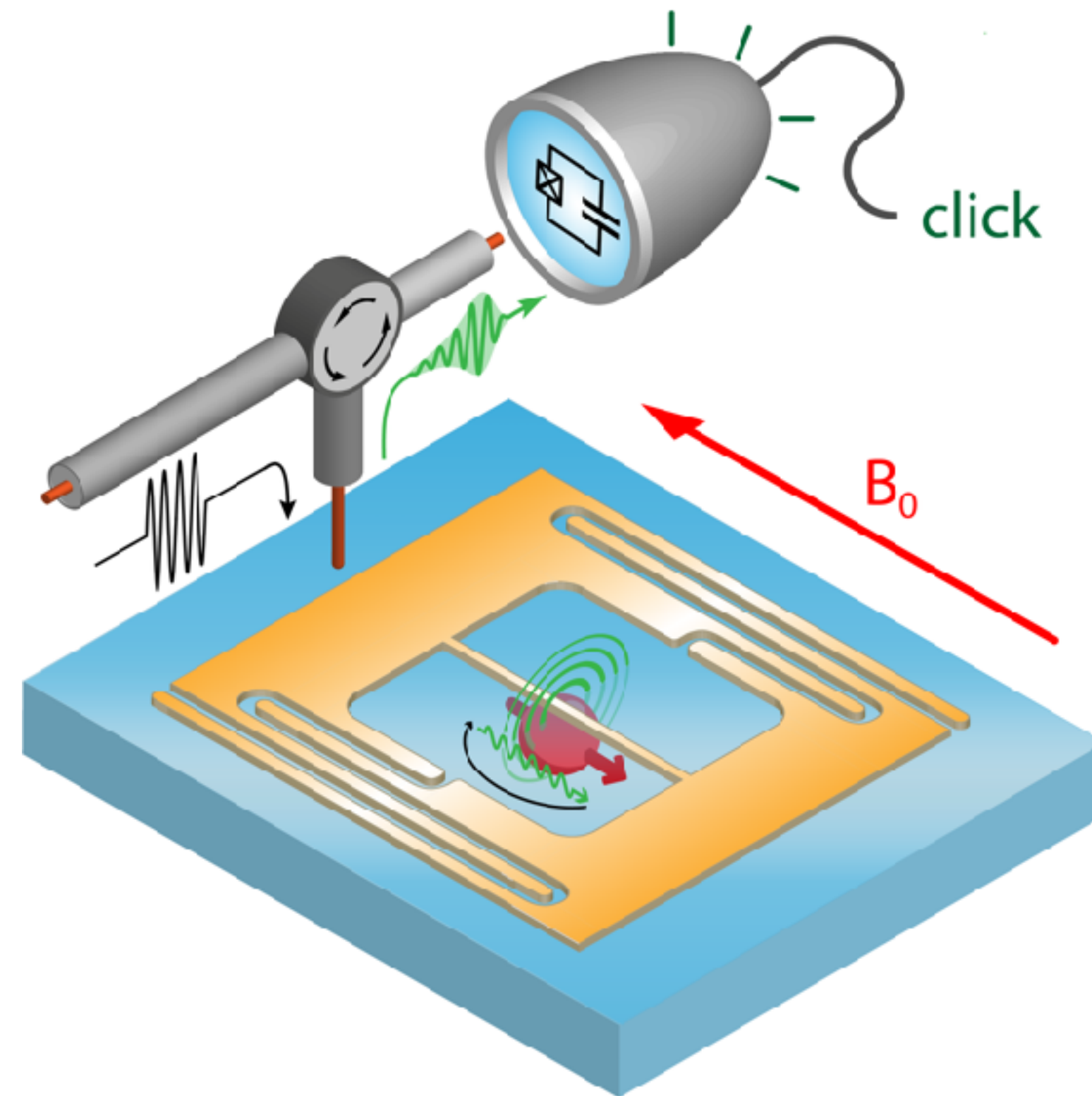


# Detecting single electron spin resonance with a single microwave photon counter

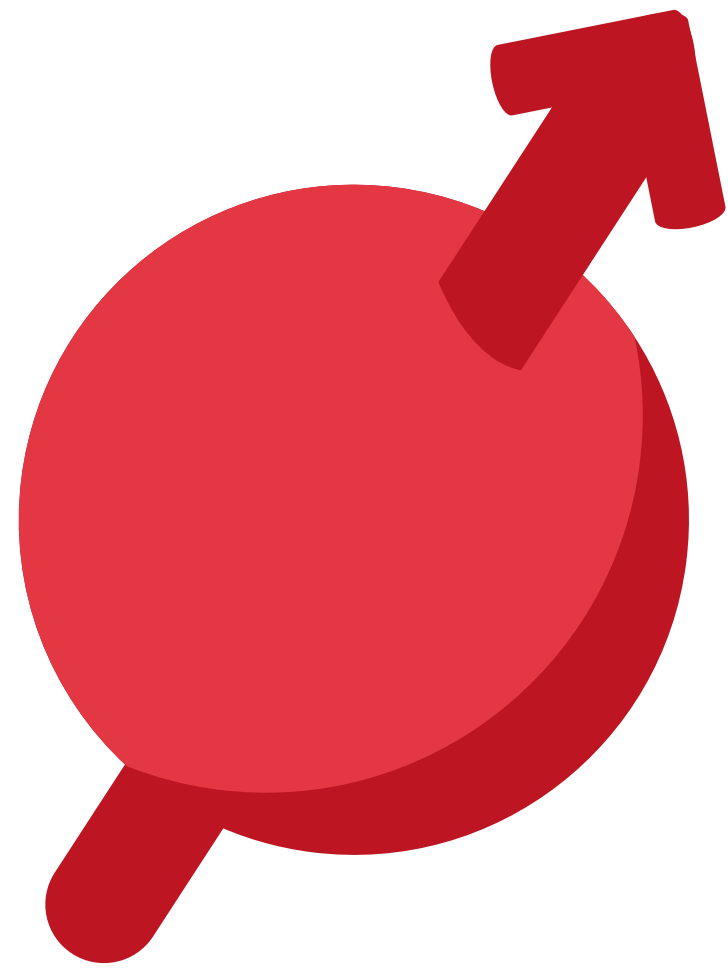


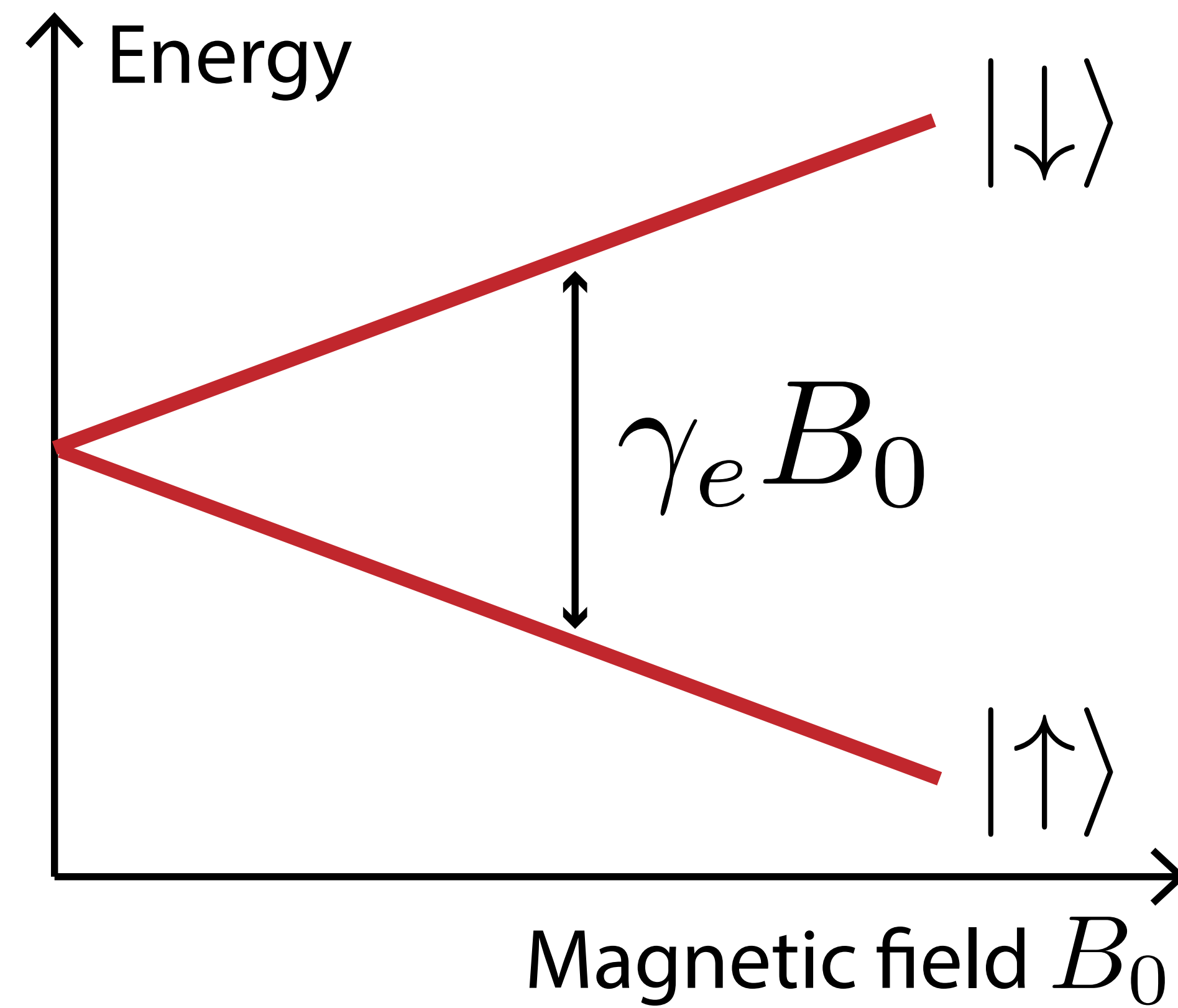
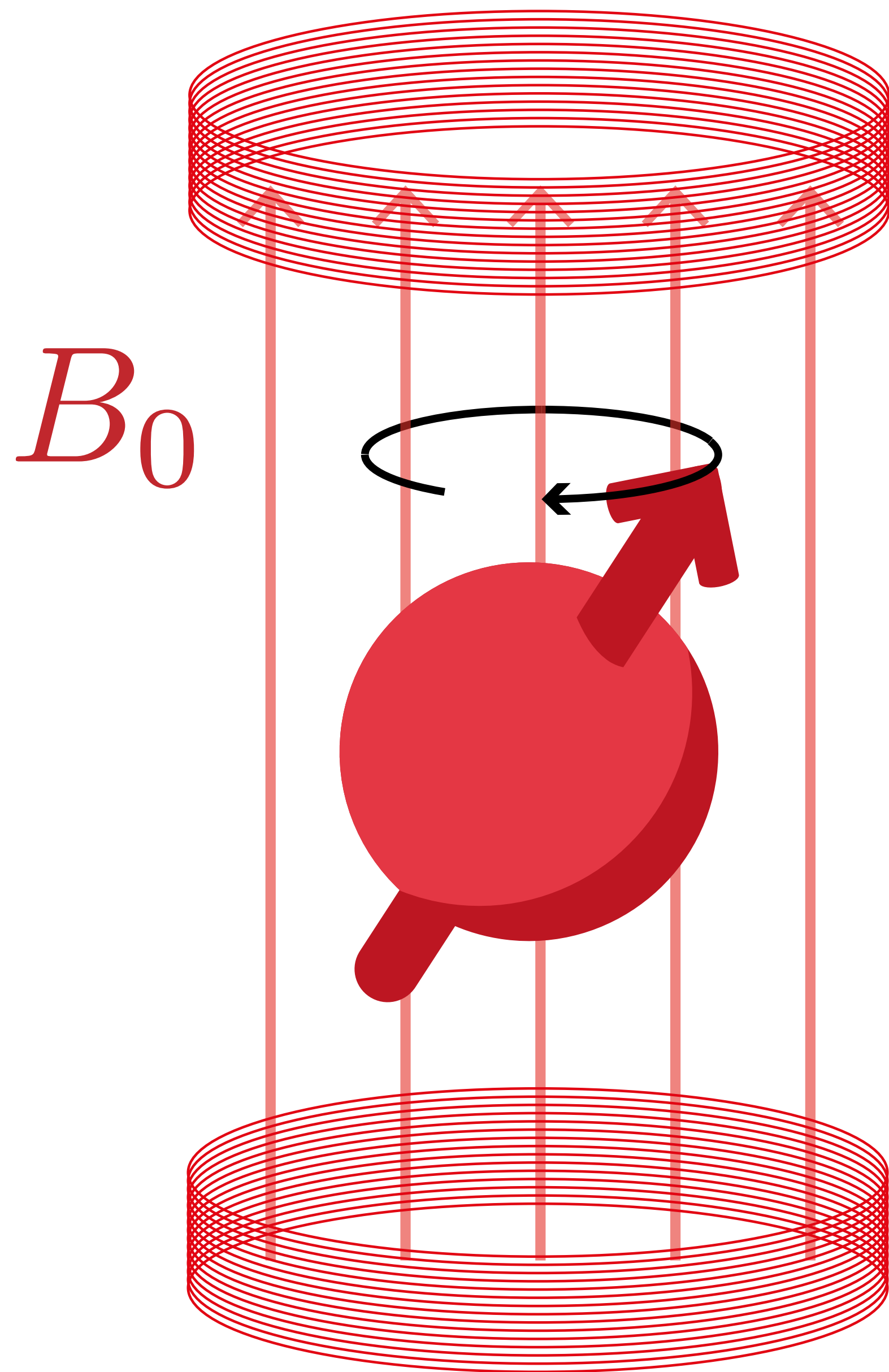
arXiv:2301.02653 (Nature *in press*)

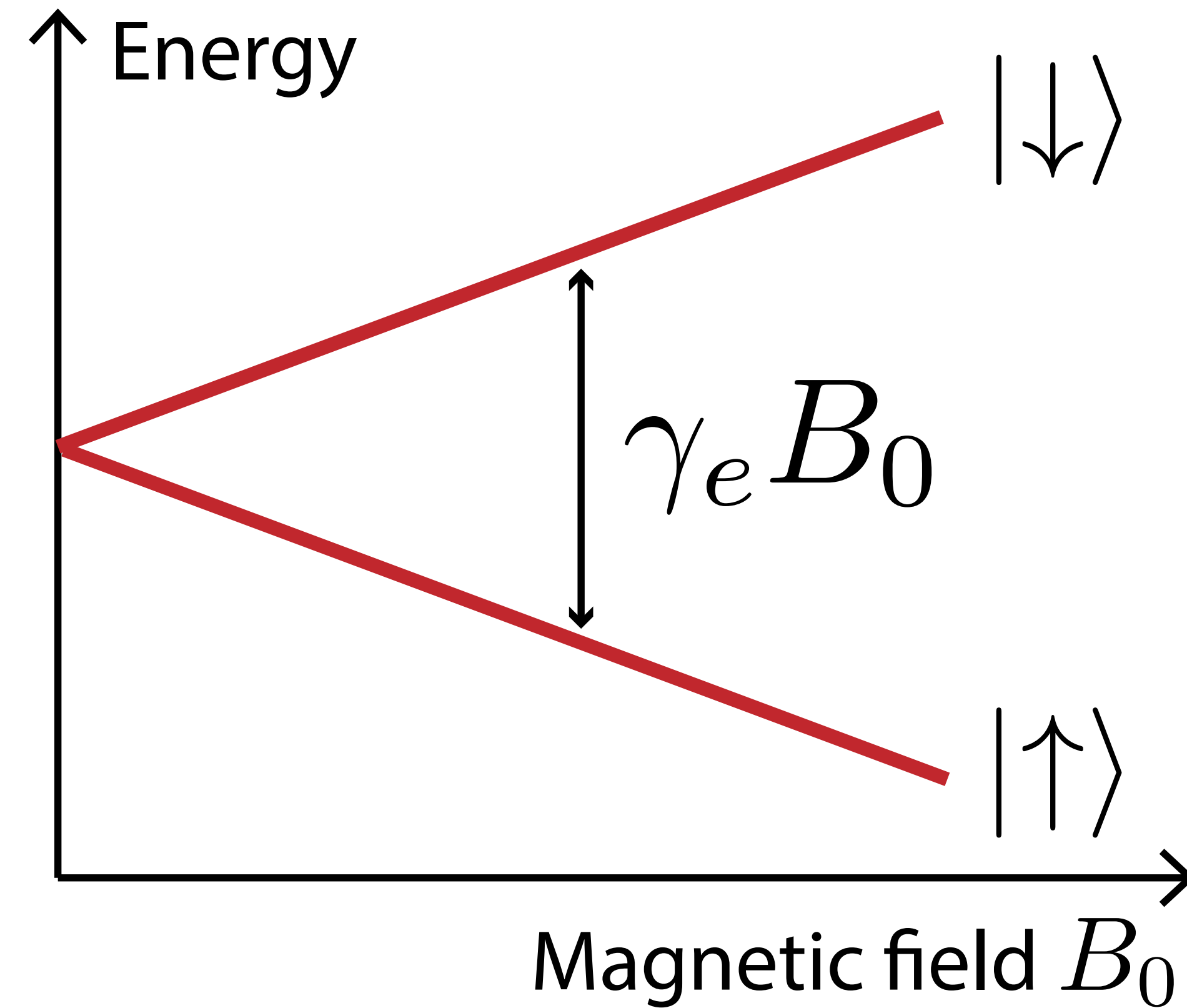
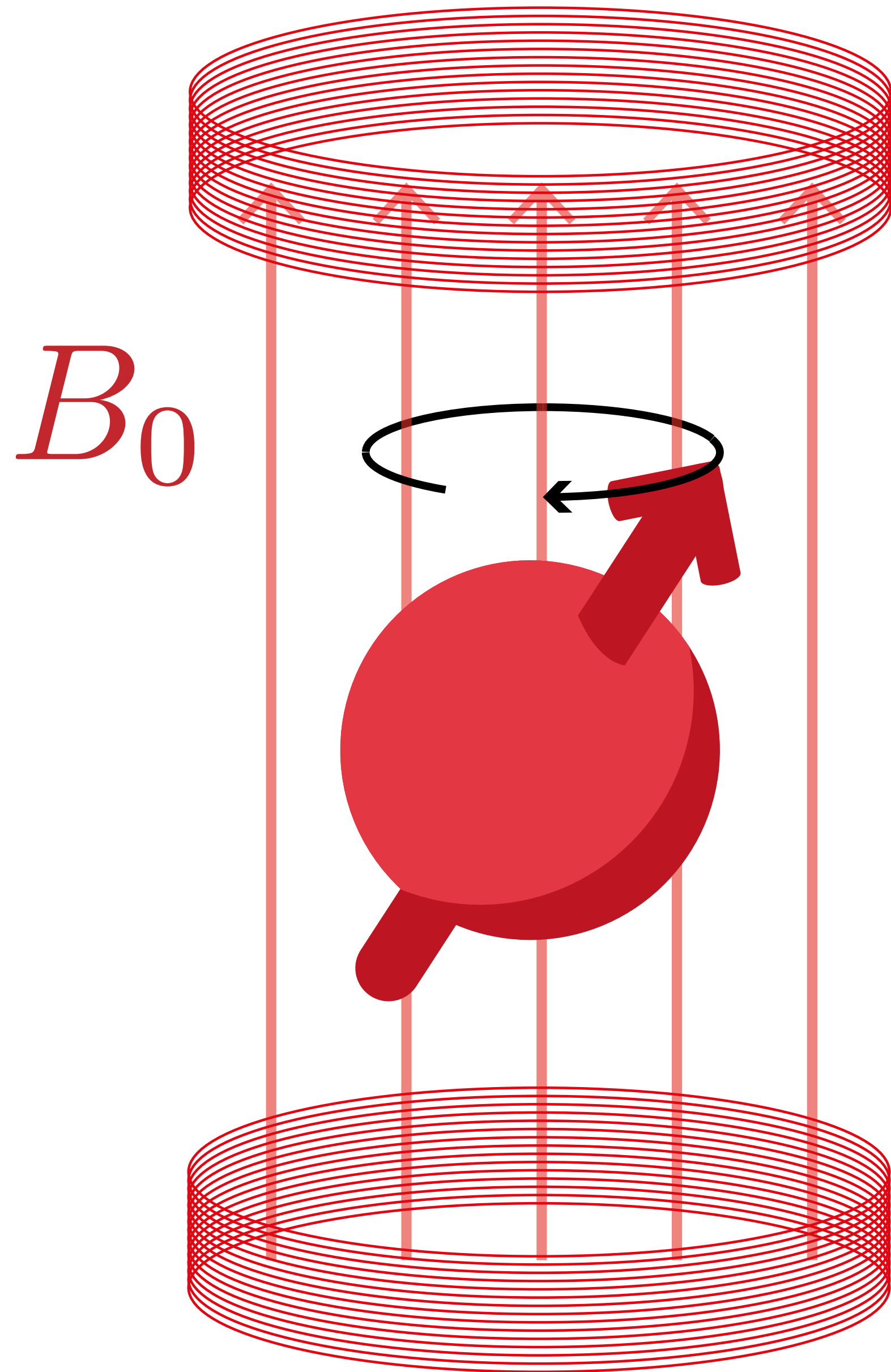
Wang, Balembois, Billaud, Albertinale, Le Dantec, Rancic  
Estève, Vion, Bertet, **Flurin**

Quantronics group / SPEC



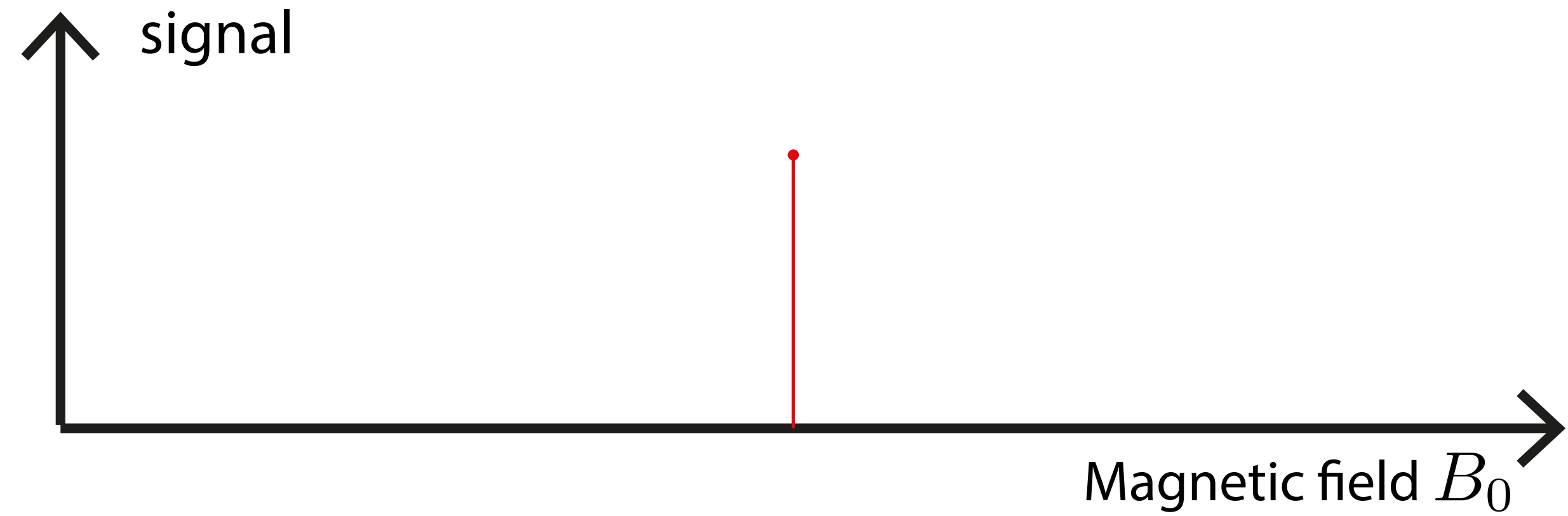
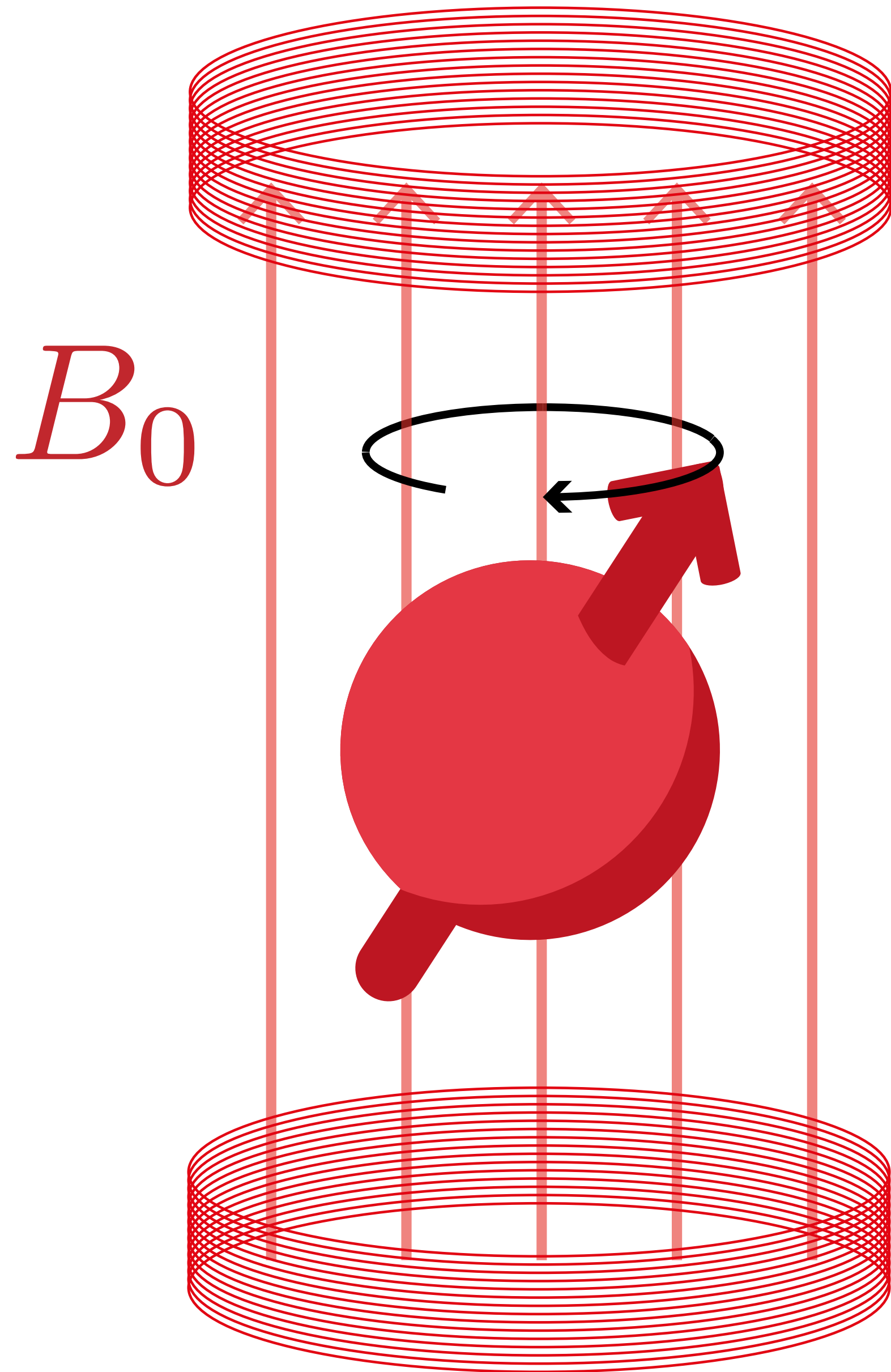






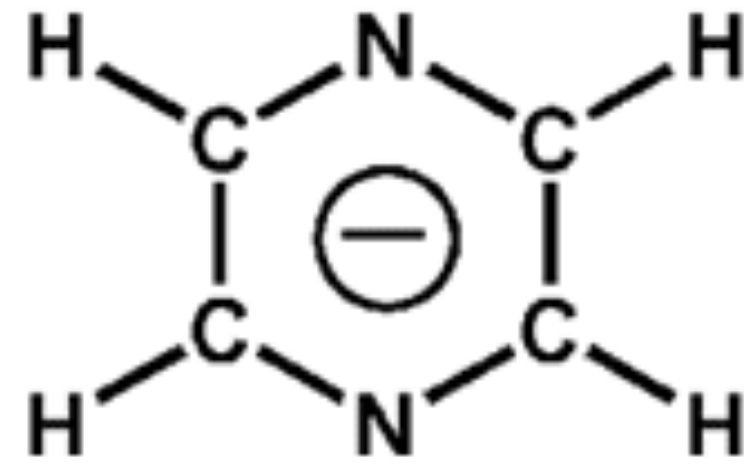
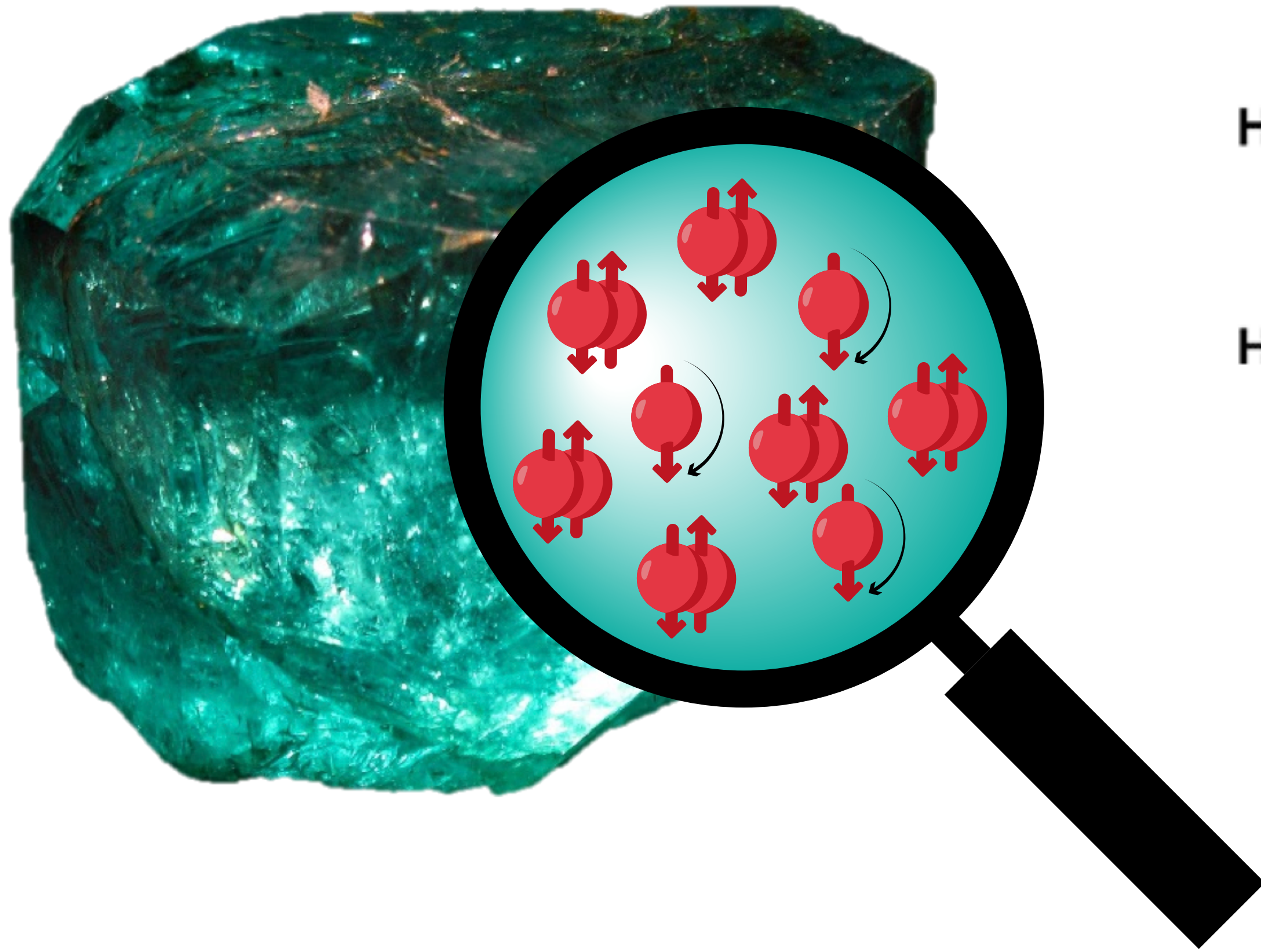
Free electron spin

$$\gamma_e = 28.0249514242(85) \text{ GHz/T}$$

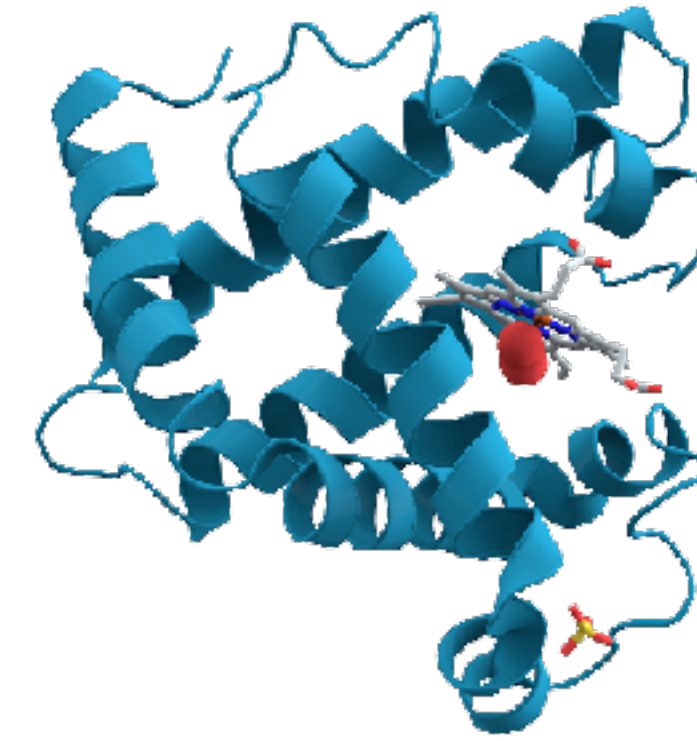


Free electron spin

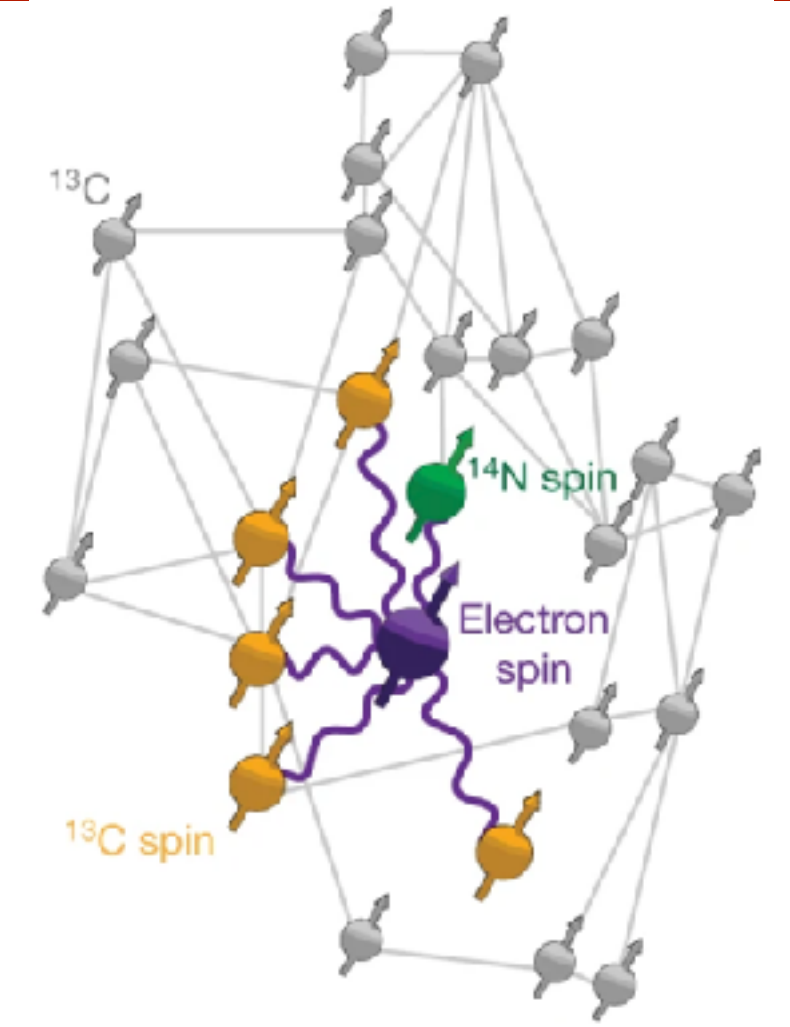
$$\gamma_e = 28.0249514242(85) \text{ GHz/T}$$



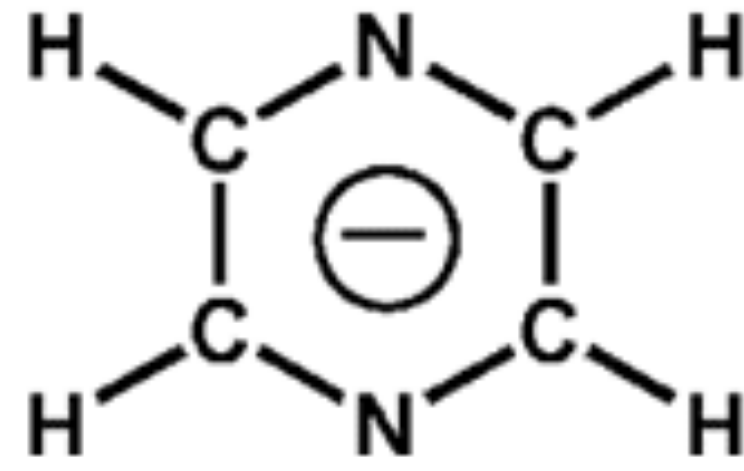
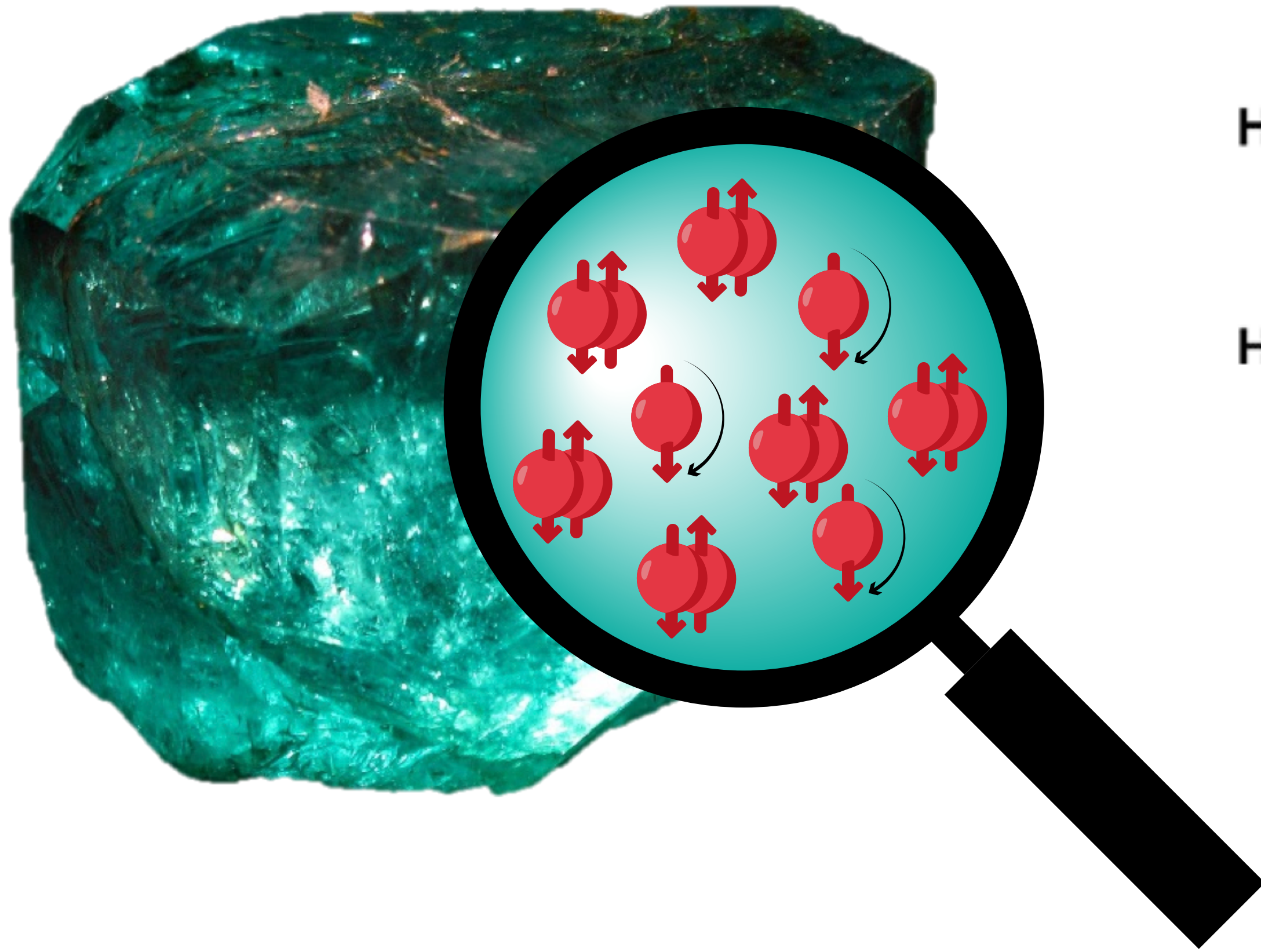
Chemistry



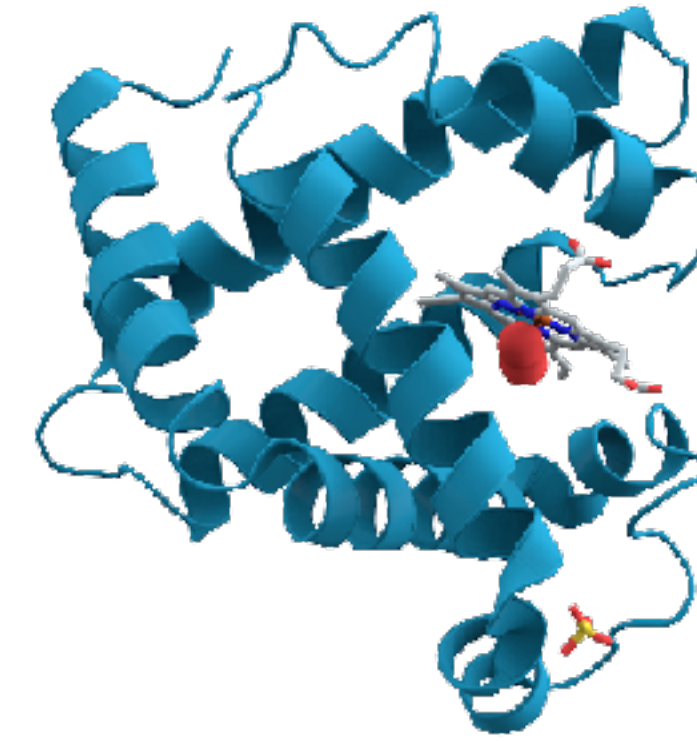
Biology



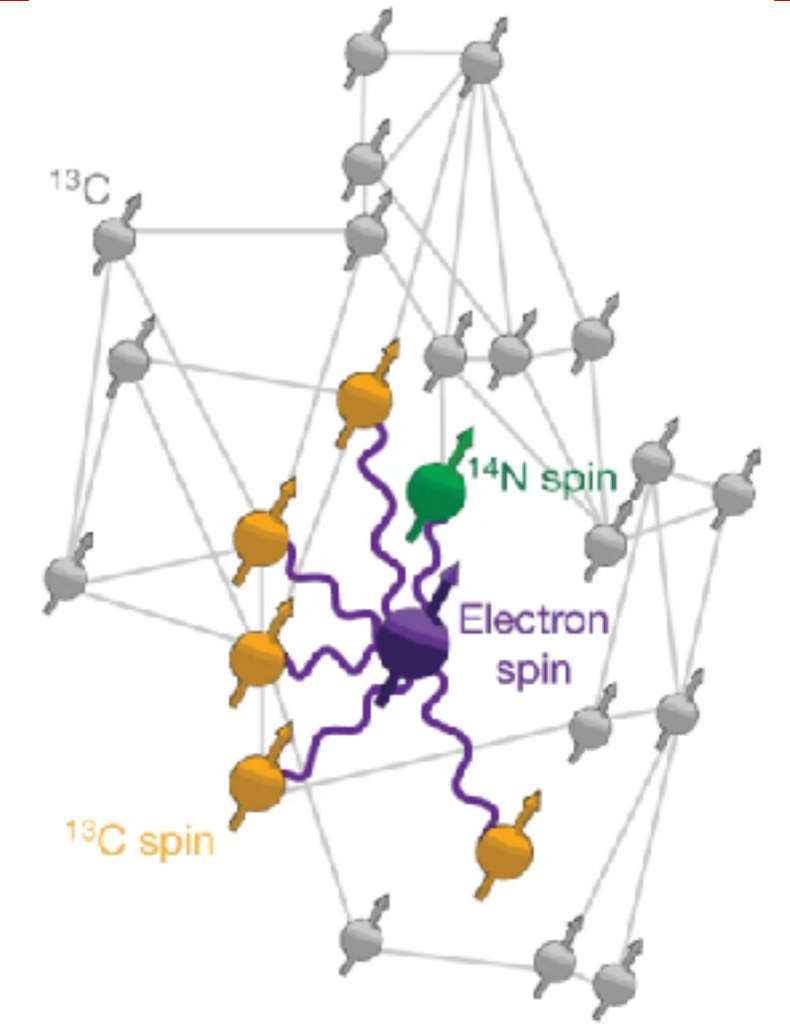
Quantum Computing



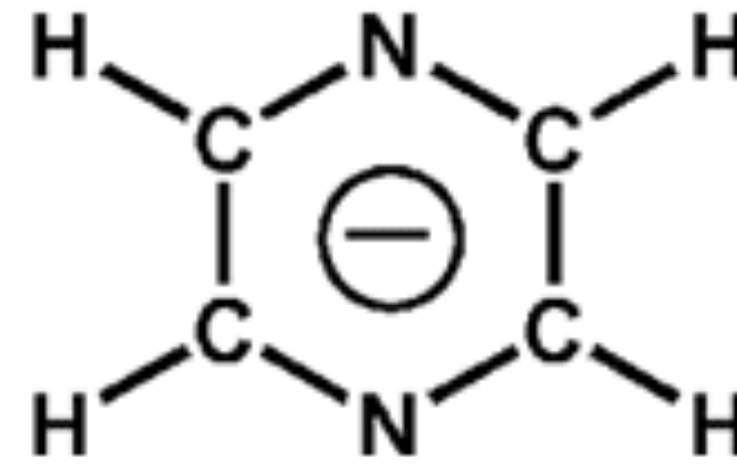
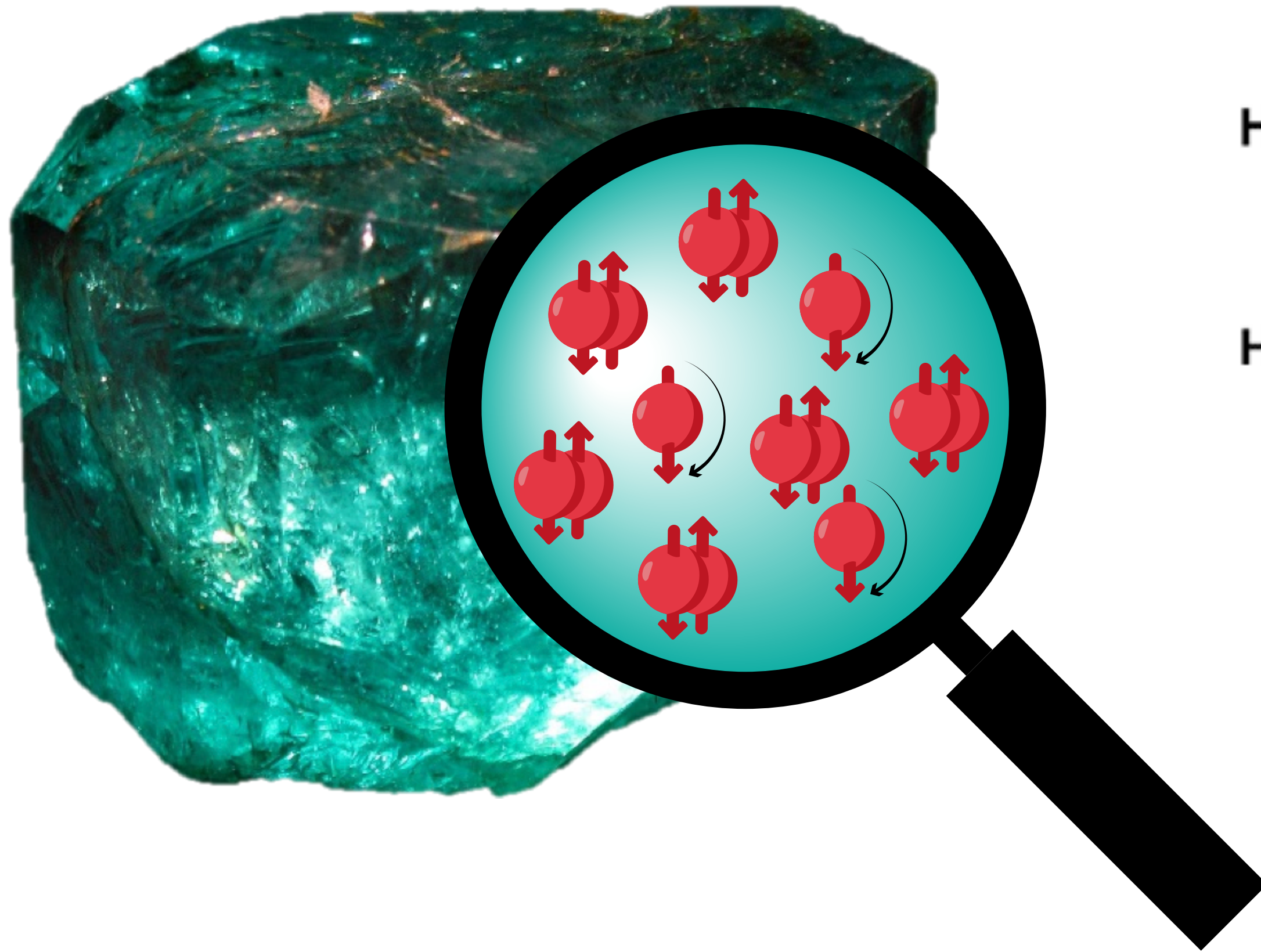
Chemistry



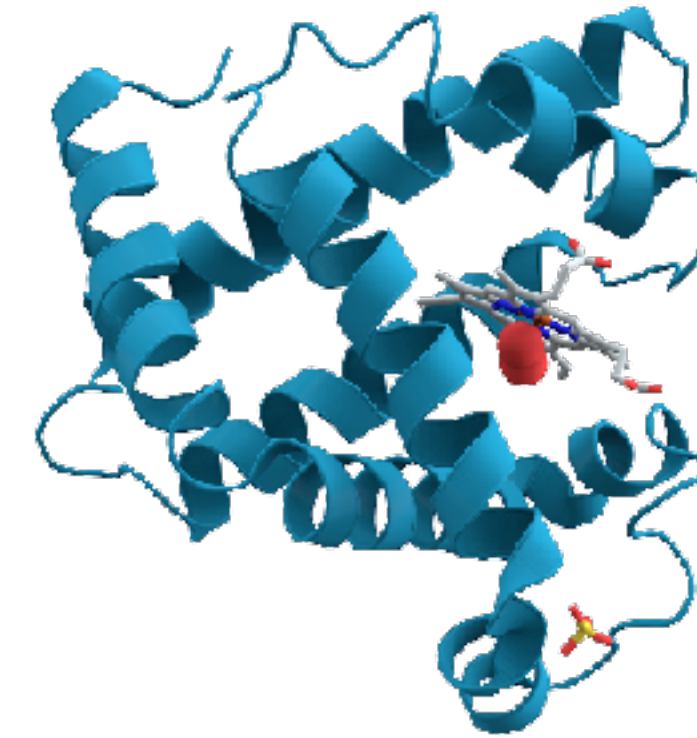
Biology



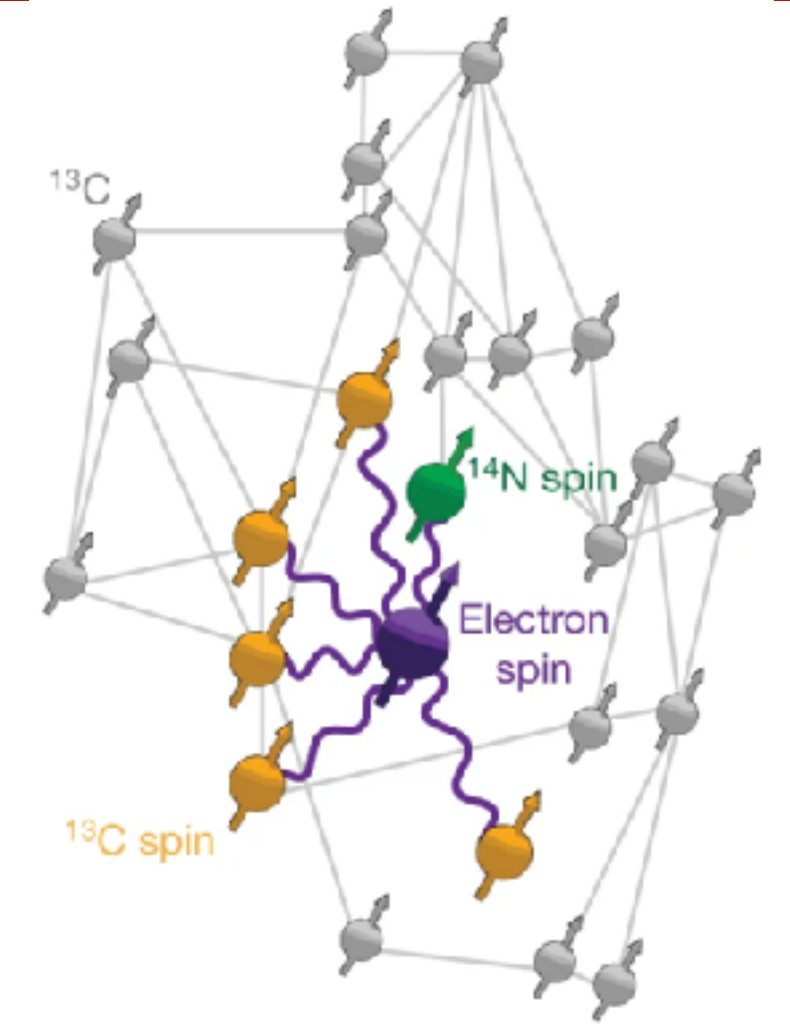
Quantum Computing



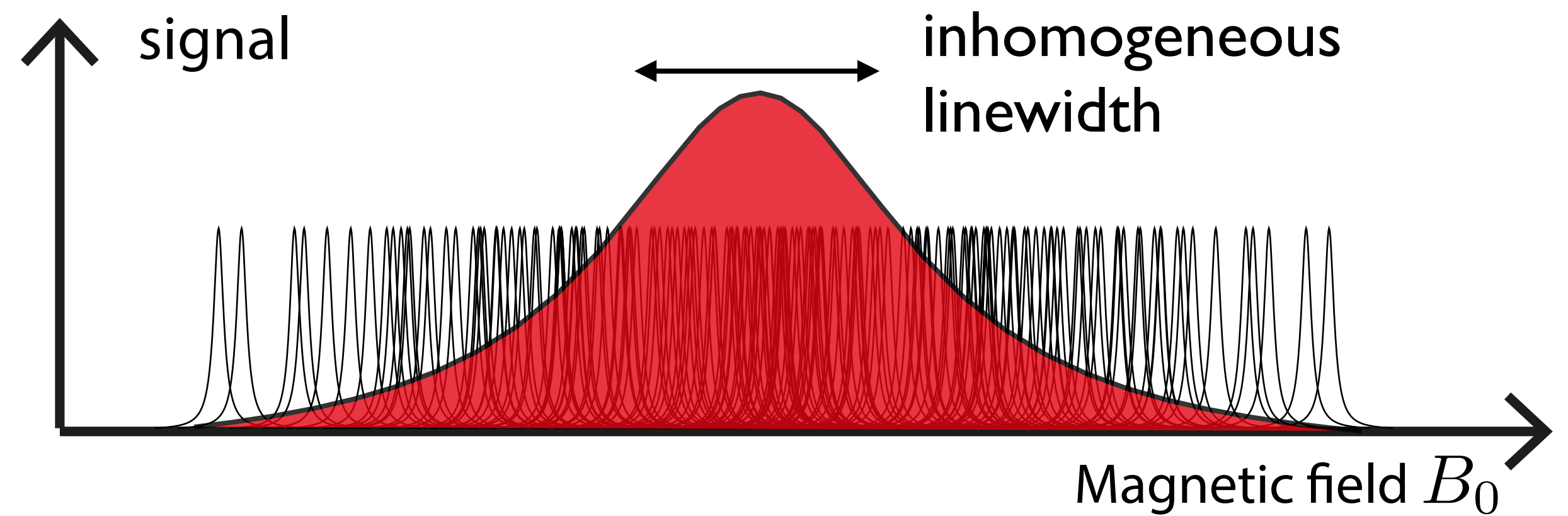
Chemistry



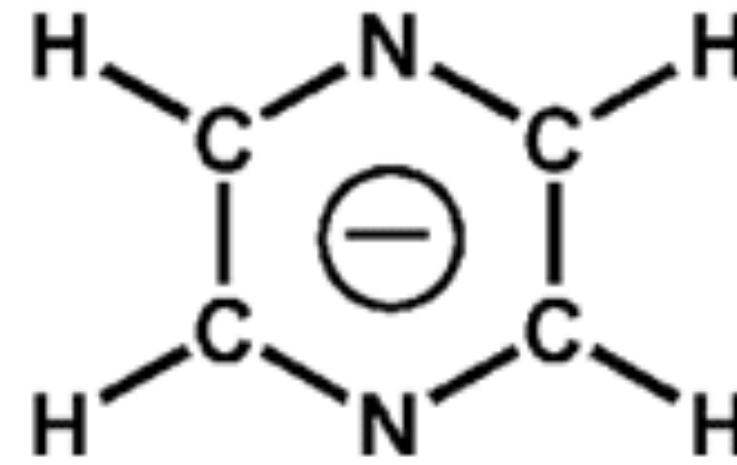
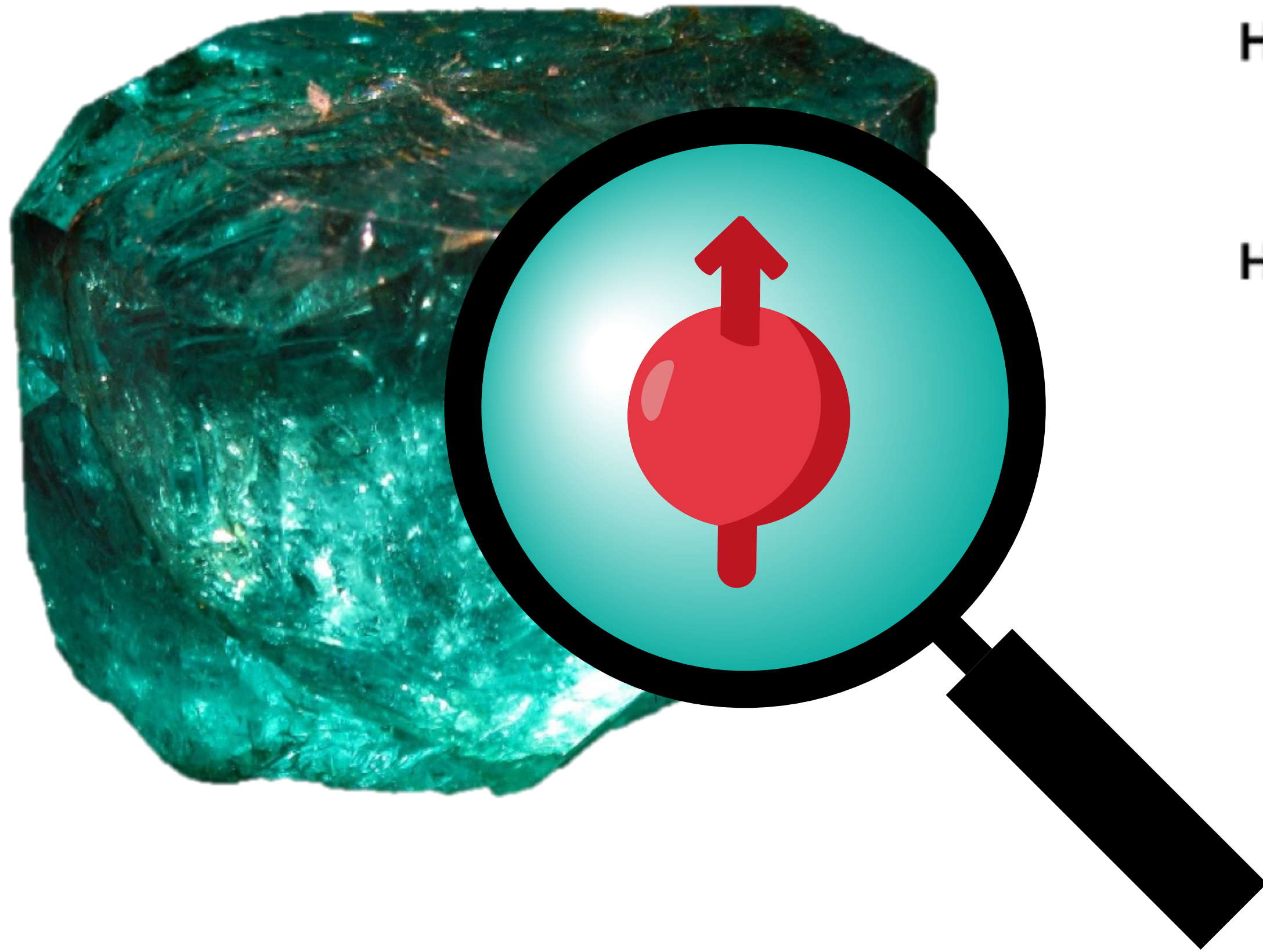
Biology



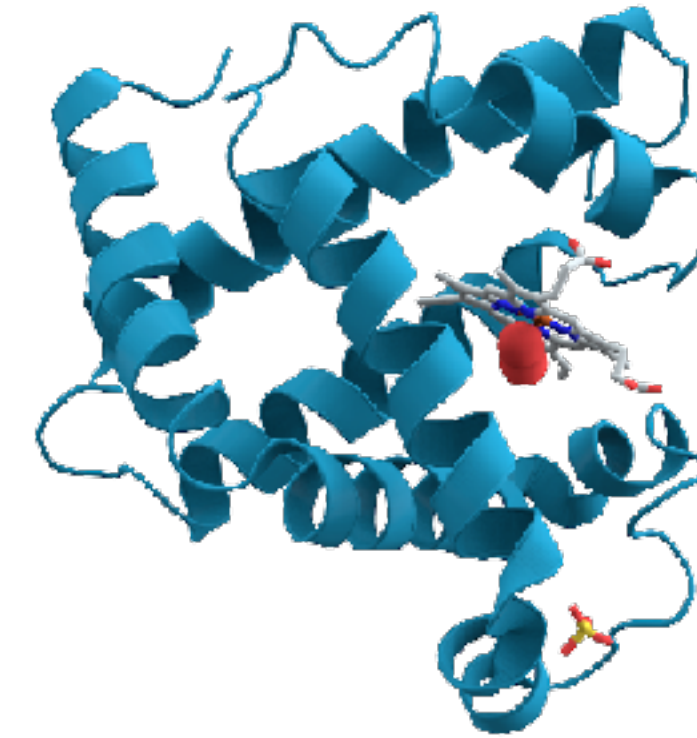
Quantum Computing



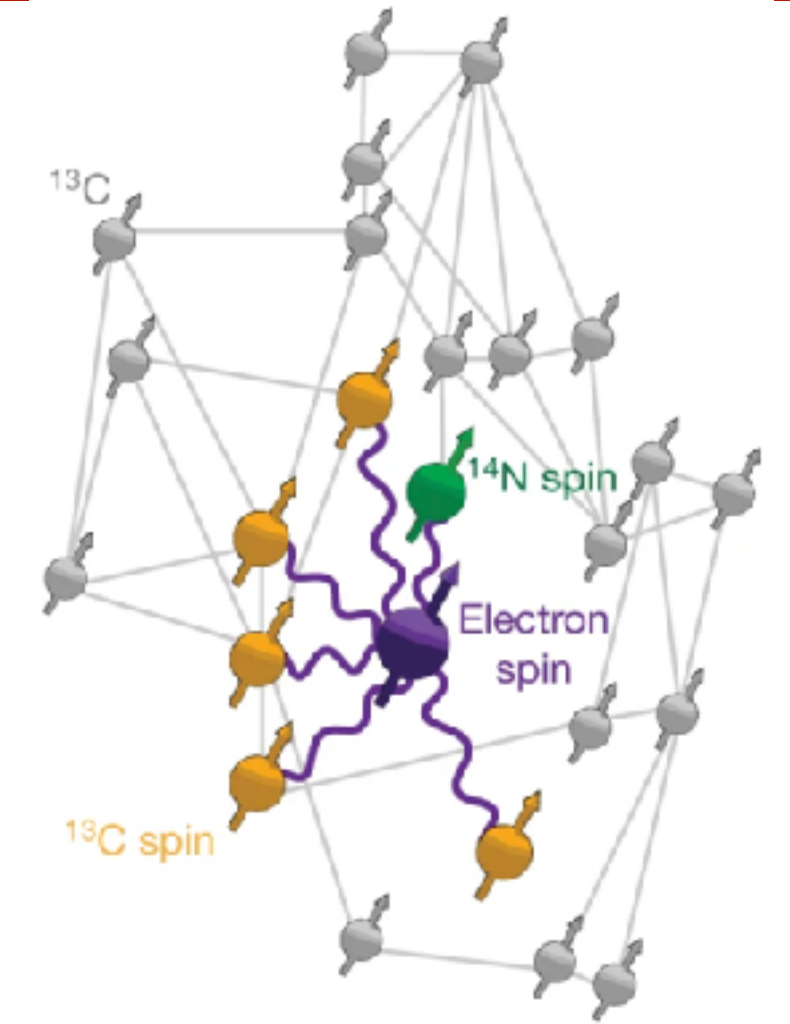




Chemistry

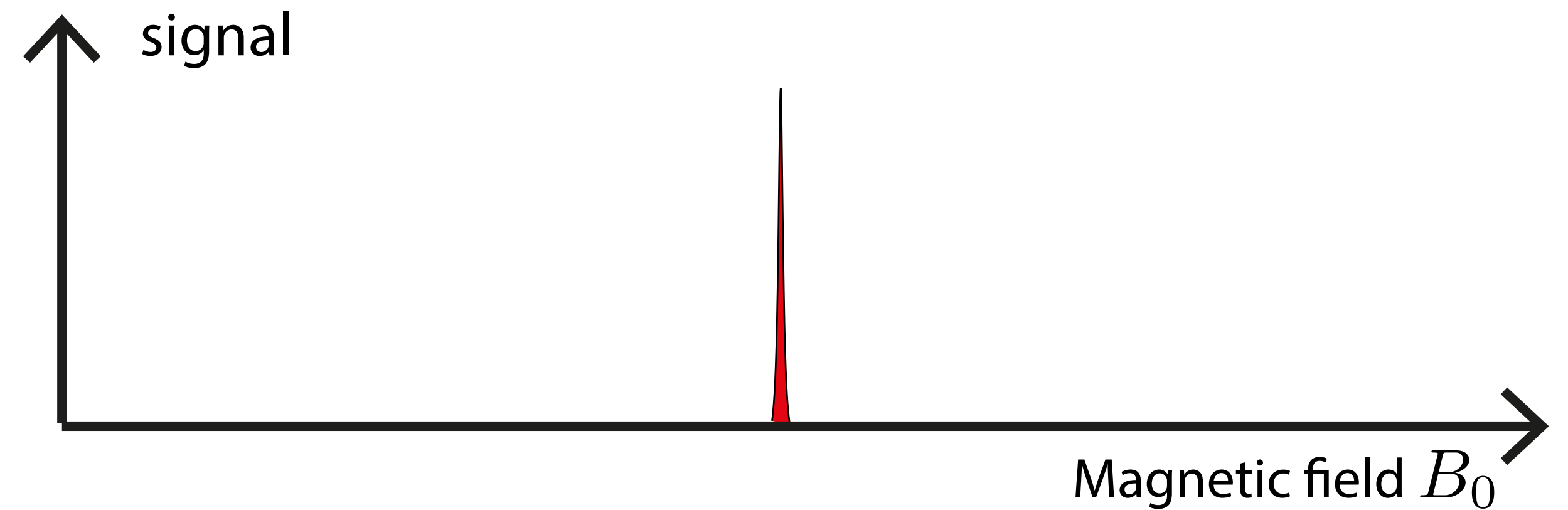


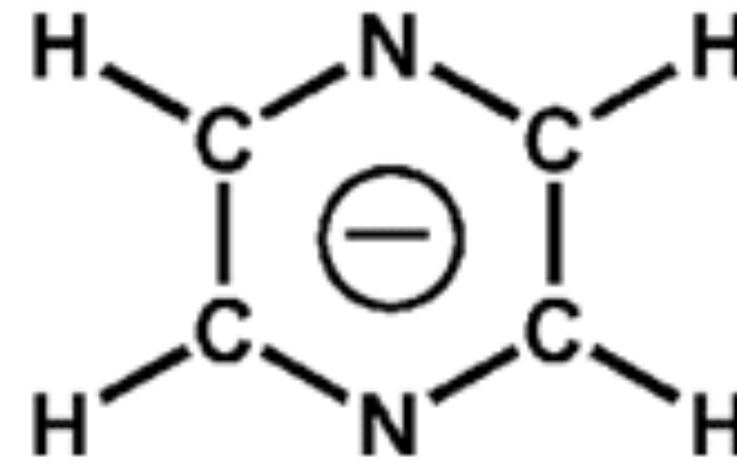
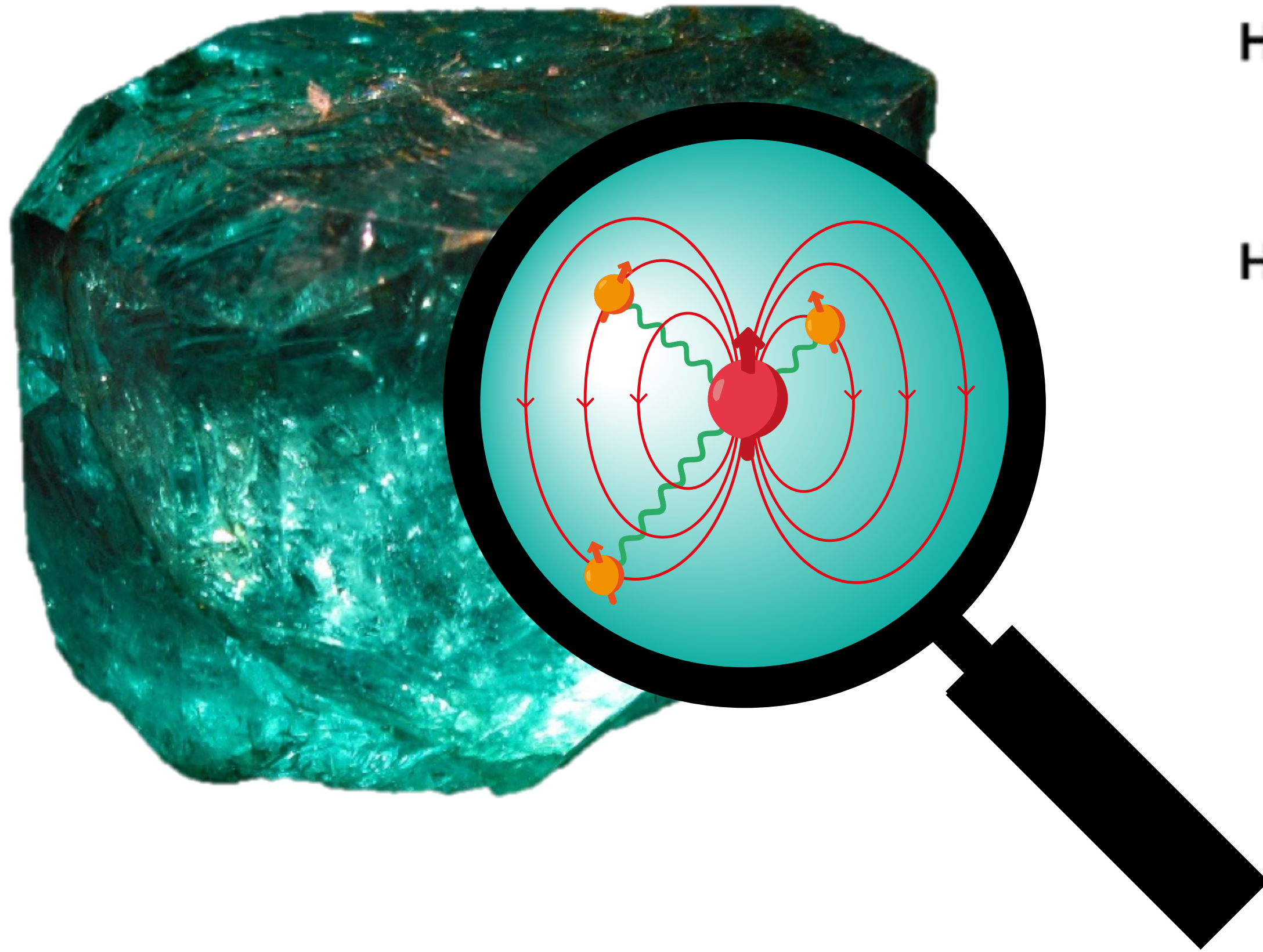
Biology



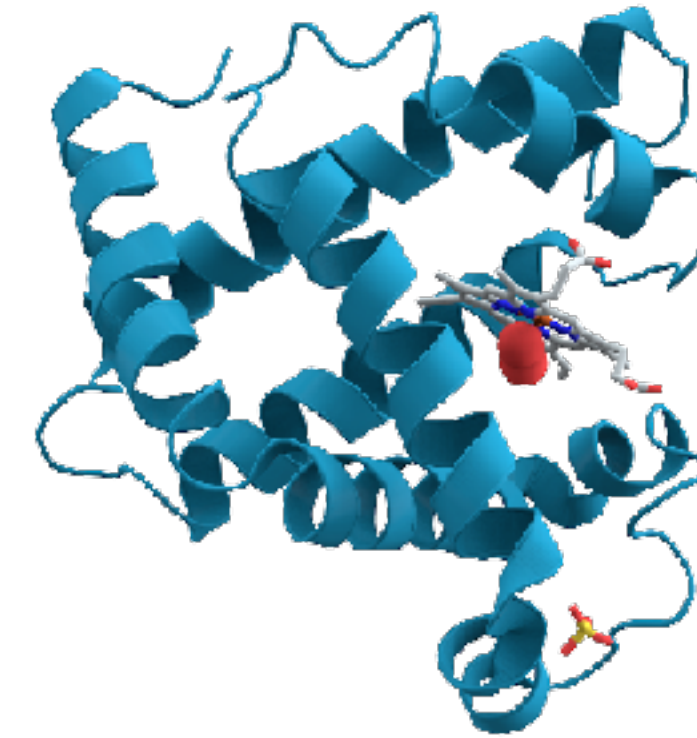
Quantum Computing

$1 \text{ spin} / \sqrt{\text{Hz}} ?$

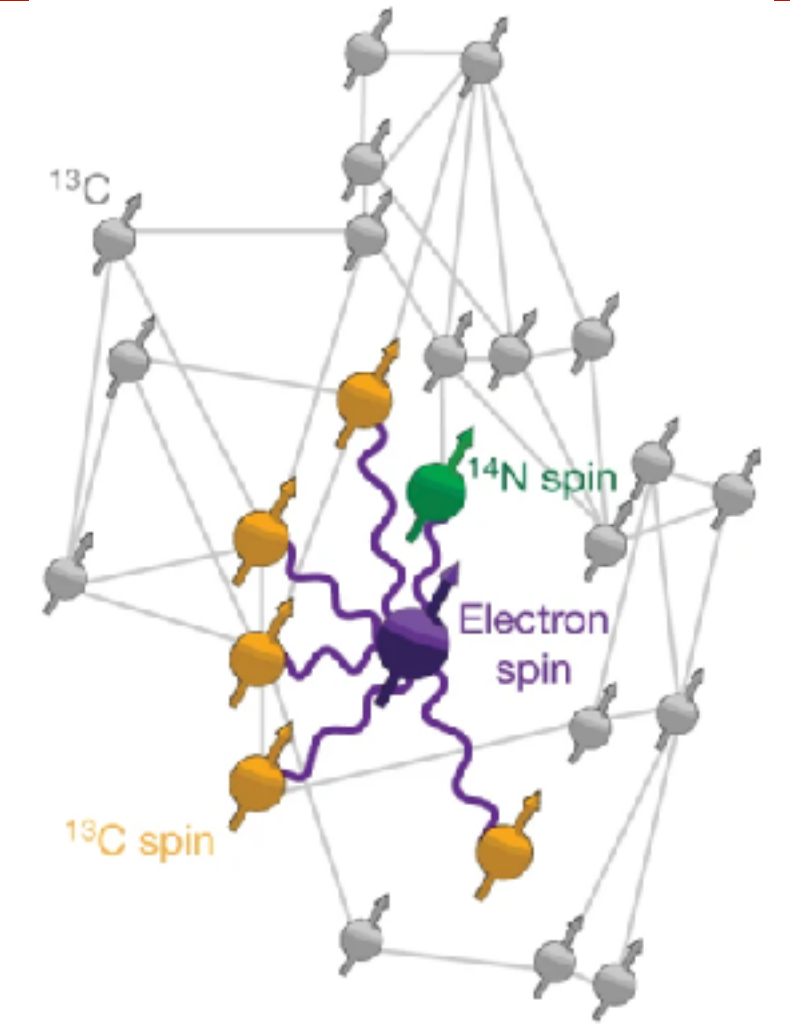




Chemistry

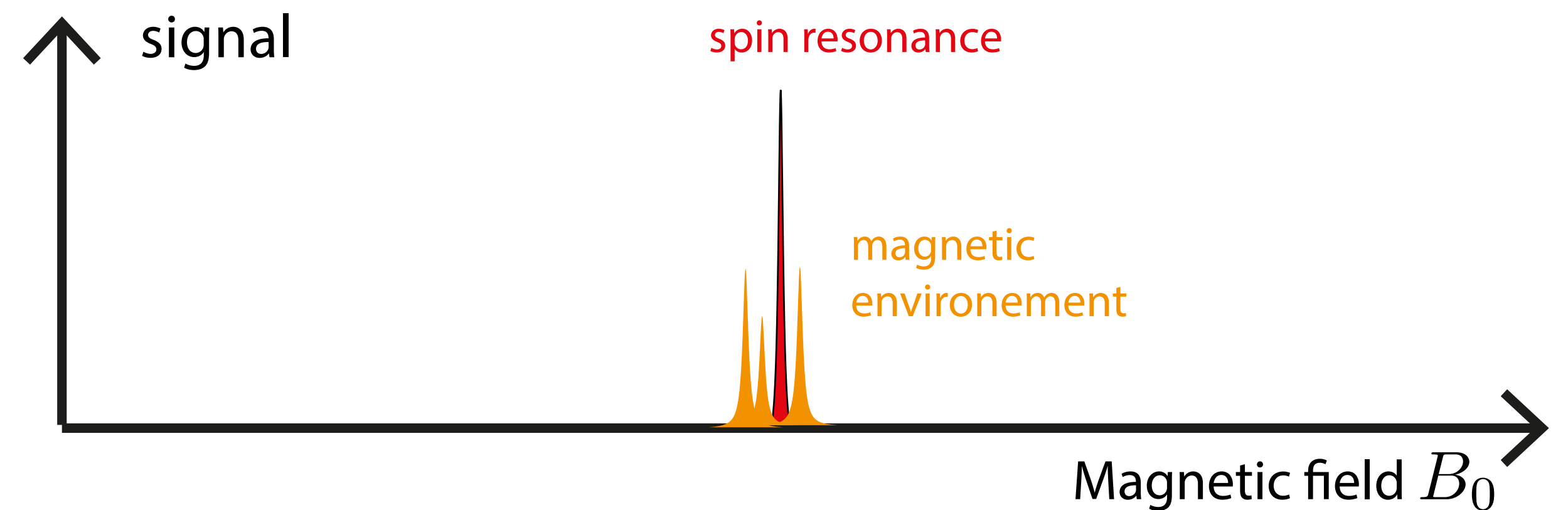


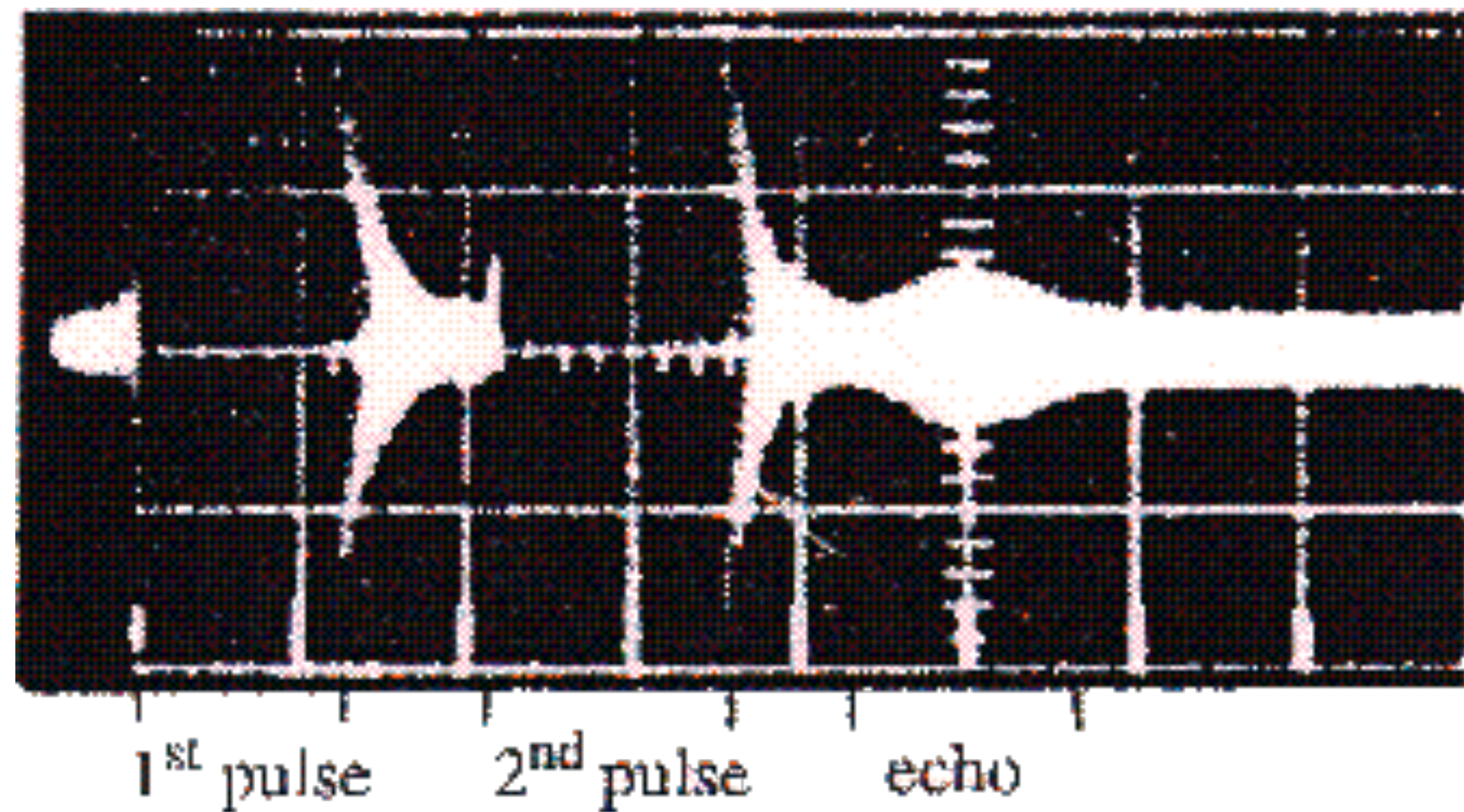
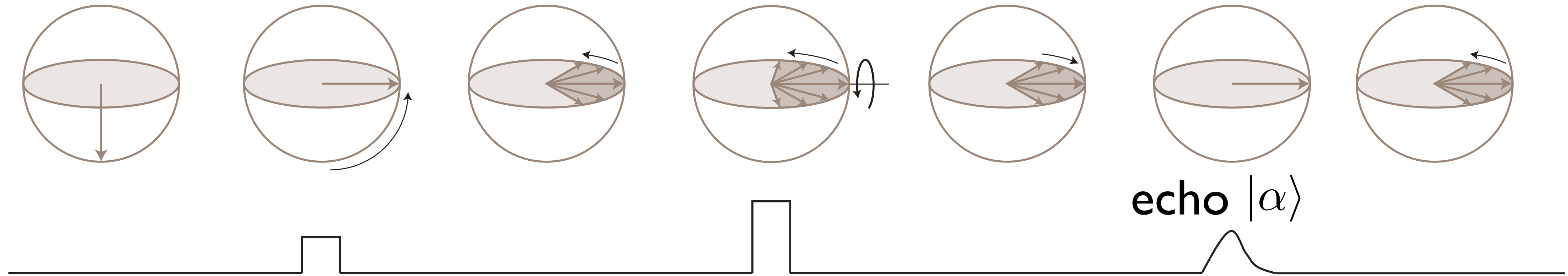
Biology



Quantum Computing

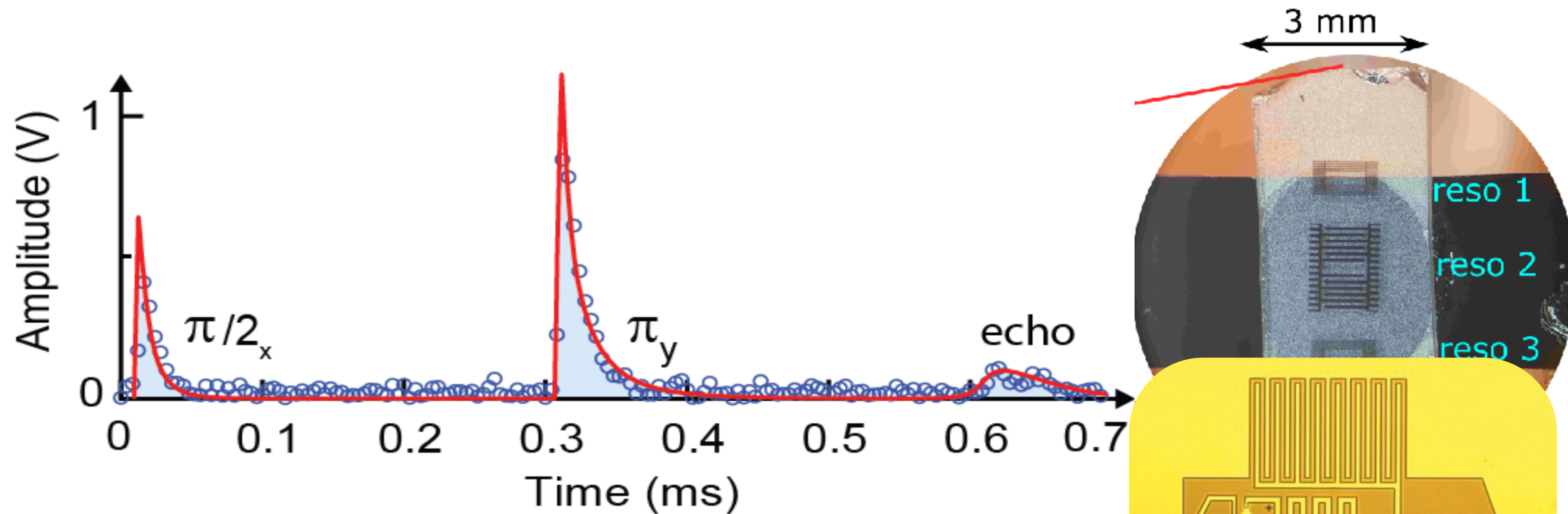
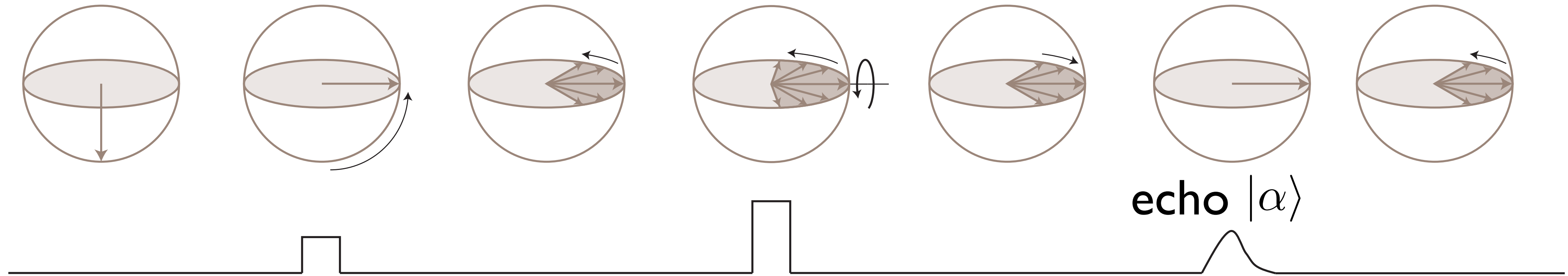
$1 \text{ spin} / \sqrt{\text{Hz}} ?$





**Electron  
Spin Resonance**

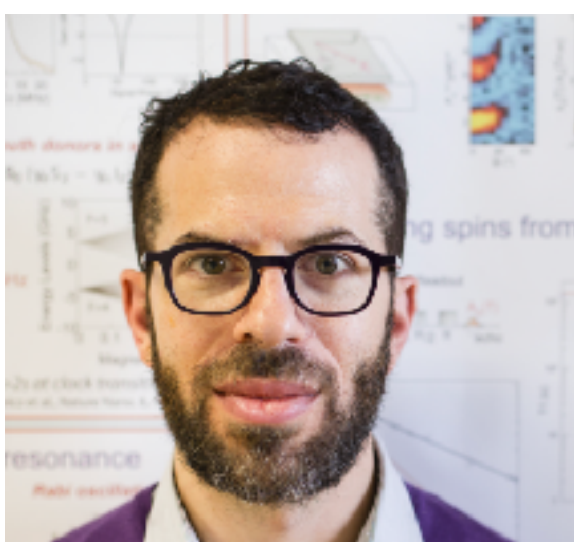
$$10^{13} \text{ spins}/\sqrt{\text{Hz}}$$



**Superconducting  
Coupling Resonator  
& Quantum Limited  
Amplifier**

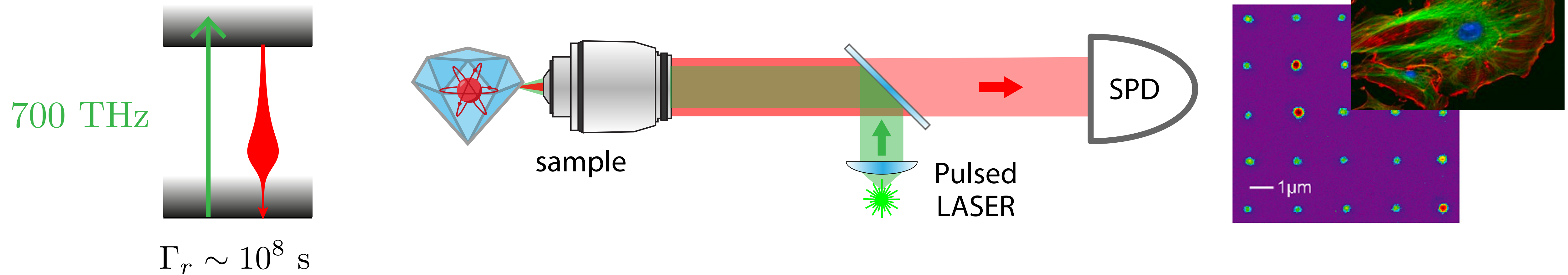
$$100 \text{ spins}/\sqrt{\text{Hz}}$$

[Ranjan et al. Appl. Phys. Lett. **116**, 184002 (2020)]

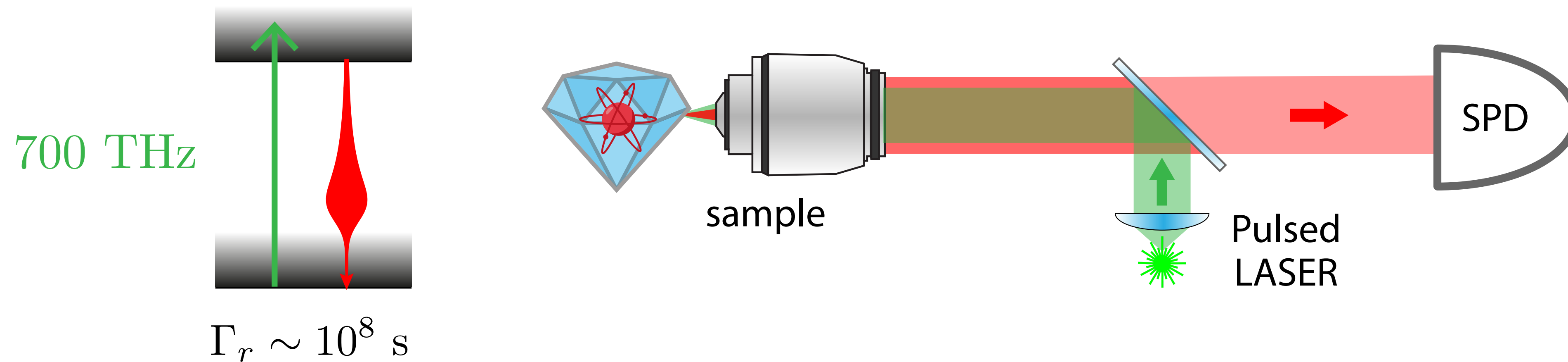


**P. Bertet**

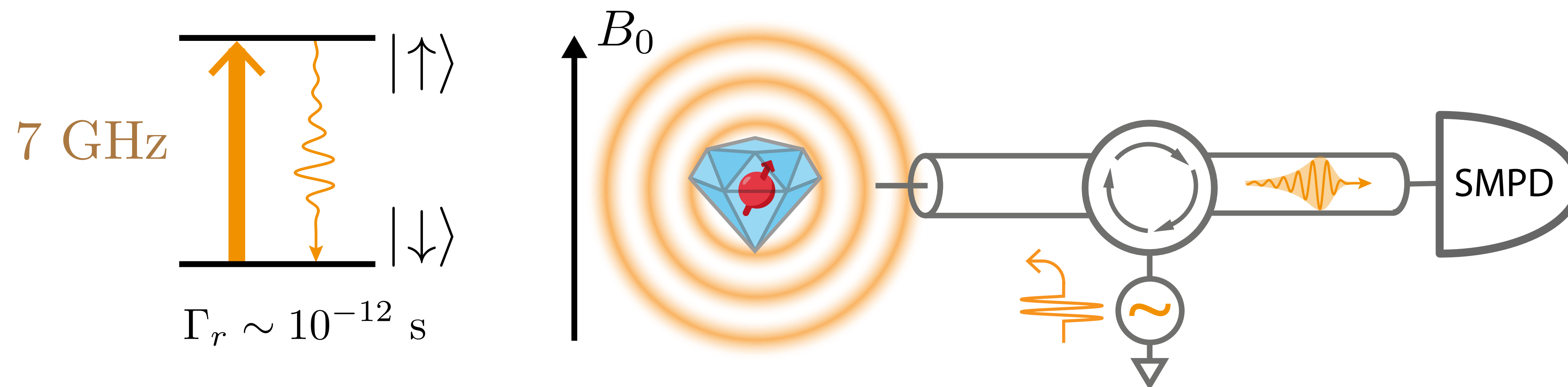
Fluorescence detection is ubiquitous in optics: atoms, molecules, NVs, ...



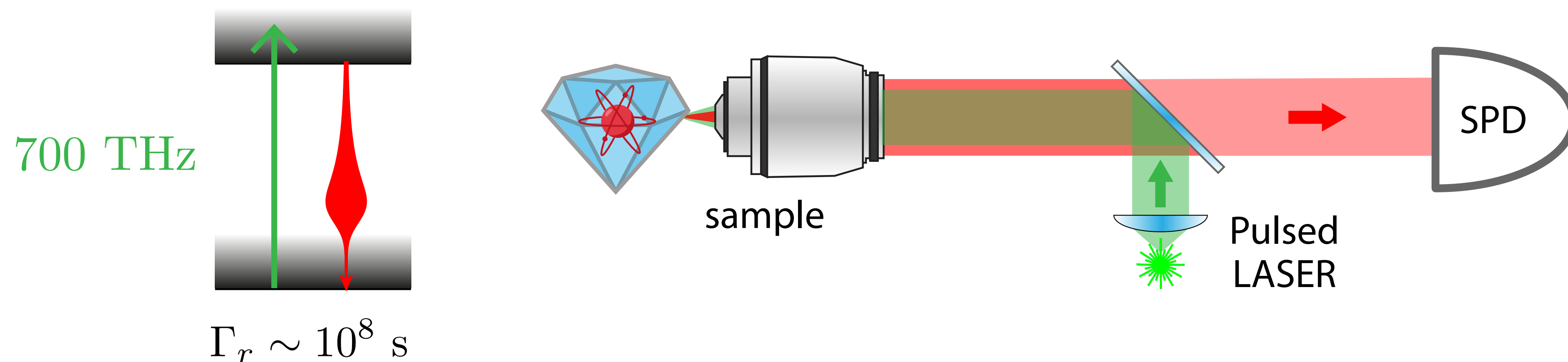
Fluorescence detection is ubiquitous in optics: atoms, molecules, NVs, ...



Can we detect spins by their microwave (MW) fluorescence ?



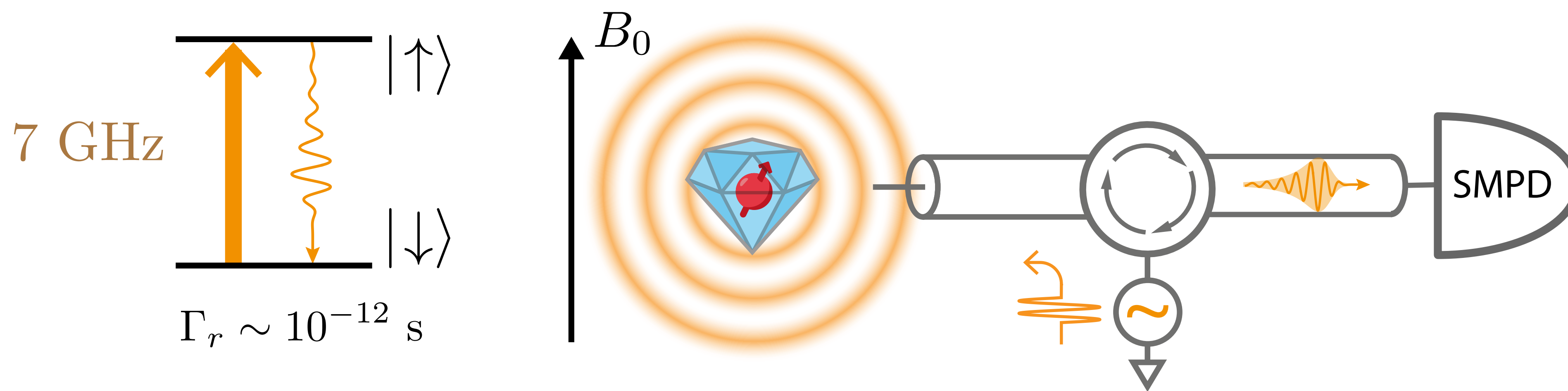
Fluorescence detection is ubiquitous in optics: atoms, molecules, NVs, ...



## WANTED

- Cryogenic temperature  
 $\hbar\omega \gg kT$
- Large microwave radiative rate
- Single **Microwave** Photon Detector

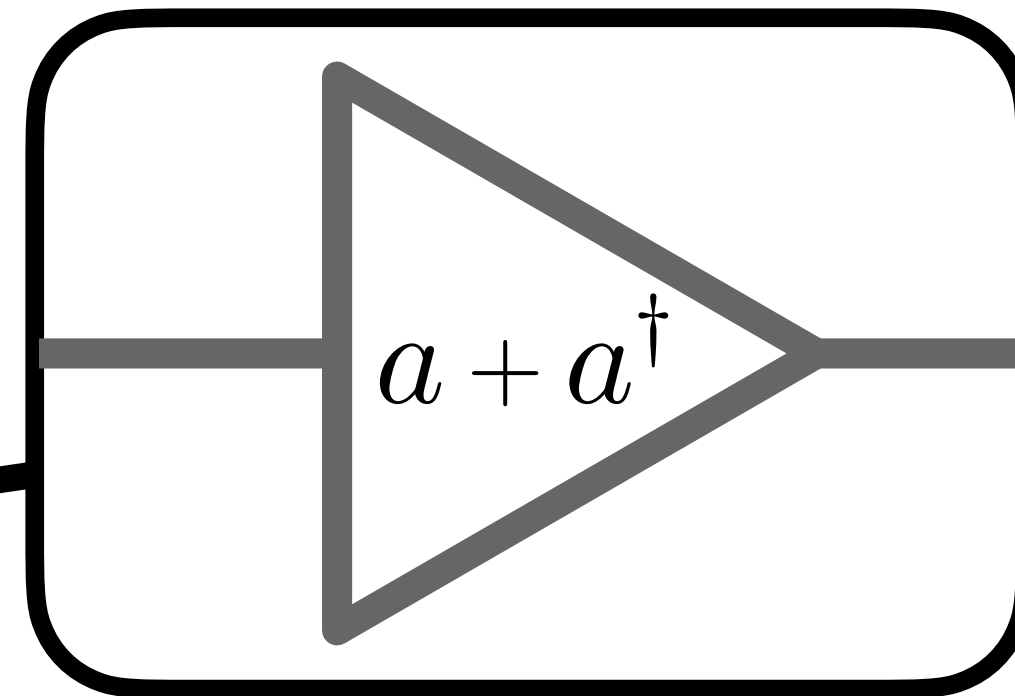
Can we detect spins by their microwave (MW) fluorescence ?



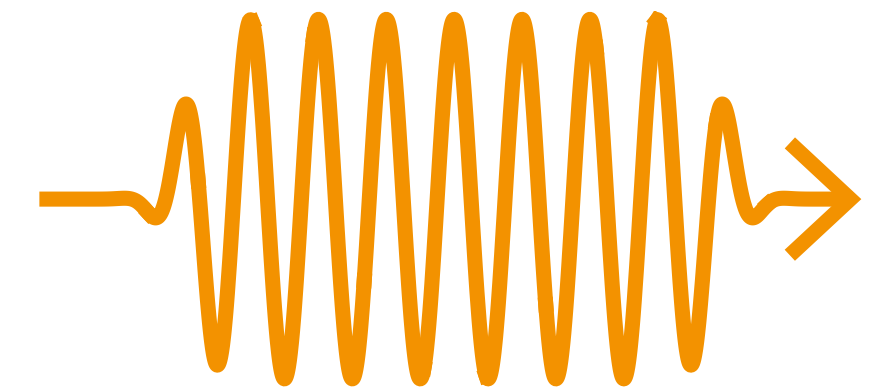
Quantum Light

$$|\psi\rangle$$

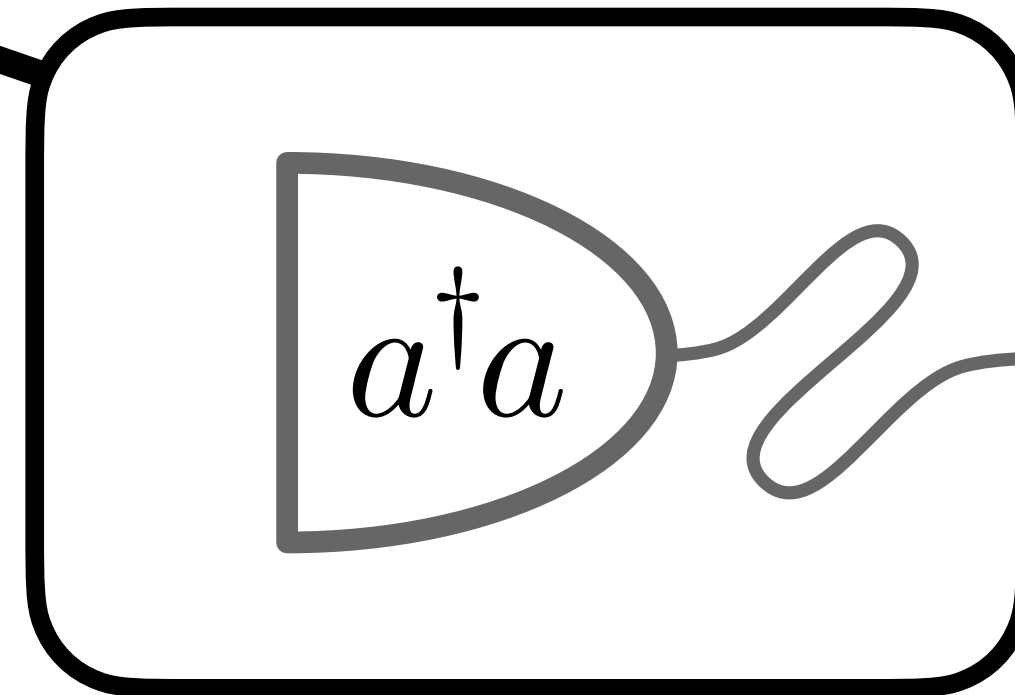
Field Detector



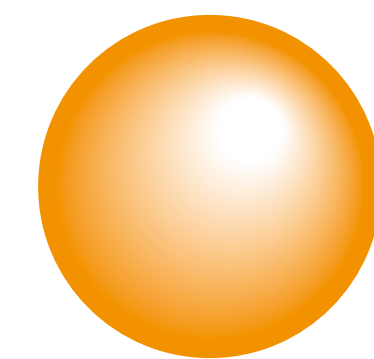
Wave-Like



Photon Detector



Particle-Like

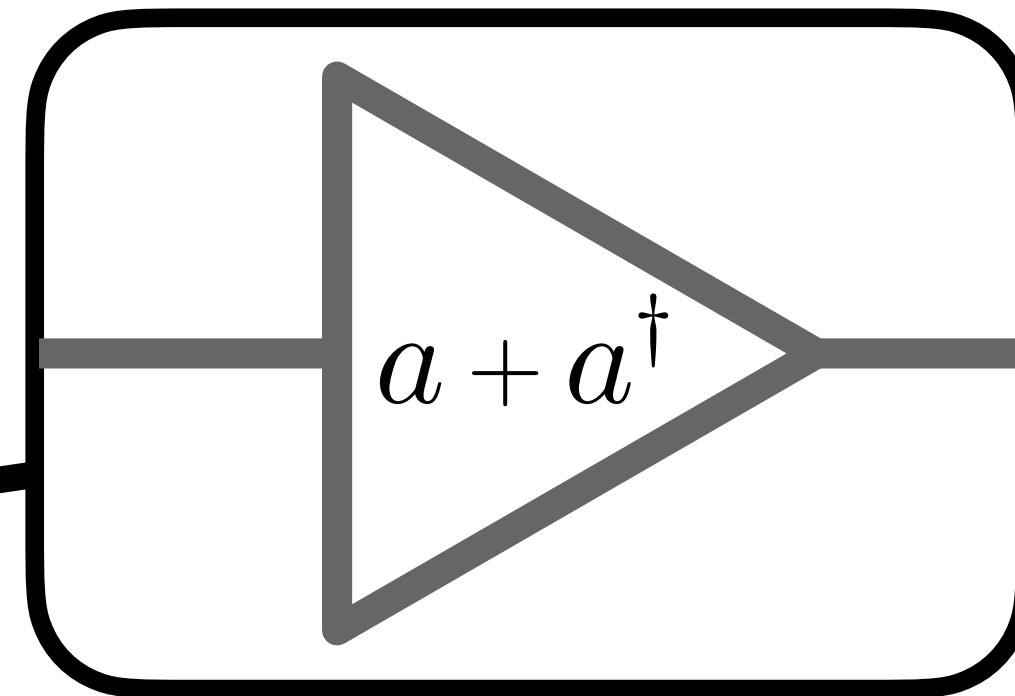




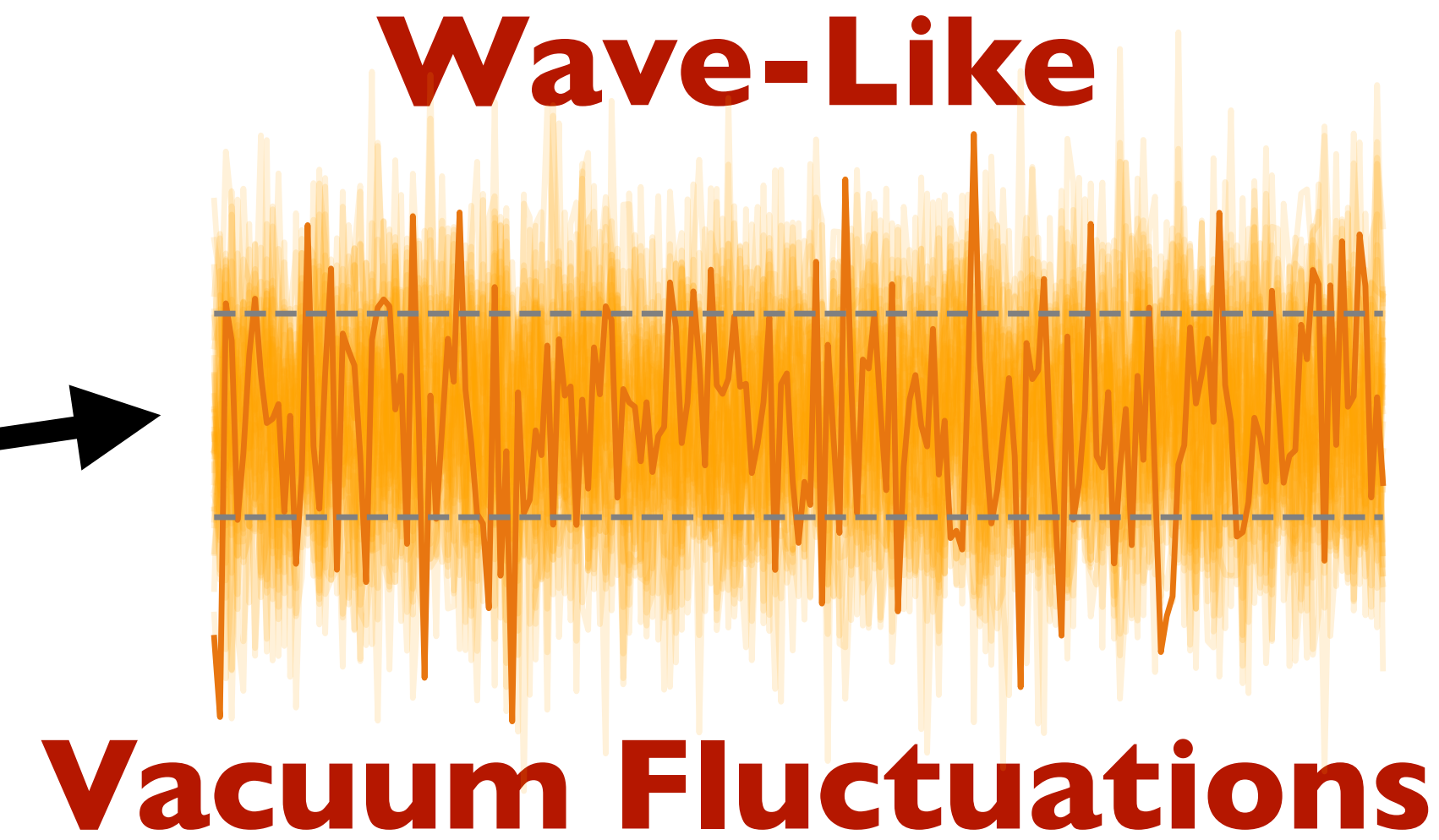
Vacuum

$$|0\rangle$$

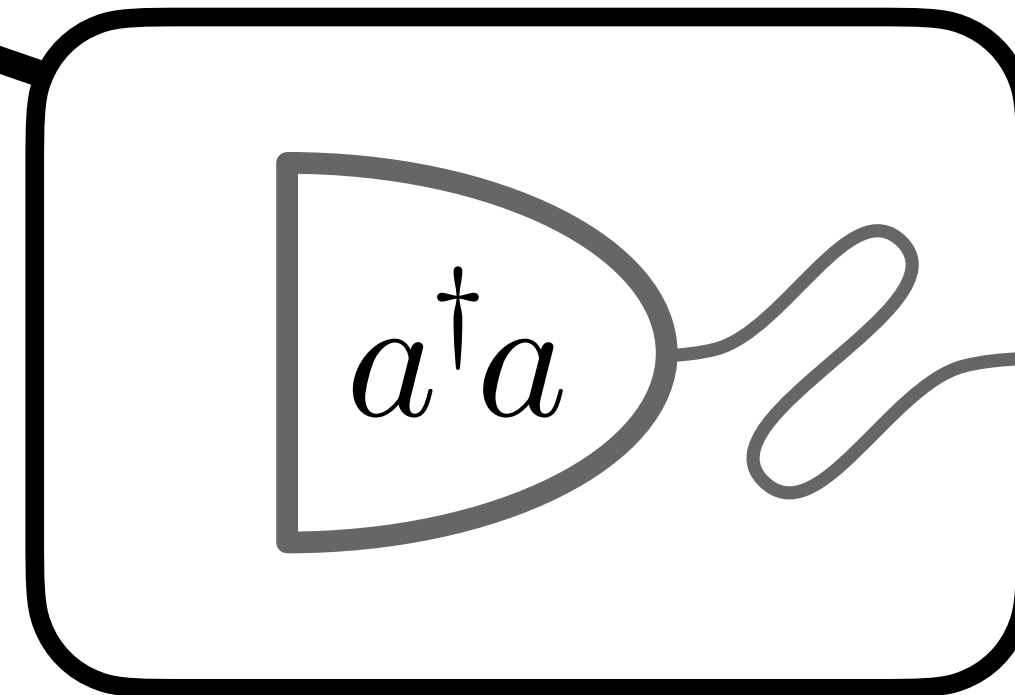
Field Detector



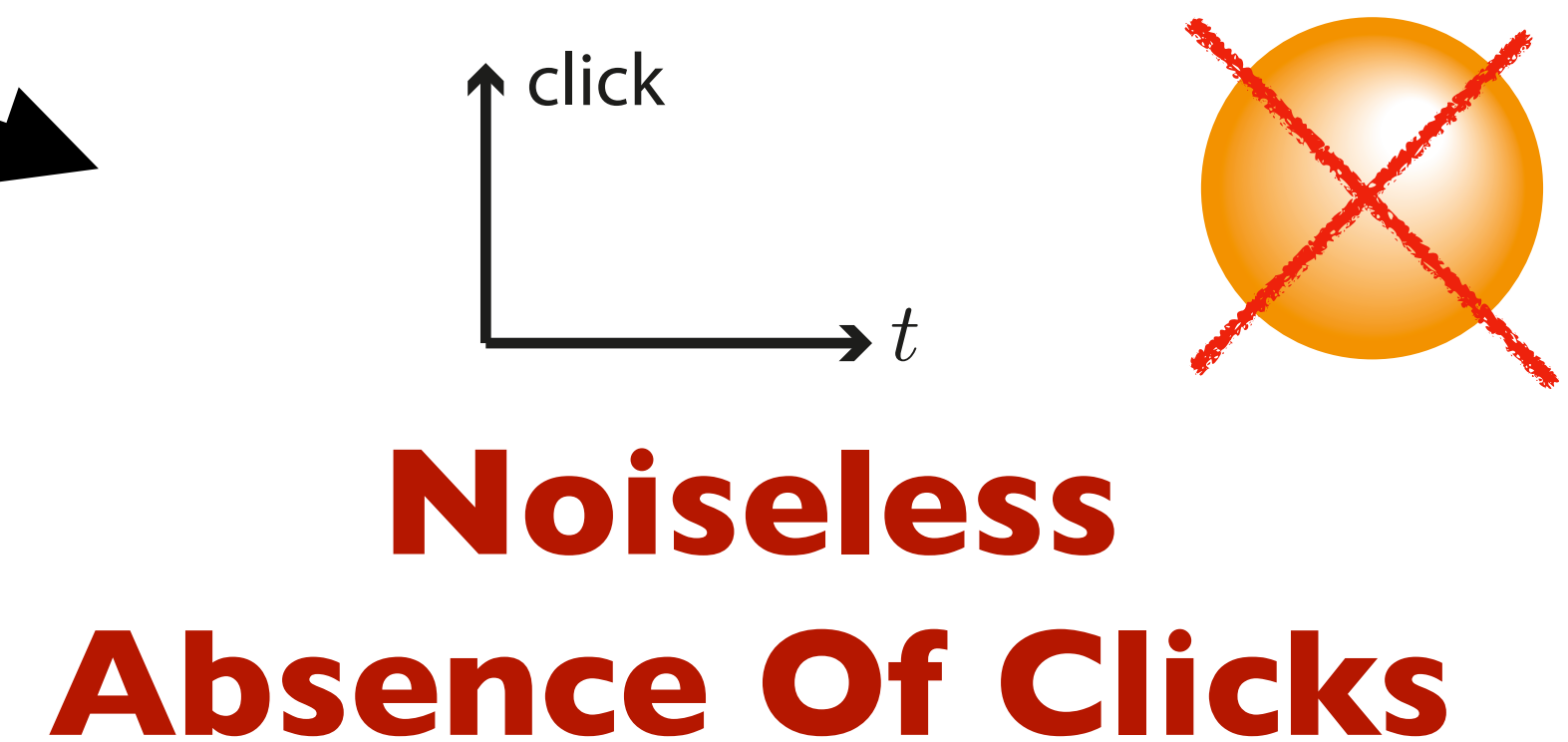
Wave-Like



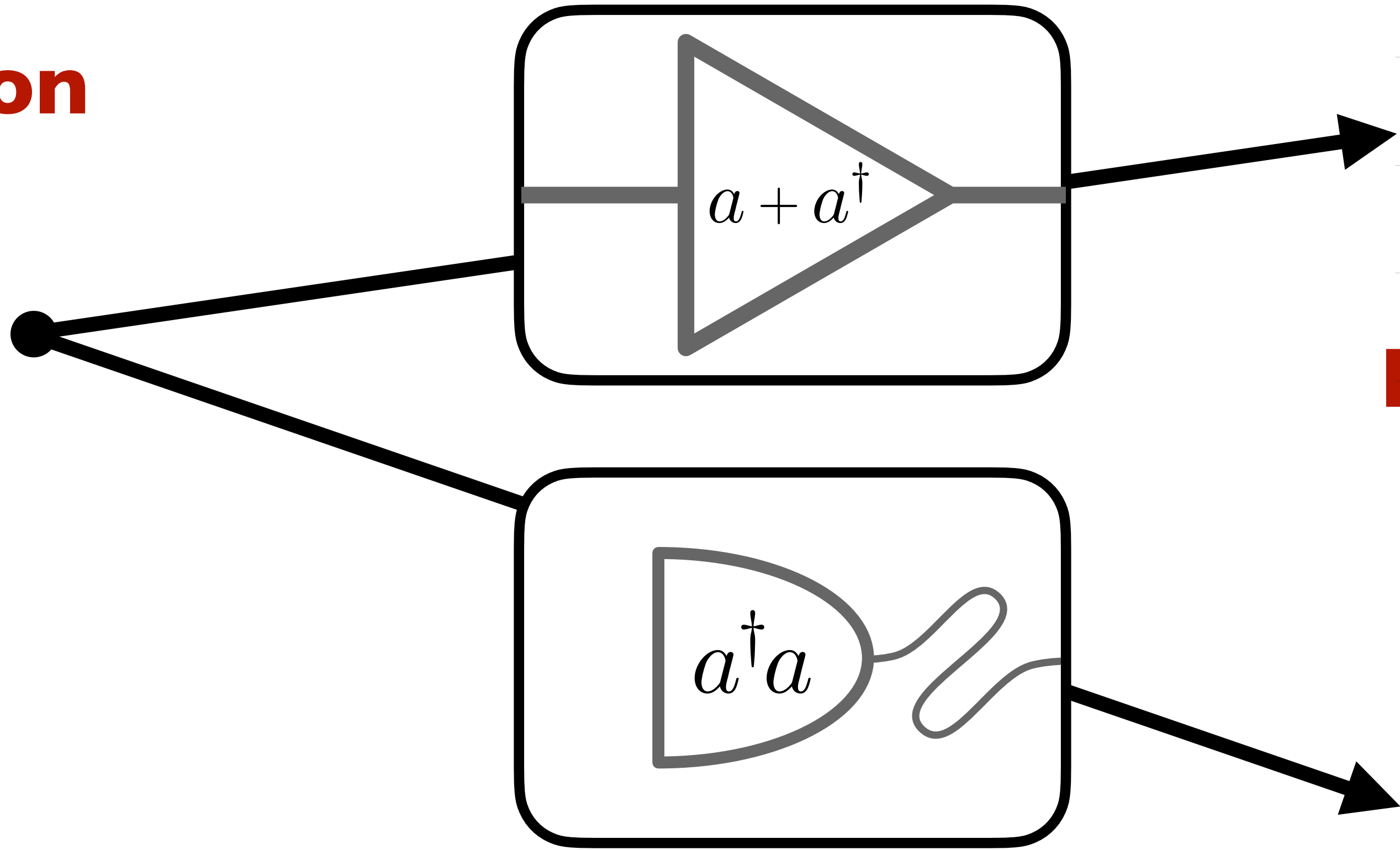
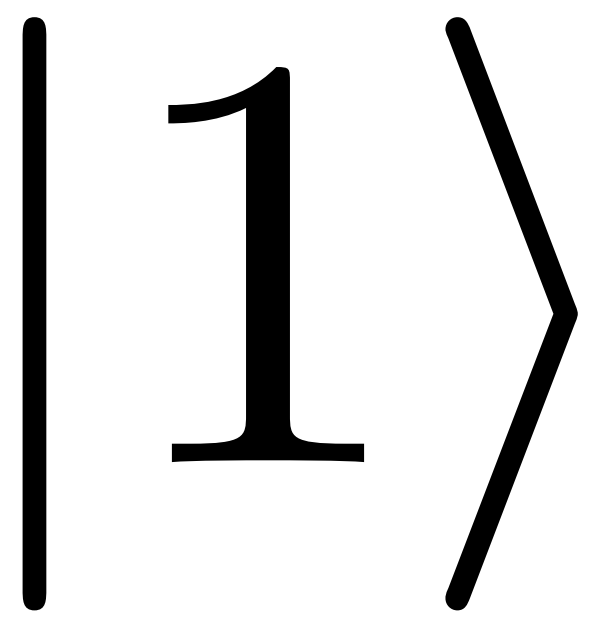
Photon Detector



Particle-Like



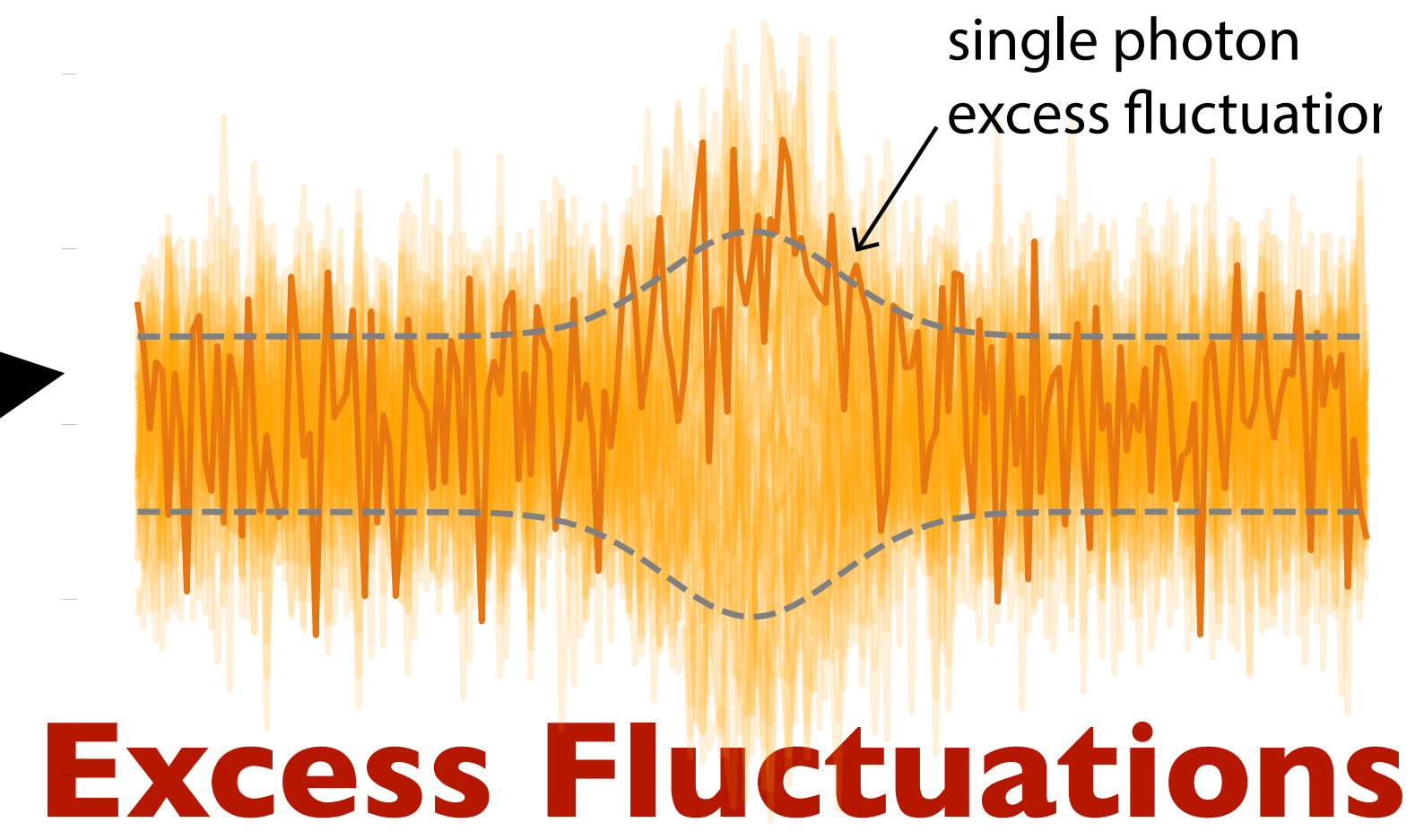
**Single Photon**



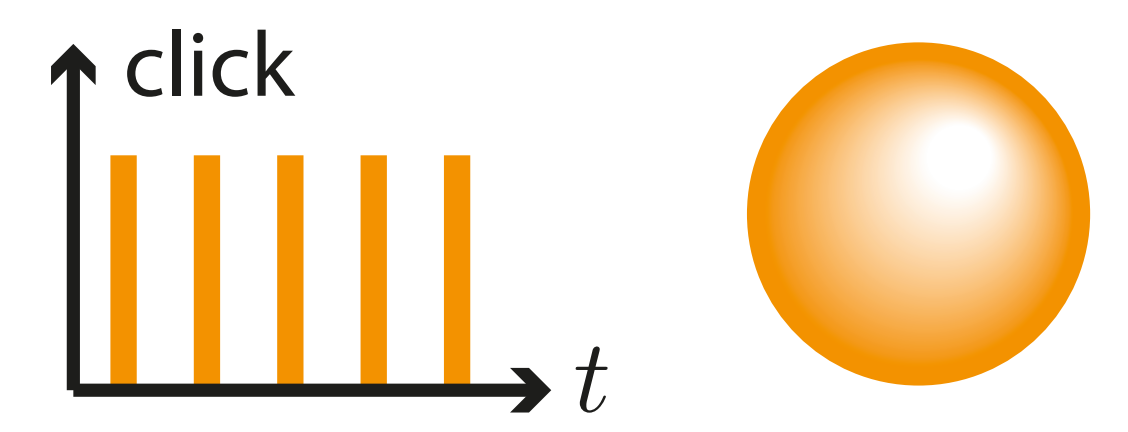
**Field Detector**

**Photon Detector**

**Wave-Like**



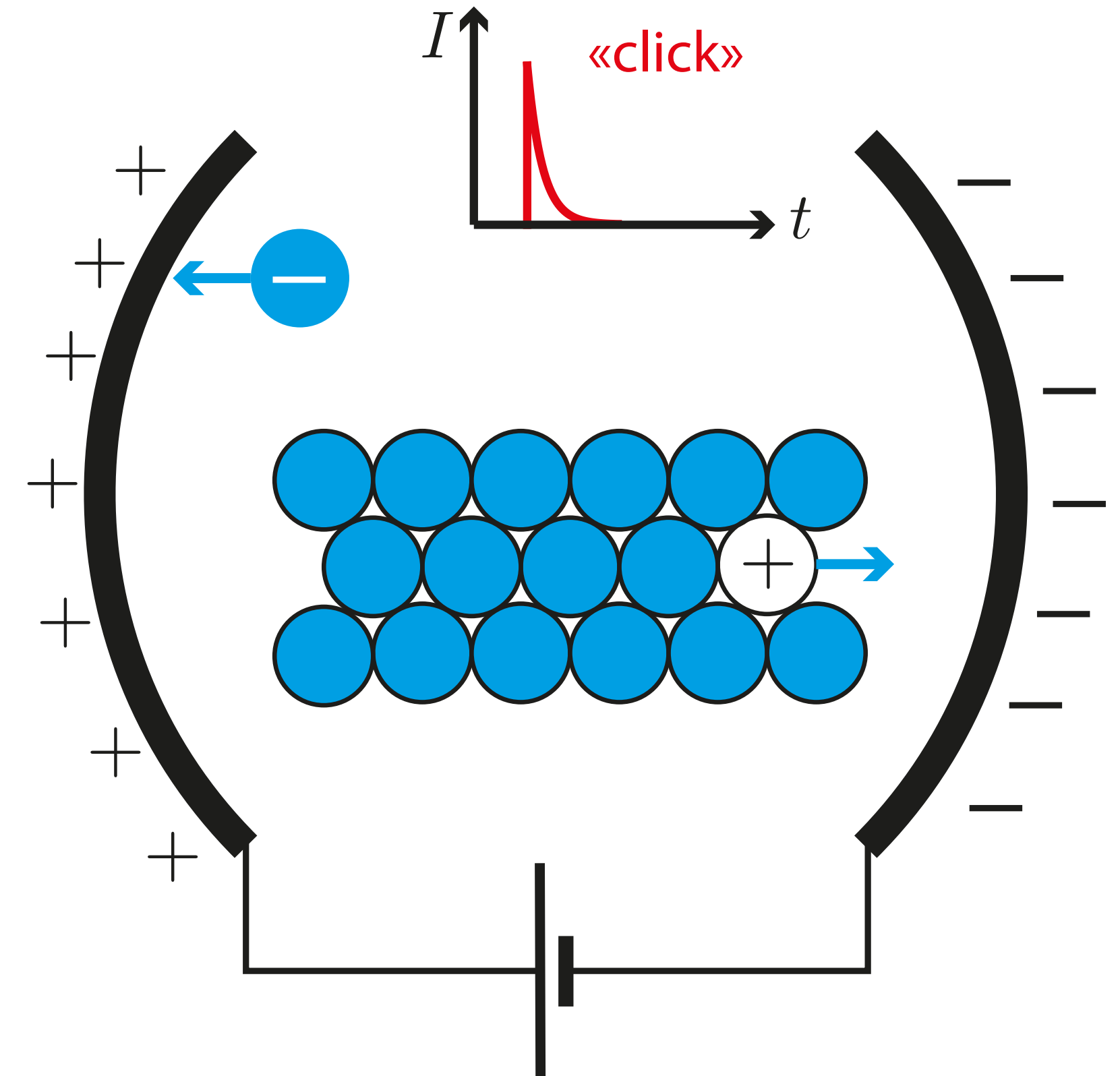
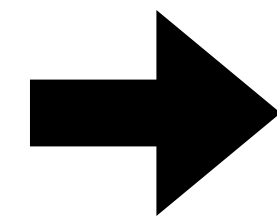
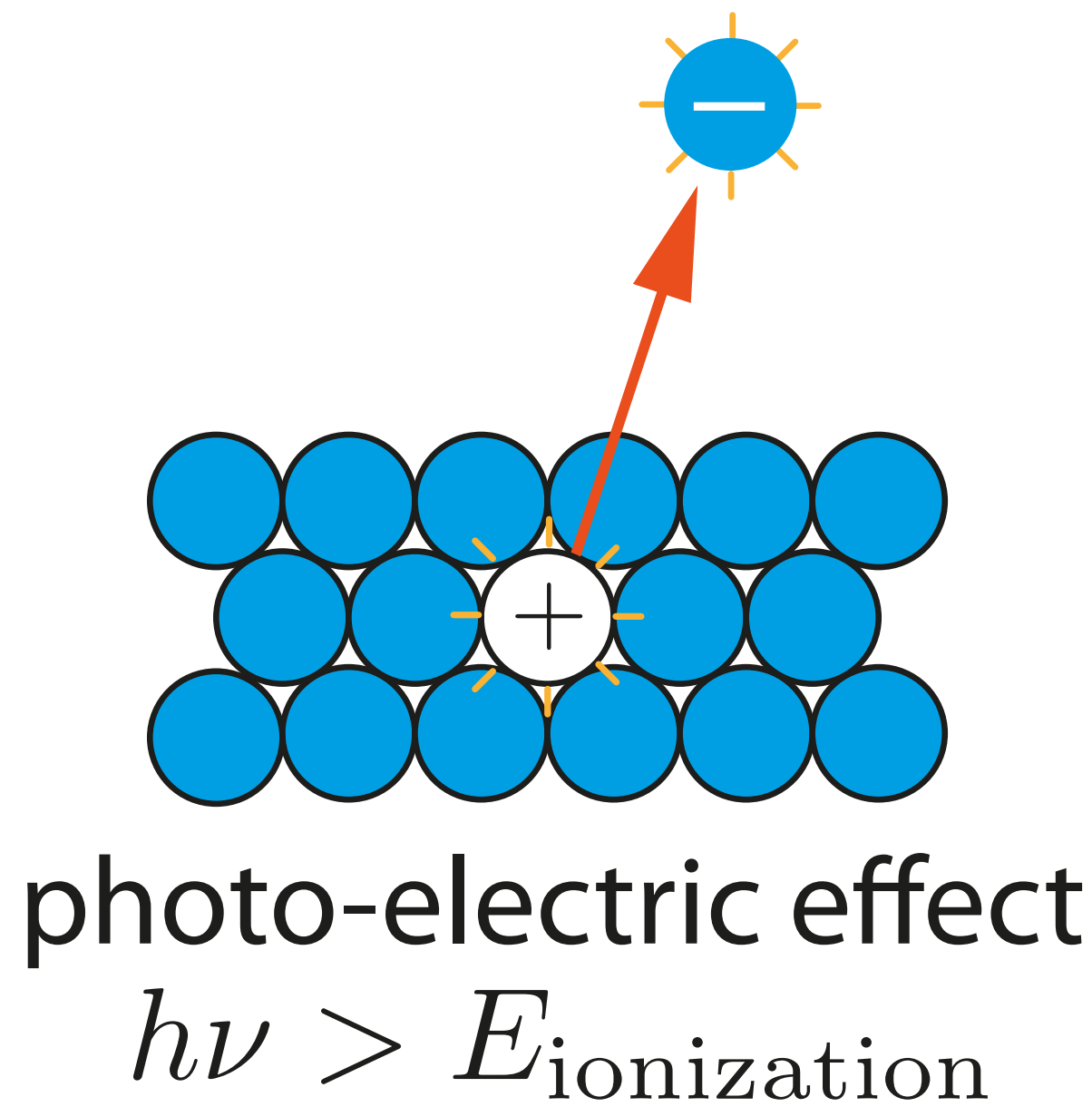
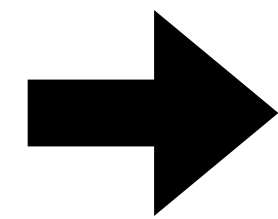
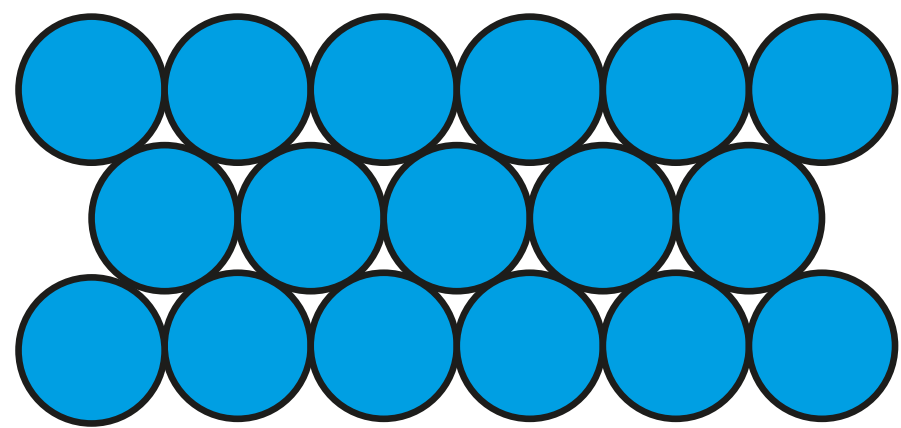
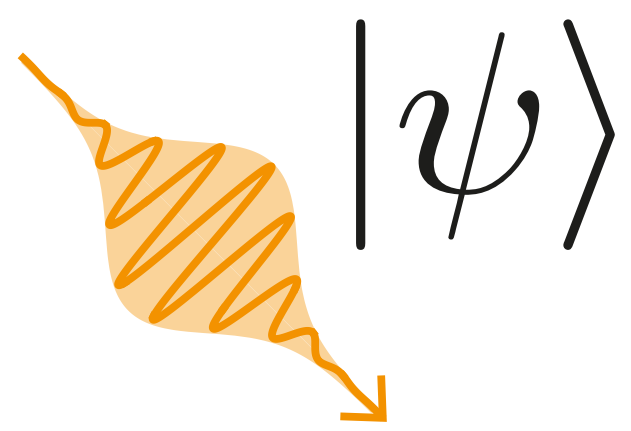
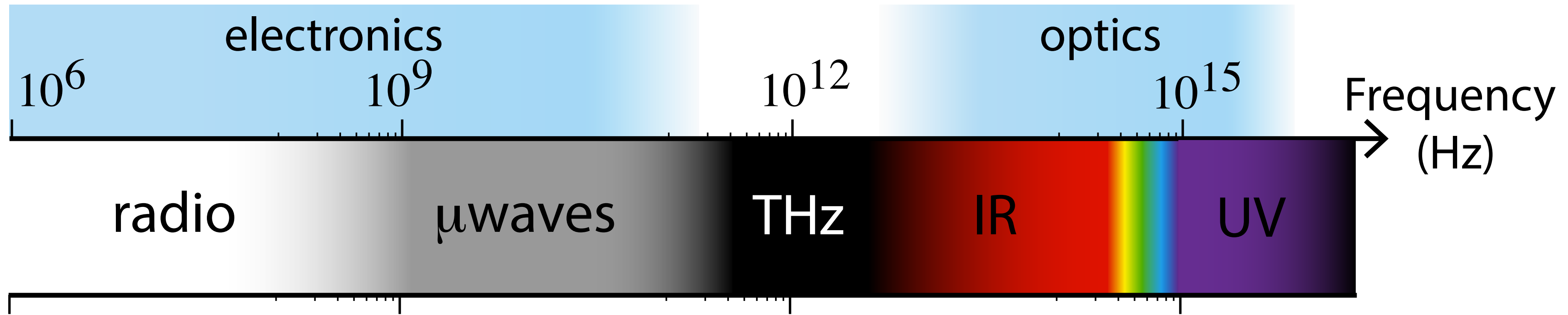
**Particle-Like**



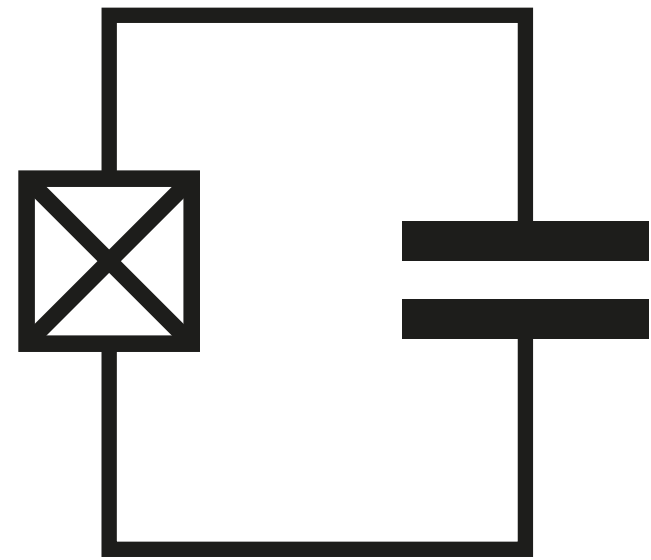
**Single Clicks**

# Photons

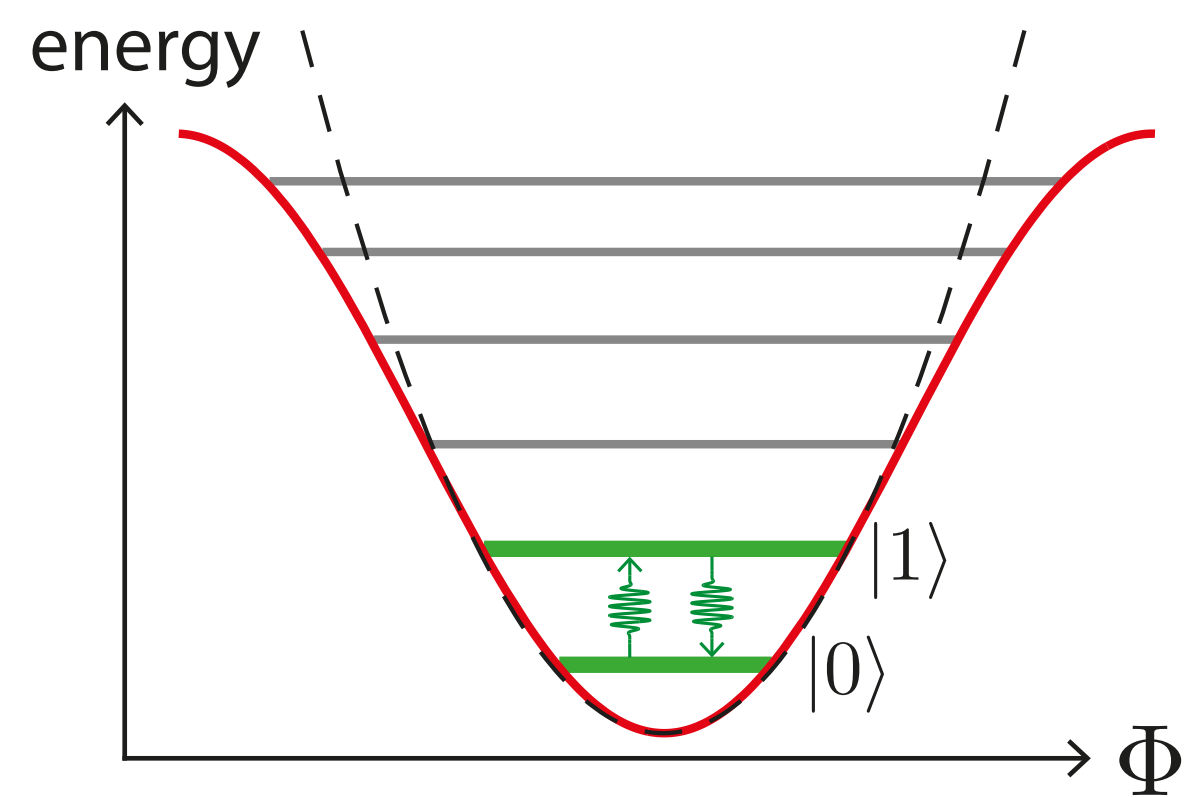
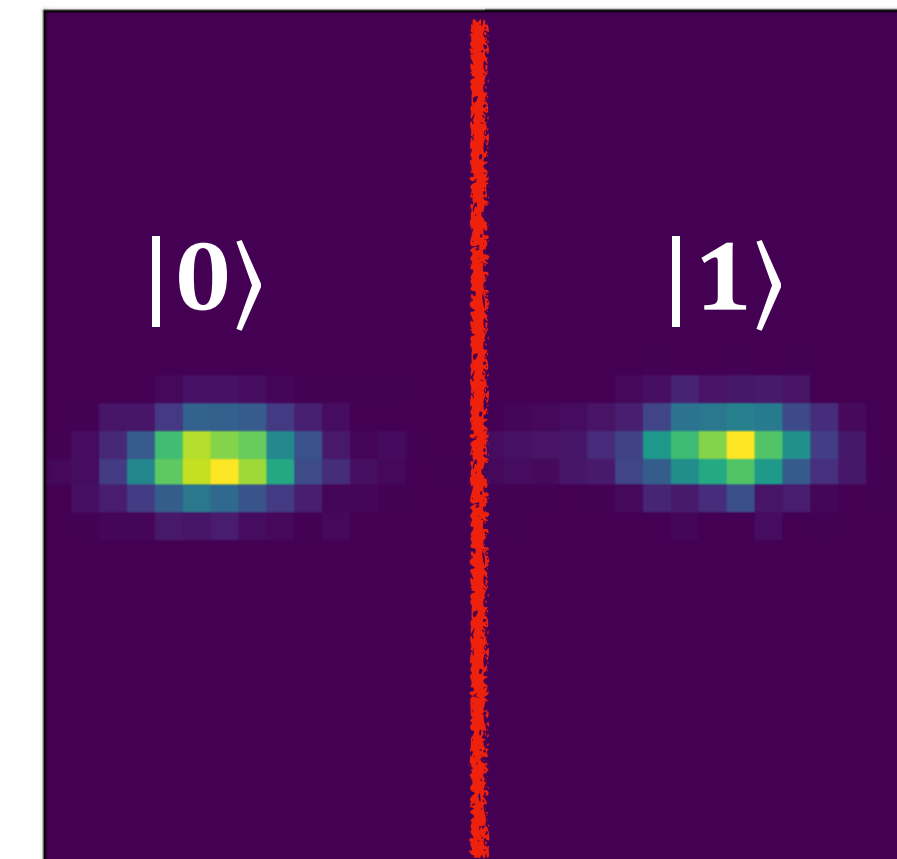
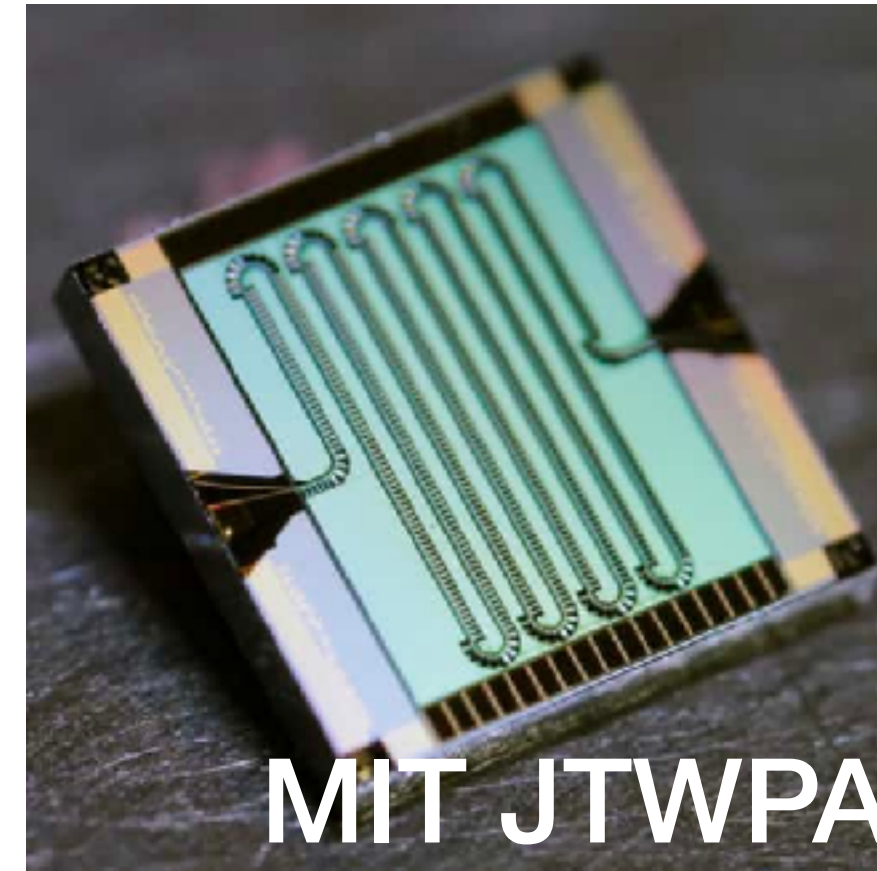
# Detecting Photons At Microwave Frequency



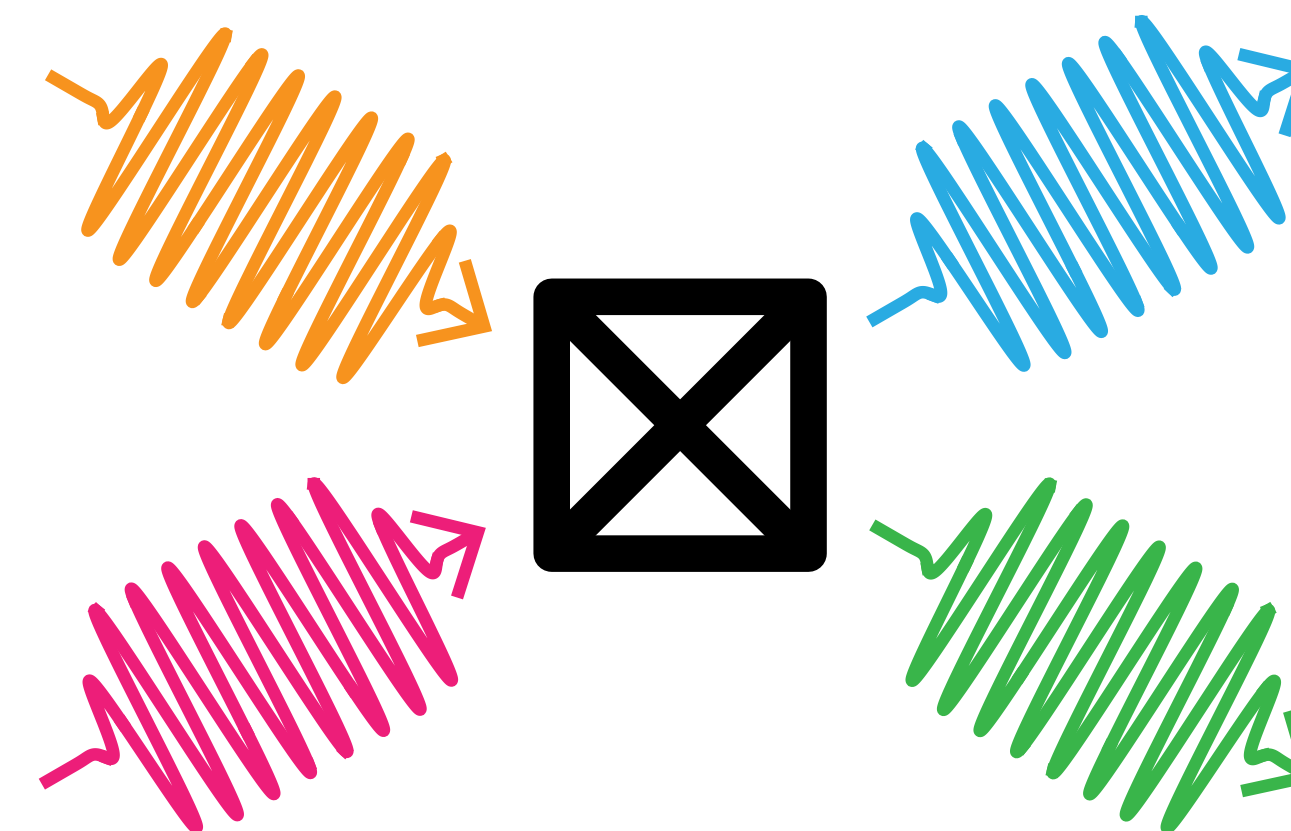
## Transmon qubit



## Quantum non-demolition measurement



## Built-in 4-wave-mixing

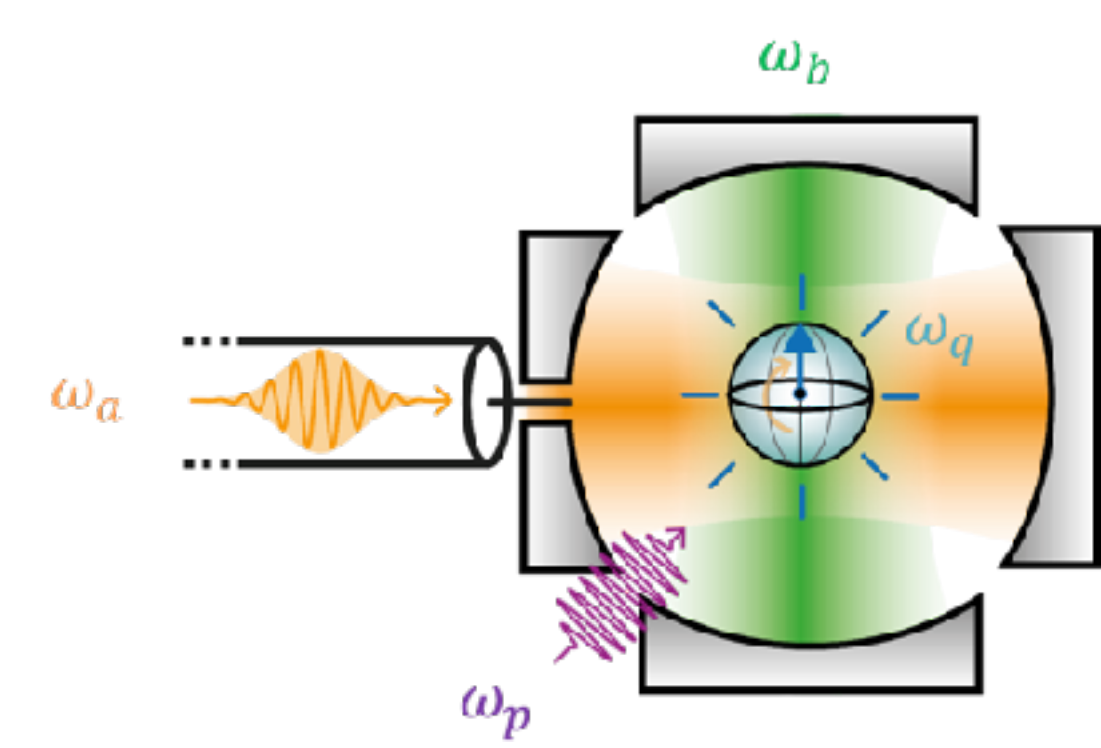


- [1] R. Lescanne et al., *PRX* (2020)
- [2] K. Inomata et al. *Nature com* (2016)
- [3] J.-C. Besse et al. arXiv:1711.11569v1 (2017)
- [4] Kono, S, et al. *Nature Physics* 14.6 (2018)
- [5] Opremcak, A., et al., *Science* 361.6408 (2018)

# Sample design



Léo Balembois



$$\frac{\omega_a}{2\pi} = 7 \text{ GHz}$$

$$Q_a = 5 \cdot 10^4$$

$$\chi_a = 5.4 \text{ MHz}$$

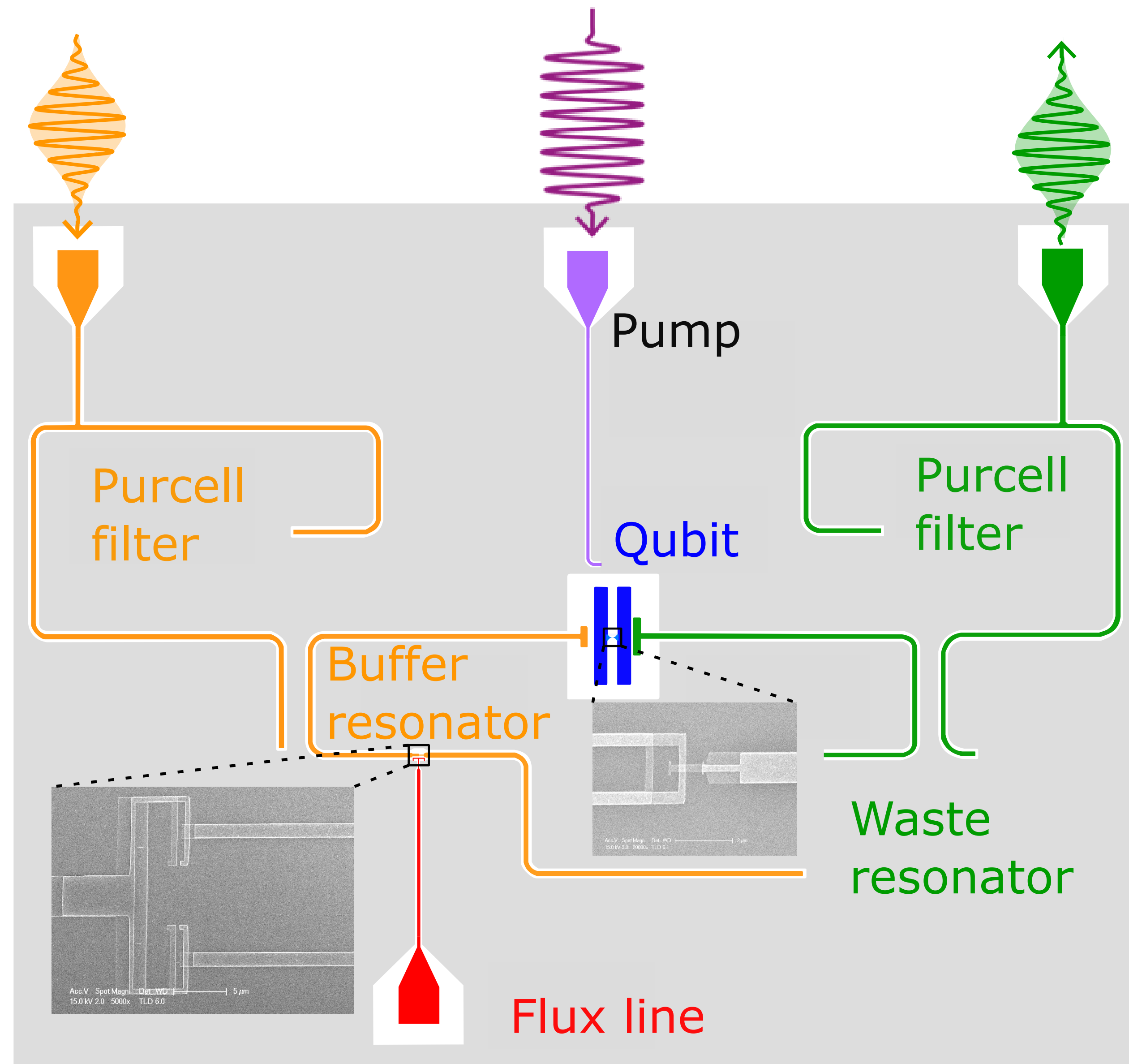
$$\frac{\omega_q}{2\pi} = 6,2 \text{ GHz}$$

$$T_1 = 30 \mu\text{s}$$

$$\frac{\omega_b}{2\pi} = 7,7 \text{ GHz}$$

$$Q_a = 4 \cdot 10^3$$

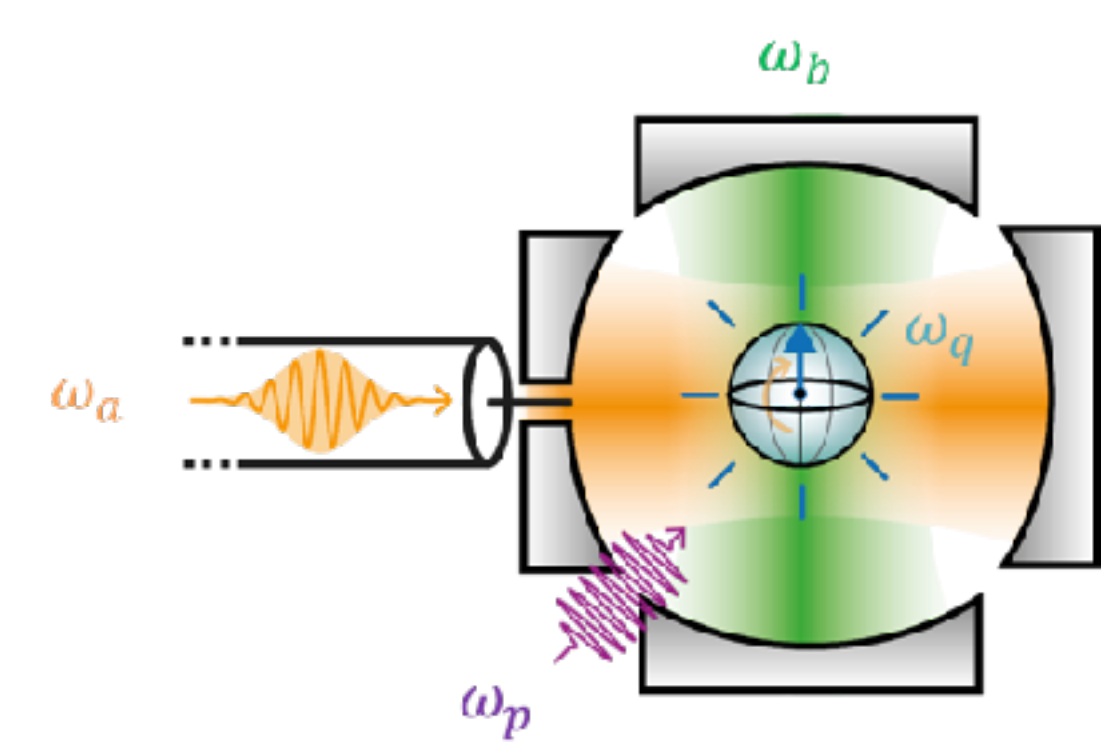
$$\chi_a = 19 \text{ MHz}$$



# Sample design



Léo Balembois



$$\frac{\omega_a}{2\pi} = 7 \text{ GHz}$$

$$Q_a = 5 \cdot 10^4$$

$$\chi_a = 5.4 \text{ MHz}$$

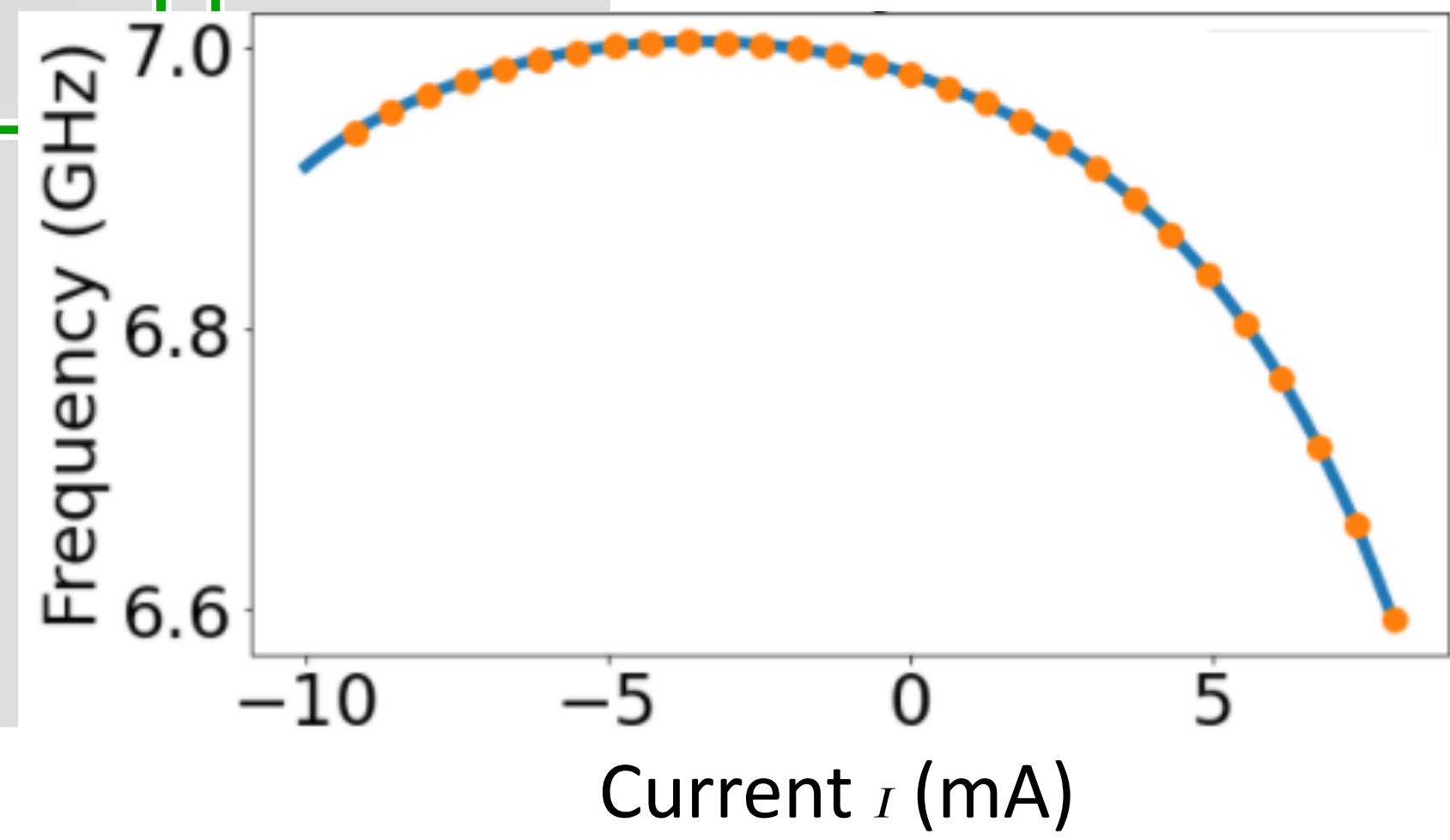
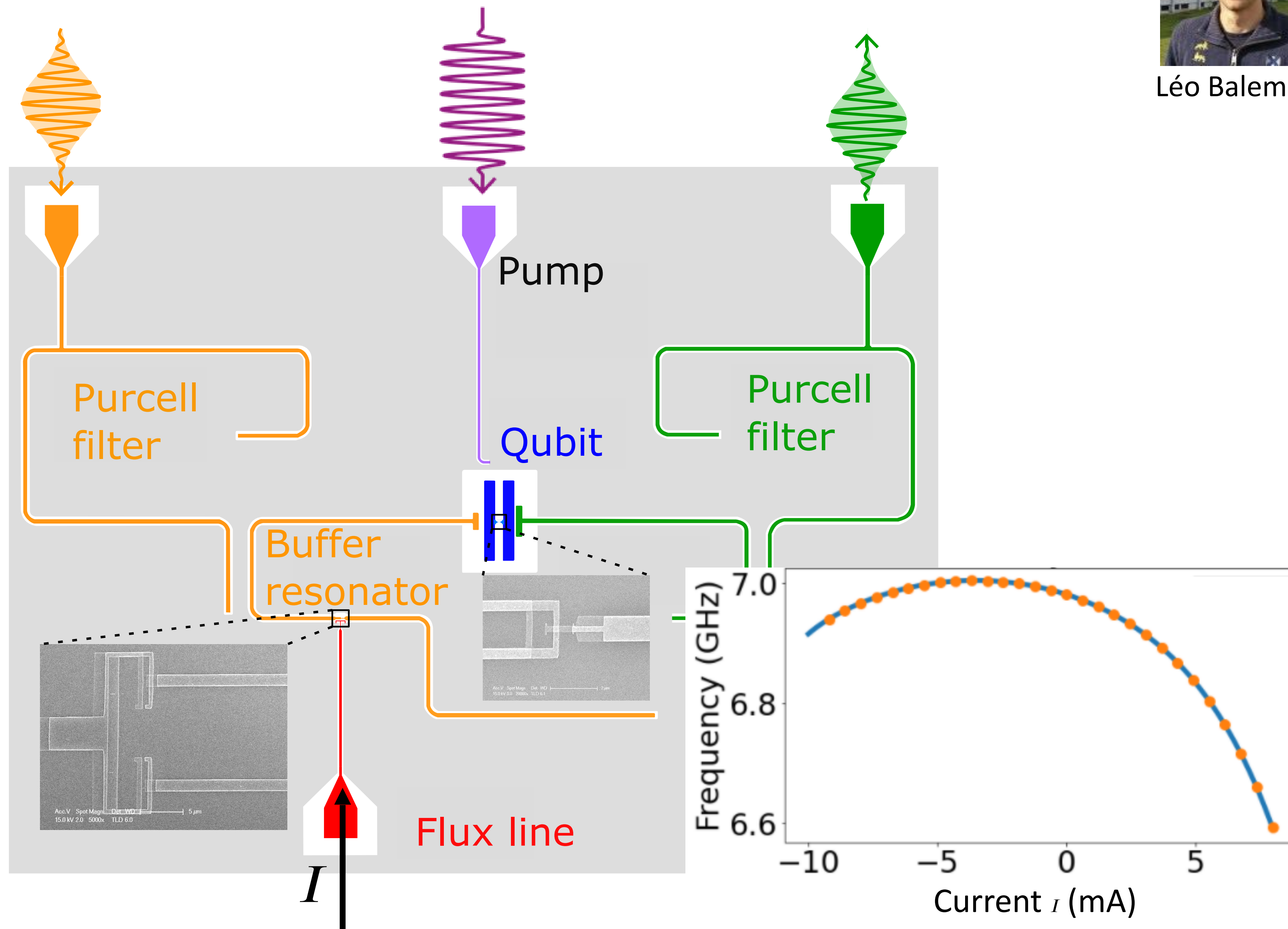
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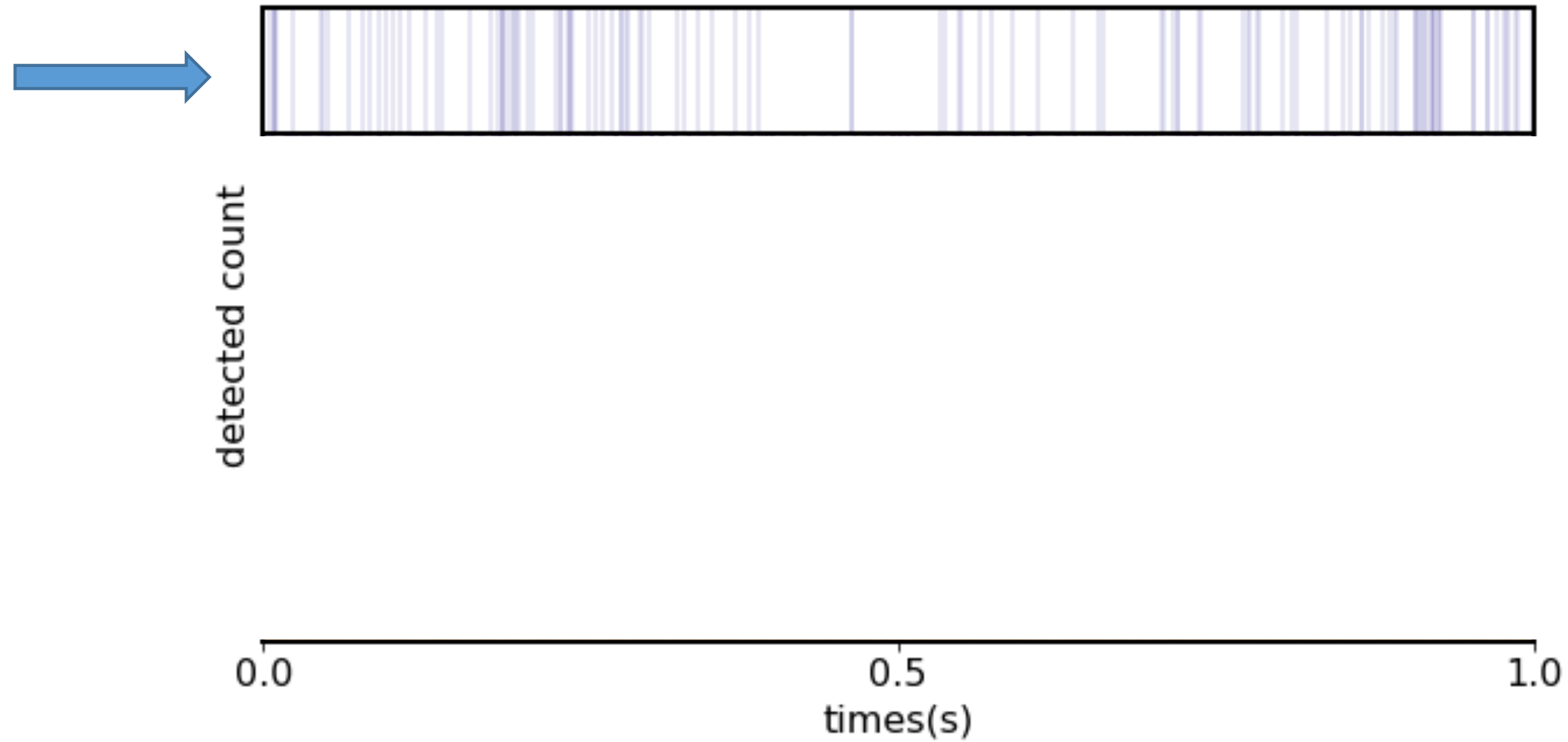
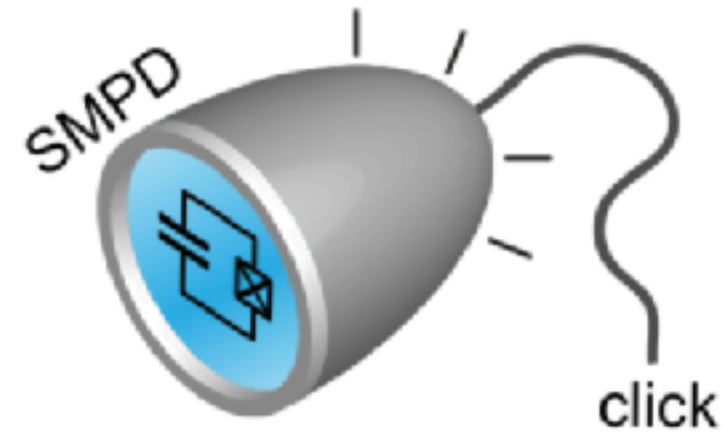
$$Q_a = 4 \cdot 10^3$$

$$\chi_a = 19 \text{ MHz}$$



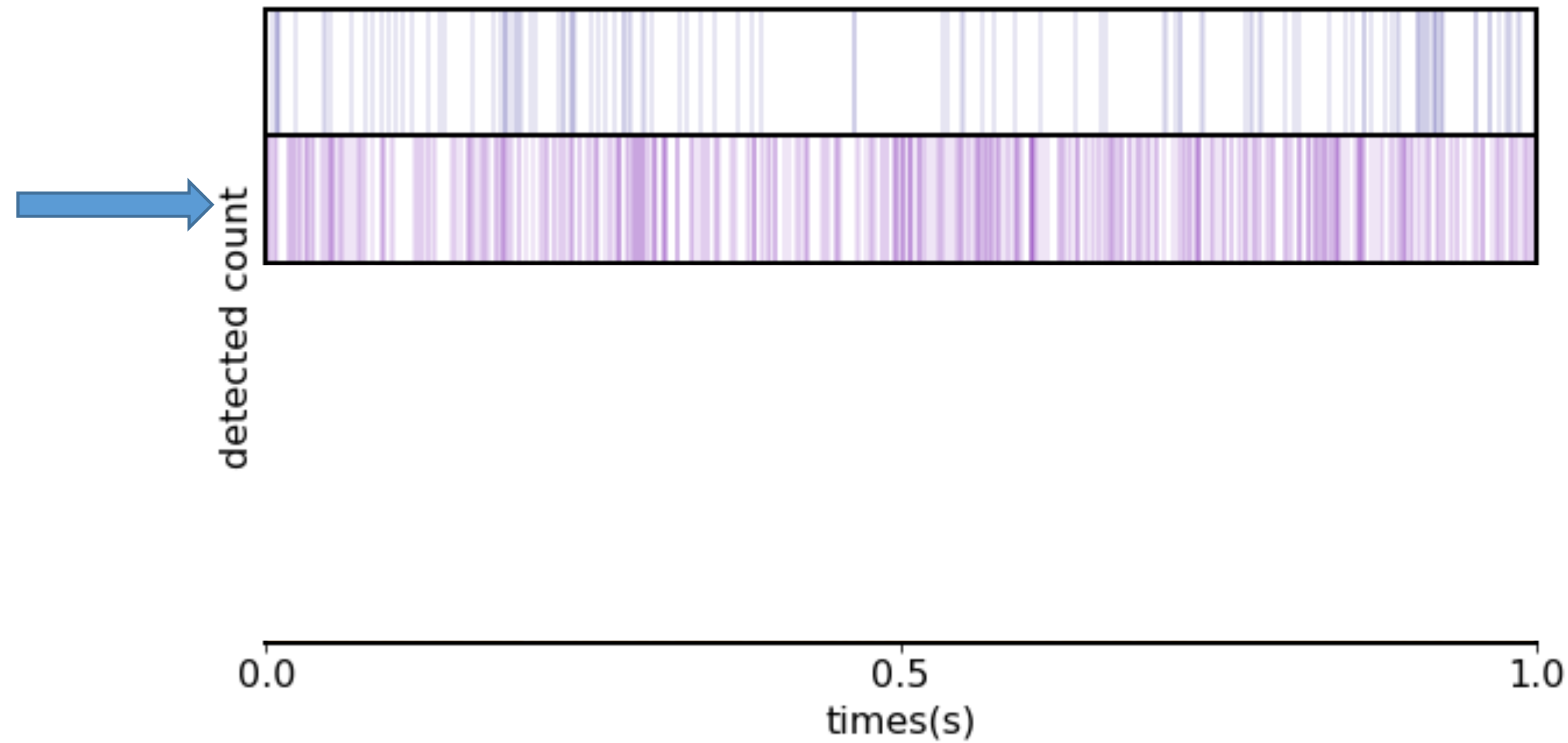
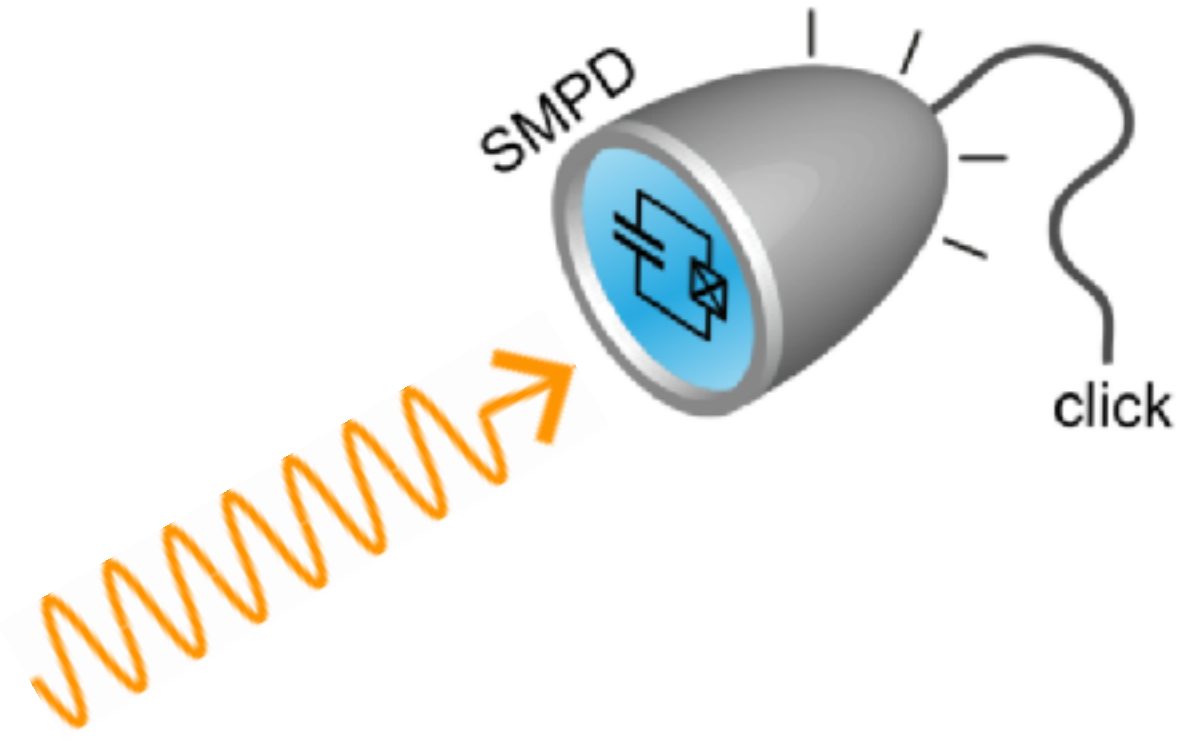
# Quantum efficiency and darkcount rate

Darkcount rate  $\alpha = 85 \text{ s}^{-1}$



# Efficacité quantique et taux de compte d'obscurité

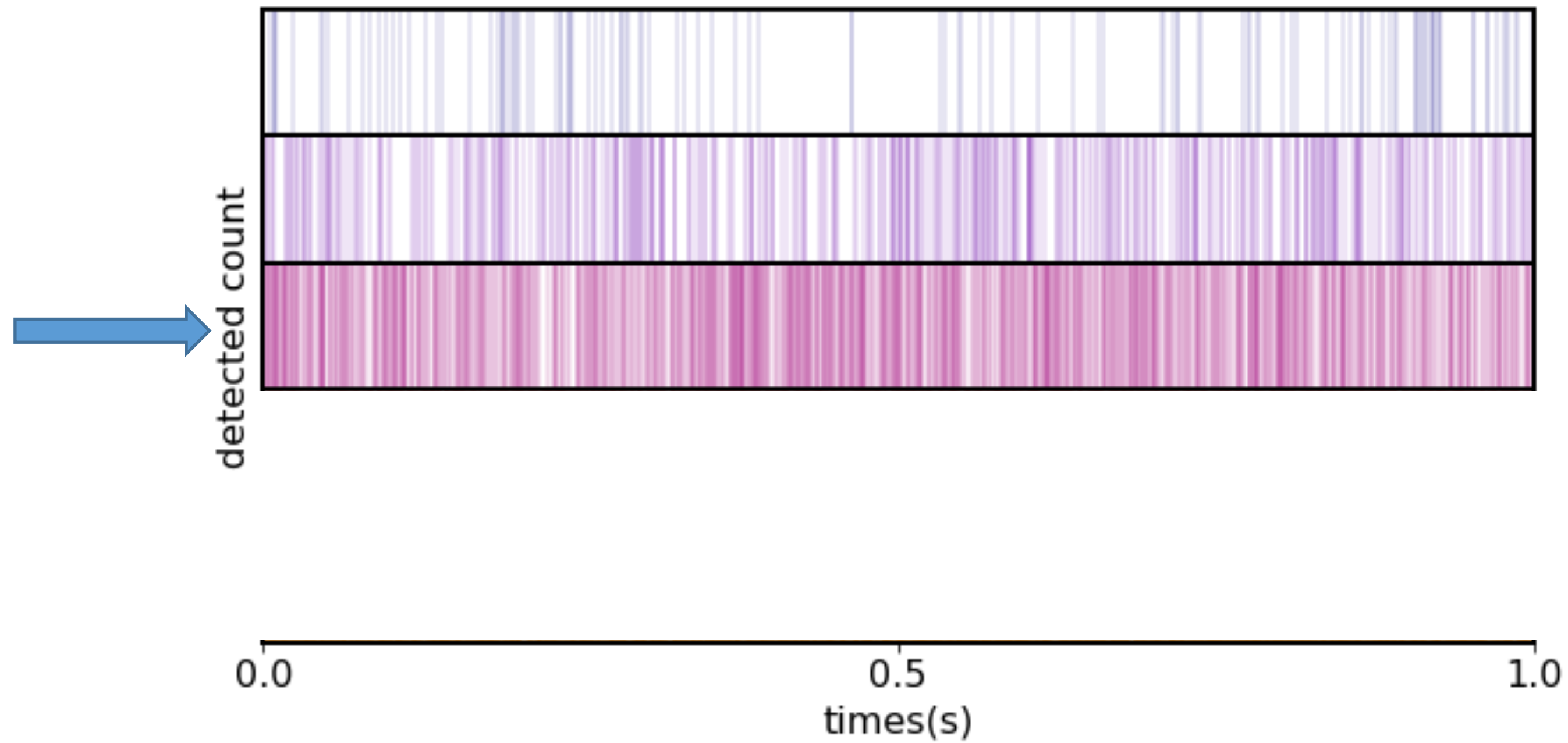
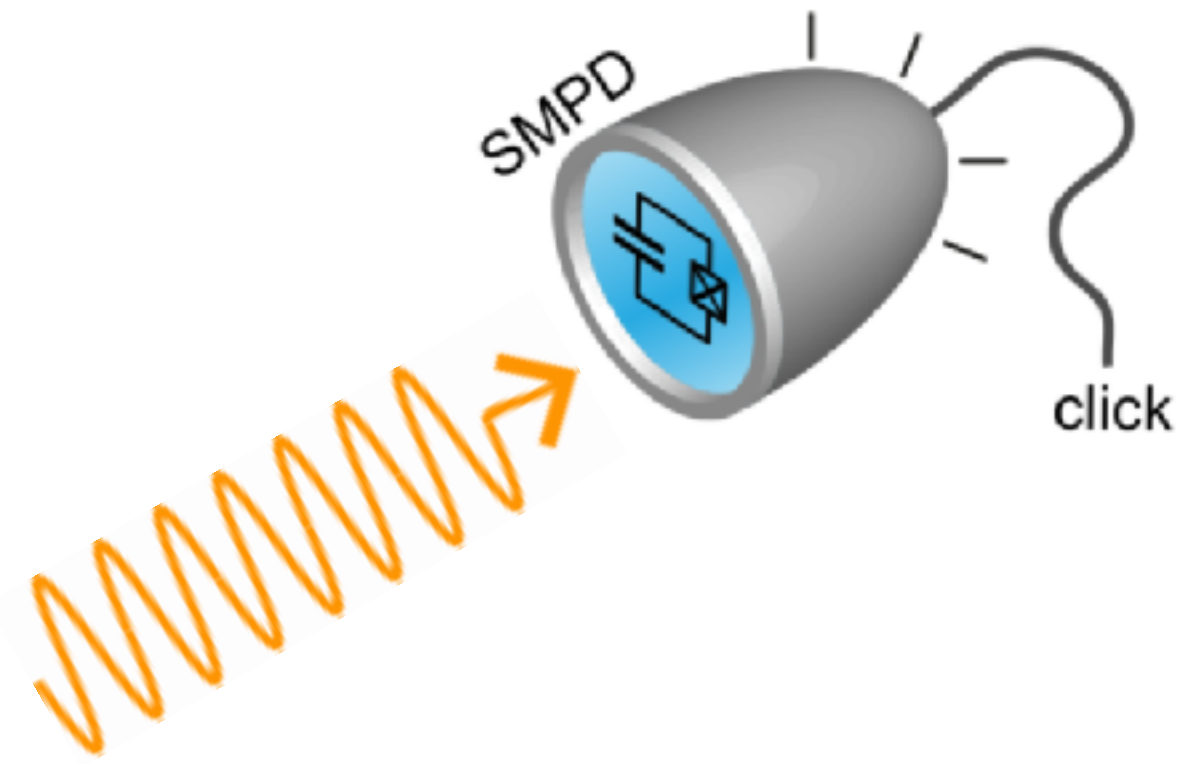
Darkcount rate  $\alpha = 85 \text{ s}^{-1}$





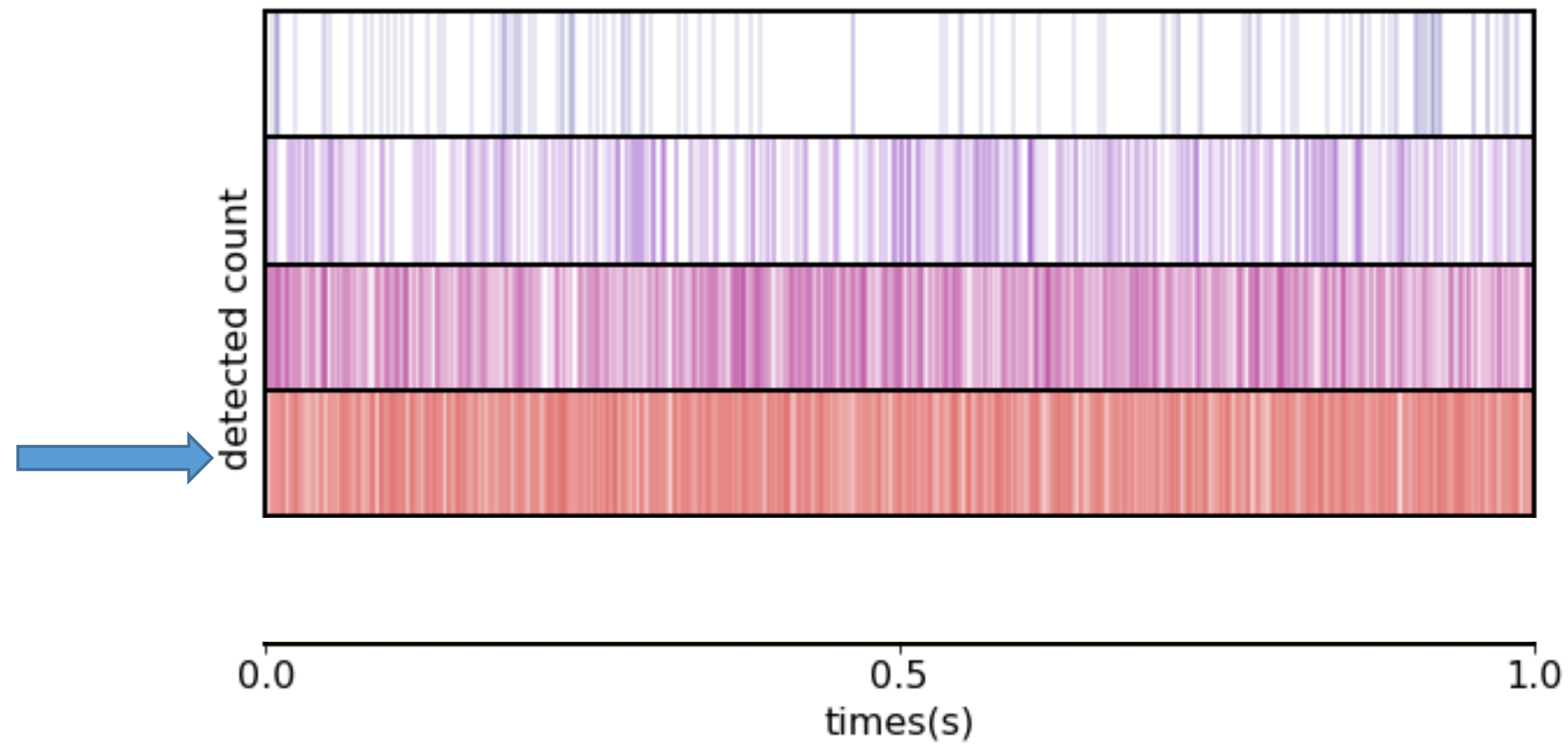
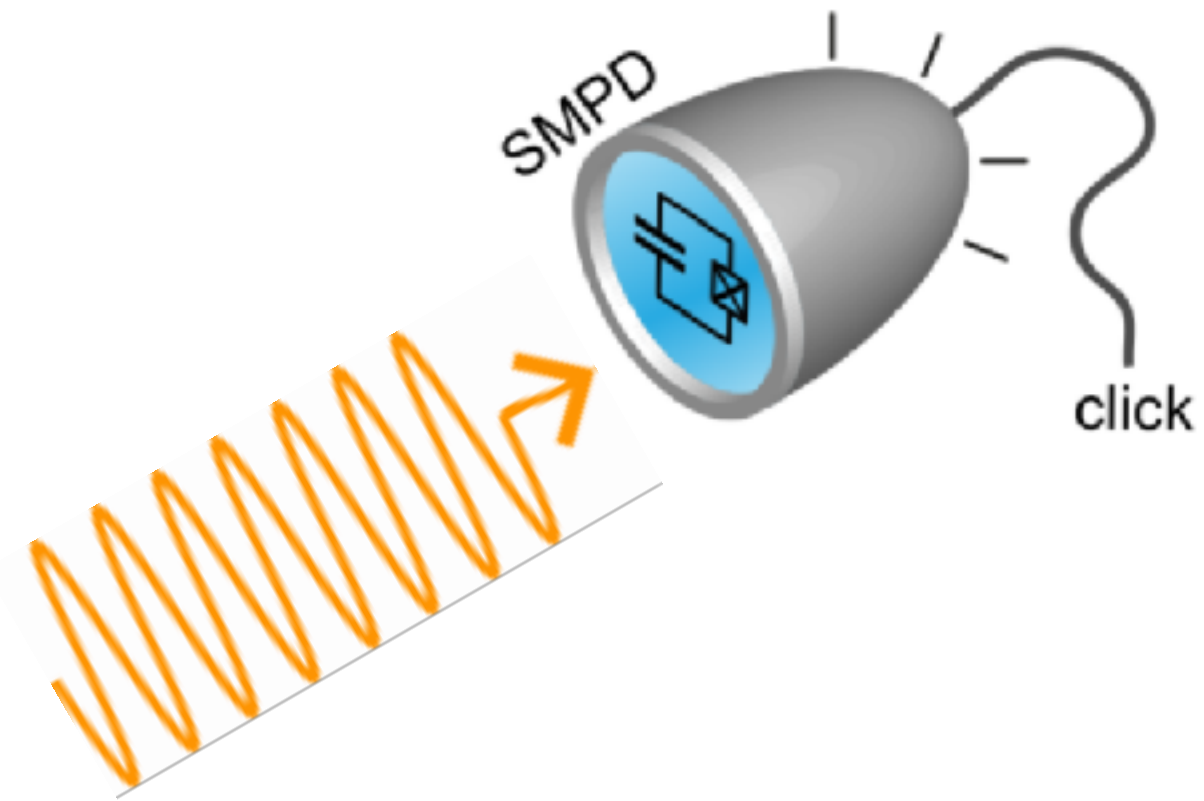
# Efficacité quantique et taux de compte d'obscurité

Darkcount rate  $\alpha = 85 \text{ s}^{-1}$



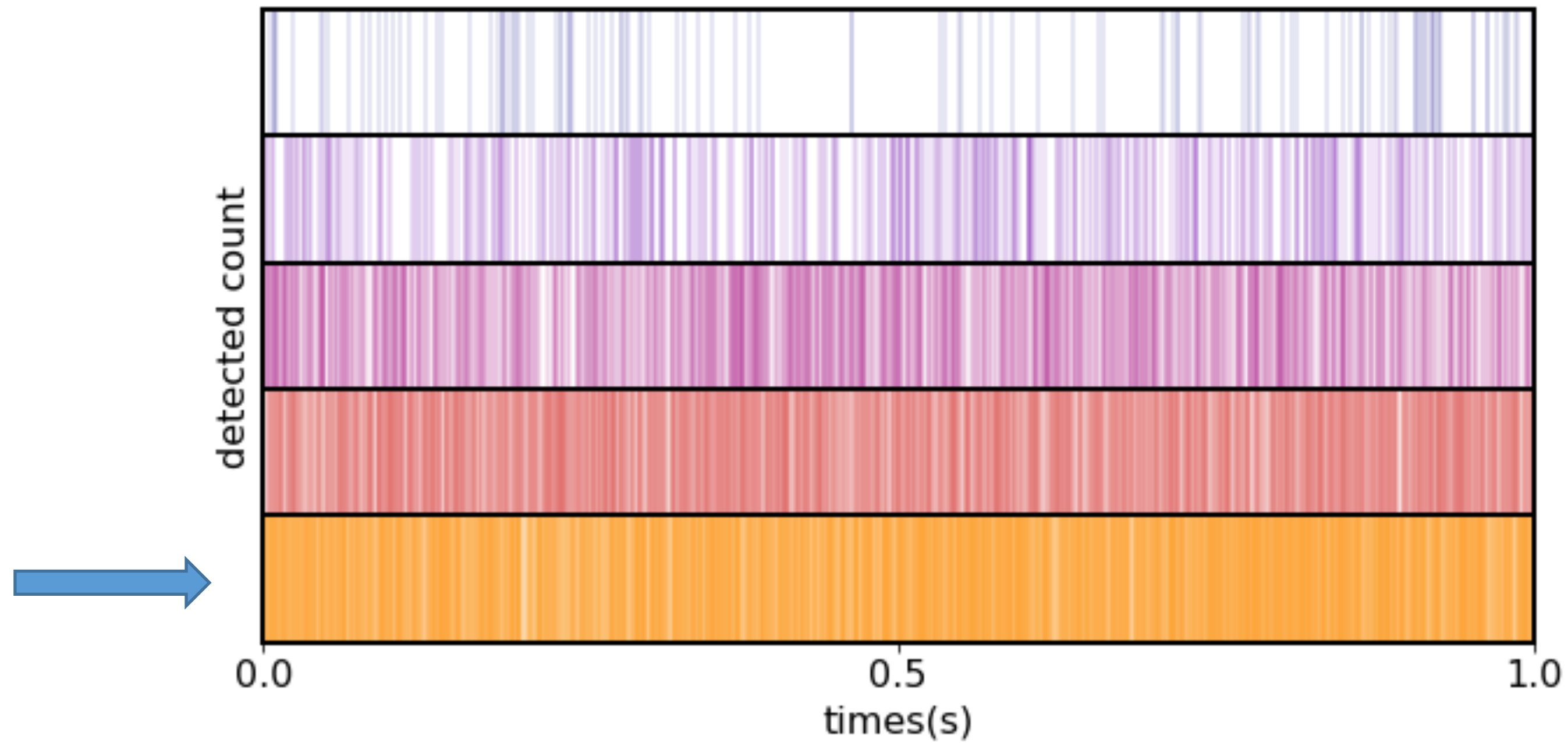
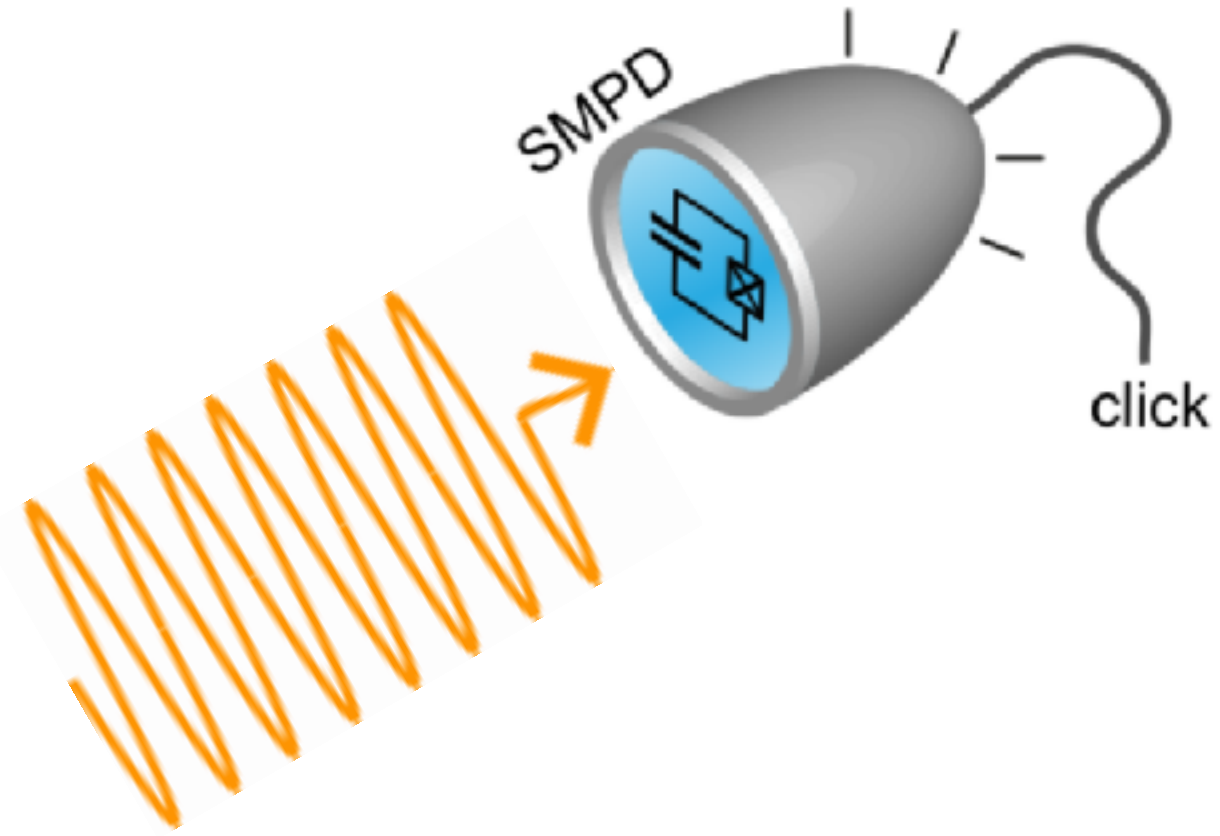
# Efficacité quantique et taux de compte d'obscurité

Darkcount rate  $\alpha = 85 \text{ s}^{-1}$

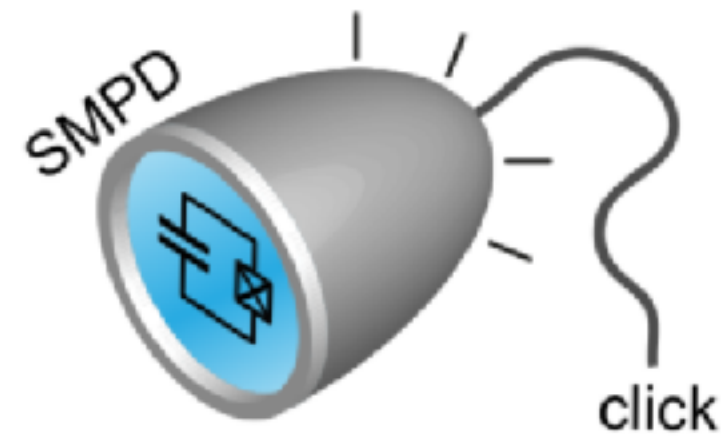


# Efficacité quantique et taux de compte d'obscurité

Darkcount rate  $\alpha = 85 \text{ s}^{-1}$

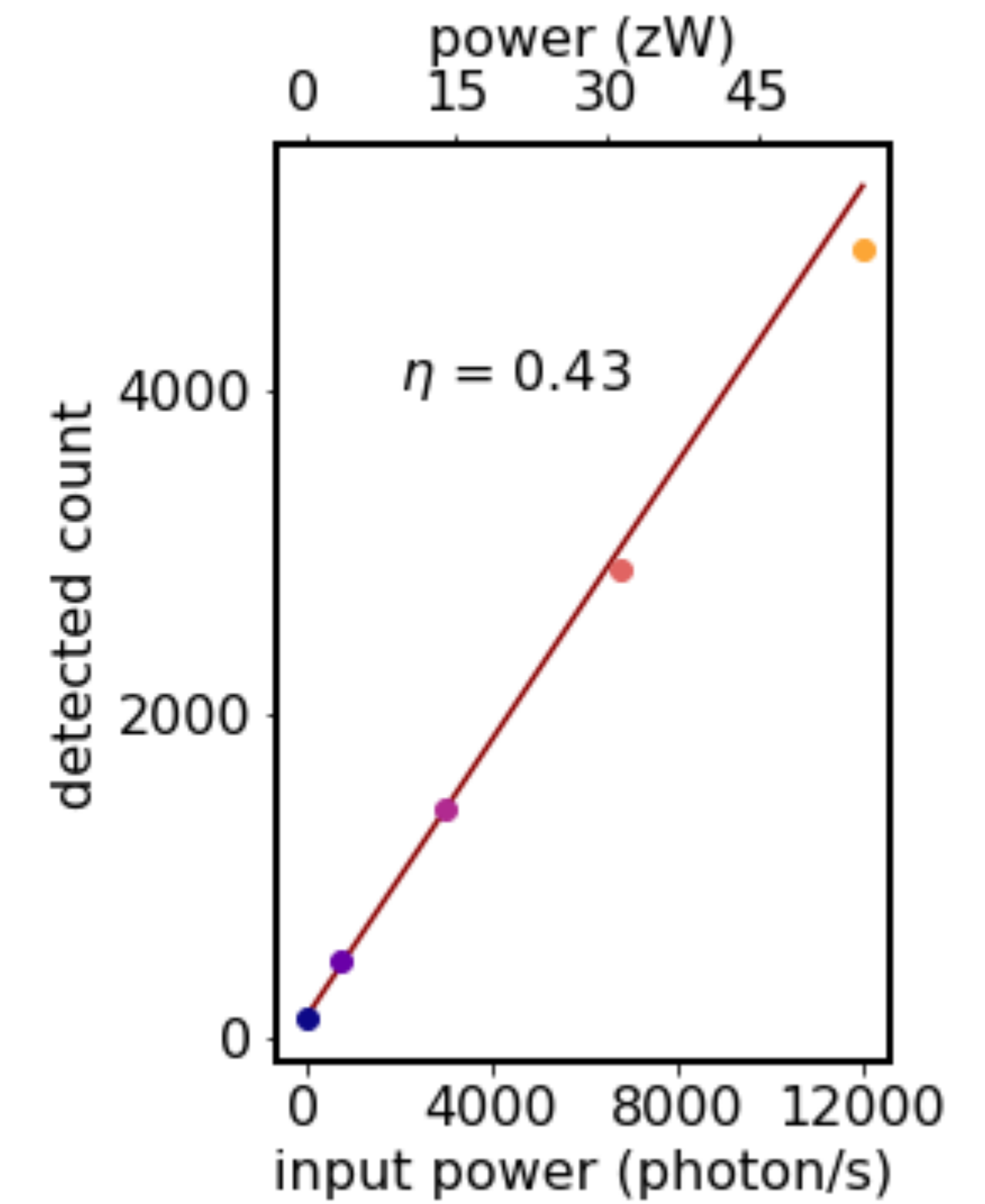
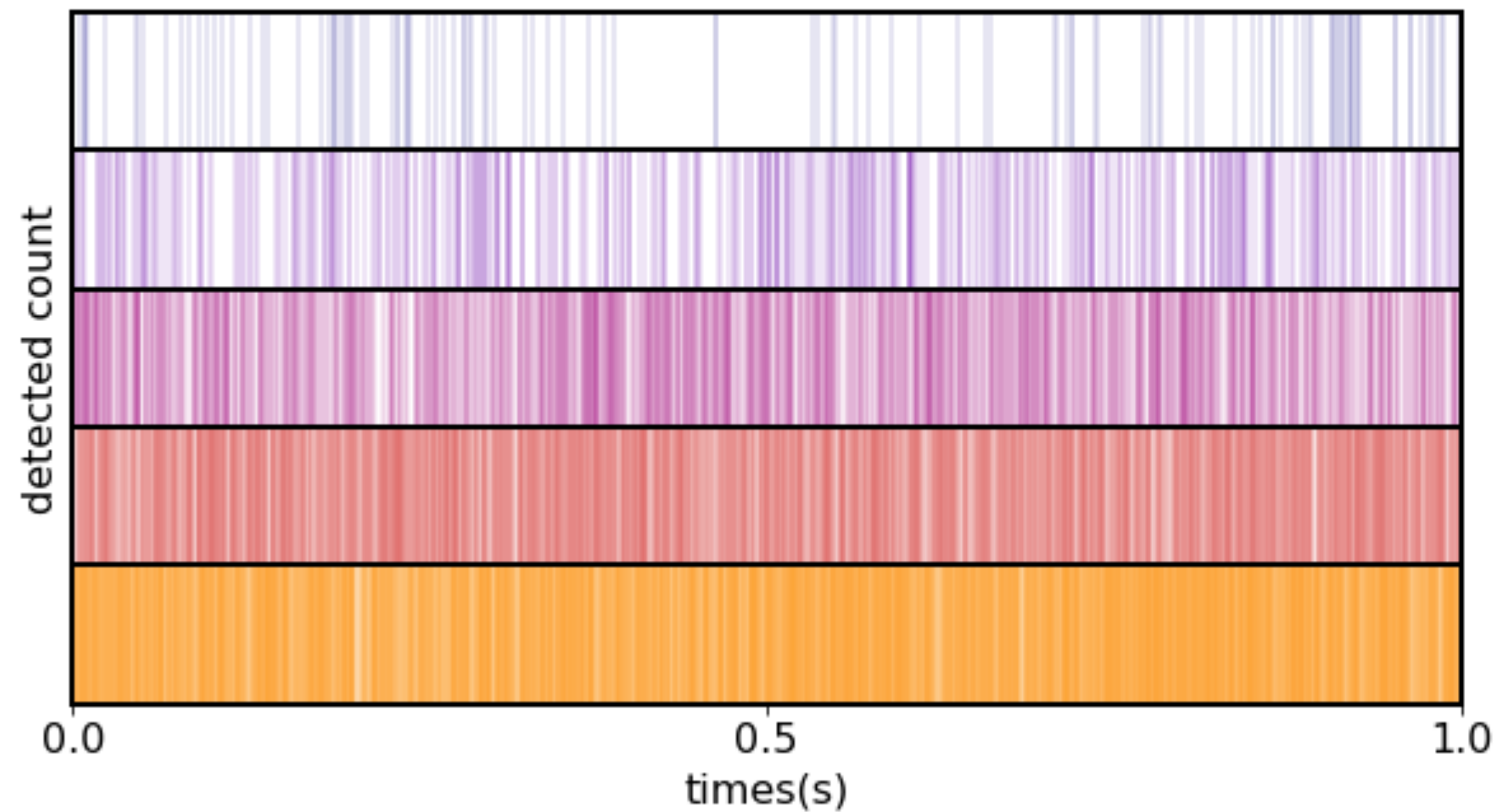


# Efficacité quantique et taux de compte d'obscurité

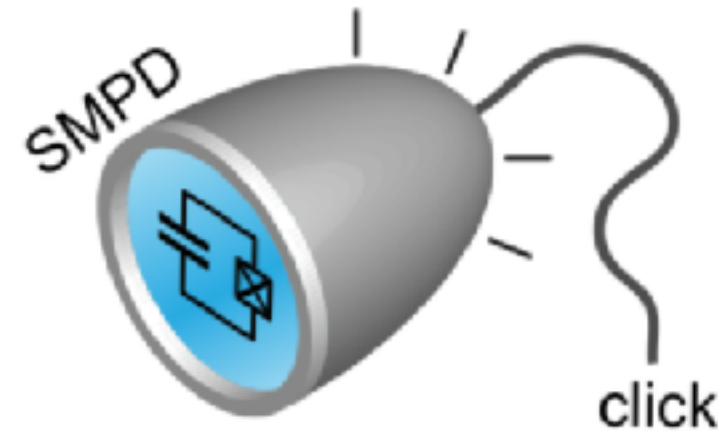


Darkcount rate  $\alpha = 85 \text{ s}^{-1}$

Operational Efficiency :  $\eta = 45\%$



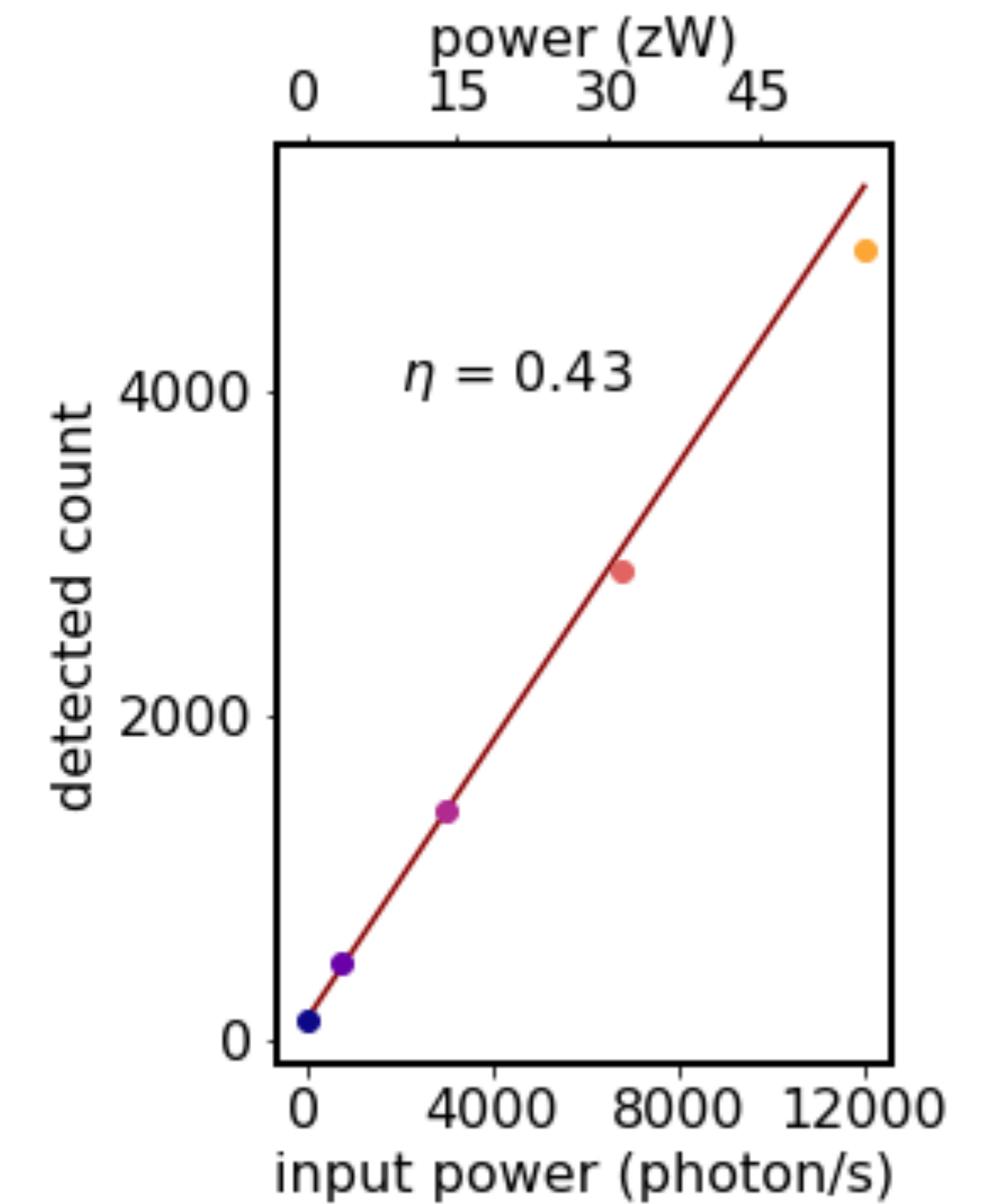
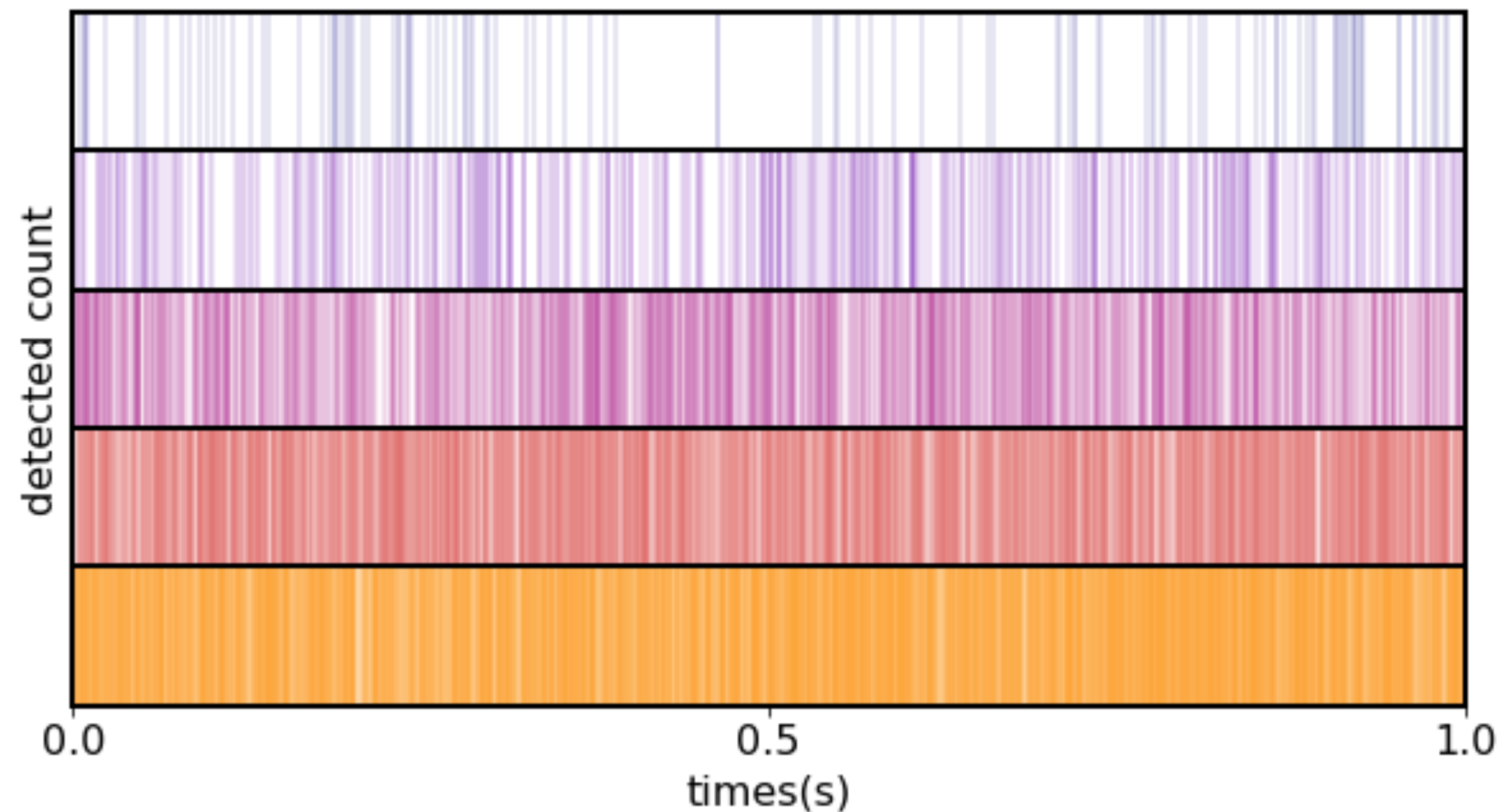
# Efficacité quantique et taux de compte d'obscurité



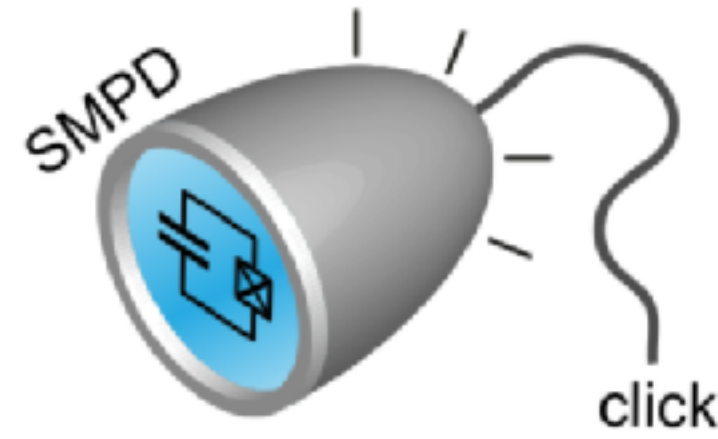
Darkcount rate  $\alpha = 85 \text{ s}^{-1}$

Operational Efficiency :  $\eta = 45\%$

Power sensitivity:  $\hbar\omega \frac{\sqrt{\alpha}}{\eta} = 10^{-22} \text{ W}/\sqrt{\text{Hz}}$



# Efficacité quantique et taux de compte d'obscurité

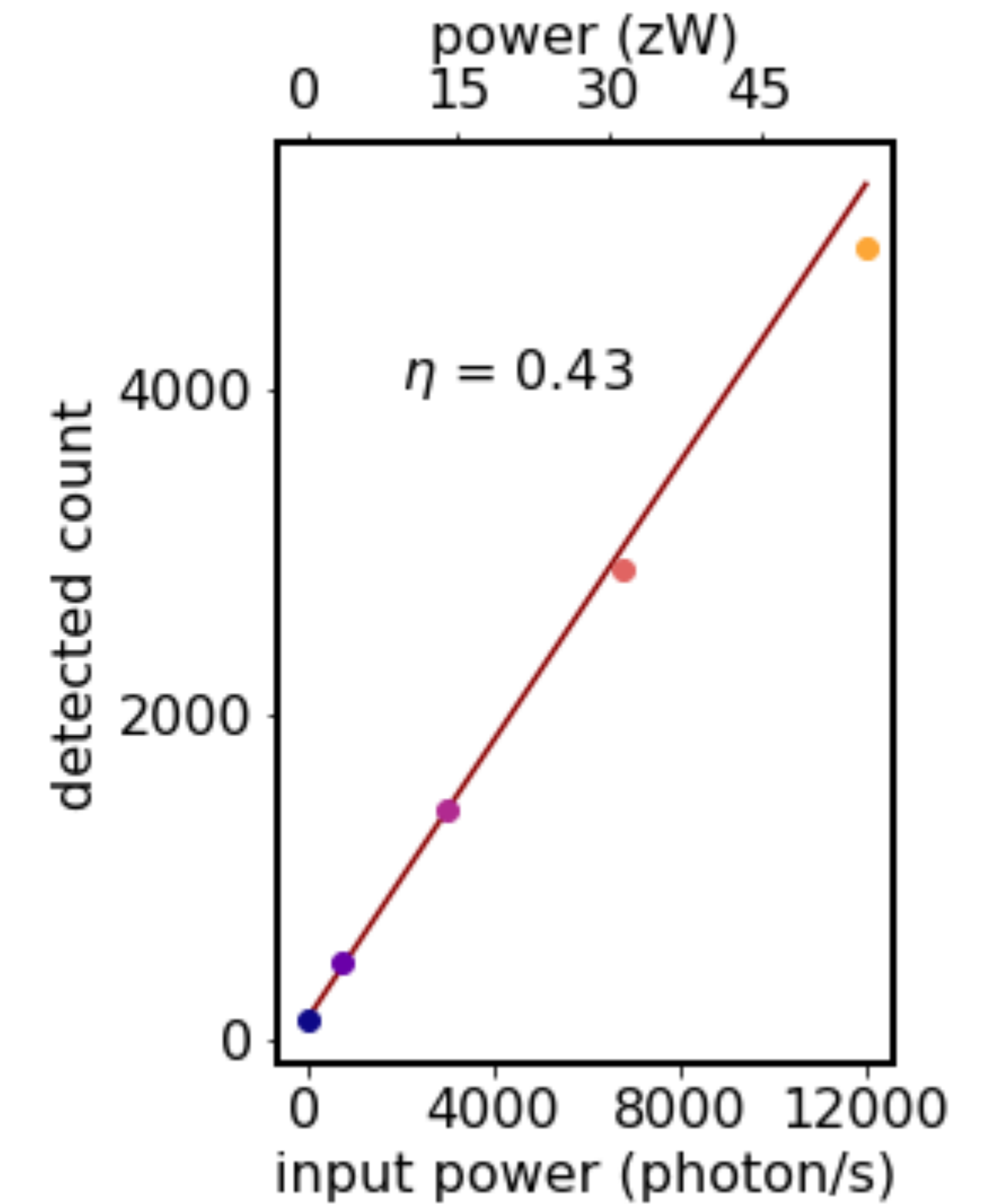
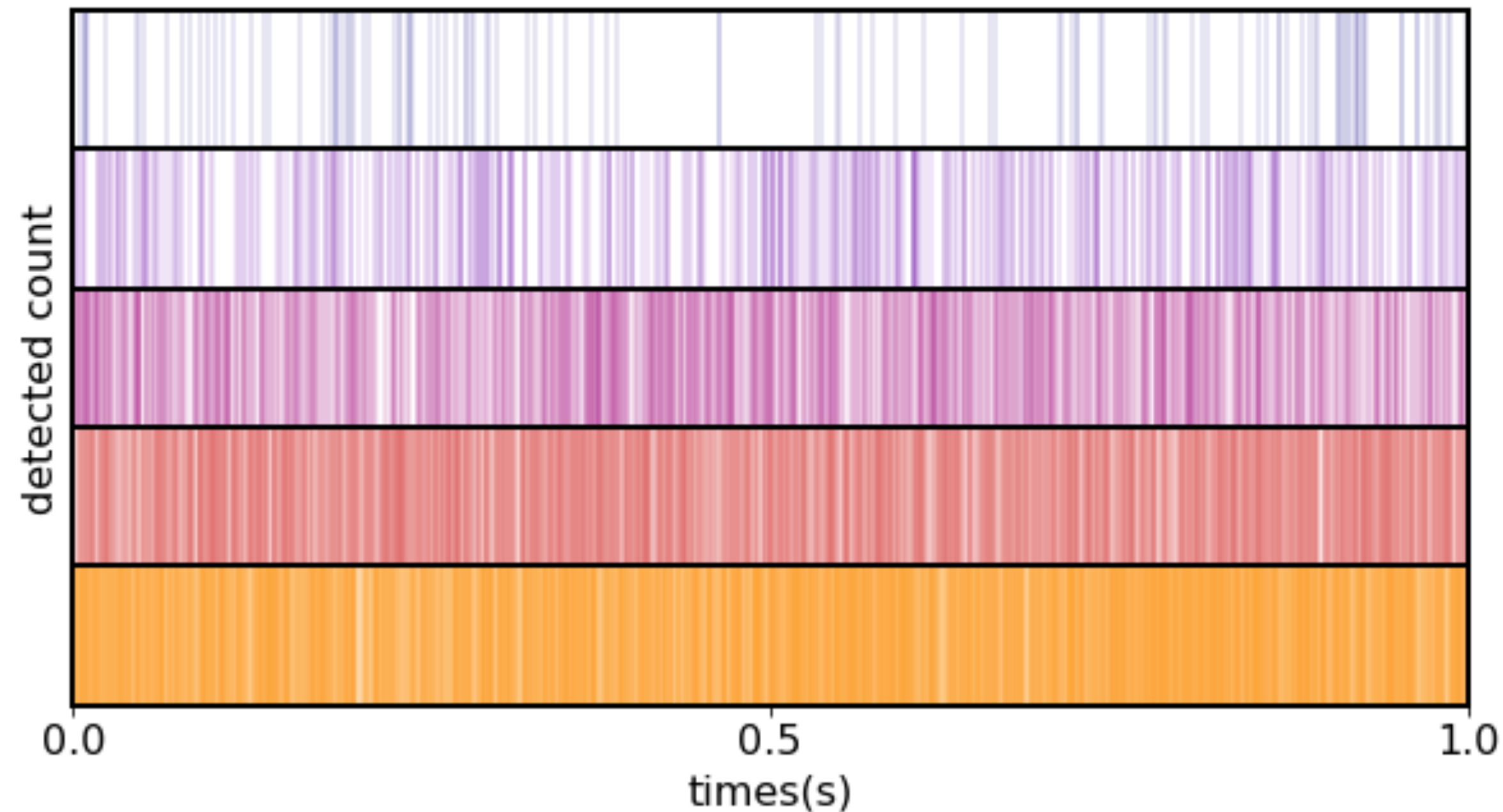
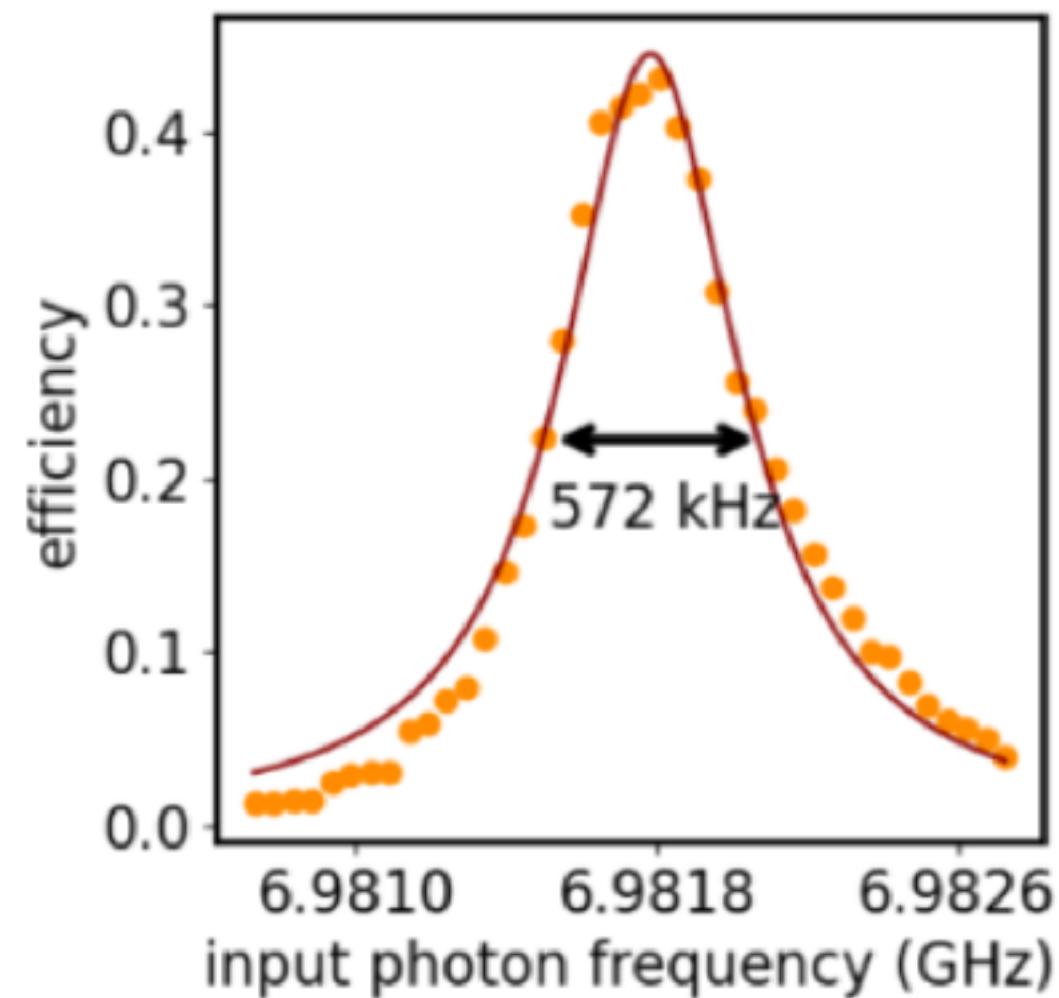


Darkcount rate  $\alpha = 85 \text{ s}^{-1}$

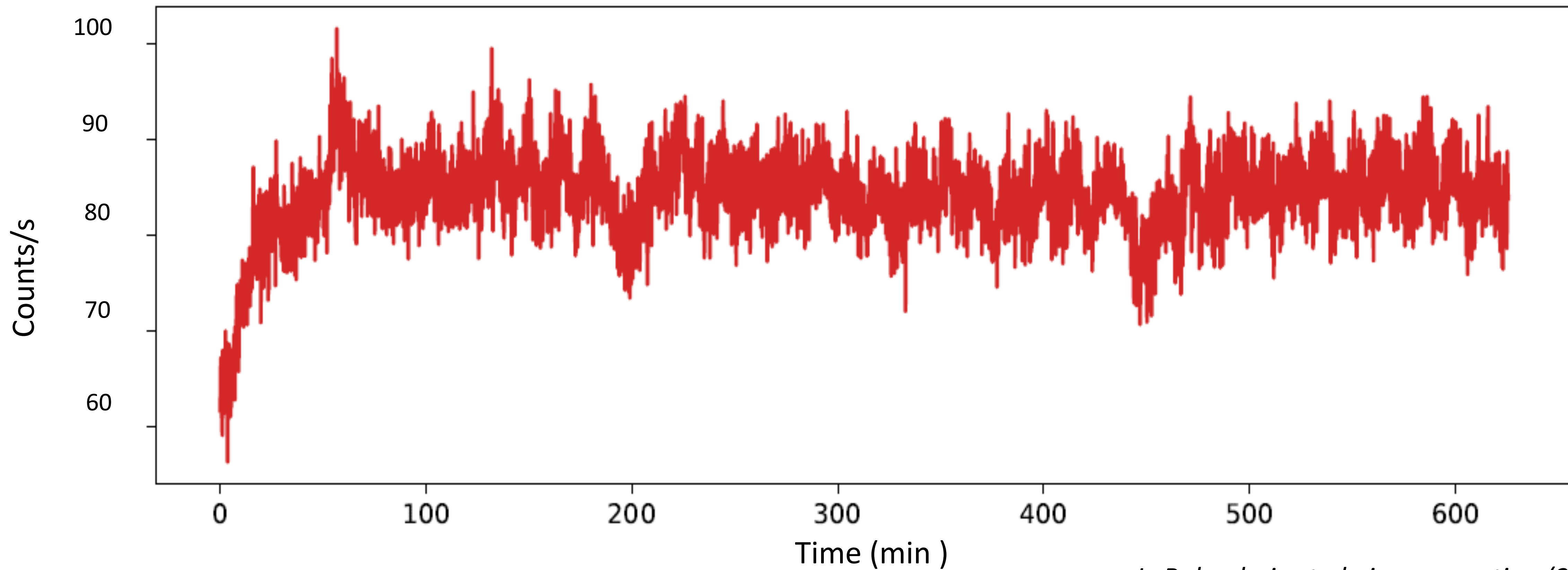
Operational Efficiency :  $\eta = 45\%$

Power sensitivity:  $\hbar\omega \frac{\sqrt{\alpha}}{\eta} = 10^{-22} \text{ W}/\sqrt{\text{Hz}}$

Bandwidth:  $\text{BW} = 0.5 \text{ MHz}$



# Long-term SMPD operation

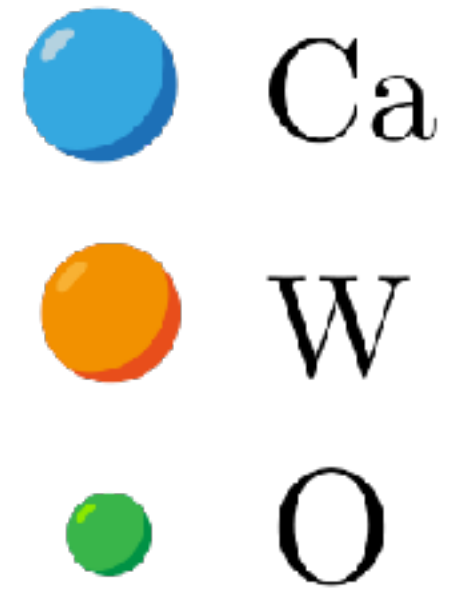
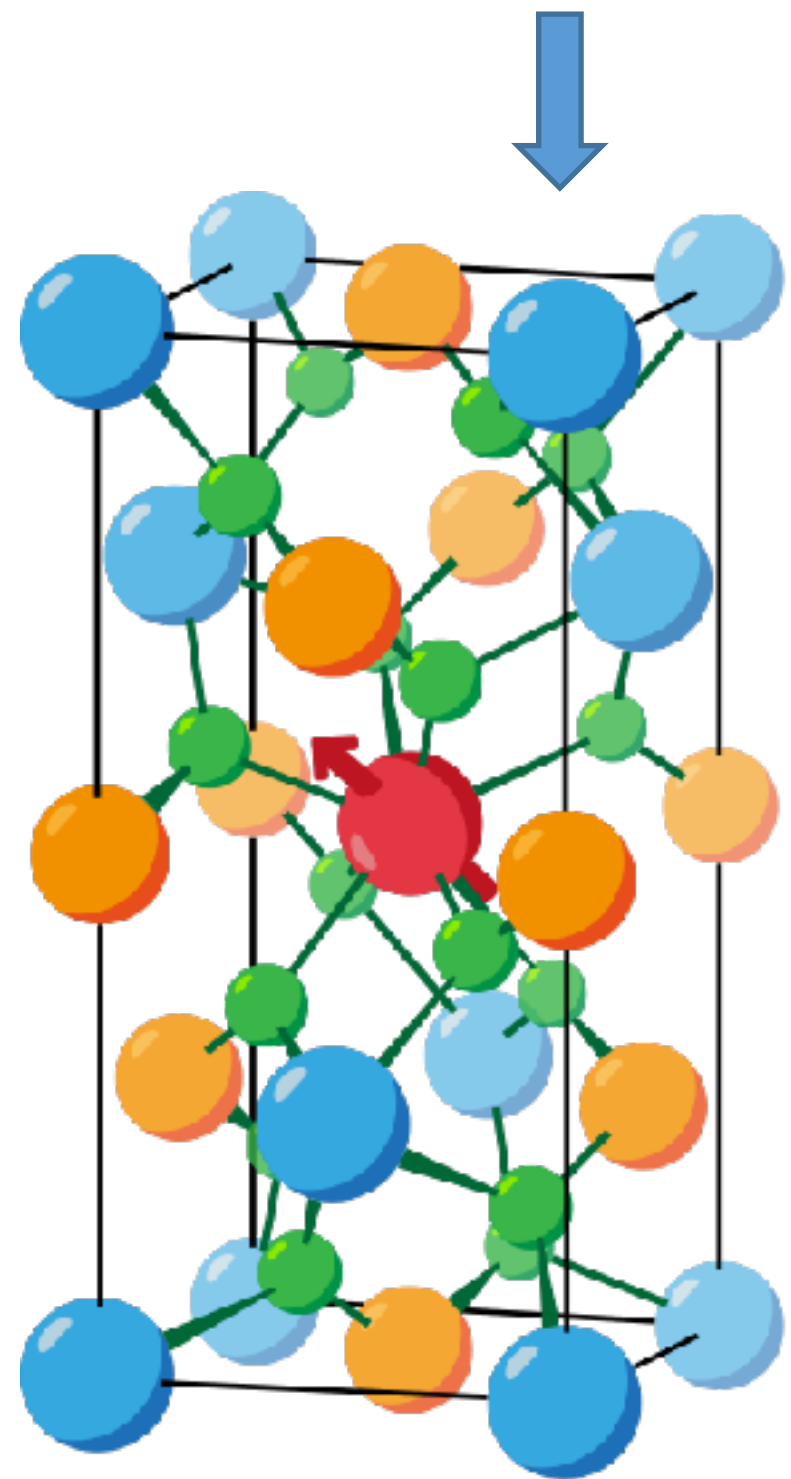


*L. Balembois et al., in preparation (2022)*

# Spins

# Er : CaWO<sub>4</sub>

Scheelite

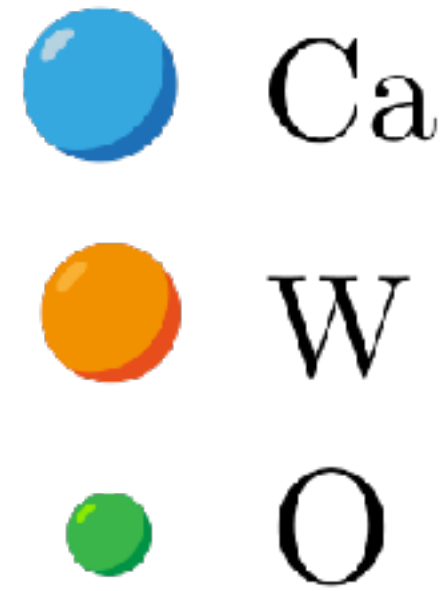
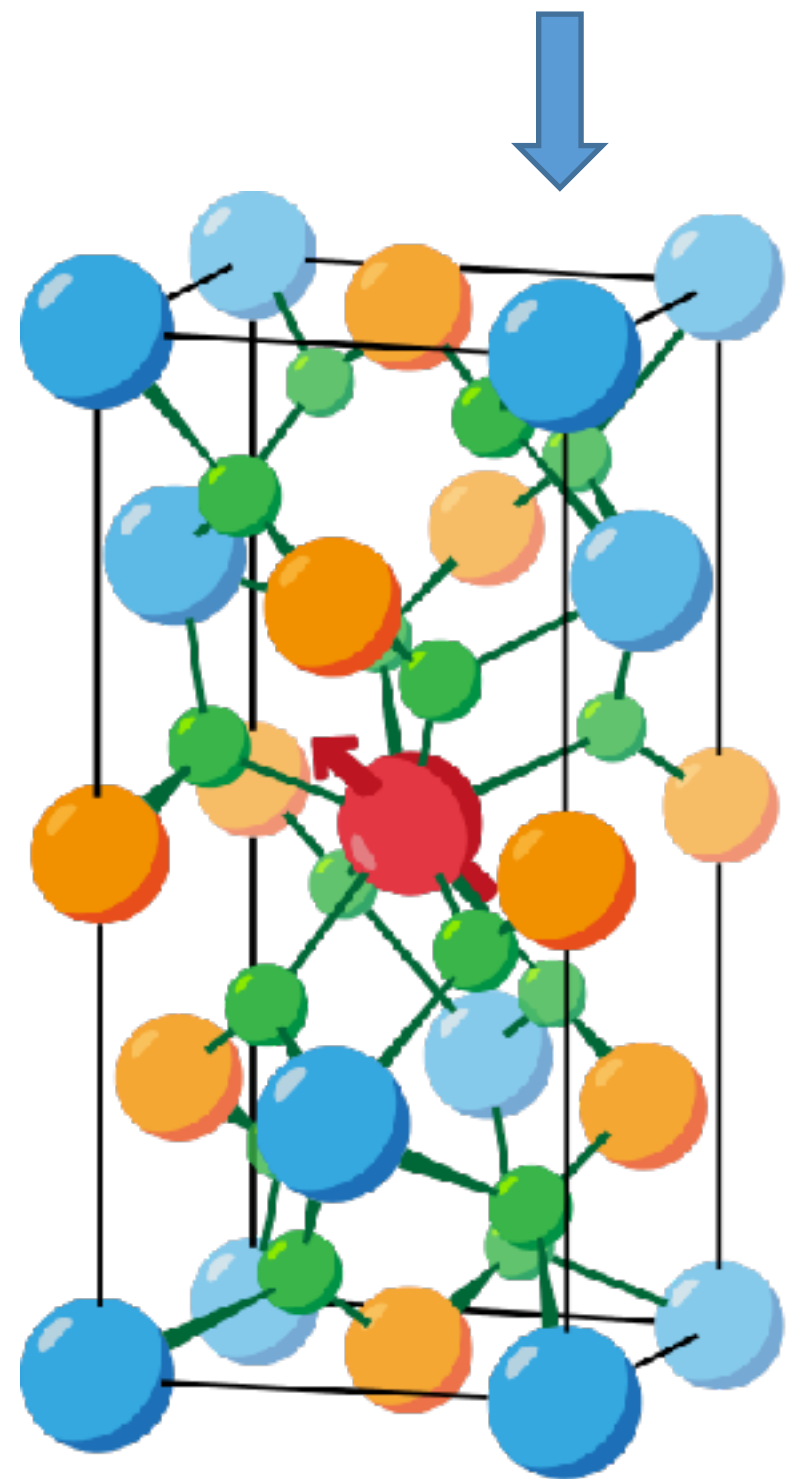




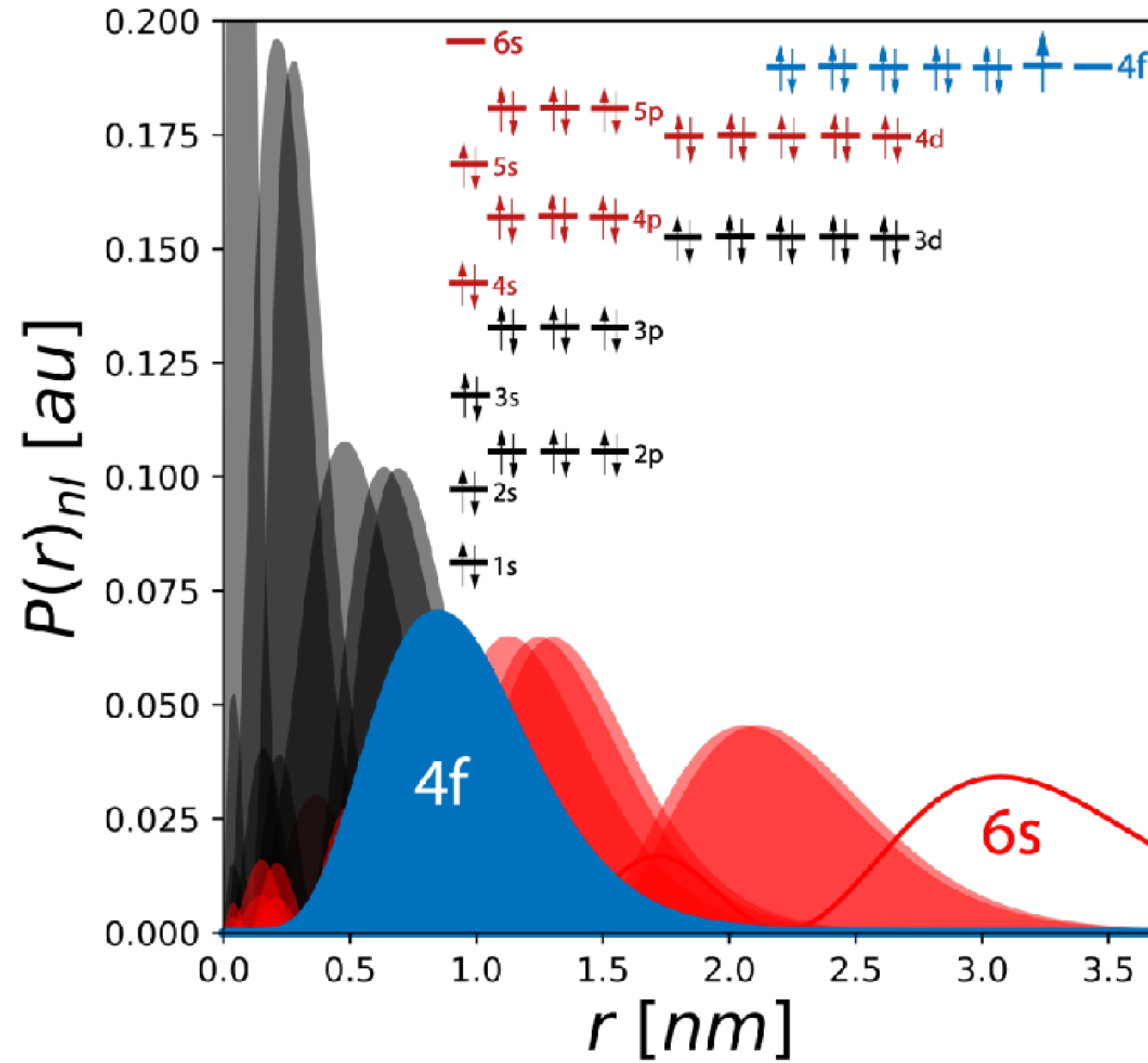
# Spins

# Er : CaWO<sub>4</sub>

## Scheelite



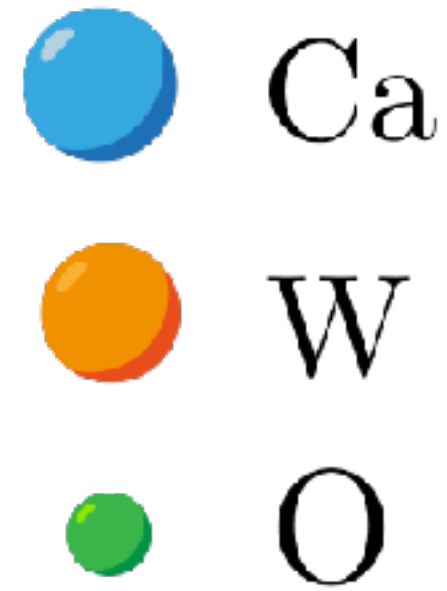
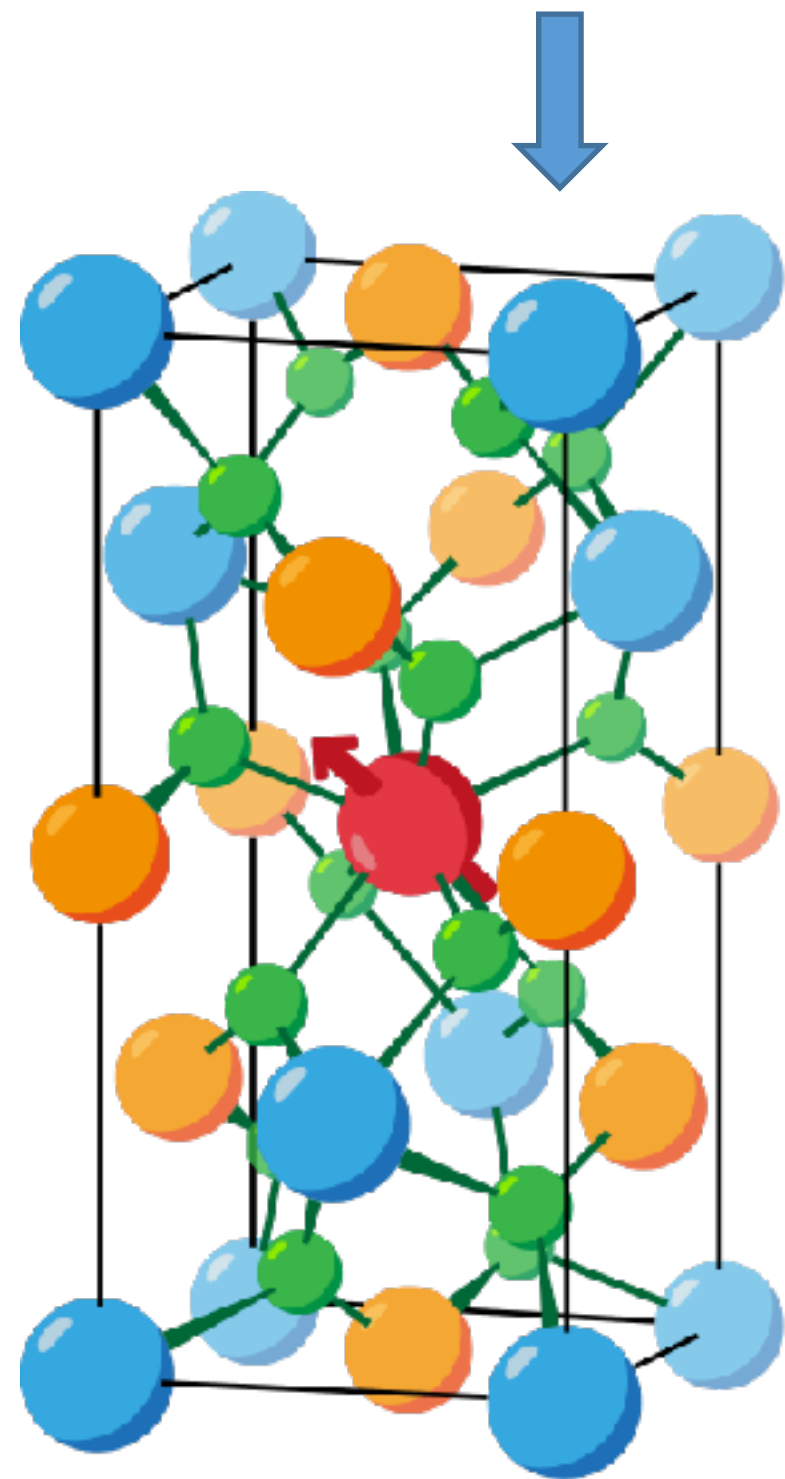
## Er<sup>3+</sup> orbitals



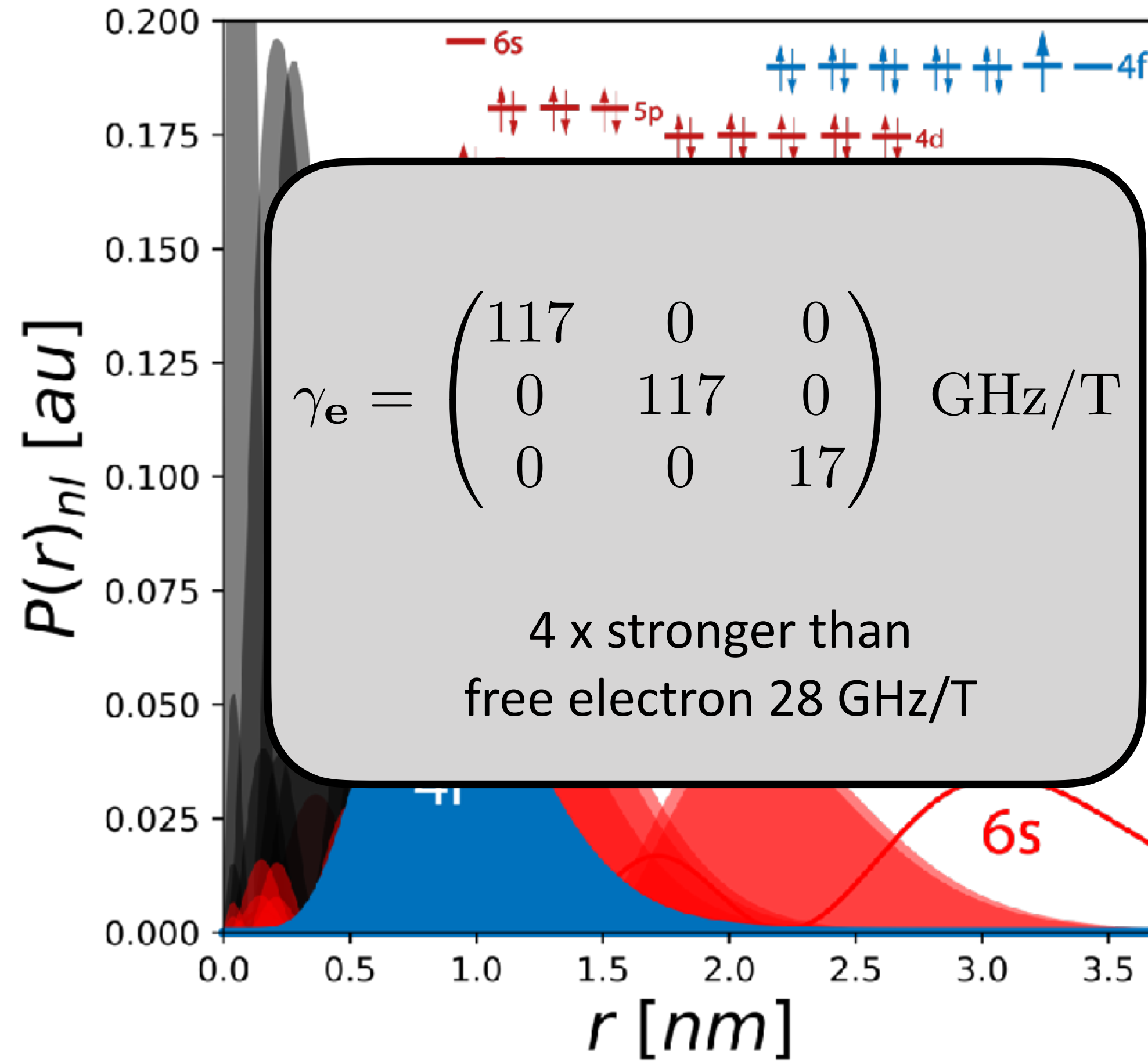
# Spins

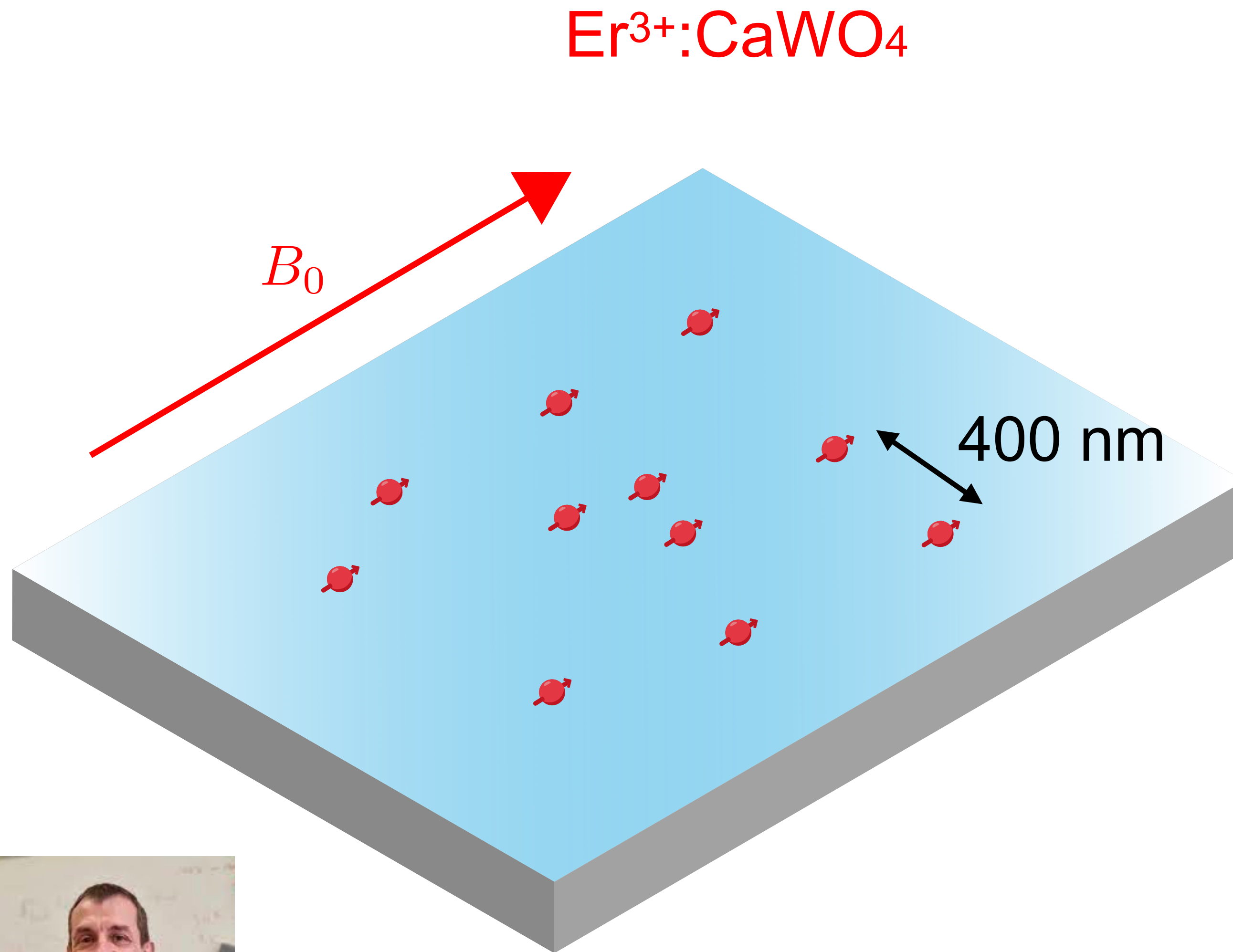
# Er : CaWO<sub>4</sub>

## Scheelite



## Er<sup>3+</sup> orbitals





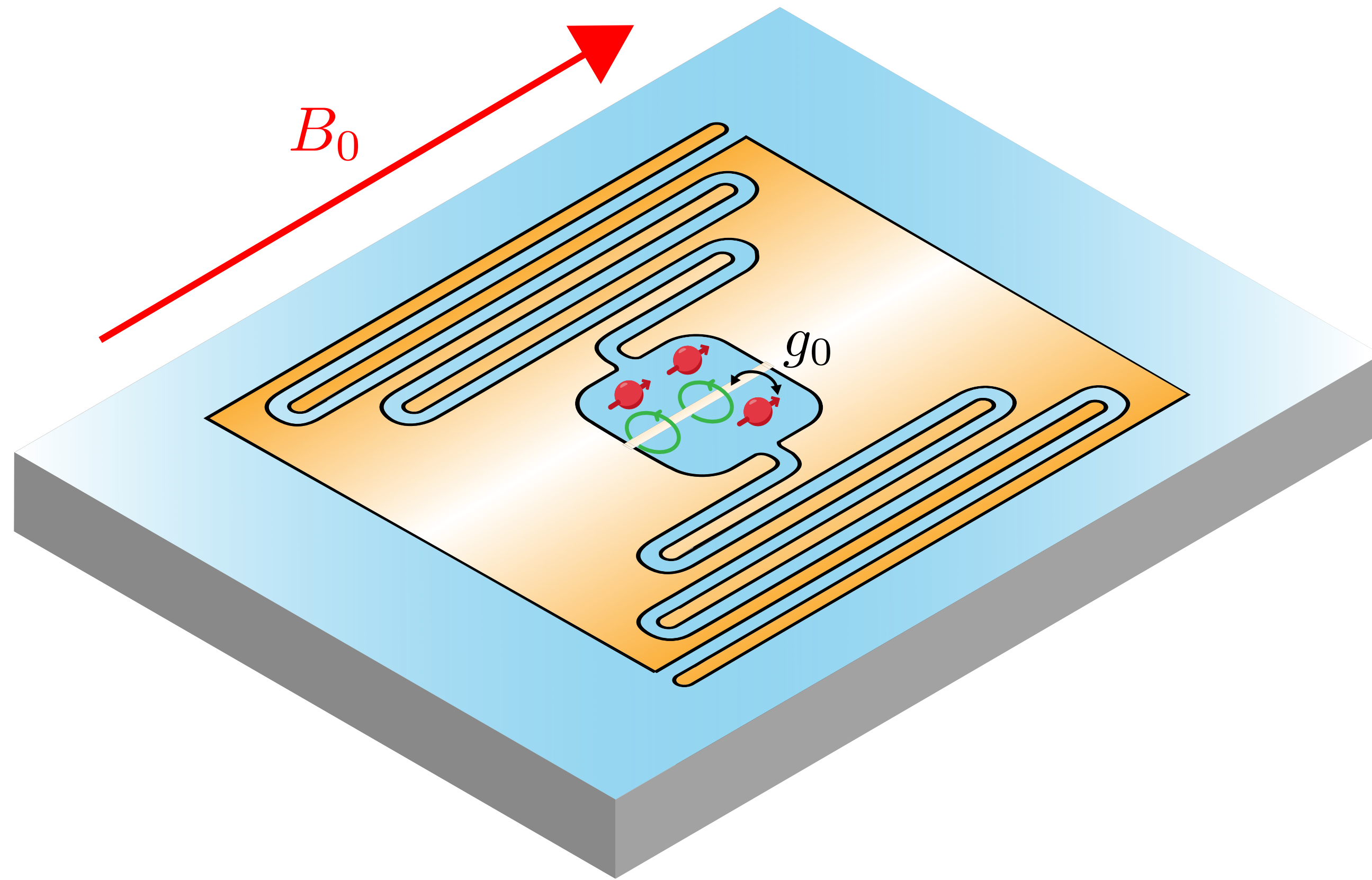
**Spin relaxation  
in the microwave domain**

Photons in free space  
~1000 years

Phonons in lattice  
~1 s

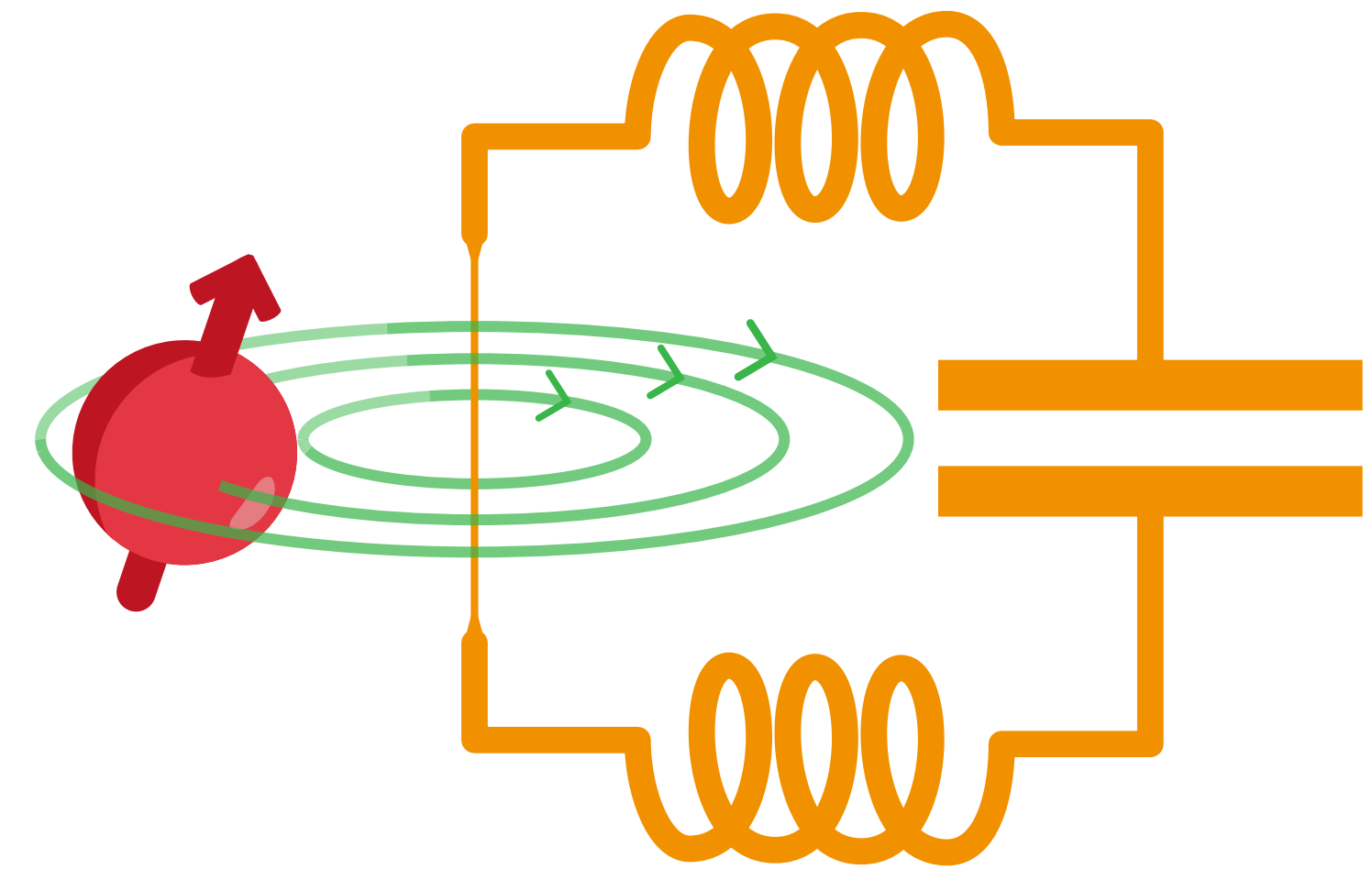


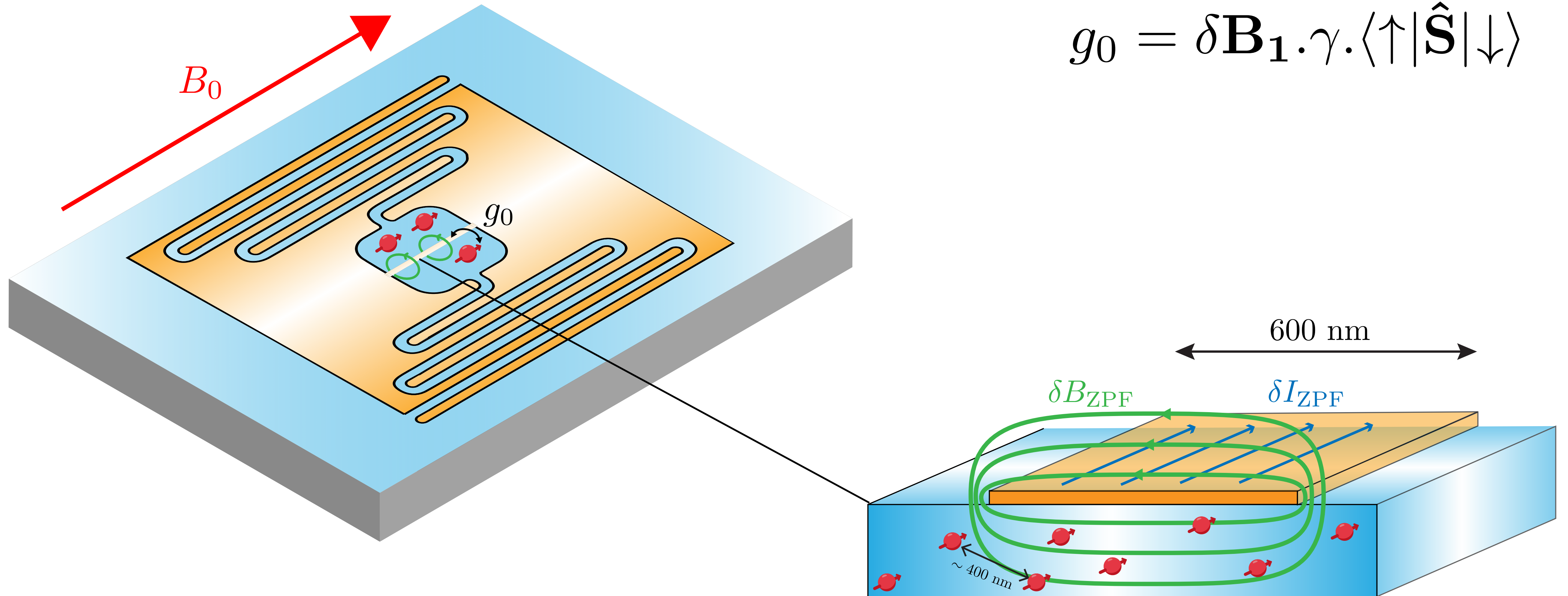
P. Goldner



Spin – microwave photon coupling

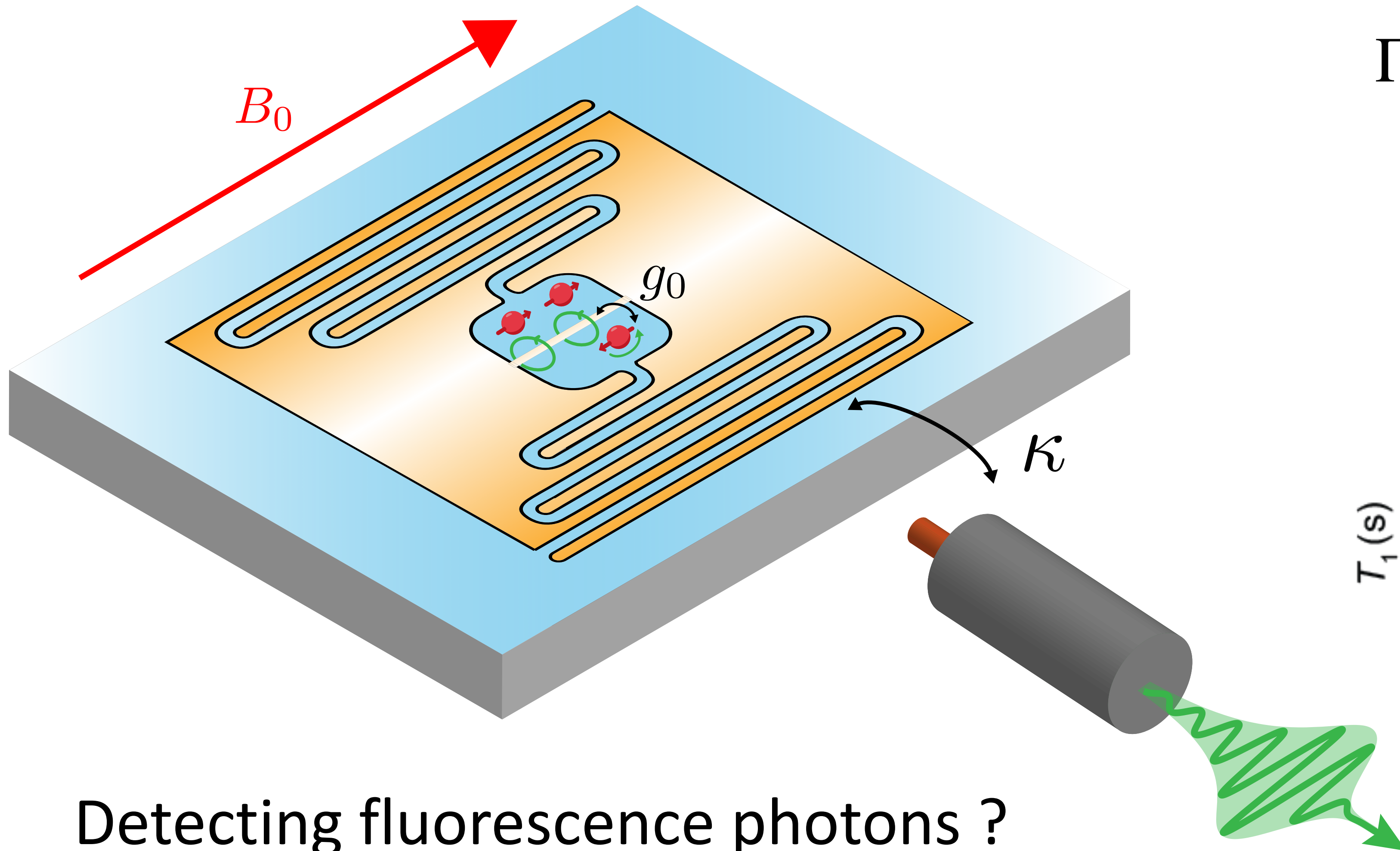
$$g_0 = \delta \mathbf{B}_1 \cdot \gamma \cdot \langle \uparrow | \hat{\mathbf{S}} | \downarrow \rangle$$



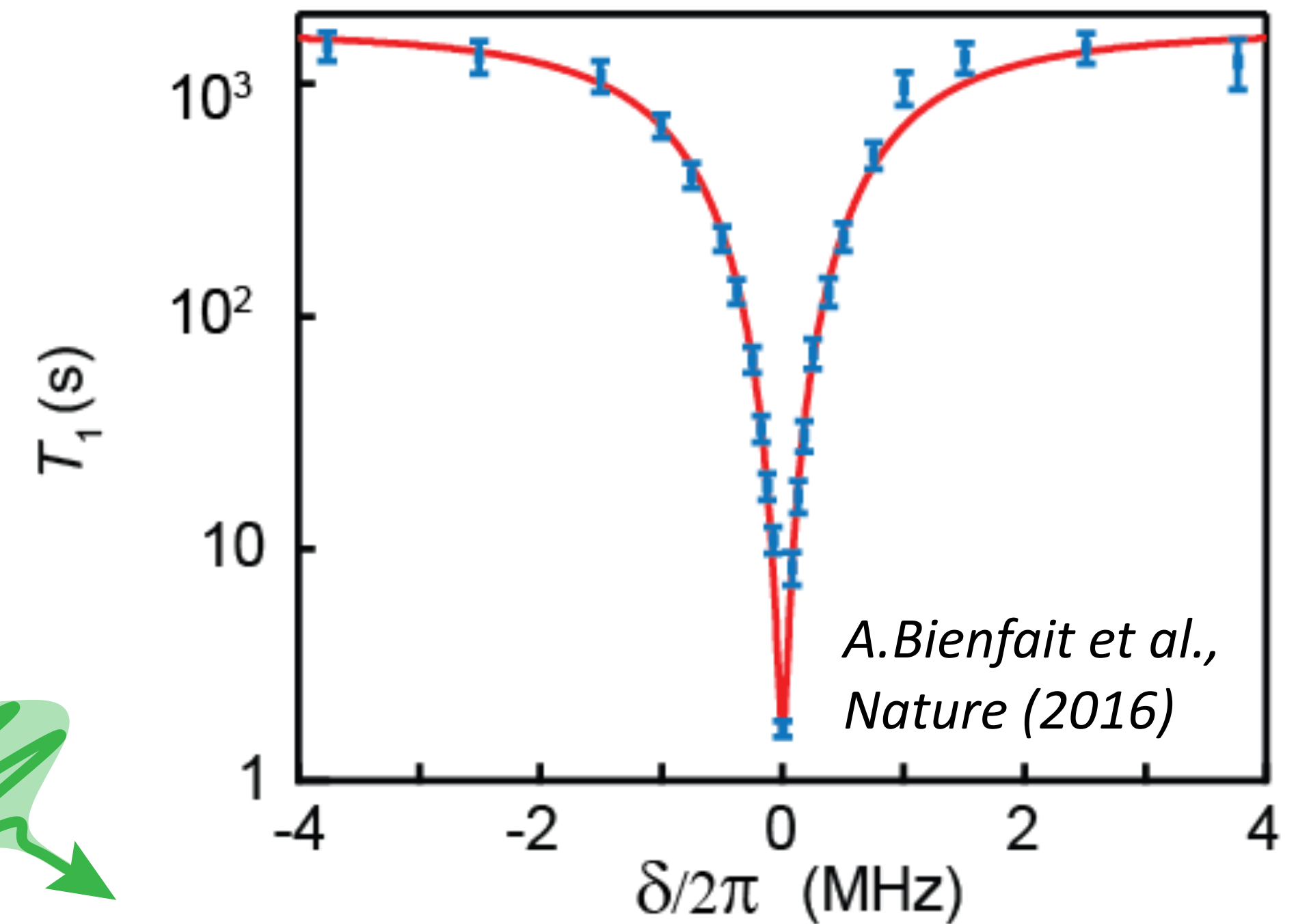


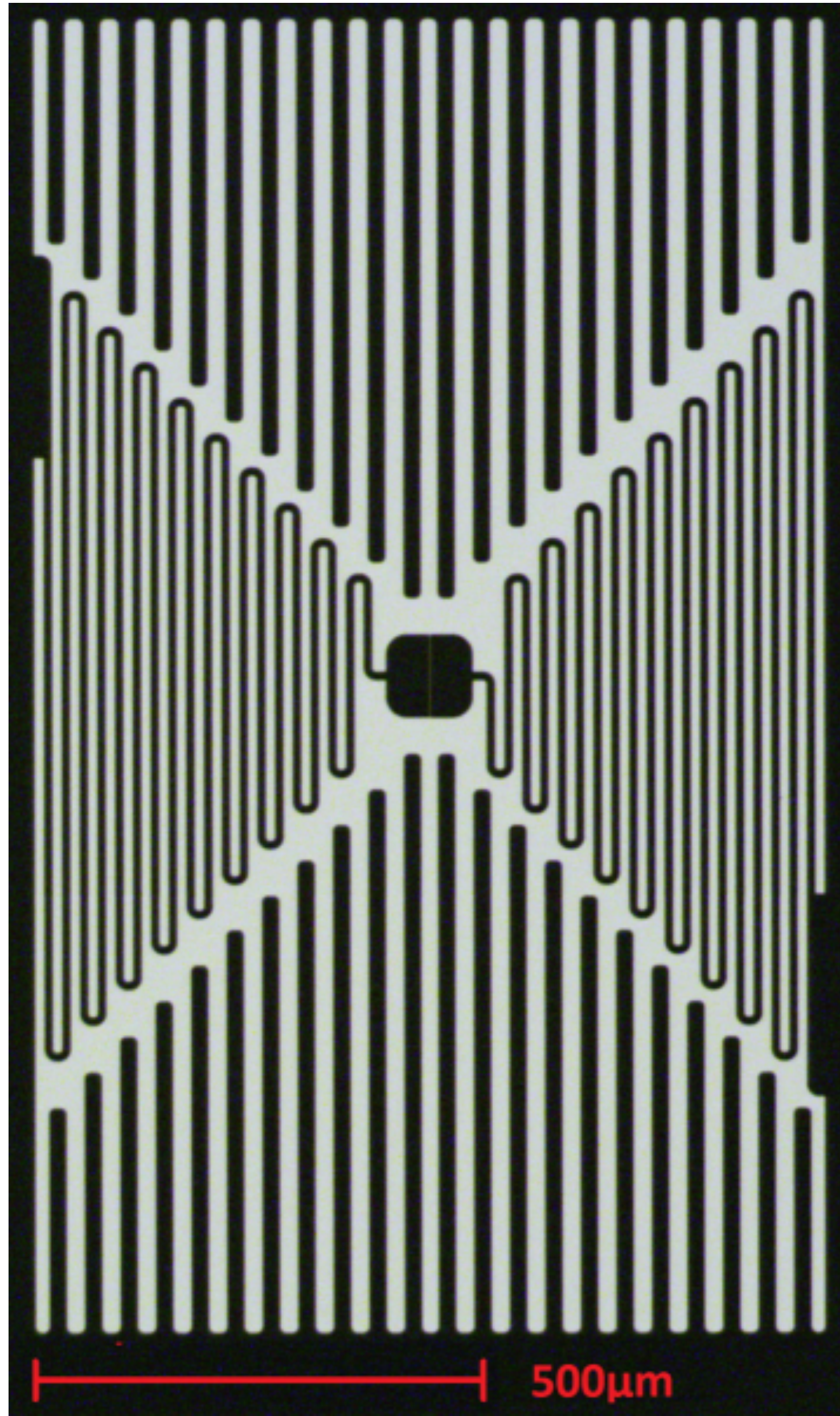


Audrey Bienfait

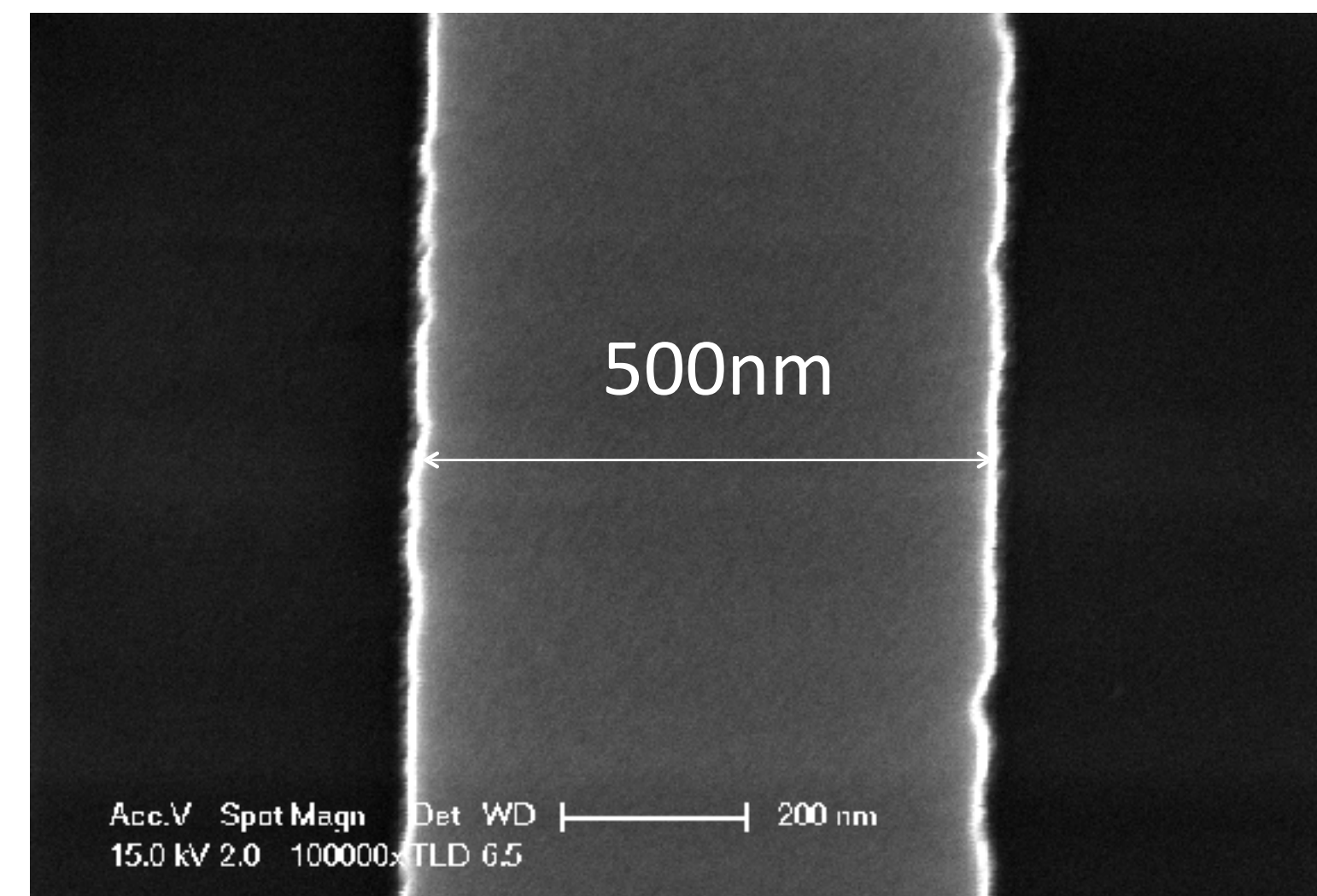
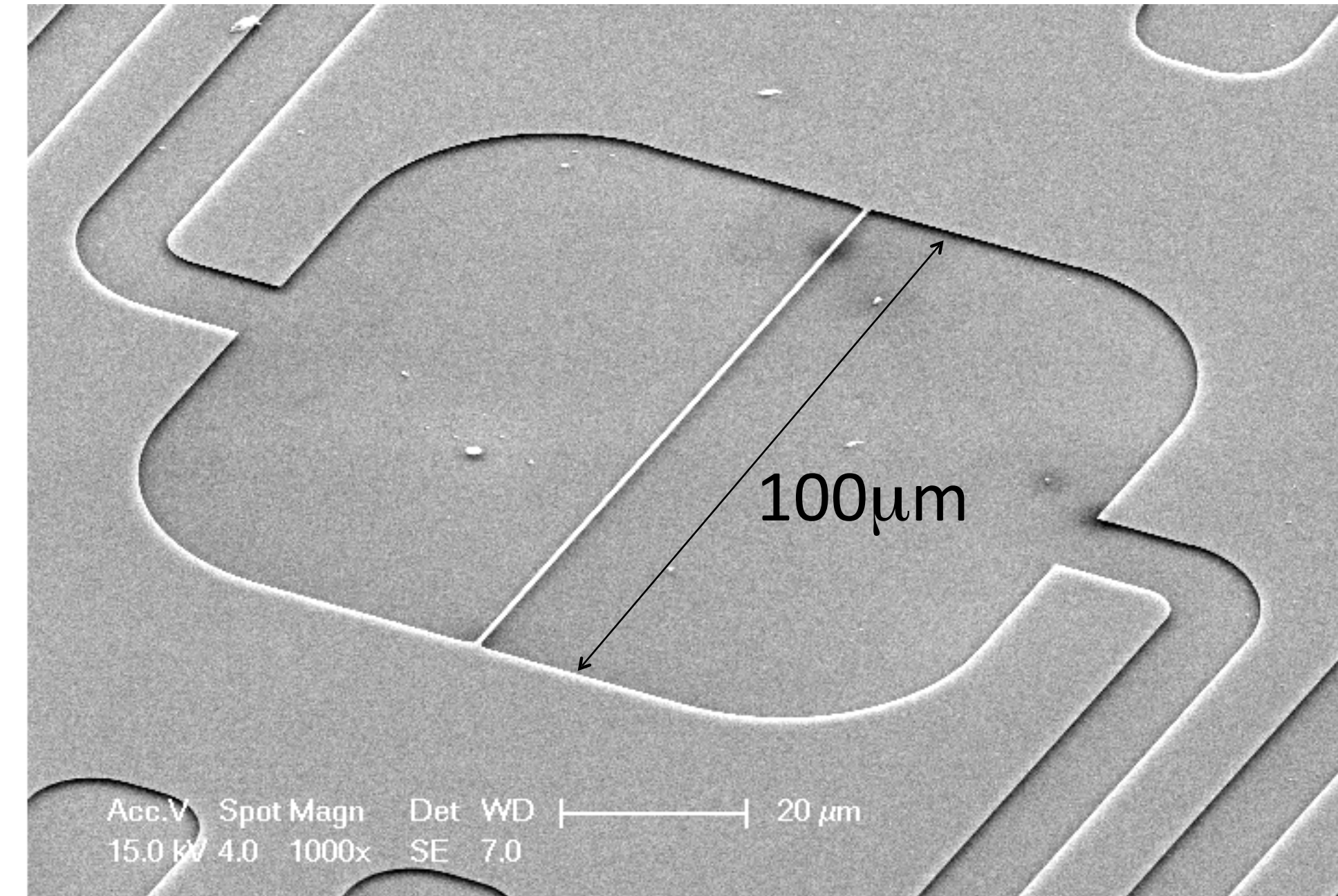


$$\Gamma_R = \frac{4g_0^2}{\kappa} \frac{1}{1 + 4 \left[ \frac{\delta}{\kappa} \right]^2}$$

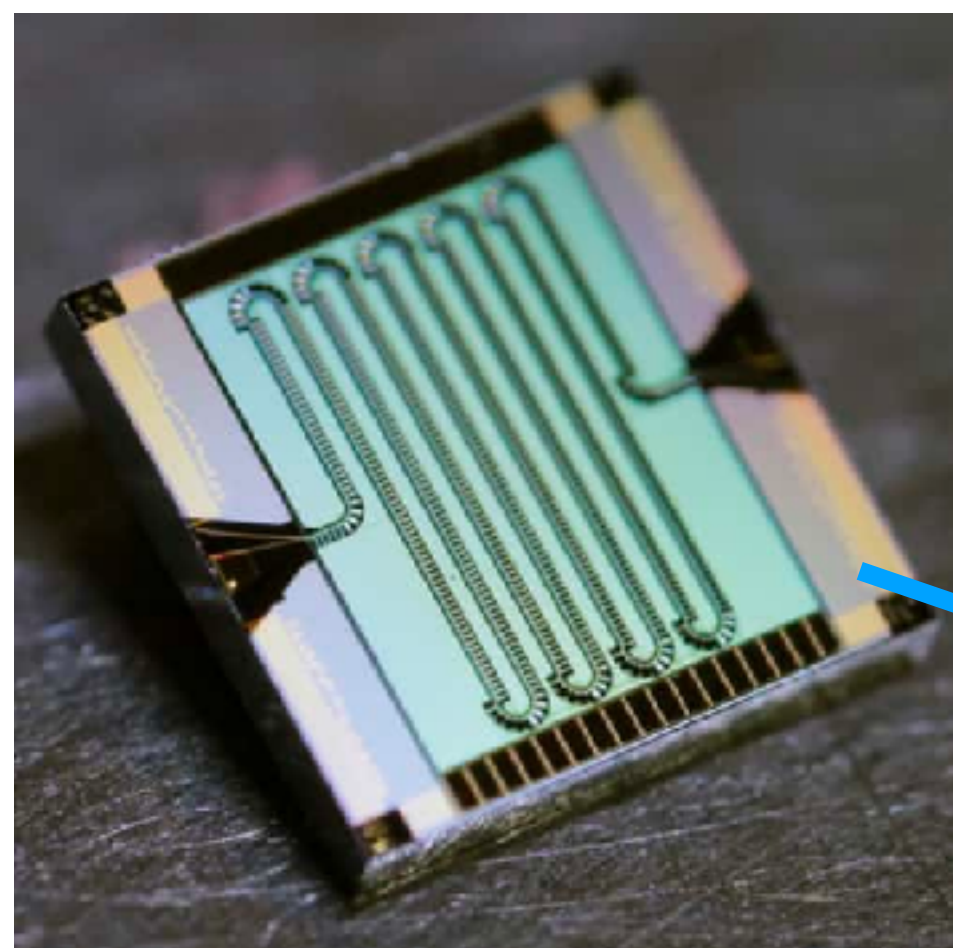




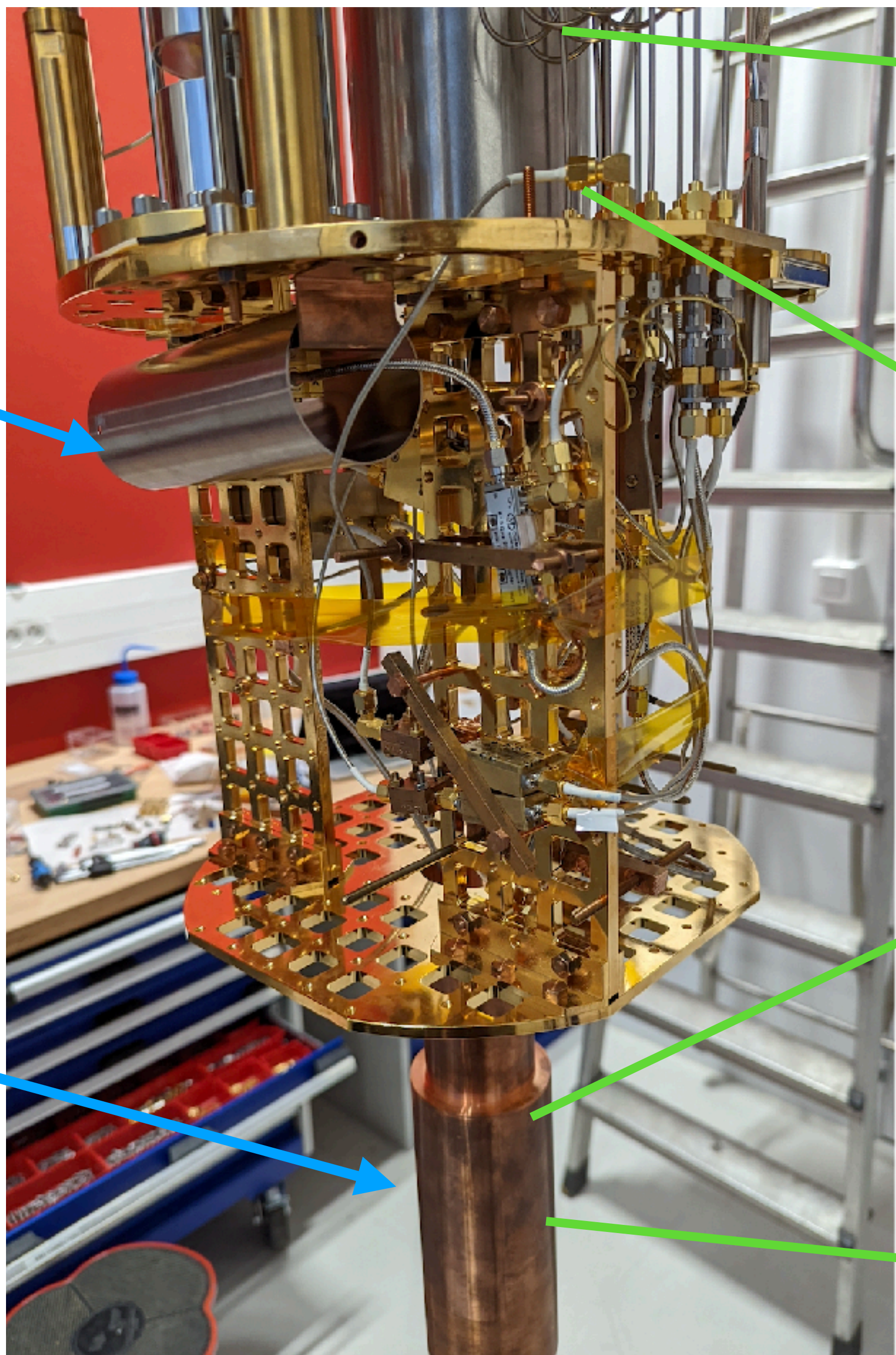
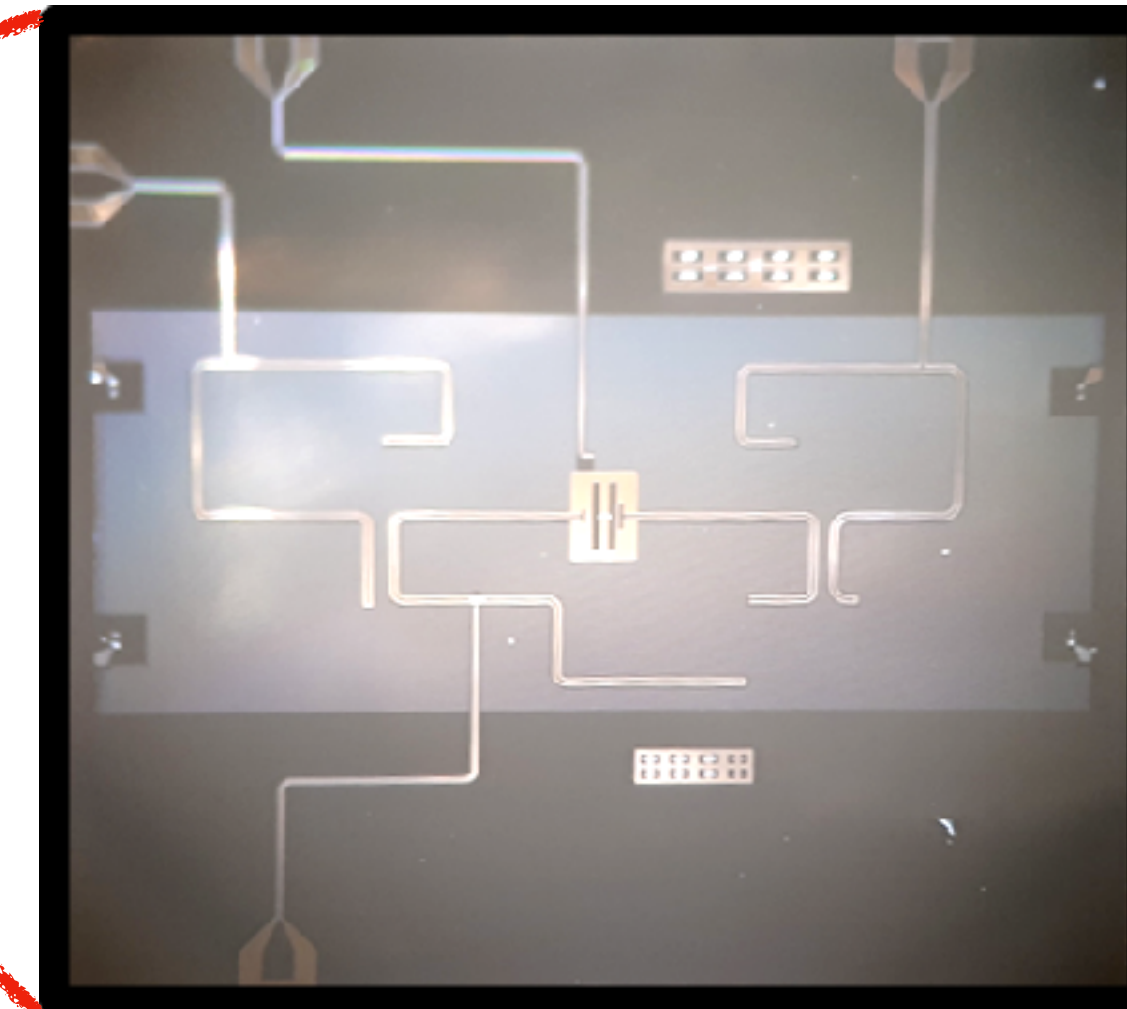
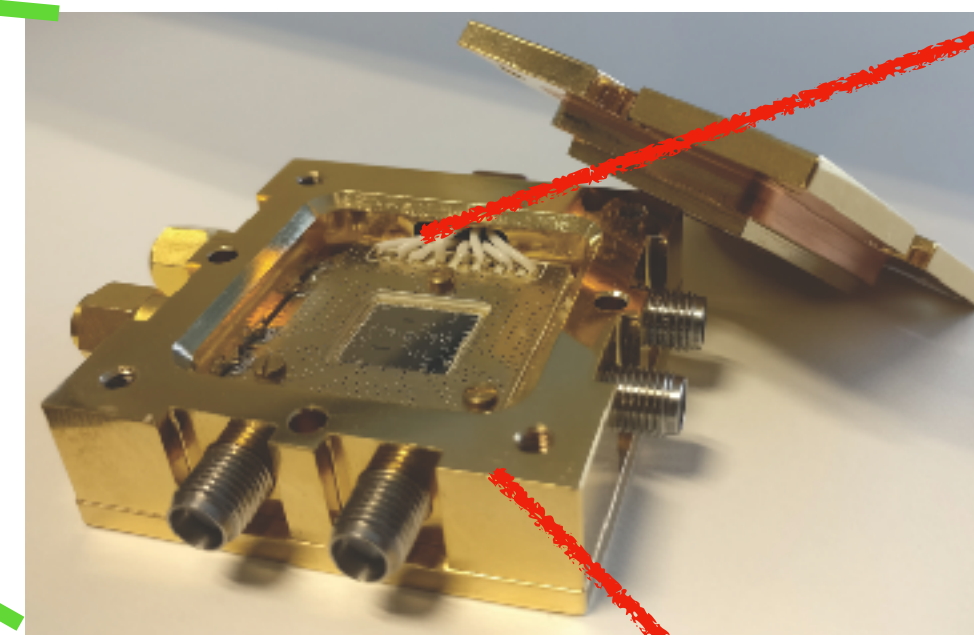
↑  $B_0 //$  c-axis



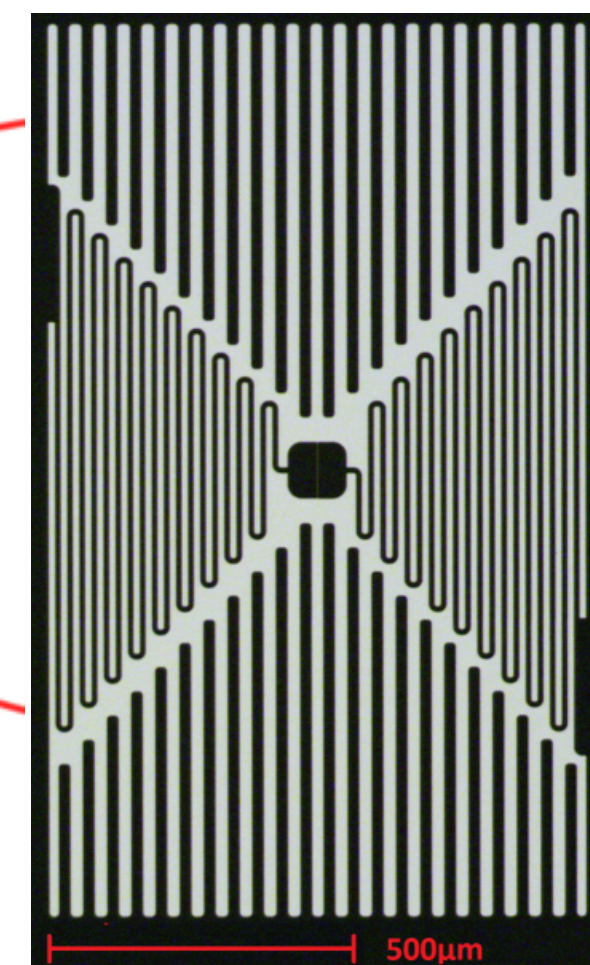
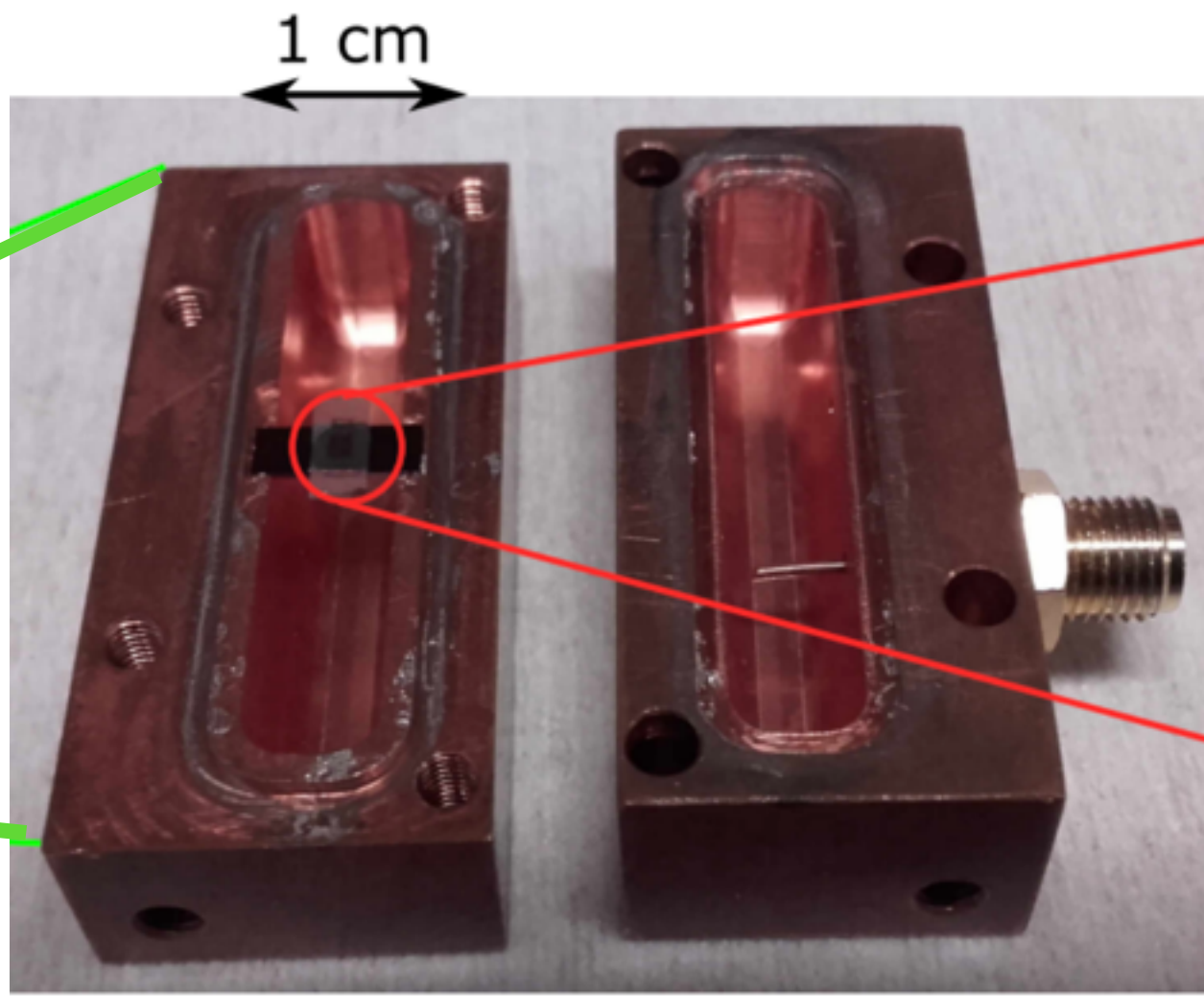
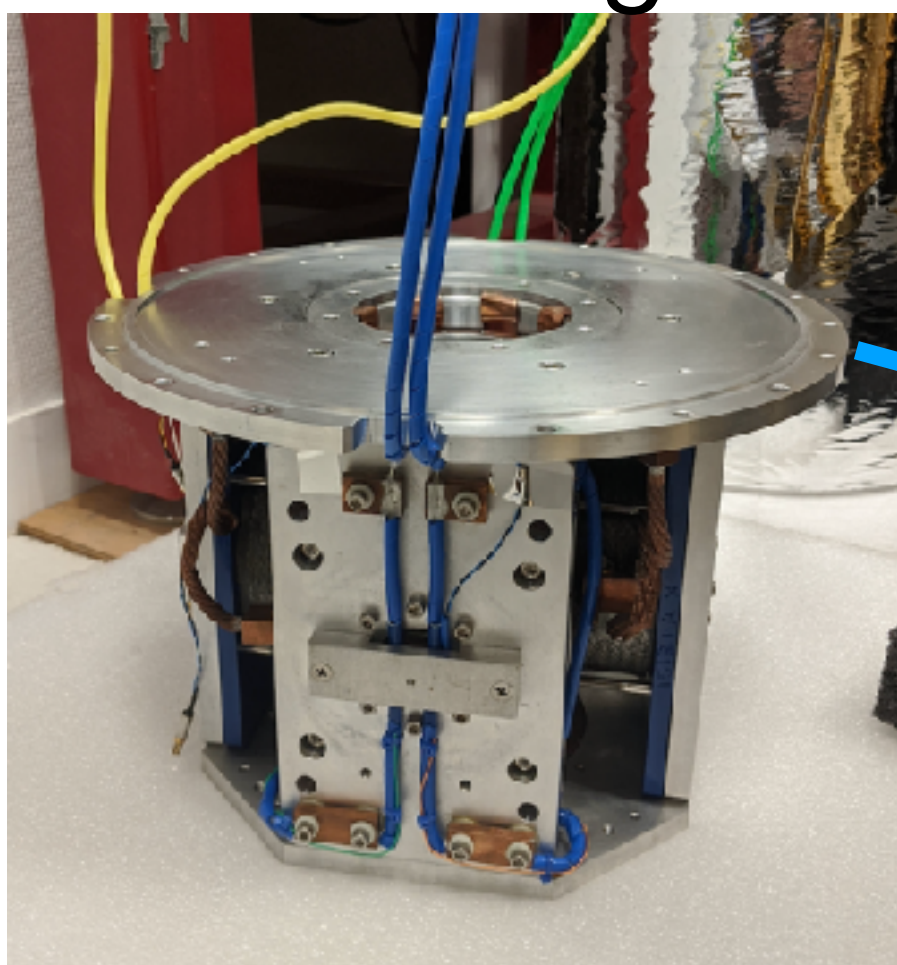
MIT JTWPA



Single Microwave Photon Detector

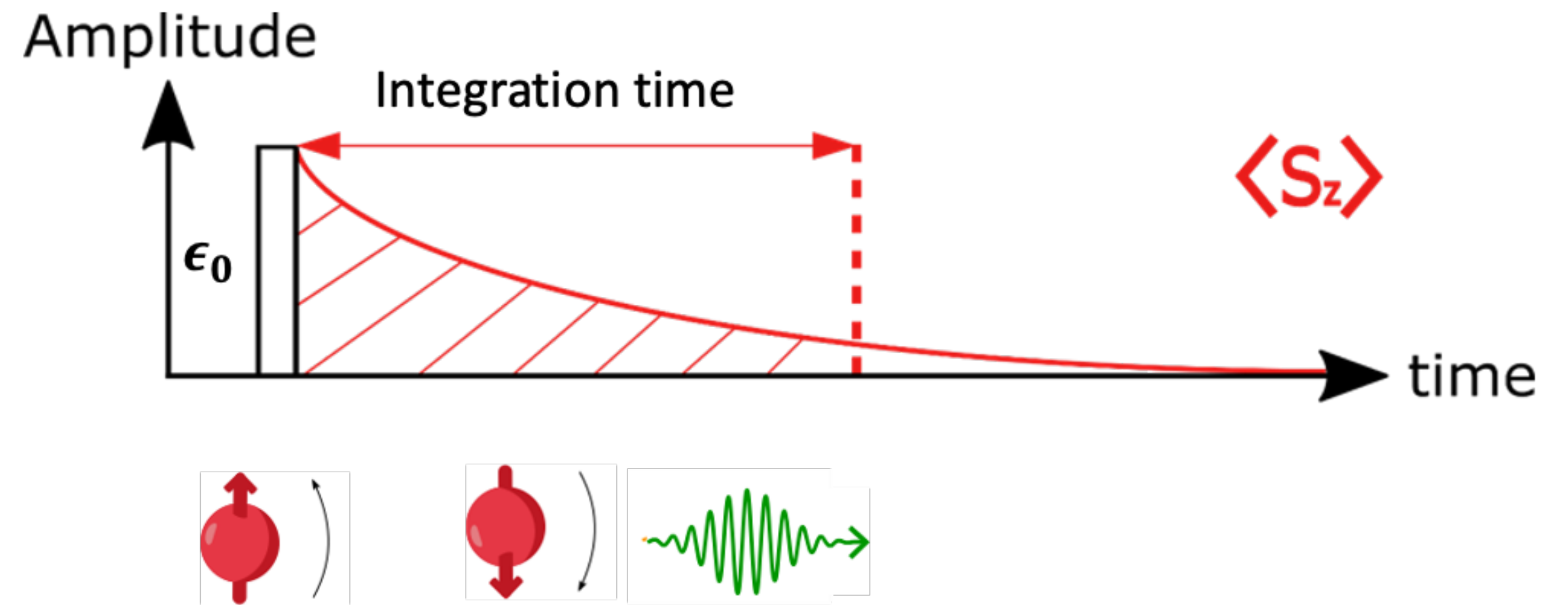
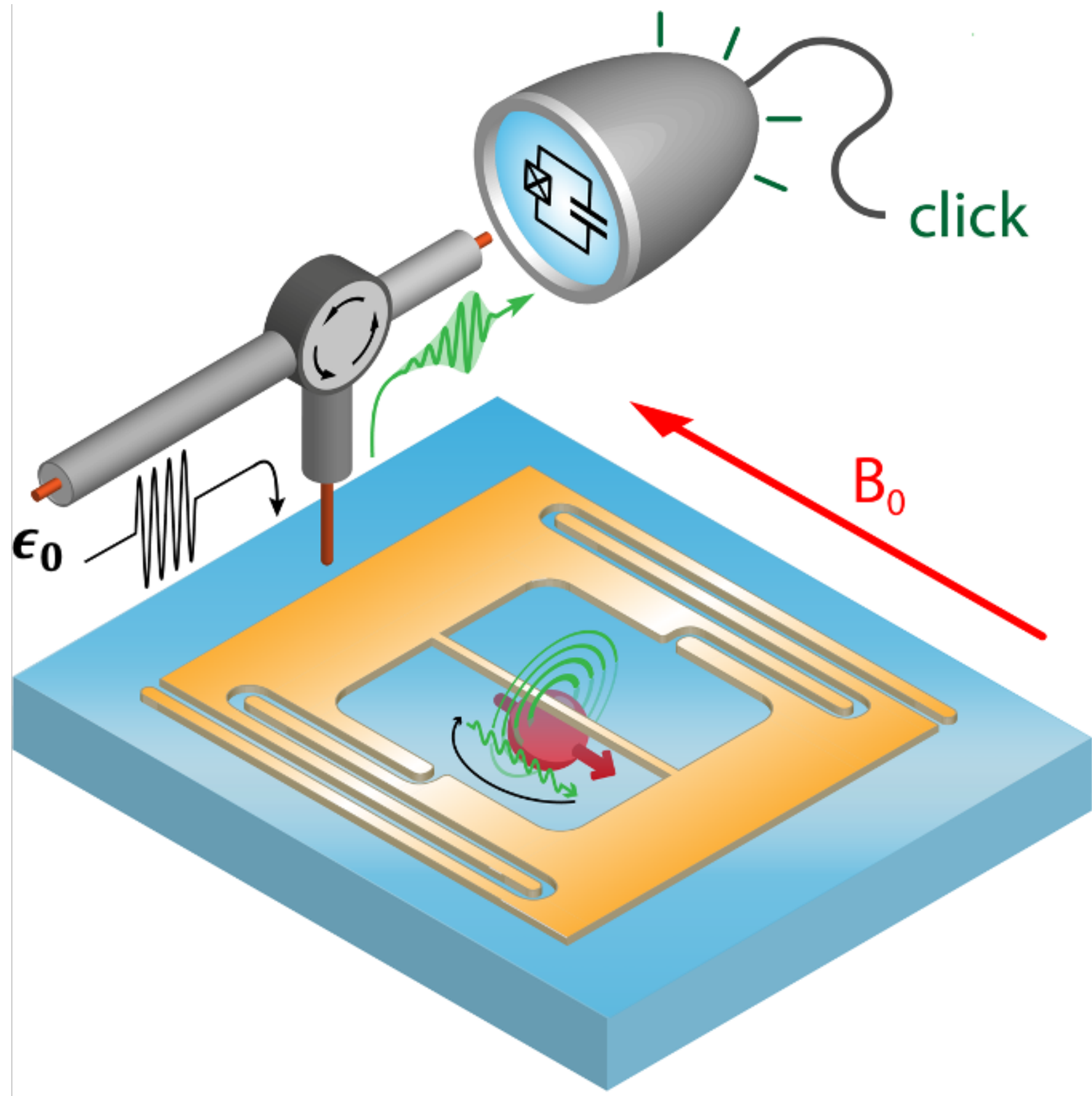


1T/1T/1T  
vector magnet

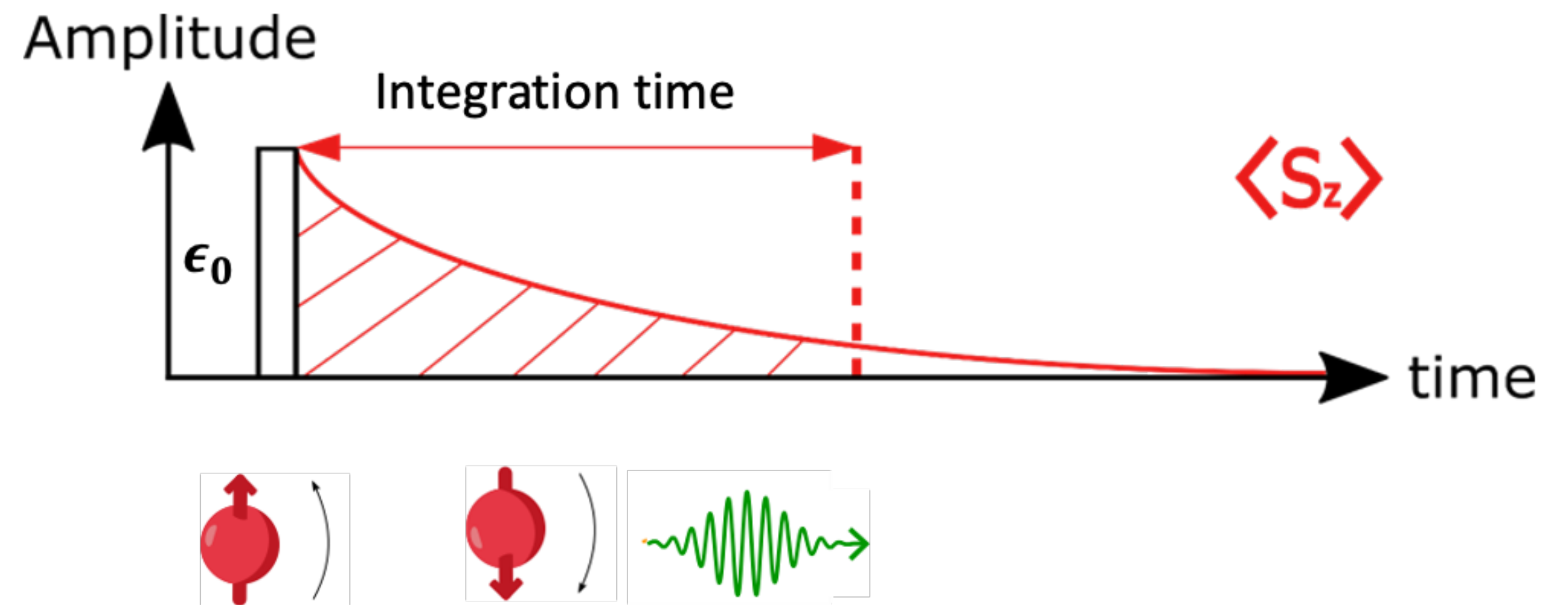
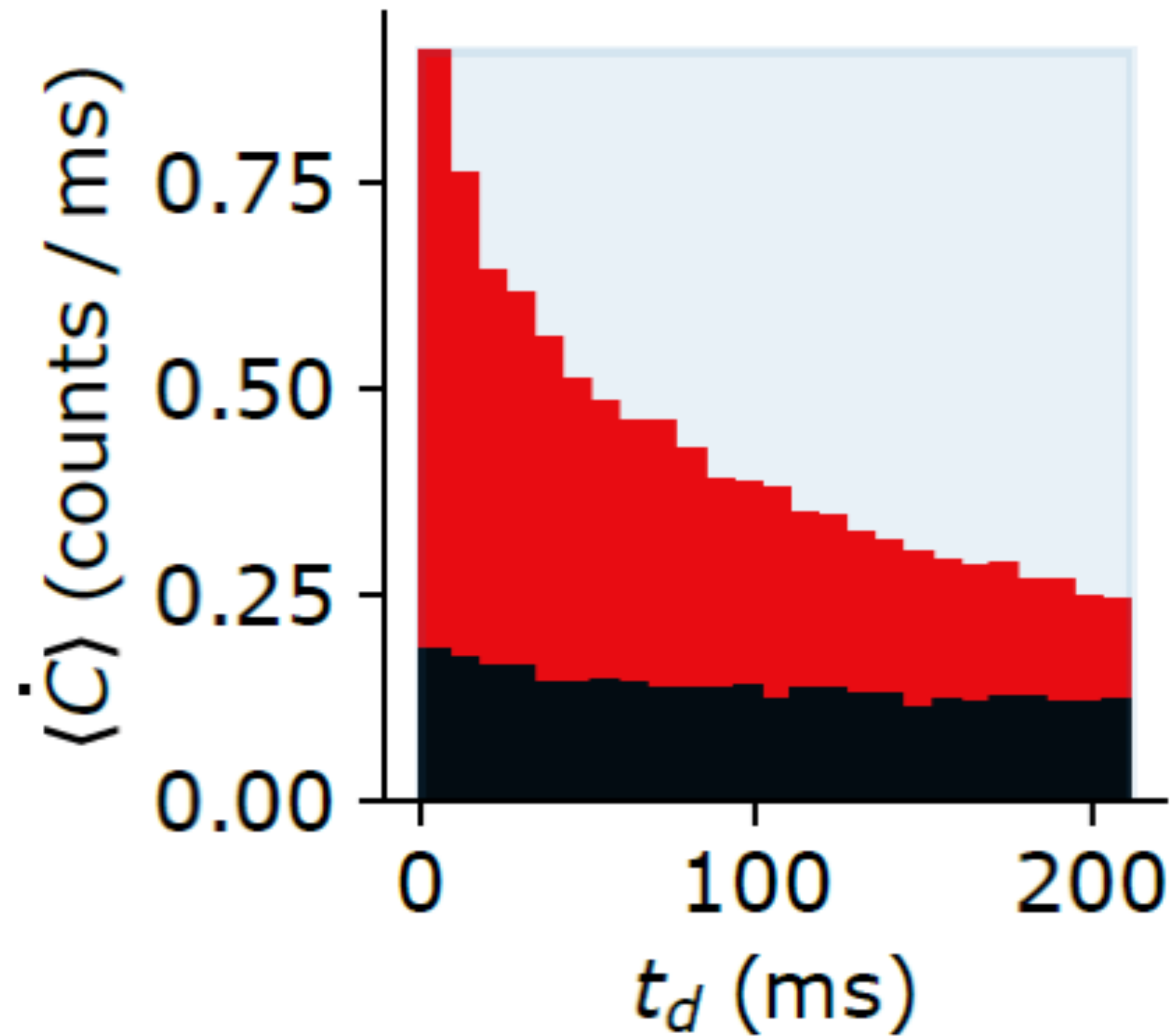




# Microwave fluorescence detection of spins



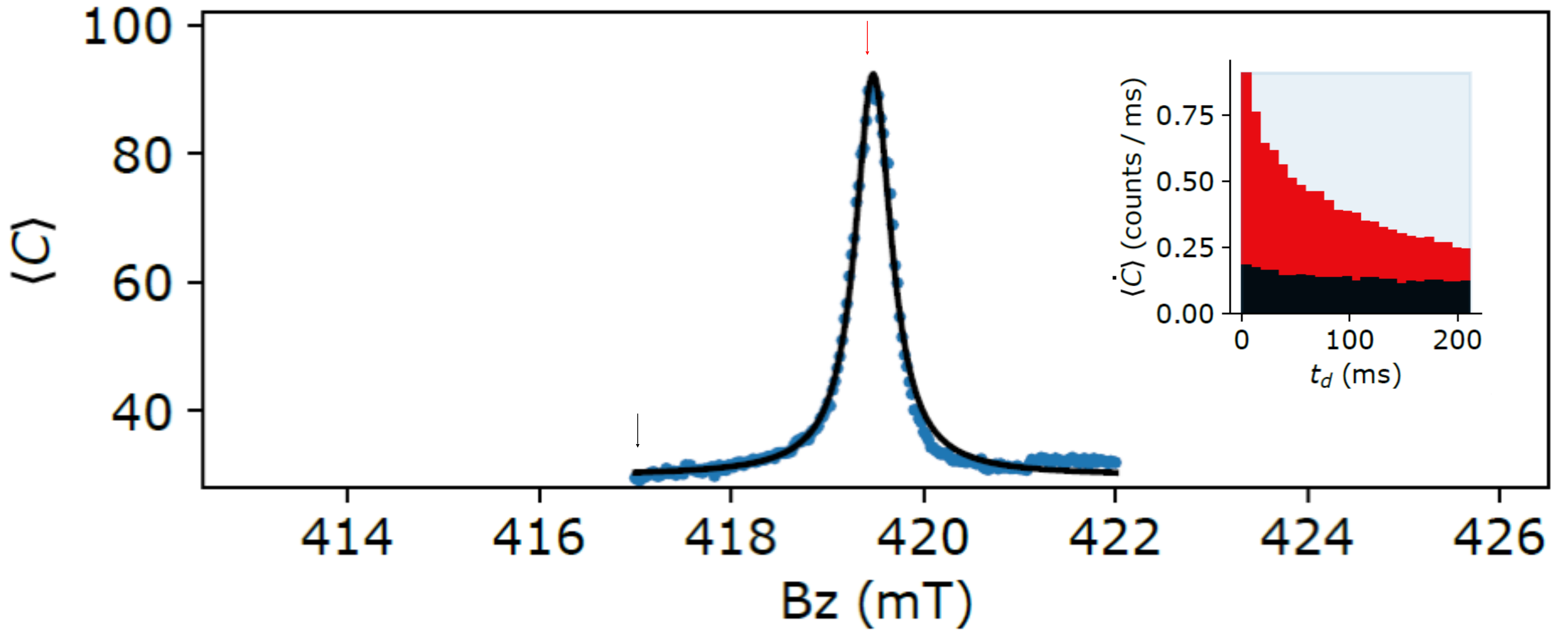
# Microwave fluorescence detection of spins



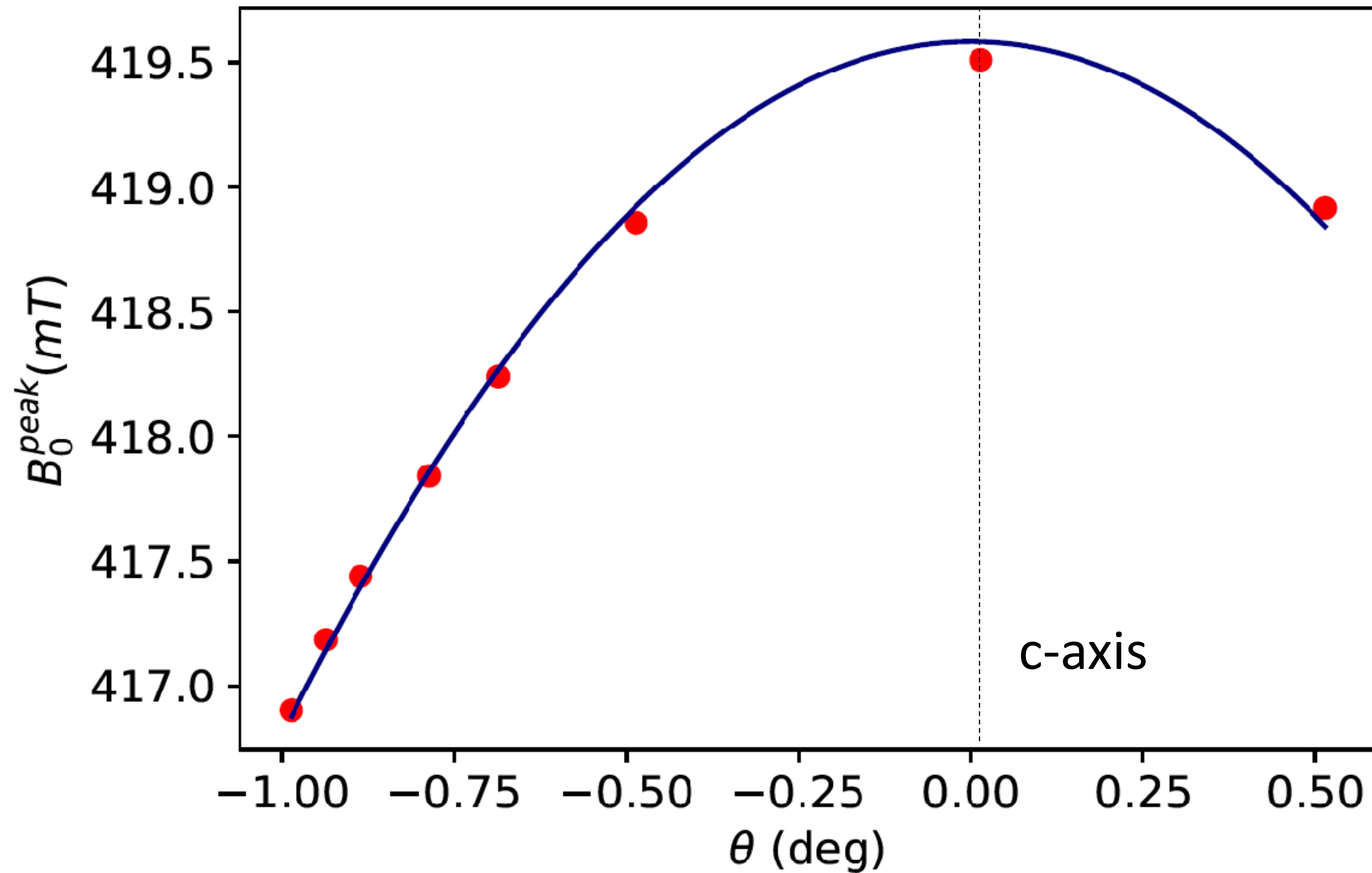
Detecting spins by their fluorescence  
with a microwave photon counter  
Nature **600**, 434-438 (2021)

# High-power spectroscopy

Integration time : 200ms



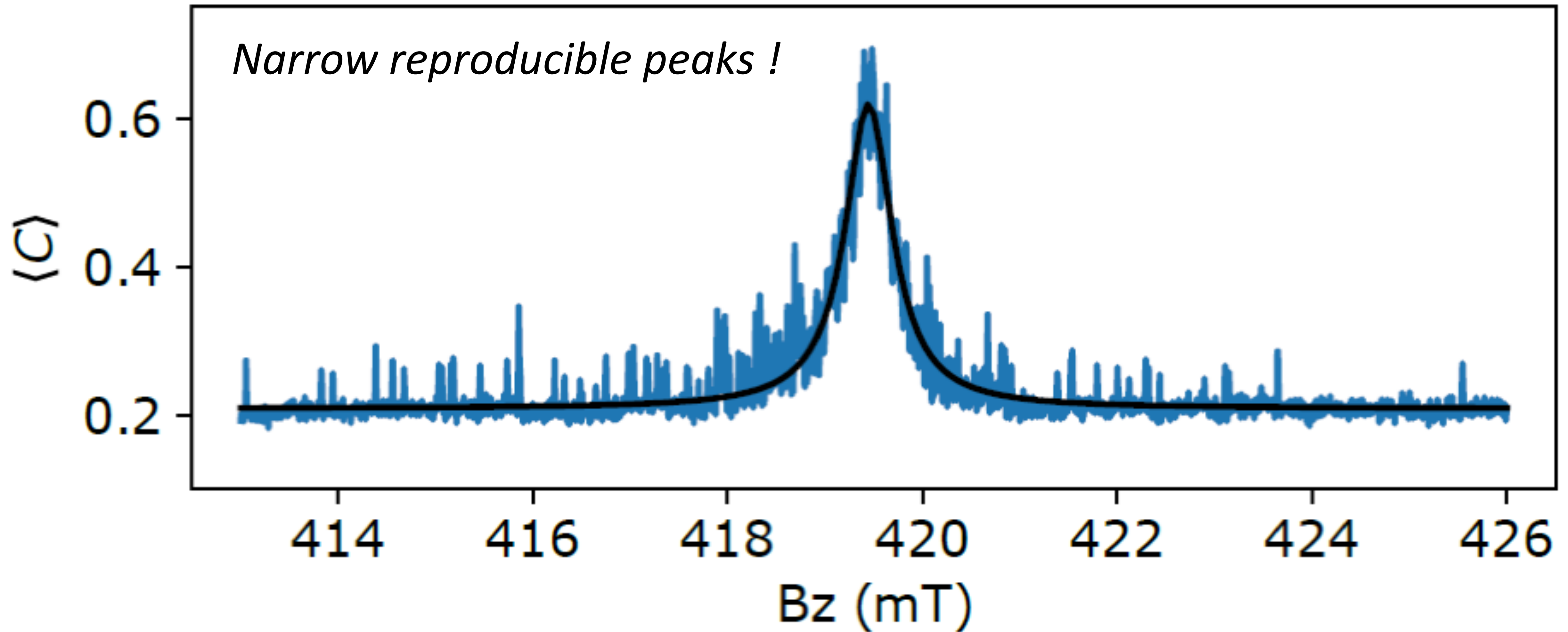
# High-power spectroscopy : angular dependence



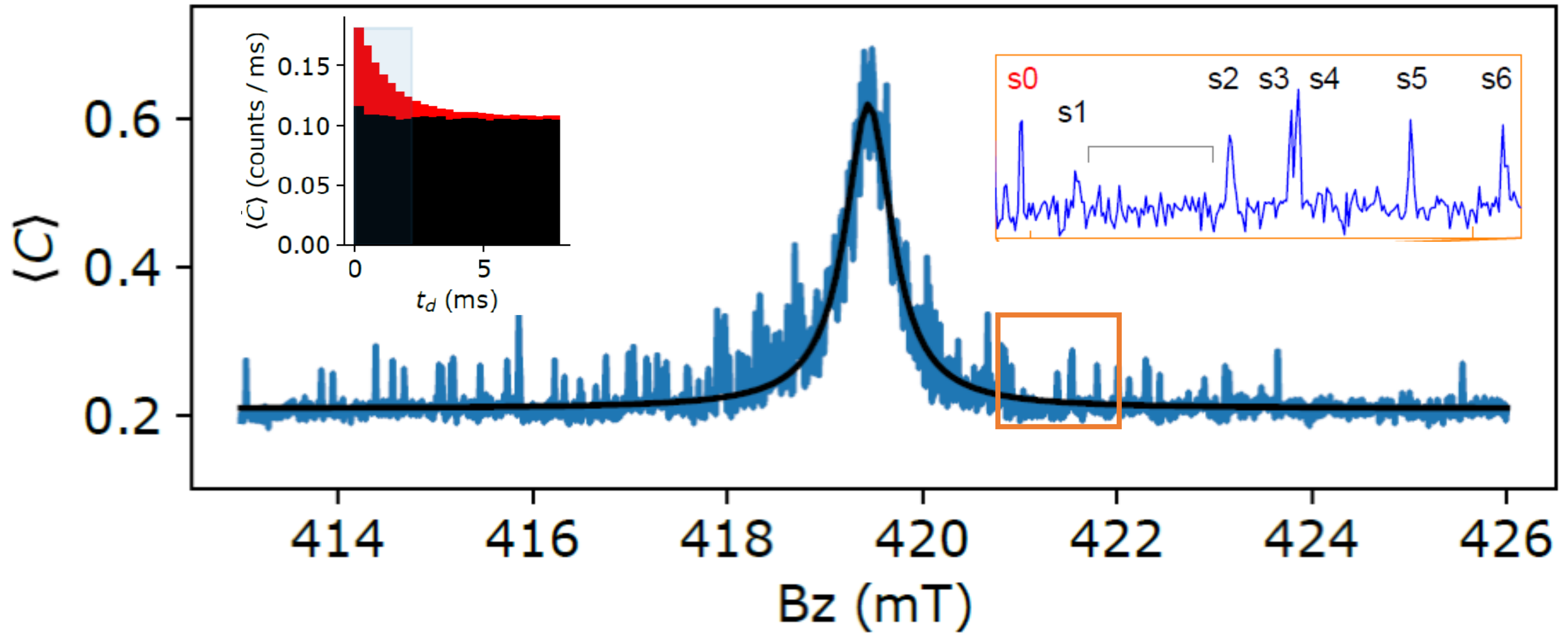
$$\gamma_{\mathbf{e}} = \begin{pmatrix} 117 & 0 & 0 \\ 0 & 117 & 0 \\ 0 & 0 & 17 \end{pmatrix} \text{ GHz/T}$$

# Low-power spectroscopy ( $\theta = 0^\circ$ )

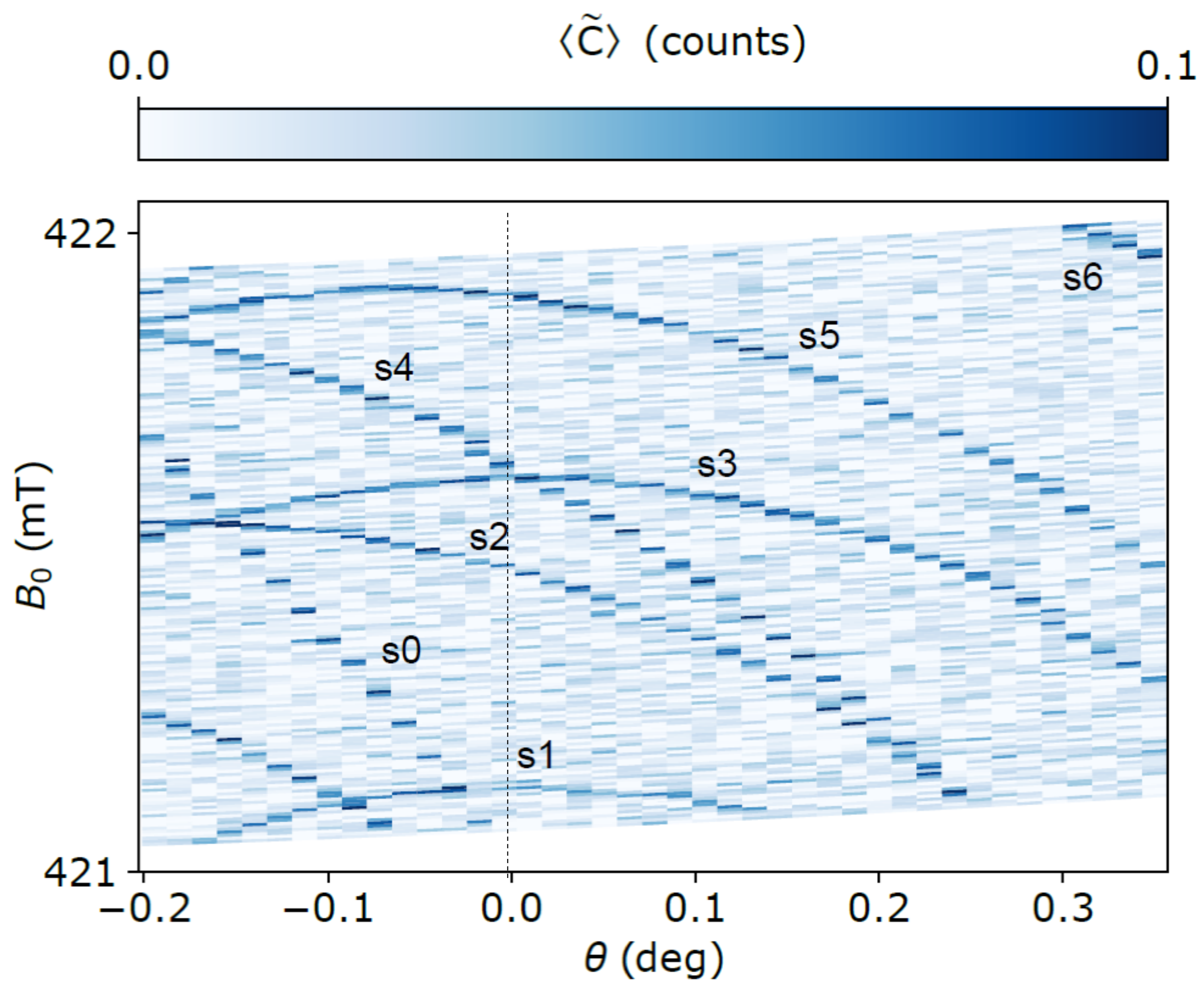
Integration time : 2ms



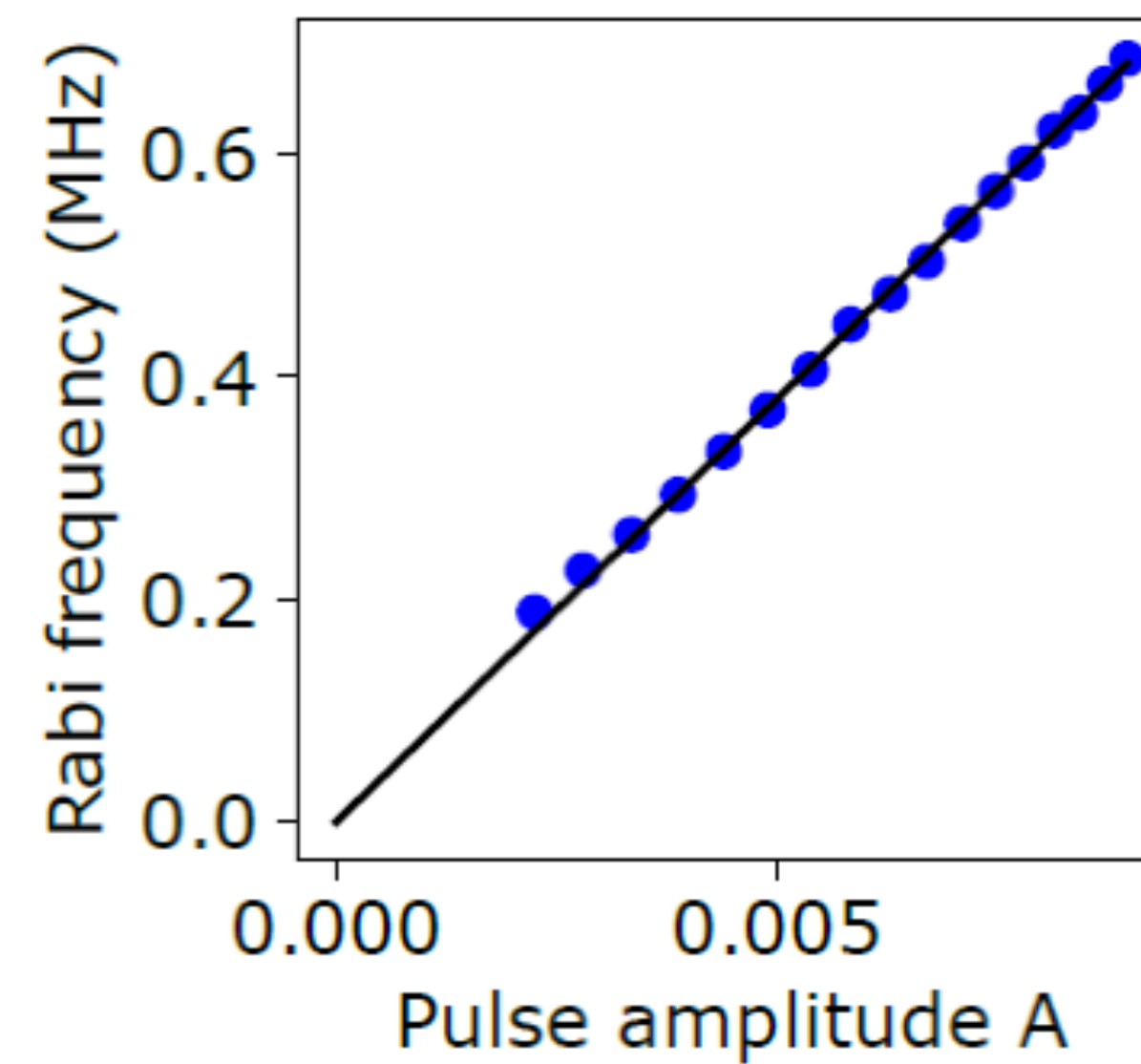
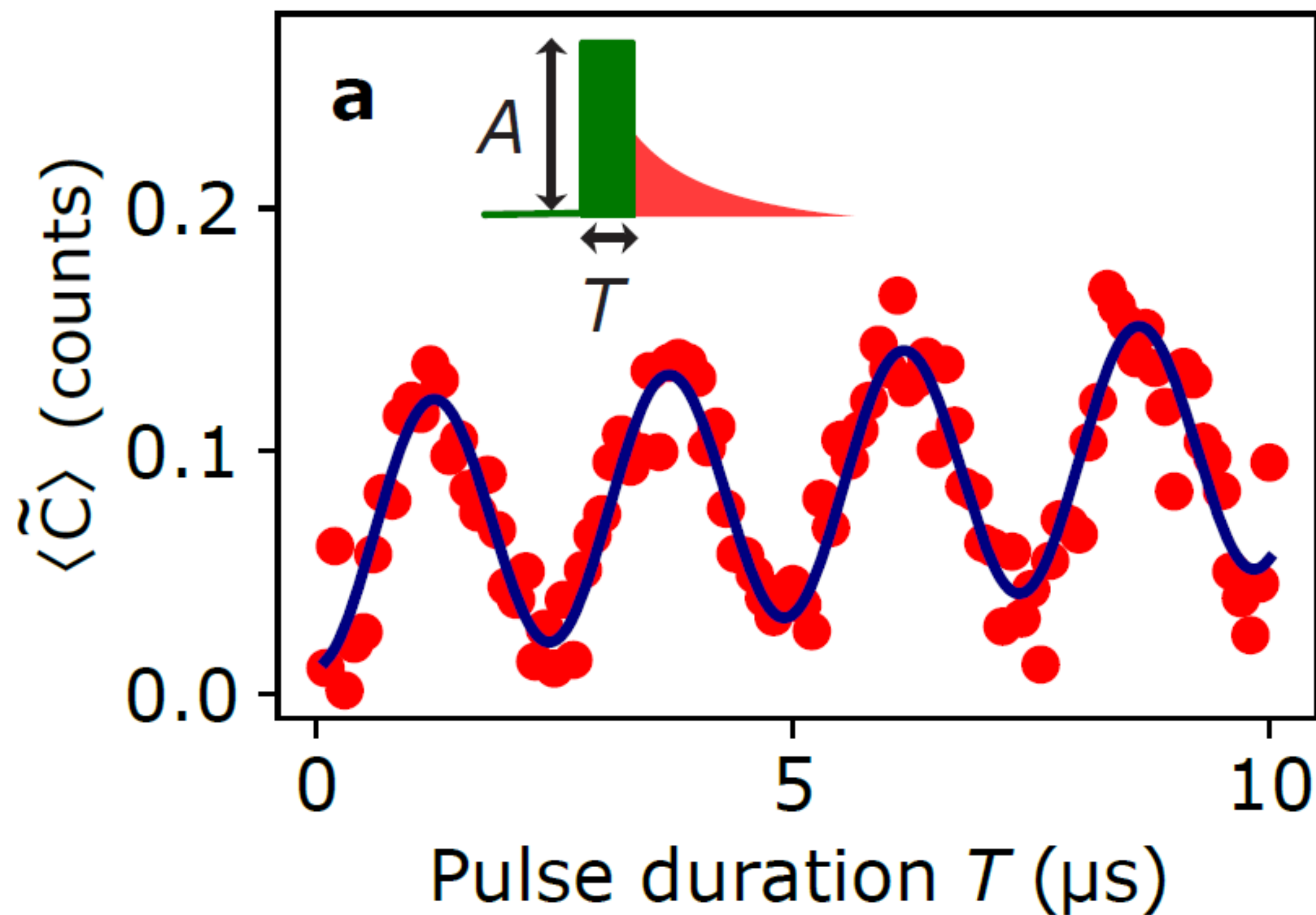
# Low-power spectroscopy ( $\theta = 0^\circ$ )



# Low-power spectroscopy : angular dependence

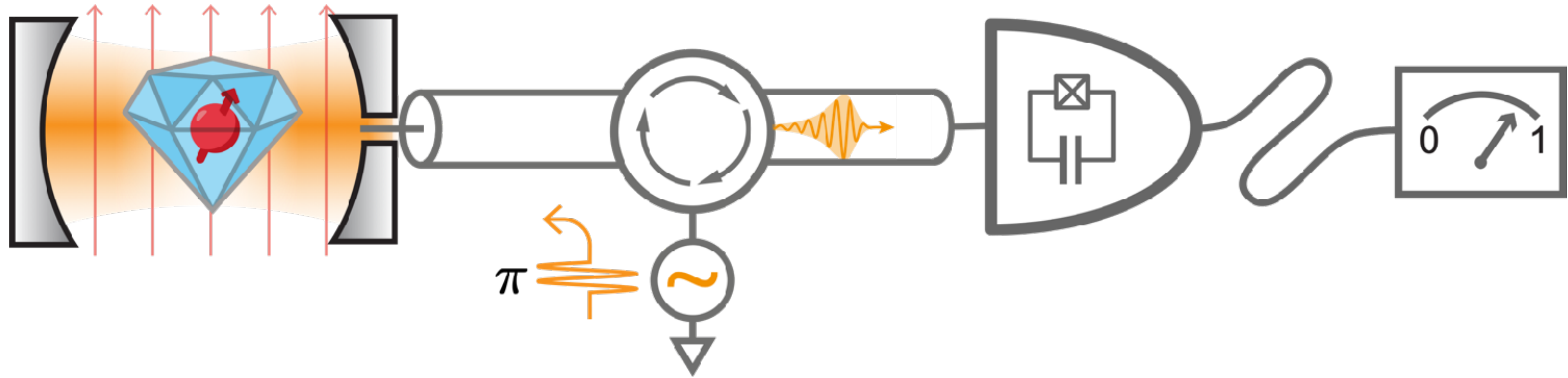


# Rabi oscillations



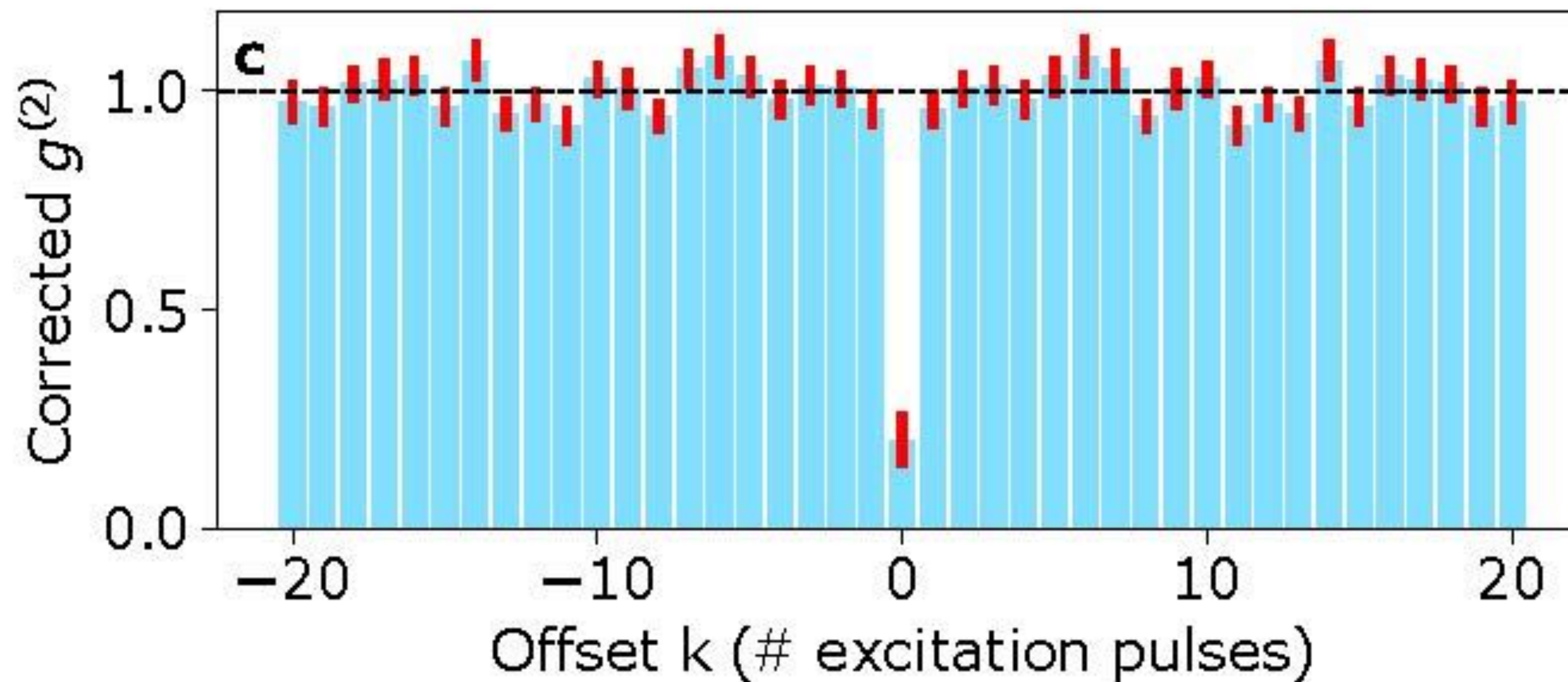


# Intensity-intensity correlations



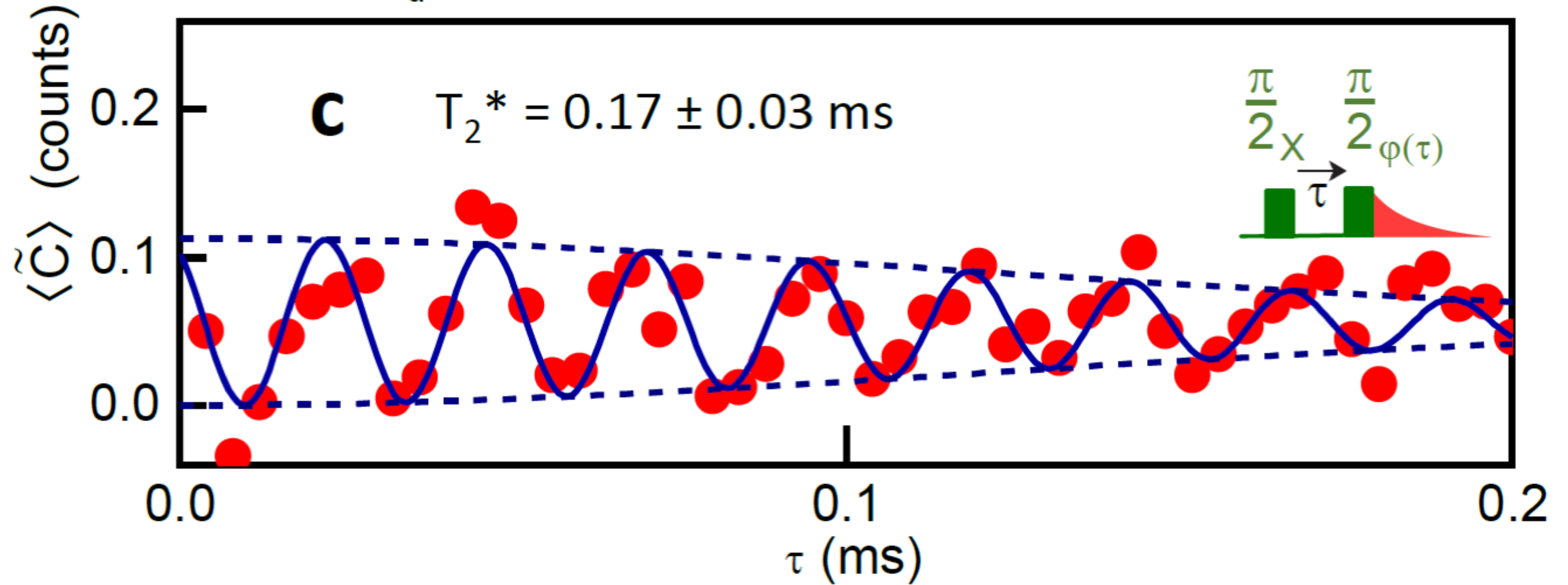
$$g^{(2)}(\tau) = \frac{\langle C(0)C(\tau) \rangle}{\langle C(0) \rangle \langle C(\tau) \rangle}$$

# Intensity-intensity correlation function

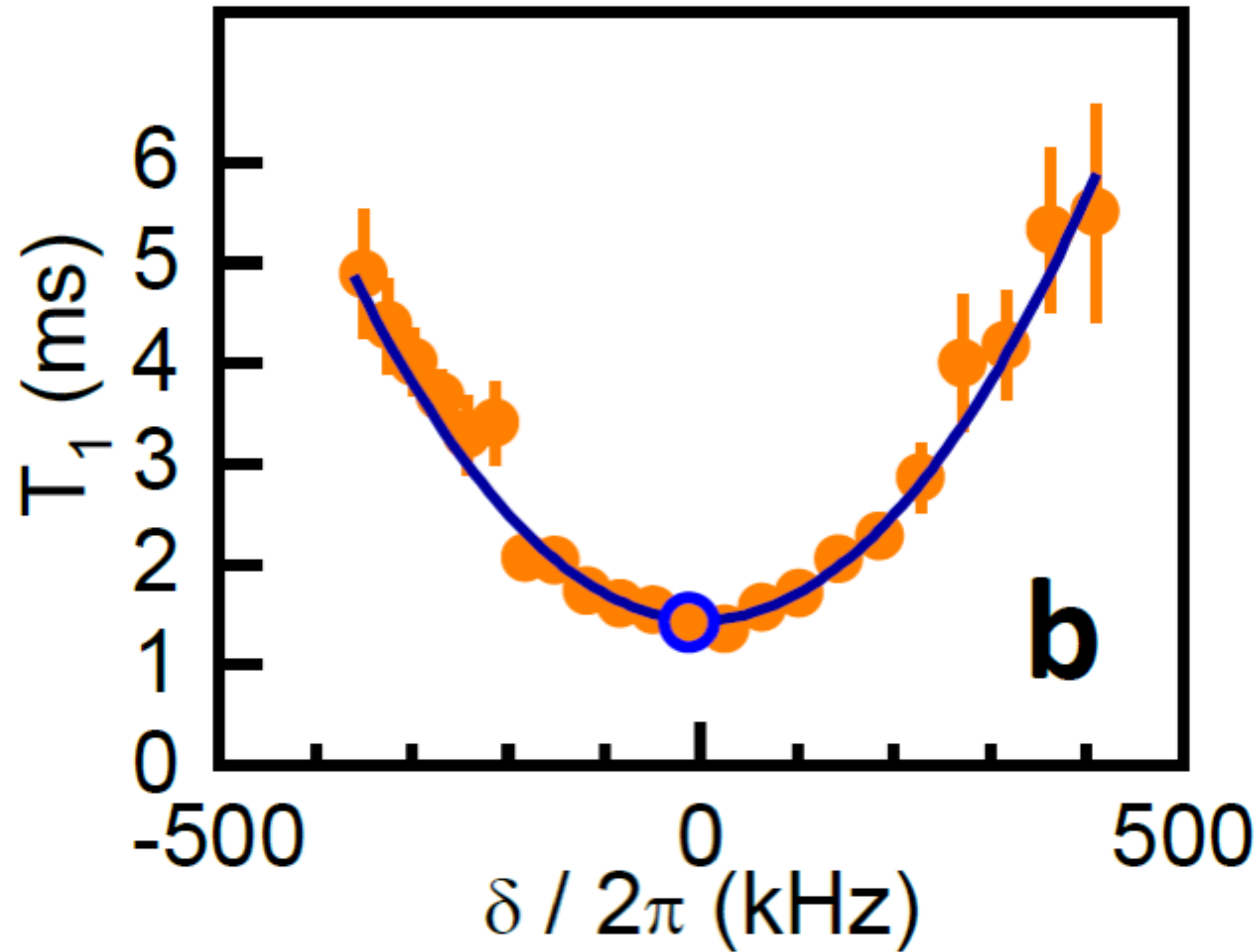


$g^2(0) = 0.23 \pm 0.06 < 0.5$   $\longrightarrow$  Single-spin emission

# Single-ion coherence time (1) : Ramsey



# Purcell effect on a single spin



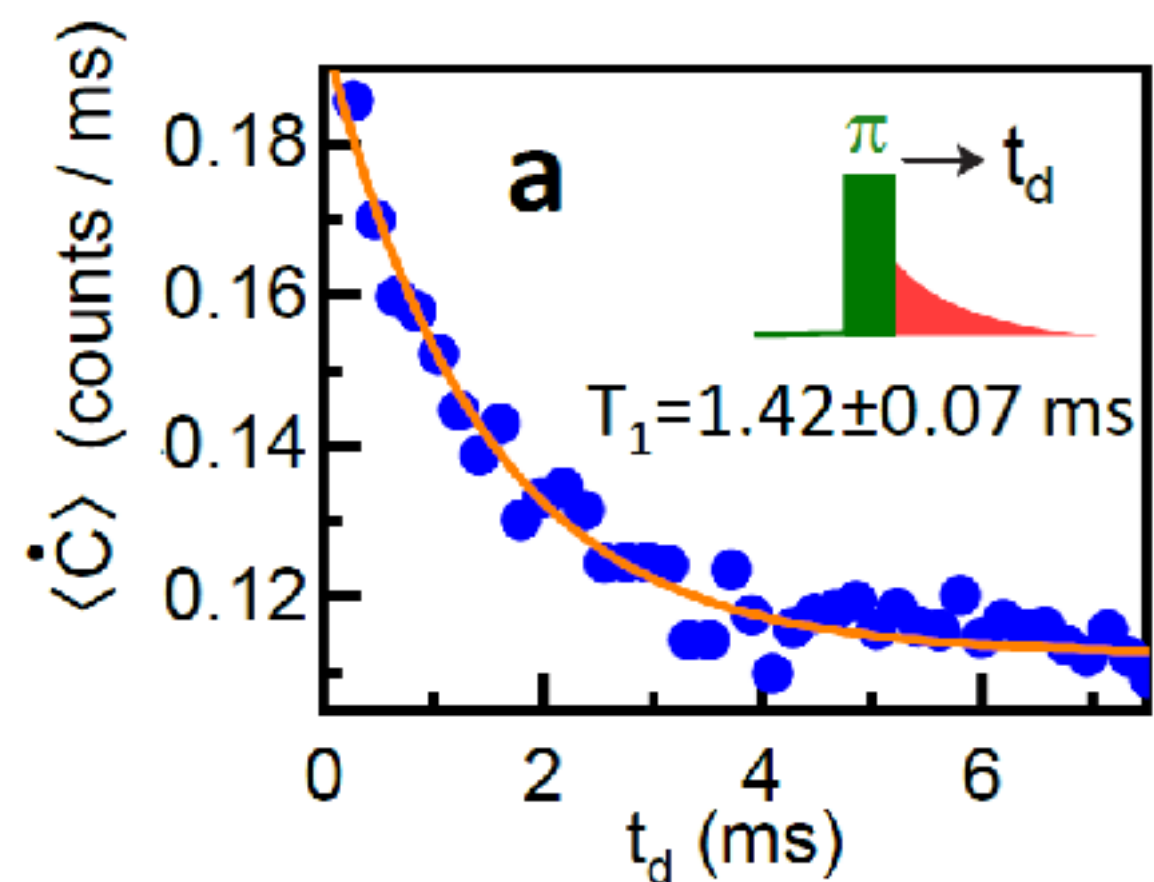
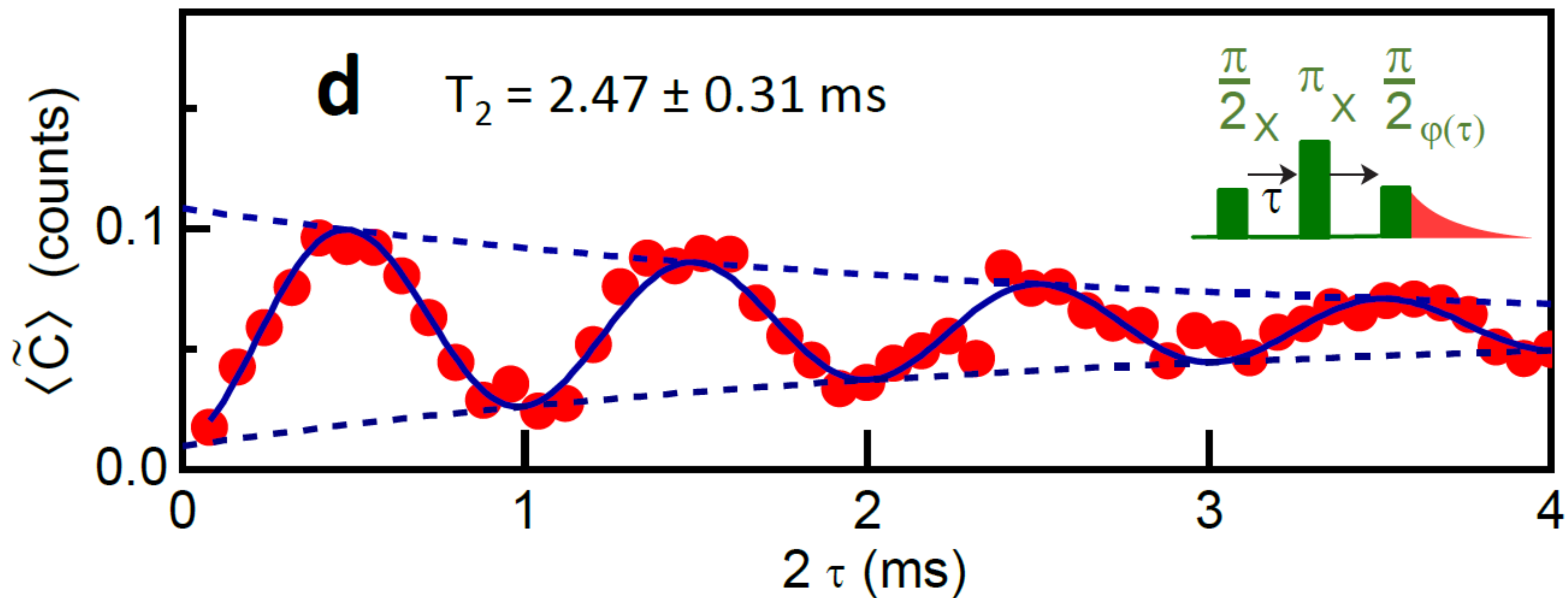
$$\Gamma_R = \frac{4g_0^2}{\kappa} \frac{1}{1 + 4\left[\frac{\delta}{\kappa}\right]^2}$$



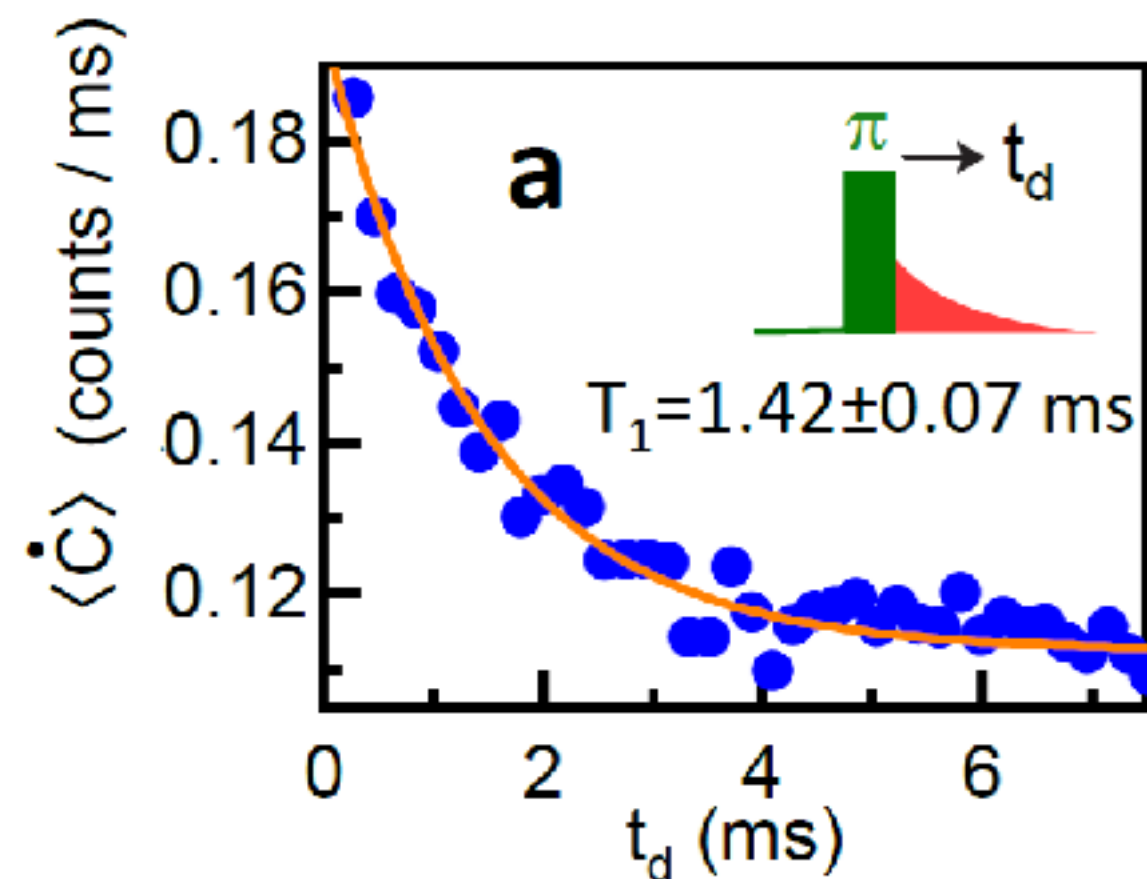
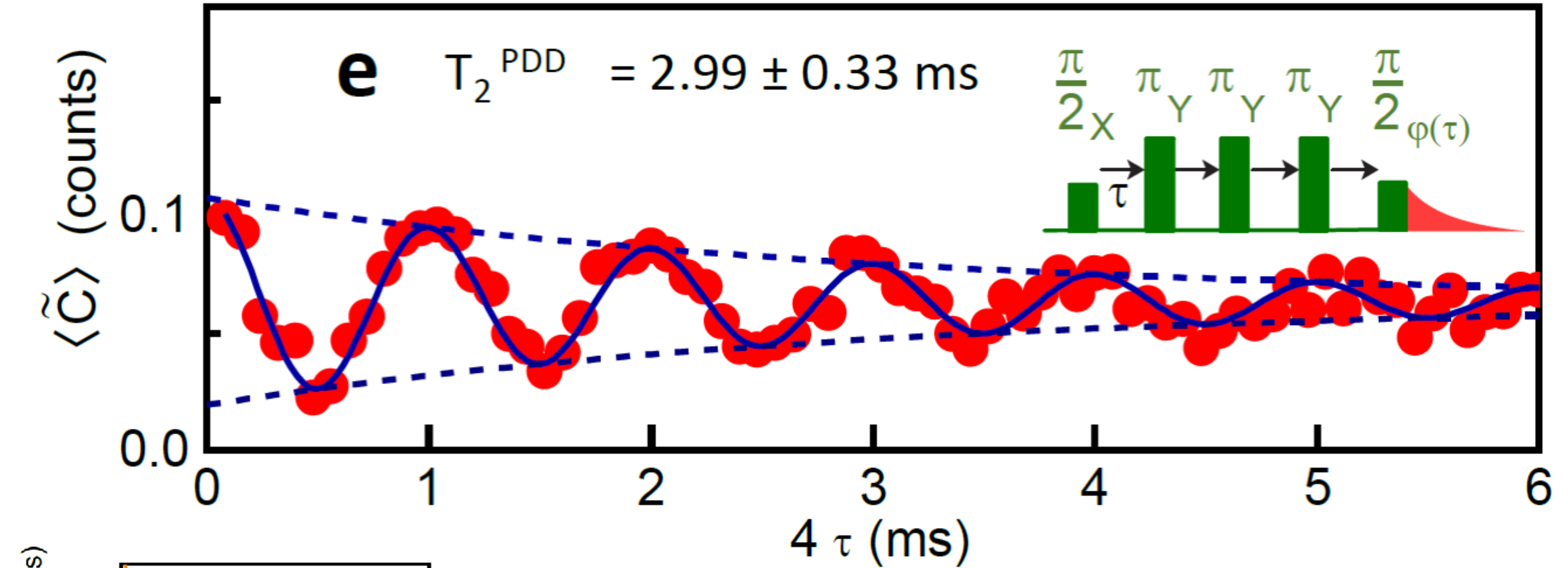
$$T_1 \cong \Gamma_R^{-1}$$

(Er<sup>3+</sup> spin in the Purcell regime)

# Single-ion coherence time (2) : Hahn echo

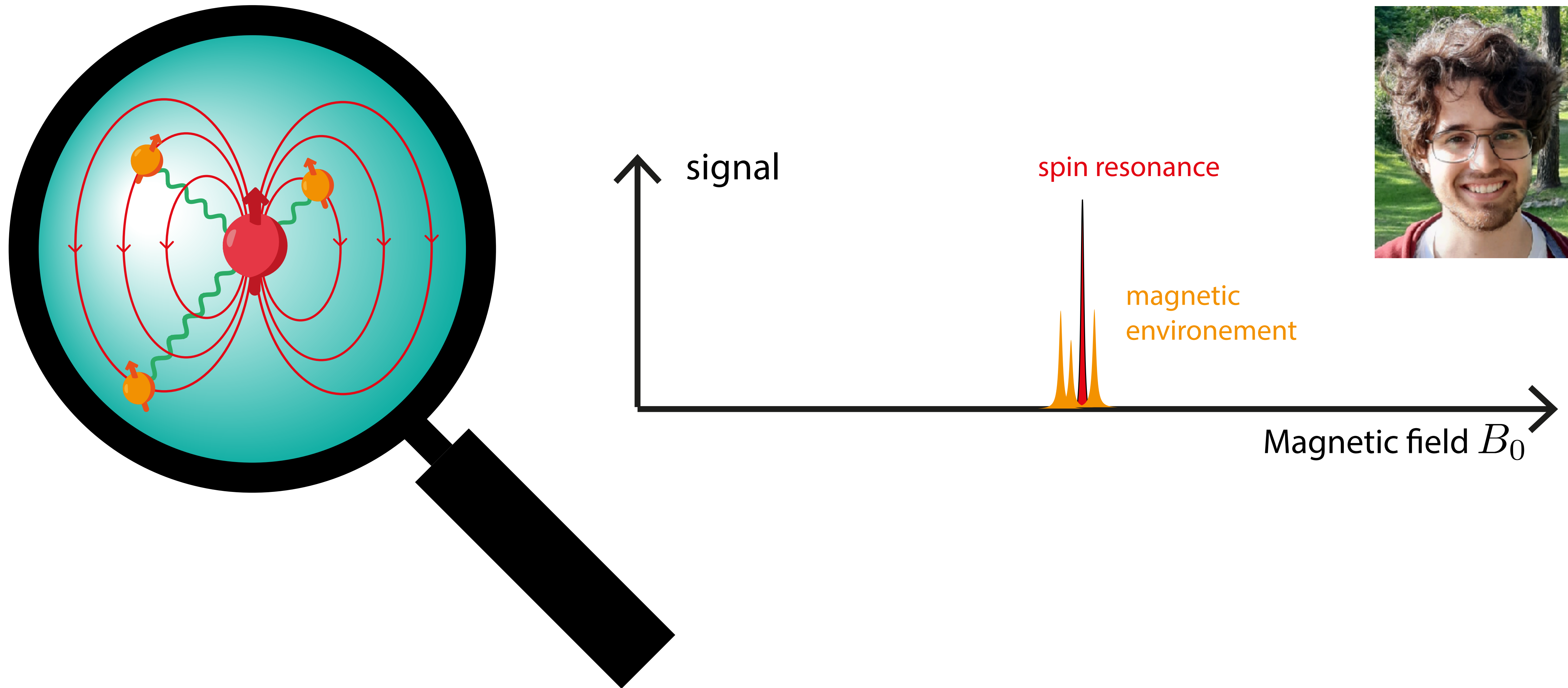


# Single-ion coherence time (3) : 3-Pulse Dynamical Decoupling

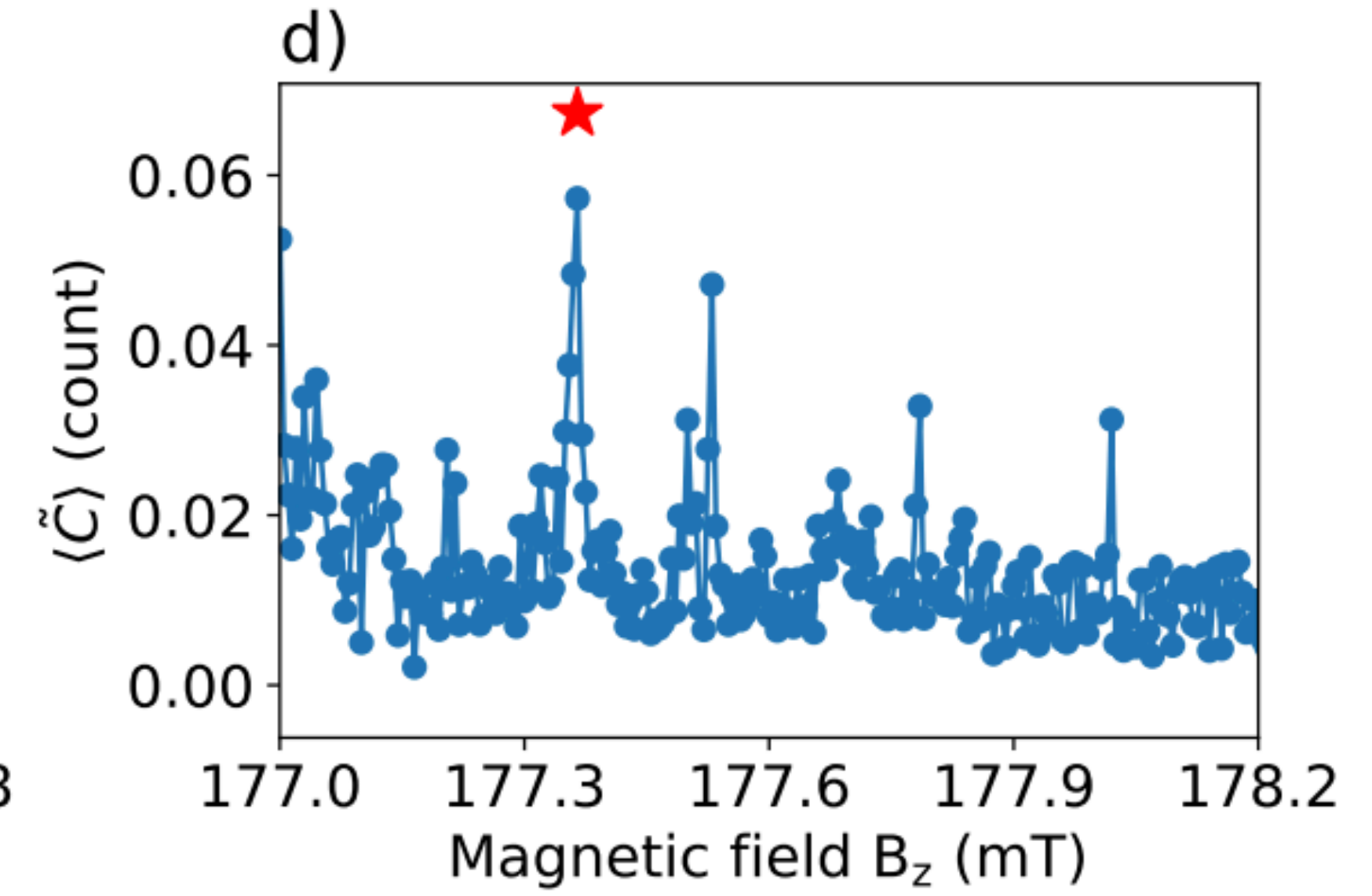
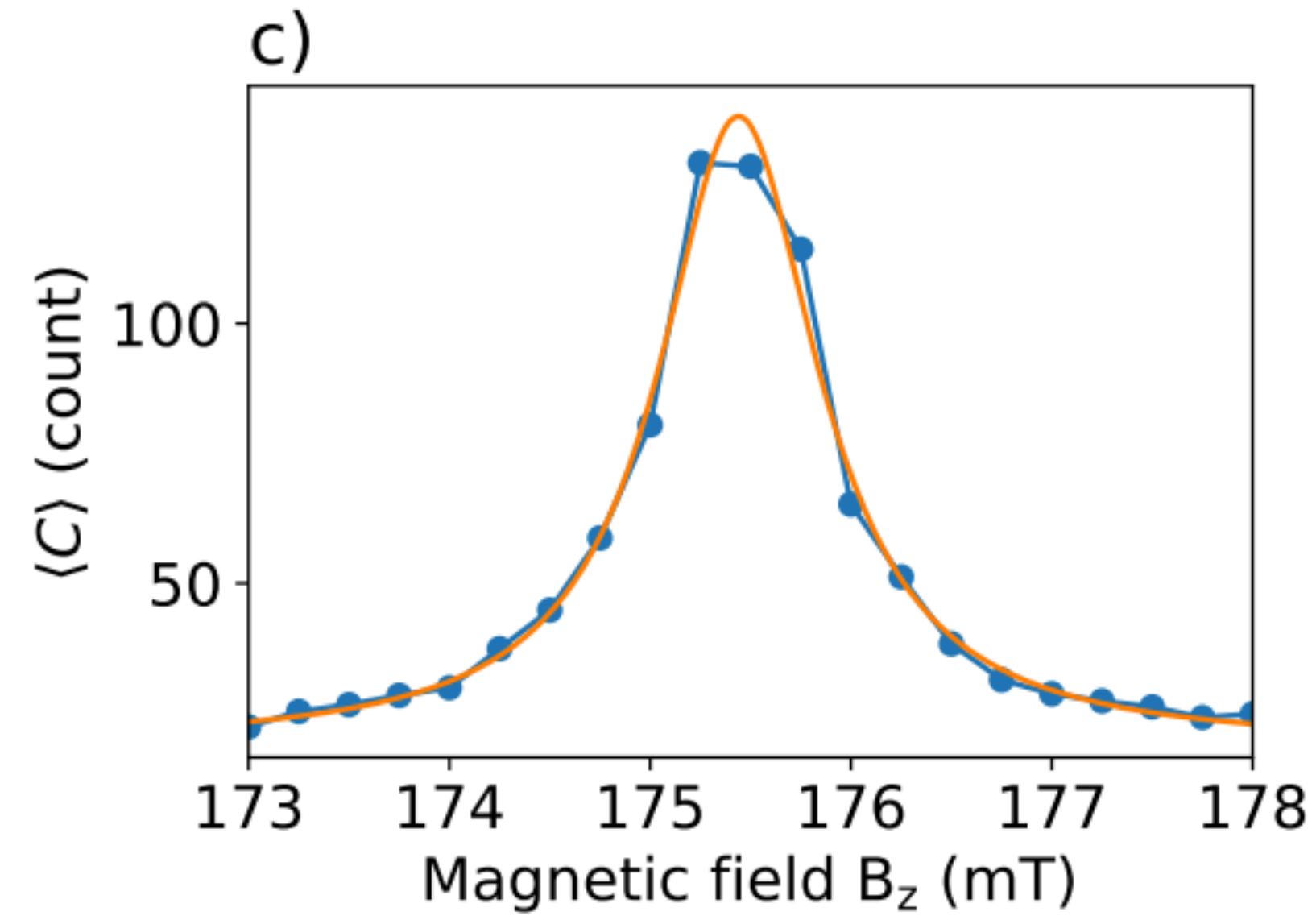
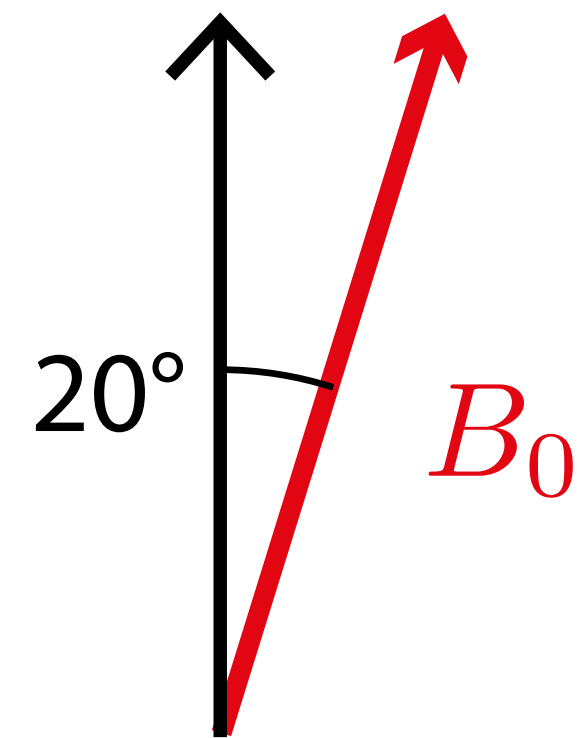
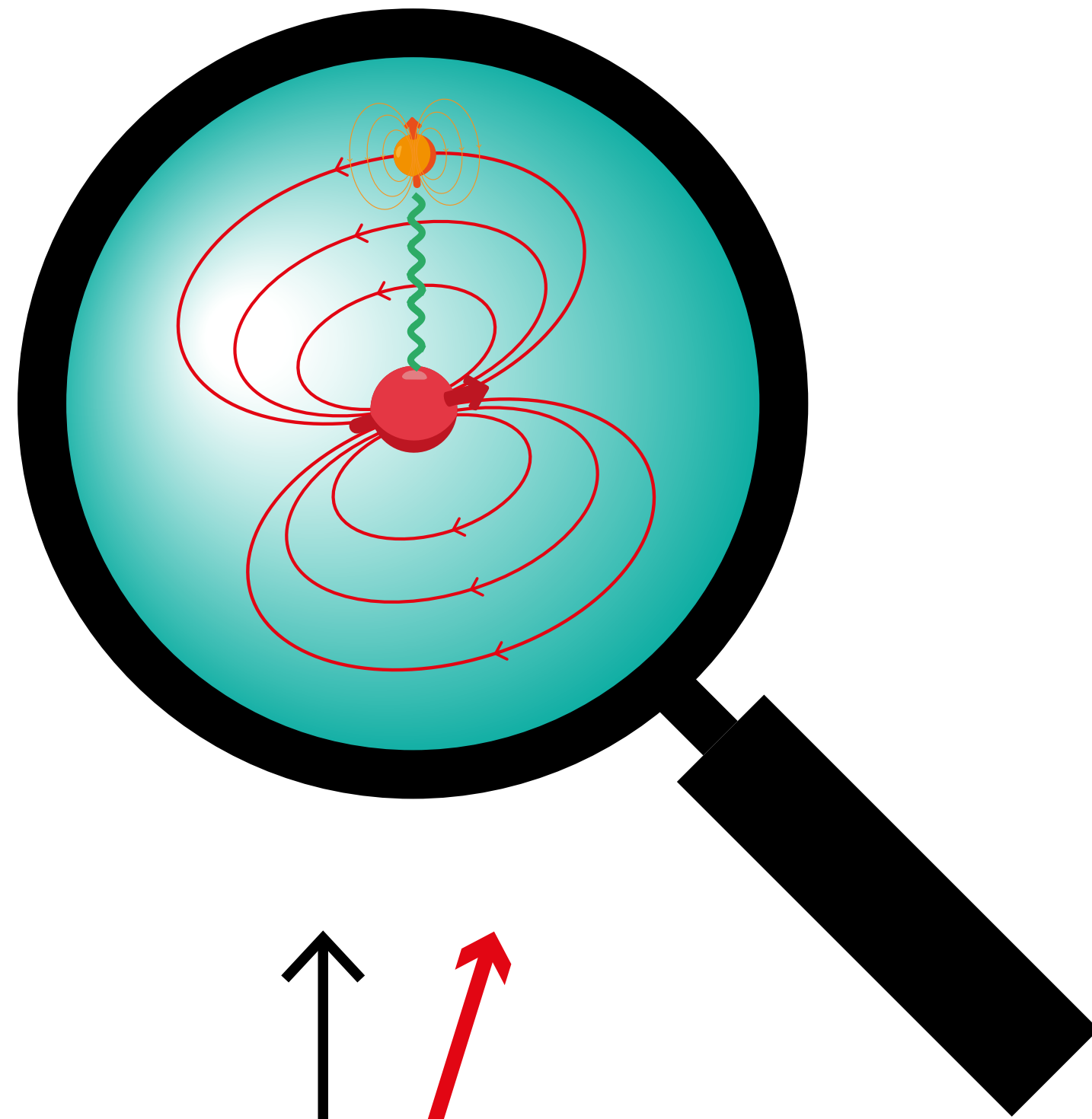


# Probing the nuclear environment

Jaime Travesedo

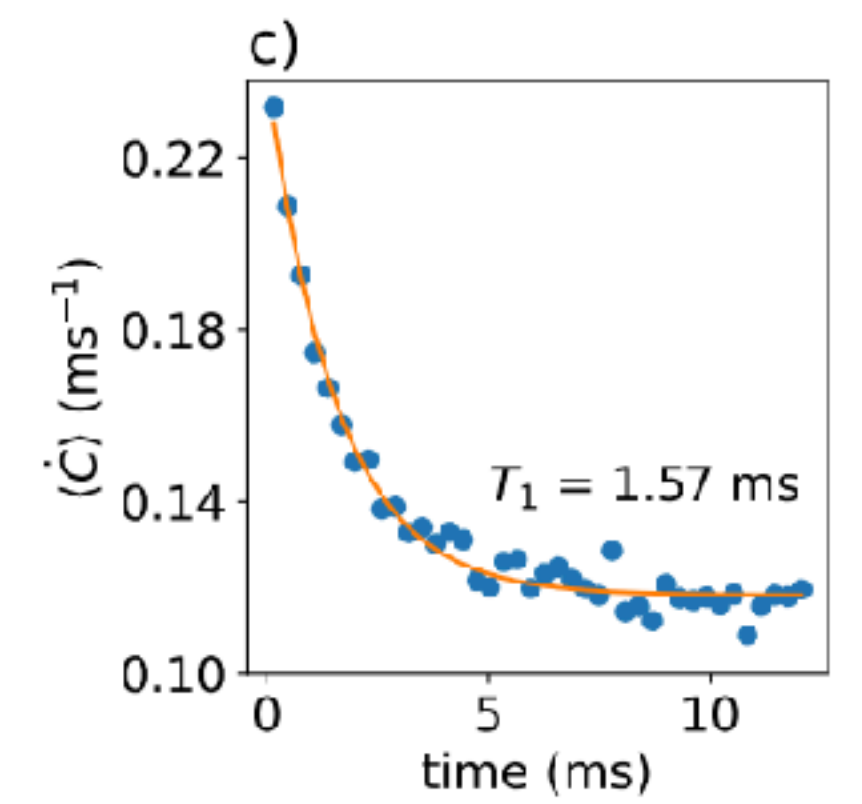
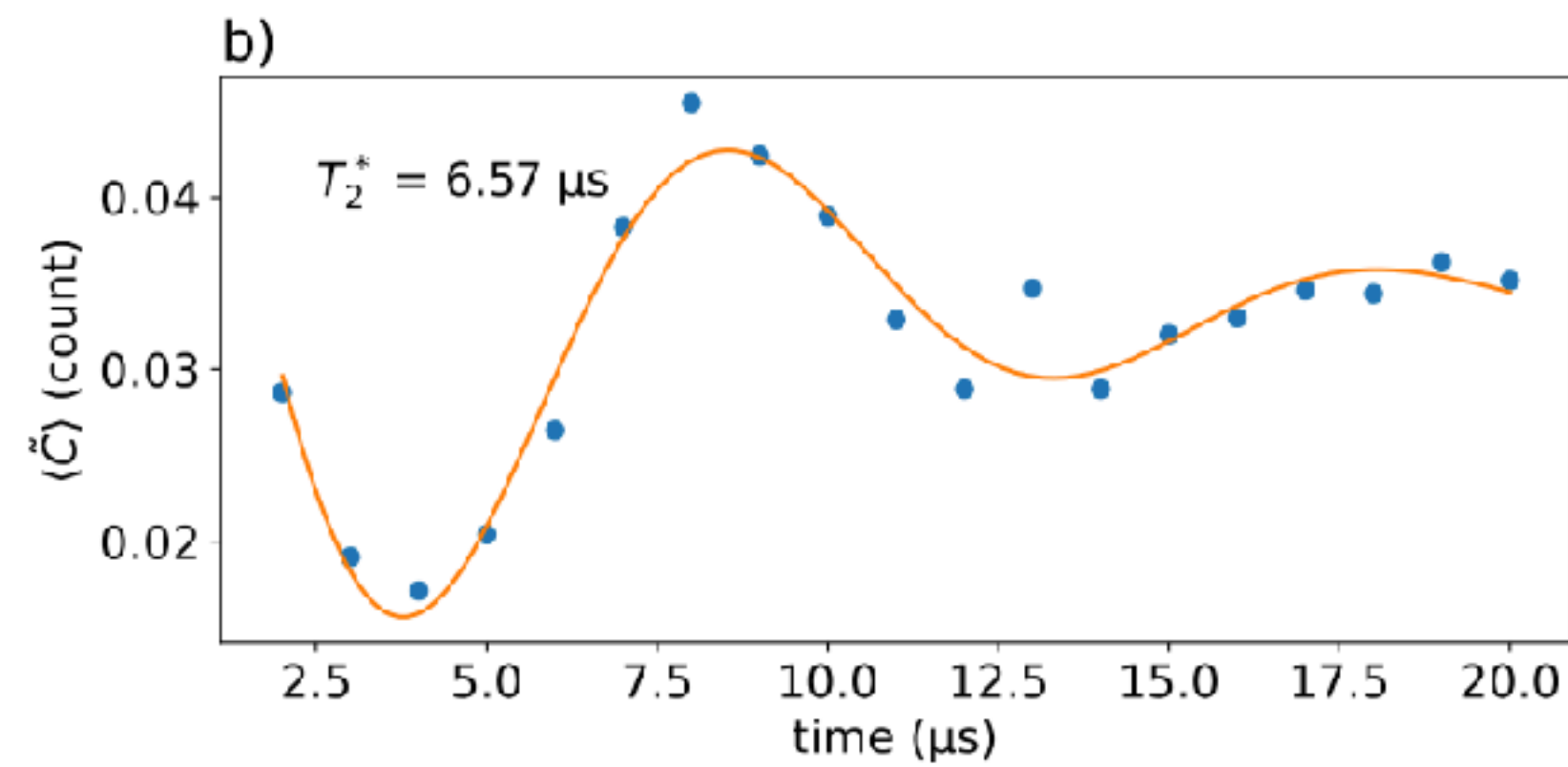
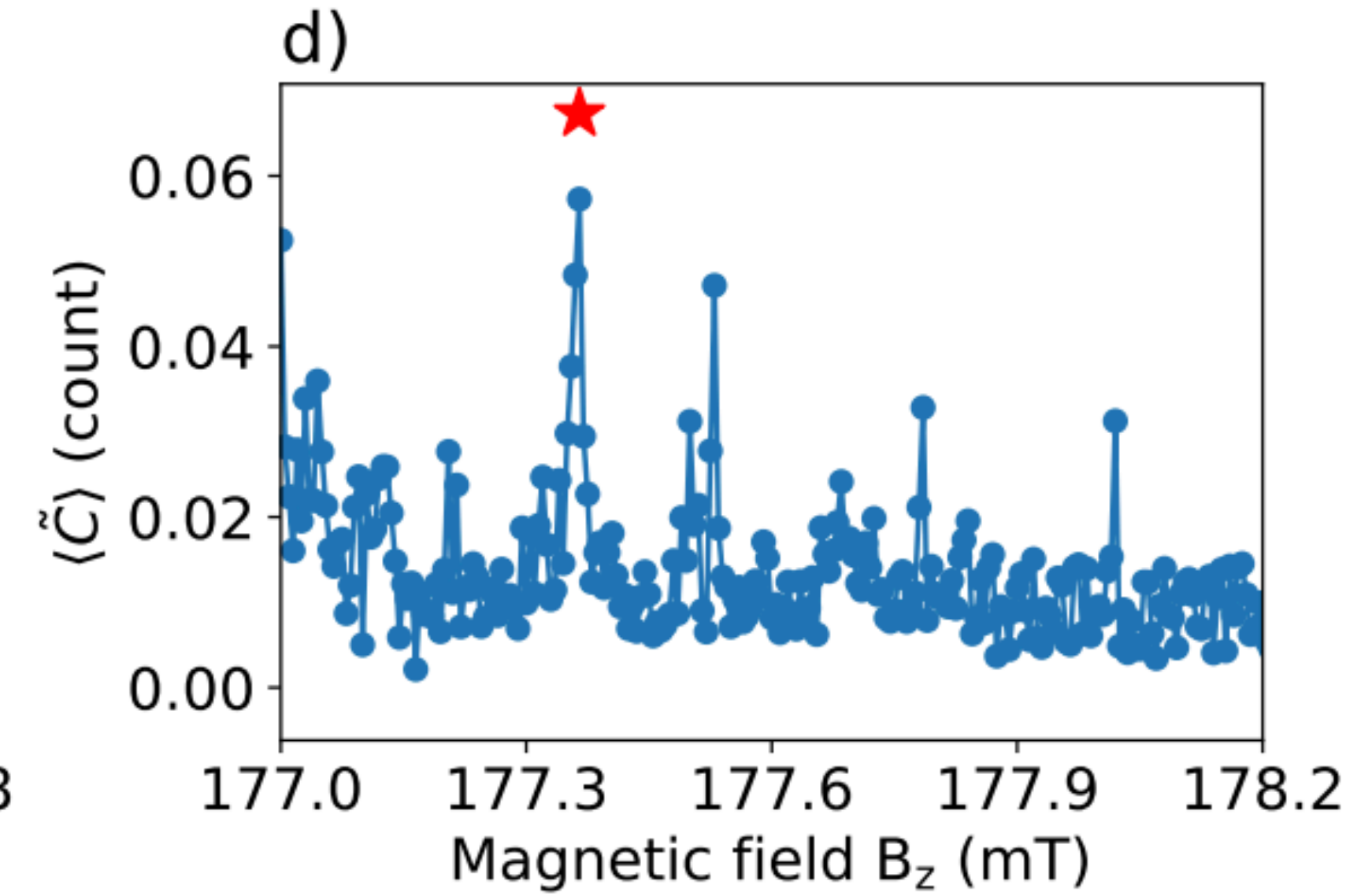
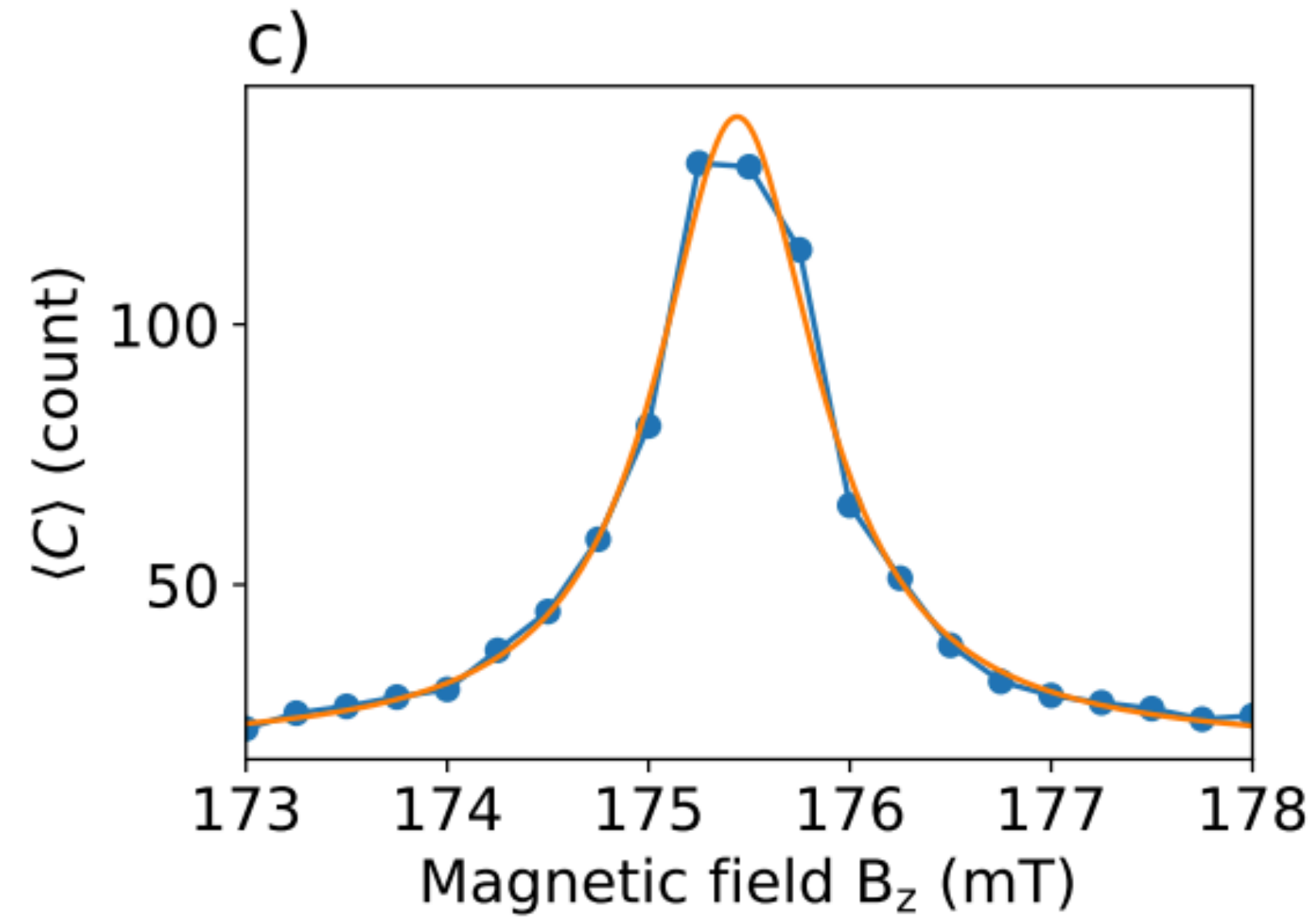
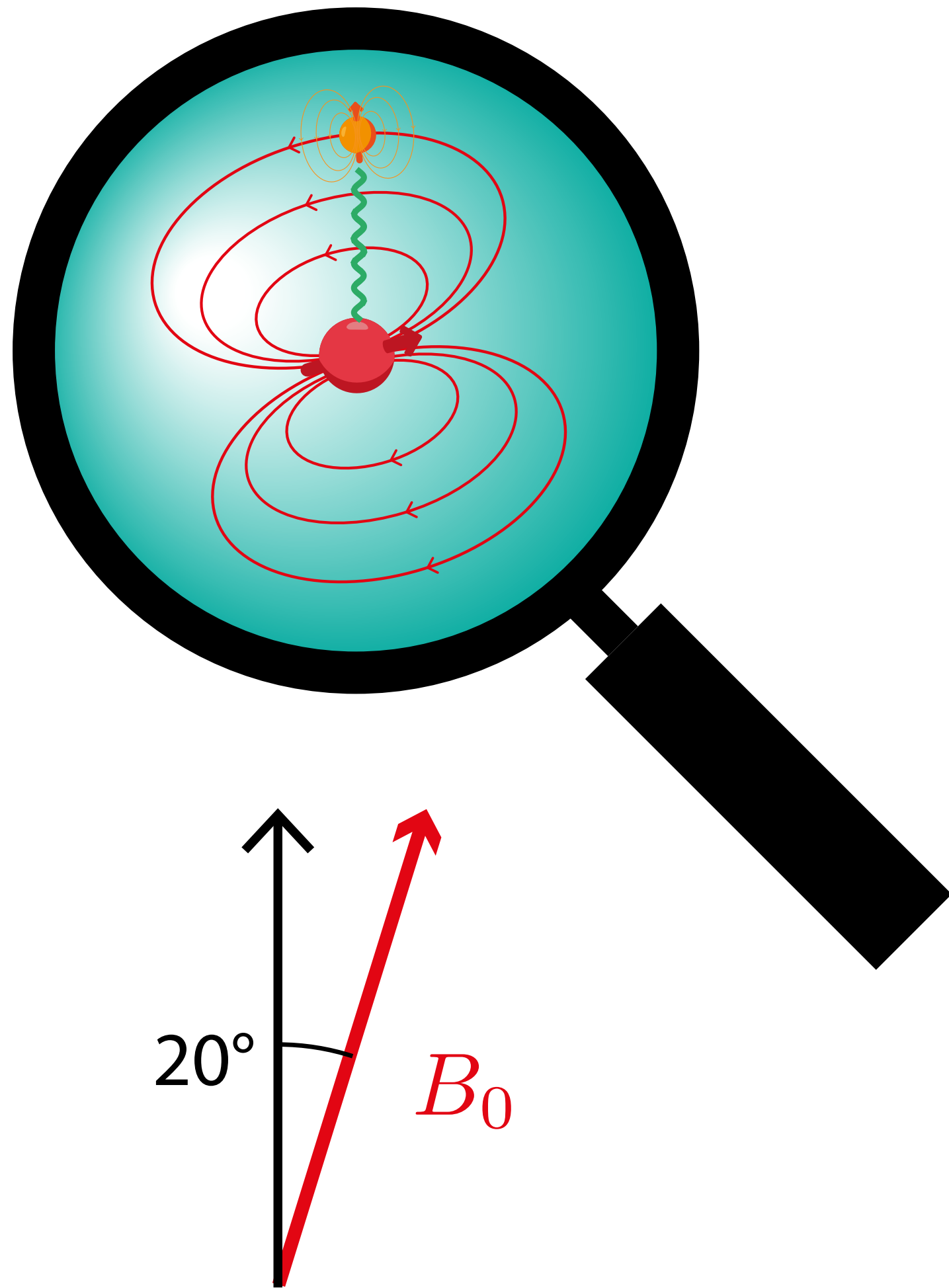


# Probing the nuclear environment

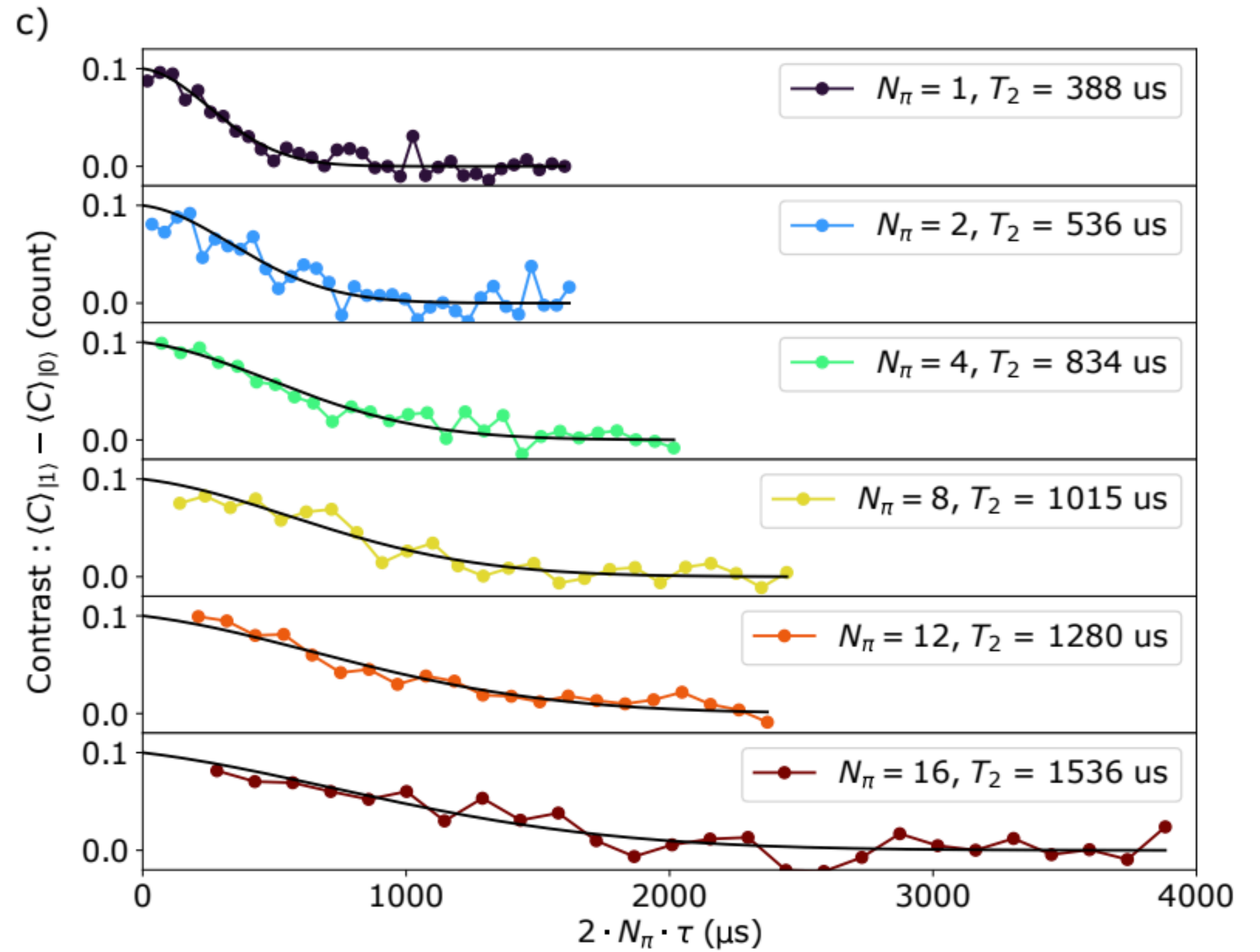
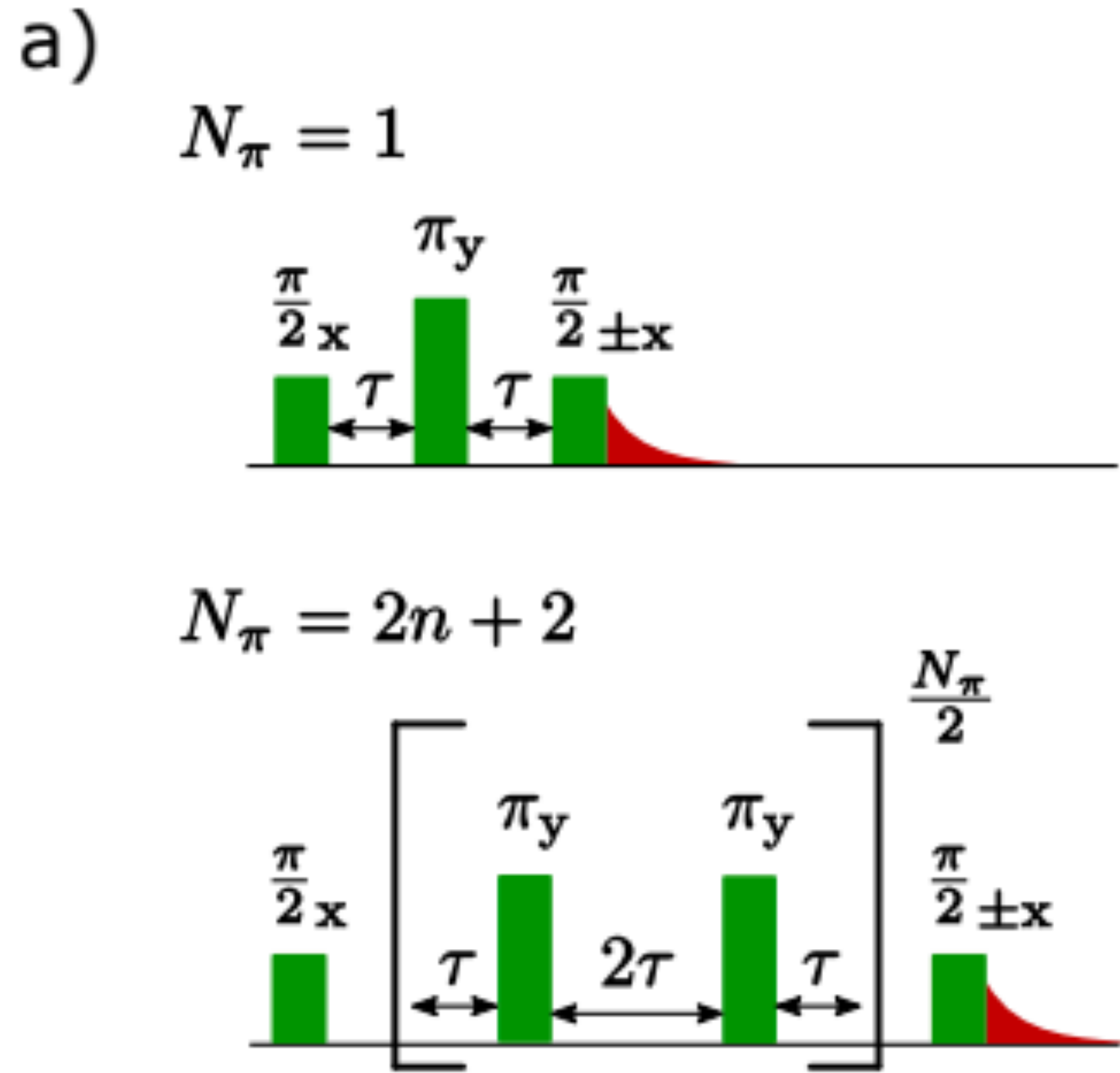




# Probing the nuclear environment

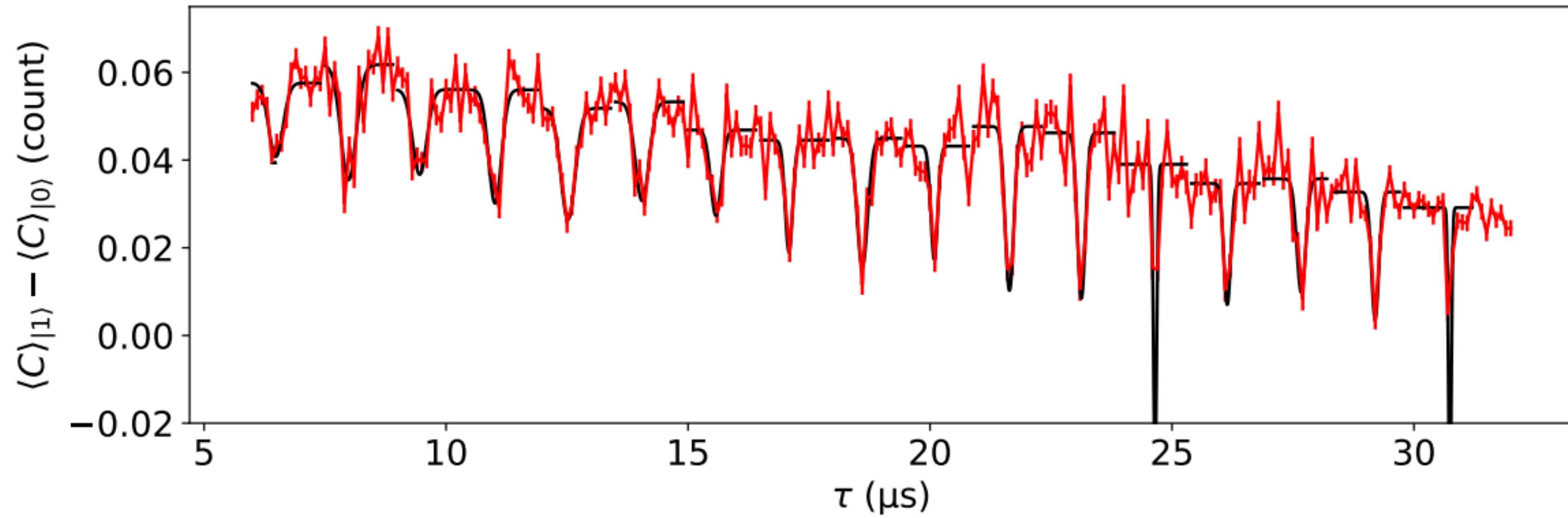
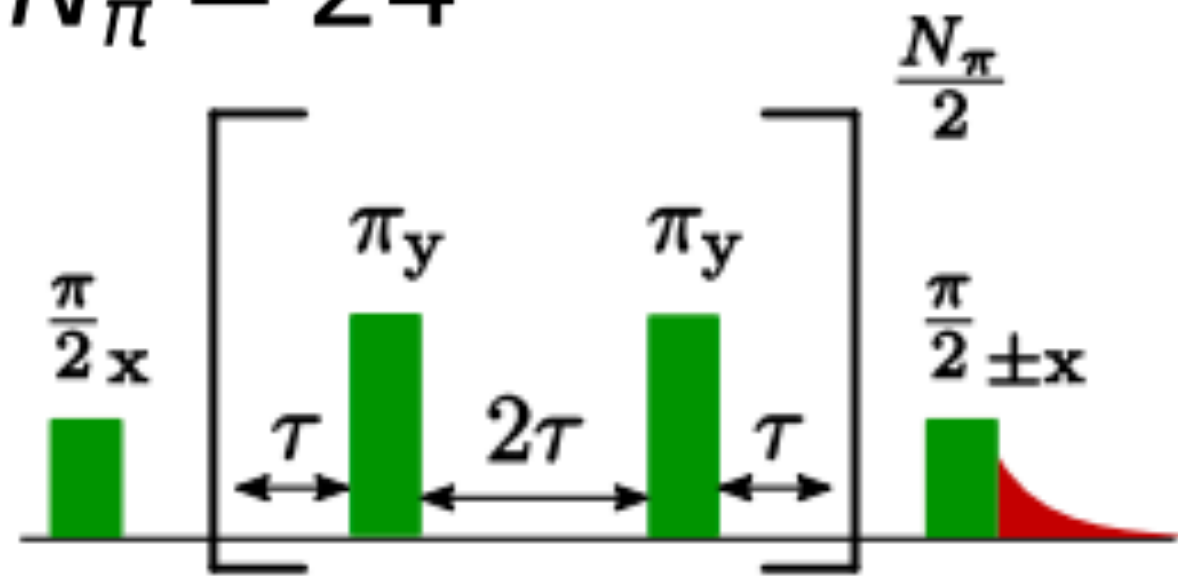


# Dynamical decoupling

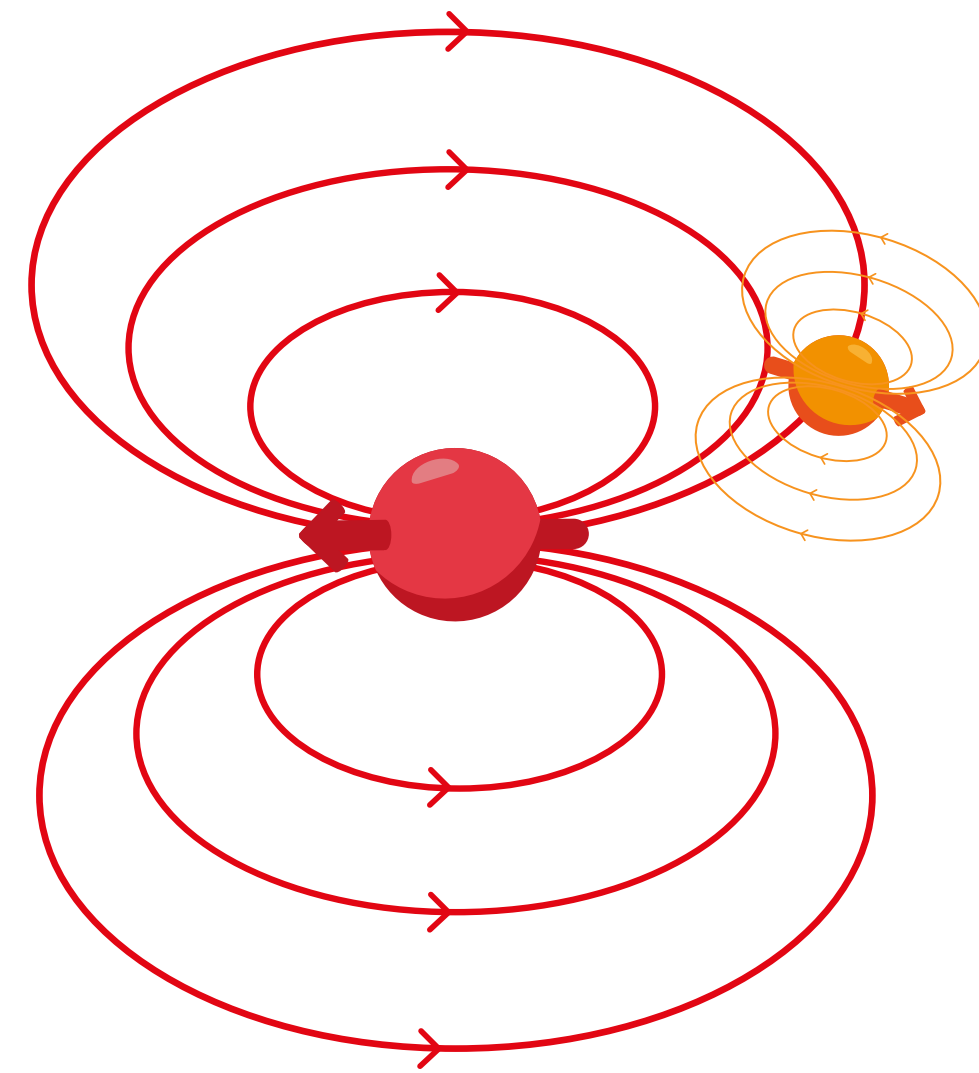
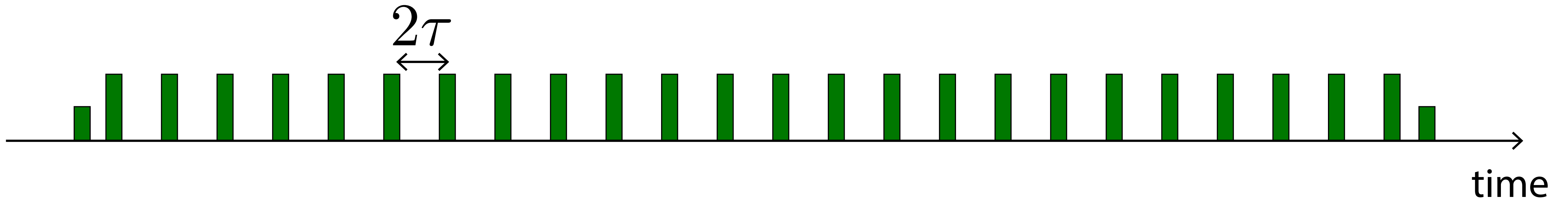


# Dynamical decoupling

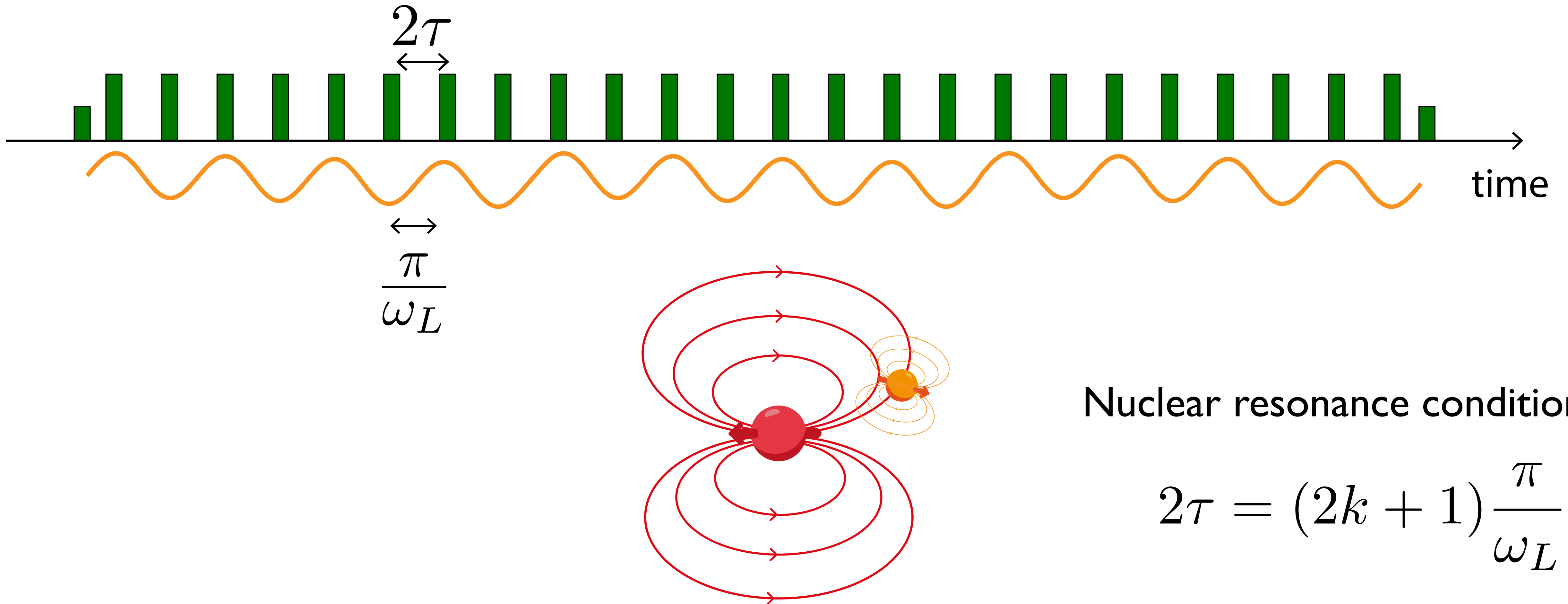
$$N_{\pi} = 24$$



# Dynamical decoupling as a nuclear spin probe



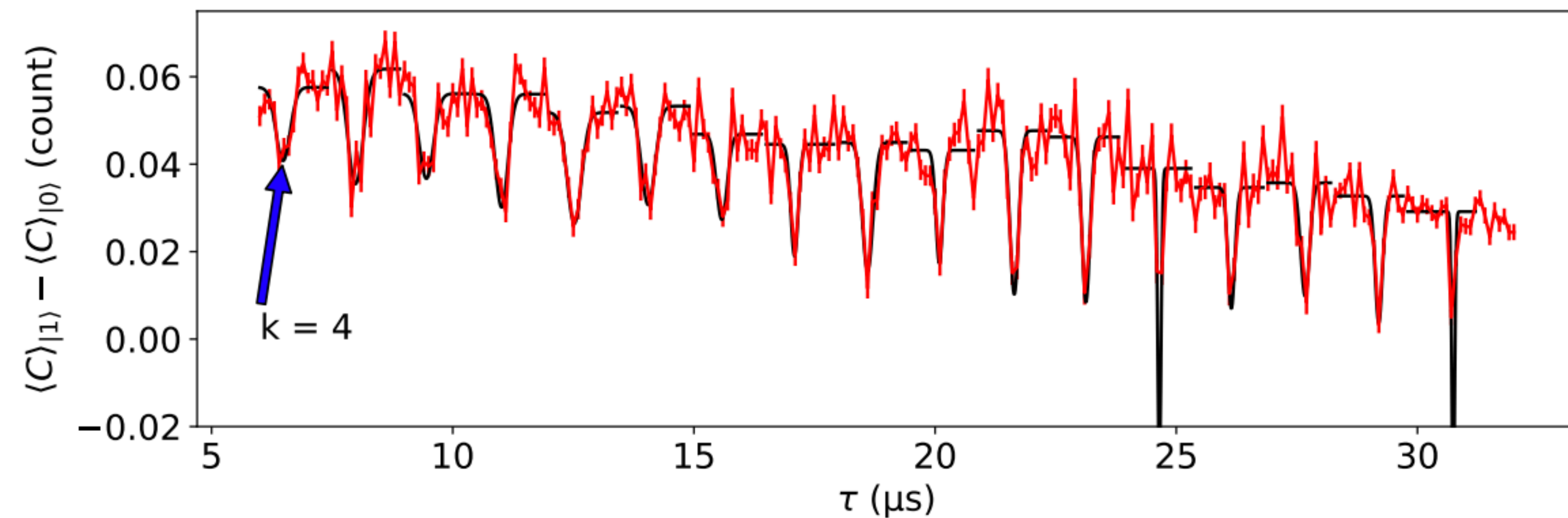
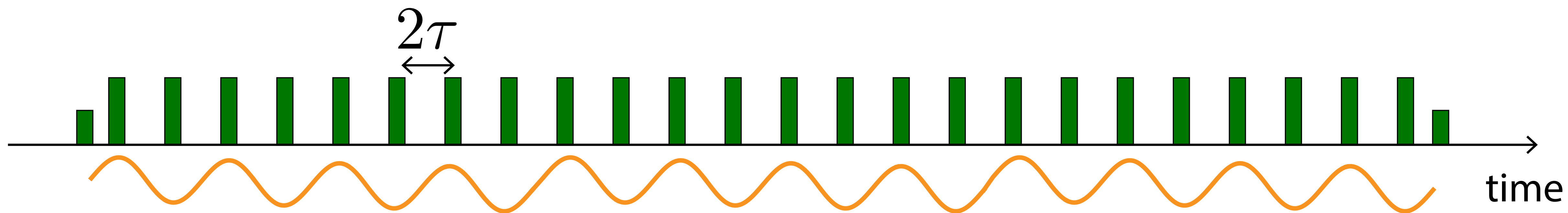
# Dynamical decoupling as a nuclear spin probe



Nuclear resonance condition :

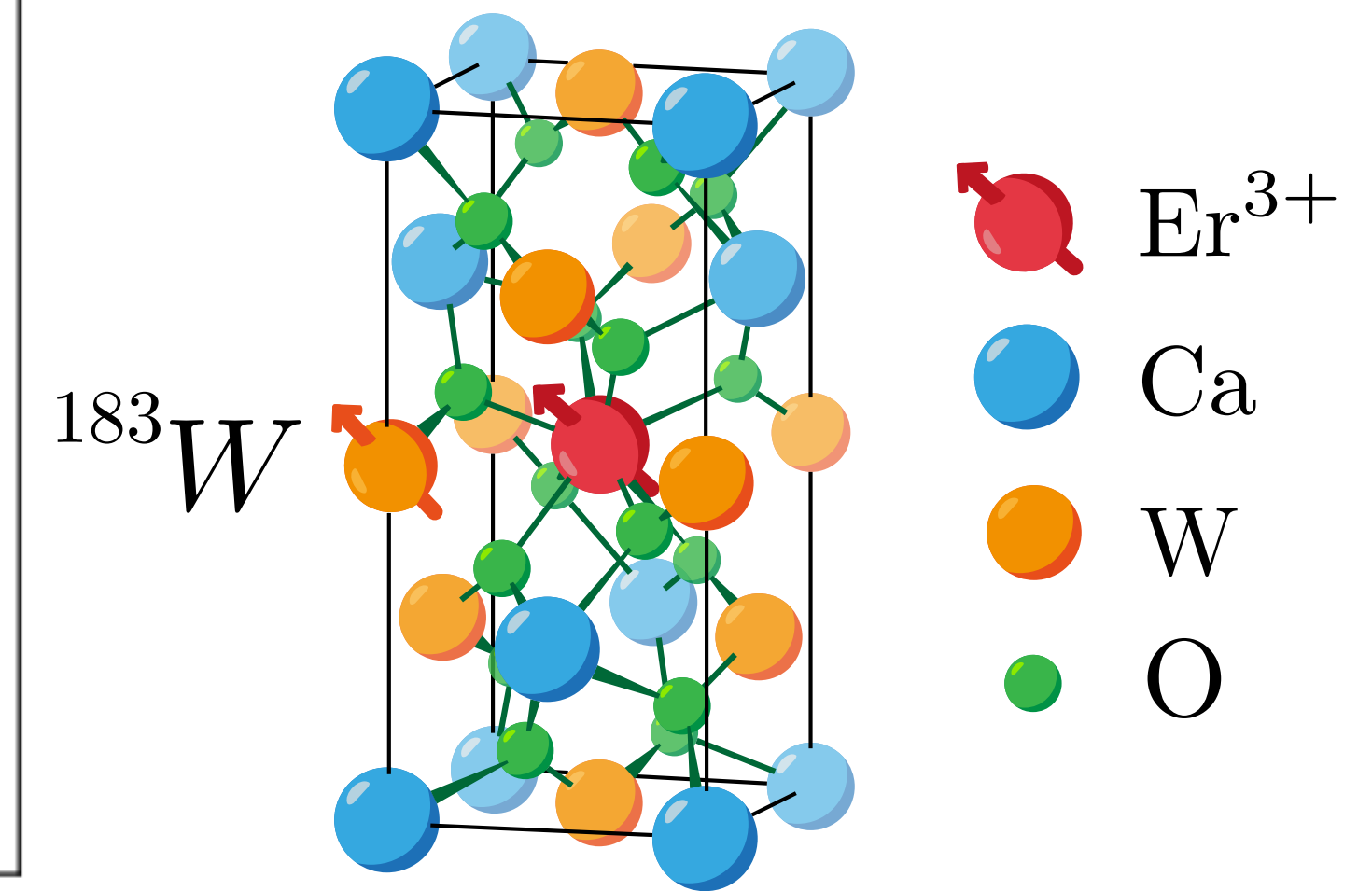
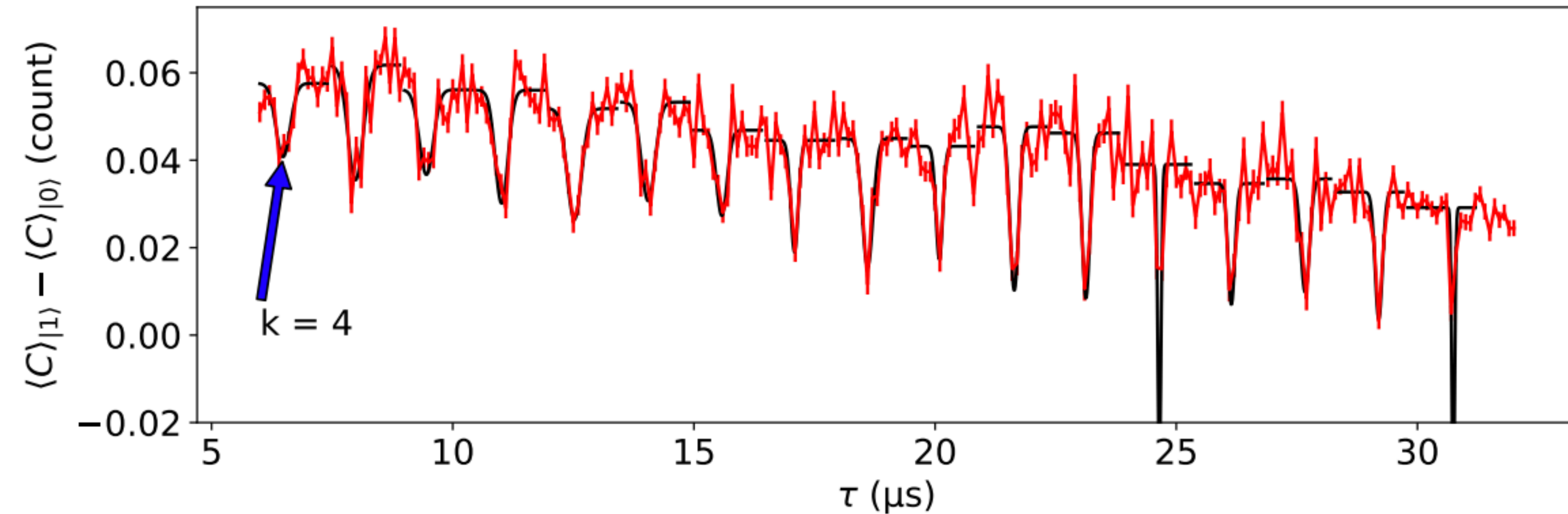
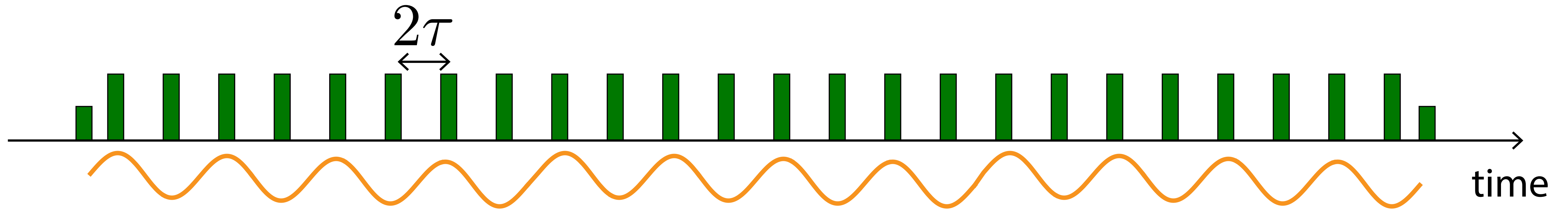
$$2\tau = (2k + 1) \frac{\pi}{\omega_L}$$

# Dynamical decoupling as a nuclear spin probe



$$\Delta\tau = \frac{\pi}{\omega_L} = 1.52 \mu\text{s} \longrightarrow \frac{\omega_L}{2\pi} = 332 \text{ kHz}$$

# Dynamical decoupling as a nuclear spin probe

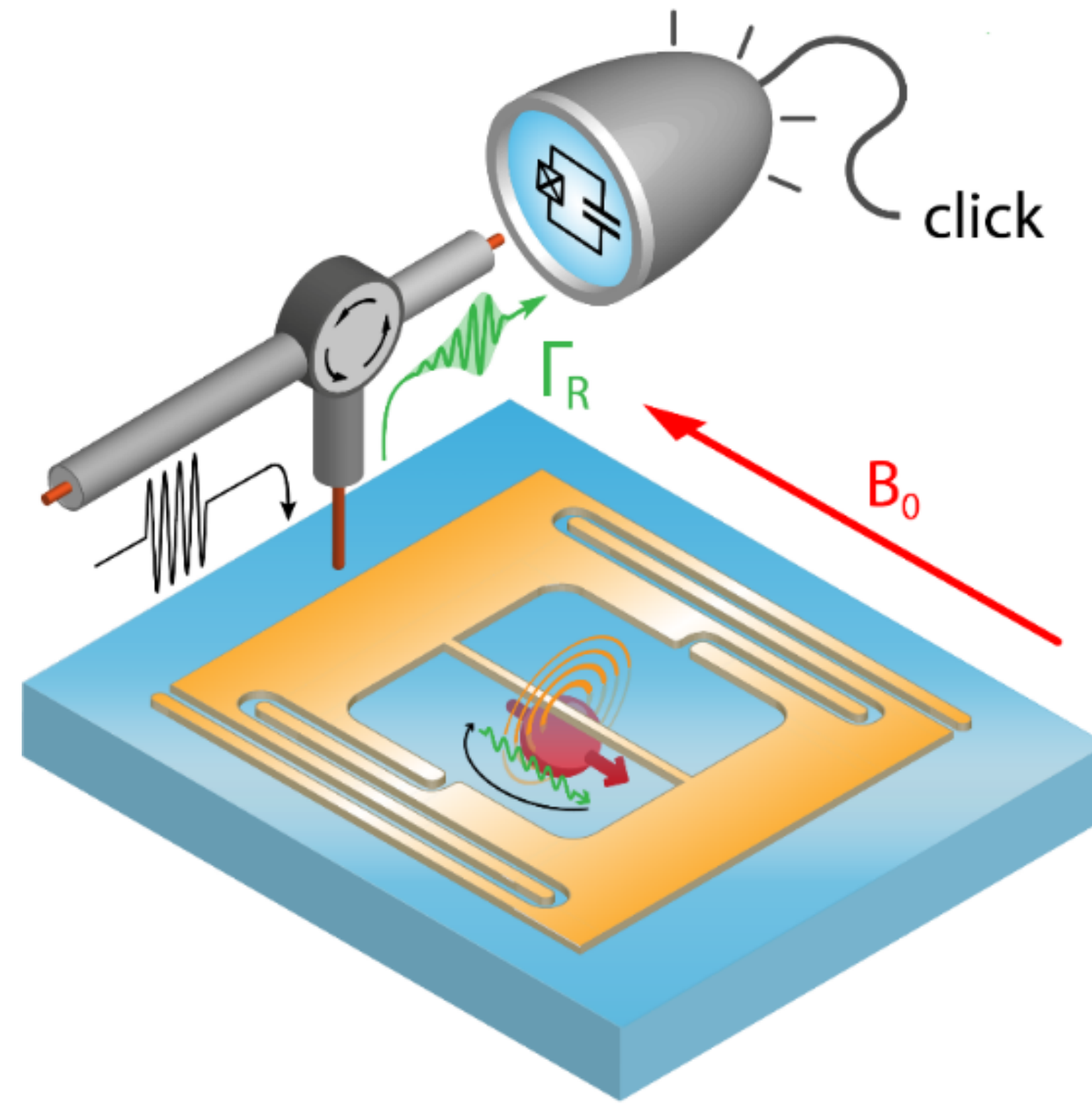


$$\Delta\tau = \frac{\pi}{\omega_L} = 1.52 \mu\text{s}$$

$$\frac{\omega_L}{2\pi} = 332 \text{ kHz}$$

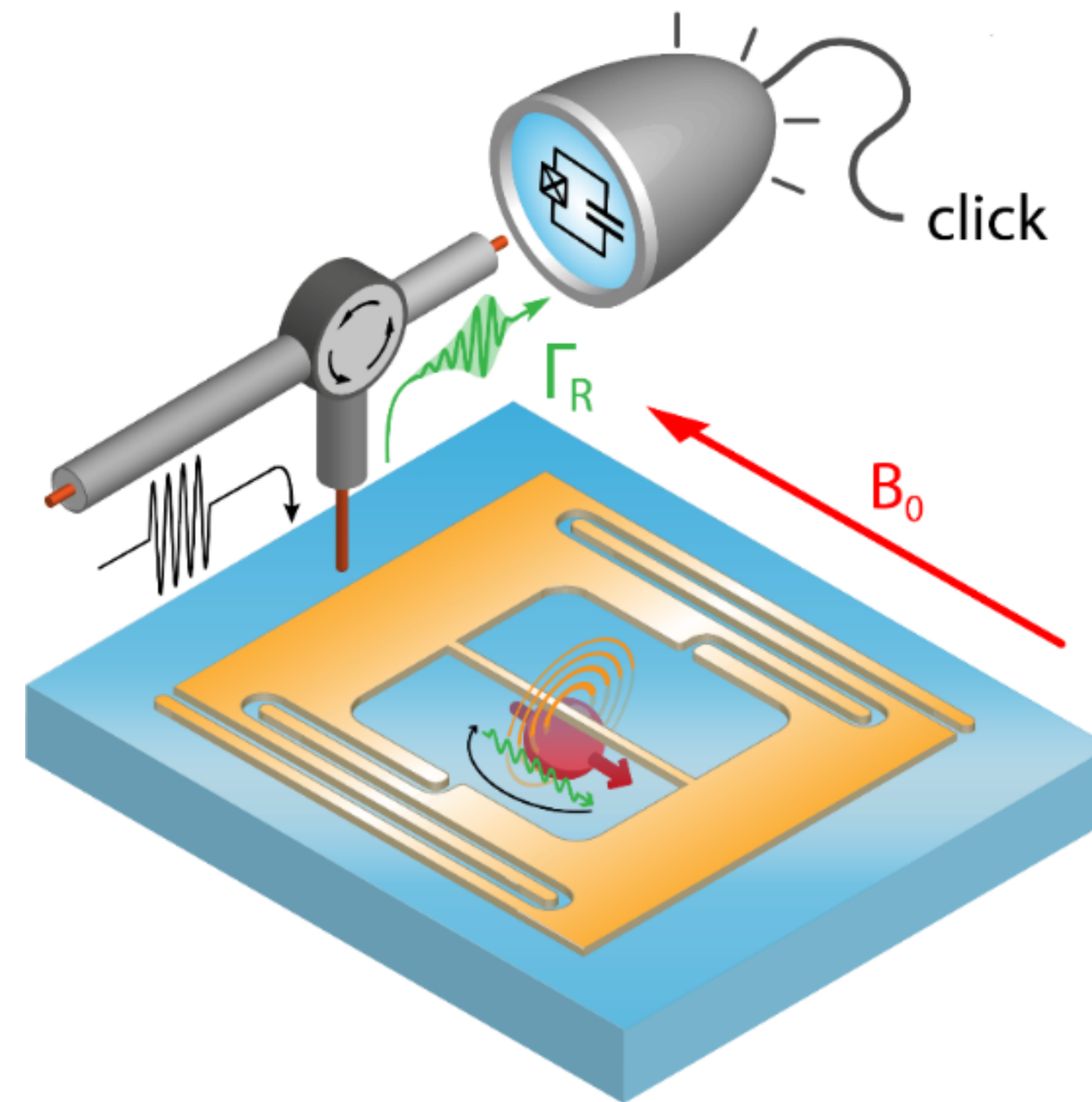
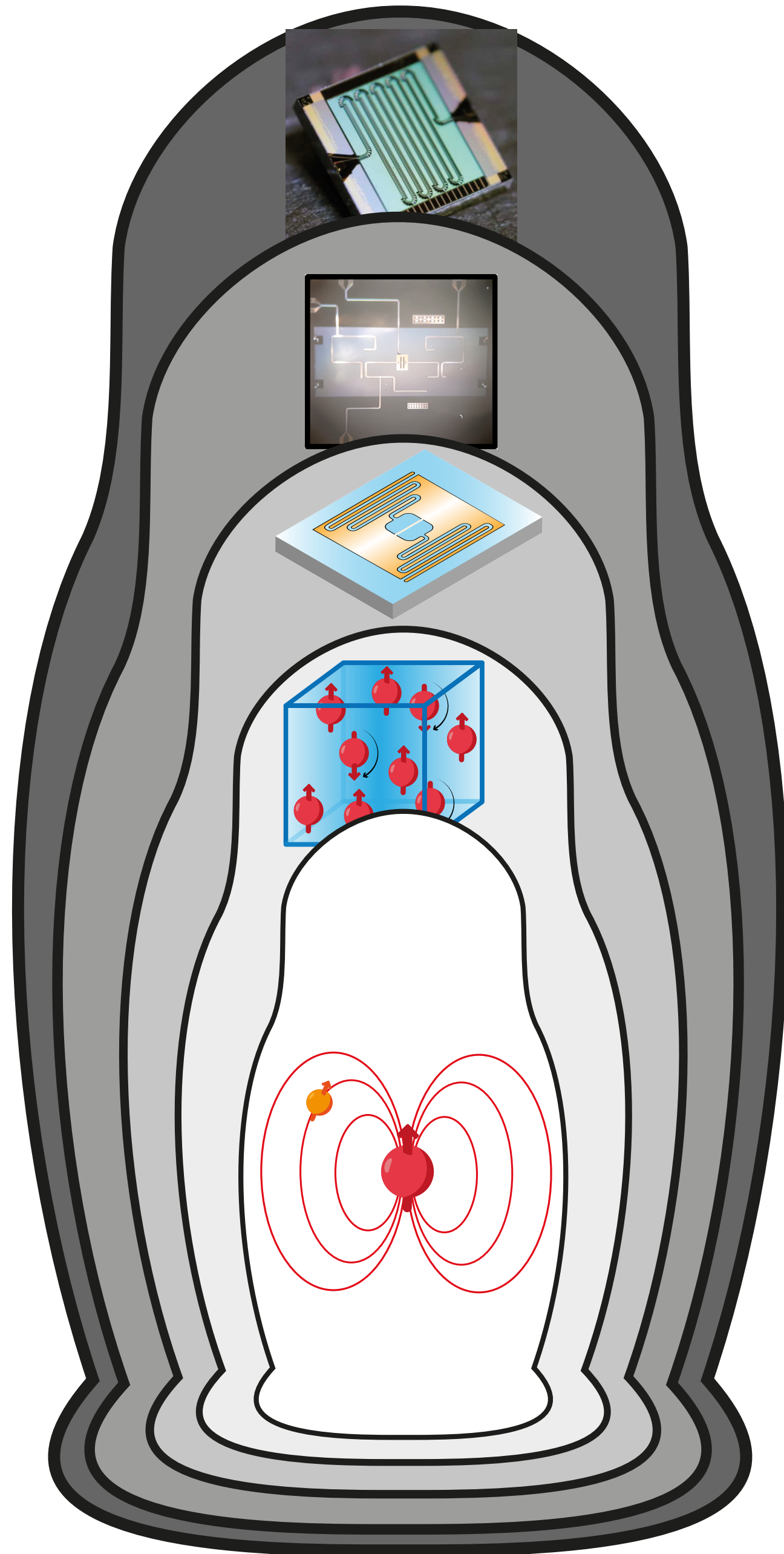
$$\frac{\omega_L}{2\pi B_0} = 1.78 \text{ MHz/mT} = \gamma_W !$$

# Conclusion





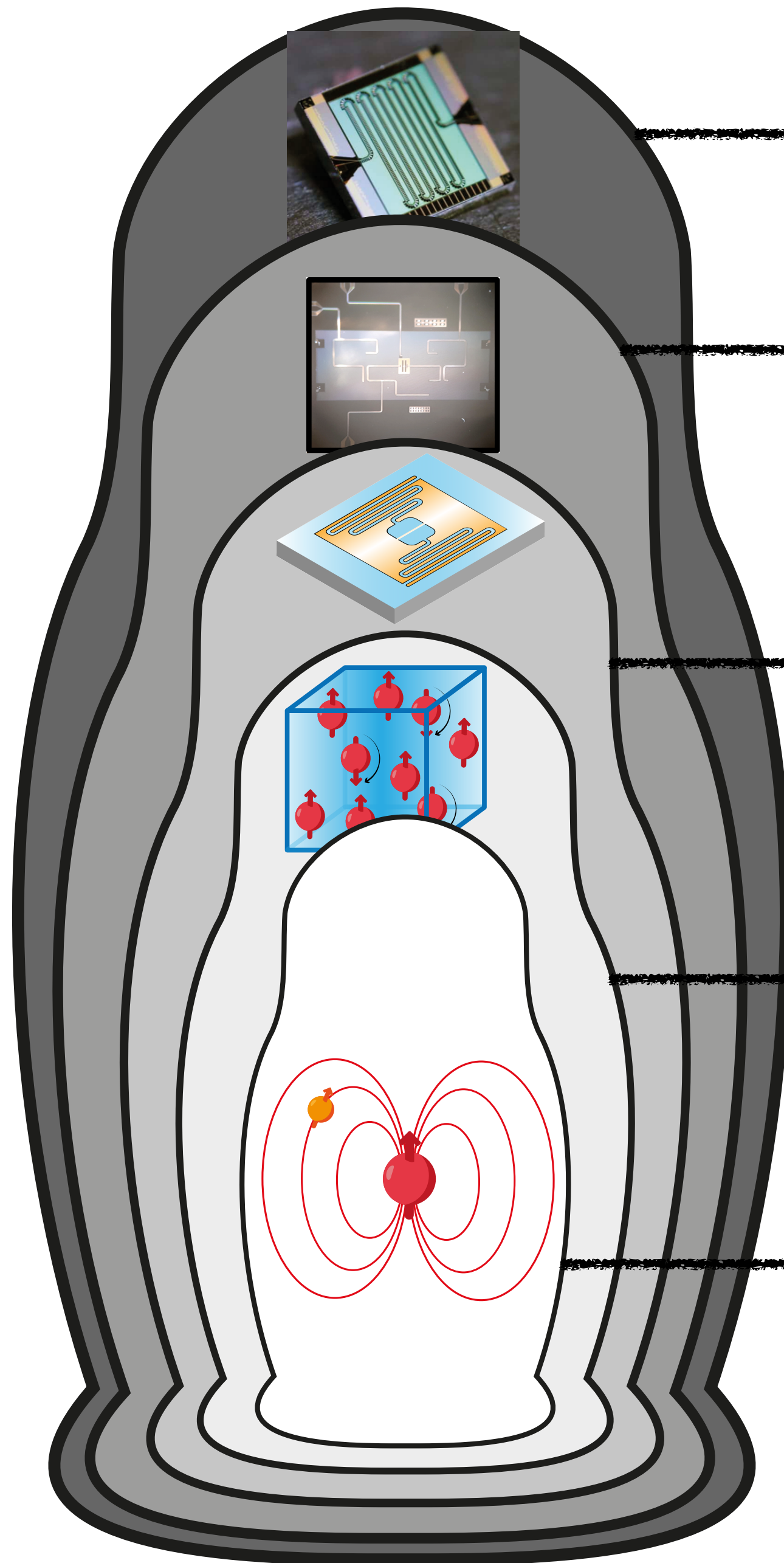
# Conclusion



## Single Spin Fluorescence Detection

- Universal
- Large detection volume ( $\sim 10\mu m^3$ )
- $1 \text{ Er}^{3+}/\sqrt{\text{Hz}}$  , large improvements possible
- Does not require long coherence time

# Perspective



Strong academic & industrial effort for circuits

**SMPD development**  $\hbar\omega \frac{\sqrt{\alpha}}{\eta} = 10^{-23} \text{ W}/\sqrt{\text{Hz}}$   
x10 sensitivity = x100 integration time

Advanced antenna design for enhanced magnetic focusing

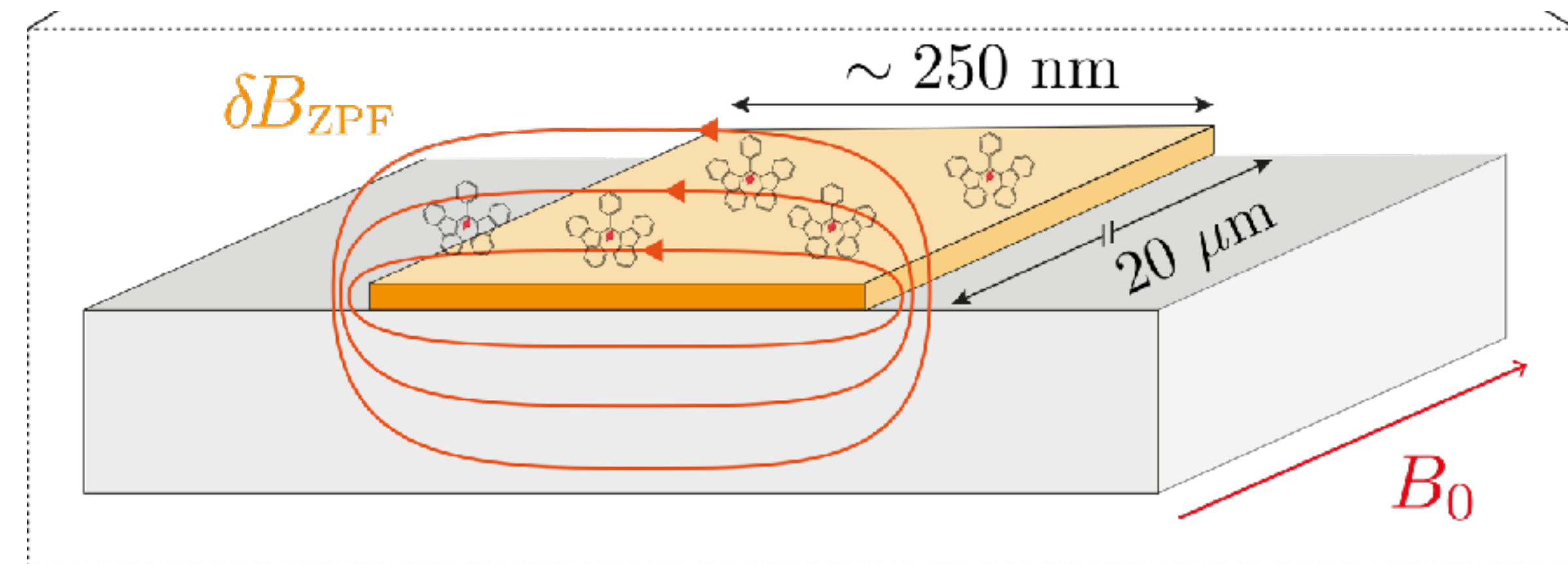
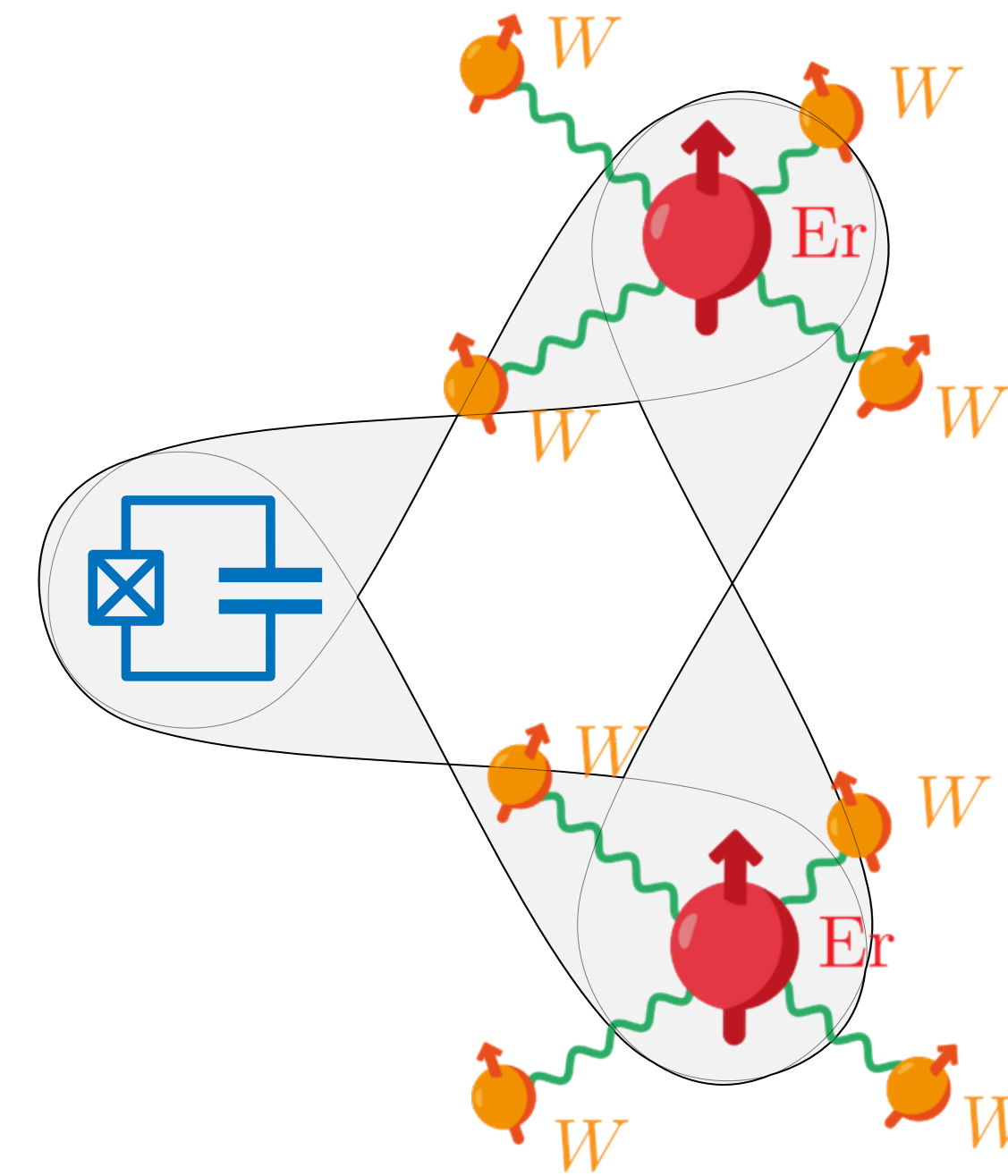
New spin species in new substrates

RF control for single nuclear spin manipulation

# Perspective

## Architecture for spin-based quantum computing

- Coherence times up to second
- Interfacing with microwave photons, superconducting circuits, and nuclear spins
- Practical single-spin EPR spectroscopy at millikelvin temperature (transition ions & radicals in molecules, ...)



# Thanks!

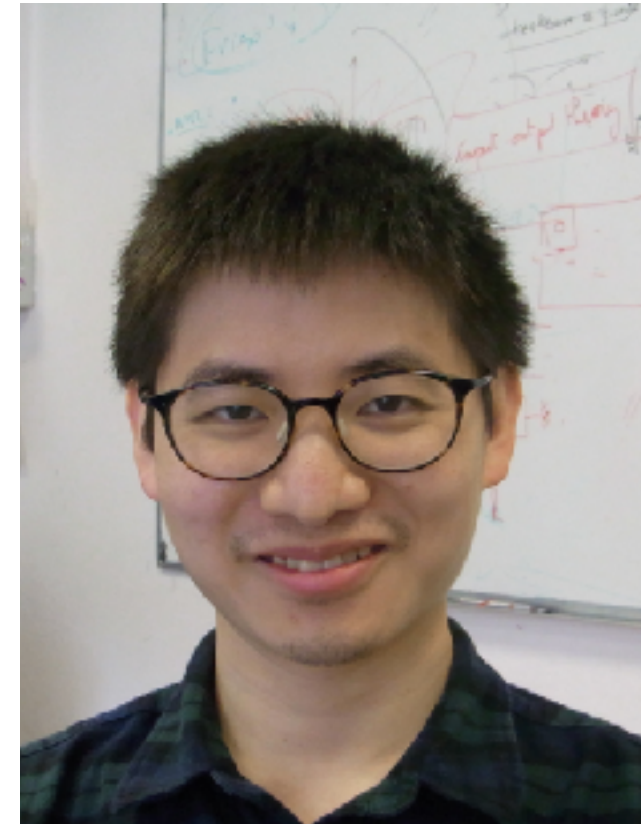
J. Travesedo



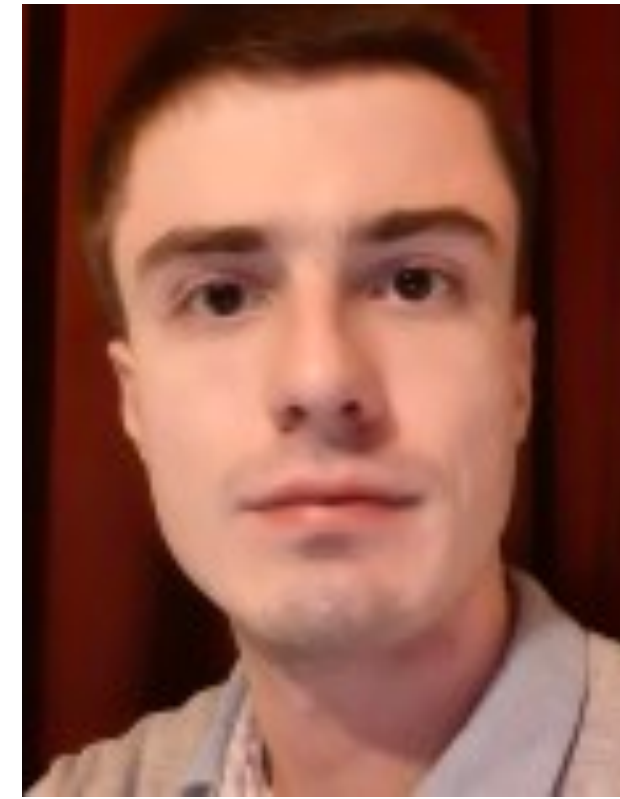
L. Balembois



Z. Wang



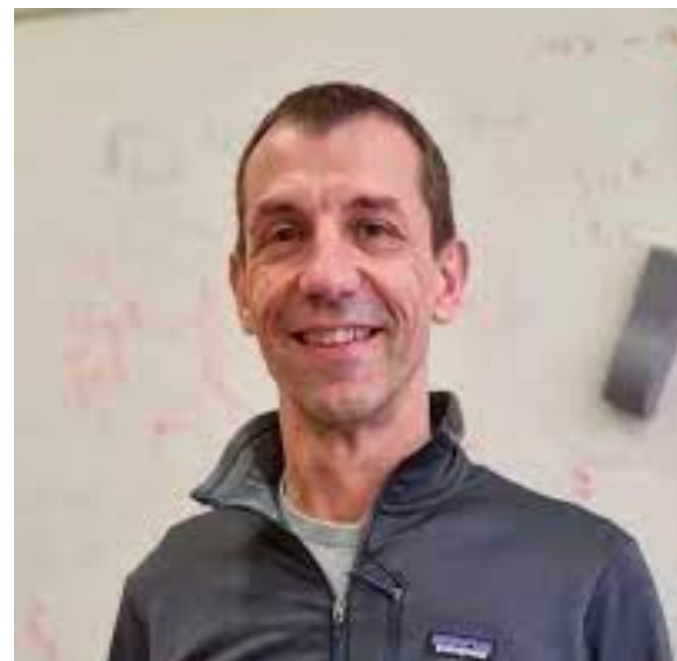
L. Pallegoix



A. May



P. Bertet



P. Goldner



Quantronics group



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