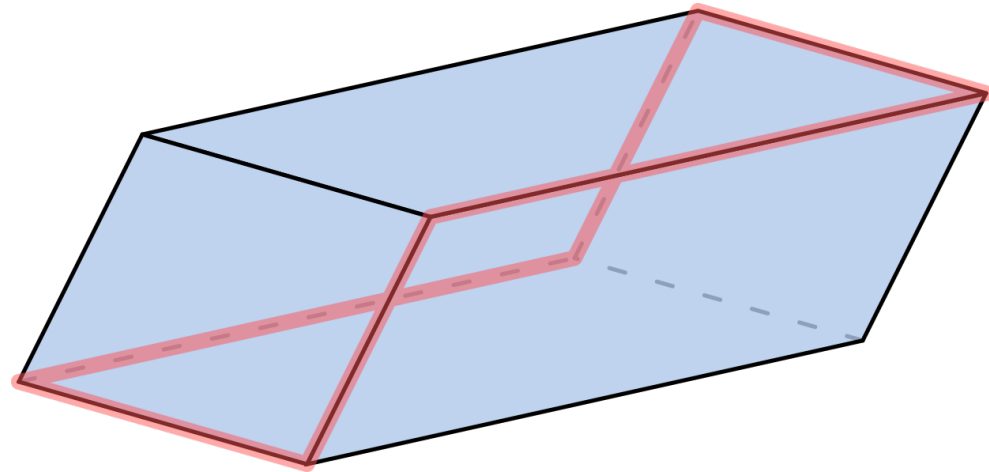
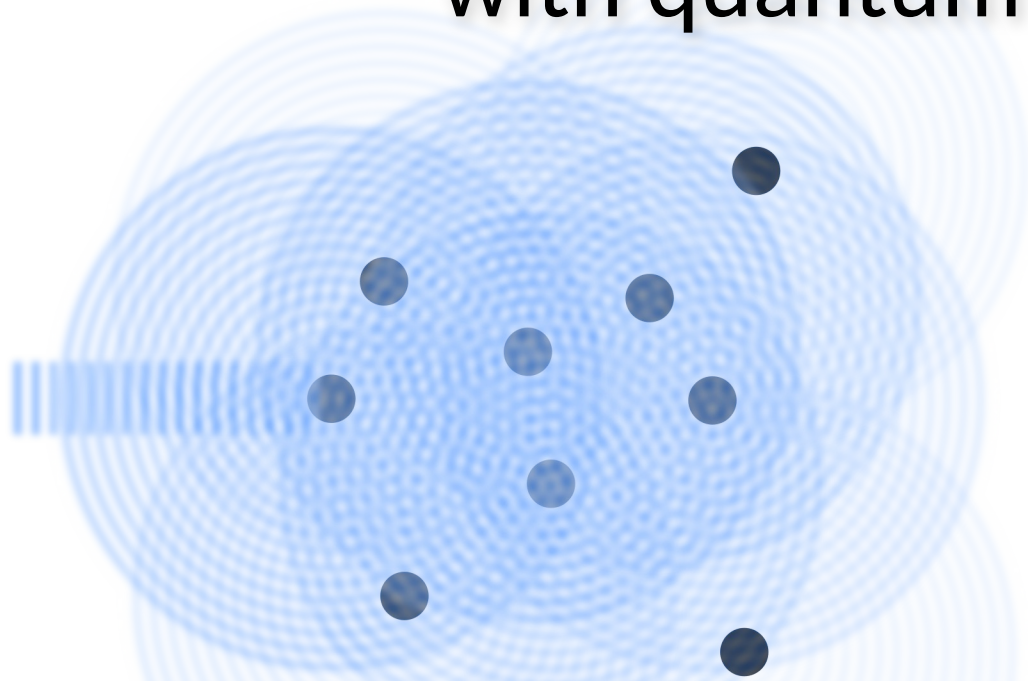


# Unveiling topological hinge states in $\text{Bi}_4\text{Br}_4$ with quantum interferences



*Jules Lefeuvre* – LPS (UP-Saclay) – MESO group

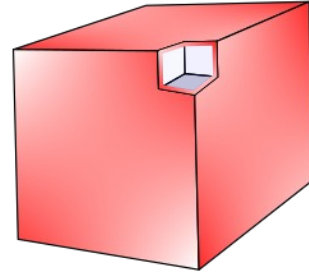
Supervised by R. Deblock, S. Guéron and H. Bouchiat

$\text{Bi}_4\text{Br}_4$  crystals from M. Kobayashi and T. Sasagawa, *Tokyo Institute of Technology*

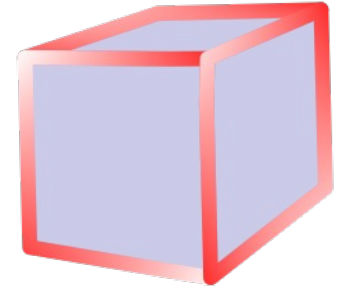
## Topological insulator :

Insulating bulk, conducting boundaries

### First-order Topological Insulators



### Second-order Topological Insulators



## Topological insulator :

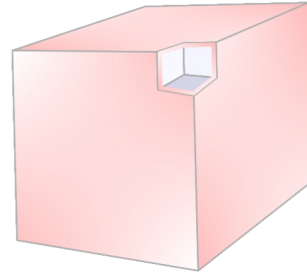
Insulating bulk, conducting boundaries

## 2<sup>nd</sup> order topological insulator :

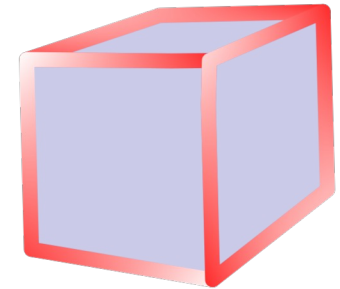
- Recent extension of the classification

→ Predicted in  $\text{Bi}_4\text{Br}_4$

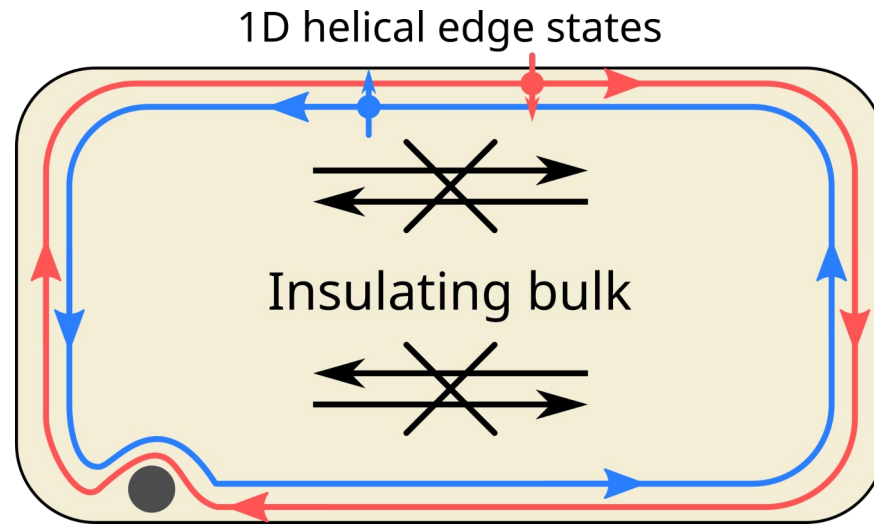
## First-order Topological Insulators



## Second-order Topological Insulators



# I) Topological protection



## Spin-momentum locking :

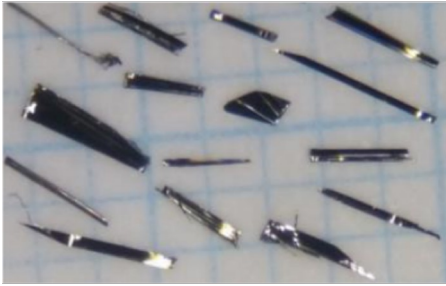
Opposite directions of propagation  
have opposite spins



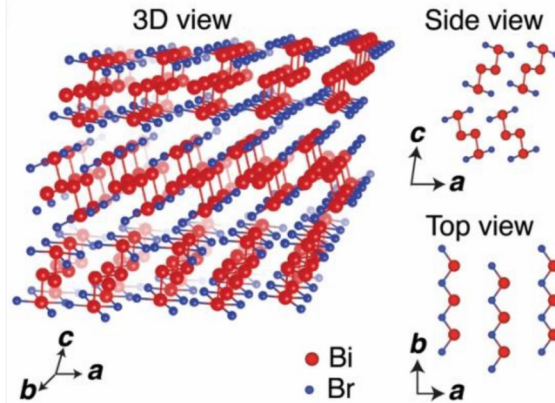
**Topological protection**  
(against non-magnetic disorder)

→ **Ballistic transport**

# 1) $\text{Bi}_4\text{Br}_4$ – A truly insulating TI ?



Noguchi, R. et al. (2021), *Nature Materials*, 20(4)



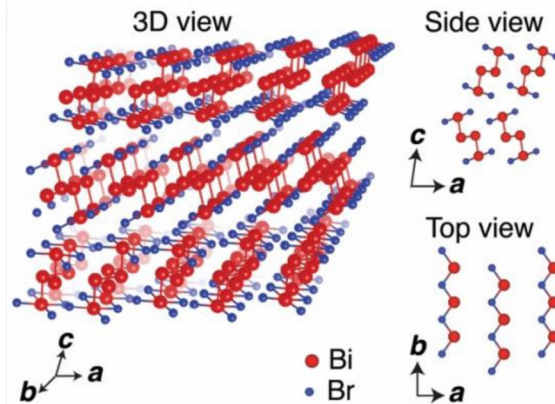
## Quasi-1D :

- Strong covalent bonds along one direction
- Weak (Van der Waals) bonds along the other two

# 1) $\text{Bi}_4\text{Br}_4$ – A truly insulating TI ?



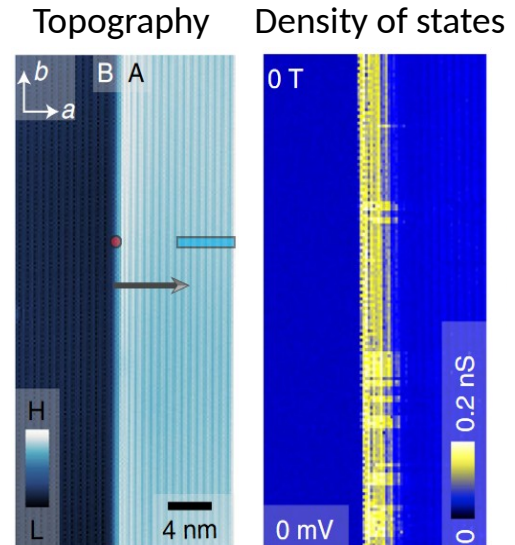
Noguchi, R. et al. (2021), *Nature Materials*, 20(4)



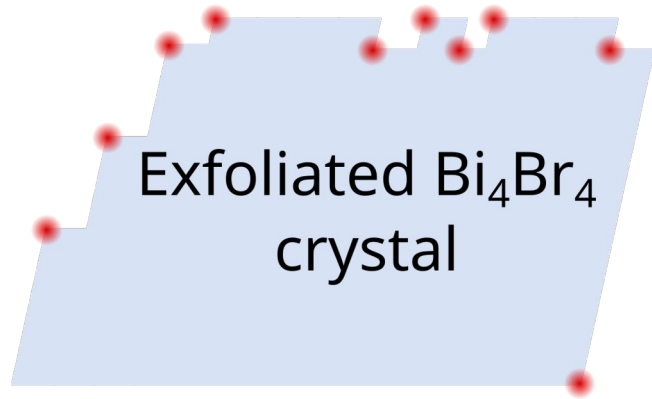
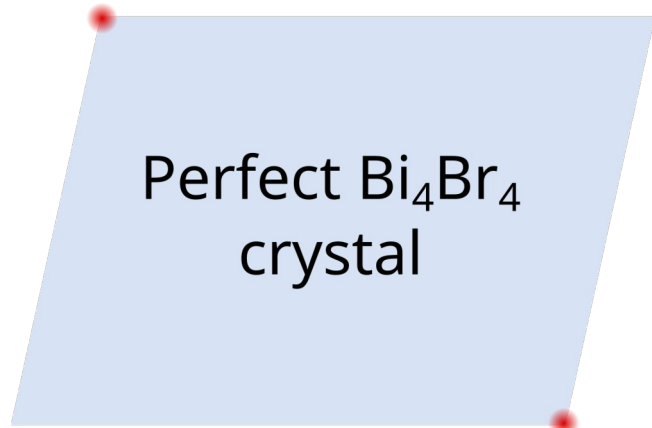
## Quasi-1D :

- Strong covalent bonds along one direction
- Weak (Van der Waals) bonds along the other two

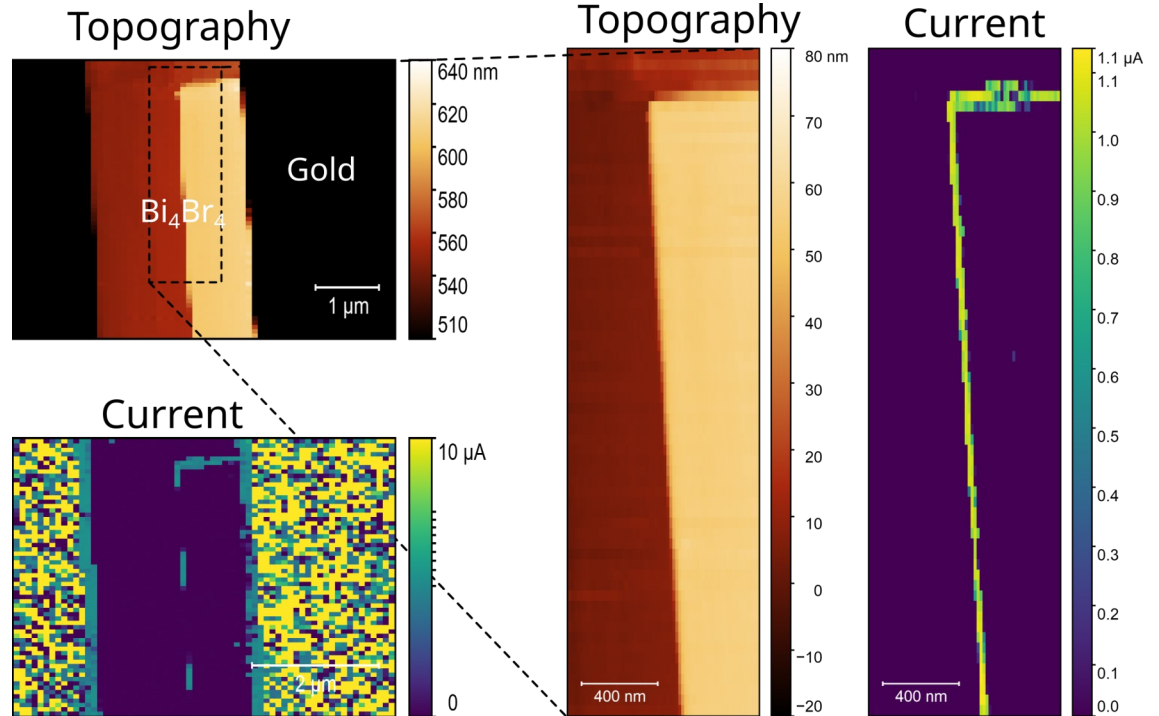
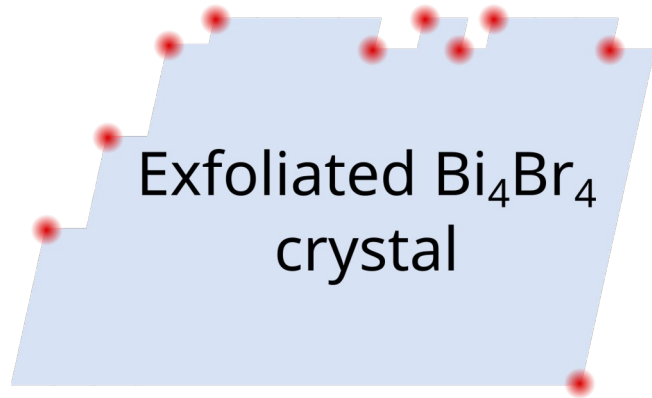
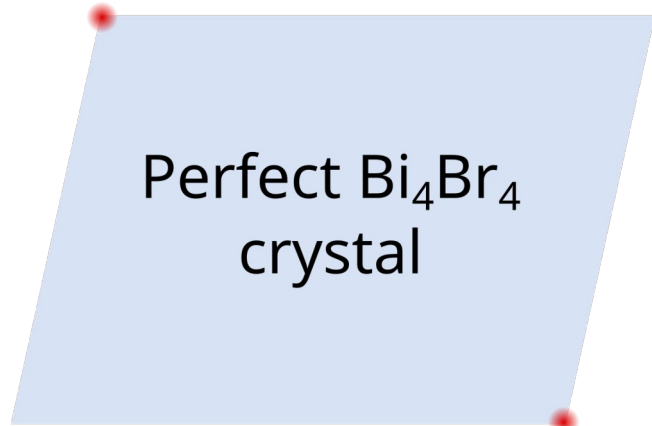
- Large spin-orbit gap (230 meV)
- Evidence of the topological states in ARPES and STM
- Topological states can survive up to **room temperature**



Shumiya, N. et al., 2022, *Nat. Mater.*



# I) Conducting hinges

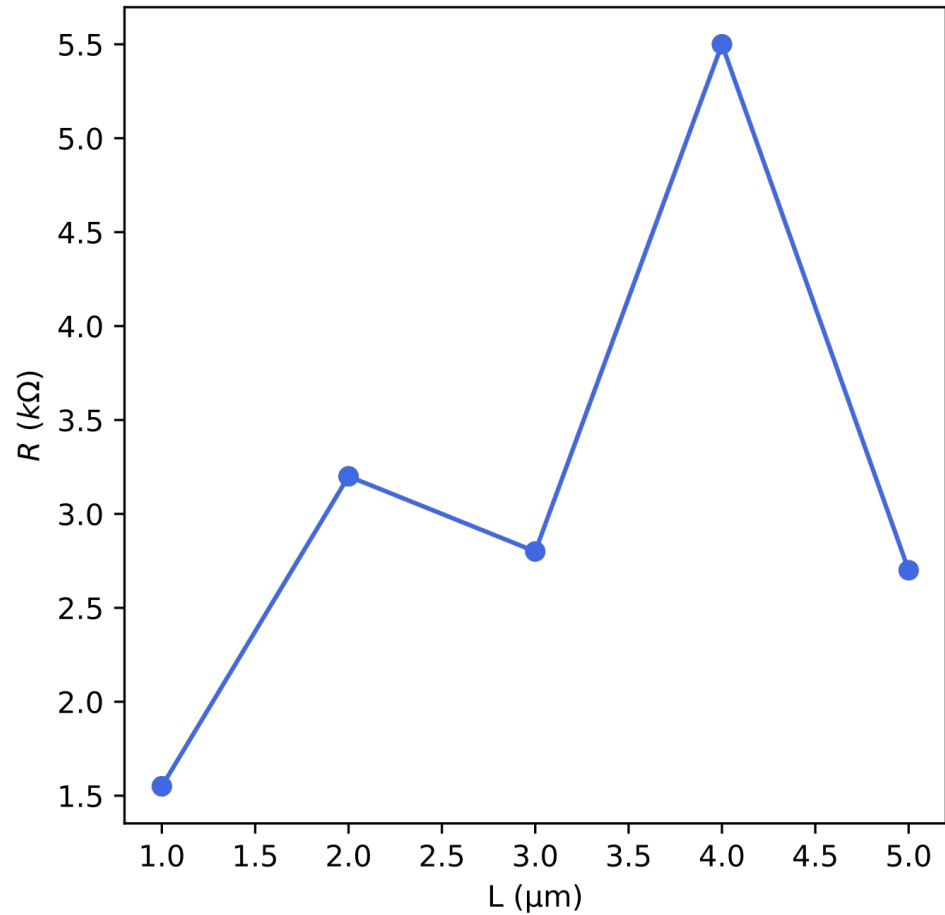


**Edge conduction** revealed by our  
conducting AFM measurements at 300 K

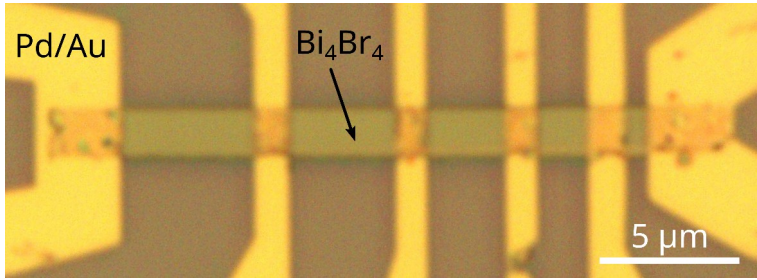


**What about its transport properties ?**

## II) Scaling of the resistance



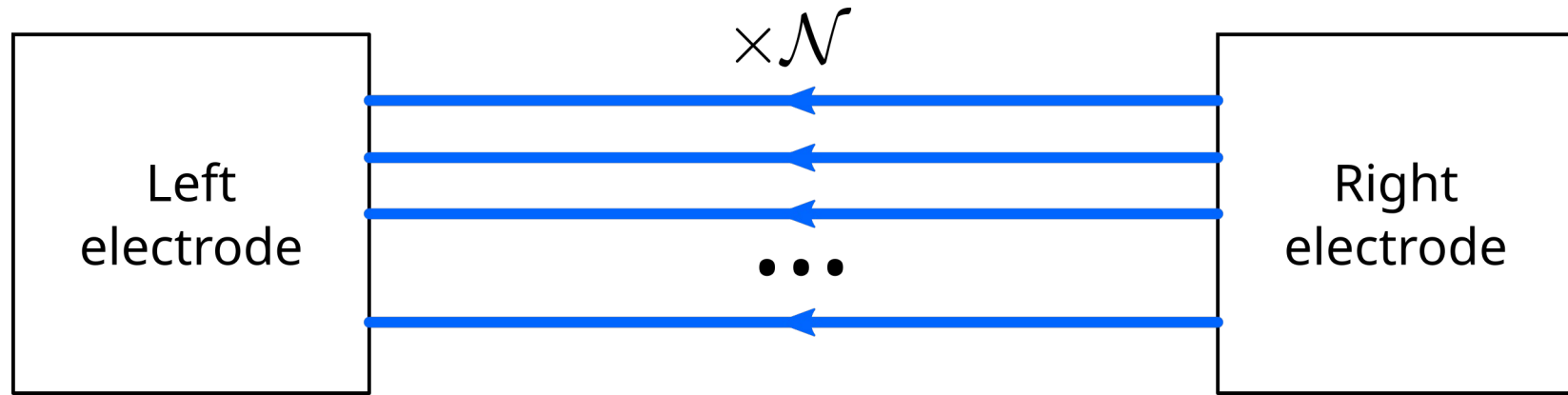
5 μm - 4 μm - 3 μm - 2 μm - 1 μm



~~$R = \frac{\rho L}{S}$~~

Diffusive conductors

Hints at **ballistic transport**

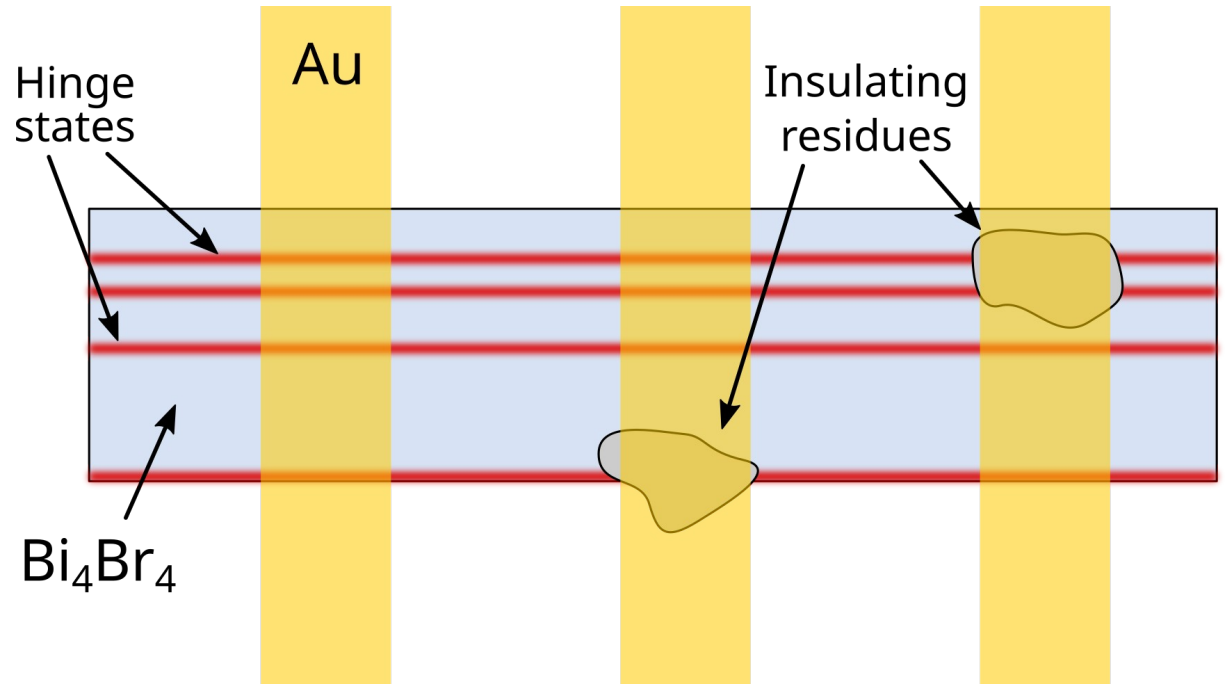
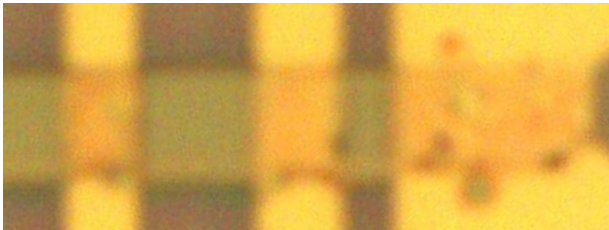
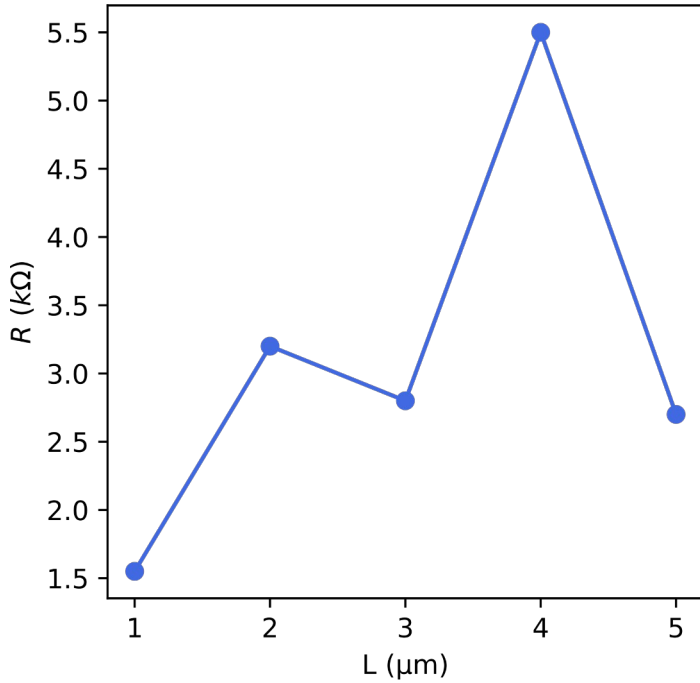


Landauer-Büttiker formula :

$$R = \frac{1}{\mathcal{N}} \times \frac{h}{e^2} \approx \frac{1}{\mathcal{N}} \times 26 \text{ k}\Omega$$

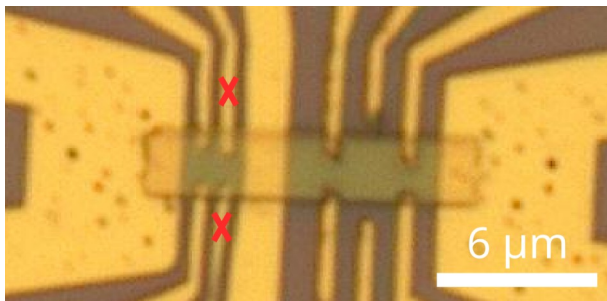
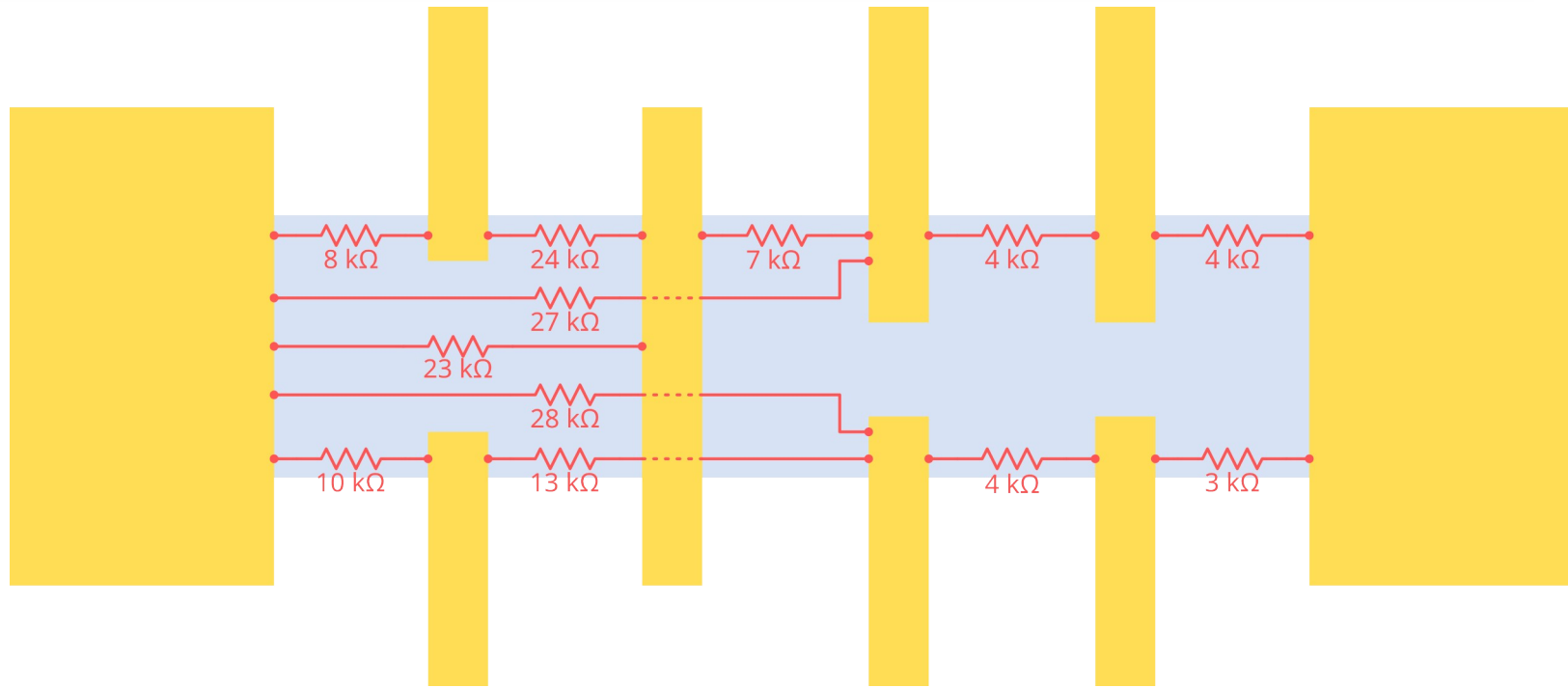
This is a **contact resistance**

## II) Edge state configuration



Number of contacted edge states can vary between contact pairs

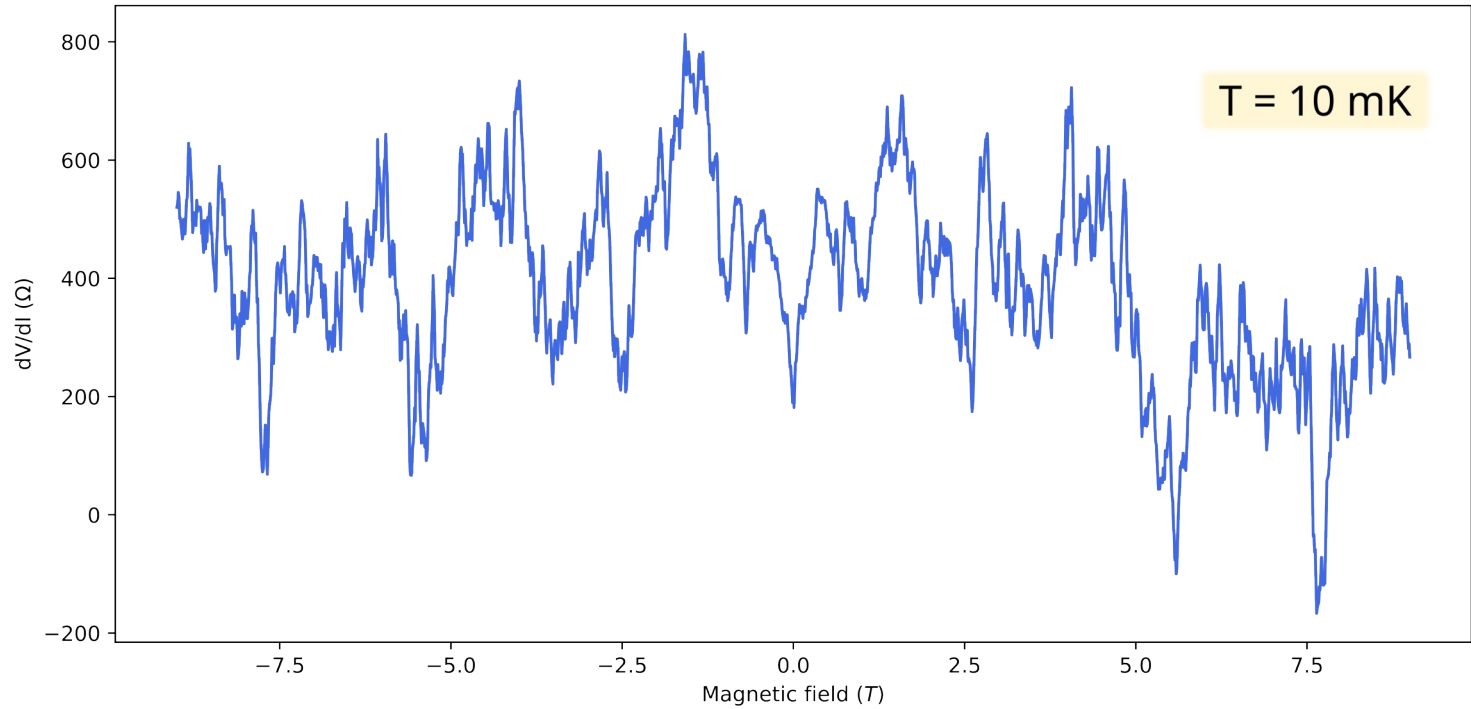
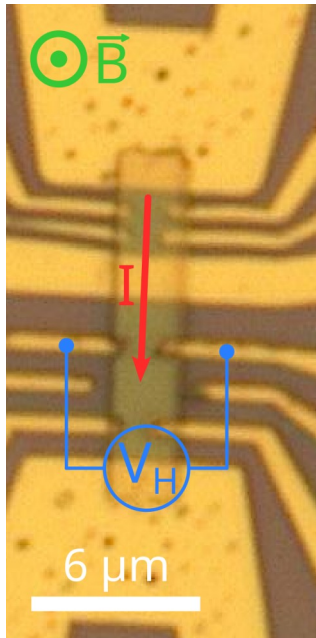
## II) Resistance network



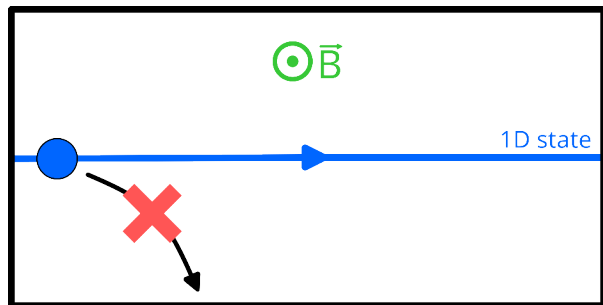
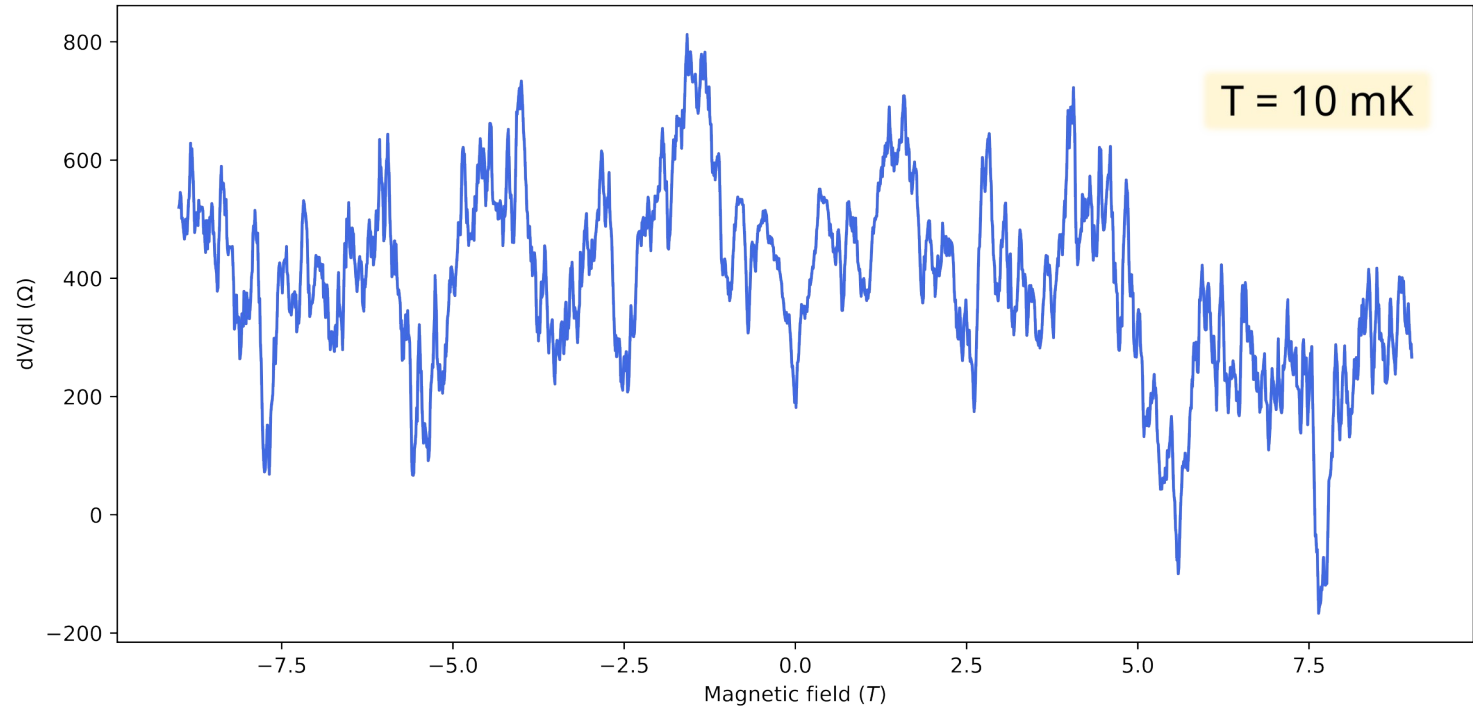
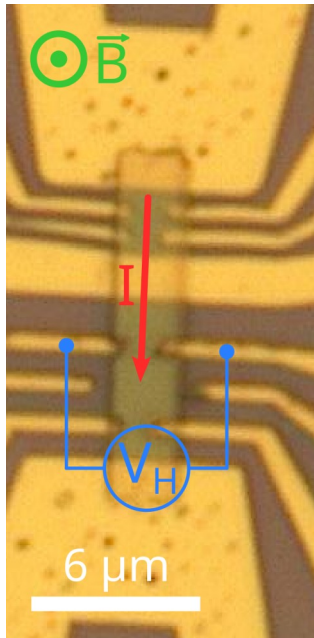
### Highly anisotropic transport

Supports the 1D nature of transport along hinge states

## II) Hall effect



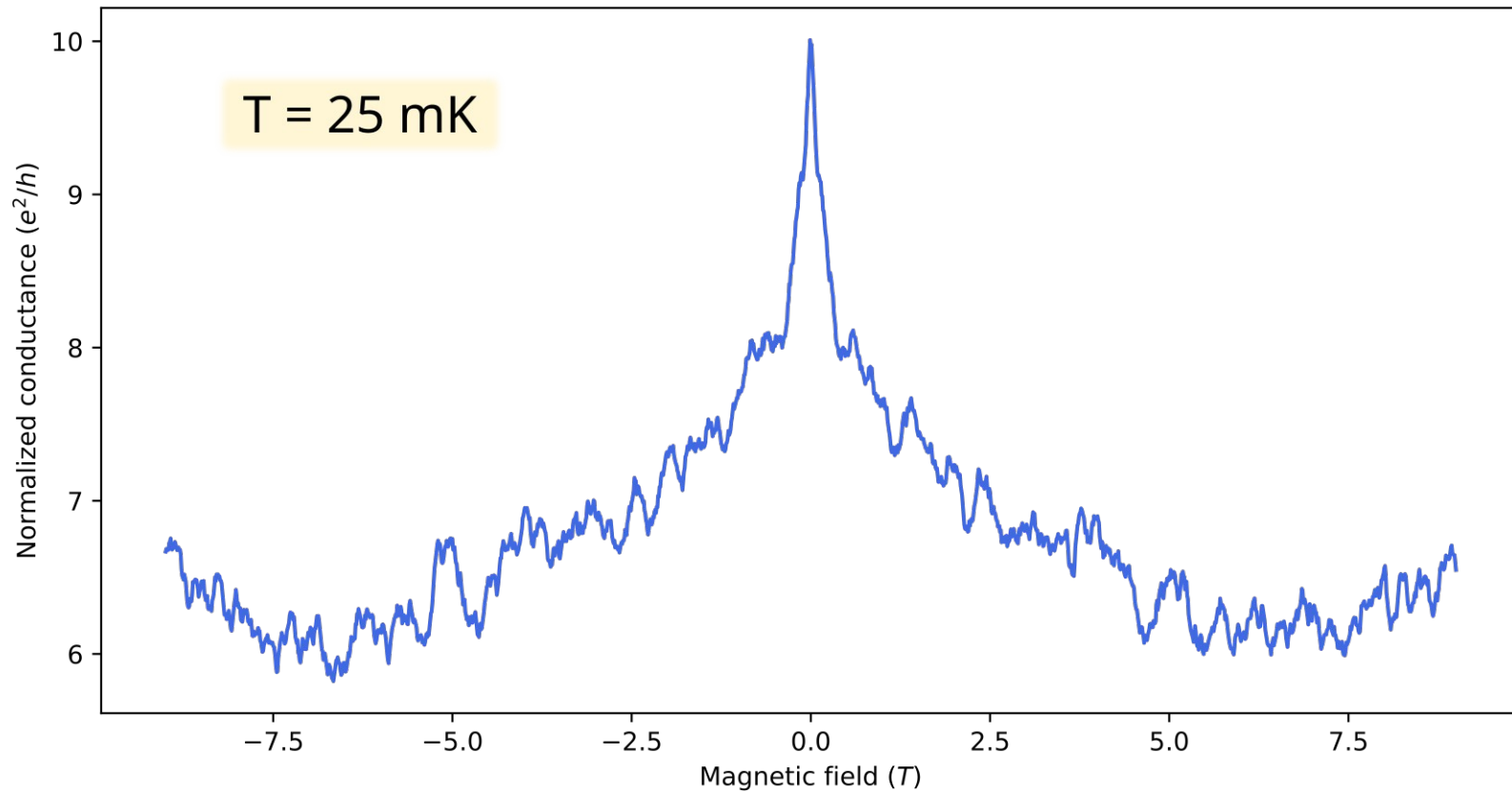
## II) Hall effect



**No Hall effect**

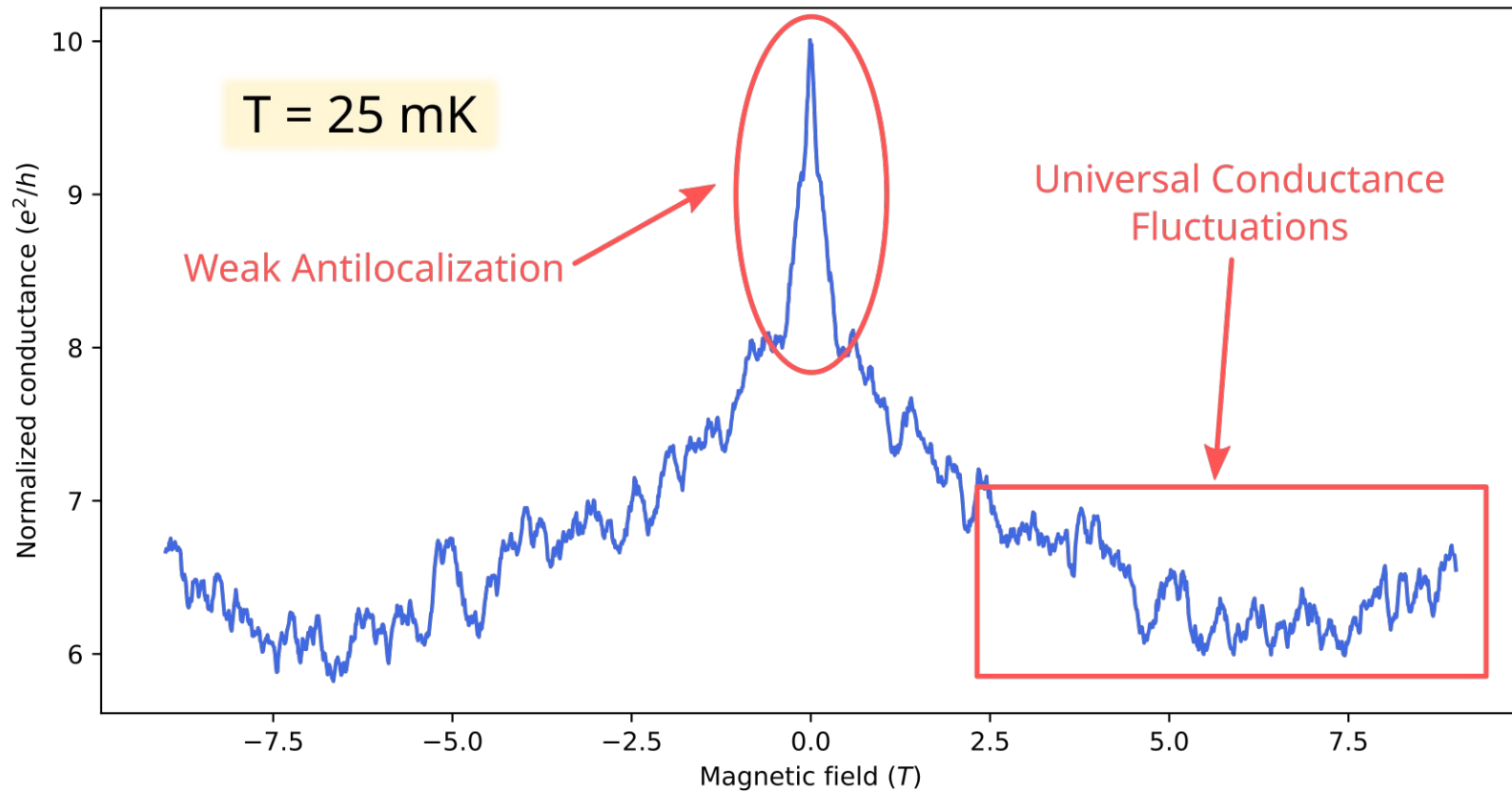
Further evidence of conduction by 1D hinge states

### III) Quantum interferences

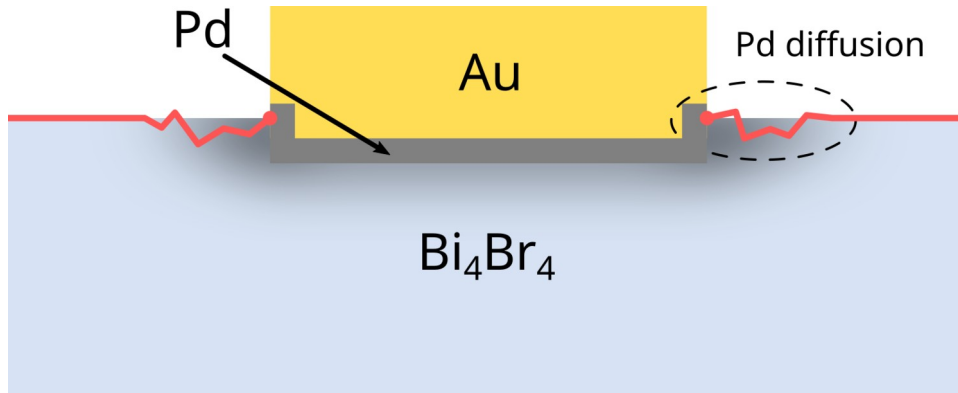




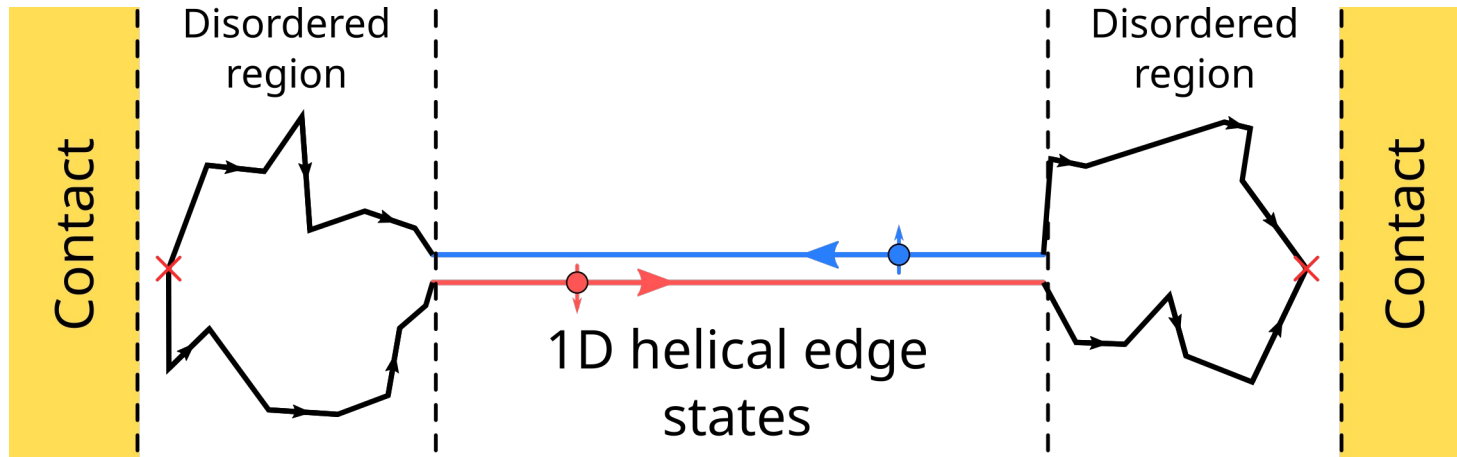
### III) Quantum interferences



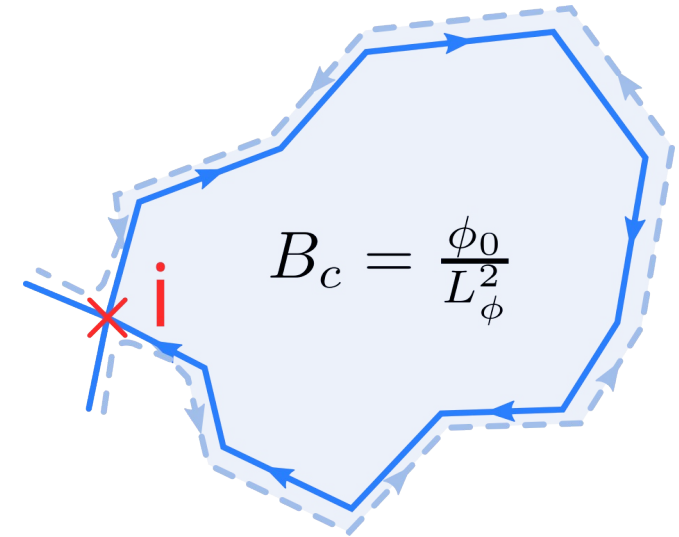
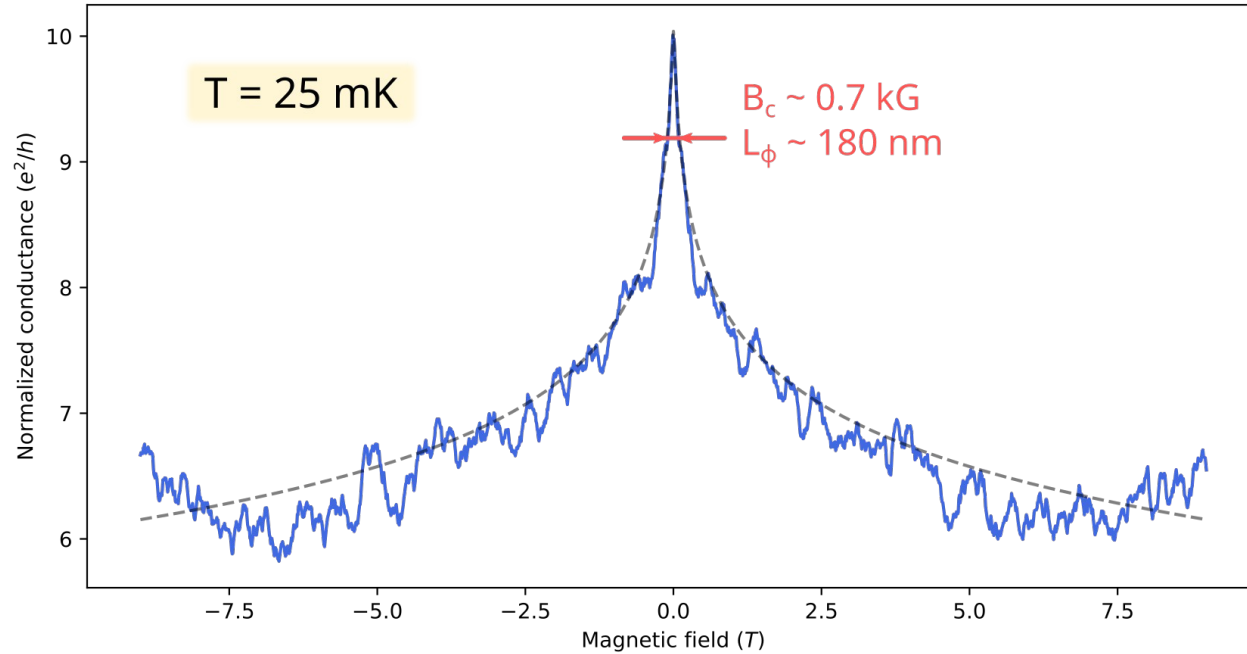
### III) Refined model for the contacts



Interdiffusion of Pd inside Bi<sub>4</sub>Br<sub>4</sub> creates a small disordered region near the contacts  
→ Quantum interferences at low T



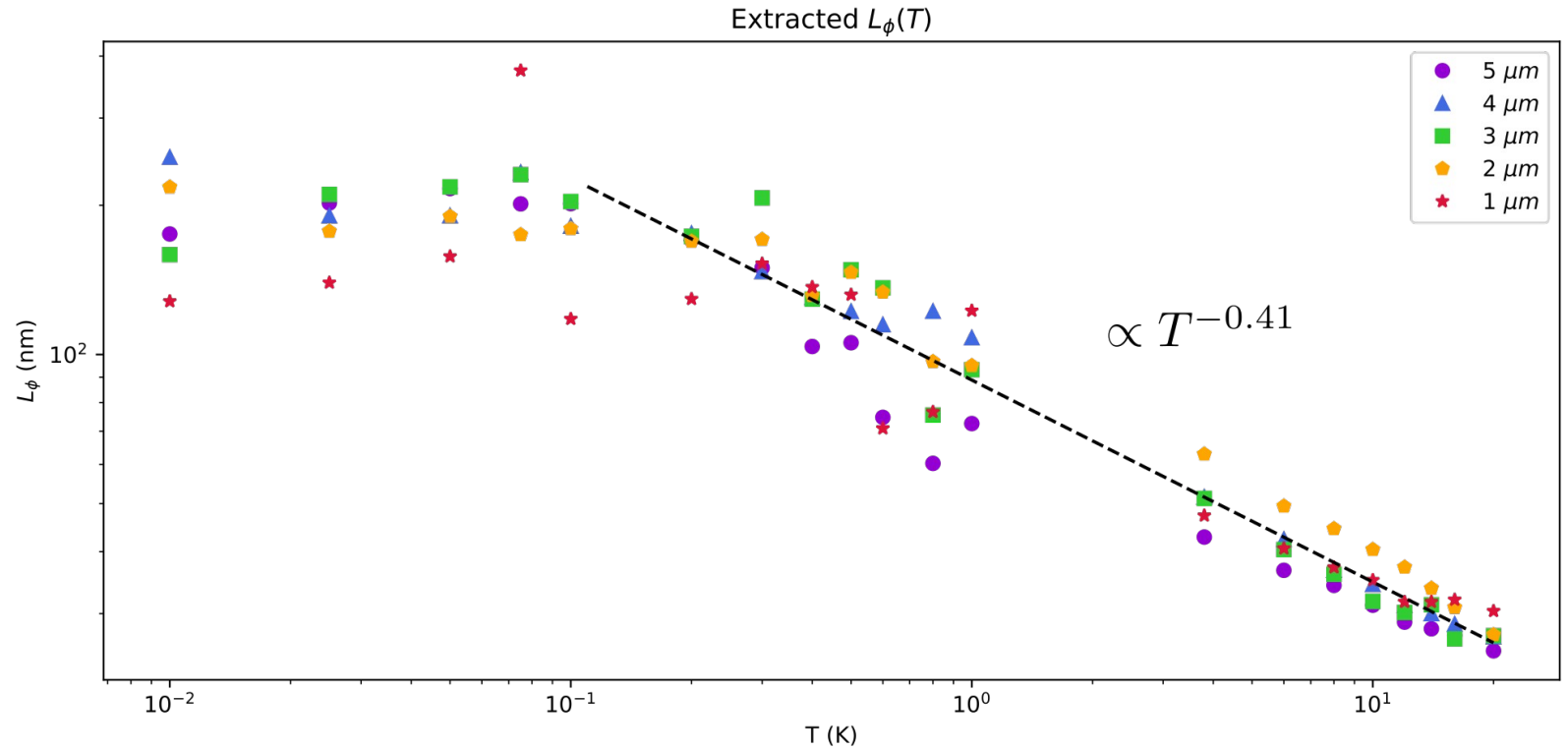
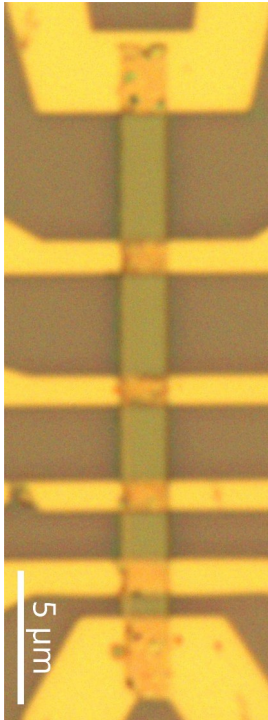
### III) Weak Antilocalization



Conductance peak  $\rightarrow$  **Weak Antilocalization**  
Indicates strong spin-orbit coupling

**Small  $L_\phi$**   
Reasonable considering  
interdiffusion hypothesis

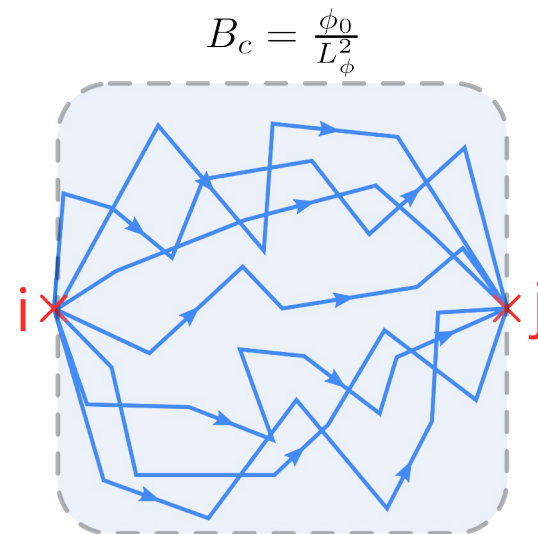
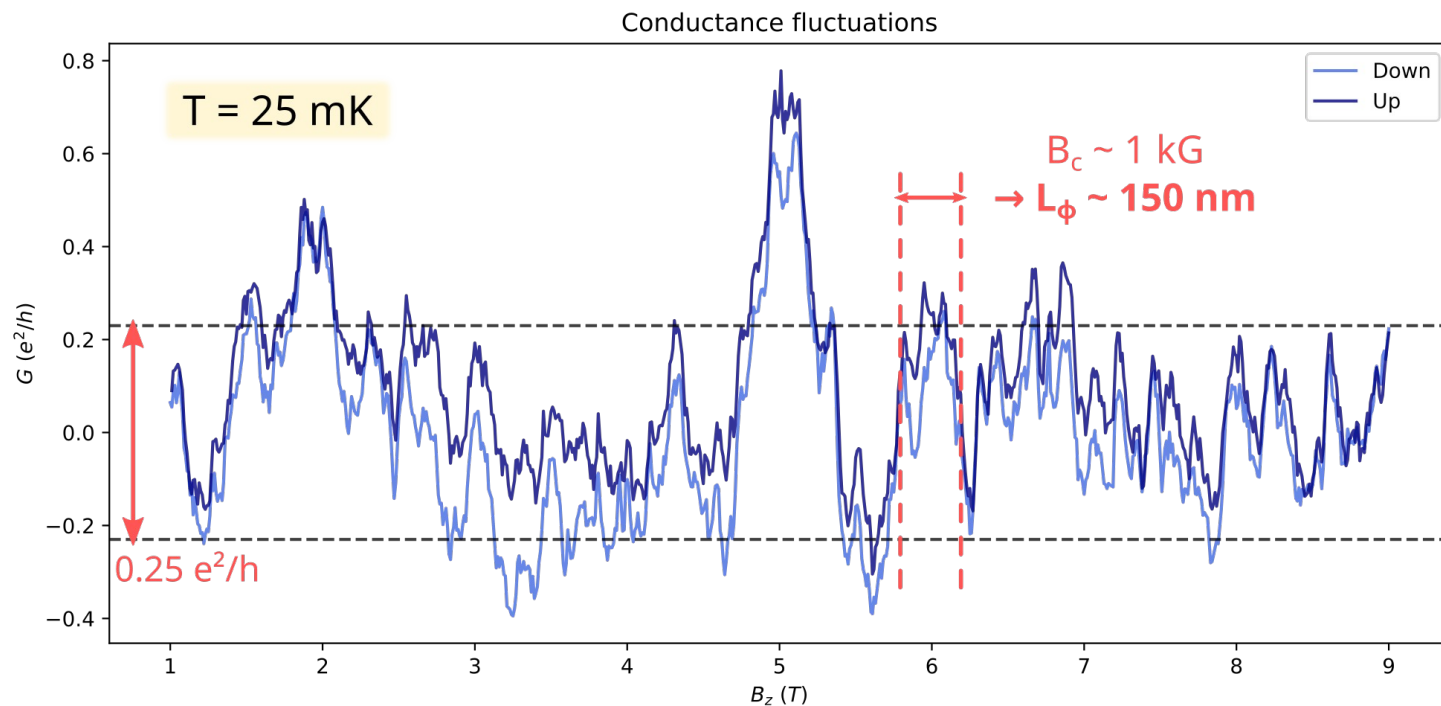
### III) Weak Antilocalization



All sections exhibit very similar behavior in  $L_\phi$

$\sim T^{-1/2}$  power law  
Dephasing by  $e^- - e^-$  interactions

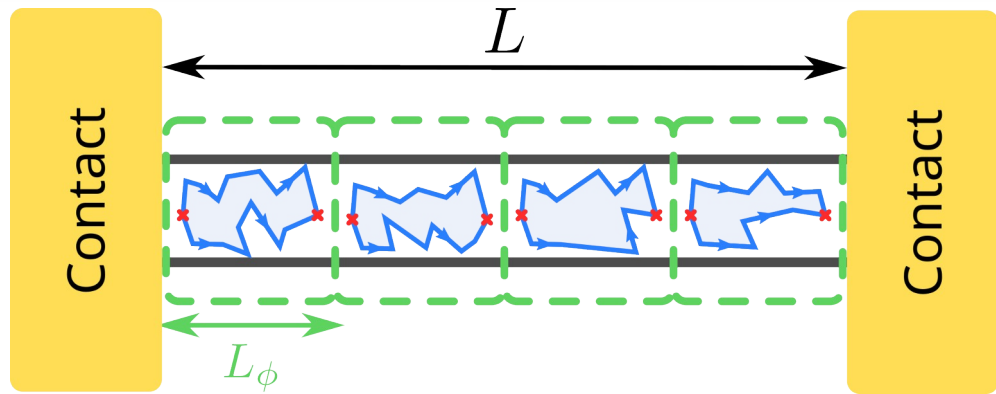
# III) Universal Conductance Fluctuations



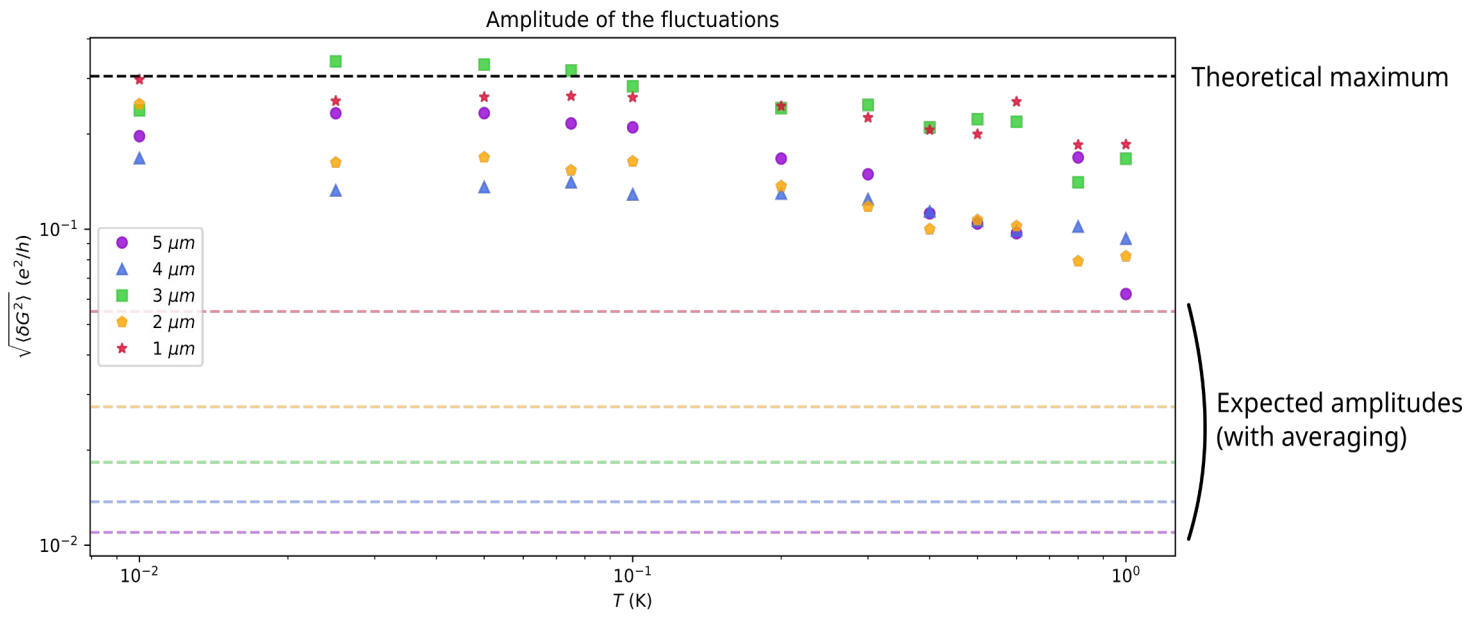
Confirms the  $L_\phi$  extracted from Weak Antilocalization

Strong fluctuations

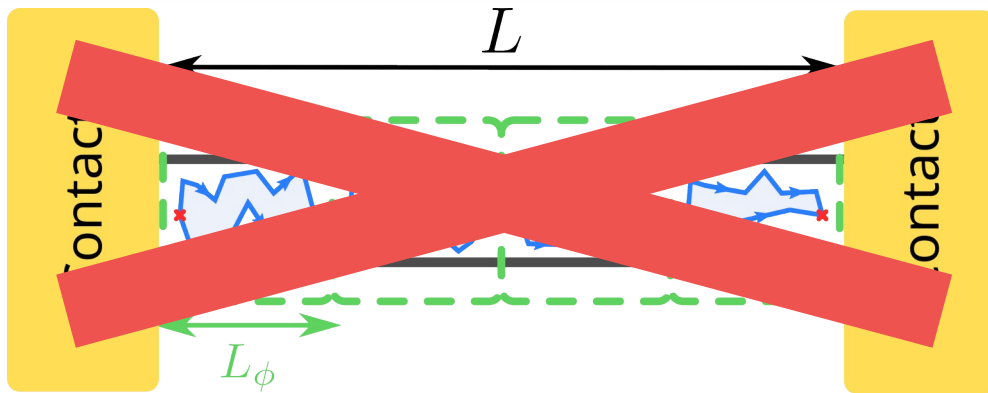
### III) Self-averaging ?



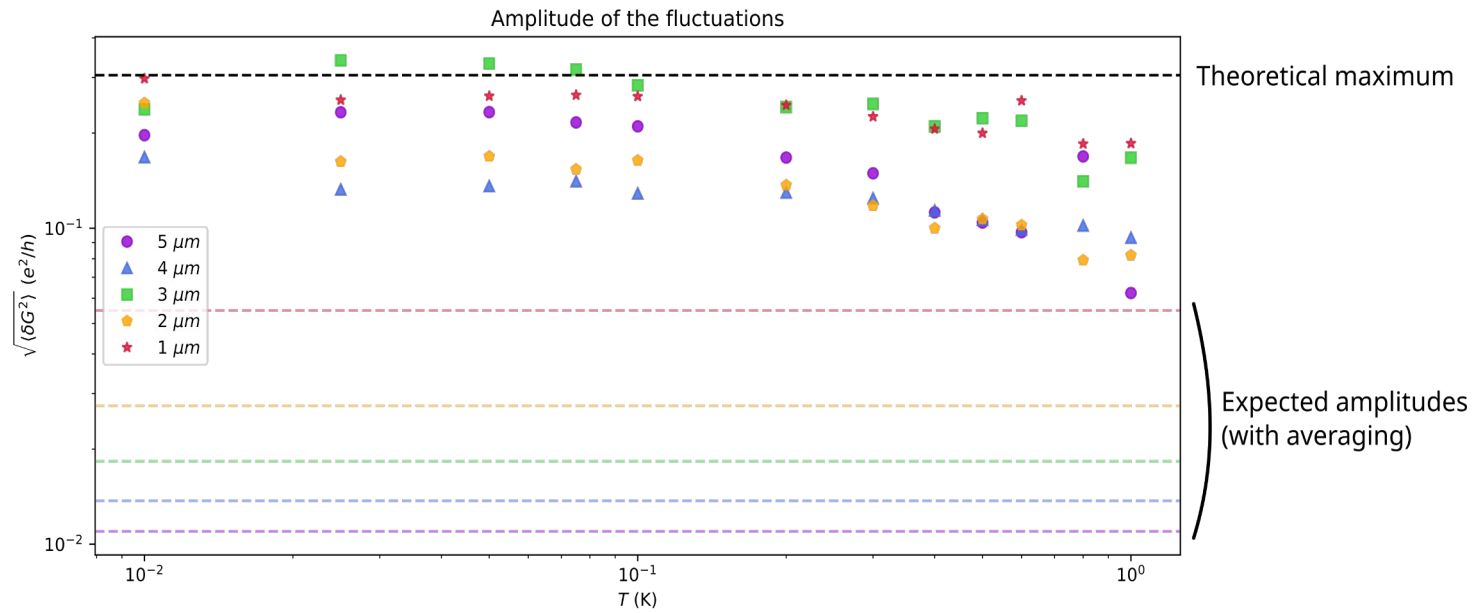
$$\sqrt{\langle \delta G^2 \rangle} \propto \left( \frac{L_\phi}{L} \right)^{2 - \frac{d}{2}}$$



### III) No self-averaging

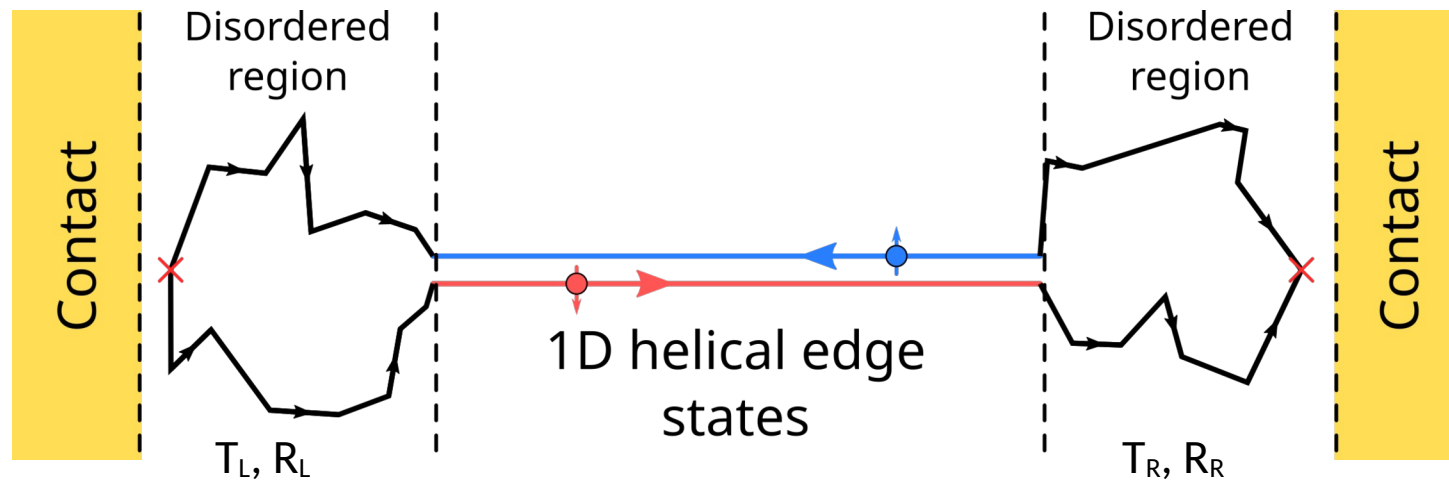


$$\sqrt{\langle \delta G^2 \rangle} \propto \left( \frac{L_\phi}{L} \right)^{2 - \frac{d}{2}}$$



Fluctuations are  
**much larger than**  
expected  
**→ No self-averaging**

### III) Transmission modulated by interferences



$T_{R,L}, R_{R,L}$ : Transmission / reflection coefficient of the left / right disordered region

Small disordered region ( $L_{\text{Pd/BiBr}} \sim L_\phi$ ) produces fluctuations of the global conductance of **1D hinge states**

$$G_{1\text{D}} = \frac{e^2}{h} \frac{T_L T_R}{1 - R_L R_R}$$

Depend on B !



- Strongly anisotropic transport suggests the existence of **1D channels**
- General lack of length dependence provide good evidence for the **ballisticity** of the 1D hinge states

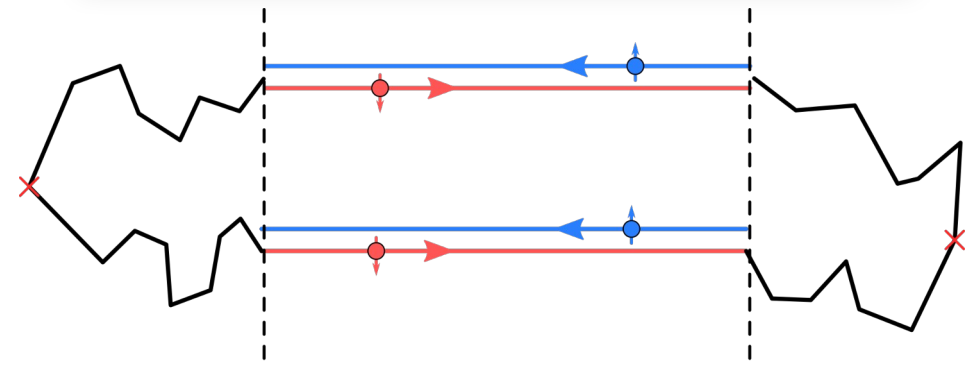
- Strongly anisotropic transport suggests the existence of **1D channels**
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→ **Bi<sub>4</sub>Br<sub>4</sub>** appears as an excellent material for the fundamental study of 1D topological states

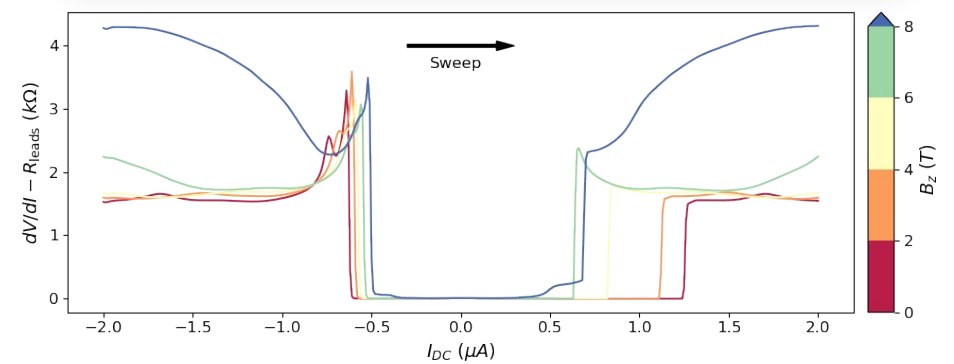
- Strongly anisotropic transport suggests the existence of **1D channels**
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→ **Bi<sub>4</sub>Br<sub>4</sub>** appears as an excellent material for the fundamental study of 1D topological states

## Aharonov-Bohm oscillations ?

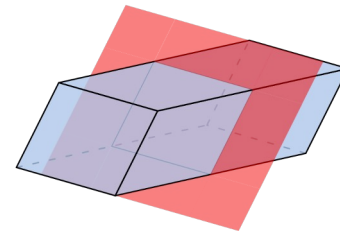
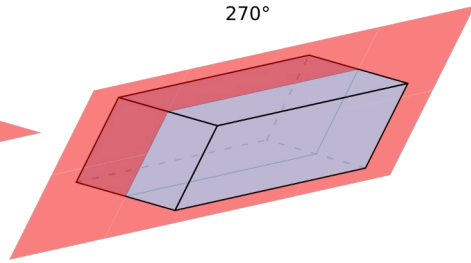
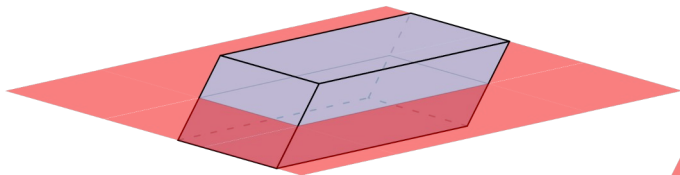
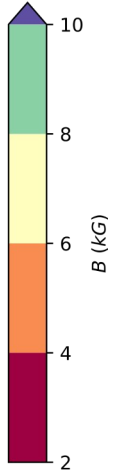
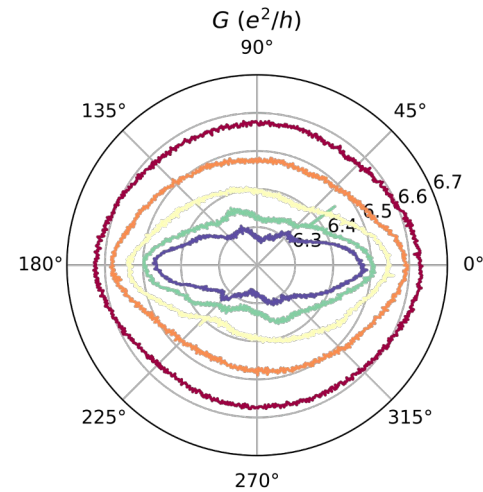
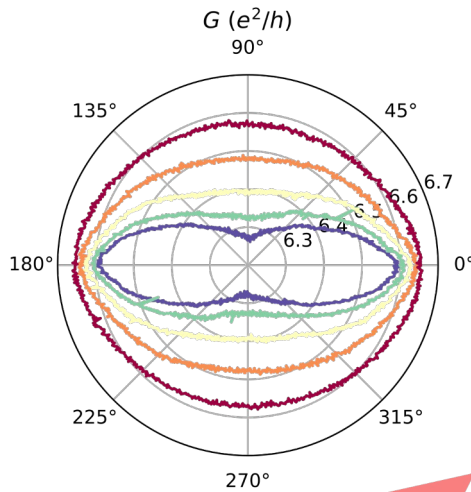
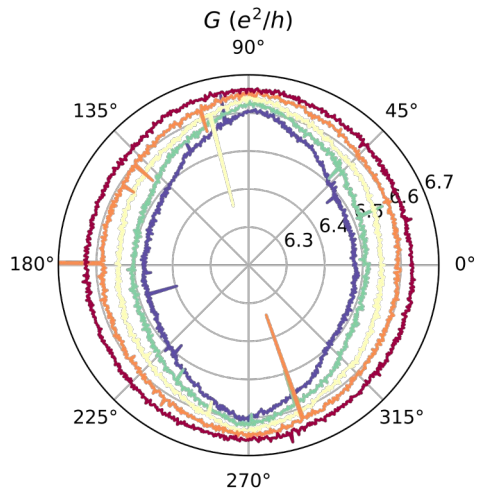


## Interplay with superconductivity ?



**Thank you !**

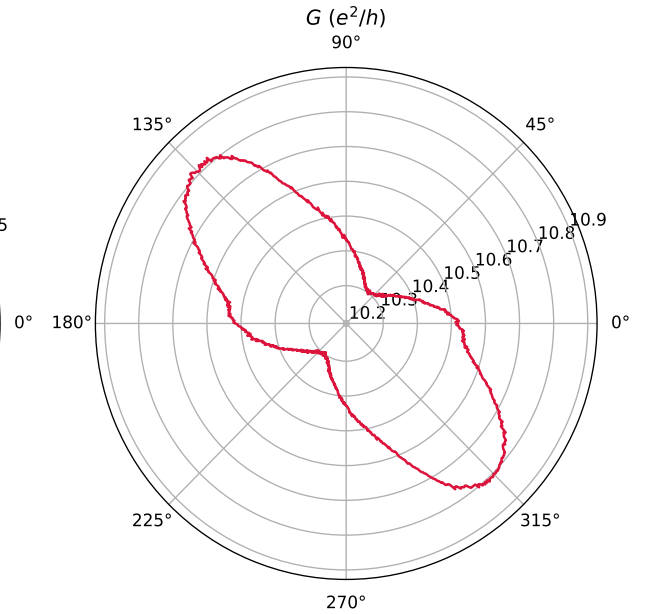
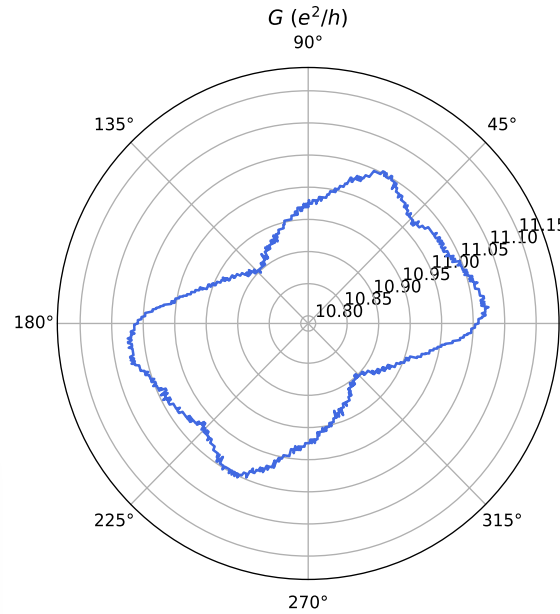
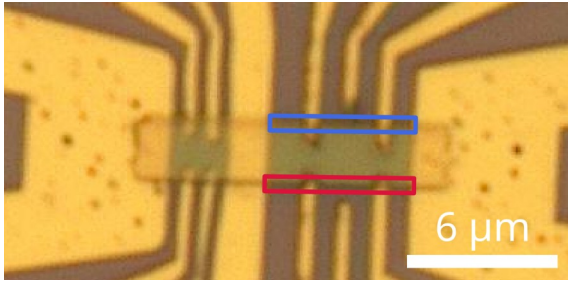
# A1) Field anisotropy



Diffusion paths do not explore the thickness of the flake → **2D diffusion**

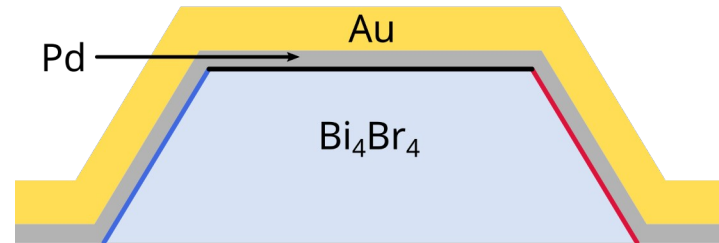
Two smaller lobes in different directions...

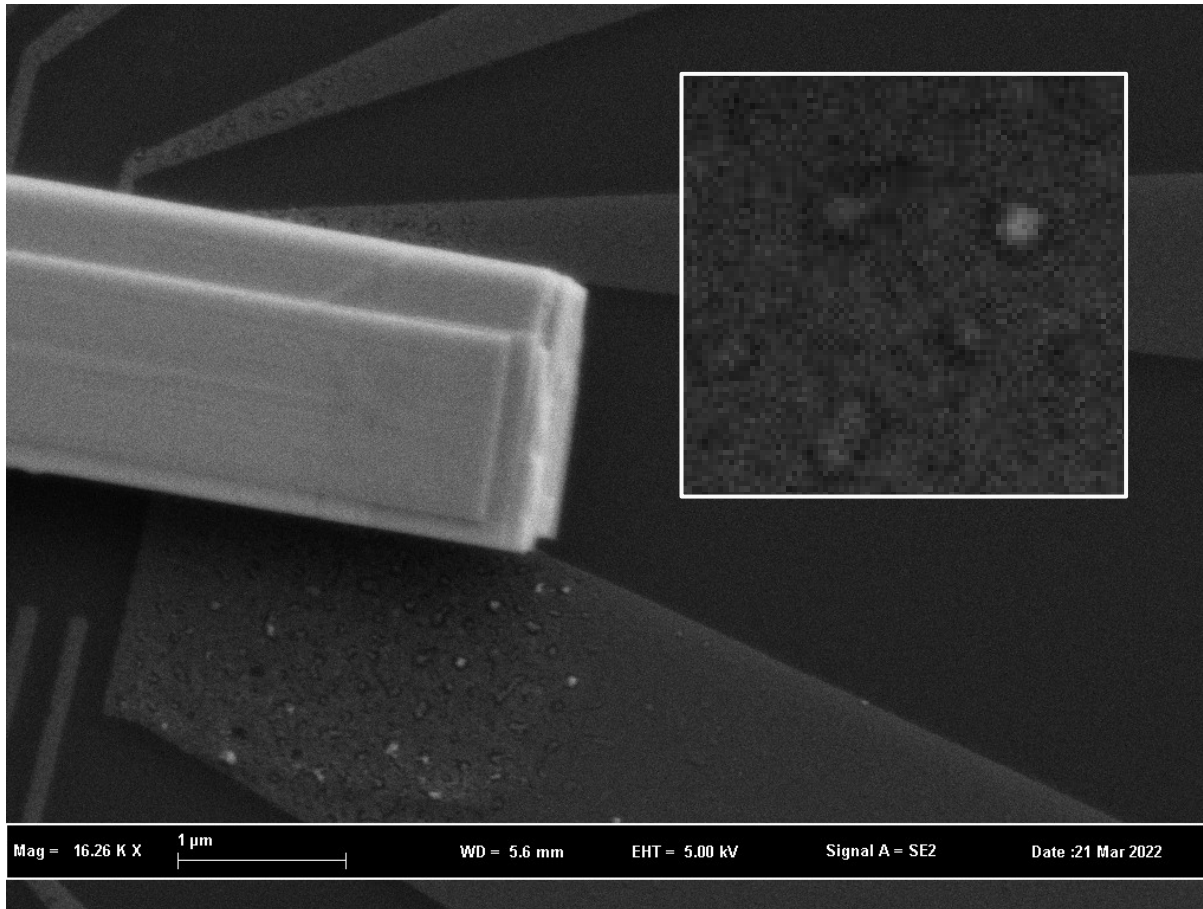
# A1) Field anisotropy



Direction of the lobes = slope of the side contacts

→ Confirms that the disordered region originates from the contacts



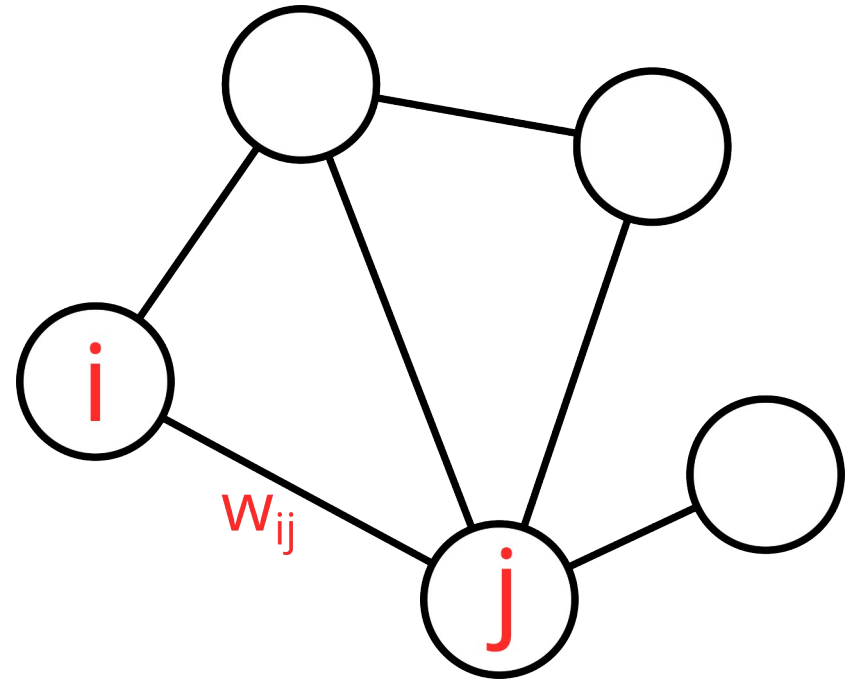


EDX measurement of the spots show **Bi** and **Pd** in their composition

Measuring the set of all 2-wire resistances  
(= the resistance distances) allow to recover  
the resistance network of the sample

Resistance distance matrix:  $\mathcal{R}_{ij}$

Laplacian matrix:  $\mathcal{L}_{ij} = \frac{-1}{w_{ij}}$  if  $i \neq j$

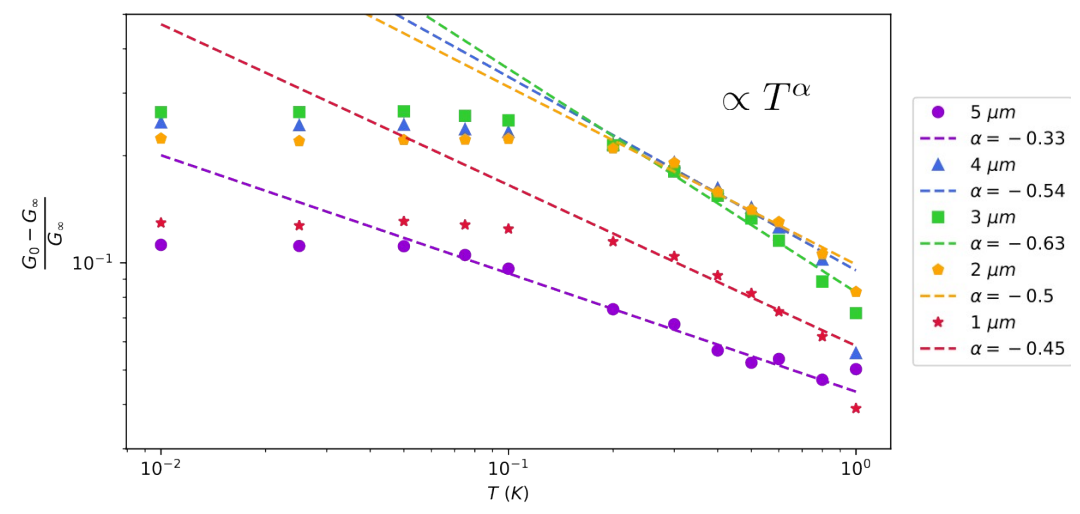
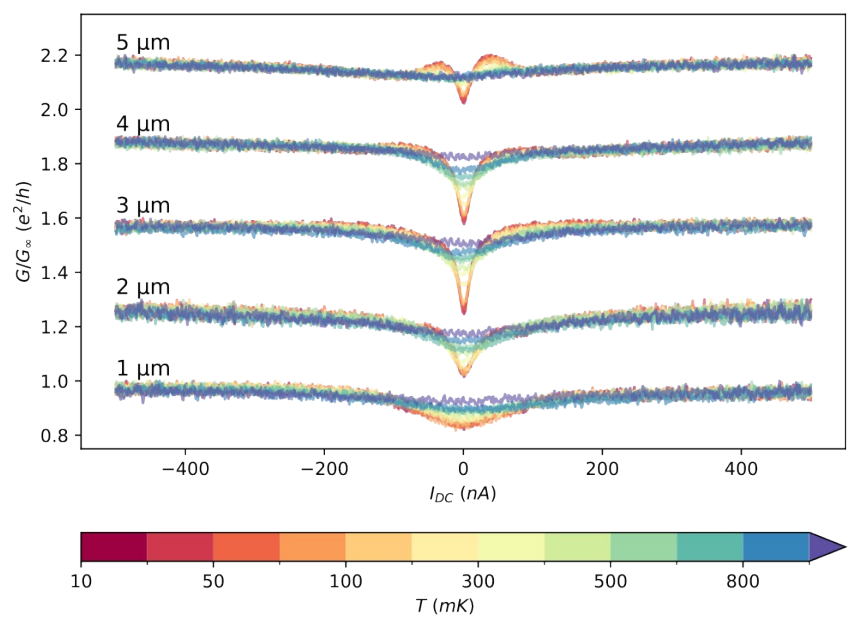


$$\mathcal{L} = 2\mathcal{R}^{-1} + \frac{2}{\mu^T \mathcal{R} \mu} \mu \mu^T$$

with  $\mu_i = 2 - \sum_{j \in \mathcal{N}(i)} \frac{R_{ij}}{w_{ij}}$



# A4) Dynamical Coulomb Blockade vs. Luttinger Liquid



$$E_{\text{Th}} \in [3.8; 20] \text{ K}$$

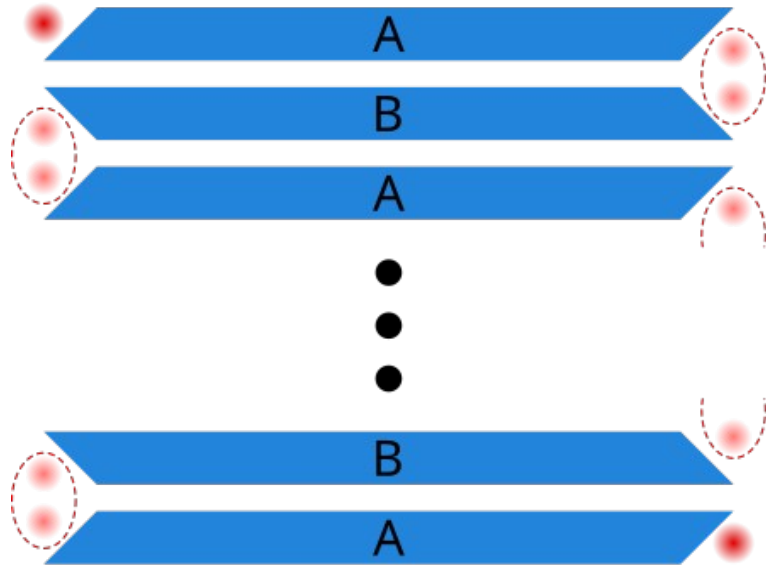
For LL power law,  $k_B T > E_{\text{th}}$   
**→ Incompatible with LL**

For DCB :

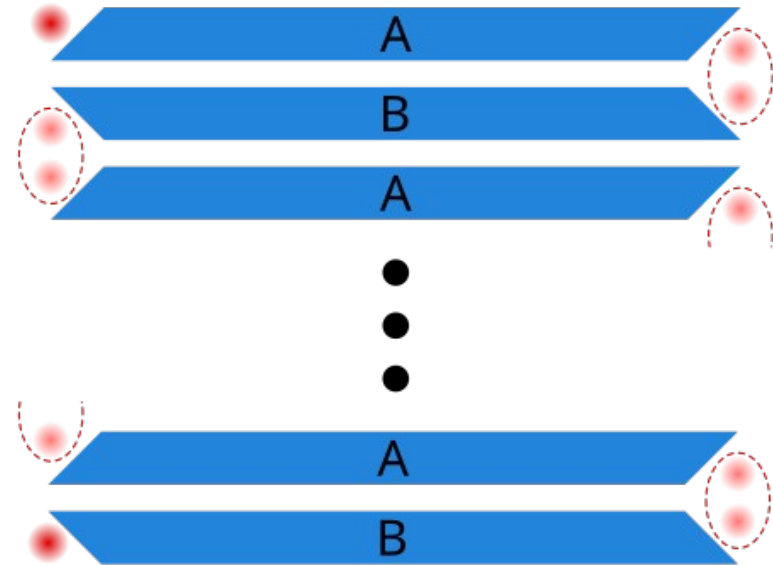
$$\alpha = -2 \frac{R_{\text{env}}}{R_Q}$$

$$\rightarrow R_{\text{env}} \sim R_Q/6 - R_Q/3$$

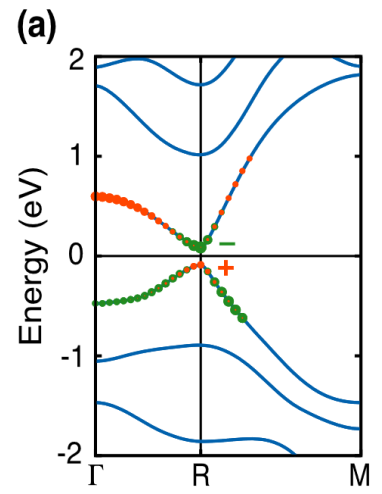
### A - A termination



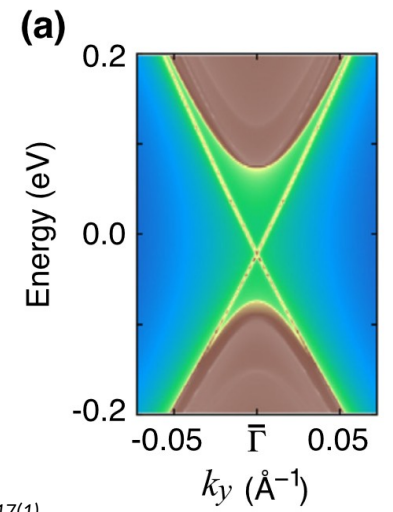
### A - B termination



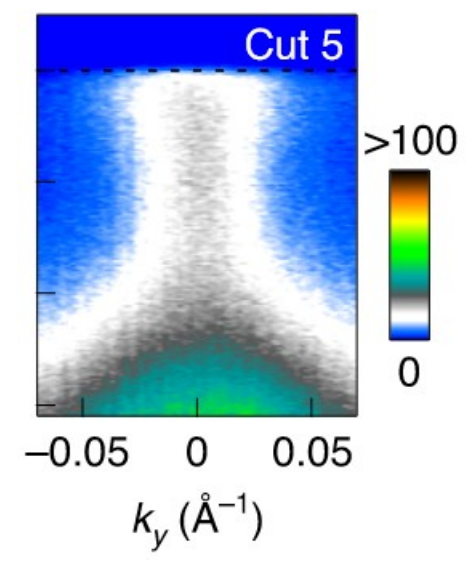
Theory :



Zhou, J.-J. et al. (2015), *New Journal of Physics*, 17(1).



ARPES :



Noguchi, R. et al. (2021), *Nature Materials*, 20(4)

