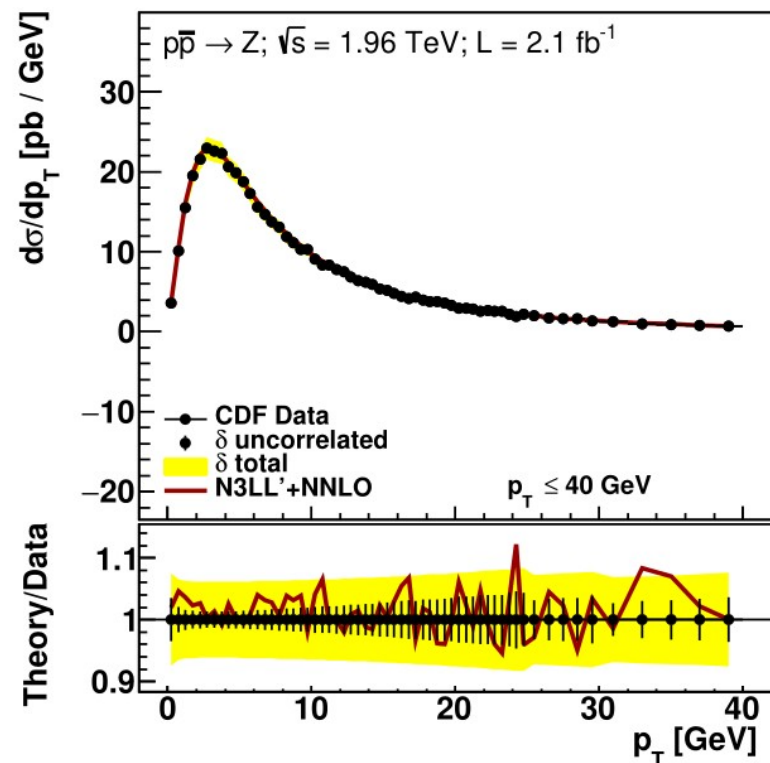
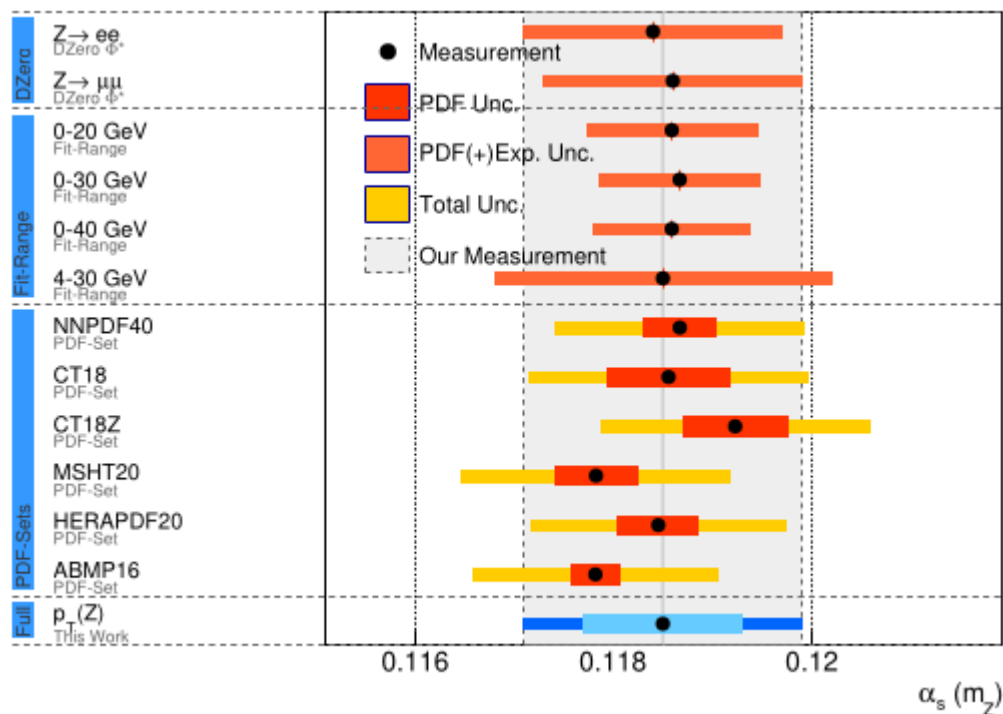
μ_{R}	μ_{F}	μ_{RES}	$\alpha_s(m_Z)$	$g(\text{GeV}^2)$	χ^2
1	1	1	0.1187	0.66	41.2
1	1	2	0.1178	0.81	39.1
1	1	0.5	0.1193	0.68	41.3
1	2	1	0.1189	0.66	40.2
1	2	2	0.1178	0.81	39.5
1	0.5	1	0.1187	0.66	41.4
1	0.5	0.5	0.1193	0.69	41.5
2	1	1	0.1190	0.67	41.3
2	1	2	0.1188	0.68	40.8
2	2	1	0.1189	0.67	41.1
2	2	2	0.1188	0.67	40.5
0.5	1	1	0.1177	0.80	40.3
0.5	1	0.5	0.1187	0.64	40.4
0.5	0.5	1	0.1177	0.79	40.0
0.5	0.5	0.5	0.1187	0.64	40.6



$$\delta\alpha_s = +0.0007 - 0.0010$$

$$\delta g = +0.15 - 0.02 \text{ (GeV}^2\text{)}$$

Fit range stability



- Remarkable stability with respect to variations of the fit range
- Confirms negligible effect of missing $O(\alpha_s^3)$ corrections in the matching to fixed order, and goodness of the NP model

	$p_T < 20$ GeV	$p_T < 30$ GeV	$p_T < 40$ GeV
$\alpha_s(m_Z)$	0.1186	0.1187	0.1186
fit unc.	0.0009	0.0008	0.0008
χ^2/dof	27/38	41/53	47/58

	$0 < p_T < 30$ GeV	$2 < p_T < 30$ GeV	$4 < p_T < 30$ GeV
$\alpha_s(m_Z)$	0.1187	0.1187	0.1185
fit unc.	0.0008	0.0008	0.0015
χ^2/dof	41/53	41/49	38/45

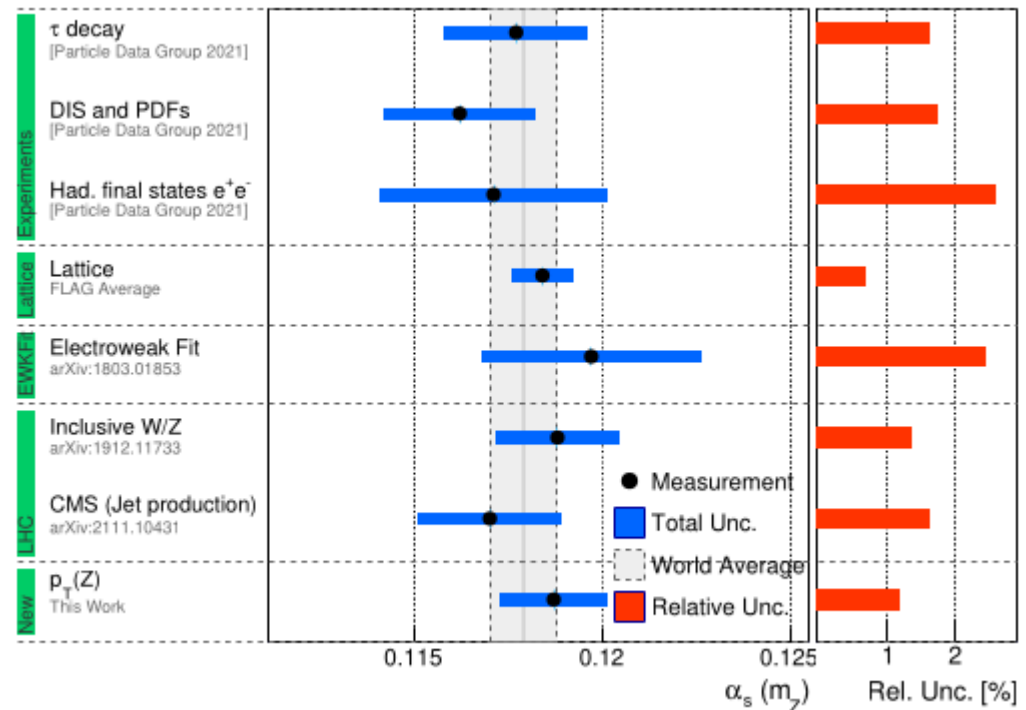
Result

$$\alpha_s = 0.1185 +0.0014 -0.0015$$

Breakdown of uncertainties

	$\delta\alpha_s(m_Z,+)$	$\delta\alpha_s(m_Z,-)$
Exp. unc.	+0.0007	-0.0007
PDF unc.	+0.0008	-0.0008
Scale var.	+0.0007	-0.0010
Theory unc.	+0.0007	-0.0004

- Measurement in agreement with the world average
- Uncertainty comparable to other determinations
- 1.2% rel. unc.: best collider measurement, second after lattice QCD average
- First N3LO $\alpha_s(m_Z)$ at hadron colliders



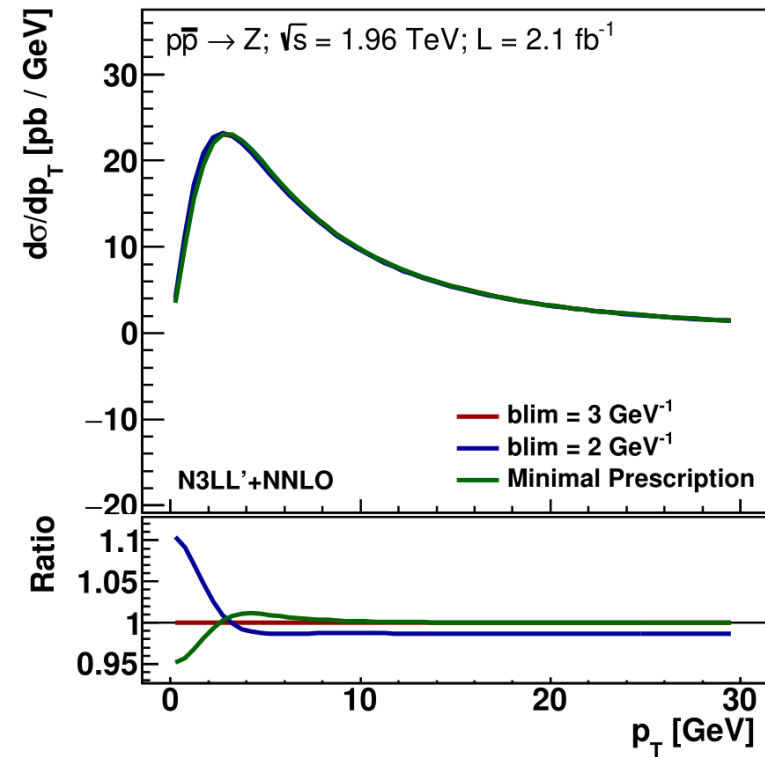
Summary

- DYTurbo interface is working, and was tested to determine α_s from Tevatron Z p_T
- Plan to add a few additional yaml settings
- Not yet tested the possibility to explicitly fit non perturbative parameters, but the functionality should be there (profiling was tested)
- Currently using the BLNY parametrisation, but in principle it should be possible to use arbitrary TMD functions in b space, controlled by xFitter
- Cross sections as functions of p_T, m, y without cuts on the leptons can be calculated relatively fast (~ 1 min). Fiducial cross sections are slower, and need a V+jet applgrid. With a sufficiently large number of cores it should be possible to test actual fits on a small number of datasets
- Lepton p_T and lepton η are possible, but currently rather slow, would need to optimise the phase space generation to make them fast

BACKUP

Theory uncertainties

- Alternative fits with $\text{blim} = 2$ and with the minimal prescription:
 $\delta\alpha_s = +0.0006 - 0.0004$
 $\delta g = +0.21 - 0.13$
- Alternative fit with VFN PDF evolution:
 $\delta\alpha_s = -0.0002$



QED ISR correction

- QED ISR estimated with Pythia 8, and applied as a multiplicative correction
- Correction to the Z-boson p_T at the level of 1%
- Effect on $\alpha_s(m_Z)$: $\Delta\alpha_s = -0.0006$
- Comparable to corrections obtained with QED qt-resummation

