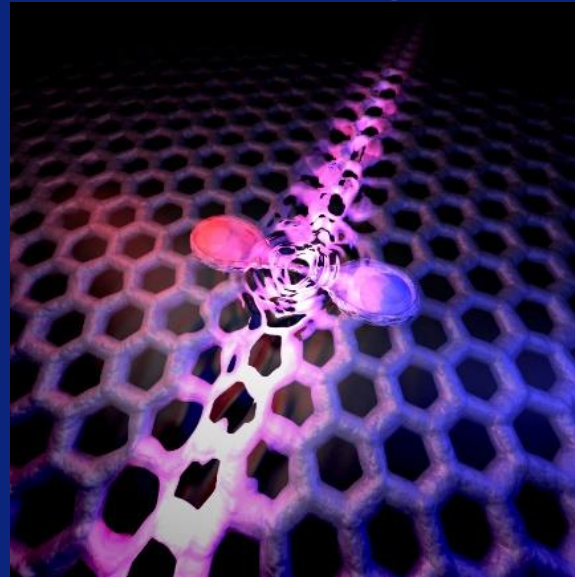
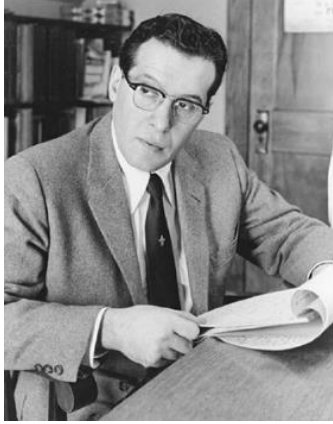


# Mesoscopic Klein-Schwinger effect in graphene



Aurélien Schmitt, P. Vallet, D. Mele, M. Rosticher, T. Taniguchi, K. Watanabe, E. Bocquillon, G. Fève, J.M. Berroir, C. Voisin, J. Cayssol, M.O. Goerbig, J. Troost, E. Baudin and B. Plaçais

# Schwinger effect: breaking vacuum in a high electric-field



F. Sauter, Z. Phys. 1931  
J. S. Schwinger, PRB 1951

- Instability of vacuum in presence of an intense electric field
- Electron-positron pair creation rate from non-perturbative theory

$$w(E) \propto \sum_{n \geq 1} \left(\frac{E}{n}\right)^{\frac{d+1}{2}} e^{-\pi \frac{n E_S}{E}}$$

d : spatial dimension  
E : electric field

- Schwinger field :  $E_S = \frac{\Delta_S^2}{e\hbar c} = \frac{m^2 c^3}{e\hbar} = 1.32 \cdot 10^{18} \frac{V}{m}$

(for electron-positron :  $\Delta_S = mc^2 = 511 \text{ keV}$  )

... on the roadmap of Zeta/Exawatt Lasers

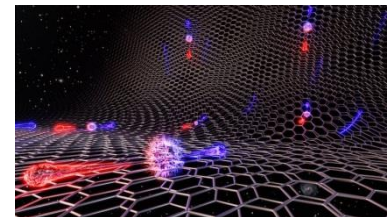
Prefactors in C. Itzykson et J. B. Zuber, Quantum Field Theory, McGraw-Hill (2006)



# 2d-Schwinger in gapless neutral 2d-graphene

$$E = v_F \hbar k$$

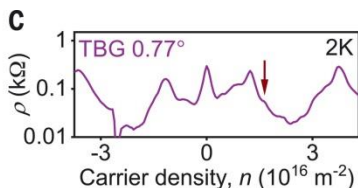
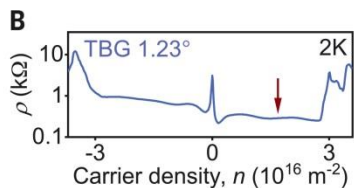
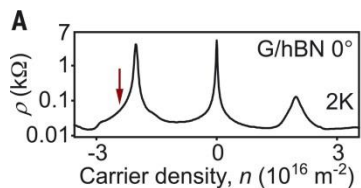
$c \rightarrow v_F$  and electron-hole symmetry



Dora-Moessner, PRB (2010),  
Katsnelson-Volovik, ZhETF (2012),...

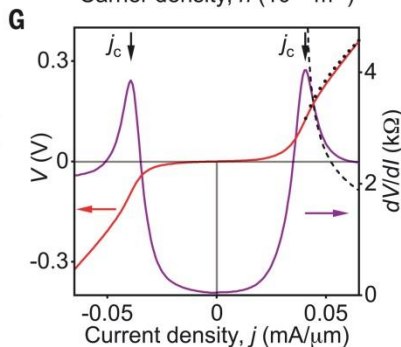
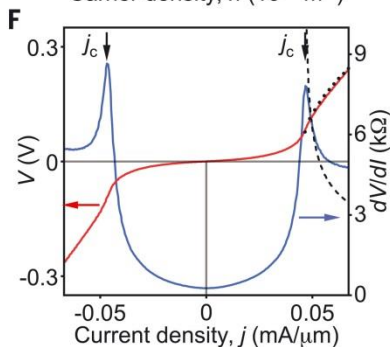
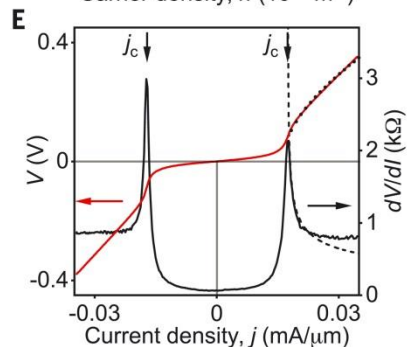
$$W_{2d} = \frac{eE}{2\pi^2 \hbar} \sqrt{\frac{eE}{v_F \hbar}} \sum_{n \geq 1} \frac{e^{-n\pi \frac{E_S}{E}}}{n^{3/2}} \propto E^{3/2}$$

$$E_S = 0$$



$$j \propto E^{3/2}$$

+ sign reversal of  
the Hall  
resistance



Berdyugin, Science (2022)

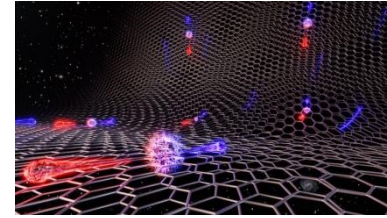
# 2d-Schwinger in gapless neutral 2d-graphene

$$E = v_F \hbar k$$

$c \rightarrow v_F$  and electron-hole symmetry

$$W_{2d} = \frac{eE}{2\pi^2 \hbar} \sqrt{\frac{eE}{v_F \hbar}} \sum_{n \geq 1} \frac{e^{-n\pi \frac{E_S}{E}}}{n^{3/2}} \propto E^{3/2}$$

$$E_S = 0$$



Dora-Moessner, PRB (2010),  
Katsnelson-Volovik, ZhETF (2012),...

**BUT**

- $E^{3/2}$  law is similar to Zener tunneling
- Electric-field induces doping-gradient, p-n junction, and 1d-collimation ....

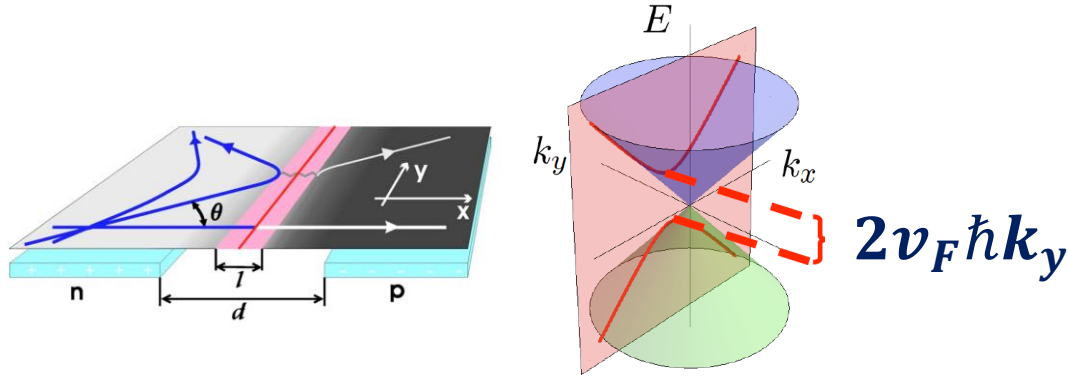
Vandecasteele et al., PRB (2010)

# **Klein-Schwinger effect**

# Klein collimation mimics massive 1d-Dirac fermions

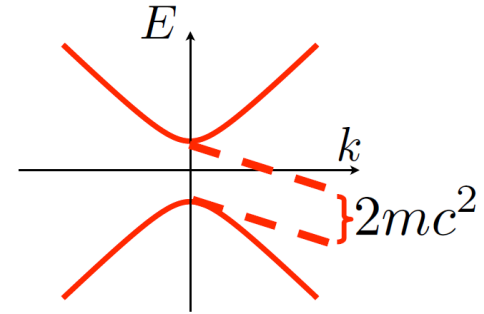
Collimating p-n junction

$$E = \mp \sqrt{(v_F \hbar k_y)^2 + (v_F \hbar k_x)^2}$$



massive Dirac fermions

$$E = \mp \sqrt{(mc^2)^2 + (c \hbar k)^2}$$



Long junction

$$T(k_y) = e^{-\pi \hbar v_F k_y^2 / e E_x}$$

V. V. Cheianov, V. I. Falko, PRB-2006

J. Cayssol, B. Huard, D. Goldhaber-Gordon, PRB-2009

E.B. Sonin, PRB-2009

P.E. Allain, J.N. Fuchs, EPJB-2011

$$T(k_C) = e^{-\pi \hbar c k_C^2 / e E_x}$$

F. Sauter, Z-Phys 1931

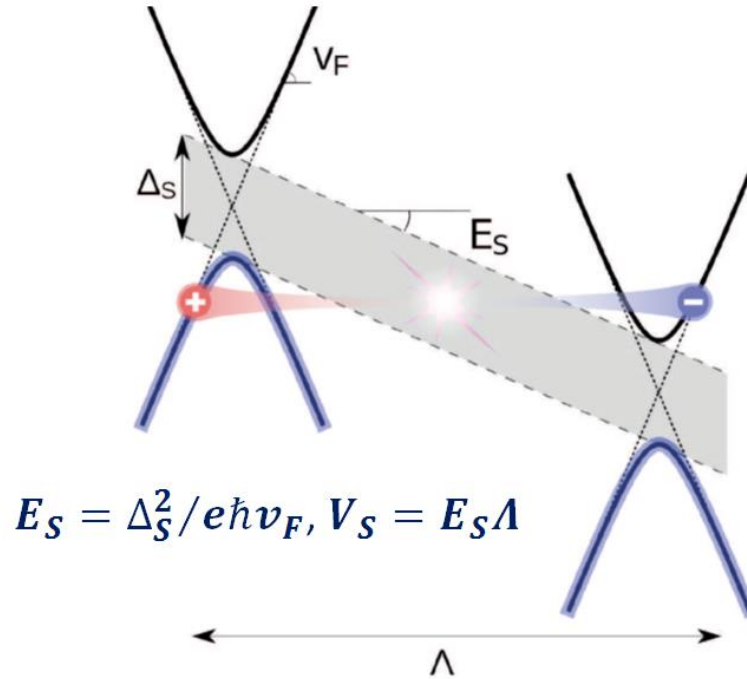
# Schwinger effect with massive 1d Dirac fermions in graphene

a universal 1d-Schwinger pair-creation rate

$$w_{1d} = \left(\frac{2e}{h}\right) E \sum_{n \geq 1} \frac{e^{-n\pi \frac{E_S}{E}}}{n}$$

$$E_S = \frac{\Delta_S^2}{e\hbar v_F} \sim 6 \cdot 10^7 \frac{V}{m}$$

for  $\Delta_S \sim \varepsilon_F \leq 0,2eV$



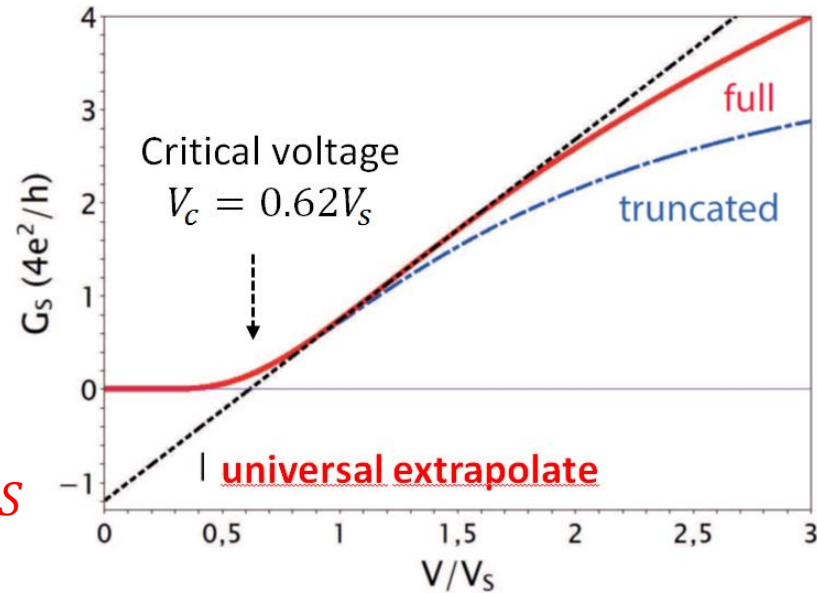
# Universal quantized 1d-Schwinger conductance

Schwinger current over a length  $\Lambda$  ( $g_s = g_v = 2$ )

$$I_{1d} = 2 \times g_s g_v \times \Lambda \times w_{1d} = 2 g_s g_v \left( \frac{2e^2}{h} \right) V \text{Ln} \left( \frac{1}{1 - e^{-\pi V_S/V}} \right) \quad V_S = E_S \times \Lambda$$

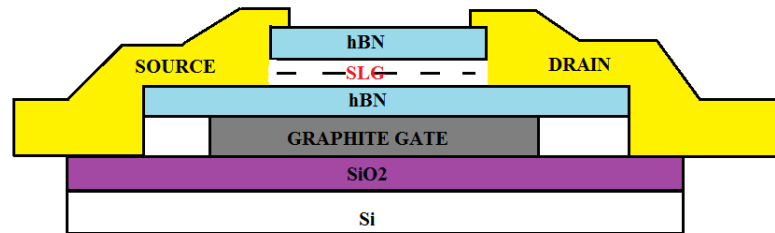
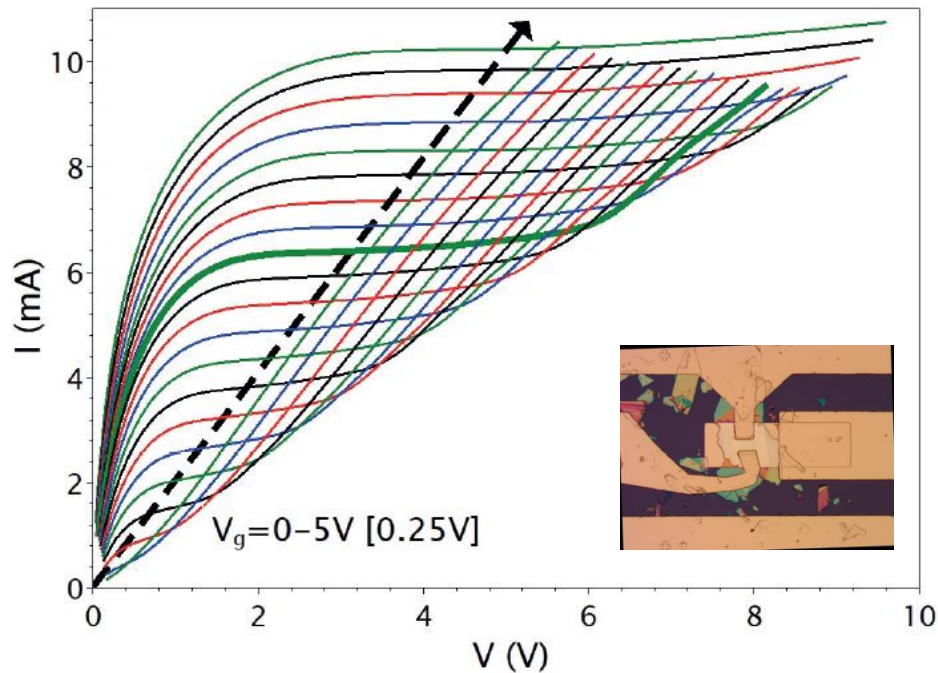
$$G_S = 4 \left[ \text{Ln} \left( \frac{1}{1 - e^{-\pi V_S/V}} \right) + \frac{\pi V_S}{V} \frac{1}{e^{\pi V_S/V} - 1} \right] \times 4e^2/h \approx 2 \times 0.60 \left[ \frac{V}{V_S} - 1 \right] \times 4e^2/h$$

$$G_0 = -0.186 mS$$

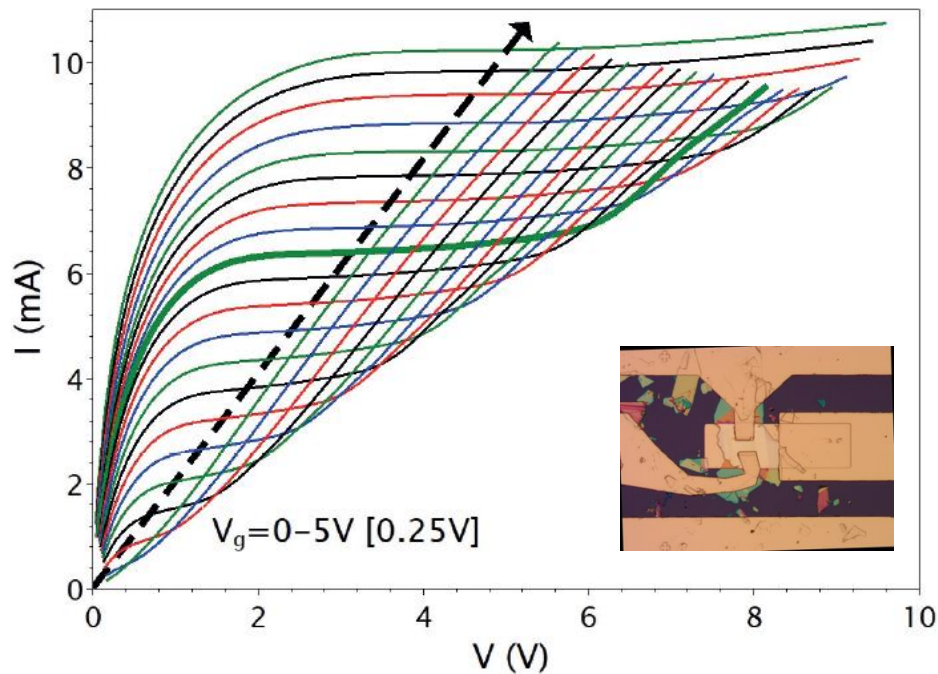




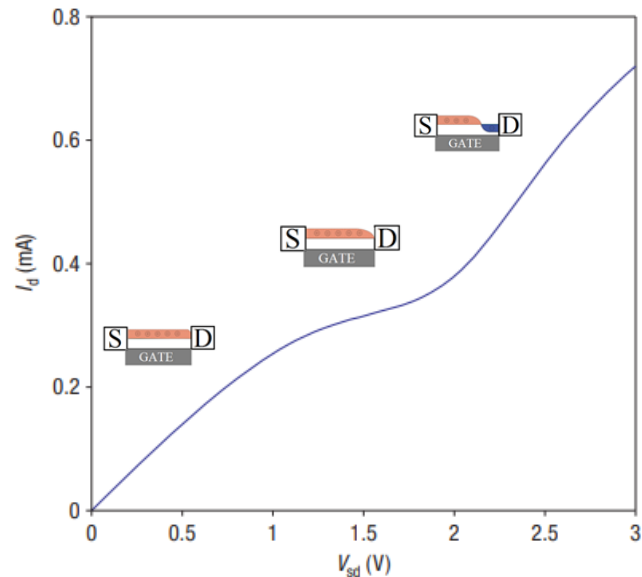
# Current saturation in hBN-encapsulated graphene FET



# Current saturation in hBN-encapsulated graphene FET

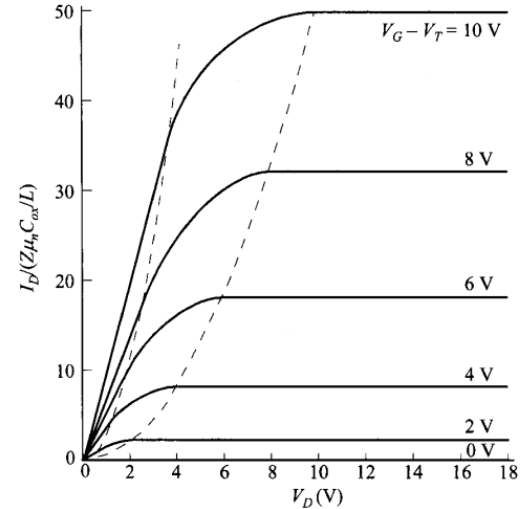
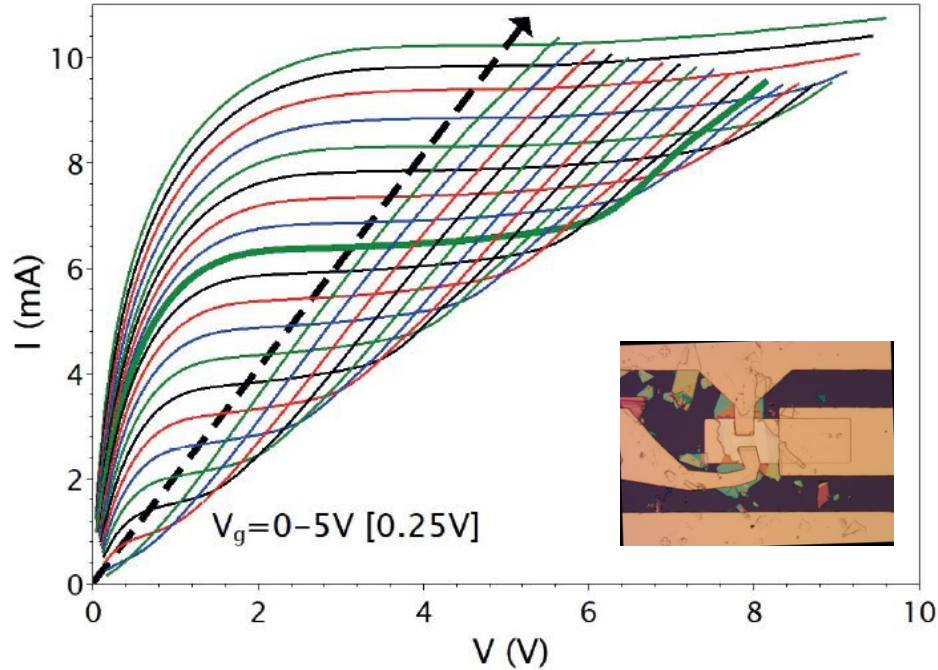


Diffusive graphene



Meric et al. *Nature Nanotechnology* 3, 654–659 (2008)

# Current saturation in hBN-encapsulated graphene FET

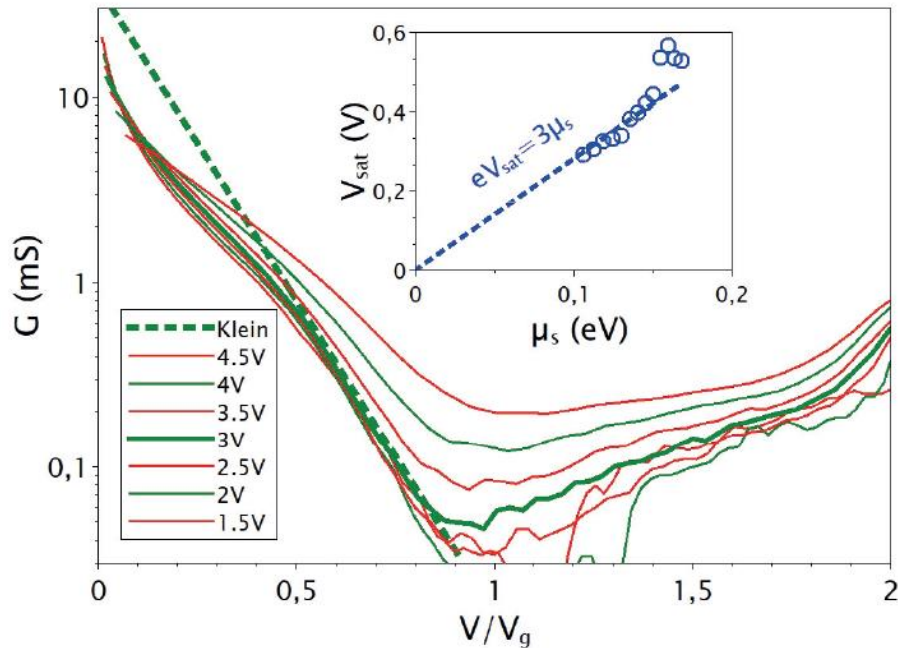
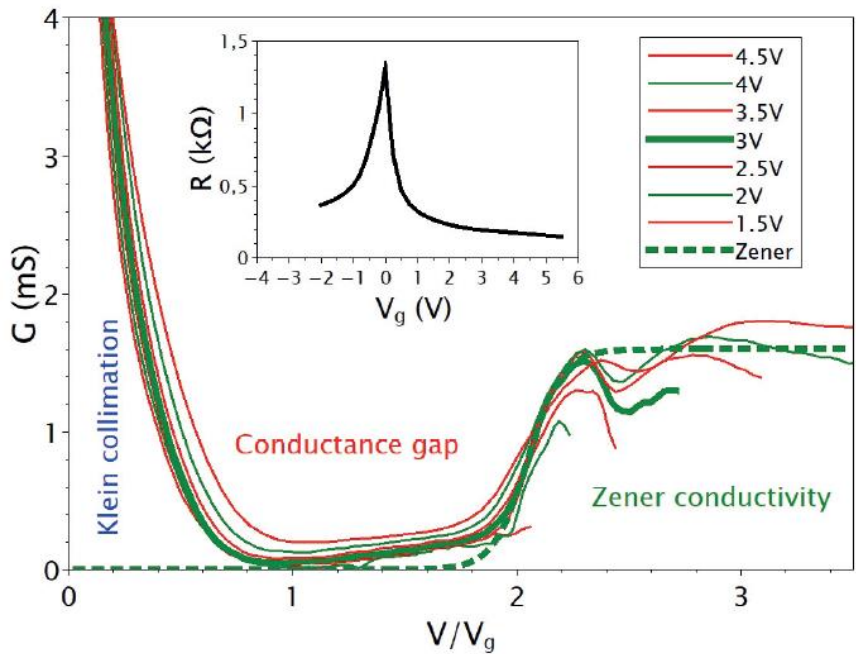


Si MOSFET (Sze, 2006)

reminiscent of MOSFET pinchoff (carrier depletion at the drain side), albeit semimetallic

**From current to differential conductance**

# Vanishing Klein-tunneling conductance $G_K \approx G(0)e^{-V/V_{sat}}$



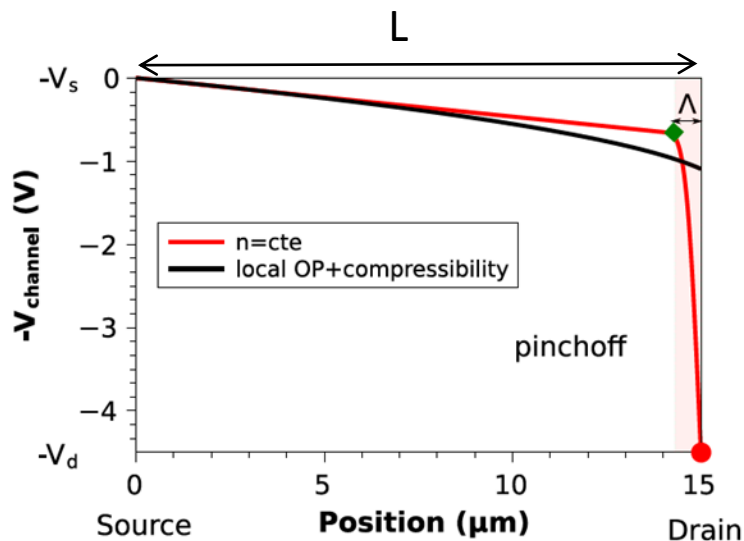
Giant Klein collimation model :

$$T(V) \propto e^{-\pi \frac{eV\Lambda}{\hbar v_F} \sin^2 \theta_{sat}} = e^{-V/V_{sat}}$$

# Toy-model of the Klein-collimation junction

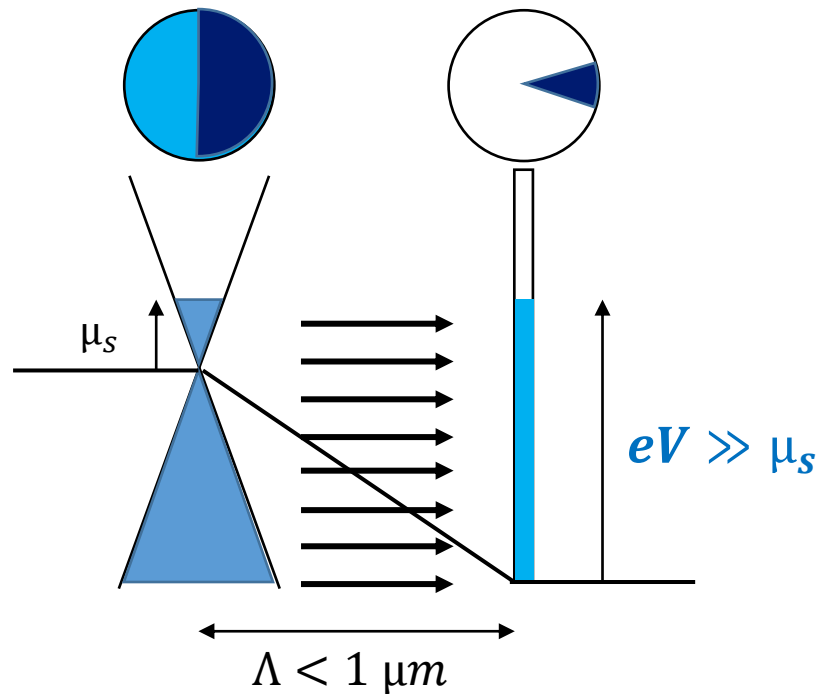
## Semi-metallic Pinchoff

$$E_x = V/\Lambda$$



## Long-junction model

$$T \propto e^{-\pi \hbar v_F k_y^2 / e E_x}$$

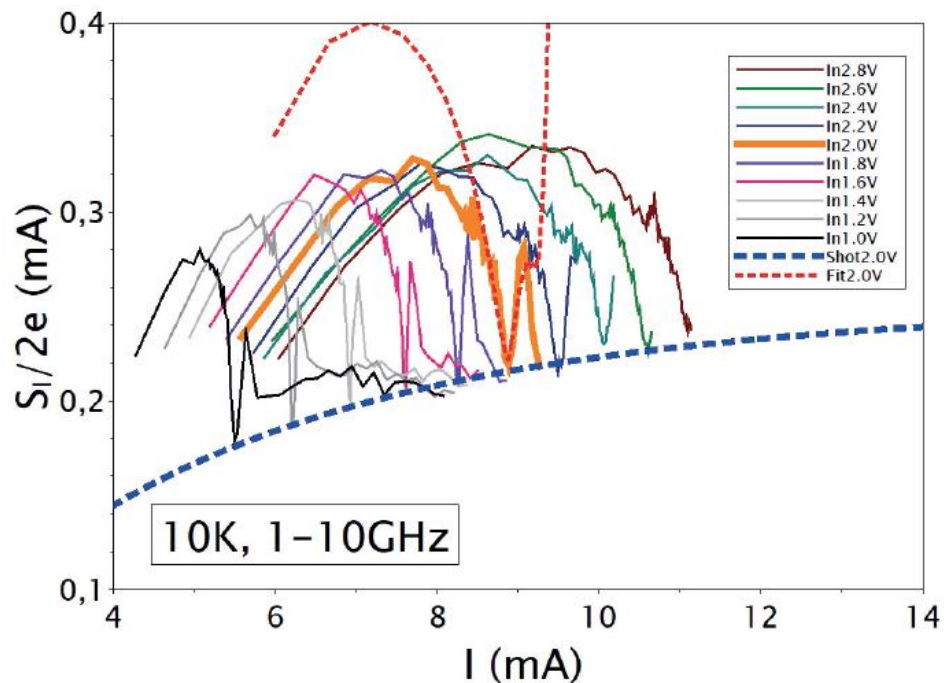


**noise signatures of Klein collimation**

# Klein tunneling junction : shot-noise

## White GHz noise

$$S_I = 4Gk_B T_e + 2eIF$$





# Klein tunneling junction : shot-noise

## White GHz noise

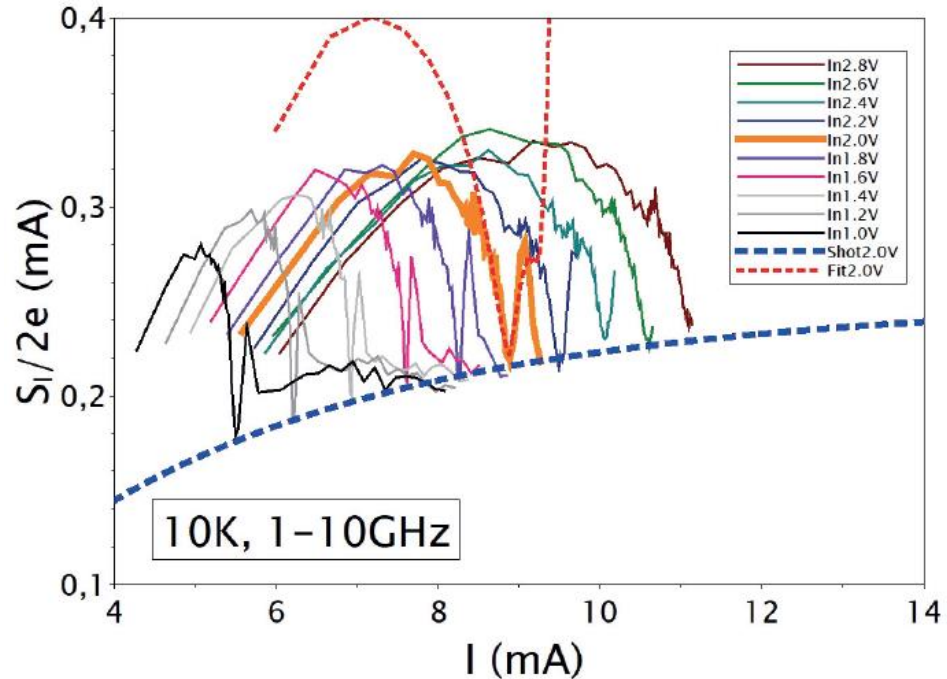
$$S_I = 4Gk_B T_e + 2eIF$$

## Sweet noise dip

$$G \rightarrow 0, S_{th.} \rightarrow 0$$

## Shot-noise limited

$$S_I(V_{dip}) \approx 2eIF$$



# Klein tunneling junction : shot-noise

## White GHz noise

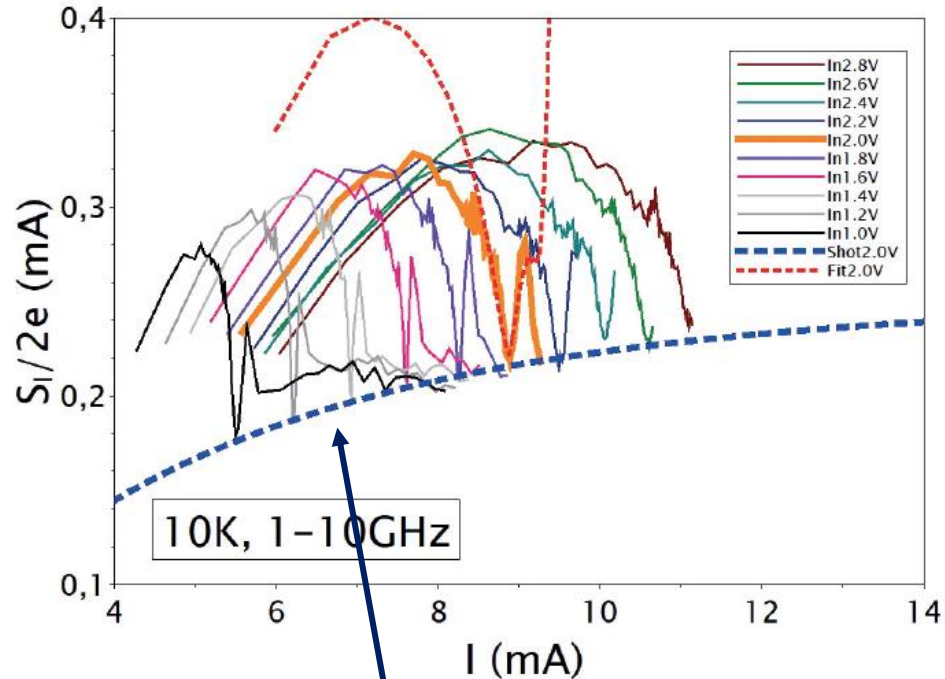
$$S_I = 4Gk_B T_e + 2eIF$$

## Sweet noise dip

$$G \rightarrow 0, S_{th.} \rightarrow 0$$

## Shot-noise limited

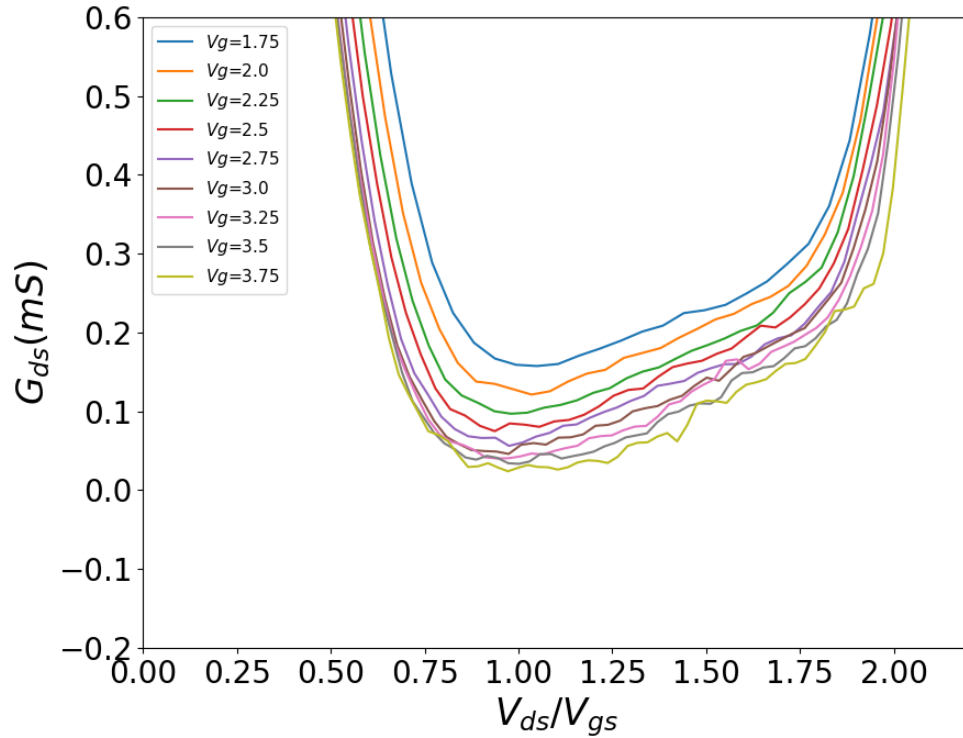
$$S_I(V_{dip}) \approx 2eIF$$



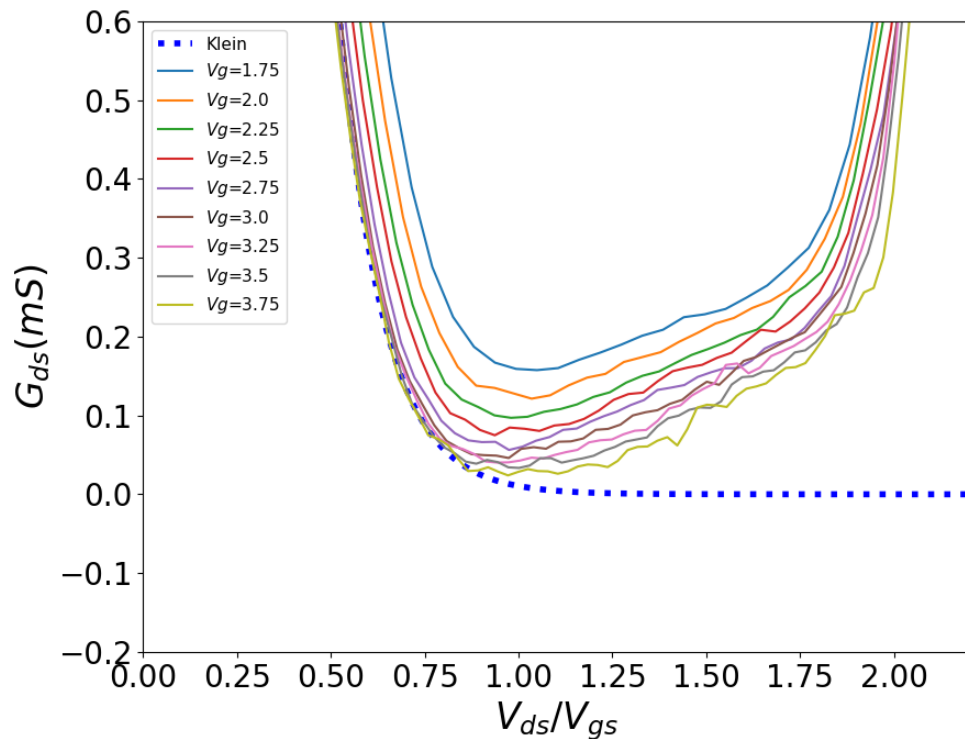
Mesoscopic junction with a Fano factor  $F \leq 0.04$

# Universal 1d Schwinger effect

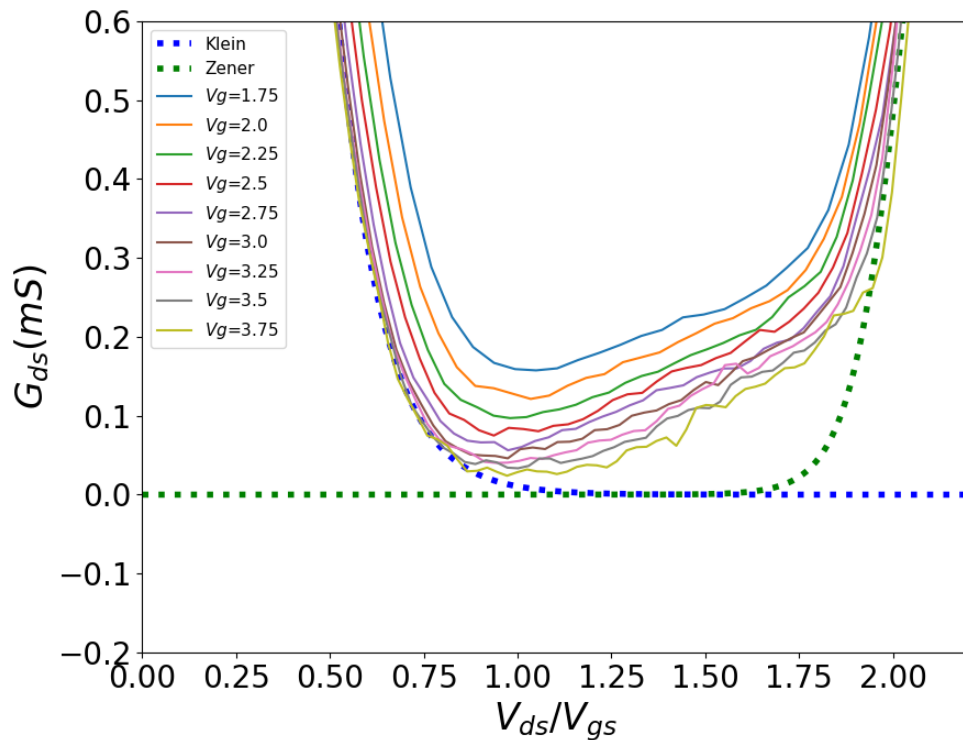
# Evidence of mesoscopic Klein-Schwinger effect



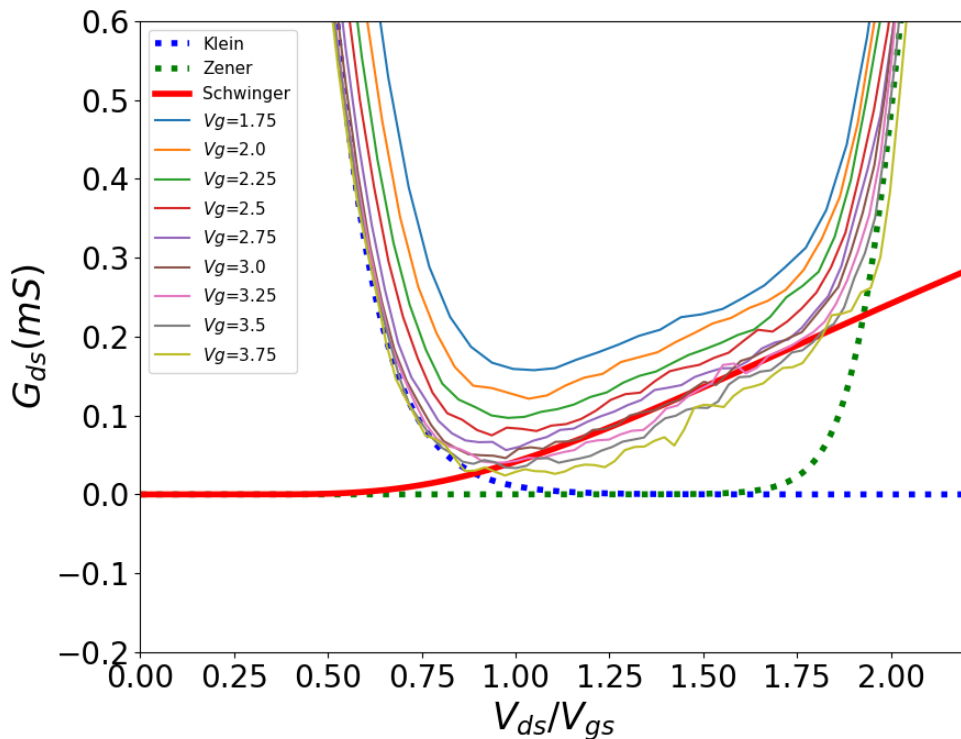
# Evidence of mesoscopic Klein-Schwinger effect



# Evidence of mesoscopic Klein-Schwinger effect



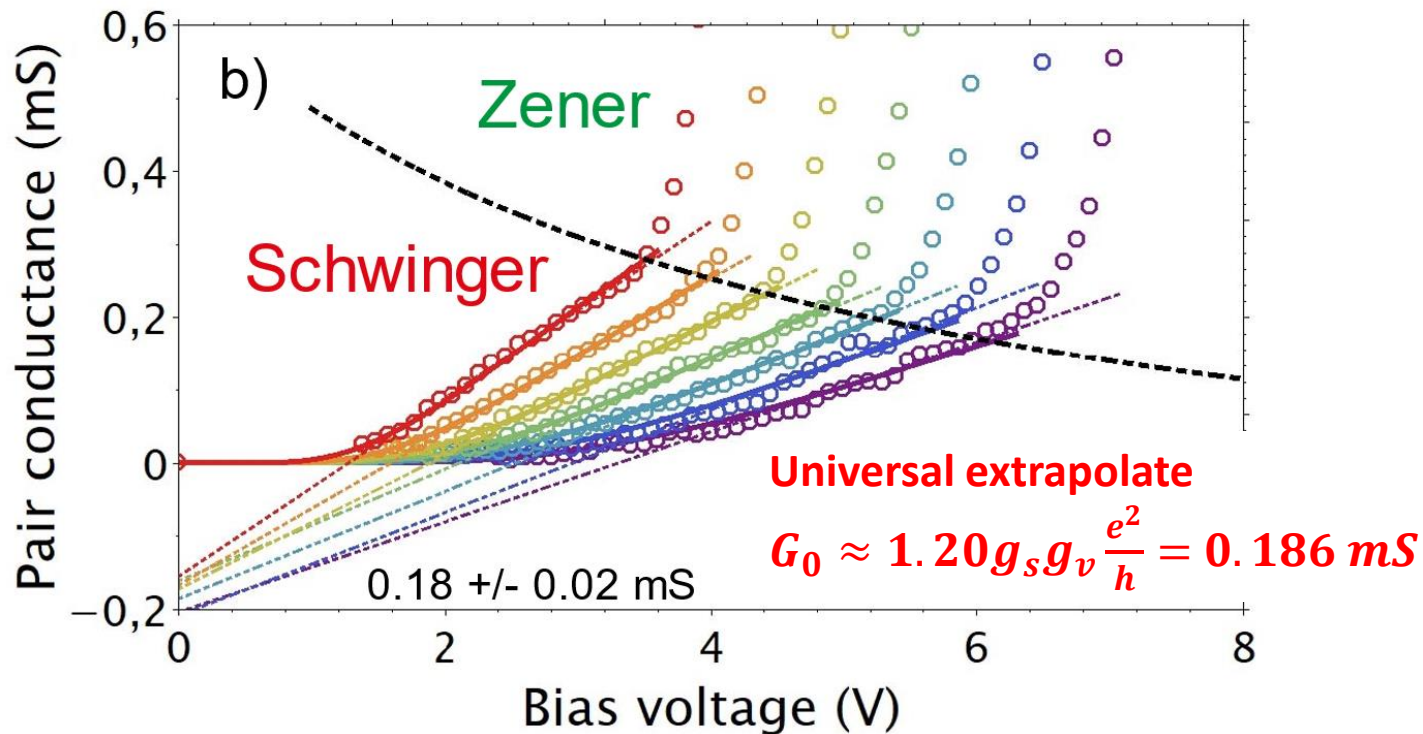
# Evidence of mesoscopic Klein-Schwinger effect



$$G \approx G_S(V)$$

$$16 \left[ \text{Ln} \left( \frac{1}{1 - e^{-\pi V_S/V}} \right) + \frac{\pi V_S/V}{e^{\pi V_S/V} - 1} \right] \frac{e^2}{h}$$

# Universal 1d-Schwinger scaling: $G_S(V) = G - G(0)e^{-V/V_{sat}}$

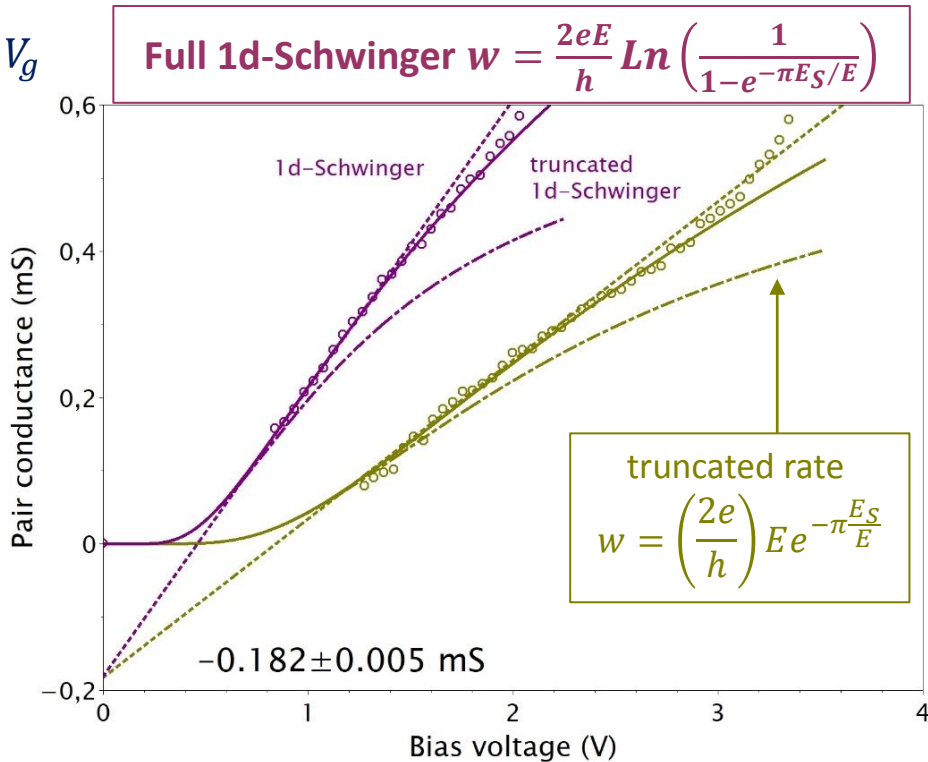
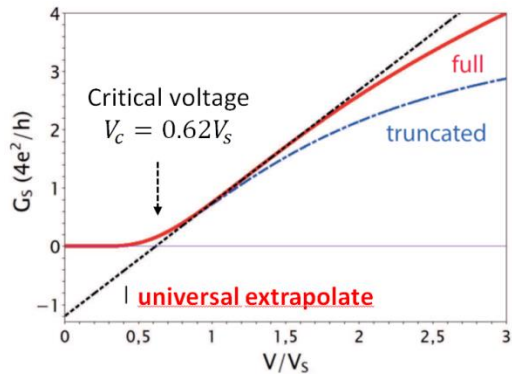


One parameter : Schwinger voltage  $V_S$



# The N-loop Schwinger prediction verified in detail

A device with a thin hBN dielectric (32nm) :  
 early onset of Schwinger pair creation  $V_S \leq 0.5 V_g$

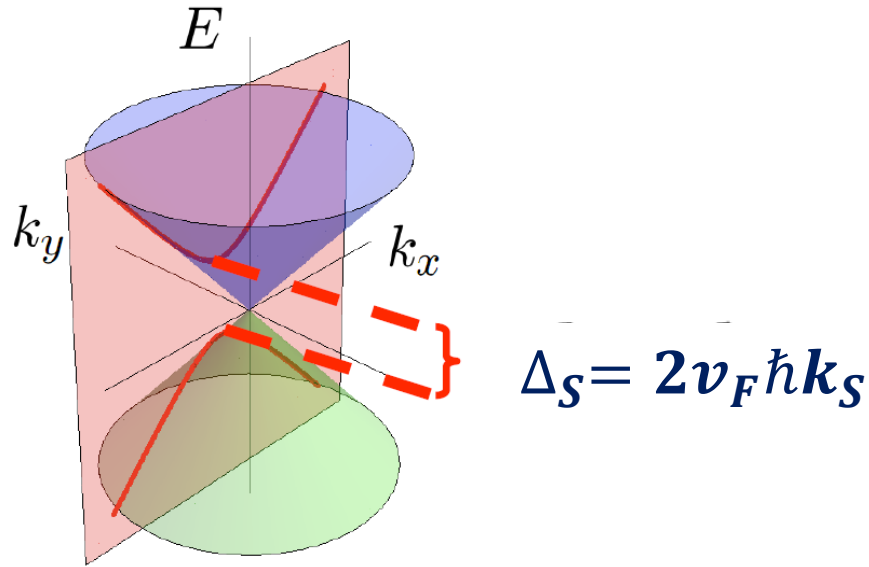


an important result for field theory

# Schwinger gap and length

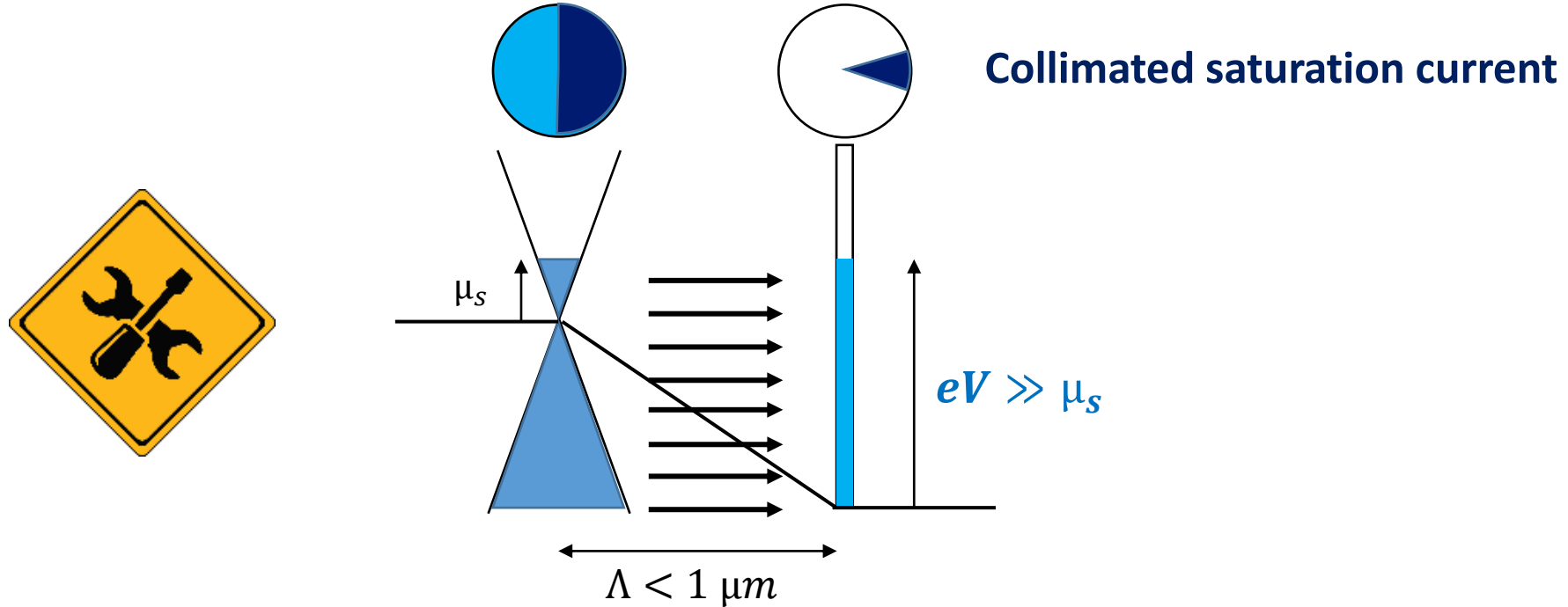
# Klein-collimation origin of the Schwinger gap

$$E = \mp \sqrt{(v_F \hbar k_y)^2 + (v_F \hbar k_x)^2}$$



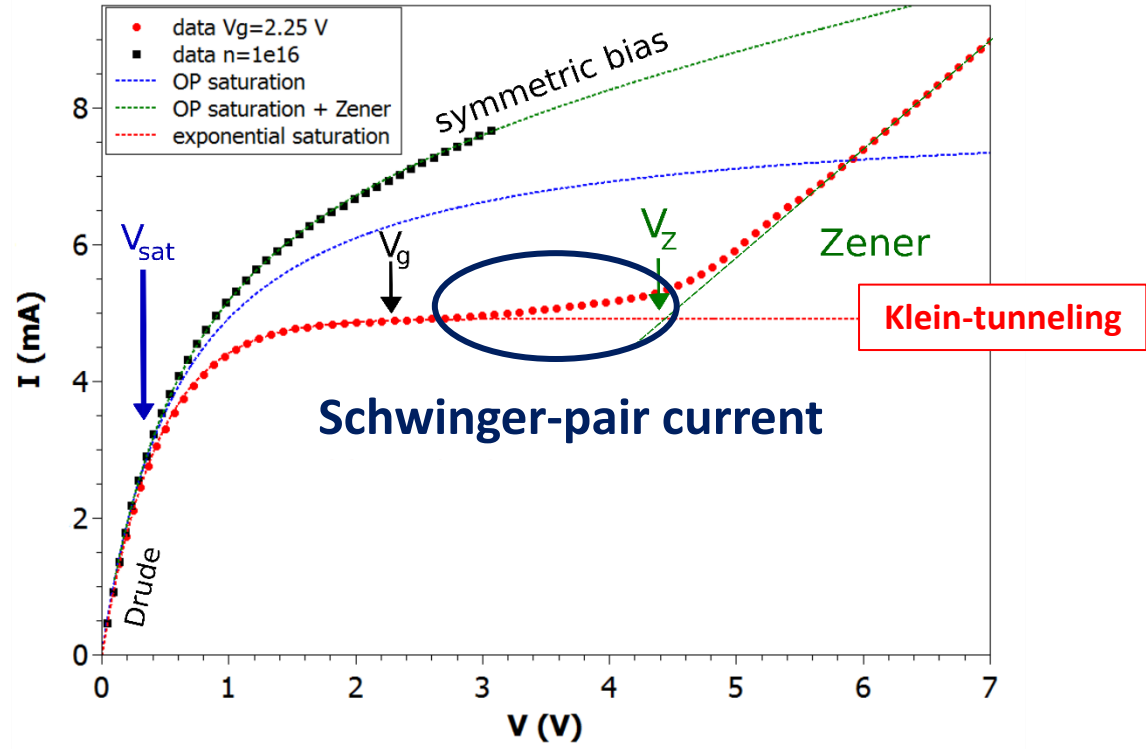
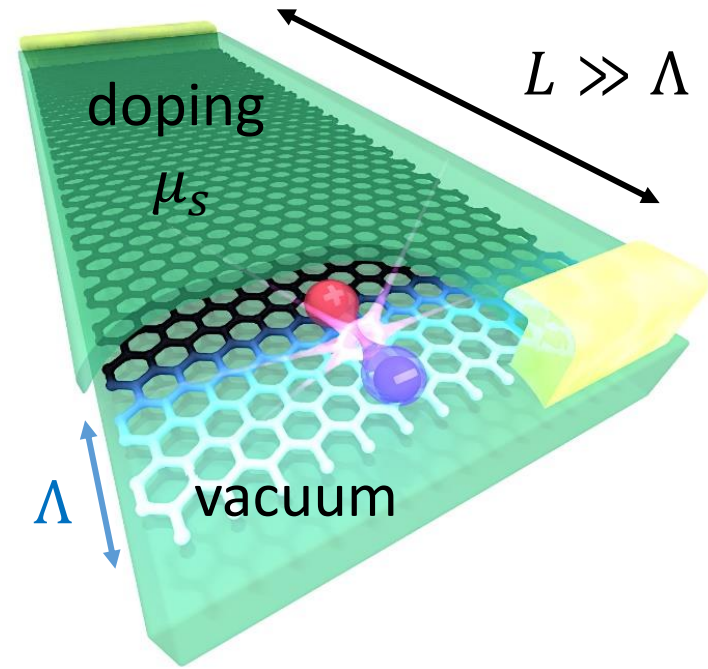
**Why finite- $k_S$  Schwinger pairs ?**

# Pauli-blocking of low- $k_y$ by collimated transmitted carriers



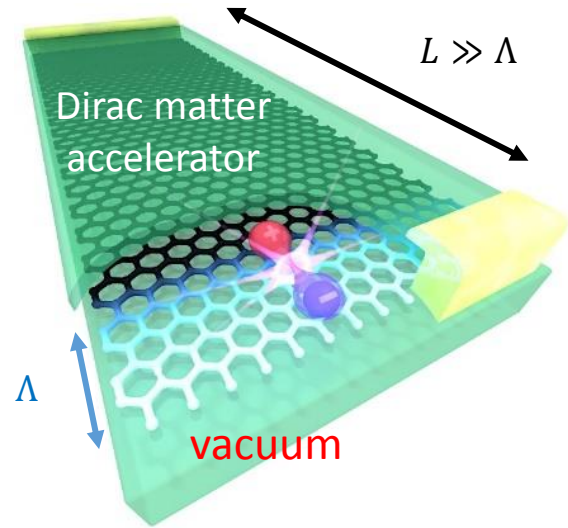
Ansatz: Schwinger-pairs created at a finite  $k_y$  with  $\Delta_S \sim \mu_s$

# Schwinger as the intrinsic breakdown of Klein collimation



# « QED in a pencil trace » → « QED in a graphene mosfet »

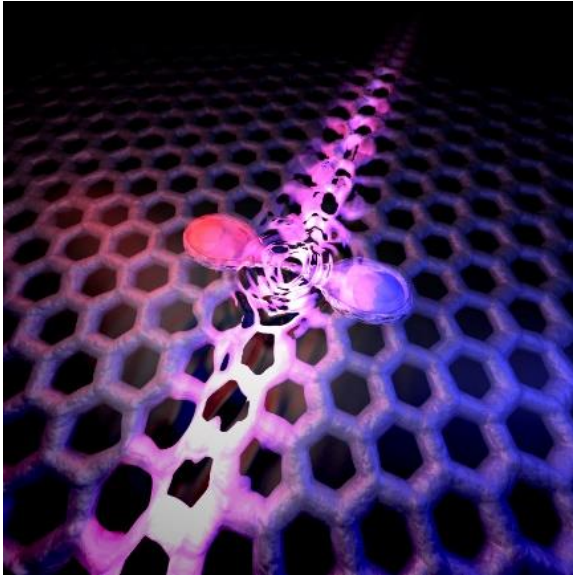
- ✓ Experimental observation of 1d-Schwinger effect
- ✓ Schwinger is the breakdown of Klein collimation
- ✓ Outlook: lifting spin/valley degeneracy ?
- ✓ Outlook: Full counting statistics ? Vacuum polarization ?  $\Lambda$



A. Schmitt et al., Nat. Phys. **19**, 830–835 (2023)

N&V R.K. Kumar **19**, 768–769 (2023)

« *QED in a pencil trace* » → « *QED in a graphene mosfet* »

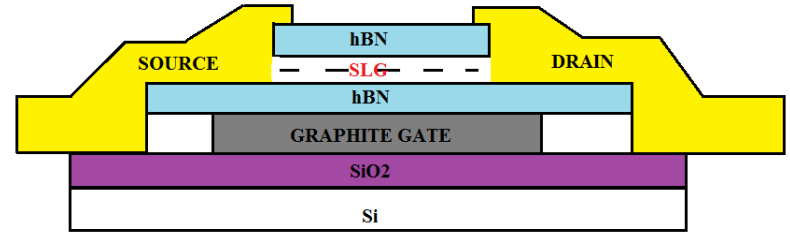
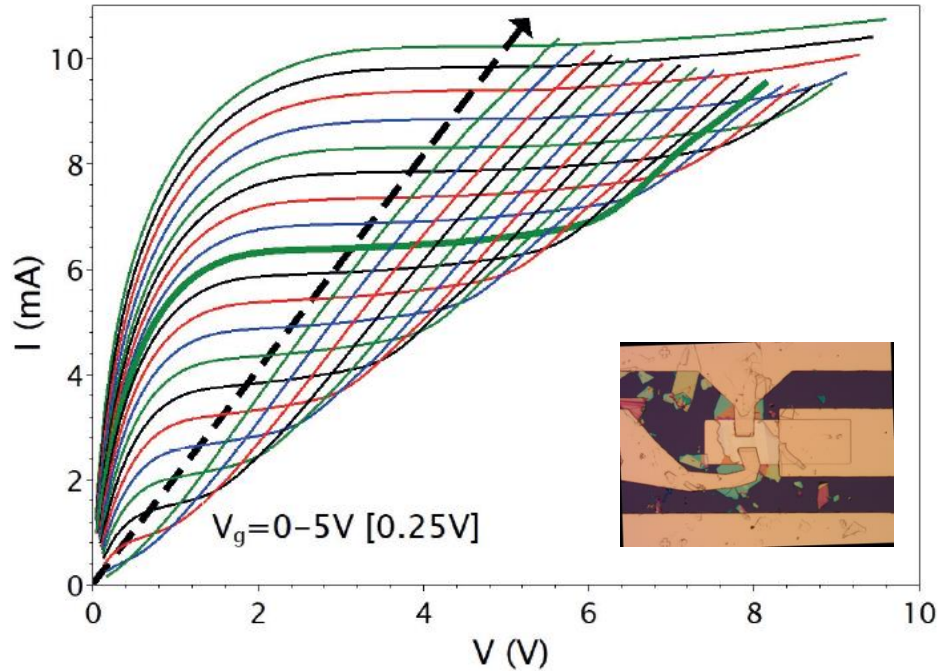


**Thank you !**

A. Schmitt et al., Nat. Phys. **19**, 830–835 (2023)

N&V R.K. Kumar **19**, 768–769 (2023)

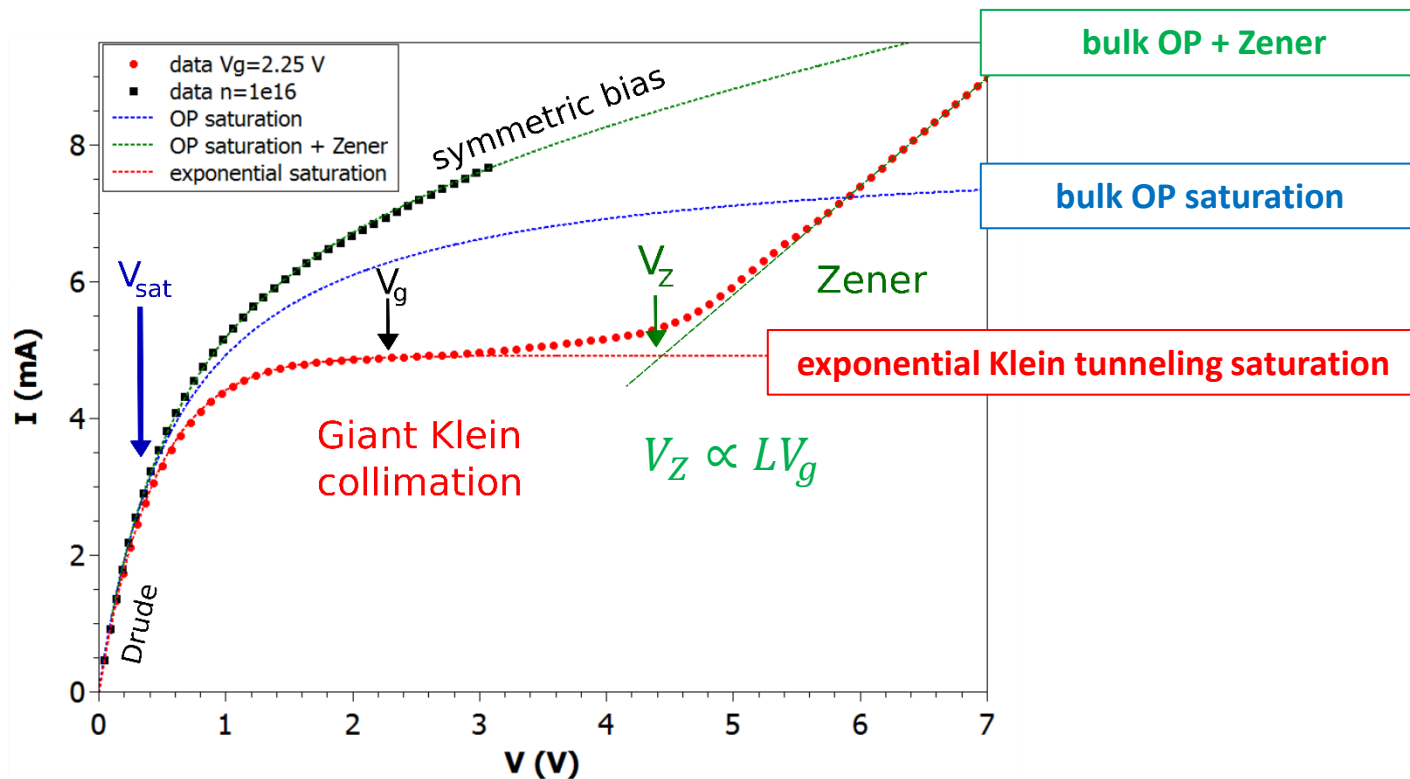
# Current saturation in hBN-encapsulated graphene FET



- Long devices  $L \sim W \geq 10 \mu m$
- High-mobility  $> 100\,000 \text{ cm}^2/Vs$
- Low edge contact resistance
- Room temperature

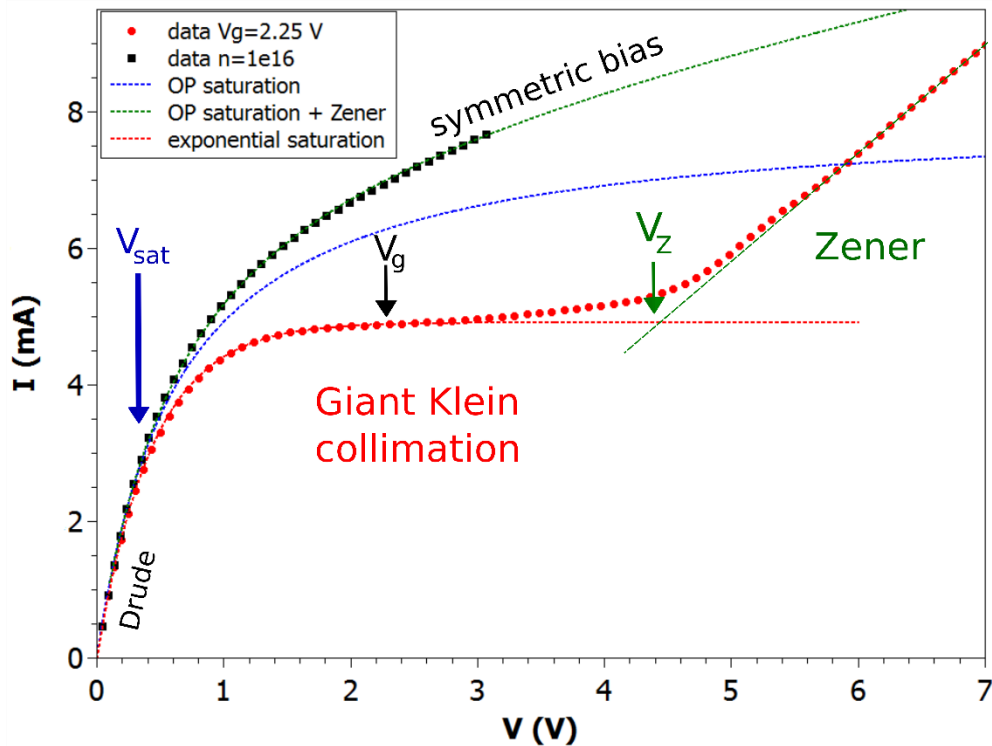


# Saturation controlled by a « Klein collimation junction »



Exponential saturation is extrinsically limited by a **Zener instability**

# Saturation controlled by a « Klein collimation junction »



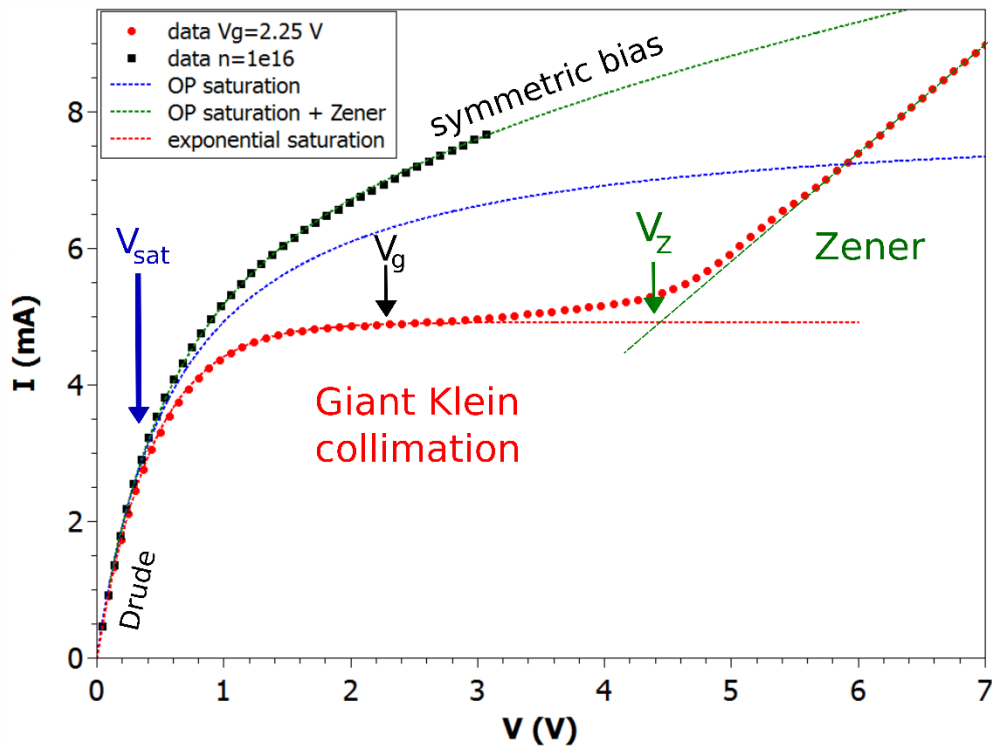
Pinch-off free regime

$$V_g(V) = V_g(0) + aV$$

Bulk current saturation controlled by optical phonons:

$$I = n_s e \left[ \frac{\mu}{1+V/V_{OP}} + \sigma_Z \right] \frac{W}{L} V$$

# Saturation controlled by a « Klein collimation junction »



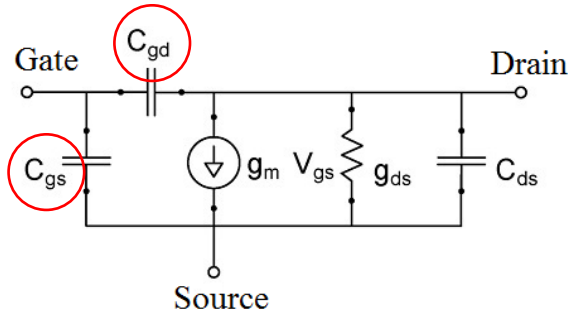
Pinch-off regime  $V_g = Cst.$

Exponential current saturation :

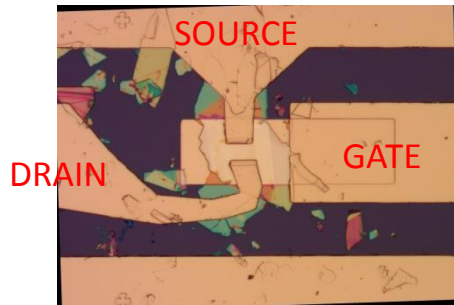
$$I(V) = I_{sat} \left(1 - e^{-\frac{V}{V_{sat}}}\right)$$

# Pinchoff regime : RF measurements

Small-signal equivalent circuit

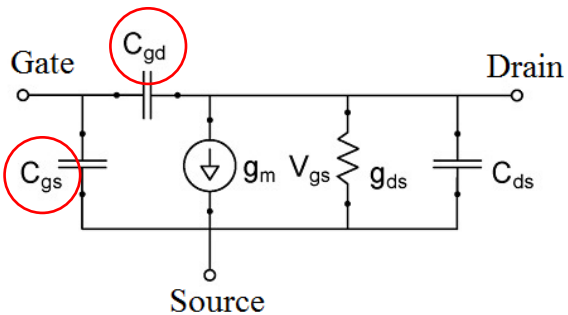


(cf Sze, 2006)

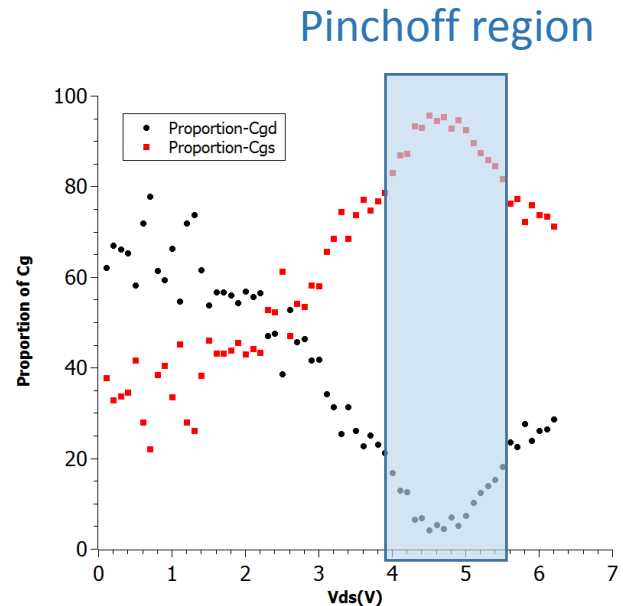
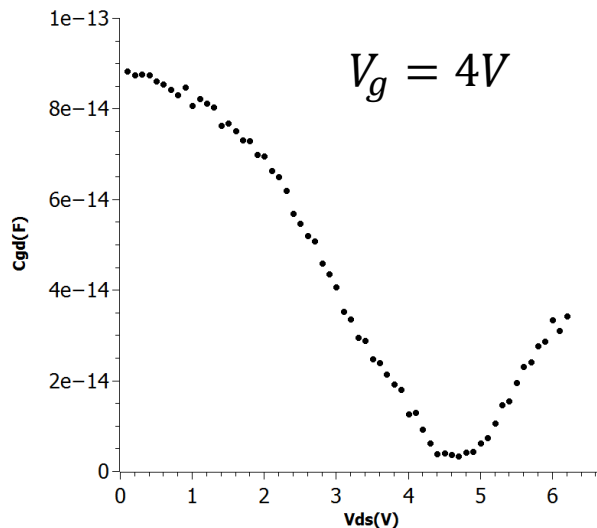
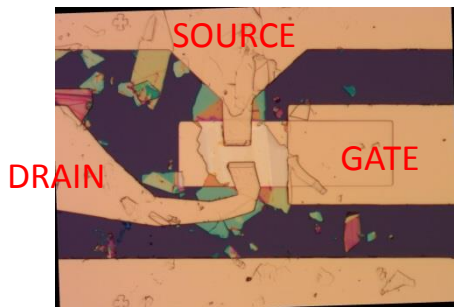


# Pinchoff regime : RF measurements

Small-signal equivalent circuit



(cf Sze, 2006)



# Toy-model of the Klein-collimation junction

Pinchoff-free case : velocity saturation (OPs) + electronic compressibility + **doping gradients** in the presence of a local gate

Current density :  $J = \mu(E)n \partial_x \mu_c^*$

$\mu(0)$  : low-bias mobility

$E_{OP}$  : saturation field

where  $\mu(E) = \mu(0) / (1 + \frac{|E|}{E_{OP}})$

$$\mu_c^* = \mu_c(x) - e V_c(x) \quad (\text{electrochemical potential})$$

For monolayer graphene on a local gate :

$$\mu_c^* - \mu_g^* = \hbar v_F \sqrt{\pi n} + \frac{e^2}{C_g} n$$

$v_F$  : Fermi velocity

$C_g$  : areal gate capacitance

$n(x)$  : carrier density

$\mu_g^*$  : electrochemical potential of the gate

+ electrostatics :  $V_c(x) - V_g = \frac{-e}{C_g} n(x)$

# Toy-model of the Klein-collimation junction

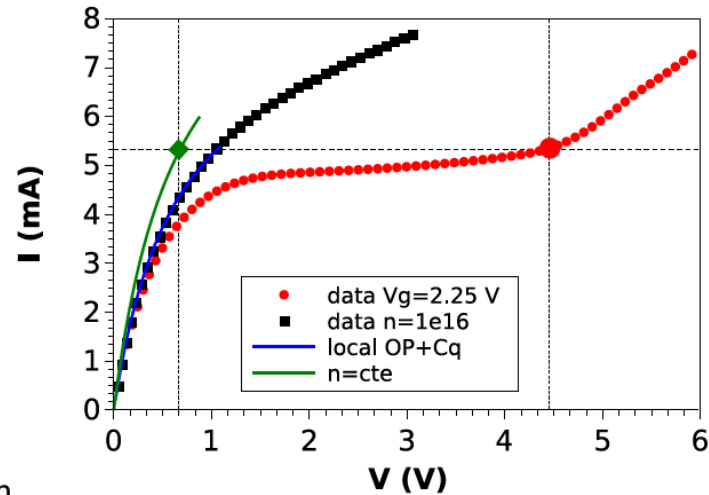
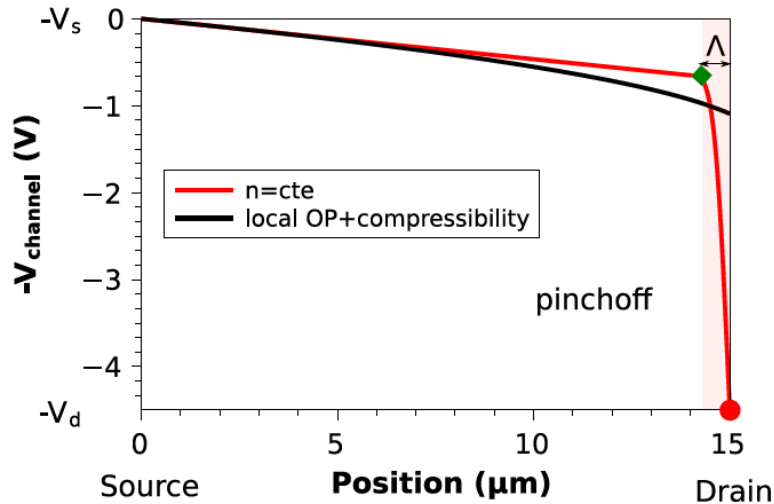
Pinchoff-free case : velocity saturation (OPs) + electronic compressibility + **doping gradients** in the presence of a local gate

Pinchoff case : constant density in the channel  $\rightarrow$  constant  $\mu_c^*$  and uniform  $E$

$$J = - \frac{\mu(0)}{1 + \frac{|\partial_x V_c|}{E_{OP}}} n \partial_x V_c$$

# Toy-model of the semi-metallic pinchoff

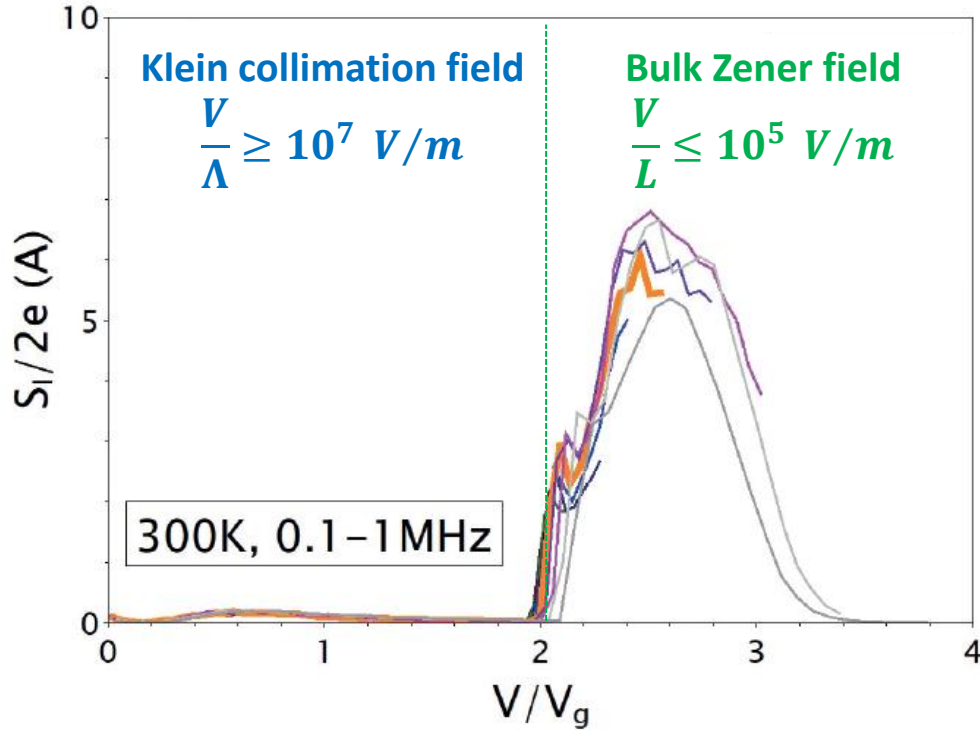
**Local drift-diffusion model** : velocity saturation + electronic compressibility + doping gradients with a local gate



Estimate of the voltage drop in the channel / in the pinchoff junction



# Zener instability : flicker-noise

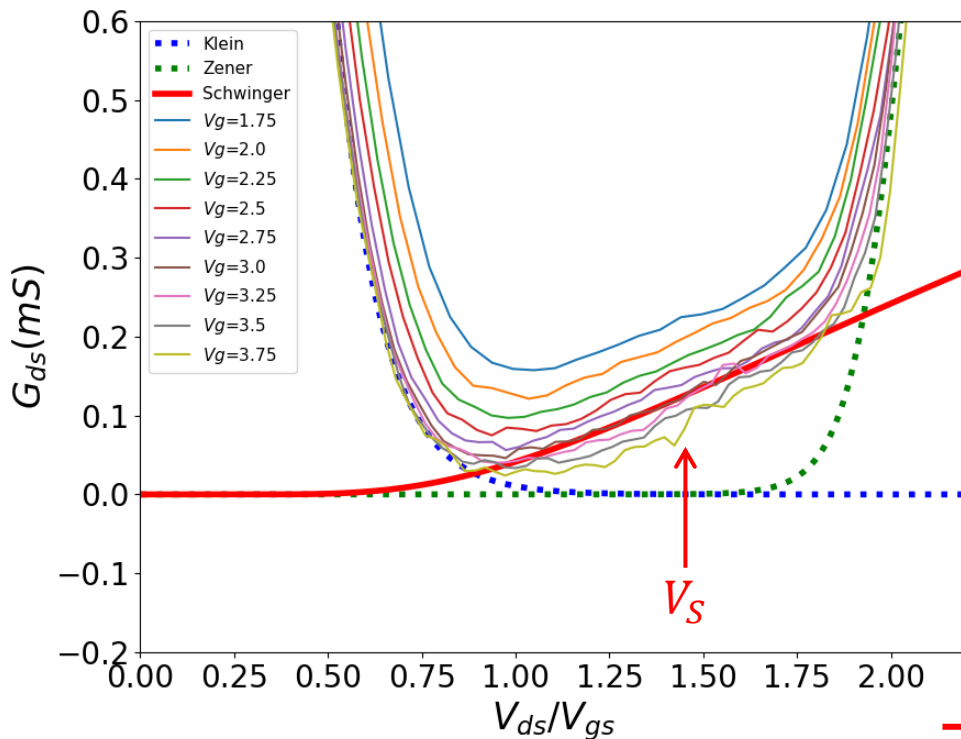


$$V_Z \propto LV_g$$

Zener instability is pushed to large  
 $V_Z \approx 2V_g$  in long ( $L \geq 10 \mu\text{m}$ ) devices

**A huge noise signals the destruction of the collimation junction**

# Evidence of mesoscopic Klein-Schwinger effect



$$G \approx G_S(V)$$

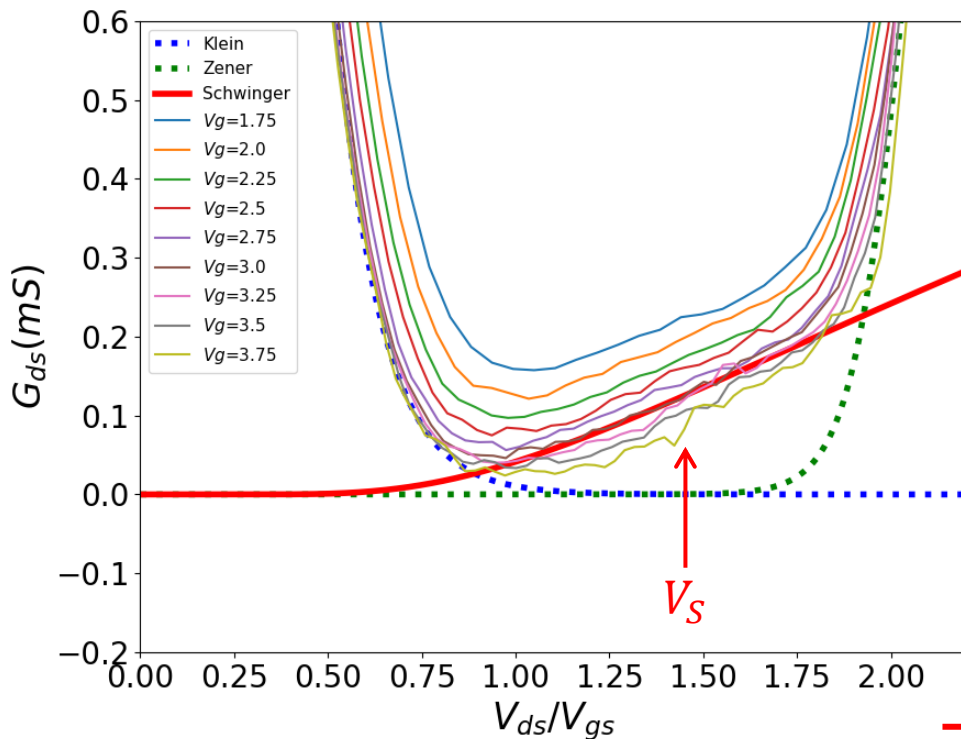
$$16 \left[ \text{Ln} \left( \frac{1}{1 - e^{-\pi V_S/V}} \right) + \frac{\pi V_S/V}{e^{\pi V_S/V} - 1} \right] \frac{e^2}{h}$$

$$\underline{V_g = 3V :}$$

$$V_S = 4.2V \quad \text{and} \quad \Lambda \sim t_{hBN}$$

$$\longrightarrow E_S \sim 5 \cdot 10^7 V/m, \quad \Delta_S \sim 0.2eV \sim \mu_S$$

# Evidence of mesoscopic Klein-Schwinger effect



$$G \approx G_S(V)$$

$$16 \left[ \text{Ln} \left( \frac{1}{1 - e^{-\pi V_S/V}} \right) + \frac{\pi V_S/V}{e^{\pi V_S/V} - 1} \right] \frac{e^2}{h}$$

$$\underline{V_g = 3V :}$$

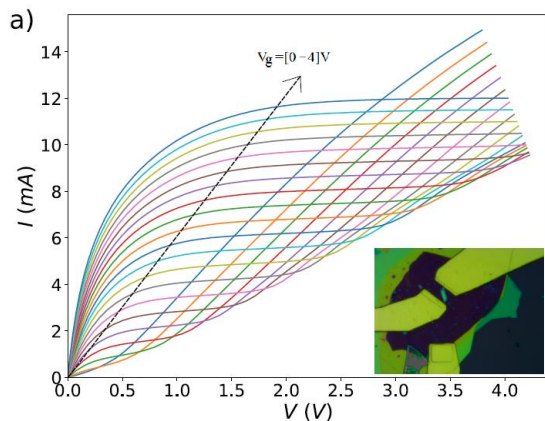
$$V_S = 4.2V \quad \text{and} \quad \Lambda \sim t_{hBN}$$

$$\longrightarrow E_S \sim 5 \cdot 10^7 V/m, \quad \Delta_S \sim 0.2eV \sim \mu_S$$

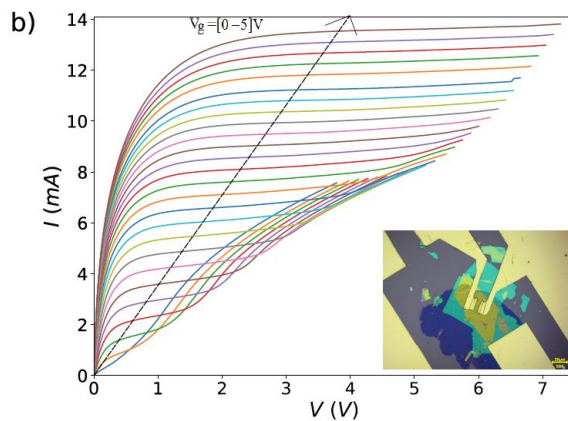
but obscured by Klein tunneling at low doping :  $G = G_S(V) + G_K(V)$

# Varied I-V according to hBN thickness / geometry ...

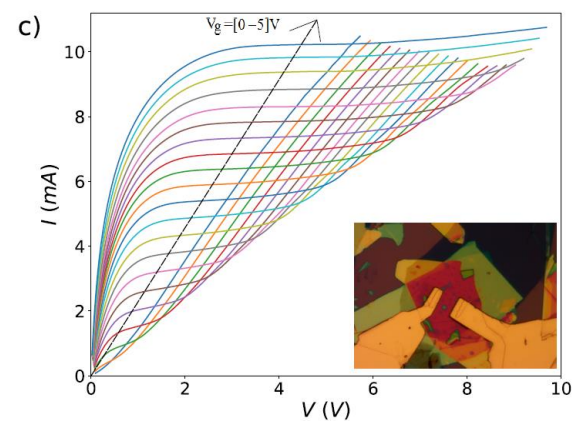
GrS1-25nm (L/W=0.75)



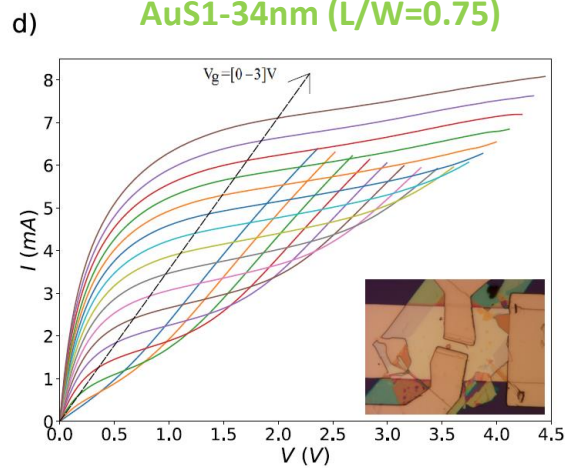
GrS2-35nm (L/W=0.7)



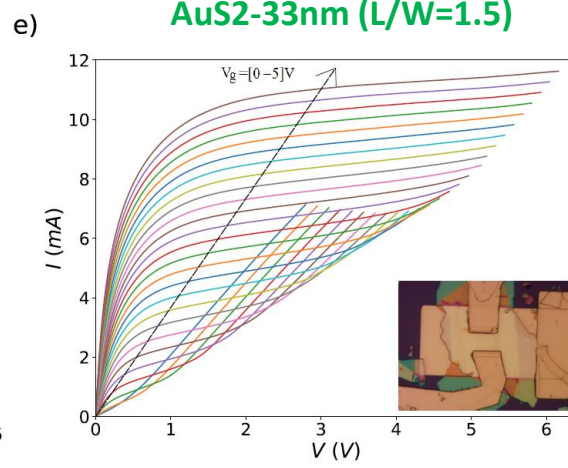
GrS3-42nm (L/W=1.5)



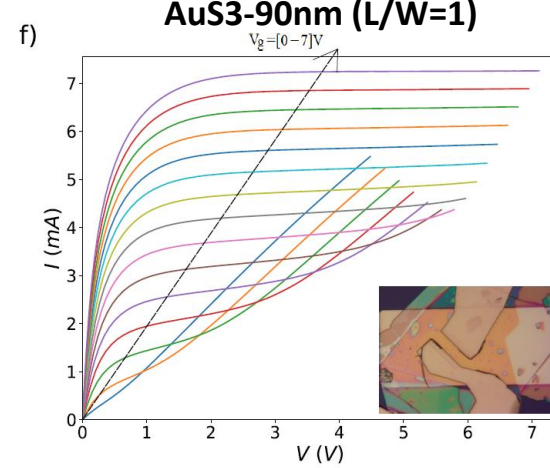
AuS1-34nm (L/W=0.75)



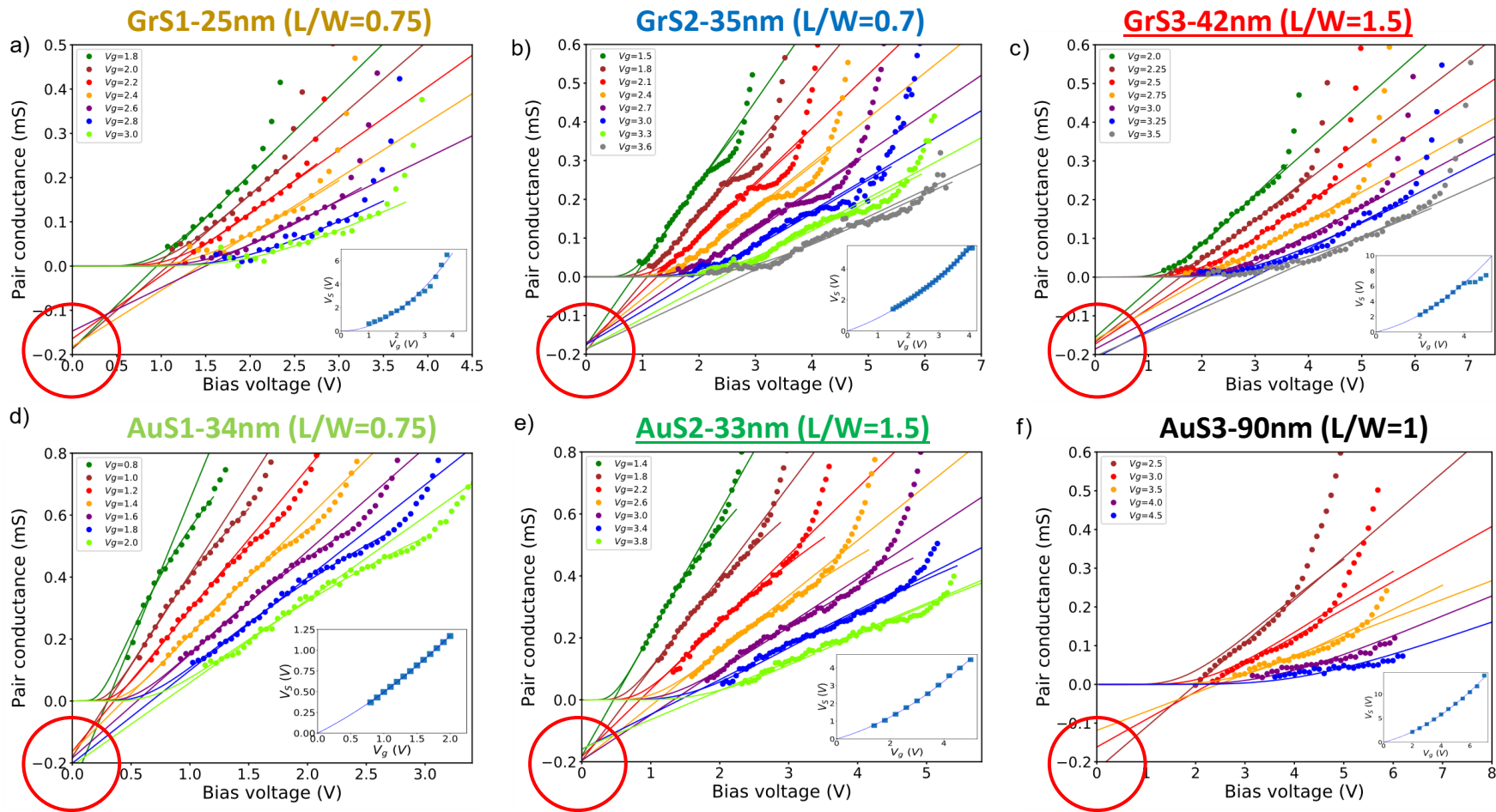
AuS2-33nm (L/W=1.5)



AuS3-90nm (L/W=1)

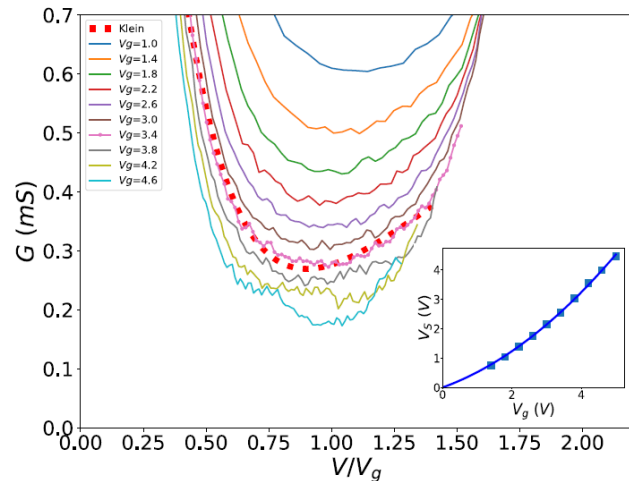
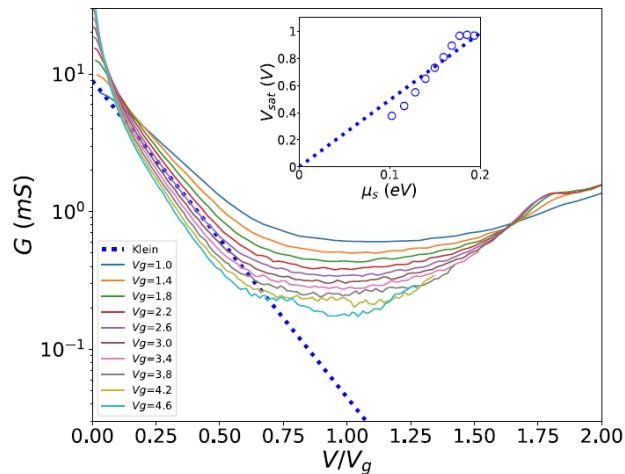
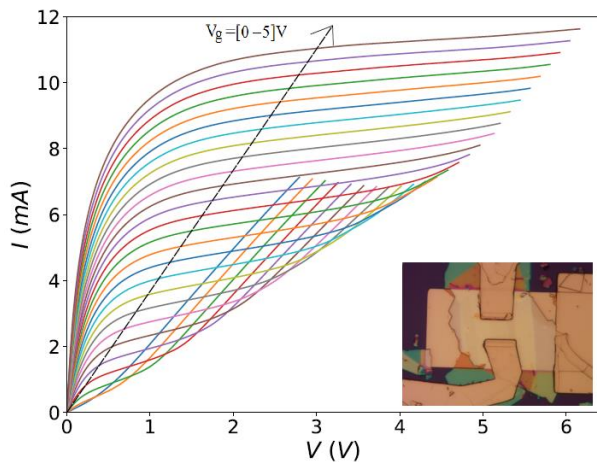


# Same 1d-Schwinger scaling in various geometry !



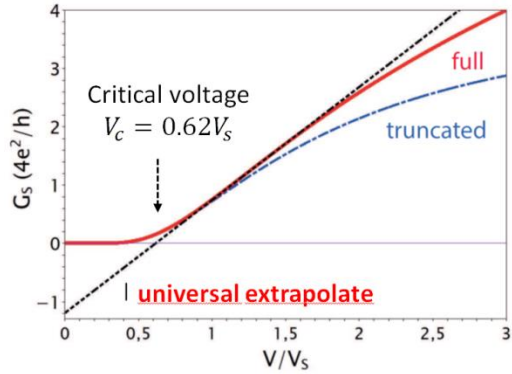
# The non-perturbative Schwinger prediction verified in detail

A device with a thin hBN dielectric (32nm)



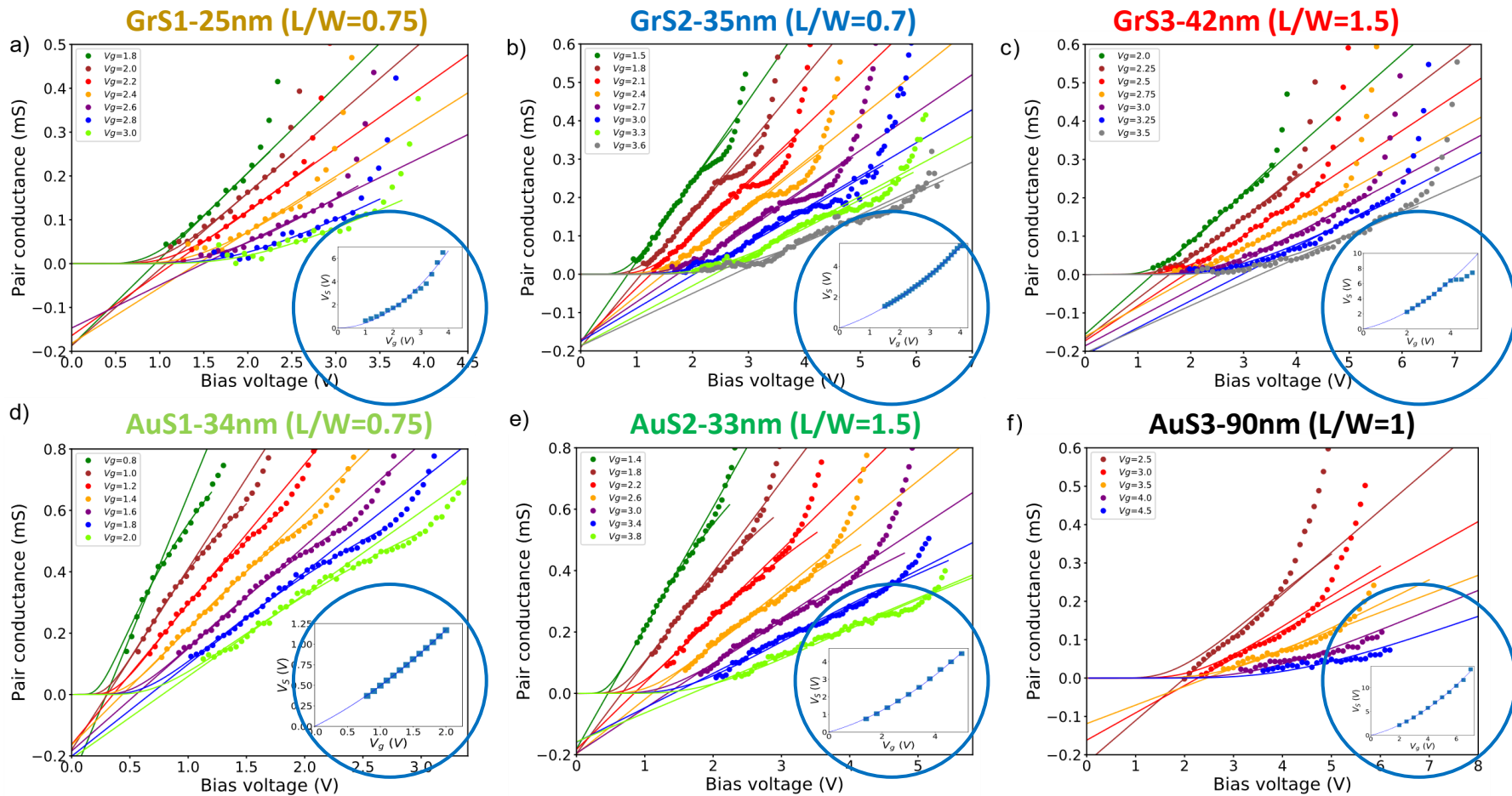
Early onset of Schwinger pair creation  $V_S \leq 0.5 V_g$

# The non-perturbative Schwinger prediction verified in detail



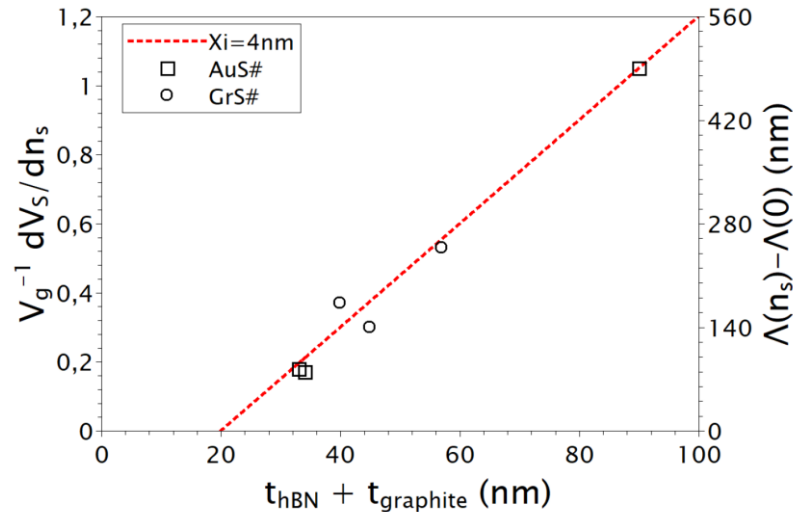
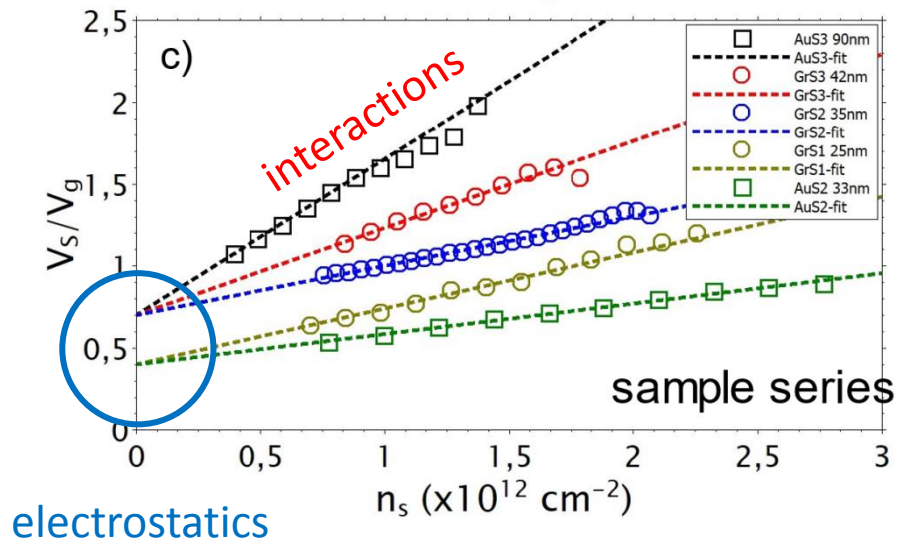
an important result for field theory

# Measured $V_S(V_g)$ dependence

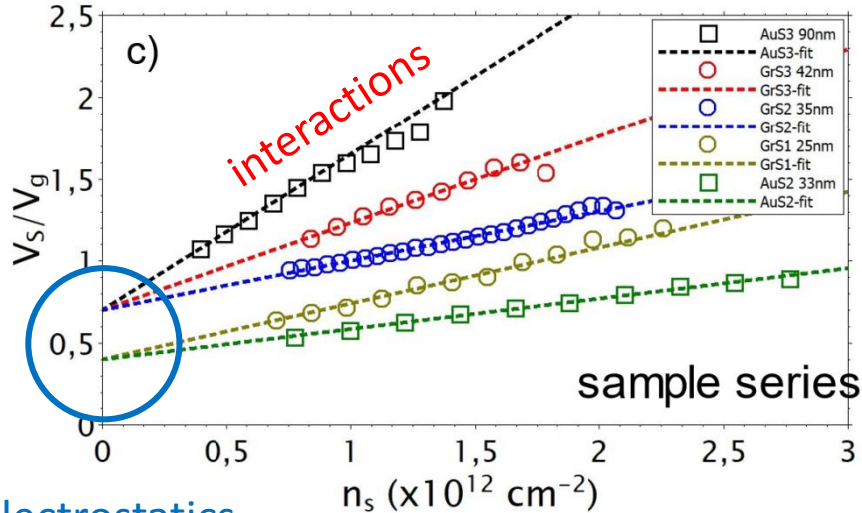




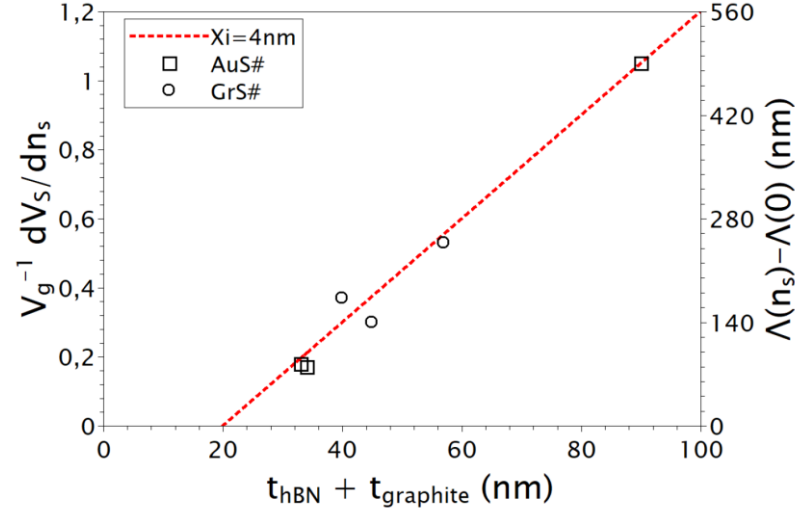
# Length of the Klein collimation junction



# Length of the Klein collimation junction



electrostatics

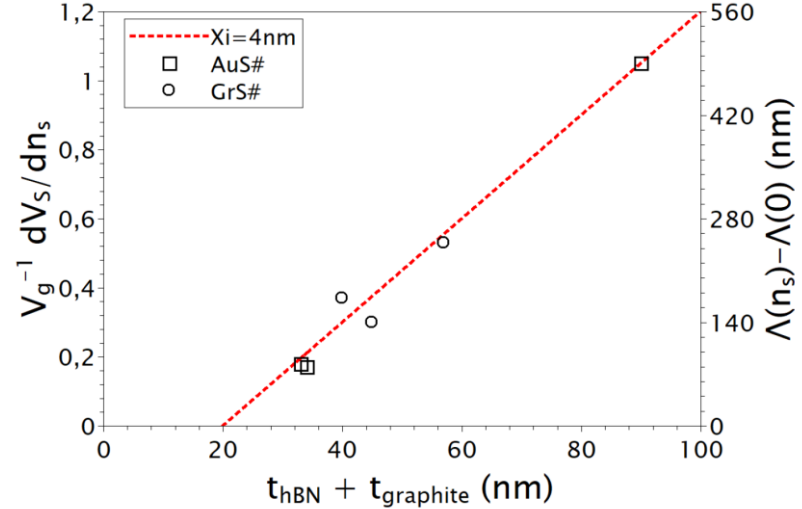
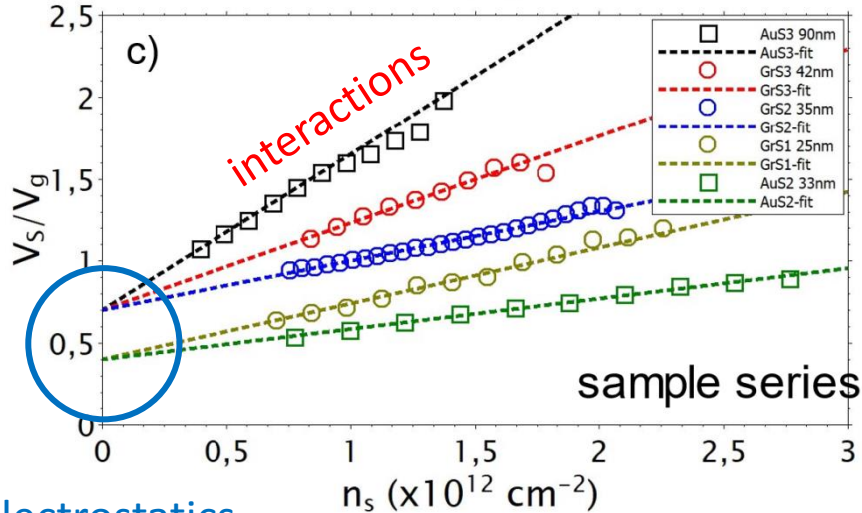


$$\Lambda \approx 2.8 \frac{V_s}{V_g} t_{hBN} \approx (1 - 2)t_{hBN} + (4 \text{ nm}) \times n_s t_{hBN}^2 = (1 - 6)t_{hBN}$$

NB:  $\frac{\Lambda(n_s, t_{hBN})}{t_{hBN}} = \frac{V_s/E_s}{V_g/E_{hBN}} = 4\alpha_g \frac{V_s}{V_g} \left(\frac{\mu_s}{\Delta_s}\right)^2 \approx 2.8 \frac{V_s}{V_g}$

with  $\alpha_g = \frac{e^2}{4\pi\epsilon_0\epsilon_{hBN}\hbar v_F} = 0.70$

# Length of the Klein collimation junction



$$\Lambda \approx 2.8 \frac{V_s}{V_g} t_{hBN} \approx (1 - 2)t_{hBN} + (4 \text{ nm}) \times n_s t_{hBN}^2 = (1 - 6)t_{hBN}$$

The  $\Delta_S \approx \mu_S$  ansatz gives consistent Klein-junction lengths