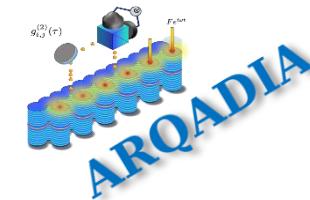


# Measuring the topological properties of exciton-polariton lattices

05/07/2023

Martin Guillot – 3rd year Ph.D.

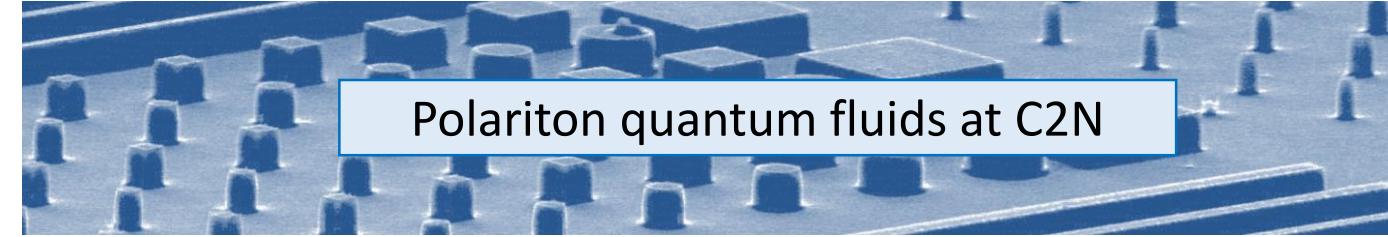
Supervisors: Jacqueline Bloch and Sylvain Ravets



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DE Nanosciences  
& DE Nanotechnologies

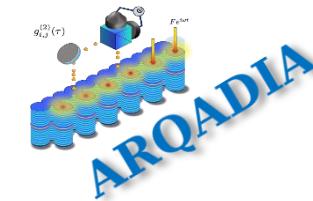


Polariton quantum fluids at C2N

# I. The valley Hall effect

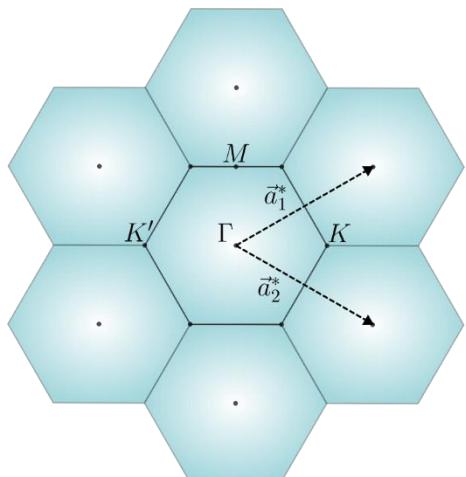
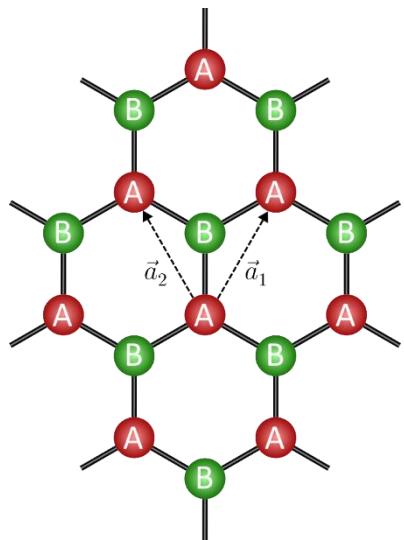


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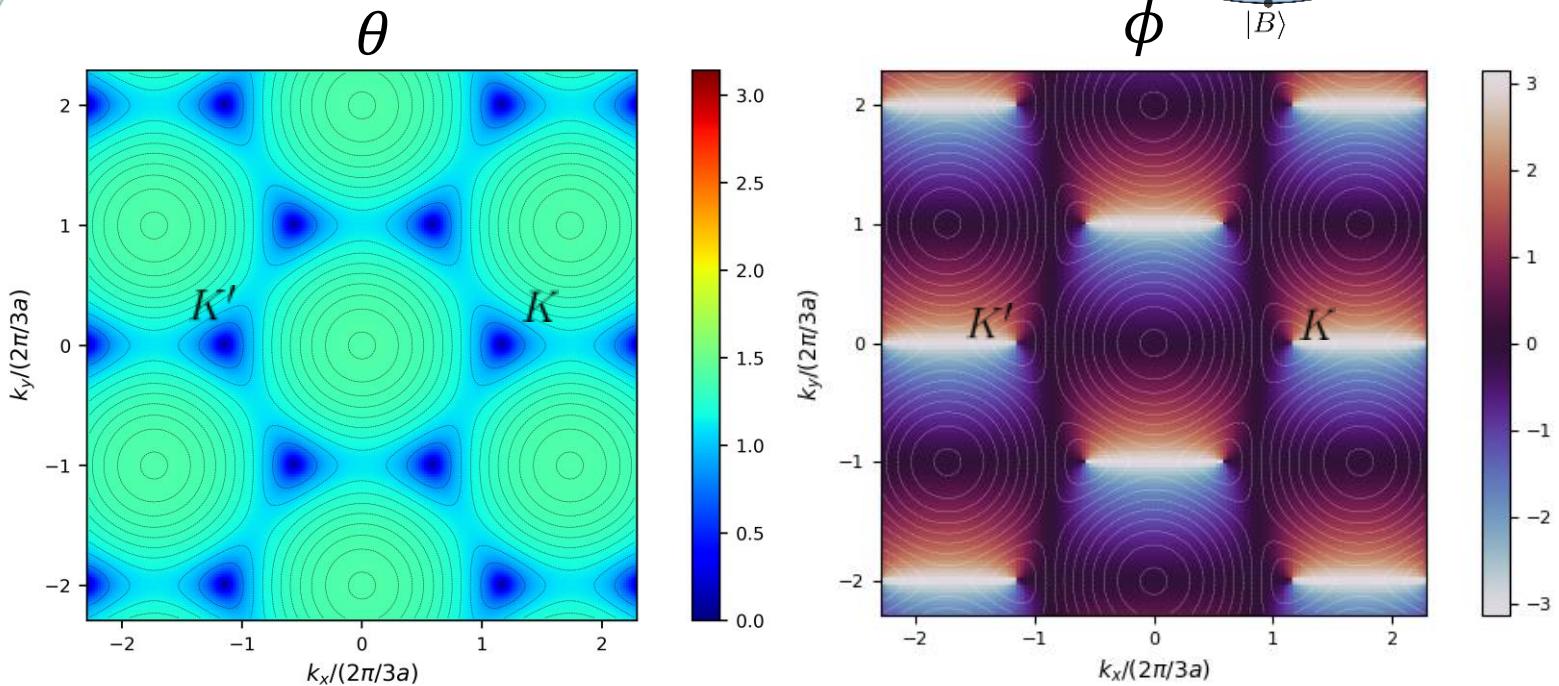
# The staggered honeycomb lattice



$$\hat{H}_{\vec{k}} = \begin{bmatrix} -\epsilon_0 & -t\gamma(\vec{k}) \\ -t\gamma^*(\vec{k}) & \epsilon_0 \end{bmatrix}$$

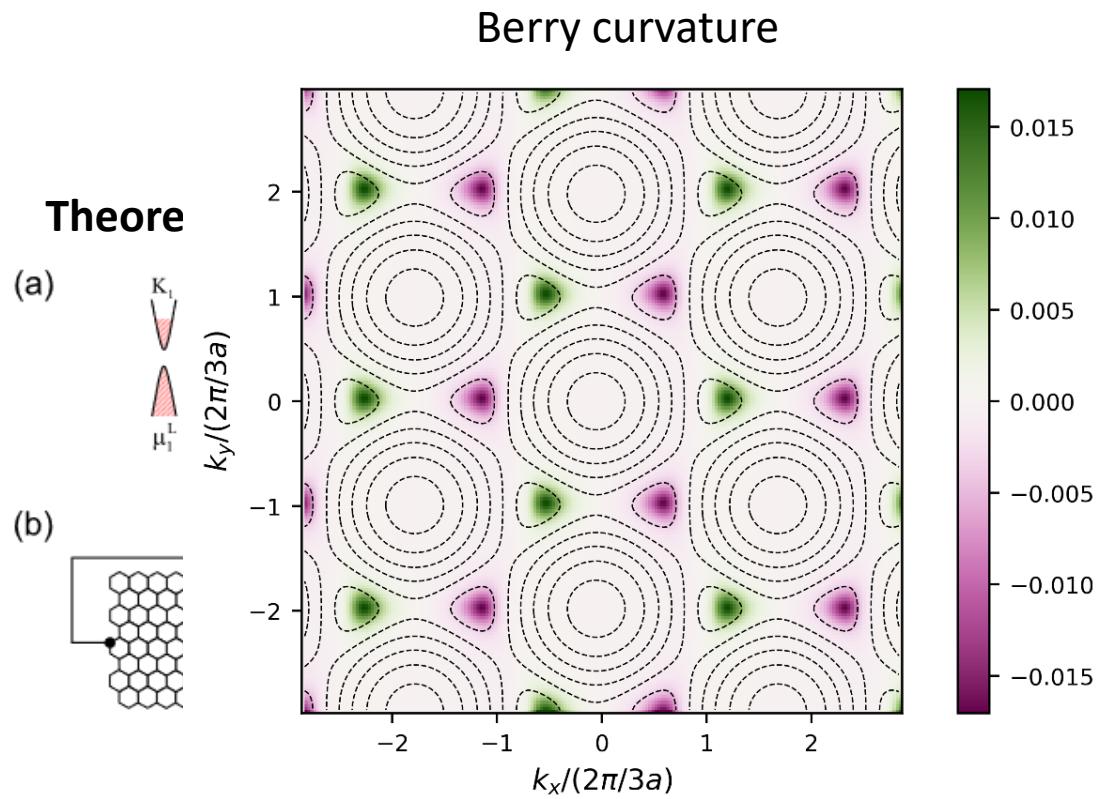
$$\gamma(\vec{k}) = 1 + e^{-i\vec{k}\cdot\vec{a}_1} + e^{-i\vec{k}\cdot\vec{a}_2}$$

$$u_{\vec{k}}^n = \begin{bmatrix} \cos(\theta/2)e^{i\phi} \\ \sin(\theta/2) \end{bmatrix}$$



Topological Origin of Zero-Energy Edge States in Particle-Hole Symmetric Systems  
 Shinsei Ryu and Yasuhiro Hatsugai  
 Phys. Rev. Lett. **89**, 077002

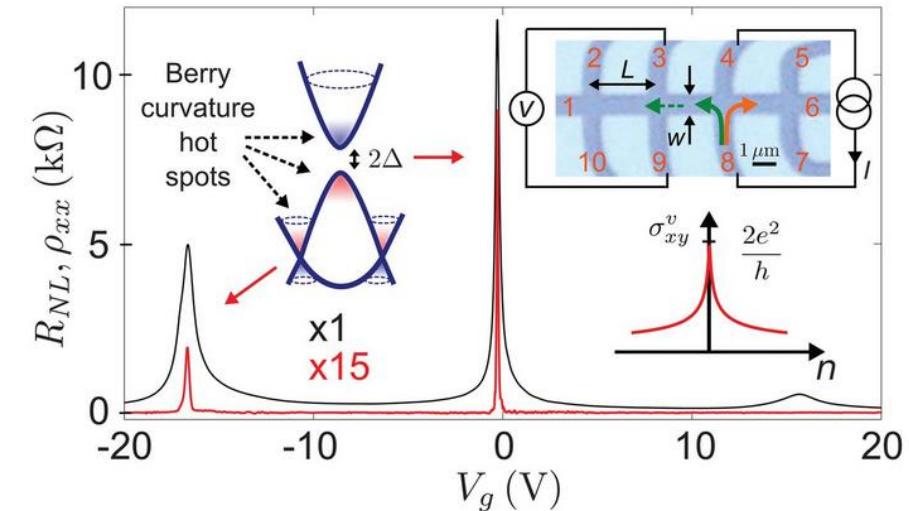
# The valley Hall effect in condensed matter



Di Xiao, et al., Valley-Contrasting Physics in Graphene: Magnetic Moment and Topological Transport. Phys. Rev. Lett. **99**, 236809 (2007).

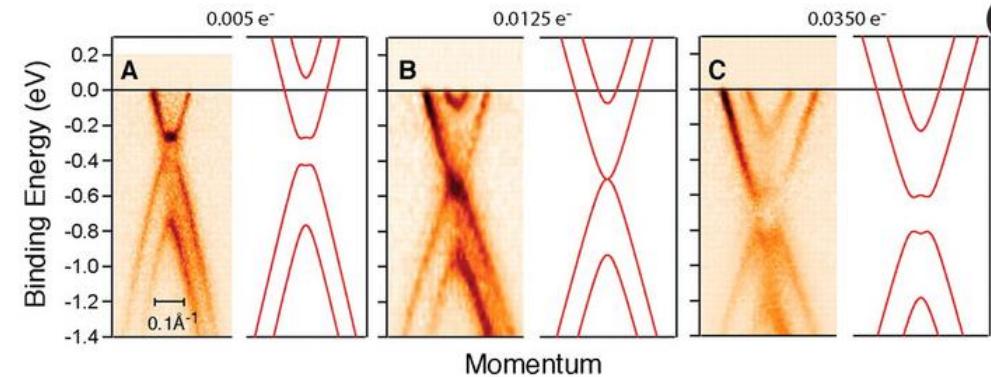
Rycerz, A., Tworzydło, J. & Beenakker, C. Valley filter and valley valve in graphene. Nature Phys **3**, 172–175 (2007).

## Valley-Hall current measurements



R. V. Gorbachev et al., Detecting topological currents in graphene superlattices. Science **346**, 448-451 (2014)

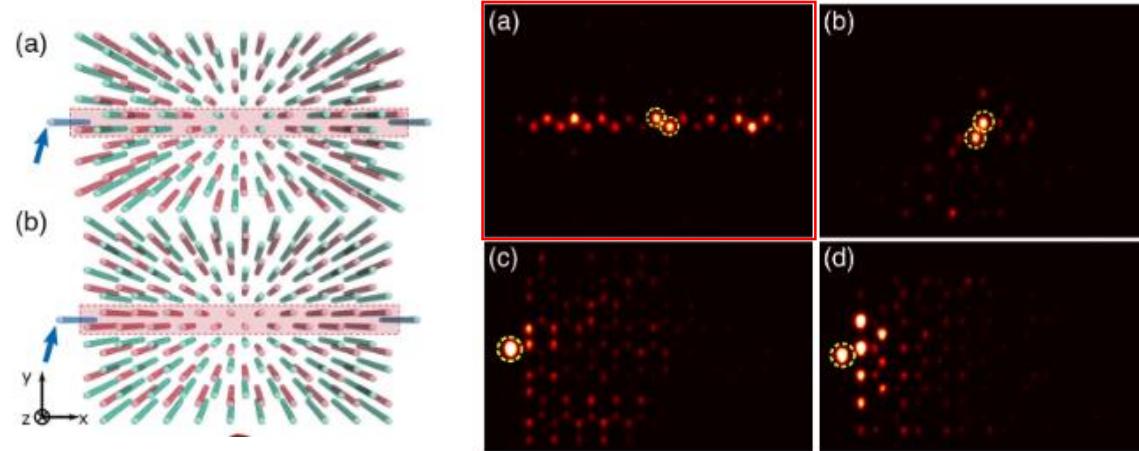
## Band imaging



Taisuke Ohta et al., Controlling the Electronic Structure of Bilayer Graphene. Science **313**, 951-954 (2006).

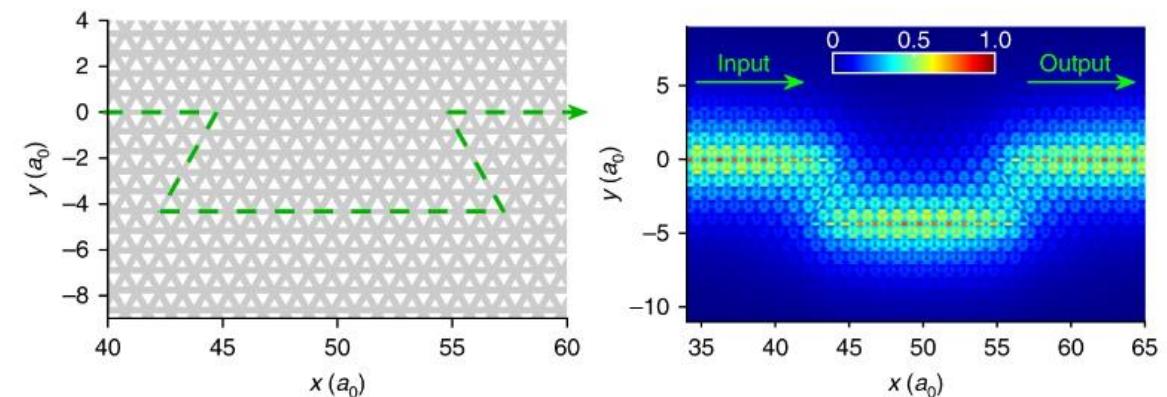
# Photonic valley Hall insulators

## In coupled waveguide arrays



Jiho Noh, et al., Observation of Photonic Topological Valley Hall Edge States.  
Phys. Rev. Lett. **120**, 063902 (2018)

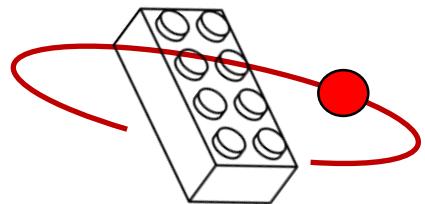
## In photonic crystals



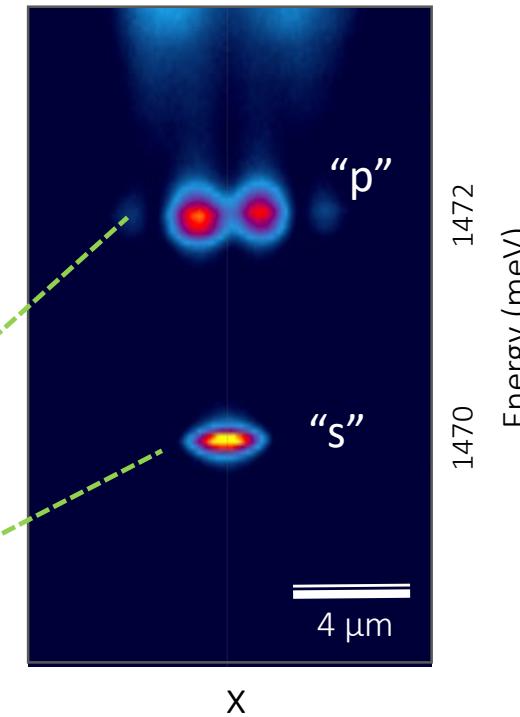
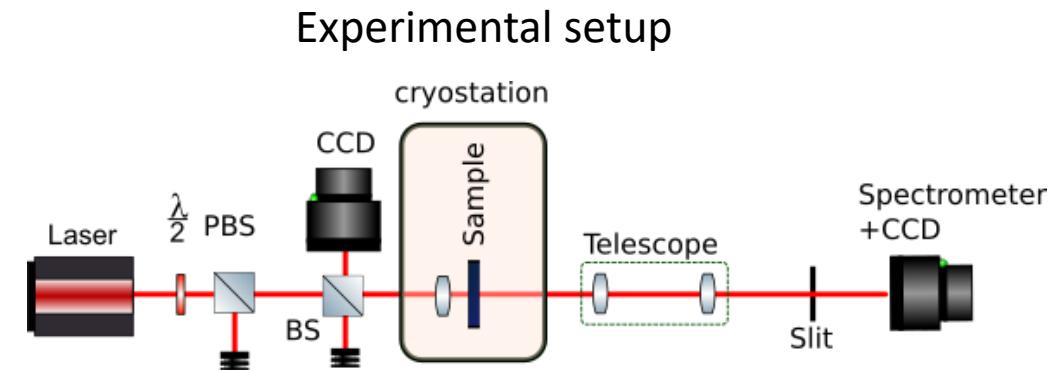
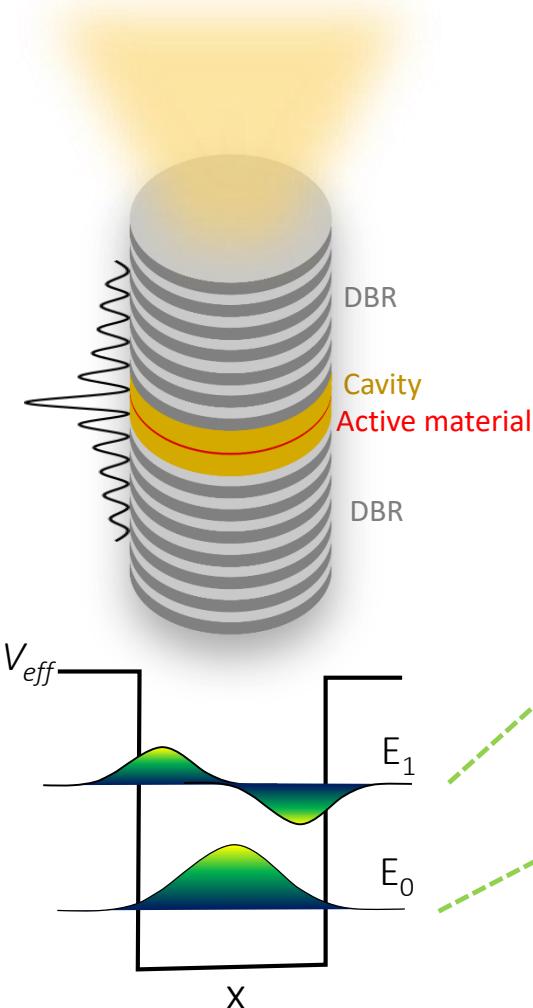
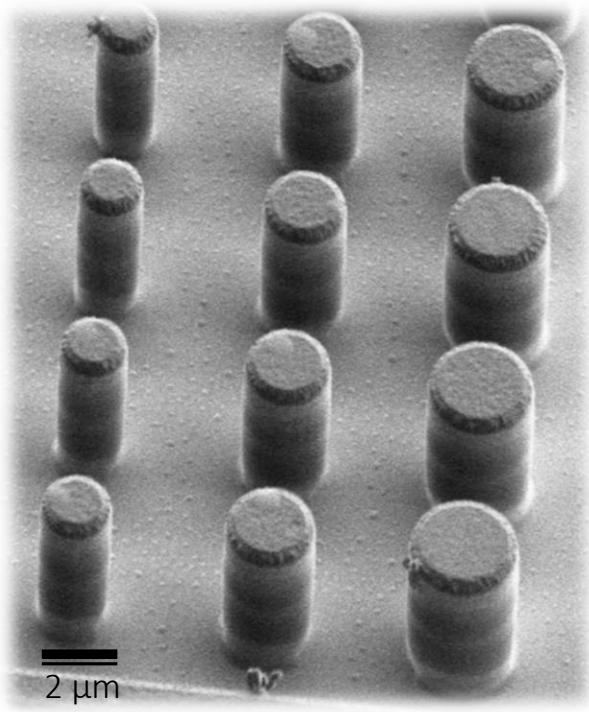
Shalaev, M.I., Walasik, W., Tsukernik, A. et al. Robust topologically protected transport in photonic crystals at telecommunication wavelengths.  
Nature Nanotech **14**, 31–34 (2019).

Can we get to the eigenvector structure ?

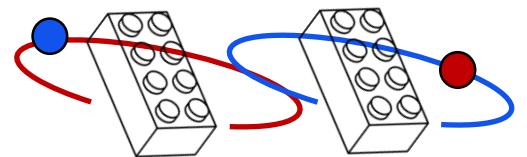
# Engineering the photonic wavefunction



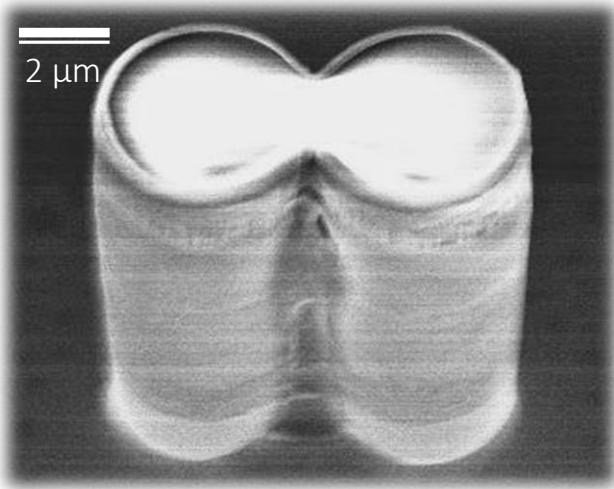
➤ Our bricks: Semiconductor micropillars



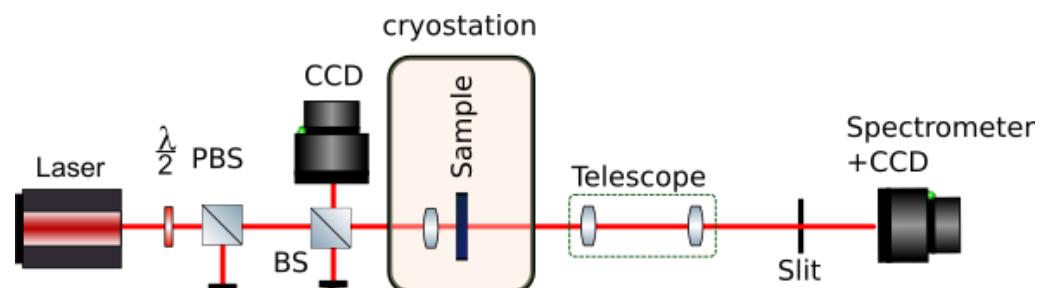
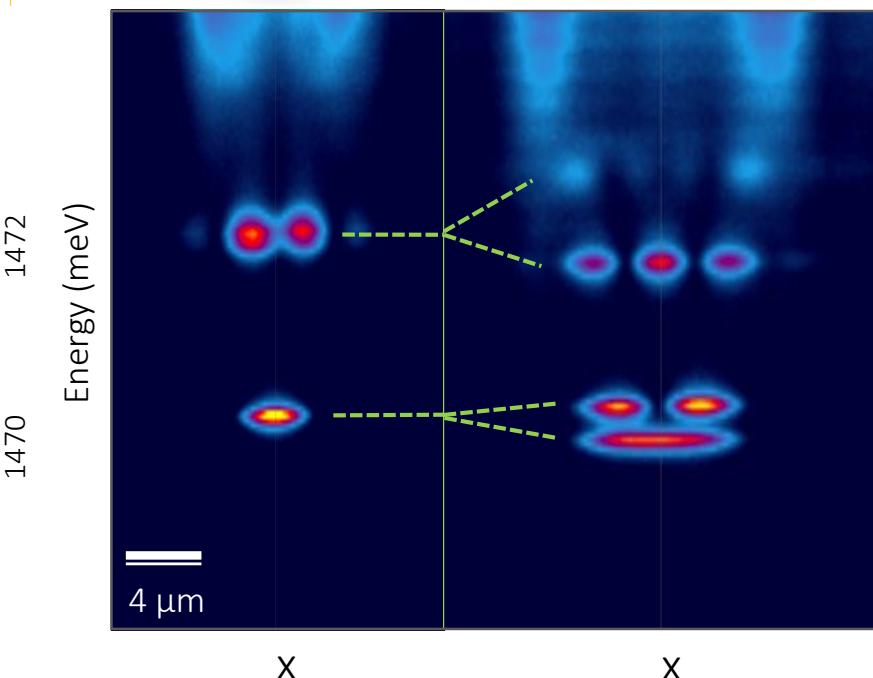
# Engineering the photonic wavefunction



➤ Coupling the bricks

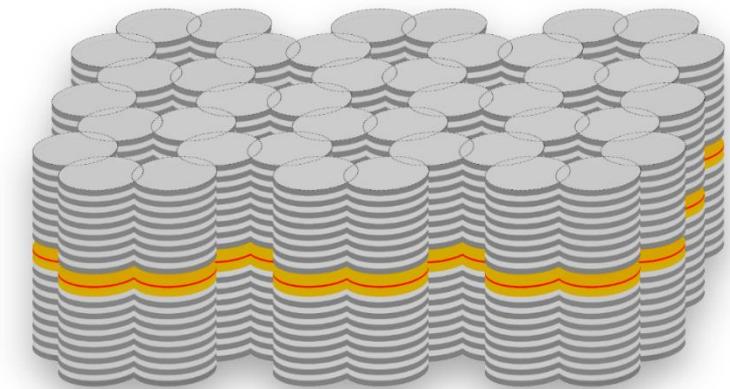
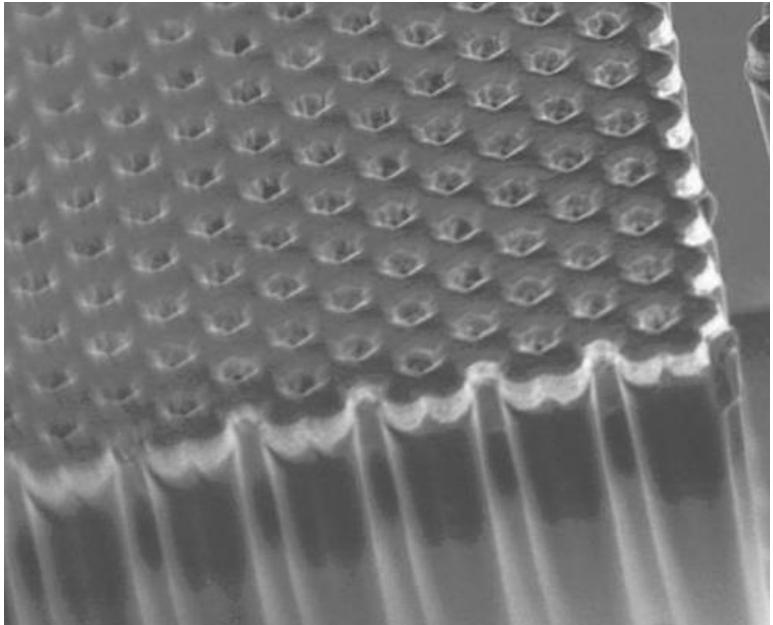


Galbiati et al., PRL 108, 126403 (2012)

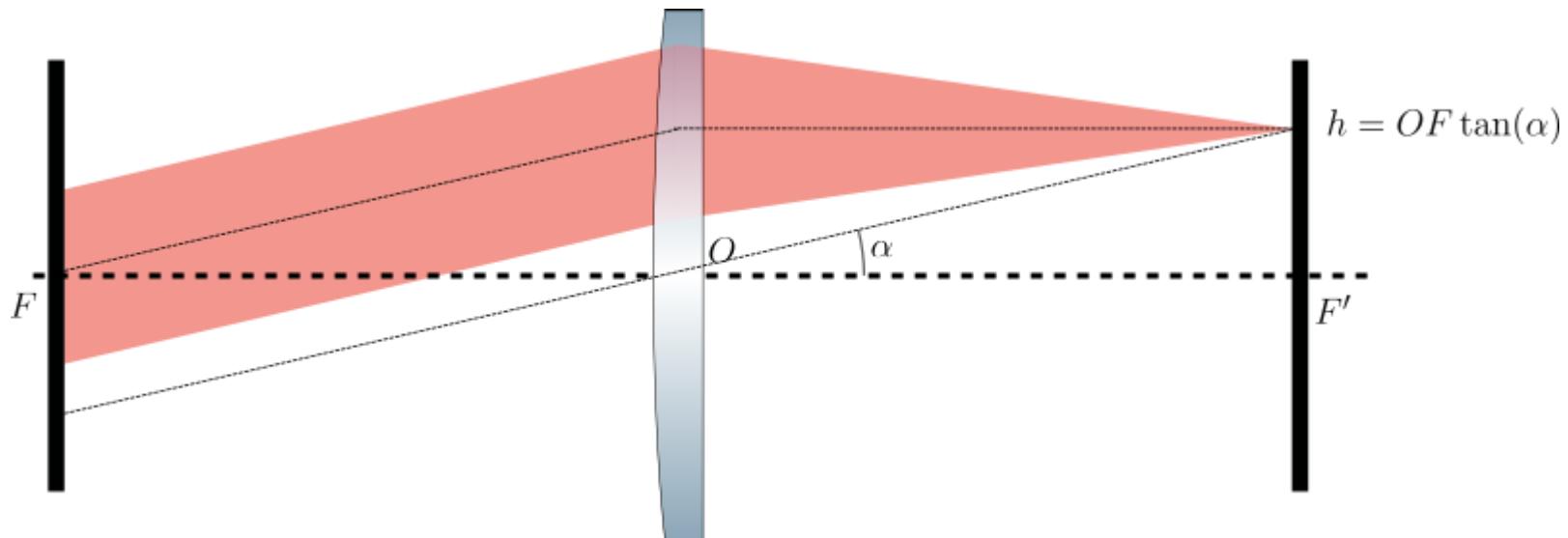


# Engineering the photonic wavefunction

... And finally lattices

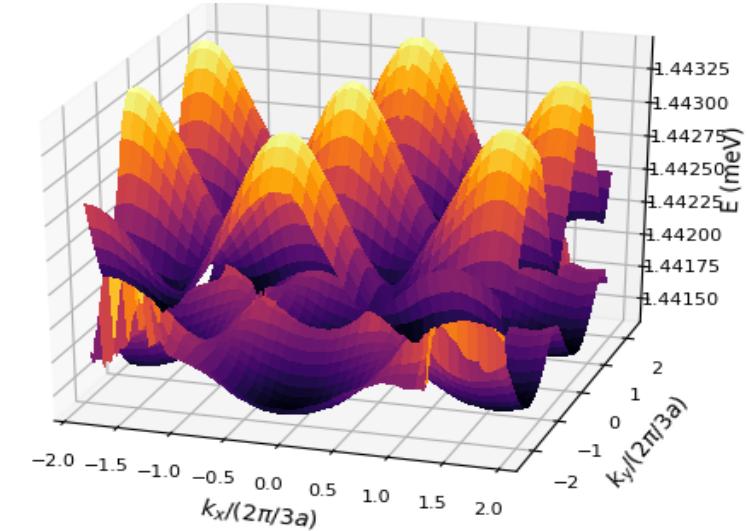
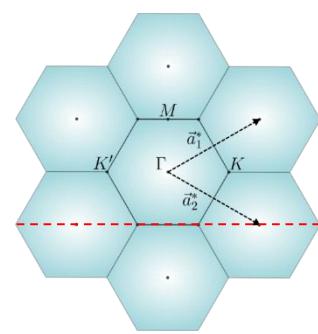
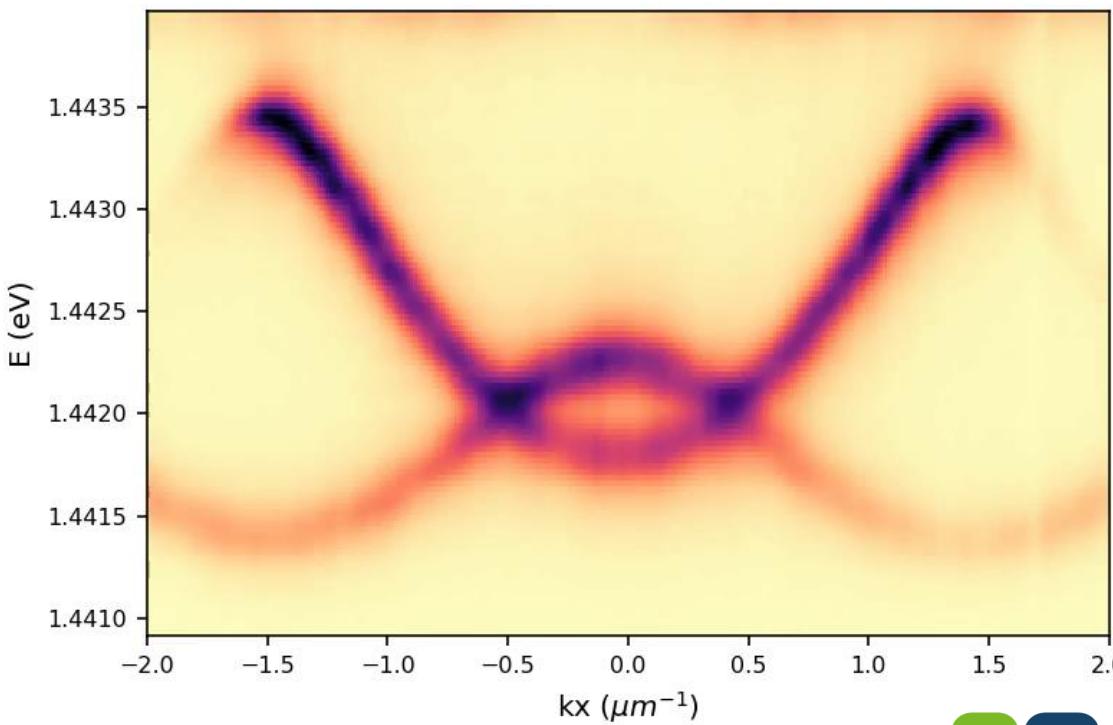
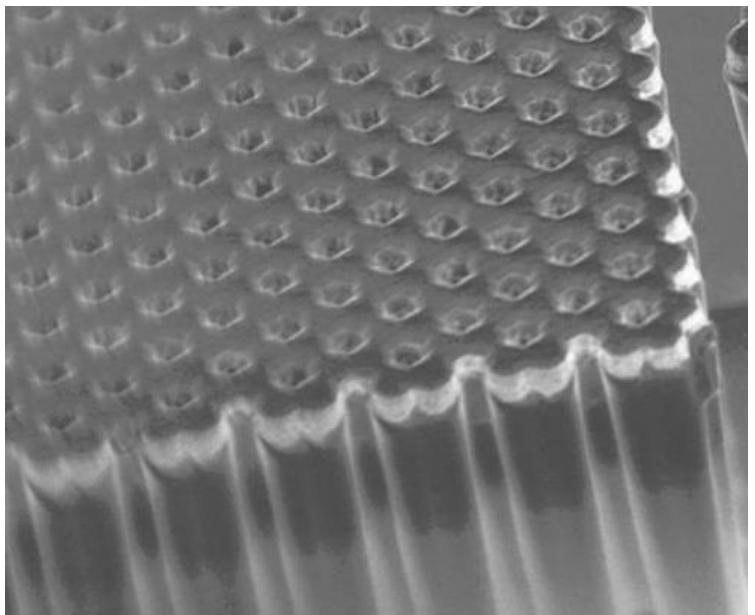


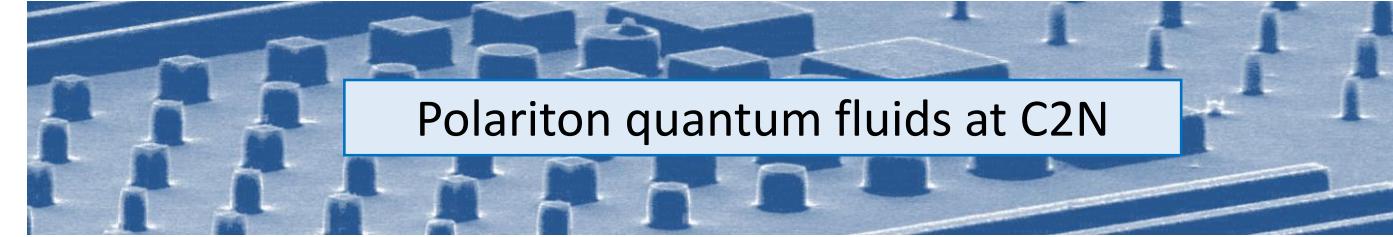
Optical Fourier transform: Imaging reciprocal space



# Engineering the photonic wavefunction

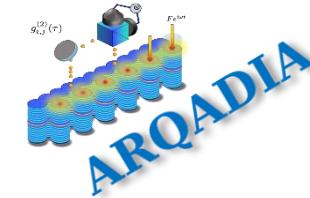
... And finally lattices





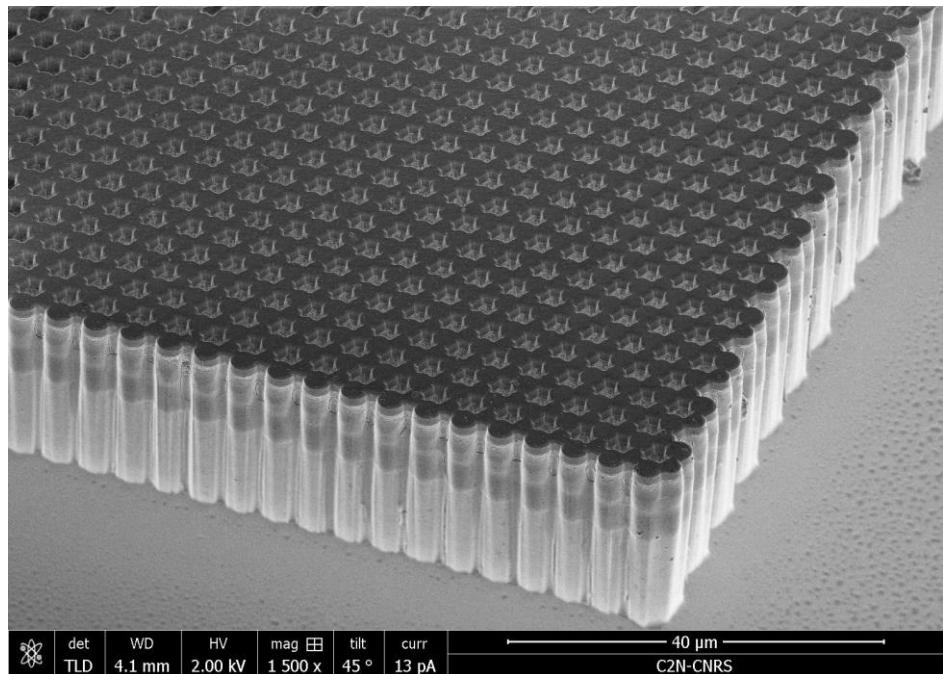
# II. Valley Hall insulator in exciton-polaritons lattices

How to probe the eigenvector structure of a polaritonic platform ?



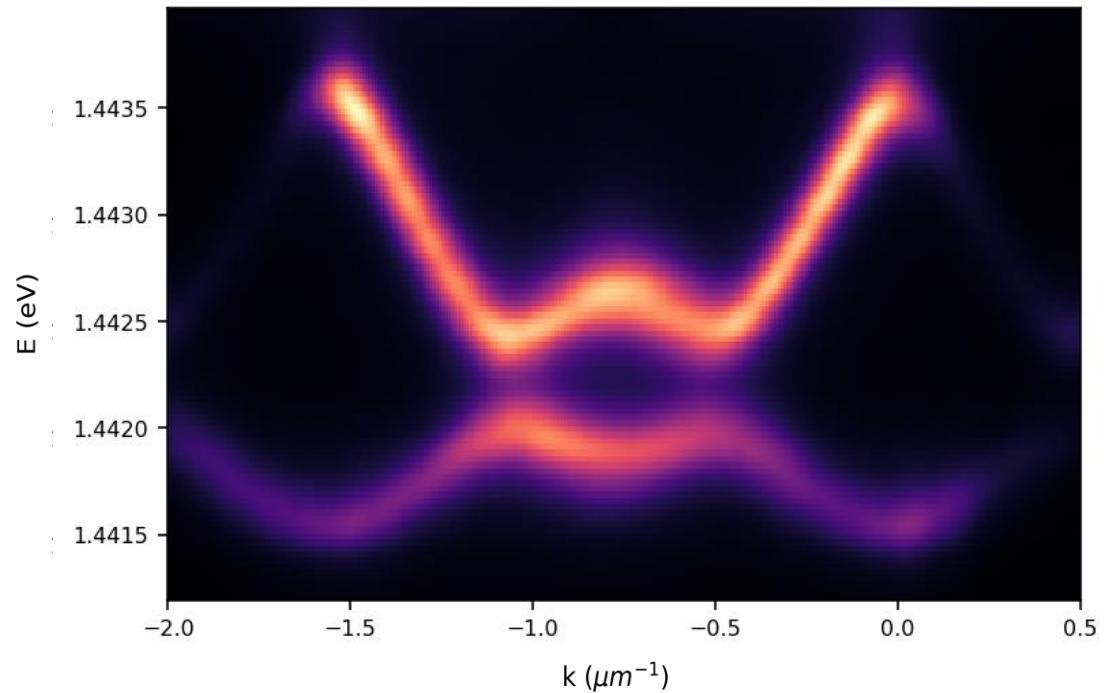
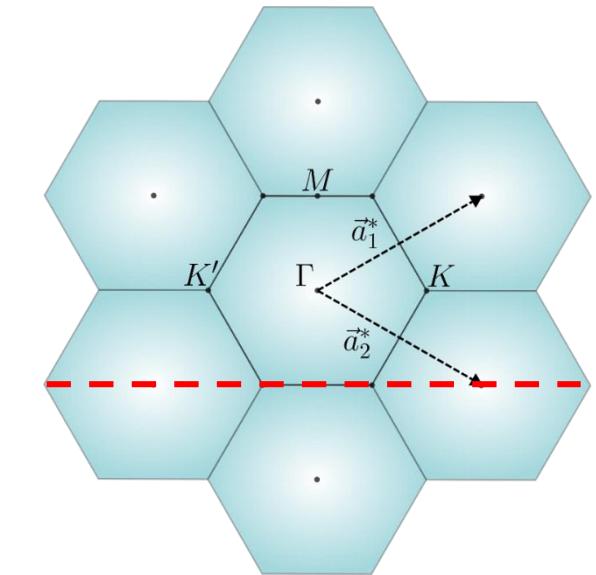
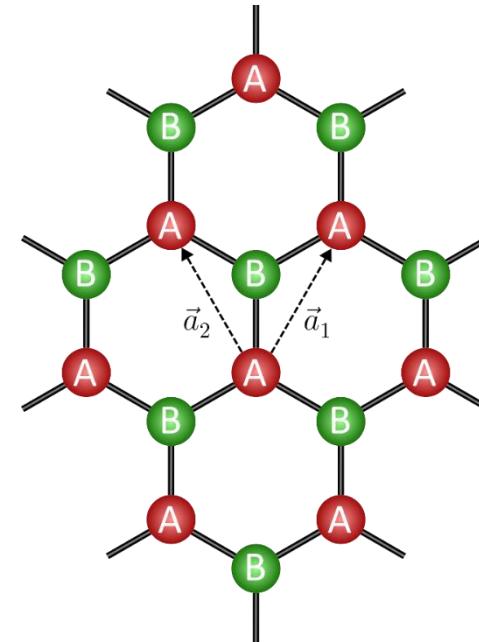
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# Polariton honeycomb lattices

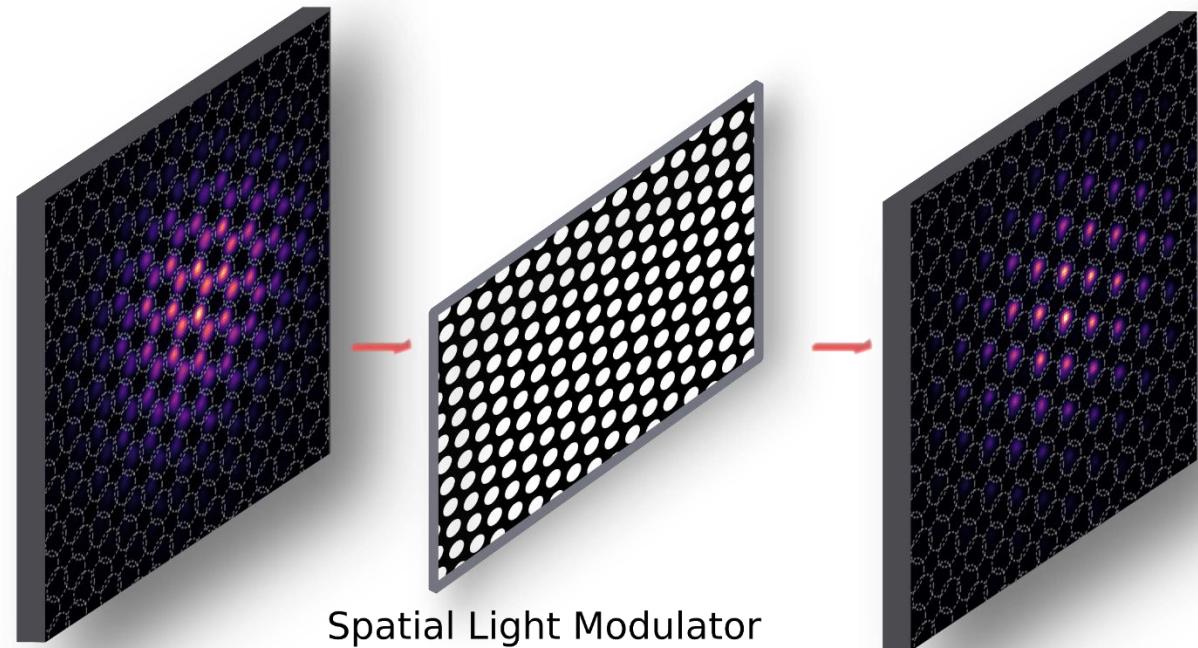
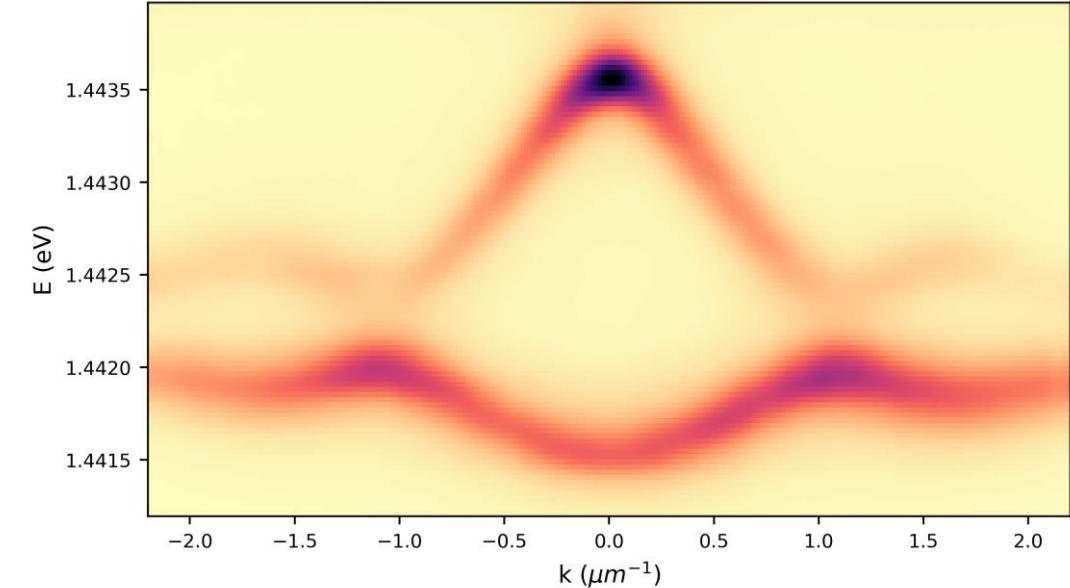
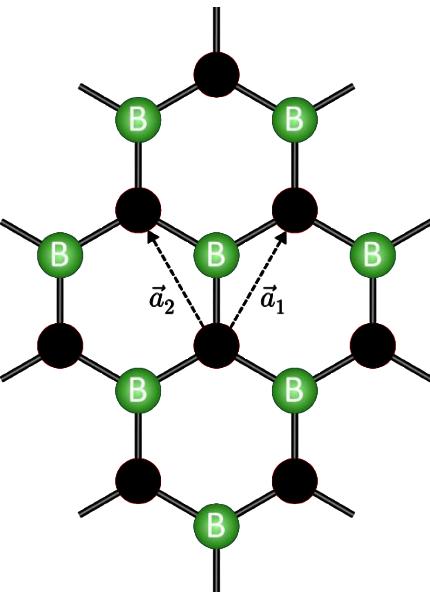
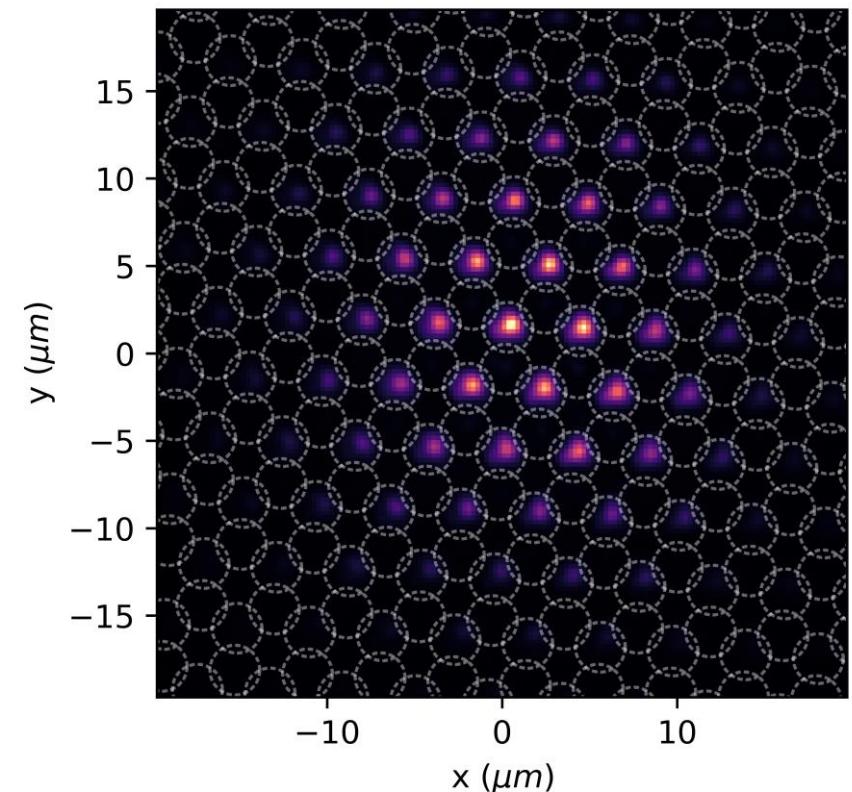


The bloch's eigenvectors are encoded in a sublattice pseudospin:

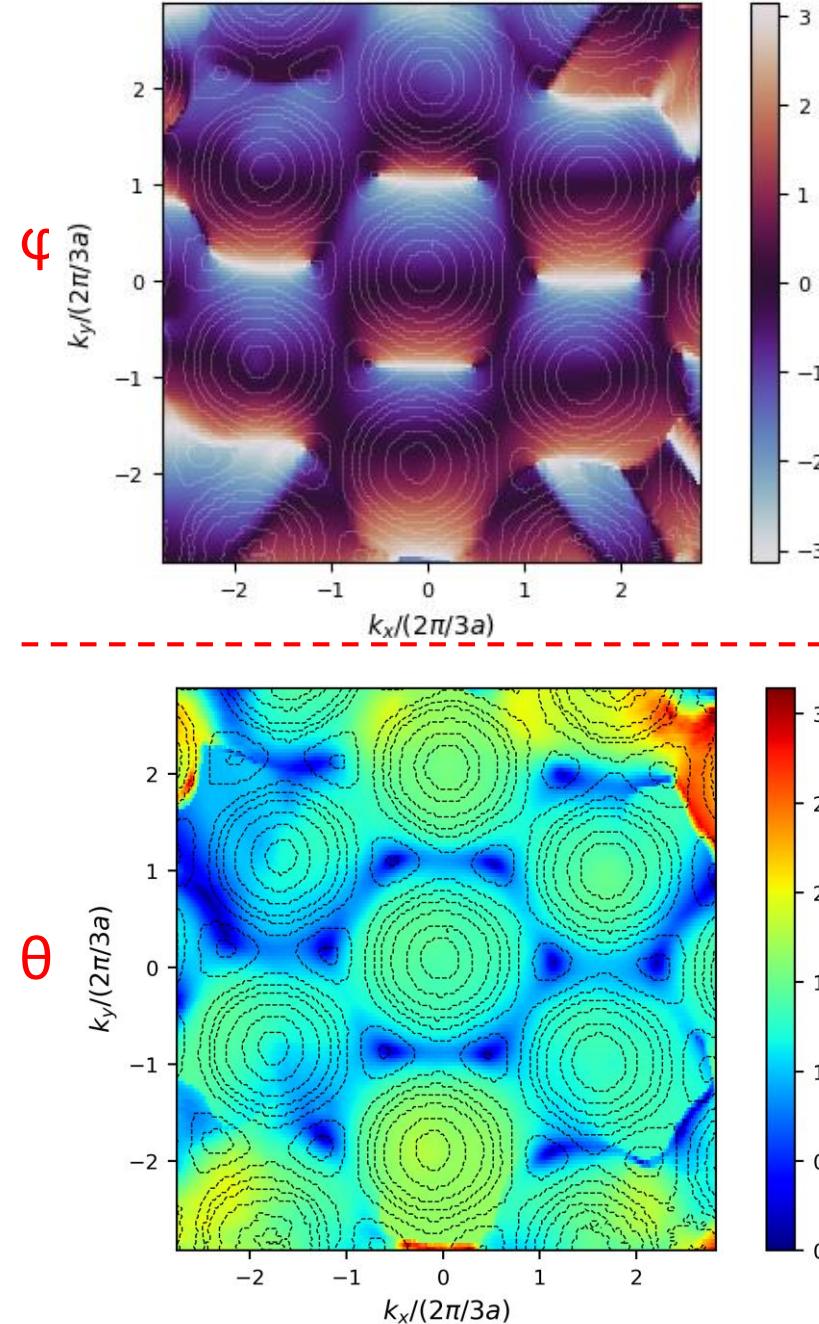
$$u_{\vec{k}}^n = \begin{bmatrix} \cos(\theta/2)e^{i\phi} \\ \sin(\theta/2) \end{bmatrix}$$



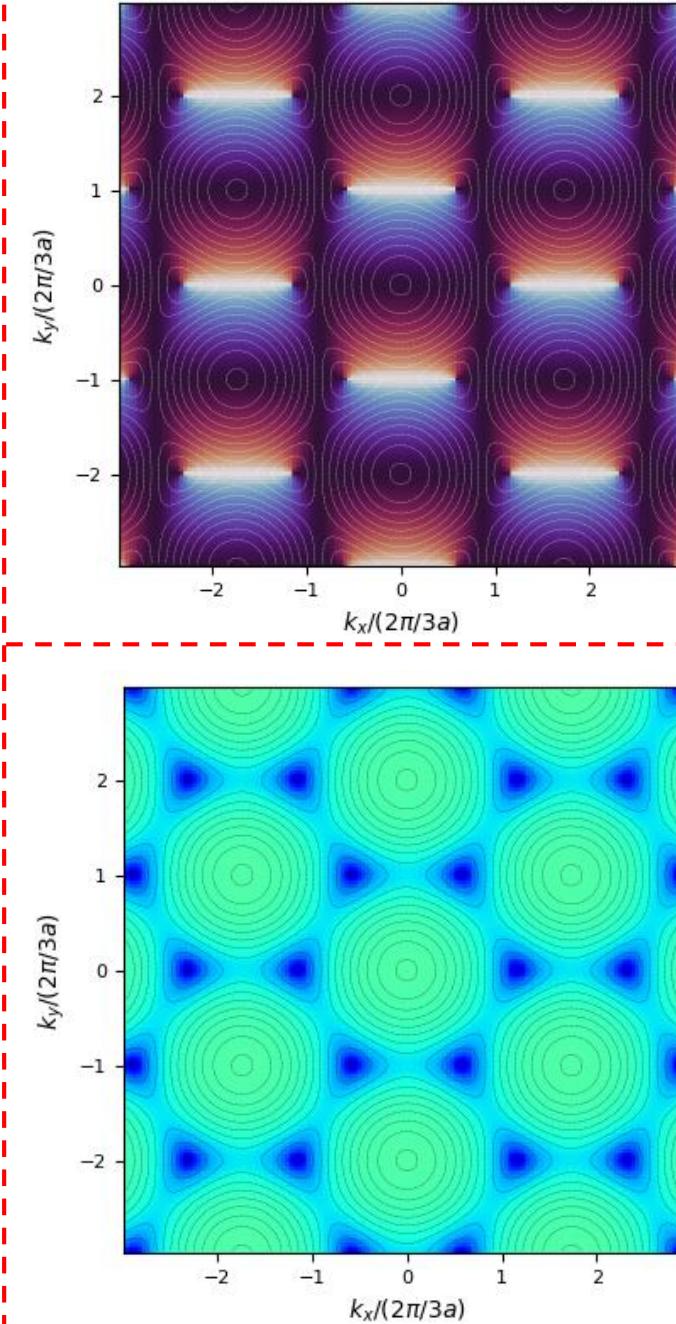
# Accessing the eigenvector structure



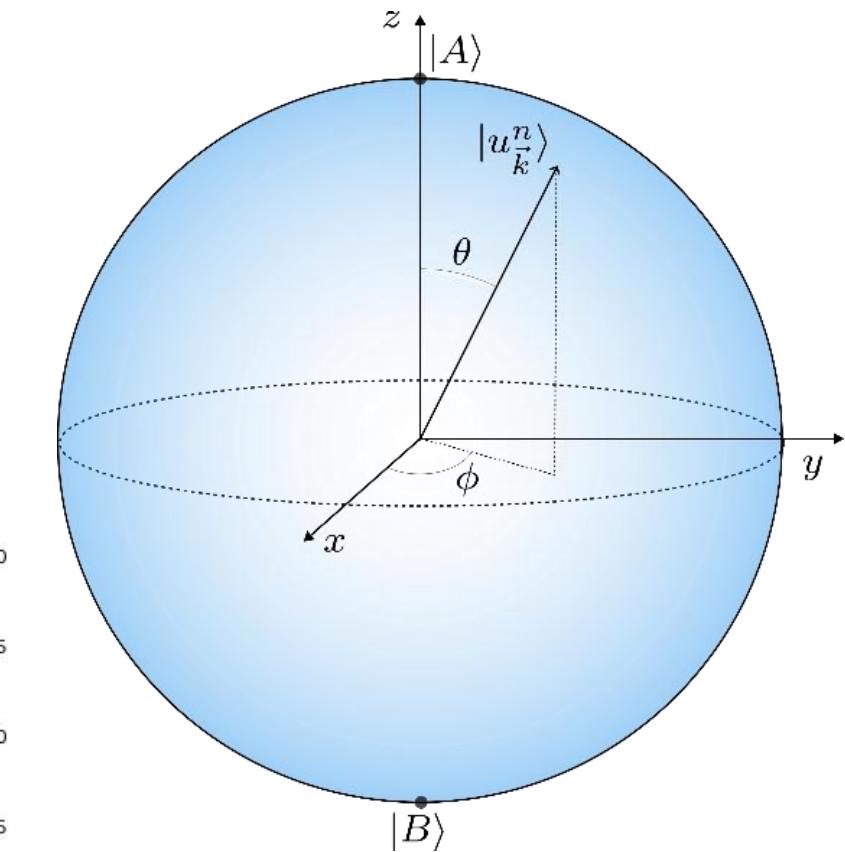
# Experimental



# Theory



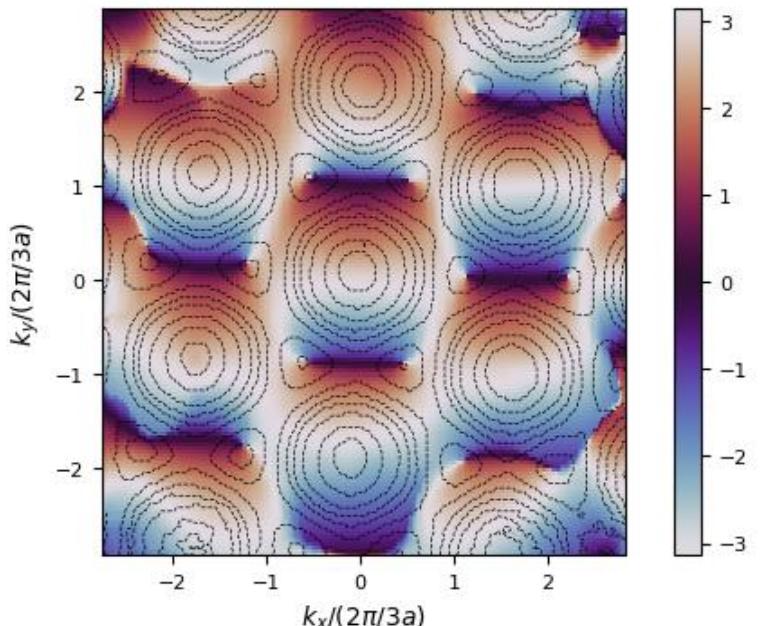
# Lower band



$$\vec{u}_k^n = \begin{bmatrix} \cos(\theta/2)e^{i\phi} \\ \sin(\theta/2) \end{bmatrix}$$

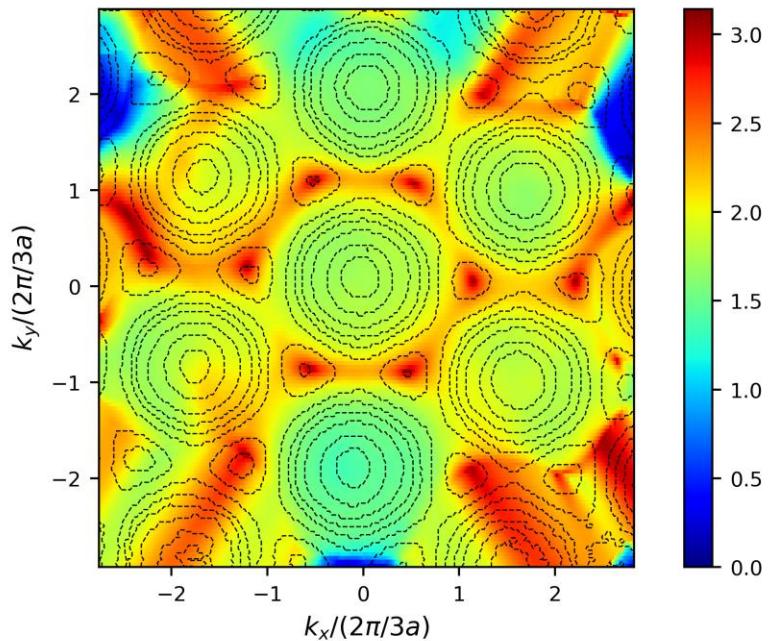
# Experimental

$\varphi$

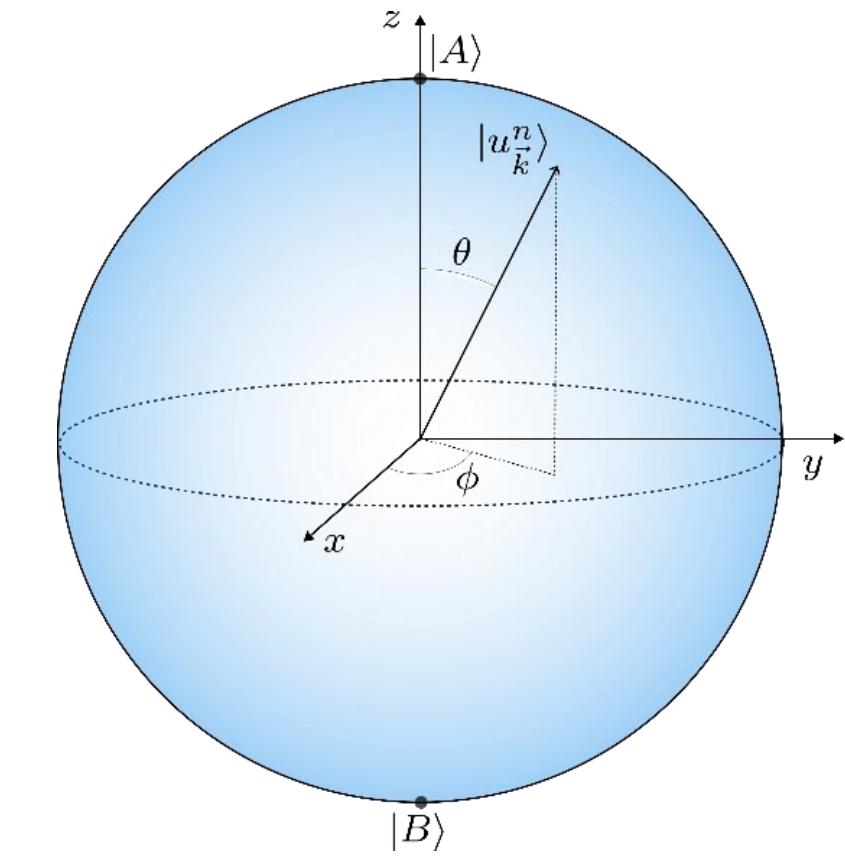


# Theory

$\Theta$



# Upper band

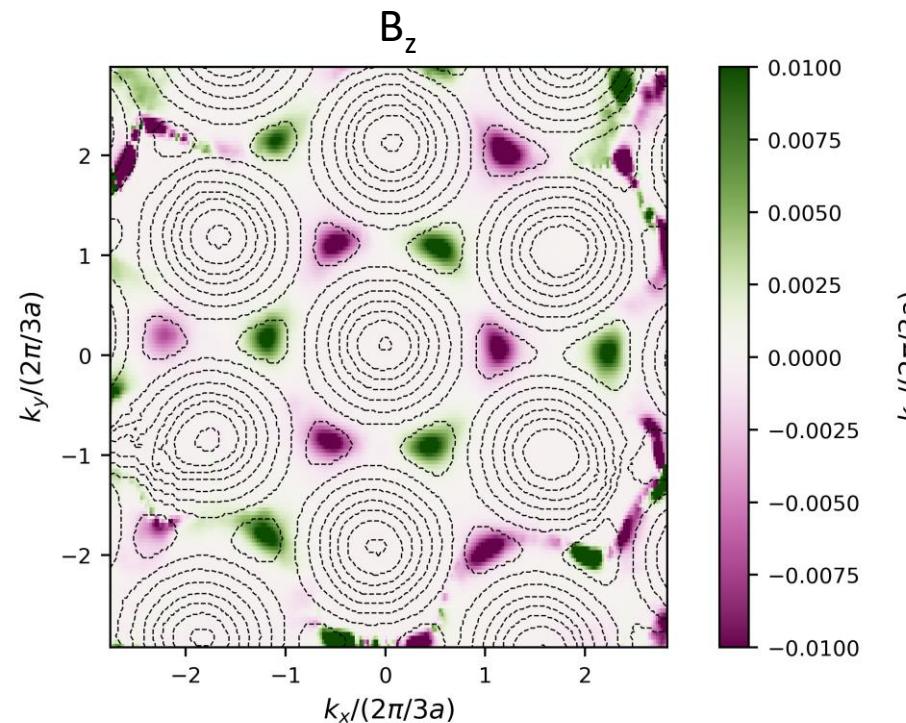


$$\vec{u}_k^n = \begin{bmatrix} \cos(\theta/2)e^{i\phi} \\ \sin(\theta/2) \end{bmatrix}$$

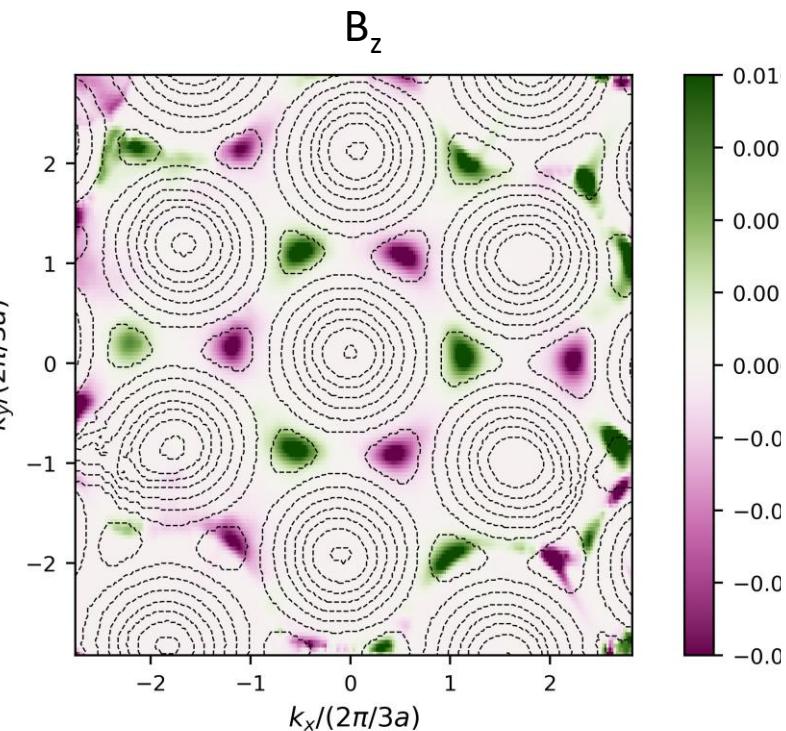
# Berry curvature computation

$$\vec{B}_n(\mathbf{k}) = \nabla_{\mathbf{k}} \times \vec{\mathcal{A}}_n(\mathbf{k}) = i \langle \nabla_{\mathbf{k}} u_n | \times | \nabla_{\mathbf{k}} u_n \rangle.$$

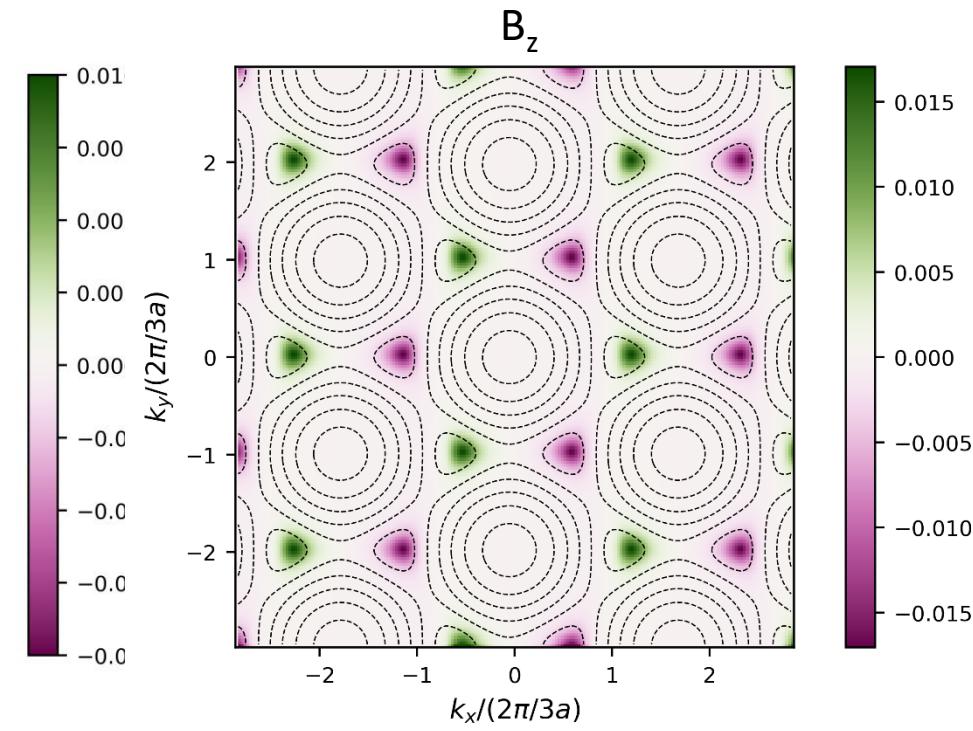
Lower band



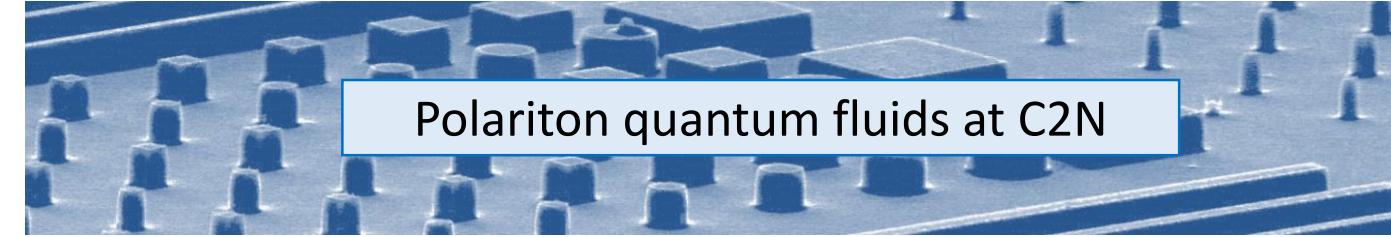
Upper band



Upper band (theory)

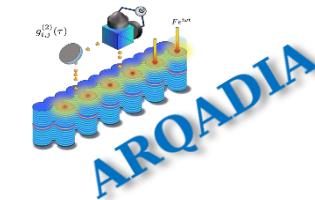


- Berry curvature of opposite sign in both valleys



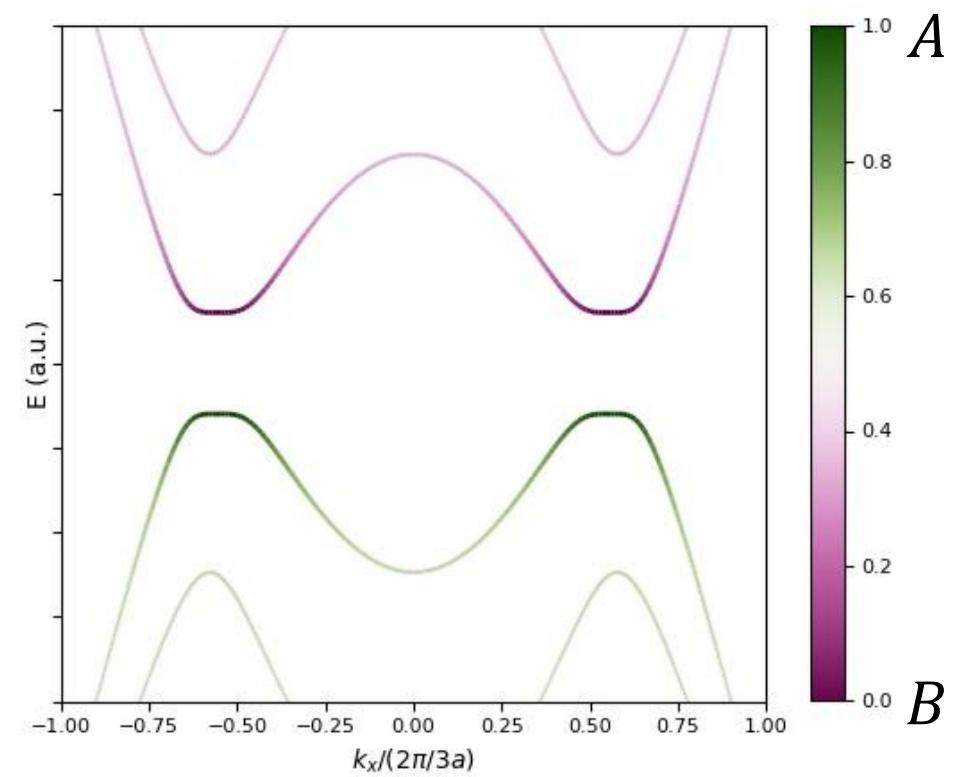
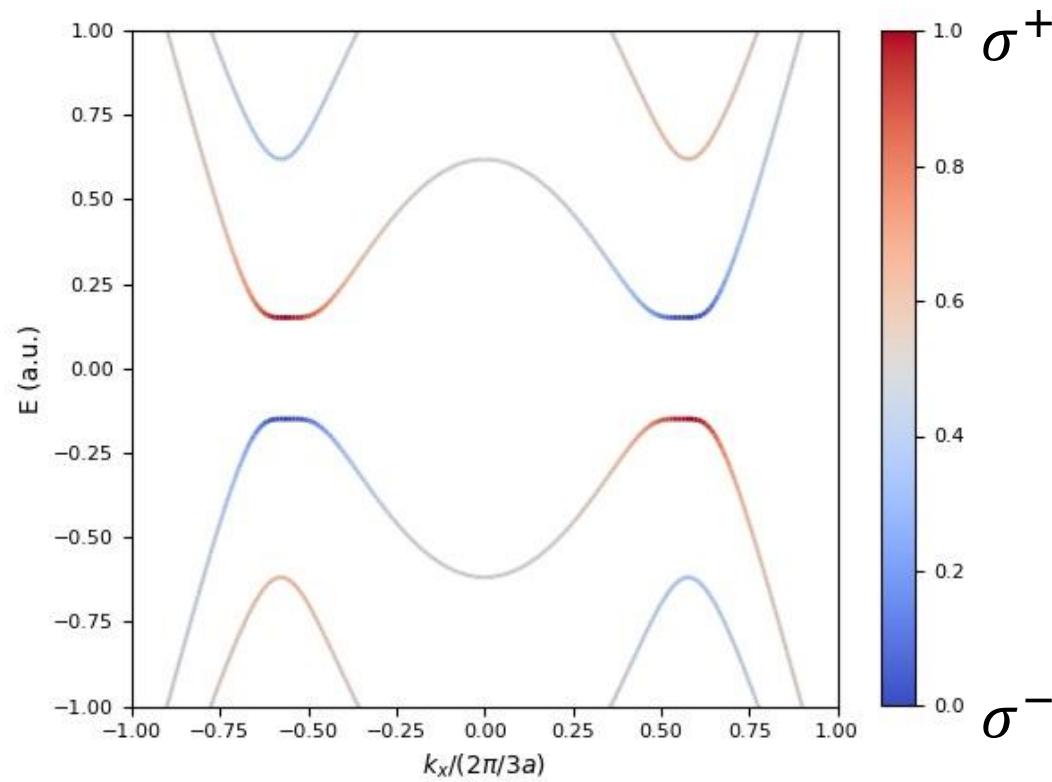
# III. Outlook: The $\mathbb{Z}$ -topological insulator

Resolving the band inversion in a 4-band system



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# Tunable spin-orbit coupling



Polariton Z Topological Insulator

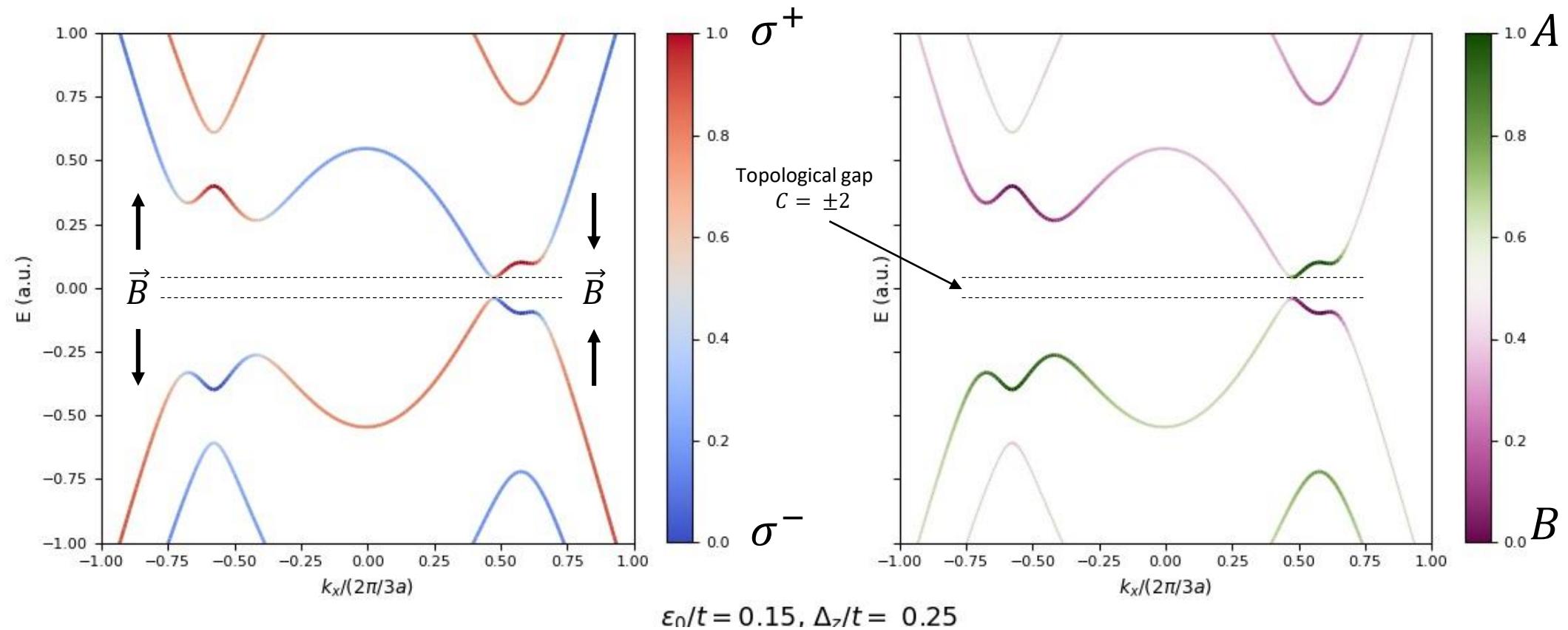
A. V. Nalitov, D. D. Solnyshkov, and G. Malpuech

Phys. Rev. Lett. **114**, 116401 (2015)

Klembt, S., Harder, T.H., Egorov, O.A. *et al.* Exciton-polariton topological insulator.

Nature **562**, 552–556 (2018)

# Optical Zeeman splitting



Polariton Z Topological Insulator

A. V. Nalitov, D. D. Solnyshkov, and G. Malpuech

Phys. Rev. Lett. **114**, 116401 (2015)

Klempt, S., Harder, T.H., Egorov, O.A. *et al.* Exciton-polariton topological insulator.

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Thanks you for listening !